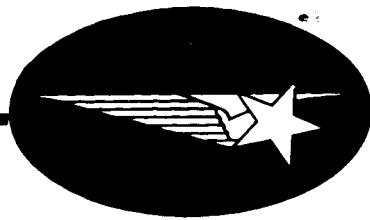


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# JUNCTURE STRESS FIELDS IN MULTICELLULAR SHELL STRUCTURES

## VOL. IV STRESSES AND DEFORMATIONS OF FIXED-EDGE SEGMENTAL SPHERICAL SHELLS

by

E. Y. W. TSUI

C. T. CHEN

P. STERN

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## JUNCTURE STRESS FIELDS IN MULTICELLULAR SHELL STRUCTURES

VOL. IV  
STRESSES AND DEFORMATIONS OF FIXED-EDGE  
SEGMENTAL SPHERICAL SHELLS

by

E. Y. W. TSUI

C. T. CHEN

P. STERN

*Lockheed*

MISSILES & SPACE COMPANY

A GROUP DIVISION OF LOCKHEED AIRCRAFT CORPORATION

SUNNYVALE, CALIFORNIA

## SUMMARY

13836

This report presents a set of basic equations for thin elastic spherical shells and a digital program for the analysis of the static response of segmental spherical shells with fixed edges under the following loading conditions:

- Uniform pressure
- Linear thermal gradient through the thickness of shell

The problem is solved numerically by means of finite-difference technique, using a direct method of solving a large system of simultaneous equations. A numerical example showing the stresses and deformations of a spherical sector under uniform pressure is also presented. For completeness as a self-contained report, much of the information presented in Vol. II is repeated here.

Author

## FOREWORD

This report is the result of a study on the numerical analysis of stresses and deformations of fixed-edge isotropic segmental spherical shells under uniform and hydrostatic pressures as well as linear thermal gradient across the thickness of the shell. Work on this study was performed by staff members of Lockheed Missiles & Space Company in cooperation with the George C. Marshall Space Flight Center of the National Aeronautics and Space Administration under Contract NAS 8-11480. Contract technical representative was H. Coldwater.

This volume is the fourth of a nine-volume final report of studies conducted by the department of Solid Mechanics, Aerospace Sciences Laboratory, Lockheed Missiles & Space Company. Project Manager was K. J. Forsberg; E. Y. W. Tsui was Technical Director for the work.

The nine volumes of the final report have the following titles:

- Vol. I Numerical Methods of Solving Large Matrices
- Vol. II Stresses and Deformations of Fixed-Edge Orthotropic Segmental Cylindrical Shells
- Vol. III Stresses and Deformations of Fixed-Edge Segmental Conical Shells
- Vol. IV Stresses and Deformations of Fixed-Edge Segmental Spherical Shells
- Vol. V Influence Coefficients of Segmental Shells
- Vol. VI Analysis of Multicellular Propellant Pressure Vessels by the Stiffness Method
- Vol. VII Buckling Analysis of Segmental Orthotropic Cylinders Under Uniform Stress Distribution
- Vol. VIII Buckling Analysis of Segmental Orthotropic Cylinders Under Non-uniform Stress Distribution
- Vol. IX Summary of Results and Recommendations

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## NOTATION

$a_i, b_i, c_i, A, B, C, \kappa$	nondimensional parameters defined in text
$D = E\hat{h}^3/12(1 - \nu^2)$	flexural rigidity of shell
$E$	modulus of elasticity
$F_i$	boundary force at Station i
$F^f$	boundary forces of fixed-edge shell due to applied forces or thermal gradients
$G$	shear modulus
$\hat{h}$	thickness of shell
$\bar{h}, \bar{k}$	mesh spacings in $\phi$ - and $\theta$ -coordinate directions
$m, n$	number of columns and rows of the mesh
$i, j$	dummy subscripts
$k, k_{ij}$	stiffness influence coefficients
$\hat{M}(\ ), \hat{N}(\ )$	moments and stress resultants
$p(\ )$	surface or body forces
$\hat{Q}(\ )$	transverse shears
$R$	radius of curvature
$T$	change of temperature from a zero thermal stress condition
$\hat{u}, \hat{v}, \hat{w}$	displacement components in directions $\phi$ , $\theta$ , and $\hat{z}$
$\phi, \theta, \hat{z}$	shell coordinates

$\alpha$	coefficient of thermal expansion
$\xi, \eta$	orthogonal coordinates along boundaries of shell
$\delta_i$	boundary deformations (displacements or rotations) at Station i
$\epsilon(\ ), \gamma(\ )$	direct and shear strains
$\hat{\chi}(\ )$	changes of curvature or torsion of middle-surface
$\nu$	Poisson's ratio
$\omega(\ )$	rotations of the normal at the middle-surface
$(\ ), \phi$	$\frac{\partial(\ )}{\partial\phi}$
$(\ )_i^j$	functions at a discrete point i, j where i, j implies the $\phi$ - and $\theta$ -directions respectively
$\Phi$	rotation in the middle-surface around the normal

Additional notations and symbols are defined in the text.

## Section 1

### INTRODUCTION

As a result of an investigation of juncture stress fields peculiar to the multicellular pressure vessels (Fig. 1), a theory for the prediction of the membrane and bending stresses and the corresponding deformations for such shell structures was formulated.\*

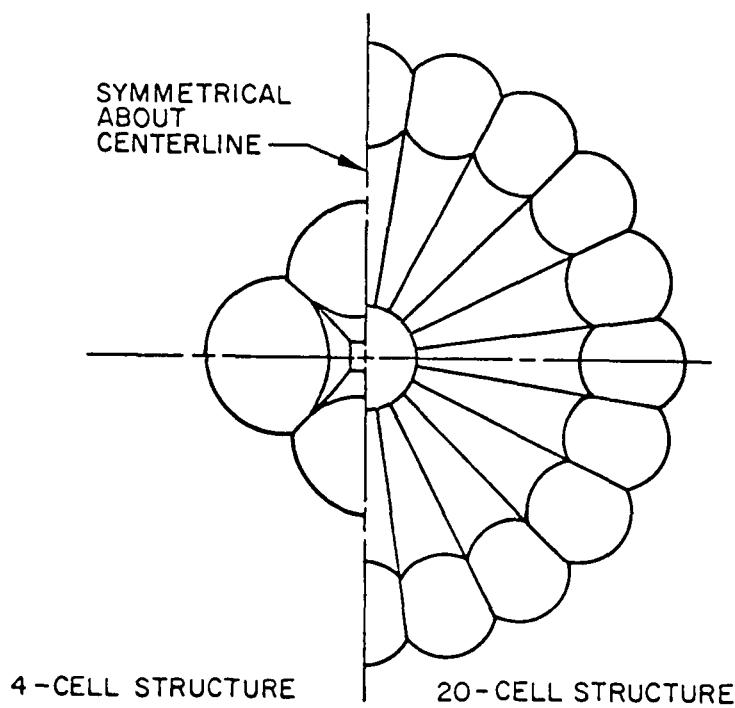


Fig. 1 Multicellular Shell Structure

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\*"Investigation of Juncture Stress Fields in Multicellular Shell Structures," by E. Y. W. Tsui, F. A. Brogan, J. M. Massard, P. Stern, and C. E. Stuhlman, Technical Report M-03-63-1, Lockheed Missiles & Space Company, Sunnyvale, Calif., Feb 1964 - NASA CR-61050.

Due to the fact that analytic solutions are still lacking, it was decided to solve the problem numerically by means of finite-difference technique. To ensure the feasibility of such a numerical solution, a direct method of solving large matrices with a high-speed digital computer was also developed.

According to the previous work, if the stiffness or displacement method is used, the total forces and hence the corresponding stresses along the juncture of the shell segments (Fig. 2) may be expressed concisely in the following matrix form

$$F = k\delta + F^f \quad (1.1)$$

where  $k$  is the stiffness matrix;  $\delta$ , the deformations; and  $F^f$ , the fixed-end forces due to applied loads or thermal gradients. In view of this situation, it is logical to solve the problem systematically by the established general procedure of analysis already described.\* This procedure may be stated briefly as follows:

1. Determination of the fixed-end forces,  $F^f$ , along the boundary as well as stresses and deformations in the interior of shell segments due to loads
2. Determination of the influence coefficients,  $k_{ij}$ , along the boundaries of shell segments, i.e., the induced forces at points  $i$  due to unit deformations ( $\delta = 1$ ) at points  $j$
3. Determination of the actual deformations,  $\delta$ , along the shell boundaries; this requires the satisfaction of both compatibility and equilibrium conditions at the junctures of the structure

Once all the work involved in these three steps is completed, the total stresses and deformations in the specific discrete interior locations may be obtained.

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\*"Investigation of Juncture Stress Fields in Multicellular Shell Structures," by E. Y. W. Tsui, F. A. Brogan, J. M. Massard, P. Stern, and C. E. Stuhlman, Technical Report M-03-63-1, Lockheed Missiles & Space Company, Sunnyvale, Calif., Feb 1964 - NASA CR-61050.

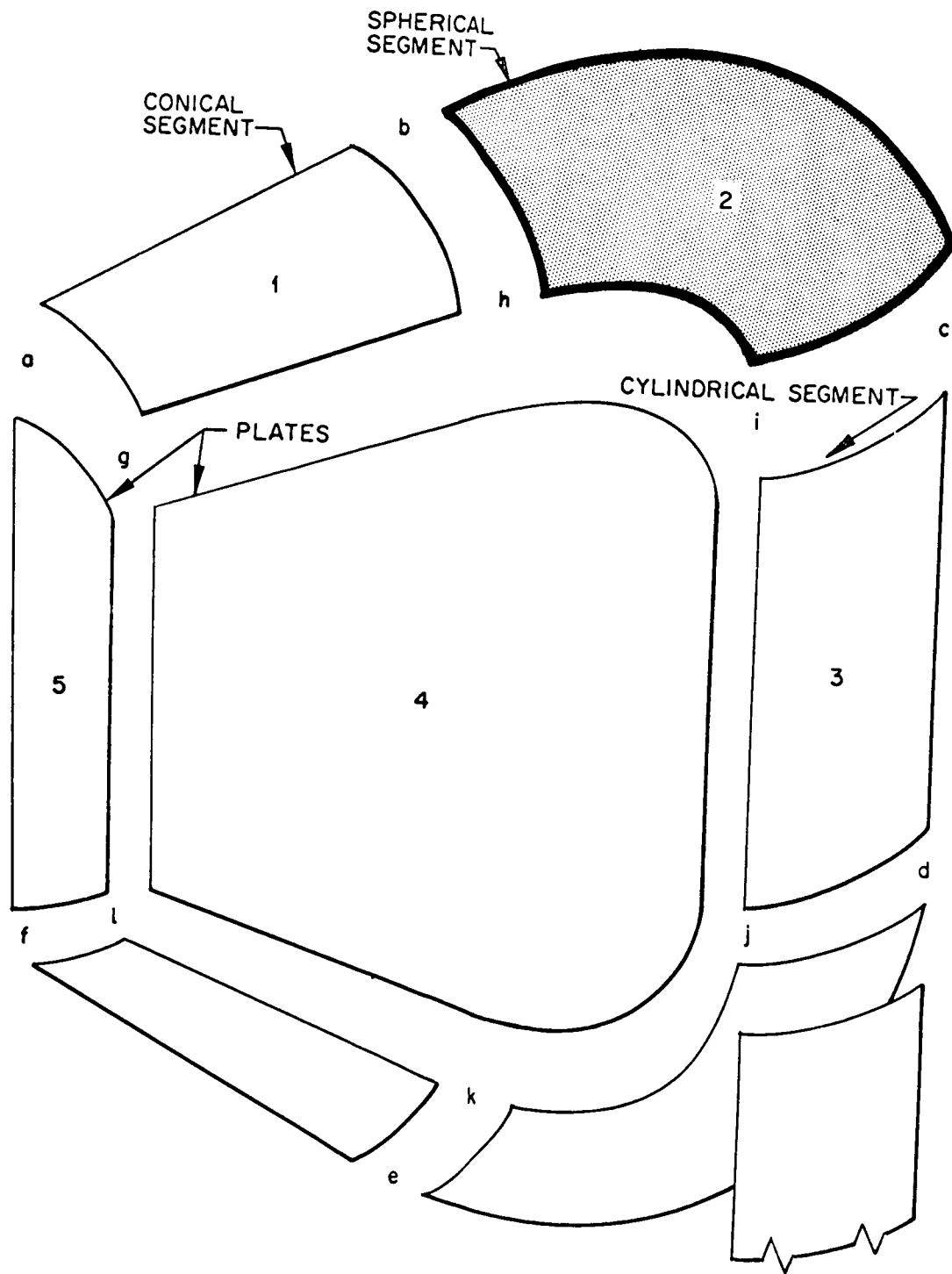


Fig. 2 Basic Shell Elements of Multicellular Structure

This volume presents results of the work involved in Step 1 only and covers the following items:

- Nondimensional formulation of the problem
- Detailed description of a workable digital program for the generation of solutions
- Example including tabulation of stresses and deformations of an isotropic spherical shell with fixed edges under uniform internal pressure

## Section 2

### FORMULATION OF THE PROBLEM

The necessary analytical expressions for a spherical shell have already been presented.\* All the required equations are repeated in this report to make it a complete unit.

#### 2.1 ANALYTICAL FORMULATION

The isotropic segmental spherical shell under consideration is of uniform thickness. It is bounded by a cylindrical panel, a segmental conical shell, and two radial plates as shown in Fig. 2. Only one half of the cell structure is shown in this figure because of the symmetry of the structure and the loading.

The geometry of the spherical segment is shown in Fig. 3. The orthogonal coordinates,  $\phi$  and  $\theta$ , can be oriented in a number of ways in the sphere so as to obtain a convenient description of the boundary curve. For example, in the orientation of Fig. 3 the intersection of the cylinder and sphere occurs at  $\theta = 0$ . It should be noted, however, that these coordinates are not parallel to all the intersections with the sphere.

In the formulation which follows the dependent variables and geometry have been non-dimensionalized by the radius of curvature,  $R$ , as follows:

$$u = \frac{\hat{u}}{R} \quad (2.1a)$$

---

\*"Investigation of Juncture Stress Fields in Multicellular Shell Structures," by E. Y. W. Tsui, F. A. Brogan, J. M. Massard, P. Stern, and C. E. Stuhlman, Technical Report M-03-63-1, Lockheed Missiles & Space Company, Sunnyvale, Calif., Feb 1964 - NASA CR-61050.

$$v = \frac{\hat{v}}{R} \quad (2.1b)$$

$$w = \frac{\hat{z}}{R} \quad (2.1c)$$

$$z = \frac{\hat{z}}{R} \quad (2.1d)$$

$$h = \frac{\hat{h}}{R} \quad (2.1e)$$

Other nondimensional quantities will be defined as they are introduced. Note that the coordinates  $\phi$  and  $\theta$  have not been normalized.

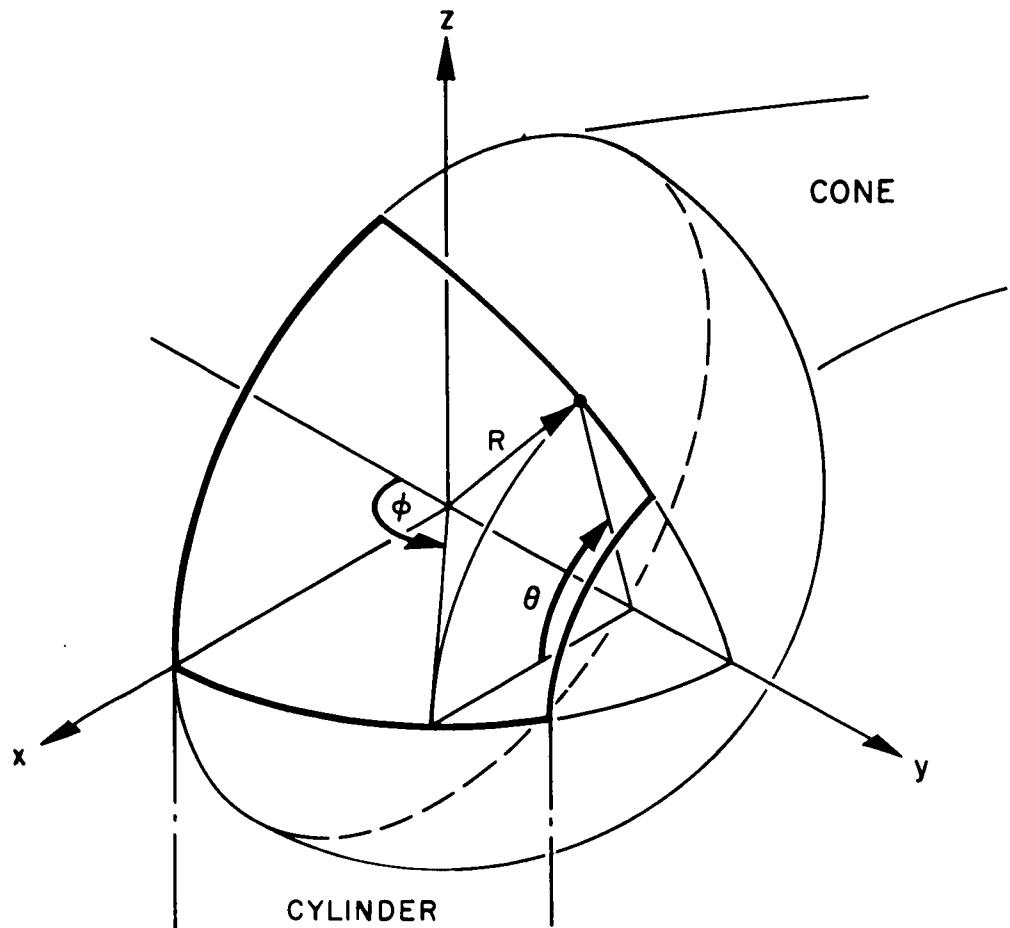


Fig. 3 Geometry of Segmental Spherical Shell

### 2.1.1 Rotation-Displacement Relations

Positive displacements and rotations of the middle-surface are shown in Fig. 4 and are related by equations:

$$\omega_\phi = u - w, \phi \quad (2.2a)$$

$$\omega_\theta = v - \left( \frac{1}{\sin \phi} \right) w, \theta \quad (2.2b)$$

$$\Phi = \frac{[v, \phi - (1/\sin \phi) u, \theta + \cot \phi v]}{2} \quad (2.2c)$$

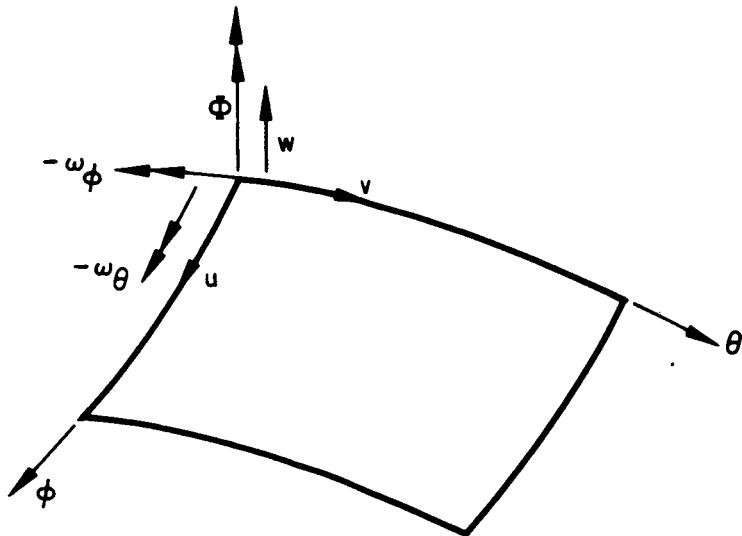


Fig. 4 Displacements and Rotations

### 2.1.2 Strain-Displacement Relations

The strains of the middle-surface are related to displacements by

$$\bar{\epsilon}_\phi = u, \phi + w \quad (2.3a)$$

$$\bar{\epsilon}_\theta = \left(\frac{1}{\sin \phi}\right)v_{,\theta} + \cot \phi u + w \quad (2.3b)$$

$$\bar{\gamma}_{\phi\theta} = v_{,\phi} - \cot \phi v + \left(\frac{1}{\sin \phi}\right)u_{,\theta} \quad (2.3c)$$

and the changes of curvature and torsion are

$$\chi_\phi = [\hat{\chi}_\phi R] = u_{,\phi} - w_{,\phi\phi} \quad (2.4a)$$

$$\chi_\theta = [\hat{\chi}_\theta R] = \frac{[v_{,\theta} - (1/\sin \phi)w_{,\theta\theta} + (u - w_{,\phi})\cos \phi]}{\sin \phi} \quad (2.4b)$$

$$\chi_{\phi\theta} = [\hat{\chi}_{\phi\theta} R] = \frac{[-w_{,\phi\theta} + \cot \phi w_{,\theta} + u_{,\theta} + \sin \phi v_{,\phi} - \cos \phi v]}{\sin \phi} \quad (2.4c)$$

The strains at a distance  $z$  from the middle-surface are

$$\epsilon_\phi = \bar{\epsilon}_\phi + z\chi_\phi \quad (2.5a)$$

$$\epsilon_\theta = \bar{\epsilon}_\theta + z\chi_\theta \quad (2.5b)$$

$$\gamma_{\phi\theta} = \bar{\gamma}_{\phi\theta} + 2z\chi_{\phi\theta} \quad (2.5c)$$

### 2.1.3 Constitutive Relations

Positive stress resultants are shown in Fig. 5. Nondimensional stress resultants are related to them and to strains by the following equations:

$$N_\phi = \left[ \frac{\hat{N}_\phi (1 - \nu^2)}{Eh} \right] = \bar{\epsilon}_\phi + \nu \bar{\epsilon}_\theta + N^T \quad (2.6a)$$

$$N_\theta = \left[ \frac{\hat{N}_\theta(1 - \nu^2)}{E\hat{h}} \right] = \bar{\epsilon}_\theta + \nu \bar{\epsilon}_\phi + N^T \quad (2.6b)$$

$$N_{\theta\phi} = N_{\phi\theta} = \left( \frac{\hat{N}_{\phi\theta}}{\hbar G} \right) = \bar{\gamma}_{\phi\theta} + 2\kappa \chi_{\phi\theta} \quad (2.6c)$$

$$M_\phi = \left( \frac{\hat{M}_\phi R}{D} \right) = \chi_\phi + \nu \chi_\theta + M^T \quad (2.6d)$$

$$M_\theta = \left( \frac{\hat{M}_\theta R}{D} \right) = \chi_\theta + \nu \chi_\phi + M^T \quad (2.6e)$$

$$M_{\phi\theta} = M_{\theta\phi} = \left[ \frac{\hat{M}_{\phi\theta} R}{(1 - \nu)D} \right] = \chi_{\phi\theta} \quad (2.6f)$$

$$Q_\phi = \left( \frac{\hat{Q}_\phi R^2}{D} \right) = \chi_{\phi,\phi} + \nu \chi_{\theta,\phi} + (1 - \nu) \cot \phi (\chi_\phi - \chi_\theta) + \left[ \frac{(1 - \nu)}{\sin \phi} \right] \chi_{\phi\theta,\phi} + M^T, \phi \quad (2.6g)$$

$$Q_\theta = \left( \frac{\hat{Q}_\theta R^2}{D} \right) = \chi_{\theta,\theta} + \nu \chi_{\phi,\theta} + 2(1 - \nu) \cot \phi \chi_{\phi\theta} + (1 - \nu) \chi_{\phi\theta,\phi} + M^T, \theta \quad (2.6h)$$

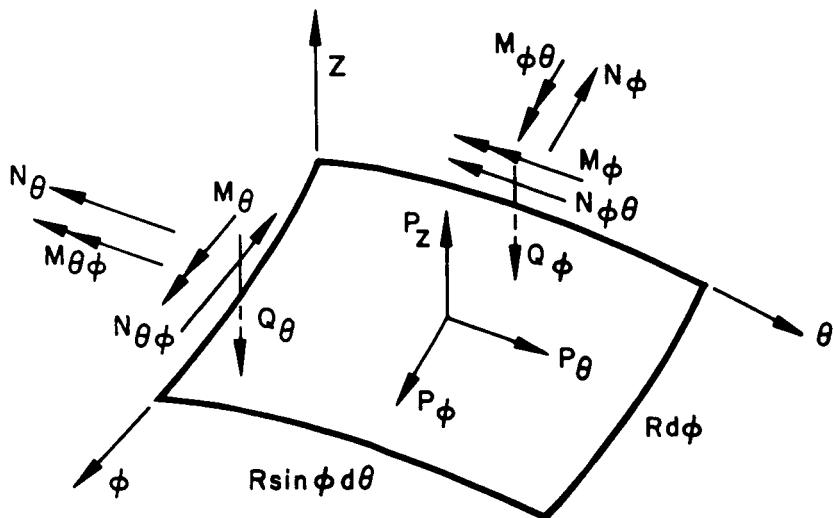


Fig. 5 Stress Resultants, Moments, and Loads

where

$$N^T = \left[ \frac{\hat{N}^T(1 - \nu^2)}{Eh} \right] = -(1 + \nu) \frac{1}{h} \int_{-h/2}^{h/2} \alpha T dz$$

$$M^T = \left( \frac{\hat{M}^T R}{D} \right) = -12(1 + \nu) \frac{1}{h^3} \int_{-h/2}^{h/2} \alpha T z dz$$

and  $T$  is temperature change relative to a zero thermal stress condition;  $\alpha$ , the coefficient of thermal expansion; and  $\kappa = h^2/12$ .

#### 2.1.4 Governing Differential Equations

The governing differential equations for a spherical shell in terms of displacement components  $u$ ,  $v$ , and  $w$  are given by

$$\begin{aligned} a_1 u_{,\phi\phi} + a_2 u_{,\theta\theta} + a_3 u_{,\phi} + a_4 u + a_5 v_{,\phi\theta} + a_6 v_{,\theta} \\ + a_7 w_{,\phi\phi\phi} + a_8 w_{,\phi\theta\theta} + a_9 w_{,\phi\phi} + a_{10} w_{,\theta\theta} + a_{11} w_{,\phi} = A \end{aligned} \quad (2.7a)$$

$$\begin{aligned} b_1 u_{,\phi\theta} + b_2 u_{,\theta} + b_3 v_{,\phi\phi} + b_4 v_{,\theta\theta} + b_5 v_{,\phi} + b_6 v \\ + b_7 w_{,\phi\phi\theta} + b_8 w_{,\theta\theta\theta} + b_9 w_{,\phi\theta} + b_{10} w_{,\theta} = B \end{aligned} \quad (2.7b)$$

$$\begin{aligned} c_1 u_{,\phi\phi\phi} + c_2 u_{,\phi\theta\theta} + c_3 u_{,\phi\phi} + c_4 u_{,\theta\theta} + c_5 u_{,\phi} + c_6 u \\ + c_7 v_{,\phi\phi\theta} + c_8 v_{,\theta\theta\theta} + c_9 v_{,\phi\theta} + c_{10} v_{,\theta} \\ + c_{11} w_{,\phi\phi\phi\phi} + c_{12} w_{,\phi\phi\theta\theta} + c_{13} w_{,\theta\theta\theta\theta} \\ + c_{14} w_{,\phi\phi\phi} + c_{15} w_{,\phi\theta\theta} + c_{16} w_{,\phi\phi} + c_{17} w_{,\theta\theta} \\ + c_{18} w_{,\phi} + c_{19} w = C \end{aligned} \quad (2.7c)$$

where

$$a_1 = (1 + \kappa) \sin \phi$$

$$a_2 = (1 + 4\kappa) \frac{1 - \nu}{2 \sin \phi}$$

$$a_3 = (1 + \kappa) \cos \phi$$

$$a_4 = - \frac{\cos^2 \phi + \nu \sin^2 \phi}{\sin \phi} (1 + \kappa)$$

$$a_5 = \frac{1 + \nu}{2} + (2 - \nu)\kappa$$

$$a_6 = - \frac{\cot \phi}{2} [3 - \nu + 2\kappa(3 - 2\nu)]$$

$$a_7 = - \kappa \sin \phi$$

$$a_8 = - (2 - \nu) \frac{\kappa}{\sin \phi}$$

$$a_9 = - \kappa \cos \phi$$

$$a_{10} = (3 - \nu) \frac{\kappa}{\sin \phi} \cot \phi$$

$$a_{11} = (1 + \nu) \sin \phi + \frac{\cos^2 \phi + \nu \sin^2 \phi}{\sin \phi} \kappa$$

$$b_1 = \frac{1 + \nu}{2} + (2 - \nu)\kappa$$

$$b_2 = \left[ \frac{3 - \nu}{2} + (3 - 2\nu)\kappa \right] \cot \phi$$

$$b_3 = \frac{1 - \nu}{2} (1 + 4\kappa) \sin \phi$$

$$b_4 = \frac{1 + \kappa}{\sin \phi}$$

$$b_5 = \frac{1 - \nu}{2} (1 + 4\kappa) \cos \phi$$

$$b_6 = \frac{1 - \nu}{2} \left( \frac{\sin^2 \phi - \cos^2 \phi}{\sin \phi} \right) (1 + 4\kappa)$$

$$b_7 = -(2 - \nu)\kappa$$

$$b_8 = -\frac{\kappa}{\sin^2 \phi}$$

$$b_9 = -\kappa \cot \phi$$

$$b_{10} = (1 + \nu) - 2\kappa(1 - \nu)$$

$$c_1 = \sin \phi$$

$$c_2 = \frac{2 - \nu}{\sin \phi}$$

$$c_3 = 2 \cos \phi$$

$$c_4 = \frac{\cos \phi}{\sin^2 \phi}$$

$$c_5 = - \left( \frac{1 + \nu \sin^2 \phi}{\sin \phi} + \frac{1 + \nu}{\kappa} \sin \phi \right)$$

$$c_6 = \left( 1 - \nu - \frac{1 + \nu}{\kappa} + \frac{1}{\sin^2 \phi} \right) \cos \phi$$

$$c_7 = 2 - \nu$$

$$c_8 = \frac{1}{\sin^2 \phi}$$

$$c_9 = - \cot \phi$$

$$c_{10} = \left[ 2(1 - \nu) - \frac{1 + \nu}{\kappa} + \frac{1}{\sin^2 \phi} \right]$$

$$c_{11} = - \sin \phi$$

$$c_{12} = - \frac{2}{\sin \phi}$$

$$c_{13} = - \frac{1}{\sin^3 \phi}$$

$$c_{14} = - 2 \cos \phi$$

$$c_{15} = 2 \frac{\cos \phi}{\sin^2 \phi}$$

$$c_{16} = \frac{1 + \nu \sin^2 \phi}{\sin \phi}$$

$$c_{17} = - \frac{4 - (1 + \nu) \sin^2 \phi}{\sin^3 \phi}$$

$$c_{18} = - \left( 1 - \nu + \frac{1}{\sin^2 \phi} \right) \cos \phi$$

$$c_{19} = - 2 \frac{1 + \nu}{\kappa} \sin \phi$$

In general, the loading functions are

$$A = - \sin \phi \left[ (1 - \nu^2) \frac{p_\phi R}{Eh} + N_{,\phi}^T + \kappa M_{,\phi}^T \right] \quad (2.8a)$$

$$B = - \left[ (1 - \nu^2) p_\theta R \frac{\sin \phi}{Eh} + N_{,\theta}^T + \kappa M_{,\theta}^T \right] \quad (2.8b)$$

$$C = - \sin \phi \left[ R^3 \frac{p_z}{D} - \frac{2N_{,\phi\phi}^T}{\kappa} + M_{,\phi\phi}^T + \cot M_{,\phi}^T + \left( \frac{1}{\sin^2 \phi} \right) M_{,\theta\theta}^T \right] \quad (2.8c)$$

As mentioned in Sec. 4, the digital computer program which has been prepared has two options for loading. Specialization of the loading functions for each of these options follows:

- Uniform pressure

$$A = B = 0$$

$$C = - \sin \phi \frac{R^2 p_z}{D} = - \sin \phi$$

This will yield solutions normalized by  $R^3 p_z / D$ . For a given pressure, modulus, and value of Poisson's ratio this quantity can be found. The values of the dimensional dependent variables,  $\hat{u}$ ,  $\hat{v}$ , and  $\hat{w}$ , can be

computed from the nondimensional  $u$ ,  $v$ , and  $w$ , obtained from the computer solution as

$$\hat{u} = \left( \frac{R^4 p_z}{D} \right) u$$

$$\hat{v} = \left( \frac{R^4 p_z}{D} \right) v$$

$$\hat{w} = \left( \frac{R^4 p_z}{D} \right) w$$

- Linear thermal gradient through the thickness of the shell  
For this special case  $T$  is given by

$$T = T_1 + T_2 z$$

where

$$T_1 = \frac{1}{2} (T_e + T_i) - 2T_o$$

$$T_2 = \frac{(T_e - T_i)}{h}$$

and

$$T_e = \text{temperature at external surface } \left( z = \frac{h}{2} \right)$$

$$T_i = \text{temperature at internal surface } \left( z = -\frac{h}{2} \right)$$

$$T_o = \text{reference temperature}$$

Then in nondimensional form

$$N^T = -(1 + \nu) \alpha T_1$$

$$M^T = -(1 + \nu) \alpha T_2$$

The loading functions in nondimensional form become

$$A = B = 0$$

$$C = -2 \sin \varphi \frac{(1 + \nu) \alpha T_1}{\kappa}$$

Dimensional displacements can be computed from the nondimensional solutions for  $u$ ,  $v$ , and  $w$  through the relationships

$$\hat{u} = uR$$

$$\hat{v} = vR$$

$$\hat{w} = wR$$

## 2.2 BOUNDARY CONDITIONS

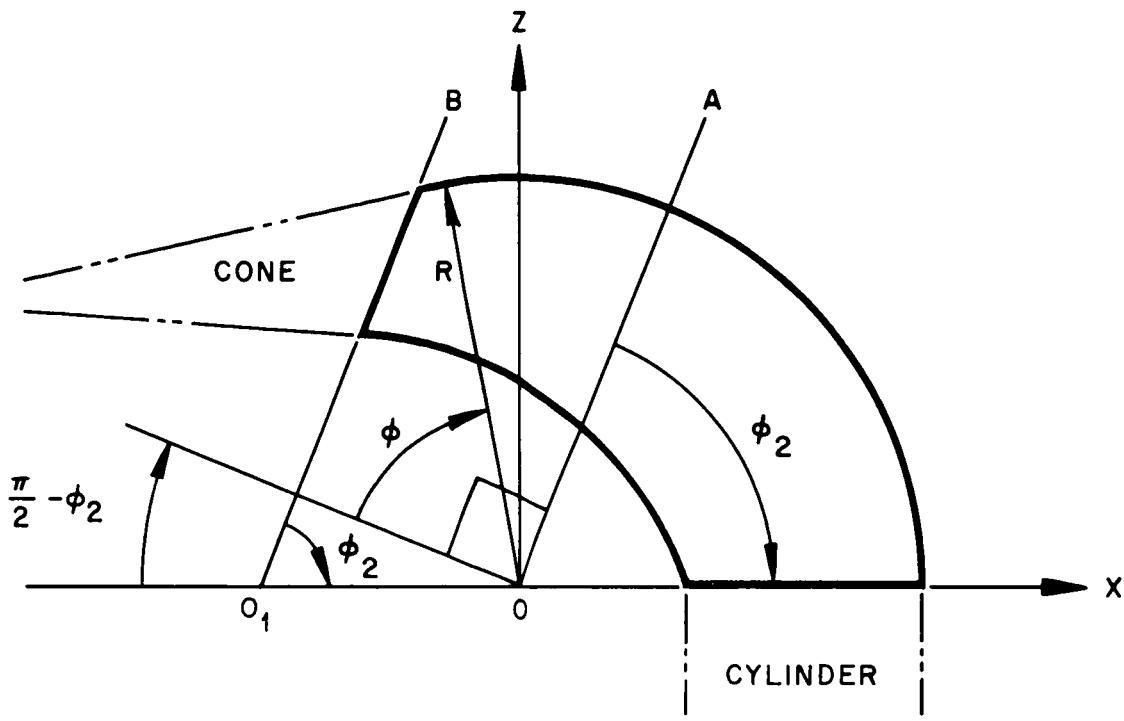
It was pointed out in Sec. 2.1 that the coordinates can be oriented so as to obtain a convenient description of the boundary curve. By such a description it is implied that the boundary is parallel or nearly parallel to coordinate lines. Two orientations of the orthogonal coordinates  $\phi$  and  $\theta$  are shown in Fig. 6. The coordinates in the two orientations are related to the rectangular coordinate system as follows:

Orientation 1

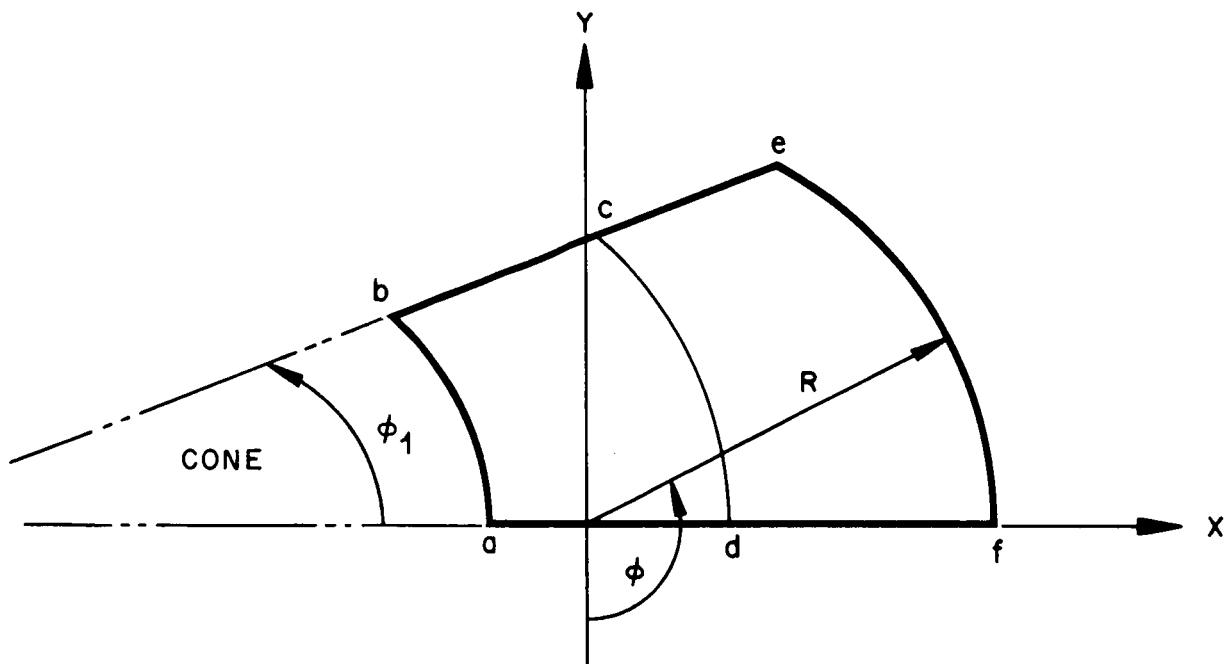
$$x = R(\sin \phi \cos \phi_2 \cos \theta - \cos \phi \sin \phi_2) \quad (2.9a)$$

$$y = R \sin \phi \sin \theta \quad (2.9b)$$

$$z = R(\cos \phi \cos \phi_2 + \sin \phi \cos \theta \sin \phi_2) \quad (2.9c)$$



Orientation 1 (Side View)



Orientation 2 (Top View)

Fig. 6 Orientations of Coordinate  $\phi$

Orientation 2

$$x = R \sin \phi \cos \theta \quad (2.10a)$$

$$y = -R \cos \phi \quad (2.10b)$$

$$z = R \sin \phi \sin \theta \quad (2.10c)$$

To use these orientations, consider the sphere cut as shown in Fig. 6 by the plane OA which is parallel to plane  $O_1B$ . That part of the sphere which is between the cone and plane OA is described by Orientation 1; the remaining portion, by Orientation 2. Thus, the sphere is divided into two parts each of which has two boundaries parallel to the curvilinear coordinates. The boundary curve and boundary conditions of Orientation 1 are given as shown in Fig. 7.

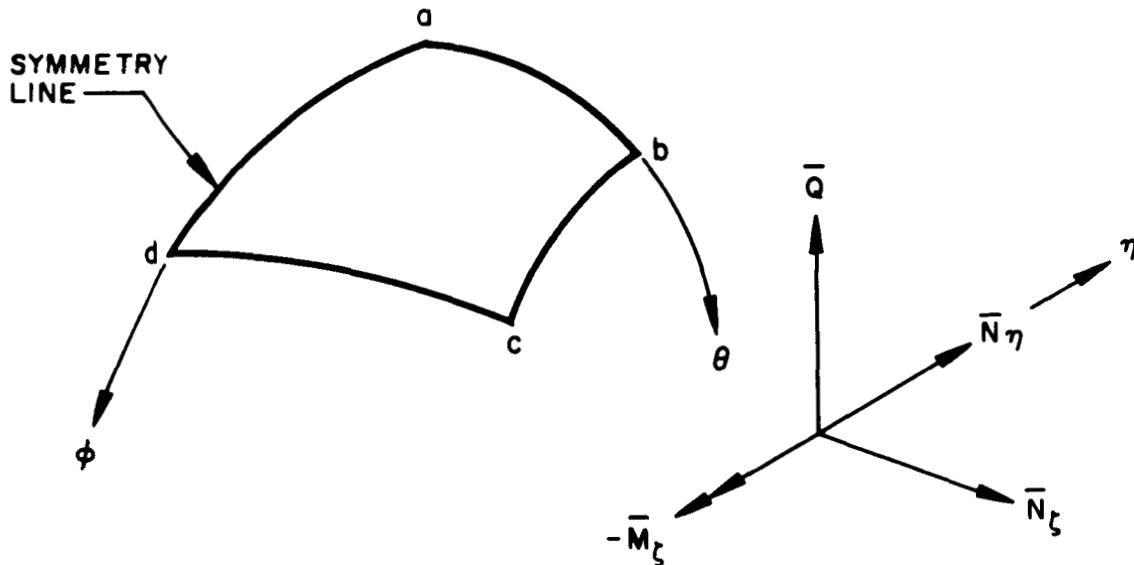


Fig. 7 Boundary Curve and Forces for Orientation 1

The boundary forces along the edges of the shell are given by the equations:

along  $\overline{ab}$

$$\bar{N}_\eta = N_\phi \theta + 2\kappa M_\phi \theta$$

$$\bar{N}_\zeta = N_\phi$$

$$\bar{Q} = - \left[ Q_\phi + \frac{(1 - \nu)}{\sin \phi} M_{\phi \theta, \theta} \right]$$

$$\bar{M}_\zeta = M_\phi$$

along  $\overline{cd}$

$$\bar{N}_\eta = N_\phi \theta + 2\kappa M_\phi \theta$$

$$\bar{N}_\zeta = N_\phi$$

$$\bar{Q} = Q_\phi + \frac{(1 - \nu)}{\sin \phi} M_{\phi \theta, \theta}$$

$$\bar{M}_\zeta = M_\phi$$

along  $\overline{bc}$

Since the curve  $\overline{bc}$  is not parallel to a coordinate line the boundary forces are given by the general expressions:

$$\hat{N}_\eta = \hat{N}_\eta + \frac{1}{R} \hat{M}_{\zeta \eta}$$

$$\hat{N}_\zeta = \hat{N}_\zeta$$

$$\hat{\hat{Q}} = \hat{Q}_3 + \frac{1}{A_\eta} \frac{\partial \hat{M}_\zeta}{\partial \eta}$$

$$\hat{\hat{M}}_\zeta = \hat{M}_\zeta$$

where

$$\hat{N}_\zeta = \cos^2 \lambda \hat{N}_\theta + \sin^2 \lambda \hat{N}_\phi + \sin 2\lambda \hat{N}_{\phi\theta}$$

$$\hat{N}_\eta = \frac{1}{2} \sin 2\lambda (\hat{N}_\theta - \hat{N}_\phi) + (\sin^2 \lambda - \cos^2 \lambda) \hat{N}_{\phi\theta}$$

$$\hat{Q}_3 = \sin \lambda \hat{Q}_\phi + \cos \lambda \hat{Q}_\theta$$

$$\hat{M}_\zeta = \cos^2 \lambda \hat{M}_\theta + \sin^2 \lambda \hat{M}_\phi + \sin 2\lambda \hat{M}_{\phi\theta}$$

$$\hat{M}_{\zeta\eta} = \frac{1}{2} \sin 2\lambda (M_\theta - M_\phi) + (\sin^2 \lambda - \cos^2 \lambda) \hat{M}_{\phi\theta}.$$

The direction cosine must be found from the following intersection relations:

$$\cos \lambda = \pm \frac{1}{[f^2 \sin^2 \phi + 1]^{1/2}}$$

where  $\lambda$  is the angle between the boundary curve and the  $\phi$ -axis and

$$f = \frac{\tan \phi_1}{\sin^2 \phi} \left[ \frac{-(R_1/R - 1) \cos \phi + \sin \phi_2}{\cos \theta + \tan \phi_1 \cos \phi_2 \sin \theta} \right]$$

The relation between  $\theta$  and  $\phi$  is found by the relation

$$\sin \theta - \tan \phi_1 \cos \phi_2 \cos \theta = \frac{\tan \phi_1}{\sin \phi} \left[ \left( \frac{R_1}{R} - 1 \right) - \sin \phi_2 \cos \phi \right].$$

For the spherical segment to have fixed edges, the displacement components are all zero. Hence, the required boundary conditions are as follows:

$$\overline{ab} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \phi} \equiv 0$$

$$\overline{bc} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \zeta} \equiv 0$$

$$\overline{cd} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \phi} \equiv 0$$

The boundary curve and boundary condition of Orientation 2 are given as shown in Fig. 8.

The boundary forces along the edges of the shell are given by the equations:

along  $\overline{dc}$

$$\bar{N}_\eta = -N_{\theta\phi} - 2\kappa M_{\phi\theta}$$

$$\bar{N}_\zeta = N_\theta$$

$$\bar{Q} = Q_\theta + (1 - \nu) M_{\phi\theta, \phi}$$

$$\bar{M}_\zeta = M_\theta$$

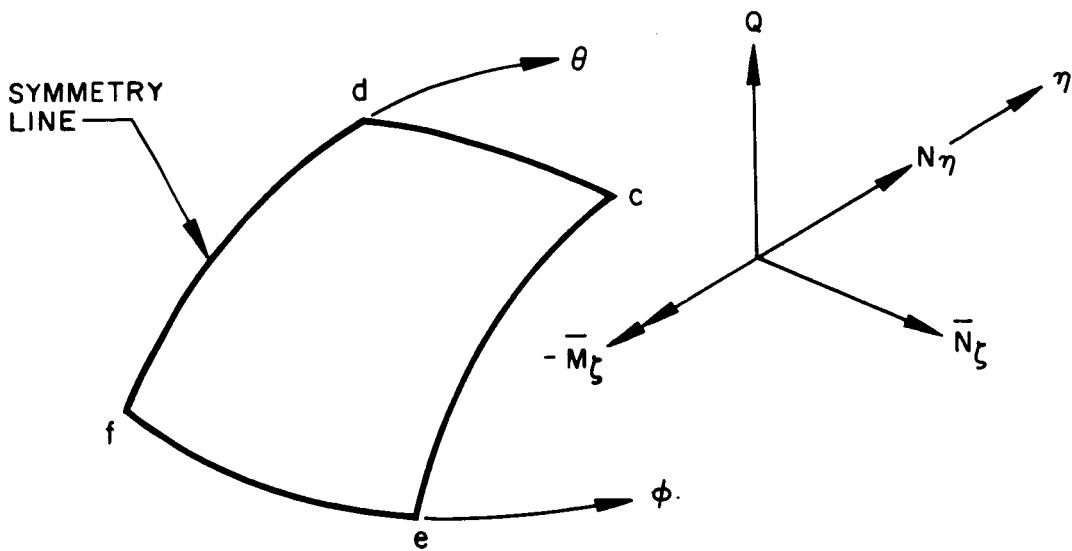


Fig. 8 Boundary Curve and Forces for Orientation 2

along  $\overline{ef}$

$$\bar{N}_\eta = -N_{\theta\phi} - 2\kappa M_{\phi\theta}$$

$$\bar{N}_\zeta = N_\theta$$

$$\bar{Q} = -[Q + (1 - \nu)M_{\phi\theta,\phi}]$$

$$\bar{M}_\zeta = M_\theta$$

along  $\overline{ce}$

The curve  $\overline{ce}$  is not parallel to a coordinate lines as was the case for line  $\overline{bc}$  for Orientation 1. Thus, the boundary forces are given by the general expressions:

$$\hat{\bar{N}}_\eta = \hat{N}_\eta + \frac{1}{R} \hat{M}_{\zeta\eta}$$

$$\hat{N}_\zeta = \hat{N}_\zeta$$

$$\hat{\bar{Q}} = \hat{Q}_3 + \frac{1}{A_\eta} \frac{\partial \hat{M}_{\zeta\eta}}{\partial \eta}$$

$$\hat{\bar{M}}_\zeta = \hat{M}_\zeta$$

The quantities  $\hat{N}_\eta$ ,  $\hat{N}_\zeta$ ,  $\hat{Q}_3$ ,  $\hat{M}_\zeta$ ,  $\hat{M}_{\zeta\eta}$  can be found by the equations given for Orientation 1, once  $\cos \lambda$  is known. For the curve  $\overline{ce}$ , the relation between  $\theta$  and  $\phi$  is

$$\cos \theta = - \frac{[\cos \phi + \tan \phi_1 (R_1/R - 1)]}{\sin \phi \tan \phi_1}$$

The direction cosine is given by

$\cos \lambda$

$$= \pm \frac{\left\{ \tan^2 \phi_1 \sin^2 \phi - [\cos \phi + \tan \phi_1 (R_1/R - 1)]^2 \right\}^{1/2}}{\left\{ [1 + \tan \phi_1 (R_1/R - 1) \cos \phi]^2 + \tan^2 \phi_1 \sin^2 \phi - [\cos \phi + \tan \phi_1 (R_1/R - 1)]^2 \right\}^{1/2}}$$

For the spherical segment,  $\overline{dc}\overline{ef}$ , the boundary conditions for a fixed edge are as follows:

$$\overline{dc} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \theta} \equiv 0$$

$$\overline{bc} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \zeta} \equiv 0$$

$$\overline{cd} \quad u \equiv v \equiv w \equiv \frac{\partial w}{\partial \theta} \equiv 0$$

### 2.3 STRESS IN SKIN

Once the stress resultant and couples are known, the corresponding maximum and minimum stress of an isotropic shell can be computed by the relations:

$$\sigma_\phi = \frac{1}{h} \hat{N}_\phi \pm \frac{6}{h^2} \hat{M}_\phi \quad (2.11a)$$

$$\sigma_\theta = \frac{1}{h} \hat{N}_\theta \pm \frac{6}{h^2} \hat{M}_\theta \quad (2.11b)$$

This development is based on the assumption of a linear stress variation through the thickness given by

$$\sigma_i = \bar{\sigma}_i + z\sigma_i^b$$

where  $\bar{\sigma}_i$  is a membrane stress and  $z\sigma_i^b$  is the stress due to bending.

Section 3  
NUMERICAL ANALYSIS

The finite-difference method is used to solve the governing equations of a spherical shell segment with fixed edges. The scheme in this numerical method is to replace the continuous problem of a continuous coordinate system by one defined at a finite number of coordinate points. To accomplish this discretization, the continuous two dimensional  $(\phi, \theta)$  domain of the spherical shell is covered by a uniform rectangular net as shown in Fig. 9. Lattice points of this net which are within the domain  $\tilde{D}$

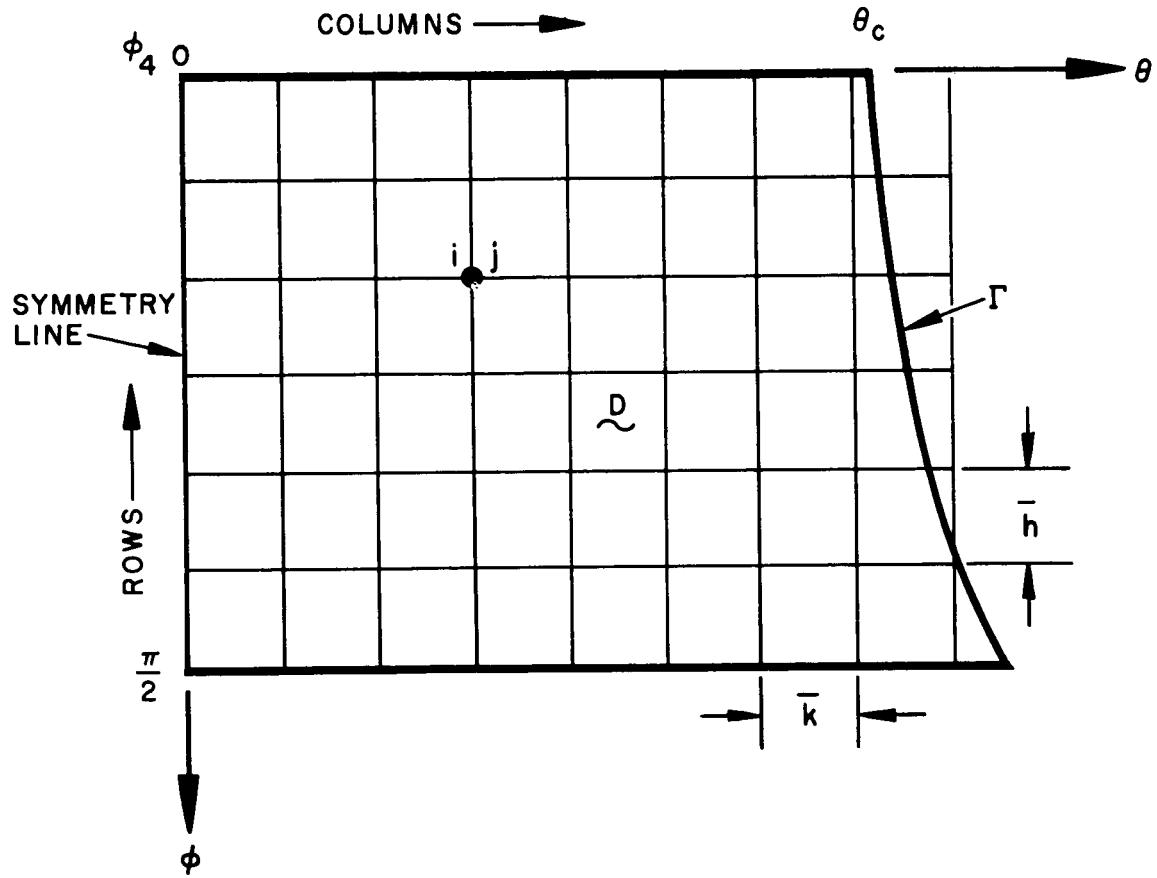


Fig. 9 Domain and Boundary of Spherical Shell Segment

are called mesh points, and lattice points on the boundary curve  $\Gamma$  are called boundary points. At these lattice points the dependent variables  $(u, v, w)$  of the governing differential equations are replaced by the discrete values of  $u_i^j, v_i^j, w_i^j$ . The subscript  $i$  of  $u_i^j$  denotes the row number and corresponds to the  $\phi$ -coordinate while the superscript  $j$  denotes the column number and corresponds to the  $\theta$ -coordinate. In general, the boundary curve does not coincide with the net as seen in Fig. 9. For the present numerical analysis, it is desirable to have the boundary curve coincide with the net so as to avoid computational complications. With the orthogonal coordinates  $\phi, \theta$ , it is not possible to have all the coordinate lines coincide exactly with the boundary. However, the coordinates can be orientated in such a manner that at least two boundary curves are parallel to coordinate lines. Two orientations are given in Sec. 2.2 which accomplish this objective. The domain shown in Fig. 9 corresponds to Orientation 1 which indicates the degree to which the actual boundary curve deviates from the rectangular net.

The difference equations which are a set of algebraic relations representing the governing equations and boundary conditions are formed by first approximating the derivatives at a given point by a function of the variable at neighboring points. These functions replace the derivatives of the governing equations. Thus, at each mesh point three algebraic equations can be written in terms of neighboring points. When the boundary conditions are accounted for in these equations the resulting set of simultaneous algebraic equations

$$\underset{\sim}{AX} = \underset{\sim}{B}$$

replaces the continuous problem. The solution of this set of algebraic equations can be accomplished by methods described in Vol. I.

### 3.1 APPROXIMATION OF DERIVATIVES

The derivatives of  $u, v, w$  are expressed in terms of their values at neighboring mesh points to transform the governing equations to difference form. These

derivatives are determined by a Taylor series approximation\* for a rectangular net and are given by the following equations:

$$f_{,\phi} = 1/2\bar{h}(f_1^o - f_{-1}^o) \quad (3.1a)$$

$$f_{,\phi\phi} = 1/\bar{h}^2(f_1^o - 2f_o^o + f_{-1}^o) \quad (3.1b)$$

$$f_{,\phi\phi\phi} = 1/2\bar{h}^3(f_2^o - 2f_1^o + 2f_{-1}^o - f_{-2}^o) \quad (3.1c)$$

$$f_{,\phi\phi\phi\phi} = 1/\bar{h}^4(f_2^o - 4f_1^o + 6f_o^o - 4f_{-1}^o + f_{-2}^o) \quad (3.1d)$$

$$f_{,\theta} = 1/2\bar{k}(f_o^1 - f_o^{-1}) \quad (3.1e)$$

$$f_{,\theta\theta} = 1/\bar{k}^2(f_o^1 - 2f_o^o + f_o^{-1}) \quad (3.1f)$$

$$f_{,\theta\theta\theta} = 1/2\bar{k}^3(f_o^2 - 2f_o^1 + 2f_o^{-1} - f_o^{-2}) \quad (3.1g)$$

$$f_{,\theta\theta\theta\theta} = 1/\bar{k}^4(f_o^2 - 4f_o^1 + 6f_o^o - 4f_o^{-1} + f_o^{-2}) \quad (3.1h)$$

$$f_{,\phi\theta} = 1/4\bar{h}\bar{k}(f_1^1 - f_{-1}^1 - f_1^{-1} + f_{-1}^{-1}) \quad (3.1i)$$

$$f_{,\phi\phi\theta} = 1/2\bar{h}^2\bar{k}(-2f_o^1 + 2f_o^{-1} + f_1^1 + f_{-1}^1 - f_1^{-1} - f_{-1}^{-1}) \quad (3.1j)$$

---

\*"Investigation of Juncture Stress Fields in Multicellular Shell Structures," by E. Y. W. Tsui, F. A. Brogan, J. M. Massard, P. Stern, and C. E. Stuhlman, Technical Report M-03-63-1, Lockheed Missiles & Space Company, Sunnyvale, Calif., Feb 1964 - NASA CR-61050.

$$f_{,\phi\theta\theta} = 1/2\bar{h}\bar{k}^{-2} \left( -2f_1^0 + 2f_{-1}^0 + f_1^1 + f_1^{-1} - f_{-1}^1 - f_{-1}^{-1} \right) \quad (3.1k)$$

$$f_{,\phi\phi\theta\theta} = 1/\bar{h}^2\bar{k}^{-2} \left( -2f_1^0 - 2f_{-1}^0 - 2f_0^1 - 2f_0^{-1} + f_1^1 + f_{-1}^1 + f_1^{-1} + f_{-1}^{-1} + 4f_0^0 \right) \quad (3.1l)$$

Lower order approximations to be used as noted

$$u_{,\phi\phi\phi} = 1/\bar{h}^3 \left( u_2^0 - 3u_1^0 + 3u_0^0 - u_{-1}^0 \right) \quad (3.1m)$$

$$u_{,\phi\phi\phi} = 1/\bar{h}^3 \left( u_1^0 - 3u_0^0 + 3u_{-1}^0 - u_{-2}^0 \right) \quad (3.1n)$$

$$v_{,\theta\theta\theta} = 1/\bar{k}^3 \left( v_0^1 - 3v_0^0 + 3v_0^{-1} - v_0^{-2} \right) \quad (3.1o)$$

### 3.2 DIFFERENCE EQUATIONS

The formation of the difference equations is effected in a straightforward manner by substituting the appropriate expressions of Eqs. (3.1) into the governing equation [Eqs. (2.7)]. Only when the equations are written one row or column from the boundary, the low-order third derivatives of  $u$  with respect to  $\phi$  [Eqs. (3.1m and n)] or the third derivative of  $v$  with respect to  $\theta$  [Eq. (3.1o)] are used to obtain a sufficient number of unknowns for the given number of equations. With these substitutions the three governing equations in difference form at a point  $0, 0$  are as follows:

$$\begin{aligned} A_1 u_1^0 + A_2 u_{-1}^0 + A_3 \left( u_0^1 + u_0^{-1} \right) + A_4 u_0^0 + A_5 \left( v_1^1 - v_1^{-1} - v_{-1}^1 + v_{-1}^{-1} \right) \\ + A_6 \left( v_0^1 - v_0^{-1} \right) + A_7 \left( w_2^0 - w_{-2}^0 \right) + A_8 w_1^0 + A_9 w_{-1}^0 + A_{10} \left( w_0^1 + w_0^{-1} \right) \\ + A_{11} \left( w_1^1 + w_1^{-1} - w_{-1}^1 - w_{-1}^{-1} \right) + A_{12} w_0^0 = A_0^0 \quad (3.2a) \end{aligned}$$

$$\begin{aligned}
& B_1(u_1^1 - u_{-1}^1 - u_1^{-1} + u_{-1}^{-1}) + B_2(u_o^1 - u_o^{-1}) + B_3 v_1^o + B_4 v_{-1}^o + B_5(v_o^1 + v_o^{-1}) \\
& + B_6 v_o^o + B_7(w_o^1 - w_o^{-1}) + B_8(w_1^1 - w_1^{-1}) + B_9(w_{-1}^1 - w_{-1}^{-1}) + B_{10}(w_o^2 - w_o^{-2}) = B_o^o
\end{aligned} \tag{3. 2b}$$

$$\begin{aligned}
& C_1(u_2^o - u_{-2}^o) + C_2 u_1^o + C_3 u_{-1}^o + C_4(-u_o^1 - u_o^{-1}) + C_5(u_1^1 - u_{-1}^1 + u_1^{-1} - u_{-1}^{-1}) \\
& + C_6 u_o^o + C_7(v_o^1 - v_o^{-1}) + C_8(v_1^1 - v_1^{-1}) + C_9(v_{-1}^1 - v_{-1}^{-1}) + C_{10}(v_o^2 - v_o^{-2}) \\
& + C_{11} w_2^o + C_{12} w_{-2}^o + C_{13}(w_o^2 + w_o^{-2}) + C_{14} w_1^o + C_{15} w_{-1}^o + C_{16}(w_o^1 + w_o^{-1}) \\
& + C_{17}(w_1^1 + w_1^{-1}) + C_{18}(w_{-1}^1 + w_{-1}^{-1}) + C_{19} w_o^o = C_o^o
\end{aligned} \tag{3. 2c}$$

where

$$A_1 = \frac{a_1}{\bar{h}^2} + \frac{a_3}{2\bar{h}}$$

$$A_2 = \frac{a_1}{\bar{h}^2} - \frac{a_3}{2\bar{h}}$$

$$A_3 = \frac{a_2}{\bar{k}^2}$$

$$A_4 = a_4 - (A_1 + A_2) - 2A_3$$

$$A_5 = \frac{a_5}{4\bar{h}\bar{k}}$$

$$A_6 = \frac{a_6}{2\bar{k}}$$

$$A_7 = \frac{a_7}{2\bar{h}^3}$$

$$A_8 = -2A_7 - 2A_{11} + \frac{a_9}{\bar{h}^2} + \frac{a_{11}}{2\bar{h}}$$

$$A_9 = 2A_7 + 2A_{11} + \frac{a_9}{\bar{h}^2} - \frac{a_{11}}{2\bar{h}}$$

$$A_{10} = \frac{a_{10}}{\bar{k}^2}$$

$$A_{11} = \frac{a_8}{2\bar{h}\bar{k}^2}$$

$$A_{12} = -\frac{2a_9}{\bar{h}^2} - 2A_{10}$$

$$A_o^o = A$$

$$B_1 = \frac{b_1}{4\bar{h}\bar{k}}$$

$$B_2 = \frac{b_2}{2\bar{k}}$$

$$B_3 = \frac{b_3}{\bar{h}^2} + \frac{b_5}{2\bar{h}}$$

$$B_4 = \frac{b_3}{\bar{h}^2} - \frac{b_5}{2\bar{h}}$$

$$B_5 = \frac{b_4}{\bar{k}^2}$$

$$B_6 = -(B_3 + B_4) - 2B_5 + b_6$$

$$B_7 = \left( -\frac{b_7}{2\bar{h}^2\bar{k}} + \frac{b_{10}}{2\bar{k}} - \frac{b_8}{\bar{k}^3} \right)$$

$$B_8 = \left( \frac{b_7}{2\bar{h}^2\bar{k}} + \frac{b_9}{4\bar{h}\bar{k}} \right)$$

$$B_9 = \left( \frac{b_7}{2\bar{h}^2\bar{k}} - \frac{b_9}{4\bar{h}\bar{k}} \right)$$

$$B_{10} = \frac{b_8}{2\bar{k}^3}$$

$$B_o^o = B$$

$$C_1 = \frac{c_1}{2\bar{h}^3}$$

$$C_2 = -2C_1 - 2C_5 + \frac{c_3}{\bar{h}^2} + \frac{c_5}{2\bar{h}}$$

$$C_3 = \frac{c_1}{\bar{h}^3} + \frac{c_2}{\bar{h}\bar{k}^2} + \frac{c_3}{\bar{h}^2} - \frac{c_5}{2\bar{h}}$$

$$C_4 = \frac{c_4}{\bar{k}^2}$$

$$C_5 = \frac{c_2}{2\bar{h}\bar{k}^2}$$

$$C_6 = -2 \frac{c_3}{\bar{h}^2} - 2 \frac{c_4}{\bar{k}^2} + c_6$$

$$C_7 = -\frac{c_7}{\bar{h}^2\bar{k}} - \frac{c_8}{\bar{k}^3} + \frac{c_{10}}{2\bar{k}}$$

$$C_8 = \frac{c_7}{2\bar{h}^2\bar{k}} + \frac{c_9}{4\bar{h}\bar{k}}$$

$$C_9 = \frac{c_7}{2\bar{h}^2\bar{k}} - \frac{c_9}{4\bar{h}\bar{k}}$$

$$C_{10} = \frac{c_8}{2\bar{k}^3}$$

$$C_{11} = \frac{c_{11}}{\bar{h}^4} + \frac{c_{14}}{2\bar{h}^3}$$

$$C_{12} = \frac{c_{11}}{\bar{h}^4} - \frac{c_{14}}{2\bar{h}^3}$$

$$C_{13} = \frac{c_{13}}{\bar{k}^4}$$

$$C_{14} = -4 \frac{c_{11}}{\bar{h}^4} - 2 \frac{c_{12}}{\bar{h}^2 \bar{k}^2} - \frac{c_{14}}{\bar{h}^3} - \frac{c_{15}}{\bar{h} \bar{k}^2} + \frac{c_{16}}{\bar{h}^2} + \frac{c_{18}}{2\bar{h}}$$

$$C_{15} = -4 \frac{c_{11}}{\bar{h}^4} - 2 \frac{c_{12}}{\bar{h}^2 \bar{k}^2} + \frac{c_{14}}{\bar{h}^3} + \frac{c_{15}}{\bar{h} \bar{k}^2} + \frac{c_{16}}{\bar{h}^2} - \frac{c_{18}}{2\bar{h}}$$

$$C_{16} = -2 \frac{c_{12}}{\bar{h}^2 \bar{k}^2} - 4 \frac{c_{13}}{\bar{k}^4} + \frac{c_{17}}{\bar{k}^2}$$

$$C_{17} = \frac{c_{12}}{\bar{h}^2 \bar{k}^2} + \frac{c_{15}}{2\bar{h} \bar{k}^2}$$

$$C_{18} = \frac{c_{12}}{\bar{h}^2 \bar{k}^2} - \frac{c_{15}}{2\bar{h} \bar{k}^2}$$

$$C_{19} = 6 \frac{c_{11}}{\bar{h}^4} + 4 \frac{c_{12}}{\bar{h}^2 \bar{k}^2} + 6 \frac{c_{13}}{\bar{k}^4} - 2 \frac{c_{16}}{\bar{h}^2} - 2 \frac{c_{17}}{\bar{k}^2} + c_{19}$$

$$C_o^o = C$$

The complete set of difference equations are obtained by writing these equations at each mesh point. Along lines of symmetry only two equations are necessary since one of the variables will be zero. After incorporation of fixed-edge boundary

conditions, a sufficient number of equations for unknowns yields a set of simultaneous algebraic equations which are written in matrix form as

$$\underset{\sim}{AX} = \underset{\sim}{B}$$

Unless care is exercised in ordering the equations and unknowns, the square matrix  $\underset{\sim}{A}$  can be full. From the aspect of solving a large number of equations (Vol. I), the ordering is important. To establish an insight into the idea of the ordering employed, it is noticed from the difference expressions [Eqs. (3.1)] that the highest derivatives are in terms of at most two rows "above;" two rows "below;" two columns to the "left," and two columns to the "right" of a given mesh point. If all the equations for a given column were written and stored in submatrix form, the unknowns would involve two columns to the "right" and "left." Thus, any column would involve, at most, five submatrices. The matrix  $\underset{\sim}{A}$  is accordingly partitioned in the manner shown below, where  $m$  is the number of columns in the finite-difference net.

$$\underset{\sim}{A} = \begin{bmatrix} E_1 F_1 G_1 \dots & 0 \\ D_2 E_2 F_2 G_2 \\ C_3 D_3 E_3 F_3 G_3 0 \\ \vdots & G_{n-2} \\ & F_{m-1} \\ C_m D_m E_m \end{bmatrix}$$

This matrix  $\underset{\sim}{A}$  is obtained by writing Eqs. (3.1) in  $\underset{\sim}{D}$  and not on the boundary  $\Gamma$ . The boundary and symmetry conditions have been used to eliminate certain equations. Fixed-edge boundary conditions are well-suited for this formulation, since they do not require complex algebraic expressions. Specifically, if Eqs. (3.1) are written one column from the boundary, then the submatrix  $F_m$  is zero ( $u = v = w = 0$ )

and the submatrix  $G_m$  contains only  $w$  terms which are reflected into  $E_m$  due to the boundary condition. Along a symmetry line, all terms are either reflected with the same or opposite sign. This fact accounts for the missing  $C_1$  and  $D_1$  matrices. Similar alterations are made in each matrix to account for boundary and symmetry conditions.

Because of the boundary behavior of shells it is desirable to incorporate a means of decreasing the mesh spacing in order to reveal the boundary solution with greater detail and accuracy. A rather simple method called grading which does not destroy the form of matrix  $\underline{A}$  is incorporated in the numerical solution. An explanation of grading was given in Vol. II, Sec. 3.3.

## Section 4

### DIGITAL PROGRAM

#### 4. 1 GENERAL DESCRIPTION

The present program provides solutions for fixed-edge spherical shell segments under loads and changes of temperature. The method of solution consists basically in obtaining the displacement components  $u$ ,  $v$ , and  $w$  at various discrete stations of the structure by finite-difference approximation (see Secs. 2 and 3). The corresponding strains and stresses may then be computed.

The program is designed to compute the fixed-edge forces due to intermediate loads or thermal gradient. However, displacements, strains, and stresses in the loaded region are also evaluated simultaneously. The following program options are available:

- Finite-difference mesh
  - (a) Uniform spacing
  - (b) Graded spacing in the  $\phi$ -direction
  - (c) Symmetry in the  $\phi$ -direction
- Loading conditions
  - (a) Uniform normal pressure
  - (b) Linear temperature gradient through the skin thickness

There are no restrictions on the geometrical dimensions of panels. However, the accuracy with which the basic differential equations are approximated may vary for different configurations of the shell.

The finite-difference mesh network is specified completely by prescribing the number of rows and columns exclusive of the boundaries, together with the grading options which have been chosen. Rows in the finite-difference mesh are parallel to the

$\theta$ -direction, and columns are parallel to the  $\phi$ -direction. The number of rows may vary from 4 to 24 and the number of columns from 4 to 80. Thus, a maximum of 5760 unknowns can be solved. Greater accuracy near the boundaries can often be obtained by selective grading. By this means, it is possible to use a mesh spacing at the boundary as little as 1/32 of that at the middle portion of the panel.

There are certain restrictions on the use of the grading option. When such an option is used, a separate input card is required to specify a mesh spacing exponent MM(J) for each row J. The finite-difference equations are written along Row J, then the mesh spacing  $XH/2^{**MM(J)}$  is used. This distance must be the least of the two distances from Row J to the row above and the row below. XH is the basic input mesh spacing along the  $\phi$ -direction. For any Row J, MM(J) and MM(J + 1) must not differ by more than 1. Also, three consecutive rows cannot have three distinct exponents. MM(J) may vary from 0 to 5.

The description of symbols and input data are shown in Tables 1 and 2; Fig. 10 shows the flow diagram of this program.

Table 1  
DESCRIPTION OF SYMBOLS

Symbol		Description
RECORD		Hollerith information describing problem
I $\phi$ PT1	0	Uniform mesh spacing
	1	Graded mesh spacing in $\phi$ -direction
I $\phi$ PT2	0	Symmetry in the $\phi$ -direction
	1	Row 1 is symmetry line
	2	Row 2 is adjacent to boundary
I $\phi$ PT3	0	Omit shell strains
	1	Print shell strains
I $\phi$ PT4	0	Uniform normal pressure
	1	Linear temperature gradient through the skin thickness

Table 1 (cont'd)

Symbol		Description
$I_\phi PT5$	0	Not last case with plots
	1	Last case with plots
$R_\phi W$		Number of rows in the finite-difference mesh
$C_\phi L$		Number of columns in the finite-difference mesh
$XH$		Basic distance between rows in the mesh
$XX$		Basic distance between columns in the mesh
$ZNU$		Poisson's ratio
$THC$		Half angle of segment $\theta_c$
$PH1$		Angle $\phi$ of upper boundary
$FF$		Ratio of angle of $\phi$ of lower boundary to $\phi$ of upper boundary
$RH$		Radius to thickness ratio, $R/h$
$TE$		External temperature
$TI$		Internal temperature
$T\phi$		Ambient temperature for zero stress
$\phi C$		Coefficient of thermal expansion
$MM(J)$ , $J = 1, R_\phi W$		Grading mesh constants, mesh spacing used for difference equations on Row J is equal to $XH/2.**MM(J)$
$MM(31)$		Number of rows to be plotted
$MM(32)$		Four row numbers for which plot output is desired
$MM(33)$		$(u, v, w, N_\phi, M_\phi, N_\theta, M_\theta)$
$MM(34)$		
$MM(35)$		
$CILBL(I, 1)$ , $I = 1, 6$		Curve labels appearing on the plot output to identify the rows selected $CILBL(I, 1)$ corresponds to $MM(32)$ ; etc.
$CILBL(I, 2)$ , $I = 1, 6$		
$CILBL(I, 3)$ , $I = 1, 6$		
$CILBL(I, 4)$ , $I = 1, 6$		

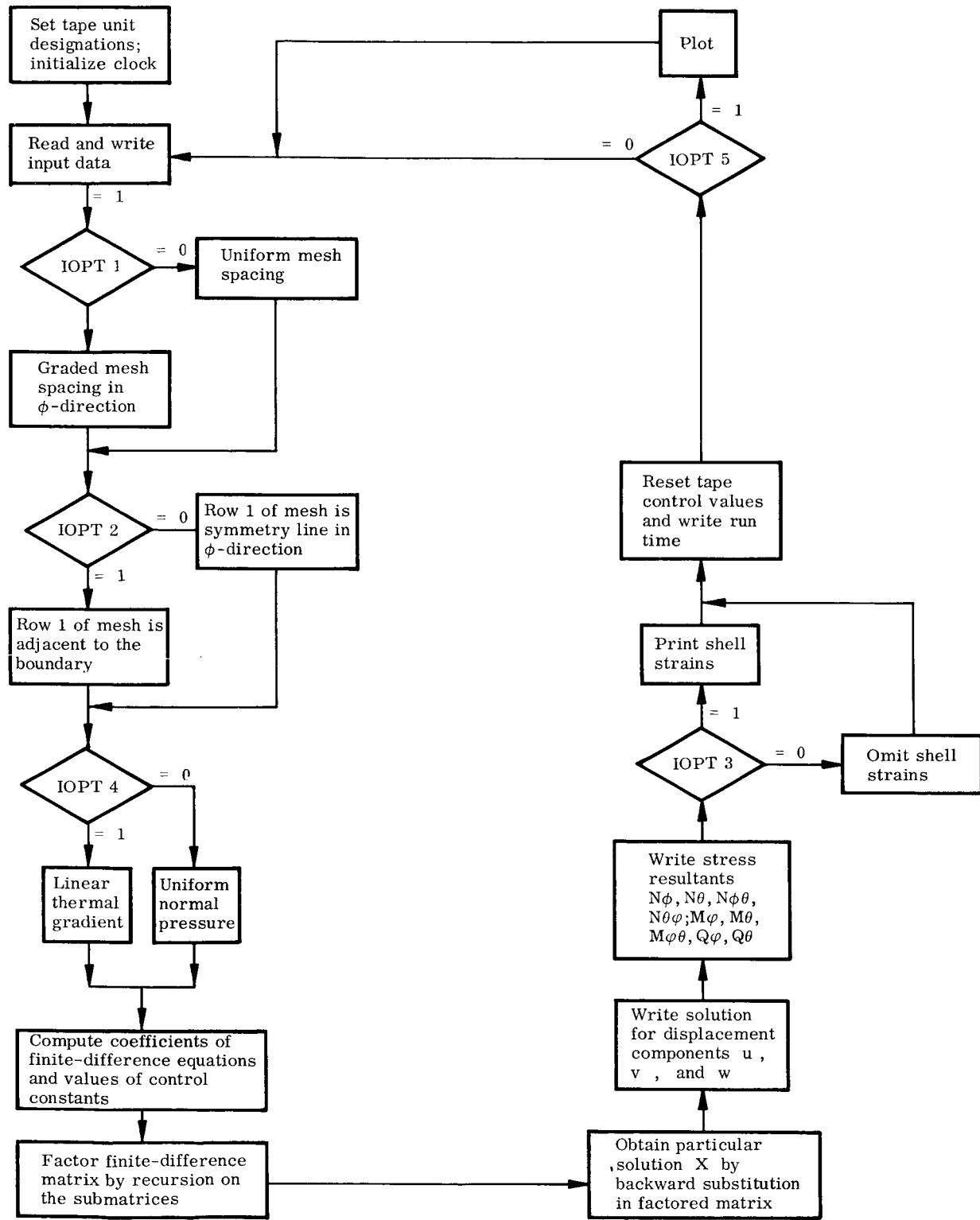


Fig. 10 Flow Chart

Table 2  
INPUT DATA SEQUENCE AND FORMAT

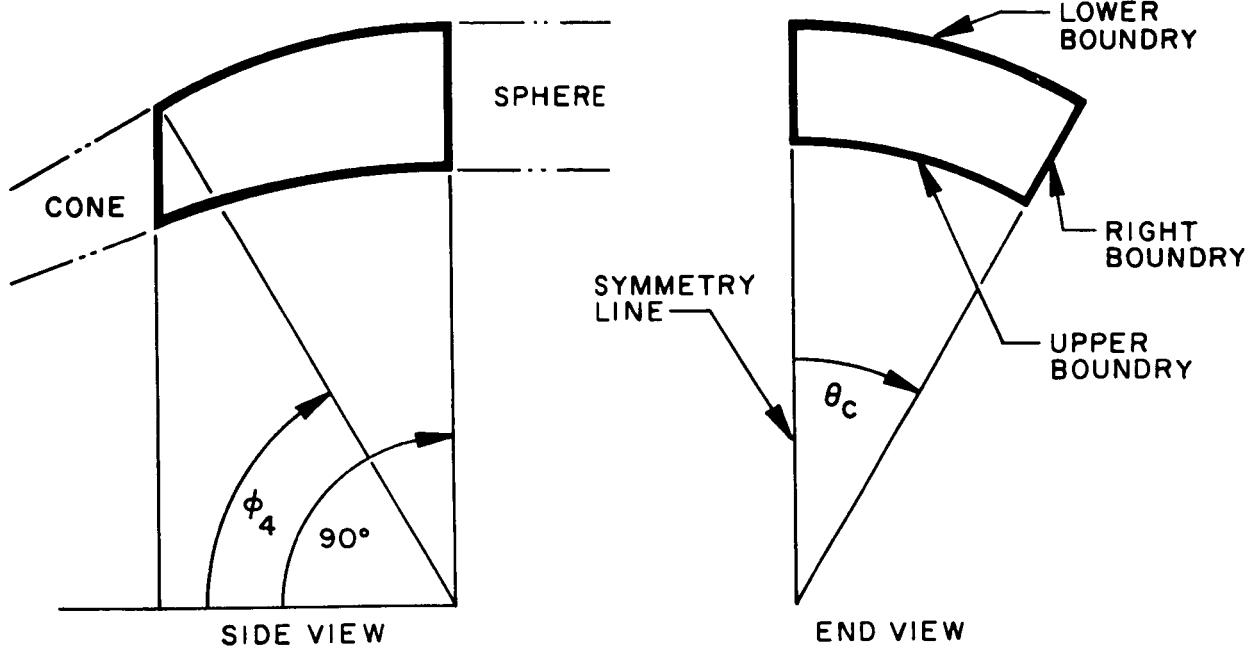
Card	FORTRAN Symbol	Format
1	RECORD	72H
2	I <sub>φ</sub> PT1, I <sub>φ</sub> PT2, I <sub>φ</sub> PT3, I <sub>φ</sub> PT4, I <sub>φ</sub> PT5	10I1
3	R <sub>φ</sub> W, C <sub>φ</sub> L, XH, XK	3E12. 8
4	ZNU, THC, PH1, FF, RH	6E12. 8
5 <sup>(a)</sup>	MM(J), J = 1, R <sub>φ</sub> W	35I2
6 <sup>(b)</sup>	TE, TI, T <sub>φ</sub> , φC	4E12. 8
7	MM(J), J = 31, 35	5I2
8 <sup>(c)</sup>	CILBL(I, 1), I = 1, 6	6A6
9 <sup>(c)</sup>	CILBL(I, 2), I = 1, 6	6A6
10 <sup>(c)</sup>	CILBL(I, 3), I = 1, 6	6A6
11 <sup>(c)</sup>	CILBL(I, 4), I = 1, 6	6A6

- (a) Omitted unless I<sub>φ</sub>PT1 = 1.
- (b) Omitted unless I<sub>φ</sub>PT4 = 1.
- (c) Omitted if MM(31) = 0.

#### 4.2 NUMERICAL EXAMPLE

Analysis of the spherical shell segment shown in Fig. 11 will serve as an example to illustrate input data, format, and the type of information that can be obtained through use of the program described in this volume.

The example is for the loading option of uniform normal pressure ( $p_z = \text{constant}$ ). Grading is used in the  $\phi$ -coordinate so as to obtain a reasonable solution with the present restrictions of the computer program (24 rows, 80 columns). The actual



$$\theta_c = \text{THC} = 0.61 \text{ RADIUS}$$

$$\phi_4 = \text{PHI} = 1.0297 \text{ RADIUS}$$

$$FF = \frac{\pi}{2} / 1.0297 = 1.5708$$

$$\frac{R}{h} = RH = 100$$

Fig. 11 Segmented Spherical Shell

mesh spacing which yields a solution of desired accuracy must be obtained by exploratory runs using different number of rows and columns. Such runs were made with the given geometry. It was found that 17 rows and 30 columns were required to obtain satisfactory results in both displacements and stress resultants. More accurate results can be obtained by use of an even finer mesh spacing.

Values of input quantities for the 17 by 30 case are given in Table 3 and a listing of the corresponding input data cards is presented in Table 4. For convenience, the  $\phi$ -coordinate corresponding to the row number follows:

Table 3  
INPUT VALUES FOR THE EXAMPLE

Symbol	Value	Symbol	Value
I <sub>φ</sub> PT1	1. 0	MM(8)	0
I <sub>φ</sub> PT2	1. 0	MM(9)	0
I <sub>φ</sub> PT3	0	MM(10)	0
I <sub>φ</sub> PT4	0	MM(11)	1. 0
I <sub>φ</sub> PT5	1. 0	MM(12)	1. 0
R <sub>φ</sub> W	17. 0	MM(13)	2. 0
C <sub>φ</sub> L	30. 0	MM(14)	2. 0
XH	0. 067635	MM(15)	2. 0
XK	0. 02033	MM(16)	3. 0
ZNU	0. 3	MM(17)	3. 0
THC	0. 61	TE , TI , T <sub>φ</sub> , φC	Not required
PH1	1. 0297	MM(31)	4. 0
FF	1. 5255	MM(32)	5. 0
RH	100. 0	MM(33)	9. 0
MM(1)	3. 0	MM(34)	16. 0
MM(2)	3. 0	MM(35)	17. 0
MM(3)	2. 0	CILBL(I, 1)I = 1, 6	PHI = 1. 503, Row 5
MM(4)	2. 0	CILBL(I, 2)I = 1, 6	PHI = 1. 300, Row 9
MM(5)	2. 0	CILBL(I, 3)I = 1, 6	PHI = 1. 038, Row 16
MM(6)	1. 0	CILBL(I, 4)I = 1, 6	PHI = 1. 029, Row 17
MM(7)	1. 0		

Table 4  
INPUT DATA IN REQUIRED FORMAT

MODULE	ORG.	BLOC.	FAC.	JOB NUMBER	DATE OF REQUEST	DISPATCH NUMBER	PROGRAM	OPR. CONTROL NO.	DATA RECORD	PRIORITY	LOCKHEED MISSILES & SPACE COMPANY
											80 COLUMN WORKSHEET
<b>EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE</b>											
<b>CARD 1</b>											
1 1 0 0 1											
1 7	+ 2	3 0			+ 2	0 6 7 6 3 5	+ 0	0 2 0 3 3	+ 0		
3	+ 0	6 1			+ 0	1 0 2 9 7	+ 1	1 6 2 5 5	+ 1	1	
0 3 0 3 0 2	0 2 0 2 0 1	0 1 0 0 0 0 0	0 1 0 2 0 2 0 2 0 3 0 3								
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$\phi = 1.0297$	- Row 18	$\phi = 1.3679$	- Row 8
$\phi = 1.0381$	- Row 17	$\phi = 1.4355$	- Row 7
$\phi = 1.0466$	- Row 16	$\phi = 1.4693$	- Row 6
$\phi = 1.0635$	- Row 15	$\phi = 1.5031$	- Row 5
$\phi = 1.0804$	- Row 14	$\phi = 1.5200$	- Row 4
$\phi = 1.0973$	- Row 13	$\phi = 1.5369$	- Row 3
$\phi = 1.1311$	- Row 12	$\phi = 1.5539$	- Row 2
$\phi = 1.1650$	- Row 11	$\phi = 1.5623$	- Row 1
$\phi = 1.2326$	- Row 10	$\phi = 1.5703$	- Row 0
$\phi = 1.3002$	- Row 9		

Results from the computer program are in the form of printed digital values and selected plots. Sample printed output given in Table 5 presents displacement components ( $u, v, w$ ), stress resultants ( $N_\phi, N_\theta, N_{\theta\phi}, N_{\phi\theta}, M_\phi, M_\theta, M_{\phi\theta}, Q_\phi, Q_\theta$ ), and boundary stress resultants ( $N_{tan}, N_{norm}, Q, M$ ). (Note that these quantities are in nondimensional form as defined in Sec. 2.) Plotted output includes displacement components ( $u, v, w$ ) and stress resultants ( $N_\phi, N_\theta, M_\phi, M_\theta$ ) along Rows 1, 2, 10, and 16 and boundary stress resultants ( $N_{tan}, N_{norm}, Q, M$ ) along the boundary curve. This plotted output is shown in Figs. 12a through o.

Table 5

## EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

## SPHERE DISPLACEMENT COMPONENTS (U,V,W)

COL	ROW		U	V	W
19, 20			0.	0.	3.658652E-02
19, 19			-2.638945E-03	1.021954E-03	7.759879E-03
19, 18	BCUNDARY		0.	0.	0.
19, 17			2.602412E-03	-9.899542E-04	7.759879E-03
19, 16			5.086261E-03	-1.945970E-03	2.549251E-02
19, 15			9.652772E-03	-3.786246E-03	7.057005E-02
19, 14			1.323534E-02	-5.476061E-03	1.238788E-01
19, 13			1.572938E-02	-7.016443E-03	1.787364E-01
19, 12			1.853742E-02	-9.803262E-03	2.864289E-01
19, 11			1.769688E-02	-1.200326E-02	3.637405E-01
19, 10			1.115614E-02	-1.531577E-02	4.653016E-01
19, 9			-1.421190E-04	-1.615930E-02	4.937291E-01
19, 8			-1.144092E-02	-1.475764E-02	4.663140E-01
19, 7			-1.792110E-02	-1.120068E-02	3.641097E-01
19, 6			-1.868753E-02	-8.990277E-03	2.861686E-01
19, 5			-1.578401E-02	-6.338675E-03	1.780603E-01
19, 4			-1.324659E-02	-4.903025E-03	1.231290E-01
19, 3			-9.636059E-03	-3.359861E-03	6.997208E-02
19, 2			-5.067179E-03	-1.713557E-03	2.523418E-02
19, 1			-2.589518E-03	-8.672638E-04	7.664569E-03
19, -0	BCUNDARY		0.	0.	0.
19, -1			2.620010E-03	8.860647E-04	7.664569E-03
19, -2			0.	0.	3.608237E-02

## SPHERE STRESS RESULTANTS,

ROW	COL	NX	NTHETA	NXTTHETA	NTHETAX
7, 30	1.0666E-01	3.1256E-01	1.8012E-01	1.8012E-01	
7, 31	9.4004E-02	3.1335E-01	1.9175E-01	1.9175E-01	
8, 1	4.1548E-01	4.9208E-01	0.	0.	
8, 2	4.1553E-01	4.9204E-01	1.0850E-03	1.0850E-03	
8, 3	4.1566E-01	4.9192E-01	2.1802E-03	2.1802E-03	
8, 4	4.1588E-01	4.9173E-01	3.2953E-03	3.2953E-03	
8, 5	4.1619E-01	4.9145E-01	4.4417E-03	4.4417E-03	
8, 6	4.1662E-01	4.9108E-01	5.6343E-03	5.6343E-03	
8, 7	4.1721E-01	4.9062E-01	6.8937E-03	6.8937E-03	
8, 8	4.1799E-01	4.9007E-01	8.2481E-03	8.2481E-03	
8, 9	4.1901E-01	4.8942E-01	9.7361E-03	9.7361E-03	
8, 10	4.2033E-01	4.8865E-01	1.1409E-02	1.1409E-02	
8, 11	4.2202E-01	4.8777E-01	1.3331E-02	1.3331E-02	
8, 12	4.2413E-01	4.8674E-01	1.5584E-02	1.5584E-02	
8, 13	4.2670E-01	4.8555E-01	1.8265E-02	1.8265E-02	
8, 14	4.2975E-01	4.8417E-01	2.1481E-02	2.1481E-02	

Table 5 (cont'd)

8, 15	4.3322E-01	4.8256E-01	2.5349E-02	2.5349E-02
8, 16	4.3699E-01	4.8068E-01	2.9978E-02	2.9978E-02
8, 17	4.4079E-01	4.7845E-01	3.5459E-02	3.5459E-02
8, 18	4.4419E-01	4.7582E-01	4.1842E-02	4.1842E-02
8, 19	4.4655E-01	4.7268E-01	4.9109E-02	4.9109E-02
8, 20	4.4694E-01	4.6895E-01	5.7146E-02	5.7146E-02
8, 21	4.4417E-01	4.6452E-01	6.5720E-02	6.5720E-02
8, 22	4.3677E-01	4.5927E-01	7.4460E-02	7.4460E-02
8, 23	4.2304E-01	4.5309E-01	8.2873E-02	8.2873E-02
8, 24	4.0125E-01	4.4589E-01	9.0384E-02	9.0384E-02
8, 25	3.6991E-01	4.3757E-01	9.6441E-02	9.6441E-02
8, 26	3.2827E-01	4.2804E-01	1.0068E-01	1.0068E-01
8, 27	2.7705E-01	4.1721E-01	1.0312E-01	1.0312E-01
8, 28	2.1947E-01	4.0492E-01	1.0444E-01	1.0444E-01
8, 29	1.6251E-01	3.9095E-01	1.0609E-01	1.0609E-01
8, 30	1.1856E-01	3.7494E-01	1.1031E-01	1.1031E-01
8, 31	1.1186E-01	3.7287E-01	1.1898E-01	1.1898E-01
9, 1	4.0953E-01	5.1282E-01	0.	0.
9, 2	4.0958E-01	5.1279E-01	3.6104E-04	3.6104E-04
9, 3	4.0973E-01	5.1267E-01	7.2488E-04	7.2488E-04
9, 4	4.0998E-01	5.1246E-01	1.0946E-03	1.0946E-03
9, 5	4.1034E-01	5.1217E-01	1.4736E-03	1.4736E-03
9, 6	4.1084E-01	5.1179E-01	1.8661E-03	1.8661E-03
9, 7	4.1152E-01	5.1131E-01	2.2768E-03	2.2768E-03
9, 8	4.1242E-01	5.1073E-01	2.7111E-03	2.7111E-03

## SPHERE STRESS RESULTANTS.

ROW	COL	MX	MTHETA	MXTHETA	QX	QTHETA
7, 30	-1.8034E 01	-6.6409E 01	-6.3016E 00	3.9493E 01	-3.2650E 03	
7, 31	-4.3271E 01	-1.4424E 02	-1.9175E-01	1.1332E 02	-3.7978E 03	
8, 1	1.4440E 01	4.1252E 00	0.	4.8136E 01	2.0322E-05	
8, 2	1.4450E 01	4.1492E 00	2.8456E-02	4.8305E 01	6.7031E-01	
8, 3	1.4456E 01	4.1439E 00	5.7105E-02	4.8467E 01	-5.3604E-01	
8, 4	1.4459E 01	4.1103E 00	8.8090E-02	4.8636E 01	-1.6947E 00	
8, 5	1.4460E 01	4.0489E 00	1.2348E-01	4.8820E 01	-2.7939E 00	
8, 6	1.4460E 01	3.9603E 00	1.6520E-01	4.9025E 01	-3.7863E 00	
8, 7	1.4460E 01	3.8464E 00	2.1487E-01	4.9254E 01	-4.5651E 00	
8, 8	1.4464E 01	3.7113E 00	2.7354E-01	4.9504E 01	-4.9409E 00	
8, 9	1.4477E 01	3.5639E 00	3.4131E-01	4.9767E 01	-4.6206E 00	
8, 10	1.4507E 01	3.4198E 00	4.1674E-01	5.0022E 01	-3.1864E 00	
8, 11	1.4563E 01	3.3043E 00	4.9617E-01	5.0236E 01	-7.5807E-02	
8, 12	1.4661E 01	3.2559E 00	5.7280E-01	5.0357E 01	5.4176E 00	
8, 13	1.4817E 01	3.3298E 00	6.3573E-01	5.0313E 01	1.4113E 01	
8, 14	1.5055E 01	3.5998E 00	6.6901E-01	5.0000E 01	2.6885E 01	
8, 15	1.5399E 01	4.1605E 00	6.5092E-01	4.9288E 01	4.4558E 01	
8, 16	1.5875E 01	5.1257E 00	5.5373E-01	4.8016E 01	6.7715E 01	
8, 17	1.6506E 01	6.6226E 00	3.4453E-01	4.5998E 01	9.6405E 01	

Table 5 (cont'd)

8, 18	1.7305E 01	8.7797E 00	-1.2557E-02	4.3033E 01	1.2975E 02
8, 19	1.8270E 01	1.1705E 01	-5.5192E-01	3.8932E 01	1.6538E 02
8, 20	1.9365E 01	1.5449E 01	-1.2993E 00	3.3554E 01	1.9877E 02
8, 21	2.0513E 01	1.9955E 01	-2.2616E 00	2.6866E 01	2.2244E 02
8, 22	2.1569E 01	2.4989E 01	-3.4135E 00	1.9017E 01	2.2506E 02
8, 23	2.2308E 01	3.0042E 01	-4.6830E 00	1.0435E 01	1.9068E 02
8, 24	2.2397E 01	3.4225E 01	-5.9383E 00	1.9232E 00	9.8242E 01
8, 25	2.1385E 01	3.6142E 01	-6.9821E 00	-5.2742E 00	-7.8293E 01
8, 26	1.8690E 01	3.3776E 01	-7.5634E 00	-9.4875E 00	-3.6866E 02
8, 27	1.3609E 01	2.4408E 01	-7.4186E 00	-8.8120E 00	-8.0323E 02
8, 28	5.3436E 00	4.6353E 00	-6.3573E 00	-1.5812E 00	-1.4073E 03
8, 29	-6.9531E 00	-2.9455E 01	-4.4022E 00	1.2757E 01	-2.1924E 03
8, 30	-2.4093E 01	-8.1850E 01	-1.9791E 00	3.2301E 01	-3.1434E 03
8, 31	-4.6744E 01	-1.5581E 02	-1.1898E-01	5.0972E 01	-3.6314E 03
9, 1	1.0706E 01	2.7788E 00	0.	4.7328E 00	2.0558E-05
9, 2	1.0717E 01	2.8047E 00	5.5560E-03	5.0009E 00	7.0565E-01
9, 3	1.0724E 01	2.7964E 00	1.1408E-02	5.2746E 00	-6.7898E-01
9, 4	1.0729E 01	2.7549E 00	1.8096E-02	5.5704E 00	-1.9872E 00
9, 5	1.0732E 01	2.6814E 00	2.6100E-02	5.9019E 00	-3.1939E 00
9, 6	1.0734E 01	2.5774E 00	3.5800E-02	6.2796E 00	-4.2344E 00
9, 7	1.0739E 01	2.4462E 00	4.7404E-02	6.7091E 00	-4.9696E 00
9, 8	1.0750E 01	2.2943E 00	6.0844E-02	7.1881E 00	-5.1727E 00

## BOUNDARY STRESS RESULTANTS.

ROW	COL	NTAN	NNORM	Q	M
18,	1	0.	3.1654E-01	-8.3278E 03	-1.9934E 02
18,	2	-2.8194E-03	3.1655E-01	-8.3267E 03	-1.9937E 02
18,	3	-5.6834E-03	3.1656E-01	-8.3274E 03	-1.9944E 02
18,	4	-8.6365E-03	3.1658E-01	-8.3296E 03	-1.9956E 02
18,	5	-1.1726E-02	3.1661E-01	-8.3332E 03	-1.9972E 02
18,	6	-1.5005E-02	3.1666E-01	-8.3385E 03	-1.9995E 02
18,	7	-1.8534E-02	3.1671E-01	-8.3457E 03	-2.0025E 02
18,	8	-2.2385E-02	3.1677E-01	-8.3555E 03	-2.0065E 02
18,	9	-2.6642E-02	3.1684E-01	-8.3686E 03	-2.0116E 02
18,	10	-3.1405E-02	3.1691E-01	-8.3861E 03	-2.0183E 02
18,	11	-3.6790E-02	3.1697E-01	-8.4092E 03	-2.0268E 02
18,	12	-4.2930E-02	3.1699E-01	-8.4394E 03	-2.0374E 02
18,	13	-4.9972E-02	3.1694E-01	-8.4785E 03	-2.0504E 02
18,	14	-5.8073E-02	3.1676E-01	-8.5283E 03	-2.0660E 02
18,	15	-6.7390E-02	3.1638E-01	-8.5906E 03	-2.0843E 02
18,	16	-7.8067E-02	3.1568E-01	-8.6666E 03	-2.1049E 02
18,	17	-9.0212E-02	3.1452E-01	-8.7569E 03	-2.1269E 02
18,	18	-1.0387E-01	3.1269E-01	-8.8602E 03	-2.1489E 02

Table 5 (cont'd)

18, 19	-1.1899E-01	3.0998E-01	-8.9730E 03	-2.1682E 02
18, 20	-1.3537E-01	3.0607E-01	-9.0883E 03	-2.1812E 02
18, 21	-1.5260E-01	3.0064E-01	-9.1941E 03	-2.1823E 02
18, 22	-1.7003E-01	2.9327E-01	-9.2718E 03	-2.1646E 02
18, 23	-1.8669E-01	2.8354E-01	-9.2945E 03	-2.1188E 02
18, 24	-2.0125E-01	2.7100E-01	-9.2247E 03	-2.0338E 02
18, 25	-2.1202E-01	2.5518E-01	-9.0124E 03	-1.8972E 02
18, 26	-2.1695E-01	2.3562E-01	-8.5922E 03	-1.6964E 02
18, 27	-2.1369E-01	2.1185E-01	-7.8802E 03	-1.4214E 02
18, 28	-1.9971E-01	1.8329E-01	-6.7676E 03	-1.0698E 02
18, 29	-1.7204E-01	1.4896E-01	-5.1084E 03	-6.5787E 01
18, 30	-1.2332E-01	1.0458E-01	-2.7357E 03	-2.4507E 01
18, 31	0.	0.	-3.7534E 00	-0.
18,	31			
18, 31	-0.	0.	-0.	0.
17, 31	6.2429E-02	6.6763E-02	-1.8459E 02	-5.6682E 00
16, 31	1.0333E-01	1.0408E-01	-5.8460E 02	-1.7943E 01
15, 31	1.5904E-01	1.5705E-01	-1.5130E 03	-4.7199E 01
14, 31	1.8736E-01	1.9392E-01	-2.2564E 03	-7.4360E 01
13, 31	2.0035E-01	2.2494E-01	-2.7428E 03	-9.5980E 01
12, 31	2.0334E-01	2.8463E-01	-3.4037E 03	-1.3038E 02
11, 31	1.7540E-01	3.2177E-01	-3.5660E 03	-1.4594E 02
10, 31	9.3693E-02	3.7727E-01	-3.4916E 03	-1.5588E 02
9, 31	-1.3941E-02	3.8796E-01	-3.4799E 03	-1.5683E 02
8, 31	-1.1898E-01	3.7287E-01	-3.6314E 03	-1.5581E 02
7, 31	-1.9174E-01	3.1335E-01	-3.7978E 03	-1.4424E 02
6, 31	-2.1314E-01	2.7501E-01	-3.6301E 03	-1.2743E 02
5, 31	-2.0256E-01	2.1514E-01	-2.8917E 03	-9.1868E 01
4, 31	-1.8584E-01	1.8463E-01	-2.3600E 03	-7.0433E 01
3, 31	-1.5398E-01	1.4857E-01	-1.5637E 03	-4.4102E 01
2, 31	-9.6554E-02	9.7046E-02	-5.9817E 02	-1.6483E 01
1, 31	-5.6772E-02	6.1051E-02	-1.9192E 02	-5.1964E 00
0, 31	0.	0.	0.	0.
0,	31			
0, 31	-0.	-0.	-3.3510E 00	-0.
0, 30	1.2570E-01	1.0769E-01	-2.1392E 02	-3.0291E 01
0, 29	1.7161E-01	1.5369E-01	-2.1461E 03	-7.5918E 01
0, 28	1.9603E-01	1.8906E-01	-4.1497E 03	-1.1849E 02
0, 27	2.0635E-01	2.1778E-01	-5.8101E 03	-1.5281E 02
0, 26	2.0607E-01	2.4103E-01	-7.0648E 03	-1.7822E 02
0, 25	1.9817E-01	2.5964E-01	-7.9498E 03	-1.9574E 02
0, 24	1.8526E-01	2.7427E-01	-8.5311E 03	-2.0689E 02
0, 23	1.6945E-01	2.8556E-01	-8.8790E 03	-2.1324E 02
0, 22	1.5239E-01	2.9408E-01	-9.0566E 03	-2.1614E 02
0, 21	1.3526E-01	3.0037E-01	-9.1169E 03	-2.1673E 02

Table 5 (concl'd)

0, 20	1.1887E-01	3.0491E-01	-9.1010E 03	-2.1585E 02
0, 19	1.0370E-01	3.0810E-01	-9.0399E 03	-2.1416E 02
0, 18	9.0002E-02	3.1028E-01	-8.9560E 03	-2.1208E 02
0, 17	7.7856E-02	3.1173E-01	-8.8641E 03	-2.0992E 02
0, 16	6.7221E-02	3.1266E-01	-8.7739E 03	-2.0787E 02
0, 15	5.7985E-02	3.1324E-01	-8.6910E 03	-2.0602E 02
0, 14	4.9999E-02	3.1360E-01	-8.6181E 03	-2.0441E 02
0, 13	4.3097E-02	3.1380E-01	-8.5561E 03	-2.0306E 02
0, 12	3.7116E-02	3.1393E-01	-8.5046E 03	-2.0194E 02
0, 11	3.1904E-02	3.1400E-01	-8.4627E 03	-2.0104E 02
0, 10	2.7324E-02	3.1406E-01	-8.4292E 03	-2.0032E 02
0, 9	2.3258E-02	3.1410E-01	-8.4025E 03	-1.9975E 02
0, 8	1.9604E-02	3.1414E-01	-8.3816E 03	-1.9931E 02
0, 7	1.6279E-02	3.1418E-01	-8.3652E 03	-1.9896E 02
0, 6	1.3213E-02	3.1422E-01	-8.3524E 03	-1.9869E 02
0, 5	1.0347E-02	3.1425E-01	-8.3425E 03	-1.9849E 02
0, 4	7.6330E-03	3.1428E-01	-8.3350E 03	-1.9833E 02
0, 3	5.0287E-03	3.1430E-01	-8.3293E 03	-1.9823E 02
0, 2	2.4962E-03	3.1431E-01	-8.3251E 03	-1.9816E 02
0, 1	-0.	3.1431E-01	-8.3224E 03	-1.9813E 02

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

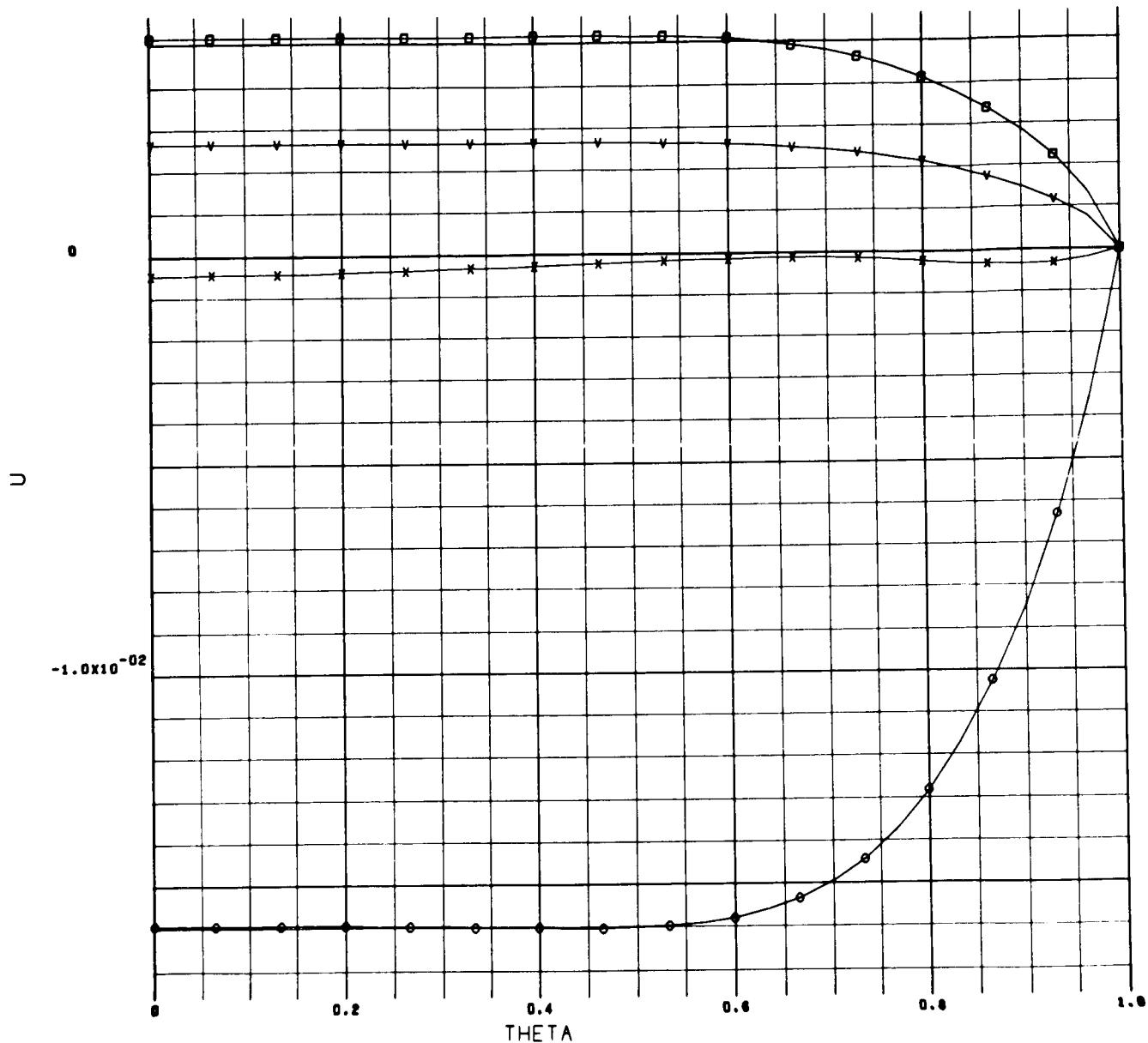
44BFYd  
001 000

O PHI = 1.503 , ROW 5

O PHI = 1.038 , ROW 16

X PHI = 1.300 , ROW 9

Y PHI = 1.029 , ROW 17



a - Sphere Displacement Components

Fig. 12 Output Plot for the Example: Spherical Segment Under Uniform Normal Pressure

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

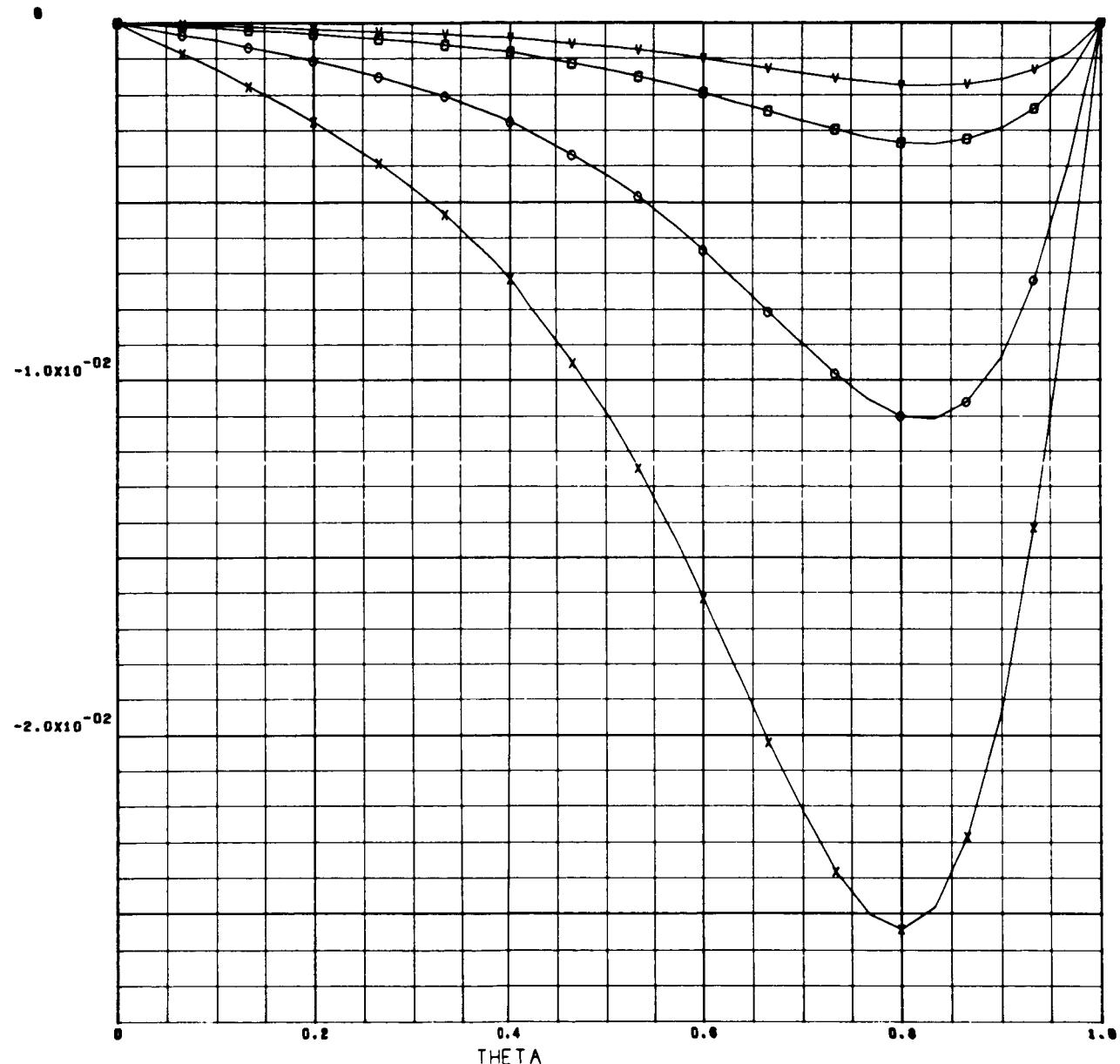
44BFYd  
002 000

O PHI = 1.503 , ROW 5

O PHI = 1.038 , ROW 16

X PHI = 1.300 , ROW 9

Y PHI = 1.029 , ROW 17



b -- Sphere Displacement Components

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

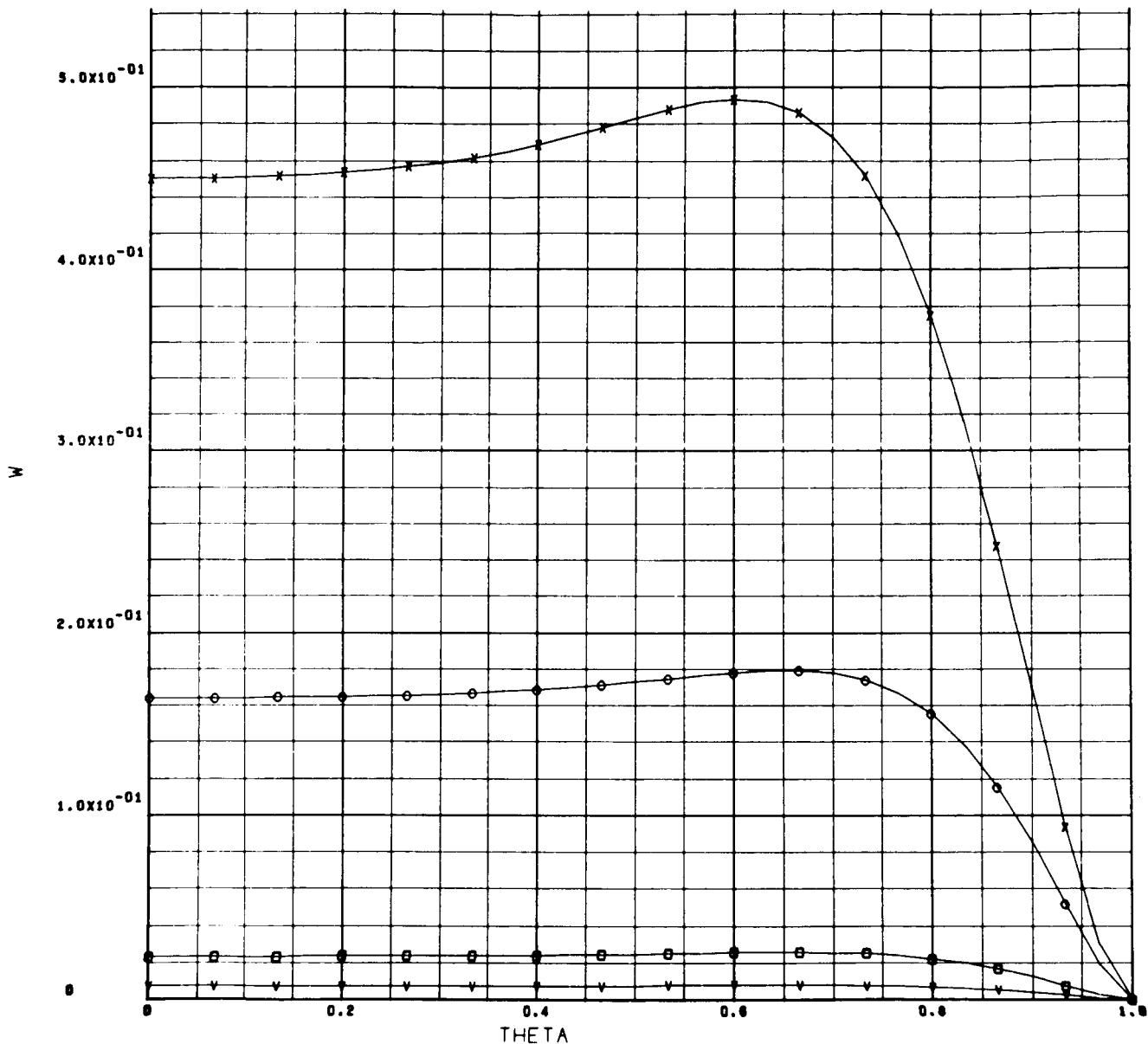
4dBFYd  
003 000

O PHI = 1.503 , ROW 5

X PHI = 1.300 , ROW 9

O PHI = 1.038 , ROW 16

Y PHI = 1.029 , ROW 17



c - Sphere Displacement Components

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

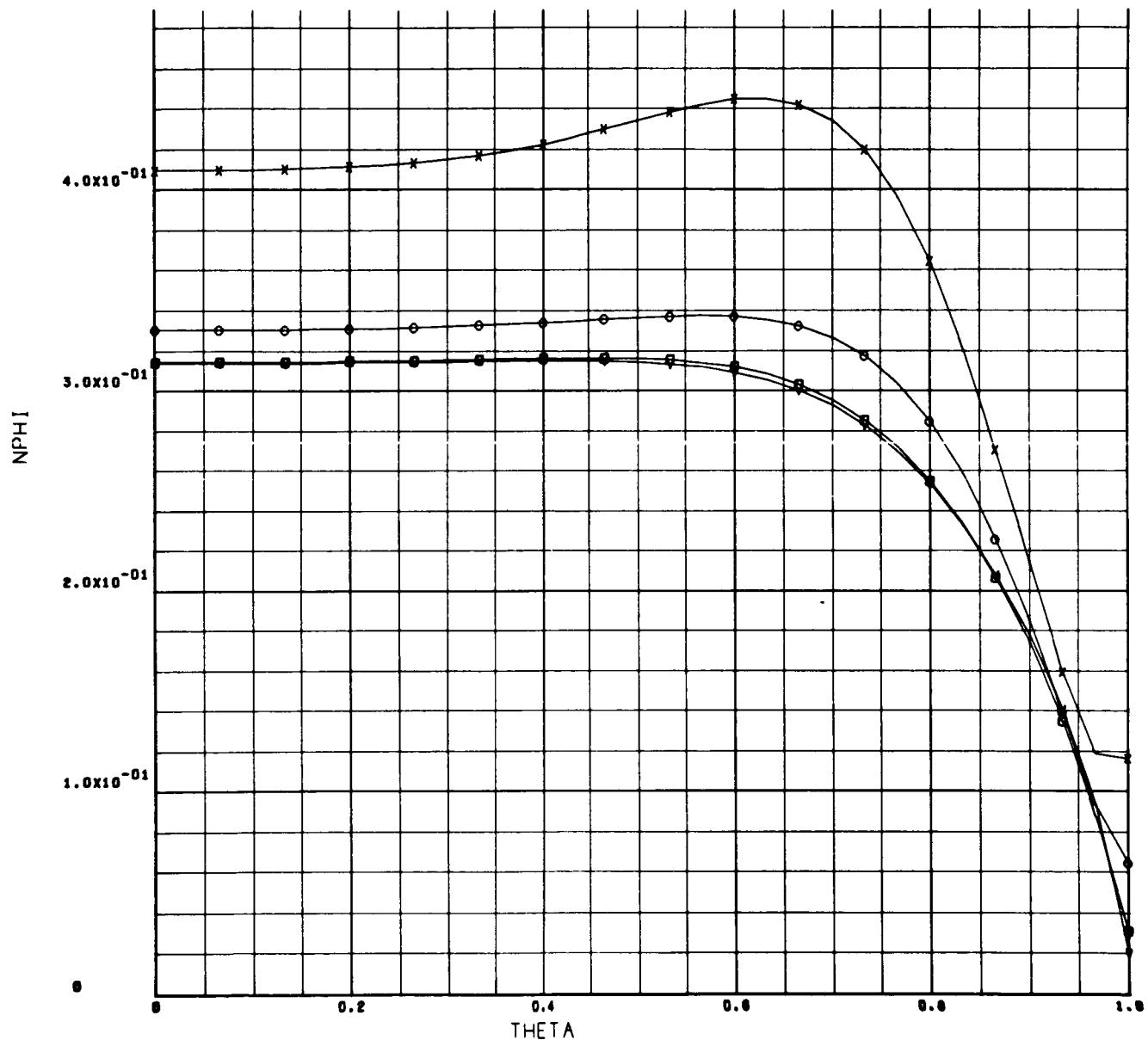
44BFYd  
004 000

G PHI = 1.503 , ROW 5

X PHI = 1.300 , ROW 9

G PHI = 1.038 , ROW 16

Y PHI = 1.029 , ROW 17



d - Sphere Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

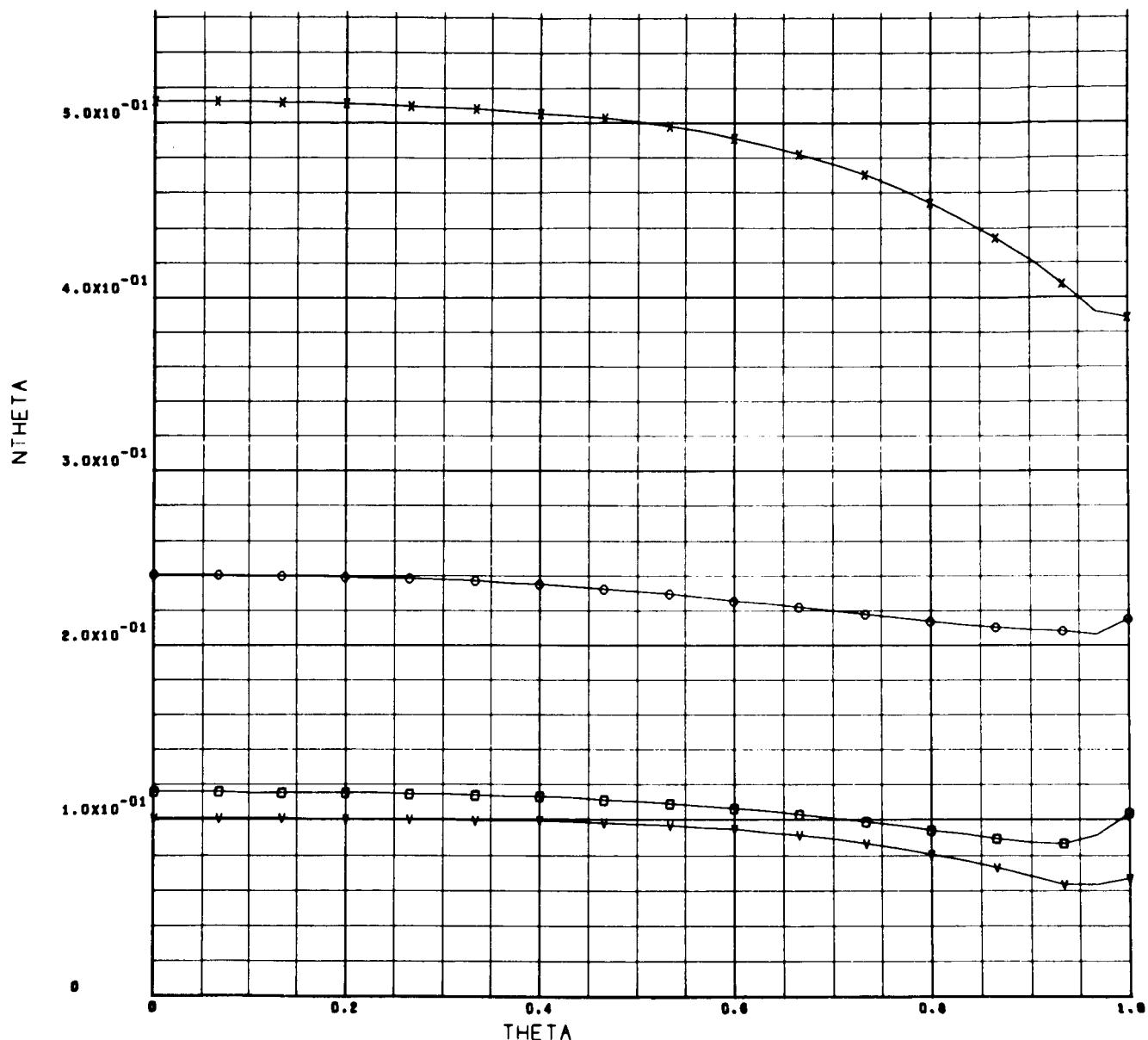
44BFY4  
005 000

G PHI = 1.503 , ROW 5

G PHI = 1.038 , ROW 16

X PHI = 1.300 , ROW 9

Y PHI = 1.029 , ROW 17



e — Sphere Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

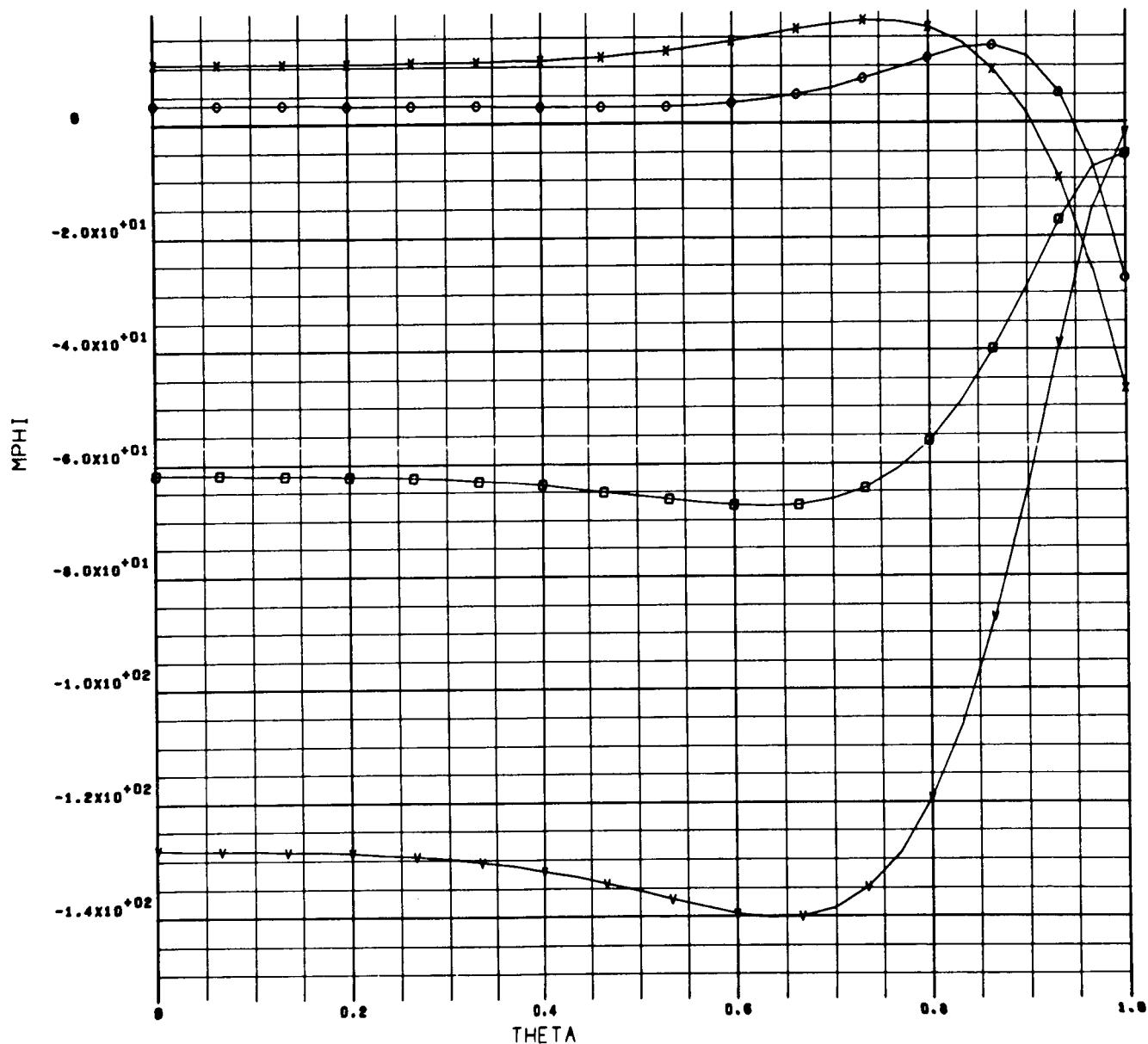
44BFYd  
006 000

O PHI = 1.503 , ROW 5

O PHI = 1.038 , ROW 16

X PHI = 1.300 , ROW 9

Y PHI = 1.029 , ROW 17



f - Sphere Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

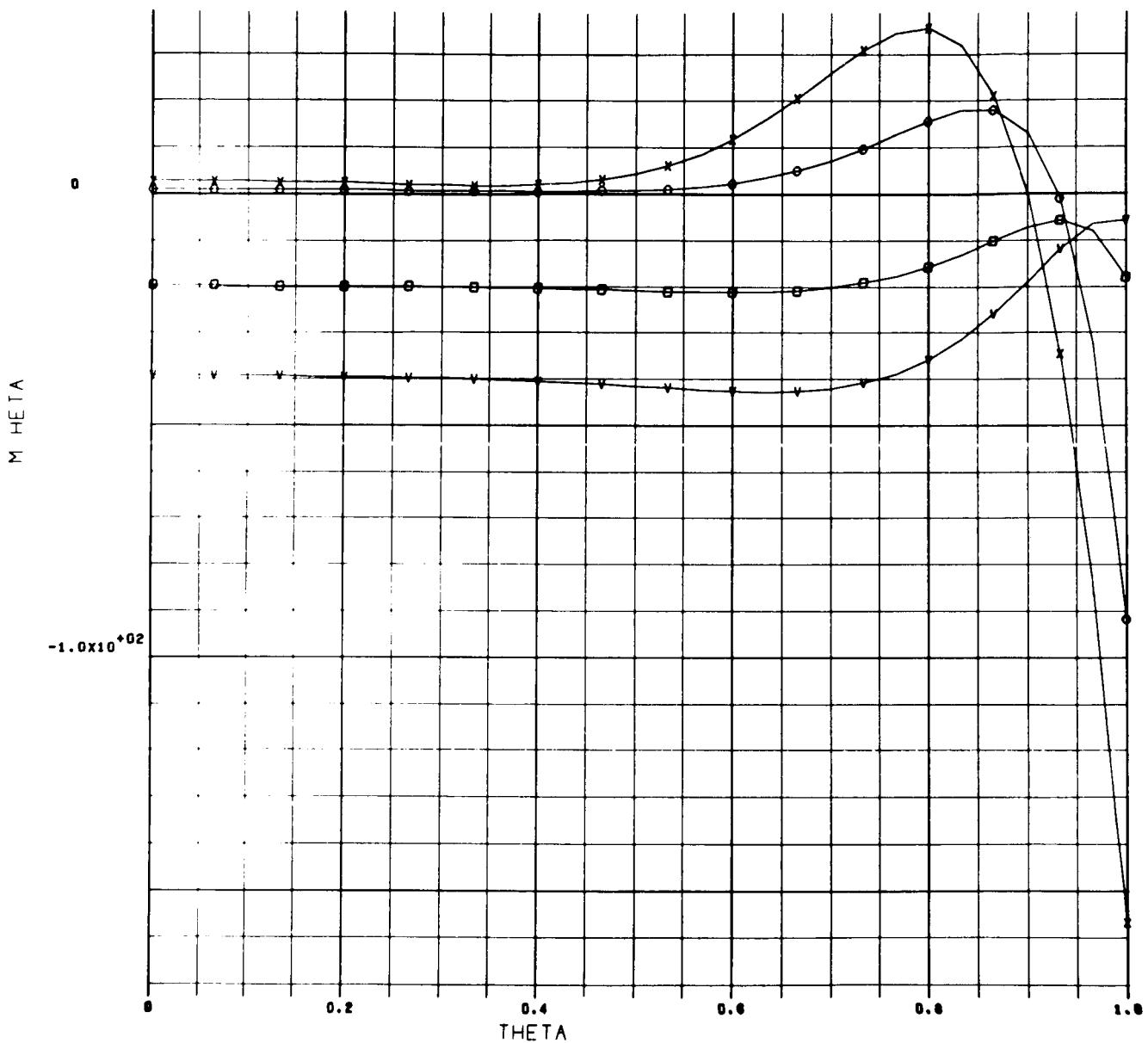
4-BFY4  
007 000

O PHI = 1.503 , ROW 5

G PHI = 1.038 , ROW 16

X PHI = 1.300 , ROW 9

Y PHI = 1.029 , ROW 17

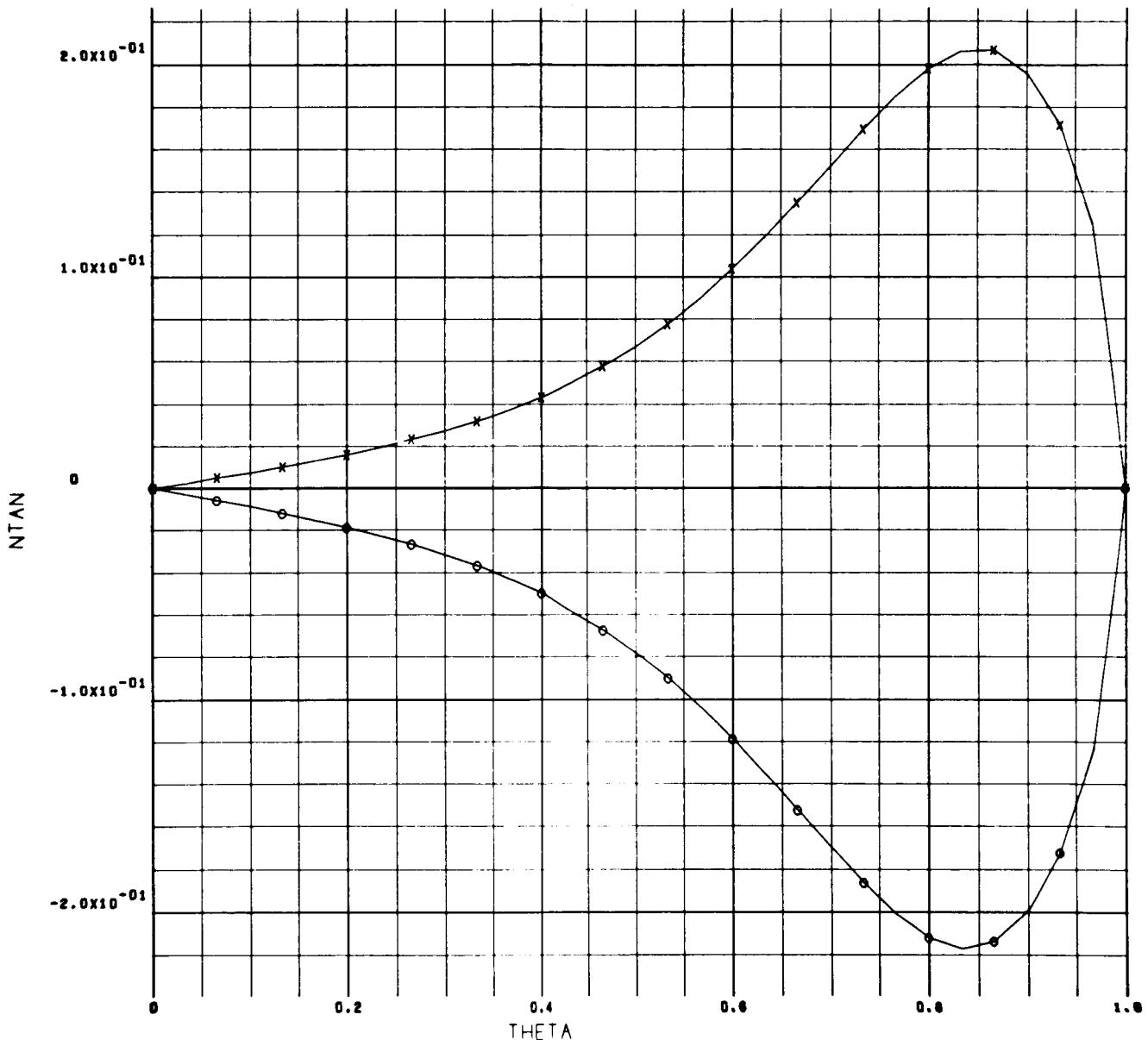


g - Sphere Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

44BFYd  
008 000

- CURVE 1= UPPER BOUNDARY
- × CURVE 2= LOWER BOUNDARY

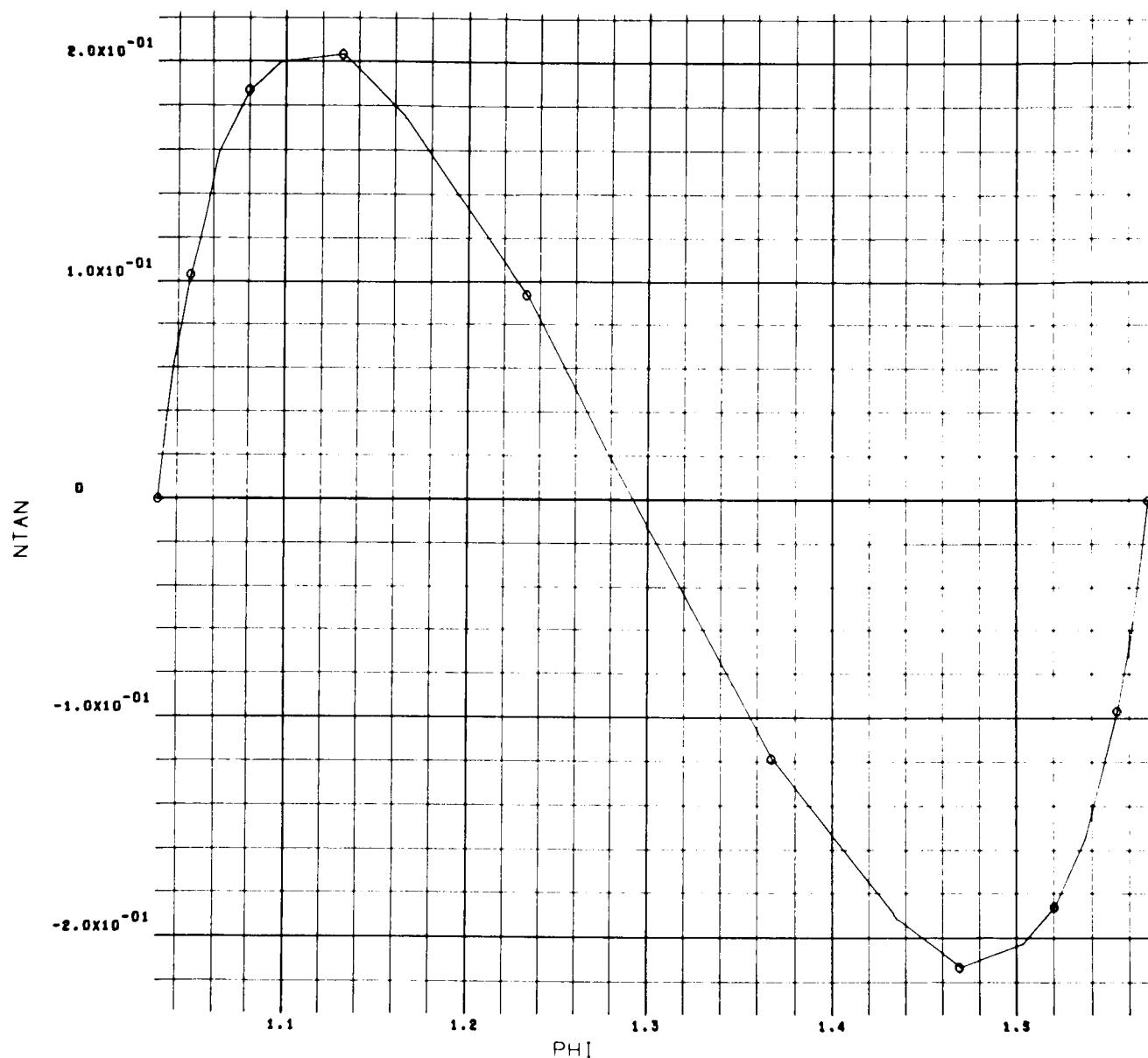


h - Boundary Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

4-BFYd  
009 000

G RIGHT BOUNDARY



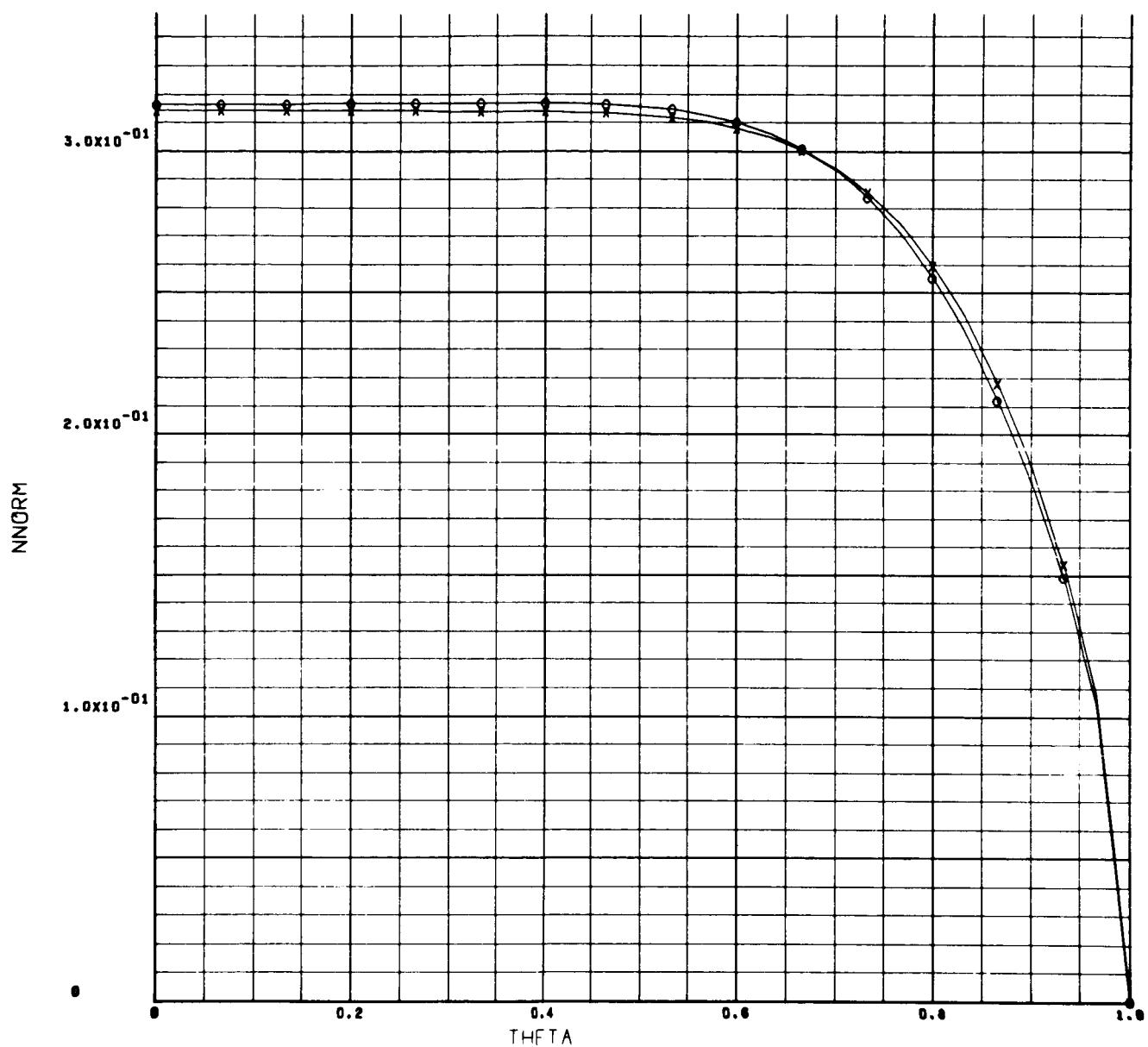
i - Boundary Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

44BFYd  
010 000

O CURVE 1= UPPER BOUNDARY

X CURVE 2= LOWER BOUNDARY

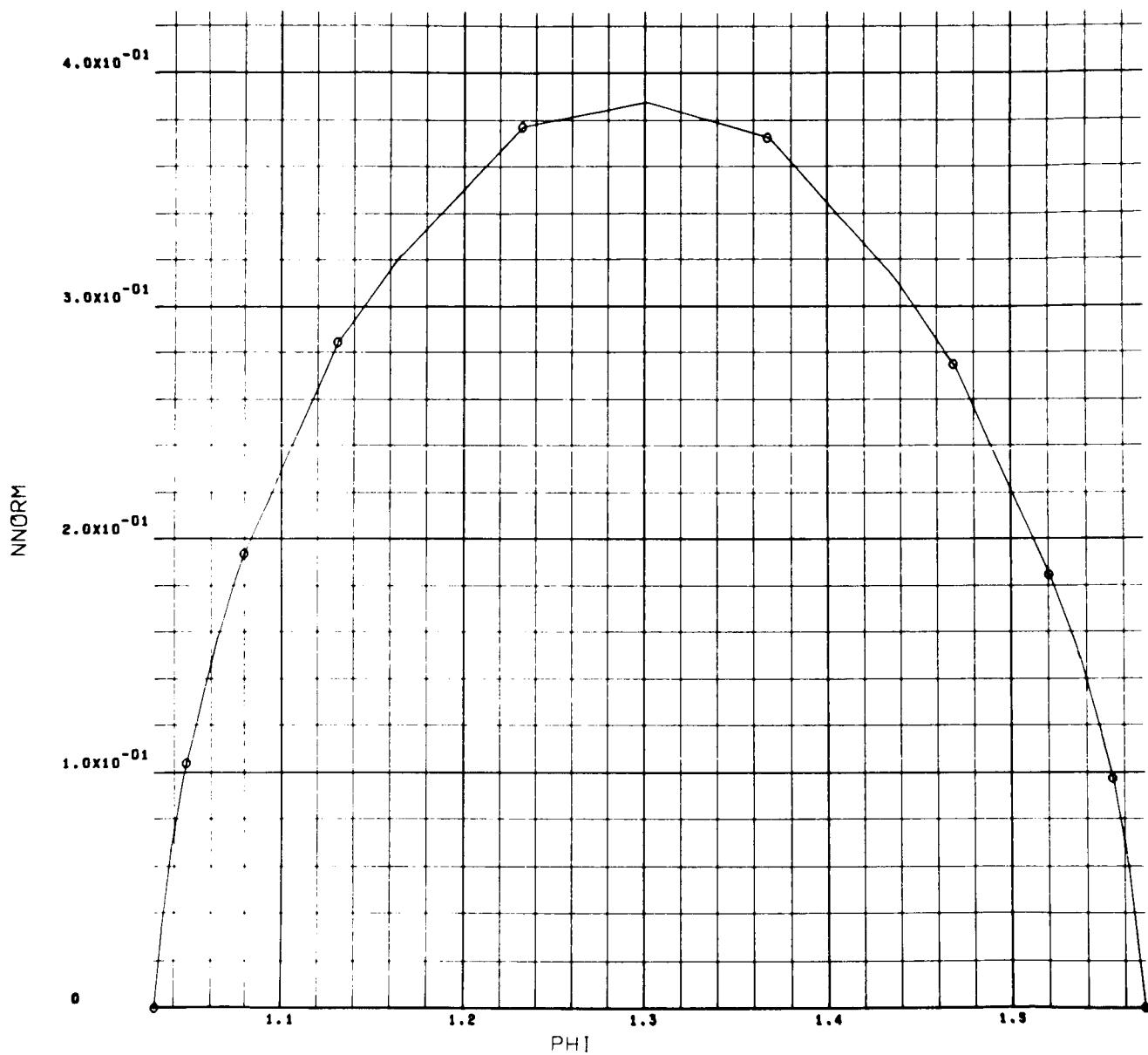


j - Boundary Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

4-BFYd  
011 000

O RIGHT BOUNDARY

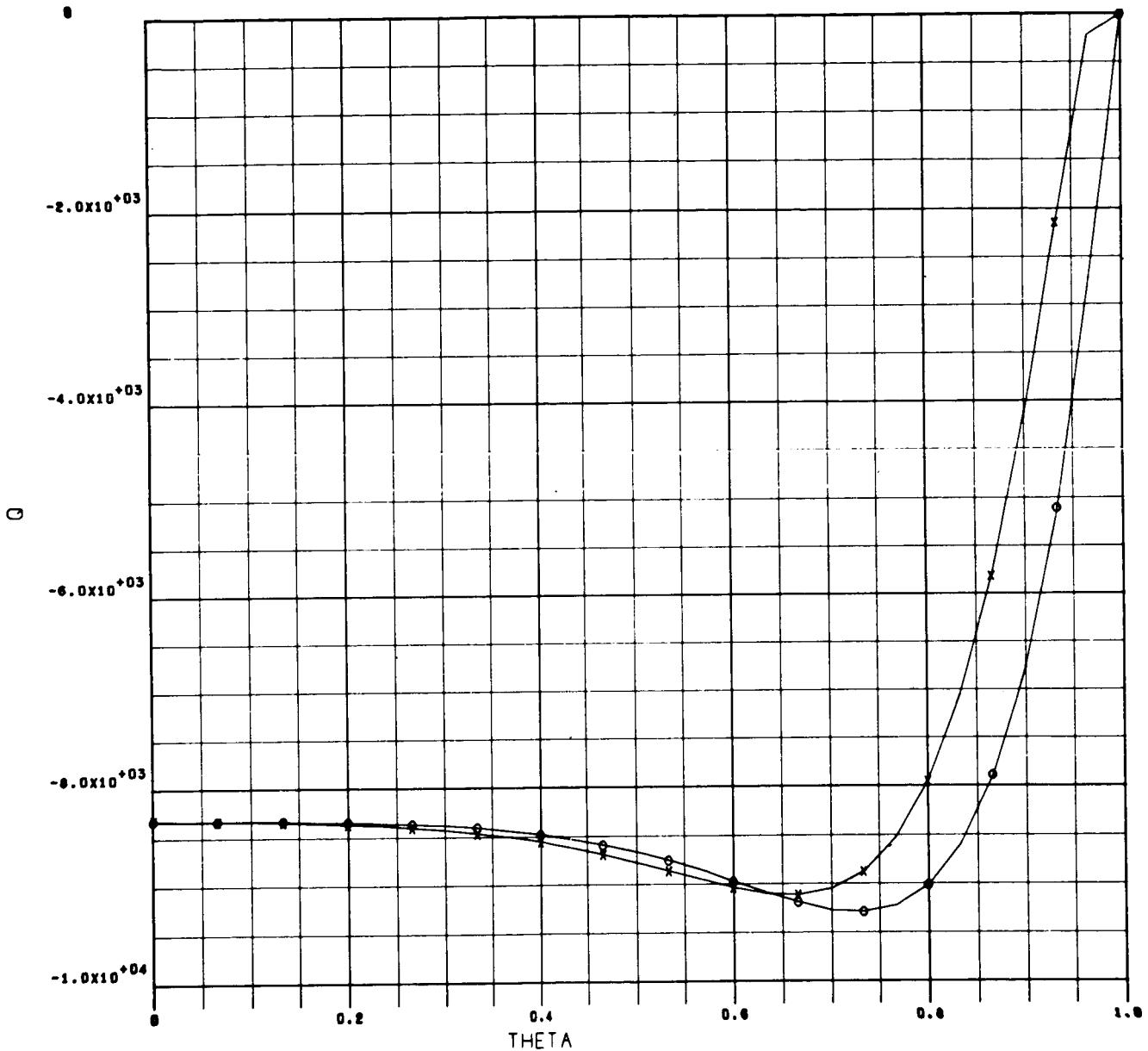


k - Boundary Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

4-BFYd  
012 000

- CURVE 1= UPPER BOUNDARY
- × CURVE 2= LOWER BOUNDARY

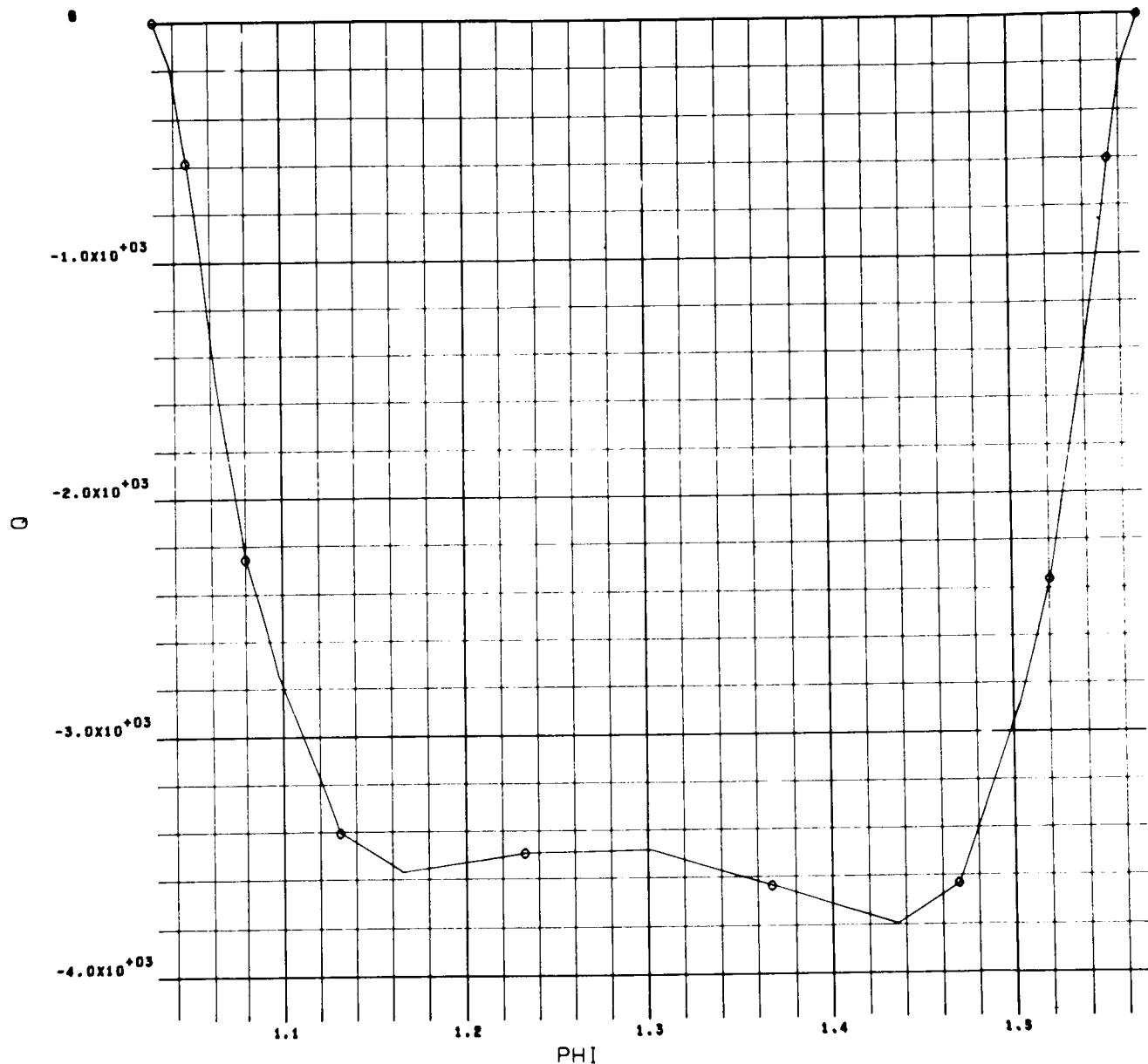


1 - Boundary Stress Resultants

EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

4-BFYd  
013 000

O RIGHT BOUNDARY

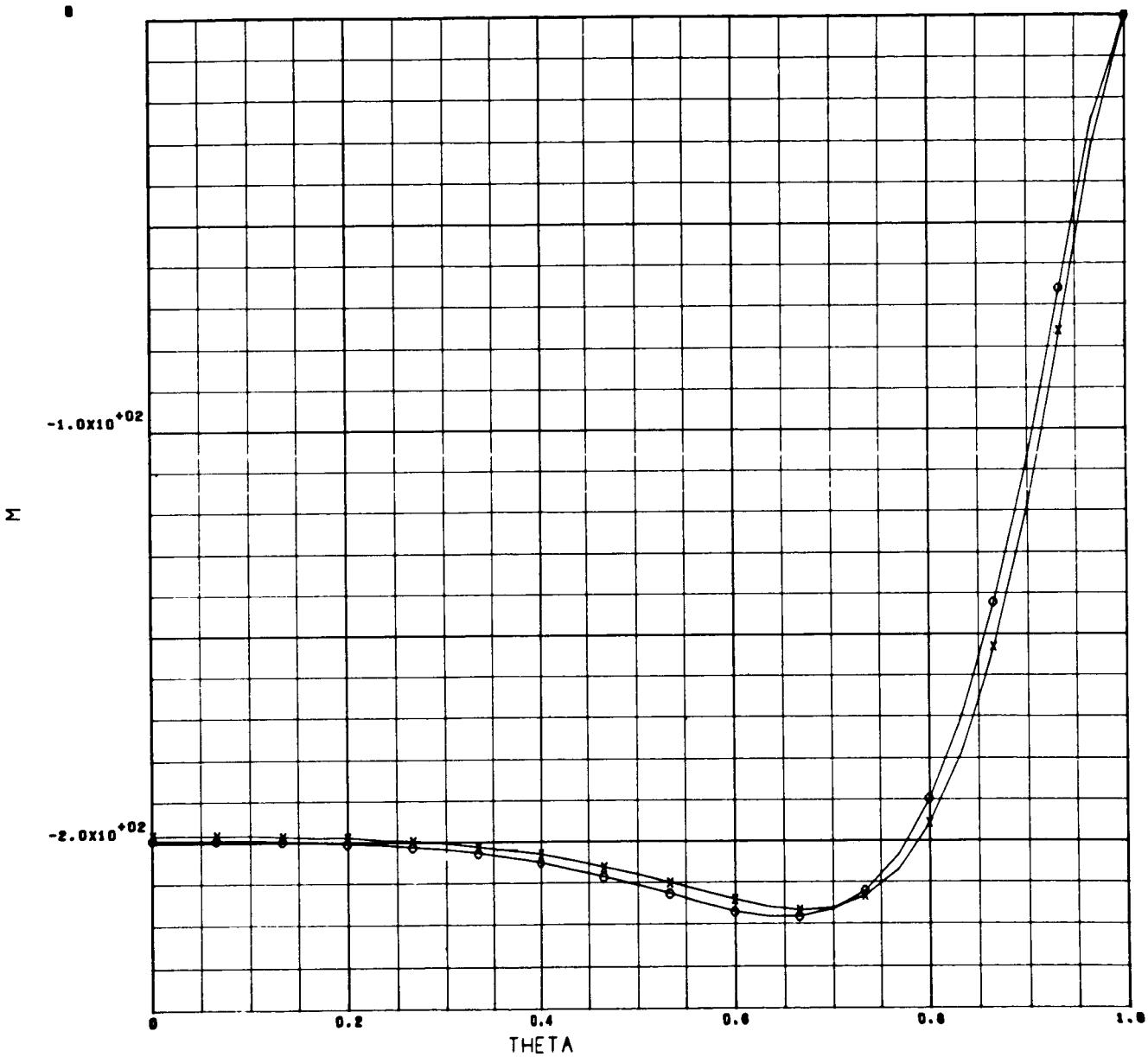


$m$  - Boundary Stress Resultants

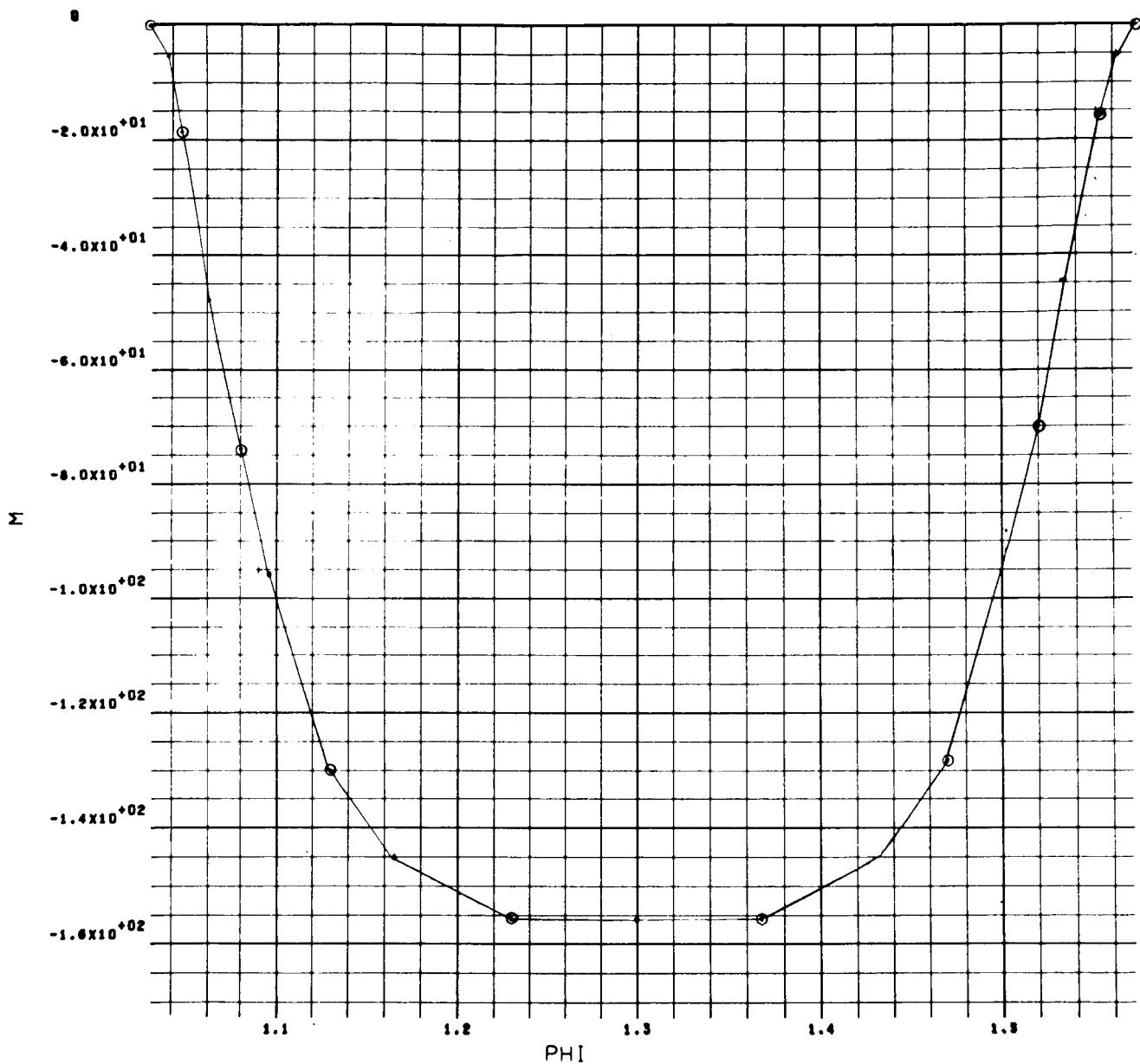
EXAMPLE SPHERICAL SEGMENT UNDER UNIFORM NORMAL PRESSURE

44BFYd  
014 000

- CURVE 1= UPPER BOUNDARY
- × CURVE 2= LOWER BOUNDARY



n - Boundary Stress Resultants



o — Boundary Stress Resultants

#### **4.3 LISTING OF THE PROGRAM**

The complete program is given in Table 6.

Table 6  
STUDY OF JUNCTURE STRESS FIELD: SPHERICAL SEGMENT

```

*      CHAIN(1,2)                                S1P00010
*      FORTRAN                                 S1P00020
*      LIST                                    S1P00030
C      CS1P SPHERICAL SEGMENT ! STUDY OF JUNCTURE STRESS FIELD !
C      CONTRACT NAS 8-114800 TO NASA G.C. MARSHALL SPACE FLIGHT CENTER   S1P00040
C      HUNTSVILLE, ALABAMA                                         S1P00050
C      BY SOLID MECHANICS , AEROSPACE SCIENCES LABORATORY , 52-20   S1P00060
C      LOCKHEED MISSILES AND SPACE COMPANY, PALO ALTO CALIF        S1P00070
C      THIS PROGRAM IS FOR USE ONLY ON FORTRAN III, VERSION II       S1P00080
C      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8    S1P00090
COMMON NCF                                         S1P00100
COMMON NROW, NCOL, MM, MFLAG, XM,XLP          S1P00110
COMMON ISW1, ISW2, ISW3                         S1P00120
COMMON A                                         S1P00130
COMMON TMP, YK, YL                               S1P00140
COMMON T1, T2, XX, XX1, Z, Z1, Z2             S1P00150
COMMON ZNU, THC, PHI, FF, RH, DD, XH, XK       S1P00160
COMMON ZETA                                       S1P00170
COMMON TE, TI, TO, OC, TC, TD, DDLD           S1P00180
COMMON RECORD                                     S1P00190
COMMON TIM1,TIM2, KTIME                         S1P00200
DIMENSION A(1232)                                S1P00210
DIMENSION MM(40)                                 S1P00220
DIMENSION T1( 89), T2( 89), XX( 89), XX1( 89), Z( 89), Z1( 89), Z2( 89)   S1P00230
DIMENSION TMP(5184), YK(5184), YL(4,4,324)     S1P00240
DIMENSION ZETA( 30)                             S1P00250
DIMENSION RECORD( 12)                           S1P00260
1 FORMAT (1H1, 12A6)                           S1P00270
2 FORMAT (6E12.8)                            S1P00280
3 FORMAT (1H1)                                S1P00290
4 FORMAT (35I2)                                S1P00300
5 FORMAT (1H1,3X,3HCOL, 15, 8I14/4H RCW)      S1P00320
6 FORMAT ( 14, 1P9E14.6)                      S1P00330
7 FORMAT (10I1)                                S1P00340

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8 FORMAT (12A6)
14 FORMAT (26H0 FINITE DIFFERENCE MESH. I2, 7H ROWS, 12, 27H COLUMNS) S1P00350
1. MESH SPACING. H= F15•7, 4H, K= E15•7 ) S1P00360
15 FORMAT (21H0 INPUT CONSTANTS. NU= 1PE12•5, 9H, THETAC= 1PE12•5, S1P00370
1 7H, PHI1= 1PE12•5, 12H, PHI1/PHI2= 1PE12•5, 6H, R/H= 1PE12•5 ) S1P00380
17 FORMAT (42H0 SPHERE DISPLACEMENT COMPONENTS (U,V,W) / S1P00390
1 10H0 COL ROW , 17X, 1HU, 15X, 1HW ) S1P00400
18 FORMAT (53H ROW COL NX NTHETA NXTHETA NTHETAX ) S1P00410
19 FORMAT (125H0ROW COL EPSX EPST GAMMA - R*SIPO0430
1 1X1 R*X12 OMEGAX OMEGAT PS1P00440
2H1 ) S1P00450
20 FORMAT (28H0 SPHERE STRESS RESULTANTS. ) S1P00460
919 FORMAT (34H GRADED MESH IN ZETA DIRECTION ) S1P00470
920 FORMAT ( 2X, 4H ROW, 15I8/ 6X, 15I8 ) S1P00480
921 FORMAT ( 6H ZETA=, 15F8•5/ 6X, 15F8•5 ) S1P00490
922 FORMAT (27H ROW 1 IS A SYMMETRY LINE ) S1P00500
925 FORMAT (25H0UNIFORM RADIAL PRESSURE ) S1P00510
930 FORMAT (1H 13, 1H, 13, 10X, 1P3E16•6 ) S1P00520
931 FORMAT (1H 13, 1H, 13, 10H BOUNDARY , 1P3E16•6 ) S1P00530
932 FORMAT (1H 13, 1H, 13, 10H SMY LINE , 1P3E16•6 ) S1P00540
936 FORMAT (30H0 BOUNDARY STRESS RESULTANTS. /84H0ROW COL NTAN S1P00550
1 NNORM Q M RBAR ) S1P00560
937 FORMAT (13,1H, 13, 1P5E12•4 ) S1P00570
938 FORMAT ( 13, 2H, 13, 66X, 1P16•7 ) S1P00580
939 FORMAT (59H0 SPHERE STRAINS, CHANGES OF CURVATURE AND ROTATION S1P00590
1 N. ) S1P00600
945 FORMAT ( 1H0 // 8H CASE NR I2, 13H COMPLETED IN F8•3, 9H MINUTES.) S1P00610
951 FORMAT (33H0LINEAR TEMPERATURE GRADIENT. TE=E15•7,5H, TI=E15•7, S1P00620
1 5H, TO=E15•7, 5H, OC=E15•7 ) S1P00630
962 FORMAT (90H ROW COL MX MTTHETA MXTHETA QX ) S1P00640
1 QTHETA ) S1P00650
C SET TAPE ASSIGNMENTS. S1P00660
KTAPE=15 S1P00670
MTAPE=7 S1P00680
B XMTP=0000000002221 S1P00690
B XZTP=0000000002223 S1P00700
B XNTP=000000001224 S1P00710
NTAPE=4 S1P00720
1ZTAPE=3 S1P00730

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REWIND MTAPE          S1P00740
REWIND NTAPE          S1P00750
REWIND ITAPE          S1P00760
CALL CLOCK (TINI)    S1P00770
NCF = 44              S1P00780
C READ AND WRITE INPUT DATA
21 READ INPUT TAPE 5, 8, RECORD      S1P00790
WRITE OUTPUT TAPE 6, 1, RECORD       S1P00800
C IOPT1 = 0 CONSTANT MESH SPACING   S1P00810
C IOPT1 = 1 GRADED MESH SPACING IN X DIRECTION  S1P00820
C IOPT2=0 SYMMETRY LINE AT PHI=PHI/2*(1+FF)  S1P00830
C IOPT2=1 NO SYMMETRY LINE          S1P00840
C IOPT3 = 0 OMIT SPHERE STRAINS, CHANGES IN CURVATURE AND ROTATION  S1P00850
C IOPT3 = 1 PRINT OUT STRAINS , ETC.  S1P00860
C IOPT4=0 UNIFORM NORMAL PRESSURE   S1P00870
C IOPT4=1 LINEAR TEMPERATURE GRADIENT  S1P00880
C IOPT5=0 NOT FINAL CASE WITH PLOTS  S1P00890
C IOPT5=1 FINAL CASE WITH PLOTS    S1P00900
C READ INPUT TAPE 5, 7, IOPT1,IOPT2, IOPT3, IOPT4, IOPT5,IOPT6,IOPT7, S1P00910
S1P00920
1, IOPT8
XM = IOPT1
XLD=IOPT4
READ INPUT TAPE 5, 2, ROW, COL, XH, XK
READ INPUT TAPE 5, 2, ZNU, THC, PHI, FF, RH
NROW=ROW
NCOL=COL
NC1=NCOL+1
NR1=NROW+1
ITOT=3*(NROW+6)
WRITE OUTPUT TAPE 6,14, NROW, NCOL, XH, XK
WRITE OUTPUT TAPE 6, 15, ZNU, THC, PHI, FF, RH
DD = 1./(12.*RH*RH)
IF (IOPT1) 23,23,22
22 READ INPUT TAPE 5, 4, (MM(I), I=1,NROW)
MM(NR1)=MM(NROW)
WRITE OUTPUT TAPE 6, 919
GO TO 25
23 DO 24 J=1, 30
24 MM(J)=0

```

```

25 IF (IOPT2) 31, 31, 26
26 YK(0)=PH1*FF
ZETA(1) = PH1*FF
      X = ZETA(1) - XH/2.*MM(1)
      YK(1)=X
      ZETA(2)=X
      NDIM=3*NROW
      MO=0
      GO TO 35
31 YK(1)=PH1*(1.+FF)/2.
      X=YK(1)
      ZETA(2)=X
      NDIM=3*NROW-1
      WRITE OUTPUT TAPE 6, 922
      NCRV1=1
      MO=1
35 WRITE OUTPUT TAPE 6, 920, (1, I=MO,NR1)
      NR4=NR1+1-MO
      DO 30 J=2, NROW
      IF (MM(J)-MM(J-1)) 27, 27, 28
      27 JM=MM(J)
      GO TO 29
      28 JM=MM(J-1)
      29 X=X-XH/2.***JM
      YK(J)=X
      ZETA(J+1)=X
      YK(NR1)=PH1
      ZFTA(NR1+1)=PH1
      WRITE OUTPUT TAPE 6, 921, (YK(I), I=MO, NR1)
      NSM=NDIM-NROW
      NSQ=72*NDIM
      IF (IOPT4-1) 82, 106, 106
      82 WRITE OUTPUT TAPE 6, 925
      GO TO 84
      106 READ INPUT TAPE 5, 2, TE, TI, TO, OC
      WRITE OUTPUT TAPE 6, 951, TE, TI, TO, OC
      TT1 = (TE + TI)/2. - TO
      TT2 = (TE - TI)

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TC = (1.+ZNU)*OC*TT1      S1P01520
TD = (1.+ZNU)*OC*TT2      S1P01530
84 CONTINUE                 S1P01540
      READ INPUT TAPE 5, 4, (MM(I), I=31, 35)
79 CONTINUE
      CALL COEFZ             S1P01560
      MFLAG=0                S1P01570
      IF (KTIME) 81,81,400    S1P01580
81 CONTINUE
      REWIND KTAPE
      COMPUTE L, M,N AND Z MATRICES OF FORWARD SWEEP
      400 KTIME=KTIME+1
      N1=NSM
      N2=NSM
      N3=NSM
      I=1
      GO TO 405
401 CALL RTAPE (XZTP,Z1,N1,1)
      CALL RTAPE (XMTP,TMP, NSQ, 0)
      CALL MTX (YK, I, 2)
      IF (I-2) 405, 403, 402
      402 CALL BACK (XNTP)
      CALL ZERO (YL, NSQ)
      CALL RTAPE (XMTP, TMP, NSQ,1)
      CALL MTXS (TMP, YL, I, 1)
      CALL RTAPE (XMTP, TMP, NSQ,0)
      CALL ADDM (YK, YL, YK, -NSQ)
      CALL RTAPE (XNTP, YL, NSQ, 0)
      403 N1=NDIM
      CALL RTAPE (XMTP, TMP, NSQ,1)
      CALL MATM (YK, TMP, TMP,NDIM,N2, NDIM)
      IF (I-2) 405, 405, 404
404 CALL RTAPE (XNTP, YL, NSQ, 1)
      CALL MTXS (YL, TMP,I, 1)
      405 CALL MTX (YL, I, 3)
      IF (I-2) 408, 406, 406
406 CALL ADDM (YL, TMP, YL,-NSQ)
      IF (I-NCOL) 407, 408, 408
407 CALL RTAPE (XNTP, TMP, NSQ,0)

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```

408 CALL INVERT (YL, N1, ISING)
    IF (I-1) 414, 414, 410
410 CALL MATM (YK, Z1, T2, NDIM, N2, 1)
    IF (I-NCOL) 411, 421, 421
411 CALL RTAPE (XNTP, TMP, NSQ, 1)
    CALL MATM (YK, TMP, NDIM, N2, NDIM)
414 CALL MTX (YK, I, 4)
    IF (I-2) 417, 416, 416
416 CALL ADDM (YK, TMP, YK, -NSQ)
417 IF (I-NCOL+1) 418, 419, 419
418 CALL ZZERO (TMP, NSQ)
    CALL MTXS (YL, TMP, I, 5)
    CALL WTAPE (XNTP, TMP, NSQ, 0)
419 CALL MATM (YL, YK, YK, N1, N1, NDIM)
    CALL WTAPE (XMTP, YK, NSQ, 0)
    IF (I-NCOL+1) 420, 421, 421
420 CALL WTAPE (XNTP, TMP, NSQ, 1)
    CALL BACK (XNTP)
421 CALL CONS(T1,I)
    IF (I-1) 426, 426, 422
422 CALL ADDM (T1, T2, T1, -NDIM)
    IF (I-2) 426, 424, 423
423 CALL MTXS (Z2, T2, I,-1)
424 DO 425 J=1,NDIM
425 Z2(J)=Z1(J)
    IF (I-NCOL) 426, 428, 428
426 CALL WTAPE (XMTP, YK, NSQ, 1)
    CALL BACK (XMTP)
    IF (I-2) 430, 429, 428
428 CALL ADDM (T1, T2, T1,-NDIM)
429 CALL BACK (XMTP)
430 CALL MATM (YL, T1, Z1, N1, N1, 1)
    CALL WTAPE (XZTP, Z1, N1, 0)
    IF (I-NCOL) 431, 450, 450
431 IF (I-2) 434, 433, 432
432 N3=NDIM
433 N2=NDIM
434 I=I+1
        GO TO 401

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C   DECOMPOSITION COMPLETED • BEGIN BACKWARD SWEEP.
450  CALL WTAPE (XZTP, Z1, N1, 1)           S1P02300
      CALL BACK (XZTP)                         S1P02310
      CALL BACK (XNTP)                         S1P02320
      CALL BACK (XNTP)                         S1P02330
      N4 = (NCOL+3)*(NRW+6)*3                 S1P02340
      CALL ZERO (TWD, N4)                      S1P02350
      451 IF (I-NCOL) 452,454,454             S1P02360
      DO 453 J=1,NDIM                         S1P02370
      XX1(J)=XX(J)                           S1P02380
      453 XX(J)=Z1(J)                         S1P02390
      CALL RTAPE (XMTP, YK, NSQ, 1)           S1P02400
      CALL BACK (XMTP)                         S1P02410
      IF (I-1) 454, 454, 4541                  S1P02420
      4541 CALL BACK (XMTP).                   S1P02430
      454 CALL RTAPE (XZTP, Z1, N1, 0)         S1P02440
      CALL RTAPE (XZTP, Z1, N1, 0)             S1P02450
      IF (I-1) 4543, 4543, 4542              S1P02460
      4542 CALL BACK (XZTP)                   S1P02470
      4543 CALL BACK (XZTP)                   S1P02480
      IF (I-NCOL+1) 456,457,462              S1P02490
      456 CALL RIAPE (XNTP, YL, NSQ, 0)       S1P02500
      457 CALL MATM(YK, XX, T1, N1, NDIM, 1)
      CALL ADDM(Z1, T1, Z1, -NDIM)
      IF (I-NCOL+1) 458,462,462              S1P02510
      458 CALL RIAPE (XNTP, YL, NSQ, 1)
      IF (I-1) 4591, 4591, 459                S1P02520
      459 CALL BACK (XNTP)                   S1P02530
      4591 CALL BACK (XNTP)                   S1P02540
      CALL MATM(YL, XX1, T1, N1, NDIM, 1)
      CALL ADDM(Z1, T1, Z1, -NDIM)
      460 IF (I-2) 463,461,462              S1P02550
      461 N1=NSM                            S1P02560
      462 CALL RTAPE (XMTP, YK, NSQ, 0)       S1P02570
      463 CALL STORE (Z1, I)                 S1P02580
      IF (I-2) 500, 464, 464                S1P02590
      464 I=I-1                            S1P02600
      GO TO 452                            S1P02610
      500 MFLAG=1                          S1P02620
      IF (IOPT2) 145, 145, 140            S1P02630
                                         S1P02640
                                         S1P02650
                                         S1P02660
                                         S1P02670
                                         S1P02680

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```

140 L0=6
    DO 141 L=1, NCOL
        TMP(L0)=TMP(L0+6)
141   L0=L0+ITOT
        L1=L0-ITOT
        L0=L0+ITOT
        TMP(L0)=TMP(L1)
145   L0=NC1*ITOT+12
        DO 147 J=1, NROW
            L1=L0-2*ITOT
            TMP(L0)=TMP(L1)
147   L0=L0+3
            L0=L0+3
            TMP(L0)=TMP(L1)
            L0=L0-ITOT
            DO 148 I=1, NCOL
                L0=L0-ITOT
                TMP(L0)=TMP(L1)
148   L1=L1-ITOT
            CALL BOUND
                IOUT=51
                NC2=NCOL+3
                IF (IOPT2) 501,501, 502
501   NR2=NROW+3
            GO TO 503
502   NR2=NROW+6
503   DO 520 I=1, NC2
            I3=I*(NROW+6)*3
            I2=I3-1
            I1=I2-1
            IF (IOUT+NR2-50) 505, 505, 504
504   WRITE OUTPUT TAPE 6, 1
            WRITE OUTPUT TAPE 6, 17
            IOUT=6
505   DO 515 JJ=1, NR2
            J=NROW-JJ+4
            IF (J-NR1) 506, 511, 510
506   IF (IOPT2) 507, 507, 508
507   IF (J-1) 512, 512, 510

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```

508 IF (J) 510, 511, 510
510 WRITE OUTPUT TAPE 6, 930, I, J, TMP(I1), TMP(I2), TMP(I3)
      GO TO 514
511 WRITE OUTPUT TAPE 6, 931, I, J, TMP(I1), TMP(I2), TMP(I3)
      GO TO 514
512 WRITE OUTPUT TAPE 6, 932, I, J, TMP(I1), TMP(I2), TMP(I3)
514 I1=I1-3
      I2=I2-3
      I3=I3-3
515 IOUT=IOUT+1
520 CONTINUE
521 ISW3=1
      IOUT=50
      L=32
      K=0
      DO 540 J=MO, NR1
      IF (IOPT1) 537, 537, 536
536 CALL GRADE (J)
      537 IF (MM(31)) 5378, 5378, 5370
      5370 IF (MM(L)-J) 5378, 5372, 5378
      5372 IF (L-35) 5374, 5374, 5378
      5374 L=L+1
      K=K+1
      K1=K
      GO TO 5380
5378 K1=0
5380 DO 540 I=1, NC1
      IF (IOUT-41) 539, 538, 538
538 WRITE OUTPUT TAPE 6, 1, RECORD
      IOUT=0
      IF (MFLAG) 532, 530, 531
531 WRITE OUTPUT TAPE 6, 20
      WRITE OUTPUT TAPE 6, 18
      GO TO 539
530 WRITE OUTPUT TAPE 6, 20
      WRITE OUTPUT TAPE 6, 962
      GO TO 539
532 WRITE OUTPUT TAPE 6, 939
      WRITE OUTPUT TAPE 6, 19

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539 IOUT=IOUT+1
      CALL STRESS ( I,J,K1)
540 CONTINUE
      IF (MFLAG) 999, 544, 541
541 MFLAG=0
      GO TO 521
544 WRITE OUTPUT TAPE 6, 1, RECORD
      I0=0
      I1=1
      I2=4
      WRITE OUTPUT TAPE 6, 936
      I=1
      DO 560 JJ=1, NR1
      J=NR1+I-JJ
      550 WRITE OUTPUT TAPE 6, 937, J, I, (YK(I3), I3=11, 12)
      I1=I1+4
      I2=I1+3
      IF (I-NCOL) 551, 552, 560
      551 I=I+1
      GO TO 550
552 I=NC1
      WRITE OUTPUT TAPE 6, 937, J, NC1, (YK(I3), I3=11, 12)
      K1=8*(NC1+NR1)-3
      WRITE OUTPUT TAPE 6, 938, J, NC1, YK(K1)
      I1=I1+4
      I2=I1+3
      GO TO 550
560 CONTINUE
      IF (IOPT2) 566, 566, 562
      562 WRITE OUTPUT TAPE 6, 937, IO, NC1, (YK(I3), I3=11, 12)
      K1=K1+4
      WRITE OUTPUT TAPE 6, 938, IO, NC1, YK(K1)
      I1=I1+4
      I2=I1+3
      IF (IOPT2) 566, 566, 564
      564 CONTINUE
      DO 565 II=1, NC1
      I=NC1+1-II
      WRITE OUTPUT TAPE 6, 937, IO, I, (YK(I3), I3=11, 12)

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I1=I1+4          S1P03860
I2=I1+3          S1P03870
565 CONTINUE      S1P03880
566 IF(IOPT3) 999,999,545
545 MFLAG=-1      S1P03890
      XM=0.          S1P03900
      GO TO 521      S1P03910
      999 CONTINUE    S1P03920
      80 CALL CLOCK (TIM2)
      TIME=TIM2-TIM1   S1P03930
      TIM1=TIM2         S1P03940
      PRINT 945, KTIME, TIME   S1P03950
      WRITE OUTPUT TAPE 6, 945, KTIME, TIME
      IF (MM(31)) 1000, 1000, 601   S1P03960
      601 CALL CHAIN (2, 2)       S1P04000
      1000 CALL RESET        S1P04010
      GO TO 21           S1P04020
      END               S1P04030
*      FORTRAN
      SUBROUTINE ADDM (X, Y, Z, M)
      DIMENSION X(3600), Y(3600), Z(3600)
      IF (M) 20,1,1
      1 DO 10 I=1,M
      10 Z(I)=X(I)+Y(I)
      11 GO TO 50
      20 M=-M
      DO 25 I=1,M
      25 Z(I)=X(I)-Y(I)
      50 RETURN
      END
*      FORTRAN
      SUBROUTINE BOUND
      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
      COMMON NCF
      COMMON NDIM, NROW, NCOL, MM, I1, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
      COMMON ISWI, ISW2, ISW3
      COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
      COMMON R, B1, B2, B3, B4, B5, B6, P7, R8, R9, B10
      COMMON C, C1, C2, C3, C4, C5, C6, C7, C8, C9, C10, C11, C12, C13, C14,

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```

1 C15, C16, C17, C18, C19
COMMON FILL
COMMON TMP, YK, YL
DIMENSION FILL(1188)
DIMENSION TMP(5184), YK(5184), YL(5184)
DIMENSION MM(35)
DIMENSION NN(3)
I1=0
NR1=NRROW+1
NC1=NCOL+1
L=0
ITOT=3*(NRROW+6)
L1=ITOT
CALL GRADE(1)
LL=KP2
CALL GRADE(NROW)
LL2=KM2
DO 460 I=1, NCOL
TP=TMP(L+15)
TP2=TMP(L1-12)
N1=L1
DO 458 K=3, 5
N=K+L
CALL EXTRA(TMP( N), TMP( N+3), TMP( N+6), TMP( N+9), TP)
CALL EXTRA(TMP(N1), TMP(N1-3), TMP(N1-6), TMP(N1-9), TP2)
N1=K+L1-8
TP=TMP(N+13)
TP2=TMP(N1-12)
IF (LL) 453, 454, 454
453 TP=(TP+TMP(N+10))*5
454 IF (LL2) 458, 458, 456
456 TP2=(TP2+TMP(N1-9))*5
458 CONTINUE
L=L+ITOT
L1=L1+ITOT
460 CONTINUE
NN(1)=NC1*ITOT+7
NN(2)=NN(1)+1
NN(3)=NN(2)+ITOT+1

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```

DO 515 J=1, NROW
DO 510 K=1, 3
N=NN(K)+3*J
N1=N-ITOT
N2=N1-ITOT
N3=N2-ITOT
N4=N3-ITOT
CALL EXTRA ( TMP(N), TMP(N1), TMP(N2), TMP(N3), TMP(N4) )
510 CONTINUE
515 CONTINUE
L=NC1*ITOT
L1=L+4
LL=L1-2*ITOT
TMP(LL)=(TMP(LL)+TMP(LL+6))/2.
TMP(LL+1)=(TMP(LL+1)+TMP(LL+7))/2.
L1=L+ITOT-5
LL=L1-2*ITOT
TMP(LL)=(TMP(LL)+TMP(LL-6))/2.
TMP(LL+1)=(TMP(LL+1)+TMP(LL-5))/2.
RETURN
END
* FORTRAN
LIST
*
SUBROUTINE CF(I, J, MF, K, AA, X)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, I1, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A
COMMON TMP, YK, YL
DIMENSION MM(35)
DIMENSION A(1232)
DIMENSION AA(1)
DIMENSION X(72, 72)
DIMENSION TMP(5184), YK(5184), YL(5184)
C COMPUTE COEFFICIENT OF KTH UNKNOWN FOR MESH PT I,J.
I2=I
J2=J
M=MF

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J4 = ISW1*NCF+1
NC1=NCOL+1
NR1=NRROW+1
IF (ISW2) 107, 108, 106
106 J4=1
      GO TO 108
107 FCTR=-1.
      GO TO 109
108 FCTR=1.
      109 IF (M) 110, 100, 120.
      110 IF (M+1) 111, 112, 112
      111 J2=J2-1
      M=0
      GO TO 100
112 FCTR=FCTR/2.
      113 J5=J2-1
      GO TO 101
114 120 IF (M-1) 122, 122, 121
      121 J2=J2+1
      M=0
      GO TO 100
122 FCTR=FCTR/2.
      123 J5=J2+1
      100 CONTINUE
      101 1F (I2-1) 2, 4, 6
      C   COL I2 IS LEFT OF X-AXIS. REFLECT OVER SYMMETRY LINE. CHANGE SIGN
      C   1F K=2
      2 12=-I2+2
      1F (K-2) 6, 3, 6
      3 FCTR=-FCTR
      GO TO 6
      C   COL I2 IS X-AXIS. OMIT COEFFICIENT IF K=2
      4 1F (K-2) 6, 99, 6
      6 1F (J2-NR1) 14, 99, 7
      7 1F (J2-NR1-1) 8, 8, 11
      8 1F (K-2) 11, 11, 9
      9 1F (I2-NC1) 10, 99, 11
      C   COL J2 IS BEYOND THE BOUNDARY. K=3. SET J2=NRW-1

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10 J2=J2-2
11 GO TO 50
12 IF (I2-NC1) 80, 99, 13
13 I2=NC1
14 GO TO 80
15 IF (J2-1) 16, 18, 25
16 J2=-J2+2
17 IF (K-1) 17, 17, 25
18 FCTR=-FCTR
19 GO TO 25
20 IF (K-1) 99, 99, 25
21 IF (J2) 20, 99, 25
22 IF (J2+1) 24, 21, 21
23 IF (K-2) 24, 24, 22
24 IF (I2-NC1) 23, 99, 24
25 J2=1
26 GO TO 50
27 IF (I2-NC1-1) 27, 27, 13
28 I2=I2-2
29 J1=INDX(I2, J2, K)
30 IF (MFLAG) 51, 51, 52
31 X(I1, J1)=X(I1, J1)+AA(J4)*FCTR
32 IF (M) 130, 99, 130
33 YK(I1+2970)=YK(I1+2970)-AA(J4)*FCTR*TMP(J1)
34 GO TO 125
35 IF (J1+5-I1)*270+I1
36 YK(J3)=YK(J3)+AA(J4)*FCTR
37 IF (M) 135, 99, 135
38 RETURN
39 J2=J5
40 M=0
41 GO TO 50
42 J2=J5
43 S1P05410
44 S1P05420
45 S1P05430
46 S1P05440
47 S1P05450
48 S1P05460
49 S1P05470
50 S1P05480
51 S1P05490
52 S1P05500
53 S1P05510
54 S1P05520
55 S1P05530
56 S1P05540
57 S1P05550
58 S1P05560
59 S1P05570
60 S1P05580
61 S1P05590
62 S1P05600
63 S1P05610
64 S1P05620
65 S1P05630
66 S1P05640
67 S1P05650
68 S1P05660
69 S1P05670
70 S1P05680
71 S1P05690
72 S1P05700
73 S1P05710
74 S1P05720
75 S1P05730
76 S1P05740
77 S1P05750
78 S1P05760
79 S1P05770
80 S1P05780
81 S1P05790
82 S1P05800

```

```

M=0
GO TO 80
END
*      FORTRAN
      FUNCTION CFZ( J, AA)
      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
      COMMON NCF
      COMMON NDIM, NROW, NCOL, MM, MFLAG, XM, XLD
      DIMENSION MM(40), AA(1)
      J1 = J*NCF+1
      CFZ=AA(J1)
      RETURN
END
*      FORTRAN
      SUBROUTINE COEFZ
      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
      COMMON NCF
      COMMON ISW1, ISW2, ISW3
      COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
      COMMON B, B1, B2, B3, B4, B5, B6, B7, B8, B9, B10
      COMMON C, C1, C2, C3, C4, C5, C6, C7, C8, C9, C10, C11, C12, C13, C14,
1     C15, C16, C17, C18, C19
      COMMON FILL
      COMMON TMP, YK, YL
      COMMON T1, T2, XX, XX1, Z, Z1, Z2
      COMMON ZNU, THC, PH1, FF, RH, DD, XXH, XK
      DIMENSION TMP(5184), YK(5184), YL(5184)
      DIMENSION T1(89), T2(89), XX(89), XX1(89), Z(89), Z1(89), Z2(89)
      DIMENSION MM(40)
      DIMENSION A(1)
      DIMENSION FILL(1188)
      NRI=NROW+1
      D1 = (1.-ZNU)
      D2 = (1.+ZNU)
      D3 = (1.+DD)
      D4 = (1.+4.*DD)
      D5 = (2.-ZNU)
      D6 = (3.-ZNU)
S1P05810
S1P05820
S1P05830
S1P05840
S1P05850
S1P05860
S1P05870
S1P05880
S1P05890
S1P05900
S1P05910
S1P05920
S1P05930
S1P05940
S1P05950
S1P05960
S1P05970
S1P05980
S1P05990
S1P06000
S1P06010
S1P06020
S1P06030
S1P06040
S1P06050
S1P06060
S1P06070
S1P06080
S1P06090
S1P06100
S1P06110
S1P06120
S1P06130
S1P06140
S1P06150
S1P06160
S1P06170
S1P06180
S1P06190

```

```

D7 = (3.-2.*ZN(J)
YA5 = D2/2. + D5*D6
YA66 = D6/2. + D7*D10
YR10 = D2 -2.*D1*D10
DO 60 JJ = 0,NR1
      J = NR1 -JJ
      IF (J) 55,55, 54
  54 XH = XXH/(2.*MM(J))
  55 X = YK(J)
      SX = SINF(X)
      CX = COSF(X)
      YA1 = D3*SX
      YA2 = D1*D4/(2.*SX)
      YA3 = D3*CX
      YA4 = -D3*(CX*CX + ZNU*SX*SX)/SX
      YA6 = -YA66*CX/SX
      YA7 = -DD*SX
      YA8 = -D5*DD/SX
      YA9 = -DD*CX
      YA10 = D6*DD*CX/(SX*SX)
      YA11 = (D2*SX - DD *YA4/D3)
      YB3 = D1*D4*SX/2.
      YB4 = D3/SX
      YB5 = D1*D4*CX/2.
      YB6 = YA2*(2.*SX*SX- 1.)
      YB7 = -D5*DD
      YR8 = -DD/(SX*SX)
      YR9 = -DD*CX/SX
      YC2 = D5/SX
      YC3 = 2.*CX
      YC4 = CX/(SX*SX)
      YC5 = -( (1.+ZNU*SX*SX)/SX + D2*SX/DD )
      YC6 = (D1-D2/DD + 1./(SX*SX))*CX
      YC8 = 1./(SX*SX)
      YC9 = -CX/SX
      YC10 = (2.*D1 -D2/DD+ YC8)
      YC12 = -2./SX
      YC13 = -YC8/SX
      YC15 = 2.*CX*YC8
      S1P06200
      S1P06210
      S1P06220
      S1P06230
      S1P06240
      S1P06250
      S1P06260
      S1P06270
      S1P06280
      S1P06290
      S1P06300
      S1P06310
      S1P06320
      S1P06330
      S1P06340
      S1P06350
      S1P06360
      S1P06370
      S1P06380
      S1P06390
      S1P06400
      S1P06410
      S1P06420
      S1P06430
      S1P06440
      S1P06450
      S1P06460
      S1P06470
      S1P06480
      S1P06490
      S1P06500
      S1P06510
      S1P06520
      S1P06530
      S1P06540
      S1P06550
      S1P06560
      S1P06570
      S1P06580

```

```

YC16 = (1.+ZNU*SX*SX)/SX
YC17 = 4.*YC13 + D2/SX
YC18 = -(D1+YC8)*CX
YC19 = -2.*D2*SX/DD
XHH = XH*XH
XHHH = XHH*XH
XKK = XK*XK
XXXX = XKK*XK
XXXXX = XKKK*XK
A1 = YA1/XHH + YA3/(2.*XH)
A2 = YA1/XHH - YA3/(2.*XH)
A3 = YA2/XKK
A4 = -(A1+A2)-2.*A3 + YA4
A5 = YA5/(4.*XH*XK)
A6 = YA6/(2.*XK)
A7 = YA7/(2.*XHHH)
A10 = YA10/XKK
A11 = YA8/(2.*XH*XKK)
A13 = YA9/XHH
A14 = YA11/(2.*XH)
A8 = -2.*A7 -2.*A11 + A13 + A14
A9 = +2.*A7 +2.*A11 + A13 - A14
A17 = -2.*A13 -2.*A10
B1 = YA5/(4.*XH*XK)
B2 = -YA6/(2.*XK)
B3 = YB3/XHH + YB5/(2.*XH)
B4 = YB3/XHH - YB5/(2.*XH)
B5 = YR4/XKK
B6 = -B3-B4-2.*B5 + YB6
B7 = -YB7/( 2.*XHH*XK) -YB8/XKKK + YB10/(2.*XK)
B8 = YB7/( 2.*XHH*XK) + YB9/(4.*XH*XK)
B9=YB7/(2.*XHH*XK)-YR9/(4.*XH*XK)
B10 = YR8/(2.*XKKK)
C1 = SX/(2.*XHHH)
C4 = YC4/XKK
C5 = YC2/(2.*XH*XKK)
C10= YC8/(2.*XKKK)
C13 = YC13/XKKK

```

S1P06590  
S1P06600  
S1P06610  
S1P06620  
S1P06630  
S1P06640  
S1P06650  
S1P06660  
S1P06670  
S1P06680  
S1P06690  
S1P06700  
S1P06710  
S1P06720  
S1P06730  
S1P06740  
S1P06750  
S1P06760  
S1P06770  
S1P06780  
S1P06790  
S1P06800  
S1P06810  
S1P06820  
S1P06830  
S1P06840  
S1P06850  
S1P06860  
S1P06870  
S1P06880  
S1P06890  
S1P06900  
S1P06910  
S1P06920  
S1P06930  
S1P06940  
S1P06950  
S1P06960  
S1P06970

```

C2 = -2.*C1-2.*C5+YC3/XHHH+YC5/(2.*XH) S1P06980
C3 = +2.*C1+2.*C5+YC3/XHHH-YC5/(2.*XH) S1P06990
C6 = -2.*YC3/XHHH -2.*C4+YC6 S1P07000
C7=-D5/(XHH*XK)-2.*C10+YC10/(2.*XK) S1P07010
C8 = D5 /(2.*XHH*XK) + YC9/(4.*XH*XK) S1P07020
C9 = D5 /(2.*XHH*XK) - YC9/(4.*XH*XK) S1P07030
C11 = -SX/XHHHH - YC3/(2.*XHHH) S1P07040
C12 = -SX/XHHHH + YC3/(2.*XHHH) S1P07050
C14 = 4.*SX/XHHHH -2.*YC12/(XHH*XKK) + YC3/XHHH-YC15/(XH*XKK) S1P07060
1 + YC16/(XHH) + YC18/(2.*XH) S1P07070
C15 = 4.*SX/XHHHH-2.*YC12/(XHH*XKK) - YC3/XHHH + YC15/(XH*XKK) S1P07080
1 + YC16/XHH -YC18/(2.*XH) S1P07090
C16 = -2.*YC12/(XHH*XKK) -4.*YC13/XKKK + YC17/XKK S1P07100
C17 = YC12/(XHH*XKK) + YC15/(2.*XH*XKK) S1P07110
C18 = YC12/(XHH*XKK) -YC15/(2.*XH*XKK) S1P07120
C19 = -6.*SX/XHHHH + 4.*YC12/(XHH*XKK) +6.*YC13/XKKKK S1P07130
1 -2.*YC16/XHH -2.*YC17/XKK + YC19 S1P07140
A=1. S1P07150
C=1. S1P07160
CALL NORM(A1,A,12) S1P07170
CALL NORM(R1,R,10) S1P07180
CALL NORM(C1,C,19) S1P07190
DO 58 L=1,NCF S1P07200
L1 = J*NCF+L S1P07210
58 A(L1)=A(L) S1P07220
CONTINUE RRETURN S1P07230
END S1P07240
S1P07250
S1P07260
S1P07270
S1P07280
S1P07290
S1P07300
S1P07310
S1P07320
S1P07330
S1P07340
S1P07350
S1P07360
* FORTRAN
SUBROUTINE CONS (X, I)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCOL, MM, MFLAG, XM, XLD
COMMON NSW1, NSW2, NSW3
COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
COMMON B, B1, B2, B3, B4, B5, B6, B7, B8, B9, B10
COMMON C, C1, C2, C3, C4, C5, C6, C7, C8, C9, C10, C11, C12, C13, C14,
1 C15, C16, C17, C18, C19
COMMON FILL

```

```

COMMON TMP, YK, YL
COMMON T1, T2, XX, XX1, Z, Z1, Z2
COMMON ZNU, THC, PH1, FF, RH, DD, XH, XK
COMMON ZETA
COMMON TE, TI, TO, OC, TC, TD, DDLD
DIMENSION TMP (5184), YK(5184), YL(5184)
DIMENSION ZETA (30)
DIMENSION T1( 89), T2(89), XX(89), XX1(89), Z(89), Z1(89), Z2(89)
DIMENSION MM(40)
DIMENSION X(72), A(1), B(1), C(1)
DIMENSION FILL(1188)
3 DO 5 J=1, NDIM
5 X(J)=0.
IF (IOPT4-1) 6, 21, 21
6 DO 10 J=1, NROW
   I1=INDX (1, J, 3)
   J4 = J*NCF+1
10 X(I1) = C(J4) * (ZNU**2-1.) * SINF(ZETA(J+1)) / DD
   GO TO 85
21 CONTINUE
   DO 31 J = 1, NROW
      J4 = J*NCF+1
      I1 = INDX (1, J, 3)
      X(I1) = C(J4) * SINF(ZETA(J+1)) * TC / DD
31 CONTINUE
QQ RETURN
END
*
```

```

FORTRAN
FUNCTION DEF (IT, JJ, KK, MF)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NRW, NCOL, MM, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A
COMMON TMP, YK, YL
DIMENSION MM(40)
DIMENSION A(1232)
DIMENSION TMP (5184), YK(5184), YL(5184)
ND=3*(NROW+6)
S1P07370
S1P07380
S1P07390
S1P07400
S1P07410
S1P07420
S1P07430
S1P07440
S1P07450
S1P07460
S1P07470
S1P07480
S1P07490
S1P07500
S1P07510
S1P07520
S1P07530
S1P07540
S1P07550
S1P07560
S1P07570
S1P07580
S1P07590
S1P07600
S1P07610
S1P07620
S1P07630
S1P07640
S1P07650
S1P07660
S1P07670
S1P07680
S1P07690
S1P07700
S1P07710
S1P07720
S1P07730
S1P07740
S1P07750

```

```

I=II
J=JJ
K=KK
M=MF
IF (M) 60, 50, 70
60 IF (M+1) 61, 62, 62
61 J=J-1
M=0
GO TO 50
62 J2=J-1
GO TO 50
70 IF (M-1) 72, 72, 71
71 J=J+1
M=0
GO TO 50
72 J2=J+1
50 SIGN=1.
IF (I-1) 1, 3, 3
1 I=2-I
IF (K-2) 3, 2, 3
2 SIGN=-1.
GO TO 5
3 IF (J-1) 4, 5, 5
4 IF (NOT2) 6, 6, 5
6 J=2-J
IF (K-1) 2, 2, 5
5 I2=(I-1)*N2+3*N2+J+K+6
IF (M) 16, 13, 16
13 IF (SIGN) 14, 15, 15
14 DEF=-TMP(I2)
GO TO 99
15 DEF=TMP(I2)
GO TO 99
16 I3=(I-1)*N2+3*N2+J2+K+6
DEF=SIGN*(TMP(I2)+TMP(I3))/2.

```

QQ RETURN  
END

\*  
FORTRAN  
SUBROUTINE EQ1 (X, III, II, JJ, MX)

```

S1P07760
S1P07770
S1P07780
S1P07790
S1P07800
S1P07810
S1P07820
S1P07830
S1P07840
S1P07850
S1P07860
S1P07870
S1P07880
S1P07890
S1P07900
S1P07910
S1P07920
S1P07930
S1P07940
S1P07950
S1P07960
S1P07970
S1P07980
S1P07990
S1P08000
S1P08010
S1P08020
S1P08030
S1P08040
S1P08050
S1P08060
S1P08070
S1P08080
S1P08090
S1P08100
S1P08110
S1P08120
S1P08130
S1P08140

```

```

C COMPUTE COEFFICIENTS FOR EQUATION ONE FOR MESH PT I,J
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, KO, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
DIMENSION MM(35)
I1=111
I=11
J=JJ
M=MX
GO TO (30, 20, 30, 40, 50), M
20 CONTINUE
MF=0
ISW2=0
CALL CF (I-1, J, MF, 1, A3, X)
CALL CF(I-1,J ,MF,3,A10,X)
ISW2=-1
CALL CF (I-1, J, MF, 2, A6, X)
MF=KM1
CALL CF (I-1, J-1, MF, 2, A5,X)
ISW2=0
CALL CF(I-1,J-1,MF,3,A11,X)
MF=KP1
CALL CF (I-1, J+1, MF, 2, A5,X)
ISW2 = -1
CALL CF(I-1,J+1,MF,3,A11,X)
GO TO 50
30 CONTINUE
ISW2=0
MF=0
CALL CF (I, J, MF, 1, A4,X)
CALL CF(I ,J ,MF,3,A12,X)
MF=KM1
CALL CF (I, J-1, MF, 1, A1, X)
CALL CF(I ,J-1,MF,3,A8 ,X)
MF=KP1
CALL CF (I, J+1, MF, 1, A2, X)
CALL CF(I ,J+1,MF,3,A9 ,X)

```

```

MF = KM2
CALL CF(I,J-2,MF,3,A7,X)
MF = KP2
ISW2 = -1
CALL CF(I,J+2,MF,3,A7,X)
IF (MFLAG) 50, 50, 40
40 CONTINUE
MF=0
ISW2=0
CALL CF(I+1,J,MF,1,A3,X)
CALL CF(I+1,J,MF,2,A6,X)
CALL CF(I+1,J,MF,3,A10,X)
MF=KM1
CALL CF(I+1,J-1,MF,2,A5,X)
CALL CF(I+1,J-1,MF,3,A11,X)
MF=KP1
ISW2=-1
CALL CF(I+1,J+1,MF,2,A5,X)
CALL CF(I+1,J+1,MF,3,A11,X)
ISW2 = 0
45 IF (I-1) 20, 20, 46
46 IF (MFLAG) 50, 50, 20
50 RETURN
END
* FORTRAN
C SUBROUTINE FQ2 (X, I11, J1, JJ, MX)
C COMPUTE EQUATION TWO FOR MESH PT I, J.
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, KO, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
COMMON R, R1, R2, R3, R4, R5, B6, B7, B8, B9, B10
DIMENSION MM(35)
I1=I11
I=II
J=JJ
M=MX
GO TO (30, 20, 30, 40, 50), M

```

20 CONTINUE

ISW2=0

MF=0

CALL CF ( I-1, J, MF, 2, B5, X)

ISW2=-1

CALL CF ( I-1, J, MF, 1, B2, X)

CALL CF ( I-1, J, MF, 3, B7, X)

MF=KM1

CALL CF ( I-1, J-1, MF, 1, B1, X)

CALL CF ( I-1, J-1, MF, 3, B8, X)

MF=KP1

CALL CF ( I-1, J+1, MF, 3, B9, X)

ISW2=0

CALL CF ( I-1, J+1, MF, 1, B1, X)

GO TO 50

30 CONTINUE

ISW2=0

MF=KM1

CALL CF ( I, J-1, MF, 2, B3, X)

MF=KP1

CALL CF ( I, J+1, MF, 2, B4, X)

MF=0

CALL CF ( I, J, MF, 2, B6, X)

33 IF (MFLAG) 34, 34, 35

34 IF (I-2) 50, 35, 36

35 CONTINUE

ISW2=-1

CALL CF ( I-2, J, MF, 3, B10, X)

IF (MFLAG) 50, 50, 37

36 IF (I-NCOL) 50, 37, 37

37 CONTINUE

ISW2=0

CALL CF ( I+2, J, MF, 3, B10, X)

IF (MFLAG) 50, 50, 40

40 CONTINUE

ISW2=0

MF=0

CALL CF ( I+1, J, MF, 1, B2, X)

CALL CF ( I+1, J, MF, 2, B5, X)

S1P08930  
S1P08940  
S1P08950

S1P08960  
S1P08970  
S1P08980

S1P08990  
S1P09000  
S1P09010

S1P09020  
S1P09030  
S1P09040

S1P09050  
S1P09060  
S1P09070

S1P09080  
S1P09090  
S1P09100

S1P09110  
S1P09120  
S1P09130

S1P09140  
S1P09150  
S1P09160

S1P09170  
S1P09180

S1P09190  
S1P09200  
S1P09210

S1P09220  
S1P09230  
S1P09240

S1P09250  
S1P09260  
S1P09270  
S1P09280

S1P09290  
S1P09300  
S1P09310

```

CALL CF ( I+1, J, MF, 3, B7, X)           S1P09320
MF=KM1                                     S1P09330
CALL CF ( I+1, J-1, MF, 1, B1, X)           S1P09340
CALL CF ( I+1, J-1, MF, 3, B8, X)           S1P09350
MF=KP1                                     S1P09360
CALL CF ( I+1, J+1, MF, 3, B9, X)           S1P09370
ISW2=-1                                    S1P09380
CALL CF ( I+1, J+1, MF, 1, B1, X)           S1P09390
45 IF (I-1) .gt. 20, 20, 46                 S1P09400
46 IF (MFLAG) 50, 50, 20
50 RETURN
END                                         S1P09420
                                             S1P09430
*                                              S1P09440
      SUBROUTINE EQ3 (X, III, JJ, MX)
      COMPUTE EQUATION THREE FOR MESH PT I,J.
      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8   S1P09460
      COMMON NCF
      COMMON NDIM, NROW, NCOL, MM, KO, KM1, KM2, KP1, KP2, MFLAG, XM, XLD   S1P09480
      COMMON ISW1, ISW2, ISW3
      COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12   S1P09510
      COMMON R, R1, R2, R3, R4, R5, R6, R7, R8, R9, R10
      COMMON C, C1, C2, C3, C4, C5, C6, C7, C8, C9, C10, C11, C12, C13, C14, C15, C16, C17, C18, C19
      1 DIMENSION MM(35)
      I1=II
      I=II
      J=JJ
      M=MX
      GO TO (30, 20, 30, 40, 50), M
20 CONTINUE
      ISW2=0
      MF=0
      CALL CF (I-1,J, MF, 1, C4, X)
      CALL CF (I-1,J, MF, 3, C16, X)
      ISW2=-1
      CALL CF (I-1,J, MF, 2, C7, X)
      MF=KP1
      CALL CF (I-1,J+1, MF, 1, C5, X)
      CALL CF (I-1,J+1, MF, 2, C9, X)

```

ISW2=0  
CALL CF(I-1,J+1,MF,3,C18,X)

MF=KM1

CALL CF(I-1,J-1,MF,1,C5,X)  
CALL CF(I-1,J-1,MF,3,C17,X)

ISW2 = -1

CALL CF(I-1,J-1,MF,2,C8,X)  
IF (I-1) 21, 21, 22

ISW2=1

CX=CFZ(J, C10)  
CALL CF(I-1, J, 0,2, -4.\*CX, X)  
GO TO 50

22 IF (I-NCOL) 50, 24, 24

ISW2=1

CX=CFZ(J, C10)  
CALL CF(I-1, J, 0, 2, 4.\*CX, X)  
GO TO 50

30 CONTINUE

ISW2=0

MF=KM1  
CALL CF(I ,J-1,MF,1,C2,X)  
CALL CF(I ,J-1,MF,3,C14,X)

MF=KP1

CALL CF(I ,J+1,MF,1,C3,X)  
CALL CF(I ,J+1,MF,3,C15,X)

MF=KM2

CALL CF(I ,J-2,MF,3,C11,X)  
ISW2=0

MF=KP2

CALL CF(I ,J+2,MF,3,C12,X)  
MF=0

CALL CF(I ,J ,MF,1,C6,X)  
CALL CF(I ,J ,MF,3,C19,X)

IF (J-NROW) 32, 31, 31

ISW2=1

CX=CFZ(J,C1)  
CALL CF(I ,J+1, KP1, 1, -4.\*CX,X)  
CALL CF(I ,J , 0, 1, 6.\*CX,X)  
CALL CF(I ,J-1, KM1, 1, -4.\*CX,X)

S1P09710  
S1P09720

S1P09730

S1P09740

S1P09750

S1P09760

S1P09770

S1P09780

S1P09790

S1P09800

S1P09810

S1P09820

S1P09830

S1P09840

S1P09850

S1P09860

S1P09870

S1P09880

S1P09890

S1P09900

S1P09910

S1P09920

S1P09930

S1P09940

S1P09950

S1P09960

S1P09970

S1P09980

S1P09990

S1P10000

S1P10010

S1P10020

S1P10030

S1P10040

S1P10050

S1P10060

S1P10070

S1P10080

S1P10090

```

CALL CF (I, J-2, KM2, 1, 2.*CX, X) S1P10100
GO TO 36 S1P10110
32 IF (J-1) 33, 33, 34 S1P10120
33 ISW2=1 S1P10130
      CX=CFZ(J,C1)
      CALL CF(I, J-1, KM1, 1, 4.*CX, X) S1P10140
      CALL CF(I, J, 0, 1, -6.*CX, X) S1P10150
      CALL CF(I, J+1, KP1, 1, 4.*CX, X) S1P10160
      CALL CF(I, J+2, KP2, 1, -2.*CX, X) S1P10170
      GO TO 36 S1P10180
34 CONTINUE S1P10190
      CALL CF (I, J-2, KM2, 1, C1, X) S1P10200
      ISW2=-1 S1P10210
      CALL CF (I, J+2, KP2, 1,C1, X) S1P10220
36 IF (I-2) 360, 361, 362 S1P10230
360 MP=MFLAG+1 S1P10240
      GO TO 365 S1P10250
361 MP=MFLAG+3 S1P10260
      GO TO 365 S1P10270
362 IF (I-NCOL) 363, 364, 364 S1P10280
363 MP=MFLAG+5 S1P10290
      GO TO 365 S1P10300
364 MP=MFLAG+7 S1P10310
365 GO TO (370, 366, 367, 366, 370, 366, 366), MP S1P10320
366 CONTINUE S1P10330
      MF=0 S1P10340
      ISW2 = 0 S1P10350
      CALL CF (I+2,J ,MF,3,C13,X) S1P10360
      IF (MFLAG) 370, 370, 367 S1P10370
367 CONTINUE S1P10380
      ISW2 = 0 S1P10390
      CALL CF (I-2,J ,MF,3,C13,X) S1P10400
370 GO TO (373, 372, 376, 375, 395, 375, 395, 382, 380), MP S1P10410
372 CONTINUE S1P10420
      ISW2=1 S1P10430
      CX=2.*CFZ(J, C10) S1P10440
      CALL CF (I+2,J, 0, 2, CX, X) S1P10450
373 CONTINUE S1P10460
      ISW2=1 S1P10470
S1P10480

```

```

CX=CFZ(J, C10)
CALL CF(I,J,0, 2, 6.*CX, X)
GO TO 395
375 CONTINUE
ISW2=0
CALL CF(I+2, J, 0, ? , C10, X)
376 CONTINUE
ISW2=-1
GO TO 395
380 CONTINUE
ISW2=1
CX=-2.*CFZ(J, C10)
CALL CF(I-2, J, 0, 2, CX, X)
382 CONTINUE
390 ISW2=1
CX=CFZ(J, C10)
CALL CF(I,J, 0, 2,-6.*CX, X)
395 CONTINUE
IF (MFLAG) 50, 50, 40
40 CONTINUE
MF=0
ISW2=0
CALL CF(I+1,J ,MF,3,C16,X)
CALL CF(I+1,J ,MF,2,C7 ,X)
CALL CF(I+1,J ,MF,1,C4 ,X)
MF=KM1
CALL CF(I+1,J-1,MF,2,C8 ,X)
CALL CF(I+1,J-1,MF,1,C5 ,X)
CALL CF(I+1,J-1,MF,3,C17,X)
MF=KP1
ISW2 = -1
CALL CF(I+1,J+1,MF,1,C5 ,X)
ISW2 = 0
CALL CF(I+1,J+1,MF,2,C9 ,X)
CALL CF(I+1,J+1,MF,3,C18,X)
IF (I-NCOL) 42, 41, 41
41 ISW2=1
CX=-4.*CFZ(J, C10)

```

S1P10490  
S1P10500  
S1P10510  
S1P10520  
S1P10530  
S1P10540  
S1P10550  
S1P10560  
S1P10570  
S1P10580  
S1P10590  
S1P10600  
S1P10610  
S1P10620  
S1P10630  
S1P10640  
S1P10650  
S1P10660  
S1P10670  
S1P10680  
S1P10690  
S1P10700  
S1P10710  
S1P10720  
S1P10730  
S1P10740  
S1P10750  
S1P10760  
S1P10770  
S1P10780  
S1P10790  
S1P10800  
S1P10810  
S1P10820  
S1P10830  
S1P10840  
S1P10850  
S1P10860  
S1P10870

```

GO TO 44
42 IF (I-1) 43,43, 45
43 ISW2=1
44 CX=4.*CFZ( J, C10)
45 CALL CF (I+1,J, 0, 2, CX, X)
45 IF (I-1) 20, 20, 46
46 IF (MFLAG) 50, 50, 20
50 RETURN
END
*   FORTRAN
SUBROUTINE EXTRA (X, X1, X2, X3, X4)
X=4.*X1-6.*X2+4.*X3-X4
RETURN
END
*   FORTRAN
SUBROUTINE GRADE (J)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW,NCOL,MM,KO,KM1,KM2,KP1,KP2,MFLAG,XM,XLD
DIMENSION MM(35)
DO 2 I=37, 40
2 MM(I)=0
1 IF (J) 99, 99, 1
JM=MM(J)
JM1=MM(J-1)
JM2= MM(J-2)
JP1= MM(J+1)
JP2= MM(J+2)
IF (J-2) 10, 10, 4
4 IF (J-NROW+1) 5, 30, 30
5 IF (JP2-JM2) 10, 20, 30
C      MESH SPACING INCREASING
10 IF (JP1-JM) 11, 12, 12
C      DOUBLE MESH SPACING AFTER THIS ROW
11 KP1=-1
KP2=-2
1 IF (J-1) 40, 40, 99
12 IF (JP2-JP1) 14, 18, 18
14 KD2=-1
S1P10880
S1P10890
S1P10900
S1P10910
S1P10920
S1P10930
S1P10940
S1P10950
S1P10960
S1P10970
S1P10980
S1P10990
S1P11000
S1P11010
S1P11020
S1P11030
S1P11040
S1P11050
S1P11060
S1P11070
S1P11080
S1P11090
S1P11100
S1P11110
S1P11120
S1P11130
S1P11140
S1P11150
S1P11160
S1P11170
S1P11180
S1P11190
S1P11200
S1P11210
S1P11220
S1P11230
S1P11240
S1P11250
S1P11260

```

```

      IF (J-2) 40, 15, 15
15 IF (JM-JM1) 16, 99, 99
C   MESH SPACING CHANGES IN BOTH DIRECTIONS
16 KM2=-2
    GO TO 40
18 IF (J-2) 40, 20, 13
13 IF (JM-JM1) 19, 20, 20
C   DOUBLE THE MESH SPACING
19 KM2=-2
    GO TO 40
20 GO TO 99
C   MESH SPACING IS DECREASING
30 IF (JM-JM1) 32, 32, 31
C   CUT MESH SPACING IN HALF
31 KM1=1
KM2=2
    GO TO 40
32 IF (JM1-JM2) 37, 37, 33
33 IF (J-NROW+1) 35, 34, 34
C   MESH SPACING AT LAST ROW WAS CUT IN HALF
34 KM2=1
    GO TO 99
35 IF (JP1-JM) 34, 34, 36
C   SPACING CHANGES IN BOTH DIRECTIONS
36 KM2=1
KP2=2
    GO TO 99
37 IF (J-NROW+1) 38, 20, 20
38 IF (JP1-JM) 20, 20, 39
C   MESH CUT IN HALF AFTER NEXT ROW
39 KP2=2
    GO TO 99
40 CONTINUE
99 RETURN
END
*   FORTRAN
      FUNCTION INDEX(II, JJ, KK)
      COMMON IOPT1, IOPT2, INPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
      COMMON NCF
      S1P11270
      S1P11280
      S1P11290
      S1P11300
      S1P11310
      S1P11320
      S1P11330
      S1P11340
      S1P11350
      S1P11360
      S1P11370
      S1P11380
      S1P11390
      S1P11400
      S1P11410
      S1P11420
      S1P11430
      S1P11440
      S1P11450
      S1P11460
      S1P11470
      S1P11480
      S1P11490
      S1P11500
      S1P11510
      S1P11520
      S1P11530
      S1P11540
      S1P11550
      S1P11560
      S1P11570
      S1P11580
      S1P11590
      S1P11600
      S1P11610
      S1P11620
      S1P11630
      S1P11640
      S1P11650

```

COMMON NDIM, NROW, NCOL, MM, MFLAG, XM, XLD  
 DIMENSION MM(40)

I=11

J=JJ

K=KK

IF (MFLAG) 100, 100, 200

100 CONTINUE

IF (IOPT2) 10, 10, 20

10 IF (I-1) 1, 1, 5

1 IF (K-1) 2, 2, 3

2 INDEX=(J-1)\*2

GO TO 50

3 INDEX= J\*2-1

GO TO 50

5 INDEX= 3\*K-4

GO TO 50

20 IF (I-1) 21, 21, 29

21 IF (K-1) 22, 22, 24

22 INDEX=J\*2-1

GO TO 50

24 INDEX=J\*2

GO TO 50

29 INDEX=3\*K-3

GO TO 50

200 IF (I-NCOL) 201, 201, 220

201 IF (J-NROW) 202, 202, 210

202 IF (J) 230, 230, 205

205 INDEX= (I-1)\*(NROW+6)\*3+3\*K+6  
 GO TO 50

210 IF (IOPT2) 211, 211, 216

211 INDEX=3\*(NROW+NCOL-I)+2+K

212 IF (I-1) 214, 214, 50

214 IF (K-3) 50, 215, 215

215 INDEX=INDEX-1

GO TO 50

216 INDEX=3\*(NROW+NCOL+NCOL-I)+K+5

GO TO 212

220 INDEX=3\*K-4

IF (IOPT2) 50, 50, 221

S1P11660

S1P11670

S1P11680

S1P11690

S1P11700

S1P11710

S1P11720

S1P11730

S1P11740

S1P11750

S1P11760

S1P11770

S1P11780

S1P11790

S1P11800

S1P11810

S1P11820

S1P11830

S1P11840

S1P11850

S1P11860

S1P11870

S1P11880

S1P11890

S1P11900

S1P11910

S1P11920

S1P11930

S1P11940

S1P11950

S1P11960

S1P11970

S1P11980

S1P11990

S1P12000

S1P12010

S1P12020

S1P12030

S1P12040

```

221 INDEX=INDEX+3*NCOL+3
      GO TO 50
230 INDEX=3*I+K-4
      IF (I-1) 231, 231, 50
231 IF (K-1) 232, 232, 50
232 INDEX=INDEX+1
      50 RETURN
END
*
FORTRAN
SUBROUTINE MTX (X, I, M)
COMMON ICPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, I1, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
DIMENSION MM(35)
DIMENSION X(72, 72)
I1=0
DO 1 I1=1, NDIM
DO 1 J1=1, NDIM
1 X(I1, J1)=0.
DO 100 J=1, NROW
ISW1=J
IF (XM) 50, 50, 7
7 CALL GRADE (J)
50 IF (J-1) 57, 57, 58
57 IF (IOPT2) 59, 59, 58
58 I1=I1+1
CALL EQ1 (X, I1, I, J, M)
59 IF (I-1) 61, 61, 60
60 I1=I1+1
CALL EQ2 (X, I1, I, J, M)
61 I1=I1+1
CALL EQ3 (X, I1, I, J, M)
100 CONTINUE
      RETURN
END
FORTRAN
LIST
*
```

```

SUBROUTINE MTXS (X, Y, II, M)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A, A1, A2, A3, A4, A5, A6, A7, A8, A9, A10, A11, A12
COMMON B, B1, B2, B3, B4, B5, B6, B7, B8, B9, B10
COMMON C, C1, C2, C3, C4, C5, C6, C7, C8, C9, C10, C11, C12, C13, C14,
C15, C16, C17, C18, C19
COMMON FIL
COMMON FILL
DIMENSION MM(40)
C      MULTIPLICATION BY A SINGLE DIAGONAL
DIMENSION X(72, 72), Y(72, 72)

I=11
  3 IF (M-1) 20, 100, 100
    C CLEAR OUT Y
  20 DO 23 J=1, NDIM
  23 Y(J,1)=0.

L1=1
  GO TO 2
100 L1=NDIM
  1F (M-1) 202,50
    C FORM A*X AND STORE IN Y
    2 DO 5 J=1,NROW
      6 CONTINUE
      7 I1=INDX (I, J, 2)
      12=I1+1
      J1=INDX (I-2, J, 3)
      J2=J1-1
      1F (I-3) 31, 31, 32
      31 CC=0.
      GO TO 33
      32 IF (I-NCOL) 322,321, 321
      321 CC=-2.*CFZ(J, C10)
      GO TO 32
      322 CC=-CFZ(J, C10)
      33 BR=CFZ(J, B10)
      CC2= CFZ (J, C13)
      DO 4 K=1, L1

```

```

Y(I1, K)=Y(I1, K)-X( J1, K)*BB
4 Y(I2, K)=Y(I2, K)+X( J2, K)*CC+X( J1, K)*CC2
5 CONTINUE
GO TO 99
C      FORM X*E AND STORE IN Y
      50 CONTINUE
      DO 60 J=1, NROW
      51 CONTINUE
      52 IF (I-1) 49, 40, 48
49 CC=2.*CFZ(J, C13)
      CC2=-2.*CFZ(J, C10)
      BR=0
      GO TO 57
48 CC= CFZ (J, C13)
      CC2=-CFZ (J, C10)
      BB= CFZ (J, B10)
      57 I2= INDX (I, J, 3)
      I1= I2-1
      J1= INDX (I+2, J, 2)
      J2=J1+1
      53 DO 54 K=1, L1
54 Y(K, J1)=Y(K, J1)-X(K, I2)*CC2
      55 DO 58 K=1, L1
58 Y(K, J2)= Y(K, J2)+X(K, I1)*BR+X(K, I2)*CC
      59 CONTINUE
      60 RETURN
99 END
*
      FORTRAN
      SUBROUTINE NORM (X, CONS, K)
      DIMENSION X(19), Y(19)
      DO 1 I=1,K
1 Y(I)=ABSF(X(I))
      DO 10 I=2,K
      1 IF (Y(I)-Y(I)) 2,10,10
2 TFMP=Y(1)
      Y(1)=Y(I)
      Y(I)=TEMP
      10 CONTINUE
      DO 20 I=1,K

```

```

20 X(I)=X(I)/Y          S1P13220
    CONS=CONS/Y        S1P13230
    RETURN             S1P13240
    END               S1P13250
    *                 S1P13260
    FORTRAN           S1P13270
    SUBROUTINE INVERT(A,IMAX,IISING) S1P13280
    C                 SUBROUTINE TO INVERT A MATRIX
    DIMENSION A(72, 72), IN(72), TEMP(72)
    IISING=0           S1P13290
    N=IMAX            S1P13300
    IMAX0=N-1         S1P13310
    I1=1              S1P13320
    IN(I1)=0           S1P13330
    SUM=ABSF(A(I1,I1)) S1P13340
    DO3I=I1,N          S1P13350
    IF(SUM-ABSF(A(I,I1)))2,3,3
    2   I3=I             S1P13360
    IN(I1)=I            S1P13370
    SUM=ABSF(A(I,I1)) S1P13380
    3   CONTINUE          S1P13390
    IF(I3-I1)4,6,4      S1P13400
    4   D05J=1,N          S1P13410
    SUM=A(I1,J)         S1P13420
    A(I1,J)=A(I3,J)    S1P13430
    5   A(I3,J)=SUM     S1P13440
    6   I3=I1+1          S1P13450
    IF(A(I1,I1))97,99,97 S1P13460
    97  D07I=I3,N        S1P13470
    7   A(I,I1)=A(I,I1)/A(I1,I1) S1P13480
    J2=I1-1             S1P13490
    IF(J2)8,11,8         S1P13500
    8   D09J=I3,N          S1P13510
    9   A(I1,J)=A(I1,J)-DPSUM(A,I1,J,1,J2) S1P13520
    11  J2=I1             S1P13530
    I1=I1+1             S1P13540
    DO12I=I1,N          S1P13550
    12  A(I,I1)=A(I,I1)-DPSUM(A,I,I1,1,J2) S1P13560
    IF(I1-N)1,14,1       S1P13570

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```

14 DO600JP=1,N
      J=N+1-JP
      A(I,J)=1.0/A(J,J)
      IF(J-1)603,700,603
603  DO600IP=2,J
      I=J+1-IP
      IPO=I+1
      SUM=-DPSUM (A,I,J,IPO,J)
      600  A(I,J)=SUM/A(I,I)
      700  DO151J=1,IMAXO
      JPO=J+1
      D0151I=JPO,N
      IMO=I-1
      SUM=-DPSUM (A,I,J,J+1,IMO)
      SUM=SUM-A(I,J)
151  A(I,J)=SUM
      D0901I=1,N
      D0900J=1,N
      IF (I-J) 897,897,898
      897  TEMP(J)=DPSUM(A,I,J,J+1,N)
      TEMP(J)=TEMP(J)+A(I,J)
      GO TO 900
      898  TEMP(J)=DPSUM(A,I,J,I,N)
      900  CONTINUE
      D0901J=1,N
      901  A(I,J)=TEMP(J)
      D0500I=2,N
      M=N+1-I
      IF(IN(M))502,500,502
502  ISS=IN(M)
      D0503L=1,N
      SUM=A(L,ISS)
      A(L,ISS)=A(L,M)
      503  A(L,M)=SUM
      500  CONTINUE
      GO TO 805
      99  ISING=1
      805  RETURN
      END

```

```

*   FORTRAN
      SUBROUTINE STORE (X, I1)
      COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
      COMMON NCF
      COMMON NDIM, NROW, NCOL, MM, MFLAG, XM, XLD
      COMMON ISW1, ISW2, ISW3
      COMMON A
      COMMON TMP, YK, YL
      DIMENSION TMP(5184), VK(5184), YL(5184)
      DIMENSION A(1232)
      DIMENSION X(59)
      DIMENSION MM(40)
      N2= (NROW+6)*3
      NC1=NCOL+1
      IF (MFLAG) 100, 100, 200
100  N1=(I1-1)*N2+10
      I2=0
      DO 110 J=1, NROW
      IF (J-1) 101, 101, 103
101  IF (IOPT2) 104, 104, 103
103  I2=I2+1
      TMP(N1)=X(I2)
104  IF (I1-1) 107, 107, 106
106  I2=I2+1
      TMP(N1+1)=X(I2)
107  I2=I2+1
      TMP(N1+2)=X(I2)
110  N1=N1+3
      GO TO 999
200  IF (IOPT2) 220, 220, 201
201  I2=11*270
      DO 210 I=1, NCOL
      N1= (I-1)*N2+1
      I2=I2+1
      TMP(N1+3)=YK(I2)
204  IF (I1-1) 208, 208, 204
      TMP(N1+4)=YK(I2)
208  I2=I2+1

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```

      TMP(N1+2)=YK(I2)
      TMP(N1+5)=TMP(N1+11)
210  CONTINUE
      N1=NC1*N2+4
      TMP(N1)=YK(I2+1)
      TMP(N1+1)=YK(I2+2)
      TMP(N1+2)=YK(I2+3)
      TMP(N1+6)=YK(I2+4)
      I2=I2+4
      GO TO 222
220  I2=I1*270
222  NO=NC1*N2+10
      N1=N0+N2
      NN=N0-N2-N2
      TMP(N0+1)=YK(I2+1)
      TMP(N1+2)=YK(I2+2)
      I2=I2+2
      TMP(N0+2)=TMP(NN+2)
230  DO 240 J=2, NROW
      NO=N0+3
      N1=N1+3
      NN=NN+3
      TMP(N0)=YK(I2+1)
      TMP(N0+1)=YK(I2+2)
      TMP(N0+2)=TMP(NN+2)
      TMP(N1+2)=YK(I2+3)
      I2=I2+3
      NO=N0+6
      TMP(N0)=YK(I2+1)
      TMP(N0+1)=YK(I2+2)
      TMP(N0+2)=YK(I2+3)
      I2=I2+3
      DO 250 I=1, NCOL
      I1=NCOL+1-I
      N1=I1*N2-5
      I2=I2+1
      TMP(N1)=YK(I2)
      TMP(N1+2)=TMP(N1-4)
      IF (I1-1) 252, 252, 251
      S1P14390
      S1P14400
      S1P14410
      S1P14420
      S1P14430
      S1P14440
      S1P14450
      S1P14460
      S1P14470
      S1P14480
      S1P14490
      S1P14500
      S1P14510
      S1P14520
      S1P14530
      S1P14540
      S1P14550
      S1P14560
      S1P14570
      S1P14580
      S1P14590
      S1P14600
      S1P14610
      S1P14620
      S1P14630
      S1P14640
      S1P14650
      S1P14660
      S1P14670
      S1P14680
      S1P14690
      S1P14700
      S1P14710
      S1P14720
      S1P14730
      S1P14740
      S1P14750
      S1P14760
      S1P14770

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251   I2=I2+1          S1P14780
      TMD(N1+1)=YK(I2)    S1P14790
252   I2=I2+1          S1P14800
      TMP(N1+5)=YK(I2)    S1P14810
250   CONTINUE          S1P14820
999   RETURN           S1P14830
END
*
FORTRAN
SUBROUTINE STRESS (II,JJ,KK)
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDIM, NROW, NCOL, MM, I1, KM1, KM2, KP1, KP2, MFLAG, XM, XLD
COMMON ISW1, ISW2, ISW3
COMMON A
COMMON TMD, YK, YL
COMMON T1, T2, XX, XX1, Z, Z1, Z2
COMMON ZNU, THC, PH1, FF, RH, DN, XXH, XK
COMMON ZETA
COMMON TE, TI, TO, OC, TC, TD, DDLD
DIMENSION A(1232)
DIMENSION MM(35)
DIMENSION T1( 89), T2(89), XX(89), XX1(89), Z(89), Z1(69), Z2(89)
DIMENSION TMP(5184), YK(4, 1296), YL(4,4,324)
DIMENSION ZETA(30)
101 FORMAT (I3, 1H, I3, 1P9E12.4)
      K = KK
      J=JJ
      NC1=NCOL+1          S1P15040
      NR1=NROW+1          S1P15050
      IF (XM) 1, 1, 5      S1P15060
      1  XH=XXH              S1P15070
      GO TO 10             S1P15080
      5  J1=XMAXNE (J2, 1)  S1P15090
      XH= XXH/2.***J1      S1P15100
      10 I=II               S1P15110
      U = DFF (I, J, 1, 0)  S1P15140
      V = DEF (I, J, 2, 0)  S1P15150
      W = DEF (I, J, 3, 0)  S1P15160

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```

UX=(DEF(I,J-1,1, KM1)-DEF(I,J+1,1,KP1))/(2.*XH)           S1P15170
UT=(DEF(I+1,J,1, 0)-DEF(I-1,J, 1, 0))/ (2.*XK)           S1P15180
VX=(DEF(I ,J-1, 2, KM1)-DEF(I ,J+1, 2, KP1))/(2.*XH)       S1P15190
VT= (DEF( I+1, J, 2, 0)-DEF( I-1, J, 2, C))/(2.*XK)        S1P15200
WX= (DEF( I, J-1, 3, KM1)-DEF( I, J+1, 3, KP1))/(2.*XH)      S1P15210
WT= (DEF( I+1, J, 3, 0)-DEF( I-1, J, 3, 0))/(2.*XK)        S1P15220
VXX= (DEF( I, J-1, 2, KM1)-2.*DEF( I, J, 2, 0)+DEF( I, J+1, 2, KP1)) / ( S1P15230
1 XH*XH)
VXT= (DEF( I+1, J-1, 2,KM1)-DEF( I+1, J+1, 2,KP1))- DEF( I-1, J-1,2,KM1)S1P15250
1 ) + DEF( I-1, J+1, 2, KP1)/(4.*XH*XK)                   S1P15260
VTX=VXT
VTT=(DEF( I+1,J,2,0)-2.*DEF( I,J,2,0)+DEF( I-1,J,2,0))/XK**2   S1P15270
WXX= (DEF( I,J-1,3,KM1)-2.*DEF( I,J,3,0)+DEF( I,J+1,3,KP1))/XH**2   S1P15280
WXT= (DEF( I+1, J-1, 3, KM1)-DEF( I+1, J+1, 3, KP1)-DEF( I-1, J-1, 3, KM1)+ S1P15290
1 DEF( I-1, J+1, 3, KP1))/(4.*XH*XK)                      S1P15300
WTX=WXT
WTT= (DEF( I+1,J,3,0)-2.*DEF( I,J,3,0)+DEF( I-1,J,3,0))/XK**2   S1P15320
WXXX= (DEF( I,J-2,3,KM2)-2.*DEF( I, J-1,3,KM1)+2.*DEF( I, J+1,3,KP1)) S1P15330
1 -DEF( I, J+2,3,KP2))/(2.*XH**3)                           S1P15340
WXTT= (DEF( I+1, J-1, 3, KM1)-2.*DEF( I, J-1, 3, KP1)+2.*DEF( I, J+1, 3, KP1)S1P15350
1 )-DEF( I+1, J+1, 3, KP1)+DEF( I-1, J-1, 3, KM1)-DEF( I-1, J+1, 3, KP1))/(2.* S1P15360
2 XH*XH*XK)
WTTT=WXTT
WTTT= (DEF( I+2,J,3,0)-2.*DEF( I+1,J,3,0)+DEF( I-1,J,3,0))-DEF( I-2,S1P15400
1 J,3,0))/(2.*XK**3)                                         S1P15410
WXXT= (DEF( I+1,J-1,3,KM1)-2.*DEF( I+1,J,3,0)+2.*DEF( I-1,J,3,0)+ S1P15420
1 DEF( I+1, J+1, 3, KP1)-DEF( I-1, J-1, 3, KP1)-DEF( I-1, J+1, 3, KP1))/(2.* S1P15430
2 XH*XH*XK)
X=ZETA(J+1)
SI = SIN(X)
CO = COSF(X)
CSC = 1./SI
COT = CO *CSC
EPSX = UX+W
EPST = COT*U + CSC*VT + W
GAM = CSC*UT + VX - COT*V
XLX1 = UX - WXX
XLX2 = CSC*(VT - CSC*WTT + CO *(U-WX))
XLX12 = CSC*(CO *V + COT*WT - UT) + VX

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S1P15560
S1P15570
S1P15580
S1P15590
S1P15600
S1P15610
S1P15620
S1P15630
S1P15640
S1P15650
S1P15660
S1P15670
S1P15680
S1P15690
S1P15700
S1P15710
S1P15720
S1P15730
S1P15740
S1P15750
S1P15760
S1P15770
S1P15780
S1P15790
S1P15800
S1P15810
S1P15820
S1P15830
S1P15840
S1P15850
S1P15860
S1P15870
S1P15880
S1P15890
S1P15900
S1P15910
S1P15920
S1P15930
S1P15940

XXX = UXX - WXXX
XXT = UXT - WXXT
XTX = CSC*(CO *(UX-WXX) + SI *(WX-U) - CSC*WTTX + VTX)
1 - COT*(CO *(U-WX) - 2.*CSC*WTT + VTT)
XTT = CSC*(CO *(UT-WXT) - CSC*WTT + VTT)
XXTX = CSC*(COT*WXT + CO *VX - SI *V - WXXT - UXT - CSC*CSC*(WT
1 - CO *(WXT + UT - COT*WT - CO *V) ) + VXX
XXTT = VXT + CSC*(UTT - WXT - CO *(VT - CSC*WTT) )
IF (MFLAG) 20, 40, 40
20 CONTINUE
OMEGAX = U - WX
OMEGAT = V - CSC*WT
PHI = •5*(VX + CSC*(CO *V - UT))
WRITE OUTPUT TAPE 6, 101, J, I, EPSX, EPST, GAM, XLX1, XLX2, XLX12,
1 OMEGAX, OMEGAT, PHI
GO TO 99
40 CONTINUE
ANX = FPSX + ZNU*EPST - TC
ANT = EPST + ZNU*EPSX - TC
ANXT = GAM + 2.*DD*X LX12
ANTX = ANXT
AMX = XLX1 + ZNU*X LX2 - TD*RH
AMT = XLX2 + ZNU*X LX1 - TD*RH
AMXT = XLX12
AMTX = AMXT
AMXTT = XXTT
AMXTX = XXTX
AQX = XXX + ZNU*X TX + (1.-ZNU)*CSC*(XXXTX + CO *(XLX1-XLX2))
AQT = XTT + ZNU*X TX + (1.-ZNU)*(2.*XLX12*COT + XXTX)
IF (K) 49, 49, 47
47 YL(1, K, I)=ANX
YL(2, K, I)=ANT
YL(3, K, I)=AMX
YL(4, K, I)=AMT
49 CONTINUE
IF (MFLAG) 45, 45, 46
45 WRITE OUTPUT TAPE 6, 101, J, I, AMX , AMT, ANX, ANXT, ANXT
GO TO 48
46 WRITE OUTPUT TAPE 6, 101, J, I, ANX, ANXT, ANXT, ANXT

```

```

48 CONTINUE
    IF (J) 60, 60, 51
51  IF (NR1-J) 70, 70, 52
52  IF (NC1-I) 80, 80, 99
C   LOWFR BOUNDARY
60  J3=NC1+NR1+2+NC1-I
    YK(1,J3) = ANXT + 2.*DD*AMXT
    YK(2,J3) = ANX
    YK(3,J3) = Aqx + CSC*(1.-ZNU)*AMXTT
    YK(4,J3) = AMX
    IF (I-NC1) 99, 69, 69
C   SPECIAL POINT
69  K1=2*(NC1+NR1)+1
    YK(1,K1)=-2.*AMXT
    GO TO 80
C   UPPER BOUNDARY
70  YK(1,I) = ANXT + 2.*DD*AMXT
    YK(2,I) = ANX
    YK(3,I) = -Aqx - CSC*(1.-ZNU)*AMXTT
    YK(4,I) = AMX
    IF (I-NC1) 99, 79, 79
C   SPECIAL CORNER POINT
79  K1=2*(NC1+NR1)
    YK(1,K1)=+2.*AMXT
C   RIGHT BOUNDARY
80  J3=NC1+NR1+1-J
    YK(1,J3) = -ANTX - 2.*DD*AMXT
    YK(2,J3) = ANT
    YK(3,J3) = AQT + (1.-ZNU)*AMXTX
    YK(4,J3) = AMT
99  RETURN
END
*
FORTRAN
    SUBROUTINE ZERO (X,N)
    DIMENSION X(8500)
    DO 1 I=1,N
1     X(I)=0.
    RETURN
END

```

```

*   *   FORTRAN
*   *   FAP
COUNT      90
*   MATRIX MULTIPLICATION IN DOUBLE PRECISION
*   MATM (X, Y, Z, NR, NC, NCY)
*   COMPUTE Z=X*Y. NR AND NC ARE NUMBER OF ROWS AND COLUMNS IN X.
*   NCYSIP16390
*   IS NUMBER OF COLUMNS IN Y. Z=Y C*K. BUT NOT Z=X.
*   ENTRY MATM
*   MATM
*   SXA    AXT,1
*   SXA    AXT+1,2
*   SXA    AXT+2,4
*   CLA    1,4          X-MATRIX
*   STA    AX
*   CLA    2,4
*   STA    AY
*   CLA    3,4
*   STA    AZ
*   CLA*   4,4          NR OF ROWS IN X
*   ARS    18           NR
*   STA    5,4          NR OF COLUMNS IN X
*   CLA*   18
*   ARS    6,4
*   STA    NC
*   CLA*   18
*   ARS    18
*   STA    NCY
*   CLA    =1
*   STO    J
*   MTO    LDQ    RWDIM
*           MPY    J
*           ADD    AZ
*           ADD    RWDIM
*           ADD    =1
*           STA    AZIJ
*           LDQ    RWDIM
*           MPY    J
*           XCA
*           ADD    AZ
*           ADD    RWDIM
*           ADD    =1
*           STA    AZIJ
*           LDQ    RWDIM
*           MPY    J
*           XCA

```

SSM	ADD	AY	RWDIM	S1P16730
	ADD		=1	S1P16740.
	ADD		YCOL	
	STA	LXA	NR,1	S1P16750
	SXD	LXA	MT4,1	S1P16760
	AXT	LXA	1,1	S1P16770
	LXA	NC,2	S1P16780	
	CLA	**,2	S1P16790	
	STO	TEM,2	S1P16800	
	TIX	YCOL,2,1	S1P16810	
	SXA	I,1	S1P16820	
MT1	LDQ	RWDIM	S1P16830	
	MPY	NC	S1P16840	
	XCA		S1P16850	
	PAX		S1P16860	
	CLA	RWDIM	S1P16870	
	ADD	AX	S1P16880	
	ADD	=1	S1P16890	
	SUR	I	S1P16900	
	STA	MT2	S1P16910	
	STA	AXIK	S1P16920	
	LXA	NC,2	S1P16930	
	STZ	TEM	S1P16940	
	STZ	TEM+1	S1P16950	
	PXA	0,0	S1P16960	
	NZT	**,*4	S1P16970	
	TXI	MT3+1,2,-1	S1P16980	
	LDQ	**,*4	S1P16990	
	FMP	TEM,2	S1P17000	
	DFA&	TEM	S1P17010	
	DST	TFW	S1P17020	
	TXN	*+2,2,1	S1P17030	
MT3	TIK	MT2,4,ROWD	S1P17040	
AZIJ	STO	**,*1	S1P17050	
	TXI	*+1,1,1	S1P17060	
MT4	TXL	MT1,1,**	S1P17070	
	CLA	J	S1P17080	
			S1P17090	
			S1P17100	
			S1P17110	
			*	
			**=NR	

```

ADD      S1P17120
CAS      S1P17130
TRA      S1P17140
TRA      S1P17150
STA      S1P17160
J       S1P17170
MT0     S1P17180
TRA      S1P17190
*+1     S1P17200
AXT     S1P17210
**,1    S1P17220
**,2    S1P17230
AXT     S1P17240
TRA      S1P17250
AXT     S1P17260
AXT     S1P17270
TRA      S1P17280
ROWDIM S1P17290
ROWD   S1P17300
TEM    S1P17310
AX     S1P17320
AY     S1P17330
AZ     S1P17340
NR     S1P17350
NC     S1P17360
NCY    S1P17370
I      S1P17380
J      S1P17390
END    S1P17400
FAP     S1P17410
COUNT  S1P17420
5,0    S1P17430
*DP SUM FUNCTION DPSUM(A,I,J,K,M). COMPUTE SUM OF A(I,L)*A(L,J), L=K..M.
*      S1P17440
SET DPSUM=0 IF K GREATER THAN M
*      S1P17450
*      SET THE VFLD OF RDIM AND ROWDIM TO THE ROW DIMENSION OF A
*      ENTRY DPSUM
CLAS*  LOAD M
CAS*   COMPARE WITH K
*      M IS BIGGER
TRA    *+4
      M=K
*      M LESS THAN K
      SET DPSUM=0
PXA    0,0
TRA    6,4
      AXT,1
SXA    AXT+1,2
STD    TEST
CLA    1,4
ADD    =1

```

STA	A1L	S1P17510
CLA*	2,4	S1P17520
ARS	18	S1P17530
STA	1	S1P17540
CLA*	4,4	S1P17550
PDX	,2	S1P17560
ARS	18	S1P17570
SUB	=1	S1P17580
XCA		S1P17590
MPY	RDIM	S1P17600
XCA		S1P17610
ADD	1	S1P17620
PAX	,1	S1P17630
CLA*	3,4	S1P17640
ARS	18	S1P17650
SUR	=1	S1P17660
XCA		S1P17670
MPY	RDIM	S1P17680
XCA		S1P17690
SSM		S1P17700
ADD	A1L	S1P17710
STA	ALJ	S1P17720
STZ	SUM	S1P17730
STZ	SUM+1	S1P17740
A1L	LDQ	**,1
ALJ	FMP	**,2
	DFAD	SUM
DST		SUM
TXI	*+1,1,ROWDIM	S1P17780
TXI	*+1,2,1	S1P17790
TEST	TXL	A1L,2,**
AXT	AXT	**,1
AXT		S1P17830
TRA	6,4	S1P17840
R	COMMON	1
SLIM	FQU	R+203
I	PZE	S1P17860
ROWDIM	EQU	72
RDIM	DEC	S1P17870
		S1P17880
		S1P17890

```

*      END
FAP      COUNT    70
        FUNCTION QDPSUM (A, I, J, K2, J2)
ENTRY    QDPSUM
QDPSUM  SXA      AXT,1
          SXA      AXT+1,2
          SXA      AXT+2,4
          CLA      1,4
          STA      DP1
          STA      DP1+1
          LXA      ROWD,1
          SXD      DP2,1
          CLA*     2,4
          ARS      18
          STA      1
          CLA*     4,4
          ARS      18
          STA      K2
          ADD      K
          SUB      I
          XCA      MPY
          XCA      ROWD
          ADD      I
          SUB      =1
          PAX      ,1
          CLA*     3,4
          ARS      18
          STA      I
          CLA      ROWD
          ADD      =1
          SUB      I
          TZF      DP
          CLA      ROWD
          SUB      =1
          PAC      ,2
          SXD      DP3,2
          CLA      I
          S1P17900
          S1P17910
          S1P17920
          S1P17930
          S1P17940
          S1P17950
          S1P17960
          S1P17970
          S1P17980
          S1P17990
          S1P18000
          S1P18010
          S1P18020
          S1P18030
          S1P18040
          S1P18050
          S1P18060
          S1P18070
          S1P18080
          S1P18090
          S1P18100
          S1P18110
          S1P18120
          S1P18130
          S1P18140
          S1P18150
          S1P18160
          S1P18170
          S1P18180
          S1P18190
          S1P18200
          S1P18210
          S1P18220
          S1P18230
          S1P18240
          S1P18250
          S1P18260
          S1P18270
          S1P18280

```

ADD		K	S1P18290
SUB		K2	S1P18300
XCA			S1P18310
MPY		ROWD	S1P18320
XCA			S1P18330
SUB		=1	S1P18340
ADD	K2		S1P18350
PAX		,2	S1P18360
TRA	DP0		S1P18370
DP	AXT	1,2	S1P18380
	SXD	DP3,2	S1P18390
	CLA	K	S1P18400
ADD	K		S1P18410
ADD	=1		S1P18420
XCA			S1P18430
MPY	ROWD		S1P18440
XCA			S1P18450
AND	K2		S1P18460
SUB	=1		S1P18470
PAX		,2	S1P18480
CLA*	5,4		S1P18490
ARS	18		S1P18500
SUB	K2		S1P18510
ADD	=1		S1P18520
PAX		,4	S1P18530
STZ	TEMP		S1P18540
STZ	TEMP+1		S1P18550
DP1	LDO	**,1	S1P18560
	FMP	**,2	S1P18570
DFAD	TEMP		S1P18580
DST	TEMP		S1P18590
DP2	TXI	*,1,1,**	S1P18600
DP3	TXI	*,1,2,**	S1P18610
	TIIX	DPI,4,1	S1P18620
AXT	AXT	**,1	S1P18630
	AXT	**,2	S1P18640
	AXT	**,4	S1P18650
	TRA	6,4	S1P18660
ROWD	DEC	270	S1P18670

K DFC 5  
 I PZE  
 K<sup>2</sup> PZE  
 TEMP BOOL 77774  
 END

```

* FAP COUNT 150           S1P18680
*          ENTRY CLOCK      S1P18690
*          ENTRY WCKA      S1P18700
*          ENTRY WCKP      S1P18710
*          SUBROUTINE CLOCK   S1P18720
*          **** * THIS SUBROUTINE PLACES THE CLOCK IN A GIVEN LOCATION SPECIFIED   S1P18730
*          BY THE CALL STATEMENT ( THAT IS STORED IN FORTRAN OR   S1P18740
*          CALL CLOCK(LOCATION TO BE STORED) (FOR ABSOLUTE ASSEMBLIES USE TSX CLOCK   S1P18750
*          CALL CLOCK (LOCATION TO BE STORED) IN FAP   S1P18760
*          OR   S1P18770
*          SVN (LOCATION TO BE STORED) GIVES THE CLOCK IN FLOATING POINT *S1P18780
*          PZE (LOCATION TO BE STORED) GIVES THE CLOCK IN BCD   S1P18790
*          IN FORTRAN THE CLOCK WILL ALWAYS BE GIVEN IN FLOATING POINT   S1P18800
*          THE CLOCK IS ALSO PRINTED ON-LINE   S1P18810
*          **** * S1P18820
*          **** * S1P18830
*          **** * S1P18840
*          **** * S1P18850
*          **** * S1P18860
*          **** * S1P18870
*          **** * S1P18880
*          **** * S1P18890
*          **** * S1P18900
*          **** * S1P18910
*          **** * S1P18920
*          **** * S1P18930
*          **** * S1P18940
*          **** * S1P18950
*          **** * S1P18960
*          **** * S1P18970
*          **** * S1P18980
*          **** * S1P18990
*          **** * S1P19000
*          **** * S1P19010
*          **** * S1P19020
*          **** * S1P19030
*          **** * S1P19040
*          **** * S1P19050
*          **** * S1P19060
  
```

CLOCK BSS 3 S1P18910
 WCKA BSS 0 S1P18920
 WCKP BSS 0 S1P18930
 SXA CLOCK+55,1 S1P18940
 SXA CLOCK+56,2 S1P18950
 SXA CLOCK+57,4 S1P18960
 RPR A 10 S1P18970
 SPR A 10 S1P18980
 RCHA CLOCK+105 S1P18990
 TCO A \* S1P19000
 STZ CLOCK+61 S1P19010
 STZ CLOCK+62 S1P19020
 CLA CLOCK+227 S1P19030
 STO CLOCK+218 S1P19040
 AXT 0,3 S1P19050
 AXT 0,3 S1P19060

S1P19070	AXT	2,4	CLOCK+104,1	
S1P19080	LDQ	0,0	CLOCK+104,1	
S1P19090	PXD	0,0	CLOCK+104,1	
	CAQ	CLOCK+153,9,1		S1P19100
	CVR	CLOCK+217,9,6		S1P19110
	ORS	CLOCK+63,9,4		S1P19120
	TIX	*-4,4,1		S1P19130
	CLA	CLOCK+226,2		S1P19140
	STO	CLOCK+218		S1P19150
	TXI	*+1,2,1		S1P19160
	TXI	*+1,1,2		S1P19170
	TXL	CLOCK+12,1,17		S1P19180
	PXD	0,0		S1P19190
	LDQ	CLOCK+61		S1P19200
	LGL	30		S1P19210
	LDQ	CLOCK+62		S1P19220
	LGL	18		S1P19230
	RQL	6		S1P19240
	LGL	12		S1P19250
	SLW	CLOCK+61		S1P19260
	LXA	CLOCK+57,4		S1P19270
	CAL	1,4		S1P19280
	ARS	18		S1P19290
	TZE	CLOCK+55		S1P19300
	PXD	0,0		S1P19310
	LDQ	CLOCK+61		S1P19320
	CAQ	CLOCK+113,9,4		S1P19330
	STQ	CLOCK+61		S1P19340
	ARS	18		S1P19350
	ADD	=0233000000000		S1P19360
	FAD	=0233000000000		S1P19370
	XCA			S1P19380
	FMP	=1,•F2		S1P19390
	STO	CLOCK+87		S1P19400
	PXD	0,0		S1P19410
	LDQ	CLOCK+61		S1P19420
	CAQ	CLOCK+133,9,2		S1P19430
	ARS	18		S1P19440

ADD	=0233000000000	S1P19450
FAD	=0233000000000	S1P19460
FAD	CLOCK+87	S1P19470
FDP	=1•F2	S1P19480
STQ	CLOCK+61	S1P19490
AXT	**,1	S1P19500
AXT	**,2	S1P19510
AXT	**,4	S1P19520
CLA	CLOCK+61	S1P19530
STO*	1,4	S1P19540
TRA	2,4	S1P19550
PZE		S1P19560
PZE		S1P19570
OCT	,	S1P19580
BSS	18	S1P19590
IOC P	CLOCK+63,,18	S1P19600
IOC PN	CLOCK+87,,2	S1P19610
IOC P	CLOCK+81,,2	S1P19620
IOC PN	CLOCK+87,,2	S1P19630
IOC P	CLOCK+83,,2	S1P19640
IOC P	CLOCK+87,,2	S1P19650
IOC P	CLOCK+85,,2	S1P19660
IOC D	CLOCK+89,,16	S1P19670
PZE	*+10	S1P19680
PZE	*+9,,1000	S1P19690
PZE	*+8,,2000	S1P19700
PZE	*+7,,3000	S1P19710
PZF	*+6,,4000	S1P19720
PZF	*+5,,5000	S1P19730
PZE	*+4,,6000	S1P19740
PZE	*+3,,7000	S1P19750
PZF	*+2,,8000	S1P19760
PZE	*+1,,9000	S1P19770
PZE	*+10,	S1P19780
PZE	*+9,,100	S1P19790
PZE	*+8,,200	S1P19800
PZE	*+7,,300	S1P19810
PZF	*+6,,400	S1P19820
PZE	*+5,,500	S1P19830
PZE	*+4,,600	S1P19840



PZE	*-8,,3*4096	S1P20240
PZE	*-9,,2*4096	S1P20250
PZE	*-10,,1*4096	S1P20260
END		S1P20270
FAP		S1P20280
COUNT	170	S1P20290
*	SUBROUTINES RTAPE, WTape, BACK, AND RESET	
ENTRY	WTAPE	S1P20300
ENTRY	RTAPE	S1P20310
ENTRY	RTAPE	S1P20320
ENTRY	RFW	S1P20330
ENTRY	BACK	S1P20340
ENTRY	RFSET	S1P20350
WTAPE	CLS	S1P20360
	WRS	S1P20370
STD	WRTP	S1P20380
STZ	FLAG1	SET FLAG1 FOR WRITING
TRA	BEGIN	S1P20390
RTAPE	CLA	S1P20400
	RDS	S1P20410
STD	WRTP	READ, NOT WRITE
STL	FLAG1	SET FOR READING
RFGIN	SXA	AXT,1
	SXA	AXT+1,2
STZ	FLAG	FIRST TIME THROUGH
CLA*	1,4	S1P20430
STA	BSR	S1P20440
ANA	MASK	S1P20450
TZE	*+3	S1P20460
STL	FLAG2	SET FLAG2 FOR CHANNEL A
TRA	*+2	S1P20470
STZ	FLAG2	SET FLAG2 FOR CHANNEL B
NZT*	4,4	S1P20480
TRA	WR	IS THIS A CHECK
TZF	CKR	GO AND START A READ OR WRITE
CK		S1P20490
CKA	TCOA	CHECK FOR REDUNDANCY.
CKB	TRCA	S1P20500
	ERR	S1P20510
CKA	TRA	S1P20520
	AXT	S1P20530
CKB	TCOB	S1P20540
	*	S1P20550
ERR	ZET	S1P20560
	TRA	S1P20570
	AXT	S1P20580
	FLAG	S1P20590
	TAPE ERROR.	S1P20600
	IS THIS THE FIRST TIME	S1P20610
		S1P20620

TRA	BLNK	NO	S1P20630
STL	FLAG		S1P20640
BSR	**		S1P20650
WR	CLA*	3,4	S1P20660
	STD	IOC	S1P20670
	ARS	WORD COUNT	S1P20680
	SSM	18	S1P20690
ADD	2,4	BOTTOM OF ARRAY IN AC	S1P20700
ADD	=1		S1P20710
STA	IOC		S1P20720
CLA*	1,4	SET TAPE UNIT ADDRESS	S1P20730
STA	WRTP		S1P20740
ANA	TPNR	PICK OUT LAST DIGIT	S1P20750
PAX	,1	TAPE M. M TO XR 1	S1P20760
CLA	TPCNT+1,1		S1P20770
STA	LD1		S1P20780
STA	COMP		S1P20790
STA	STORE		S1P20800
PDX	,2		S1P20810
LDO	**,2		S1P20820
ZET	FLAG	IF RERUN, DONT BUMP COUNTERS	S1P20830
TRA	RERUN		S1P20840
SSP	NOT A BACKSPACE SO SIGN PLUS		S1P20850
ADD	ONE		S1P20860
PDX	,2		S1P20870
STD	TPCNT+1,1		S1P20880
STA	TPCNT+1,1		S1P20890
ZET	FLAG1	IS IT READ OR WRITE	S1P20900
TRA	WR1	READ OPERATION	S1P20910
XCA	WRITE OPERATION.	MUST MAKE UP NEXT RECORD ID NR.	S1P20920
ADD	ONE		S1P20930
ADD	=1		S1P20940
STORE	**,2	STORE NEXT RECORD ID WORD IN TABLE	S1P20950
	STO	IDENT FIRST WORD OF RECORD	S1P20960
WR1	NZT	FLAG2 CHANNEL A OR B	S1P20970
	TRA	TPB	S1P20980
TPA	TCOA	*	S1P20990
	TRCA	*+1	S1P21000
XEC	WRTP		S1P21010

RCHA	ICID		S1P21020
LCHA	IOC		S1P21030
ZET	FLAG1	IF READING,	GO CHECK RECORD ID
TRA	COMP		S1P21040
ZET	FLAG	IS THIS A RERUN	
TRA	CKA	YES • GO AND CHECK FOR REDUNDANCY	S1P21070
TRA	AXT	NO. GO BACK AND COMPUTE SOME MORE	S1P21080
TCOB	*		S1P21090
TDB	TRCB	**+1	S1P21100
	XEC	WRTP	S1P21110
	RCHR	ICID	S1P21120
	LCHR	IOC	S1P21130
	ZFT	FLAG1	S1P21140
	TRA	COMP	S1P21150
	ZFT	FLAG	S1P21160
	TRA	CKB	S1P21170
	TRA	AXT	S1P21180
COMP	CLA	** ,2	S1P21190
	SUB	IDENT	DOES FIRST WORD OF RECORD AGREE WITH ID
	TNZ	SHIFT NO.	S1P21200
	STP	TRY ANOTHER RECORD	S1P21210
	NZT	TPCNT+1,1	S1P21220
		FLAG YES • IS THIS A RERUN	S1P21230
	TRA	AXT	S1P21240
	CLA	FLAG2	S1P21250
	TPA	(K	S1P21260
REFUN	ZET	FLAG1	S1P21270
	TRA	WR1	S1P21280
	XCA	RESET ID WORD	S1P21290
	TRA	STORE+1	S1P21300
BLNK	ZET	FLAG1 IS THIS A READ	S1P21310
	TRA	OUT IF SO GIVE UP	S1P21320
	XEC	BSR	S1P21330
	XEC	WRTP	S1P21340
	XEC	WRTP	S1P21350
	XEC	WRTP	S1P21360
	CLA	MAX	S1P21370
SUR	=1		S1P21380
TMI	OUT	QUIT AFTER MAX TIME	S1P21390
STO	MAX		S1P21400

CLA  
 TRA  
 SHIFT CLA MAX  
 SIR =1  
 TMI OUT  
 STO MAX  
 CLA TPCNT+1,1  
 TPL WR1 LAST ACTIVITY WAS READ OR WRITE SO GO AHEAD  
 XFC PSR LAST ACTIVITY WAS PACKSPACE. MUST GO BACK  
 XFC PQR  
 TRA WR1 LOOK FOR MISSING RECORD AGAIN  
 AXT AXT \*\*,1  
 AXT \*\*,2  
 TRA 5,4  
 CALL DUMP  
 CLA\* 1,4  
 STA \*\*+1  
 REW \*\*  
 SXA AX,1  
 ANA TPMR  
 PAX ,1  
 DXA 2,0  
 STD TPCNT+1,1  
 AX AXT \*\*,1  
 TRA 2,4  
 BACK CLA\* 1,4  
 STA RSR  
 XFC BSR  
 SXA BX,1  
 ANA TPMR  
 PAX ,1  
 CLA TPCNT+1,1  
 SSP SIR ONE  
 SSM SIR TPCNT+1,1  
 STO AXT ,1  
 TRA 2,4  
 NOP

```

      RESET  PXA    0,0
      STD    TPCNT-3
      STD    TPCNT-2
      STD    TPCNT-1
      STD    TPCNT
      TPA    1,4
      ICID   IOST   IDENT,,1
      IOC    IOPT   0,,0
      WRTP   WRS    ***
      WRS   WRS    ***
      QDS   RDS    ***
      PZE   PZE    TRL4
      PZE   PZE    TBL3
      TPCNT TPCNT TBL2
      TDNR   OCT    00000001000
      MACK   OCT    00000001000
      MAX    DFC    40
      ONE    OCT    1000000
      FLAG   FLAG1
      FLAG2
      IDENT  PZF
      TRL1   RFS    80
      TRL2   RFS    80
      TRL3   RFS    80
      TRL4   RFS    80
      END
      *   CHAIN(?,2)
      *   ENDTRAN
CSITM COMMON CHAIN LINK 2 FOR SPHERE
COMMON IOPT1, IOPT2, IOPT3, IOPT4, IOPT5, IOPT6, IOPT7, IOPT8
COMMON NCF
COMMON NDI4, NROW, NCOL, NM, MFLAG, XM,XLD
COMMON ISW1, ISW2, ISW3
COMMON A
COMMON TWO, YK, YL
COMMON T1, T2, XX, XY1, Z, Z1, Z2
      S1P21800
      S1P21810
      S1P21820
      S1P21830
      S1P21840
      S1P21850
      S1P21860
      S1P21870
      S1P21880
      S1P21890
      S1P21900
      S1P21910
      S1P21920
      S1P21930
      S1P21940
      S1P21950
      S1P21960
      S1P21970
      S1P21980
      S1P21990
      S1P22000
      S1P22010
      S1P22020
      S1P22030
      S1P22040
      S1P22050
      S1P22060
      S1P22070
      S1P22080
      S1P22100
      S1P22110
      S1P22120
      S1P22130
      S1P22140
      S1P22150
      S1P22160
      S1P22170
      S1P22180

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COMMON ZNU, THC, PH1, FF, RH, DD, XH, XK
COMMON ZFTA
COMMON TE, TI, TO, OC, TC, TD, DDLD
COMMON RECORD
DIMENSION A(1232)
DIMENSION MM(40)
DIMENSION T1( 89), T2(89), XX(89), XX1(89), Z(89), Z1(89), Z2(89)
DIMENSION TMP(5184), YK(5184), YL(4,4,324)
DIMENSION ZETA( 30)
DIMENSION RECORD(12)
DIMENSION DISP(9), STRSS(9), ORDLBL(6,11), ABLEBL(6), CILBL(6,4)
DIMENSION ARSC(80), AORD(25), BOND(9)
DIMENSION CRLBL(6, 4)
DIMENSION AXLBL(6)
FORMAT(1H1, 12A6)
966 FORMAT(6A6)
B      XXN=255151606060
KTAPF=15
MO=1-I OPT2
NR1=NROW+1
NC1=NCOL+1
NR3=3*(NROW+6)
NR4=NR1+1-MO
51 READ INPUT TAPE 5, 966, ((CILBL(I, J), I=1, 6), J=1, 4)
NFND=0
NCRV=MM(31)
NCRY1=2-MO
NPTS=NCOL/26+1
NFLAGE=1
CALL PLTBL (DISP, STRSS, ORDLBL, ABLEBL, BOND, AXLBL)
TH=0.
COL=NCOL
DElh=1.0/COL
DO 52 I=1, NC1
ARSC(I)=TH
52 TH=TH+DElh
DO 53 J=1, NR1
JJ=NR1+2-J
53 AORD(J)=ZFTA(JJ)

```

```

      AND(NR1+1)=ZFTA(1)
      DO 650 K=1,2
      WRITE TAPE KTape, RFCORD
      WRITE TAPE KTape, NC1, NCRV, NPTS, NEND, NFLAG
      WRITE TAPE KTape, ABLBL, (3RDLBL(M,K),M=1,6), DISP
      WRITE TAPE KTape, CILBL
      DO 610 I=1, NC1
      WRITE TAPE KTape, ARSC(I)
      CONTINUE
      L=32
      L=31+MM(31)
      DO 620 J=0, NPT1
      IF (MM(L)-J) 620, 611, 620
      I1=2*(J+2)+K
      DO 615 I=1, NC1
      WRITE TAPE KTape, TMP(I1)
      I1=I1+NQR3
      L=L+1
      IF (L-L3) 620, 620, 650
      CONTINUE
      620 CONTINUE
      650 CONTINUE
      DO 720 K=1, 4
      K1=K+3
      WRITE TAPE KTape, RFCORD
      WRITE TAPE KTape, NC1, NCRV, NPTS, NEND, NFLAG
      WRITE TAPE KTape, ABLBL, (3RDLBL(M, K1), M=1, 6), STRSS
      WRITE TAPE KTape, CILBL
      DO 662 I=1, NC1
      WRITE TAPE KTape, ARSC(I)
      CONTINUE
      DO 660 M=1, NCRV
      DO 650 I=1, NC1
      WRITE TAPE KTape, YL(K,M,I)
      720 CONTINUE
      DO 740 K1=1, 4
      K=K1+7
      NCRV=NCRV1
      NCR=0
      NCX=NC1
      S1P22580
      S1P22590
      S1P22600
      S1P22610
      S1P22620
      S1P22630
      S1P22640
      S1P22650
      S1P22660
      S1P22670
      S1P22680
      S1P22690
      S1P22700
      S1P22710
      S1P22720
      S1P22730
      S1P22740
      S1P22750
      S1P22760
      S1P22770
      S1P22780
      S1P22790
      S1P22800
      S1P22810
      S1P22820
      S1P22830
      S1P22840
      S1P22850
      S1P22860
      S1P22870
      S1P22880
      S1P22890
      S1P22900
      S1P22910
      S1P22920
      S1P22930
      S1P22940
      S1P22950
      S1P22960

```

```

    725 WRITE TAPE KTAPE, RECORD
    WRITE TAPE KTAPE, NCX, NCRV, NPTS, NEND, NFLAG
    IF (NCR) 723, 723, 724
  723 CONTINUE
    WRITE TAPE KTAPE, ABLBL, (ORDLBL(M,K), M=1, 6), BOND
    GO TO 726
  724 CONTINUE
    WRITE TAPE KTAPE, AXRL, (ORDLBL(M,K), M=1, 6), BOND
  726 CONTINUE
    CALL PLBL (CBLRL, NCR)
    WRITE TAPE KTAPE, CBLBL
    IF (NCR) 727, 727, 729
  727 DO 728 I=1, NC1
  728 WRITE TAPE KTAPE, ABSC(I)
    I1=K1
    GO TO 731
  729 DO 730 I=1, NR4
  730 WRITE TAPE KTAPE, AORD(I)
  731 CONTINUE
    KAD=4
    DO 735 M=1, NCRV
    DO 732 L=1, NCX
      WRITE TAPE KTAPE, YK(I1)
  732 I1=I1+KAD
    I1=4*(NC1+NR1)+K1
  735 KAD=-4
    IF (NCR) 736, 736, 740
  736 NCR=1
    I1=4*NCR1+K1
    KAD=4
    NCX=NR4
    NCRV=1
    IF (K1-4) 714, 714, 714
  714 NFND=1
  715 CONTINUE
    GO TO 725
  740 CONTINUE
    WRITE TAPE KTAPE, XXN
    BACKSPACE KTAPE

```

```

IF (IOPT5) 1010, 1010, 1011
1010 CALL CHAIN (1, 2)
1011 CALL CHAIN (3, 2)
END
*      FAP
      COUNT   80
*PLTLBL  SUBROUTINE PLTLBL (DISP, STRSS, ORDLBL, ABLBL, BOND )
      ENTRY    PLTLBL
      PLTLBL SXA      AXT,1
      SXA      AXT+1,2
      CLA      1,4
      STA      D1+1
      AXT      9,1
      AXT      0,2
D1      CLA      DISP+9,1
      STO      **,2
      TXN      *+2,1,1
      TXI      D1,2,1
      CLA      2,4
      STA      S1+1
      AXT      9,1
      AXT      0,2
      CLA      STRSS+9,1
      STO      **,2
      TXN      *+2,1,1
      TXI      S1,2,1
      CLA      3,4
      STA      C1+1
      AXT      66,1
      AXT      0,2
      CLA      ORDU+66,1
      STO      **,2
      TXN      *+2,1,1
      TXI      01,2,1
      CLA      4,4
      STA      A1+1
      AXT      6,1
      AXT      0,2
      CLA      ARLBL+6,1

```

STO	***,2		
TNX	*+2,1,1		
TXI	A1,2,1		
CLA	5,4	S1P23770	
STA	B1+1	S1P23780	
AXT	9,1	S1P23790	
AXT	0,2	S1P23800	
B1	CLA	BON+9,1	S1P23810
	STO	***,2	S1P23820
	TNX	*+2,1,1	S1P23840
	TXI	R1,2,1	S1P23850
	CLA	6,4	S1P23860
	STA	AX1+1	S1P23870
	AXT	6,1	S1P23880
	AXT	0,2	S1P23890
	AX1	AXLRL+6,1	S1P23900
	STO	***,2	S1P23910
	TNX	*+2,1,1	S1P23920
	TXI	AX1,2,1	S1P23930
	AXT	***,1	S1P23940
	AXT	***,2	S1P23950
	TRA	7,4	S1P23960
	ORDU	BCI	U
	ORDV	BCI	V
	ORDW	BCI	W
	ORDNX	BCI	NPHI
	ORDNT	BCI	NTHETA
	ORDMX	BCI	MPHI
	ORDMT	BCI	MTHETA
	ORDN	BCI	NTAN
	ORDNB	BCI	NNORM
	ORDQ	BCI	Q
	ORDM	BCI	M
	ARLRL	BCI	THETA
	AXLRL	BCI	PHI
	DISP	BCI	FIG6.
	STRESS	BCI	SPHERF DISPLACEMENT COMPONENTS
	RON	BCI	FIG6.
	FND		SPHERE STRESS RESULTANTS
		9,	S1P24100
		9,	S1P24110
		9,	S1P24120
		9,	S1P24130

```

*      FAP      COUNT    40
*PLBL   SUBROUTINE PLBL (CBLBL, NCR)
      ENTRY  PLRL
      SXA    AXT,1
      SXA    AXT+1,2
      NZT*   2,4
      TRA    UPPER
      S1CT   CLA   1,4
      STA    R1+1
      AXT   6,1
      AXT   0,2
      CLA.  RT+6,1
      STO   ***,2
      TNX   AXT,1,1
      TXI   R1,2,1
      UPPER CLA   1,4
      STA    UP+1
      AXT   12,1
      AXT   0,2
      CLA.  IPP+12,1
      STO   ***,2
      TNX   AXT,1,1
      TXI   UP,2,1
      AXT   ***,1
      AXT   ***,2
      TRA   3,4
      RT    BC1   6,
      UPP   RC1   6,
            BC1   6,
            END
      *     CHAIN(3,2)
      *     FORTRAN
      *     INDFX (1270)
C      PROGRAM TO CONTROL PLOTTING FROM SCRATCH TAPE
C      CAN PLOT SEQUENTIAL GRAPHS EACH HAVING SEVERAL CURVES
C      NX = NUMBER OF VALUES OF INDEPENDENT VARIABLE FOR A GIVEN GRAPH
C      NCRVS = NUMBER OF CURVES TO BE PLOTTED ON A GIVEN GRAPH
C      NPTS = NUMBER OF INTERVALS BETWEEN DEPENDENT VARIABLE VALUFS

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C AT WHICH IDENTIFYING SYMBOLS ARE TO BE PLACED
C IF NEND = 0, OTHER GRAPHS ARE TO FOLLOW
C IF NEND = 1, CURRENT GRAPH IS THE LAST
C IF NFLAG = 0, CONTROL WILL BE RETURNED TO CHAIN (1,3)
C IF NFLAG = 1, RUN WILL BE TERMINATED BY CALL EXIT
DIMENSION XP(200),YP(200,4),ARLRL(6),ORDLRL(6),GPHLBL(9),
1 CILRL(6,4),RFCORD(12),YT(200)
EQUIVALENCE (KR,FR), (XXN, NFRR)
KP=15

      REWIND KP
      XXN=255151606060
      NEND=0

      20 READ TAPE KP, RFCORD
          READ TAPE KP, NXP, NCRVS, NPTS, NEND, NFLAG
          READ TAPE KP, ABLBL, ORDLBL, GPHLBL
          READ TAPE KP, CILRL
          DO 32 KT = 1, NXP
          READ TAPE KP, XP(KT)
          DO 33 L = 1, NCRVS
          DO 33 KT = 1, NXP
          READ TAPE KP, YT(KT)
          33 YP(KT,L) = YT(KT)
          READ TAPE KP, ER
          BACKSPACE KP
          IF (KR-NERR) 61, 60, 61
          60 NEND=1
          61 CONTINUE
          CALL PLOTS(NXP,NCRVS,NPTS,NEND,NFLAG,XP,YP,RECORD,AELBL,ORDLBL,
1 GPHLBL,CILRL)
          1 IF (NEND) 20, 20, 21
          21 IF (NFLAG) 40, 40, 41
          40 CALL CHAIN (1,2)
          41 CALL EXIT
          END

* FORTRAN
SUBROUTINE PLOTS(NXP,NCRVS,NPTS,NEND,NFLAG,X,Y,RECORD,ABLBL,
1 ORDLBL,GPHLBL,CILRL)
SC 4020 ROUTINE FOR PLOTTING SEVERAL CURVFS ON A SINGLE GRAPH
INDEX (1280)

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```

DIMENSION X(200),Y(200,4),ABLBL(6),ORDLBL(6),GPHLBL(6),CLBL(6),
DIMENSION KX1(4),KY1(4),KX2(4),CY2(4),CILRL(6,4),CLBL(6),
1  ORDLBL(6),GPHL(5),YP(200),MRK(4)
      WRITE OUTPUT TAPE 6,10
      10 FORMAT(15HO PLOT CALLED )
      F TABLIV
      CALL CAMRAV(9)
      XL = X(1)
      XR = X(1)
      DO 20 I = 2,NXP
      XL = MIN1F(XL,X(I))
      20 XR = MAX1F(XR,X(I))
      DC = 20.0
      CALL DDXDV(1,XL,XR,DX,N,II,NX,DC,IERR)
      KX1(1) = 185
      KX1(2) = 185
      KX1(3) = 585
      KX1(4) = 585
      KY1(1) = 985
      KY1(2) = 955
      KY1(3) = 985
      KY1(4) = 955
      KX2(1) = 200
      KX2(2) = 200
      KX2(3) = 600
      KX2(4) = 600
      MRK(1) = 38
      MRK(2) = 55
      MRK(3) = 63
      MRK(4) = 53
      YB = 0.0
      YT = 0.0
      DC 40 J = 1,NCRVS
      DO 40 I = 2,NXP
      YR = MIN1F(YB,Y(I,J))
      40 YT = MAX1F(YT,Y(I,J))
      YB = YT*1.10
      YT = YT*1.10
      L = 1

```

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S1P25310
S1P25320
S1P25330
S1P25340
S1P25350
S1P25360
S1P25370
S1P25380
S1P25390
S1P25400
S1P25410
S1P25420
S1P25430
S1P25440
S1P25450
S1P25460
S1P25470
S1P25480
S1P25490
S1P25500
S1P25510
S1P25520
S1P25530
S1P25540
S1P25550
S1P25560
S1P25570
S1P25580
S1P25590
S1P25600
S1P25610
S1P25620
S1P25630
S1P25640
S1P25650
S1P25660
S1P25670
S1P25680
S1P25690

CALL DXDYV(2,YR,YT,DY,M,JJ,NY,DC,IERR1)
NX = + 3
NY=-2
II = -II
JJ = -JJ
CALL SFTMIV(100,10,100)
CALL GRIDIV(L,XL,XR,YR,YT,DX,DY,N,M,II,JJ,NX,NY)
DO 60 K = 1,6
60 QRDL(K) = QRDLBL(K)
CALL CH17V(2,2)
CALL RITSTV(12,18,TAPLIV)
CALL RITE2V(75,330,1023,180,1,36,1,OPDL,NLAST)
CALL RITE2V(330,57,1023,90,1,36,1,ARLBL,NLAST)
CALL PRINTV(72,RECORD,100,1015)
DO 61 K = 1,9
61 GPHL(K) = GPHLBL(K)
CALL CHSIZV(3,4)
CALL RITSTV(18,30,TABLIV)
CALL RITE2V(40,20,1023,90,2,54,1,GPHL,NLAST)
DO 70 J = 1,NCRVS
YP(1) = Y(1,J)
NX1 = NXV(X(1))
NY1 = NYV(YP(1))
DO 50 I = 1,NXP
YP(I) = Y(I,J)
NX2 = NXV(X(I))
NY2 = NYV(YP(I))
IF(NX2*NY2)45,50,45
45 CALL LINEV(NX1,NY1,NX2,NY2)
NX1 = NX2
NY1 = NY2
50 CONTINUE
MRKPT = MRK(J)
CALL APLOTV(NXP,X,YP,NPTS,NPTS,1,MRKPT,IERR)
KX = KX1(J)
KY = KY1(J)
NS = J
CALL POINTV(KX,KY,NS,ANY)
KXC = KX2(J)

```

```
DO 93 K = 1,6
93 CLBL(K) = CILBL(K,J)
92 CALL PRINTV(36,CLBL,KXC,KY)
70 CONTINUE
1 IF(NEND)90,90,91
C1 CALL FOFTV
      WRITE OUTPUT TAPE 6,80
      FORMAT(22H0 PLOTTING COMPLETED )
80 RETURN
90 END
```