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**On the secondary eyewall formation of  
Hurricane Edouard (2014)**

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## Abstract

19

20 A first observationally-based estimation of departures from gradient wind balance during  
21 secondary eyewall formation is presented. The study is based on the Atlantic Hurricane  
22 Edouard (2014). This storm was observed during the National Aeronautics and Space  
23 Administration's (NASA) Hurricane and Severe Storm Sentinel (HS3) experiment, a  
24 field campaign conducted in collaboration with the National Oceanic and Atmospheric  
25 Administration (NOAA). A total of 135 dropsondes are analyzed in two separate time  
26 periods: one named the *secondary eyewall formation* period and the other one referred to  
27 as the *decaying-double eyewalled storm* period. During the secondary eyewall formation  
28 period, a time when the storm was observed to have only one eyewall, the diagnosed  
29 agradient force has a secondary maxima that coincides with the radial location of the  
30 secondary eyewall observed in the second period of study. The maximum spin up  
31 tendency of the radial influx of absolute vertical vorticity is within the boundary layer in  
32 the region of the eyewall of the storm and the spin up tendency structure elongates  
33 radially outward into the secondary region of supergradient wind, where the secondary  
34 wind maxima is observed in the second period of study. An analysis of the boundary-  
35 layer averaged vertical structure of equivalent potential temperature reveals a  
36 conditionally unstable environment in the secondary eyewall formation region. These  
37 findings support the hypothesis that deep convective activity in this region contributed to  
38 spin up of the boundary layer tangential winds and the formation of a secondary eyewall  
39 that is observed during the *decaying-double eyewalled storm* period.

40 **1) Introduction**

41 Secondary eyewalls are structures concentric to the primary eyewall of tropical cyclones  
42 and are characterized by maxima in tangential winds and convective activity. Given their  
43 frequency of occurrence (Hawkins and Helveston 2004, 2008; Kuo et al. 2008), their  
44 relationship with intensity change (e.g. Willoughby 1982; Houze et al. 2007; Yang et al.  
45 2013), their association with longer duration of higher storm intensity (Kuo et al 2009)  
46 and their linkage to storm growth (Maclay et al. 2008), there is great interest in  
47 developing secondary eyewall forecasting tools. Today, the valuable and sophisticated  
48 forecasting tools tend to rely on empirical relationships (e.g. Kossin and Sitkowski 2009)  
49 and do not necessarily directly incorporate the physical processes of secondary eyewall  
50 formation.

51

52 Secondary eyewall formation dynamics have been the subject of intense contemporary  
53 research and contrasting views of the azimuthally averaged dynamics prevail. One line of  
54 thought suggests that the boundary layer contributes to the formation of secondary  
55 eyewalls by its participation in a feedback between a local enhancement of the radial  
56 vorticity gradient above the boundary layer, a corresponding frictional updraft and  
57 increased convective intensity (Kepert 2013). This view is based on the conception that  
58 linearized idealizations of the boundary layer of the hurricane inner core are useful  
59 representations of the dynamics of such regions of the storm (Kepert 2001; Kepert and  
60 Wang 2001). In this view, supergradient winds are a result of the existence of eyewalls  
61 and not precursors of them.

62

63 Another view of the role of boundary layer dynamics in secondary eyewall formation  
64 envisions the Eliassen axisymmetric balanced vortex dynamics being an appropriate  
65 framework to describe secondary eyewall formation and evolution (e.g. Zhu and Zhu  
66 2012). In this view, proposed initially by Shapiro and Willoughby (1982), the boundary  
67 layer plays a role only as a sink of tangential momentum. In this model, the boundary  
68 layer acts to spin down the tangential wind in the layer. Studies, like that of Rozoff et al.  
69 2012, focus on the balanced aspects of the problem.

70

71 In contrast with the two foregoing lines of thought, another perspective suggests that  
72 nonlinear boundary layer dynamics are essential to secondary eyewall formation and  
73 evolution (Huang et al. 2012; Abarca and Montgomery 2013; Abarca and Montgomery  
74 2014). Huang et al. (2012) proposed that secondary eyewall formation is a progressive  
75 process that begins with a broadening of the tangential winds above the boundary layer,  
76 which is then followed by an increase of boundary layer inflow and amplification of the  
77 tangential wind in the boundary layer. The radial region of strong boundary layer  
78 convergence is associated with the generation of supergradient winds in and just above  
79 the boundary layer. These supergradient winds act in the radial momentum equation to  
80 arrest the inflow and cause a vertical eruption of moist air out of the boundary layer. In  
81 this model, the rising moist air will induce deep convection if the local environment  
82 supports convective instability.

83

84 The foregoing views highlight distinct and largely incompatible physical processes in the  
85 secondary eyewall formation problem. Despite their contrasting nature, these views have

86 been invoked recently as acting simultaneously in a positive feedback process (e.g. Sun et  
87 al. 2013). In the current debate regarding the essential role of boundary layer dynamics in  
88 secondary eyewall formation a key point is *the existence of supergradient winds prior to*  
89 *the presence of the secondary eyewall itself.*

90

91 While most secondary eyewall studies have been based on numerical evidence, some are  
92 based on observations. Remote-sensing observational data of secondary eyewalls using  
93 various satellite microwave channels have resulted in useful knowledge of their  
94 frequency of occurrence around the world (e.g. Kuo et al. 2009; Yang et al. 2013). *In-situ*  
95 observations of secondary eyewalls have confirmed, *inter alia*, the existence of  
96 supergradient flow in the secondary eyewall (Didlake and Houze 2011; Bell et al. 2012).  
97 Using a model-derived dataset based on observations collected during the Tropical  
98 Cyclone Structure-2008 (TCS-08) field experiment (Elsberry and Harr, 2008), Huang et  
99 al. (2012) suggested that secondary eyewalls can be potentially predicted by diagnosing  
100 supergradient flow during secondary eyewall formation. To the knowledge of the authors,  
101 there has not been an attempt to assess the existence of supergradient flow in the  
102 boundary layer and its potential ramifications during secondary eyewall formation. In the  
103 light of the foregoing discussion, it is scientifically relevant to investigate the role of the  
104 boundary layer in supporting the formation of secondary eyewalls.

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106 In the remainder of this article, we examine the secondary eyewall event of Hurricane  
107 Edouard (2014). Our emphasis is on the formation period of Edouard's secondary  
108 eyewall as captured jointly by in-situ observations made during the 2014 phase of the

109 National Aeronautics and Space Administration's (NASA) Hurricane and Severe Storm  
110 Sentinel (HS3) experiment (Braun et al. 2015) and Intensity Forecasting Experiment  
111 (IFEX, Rogers et al. 2013) research flights by the Hurricane Research Division of the  
112 National Oceanic and Atmospheric Administration (NOAA). Section 2 details the data  
113 and methodologies applied in the analysis of this work. Section 3 describes the synoptic  
114 evolution of Hurricane Edouard. Section 4 presents the scientific findings of this study.  
115 Section 5 offers conclusions and recommendations.

116

## 117 **2) Summary of Hurricane Edouard (2014)**

118 Figure 1 shows the track, maximum 1-min sustained surface winds, and minimum surface  
119 pressure of Edouard, as reported by the Best-Track dataset (Jarvinen et al. 1984). The  
120 storm developed from a tropical wave accompanied by a broad low pressure system and  
121 disorganized deep convection. The system was designated a tropical depression on 11  
122 September and maintained a northwestward motion (Figure 1) for five days as it moved  
123 around the southwestern periphery of a subtropical ridge. Slow, but steady, strengthening  
124 occurred while the cyclone moved northwestward, with the system becoming a tropical  
125 storm on 12 September, a hurricane on 14 September, and a major hurricane on 16  
126 September. Based on HS3 and satellite observations Braun et al. (2016) documented  
127 storm intensity and structural changes between 15 UTC 14 September and 09 UTC 15  
128 September. The intensity changes included significant intensification before 00 UTC 15  
129 September and weakening afterwards. They also included evidence of asymmetric  
130 eyewall convection and the existence of a larger eye at the end of the period than at its  
131 beginning. At 1500 UTC 14 September the storm exhibited strong winds in the

132 northeastern quadrant (their Figure 4a), including an asymmetric secondary wind  
133 maxima. The radius of maximum winds was ~25 km and the secondary wind maxima  
134 was located ~50 km from the center of the storm. At 1315 UTC 15 September  
135 2014 (their Fig. 3f) the eye had a radius about 4-5 times larger than seen earlier  
136 (their Fig. 3c). The authors interpreted such evolution as a possible eyewall replacement  
137 cycle, although as they show, there is no evidence of a concentric wind and precipitation  
138 maxima and at that time, and the storm was a Category 1 in the Saffir-Simpson scale.

139 Based on microwave satellite imagery [85/91 GHz brightness temperatures of 180-225 K  
140 (red to yellow shading) in the inner 150 km of the storm), Figure 1 shows observational  
141 evidence that Edouard evolved from a storm with a single eyewall on 15 September to  
142 one with a secondary eyewall on 17 September. The aircraft-borne data (as shown in  
143 upcoming sections) suggest that a secondary eyewall formed between these observation  
144 periods. For this reason, the time interval spanning the first set of observations will be  
145 referred to as the secondary eyewall formation period. After reaching its peak intensity  
146 (on 16 September), Edouard weakened quickly at a rate of  $20 \text{ m s}^{-1}$  per day.

147 The eyewall replacement cycle that took place, along with cold upwelling/mixing (of  
148 about  $7^\circ\text{C}$  (Stewart 2014, their Figure 5), were likely factors involved in the initial  
149 weakening of Edouard's maximum intensity. The vertical wind shear had a magnitude of  
150  $5\text{-}9 \text{ m s}^{-1}$  (Figure 1) for most of the intensification period of the storm and during the first  
151 6 hours of its weakening. At the time of its peak intensity, the storm changed its  
152 movement from northwestward to northeastward ahead of an approaching mid-latitude  
153 trough. After the initial 6 hours of weakening, the vertical wind shear magnitude

154 dropped relatively rapidly, and it then slowly increased over the following two days up to  
155 a value of  $17 \text{ m s}^{-1}$  on 19 September as the storm became embedded in the mid-latitude  
156 westerlies. On 19 September, Edouard was downgraded to a tropical storm and on 21  
157 September, it merged with a frontal system (Stewart, 2014).

158

### 159 **3) Data and methodology**

160 The data used in this study consists of GPS dropsondes deployed from the unmanned  
161 Global Hawk as part of the HS3 campaign (Wick 2015) and the NOAA G-IV jet and WP-  
162 3Ds as part of the NOAA IFEX program, the National Hurricane Center (NHC)–Tropical  
163 Prediction Center (TPC) Best-Track dataset, the Statistical Hurricane Intensity Prediction  
164 Scheme (SHIPS) 200-850 hPa vertical wind-shear analyses (DeMaria and Kaplan, 1994;  
165 DeMaria and Kaplan, 1999; and DeMaria et al., 2005) and 85/91 GHz microwave  
166 satellite imagery from the Defense Meteorological Satellite Program (DMSP)  
167 microwave imagers [Special Sensor Microwave Imager (SSM/I; F-15) and the  
168 Special Sensor Microwave Imager/ Sounder (SSMIS; F-18)].

169 This study focuses on two study periods defined by the dropsonde availability. The first  
170 study period is referred to hereafter as the *secondary eyewall formation period*. This  
171 period uses 48 GPS dropsondes deployed from the NOAA research missions on 15 Sep  
172 between 14:13 UTC and 19:20 UTC. The flights are NOAA 42 (13 GPS dropsondes;  
173 while 14 GPS dropsondes were deployed, the 1802 UTC drop had no altitude information  
174 and was not included in this study), NOAA 43 (19 GPS dropsondes) and NOAA 49 (16  
175 GPS dropsondes). The GPS dropsondes during the secondary eyewall formation period



176 were deployed at about 700 hPa pressure altitude, which roughly corresponds to 3-km  
177 height.

178 The second period of study is referred to hereafter as the *decaying double eyewalled*  
179 *storm*. It includes 87 GPS dropsondes (Black et al. 2011) deployed from the Global Hawk  
180 at altitudes of ~17-19 km during the period from 16 Sep 1506 UTC to 17 Sep 0828 UTC.  
181 While three NOAA research missions deployed 52 GPS dropsondes between 16 Sep  
182 1357 UTC and 17 Sep 1656 UTC (i.e. within our second period of study), these GPS  
183 dropsondes were mostly deployed in the south-southwest region of the storm. This  
184 quadrant of the storm was characterized by inflow throughout the troposphere (not  
185 shown) and is not representative of the azimuthal averages aimed in this study (see  
186 below). As a result, these NOAA GPS dropsondes deployed on 16-17 Sep are not  
187 included in this work.

188 The Best Track tropical cyclone latitude, longitude, and intensity (originally every 6  
189 hours) were linearly interpolated to a temporal frequency of 10-minutes. The 10-minute  
190 storm center was then used to determine the storm-relative location of GPS dropsondes  
191 throughout their descent. Figure 2 shows the radial and azimuthal locations of all GPS  
192 dropsondes relative to the center of the storm. Note in the figure the homogeneity of the  
193 azimuthal distribution of the dropsondes and the high density of data within 400 km from  
194 the storm center. The dropsondes are also well distributed in the observation periods with  
195 about 10 GPS dropsondes per hour in the secondary eyewall formation period and about  
196 5 dropsondes per hour in the decaying double-eyewalled storm period.

197

198 The secondary eyewall formation period spans 5 hours. This unprecedented observational  
199 density of the phenomena offers a unique opportunity to capture essentially a snap shot of  
200 the storm's processes resulting in the secondary eyewall. The decaying double-eyewalled  
201 storm observation period spanned 18 hours. During this time the inner core of the storm  
202 evolved substantially as the eyewall replacement was taking place, and here the  
203 observations are not to be interpreted as a snap shot of the storm, but rather diagnosing  
204 the processes that were ongoing during the 18 hours.

205

206 The GPS dropsonde wind and pressure/temperature/humidity observations have a  
207 frequency of 4 Hz and 2 Hz respectively and were interpolated to a uniform vertical grid  
208 with 301 points with 50 m of distance between grid points. This choice of vertical  
209 resolution represents a reduction of resolution from the original ~10 m. Such reduction  
210 does not impact the conclusions of this study. The lowest point was chosen at 10 m  
211 height and highest point was chosen at 15,010 m. Each GPS dropsonde profile  
212 interpolated to the fixed vertical grid was assigned to a radial bin according to the radial  
213 location of its deployment. In this work, it is assumed that the storm is axisymmetric  
214 enough to get estimates of the azimuthal averages of the different variables by averaging  
215 all GPS dropsondes available in a given radial bin. The radial bins are uniformly  
216 distributed using a subjective criterion as a compromise between number of radial bins  
217 and number of GPS dropsondes in each bin. For the secondary eyewall formation period,  
218 the radial bins are centered at 8.7, 22.5, 32.5, 48.8, 69.6, 101.0, 150.0, 212.5, and 305.0  
219 km radius (Figures 4-6) and for the decaying double-eyewalled storm the radial bins are  
220 centered at 5.0, 16.3, 31.3, 51.3, 76.3, 121.3, 188.8, 255.0, 322.5, 400.0, 475.0, 550.0 and

221 720.0 km (Figure 3). While GPS dropsondes drift radially as they descend through the  
 222 troposphere, such displacements are smaller than the radial length of the bins considered  
 223 in this study. The results discussed here are robust to data being assigned to radial bins  
 224 using their individual radius, irrespective of the dropsonde they belong to. The data is  
 225 also robust to different bin-length choices (not shown).

226

227 The quantities reported by the GPS dropsondes used in this study are height<sup>1</sup>, horizontal  
 228 wind velocities, pressure, temperature and relative humidity. We present results of  
 229 composite (azimuthally averaged) quantities derived as described above, of (storm-  
 230 relative) radial and tangential velocities, relative humidity and the following quantities:  
 231 radial vorticity flux  $-u\zeta_a$  (where  $\zeta_a = \partial v / \partial r + v / r + f$  is the azimuthally averaged absolute  
 232 vertical vorticity,  $r$  is the radial distance,  $v$  is the azimuthally averaged tangential  
 233 velocity, and  $f$  the Coriolis parameter at the latitude of the measurement, equivalent  
 234 potential temperature  $\theta_e$ , as defined by the Bolton formula (Bolton 1982), and the  
 235 *agradiant force per unit mass*, as defined by Smith *et al.* (2009):

236

$$AF = -\frac{1}{\rho} \frac{\partial p}{\partial r} + \frac{v^2}{r} + fv$$

237 where the indicated variables have their usual meaning,  $\rho$  is the azimuthally averaged  
 238 density (computed with the equation of state), and  $p$  is the azimuthally averaged  
 239 pressure. The centrifugal and Coriolis forces are computed at every measurement  
 240 location, then interpolated to the vertical grid and finally composited, similar to the other

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<sup>1</sup> Using geopotential height renders plots virtually indistinguishable from those presented here (not shown).

241 quantities, into the radial bins introduced above. The radial derivatives (e.g. pressure  
242 gradient in the computation of the gradient force) are computed as centered differences,  
243 based on the radial grid introduced above. One-sided centered differences are used in the  
244 first and last radial grid points.

245

#### 246 **4) Results**

247 Figure 3 shows the estimated azimuthal average tangential velocity during the double-  
248 eyewalled storm period along with the radial location of the GPS dropsondes as discussed  
249 in Section 2. The tangential velocity exhibits a deep cyclonic circulation extending  
250 through the troposphere to an altitude in excess of 15 km within 100 km radius. The  
251 cyclonic circulation extends outwards to approximately 600 km and is surrounded by an  
252 anticyclonic circulation confined to the upper troposphere between 200 km and 500 km  
253 and that deepens with increasing radius beyond 500 km. The dropsonde analysis reveals  
254 two maxima in the tangential wind field. The inner maximum is located in the radial bin  
255 centered at 31.3 km radius. The outer maximum is located in the radial bin centered near  
256 100 km radius. These wind maxima are approximately superposed with convective  
257 maxima in the storm, as evidence by microwave imagery (e.g. Figure 1). This combined  
258 evidence establishes the existence of a secondary eyewall in the second period of  
259 observation.

260

261 Figures 4 and 5 show the composite analysis during the secondary eyewall formation  
262 period. The figures include the radial location of the dropsondes in the analysis (Section  
263 2) and focus on the lower troposphere below 3 km within 310 km radius of the storm

264 center. This focus enables one to examine the physical processes of secondary eyewall  
265 formation in the boundary layer, the region containing the tangential wind maxima in  
266 both the primary and secondary eyewalls. Figure 4a shows the composite tangential  
267 velocity. This variable reaches its maximum (of roughly  $60 \text{ m s}^{-1}$ ) at 310-m altitude and  
268 25-km radius. At all altitudes observed in the domain, the tangential wind decreases  
269 monotonically with radius beyond the radius of maximum tangential wind and there is no  
270 evidence of a secondary wind maximum. Along with the satellite imagery corresponding  
271 to 15 Sep (Figure 1), the data demonstrate the one-eyewall configuration of the storm at  
272 the time of the analysis.

273

274 Figure 4b shows the composite agradient force during the secondary eyewall formation  
275 period. As expected, the agradient force in the outer region of the domain is relatively  
276 weak and negative i.e. the force is directed radially inward. Because the pressure gradient  
277 is essentially independent of height in the boundary layer, the inward directed agradient  
278 force is a reflection of the frictional reduction of the tangential wind and related reduction  
279 of the (outwardly directed) centrifugal and Coriolis forces. In the inner region of the  
280 vortex, the agradient force has two distinct regions of positive values. A positive  
281 agradient force implies that the tangential winds are supergradient. A positive agradient  
282 force in the boundary layer is dynamically important because it acts to arrest the inflow  
283 and influences where the air ascends into the vortex interior. In the presence of a  
284 convectively unstable environment, air lifted out of the boundary layer can reach its level  
285 of free convection and result in deep convective activity.

286 One of the regions of positive agradient force corresponds to the eyewall of the storm.

287 This region roughly extends radially from 10 to 65 km radius. This region of  
288 supergradient flow exhibits a maximum agradient force of several hundred  $\text{m s}^{-1} \text{hr}^{-1}$ .  
289 Large values of agradient force are expected in the boundary layer of the primary eyewall  
290 (Smith et al. 2009, Kepert and Wang 2011) of the storm and have been shown to extend  
291 vertically upwards several kilometers (e.g. Abarca and Montgomery 2014).

292 There is a second region of positive agradient force that is distinct from that of the  
293 primary eyewall. This region of supergradient flow roughly extends from 90 to 150 km  
294 radius (Fig. 4b). The maximum agradient force in this region surpasses  $20 \text{ m s}^{-1} \text{hr}^{-1}$ .  
295 Within the constraints of the radial and temporal sampling of the data, the secondary  
296 maxima in agradient force coincides with the radial location of the secondary eyewall  
297 observed in the second period of observation of this study, as discussed above (Figure  
298 3a). The secondary maximum in the agradient force occurs before the secondary  
299 tangential wind maximum is observed. The existence of this secondary agradient force  
300 maximum supports the hypothesis that the processes of secondary eyewall formation are  
301 underway.

302 Figure 5 shows the estimated azimuthally averaged radial flow, absolute vorticity, and  
303 radial vorticity flux. The azimuthally averaged radial flow is characterized by large  
304 inflow at the lowest levels, with inflow larger than  $2 \text{ m s}^{-1}$  below about 1-km height. This  
305 layer of strong inflow is due primarily to the agradient force (Smith *et al.*, 2009; Bui *et*  
306 *al.*, 2009). In the analyzed grid (lowest vertical level at 10 m and 50 m vertical grid  
307 spacing), the vertical location of the inflow maxima increases with radius, going from 10  
308 m to about 110 m height. The low elevation of the inflow maxima is consistent with fluid  
309 dynamical considerations for a swirling-flow boundary layer (e.g. Bo Dewadt, 1940;

310 Schlichting, 1968, chapter 11) and with observations of a mature hurricane (e.g.  
311 Montgomery et al. 2014). In the domain, there are two extended regions of outflow. One  
312 corresponds to the eyewall of the storm, located above 700-m height, between 30- and  
313 70-km radius. Within the analysis domain, the outflow reaches its maximum at 2.3 km  
314 height in the radial bin centered near 50-km radius. The other extended region of outflow  
315 is roughly located between 85- to 170-km radius and between about 1.7- and 2.1-km  
316 height.

317 Figure 5b shows the estimated azimuthally averaged absolute vorticity. In the inner core  
318 of mature tropical cyclones, this field is generally characterized by a central region of  
319 large vorticity surrounded by a skirt of smaller values (Mallen et al. 2005). Not  
320 withstanding the limitations of the data, the overall vorticity structure is as expected, with  
321 the largest values in the innermost points. The absolute vorticity structure includes a  
322 monotonic decrease of vorticity with radius above 1-km height. The field exhibits no  
323 discernable relative maxima of vorticity near the top of the boundary layer. Near 211 km  
324 radius, there is a small relative maximum in vorticity below 1 km.

325 Figure 5c shows the estimated mean radial absolute vertical vorticity flux (hereafter  
326 radial vorticity flux), as it appears in the right hand side of the tangential momentum  
327 equation (with a minus sign, see Eq. 4 in Abarca and Montgomery 2013). Radial vorticity  
328 flux is a key diagnostic of whether the secondary eyewall formation process is underway  
329 at the time analyzed. We present radial vorticity flux as it can be directly interpreted as a  
330 term in the tangential tendency equation, but we note here that such a quantity only  
331 differs from the radial advection of absolute angular momentum by a factor of  $r$ . From  
332 the perspective of the azimuthally averaged system-scale flow, the radial vorticity flux is

333 one of the dominant terms in the tangential tendency equation during spinup of tropical  
334 cyclones in general (Ooyama 1969, Willoughby 1995, Smith et al. 2009), and during  
335 secondary eyewall formation in particular (e.g. Abarca and Montgomery 2013, their  
336 Figure 5). The maximum spin up tendency of the vorticity flux is within the boundary  
337 layer in the region of the eyewall of the storm and it elongates radially outward into the  
338 secondary region of supergradient wind where the secondary wind maxima is observed in  
339 the second period of study. Note that while the secondary eyewall formation is underway,  
340 there is no evidence of a vorticity bump above the boundary layer (Figure 5b) to support  
341 the idea that secondary eyewall formation is a feedback process that begins once a local  
342 vorticity maximum is present above the boundary layer (Kepert 2013, Kepert and Nolan  
343 2014).

344

345 To gain additional insight into the relevant physical processes in the boundary layer of  
346 the storm during this early period of study, we calculate the vertical average of radial  
347 inflow. Collapsing the data in this way helps highlight the bulk features of the storm's  
348 boundary layer as it is undergoing secondary eyewall formation. Figure 6a shows the  
349 storm-relative radial velocity averaged below 1 km height (the results here after are not  
350 dependent on the choice of height, they are robust to other choices, like 0.8, 0.9 and 1.2  
351 km, not shown). As suggested by Figure 5a, this height is chosen as the nominal depth of  
352 the boundary layer as it contains the region of relatively strong inflow. Figure 6a shows  
353 that, at the time of the analysis, the radial inflow depicts a structure with two maxima.  
354 The primary inflow maximum is at the radial bin centered near 30 km radius and is  
355 associated with the primary eyewall. The secondary inflow maximum is located at the



356 radial bin centered near 100 km radius. It can be shown that the double inflow maximum  
357 structure cannot be explained by an argument based on frictional stress alone. The  
358 secondary inflow maximum can be explained plausibly by the action of the positive  
359 agradient force shown in Figure 4b around the interval centered near 100-km radius. As  
360 discussed above, this force field acts to arrest the inflow and promote ascent of moist air  
361 out of the boundary layer.

362

363 Figure 6b shows the composite vertical profile of the equivalent potential temperature  
364 ( $\theta_e$ ) and the corresponding saturated equivalent potential temperature ( $\theta_{es}$ ) at the radial  
365 bin centered near 100 km radius. The figure depicts a conditionally unstable environment  
366 in the secondary eyewall formation region. As an example, if one vertically averages  $\theta_e$  in  
367 the lowest 200 m, this renders a mean value of 349.6 K. A parcel lifted from 100 m with  
368 such a  $\theta_e$  would acquire positive buoyancy above about 1-km height (e.g., Holton 2004).  
369 Thus, this thermodynamic structure is capable of supporting deep convective activity in  
370 the radial region of secondary eyewall formation.

371

## 372 **Conclusions**

373 Secondary eyewall formation (SEF) dynamics have been the subject of intense  
374 contemporary research and contrasting views of the SEF azimuthally averaged dynamics  
375 prevail. In an effort to help provide an improved understanding of the physical processes  
376 controlling the formation of secondary eyewalls in real storms, we presented herein an  
377 estimation of azimuthally-averaged dynamical and thermodynamical fields derived from  
378 in-situ observations during SEF. The case study is that of Atlantic Hurricane Edouard

379 (2014). This storm was intensely observed during the 2014 phase of the NASA HS3  
380 experiment, in conjunction with NOAA IFEX research flights by the Hurricane Research  
381 Division. A total of 135 GPS dropsondes were analyzed. The GPS dropsondes were  
382 deployed in two time periods: one named the *secondary eyewall formation* period (48  
383 dropsondes deployed on 14 Sep within 5 hours) and the other one referred to as the  
384 *decaying-double eyewalled storm* period (87 GPS-dropsondes deployed on 16-17 Sep  
385 within 18 hours).

386

387 During the period designated as the secondary eyewall formation period, the estimates of  
388 azimuthally-averaged fields reveal that the storm had a single tangential wind maximum.  
389 During the double eyewall storm period, the azimuthally-averaged wind data confirmed a  
390 double tangential wind maximum, with the tangential wind maxima located within the  
391 boundary layer of the storm. During the secondary eyewall formation period, the  
392 agradient force had a secondary maxima that coincided with the radial location of the  
393 secondary eyewall observed in the second period of study. The storm-relative radial  
394 velocity averaged below 1 km height depicted a structure with two maxima, with the  
395 secondary inflow maximum coinciding with the radial location of the secondary eyewall  
396 observed in the second period of study. The maximum spin up tendency of the radial  
397 influx of absolute vertical vorticity was within the boundary layer in the region of the  
398 eyewall of the storm and it elongated radially outward into the secondary region of  
399 supergradient wind, where the secondary wind maxima was observed in the second  
400 period of study. An analysis of the average vertical structure of potential temperature  
401 revealed a conditionally unstable environment in the secondary eyewall formation region.

402

403 The evidence presented supports the hypothesis that secondary eyewall formation is  
404 underway during the first period of observations and the underlying mechanisms at work  
405 are in line with the dynamical and thermodynamical processes as articulated in Smith et  
406 al. (2009) and Huang et al. (2012).

407

408 The vertical coherence of the azimuthally-averaged estimates (using the 2-4 Hz GPS  
409 dropsonde observations interpolated to a regular vertical grid with spacing of 50 m) and  
410 the robustness of the results to radial bin choices suggest that the data presented herein is  
411 physically meaningful and useful.

412

413 In the light of the results presented, it is scientifically desirable from the operational point  
414 of view to investigate the role of the boundary layer in supporting the formation of  
415 secondary eyewalls in other observational cases. Analogous estimates of the quantities  
416 examined here in other storms are recommended to assess the generality of the results.

417

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425 School.

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548 study, between 09/16 15:06:37 UTC and 09/17 08:28:03 UTC is highlighted with  
549 solid thick lines. Also shown are the shear magnitude (blue line) and direction  
550 (green line), as captured by Statistical Hurricane Intensity Predictor Scheme (SHIPS).

551 **Figure 2.** Locations of dropsonde deployments, relative to the storm center, during  
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554 08:28 UTC). The concentric circles indicate the radial distance (in km) from the  
555 center of the storm.

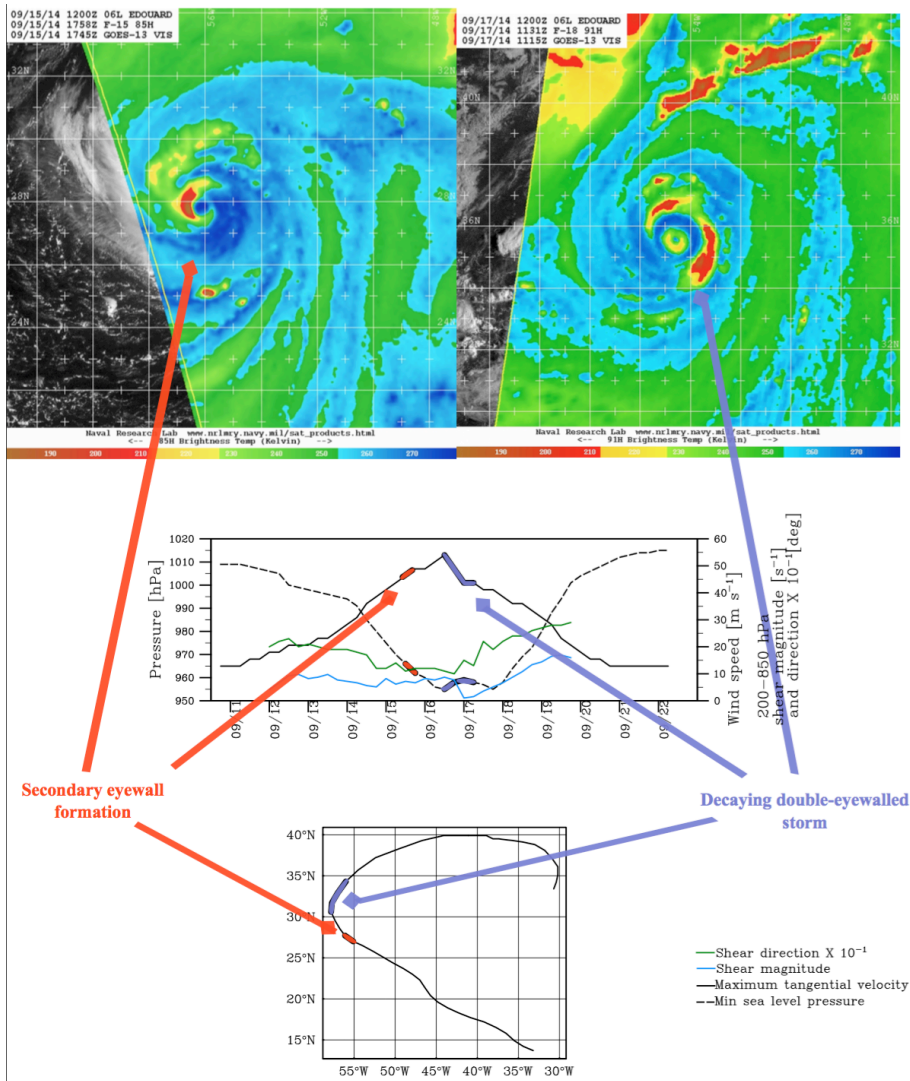
556 **Figure 3.** Composite a) tangential wind velocity ( $\text{m s}^{-1}$ ), and b) radial location of the  
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561 the radial location of the center of the analysis bins. The bins are delimited by the  
562 locations of the vertical blue lines. The numbers superposed on the red lines  
563 indicate the number of dropsondes in each radial bin (see text for further details).

564 **Figure 4.** Composite a) tangential wind velocity ( $\text{m s}^{-1}$ ), b) Agradient Force ( $\text{m}^2 \text{s}^{-1}$   
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577 shades of blue. For b) the color bar indicates only positive values. (See text for  
578 further details.)

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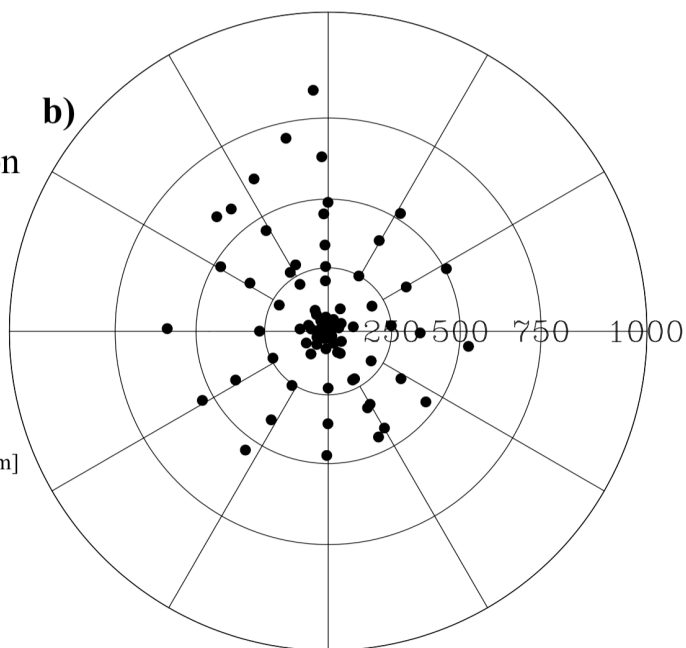
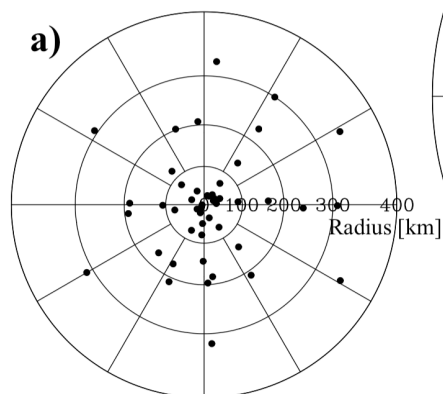
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Decaying double-eyewalled storm  
9/16 15:06 UTC - 9/17 08:28 UTC

Secondary eyewall formation  
9/15 14:13 - 19:20 UTC

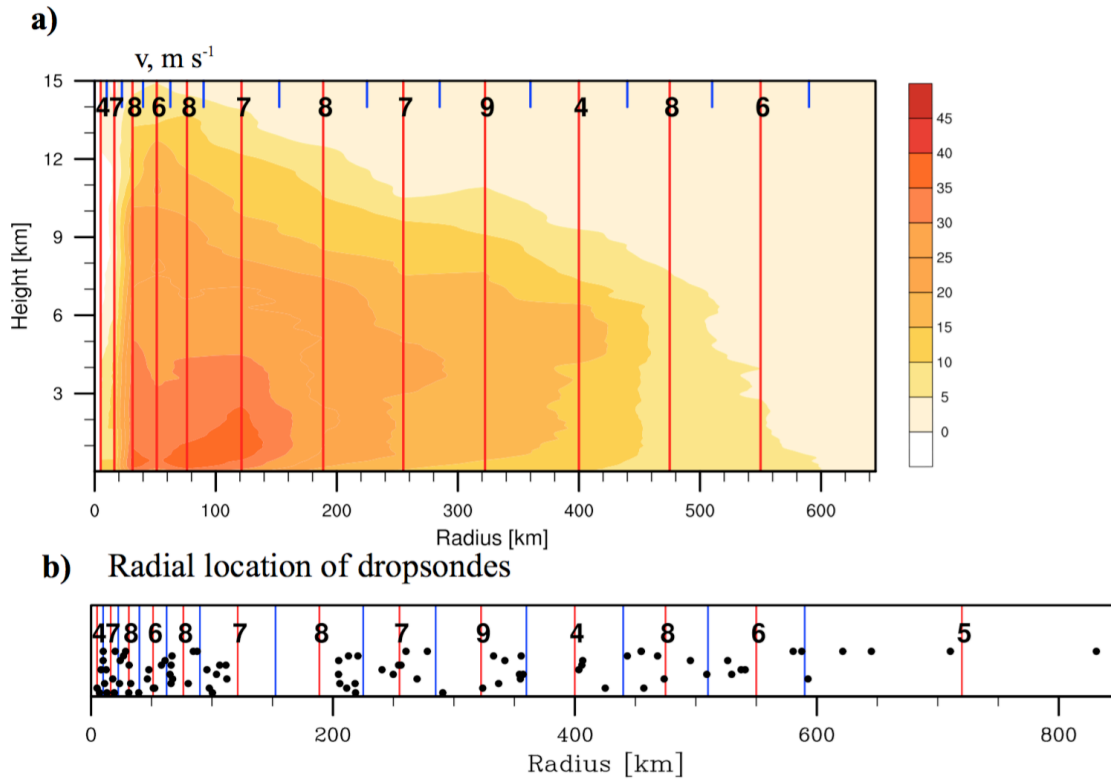


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601 (b).)

# Decaying duple-eyewalled storm



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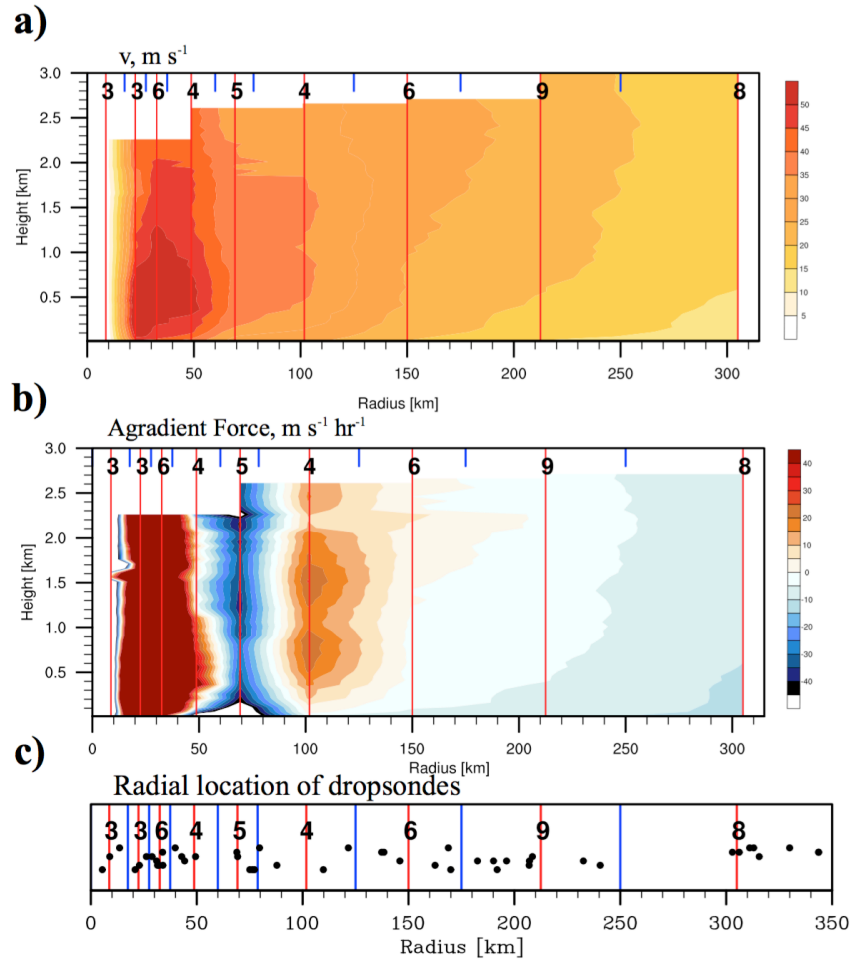
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612

## Secondary eyewall formation



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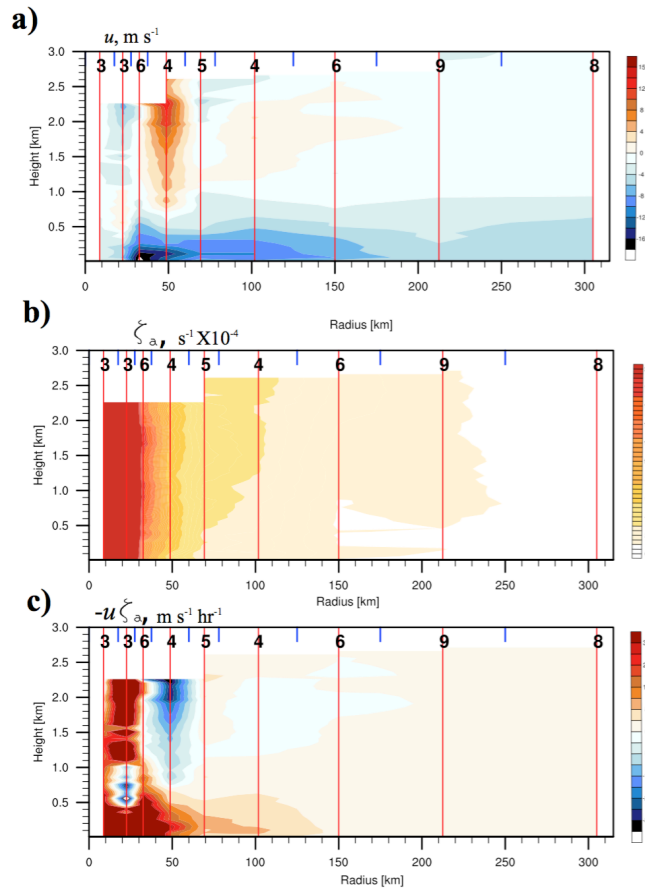
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## Secondary eyewall formation



623

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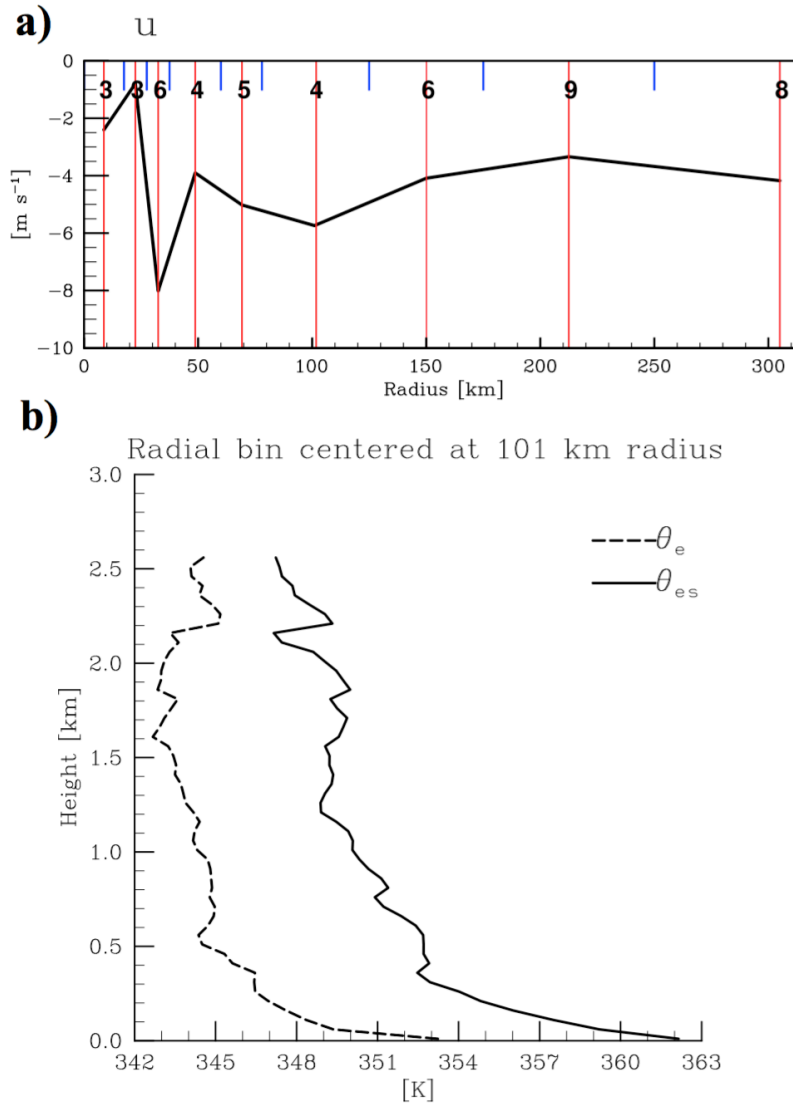
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