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**ME-661** 

## **HEAT TRANSFER CHARACTERISTICS** OF ARC TUNNEL CONSTRICTORS

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Prepared under Contract NAS2-2640 For **NASA-Ames** Research Center

by

Darryl **E.** Metzger

# **HEAT** TRANSFER **CHARACTERISTICS OF** *ARC* TUNNEL CONSTRICTORS

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\*

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#### ABSTRACT

Arc tunnel constrictors have been designed and tested which will tolerate heat fluxes up to  $12,000$  Btu/(sec  $ft^2$ ). Thick walled constrictors failed by local melting on the arc side of the wall at flux levels in agreement with predictions based on axisymmetric conduction through the wall. Burnout type failures were observed with thinner walled constrictors at flux levels **up** to four times higher than predicted by Gambill's additive method, and the difference **is** attributed to high non-boiling convective heat transfer rates. The results of this study indicate that with proper **coolant** passzge design **and** high coolant pressures, heat fluxes up to 20,000 Btu/(sec  $\mathrm{ft}^2$ ) may be tolerable without constrictor failure.

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# LIST **OF** FIGURES



#### **REFERENCES**

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- **3.**  "Heat Transfer in Tube Coils With Laminar and Turbulent Flow", by R. A. Seban and E. F. McLaughlin, International Journal of Heat and Mass Transfer,  $Vol. 6$ , pp. 387-395, 1963.
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- **5.**  "Generalized Prediction of Burnout Heat **Flux** for Flowing, Subcooled, Wetting Liquids", by **W.** R. Gambill, Chemical Engineering Progress Symposium Series, Volume 59, No. 41, 1963.
- 6. "Correlation of Maximum Heat Transfer Data for Boiling of Saturated Liquids", by **11.** Rohsenow and P. Griffith, Chemical Engineering Progress Symposium Series, **Vol.** 52, No. 18, 1956.
- *7.*  Nuclear Engineering, pp. 399-431, McGraw-Hill, New York, 1957.
- *8.*  **"A** Theory of Local. Boiling Burnout and Its Application to Existing Data", **by** L. Bernath, Chemical Engineering Progress Symposium Series, **Vol.** 56, **No.** 30, **1960.**
- *9.*  "Subcooled Burnout in Tubes of **Snall** Diameter", by A. E. Bergles, ASHE Paper No. 63-WA-182, November, 1963.

## NOMENCLATURE

English Letter Synibols



## Greek Letter Symbols



 $\overline{a}$ 

# Non-Dimensional Quantities



## **Subscripts**



**V** 

#### I. Introduction

The constricted arc wind tunnel is a research facility currently in use wherever steady **flows of** high enthalpy *are* required. Such devices are used, for example, to study ablation and heat transfer characteristics of space vehicles upon entry into various planetary atmospheres. NASA's Ames Research Center has been involved both in the development of the constricted arc tunnels and in their use as a research tool. The present report, dealing with performance characteristics of arc tunnels, covers work carried out by the Engineering Research Center at Arizona State University under NASA-Ames Research Center sponsorship.

**<sup>A</sup>**schematic of a constricted arc tunnel is shown in Fig. 1. Basically, the device consists of **an** anode and cathode separated by a segmented, cooled nozzle, . In operation, the test gas is injected near the cathode and accelerated through the nozzle into the test section of the tunnel. The ionized test gas carries a high d.c, current between the cathode and the anode; in effect the arc is carried through the nozzle, heating the test **gas** *to* high enthalpy levels in the process.

**<sup>A</sup>**considerable portion of the electrical power dissipated in the plasma is lost to the constrictor **walls** through heat transfer. The operation of the device **is** such that increases in energy content of the test gas are necessarily accompanied by increases in constrictor **wall** heat transfer. **As** a consequence, the ultimate performance of these devices is limited by the maximum tolerable **wall**  heat flux.

For steady state operation, the wall heating from the plasma must be removed by the coolant. **The** basic constrictor configuration is shown in Fig. 2, and consists of a thin disk with a circular plasma passage and **an annular** coolant passage. The disk material usually employed is copper **and** the coolant is usually water. The capability of the coolant for removing the **wall** heating is enhanced by allowing the coolant to boil; however, the crisis point associated with the transition from nucleate to pool boiling suggests that constricted **arc** performance **will be** limited to coolant heat fluxes lower than this transition value.

The present **study** deals with the heat removal capabilities of cooled constricted disks; further discussion of the theory of constricted arc jets may be found in References 1 and 2.

SCHEMATIC OF A CONSTRICTED ARC FIGURE



#### II. Basic Considerations of the Heat Transfer Problem

I

The constrictor geometry under considerction may be idealized as follows. **A** plasma passage of circular cross section is separated from a concentric cooling passage by a copper annulus **as shown** in Fig. 2. **Assuming** one-dimensional axi-symmetrical radial conduction, the temperature drop through the copper wall. and the heat fluxes at the inner and outer radii are related through the steady state conduction rate equation:

$$
\frac{q}{A_1} = \frac{\frac{T_1 - T_0}{\ln(r_0/r_1)} \cdot \frac{k}{r_1}}{\frac{q}{\ln(r_0/r_1)} \cdot \frac{k}{r_1}}
$$

<sup>1</sup>For a given plasma passage diameter, the inner and outer heat fluxes can be evaluated fromEquation 1 **as** a function of the **wall** temperature drop and radius ratio,  $r_o/r_i$ , as shown in Fig. 3 for a 1/4" diameter copper constrictor.

The inner temperature,  $T_i$ , cannot exceed the wall material melting point, which for copper is approximately 1980°F. The **wall** temperature on the coolant side, **will** vary depending on the coolant, coolant pressure, flow conditions, and whether or **not** surface boiling is occurring. Nevertheless, for the flux levels under consideration, T<sub>o</sub> will rarely either exceed 450<sup>0</sup>F or be less than 250<sup>0</sup>F. Thus the maximum possible non-melting wall temperature difference may be represented as a band centering at 1650<sup>°</sup>F as shown in Fig. 3.

The coolant **wall** temperatures quoted above are valid only in the non-boiling and nucleate boiling coolant regimes. At some value of the coolant flux,  $(\dot{q}/A_{\rm o}),$ nucleate boiling cannot be maintained, and as *a* transition to the film boiling regime occurs, with a concurrent rapid rise in  $T_o$ ,  $T_i$  also rapidly rises past the melting point, thus the critical heat flux must be considered as a limit, beyond **which** the constrictor cannot operate. **An** often quoted, though seldom achieved, limiting value of the critical heat flux is 10,000 Btu/sec.ft.<sup>2</sup>, and this value **is also** indicated in Fig. **3.** 

From Fig. **3,** it can be seen that two modes of constrictor failure **axe**   $\alpha$  . possible. Failure may be due to a transition to film boiling; alternatively, the large gradients set **up** in **a** relatively thick wall may cause melting at flux levels **well** below the critical level.

**Figs.** 4 **and** *5* **show** similar plots of equations 1 for **1/2" and** 1" diameter constrictors.















### 111. Performance Possibilities of Non-Boiling Convective Cooling

Seban and McLaughlin (Reference **3)** report heat transfer coefficients **ob**tained fron experiments **with** turbulent flow in curved passages, the general configuration of the constrictor coolant passages. Data is reported only for passages of circular cross section and uniform peripheral heating; whereas the constrictors have rectangular passages with the heating concentrated at one side. They found that the average peripheral heat transfer coefficients ex ceeded those for straight tubes. Expressed emperically:

$$
\frac{h_{\text{curved}}}{h_{\text{straight}}} = 1 + 3.5 \text{ (d/D)} \qquad \qquad \text{---} \qquad \text{---} \qquad (2)
$$

where d is the tube cross section diameter and D is twice the radius of curvature of the tube.

Seban and McLaughlin **also** measured the difference between the heat transfer coefficients on the inside and outside of the tube curvature. They found that the secondary flow induced **jn** the curved passage significantly lowered the coefficients *on* the inside. (For d/D = **0.0096** and d/D = 0.059, the inside coefficients were respectively 0.75 and 0.5 of the **mean** peripheral values.)

In some of the  $1/4$ <sup>"</sup> diameter constrictors, the coolant passages have  $d/D$ ratios of 0.2 and greater, so secondary **flow may** be expected to have a significant effect on the constrictor heat transfer coefficients. **A** qualitative picture of the secondary flow pattern is shown in Fig. *6.*  For the case where heating **is**  at one side of the passage only, it can be seen that the heated wall is continually flushed with fluid from the unheated sides, and the heat transfer rates **may** be considerably enhanced over the uniform peripheral heating case.

In view of the lack of information available on heat transfer coefficients for the constrictor geometry, the estimation of the performance possibilities of the non-boiling cooling must be considered a rough estimate at best.

For estimation purposes, the heat transfer in the coolant passages **will** be predicted from the Colburn Equation:

$$
St = \frac{h}{pv_{cp}} = 0.023 \text{ Pr}^{-2/3} \text{ Re }^{-0.2} \text{ ... } (3)
$$

**I.** 

The heat **flux** per unit area is given by:

$$
\frac{d}{dt} = h (t_w - t_{b,av})
$$

where

$$
t_{b,av} = (t_{b,i} + t_{b,0}) / 2 \qquad \qquad \ldots \qquad (5)
$$

The maximum possible non-boiling heat transfer rate is attained with the **wall**   $t$ emperature at the point of incipient nucleate boiling. The wall temperature at this point has been shown to be of the order of 20<sup>0</sup>F of superheat (Reference 4). Thus:

$$
t_w = t_{s,0} + 20
$$

Note that the bulk temperature rise in the coolant passage is related to the heat flux:

$$
q = \dot{m} c_p (t_{b,0} - t_{b,1}) \qquad \qquad - - - - - - - \tag{7}
$$

For a given passage cross section, **flow** velocity, **and** outlet pressure, equations **3** - 7 can be solved iteratively to yield the heat flux at incipient boiling.

Generally, the flow velocity and outlet pressure is related through the total head capability **of** the system. If **we** consider the upstream pressure a constant, as dictated by the pressure capabilities **of** the fittings, etc., then **an** lncrease in exit pressure obtained by doimstream throttling **will** be accompanied by a decrease in flow velocity. Experience shows that in the constrictors only about one-half the pressure head difference is converted into kinetic energy, frictional losses accounting for the remainder.

With these assumptions, equations **3** - *7* have been solved for one passage cross section  $(D_h = 0.09 \text{ in.})$ , one bulk inlet temperature  $(70^{\circ}\text{F})$ , and three supply pressures  $(P_i = 1000, 500, 100)$  with various outlet pressures. The results are shown in Fig. 7. **An** increase in outlet pressure at a given supply pressure results in a decrease in flow velocity and an increase in wall temperature, the latter tending to increase the heat transfer and the former tending to decrease it. The result is **an** optimum outlet pressure for each supply pressure; however, the curves are rather flat near their maximum point.







#### *N.* Performance Possibilities with Surf ace Boiling

The most workable scheme at present for predicting the burnout heat flux in a flow boiling situation is the superposition method where a pool boiling burnout heat flux is added to a forced convection, non-boiling heat flux. particular scheme which has been most extensively compared with available experimental data is that proposed by Gam'bill (Reference *5).*  "his scheme predicts the burnout heat flux,  $(\dot{q}/A)_{b=0}$  as: The

$$
\left(\frac{\dot{\tilde{q}}}{A}\right)_{b.o.} = \left(\frac{\dot{\tilde{q}}}{A}\right)_{Sat-pool,b.o.} \cdot F_{sub} + \left(\frac{\dot{\tilde{q}}}{A}\right)_{non-boil,b.o.} \cdot \cdot \cdot - - - (8)
$$

where  $(\dot{q}/A)_{Sat-pool,b.o.}$   $\cdot$  F<sub>sub</sub> represents the boiling contribution to the burnout heat flux in the absence of forced convection and  $(\dot{q}/A)_{\text{non-boil},b.o.}$  $\text{term } (\dot{q}/A)_{\text{Sat-pool},b.o.}$  represents saturated pool boiling burnout and  $F_{sub}$  is a factor introduced to correct the saturated pool boiling burnout results for nonsaturated, or subcooled, conditions. represents the forced convection contribution in the absence of boiling.

The available experimental evidence indicates that many of the available correlations for  $(\dot{q}/A)_{Sat-pool,b.o.}$  can be used with success in this superposition method. For simplicity, the Rohsenow-Griffith equation (Reference 6) has been used in the present study.

$$
\left(\frac{\dot{q}}{A}\right)_{\text{Sat-pool},b.o.} = 143 \, h_{fg} \left(\frac{1}{v_g}\right) \left[\frac{v_g}{v_f} - 1\right]^{0.6} \qquad \qquad -- -- -- (9)
$$

The ratio of the subcooled to saturated pool-boiling burnout heat flux,  $F_{sub}$ , **is** given by Bonilla (Reference 7). .

$$
F_{sub} = 1 + \frac{c_p \Delta t_{sub}}{25 h_{fg}} \left(\frac{v_g}{g}\right)^{0.923} \qquad \qquad -- -- -- (10)
$$

The non-boiling contribution at burnout is calculated from the convective rate equation :

rg r  
contribution at burnout is calculated from the convective  

$$
\left(\frac{\dot{q}}{A}\right)_{non-boil,b.o.} = h \left(t_w - t_{b,av}\right)_{b.o.} \qquad -- -- -- -- (11)
$$

The calculation of this latter contribution requires knowledge of the amount of wall superheat at burnout; however, considerable disagreement exists in the published literature **6s** to this amount. Bernath (Reference 8) has given a general relation for the amount of wall superheat (at burnout) which **indi**cates reductions in **wall** superheat with increases in flow velocity. Because of the evident uncertainty in the exact level of wall superheat at burnout, the convective contribution to the burnout heat flux has been calculated with wall temperatures of 20<sup>°</sup>F above saturation. This is approximately the amount of superheat at incipient boiling, and should result in a somewhat conservative estimate of the burnout heat **flux.** 

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The non-boiling contribution,  $(\dot{q}/A)_{\text{non-boil},b.o.}$ , is thus given for the present system by Figure 7. The saturated pool boiling contribution and subcooling factor have been evaluated for a bulk temperature of *70%* for a range of pressures **up** to the critical pressure, and these are presented in Figures 8 and *9.*  The total non-convective contribution,  $(\dot{q}/A)_{Sat-pool,b.o.}$  <sup>\*</sup> F<sub>sub</sub> is plotted in Figure 10. It should be noted that one apparent effect of large amounts of subcooling is to lower the optimum pressure for **maximum** heat flux far below the one-third critical pressure generally recognized for saturated boiling and evident in Figure  $8$ .

Finally, if the boiling and convective contribution of Figures *7* and **LO** are summed, the predicted burnout flux as a function of supply and discharge pressures is as shown in Figure 11. These results indicate that for maximum heat fluxes, the passage outlet pressure should be maintained at from one-third to one-half the supply pressure.

Most of the available experimental data for subcooled flow boiling has been obtained with passage hydraulic diameters much larger than those required for the constrictor cooling. **One** notable exception to this is the work of Bergles (Reference  $9$ ). He presents burnout data for straight circular tubes with diameters and lengths congarable to those employed in the constrictors.

The superposition scheme outlined above has been used to predict the effect of outlet pressure on burnout flux for the condition presented in Figure **3** of Reference 9. This comparison is shown in Figure 12, and indicates the predicted values are approximately 50% of the observed values. Nevertheless, the observed trend of the results with outlet pressure is similar to that predicted, and the

difference in magnitude can perhaps be explained by the inadequacy of Equation 3 and the conservative estimate of the wall superheat at burnout. This comparison **lends** some degree of confidence to the use of the superposition scheme for predicting the effect of coolant pressure on the burnout flux.

.









FIGURE 12

COMPARISON - DATA OF REF, 9 AND PREDICTIONS



psia

#### **<sup>V</sup>**. Experimental Apparatus

Constrictors with several different coolant passage configurations were built and tested in the apparatus shown in Fig. **13. A** direct current arc **was** initiated between the cazbon electrodes through three test constrictors. Distilled water was circulated through each constrictor, and the flow rate through the center constrictor was metered with a rotameter. The energy input to the center constrictor **was** determined by **an** energy balance on its coolant flow, utilizing upstream and downstream thermocouples on the center constrictor flow lines. This coolant flow temperature difference was recorded on a **CEC** recording oscillograph along with the arc current.

Boron nitride was used for the insulating mfers on both sides of **all** three constrictors. The outermost wafers were replaced after each run, and these plus the larger boron nitride end pieces, served to shield the constrictors from the anode and cathode heating. It is felt that this shielding was successful in reducing **end** effects since some **runs** were'taken with only the test constrictor between the two shields, and the results of these **runs** compared favorably with those obtained with three constrictors.

The constrictor configurations tested *are* shown in **Figures 14** through 17. Ten constrictors of each type were fabricated. The radius ration,  $r_o/r_i$ , on the' two port and four port configuration is **1.4.**  *On* the eight port configuration, radius ratios of both 1.4 and 1.6 were tested. In addition, some older constrictors of both two port and four port designs, but with a radius ratio of 2.75, were tested. These older constrictors were electron beam fabricated rather than silver brazed. **All** of the test constrictors had plasma hole diameters of 0.25 inches.

# FIGURE 13



EXPERIMENTAL APPARATUS









#### VI. Experimental Results

Melting Failures. In testing each constrictor configuration, successive runs were made with increasing arc currents until rupture of the coolant passage occurred. The time required to achieve steady state, as indicated by the recorder traces, **&as** approximately two seconds. **<sup>A</sup>**typical recorder trace is shown in Figure 18.

**Many** of the test sequences with the electron beam welded constrictors were terminated prior to **a** true failure by the appearance of stress leaks at the **weld.**  Some of the silver brazed constrictors **also** developed leaks around the braze, but these were found to **be** much more reliable than the beam welded disks.

For the 2.75 radius ratio constrictors with good **welds,** the pattern of failure **was** as follows. First, after a run at a certain current level, the dismantled constrictors exhibited melting at the edges of the plasma hole. In most cases, there **was** mainly rounding of the edges of the hole, but in some cases there was a noticeable enlargement of the hole diameter. This first stage of melting took place without causing any coolant passage leaks; however, subsequent runs with slightly higher arc currents always resulted in a complete failure of the coolant passage. For both the two **and** four port 2-75 radius ratio constrictors, the first signs of melting occurred at plasma side heat fluxes of from 3500 to 4000 Btu/(ft<sup>2</sup>sec). This value is consistent with Figure **3,** which predicts premature melting for these constrictors.

**<sup>A</sup>**possible explanation for the subsequent failure of these constrictors is that the liquid copper shorts ecross the boron nitride separating the constrictors, resulting in attachment of the *arc* to the constrictors and increased local heating rates at the attachment points.

Burnout Failures. **The** failure pattern observed in the test sequences for. the 1.4 and 1.6 radius ratio constrictors was quite different than that followed by the larger radius ratio disks. Failure in these tests occurred before steady state **was** reached, but at a flux level higher than that reached in the preceding run at steady state. No local melting **was** noted in the run immediately preceding the failure. This conforms to the pattern that would be expected for a burnout failure. The failure in **all** cases **was** accompanied **by** a distinct "pop" sound,

which could be characteristic of burnout in this situation. The failure in these tests **was** generally very complete, with large portions of the coolant passage WaJl completely destroyed.

In the two and four port constrictors, the flow turning and accelerations are such that any vapor formed which remains in the flow would be forced to the heated side of the passage by buoyant forces. This would enhance the possibility of the vapor coalescing into a film, triggering burnout. is overcome by the eight port design which essentially reverses the turning direction. Moreover, this design takes advantage of the high convective heat transfer coefficients normally associated with flow impingement normal to a surface. This tendency

The test results indicate burnout fluxes from  $5,000$  to  $6,000$  Btu/(ft<sup>2</sup>sec) <sup>2</sup>for the two port design, around 6,400 Btu/(ft sec) for the **four** port design, and between  $7,000$  and  $8,000$  Btu/(ft<sup>2</sup>sec) for the eight port design.

The failure results for test sequences not spoiled by stress leaks are summarized in Table I. For all **the** runs the supply pressure **was** approximately **100** psia; the discharge pressure approximately **30** psia.

# TABLE **I** - EXPERIMENTAL RESULTS



 $Btu/(ft<sup>2</sup>sec)$ **a** 

**b**  Melting, further increases in heat flux result in failure

*C*  Apparent burnout **<sup>3</sup>**



#### VII. Discussion

The eight port constrictor configuration **vas** designed and tested with the thought that the reverse turning of the flow would result in a delaying of transition boiling and an increase in the critical. heat flux. The present test results appear to support this argument; however, it may be that the higher burnout flux is due **more** to higher non-boiling convection coefficients than to any enhancement of the boiling behavior. It can be observed in a comparison of Figures  $7$  and  $11$  that the non-boiling convective contribution to the burnout heat flux is a large percentage of the total flux even at low supply pressures, and accounts for an even larger amount at higher supply pressures. *As* a result, increases in the non-boiling convective coefficient result in significantly higher burnout fluxes.

The highest burnout fluxes observed in the present tests are approximately four times higher than those predicted by Figure 11; however, it is not inconceivable that the convective coefficients are four times higher than those calculated by the Colburn Equation. The developing, impinging flow, together with heating **on** only one wall and a strong secondary flow pattern, **are** factors which would tend to increase the average passage heat transfer coefficient. In addition, it should be noted that the reported heat fluxes *are* based on the heated side area only. Some heating does occur on the sides of the passage, and the effective coolant side fluxes may be only **1/2** to **2/3**  the reported values.

Without specific non-boiling heat transfer correlations for the constrictor geometry and boundary conditions, it is impossible to determine the relative magnitude of the burnout flux and the flux at incipient boiling. **If** . the boiling contribution is **small,** then constrictors should be designed to operate below incipient boiling, where problems such as flow oscillation and flow excursion do not occur.

The compressibility of the flow system can lead to these instabilities when boiling takes place inside the flow passage. The instabilities result in premature burnout soon after boiling starts. **The** problem can be solved by throttling the flow immediately upstream of the heated section, but this

reduces the system head and the convective coefficient. In the present tests, no throttling **was** done upstream of the constrictors, **and** the burnout observed could be the result of' flow oscillation.

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**4** 

With the present test data, **and the** trends predicted by Figure 11, it **seems** possible that coolant side fluxes up to 2-1/2 times the present values, or 18,000 Btu/(sec ft $^2$ ) can be achieved with a 1000 psia supply pressure.