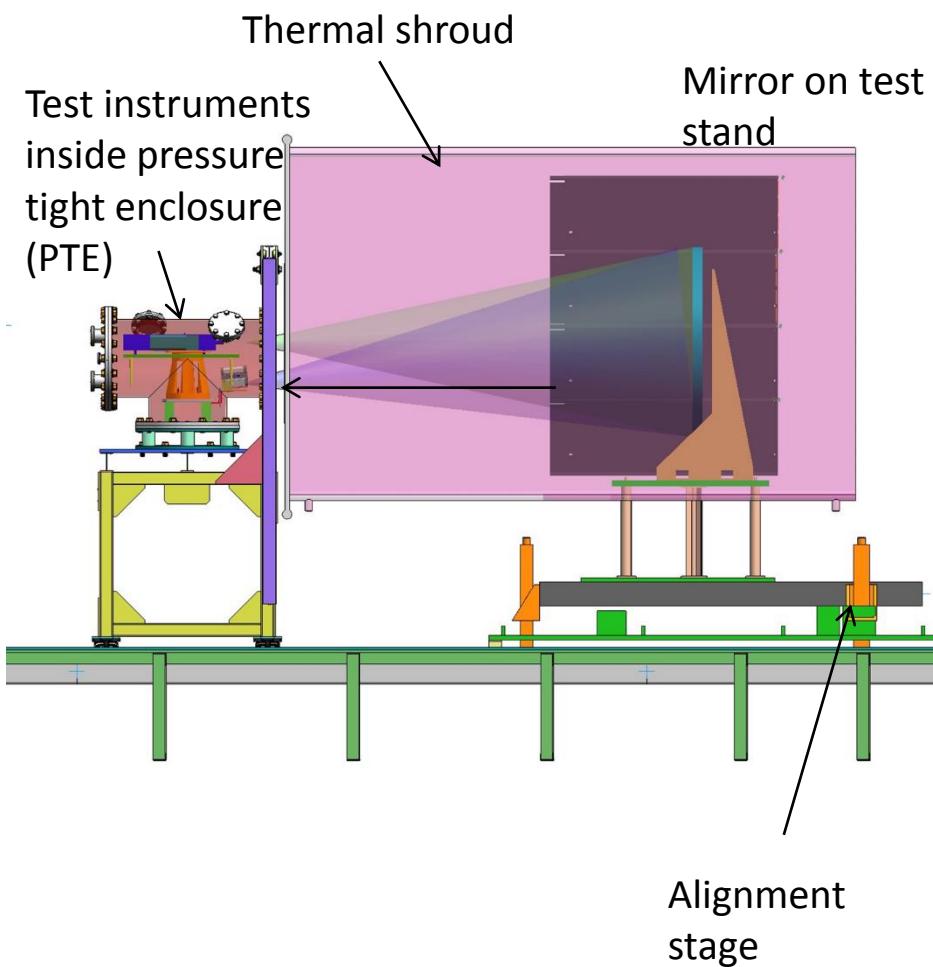
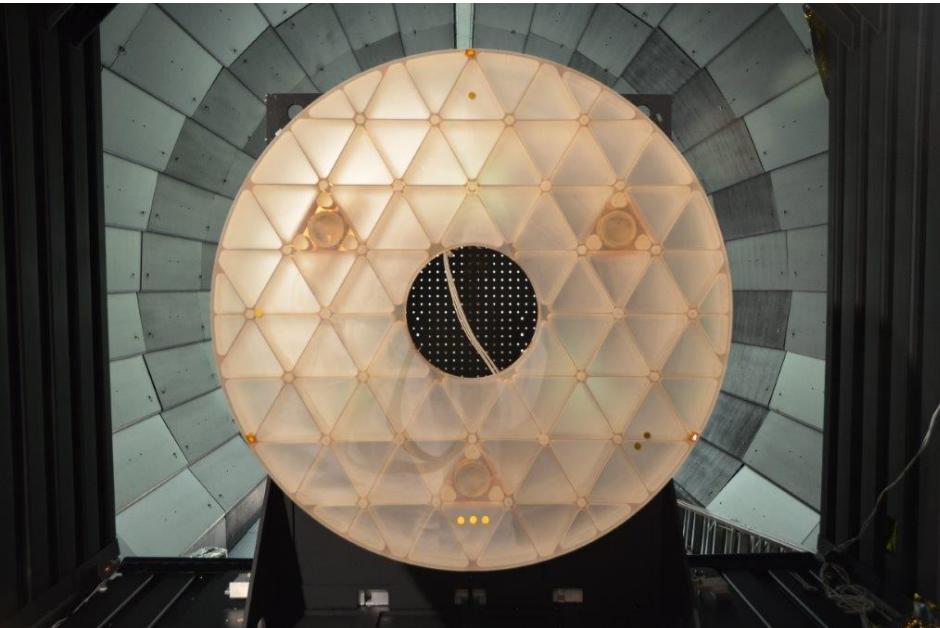


Modeling the Extremely Lightweight Zerodur Mirror (ELZM) thermal soak test

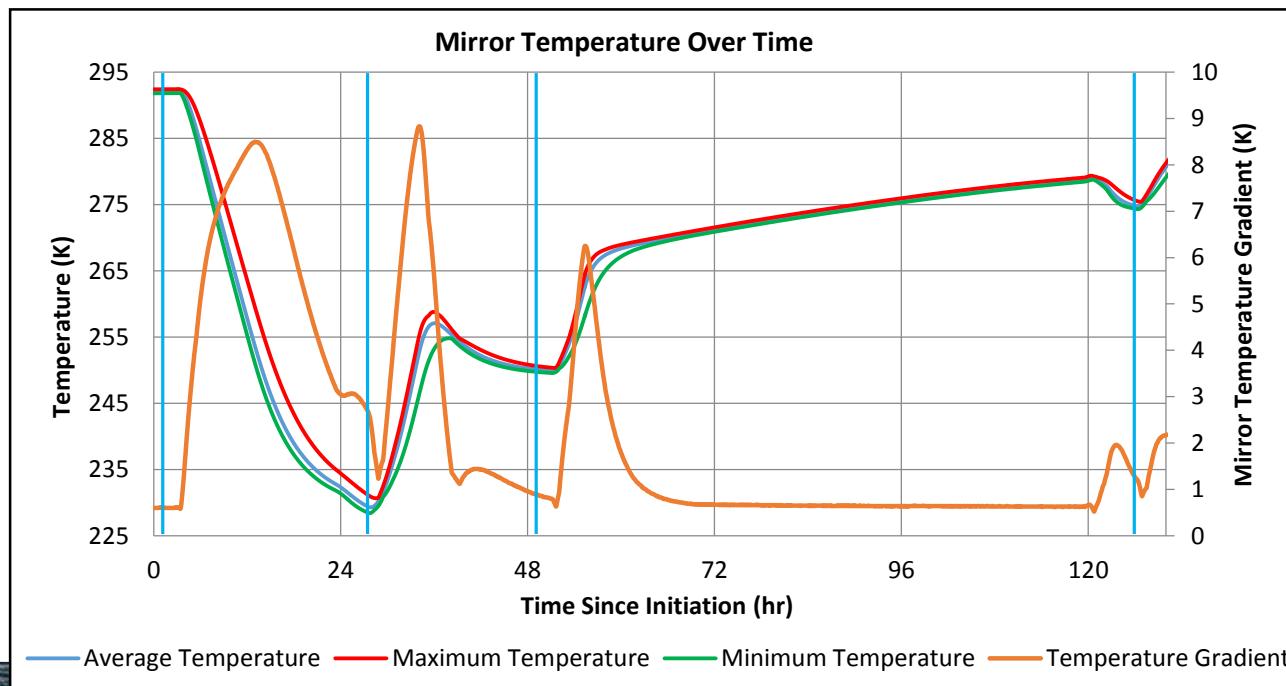
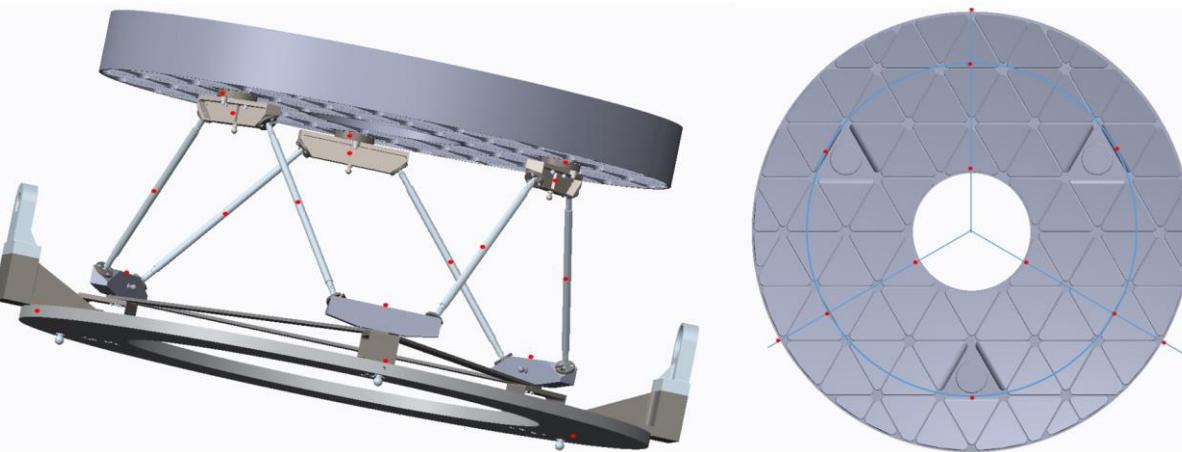
Thomas Brooks
Marshall Space Flight Center

256.797.3147

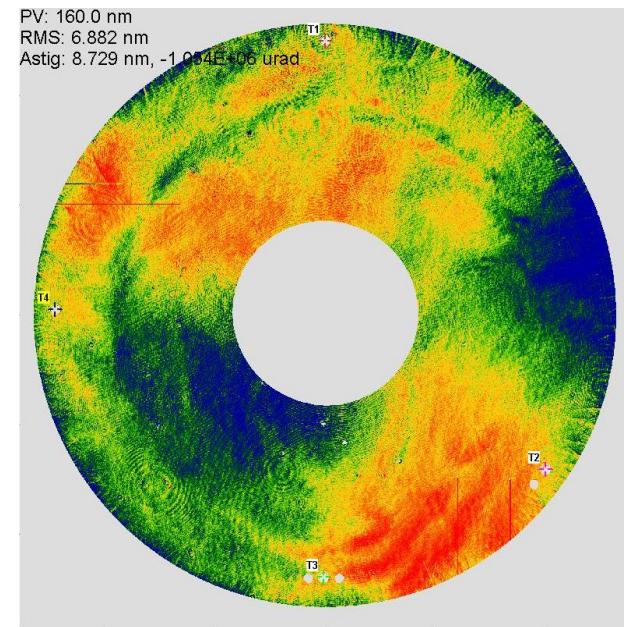
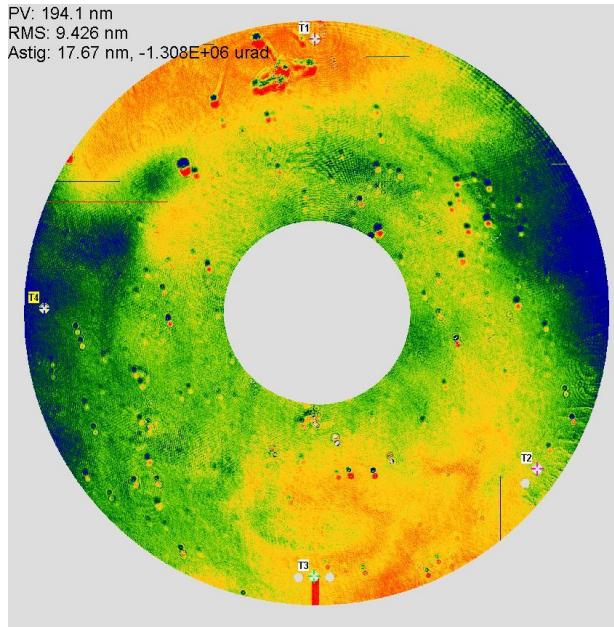
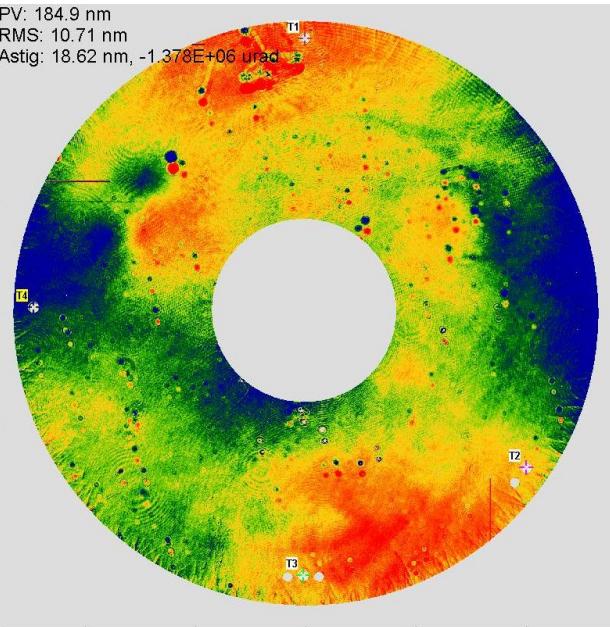
Opto-thermal test of Zerodur Mirror



Temperature Measurements



Surface Measurements



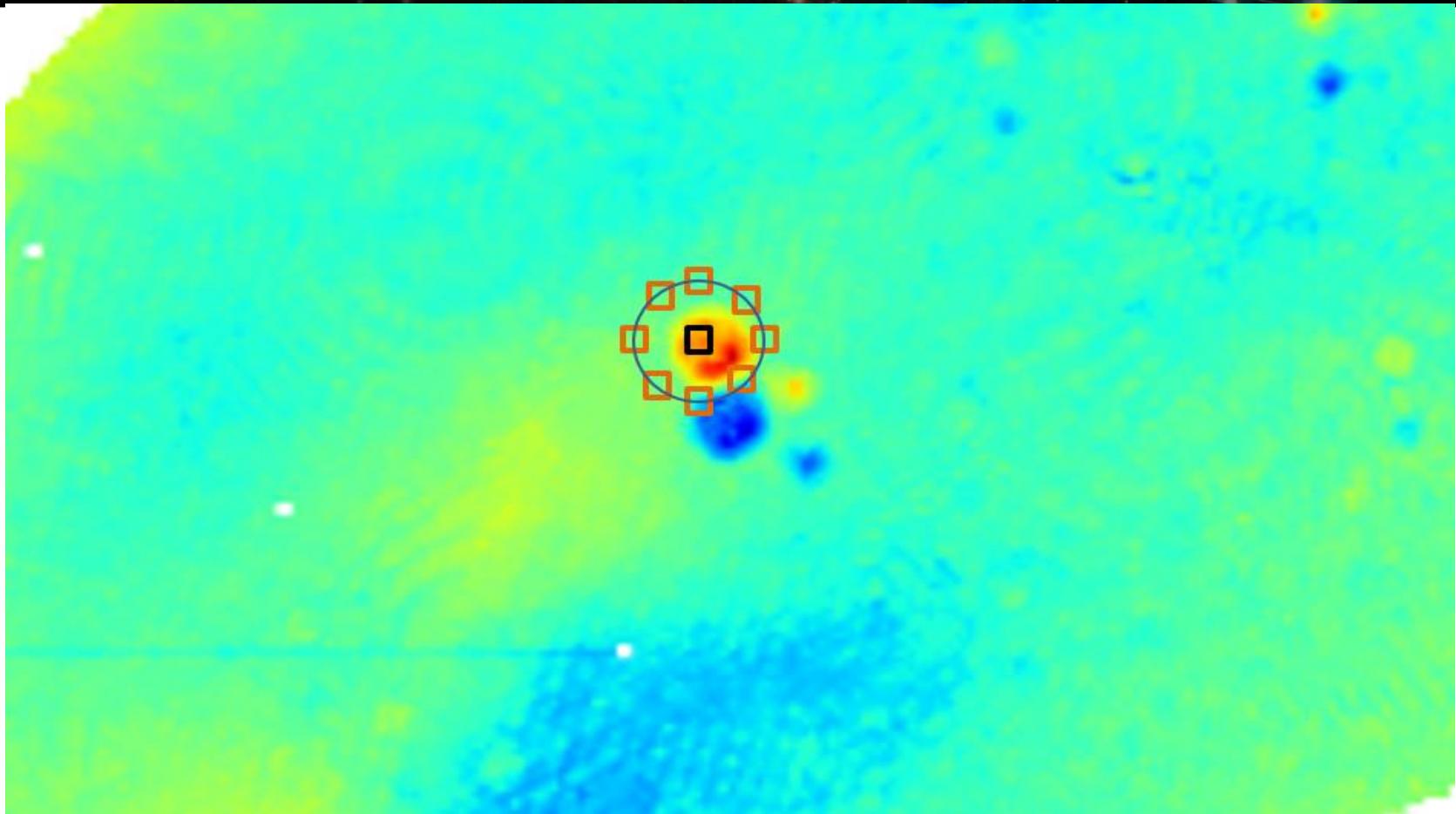
Surface at 230K - Surface at 292K
RMS SFE = 10.7nm
P-V SFE = 185nm

Surface at 250K - Surface at 292K
RMS SFE = 9.4nm
P-V SFE = 194nm

Surface at 275K - Surface at 292K
RMS SFE = 6.9nm
P-V SFE = 160nm

Test Repeatability of 6nm

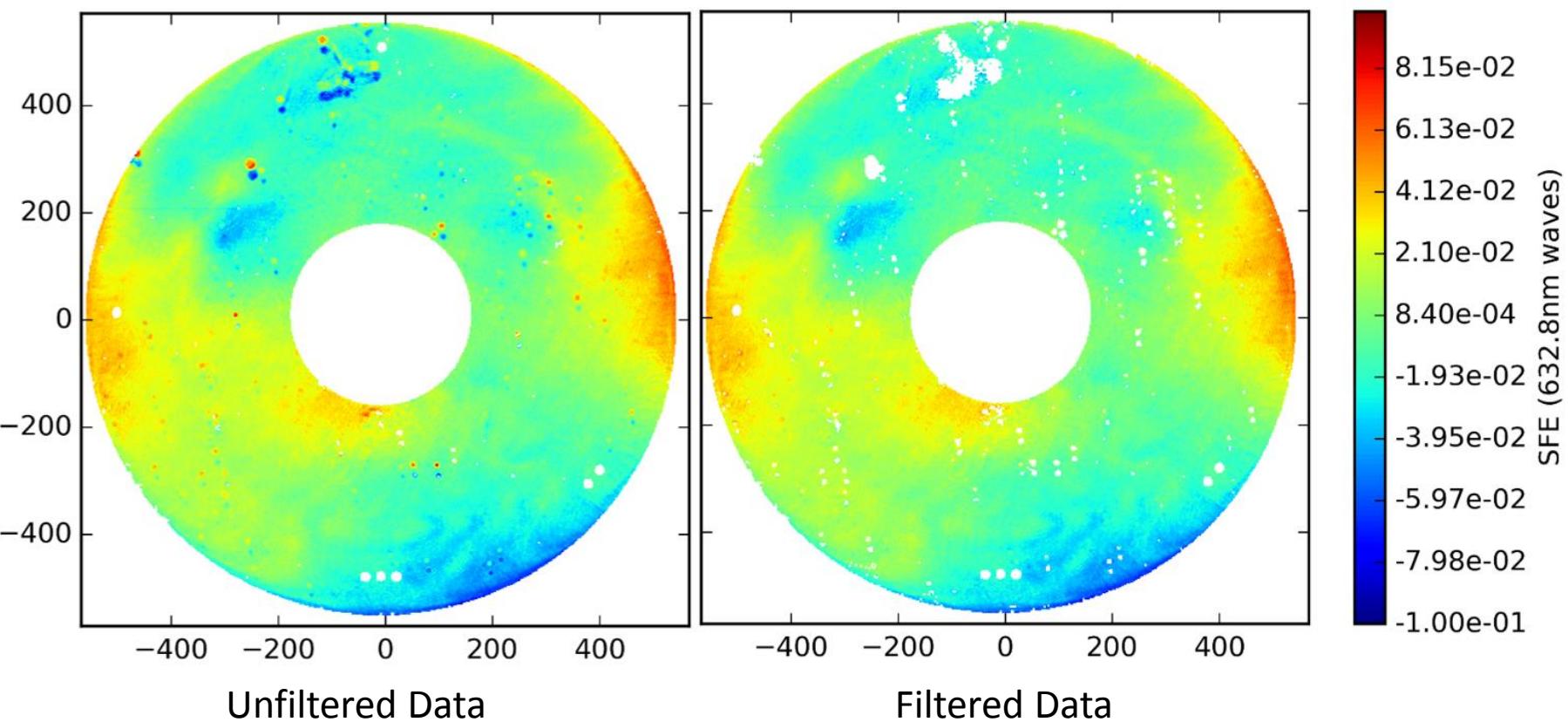
Surface Filtering



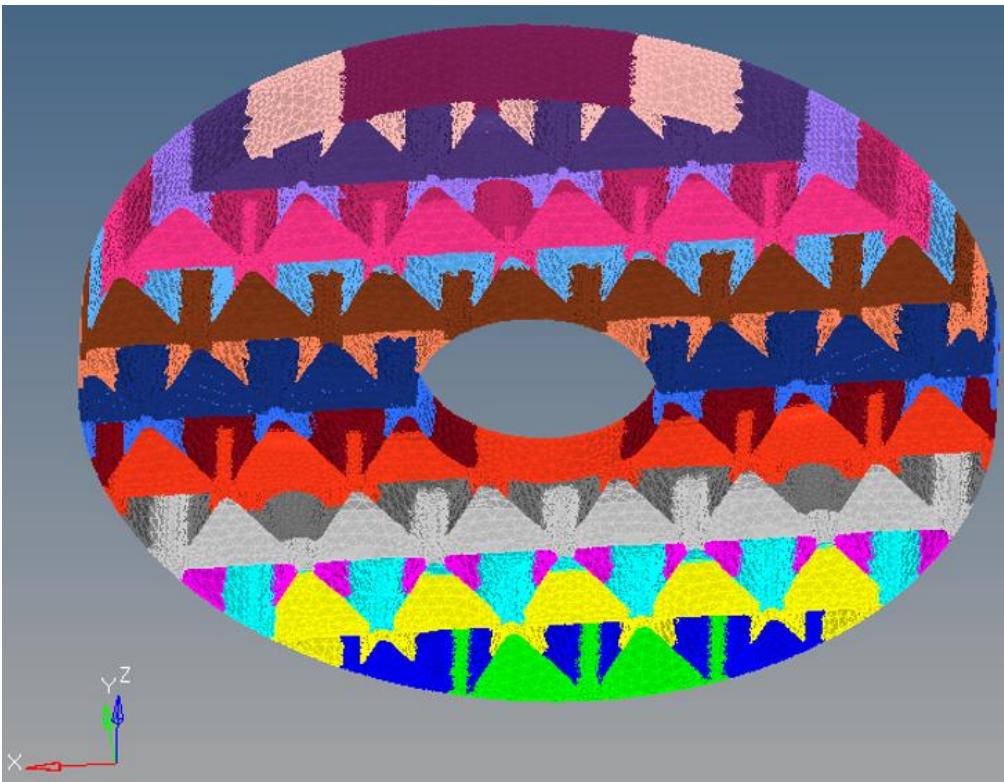
Gradient Method

If the black pixel is too different than more than half of the orange pixels then throw out the black pixel

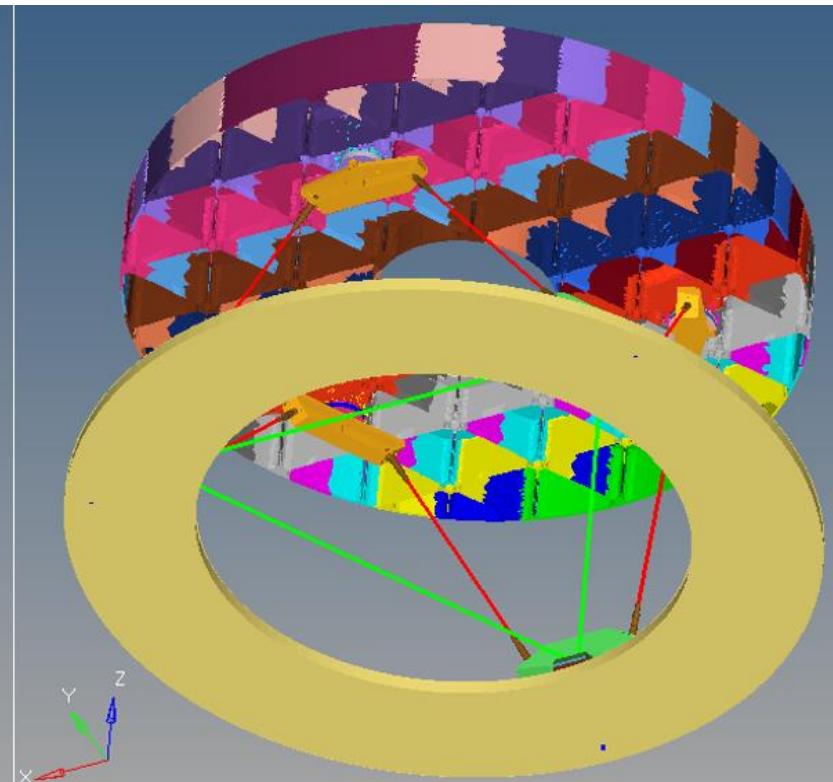
Surface Filtering



Analysis



Mirror with lateral CTE gradient



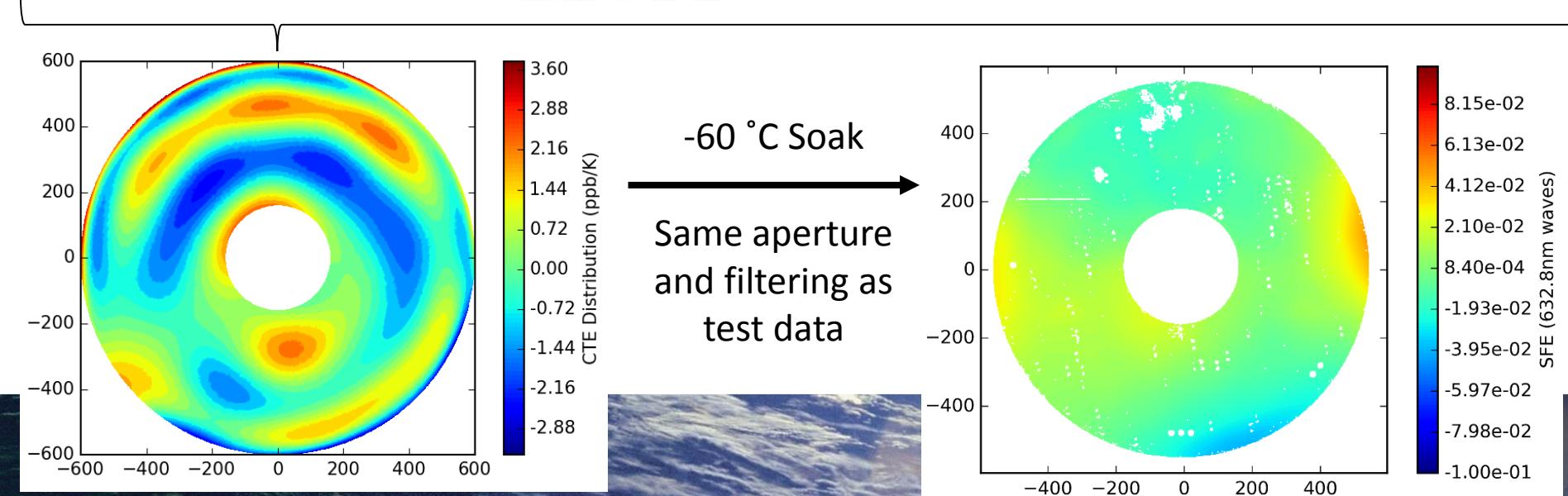
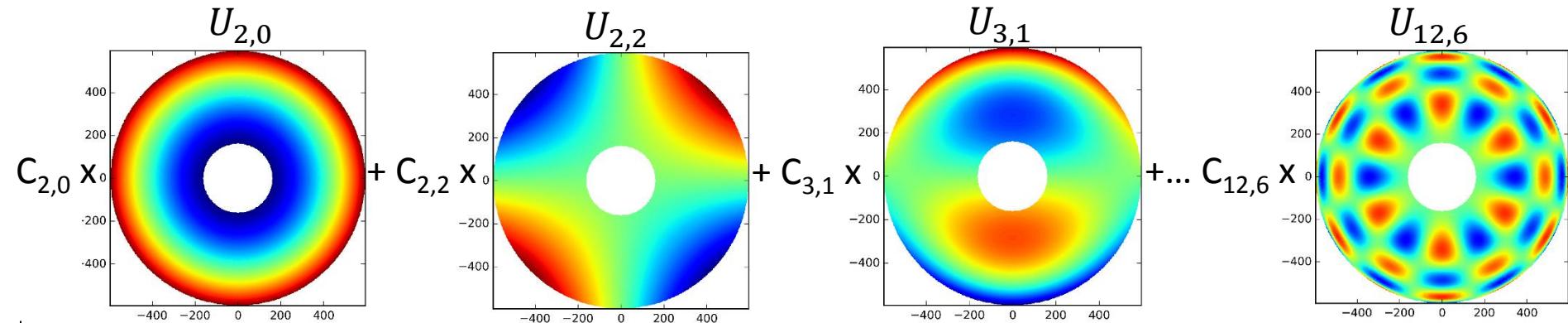
Model with Mount

Correlation Process

Produce CTE Map from Zernike Shapes:

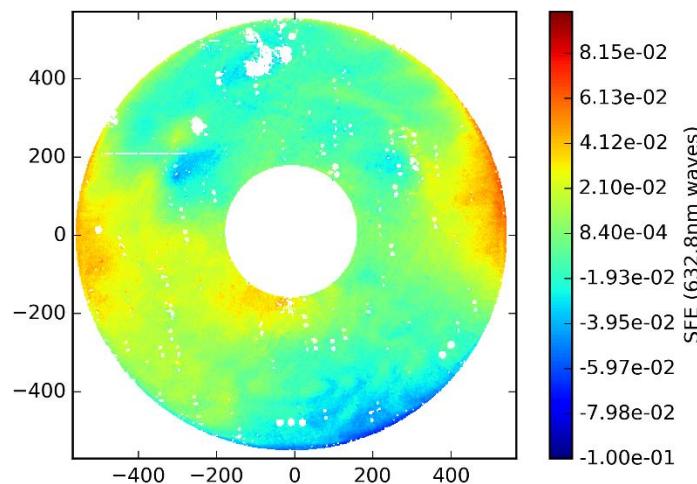
$$[\alpha_{x,y}] = \sum_{n=2}^{12} \sum_{m=0}^n c_{n,m} [U_{n,m}]$$

$[\alpha_{x,y}]$ is the CTE Map

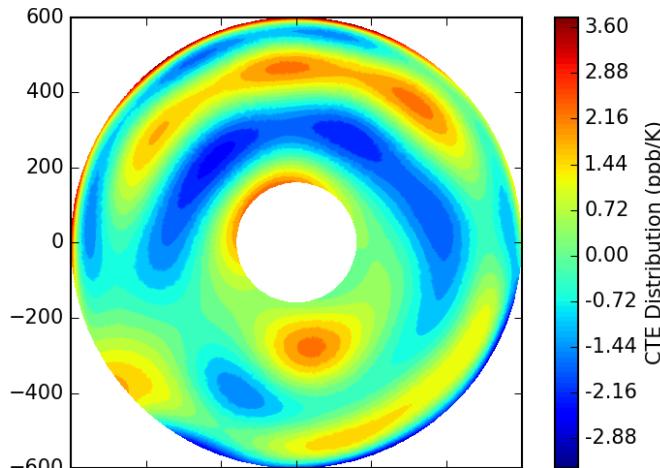
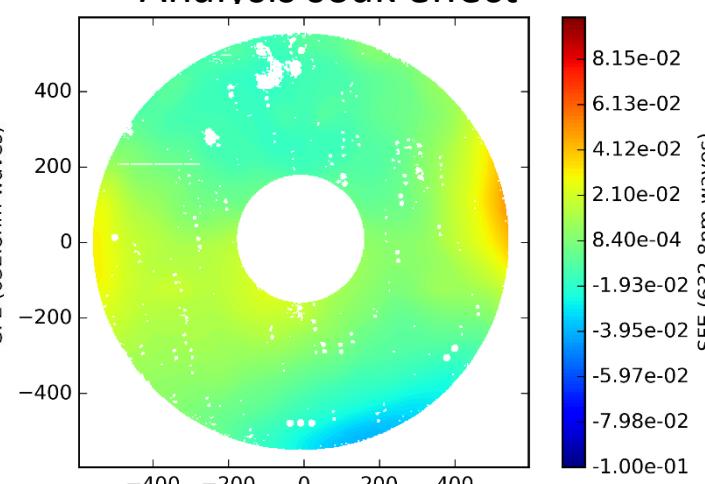


Test and Correlation Delta

Measured soak effect



Analysis soak effect



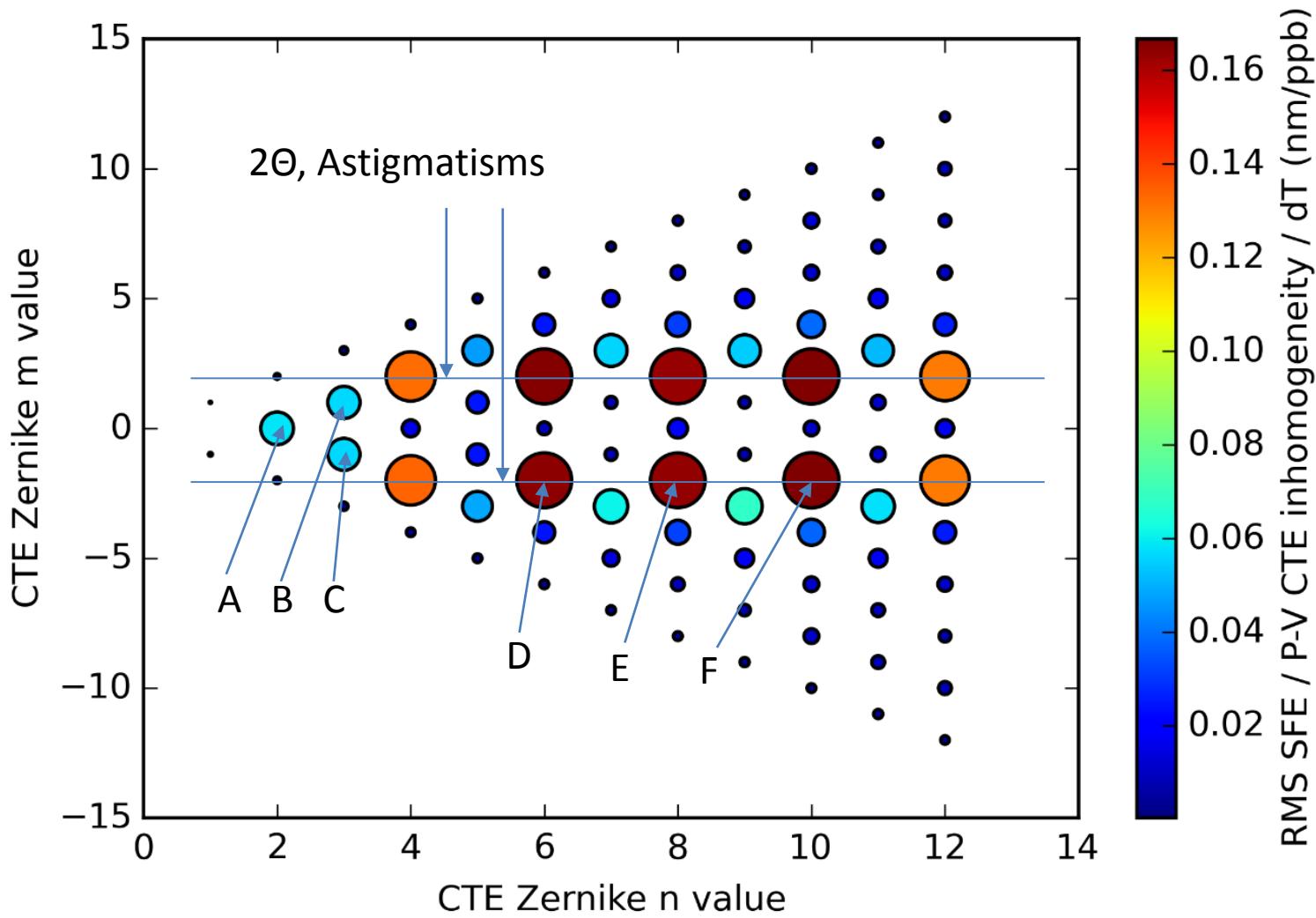
CTE Map

RMS SFE
0.0093 waves
5.9 nm

Measured – Analysis

5.9 nm < repeatability

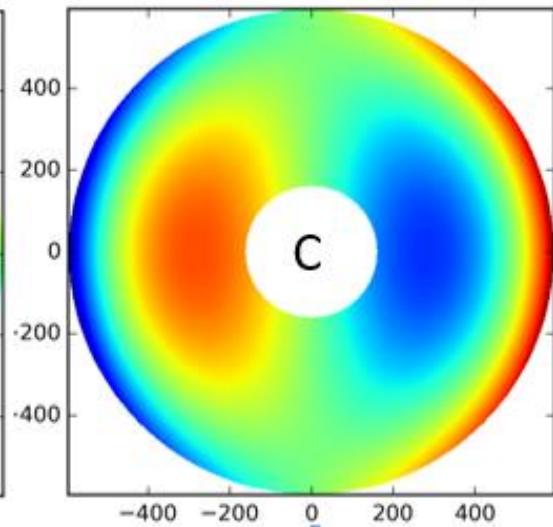
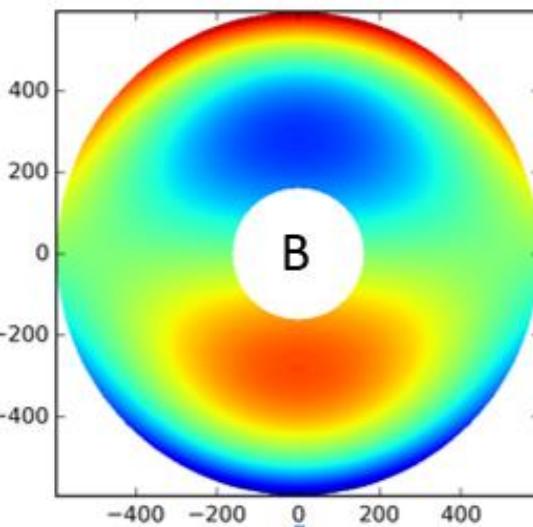
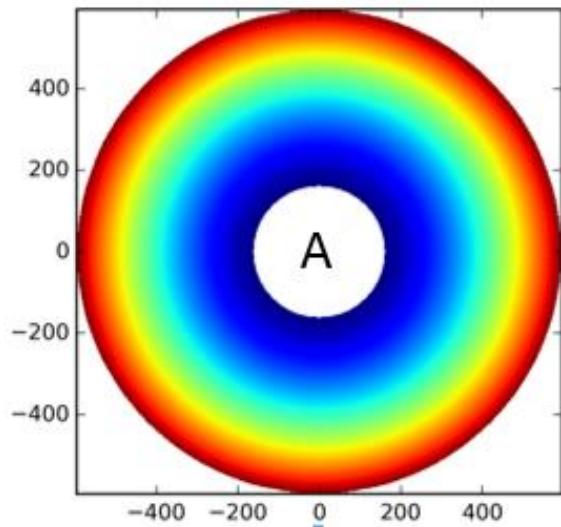
SFE Sensitivities



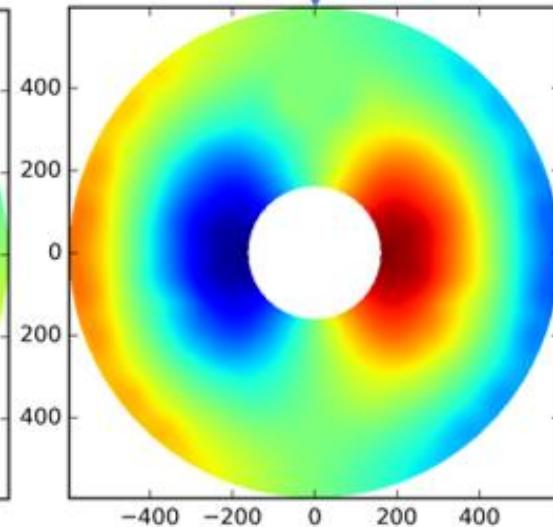
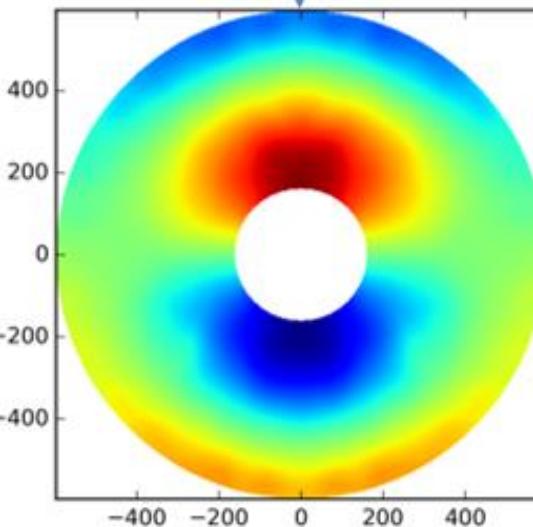
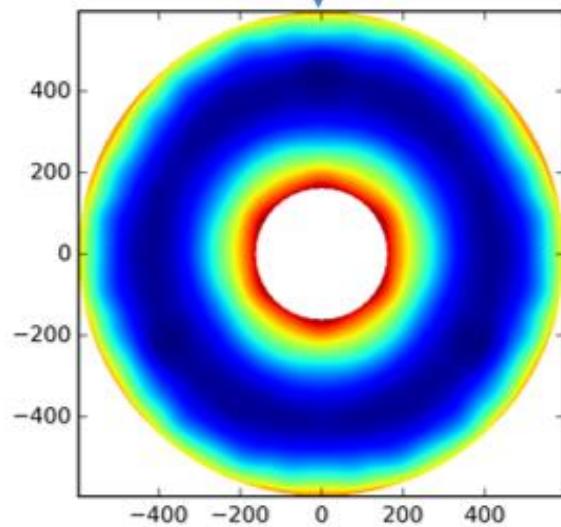
SFE A, B, and C Sensitivities



CTE



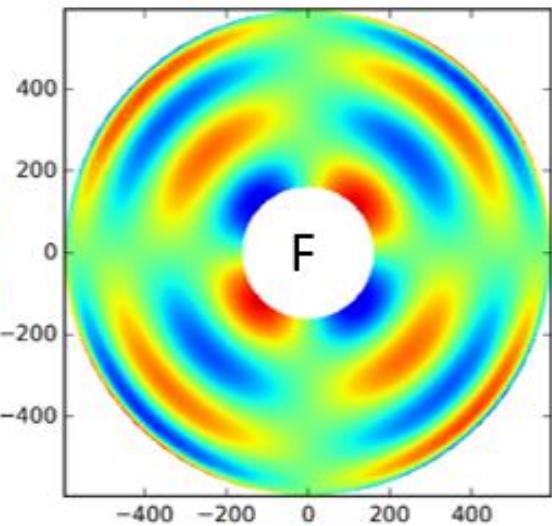
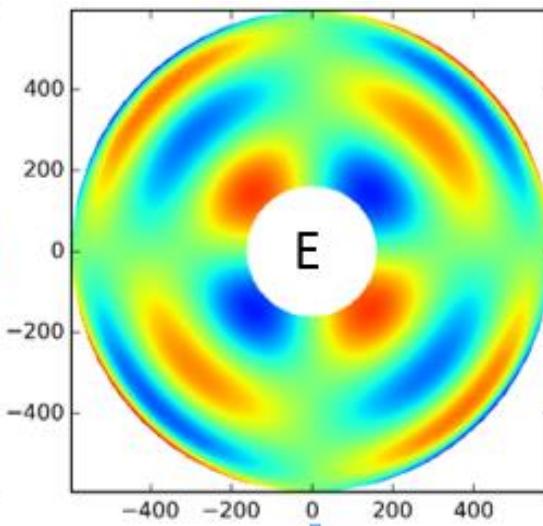
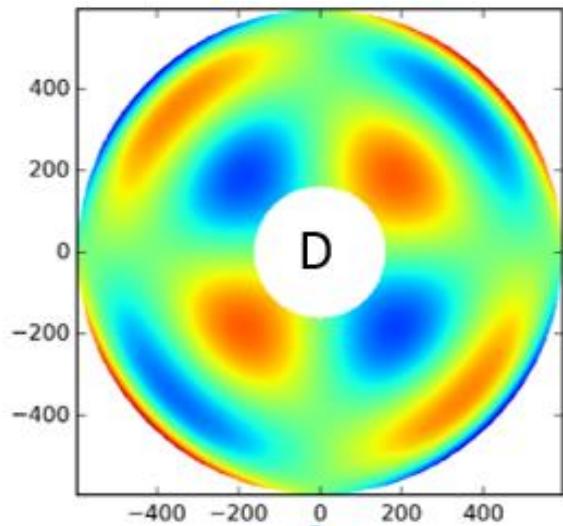
SFE



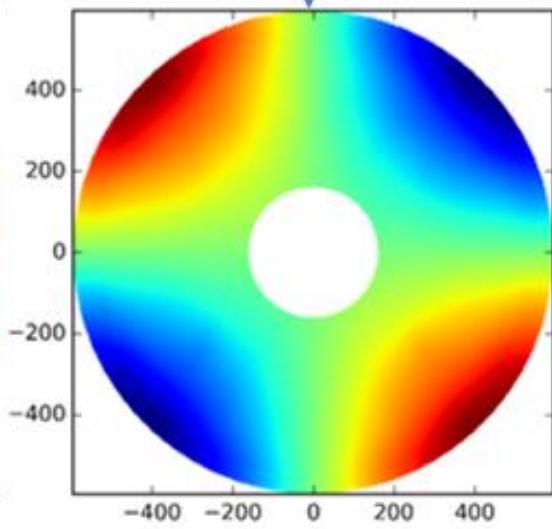
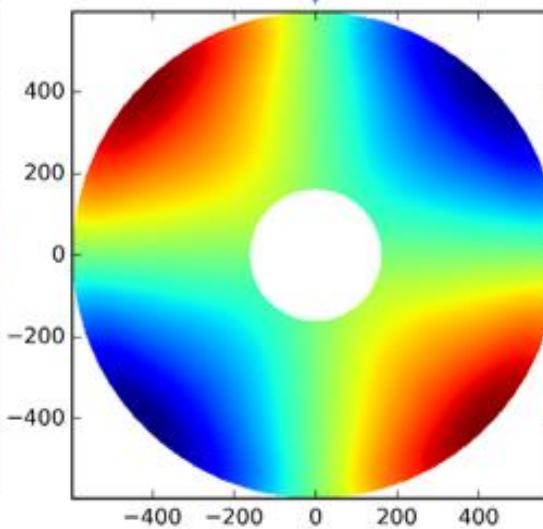
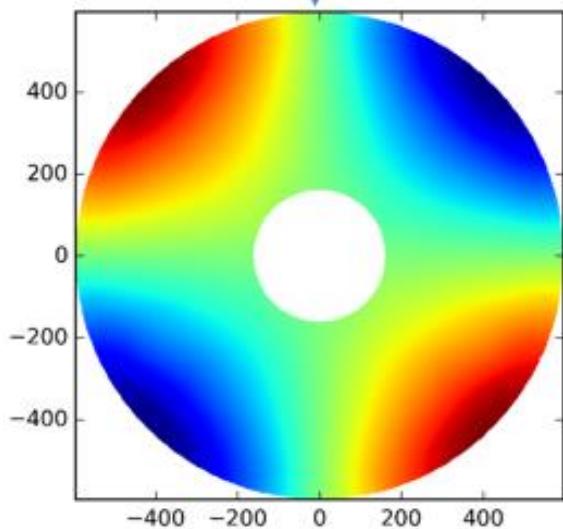
SFE D, E, and F Sensitivities



CTE



SFE



Sensitivity Tables

SFE Sensitivities, c (nm RMS SFE/(ppb/C)/(C)/m												
n \ m	-5	-4	-3	-2	-1	0	1	2	3	4	5	
1					0.007		0.003					
2				0.02		0.47		0.02				
3			0.03		0.45		0.45		0.03			
4		0.03		1.07		0.13		1.06		0.03		
5	0.03		0.39		0.19		0.20		0.38		0.04	

$$SFE = ch\alpha T_{p-v}$$

SFE = RMS SFE after removing power (nm)

c = SFE sensitivity coefficient found in the table

h = mirror's depth (m)

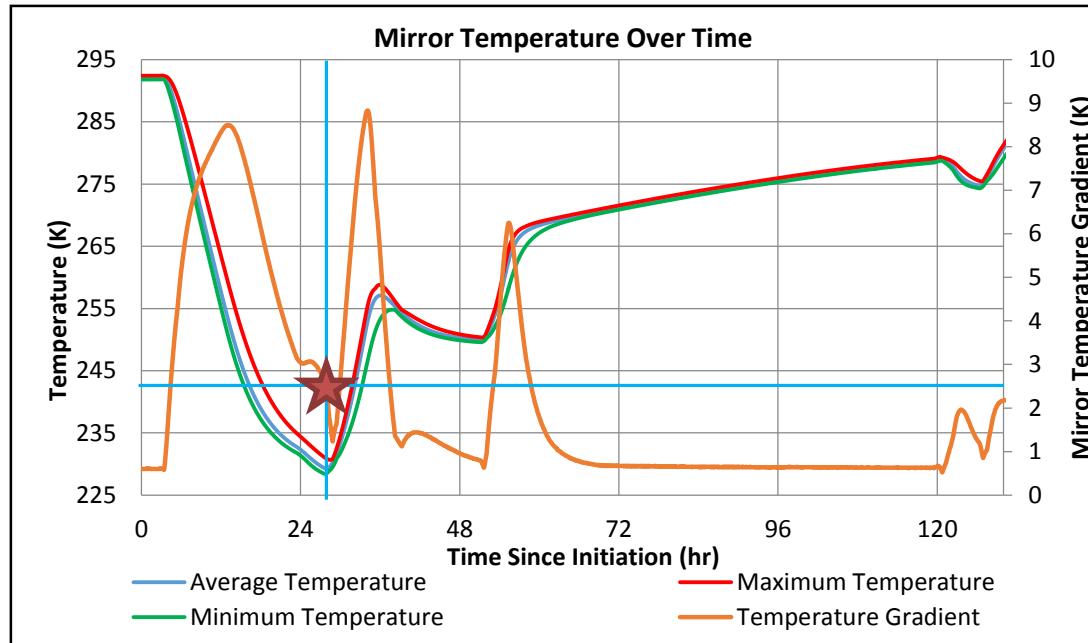
α = mirror's CTE (ppb/K)

T_{p-v} = P-V mirror temperature (K).

SFE Hand Calculation Example



How much SFE is caused by the temperature gradient at the 230K measurement?



The mirror's depth is 0.125m, assume its CTE is 20ppb/K, and the T_{p-v} is 2.5 K:

$$h = 0.125 \text{ m}$$

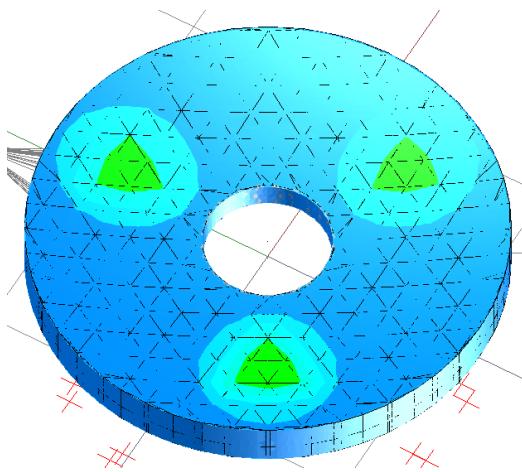
$$\alpha = 20 * 10^{-9} \text{ 1/K}$$

$$T_{p-v} = 2.5 \text{ K}$$

SFE Hand Calculation Example

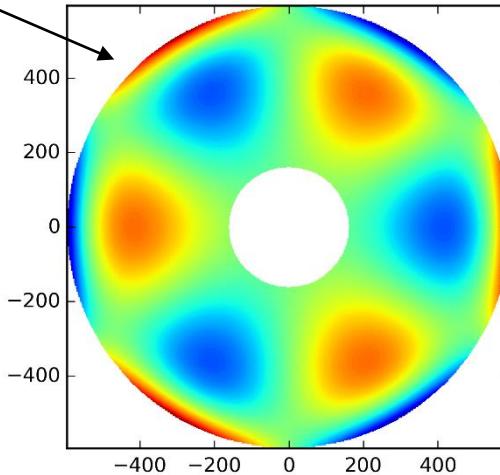


SFE Sensitivities, c (nm RMS SFE/(ppb/C)/(C)/m											
n \ m	-5	-4	-3	-2	-1	0	1	2	3	4	5
1					0.007		0.003				
2				0.02		0.47		0.02			
3			0.03		0.45		0.45		0.03		
4		0.03		1.07		0.13		1.06		0.03	
5	0.03		0.39		0.19		0.20		0.38		0.04



Expected Temperature Distribution

Closest Zernike



$$h = 0.125 \text{ m}$$

$$\alpha = 20 * 10^{-9} \text{ 1/K}$$

$$T_{p-v} = 2.5 \text{ K}$$

$$SFE = ch\alpha T_{p-v}$$

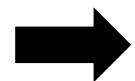
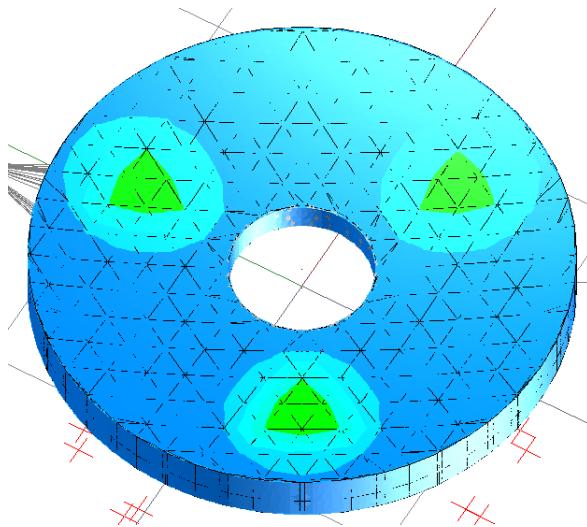
$$SFE = 0.39 * 0.125 * 20 * 10^{-9} * 2.5 \left[m \frac{1}{^{\circ}\text{C}} \right]$$

$$= 2.43 \text{ nm RMS SFE}$$

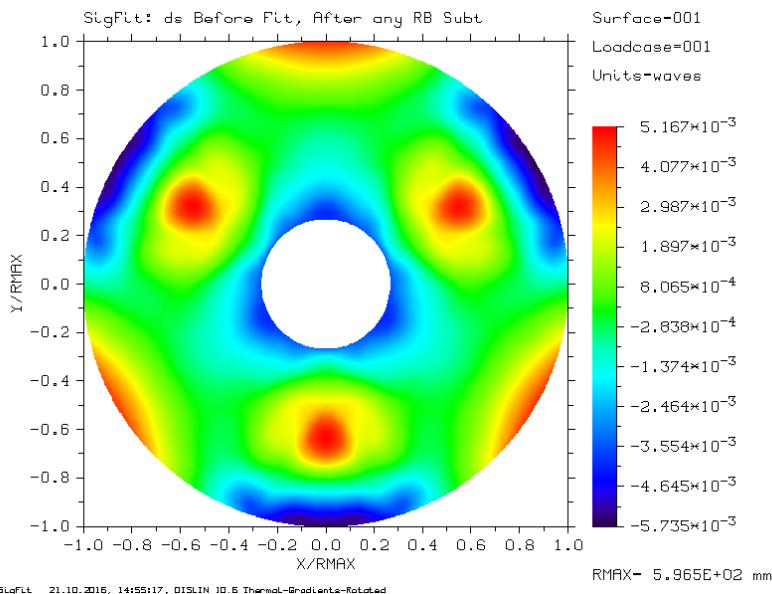
Hand Calculation Compared to FEA



Temperature Distribution

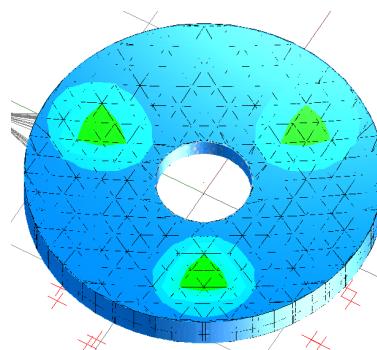


RMS SFE = 1.28nm

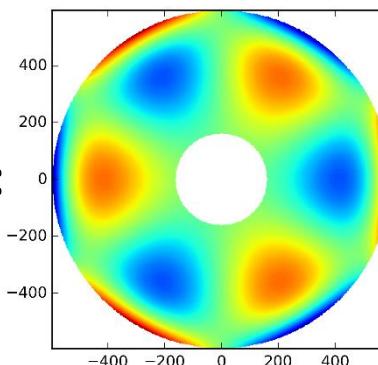


Hand Calculation	2.4 nm RMS SFE
Numerical STOP Analysis	1.3 nm RMS SFE

Why different?



≠



Questions or Comments?



Contact Information

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Cell - (256) 544 -5596