THE ABSOLUTE PHOTOMETRY OF THE ZODIACAL LIGHT
I. I. Smith, F. E. Roach* and R. W. Owen

Central Radio Propagation Laboratory National Bureau of Standards, Boulder, Colorado and

Hawaii Institute of Geophysics University of Hawaii, Honolulu, Hawaii

Abstract-Interpretation is made of photometric records obtained at the Haleakala Observatory during six nights between August 1961 and June 1962. An interference filter centered on wavelength 5300 A was used. After allowance for the airglow continuum and the integrated starlight, the residual is interpreted as due to zodiacal light. The brightness of the zodiacal light is tabulated for that part observable in the night sky. Graphical representations illustrate the distribution of brightness in ecliptic coordinates.


## I. INTRODUCTION

As a part of the airglow-zodiacal light program of the Haleakala Observatory of the Hawaii Institute of Geophysics (latitude $\mathrm{N} 20^{\circ} \cdot 7$, longitude $W 156^{\circ} .16$ ), a photometer having an interference filter centered on wavelength 5300 A was used in systematic observations of the night sky during the period from May 1961 to September 1962.

[^0]The observing program involved scanning the sky in a series of a.lmucantars at zenith distances $80^{\circ}, 75^{\circ}, 70^{\circ}, 60^{\circ}, 40^{\circ}$ plus the zenith. In addition to the photometer (designated by us as RP), the alt-azimuth mount carried (a) a birefringent filter photometer for the study of the night airglow (I) and (b) a polarimeter-photometer used by J. L. Weinberg ${ }^{(2)}$ for a detailed study of the polarization (and photometry) of the zodiacal light. An auxiliary zenith photometer having a built-in and absolutely calibrated standard light was operated during all the observations (3) making it possible to obtain the calibration of the RP photometer by comparison of the simultaneous zenith sky readings throughout a night.
II. THE OBSERVATIONAL MATERIAL

The six nights included in the study (Table l) were distributed throughout the year in approximately 2-month intervals. The principal reason for such a spread was to give a complete coverage of the astronomical sky for a photometric study of the integrated starlight especially in the Milky Way. In the present study, we have avoided galactic latitudes less than $30^{\circ}$ in order to minimize uncertainties due to corrections for integrated starlight. Subsequently, we plan to return to the Milky Way study.

The large ensemble of data (more than one million individual readings) resulted in a library of print-outs of the absolute brightness of the night sky referred to outside the atmosphere for each degree of the sky and for the several almucantars involved in each sky survey.

The data have been examined in both systematic and specialized ways. An example of systematic use was the plotting of the $40^{\circ}$ zenith distance readings for each half hour of sidereal time. An example of a specialized use of the data was the detailed coverage of the region near the ecliptic pole for which plots for each 5-minute survey were made over an extended period in order to delineate the details. We have been able to make corrections for errors in azimuth settings by comparison of peaks of maximum star deflections with their computed azimuths. Based on such comparisons, we believe that an individual azimuth is known to about $\pm 5^{\circ}$, not good enough for any finesse concerning the photometric axis of the zodiacal light but consistent with the $4^{\circ}$ field of view of the photometer. Our final results based on a large quantity of data are probably good to $\pm 2^{\circ}$ in the various coordinates.

We have referred the readings to outside the atmosphere by allowing for (a) the extinction of the lower atmosphere plus ozone, (b) the scattering of the lower atmosphere and (c) the increase of
the airglow component toward the horizon. Some coment is in order on the problem of correcting for scattered light. We have used the tables by Ashburn ${ }^{(4)}$ who made numerical integrations of Rayleigh scattering for (a) a uniform sky with all the light coming from astronomical sources (assumed to be at an infinite distance) and (b) an emitting layer in the upper atmosphere, uniform as seen from the center of the earth but not uniform as seen from the earth's surface. The problem of coping with a non-uniform sky has not been solved (except for the special case of a single point source such as the sun) and, therefore, the use of the Ashburn tables introduces some errors, fortunately small, when applied to an actual sky in which both the astronomical (zodiacal light, Milky Way) and the airglow (dependence on azimuth) components are not uniform.

The principal difficulty in practice is that the Ashburn constants require multiplication by an average sky brightness as seen outside the scattering atmosphere. It is not possible to utilize for this purpose any particular region of the sky such as the zenith which is frequently strongly affected by the Milky Way. We have, therefore, made an estimate of the "average" sky brightness, $J$, for purposes of obtaining the scattering correction by an approximation technique. This is best shown by indicating analytically our data processing procedure. We define the following quantities:

$$
\begin{aligned}
z= & \text { zenith distance, } \\
A= & \text { azimuth, } \\
m(z)= & \text { air mass from Haleakala, } \\
\tau_{1}= & \text { extinction coefficient to refer a reading to } \\
& \text { outside the atmosphere, } \\
\tau_{2}= & \text { extinction coefficient to refer a reading to } \\
& \quad \text { outside the lower atmosphere but just inside } \\
& \text { the ozone layer, } \\
\tau_{3}= & \text { molecular (Rayleigh) coefficient, } \\
J= & \text { average brightness of a uniform sky corresponding } \\
& \text { to the actual non-uniform sky just inside the } \\
& \text { ozone layer, } \\
S c(z)= & \text { scattering factor from Ashburn's tables to be } \\
& \text { multiplied into } J, \\
V(z)= & \text { the van Rhijn function giving the increase with } \\
& \text { zenith distance of an airglow layer as seen from } \\
& \text { the surface of the earth, } \\
R(z, A)= & \text { the observed reading at z and } A, \\
L(z)= & \text { the slant brightness in reading units of the } \\
& \text { sky just inside the ozone layer. }
\end{aligned}
$$

The observed brightness in reading units can be defined as

$$
\begin{equation*}
R(z, A)=L(z) e^{-\tau} 2^{m(z)}+S c(z) \cdot J . \tag{I}
\end{equation*}
$$

Assuming the upper atmosphere component of $J$ as $25 \%$ and the infinity component as $75 \%^{*}$, then

$$
\begin{equation*}
L(z)=.25 \cdot V(z) \cdot J+.75 \cdot J \tag{2}
\end{equation*}
$$

Substituting $L(z)$ from equation (2) into equation (1), we find

$$
\begin{equation*}
J=R(z, A) /\left[(.25 \cdot V(z)+.75) e^{-\tau_{2}(z)}+S c(z)\right] \tag{3}
\end{equation*}
$$

J was determined for each survey by computing it for each zenith distance and azimuth observed and taking the average of the 1800 (360 azimuth readings for each of 5 zenith distances) computations. Finally, we arrive at an expression for the brightness in absolute units $\left[\mathrm{S}_{10}\right.$ (vis)] outside the atmosphere by the formula

$$
\begin{equation*}
I(0 / a)=[R(z, A)-S c(z) J] e^{\tau_{1} m(z)} \cdot Q \tag{4}
\end{equation*}
$$

where $Q$ is the calibration constant to refer our galvanometer readings to $S_{10}$ (vis) units of brightness. For a discussion of the $S_{10}$ (vis)

[^1] assumed percentage of infinity and atmospheric light. As we have later determined (Table 4), it would have been better to have used a lower percentage for the airglow component. We did not repeat the calculations to correspond to the deduced percentages of airglow (Table 4) since the effect on the final result would have been small.
unit and of the methods we have used to evaluate $Q$, we refer to Roach and Smith (5). Table 2 is a surmary of the constants used in equations (3) and (4).

## III. THE INIEGRAITED STARLIGHT

As mentioned above, we avoided regions of the sky with galactic latitudes smaller than $30^{\circ}$. In a recent study, Roach and Smith (5) concluded that the integrated starlight for high galactic latitudes deduced from the Groningen $43^{(6)}$ star counts [see Roach and Megill (7)] represents the true integrated starlight when multiplied by 1.26 . In the present study, we have taken 1.26 times the integrations from Groningen 43 for our estimations of the photometric effect of the integrated starlight. A point by point evaluation of the integrated starlight was made by a double interpolation between the values obtained from the tabular entries in Groningen 43.

The magnitude of the integrated starlight corrections is indicated in Table 3 in which the average values are given for selected galactic latitudes.

[^2]
## IV. THE AIRGIOW CONITNUUM

The filter of our photometer was chosen so as to avoid any bright airglow emissions. Nevertheless, the presence of an airglow "continuum" in our observations is indicated by the systematic increase of the measured intensities toward the horizon. Such an increase has long been associated with the presence of an airglow component in the observations (the so-called van Rhijn effect). In a later study, we propose to go into the airglow problem in detail and here record in Table 4 the absolute airglow brightness used for each of the nights in the present analysis.

The airglow continuum was as much as $24 \%$ of the total light (J), but that this percentage does change significantly from night to night is indicated by the spread in the values listed in Table 4. Changes during a night and variations of brightness with azimuth were ignored in our treatment and errors due to ignoring these changes contribute slightly to the scatter in our final results. We refer to such errors as "subtractive" since they arise from uncertainties in subtracting out the non-zodiacal light components.
V. THE OBSERVATIONAL RESULTS

The numerical results of our study are assembled in Table 5 in the form of zodiacal light brightnesses over the observable domain
with $5^{\circ}$ intervals in the parameters ecliptic latitude, $\beta$, and the differential ecliptic longitude, $\lambda-\lambda_{0}$.

In Fig. 1 the ensemble of data is plotted as isophotes in polar coordinates, $\beta$ and $\lambda-\lambda_{\odot}$. The center of the plot is the ecliptic pole and the periphery is the ecliptic. In our analysis, we have averaged evening and morning results which correspond to the upper and lower parts of the plot which are thus mirror images of each other.

## VI. DISCUSSION

The gross characteristic that stands out from an inspection of Fig. 1 is the contrast between the left and right halves of the plot. The right half represents intensities due to light originating from the dark or night side of the earth if one considers the problem in its diurnal context. It is probably preferable to consider it as a solar system problem and in this sense the right half of the plot is due to light from beyond the earth's orbit. The gegenschein shows as a small enhancement at $\lambda-\lambda_{0}=180$. There is a steady decline in brightness toward the ecliptic pole, but the distortion of the isophotes just on the sunward side of the pole gives an illusion that the center of the photometric minimum is not centered on the pole itself. On the left side of the plot, a dramatic increase of brightness is noted. The very bright zodiacal light $\left[>1000 \mathrm{~S}_{10}\right.$ (vis)] is brighter than most of our present observations and is shown without structure.

We show in Fig. 2 a plot of the zodiacal light brightness as a function of the ecliptic latitude for a differential ecliptic longitude, $\lambda$ - $\lambda_{\odot}$, of $90^{\circ}$, a value chosen since it corresponds to a constant elongation, $\epsilon$, of $90^{\circ}$ over the whole plot*. The brightness goes steadily down from $250 \mathrm{~S}_{10}$ (vis) at the ecliptic to $110 \mathrm{~S}_{10}$ (vis) at the pole.

In Fig. 3 we show the brightness of the zodiacal light as a function of $\in$ for two cases: (a) in the plane of the ecliptic where $\epsilon=\lambda-\lambda_{\odot}$, and (b) perpendicular to the plane of the ecliptic where $\epsilon=\beta$ for $\lambda-\lambda_{0}=0^{\circ}$ up to $\beta=90^{\circ}$ and where $\epsilon=180^{\circ}-\beta$ For $\lambda-\lambda_{\odot}=180^{\circ}$. The two curves come together at the gegenschein $\left(\epsilon=180^{\circ}\right)$ and would do so at the sun $\left(\epsilon=0^{\circ}\right)$ if we were able to carry our observations to that direction in space.

An interesting empirical quantity is the ratio, $P$, of the brightness of the zodiacal light at a given elongation in the ecliptic to that at the same elongation in a plane perpendicular to the ecliptic. For $\epsilon=90^{\circ}$ we note that $P=\frac{250}{110}=2.27$. We have attempted to make an approximate evaluation of $P$ over the domain from the sun to the gegenschein based on a number of published sources plus the observations of this study. The last row (for $\lambda-\lambda_{\odot}=0^{\circ}$ ) in Table 5

[^3]contains a number of entries in parentheses* which represent graphical extrapolations down each column. These numbers are included in Table 6 in the column headed "Brightness, $\perp$ ecliptic". The three entries in the "in ecliptic" column for $15^{\circ}, 20^{\circ}$ and $25^{\circ}$ elongation are from Table III in Ingham ${ }^{(8)}$ with a factor of 1.20 found empirically necessary to put his observations into our scale ${ }^{* *}$. The ratio, $P$, must necessarily be unity at elongations of $0^{\circ}$ (the sun) and $180^{\circ}$ (the gegenschein). Any photometric concentration toward the ecliptic requires that the ratio be greater than one at intermediate elongations. An inspection of Fig. 4 indicates a maximum ratio of almost 5 at an elongation of $35^{\circ}$. We suggest that a refinement of Fig. 4 might be an interesting observational goal.

In the region between $\epsilon=50^{\circ}$ and $90^{\circ}$ in the plot of Fig. 4, a departure of $P$ from the smooth curve (as dashed by us) is noted.

[^4]When this came to our attention in the early examination of the data, we made a concentrated study of the region. Inspection of Fig. 1 demonstrates that the photometric irregularity seems to persist away from the $\lambda-\lambda_{0}=0^{\circ}$ domain as evidenced by the $200 \mathrm{~s}_{10}$ (vis) islands near $\beta=55^{\circ}$ and $\lambda-\lambda_{\odot}=45^{\circ}$ (corresponding to $\epsilon=66^{\circ}$ ). We cannot detect any such perturbation extending down to the ecliptic in the $\epsilon=65^{\circ}\left(\lambda-\lambda_{\odot}=65^{\circ}\right.$ also) region*. It should be remarked that the region of enhancement was included in our records over almost a 4 -month period from August $14 / 15$ to November $6 / 7$, 1961, a period during which the position of the Milky Way in the sky permitted a definitive test.

In order to indicate the evidence for the excess which led to the $S_{10}$ (vis) $=200$ islands in Fig. I, we show in Fig. 5 plots of the brightness versus differential elongation for a family of values of $\beta$ from $25^{\circ}$ to $80^{\circ}$. The region of excess is seen as a progression of maxima especially in the curves for $\beta=45^{\circ}, 50^{\circ}$ and $55^{\circ}$. In Fig. 6 we have isolated the excess in the plane perpendicular to the ecliptic based on the departure of the distorted region (Fig. 4) from the smooth curve (dashed) indicating a brightness of some $50 \mathrm{~s}_{10}$ (vis) units.
*In a detailed plot of the zodiacal light brightness in the ecliptic by Weinberg $(2)$, there is a hint of a slight enhancement in the $\epsilon=65^{\circ}$ region.

We assume the privilege of the observer to be the first to speculate about the physical significance of his own observations and suggest that the excess may be due to a concentration of scattering material some $50^{\circ}$ to $90^{\circ}$ from the sun in the general region away from the ecliptic. If this be the explanation then a localized (with respect to the earth) concentration seems to us more reasonable than one extending over some $120^{\circ}$ of ecliptic longitude over the four months that the excess was observed.
VII. CONCLUSIONS

From systematic photometric observations of the night sky at the Haleakala Observatory, we have isolated the zodiacal light component and recorded it in terms of ecliptic coordinates. We find a photometric ecliptic enhancement of 4.88 at its maximum for an elongation of $35^{\circ}$ and of 2.27 at an elongation of $90^{\circ}$. We find evidence for a.photometric perturbation some $70^{\circ}$ from the sun in regions well away from the ecliptic.
VIII. ACKNOWLEDGMENTS

It is a pleasure to acknowledge the help we have received from several colleagues in the prosecution of this study. We are indebted to Mr. H. M. Mann and to Mr. H. Tanabe for obtaining the original photometric records; to Dr. Robert Sparks for assistance
in several aspects of the use of the University of Hawaii computing facilities; and to Mr. George Sugar of the National Bureau of Standards for his contribution to the program through his design of the equipment for digitizing our records. We particularly express our thanks to Professor Walter Steiger for many courtesies extended to us during the 1963-64 period, during which we initiated this report as guests of the Hawaii Institute of coophysics. One of us (FER) gratefully acknowledges the debt he owes to the East-West Center of the University of Hawaii as a recipient of a Senior Research Scholarship for the 1963-64 period. A part of the expense of the investigations was covered by NASA Grant R 18 .

## REFERENCES

1. D. Barbier, F. E. Roach, and W. R. Steiger, J. Research NBS 66D, 145 (1962).
2. J. L. Weinberg, PhD. dissertation, University of Colorado (1963).
3. C. M. Purdy, I. R. Megill, and F. E. Roach, J. Research NBS 65C, 213 (1961).
4. E. V. Ashburn, J. Atmospheric Terrest. Phys. 5, 83 (1954).
5. F. E. Roach and L. L. Smith, NBS Iech. Note 214 (I964).
6. P. J. van Rhijn, Groningen Publication No. 43 (1925).
7. F. E. Roach and L. R. Megill, Astrophys. J. 133, 228 (1961).
8. M. F. Ingham, Monthly Notices Roy. Astron. Soc. 122, 157 (1961).
9. F. E. Roach and A. B. Meinel, Astrophys. J. 122, 530 (1955).
10. C. W. Allen, Astrophys. Quant. p. 116 (1955).
11. R. Michard, A. Dollfuss, J. C. Pecker, M. Laffineur, and Mme. M. $\mathrm{d}^{\mathrm{I} A z a m b u j a, ~ A n n . ~ d ' A s t r o p h y s . ~ 17, ~} 4$ (1954).

Tabla 1
The Six Nights Includod in this Study

| Night | Period of Observations |  |  |  | Number <br> of Sky Surveys |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Beginnins |  | End |  |  |
|  | $\begin{gathered} \text { H.S.T. } \\ \text { (hrs.:mins.) } \end{gathered}$ | Sid 'rine (degrees) | $\begin{gathered} \text { H.S.T. } \\ \text { (hrs.:mins.) } \end{gathered}$ | Sid Tine (degrees) |  |
| 1961 |  |  |  |  |  |
| Aug. 14/15 | 21:00 | 272 | 04:55 | 31 | 96 |
| Sept. 11/12 | 19:40 | 280 | 04:55 | 59 | 112 |
| Nov. 6/7 | 22:55 | 23 | c5:30 | 122 | 79 |
| Feb. 3/4 | 19:45 | 63 | 05:30 | 210 | 117 |
| March 31/ ipr 1 | 19:50 | 120 | 04:10 | 245 | 99 |
| June 27/28 | 20:30 | 217 | 03:20 | 319 | 82 |
|  |  |  |  |  | 585 (total) |



TAELE 3
Mean Integrated Starlight

| Galactic <br> Latitude | Mean Integrated Starlight <br> (Irom Groningen 43) <br> in $S_{10}$ (vis) units | Mear Integrated <br> Starlight used <br> $(1.20$ X GR 43) |
| :---: | :---: | :---: |
| 80 | 31.1 |  |
| 70 | 32.5 | 39.2 |
| 60 | 35.5 | 41.0 |
| 50 | 41.3 | 44.7 |
| 40 | 51.5 | 52.0 |
| 30 | 68.7 | 64.9 |

Table 4
The Airglow Continum




[^5]Fig. 1. Isophotal map of the zodiacal licit in polar coordinates. The circumference represents the plane of the ecliptic with values of differential Iorgitude, $\lambda-\lambda_{0}$, increasing from $0^{\circ}$ to $90^{\circ}$ to $180^{\circ}$ (the gegenschein). The ecliptic latitude, $\beta$, increases from $0^{\circ}$ at the ecliptic to $90^{\circ}$ in the center of the circle.

Fig. 2 Brightness of the zodiacal light as a function of ecliptic latituce for an elongation of $90^{\circ}$.

Fig. 3 Brightness of the zodiacal light as a function of the elorgation for two planes: above in the ecliptic, below at right angles to the ecliptic. The gegenschein is the slight rise at $\epsilon=180^{\circ}$ 。

Fig. 4 Ratio of brightress of the zodiacal light in the ecliptic to that in a plane at right angles to the ecliptic as a function of elongation irom the entries in Table 7.
Fig. 5 Brightness of the zodiacal/as a function of differential longitude for ecliptic: latitudes ranging from $25^{\circ}$ to $80^{\circ}$. The successive curves are displaced from each other by $50 \mathrm{~S}_{10}$ (vis) units.

Fig. 6 Brightness of the excess zodiacal light in a plane perpendicular to the ecliptic as a function of elongation. The excess is thought to be due to a terrestrial component (soe text).



RATIO OF BRIGHTNESS





[^0]:    *The paper was prepared while FER was the recipient of a Senior Research Scholarship at the East-West Center of the University of HawaiI.

[^1]:    *The scattering correction is relatively insensitive to the

[^2]:    *The single exception is the ecliptic pole for which the galactic latitude is $28^{\circ}$.

[^3]:    *The elongation, $\epsilon$, is conveniently derived from the expression: $\cos \epsilon=\cos \left(\lambda-\lambda_{\odot}\right) \cos \beta$.

[^4]:    *The quantities within parentheses in the first two columns also represent graphical extrapolations, but in this case, the reason for the extrapolation was to attempt to allow for the slow time response of our recording galvanometer.
    **Example: At $\epsilon=35^{\circ}$, Ingham records a brightness of 1340 compared to our value of 1595 .

[^5]:    From Fichard et al. (11).
    From Ingham (8) (Table III) multiplied by 1.20.

