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NASA CR-353

# ANALYSES OF VAPORIZATION IN LIQUID URANIUM BEARING SYSTEMS AT VERY HIGH TEMPERATURES

by L. Kaufman and E. T. Peters

Prepared under Contract No. NAS 3-7168 by  
MANLABS, INC.  
Cambridge, Mass.  
for Lewis Research Center

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION - WASHINGTON, D. C. - DECEMBER 1965





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## **FOREWORD**

Research related to advanced nuclear rocket propulsion is described herein. This work was performed under NASA Contract Number NAS 3-7168 with Mr. Maynard F. Taylor, Nuclear Reactor Division, NASA Lewis Research Center as Technical Manager.

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## 1. INTRODUCTION

An analysis has been carried out to explore the feasibility of selecting a liquid uranium bearing material system which might function as a heat exchanger for hydrogen gas at 100 atm. pressure and  $8,000 - 10,000^{\circ}$  R. Additional constraints are imposed by the requirements of a high impulse nuclear engine.

The over-all objectives of this study are the identification of candidate elemental components to be alloyed with uranium, the specification of compositions which could provide possibilities for unique stability such as congruencies, and the comparison of mass loss rates due to vaporization of elemental components from the liquid surface and diffusion of backing material into the liquid.

The investigation carried out has concerned a reference ternary system U-X<sub>1</sub>-X<sub>2</sub> having the following characteristics:

- a) The system, when heated to temperatures between  $8,000 - 10,000^{\circ}$  R in contact with 100 atm. of hydrogen gas, will exhibit a partial pressure of uranium less than or equal to 0.016 atm.
- b) None of the components considered for inclusion (i.e., X<sub>1</sub> and X<sub>2</sub>) shall have a nuclear capture cross section greater than 5 barns.
- c) The selection of X<sub>1</sub> and X<sub>2</sub> will be subject to the requirement that the average molecular weight of U + X<sub>1</sub> + X<sub>2</sub> plus hydrogen at temperatures between  $8,000^{\circ}$  R and  $10,000^{\circ}$  R shall not exceed that of pure hydrogen by a factor which is more than 1.5.

d) The atomic fraction of uranium in the alloy will be constrained to lie between 0.001 and 0.02.

Based upon the initial choice of components ( $X_1 = \text{Zr or Nb}$  and  $X_2 = \text{C}$ ) the existence or nonexistence of congruency potential in the  $\text{U}-X_1-X_2$  system has been investigated by assuming that the liquid can be approximated by a regular solution.

## 2. THERMODYNAMIC FORMULATION

The free energy of the liquid phase of a ternary system  $X_1-X_2-U$  is given by:

$$F^L = (1-x-y) F_{X_1}^L + x F_{X_2}^L + y F_U^L + F_E^L \\ + RT \left( (1-x-y) \ln(1-x-y) + x \ln x + y \ln y \right) \quad (1)$$

where  $x$  = atomic fraction of element  $X_2$  and  $y$  = atomic fraction of uranium, and  $F_E^L$ , the excess free energy of mixing, is given by

$$F_E^L = (1-x-y) x L_{X_1-X_2} + x y L_{X_2-U} + (1-x-y) y L_{X_1-U} \quad (2)$$

where the  $L$  terms are constants (1\*).

The partial molar free energies of each component are, by definition \*\*

$$\bar{F}_{X_1}^L = F^L - x \left( \frac{\partial F^L}{\partial x} \right)_y - y \left( \frac{\partial F^L}{\partial y} \right)_x \quad (3a)$$

$$\bar{F}_{X_2}^L = F^L + (1-x) \left( \frac{\partial F^L}{\partial x} \right)_y - y \left( \frac{\partial F^L}{\partial y} \right)_x \quad (3b)$$

$$\bar{F}_U^L = F^L - x \left( \frac{\partial F^L}{\partial x} \right)_y + (1-y) \left( \frac{\partial F^L}{\partial y} \right)_x \quad (3c)$$

Differentiation and combination with Eq. (1) yields

$$\bar{F}_{X_1}^L = F_{X_1}^L + RT \ln(1-x-y) + \bar{F}_{E-X_1}^L \quad (4a)$$

$$\bar{F}_{X_2}^L = F_{X_2}^L + RT \ln x + \bar{F}_{E-X_2}^L \quad (4b)$$

\* Underscored numbers in parentheses designate References given at end of report.

\*\* The partial molar excess free energies, i.e.,  $\bar{F}_{E-X_1}^L$  etc., are defined in the same manner.

$$\bar{F}_U^L = F_U^L + RT \ln y + \bar{F}_{E-U}^L \quad (4c)$$

The approximations that have been indicated above and Eqs. (1) and (3) give

$$\bar{F}_{E-X_1}^L = L_{X_1-X_2}(x^2 + xy) - L_{X_2-U}(xy) + L_{X_1-U}(y^2 + xy) \quad (5a)$$

$$\bar{F}_{E-X_2}^L = L_{X_1-X_2}((1+x)^2 - y(1-x)) + L_{X_2-U}y(1-x) - L_{X_1-U}y(1-x-y) \quad (5b)$$

$$\bar{F}_{E-U}^L = -L_{X_1-X_2}x(1-x-y) + L_{X_2-U}x(1-y) + L_{X_1-U}((1-y)^2 - x(1-y)) \quad (5c)$$

Since  $\bar{F}_i^L - F_i^{\circ} \equiv RT \ln a_i^L / a_i^{\circ} = RT \ln p_i / p_i^{\circ}$ , where  $i$  stands for any component, Eqs. (1)-(5) yields

$$\log(p_{X_1}/p_{X_1}^{\circ}) = \log(1-x-y) + (1/4.575T) \bar{F}_{E-X_1}^L \quad (6a)$$

$$\log(p_{X_2}/p_{X_2}^{\circ}) = \log x + (1/4.575T) \bar{F}_{E-X_2}^L \quad (6b)$$

$$\log(p_U/p_U^{\circ}) = \log y + (1/4.575T) \bar{F}_{E-U}^L \quad (6c)$$

where the excess free energies are given by Eq. (5), temperature is in degrees Kelvin and the logs refer to base ten.

Eq. (6) completely specifies the equilibrium partial pressures of  $X_1$ ,  $X_2$ , and  $U$  as a function of composition. The average molecular weight ( $\tilde{M}$ ) of the gaseous phase is given by

$$\tilde{M} = \frac{\sum M_i P_i}{P_T} \quad (7)$$

where the total pressure  $P_T = \sum p_i$ .

### 3. ANALYSIS OF SELECTED SYSTEMS

The desirable characteristics for selecting  $X_1$  and  $X_2$  are low atomic weight, refractoriness, i.e., low vapor pressure at high temperature, low activity of both species in  $X_1$ - $X_2$  alloys, and low nuclear capture cross sections (see Table 1). The elements which most nearly fulfill these conditions are  $X_1 = \text{Nb}$  or  $\text{Zr}$  and  $X_2 = \text{C}$ . The L factors required for Eq. (5) are calculated by appropriate equilibration of the free energy of liquid (L) and solid ( $\sigma$ ) at a composition of 0.5 (2). For the Zr-C case,

$$L_{\text{Zr-C}} = 4(\Delta F^\sigma[\bar{T}^\sigma] + \bar{T}^\sigma R \ln 2 + 0.5 \Delta F^{\text{L} \rightarrow \text{S}}[\bar{T}^\sigma])$$

This yields

$$L_{\text{Zr-C}} = -36,080 \text{ cal/mol.} \quad (8a)$$

Similarly

$$L_{\text{Nb-C}} = -37,500 \text{ cal/mol.} \quad (8b)$$

$$L_{\text{U-C}} = -36,000 \text{ cal/mol.} \quad (8c)$$

The  $\beta$  phase of the Nb-U system (4) exhibits a miscibility gap at  $1300^\circ \text{K} = T_C$ ; the  $\beta/\text{L}$  equilibria decreases linearly from  $\bar{T}_{\text{Nb}}^\beta$  to  $\bar{T}_{\text{U}}^\beta$ . Hence,

$$L_{\text{Nb-U}} \approx 2RT_C \approx +5,200 \text{ cal/mol.} \quad (8d)$$

TABLE 1  
NUCLEAR CAPTURE CROSS SECTIONS,  $\sigma$  (barns) (5)

<u>Element</u>	<u><math>\sigma</math></u>	<u>Element</u>	<u><math>\sigma</math></u>
C	0.004	Nb	1.1
B <sup>11</sup>	0.05	Ta	21.3
N	1.9	Cr	2.9
O	0.0002	Mo	2.5
Si	0.13	W <sup>184</sup>	2.0 → 5.0
Ti	5.6	W <sup>Natural</sup>	19.2
Zr	0.18	U <sup>235</sup>	6.00
Hf	105	U <sup>Natural</sup>	7.5
V	5.0		

According to the initial conditions, the atomic fraction of uranium is constrained to lie between 0.001 and 0.02, i.e.,  $y_{\text{max}} = 0.02$ . The  $y$  terms in Eqs. (5a) and (5b) become very small and can be ignored. The equilibrium partial pressures for the Nb-C-U ternary system are therefore given as

$$\log(p_{\text{Nb}}/p_{\text{Nb}}^{\circ}) \approx \log(1-x) - 37,500 x^2 / 4.575 T \quad (9a)$$

$$\log a_C \approx \log x - 37,500 (1-x)^2 / 4.575 T \quad * \quad (9b)$$

$$\log(p_U/p_U^{\circ}) = \log y + (1/4.575 T)(-37,500 x^2 - 3700 x(1-y) + 5200 (1-y)^2) \quad (9c)$$

and, assuming  $L_{\text{Nb-U}} \approx L_{\text{Zr-U}}$ , the equilibrium partial pressures for the Zr-C-U ternary system are

$$\log(p_{\text{Zr}}/p_{\text{Zr}}^{\circ}) \approx \log(1-x) - 36,080 x^2 / 4.575 T \quad (10a)$$

$$\log a_C \approx \log x - 36,080 (1-x)^2 / 4.575 T \quad (10b)$$

$$\log(p_U/p_U^{\circ}) = \log y + (1/4.575 T)(-36,080 x^2 - 5120 x(1-y) + 5200 (1-y)^2) \quad (10c)$$

\* The total partial pressure of carbon ( $p_C$  (total)) is taken as the vapor pressure of the monomer C plus the pressures of the polymers  $C_2$ ,  $C_3$ ,  $C_4$ , and  $C_5$ . For the general reaction  $nC(s) \rightleftharpoons C_n(v)$ , one determines the partial pressure of the n polymer from the expression

$$p_{C_n} = a_C^n p_{C_n}^{\circ}$$

The pressures of the polymers over pure carbon and the tabulations of  $p_C$  (total) required for the various systems studied are presented in Appendix A.

Values of  $\log p^{\circ}$  vs. T for the various elements of concern are tabulated in Table 2. When necessary, the data were extrapolated to  $10,000^{\circ}\text{R}$  ( $\sim 5555^{\circ}\text{K}$ ) by means of the formula

$$\log p^{\circ} = a/T^{\circ}\text{K} + b \quad (11)$$

with the constants a and b being evaluated from the high temperature data.

a) Zr-C-U

The partial pressures of Zr and C were calculated as a function of x at  $9000^{\circ}\text{R}$  according to Eqs. (10a) and (10b). The calculation steps are tabulated in Table 3 and the results are presented in Figure 1. The pressures of Zr plus C are a minimum at  $x = 0.30$ . This value is used in Eq. (10c) for calculation of  $P_U$  as a function of y between the imposed limits of 0.001 and 0.02. These calculations are tabulated in Table 4a. With reference to Eq. (10a), it is seen that  $\bar{F}_{E-U}^L$  term becomes more negative as x increases. Therefore, high C content reduces the vapor pressure of U, y held constant.

The average molecular weight of the gaseous mixture ( $M$ ) is calculated as a function of x by means of Eq. (7) for  $T=9000^{\circ}\text{R}$ ,  $p_U^{\circ} = 4.677$ , and  $P_H = 100 \text{ atm}$  at  $y = 0.001, 0.01$ , and  $0.02$ . (The molecular weight of hydrogen vs. temperature at 100 atm. is plotted in Figure 2.) The results are tabulated in Table 4b and are presented graphically in Figure 3. The condition that the average molecular weight of the gaseous mixture be no more than 1.5 times the molecular weight of hydrogen is not met by the Zr-C-U-H system at  $9000^{\circ}\text{R}$ .

TABLE 2  
 THE VAPOR PRESSURES OF U, Zr, AND Nb  
 AS A FUNCTION OF TEMPERATURE

<u>T(°K)</u>	<u>T(°R)</u>	<u>log p<sub>U</sub> °(6)</u>	<u>log p<sub>U</sub> °(7)</u>	<u>log p<sub>U</sub> °(8)</u>	<u>log p<sub>Zr</sub> °(9)</u>	<u>log p<sub>Nb</sub> °(10)</u>
3000	5,400	-2.11	-2.08	-2.79	-3.66	-4.78
3200	5,760	-1.63	-1.60	-2.25	-3.03	-4.40
3400	6,120	-1.20	-1.17	-1.77	-2.49	-3.39
3600	6,480	-0.82	-0.79	-1.35	-2.02	-2.81
3800	6,840	-0.48	-0.44	-0.97	-1.56	-2.29
4000	7,200	-0.18	-0.14	-0.63	-1.17	-1.82
4100	7,380	-0.03	0.01	-0.47	-0.99	-1.61
4200	7,560		0.14	-0.32	-0.82	-1.40
4300	7,740		0.27	-0.17	-0.65	-1.20
4400	7,920		0.39	-0.04	-0.49	-1.02
4500	8,100		0.51	+0.09	-0.35	-0.84
4600	8,280		0.63	0.22	-0.20	-0.67
4700	8,460		0.73	0.34	-0.06	-0.50
4800	8,640		0.84	0.45	0.07*	-0.34
4900	8,820		0.94	0.57	0.19*	-0.19
5000	9,000		1.03	0.67	0.31*	-0.05
5100	9,180		1.12	0.77		0.09*
5200	9,360		1.21	0.87		0.22*
5300	9,540		1.30	0.96		0.34*
5400	9,720		1.38	1.14		0.47*
5500	9,900		1.46	1.23		0.58*
5555	10,000		1.50	1.27		0.65*
5600	10,080		1.53	1.31		0.70*

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\* Extrapolated

TABLE 3

CALCULATION PARAMETERS FOR THE PARTIAL PRESSURES  
OF ZIRCONIUM AND CARBON OVER Zr-C ALLOYS AT 9000°R

<u>x</u>	<u>x<sup>2</sup></u>	<u>(1-x)</u>	<u>log(1-x)</u>	<u>log(p<sub>Zr</sub>/p<sub>Zr</sub><sup>0</sup>)</u>	<u>(p<sub>Zr</sub>/p<sub>Zr</sub><sup>0</sup>)</u>	<u>p<sub>Zr</sub></u>
0.01	10 <sup>-4</sup>	0.99	-0.0044	-0.0045	0.9897	2.021
0.10	0.01	0.90	-0.0458	-0.0592	0.8726	1.782
0.20	0.04	0.80	-0.0969	-0.1505	0.7071	1.444
0.30	0.09	0.70	-0.1549	-0.2755	0.5303	1.083
0.40	0.16	0.60	-0.2219	-0.4363	0.3662	0.748
0.50	0.25	0.50	-0.3010	-0.6360	0.2312	0.472
0.60	0.36	0.40	-0.3979	-0.8803	0.1317	0.269
0.70	0.49	0.30	-0.5229	-1.1795	0.0662	0.135
0.80	0.64	0.20	-0.6990	-1.5566	0.0278	0.0569
0.90	0.81	0.10	-1.0000	-2.0854	0.0082	0.0168
0.99	0.98	0.01	-2.0000	-3.3132	0.0005	0.0010

<u>(1-x)</u>	<u>(1-x)<sup>2</sup></u>	<u>x</u>	<u>log x</u>	<u>log(a<sub>C</sub>)</u>	<u>a<sub>C</sub></u>	<u>p<sub>C</sub> (Total)</u>
0.99	0.98	0.01	-2.00	-3.3132	0.0005	0.0023
0.90	0.81	0.10	-1.00	-2.0854	0.0082	0.0384
0.80	0.64	0.20	-0.699	-1.5566	0.0278	0.140
0.70	0.49	0.30	-0.5229	-1.1795	0.0662	0.380
0.60	0.36	0.40	-0.3979	-0.8803	0.1317	0.896
0.50	0.25	0.50	-0.3010	-0.6360	0.2312	2.08
0.40	0.16	0.60	-0.2219	-0.4363	0.3662	4.76
0.30	0.09	0.70	-0.1549	-0.2755	0.5303	10.33
0.20	0.04	0.80	-0.0969	-0.1505	0.7071	20.48
0.10	0.01	0.90	-0.0458	-0.0592	0.8726	35.33
0.01	10 <sup>-4</sup>	0.99	-0.0044	-0.0045	0.9897	50.00

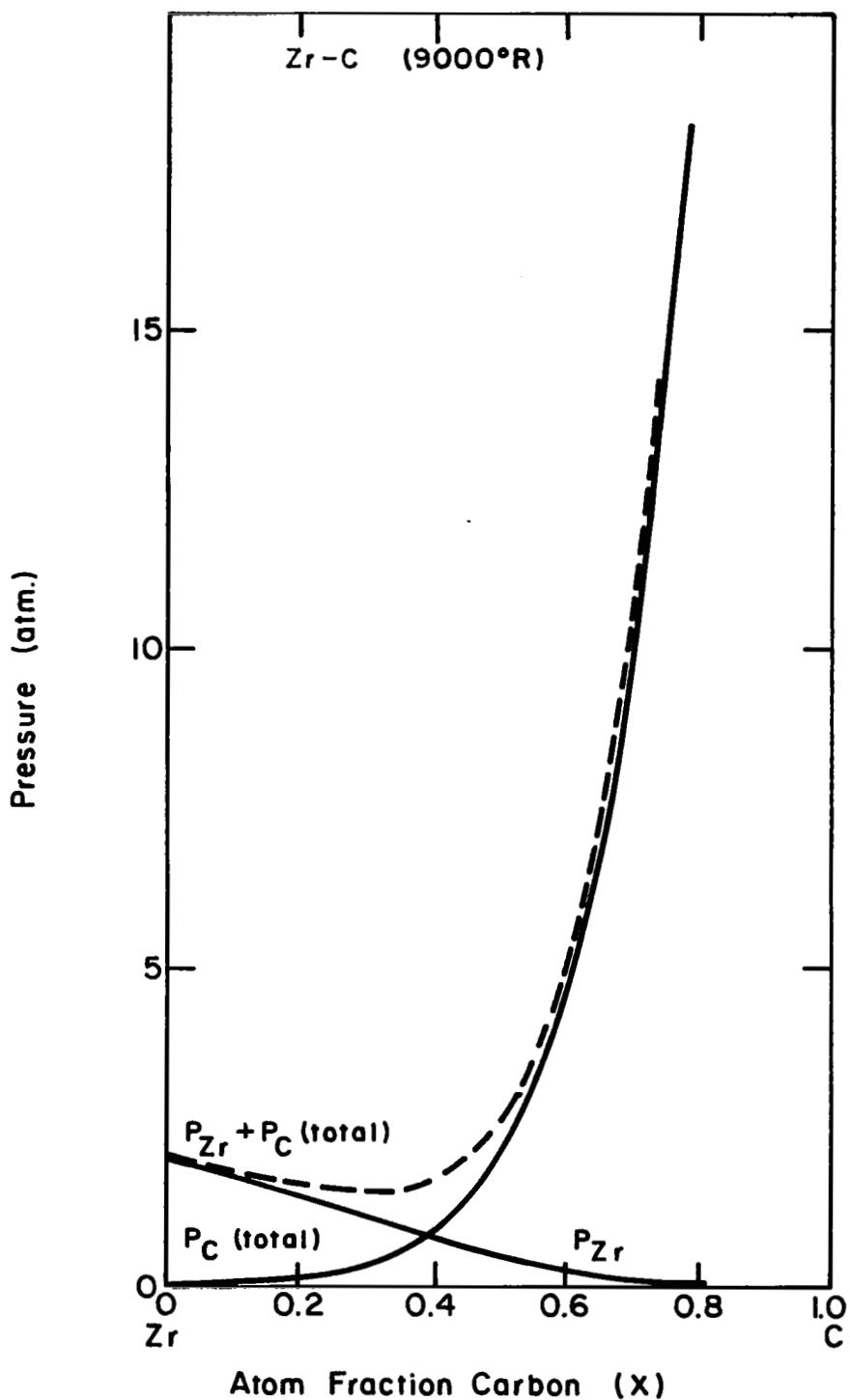


Figure 1. The Partial Pressures of Zirconium and Carbon at 9000°R as a Function of Alloy Composition.

TABLE 4

THE PARTIAL PRESSURE OF URANIUM OVER  
Zr-C-U ALLOYS AT 9000°R

a)  $x = 0.30$ 

<u>y</u>	<u>log y</u>	<u><math>\bar{F}_{E-U}^L</math></u>	<u><math>\log(p_U/p_{U}^{\circ})</math></u>	<u><math>(p_U/p_{U}^{\circ}) \times 10^2</math></u>	<u><math>p_U^{(7)}</math></u>	<u><math>p_U^{(8)}</math></u>
0.001	-3.0	+0.018	-2.982	0.104	0.0112	0.0049
0.005	-2.301	+0.016	-2.285	0.412	0.0442	0.0192
0.010	-2.0	+0.014	-1.986	1.033	0.1107	0.0483
0.015	-1.824	+0.012	-1.812	1.542	0.1653	0.0721
0.020	-1.699	+0.010	-1.689	2.047	0.2194	0.0958

b)  $y = 0.001; p_U^{\circ} = 4.678$  (8)

<u>x</u>	<u><math>\bar{F}_{E-U}^L</math></u>	<u><math>\log(p_U/p_{U}^{\circ})</math></u>	<u><math>(p_U/p_{U}^{\circ}) \times 10^3</math></u>	<u><math>p_U^{(8)}</math></u>	<u><math>\tilde{M}</math></u>	<u><math>\frac{\tilde{M}}{(y = 0.01)}</math></u>	<u><math>\frac{\tilde{M}}{(y = 0.02)}</math></u>
0.10	+0.194	-2.806	1.563	.0073	3.125	3.273	3.435
0.20	+0.131	-2.869	1.352	.0063	2.840	2.968	3.109
0.30	+0.036	-2.964	1.086	.0051	2.551	2.654	2.767
0.40	-0.099	-3.099	0.796	.0037	2.336	2.412	2.494
0.50	-0.249	-3.249	0.564	.0026	2.322	2.375	2.433
0.60	-0.438	-3.438	0.365	.0017	2.747	2.768	2.817

$$\underline{1.5 \times M_H = 2.303}$$

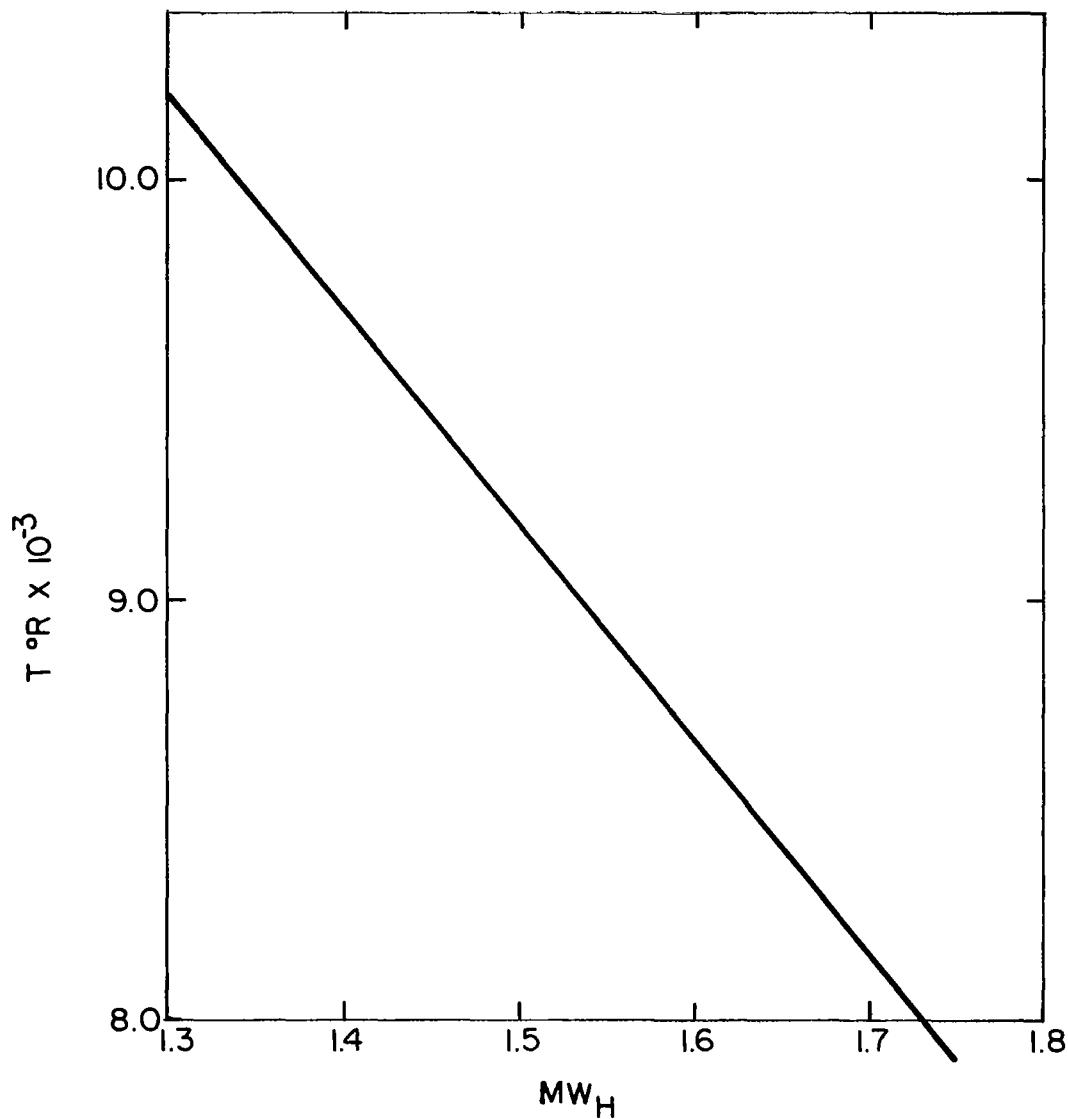


Figure 2. Molecular Weight of Hydrogen as a Function of Temperature (5)  
(Pressure = 100 atm.).

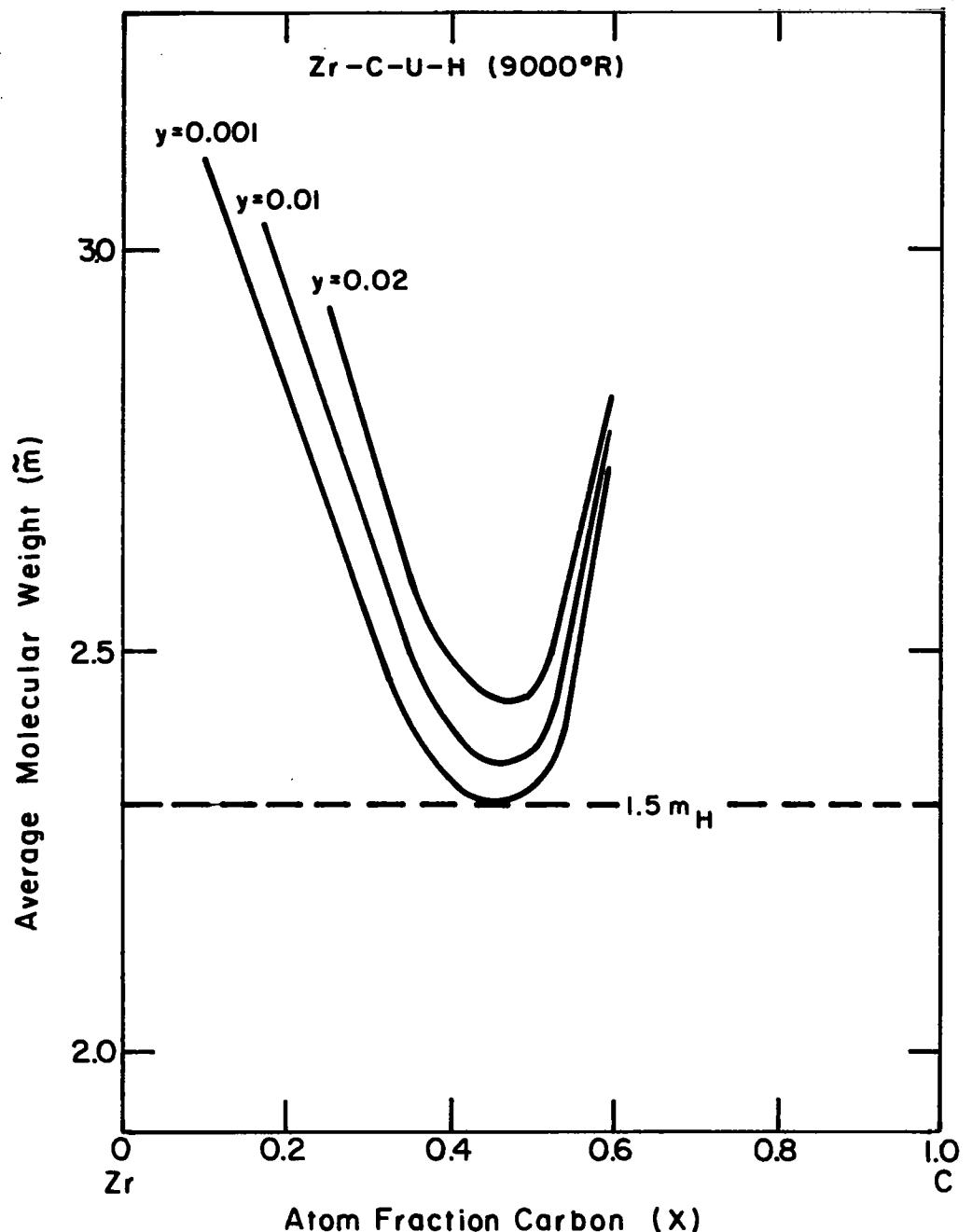


Figure 3. Average Molecular Weight of Gaseous Zr-C-U-H at 9000°R for Variable Zr-C Compositions.

b) Nb-C-U

The partial pressures of Nb and C were calculated as a function of  $x$  at  $9000$  and  $10,000^{\circ}$  R according to Eqs. (9a) and (9b). The results are presented in Table 5 and Figures 4 and 5. The compositions at which Nb plus C is a minimum are  $x = 0.25$  ( $9000^{\circ}$  R) and  $x = 0.23$  ( $10,000^{\circ}$  R). These compositions were used together with Eq. (9c) to determine the partial pressure of uranium for  $y = 0.001$  to  $y = 0.020$  (Table 6a and 7a). The partial pressure of uranium ( $y = 0.001$ ) and the average molecular weight of the gaseous mixture as a function of  $x$  (for  $y = 0.001$ ,  $0.01$ , and  $0.02$ ) are given in Tables 6b and 7b and are plotted in Figure 6 and 7. The average molecular weight of the gaseous mixture is less than  $1.5 \times MW_H$  over a selected range of  $x$  at  $9000^{\circ}$  R but is greater than  $1.5 \times MW_H$  for all compositions at  $10,000^{\circ}$  R.

TABLE 5  
 CALCULATION PARAMETERS FOR THE PARTIAL PRESSURES  
 NIOBIUM AND CARBON OVER  
 Nb-C ALLOYS AT 9000 AND 10,000° R

a) 9000° R

<u>x</u>	<u>x<sup>2</sup></u>	<u>log(1-x)</u>	<u>log(p<sub>Nb</sub>/p<sub>Nb</sub><sup>0</sup>)</u>	<u>(p<sub>Nb</sub>/p<sub>Nb</sub><sup>0</sup>)</u>	<u>p<sub>Nb</sub></u>	<u>p<sub>C</sub>(Total)</u>
0.01	10 <sup>-4</sup>	-0.0044	-0.0045	0.9897	0.8821	0.001
0.10	0.01	-0.0458	-0.0622	0.8470	0.7549	0.02
0.20	0.04	-0.0969	-0.1625	0.6880	0.6132	0.08
0.30	0.09	-0.1549	-0.3024	0.4984	0.4442	0.25
0.40	0.16	-0.2219	-0.4841	0.3280	0.2923	0.65
0.50	0.25	-0.3010	-0.7108	0.1964	0.1734	1.61
0.60	0.36	-0.3979	-0.9880	0.1028	0.0916	3.86
0.70	0.49	-0.5229	-1.3260	0.0472	0.0421	9.00
0.80	0.64	-0.6990	-1.7479	0.0179	0.0159	19.06
0.90	0.81	-1.0000	-2.3276	0.0047	0.0042	32.49
0.99	0.98	-2.0000	-3.6062	0.0003	0.0002	48.92

b) 10,000° R

<u>x</u>	<u>log(p<sub>Nb</sub>/p<sub>Nb</sub><sup>0</sup>)</u>	<u>(p<sub>Nb</sub>/p<sub>Nb</sub><sup>0</sup>)</u>	<u>p<sub>Nb</sub></u>	<u>p<sub>C</sub>(Total)</u>
0.01	-0.0045	0.9897	4.421	0.01
0.10	-0.0606	0.8698	3.885	0.16
0.20	-0.1559	0.6984	3.120	0.58
0.30	-0.2877	0.5168	2.309	1.52
0.40	-0.4581	0.3483	1.556	3.46
0.50	-0.6700	0.2138	0.955	7.48
0.60	-0.9293	0.1177	0.526	16.29
0.70	-1.2461	0.0567	0.253	36.10
0.80	-1.6436	0.0227	0.101	76.15
0.90	-2.1956	0.0064	0.028	142.87
0.99	-3.4465	0.0004	0.002	214.54

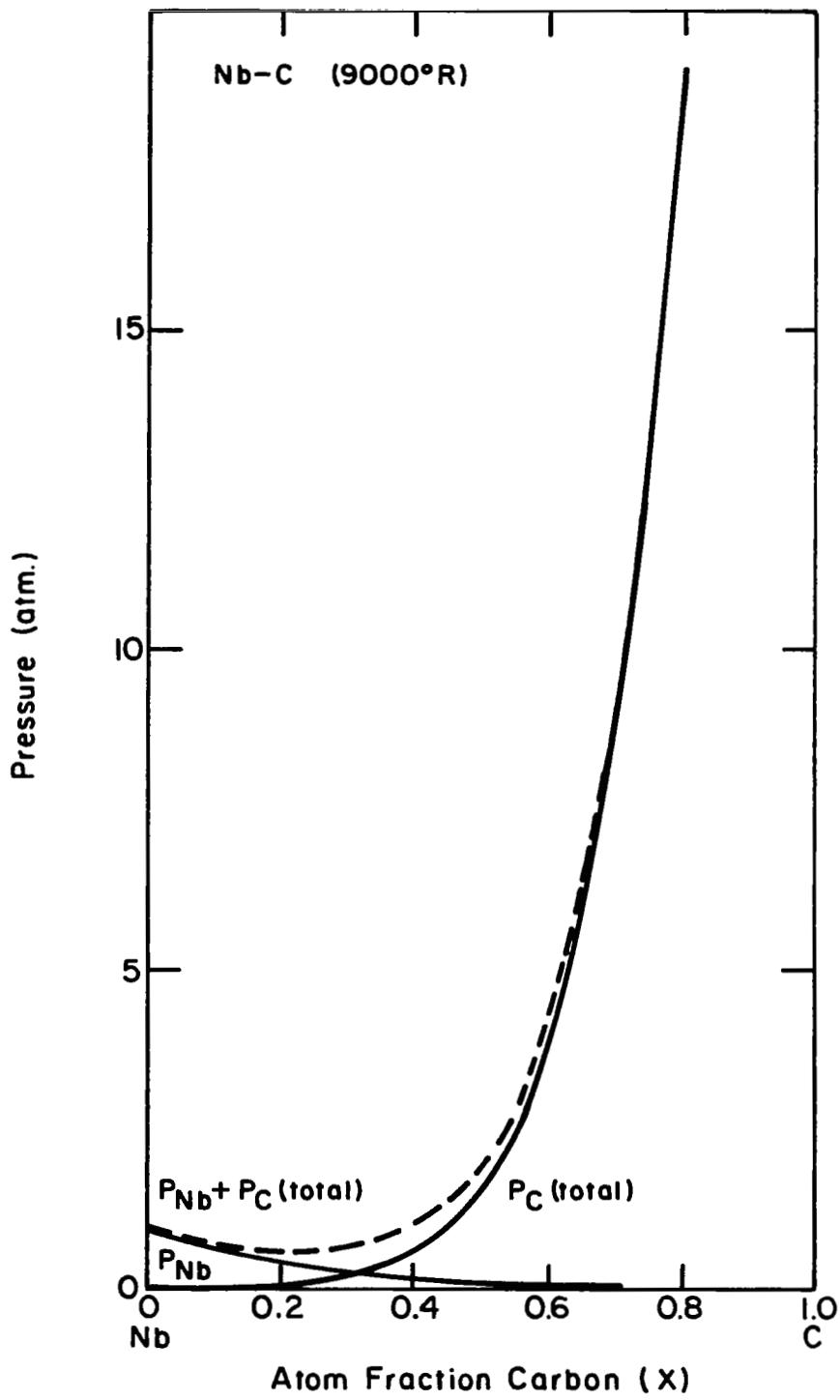


Figure 4. The Partial Pressures of Niobium and Carbon at  $9000^{\circ}$  R as a Function of Alloy Composition.

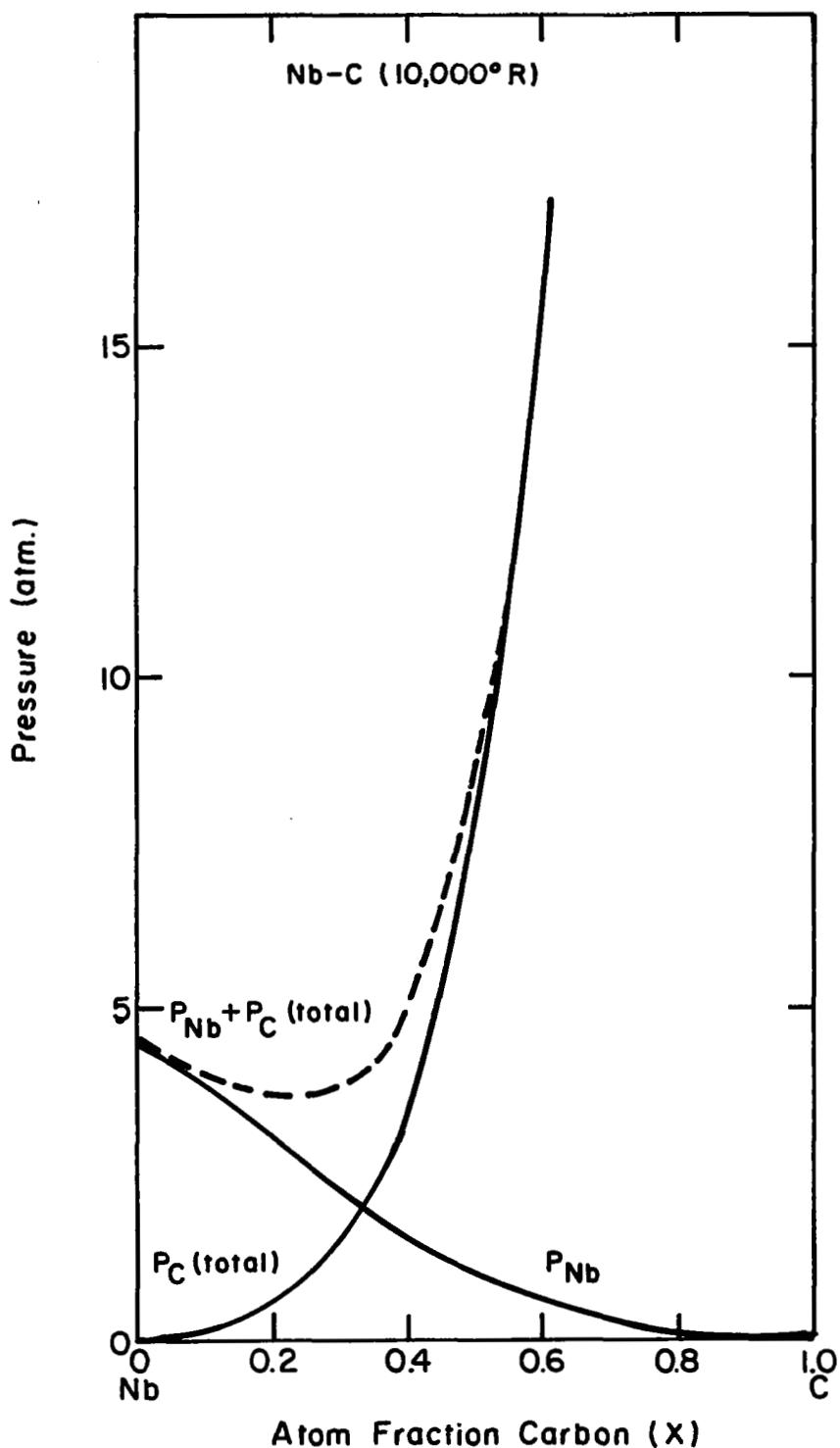


Figure 5. The Partial Pressures of Niobium and Carbon at 10,000° R as a Function of Alloy Composition.

TABLE 6  
THE PARTIAL PRESSURE OF URANIUM OVER  
Nb-C-U ALLOYS AT  $9000^{\circ}\text{R}$

a)  $x = 0.25$

<u>y</u>	<u>log y</u>	<u><math>\bar{F}_{\text{E-U}}^L</math></u>	<u><math>\log(p_{\text{U}}/p_{\text{U}}^{\circ})</math></u>	<u><math>(p_{\text{U}}/p_{\text{U}}^{\circ}) \times 10^2</math></u>	<u><math>p_{\text{U}}(7)</math></u>	<u><math>p_{\text{U}}(8)</math></u>
0.001	-3.0	+0.084	-2.916	0.121	0.0130	0.0057
0.005	-2.301	+0.082	-2.219	0.604	0.0647	0.0283
0.010	-2.0	+0.080	-1.920	1.203	0.129	0.0563
0.015	-1.824	+0.078	-1.746	1.795	0.192	0.0840
0.020	-1.699	+0.076	-1.623	2.382	0.255	0.1114

b)  $y = 0.001, p_{\text{U}}^{\circ} = 4.677$

<u>x</u>	<u><math>\bar{F}_{\text{E-U}}^L</math></u>	<u><math>\log(p_{\text{U}}/p_{\text{U}}^{\circ})</math></u>	<u><math>(p_{\text{U}}/p_{\text{U}}^{\circ}) \times 10^3</math></u>	<u><math>p_{\text{U}}(8)</math></u>	<u><math>\tilde{M}</math></u>	<u><math>\tilde{M}_{(y=0.01)}</math></u>	<u><math>\tilde{M}_{(y=0.02)}</math></u>
0.10	+0.194	-2.806	1.563	0.0073	2.239	2.389	2.650
0.20	+0.129	-2.871	1.346	0.0063	2.115	2.244	2.469
0.30	+0.031	-2.969	1.074	0.0050	1.984	2.087	2.264
0.40	-0.100	-3.100	0.794	0.0037	1.899	1.976	2.110
0.50	-0.264	-3.264	0.545	0.0025	1.969	2.021	2.111
0.60	-0.460	-3.460	0.347	0.0016	2.395	2.428	2.485

$$\underline{1.5 \times M_H = 2.303}$$

TABLE 7  
THE PARTIAL PRESSURE OF URANIUM OVER  
Nb-C-U ALLOYS AT  $10,000^{\circ}\text{R}$

a)  $x = 0.23$

<u>y</u>	<u>log y</u>	<u><math>\bar{F}_{\text{E-U}}^L</math></u>	<u><math>\log(p_{\text{U}}/p_{\text{U}}^{\circ})</math></u>	<u><math>(p_{\text{U}}/p_{\text{U}}^{\circ}) \times 10^2</math></u>	<u><math>p_{\text{U}}(7)</math></u>	<u><math>p_{\text{U}}(8)</math></u>
0.001	-3.0	+0.101	-2.899	0.126	0.0399	0.0235
0.005	-2.301	+0.099	-2.202	0.628	0.1990	0.1170
0.010	-2.0	+0.097	-1.913	1.250	0.395	0.233
0.015	-1.824	+0.096	-1.728	1.871	0.592	0.348
0.020	-1.699	+0.094	-1.605	2.483	0.785	0.462

b)  $y = 0.001, p_{\text{U}}^{\circ} = 18.62$

<u>x</u>	<u><math>\bar{F}_{\text{E-U}}^L</math></u>	<u><math>\log(p_{\text{U}}/p_{\text{U}}^{\circ})</math></u>	<u><math>(p_{\text{U}}/p_{\text{U}}^{\circ}) \times 10^3</math></u>	<u><math>p_{\text{U}}(8)</math></u>	<u><math>\tilde{M}</math></u>	<u><math>\frac{\tilde{M}}{(y=0.01)}</math></u>	<u><math>\frac{\tilde{M}}{(y=0.02)}</math></u>
0.10	+0.175	-2.825	1.496	0.0219	4.837	5.385	6.042
0.20	+0.116	-2.884	1.306	0.0243	4.210	4.691	5.269
0.30	+0.028	-2.972	1.067	0.0198	3.591	3.984	4.458
0.40	-0.090	-3.090	0.813	0.0151	3.158	3.456	3.813
0.50	-0.237	-3.237	0.593	0.0110	3.255	3.459	3.707
0.60	-0.414	-3.414	0.386	0.0072	4.589	4.715	4.867

$$\underline{1.5 \times M_H = 2.01}$$

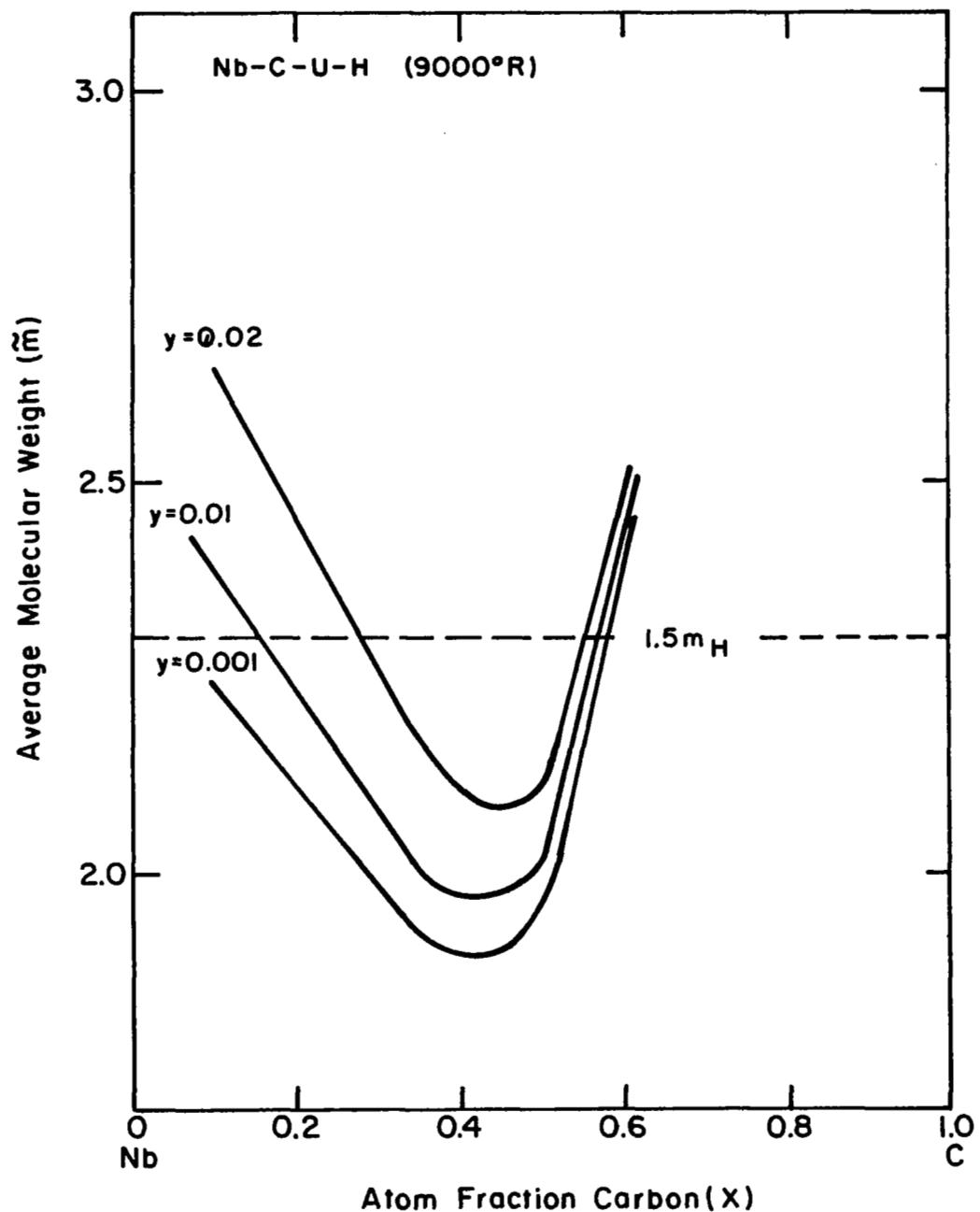


Figure 6. Average Molecular Weight of Gaseous Nb-C-U-H at 9000°R for Variable Nb-C Compositions.

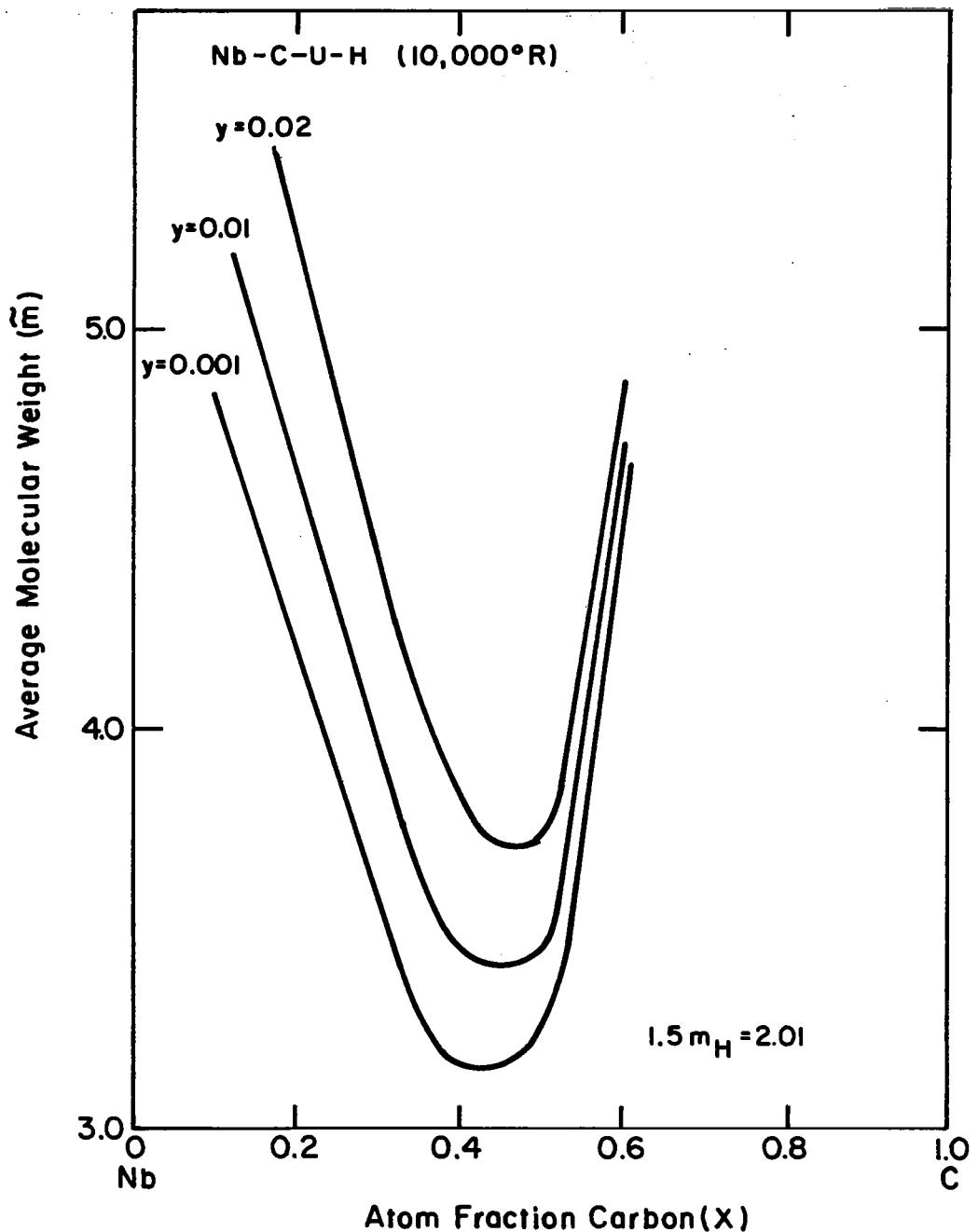


Figure 7. Average Molecular Weight of Gaseous Nb-C-U-H at 10,000° R for Variable Nb-C Compositions.

#### 4. POTENTIAL OF OTHER SYSTEMS

Selection of other elements for  $X_1$  and  $X_2$  is generally precluded by one or more of the following unfavorable conditions:

- 1) High nuclear capture cross sections,
- 2) High vapor pressure over the element in the temperature range of interest, and
- 3) Unfavorable excess free energy of mixing.

The common refractory metals must be eliminated on the basis of condition 1), with the possible exceptions of molybdenum and tungsten-184 (see Table 1). The free energies of formation of Mo-C compounds are less negative than the Zr-C and Nb-C compounds, and the activity (and thus, partial pressure) of Mo in Mo-C alloys is higher over the practical range of alloy composition.

$W^{184}$ -C-U alloys are expected to have properties similar to those studied. It is recommended that this system be considered for a future investigation.

Of the non-metals ( $X_2$ ), boron is the most likely candidate. However, at  $9000^{\circ}\text{R}$  the vapor pressure of boron over pure boron is about ten times the vapor pressure of carbon over pure carbon. As the heats of formation of MeB and MeC compounds are comparable, there would not be a sufficient increase in the negativity of the excess free energy of mixing to offset the increased boron partial pressures.

It is considered to be most appropriate to re-evaluate the initial constraints listed in the introduction in light of the findings that are reported herein.

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APPENDIX A

VAPOR PRESSURE DATA FOR  
CARBON POLYMORPHS

TABLE 1A  
VAPOR PRESSURE OF C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub>, C<sub>4</sub> AND C<sub>5</sub> (11)

T°K	T°R	$\log p_C/a_C$	$p_C^o$	$\log p_{C_2}/a_C^2$	$p_{C_2}^o$	$\log p_{C_3}/a_C^3$	$p_{C_3}^o$	$\log p_{C_4}/a_C^4$	$p_{C_4}^o$	$\log p_{C_5}/a_C^5$	$p_{C_5}$
3500	6300	-2.50	0.0031	-2.50	0.0031	-1.95	0.011	-3.76	0.0002	-3.60	0.0003
3600	6480	-2.20	0.0063	-2.16	0.0069	-1.63	0.023	-3.37	0.0004	-3.20	0.0006
3700	6660	-1.93	0.012	-1.84	0.0145	-1.33	0.047	-2.99	0.001	-2.82	0.0015
3800	6840	-1.66	0.022	-1.54	0.029	-1.06	0.087	-2.63	0.0024	-2.45	0.0036
3900	7020	-1.41	0.039	-1.26	0.055	-0.79	0.16	-2.28	0.0055	-2.11	0.0078
4000	7200	-1.18	0.066	-0.99	0.102	-0.54	0.29	-1.96	0.011	-1.79	0.016
4100	7380	-0.96	0.11	-0.73	0.19	-0.30	0.50	-1.65	0.022	-1.48	0.033
4200	7560	-0.74	0.18	-0.49	0.32	-0.07	0.85	-1.36	0.044	-1.19	0.065
4300	7740	-0.53	0.30	-0.25	0.56	+0.14	1.38	-1.08	0.083	-0.91	0.123
4400	7920	-0.33	0.47	-0.03	0.93	0.35	2.24	-0.81	0.155	-0.64	0.229
4444	8000	-0.25	0.56	+0.06	1.15	0.44	2.76	-0.70	0.20	-0.53	0.295
4500	8100	-0.15	0.71	+0.18	1.51	0.54	3.47	-0.56	0.28	-0.40	0.400
4600	8280	+0.03	1.07	+0.38	2.40	0.73	5.37	-0.32	0.48	-0.15	0.71
4700	8460	0.20	1.59	+0.58	3.80	0.91	8.13	-0.09	0.81	+0.08	1.20
4800	8640	0.36	2.29	+0.76	5.76	1.08	12.0	+0.13	1.35	0.30	2.00
4900	8820	0.52	3.31	0.94	8.71	1.24	17.3	+0.36	2.29	0.51	3.24
5000	9000	0.67	4.7	1.11	12.89	1.40	25.1	0.55	3.55	0.72	5.25
5100	9180	0.81	6.5	1.27	18.62	1.55	35.5	0.74	5.50	0.91	8.13
5200	9360	0.95	8.9	1.43	26.92	1.69	49.0	0.93	8.51	1.10	12.6
5300	9540	1.08	12.0	1.58	38.02	1.83	67.6	1.11	12.90	1.27	18.63
5400	9720	1.21	16.2	1.72	52.50	1.96	91.2	1.28	19.10	1.44	27.55
5500	9900	1.34	21.9	1.86	72.45	2.09	123	1.44	27.55	1.61	40.74
*5555	10,000	1.41	25.7	1.94	87.10	2.16	145	1.53	33.90	1.70	50.1
5600	10,080	1.46	28.8	2.00	100	2.21	162	1.60	39.80	1.77	58.9

\* Extrapolated

TABLE 2A  
 PRESSURE OF CARBON POLYMORPHS OVER  
 Zr-C ALLOYS AT 9000° R

<u>x</u>	<u>a<sub>C</sub></u>	<u>p<sub>C</sub></u>	<u>p<sub>C<sub>2</sub></sub></u>	<u>p<sub>C<sub>3</sub></sub></u>	<u>p<sub>C<sub>4</sub></sub></u>	<u>p<sub>C<sub>5</sub></sub></u>	<u>p<sub>C</sub>(T)</u>
0.01	0.0005	0.0023					0.002
0.10	0.0082	0.0384					0.038
0.20	0.0278	0.1298	0.01				0.140
0.30	0.0662	0.3096	0.06	0.01			0.380
0.40	0.1317	0.616	0.22	0.06			0.896
0.50	0.2312	1.081	0.68	0.31	0.01		2.08
0.60	0.3662	1.713	1.73	1.23	0.06	.03	4.76
0.70	0.5303	2.480	3.62	3.74	0.28	.21	10.33
0.80	0.7071	3.307	6.45	8.88	0.89	.95	20.48
0.90	0.8726	4.081	9.82	16.69	2.06	2.68	35.33
0.99	0.9897	4.629	12.63	24.35	3.41	4.99	50.00

TABLE 3A  
PRESSURE OF CARBON POLYMORPHS OVER  
Nb-C ALLOYS AT 9000 AND 10,000° R

a) 9000° R

<u>x</u>	<u>a<sub>C</sub></u>	<u>P<sub>C</sub></u>	<u>P<sub>C<sub>2</sub></sub></u>	<u>P<sub>C<sub>3</sub></sub></u>	<u>P<sub>C<sub>4</sub></sub></u>	<u>P<sub>C<sub>5</sub></sub></u>	<u>P<sub>C (T)</sub></u>
0.01	0.0003	0.0012					0.001
0.10	0.0047	0.022					0.02
0.20	0.0179	0.084					0.08
0.30	0.0472	0.221	0.03				0.25
0.40	0.1028	0.481	0.14	0.03			0.65
0.50	0.1964	0.910	0.50	0.19	0.01		1.61
0.60	0.3280	1.534	1.39	0.88	0.04	0.02	3.86
0.70	0.4984	2.331	3.20	3.09	0.22	0.16	9.00
0.80	0.6880	3.218	6.10	8.14	0.79	0.81	19.06
0.90	0.8470	3.961	9.25	15.18	1.82	2.28	32.49
0.99	0.9897	4.629	12.64	24.25	3.41	4.99	48.92

b) 10,000° R

<u>x</u>	<u>a<sub>C</sub></u>	<u>P<sub>C</sub></u>	<u>P<sub>C<sub>2</sub></sub></u>	<u>P<sub>C<sub>3</sub></sub></u>	<u>P<sub>C<sub>4</sub></sub></u>	<u>P<sub>C<sub>5</sub></sub></u>	<u>P<sub>C (T)</sub></u>
0.01	0.0004	0.009					0.01
0.10	0.0064	0.160					0.16
0.20	0.0227	0.570	0.01				0.58
0.30	0.0567	1.423	0.08	0.02			1.52
0.40	0.1177	2.954	0.36	0.14	0.01		3.46
0.50	0.2138	5.366	1.17	0.85	0.07	0.02	7.48
0.60	0.3483	8.742	3.12	3.67	0.50	0.26	16.29
0.70	0.5168	12.972	6.86	12.01	2.42	1.84	36.10
0.80	0.6984	17.530	12.53	29.70	8.07	8.32	76.15
0.90	0.8698	21.832	19.44	57.31	19.39	24.90	142.87
0.99	0.9897	24.841	25.17	84.49	32.54	47.50	241.54