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Automated Storm Tracking and the Lightning Jump Algorithm Using GOES-R Geostationary Lightning Mapper (GLM) Proxy Data

ELISE V. SCHULTZ

University of Alabama in Huntsville, Huntsville, AL

CHRISTOPHER J. SCHULTZ

NASA/MSFC, Huntsville, AL

LAWRENCE D. CAREY

University of Alabama in Huntsville, Huntsville, AL

DANIEL J. CECIL

NASA/MSFC, Huntsville, AL

MONTE BATEMAN

USRA, Huntsville, AL

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ABSTRACT

This study develops a fully automated lightning jump system encompassing objective storm tracking, Geostationary Lightning Mapper proxy data, and the lightning jump algorithm (LJA), which are important elements in the transition of the LJA concept from a research to an operational based algorithm. Storm cluster tracking is based on a product created from the combination of a radar parameter (vertically integrated liquid, VIL), and lightning information (flash rate density). Evaluations showed that the spatial scale of tracked features or storm clusters had a large impact on the lightning jump system performance, where increasing spatial scale size resulted in decreased dynamic range of the system's performance. This framework will also serve as a means to refine the LJA itself to enhance its operational applicability. Parameters within the system are isolated and the system's performance is evaluated with adjustments to parameter sensitivity. The system's performance is evaluated using the probability of detection (POD) and false alarm ratio (FAR) statistics. Of the algorithm parameters tested, sigma-level (metric of lightning jump strength) and flash rate threshold influenced the system's performance the most. Finally, verification methodologies are investigated. It is discovered that minor changes in verification methodology can dramatically impact the evaluation of the lightning jump system.

1. Introduction

Previous research has shown that rapid increases in lightning activity are highly correlated to the occurrence of severe weather using lightning data from available three-dimensional lightning networks throughout the United States. Analysis by Williams et al. (1999), Schultz et al. (2009), and Gatlin and Goodman (2010) demonstrate the correlation between rapid increases in total flash rate (i.e., "lightning

Corresponding author address: Elise V. Schultz, 320 Sparkman Dr., Huntsville, AL 35805

E-mail: elise.schultz@nssstc.uah.edu

46 jumps") and severe weather occurrence. Furthermore, recent studies (Schultz et al. 2009, Gatlin and
47 Goodman 2010, Schultz et al. 2011) have quantified the lightning jump based on statistical performance
48 metrics including probability of detection (POD) and false alarm ratio (FAR). Schultz et al. (2009, 2011)
49 presented strong performance results (79% POD, 36% FAR) using total lightning from lightning mapping
50 arrays (LMAs) to aid in the prediction of severe and hazardous weather using an objective lightning jump
51 algorithm (LJA) with semi-automated tracking on a large number of storms. Schultz et al. (2009) developed
52 and tested 4 different LJA configurations and determined that the 2σ algorithm (sigma-level of 2; see
53 Schultz et al. 2011 section 2c) had the best skill in nowcasting severe weather potential.

54 However, Schultz et al. (2009, 2011) and others lack full automation and semi-objective tracking
55 techniques that are needed for operational usage of the LJA. In addition, these previous studies have not
56 taken advantage of adding satellite based products to that of commonly used radar based products. Rudlosky
57 and Fuelberg (2013) used objective tracking techniques, but also lacked full automation. Chronis et al.
58 (2015) also used objective and automatic tracking techniques to understand how performance metrics for
59 the lightning jump change using real-time datasets. However, all of these studies arrived at their conclusions
60 from LMA datasets and did not account for or anticipate what the Geostationary Lightning Mapper (GLM)
61 will observe once in orbit on the GOES-R satellite (Goodman et al. 2013). Proch (2010) is the only previous
62 study to use the LMA derived GLM proxy data. He used storms from the Schultz et al. (2009) database to
63 evaluate the LJA with GLM proxy data. His results showed a lower sigma-level and lower flash rate
64 threshold might be needed to optimize the algorithm for severe weather detection with GLM proxy data.
65 Therefore, the goal of this study is to develop a fully automated framework encompassing objective
66 tracking, GLM proxy lightning data, and the LJA to build toward operational assessment of storm intensity
67 in real-time. This framework will also serve as a means to refine the LJA itself to enhance its operational
68 applicability. This paper will describe the methodology involved with establishing this fully automated
69 system and discuss how adjustments to parameters within various parts of the system affect the overall
70 performance. In section 2, we will describe the components of the lightning jump system and illustrate the

71 automated, objective tracking methodology including how this differs from past research, which solely
72 relied on radar information for tracking. The components of the LJA will be described including the
73 parameters involved in sensitivity testing. Finally, verification methodology will be addressed as an
74 additional method of assessing the system's performance. Section 3 will examine the sensitivity tests
75 performed and the influence individual and combined parameters had on the LJ system. Section 4 will
76 summarize the key influences on the system's performance and look forward to future research and
77 considerations.

78

79 **2. Data and methodology**

80

81 The lightning jump system consists of three components: radar and lightning data, thunderstorm
82 tracking, and the LJA. Each component plays a vital role in the automation of the LJA towards operational
83 use. The database for this study includes over 90 event days consisting of up to 1000¹ storm clusters between
84 the years of 2002 and 2011 within 125 km range of the North Alabama Lightning Mapping Array
85 (NALMA) network center (Fig. 1; Table 1). This dataset is a significant subset of the event days included
86 in Schultz et al. (2011). Storm clusters are included in the database if they have a minimum lifetime of at
87 least 30 minutes while the cluster is within 125 km of the center of NALMA. Only the portion of the cluster
88 track that is within the domain is included in the dataset. Unlike previous studies that subjectively select
89 storms on each event day to include in the database, this study includes all identified storms that meet the
90 tracking criteria as identified by the tracking methodology discussed in section 2b.

91

92 *a. Radar and lightning data*

93

94 1) RADAR

¹ The number of storm clusters is dependent upon the tracked feature size.

95

96 For each event day, NEXRAD Level II radar data for the five radars (KHTX, KGWX, KOHX, KFFC,
97 KBMX) closest to the NALMA center are merged and gridded ($0.009^\circ \times 0.009^\circ \times 1\text{km}$ resolution; Fig. 2b)
98 using the Warning Decision Support System – integrated information (WDSSII; Lakshmanan et al., 2006,
99 Lakshmanan et al., 2007). While previous studies have used reflectivity based thresholds for thunderstorm
100 tracking (35 dBZ at -15°C , Schultz et al. 2009), this study uses vertically integrated liquid (VIL) in
101 combination with lightning data. VIL is calculated from the merged and gridded radar data following the
102 same methodology for single radar quality control and multi-radar blending as the national Multi-Radar
103 Multi-Sensor (MRMS) system at the National Centers for Environmental Prediction (NCEP) and provided
104 to the National Weather Service (NWS) in real-time (Smith et al. 2016).

105

106 2) LIGHTNING DATA: GLM PROXY DATA

107

108 Previous implementations of the LJA involved ground-based datasets which use three-dimensional
109 LMA data and have not included observations from a satellite based sensor. The challenge is that an optical
110 lightning detection instrument does not currently exist at geostationary orbit. Furthermore, optical
111 instruments like GLM observe a different component of lightning than the LMA (optical radiances at cloud
112 top vs. VHF observations). This study uses GLM proxy data generated from NALMA data (Bateman 2013).
113 The GLM proxy data converts NALMA flashes into what a “best guess” is that GLM will see when in orbit.
114 The GLM proxy data set accomplishes this by using flash statistics collected from the space-borne
115 Lightning Imager Sensor (LIS) onboard the Tropical Rainfall Measuring Mission (TRMM; Kummerow et
116 al. 1998) and the NALMA (Bateman et al. 2008). Like the GLM, the LIS records optical events which are
117 grouped into flashes (Mach et al. 2007), whereas the LMA detects VHF electromagnetic radiation sources
118 which are combined into flashes using a separate clustering algorithm (McCaul et al. 2009). An example
119 of a visual comparison for a flash between the LIS and LMA is shown in Fig. 3. Essentially, the GLM proxy

120 flashes are transformed to match the lower spatial resolution of the GLM (compared with NALMA). This
121 causes some “smearing out” and some merging of NALMA flashes but the overall flash rate is basically
122 unchanged. The GLM proxy data algorithm creates “proxy pixels” and the flash-clustering software
123 converts these into “proxy flashes”. Using this intercomparison methodology, the GLM proxy flashes are
124 composed of merged LMA 15% of the time. In other words, there are roughly 15% fewer GLM proxy
125 flashes than LMA flashes. Each GLM proxy flash location is determined by the amplitude-weighted
126 centroid of the groups/events. GLM proxy flashes are gridded to a 0.08° x 0.08° grid which approximates
127 GLM resolution and 1 and 5 minute flash count total grids (FLCT1 and FLCT5) are calculated each minute
128 to produce flash rate density products (FRD).

129

130 3) VILFRD

131

132 This study extends beyond traditional utilization of radar parameters to track storm features and
133 combines lightning data with VIL to compute a new trackable quantity. VIL and the 5-minute average GLM
134 proxy FRD (FLCT5; Fig. 2a) products are combined to track storm clusters within the WDSSII framework.
135 These products are combined as seen in Equation 1 to produce a new product, aptly named, VILFRD (Fig.
136 2c).

$$137 \quad VILFRD = 100 \times \left[\left(\frac{VIL}{45} \leq 1 \right) + \sqrt{\frac{FLCT5}{45} \leq 1} \right] \quad (1)$$

138 The VILFRD formula is subjectively determined in order to have a trackable product that relies more on
139 radar-based information when flash rates are low and then transitions to more weight applied towards
140 lightning information when flash rates are high. These two components inside the brackets each are limited
141 to a maximum value of one resulting in maximum VILFRD values of 200. The maximum limits are set to
142 treat anything larger than moderate VIL values (~45 kg m⁻²) the same as this indicates a strong
143 thunderstorm. In addition, flash rates of 45 flashes min⁻¹ or greater are also indicative of a strong
144 thunderstorm. While an in-depth comparison between the two tracking methods mentioned (radar vs. radar

145 and lightning) has not been completed with this dataset, initial observations place added value to the
146 addition of lightning information compared to radar tracking alone as it increased the consistency of
147 tracking a storm's core and updraft region. This agrees with results from Meyer et al. (2013) which uses
148 radar and lightning data to track storms. Lightning and lightning jumps are physically related to the storm's
149 updraft (e.g., Schultz et al. 2015) and thus the combination of radar and lightning information provides the
150 tracking system a product that is weighted towards the most intense part of the storm cluster.

151

152 *b. Thunderstorm tracking*

153

154 To compute lightning time histories for jump identification, it is necessary to utilize an automated,
155 objective tracking scheme to assign lightning flashes to individual storms. VILFRD is tracked using K-
156 means clustering in w2segmotionll in WDSSII (Lakshmanan et al. 2009). WDSSII w2segmotionll is used
157 to track features where VILFRD values are ≥ 20 , at increments of 20. Any pixel with a value greater than
158 100 is assigned the value of 100. Clusters are built outward from a local maximum until a minimum size or
159 spatial scale threshold is met (Table 2) with a maximum overlap approach (combining cells within 5km of
160 the cell boundary) for associating cells from one time step to the next. Cells are not included that are not
161 tracked at each time step. The WDSSII tracking included 8 scales (scales 0 to 7) however, only scales 1
162 through 6 are included as scale 0 and scale 7 are unusable as the extremely small and large area parameters,
163 respectively, failed to produce output for the vast majority of cases. The scales used are tracked at 40, 80,
164 120, 160, 200, and 300 pixels. The exact area scale thresholds in Table 2 account for the fact that a pixel is
165 less than 1 km². Figure 4 depicts two example clusters used to help describe this tracking method. VILFRD
166 values are denoted by different colors. If VILFRD values ≥ 100 (red in Fig. 4) meet the required minimum
167 area of a spatial scale threshold, a cluster is identified and the algorithm moves on to other clusters during
168 that time step. If not, the algorithm reduces the VILFRD threshold to the value of 80 and searches for
169 clusters that meet the minimum area of the spatial scale threshold. The VILFRD threshold continues to

170 reduce in increments of 20 until it reaches a floor VILFRD value of 20. If the VILFRD feature footprint at
171 the level of 20 does not reach the minimum area of a spatial scale threshold, no cluster is identified at the
172 time and location. For example, a feature at scale 5, minimum required area is 162 km² (Table 2), would be
173 represented as the area included in D (VILFRD ≥ 40) in Cluster 1 and as area included in B (VILFRD ≥ 40)
174 for Cluster 2.

175 The result of this iterative identification technique is that tracked clusters will differ in area and lifetime
176 at each spatial scale. Each individual cluster is given a unique cluster identification number during its
177 lifetime. Individual clusters at a select time are shown as an example in Fig. 2d. Outside of WDSSII,
178 “broken tracks” are objectively merged if a WDSSII cell begins at t+1 within 15 km of where a previous
179 track ended at time t. Time histories are tied together for merged cells.

180

181 *c. Lightning Jump Algorithm*

182

183 The LJA as defined by Schultz et al. (2009) laid the foundation for this study. In their studies, Schultz
184 et al. (2009, 2011) objectively identified lightning jumps using the “2 σ ” algorithm. Figure 5 diagrams the
185 flow chart depicting the following five steps describing the LJA process for the “2 σ ” threshold.

- 186 1) The total lightning flash rate (as calculated from the 1 minute GLM proxy FRD) from the time
187 period, t, is binned into 2 minute time periods and averaged.
- 188 2) The time rate of change of the total flash rate (DFRDT) is calculated by subtracting consecutive bins
189 from each other (i.e., bin₂-bin₁, bin₃-bin₂,... bin_t-bin_{t-1}). This results in DFRDT values with the units
190 of flashes min⁻².
- 191 3) The standard deviation of the 5 previous DFRDT values is calculated. Twice this standard deviation
192 value determines the level for the current DFRDT to exceed to be classified a jump in the
193 “2 σ ” algorithm.

- 194 4) Taking the ratio of the current DFRDT value to the standard deviation of the previous 5 time periods
195 (Step 3) is further referred to as the sigma-level. Thus, a previously defined 2σ jump would have a
196 sigma-level of 2. This presentation allows the end user to have the ability to understand how a
197 current increase in the total flash rate compares to other recent increases in the storms total flash
198 rate. For instance, a sigma-level of 8 would indicate a more rapid increase in the flash rate than a
199 sigma-level increase of 2. This extra information directly corresponds to the kinematic and
200 microphysical growth of the storm leading up to the time of the lightning jump and can aid in the
201 forecaster's warning decision making process (Schultz et al. 2015).
- 202 5) In addition to reaching the required sigma-level to determine a jump, the following must also be met
203 for the original approach to the algorithm: the minimum spin-up time of 14 minutes is reached (6
204 time periods to achieve 5 DFRDT values plus the current time period), the current flash rate exceeds
205 the flash rate threshold of $10 \text{ flashes min}^{-1}$, and the classification of an individual jump ends once
206 the sigma-level drops below 0.
- 207 5) This process is repeated every two minutes as new total lightning flash rates are collected until the
208 storm dissipates. If a jump is currently in progress, the jump is continued until the sigma-level drops
209 below 0. In the event multiple jumps occur within 6 minutes of each other, only the first jump
210 remains for verification to follow the original Schultz et al. (2009) verification methodology (Table
211 3).

212

213 *d. Parameter sensitivity testing*

214 Seven parameters (Table 1) within the lightning jump system have been identified as having potential
215 impact on the performance of the LJA. A range of values for sigma-level threshold, flash rate threshold,
216 spin-up time, severe storm report distance, verification window, domain range, and spatial scale are used
217 to determine which parameters the algorithm is the most sensitive to and what those values are. With the
218 initial development of the LJA, Schultz et al. (2009) tested a 2σ and 3σ configuration of the LJA and

219 determined that the 2σ version produced more optimal skill scores when the 10 flashes min^{-1} flash rate
220 threshold is implemented. Based on the Schultz et al. (2009) findings, the 2σ configuration is tested further
221 in Schultz et al. (2011). This study expands upon the LJA configuration results from Schultz et al. (2009,
222 2011) and further exploration by Chronis et al. (2015) through further sensitivity testing of the sigma-level
223 threshold by varying the sigma-level from 0.75 to 2.5 in 0.25 increments (Table 1). Furthermore, a range
224 of flash rate thresholds (1, 5, 10, 15, and 20) are tested in order to determine the algorithm sensitivity (Table
225 1). The minimum time required for the spin-up of the algorithm is 14 minutes (12 minutes to calculate the
226 sigma-level, 2 additional minutes to determine if a lightning jump has occurred; Section 2c).

227 Tunable parameters that are investigated within the verification framework are severe storm report
228 distance and verification window. Severe storm reports are obtained from NOAA's National Climatic Data
229 Center's (NCDC) Storm Data and used as ground truth for validation. Storm Data has known temporal and
230 spatial errors in reporting of events and known underreporting in data sparse regions (e.g., Witt et al. 1998,
231 Williams et al. 1999, Trapp et al. 2006, and Chronis et al. 2015), so effort is taken to mitigate small timing
232 and spatial errors that may exist in the database. This mitigation includes an additional "buffer" space
233 around the footprint of a tracked storm cluster at each time step to assign reports to specific clusters. Storm
234 report distance is defined as the maximum distance from the storm cluster's footprint edge that a storm
235 report can be associated with that storm. This distance is set to 5 km (Table 1). The verification window
236 starts at the occurrence of a jump and lasts for 45 minutes (Table 1). Reports that occur within this
237 verification window are used to verify the jump. For the results shown within, these parameters remained
238 constant as initial sensitivity testing showed less impact to the overall system performance than other
239 parameters.

240 Finally, two parameters are used to ensure quality and define the database. The domain range is limited
241 to the areal coverage of the LMA network (Fig. 1). The closer the lightning activity is to the network, the
242 higher the detection efficiency (Koshak et al. 2004). Therefore, extending the domain can decrease the
243 detectable flashes and flash rates that can have an effect on the classification of jumps. A default distance

244 is chosen as 125 km to remain in close proximity to the LMA network, which is used to statistically generate
245 the GLM proxy data. Only portions of the storm life cycle (inclusion of entire storm's footprint determined
246 by the storm's centroid location) occurring for at least 30 minutes within 125 km of the center of the LMA
247 network are included in this study. The variance in spatial scale introduced in this study is a result of the
248 options available in w2segmotionll in WDSSII to track features at different areal extents. Six different
249 spatial scales (Table 2) are chosen ranging in sizes from that of small thunderstorms (scale 1 at 32 km²) to
250 that of larger storm clusters (scale 6 at 243 km²). These values serve as the benchmark storm size for the
251 sensitivity testing of the LJA.

252

253 *e. Verification*

254

255 The verification methodology initially applied in this study closely reflects the methodology outlined
256 in Schultz et al. (2009). In order to evaluate the lightning jump system, severe storm reports are used as
257 ground truth validation. As mentioned in Section 2d, there are caveats with using NCDC Storm Data. In an
258 attempt to mitigate these effects, a temporal clustering of reports (same type) in 6 minutes bins is
259 implemented. This binning begins at the time of the first report. Any report grouped into this bin counts as
260 a single event and the time of the first report within the group is used for any calculations.

261 The window for jump verification is the time window (default length of 45 minutes; Table 1) starting
262 at the time of the jump. However, in the method outlined by Schultz et al. (2009), only one jump can be
263 evaluated at a given time. As mentioned in Section 2d, jumps are grouped if they occur within 6 minutes of
264 each other (3 consecutive time periods). This leaves open the potential for additional jumps to occur within
265 the verification window (after the 6 minute grouping) of a previous jump. In these cases, initial or "first"
266 jumps and subsequent or "second" jumps are denoted as shown in Fig. 6. Each jump has a verification
267 window equal to that of the verification window parameter, which is 45 minutes for this study. The first
268 jump is verified and a "hit" (defined as the number of storm report groups within the verification window)

269 if a storm report occurs during the verification window as denoted by the green vertical bar at approximately
270 10 minutes in Fig. 6. A second jump's verification window, however, is limited to the time period remaining
271 following the expiration of the first jump's verification window. For example, if the second jump started
272 30 minutes after the first, its verification window would begin 15 minutes later (considering a 45 minute
273 verification window) leaving a 30 minute verification window for the second jump. This can be visualized
274 in Fig. 6. Despite what reports exist within the 15 minute overlap of the two jumps (minutes 30 to 45 or
275 example report at approximately 40 minutes), the second jump is classified as a false alarm if no reports
276 are present for the remaining 30 minutes (minutes 45 to 75). This methodology is applied for any additional
277 jumps.

278 In order to evaluate the algorithm, the skill scores of POD and FAR (Wilks 2011, 310-311) are
279 calculated. In this process, a hit is defined as the grouped severe storm reports that occur during a
280 verification window of a jump within the set bounds around a storm cluster (based on the radius from the
281 edge of the cluster's footprint). A miss is defined as a severe storm report group that occurs outside of a
282 verification window. A false alarm is defined as a jump that is not followed by any severe storm reports
283 within the associated verification window as well as the qualification involving subsequent jumps as
284 described in the previous paragraph.

285 Verification methodology from Schultz et al. (2009, 2011) is not equivalent to that of the methodology
286 employed by the National Weather Service (NWS) storm warning verification (NWS 2011). The main
287 difference that exists between these two is the grouping of severe storm reports and the false alarm
288 classification for subsequent jumps. A side by side comparison of these two methodologies can be seen in
289 Table 3. Unlike Schultz et al. (2009), the NWS validates each warning separately even if they overlap.
290 However, reports in the overlapping region only count as a single hit and not a hit for each warning. In an
291 effort to more closely compare our results to the techniques used by the NWS, we included what we will
292 call an alternative (in reference to Schultz et al. 2009) verification method. The discussion of our results

293 will use both of these verification methods to evaluate the LJA algorithm and analyze sensitivity within the
294 tunable parameters listed in Table 1.

295

296 **3. Results**

297

298 Numerous iterations of tunable parameter combinations (Table 1) are processed through the lightning
299 jump system, analyzed, and evaluated using the skill score metrics of POD and FAR. The sensitivity
300 analysis revealed the level of influence that individual parameters and parameter combinations have on the
301 system performance. In addition, the verification methodology notably affected evaluation of the lightning
302 jump system. The key results shown are the influence of spatial scale used in storm cluster tracking, the
303 effect of sigma-level and the flash rate threshold on the LJA, and the impact verification methodology has
304 on these results.

305

306 *a. Spatial scale*

307

308 One component of the tracking methodology is choosing a representative storm scale size. However,
309 storm size and appropriate scale size can greatly vary depending on storm mode. Scales ranging in areal
310 size from scale 1 at 32 km² to scale 6 at 243 km² (Table 2) are tested. Figure 7 shows cluster footprints for
311 all six scales discussed in this study at a given time (same date/time as Fig. 2). This figure depicts the
312 similarities and differences inherent to the different tracking scales. Most notably different is cluster A on
313 the left-hand side of the figures, which varies drastically in size from scale 1 to scale 6. Cluster B, remains
314 the same size throughout the different scales. This consistent size is most likely due to a strong, active
315 lightning core within this thunderstorm as can be noted by the influence of the lightning contribution to
316 VILFRD as seen in Fig. 2a, b, and c.

317 Figure 8 shows a color-coded comparison between the 6 different spatial scales that are used by
318 WDSSII to track storm clusters. Each symbol represents one iteration of the algorithm for all event days
319 for a given set of parameters. Larger spatial scales show increased POD values due mainly to the large areal
320 extent of the storm clusters' footprints. Quantitative evidence of this is shown in Tables 4 and 5. These
321 larger areal extents allow for the inclusion of more lightning flashes and thus higher flash rates. Over 37
322 percent of time steps in the scale 6 database have flash rates over 20 flashes min^{-1} . At the lower spatial
323 scales, the flash rates often do not reach the minimum flash rate threshold (default of 10 flashes min^{-1}). This
324 is true for 87 percent of time steps for the entire scale 1 database. In contrast, only 22 percent of time steps
325 at scale 6 have total flash rates below 10 flashes min^{-1} . In scale 1, 4.5 percent of the database reaches a
326 sigma-level of 2 but are not calculated as jumps because the flash rate is below 10 flashes min^{-1} . Not meeting
327 the minimum flash rate threshold prevents the LJA from activating and leads to any event occurring within
328 the areal bounds set for that storm to be considered a miss. This causes both an increase in the number of
329 misses and a decrease in the relative amount of hits as compared to larger scales and thus, leads to lower
330 POD values in the smaller scales. POD values increase from a range of 0.19 to 0.88 at scale 1 to 0.44 to
331 0.97 at scale 6 (due to a variance of other parameters). The range of FAR values between scales shows less
332 spread than POD. The range of values decreases with increasing spatial scales, from a range of 0.5 to 0.91
333 at scale 1 to 0.63 to 0.86 at scale 6.

334 During early investigation of the interplay between spatial scale and storm tracking, it is found that
335 smaller scales are more ideal for isolated, small-scale thunderstorms as they are easier for the tracking
336 algorithm to separate. Larger scales are more ideal for more complex and larger storms such as supercells.
337 The larger scales are less likely to split apart a cluster that would naturally be considered as one entity
338 although it may consist of multiple updrafts. In order to evaluate flash rate threshold and sigma-level, an
339 optimal scale needs to be selected. Scale 5 (minimum areal size of 162 km^2) is selected based on the balance
340 of a high number of verified jumps per cluster (0.3, Table 5) with fewer missed events per cluster (0.26,
341 Table 5). Scale 5 also balances the penalty of increasing FAR as it increases less than the POD increases

342 with larger scales. While all scales 1 through 6 are explored in this research, scale 5 is fixed for analysis
343 and comparisons shown here within.

344

345 *b. Algorithm parameters: Flash rate threshold and sigma-level*

346

347 Compared to all the tunable parameters listed in Table 1, the combined effect of the flash rate threshold
348 and sigma-level show the most promise in improving the LJA performance as evaluated by POD and FAR.
349 The POD and FAR values for the sigma-level and flash rate thresholds for the Schultz et al. (2009) and
350 alternative verification methods are shown in Figs. 9 and 10, respectively. The Schultz et al. (2009)
351 verification methodology (Fig. 9) shows that decreasing sigma-level values (cooler colors) and lowering
352 the flash rate threshold (symbols) results in the POD increasing slightly more than the increasing FAR. The
353 POD and FAR are strongly coupled with a linear correlation coefficient of 0.95. In order to help break down
354 the individual effects of sigma-level and flash rate towards POD and FAR, a linear regression model is
355 applied at each constant sigma-level or flash rate. The trends of the slope of the linear regression models
356 show that as the sigma-level decreases, the effect of flash rate become more pronounced (slope or rate of
357 change of 0.88 at 2.5 sigma-level and 0.57 at 0.75 sigma-level). These slopes help reveal a smaller increase
358 in FAR values with increasing POD values.

359 The overall effect of sigma-level and flash rate threshold on the algorithm with the alternative
360 verification (Fig. 10) shows a decoupled POD-FAR relationship ($R^2=0.20$). This is noted by little change
361 in the FAR and an increase in the POD with decreasing sigma-level values. In addition, decreasing the flash
362 rate threshold leads to an increase in FAR and POD with FAR increasing at a slightly lower rate of change
363 than the POD. The addition of more storms meeting the low flash rate requirements allow for jumps to be
364 calculated (whereas the algorithm would not be initialized at higher flash rates) and more storm reports to
365 be counted as potential hits. Linear regression analysis while holding the sigma-level constant reveals linear
366 regression fits (or slopes) of 0.99 (at 0.75 sigma-level) to 0.59 (at 2.5 sigma-level). This quantifies the

367 coupled effect flash rate threshold has on the POD-FAR relationship at low sigma-level values and the
368 decoupling of this relationship with increasing values of the sigma-level. Thus, the sigma-level contributes
369 to the overall decoupled POD-FAR relationship with the alternative verification.

370

371 *c. Verification methodology*

372

373 Two similar yet different verification methodologies are explored for this study. Figure 11 shows the
374 spread of the verification methodology established in Schultz et al. (2009; black) and the alternative
375 verification method (red) for all spatial scales. As mentioned, the Schultz et al. (2009) verification shows
376 how closely coupled the relationship is between POD and FAR. The alternative method of verification
377 shows improved performance of the LJA system on the order of reducing the FAR by 20% while
378 maintaining a high POD. This is most likely due to the reduced amount of subsequent jumps classified as
379 false alarms in Schultz et al.'s methodology (Table 4).

380 Figure 12 shows a comparison of the two methodologies for an individual cluster track. The difference
381 comes in the classification of a jump that occurs during the verification window of a previous jump. The
382 difference between the two methodologies is evident in the fourth jump or jump D. Under the methodology
383 in Schultz et al. (2009), jump D is a false alarm because the severe events that follow jump D are also in
384 the verification window of jump C. If an event is reported after the verification window of the previous
385 jump then jump D would be a hit or verified jump in the Schultz et al. methodology. Jump D is a hit, or
386 verified jump, in the alternative verification because that method removes the restriction of only allowing
387 one jump to be verified at a given time. While false alarms and hits will be different between the two
388 methodologies due to the reasons discussed above, the number of misses remain constant as no jumps are
389 created or removed that could increase or reduce the number of misses.

390

391 **4. Discussion and summary**

392

393 Storm tracking is a challenging aspect of research at the storm scale. Previous tracking methodologies
394 have involved radar reflectivity thresholds, radar reflectivity at specific temperature thresholds, satellite
395 features, etc. This study has taken a new, unique approach and combined VIL and gridded lightning flash
396 rate density to develop a trackable product. This product, VILFRD, helps track the portions of the storm
397 where relevant ice production and lightning activity are occurring to focus on the intense portions of the
398 storm. Most importantly, this method of utilizing lightning information in addition to radar derived
399 parameters lays groundwork for future methods of tracking storms by lightning in the absence of radar
400 information (e.g., over oceans, in terrain where radars encounter blockage). This type of tracking is
401 potentially game changing from the perspective of GOES-R. With GOES-R, the community will have the
402 ability for hemispheric tracking of storm systems with the added lightning capabilities of GLM, providing
403 additional information on the intensity of storms not only over land, but also in data sparse regions.

404 One of the key points of this study is the testing of various spatial scales in storm tracking. Table 2
405 documents these various scales. As is noted, results differed based on spatial scale. A large part of this
406 result is the inability for the lightning flash count within the smaller spatial scales to reach a minimum
407 threshold. For some of the clusters in the smaller scales, the tracked feature is a more intense core within
408 what is tracked as a larger multicell cluster at larger spatial scales. This is an advantage when trying to
409 separate features to trackable sizes but a disadvantage when verification techniques are applied and smaller
410 clusters perform poorly due to only covering a limited spatial area. There has been initial research and
411 testing into combining different scales (Herzog et al. 2014).

412 Both sigma-level and flash rate play an important role in the lightning jump system's ability to predict
413 severe storms, especially based on the results shown for the Schultz et al. (2009, 2011) methodology.
414 Recent work by Chronis et al. (2015) and Schultz et al. (2015) demonstrate both empirically and physically
415 how these two parameters work in concert with each other and provide valuable information into the
416 intensification of storms. The lightning jump provides lead time on the higher flash rates that are to come,

417 and higher flash rates are physically and dynamically tied to the development and manifestation of severe
418 weather at the surface. There are notable differences in skill scores between this study (~60% POD and
419 ~73%) and Schultz et al. (2011; 79% POD and 35% FAR) despite using the same event days from the
420 Tennessee Valley. The most obvious difference between the two studies is in the number of cluster/storms.
421 The automated tracking employed in this study identified more storm clusters in the same event database
422 at each spatial scale (Table 1) than the 555 storms identified in Schultz et al. (2011). Another key difference
423 is the lightning data input. In general, the GLM proxy data has fewer number of flashes identified than the
424 full LMA dataset used in Schultz et al. (2011). When the alternative methodology is applied, the sigma-
425 level influences the performance of the algorithm to a larger extent than the flash rate threshold. Decreasing
426 the sigma-level will increase the number of jumps and will increase the likelihood of event detection
427 (increase in POD). In the alternative methodology, the algorithm is not penalized the same as the Schultz
428 et al. methodology for repetitive or subsequent jumps that overlap with previous jump forecasts. Therefore,
429 this increase in jumps does not increase FAR. In actuality, the FAR decreases with decreasing sigma-level
430 because the added number of jumps associated with a lower sigma-level threshold are not penalized for
431 overlapping.

432 For both verification methodologies, the increase of the flash rate threshold reduces the number of
433 jumps. In turn, this change decreases FAR (jumps are not identified until they reach a higher flash rate)
434 and POD because many severe events are counted as missed events due to no jump or forecast being issued.
435 The change in FAR and POD are most notable at smaller spatial scales. Flash rate threshold changes,
436 independent of sigma-level, weakly influences the skill score metrics more using the Schultz et al.
437 verification methodology.

438 Finally, it is important to determine how this LJA system can be applied to real-time operations utilizing
439 hemispheric lightning coverage with GOES-R GLM, as the launch of GOES-R approaches,. The LJA is
440 shown to add value in the operational forecasting paradigm from a satellite, hemispheric perspective (e.g.,
441 Darden et al. 2010). Allowing forecasters the ability to evaluate the LJA through tracked clusters color-

442 coded by sigma-level, as seen in the Hazardous Weather Testbed (HWT; Calhoun et al. 2014), also allows
443 for individual assessment of the variations of sigma-level presented in this and other studies. Tracking
444 methodologies also can greatly impact the usability of any algorithm including the LJA, as is shown by this
445 study. This study has shown that the best results are achieved when there is balance between small and
446 large feature tracking methods. Scale 5 (162 km² or about 13 x 13 km cluster size) exhibited this balance
447 and is just smaller than that used by the HWT tracking used for real-time lightning jump evaluation.

448 This work summarizes a technique that combines radar and lightning information to track
449 thunderstorms to assess storm intensity for operational weather applications. Validation using Storm Data
450 shows that key components of the algorithm (flash rate and sigma-level thresholds) have the greatest
451 influence on the performance of the algorithm. The analysis of the lightning jump system using GLM proxy
452 data has shown POD values around 60% with FAR around 73% using similar methodology to Schultz et
453 al. (2011) which had a POD of 79% and a FAR of 36%. However, when applying verification methods
454 similar to those employed by the National Weather Service, POD values increase slightly (69%, range of
455 35-95%) and FAR values decrease (63%, range of 48-66%). These results show the POD and FAR are
456 highly correlated ($R^2=0.95$) in the Schultz et al. verification but not in the alternative verification ($R^2=0.20$).
457 This evaluation also highlights the sensitivity of the algorithm's evaluation based on verification
458 methodologies involving storm reports.

459
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461 particular, the authors thank Dr. Steven Goodman, Senior (Chief) Scientist, GOES-R System Program, for his
462 guidance and support throughout this effort.

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523

TABLES AND FIGURES

524

525 **Table 1.** Comparison of the tunable parameters in the LJA, verification, and database used in Schultz et al.
526 (2011) and this study.

527

Tunable Parameter	Schultz et al. 2011	This study
Sigma-level threshold (statistical jump threshold)	2.0	0.75, 1.0, 1.25, 1.5, 1.75, 2.0, 2.25, 2.5
Flash rate threshold Minimum flash rate (flashes min ⁻¹) required to activate the algorithm	10	1, 5, 10, 15, 20
Algorithm spin-up Minimum time required to determine a jump	14 minutes	14 minutes
Storm report distance Additional distance from cell boundary	0 (Only area within cell)	5 km
Verification window Time following a jump	45 minutes	45 minutes
Domain range From NALMA center	200 km (most within 150 km)	125 km
Spatial scale Based on WDSSII tracking parameters	60 km ²	See Table 2

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Table 2. Spatial scale levels with minimum area required to track storm clusters using WDSSII, and average storm track duration, length, and cluster size.

Spatial Scale	~Area (km²)	Track Duration (hrs)	Track Length (km)	Cluster Size (km²)
1	32	1.003	42.57	122.77
2	65	1.032	44.80	175.57
3	97	1.028	44.89	224.91
4	130	1.046	46.55	270.32
5	162	1.039	47.15	318.23
6	243	1.042	48.55	443.37

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533 **Table 3.** A comparison of verification methodologies between the method used in Schultz et al. (2009,
 534 2011) and a method aligning with the National Weather Service.
 535

Verification Methodologies	Verification Schultz et al. 2009, 2011	Alternative Verification (Based on NWS, NWS-HUN personal communication)
Storm report grouping	Yes (6 minutes)	No
1 storm report verifies 2 overlapping forecasts	No (only first forecast, 1 hit)	Yes (1 hit)
Jump grouping	Yes (6 minutes)	Yes (6 minutes)
False alarm	No report during forecast OR For overlapping forecasts, no report in time period following first forecast expiration	No report during forecast

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Table 4. Total scale attributes using the Schultz et al. verification and alternative verification methodologies.

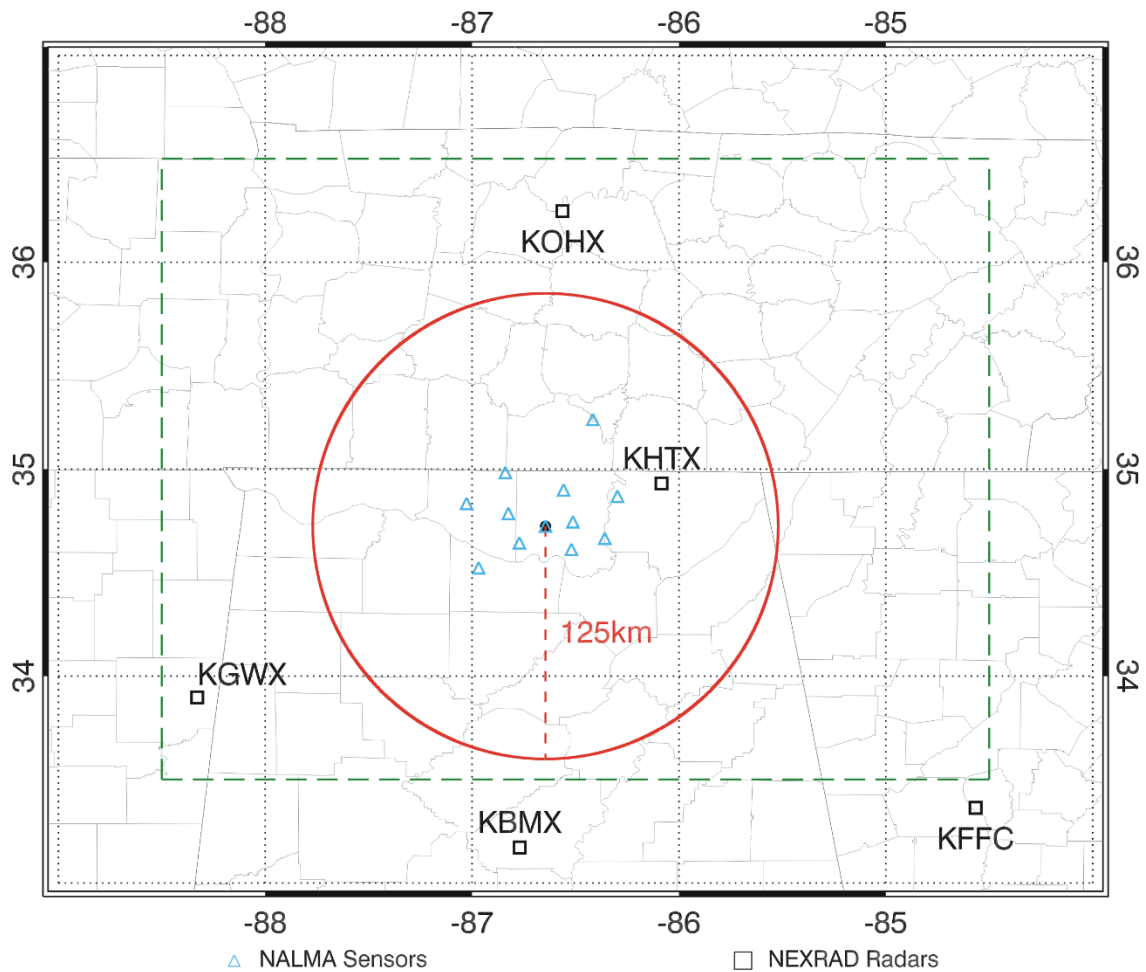
Scale	Clusters	Jumps	False Alarms	Hits	Misses	Alt. False Alarm	Alt. Hits
1	1377	505	378	200	330	344	276
2	1121	724	567	233	311	519	323
3	978	949	760	274	259	705	279
4	842	1044	858	285	219	801	387
5	737	992	769	295	194	725	430
6	583	851	665	291	169	608	410

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542 **Table 5.** Normalized scale attributes by number of clusters using the Schultz et al. and alternative
543 verification methodologies.
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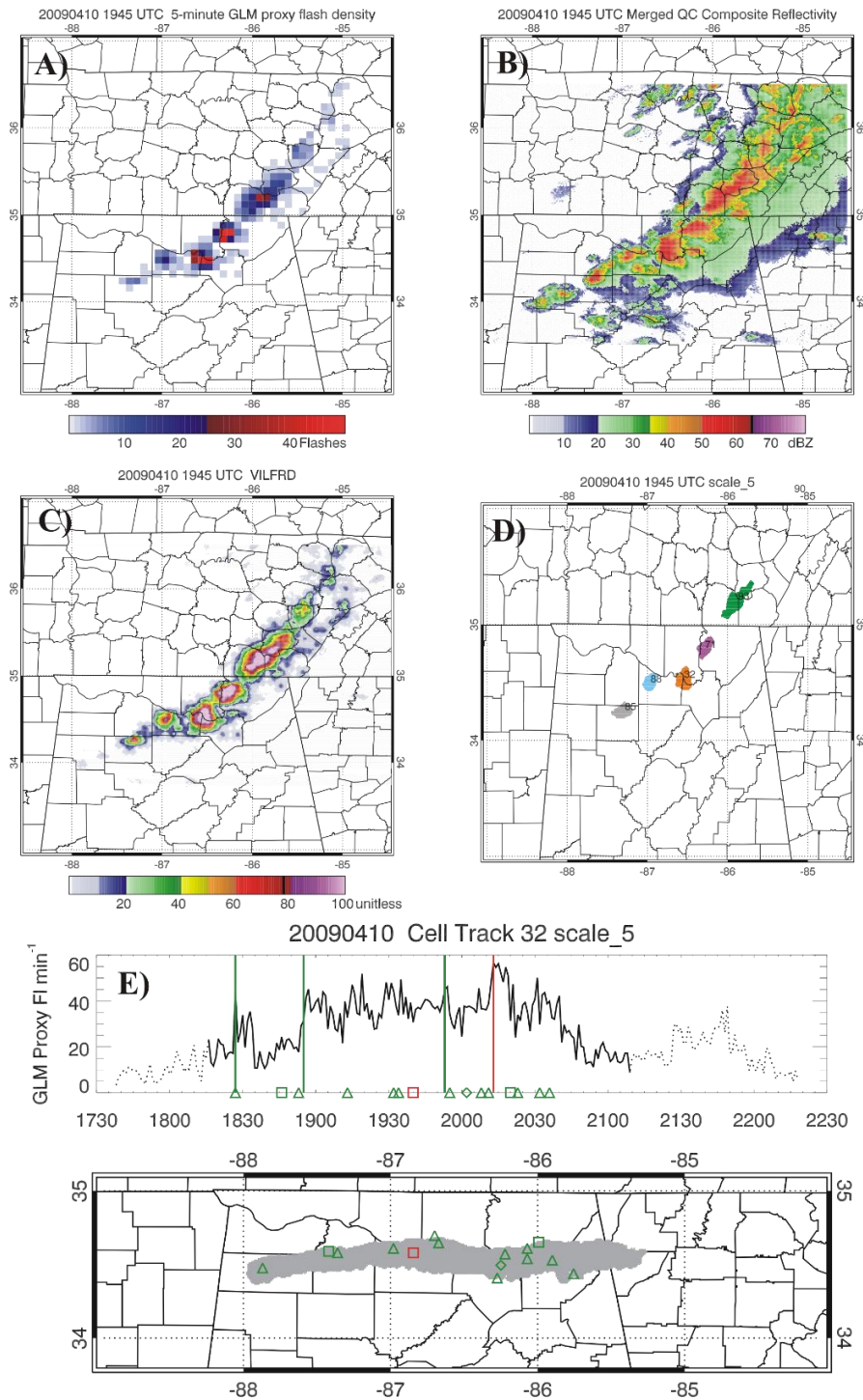
Scale	Jumps	Hits	False Alarms	Misses	Verified Jumps	Alt. False Alarms	Alt. Hits
1	0.37	0.15	0.27	0.24	0.09	0.25	0.20
2	0.65	0.21	0.51	0.28	0.14	0.46	0.29
3	0.97	0.28	0.78	0.26	0.19	0.72	0.29
4	1.24	0.34	1.02	0.26	0.22	0.95	0.46
5	1.35	0.40	1.04	0.26	0.30	0.98	0.58
6	1.46	0.50	1.14	0.29	0.32	1.04	0.70

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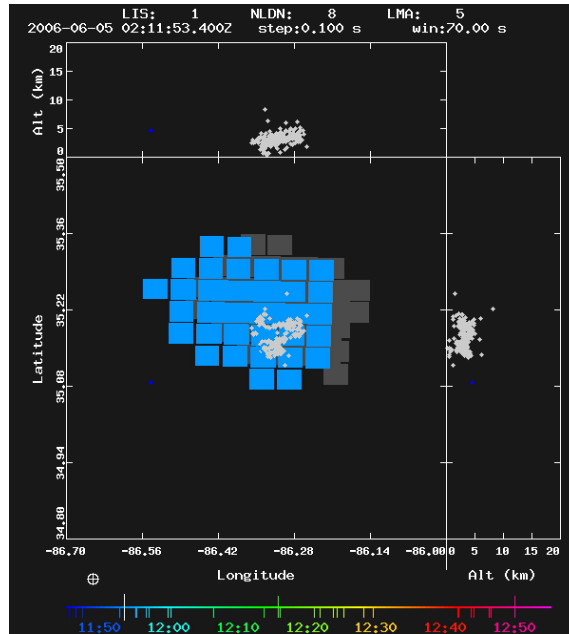
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Figure 1. A diagram of the study’s domain and instrumentation locations. The large rectangle (green dot-dash lines) indicates the domain used in the WDSSII storm tracking algorithms. The red circle indicates the area within 125 km of the center of the NALMA. This is the area used for lightning jump system sensitivity testing and verification. The blue triangles represent NALMA sensors and the black boxes represented NEXRAD radar locations.



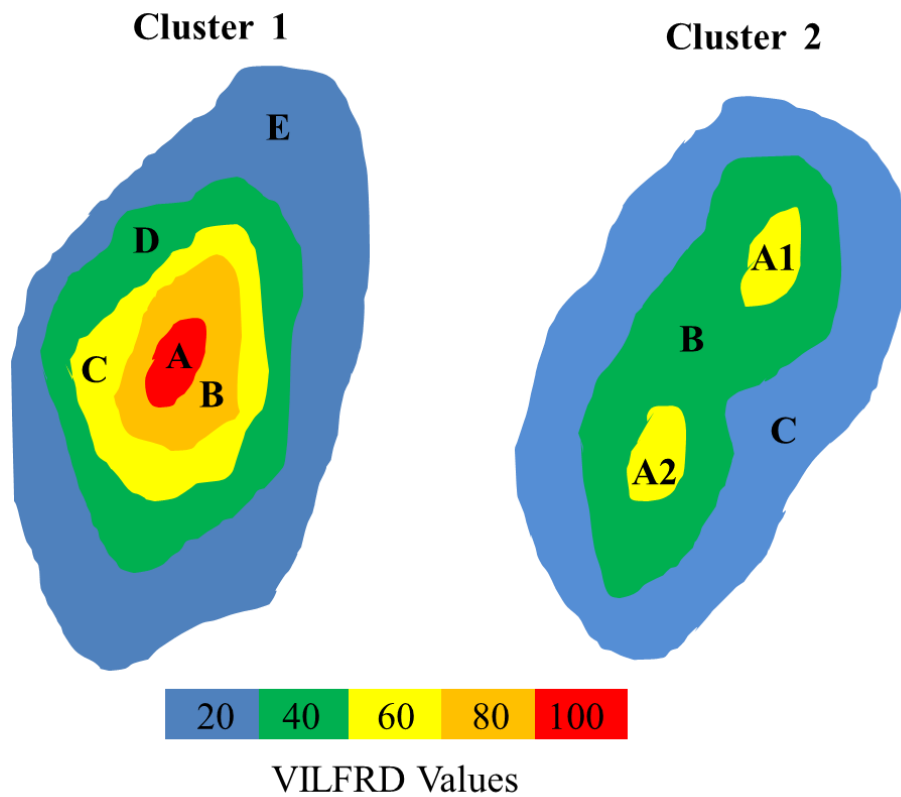
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Figure 2. a) 5-min GLM proxy gridded flash density, b) merged composite reflectivity, c) VILFRD, and d) tracked storm clusters at scale 5 at 1945 UTC on 10 Apr 2009. e) Top panel: Lightning flash rate time series for cell 32 with the timing of lightning jumps depicted by green (hit) and red (false alarm) vertical lines, light gray flash rate (i.e., 1730-1815 and 2120-2230) depicts the time the cluster is outside of the 125 km LMA range. Bottom panel: Cluster footprint with storm reports (green = hit, red = miss) for the LJA from 1730-2230.



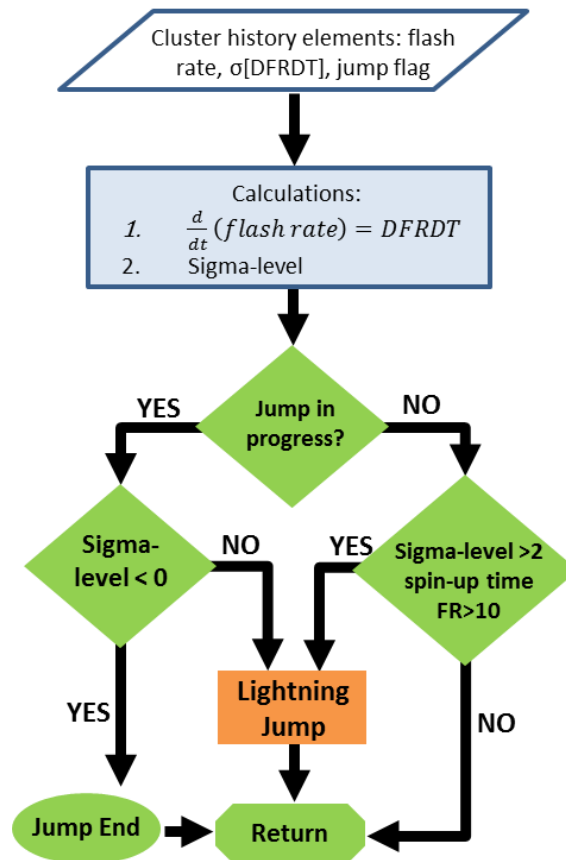
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Figure 3. A comparison of the spatial differences of an example flash between an optical observation from the TRMM-LIS (blue/gray pixels) and the VHF radiation from the North Alabama LMA (gray source points) on 5 June 2006. Each LIS flash location is determined by the amplitude weighted centroid of the groups/events. The LMA flash consist of clustered radiation sources recorded at 80 μ s intervals along the path of the flash.



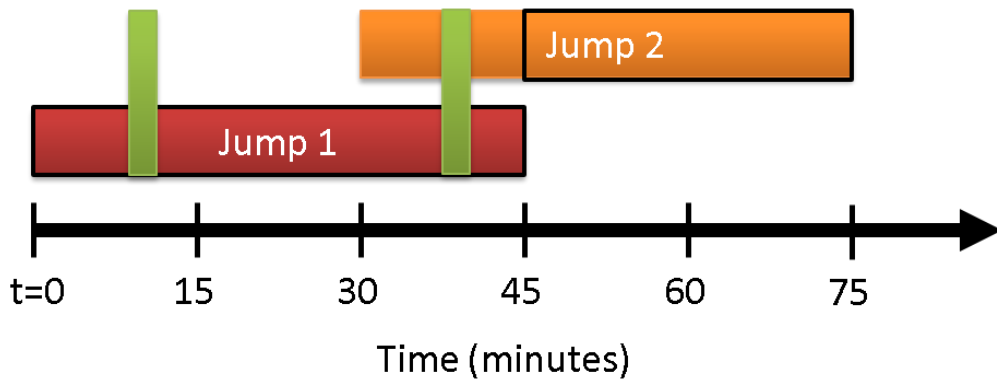
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 570 **Figure 4.** Schematic of two example storm clusters used to describe the VILFRD cluster identification and
 571 tracking process at multiple scales. Scale 1: Left – Cluster A (40 km²), Right – Cluster A1 (35 km²) Cluster
 572 A2 (38 km²). Scale 3: Left – Cluster B (100 km²). Scale 4: Left – Cluster C (150 km²). Scale 5: Left –
 573 Cluster D (200 km²), Right – Cluster B (200 km²). Scale 6: Left – Cluster E (300 km²), Right – Cluster C
 574 (300 km²).

Lightning Jump Process for each cluster



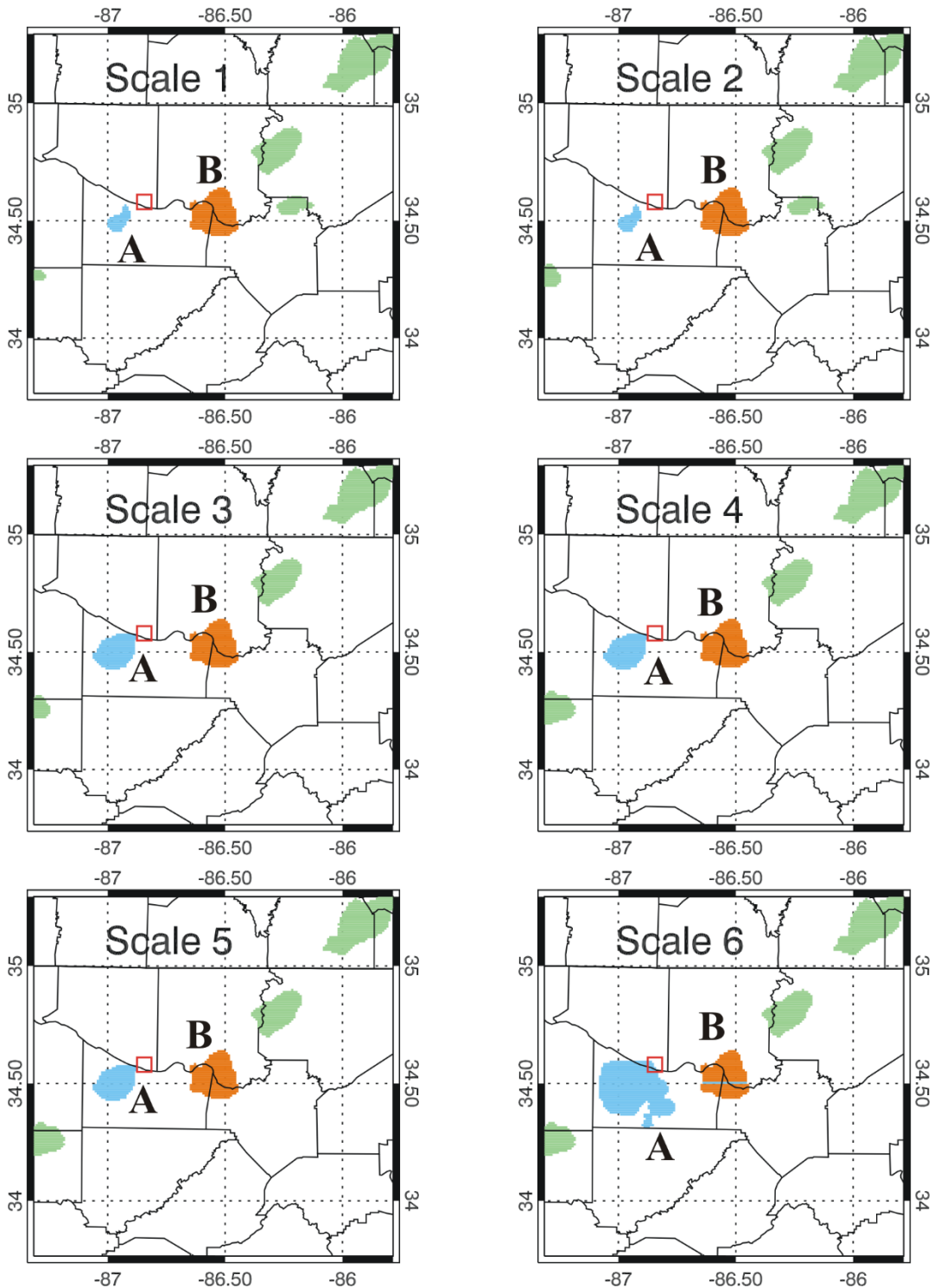
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Figure 5. Flowchart for the lightning jump classification process using the “ 2σ ” algorithm from Schultz et al. (2009).

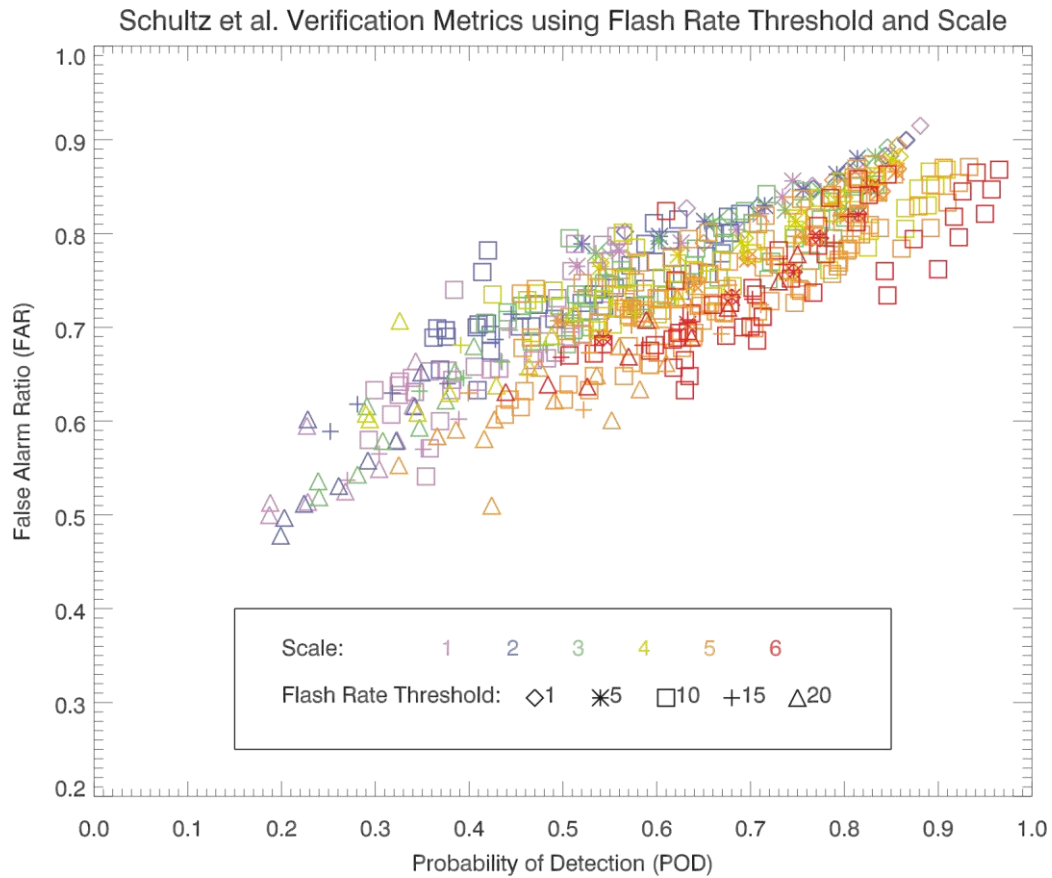


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Figure 6. A schematic of respective verification windows for two lightning jumps (red and orange boxes). Following the verification methodology found in Schultz et al. (2009), only one jump can be verified at a given time with the given example storm reports (vertical green rectangles). Therefore, Jump 2 is not able to validate until after Jump 1’s verification period has ended. The black outlines indicate the valid time period for each jump.



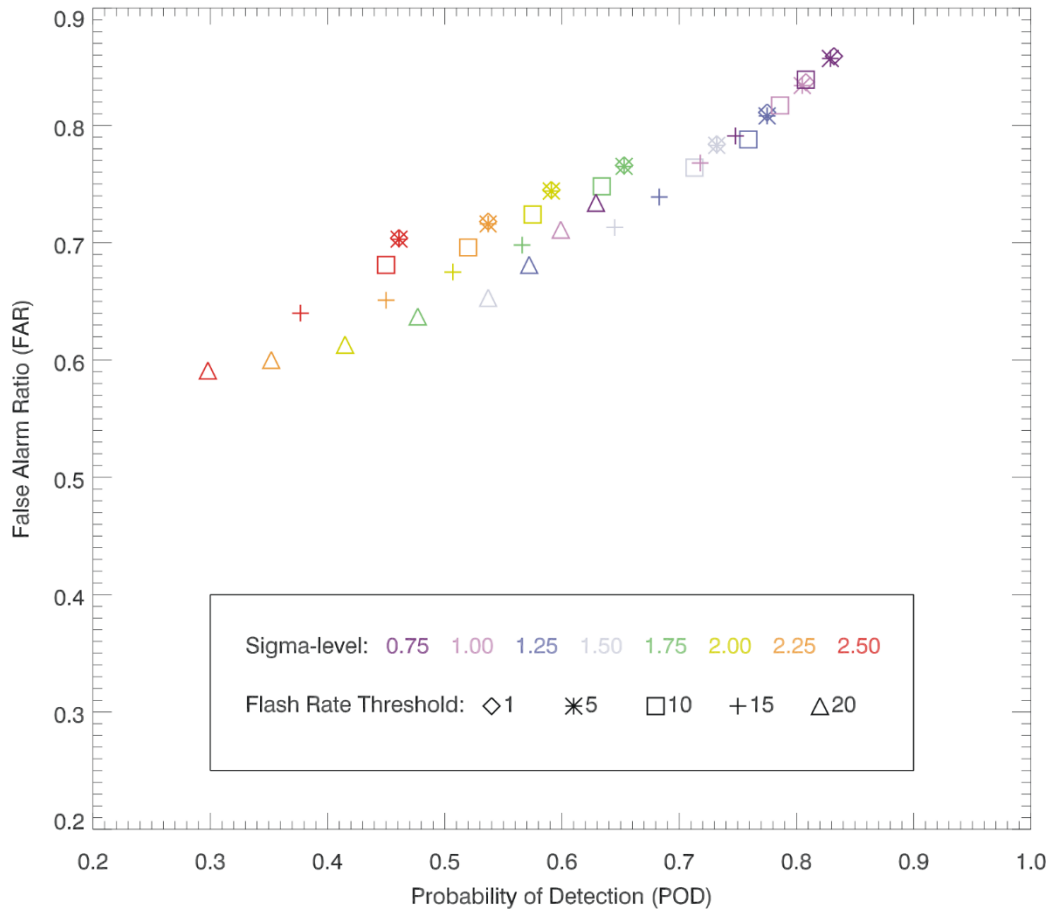
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 587 **Figure 7.** Cluster footprint comparisons for scale 1 (upper left) to scale 6 (lower right) at 1945 UTC on 10
 588 Apr 2009, same time shown as Figure 2. Storm A is blue and the same as cluster 88 in Fig. 2d. Storm B is
 589 in orange and cluster 32 in Fig. 2d. Storm reports are plotted with the red square representing a missed
 590 wind report.



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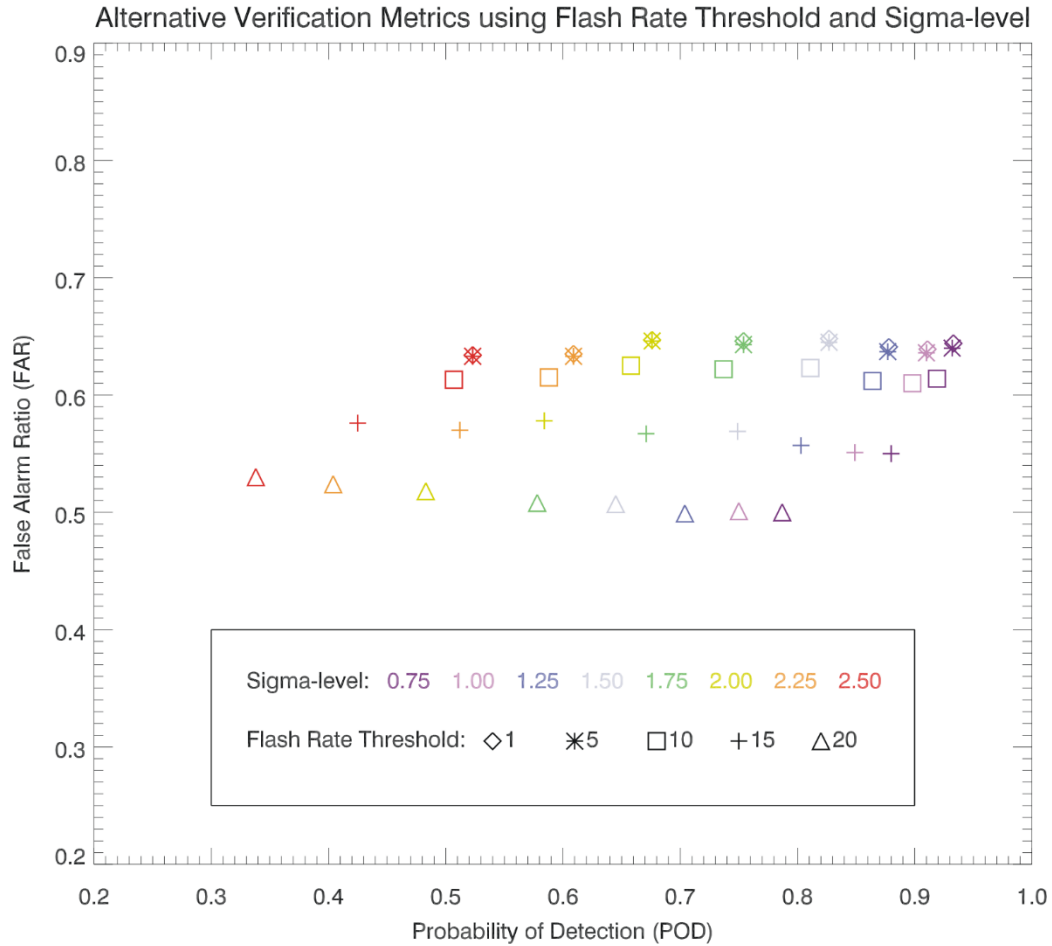
Figure 8. FAR vs. POD comparison of the 6 spatial scales (areal extent). Color represent the spatial scale at which storms are tracked and symbols represent flash rate thresholds for the Schultz et al. (2009) verification methodology. Each symbol represents one iteration of the algorithm for all event days for a set of given parameters.

Schultz et al. Verification Metrics using Flash Rate Threshold and Sigma-level

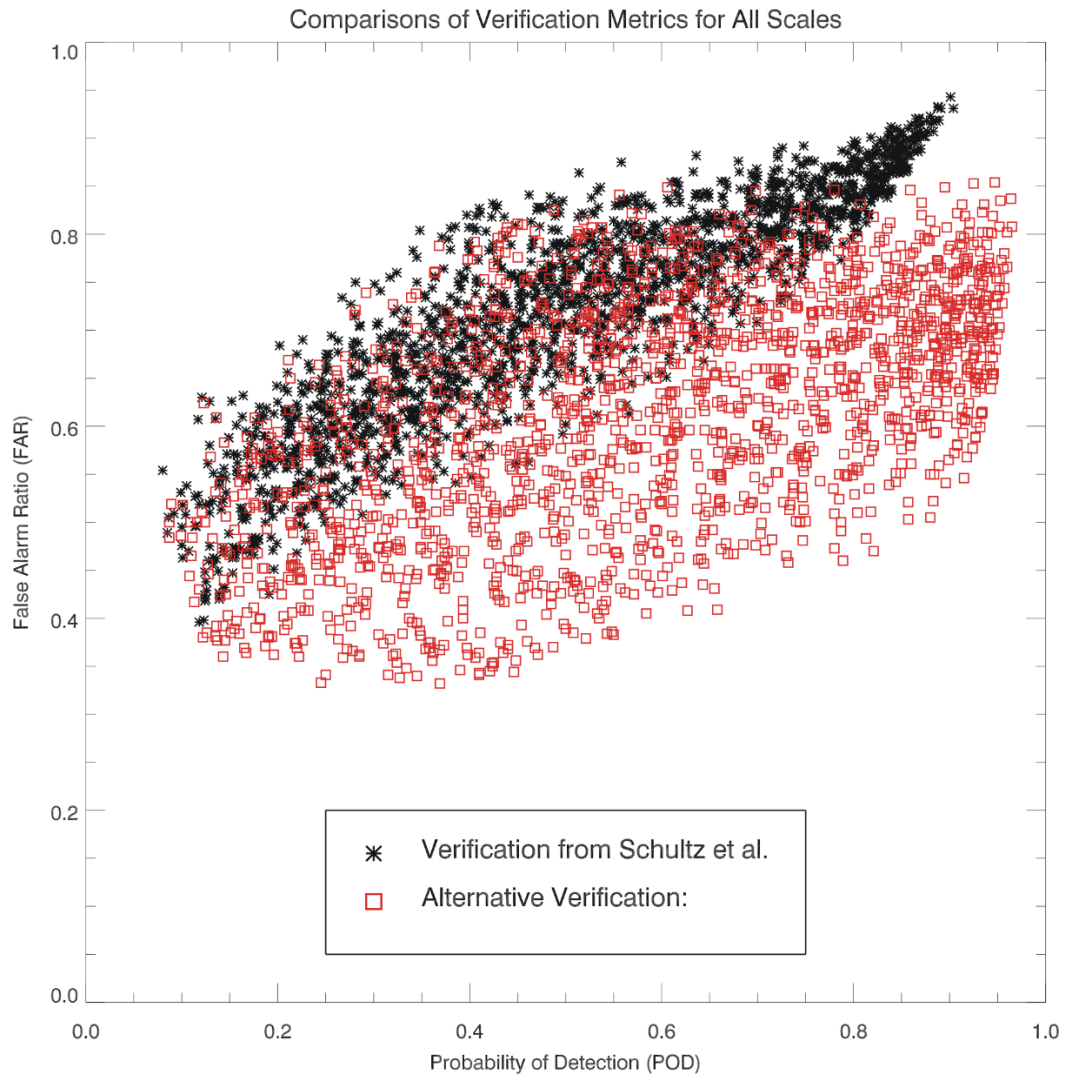


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Figure 9. FAR vs POD comparisons using the Schultz verification methodology showing the relationship of sigma-level (color) and flash rate threshold (symbols) on the algorithm’s performance at spatial scale 5. Flash rate threshold of 1 (diamond) and 5 (asterisk) flashes min^{-1} are very similar at each sigma-level and may be difficult to discern. A linear regression analysis ($y=0.52x+0.40$) for these data resulted in a strong correlation between POD and FAR ($R^2=0.95$). A linear regression analysis while holding each sigma-level constant resulted in $R^2=0.99$ and slopes ranging from 0.57 (at 0.75 sigma-level) to 0.88 (at 2.5 sigma-level).

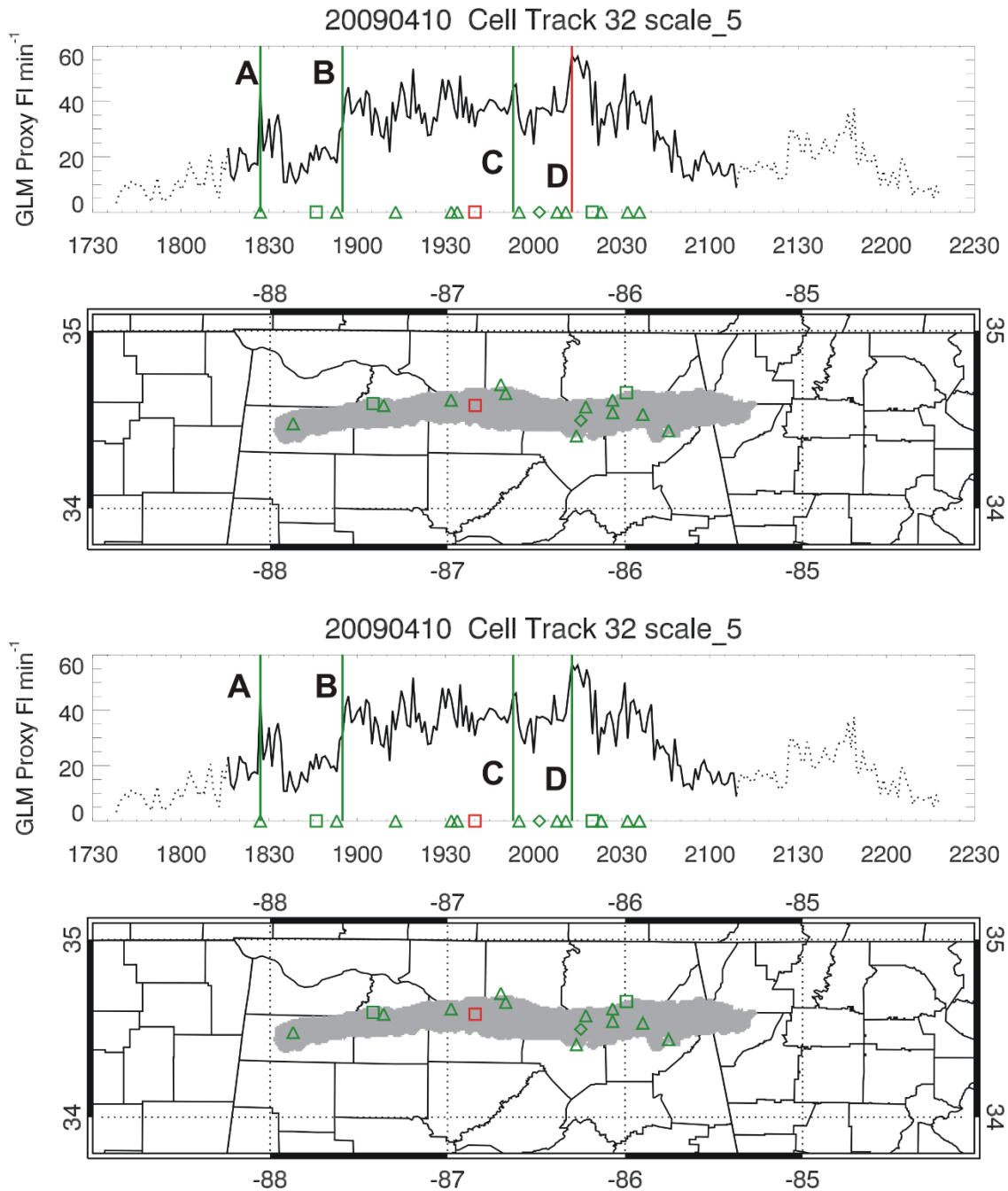


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607 **Figure 10.** FAR vs POD comparisons using the alternative verification method showing the relationship of
608 sigma-level (color) and flash rate threshold (symbols) on the algorithm’s performance at spatial scale 5. A
609 linear regression analysis ($y=0.16x+0.48$) for these data resulted in almost no correlation between POD and
610 FAR ($R^2=0.20$). A linear regression analysis while holding each sigma-level constant resulted in correlation
611 values above 0.9 ($R^2=0.93$ to 0.99) and slopes ranging from 0.99 (at 0.75 sigma-level) to 0.59 (at 2.5 sigma-
612 level).



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Figure 11. A complete dataset distribution, from all ranges of sensitivity testing, showing for FAR vs POD comparisons of the differences between the verification Schultz et al. (2009; black) and alternative (red) verification methodologies.



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Figure 12. Similar to Fig. 2e except a comparison of verification methodology for a single example case. The top half of the figure shows Schultz et al. (2009) verification methodology and the bottom half shows the alternative verification methodology applied. The key difference is the classification of the fourth jump (jump D) as a false alarm in the top image and a hit in the bottom image.