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GA-8705

FINAL REPORT

for

COLLISIONS OF ELECTRONS AND IONS WITH HYDROGEN ATOMS

(8 May 1967 - 7 May 1968)

Contract No.: NAS 5-11025

Prepared by Gulf General Atom': Incorporated P.O. Box 608, San Diego, California 92112

for

Goddard Space Flight Center Greenbelt, Maryland

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ABSTRACT

A study of 2p excitation of the hydrogen atom under electron impact is reported. The major finds have been the resonance structure just above the threshold of excitation, which was not predicted, and just below the threshold of n = 3, which was predicted but which for higher angular momentum states does not agree with theory. Resonance structure above n + 3 has also been observed.

Dissociative excitation of H_2 and D_2 has been studied under high electron energy resolution. Several new dissociation channels have been identified. Gaseous filtering techniques to be applied to radiations in the vacuum ultraviolet were studied. Some of the computer codes used on this program are given in the report, along with abstracts and papers published this year.

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1. INTRODUCTION

During the past year, primary attention has been focused upon the collision of highly resolved electrons with hydrogen atoms leading to the excitation of the lowest radiative state of the atom, i.e.,

$$e + H(1s) = H(2p) + e$$
.

As in the case of elastic scattering of electrons from hydrogen atoms, inelastic scattering, particularly in the vicinity of the various levels of the hydrogen atom, is dominated by the formation of the temporary compound negative ion states.

In Section 3 of this report, the resonances found in the 2p channel immediately above the excitation threshold are discussed; in Section 4, those below and above the n = 3 level of the hydrogen atom are considered. In Section 5, a comparison is made between the measured cross section in the vicinity of threshold and the best calculated values.

Complementing the study of electrons colliding with the hydrogen atom, a study has been made of the collision of electrons with the hydrogen molecule and the subsequent dissociative excitation of the 2p state of the hydrogen atom,

in competition with

 $e + H_2 = H(2p) + H(1s) + e$ $e + H_2 = H(2p) + H^-$.

The contribution to 2p excitation from the second reaction is small. The measurements made on H_2 are unfortunately complicated by ultraviolet radiation other than Lyman-alpha which passes through the few narrow windows in the O_2 filter. In Section 6, the results of a short study of gaseous and chemical filters are discussed; in Section 7, the results of dissociative excitation are reviewed.

Since the primary purpose of the program is to test theory and to relate the results with the theory, we have been conducting under NASA's support a small theoretical program. This program is discussed in Section 8. Because of the extreme complexity of the 2p excitation problem, we have developed a number of computer codes to process and analyze the data in next year's program. In Section 9 these codes are discussed and are thus made generally available to the scientific community. Finally, Section 10 presents a discussion of other activities that have complemented the program.

Abstracts of papers presented at scientific meetings appear in Appendix I, and articles that resulted from studies made on this program are included as Appendix II.

2. NEW INSTRUMENTATION

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The apparatus used this year is essentially that used last year except for minor changes in electronics and the addition of a photo detector on a rotating table. The photo detector was designed to detect Lyman-alpha radiation. During this period two types of photon counter were used. The first was the iodine-filled Geiger counters developed some years ago in this laboratory. This was replaced by an Electromechanical Research multiplier photo tube with lithium fluoride optics. It is an 18-stage silver magnesium dynode multiplier with a potassium bromide photocathode. The geometry chosen had a side window.

The spectral sensitivity of the tube extended from 1050 Å to 1500 Å with very high sensitivity at the Lyman-alpha level (1216 Å). This new photo tube has the necessary characteristic that long wavelengths are amply rejected. The photo tube was chosen to replace the iodine-filled Geiger counter for two reasons. First, estimates indicated that the photo tube would be from a factor of 3 to 10 more sensitive than the Geiger counter. Second, since the experiments required extensive counting times, extreme reliability of all parts was necessary. It was felt that the photo tube, which has essentially infinite lifetime, would be a sensible substitute for the Geiger counter, which is unpredictable in its operating characteristics and comparatively short lived.

Unfortunately, the expectations for the sensitivity of this tube have not been met. At the very most, sensitivity has been increased by a factor of 2. However, since the time of its installation six months ago, the photo tube has required no service even though it has been in continuous operation for most of this time.

Between the photo detector and the interaction volume defined by the electron and hydrogen atom beams, a 1-cm-long cell with lithium fluoride windows is placed and is filled with molecular oxygen. It is a strange quirk of nature that in the absorption spectrum of molecular oxygen, one of seven very narrow windows is centered around Lyman-alpha, i. e., at 1216 Å. For the chemical (gaseous) filter to pass Lyman-alpha, the oxygen must be dry. If any moisture is present, the transmission of the cell can be greatly reduced. Consequently, dried oxygen is continuously flowed through the cell.

The experimental demands associated with the study of 2p excitation of atomic hydrogen have been excessive. The experiments have required the complete stability of the electronics, the electron beam, the hydrogen atom beam, etc., over periods well in excess of 24 hr to collect a significant number of data. In many experiments, data have been taken in 0.015-V intervals with from 60 to 100 points per cycle. For each cycle, then, the total interval is 0.9 eV for 60 data points and 1.5 eV for 100 data points. The normal counting time per data point is 1 min. If there are 60 points per cycle, the time for one cycle is 1 hr. It is interesting to compare the results that can be obtained from one cycle with those that can be obtained when a number of cycles are summed together. An example (Run 39C) is given in Figs. 1 and 2. Figure 1 shows one of 35 cycles, while in Fig. 2 all 35 cycles have been summed. In the single cycle, no feature is recognizable. In the composite Fig. 2, the 2p excitation threshold is clearly defined and the resonance near the threshold can be seen. The randomness observed below threshold gives some idea of the fluctuation of the background.

At the peak of the resonance, Fig. 2 shows approximately 300 counts for the integrated signal. One standard deviation for the (signal plus background) and background combined is approximately ± 30 counts. The resonance peak, as shown in Fig. 2 and in many of the earlier runs, was only slightly more than twice this standard deviation.

To define the first resonance above the 2p excitation threshold and to determine whether or not there are subsequent resonances, it was necessary to conduct an experiment that ran for 109 cycles. In this instance, there were 40 points per cycle. The time required for continuous running was in excess of 70 hr.









3. THE 2p EXCITATION THRESHOLD

In this section, we discuss the excitation of H(2p) from threshold to 0.6 eV above threshold. The collision region is shown schematically in Fig. 3. A modulated rectangular beam of hydrogen atoms nearly 90% pure is crossed with a rectangular beam of electrons with an energy distribution that ranges from 0.06 eV to 0.18 eV. Electrons from a source 127° electrostatic electron energy analyzer enter a magnetic and electric field free region, cross the modulated hydrogen atom beam from below, and pass into a collector in which a crossed electric field can be applied to collect all the electrons. When this crossed field is removed, the electrons can pass through the collector to a second electrostatic energy analyzer, where the energy distribution of the electrons is measured.

Photons from the interaction of the two beams were normally detected at an angle of 54.5° with respect to the direction of the bombarding electrons. At this angle the measured signal was proportional to the total 2p excitation cross section. (1) Ions from the interaction region were accelerated along the atomic beam axis into a Paul mass filter. As in previous experiments at this laboratory, the linear extrapolation of the ionization efficiency curve to its energy axis was used as a calibration for the electron energy scale. The data were recorded automatically over many hours, as described in Section 2. The system can be programmed to step through a prescribed energy interval. All data were collected digitally; i.e., for each energy interval, the signal plus background (S+N), the background (N), and the electron current were recorded on punched tape to be processed later by the computer. Every 8 to 12 hr, the excitation process was interrupted and an ionization efficiency curve for atomic hydrogen was taken to help fix the electron energy scale for excitation. Over more than 100 hr, in many instances the reproducibility of the onset of the ionization efficiency curves was within ± 0.015 eV.

In Fig. 4, the total cross section measurements near threshold are compared with theory⁽²⁾ and with the previously reported results of Chamberlain <u>et al.</u>⁽³⁾ This comparison is made primarily to show the difference between the resolutions of the two experiments and the width of the structure that one is looking for compared with what has been observed experimentally. In the left-hand portion of Fig. 5, theoretical results are compared with the theoretical predictions wherein the energy



Fig. 3. A sketch of the electron hydrogen atom collision region showing roughly the geometry used in the experiment







Theoretical and experimental values for the total excitation cross section in the approximately $\pm 1\%$. Between 11.60 and 12.20 the uncertainty is less than $\pm 2\%$. vicinity of threshold. From threshold to 10.5 eV the statistical uncertainty is For the rest of the 0.07-eV resolution data it is $\sim 3\%$. Fig. 5.

distribution, approximately 0.07 eV, has been folded into the theoretical curve. As can be seen, the agreement between the measured and predicted shapes of the first resonance is good. It follows, then, that the excitation cross section does consist of a sharp rise, as predicted by Damburg and Gailitis, $^{(4)}$ from a close-coupling approximation calculation that includes the three lowest hydrogen atom states, 1s, 2s, and 2p. It is also clear from our measurements that the sharp resonance predicted by Taylor and Burke, $^{(5)}$ who also used a close-coupling approximation, does really exist within 0.03 eV of threshold. Burke and his associates have shown that the total flux of this resonance is in the ¹P channel of the H⁻ compound state. This resonance unfortunately was not recognizable in the previous calculations of Damburg and Gailitis because of the coarseness of the energy grid used by them.

In the experimental results immediately following the first resonance, there appear to be at least two other broad resonance structures. Although these structures have been recognized from our earliest measurements, it was only recently that the statistics were good enough to permit us to say definitely that they exist. It was also necessary to make certain that these small structures were not due to the excitation of some countable ultraviolet from the collision of electrons with the residual H_2 in the system. Table 1 lists the positions of the most promient structures; however, one must remember that these positions may not correspond exactly to the positions of the resonances themselves, but rather to the resonances with the electron energy distribution folded into them. The use of the finite number of terms in the close-coupling expansion used to describe even these lowest states may be subject to some question since it is not clear how quickly the expansion converges. In the case of the elastic scattering resonances below the first inelastic threshold n = 2, there is every indication that the convergence is rapid. However, it is not yet clear that the ¹P "shape" resonance described by the three-state approximation above = 2 is not better described by an expansion that includes the first six or more states of the hydrogen atom. Unfortunately, Burke <u>et al.</u> (2) have carried out their six-state approximation calculations only from just below the n = 3 level down to within 0.2 eV of the 2p excitation threshold. Over the range where the three- and six-state approximations overlap, i.e., in the region from 0.2 to 1.0 eV above the 2p threshold, the six-state calculation gives a cross section value approximately 8% lower than that given by the three-state approximation.

Another calculation reported by Taylor and Burke⁽⁵⁾ has been carried out using the close-cupling approximation that includes the first three states of the hydrogen atom and potential terms that describe the electronelectron interaction (correlation) as a power series of terms involving r_{12} ,

the distance between the two electrons. Over the same energy range as taken above, the later calculation gives a cross section value that is approximately 20% below that given by the three-state approximation. Near threshold, the correlation terms have now shifted the calculated resonance closer to the threshold and have considerably reduced its width. This is in keeping with the experimental finding. The need for more work on the theory has recently been recognized by Damburg and Geltman, ⁽⁶⁾ who indicate that another possible source of incompleteness results from the lack of the inclusion of polarization terms of order α/r^4 . In the case of 2s excitation, the inclusion of polarization has had a marked effect on the calculated cross section.

TABLE 1

Energy	Description of Structure	Comments
$\overline{10.20 \pm 0.02}$	Steep slope	Onset
10.29 ± 0.02	First max	Predicted ¹ P "shape" resonance
10.45 ± 0.03	Second max	
10.65 ± 0.03	Third max	
11.65 ± 0.03	Small min	Predicted ¹ S resonance
11. 7 7 ± 0.02	Possible min	Predicted ¹ D resonance
11.89 \pm 0.02	Large min	Predicted ¹ P resonance
12.06 ± 0.04	Broad max	"Shape" resonance at n = 3 threshold
12. 16 \pm 0. 05	Min	
12.23 ± 0.05	Small max	
12.35 \pm 0.05	Small max	

STRUCTURE IN 2p EXCITATION CURVE

4. THE 2p EXCITATION IN THE VICINITY OF n = 3

Figure 5 shows details of the experimental cross section from 11. 35 eV to 12. 55 eV. This region overlaps the n = 3 threshold. Bridging the two threshold regions are low resolution measurements. Just below the n = 3 threshold can be seen several recognizable resonances, the most predominant of which appears near 11. 88 eV. A smaller resonance appears in the vicinity of 11. 65 eV. Also shown in the figure is the calculation for the six-state approximation showing a number of resonances. Folded into the calculated cross section is the experimental energy distribution, which is approximately 0. 07 eV. The agreement between theory⁽²⁾ and experiment is not considered good for the ¹P resonance, while for the ¹S resonances the agreement is thought to be quite satisfactory. and the second second

At and above the threshold of n = 3 can be seen a prominent bump, which is most likely associated with a "shape" resonance just above the n = 3 threshold. Part of the flux for this resonance appears directly in the 2p channel. Another portion, most likely the largest part, arrives through cascade from the 3s and 3d states of the atom. The positions of the resonance structure below and above the n = 3 level are included in Table 1.

5. TOTAL CROSS SECTION MEASUREMENTS

Since it is impossible to measure the cross section absolutely, we have determined it from a normalization to the Borne approximation at energies in excess of 200 eV. Although this procedure is not entirely satisfactory, at present there is no simple method available for making an absolute determination. Data have been taken between the 2p excitation threshold and 200 eV; the most precise data, however, have been taken below 60 eV. In fact, continuous data have been taken every 0.1 V from 60 eV until threshold. We have found the most precise way to determine our cross section is to normalize our data to those of Long, Cox, and Smith, who in turn have normalized theirs to the Born approximation. The relative accuracy of their data is $\pm 2\%$.

Although we have not been able to assign to our data relative accuracies as small as this, we have compared our data with those of Long, Cox, and Smith (see Fig. 6). The cross sections defined by the two sets of data points are indistinguishable. It is interesting to note in our data that the finite excitation threshold is recognizable just above 10.2 eV, even though the resolution in this experiment is only 0.18 eV. Also, one can see a hint of the resonance structure in the vicinity of n = 3 and in the continuously taken data below n = 4.

To obtain an accurate estimate of the cross section in the threshold region, the high resolution data were subsequently normalized to the lowest resolution data, thus fixing the cross section scale. The values of the cross section given in Fig. 4 were fixed in this way. It is interesting to note that the cross section thus obtained is only 80% of the lowest cross section predicted. The approximation used to arrive at the cross section closest to the experimental value is the three-state close-coupling approximation, which includes 20 electron-electron correlation terms.

Quite recently, Fite et al. (8) have determined that the Lyman-alpha radiation emitted by hydrogen 2s atoms in a weak electric field is polarized. Consequently, all earlier measurements or estimates of the 2s excitation cross section are in error since no allowance was made for this polarization. Once the cross sections have been corrected for the polarization, at the cross section maximum, which is in the vicinity of n = 3, the value obtained is only 80% of the lowest predicted cross section resulting from the six-state close-coupling approximation.



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It is an informative exercise to estimate the size of the combined excitation cross section for the 3s and 3d states of atomic hydrogen. These data are reflected in the total cross section measurements for the production of the Lyman-alpha radiation since the 3s and 3d cross sections can only couple with the ground state by passing through the 2p state. Although our total excitation cross section for the 2p state does not agree in absolute magnitude with that predicted by Burke et al., it is quite obvious that below the n = 3 level the general shape of the measured and calculated cross sections is the same. Consequently, there is some justification in normalizing the magnitude of the calculated cross section to that of the measured cross section in the region just above the n = 2 level. Having done this, we observe that the calculated portion of the cross section for the 2p state above n = 3 is considerably lower than the total measured cross section (Fig. 5, broken line above n = 3). To a first and perhaps crude approximation, the difference between the measured and normalized theoretical curves can be said to be due to cascade. This difference is shown in Fig. 7. No attempt has been made to include any contribution for the shape resonance above n = 3 in the calculations or to allow for the addition of states above n = 4 in the theory.

It is now possible to compare this difference with the predicted cross sections of Burke et al. As shown in Fig. 7, the agreement between experiment and theory is satisfactory. In fact, even with this crude approximation in which no attempt has been made to account for polarization or other factors, as in the case of 2p excitation, the value of the estimated cross section again lies slightly below that of the predicted cross section. This result is not at all in agreement with the recently published data of Kleinpoppin and Krase⁽⁹⁾ for Balmer-alpha excitation. Since our result depends upon a normalizing of the six-state approximation to the results below n = 3, we hesitate to say their result is in error. Furthermore, it is not clear that the six-state approximation necessarily gives an accurate description of the region above n = 3, although it seems reasonable that it is not in error by much.







6. GASEOUS FILTERS

One of the most important problems associated with the study of the excitation of atomic hydrogen is the unequivocal detection of Lyman-alpha (1216 Å). Provided a large enough signal is available from the experiment, one can use a vacuum ultraviolet spectrometer. However, in experiments such as those performed in this laboratory where the number of photons available is very small, it becomes absolutely necessary to have the largest possible collection efficiency and reasonably large angle of acceptance. It has long been recognized that the Geiger counter, filled with either nitric oxide or iodine and with lithium fluoride optics, could be used to detect vacuum ultraviolet radiation in the vicinity of Lyman-alpha. However, to ensure the unequivocal detection of the Lyman-alpha and particularly to eliminate the molecular radiation normally associated with the bombardment of residual H_2 in the experiment, it was necessary to find a filter that would preferentially pass the 1216 Å radiation.

It was observed by Watanabe⁽¹⁰⁾ and others that in the absorption spectrum of O_2 in the vacuum ultraviolet and in the vicinity of 10 eV there are seven very deep transmission windows, one of which is centered at the Lyman-alpha. It has been the repeated observation in our laboratory that in the study of the excitation of atomic hydrogen to the n = 2 level, the combination of the chemical filter filled with oxygen and either a Geiger counter or a photomultiplier has been an effective detector of Lyman-alpha. However, in the study of the dissociative excitation of H₂, either by proton or electron impact, it has been recognized that there is a large contribution of molecular radiation, which passes either through the other windows or through the optically thick portion of the chemical filter.

To effectively study the dissociative excitation process it is therefore necessary to eliminate this background radiation. To do this, a series of experiments was carried out in which different gases were used as the optical filter. In Fig. 8 we show a schematic diagram of our experiment. In all cases the gases used in the chemical filter flowed through the filter continuously. However, in the case of CO_2 the rate of flow was much slower than in the cases of nitrogen, helium, and oxygen, which were virtually the same. The pressure in all filters was slightly in excess of 1 atm.



A schematic diagram of the photodetector and chemical filter used in these experiments ŝ Fig.

In Fig. 9 we show the relative number of photons reaching the counter as a function of electron energy when electrons bombard H_2 . Four different gases have been used in the chemical filter. The electron energy for these experiments ranges from approximately 10 to 20 eV, an interval which embraces the onset of the molecular radiation at approximately 10.3 eV and the onset of dissociative excitation in the vicinity of 14.7 eV. Figure 9 shows the results when the O₂ filter was used. The onset of the molecular radiation is clearly visible at 10.3 eV, as is the onset of the dissociative excitation of the hydrogen atom in the 2p state near 14.7 eV. From this curve alone we can judge that, once we have moved a few electron volts from the threshold of dissociative excitation, the molecular contribution to the total curve is in the vicinity of 20%. Near threshold for dissociative excitation, of course, the molecular contribution is proportionately larger. Looking at Fig. 9, one can see virtually no difference in the magnitude and shape of the curves for He and N_2 (b and c, respectively), verifying what we already know, i.e., that both He and N2 are transparent in this optical region.

Now that we recognize in curve (a) the onset of the dissociative excitation, we can use curves (b) and (c) to estimate the relative contribution of Lyman-alpha and other molecular radiation as seen by the counter. A reasonable extension of the curve, from below the dissociative excitation threshold to above, gives us this information. Above approximately 16 eV we estimate that the radiation from dissociative excitation is in the vicinity of 20% of the total radiation. This estimate, of course, is approximate, but it is reasonable. In curve (d) the complicated absorption spectrum of CO_2 is seen reflected in the structure of the curve.

To generate Fig. 10, the helium curve has been normalized to the O_2 curve in the vicinity below 14 eV and the helium curve has been subtracted from the O_2 curve in this region. The residual signal is shown in Fig. 10. The fine structure below 14. 7 eV appears to be real for it is present in the curves when either helium or nitrogen is subtracted from the oxygen data. In both cases there is a sharp onset in the vicinity of the dissociative excitation threshold. It is interesting to note that above 16 eV, structure is quite pronounced in the curve.

It must be realized that by subtracting the helium (or nitrogen) data from the O_2 data, we have eliminated part of the dissociative excitation signal in the vicinity above the dissociative excitation threshold. However, this is small (20% of 20%), approximately 4% of the total signal. From this study it is clear that the estimates of the total cross section made earlier by Fite and Brackmann⁽¹⁾ are high by approximately 20%.



Fig. 9. Relative excitation curves obtained with four different chemical filters: (a) molecular oxygen; (b) dry atomic helium; (c) dry molecular nitrogen; and (d) dry CO₂. The pressure in the CO₂ filter is slightly higher than in the other filters



45

The excitation curve for dissociative excitation resulting from the removal of the molecular contribution below 14 eV. This curve is generated by subtracting ~5% of the helium signal from the O_2 curve Fig. 10.

7. DISSOCIATIVE EXCITATION OF MOLECULAR HYDROGEN

From the discussion in Section 6, it is clear that the originally reported value for the dissociative excitation of the 2p state of atomic hydrogen from H₂ was in error due to a large contribution of molecular radiation coming from the interaction region. As can be seen in Fig. 11. the cross section for H₂ is nearly 20% lower than the original measurements of Fite and Brackmann. (1) It is also clear from Fig. 11 that the dissociative excitation of D_2 has a cross section that is only 90% of that of H_2 . This isotope effect is in keeping with the predictions of Platzman, (11) who pointed out that there are a number of molecular states that lie above the first ionization potential. In general, there are two major deexcitation paths available for such excited states, autoionization and predissociation. The first of these processes is nearly mass independent; the time for it therefore should almost be independent of isotope substitution. The time required for dissociation depends on the velocity with which the particles separate and therefore is strongly mass dependent. A similar isotope effect has recently been reported by Burrows and Dunn(12) and by Vroom and deHeer. (13) Shown also in Fig. 11 is the maximum of the Balmeralpha excitation curve of Burrows and Dunn. The shape of the curve is very similar to our H₂ curve.

In our preliminary data, the break in the total excitation curve in the case of H_2 is at a higher potential than in the case of D_2 . It is clear from the figure that in the case of D_2 the channel that includes excitation plus proton formation does not play a major role, whereas in the case of H_2 the onsets of both the formation of two excited states and the formation of the (2p) atom plus a proton are below the major structure that appears in our curve. No doubt this is associated with the isotope effect, details of which are not yet completely understood.

In Fig. 12 we show the excitation curve near threshold. The data shown are only relative. This curve is one from which the energy distribution of our beam has been largely removed. Three sets of data are overlapped. The structure that appears at the end of the first also appears in the beginning of the second; similarly, the structure that appears at the end of the second appears in the beginning of the third. The onset is in the vicinity of 14. 7 eV. There follows a rather straight portion of the curve with very little structure. Then, in the vicinity of 15.8 eV the onset of nearly 12 small ripples, which are fairly evenly spaced, is seen. The spacing between the







12. A segment of the dissociative excitation curve near threshold, from which much of the 0.07-eV electron energy distribution is analytically removed from the curve ripples is in the vicinity of 0. 14 to 18 eV. This series of ripples shows a change above the ionization potential, 15. 43 eV. In fact, the continuous ripple form goes on until nearly 17.8 eV, the dissociation limit of H_2^+ . Above this the nature of the structure changes, and the orderliness seems to disappear. The larger ripples which are apparent in Fig. 10 then seem to dominate. The cause of this structure is not completely understood. It is possible, although not likely, that it is due to the structure in the molecular radiation in the background of our signal, which has not been completely removed. If, however, this structure is related to the dissociative excitation of H_2 into the 2p channel, then one is prompted to suggest either that it results from a temporary formation of an H_2^- compound state, which decays into several modes, one the dissociative channel and the other the excitation of molecular levels, or that it reflects competition between predissociation and autoionization, i. e.,

$$e + H_2 \rightarrow H_2^* + e$$
,

followed by

 $H_2^* \rightarrow H(2p) + H(1s)$

 \rightarrow H₂^{*} + e.

competing with

8. THE THEORETICAL COMPLEMENT

During this contract period, Professor J. C. Y. Chen, University of California, San Diego (UCSD), has participated in our study of electron hydrogen collisions. His activities at Gulf General Atomic and at the University have covered the following subjects:

- 1. The application of Faddeev's equation to a number of atomic problems
 - a. (e-H) elastic scattering resonances
 - b. (e-H) excitation threshold
 - c. (e⁺-H) elastic scattering and positronium formation
- 2. Close-coupling calculations (or the (e-H) system in momentum space)
- 3. Electron resonance scattering from molecules

Work is also under way at UCSD on a new variational calculation for (e-H) scattering and on the field detachment of H⁻.

Included in Appendix II is an article that resulted from these studies. In it, Ball, Chen, and Wong have investigated various solutions of the Faddeev equation for Coulomb potentials, and a practical method for solving the Faddeev equations below the three-particle breakup threshold is developed. The method is then applied to the (e, H) system in which the H⁻ bound state and the lowest members of the compound states in both the singlet and triplet series are calculated. The calculated position of the lowest ¹S resonance is in excellent agreement with the experiment, while the width of the lowest ¹S resonance is slightly less than that found experimentally.

Also during this contract year, with the support of NASA and Gulf General Atomic, a series of colloquia on atomic and molecular processes (CAMP) has been conducted. Many of the colloquia were given by people who are actively participating in electron proton and positron hydrogen atom scattering studies. A list of colloquia speakers and their topics is given in Section 10. This spring a two-day "working session" on electron hydrogen atom collisions was held in La Jolla. The primary purpose of this session was to consider the programs presently under way and to determine what information could best be obtained from experiment to direct further theoretical studies. The program for this successful working session is also listed in Section 10.

9. DATA PROCESSING FOR ELECTRON-ATOM ELASTIC AND INELASTIC EXPERIMENTS AND A PROGRAM LISTING

The output data from the experimental devices are on punched paper tape. In order to process these data using the 1108 FORTRAN IV programs, the data first must be converted to punched cards or magnetic tape. Because of the ease in handling, storing, etc., the latter was chosen. To aid in understanding the descriptions and the instructions for the use of the various programs involved, a brief listing of terms and definitions is presented below.

9.1. TERMINOLOGY

Paper Tape

Data word: a fixed number of digits plus separator character

Data block: a block consisting of four data words--channel chamber, signal + noise, noise, and current, respectively

Data section: a section of paper tape that contains a finite number of data blocks

Leader: a section of paper tape that is comprised of feed characters

<u>Illegal character</u>: any punch or combination of punches that does not represents digits 0 through 9, a separator, or a feed character

Magnetic Tape

FD (Field Data Code): 2 octal digit code representation for character and digit

Floating point: the form in which a number containing an implied decimal must be before computation in FORTRAN IV can take place with meaningful results

Image tape: magnetic tape on which the image of a paper tape is written, except illegal characters, which are represented as slashes (/) (FD format) Library tape: magnetic tape in which many data sections are stored for later retrieval

Scratch tape: tape used for one computer run only; its contents are not saved

Backup tape: a copy of any magnetic tapo, used for protection purposes

9.2. PAPER TAPE FORMAT

The paper tape must contain a minimum of five feet of leader before the first data section. The leader must be marked "START" in large letters. Each data section must be separated by a minimum of 18 inches of feed characters. Five feet of 'eader must follow the last data section.

9.3. DESCRIPTION AND INSTRUCTIONS

This section contains a description of the function of each of the following programs used in conjunction with the electron scattering experiments, along with a detailed set of directions for use and a listing of the complete program for each.

Program Name

Program Function

- 1. READPT Used with the 1004 paper tape reader to read the paper tape and write the information on a magnetic tape. A slash (/) is written on the magnetic tape for any illegal character in the paper tape.
- 2. TEDIT Reads the magnetic tape as written by READPT, converts data from FD to floating point format, and stacks information on a library data tape. Output consists of printed tape and printer plots. Eliminates any illegal characters (slashes) by linear interpolation or direct substitution.
- 3. TREAD Reads the data library tape written by TEDIT and lists all runs on this tape.
- 4. ABEAM4 Reads the data library tape written by TEDIT and provides various calculations and printer plots as requested by user.
- 5. COPY Reads the data library tape and copies the information onto backup tape.
| 6. | UPIATE | Allows the user to make certain changes to the data
on the library tape. A new library tape is written
and the original library tape remains unchanged. |
|-----|--------|--|
| 7. | LEØF | Reads the data library tape, lists all experiments by
number, and writes end of file on the tape. (It was
designed to place an end of file on the library tape
when it was omitted by TEDIT through oversight on
the part of user or through a fault of the computer
during a TEDIT run.) |
| 8. | SMØØTH | Fourier-smooths data, unfolds a given Gaussian
electron energy distribution from the data, and gives
the results in tabular form. At present only the
derivatives of the data are given. The program is
prepared to accept card input. The deck of cards
needed is generated as one of the options in ABEAM4. |
| 9. | SIMCUR | Folds into any given function a Gaussian distribution
of specified full width at half maximum. The results
are generated in both tabular and graphic form. |
| 10. | SIMTAB | Folds into any function in tabular form a Gaussian
distribution of specified full width at half maximum.
A ninth-order polynomial interpolation scheme is
included in this program. The results are given in
both tabular and graphic form. |

STEP 1: READPT

The information contained on the paper tape is transferred to a magnetic tape by the READPT program. The READPT program is an integral part of the 1108 system; therefore, no program deck is required by the user.

The paper tape must be in the format described in Section 9.2. A data card must be punched for each data section on the paper tape to be read by READPT. The format of the data card is as follows:

1	B	9	0 5 6	07	e e	ŀ	11	ļ	14	1 1 5 6	17	13	! 9	2	2	22	2 2	2	2	27		j 0	3	3			211	2		6	4	2		4	6	4	4	5	5 5	5	5	5 5 5 6	5	5	5 6 9 0	6	6 2	6 6 3 4	6	6 6	6 8 7 8	6 6 9 9	7 0	7	77	<u>]</u> [ŝ	7	7 7 7 2	- 8 9 0
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4	ا_ل	Ц	سل	Ļ		1.	<u>. </u>	ŀ	_		1		Ļ	_	1	_L		┞	ப		-1-	1	μ	1	ı	1.	-	μ	J.	41		+	.1.,		_	I.	┢	L		1.1	4	_1_	-		1	ŀ		4	L_)	4		-	-		╀	_ <u>_</u>		L	4	1.1
4		ப		+	4	+	ĿĿ	╀			1	•	μ	-	-	-	1	╞	<u> </u>	-	-	1	μ		1	1	1	┝╍	4	لب ه		+	-1-				┢	Ц	-		┥	<u> </u>	-		_1	ľ		+	<u>ل</u> ـــه	Ì	-1	_	<u> </u>		╉	_	<u>н</u>			<u>.</u>
1	<u>ب</u>		L.H.,	t	- -	1	<u></u>	ť			<u>+</u>		μ		-		- <u>1</u> -	t			_ب_ ر		Η		<u>ــ</u>		4 1		1	1 		†	-		 ,	.) ,	Ľ		 1		Ì	-	<u>.</u>	1_1 1_1		Ľ		1	<u>.</u>		_1	ــد. ــاــــــــــــــــــــــــــــــــ	<u></u>		t		<u>–</u>	1- 1-		і_І_
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The information in columns 1 through 7 is mandatory. The information starting in column 19 for identification of each data section is arbitrary. Below is an example READPT input deck for a paper tape containing three data sections.

	C C C C L Z		22222	222222		111444 111444	444444	455555	5 5 5 5 5 6	666666	666777	7 7 7 7 7 7 7 8
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The printed output from READPT consists of three data blocks per line. Slashes are substituted for any illegal characters in the paper tape.

Prior to the start of step 2, the TEDIT program, the output listing from READPT is examined for errors. A data section is made up of one or more cycles. The channel numbers normally run sequentially, starting at 00000, to a maximum of 00099 for each cycle. In order for TEDIT to recognize the start of a new cycle it is mandatory that each starting channel number be all zeros (00000) and contain no slashes. TEDIT will correct all other channel numbers that contain slashes.

On the output listing from READPT, columns 1, 5, and 9 are the channel numbers. If errors in the paper tape have caused the channel numbers to shift from these columns, the paper tape must be corrected and step 1 repeated until all errors of this type have been eliminated.

The computer program is not included in this report since it is a standard library program held at the computer center.

STEP 2: TEDIT

TEDIT reads a data card, then reads a data section from the magnetic tape written by READPT. It converts the tape data from FD to floating point and a fixed point (integer) and writes the information on the library tape (to be used by ABEAM4 program). The printed output from TEDIT contains the following:

- 1. A listing of each data section by cycle
- 2. A printer plot of (signal + noise) (noise) = signal
- 3. A printer plot of current by cycle
- 4. After processing each data section, a listing of $\Sigma^{\tilde{\pi}}$ signal, Σ (signal + noise), Σ noise, Σ (signal/current), Σ ((signal + noise)/current), Σ (noise/current) is given. Also, aprinter plot of Σ signal and Σ (signal/current) is given.

When a blank data card is encountered, an end of file is written on the library tape and processing is completed.

The data card for each data section must be in the following format:

Column	Name of Variables	FORTRAN Format
1-6	Experiment number	A6
7-12	Gas type	A6
13-18	Current variance	F 6.0
19-24	Time of starting experiment	A6
25-30	Resolution	F6.0
31-36	Voltage interval	F6.0
37-42	Initial voltage	F 6.0
43-48	Time interval (sec)	F 6.0
49-54	Approximate minimum signal	F 6.0
55-60	Approximate maximum signal	F6.0
61-66	Approximate minimum current	F 6.0
67-72	Approximate maximum current	F6.0

 $[\]Sigma$ is defined as the summing of each respective channel number over all cycles.

73-79	Date of experiment	A6, A1
80	When a <u>new</u> library tape is to be created, a one (1) must be punched in column 80 of the <u>first</u> data card only. Otherwise, this column is left blank.	I1

Data cards must be in the same sequence as the experiments (data sections) on the paper tape. The information from the data cards is also written on the library tape (except column 80).

Below is an example deck setup consisting of three experiments. The last card must be a blank card.

0	0 C C 2 3 4	0 56	000	c z	1	4 4	79	20	2	2	22	2 2	222	3 3	3	336	1.0	34	442		44 56	4478	45	55	54	55	556 890	66	6 6 3 4	6 6 5 6	6 6 7 8	67 90	7 7	77	777	778 890
R	A.	16	A-I	MAG	E	T/	P	L	<i>U.</i> !	NO.	R	4.4		ļ		44		ட	4	4		-			4		ட்ட	Ŀ		-				11	<u></u> ı	
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[L.I	45		, .H.1			کرر	Ł	4	534	<u>, k</u>		اس			5		1.0	.0		5	. 0		.a.,	d	1,5	a.1		0	.o	1	00	0	1.0	DE:C	6.7
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					Ι.		11			1.1			11			11							.1.1			4 . L . I										

On the 1108 run request form, check "<u>Do Not</u> Rerun This Job." The number of experiments that may be stacked on the data library tape depends on tape size; the maximum number is 200.

A program listing follows.

READ MAIN DATA CARD, ONE PER EACH PAPER TAPE IMAGE ON MAG. TAPE (PTAPE). DIMENSION CHAN(100) . SPLUSN(100) . NOISE(100) . CURR(100) . SIG(100) . 10_READ(5,11) NUM, ITYPE, VAR, TIME, RES, DVOLT, VOLTST, TINT, SIGMIN INTEGER BUFF, BLANK, SLASH, FIVE, ASTER, ERROR, ERRI, ERR2, ERR3, DIMENSION_SUM1(100) . SUM2(100) . SUM3(100) . SUM4(100) . SUM5(100) . 1......C.....CHE PURPOSE OF THIS ROUTINE IS TO READ A MAG. TAPE CONTAINING THE ASTER/6H DIMENSION ERR1(100) . ERR2(100) . ERR3(100) . ERR4(100) . BUFF(90) . ÷ . ; / FIVE/6H5 : i UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 This compilation was done on 02 may 68 at 10:19:07 1 : . PARAMETER PTAPE = 9. LTAPE = 10 ENTRY POINT 000000 / SLASH/6H/ / TEE/6HT 1 WORD (72) . ERROR (12) . DATE (2) ON A LIBRARY DATA TAPE. ł ţ SUM6(100) DATA BLANK/6H X(102) , Y(102) / MINUS/6H-INTEGER CHAN ERR4. TEE REWIND LTAPE REWIND PTAPE COMMON BUFF REAL NOISE IBEGIN = 0 G FOR TEDIT, TEDIT MAIN PROGRAM : 3. C U 18. 21. 22. ÷. 11. 12. 15. 16. 17. ~ **6** 10. 13 19. 23. ŝ ġ 20.

24. 1 ' SIGMAX' CURMIN' CURMAX' DATE(1)' DATE(2)' ITIME		:
25. 11 FORMATÉ 246, F6.0, A6, 8F6.0, A6, A1, I1)		
26. C HAS THE LAST PAPER TAPE IMAGE BEEN PROCESSED?		
27. IF(NUM.NE.BLANK) GO TO 14	•	i
28. 12 CALL REWIGLAPE)		
29CALL REWI (PTAPE)		
30• STOP *	•	
31. C. INITIALIZE CYCLE COUNTER TO ZERO, SET LAST CYCLE FLAG TO ZERO.		
32. 14 KOUNT = 0		
33. DO 15 I=1.100	1	
34•SUM1(1) = 0•0		
35. SUM2(I) = 0.0	•	
36. SUM3(I) = 0.0		1
37. SUM4(I) = 0.0	•	
38SUM5(I) = 0.0		
39. 15 SUM6(I) = 0.0		
40. C SET INDEX COUNTER FOR CHAN, SPLUSN, NOISE AND CURR ARRAYS TO ZERO.		
41. L = 0	· .	
42. WRITE(6+17) NUM+ ITYPE+ VAR+ TIME+ RES		
43. 17 FORMAT(1H1, 9X 10HRUN NUMBER, 1X, A6, // 10X 3HGAS 1X A6,// 10X		
441 10HVARIANCE %, 1X F6.2, // 10X 4HTIME, 1X A6, // 10X 4HRES, 1X		
45. 2 F6.2 /)		
46. WRITE(6/18) DVOLT' VOLTST' TINT' SIGMIN' SIGMAX' CURMIN' CURMAX		
47. 18 FORMAT(10X 17HVOLTAGE INCREMENT 1X F6.2" // 10X 17HSTARTING VOLTA	•	
48. IGE 1X F6.2' // 10X 14HTIME INTERVAL ' F6.2' // 10X 12HMIN. SIGNAL		
49. 2 F10.2' // 10X 12HMAX, SIGNAL 'F10.2' // 10X 13HMIN. CURRENT '		
50 3 F10.2' // 10X 13HMAX. CURRENT , F10.2, /)		•

Name and a

78. 60 T0 70
79. 60 IF(BUFF(I).EQ.BLANK) 60 TO 70
80BUFF(1) = BLANK
B1. 70 CONTINUE
82. C RETRANSLATE RECORD, RECORD NOW CONTAINS DIGITS AND BLANKS ONLY, NO SLASHES.
83. CALL GINPUT (WORD' N)
84. C., SEE IF A NEW CYCLE IS STARTING WITHIN LAST TRANSLATED RECORD, WORD(1),
85. C WORD(S) OR WORD(S) WILL EQUAL ZERO.
8680 IF(L.EQ.0.AND.KOUNT.EQ.1) 60 TO 100
87. IF(N.6T.4) 60 TO 82
80. Zit
89
90 82 IF(N.6T.8) 60 TO 84
91. <i>N</i> = 6
92. 60 TO 85
93. 84 N = 12
94 85 D0 90 K=4.1.4
95
96. IF(WORD(J)) 90, 120, 90
97. 90 CONTINUE
98. C NO NEW CYCLE PLACE ALL WORDS INTO PROPER ARRAYS.
99. JSAVE=0
100. 100 DO 110 J =1.N.4
101. L = L + 1
102. C TEST FOR EXCEEDING RESERVED STORAGE.
103. IF(L.6T.100) GO TO 300
104. CHAN(L) = WORD(J) + .5

105. \$PLUSW(L) = WORD(J-42) 107. 0015E(L) = WORD(J-42) 107. CURR(L) = WORD(J-42) 107. ERRAIL) = ERROR(J-4) 108. ERRAIL) = ERROR(J-4) 109. ERRAIL) = ERROR(J-4) 111. ERRAIL) = ERROR(J-4) 112. EON TO 40 113. EON TO 40 114. LIO ERRAIL) = ERROR(J-4) 115. JASNE = J 114. LIO ERRAIL) = ERROR(J-4) 115. LA EXTER ITTHIN LAST RECORD. 116. LO ERRAIL) = ERROR(J-4) 117. K = JANE = J 118. L = L + 1 128. CHRIL) = WORD(J+2) 128. CHRIL) = WORD(J+2)		
106. NOISC(L) = VORD(J+2) 107. CURR(L) = ERROR(J+1) 108. ERR(L) = ERROR(J+1) 109. ERR(L) = ERROR(J+1) 109. ERR(L) = ERROR(J+2) 110. ERR(L) = ERROR(J+2) 111. ERROR(J+2) 112. ERROR(J+2) 113. GO TO 40 114. LE0 JSMTCH = 0 115. JSMTCH = 0 116. IF(JSMC.Ec.L) 60 TO 140 117. K = JSMTCH = 0 118. JSMTCH = 0 119. L = L + 1 110. IS JSMTCH = 0 111. K = SAWE = 4 112. K = SAWE = 0 113. L = L + 1 114. L = L + 1 112. L = L + 1 113. L = L + 1 114. L = L + 1 112. L = L + 1 113. L = L + 1 120. CHINICI = MORCU+1 121. L = L + 1 122. CHINICI = WORCU+1 123. CHINICI = MORCU+1 124. L = L + 1	105. SPLUSN(L) = WORD(J+1)	
107. CURR(L) = KANG(L+3) 108. ERR(L) = ERNOR(J+1) 110. ERR(L) = ERNOR(J+2) 111. 110. ERN(L) = ERNOR(J+2) 111. 110. ENTE = U III. 111. 120. ENTE = U III. 112. FC.A. A NEW CYCLE STARTS WITHIN LAST RECOMD. III. 113. L.O. A NEW CYCLE STARTS WITHIN LAST RECOMD. III. 114. L20. ENTE = U 115. L21. FC III. 116. L21. ENDIXI. ENDIX. 117. K = JANE III. ENDIXI. 118. DO 130. GaT VARCE III. III. 119. L11. L = L + 1 III. III. 120. C TEST FOR EXCEEDIAG RESENTED STORAGE. IIII. III. <	106. NOISE(L) = WORD(J+2)	
108. ERRIL, 1 = ERROR(J) 109. ERRIL, 1 = ERROR(J) 111. ERRIL, 2 = ERROR(J) 112. G0 TO 40 113. EGNL = J 114. EGNL = J 115. ERRIL, 0 116. ERRIL, 0 117. K = JSAVE.EG.J) 60 TO 140 118. EGNL = J 119. L = L + 1 120. EGNL = VORD(J) + JS 121. L = L + 1 122. EGNL = VORD(J) + JS 123. EFUL.6F.100 60 TO 300 124. L = L + 1 129. L = L + 1 120. C TEST FOR EXCEDIAG RESERVED STORAGE. 121. EFUL.6F.100 60 TO 300 122. EVRIL, 1 = VORD(J) + JS 123. EVRIL, 1 = VORD(J) + JS 124. ERRIL, 1 = SCORD(J) 125. ERRIL, 1 = SCORD(J) 126.	107. CURR(L) = WORD(J+3)	
109. ERR2(L) = ERROR(J*1) 110. ERR3(L) = ERROR(J*2) 111. 110 ERR*(L) = ERROR(J*2) 112. 60 To 40 113. Co. A NEW CYCLE STARTS WITHIN LAST RECORD. 114. 120 ERR*(L) = ERROR(J*3) 115. Co. A NEW CYCLE STARTS WITHIN LAST RECORD. 115. USWE = J 116. TF'USARE-E0.1) 60 TO 140 117. K = JSWE - 4 118. D0 130 JER/CH = 0 119. D0 130 JER/CH = 0 110. D0 130 JER/CH = 0 111. K = JSWE - 4 112. L = L + 1 123. L = L + 1 124. L = L + 1 125. CHAN(L) = WORD(J+1) + 5 126. C++. TEST FOR (-H) 127. ERRAR(J-+2) 128. MORD(J+2) 129.	108. ERR1(L) = ERROR(J)	
110. ERRS(L) = ERROR(J+2) 111. 110 ERR*(L) = ERROR(J+3) 112. 60 TO 40 113. G.0. A NEW CYCLE STATTS WITHIN LAST RECOND. 114. 120 ISWTCH = 0 115. USAVE = J 116. 117. 117. K = JSAVE - 4 117. K = JSAVE - 4 118. D0 130 JE1/K+4 119. D1 30 JE1/K+4 110. L = L + 1 120. L+ = L + 1 121. L = L + 1 122. CHANIL) = WOR(J+1) + .5 123. FIL-61100 60 TO 300 124. L = L + 1 120. C++. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 120. C++. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 122. CHANIL) = WOR(J+1) + .5 123. FIL-61100 60 TO 300 124. L = L + 1 125. CHANIL) = WOR(J+1) + .5 126. C++. TEST FOR (-+	109. ERR2(L) = ERROR(J+1)	
111. 110 ERAN(L) = ERGR(LU*3) 112. 60 T0 40 113. Co. A NEW CYCLE STARTS WITHIN LAST RECORD. 114. 120 ISWTCH = 0 115. USAVE = J 116. IF(LSAVE.E0.1) 60 TO 140 117. K = JSAVE - 4 118. D0 130 JE_1K.W 119. L = L + 1 120. L. = L + 1 121. K = JSAVE - 4 121. Mature State Storace. 121. L = L + 1 120. L. = L + 1 121. L = L + 1 122. CHAN(L) = WOR(J) + .5 123. SPLUSN(L) = WOR(J) + .5 124. MOTECI) = WOR(J) + .5 125. CHAN(L) = WOR(J) + .5 126. GNR(L) = WOR(J) + .5 128. SPLUSN(L) = WOR(J) + .5 129. FRIL) = ERROR(J+1) 120. CHAR(L) = ERROR(J+2) 121. ERROL(J+2) 122. ERROL(J+2) 123. FROR(J+2) 124. ERROR(J+2) 125. ERROR(J+2) 126. FROR(J+2	110 ERR3(L) = ERROR(J+2)	
112. 60 T0 40 113. C A NEW CYCLE STARTS WITHIN LAST RECORD. 114. 120 ISATCH = 0 115. JSAVE = J 116. IF(JSAVE.E0.1) 60 TO 140 117. K = JSAVE - 4 118. D0 130 J=1.K.4 117. K = JSAVE - 4 118. D0 130 J=1.K.4 119. L = L + 1 120. C.+. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 120. C.+. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 120. C.+. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 120. C.+. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 120. C.+. TEST FOR EXCEEDING RESERVED STORAGE. 121. L = L + 1 122. CHAN(L) = WOR(L+2) 123. FRAIL(L) = WOR(L+2) 124. NOTSE(L) = WOR(L+2) 125. ERR1(L) = ERROR(L+2) 126. TSERVEL (-1) 127. ERR2(L) = ERROR(L+2) 128. TSEROR(L+2) 1	111110 ERR4(L) _ = ERROR(J+3)	
113. C A NEW CYCLE STARTS WITHIN LAST RECOND. 114. 120 ISATCH = 0 115. USAVE.EE4.1) 60 T0 140 116. IF (USAVE.EE4.1) 60 T0 140 117. K = USAVE.e4.1) 60 T0 140 118. Do 130 J=1.64.4 119. L = L + 1 119. L = L + 1 120. L = E + 1 121. IF (L.6T.100) 60 TO 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSH(L) = WORD(J) + .5 124. IF (L.6T.100) 60 TO 300 125. CHAN(L) = WORD(J) + .5 126. C TEST FOR EXCEEDING RESERVED STORAGE. 121. IF (L.6T.100) 60 TO 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSH(L) = WORD(J) + .5 124. IS (L.0TL) = WORD(J) + .5 125. CURR(L) = WORD(J) + .5 126. ER1(L) = ERROR(J) 127. ER1(L) = ERROR(J+1) 128. ER1(L) = ERROR(J+1) 129. I20. ER1(L) = ERROR(J+1) 120. C TEST EACH ERROR L+2) 121. ER13. TO CLAST TOTE I-1.	112. GO TO 40	•
114. 120. ISMTCH = 0 115. JSAVE = J 116. IF(JSAVE.EG.1) 60 TO 140 117. K = JSAVE - 4 118. DO 130 J=1KK4 119. L = L + 1 120. CTEST FOR EXCEEDING RESERVED STORAGE. 121. IF(L.GF.100) 60 TO 300 122. CHAN(L) = WORD(J) + .S 123. SPLUSN(L) = WORD(J) + .S 124. NOISE(L) = WORD(J) + .S 125. CURR(L) = WORD(J) + .S 126. CHAN(L) = WORD(J) + .S 127. SRU(L) = WORD(J) + .S 128. ERR(L) = ERROR(J) 129. IZ7. 120. C TEST EACH ERROR (LA-1) 121. ERROR(J+1) 122. CURR(L) = ERROR(J+1) 123. ERR2(L) = ERROR(J+1) 124. IZ8. 125. CURR(L) = ERROR(J+2) 126. ERR2(L) = ERROR(J+1) 127. ERR2(L) = ERROR(J+2) 128. ERR2(L) = ERROR(J+2) 129. C TEST EACH ERROR FLAGE IS USETITUTE I-1. 130. C TEST EACH ERROR FLAGE IF CORRELI) OR CURRITI IS IN ERROR </td <td>113C A NEW CYCLE STARTS WITHIN LAST RECORD.</td> <td></td>	113C A NEW CYCLE STARTS WITHIN LAST RECORD.	
115. JSAVE = J 116. IF(JSAVE.Ee.1) 60 T0 140 117. K = JSAVE - 4 118. D0 130 J=1,K.4 119. D0 130 J=1,K.4 119. D0 130 J=1,K.4 120. L = L + 1 121. IF(L.6F.100) 60 T0 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSN(L) = WORD(J) + .5 124. MOISE(L) = WORD(J) + .5 125. CURR(L) = WORD(J+1) 126. ERR1(L) = WORD(J+1) 127. ERR1(L) = WORD(J+1) 128. FRR1(L) = ERROR(J+2) 129. I28. 129. I28. 129. I29. 129. I29. 129. C TEST EACH ERROR (J+2) 129. LEST EACH ERROR (J+2) 129. C TEST EACH ERROR LJ+1) 129. C TEST EACH ERROR LJ+1) 129. C TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 130. C TEST EACH ERROR LJ+1)	114120ISWTCH = 0	
116. IF (USAVE.E0.1) 60 T0 140 117. K = USAVE - 4 118. D0 130 U=1:K:4 119. D0 130 U=1:K:4 119. D0 130 U=1:K:4 120. L=L+1 121. IF(L.61.100) 60 T0 300 122. CHAN(L) = WOR0(J) + .5 123. SPLUSN(L) = WOR0(J+1) 124. NOISE(L) = WOR0(J+2) 125. CURR(L) = WOR0(J+2) 126. ERR1(L) = WOR0(J+2) 127. ERR2(L) = WOR0(J+2) 128. ERR2(L) = ERROR(J) 129. I28. 129. I29. 120. Los IN (J+1) 121. ERR0R(J+1) 122. ERR3(L) = ERROR(J+1) 124. I30. 125. I30. 126. ERR3(L) = ERROR(J+1) 129. C TEST EACH ERROR FLAGE. 130. C TEST EACH ERROR FLAGE. 131. C. 131. C. 131. C. 131. C.	115. JSAVE = J	
117. K = JSAVE - 4 119. D0 130 J=1.4(.4 119. L = L + 1 20. C TEST FOR EXCEDING RESERVED STORAGE. 121. IF(L.6T.100) 60 TO 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSN(L) = WORD(J+1) 124. MOISE(L) = WORD(J+1) 125. CURR(L) = WORD(J+2) 126. ERR1(L) = WORD(J+2) 127. ERR2(L) = ERROR(J+1) 128. ERR2(L) = ERROR(J+1) 129. 130 ERR4(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 129. C TEST EACH ERROR FLAG. IF CHAN(1) IS IN ERROR SUBSTITUTE I-1. 130. C TEST EACH ERROR FLAG. IF CHAN(1) IS IN ERROR SUBSTITUTE I-1. 131. C	116. IF(JSAVE.EQ.1) 60 TO 140	
110. D0 130 J=1.K.4 119. L = L + 1 120. C TEST FOR EXCEEDING RESERVED STORAGE. 121. IF(L.61.100) 60 T0 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSN(L) = WORD(J+1) 123. SPLUSN(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+2) 126. ERR1(L) = ERROR(J+1) 126. ERR1(L) = ERROR(J+1) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 129. C TEST EACH ERROR FLAGE. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 130. C TEST EACH ERROR FLAGE. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1.	117. K = JSAVE - 4	
119. L = L + 1 120. C TEST FOR EXCEEDING RESERVED STORAGE. 121. IF(L.6T.100) 60 TO 300 122. CHAN(L) = WORD(J) + .5 123. SPLUSN(L) = WORD(J+1) 124. NOISE(L) = WORD(J+1) 124. NOISE(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 124. NOISE(L) = ERROR(J+2) 125. CURR(L) = WORD(J+2) 126. ERR1(L) = ERROR(J+2) 127. ERR2(L) = ERROR(J+1) 127. ERR2(L) = ERROR(J+1) 128. ERR2(L) = ERROR(J+1) 129. I30 ERR4(L) = ERROR(J+2) 129. C TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C 131. C 131. C	118. DO 130 J=1.K.4	
120. C TEST FOR EXCEEDING RESERVED STORAGE. 121. IF(L.GT.100) 60 T0 300 122. CHAN(L) = WORD(J+1) 123. SPLUSN(L) = WORD(J+1) 124. WOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+2) 126. ENR1(L) = ERROR(J+3) 126. ENR1(L) = ERROR(J+1) 127. ERR1(L) = ERROR(J+1) 128. ENR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 129. 130 C TEST EACH ERROR FLAG: IF CHAN(I) IS IN EROR SUBSTITUTE I-1. 131. C	119. L = L + 1	
121. IF(L.6T.100) 60 T0 300 122. CHAN(L) = WORD(J+1) 123. SPLUSN(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+3) 126. ERR1(L) = ERROR(J) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+1) 129. I30 ERR4(L) = ERROR(J+3) 129. I30 ERR4(L) = ERROR(J+3) 129. C TEST EACH ERROR FLAG: IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C IF SPLUSN(I), NOISE(I) OR CURRIT) IS TU EDROP	120. C TEST FOR EXCEEDING RESERVED STORAGE.	
122. CHAN(L) = WORD(J) + .5 123. SPLUSN(L) = WORD(J+2) 124. NOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+3) 126. ERR1(L) = ERROR(J) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+1) 129. 130 ERR4(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+3) 129. 130 ERR4(L) = ERROR(J+3) 120. C TEST EACH ERROR FLAG: IF CHAN(I) IS IN ERROR SUBSTITUTE I=1. 131. C	121. IF(L.6T.100) 60 TO 300	
123. SPLUSN(L) = WORD(J+1) 124. NOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+3) 126. ERR1(L) = ERROR(J+3) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 130. C TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C	122. CHAN(L) = WORD(J) + .5	•
124. NOISE(L) = WORD(J+2) 125. CURR(L) = WORD(J+3) 126. ERR1(L) = ERROR(J) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+2) 120. C TEST EACH ERROR (J+3) 131. C IF SPLUSN(I) MOISE(I) OR CURR(I) IS IN ERROR	123. SPLUSN(L) = WORD(J+1)	
125. CURR(L) = WORD(J+3) 126. ERR1(L) = ERROR(J) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+3) 129. 130 ERR4(L) = ERROR(J+3) 130. C TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C	124. NOISE(L) = WORD(J+2)	
126. ERR1(L) = ERROR(J) 127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+3) 120. C TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C	125. CURR(L) = WORD(J+3)	
127. ERR2(L) = ERROR(J+1) 128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+3) 130. C. TEST EACH ERROR FLAG. IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C IF SPLUSN(I), NOISE(I) OR CURR(I) IS IN ERROR	126. ERR1(L) = ERROR(J)	
128. ERR3(L) = ERROR(J+2) 129. 130 ERR4(L) = ERROR(J+3) 130. C TEST EACH ERROR FLAG, IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C IF SPLUSN(I), NOISE(I) OR CURR(I) IS IN ERROR	127. ERR2(L) = ERROR(J+1)	
129. 130 ERR4(L) = ERROR(J+3) 130. C TEST EACH ERROR FLAG, IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C IF SPLUSN(I), NOISE(I) OR CURR(I) IS IN FEBOR	128. ERR3(L) = ERROR(J+2)	
130. C TEST EACH ERROR FLAG, IF CHAN(I) IS IN ERROR SUBSTITUTE I-1. 131. C IF SPLUSN(I), NOISE(I) OR CURR(I) IS IN FOROP	129. 130 ERR4(L) = ERROR(J+3)	
131. C IF SPLUSN(1), NOISE(1) OR CURR(1) IS IN FAROR	130. C TEST EACH ERROR FLAG, IF CHAN(I) IS IN ERROR SUBSTITUTE I-	
	131. C IF SPLUSN(1), NOISE(1) OR CURR(1) IS	IN FEROR

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132.	C INTERPOLATE FOR ITS VALUE.
133.	140 D0 180 I=1.L
134.	IF(ERR1(1).NE.BLANK) CHAN(1) = I-1
135.	IF(I.NE.1) 60 TO 150
136.	11 = 2
137.	12 2 3
138.	G0 T0 170
139.	150 IF(I.NE.L) 60 TO 160
140.	
141.	12 = L-1
142.	G0 T0 170
143.	160 II = I-1
144.	
145.	170 IF(ERR2(I).EQ.BLANK) 60 TO 172
146	<pre>SPLUSN(I) = (SPLUSN(I2)-SPLUSN(I1))+FLOAT(I-I2)/FLOAT(I2-I1) +</pre>
147.	1 SPLUSN(12)
148.	172 IF(ERR3(I).EQ.BLANK) 60 TO 174
149.	NOISE(I) = (NOISE(I2)-NOISE(I1))+FLOAT(I-I2)/FLOAT(I2-I1) +
150.	1 NOISE(12)
151.	174 IF(ERR4(1).EQ.BLANK) 60 TO 180
152.	CURR(I) = (CURR(I2)-CURR(I1))+FLOAT(I-12)/FLOAT(I2-I1) + CURR(I2)
153.	180 CONTINUE
154.	C UPDATE LTAPE WITH THIS CYCLE DATA.
155.	IF(IBEGIN.NE.0) 60 TO 182
156.	IBEGIN = 1
157.	IF(ITIME.EQ.1) 60 TO 184
158.	CALL NTRAN(LTAPE, 8, 1, 8, -1)

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159.	BACKSPACE LTAPE
160.	GO TO 183
161	CALL NTRAN(LTAPE, 8, -1)
162.	BACKSPACE LTAPE
163.	IF(KOUNT.GT.1) 60 TO 185
164. 183	LAST = 1 .
165.	WRITE(LTAPE) LAST
156. 184	WRITE(LTAPE) NUM+ ITYPE+ VAR+ TIME+ RES+ DVOLT+ VOLT5+ TINT+
167	* SIGMIN' SIGMAX' CURMIN' CURMAX' DATE(1), DATE(2)
168.	60 TO 186
169. 185	LAST = 0
170.	WRJTE(LTAPE) LAST
171. 186	WRITE(LTAPE) KOUNT, L
172.	WRITE(LTAPE) (CHAN(I), SPLUSN(I), NOISE(I), CURR(I), I=1,L)
173.	LAST = 2
174.	WRITE(LTAPE) LAST
175.	END FILE LTAPE
176CCA	LCULATE SIGNAL VALUE FOR PLOTTING.
·77.	X(1) = VOLTST
178.	X(L+2) = VOLTST + FLOAT(L=1)+DVOLT
179.	NIW9IS = (T)A
180.	Y(L+2) = SIGMAX
l81.	D0 190 I=3rL
182.	X(I+I) = VOLTST + FLOAT(I-I)*DVOLT
183.	SIG(I) = SPLUSN(I) - NOISE(I)
184.	SNW1(I) = SNW1(I) + SIG(I)
85.	SUM2(I) = SUM2(I) + SPLUSN(I)

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186.	SUMB(I) = SUMB(I) + NOISE(I)
187.	SUM4(I) = SUM4(I) + SIG(I)/CURR(I)
188.	SUMS(I) = SUMS(I) + SPLUSN(I)/CURR(I)
189.	SUM6(I) = SUM6(I) + NOISE(I)/CURR(I)
196.	190 Y(I+1) = SIG(I)
191.	200 WRITE(6+201) NUM+ KOUNT
192.	201 FORMAT(30X+ 14HPLOT OF SIGNAL 5X 4HRUN A6+ 5X 5HCYCLE+ 13)
193.	C PLOT VALUES OF SIGNAL.
194.	CALL PLOT(X, Y, L+2, 102, 46, 6)
195.	C PLOT VALUES OF CURRENT.
196.	WRITE(6,31)
197.	WRITE(6,202) NUM KOUNT
198.	202 FORMAT(30X' 15HPLOT OF CURRENT 5X 4HRUN A6, 5X 5HCYCLE' 13)
199.	Y(1) = CURMIN
200.	Y(L+2) = CURMAX
201.	DO 203 I=1.L
202.	203 Y%I+1) = CURR(I)
203.	CALL PLOT(X, Y, L+2, 102, 46, 6)
204.	C LIST ALL DATA FOR THIS CYCLE.
205.	KRITE(6,31)
206.	WRITE(6+204) NUM+ KOUNT
207.	204 FORMAT(22X+ 4HRUN A6+ 5X 5HCYCLE+ 13, // 16X 5HCHAN. 5X 3H5+N+
208.	1 9X 14W1 10X1 1411 10X1 142 //
209.	WRITE(6/206) (ERR1(1), CHAN(1), ERR2(1), SPLUSN(1) ERR3(1),
210.	1 NOISE(I), ERR4(I), CURR(I), SIG(I), I=1,L)
211.	206 FORMAT(14X+ A2+ I3+ 2X+ A2+ F7+0+ 2X+ A2+ F7+0+ 2X+ A2+ F7+0+
212.	1 4X, F10.3)

WRITE (6+208)

213.

208 FORMET(6X+ 66H* INDICATES THE VALUE TO THE RIGHT CONTAINED AN ILL 214.

215. IEGAL CHARACTER. / 8X 36HTHE NEW VALUE HAS BEEN INTERPOLATED.

216. C., TEST FOR END OF PAPER TAPE IMAGE.

217. IF(ISWTCH.NE.0) 60 TO 240

218. C. PREPARE FOR A NEW CYCLE ON PRESENT PAPER TAPE IMAGE.

C++ RESET INDEX COUNTER FOR CHAN+ SPLUSN+ NOISE AND CURR ARRAYS TO ZERO+ 219.

220. L= 0

221. IF(JSAVE.EQ.0) 60 TO 30

222. DO 210 I=JSAVE,N.4

223. L = L + 1

224. C. TEST FOR EXCEEDING RESERVED STORAGE.

225. IF(L.6T.100) 60 TO 300

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226. CHAN(L) = WORD(I) + .5

227. SPLUSN(L) = WORD(I+1)

228. _____ NOISE(L) = WORD(I+2)

= WORD(1+3)

CURR (L)

229.

230. ERAJ(L) = ERROR(I)

231. ERR2(L) = ERROR(I+1)

232. ERR3(L) = ERROR(1+2)

233. 210 ERR4(L) = ERROR(1+3)

234. 60 T0 30

235. C.. END OF THIS PAPER TAPE IMAGE.

236. C.. PLOT VALUES FOR SUMMATION OF SIGNAL VS. VOLTS.

237. 240 WRITE(6/31)

238. 260 WRITE(6/261) NUM

239. 261 FORMAT(30X 27HPLOT OF SUMMATION OF SIGNAL 5X 3HRUN A6

WRITE(6+293) (CHAN(I), X(I+1), SUM1(I), SUM2(I), SUM3(I), SUM4(I), 301 FORMAT(1H1, 14H **ERROR** RUN, A6, 3X, 5HCYCLE, I6, 33H CONTAINS 291 FORMATI 30X 35HPLOT OF SUMMATION OF SIGNAL/CURRENT 5X 3HRUN A6) 292 FORMAT(50X 3HRUN A6# 5X 23HSUMMATION OF ALL CYCLES // 5X 5HCHAN. 1 10X SHVOLTS 12X 1HS 13X 3HS+N 13X 1HN 13X 3HS/I 9X 7H(S+N)/I IMORE THAN 100 CHANNELS. / 27H REMAINDER OF DATA IGNORED. PLOT VALUES FOR SUMMATION OF SIGNAL/CURRENT VS. VOLTS. SUM5(I), SUM6(I), I=1,L) CALL PLOT (X, SUM1, L, 100, 46, 6) CALL PLOT (X, SUM4, L, 100, 46, 6) 0 *DIAGNOSTIC* MESSAGE(S) . 253 FORMAT(18, 4X, 1P7E15.4) 300 WRITE(6,301) NUM. KOUNT 11X 3HN/I /) WRITE(6+291) NUM WRITE(6,292) NUM WRITE(6,31) WRITE (6,31) G0 T0 12 GO TO 10 END OF LISTING. βNO 5 242. 245. 254. 257. 248. 250. 251. 255; 259. 243. 246. 249. 256. 240. 244. 247. 252. 253. 258. 241.

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UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F4614B THIS COMPILATION WAS DUNE ON 02 MAY 68 AT 10:19:11 B FOR GINPUT, GINPUT

ENTRY POINT 000314 SUBROUTINE GINPUT

SUBROUTINE GINPUT (WORD, N) -

C.. THIS ROUTINE IS A MODIFIED VERSION OF GINPUT. . م

3. ____C... THE FOLLOWING MODIFICATIONS WERE MADE

C __ 1) COL IS NOW IN COMMON. ÷

2) STATEMENTS 5 AND 6 ARE NOW COMMENTS. U 5.

6. C THE PURPOSE OF THIS ROUTINE IS TO READ 72 COLUMNS OF FREE FORMATED

7.

C... WORD IS THE ARRAY IN WHICH THIS ROUTINE STORES THE CARD INFORMATION. **.**

C....IT MUST BE DIMENSION 72 IN THE MAIN PROGRAM FOR ALPHA-NUMERIC INFO.

TITLE CARDS ARE THEN WRITTEN USING 72A1 FORMAT. υ 10.

C.. N WILL INDICATE THE FOLLOWING TO THE MAIN PROGRAM... 11.

1) N = 72 . CARD WAS ALPHA-NUMERIC. U 12.

2) N =-72 + CARD WAS ALL BLANK EXCEPT FOR AN EQUAL SIGN. 13.

3) OCNC72 • CARD CONTAINED N FLOATING POINT VALUES, THE FIRST IS ÷

STORED IN WORD(1), SECOND ONE IN WORD(2), ETC. ŝ

-724N40+ SAME AS 3) EXCEPT AN EQUAL SIGN WAS FOUND AT LEAST 3 ۇ

ONE SPACE BEYOUND THE LAST FLOATING POINT NUMBER.

ALL BLANK CARD. 5) N = 0 18.

C.. IF A CHARACTER OTHER THAN A PLUS OR MINUS SIGN, COMMA, BLANK, DIGIT, 19.

DECIMAL POINT OR EQUAL SIGN IS DETECTED ON A CARD THEN THE CARD IS υ 20.

INTERPRETED AS ALPHA-NUMERIC IMEDIATELY. 21. C

C.. THE PURPOSE OF THE EQUAL SIGN IS TO SERVE AS A FLAG FOR WHATEVER THE 22.

USER WISHES. Ų 23.

C.. THE FORTRAN E FORMAT IS NOT ALLOWED. THE LARGEST ALLOWABLE NUMBER IS 24.

999999999. OR 9X10**9. J 25.

INTEGER COL. TESTWD 26. DIMENSION WORD(72) + TESTWD(16) + COL(72) + FWORD(72) 27.

COMMON COL 28.

EQUIVALENCE (FWORD, COL) 29.

DATA (TESTWD(1),I=1,16)/1H0, 1H1, 1H2, 1H3, 1H4, 1H5, 1H6, 1H7, 30.

1 148, 149, 14 , 14, 0 14, 14, 14, 14- 14- / 31.

5 READ 61 (COL(1) 1 11172) U 32.

C. 6 FORMAT(72A1). 33.

X N O 34.

46

SUM = 0.0 36. DEC = 0.037.

I = 09I 38.

....8 SIGN = 1.0 39.

C.. FIND FIRST NON-BLANK CHARACTER. 40.

D0 7 1=1.72 41.

IF (COL(I) .NE.TESTWD(II)) 60 TO 11 42.

7 CONTINUE • 10 =

0 H Z

44.

GO TO 16 45.

C.. BEGIN TESTING AT START OF NEW WORD. 46.

10 IF(COL(I).EG.TESTWD(11)) 60 T0 20 47.

11 IF(COL(I).EQ.TESTWD(15)) 60 T0 30 48.

MINUS BLANK

49. IF(CoL(I).EQ.TESTWD(16)) 60 TO 40	PLUS
50. IF(COL(I).EG.TESTWD(13)) 60 TO 50	DECIMAL
51	
52. IF(COL(I).EG.TESTWD(J)) 60 TO 60	0 THRU
53. 12 CONTINUE	
54IF(COL(I).E0.TESTWD(12)) 60_T0_70	COMMA
55. 15 IF(COL(I).E0.TESTWD(14)) G0 T0 80	EQUAL
56. C. CHARACTER WAS ALPHA-NUMBERIC.	I
57• N = 72	
58. 16 D0 17 1=1.72	
59. 17 WORD(I) = FWORD(I)	
60. 18 RETURN	
61. Z0 G0 T0(22, 18),1G0	
62. $22.1 = 1 + 1$	
63	
64• C	
65. 30 SIGN = -1.0	
66. C. CHARACTER WAS A MINUS SIGN.	
67. GO TO 22	•
68• C	
69. 40 SIGN = +1.0	
70. C CHARACTER WAS A PLUS SIGN.	
71. 60 TO 22	
72. C	
73. 50 K = -1	
74. C CHARACTER WAS A DECIMAL POINT.	

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75. KSAVE = 0
76. C INDICATE DECIMAL WAS FOUND.
77. DEC = 1.0
78. 60 TO 100
79. C
80. 60 K = 10
81. C CHARACTER WAS A DIGIT.
82. C ASSUME WORD HAS 10 SIGNIFICANT DIGITS TO THE LEFT OF THE DECIMAL.
83. 60 TO 120
84•C
85. C CHARACTER WAS A COMMA PRECEDED BY BLANKS OR ANOTHER COMMA.
36. 70 N = N + 1
87. WORD(N) = 0.0
86. I = I + 1
89. 60 TO 10
90
91. C CHARACTER WAS AN EQUAL SIGN.
92• 80 IF(N) 84• 82• 84
9382 N = -72
94. RETURN
95• 84 N II =N
96. RETURN
97 . C
98. 100 I = I + 1
36.
100. IF(I-72) 110. 110. 105

0 THRU 9 DECIMAL COMMA BLANK C... BUILD UP WORD BY ADDING ON DIGIT JUST FOUND. 101. C.. INDICATE ENTIRE RECORD HAS BEEN TRANSLATED. 117. ____C. SAVE POSITION WHERE DECIMAL WAS FOUND. IF (COL(1) . E0. TESTWD(J)) 60 TO 120 IF(COL(I).E0.TESTWD(13)) 60 T0 130 IF(COL(I).E0.TESTWD(12)) 60 T0 135 IF(COL(I).E0.TESTWD(11)) G0 T0 135 120 SUM = SUM + FLOAT(J=1)+10+0++K C... SEE IF A DECIMAL POINT WAS FOUND. C.. INDICATE THAT DECIMAL WAS FOUND. 135 IF(DEC) 140, 138, 140 110 D0 112 J=1.10 130 KSAVE = K + 1 138 KSAVE = K + 1 60 T0 135 GO TO 100 112 CONTINUE DEC = 1.0GC TO 100 60 TO 10 _ 105 IG0 =2 111. C 107. 116. 104. 106. 102. 115.___ 120. 105. 103. 110. 109. 112. 114. 119. 108. 113. 118. 123. 122. 124. 121. 125. 126.

49

a

COUNTER.
WORD
UPDATE
127.

140 N = N + 1 128.

_ WORD(N) = (SUM/10.0**KSAVE)*SIGN 129.

0°0 = WNS 130.

SIGN = 1.0 131.

DEC = 0.0 60 TO 20 132.

133.

END 134.

0 +DIAGNOSTIC+_MESSAGE(S). END OF LISTING.

B FOR PLOT.PLOT UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F4614B This compilation was done on 02 may 68 at 10:14:13

122

No. of the No.

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SUBROUTINE PLOT ENTRY POINT 000510

:

1

#DIAGNOSTIC* THE NAME OR ADDEADS IN A DIVENCIAN AS ------

		THE WARE ON AFPEARS IN A ULMENSION OR TYPE STATEMENT BUT IS A	JEVER F	REFERENCED.
		SUBROUTINE PLOT(X,Y,N,N1,N2,NOUT)		PL070010
2	•••	DIMENSION X(1),Y(1),IP(150),B(6),A(18),NB(6),NA(18)	u	2010020
· m		DIMENSION_B1(6)+82(6)+83(6)+NB1(6)+NB2(6)+NB3(6)	<u>a</u>	PLOTOO30
* *		EQUIVALENCE (A,NA) + (B+NB) + (C+NC) + (D+NC)	. 4	
5.		EQUIVALENCE (B1/NB1)/(B2/NB2)/(B3/NB3)	. 0	N OTORA
• •	J	X=ABCISSA VALUES TO BE PLOTTED		
7.	U U	Y=ORDINATE VALUES TO BE PLOTTED		
8.	U	N=NUMBER OF POINTS TO BE PLOTTED (150 OR LESS)		
•6	U U	IF N IS NEGATIVE THE Y ARRAY IS IN DESCENDING ORDER		
10.	U	NI=NUMBER OF PRINT WHEELS TO BE USED (108 OR LESS)		
11.	U	N2=NUMBER OF LINES TO BE USED (RECOMMEND 50)		0010101
12.	U	NOUT=TAPE NO. OF OUTPUT TAPE	E 1	
13.	U	RESTORATION AND HEADING OF DICT TO LITTE TO THE	ī.	L010120
14.2		THE PART AND THE AUTING OF PAGE IS LEFT TO USER	đ	LOT0130
			Ìd	_0T0140
15.	U	ALL BLANKS	đ	-070150
16.		DATA C/6H /	. đ	010160
17.	U	ALL NEGATIVE SIGNS - BOTTOM LINE USE	ā	010170
18.		DATA D/6H/		
10,	Ĺ		2	010180
•	, ر	STARS IN VARIOUS POSITIONS - BLANKS FILLED IN (6)	۲ ۲	070190
20.	U	SUBSTITUTE OCTAL EQUIVALENT OF * IN THIS STATEMENT	Ъ.	0T0200
21.		DATA в/6н<верда•6на<врда•6насрада•6наасрав•6надасла•6надарся•6надарс/	L L	0T0210

U	MASK FOR PICKING OUT SECTOR	PL0T0220
	UATA B1/0770000000000000000000000000000000000	PL0T0230
	10000000770000,00000007700,000000000000	PL0T0240
υ	MASK FOR COMPARING TO BLANK	PL0T0250
	DATA 82/64 89980,648 9988,6498 888,6408 99,64088 9,640888 8,6499888 /	PL070260
U	WASK FOR SUBTRACTING ONE	PL0T0270
i	0 A T A B3/6HE 99999 • 6HOE 9999 • 6HOE 999 • 6H009E 90 • 6H0090E 9 • 6H09999E /	PL0T0280
	DATA LARGE/000100000000/	PL0T0290
	INTEGER AND.OR	PL0T0300
ů		
•	IFLGEL	PL0T0320
	IF (N.LT.0) IFL6=2	PLCT0330
	(N) SAFTEN	PL0T0340
U	INITIALIZES FORMAT	PL0T0350
	D0 9 L=1+18	PL070360
	6 V(T)=C	PL0T0370
Ċ,	SEARCHES X POINTS FOR HIGHEST AND LONEST VALUES	PL.0T0380
:	X#IN=1.6438	PL0T0390
	XMAX::+1.E+38	PL0T0400
	D0 10 1=1*N	PL0T0416
	XMAX=AMAX1(XMAX*X(I))	PL0T0420
	10 XMIN=AMINI(XMIN*X(I))	PL0T0430
	DELTAX=(XMAX-XMIN)/(FLOAT(N1-1))	PL0T0440
U,	REORDERS Y INTO DESCENDING VALUES	PL0T0450
	60 T0 (20,15),1FLG	PL0T0460

17. 15	00 16 1=1 N/1=1	PL0T0470
48.	IP(I)=I	PLOTG480
4916	CONTINUE	PL0T6490
50.	YMAX=Y (I)	PLOT0500
51.	(N) L=NIWL	PL0T0510
52.	60 TO 25	PL0T0520
53. 20	D0 21 I=1 N/	PL0T0530
54.	IP(I)=0	PL0T0540
55. 21	CONTINUE	PL0T0550
56.	DO 23 I=1.N	PL0T0560
57.	YMAX=-1.E38	PL0T0570
58.	DO 22 J=11N	PL0T0580
59.	IF(IP(J).GE.LARGE) 60 TO 22	PL0T0590
DIAGNOSTIC+	THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.	
60.	IF(Y(J).LE.YMAX) 60 TO 22	PL0T0600
61.		PL0T0610
62•	KK=J	PL0T0620
63. 22	CONTINUE	PL0T0630
64.	IP(I)=IP(I)+KK	PL0T0640
65.	IP (KK) = IP (KK) + L ARGE	PLOT0650
66. 23	CONTINUE	PL0T0660
67.	D0 24 I=1*N	PL0T0670
68.	IP(I)=IP(I)-LApGE	PL0T0680
69. 24	CONTINUE	PLOT0690
70.	IXI=Ib(1)	PL0T0700
71.	IX2=IP(N)	010010

72.		YMAX=Y(IX1)	PLOT072
73.		YMIN=Y (IX2)	PLOT073
74.	52	<pre>beltay=(YMAX-YMIN)/(FLOAT(N2-1))</pre>	PL0T074
75.		DELT=YMAX	PL0T075
76.	U U	PLOTTING SECTION	PL0T076
.17.	•	Nº 141 K=1,N	PL0T077
78.		I=IP(K)	PL01078
79.		J=IP(K+1)	PL0T079
80.	•	IF (K-1) 33, 33, 30	PLOT080
81.	90 20 20) IF(L)31,31,33	PL0T081(
82.	31	. DELT=DELT-DELTAY	PL07082(
83.	•	IF(Y(I)-DELT+.0001) 32/ 33/ 33	
84.	JU ¹	PRINTS BLANK LINES	PL0T084(
85.	32	- T==1	PL07085(
86.		G0 T0 37	PL0T086(
87.	U	PRINT WHEEL POSITION (D.1.2.3N1-1)	PL0T087(
88.	5	NPWP=(X(I)-XMIN)/DELTAX	PL0T088(
89 •	U,	SECTOR(1,2,3,4,5,N1/6+1)	PL0T089(
•06		NSECT= (NPWP/6)+1	PL0T090(
91.	J	POSITION IN SECTOR(1,2,3,4,5,6)	PL0T091(
92.		NF=MOD (NPWP+6)+1	PL0T092(
93.	Ö	PLACES * IN FORMAT	PL0T0930
• 46	5		-PLOT0940
95.		NTST=AND (NA (NSECT) + NB1 (NF))	PL0T0950
96.		IF(NTST+EQ+NB2(NF))G0 T0 100	PL0T0960
97.		NA (NSECT) =NA (NSECT) =NB3 (NF)	PL0T0970

	98.			50 TO 101	
4	Ę				
	• 66	-	100	IA (NSECT) =NA (NSECT) +NB (NF)	PL0T0990
	100.		101	ONTINUE	PL0T1000
	101.	5			-PL0T1010
	102.			(F (K-N) 34, 36, 36	PLOT1020
	103.	U		(EPEATS IF Y(I) AND Y(J) ARE CLOSER THAN DELTAY	PL0T1030
	104.		まの	F(Y(J)-DELT+.0001) 36, 35, 35	
	105.		35		PL0T1050
	106.		-	0 TO 41	PL0T1060
	107.		36		PL071070
	108.	с С		RINTING ROUTINE	PL0T1080
	109.		37	ONTINUE	PL071090
5	110.	- 1	-	RITE (NOUT'38)DELT'(A(IL)'IL=1'18)	PLOT1100
55	111.		38 1	ORMAT (1PE10.3/ 2H I, 1846)	
	112.			F(L)31,39,39	PLOT1120
	113.	U	-	ESTORES FORMAT	PL0T1130
	114.		39 [0 40 IL=1.18	PL0T1140
	115.		104	(11)=C	PLOT1150
	116.		141	ONTINUE	PL0T1160
	117.	U	.	RAWS BOTTOM AXIS	PLOT1170
	118.		.	0 42 I=1,18	PLOT1180
	119.		42	□=(1)	PL0T1190
	120.		<u> </u>	RITE (NOUT+43)(A(I)+1=1+18)	PL0T1200
	121.		43 F	0RMAT(12X+18A6)	PL0T1210
	122.	U	u£.	ESTORES A ARRAY TO BLANKS	PL0T1220
	123.			0 44 I=1,18	PL0T1230

124.	3=(I)V ++	PL071240
125.	C SETS UP * EVERY 10 PLACES FOR LOWER AXIS	PL0T1250
126.	D0 45 I=2,12,5	PL071260
127.	NA(I)=NA(I)+NB(4)	PL011270
128.	NA(I+2)=NA(I+2)+NB(2)	PL0T1280
129.	45 NA(I+3)=NA(I+3)+NB(6)	PL0T1290
130.	NA(17)=NA(17)+NB(4)	PL0T1300
131.	NA(1)=NA(1)+NB(1)	PL071310
132.	WRITE (NOUT+43)(A(I),I=1,18)	PL0T1320
133.	DELTAX=((XMAX-XMIN)/FLOAT(N1))+10.0	PL071330
134.	00 46 1=1,11	PL0T1340
135.	46 A(I)=XMIN+FLOAT(I-1)*DELTAX	PL0T1350
136.	WRITE (NOUT+47)(A(I)+I=2+11)	PL011360
137.	47 FORMAT(16X+1P10E10+4)	PL0T1370
138.	RETURN	PL0T1380
139.	ENO	PL071390
END OF	<pre>> I TETING. 2 #DIAGNOSTIC* MESSAGE(S).</pre>	

STEP 3: TREAD

This program lists the contents of the data library tape as follows:

- 1. All the data on the TEDIT card except column 80
- 2. The cycle numbers in sequence for each experiment (data section) and the number of data blocks (points) that are in each cycle

A version of this program called TREAD LONG PRINT lists signal + noise, noise, and current values for each channel number.

Below is a typical TREAD deck setup.

P	¢) 2 / ?	2	0 5 6	07	e (Ċ				3	; ;	a		ð	2 2	2	2	3	2	5	2	F	2	3	3	16	1	3	4	14	3	4	6	44 78	49	55	52	55 34	5	55	8	56 90	6	6 6 2 3	6	6	6 6 6 7	68	67 90	7	7	7734	7 7 5 6	37		78 90
F		5	G	ø	=,[2	T		4	L)	7		k	Y.	J	64	P	E	Å	u	M	- 2	R	_						_				_				_	L				Ŀ		1	_	1	<u> </u>	_		4				<u>_</u>	_
Ľ								L					L		1	1	Ы	5,1	Ē	đ	Lī	ĽВ	£	40	L.	P	RL	6	ßĮ	10	L	2.E	21	٤.	H.	E	ŝΕ	2	Ļ		1		Ŀ		L	L	1		_		4		L 1	,	L.I	
z	لاب	a	T.	T	RE		DL	L		1	1	_	L	_	Ļ	L	Ц		ı		_	i	<u> </u>	4	1	4			_	Ц	L	1	1.1	L	L				Ļ	_	1	-	┶	-	1.1	ا	1	ب		11	4			1	L	
Ĺ	1			L	_	_		L		_		-		_ 1		L			L	L	_	1		. L		4	<u> </u>		_	_	Ŀ	L		ı	L	_	-	_ 1	Ļ	_	ı		Ŀ	-1-	1	L.	ļ		_		4		<u></u>	L	Ē	_
L	1.				_			L	Ц	J.	L	L			1	L	Ц				_	Ļ	1.1	1		4				-	L	1			Ŀ	_		4	Ļ	_			Ļ			<u>ц</u>	4		-1-	<u></u>	4				با	-
L								L					L		í		Ц		1	L	ц	ł	<u></u>		L	Ц	1	L	_	4	Ļ	Ŧ	ĻĻ	_	L	L	1.1	ц.	Ļ		L	L	Ļ		4	-	1		_		4	1		1		
L	_	Ļ	1	L			1.1	L			-		L			,	1		1			ļ	1			4		1.1		ц	4	ı			L	<u>ب</u>		.1	Ļ	1	1		┶			_	ļ		-		4		ц.		<u></u>	<u>.</u> .
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A program listing follows.

B FOR TREAD,TREAD UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 THIS COMPILATION WAS DONE ON 02 MAY 68 AT 10:19:05

MAIN PROGRAM ENTRY POINT 000000

C.. THE PURPOSE OF THIS ROUTINE IS TO READ THE LIBRARY TAPE AND LIST ALL 4

2. C DATA BY RUN NUMBER AND BY CYCLE NUMBER.

. INTEGER CHAN

REAL NOISE

DIMENSION CHAN(100) / SPLUSN(100) / NOISE(100) / CURR(100) / DATE(2)

PARAMETER LTAPE = 10

REWIND LTAPE

8 READ(LTAPE) NUM, ITYPE, VAR, TIME, RES, DVOLT, VOLTST, TINT,

1 SIGMIN' SIGMAX' CURMIN' CURMAX' DATE(1), DATE(2)

WRITE(6,11) NUM

10.

58

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11. 11 FORMAT(10X, 10HRUN NUMBERA 1X, A6, /)

12. WRITE(6.12) ITYPE

13. 12 FORMAT(10X+ 3HGAS+ 1X+ A6+ /)

WRITE(6,13) VAR

14.

15. 13 FORMATÍ 10X, 10HVARIANCE %, 1X, F6.2, /)

16. WRITE(6,14) TIME

17. 14 FORMAT(10X, 4HTIME, 1X, A6, /)

18. WRITE(6,15) RES

19. 15 FORMAT(10X, 4HRES, 1X, F6.2, /)

20. WRITE(6,16) DVOLT

21. 16 FORMAT(10X, 17HVOLTAGE INCREMENT, 1X, F6.2, /)

22. WRITE(6,17) VOLTST

				·												L. PRNT		•		1,4)	I'L) L. PRNT	L. PRNT			
17 FORMAT(10X+ 17HSTARTING VOLTAGE + 1X+ F6+2+ /)	WRITE(6,18) TINT	18 FCRMAT(10X+ 14HTIME INTERVAL + F6.2, /)	WRITE(6,19) SIGMIN	19 FORMAT(10X+ 12HMIN+ SIGNAL + F10+2+ /)	WRITE(6+20) SIGMAX	20 FORMAT(10X, 12HMAX, SIGNAL , F10.2, /)	WRITE(6+21) CURMIN	21 FORMAT(10X+ 13HMIN+ CURRENT + F10+2+ /)	WRITE(6,22) CURMAX	22 FORMAT(10X+ 13HMAX+ CURRENT + F10+2+ /)	WRITE(6,23) DATE(1), DATE(2)	23 FORMAT(10X+ 4HDATE+ 1X+ 2A6+ /)	10 READ(LTAPE) KOUNT, L	•	WRITE(6+24) KOUNT	24 FORMAT(1H1, 10X, 12HCYCLE NUMBER, 1X, 13, /)	WRITE(6,25) L	25 FORMAT(10X* 16HNUMBER OF POINTS, I5, //)		READ(LTAPE) (CHAN(I), SPLUSN(I), NOISE(I), CURR(I), I=	WRITE(6+27) (CHAN(I)+ SPLUSN(I)+ NOISE(I)+ CURR(I)+ I=	27 FORMAT(110, 3F10.1)	READ(LTAPE) LAST	IF(LAST.EQ.0) 60 TO 10	
							•							U					J						
23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	- 10	35.	36.	37.	38.	39.	+0 •	41.	42.	• 2 +	• † †	45 .	•9•	.7.	

31 FORMAT(1H1) 49. 50.

IF(LAST.EQ.1) G0 T0 8

WRITE(6+28) 51.

28 FORMAT(/ 12H END OF FILE) 52.

CALL REWI(LTAPE) 53.

CALL EXIT Sµ.

END 55. 0 *DIAGNOSTIC* MESSAGE(S). END OF LISTING.

STEP 4: ABEAM4

Input for this program consists of the data library tape, as written by TEDIT, and a set of data cards. The purpose of the program is to perform various calculations based on data from different cycles of the same experiment or from different experiments. The normal output from ABEAM4 is the following (see option 3, below):

1. Σ signal

2. Σ signal smoothed once

- 3. Σ (signal + noise)
- 4. Σ (signal + noise) smoothed once
- 5. Σ (signal/noise)
- 6. Σ noise
- 7. Σ current

Printer plots of the following are also given:

1. Σ signal

2. Σ signal smoothed once

- 3. Σ (signal + noise)
- 4. Σ (signal + noise) smoothed once
- 5. Σ (signal/noise)
- 6. Σ noise

By the use of an option (see option 1, below), the additional information may be obtained along with a printer plot of each.

- 1. first derivative of Σ signal
- 2. first derivative of Σ signal smoothed once
- 3. first derivative of Σ signal smoothed twice
- 4. second derivative of Σ signal smoothed twice
- 5. first derivative of Σ (signal + noise) smoothed once

The input card formats are as follows:

Title Card: FORTRAN format is (12A6)

Column

1-72 Title (printed at top of first page)

Option Card: FORTRAN format is (316)

Column

6	Option 1 = 0 or blank: derivative output not desired
	= 1: desire derivative output
12	Option 2 = 0 or blank: parabolic least squares fit
	for smoothing
	= 1: Fourier series smoothing
18	Option $3 = 0$ or blank: all output is calculated as
	shown below
	= 1: each term in the summation is divided by
	its respective value of current (i. e.,

 Σ (signal/current) etc.)

Run No. Card: FORTRAN format is (A6, 216)

Column

1 -6	Experiment number (IRUN)									
7-12	Number of cycles (NCYC) requested from this experimer									
18	ILAST = 0 or blank: another Run No. card follows the									
	Cycle No. card									
	= 1: another title card follows the next Cycle									
	No. card									
	= 2: no more cards follow the next Cycle No. card.									
	The next Cycle No. card is the last to be									
	summed and all processing is complete									

Cycle No. Card: FORTRAN format is (1216)

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Column	
1-6	Cyc (1) = first requested cycle number
7-12	REFPNT (1)
13-18	Cyc (2) = second requested cycle number
19-24	REFPNT (2)
•	•
•	
•	•
25-66	Cyc (6) = sixth requested cycle number (6)
67-72	REFPNT (6)

Two or more cards of this type may be used if the number of cycles (NCYC) requested exceeds six.

Below is an example deck setup for summing together cycles 3, 5, and 6 from experiment 115; cycles 1 through 10 of experiment L25; and cycles 4 through 9 from experiment 145.

			. 2 2 2 2 2				444444				28321	<u> </u>
ASG.	8-DATA	LIDRA	RY. TAP	e nune	FR				L.A.J. J. J.	بىلىرەلىيە مەلىرەل	مادد فهلباء ،	والمعادية والمراجع
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SUMMIN	6 46 0	15. 12	5. 545		DATE 4	1.1.1.68				1 4 4 4 4		
[
U.I.I.S									1.1.1.1.1.	1.1.1.1.1		4.4.1.4.1.1.4
		5										1.1.1.2
. 1.25												
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htter a	<u>,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,</u>		him	L		<mark>┟╷╀┈┖╓┖╶┛╴┖╴</mark>	╷╄┉┸╶╀╷┻┈╇┯	╶ ╊ _┍ ╺╋ _┲ ╋╼╋╍╇╍		⊷∔⊷∔∼, {⊷ ∔ ⊷∔⊷		╺╂╌╉╌╉╼╉╍╂╍╂╌╂╺╄
			┝┹┹╼┺┸╼			┟┸┺┸┷┥		.↓.↓.↓	╺┻╍╋╍╄╍╇╺┻╍	₋ﻠ _┺ ╬ _╋ ╋╍╇╼┻╼		-t-t-l-t-t-t-t-t-t-t-t-t-t-t-t-t-t-t-t-
يبيبهما	<u> </u>	<u> </u>	L. L.L.	سببنا	سيبينا	Luur	ليتربينا			لمسيبي		لنسب والمساحد

Below is a diagram showing how the summing, Σ , takes place with reference to the channel numbers.



In the diagram, CYC(1) through CYC(4) are arbitrary cycles. The reference points, REFPNT(1) through REFPNT(4), are 3, 5, 1, 3, respectively. In this particular case $N_2 < N_1 < N_3 < N_4$; therefore, it is meaningless to sum past N_2 . The total number of sums that would be printed is $(N_2 - 4) + 1$.

A program listing follows.

WP FOR ABEAM4,ABEAM4 UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 This completion was done on 29 May 68 At 13:59:52

MAIN PROGRAM ENTRY POINT 000000

1. PARAMETER LTAPE = 10

PARAMETER ID=200

INTEGER PCHAR, SLI

INTEGER BLANK, CYC, REFPNT, OPT1, OPT2, OPT3, RFPNT1, OPT4

REAL NOISE

· DIMENSION SPLUSN(100), NOISE(100), SIG(100), SIG1(100), SIG2(100),

1 SPN(100), SPN1(100), SIGDN(100), DSPN1(100), DSIG(100), IP(100),

2 DSIG1(100), DSIG2(100), D2SIG2(100), NUMTAB(1D), TITLE(12),

3 CYC(10), REFPNT(10), CURR(100), SNOISE(100), VOLT(100),

4 SUMCUR(100)

65

1.5LI/2H/1/ CCHMON DVOLT, KEY DATA BLANK/6H 5 NUMTAB(I) = 0 REWIND LTAPE DO 5 I=1/ID $IGE = 100^{\circ}$ 10 IGB = 1 13. 14. 15. 10. 17. 11. 12.

18. ITIME = 0

19. ILAST = 0

20. READ(5,11) (TITLE(1), J=1,12)

C .. CHECK KUN NUMBER TABLE TO SEE TAPE DATA CAN BE FOUND BY FORWARD READING. 13 FORMAT(1H1, 30X, 12A6, // 40X 32HREQUESTED DATA FROM LIBRARY TAPE 24 FORMAT(/ 40%, 4HRUN , A6, 2%, 5HCYCLE, I3, 2%, 10HREF, POINT I3) WRITE(6,24) (IRUN, CYC(I), REFPNT(I), I=1,NCYC) KEAD(5,22) (CYC(I), REFPNT(I), I=1,NCYC) REAU(5,15) 0PT1, 0PT2, 0PT3, 0PT4 IF(IKUN.EQ.NUMTAB(I)) 60 TO 40 WRITE(6,13) (TITLE(1), 1=1,12) 20 READ(5+21) IRUNA NCYC, ILAST IF (NUMTAB(I) .NE.0) GO TO 30 IF(ITIME.NE.0) GO TO 28 16 IF(ILAST) 150, 20, 150 21 FORMAT(A6, 1116) RFPNT1 = REFPNT(1) SUMCUK(I) = 0.0 14 SNOISE(I) = 0.0 IGB = REFPNT(1) 15 FORMAT(1216) 22 FURMATIC 1216) 11 FORMAT(1246) DO 14 I=1,100 SPN(I) = 0.028 DO 30 I=1.ID = (I)NO9IS SIG(1) = 0ITIME = 1 21. 22. 23. 24. 25. 26. 27. 26. 29. 30. 31. 37. 39. 40. 42. - 11 32 % 30. 38. 41 · · 43. 45**.** 46**.** 47. 3 ຂູ່
 - 1 TAPE TAPE TAPE TAPE TAPE TAPE TAPE TAPE TOWN DUMMY, DUMMY, DUMMY, DVOLT, VOLTST POS + 1 /ul>

75.	NUIF = REFPNT(J) - RFPNT1	
76.	IF(NDIF) 80, 90, 100	
т.	80 IGB = MAXU(1GB,1-NDIF)	
76.	IGE = MINO(IGE,IGB+(L-REFPNT(J)))	
.61	GO TO 110	
• 7 8	90 IGB = IGB	
81.	IGE = WIND(IGE,L)	
82.	GU TO 110	
63.	100 IGB = IGB	
. 48	IGE = MINO(IGE,L-NDIF)	
85.	110 DU 120 I=IGB,IGÉ	
86.		
87.	U = 1.0	
88.	IF(OPT3.NE.0) D = CURR(NA)	
	SPN(I) = SPN(I) + SPLUSN(NA)/D	•
	SIG(I) = SIG(I) + (SPLUSN(NA)-NOISE(NA))/D	
.16	SNOISE(I) = SNOISE(I) + NOISE(NA)/D	
92.	SIGDN(I) = SIGDN(I) + (SPLUSN(NA)-NOISE(NA))/(NOISE(NA)+D)	
93.	SUMCUR(I) = SUMCUR(I) + CURR(NA)	
. 46	120 CONTINUE	
95.	GO TO 140	:
	130 IF(LAST.EQ.0) 60 TO 72	
97.	WRITE(6,131) CYC(J)	
96.	131 FORMAT(13H CYCLE NUMBER 16,28H IS NOT ON THE LIBRARY TAPE.)	
99.	CALL REWI (LTAPE)	
• 00	CALL EXIT	
01.	140 CONTINUE	

C.. POSITION TAPE AT THE BEGINNING OF THE NEXT LOGICAL RECORD CONTAINING READ(LTAPE) (DUMMY, DUMMY, DUMMY, DUMMY, I=1,L) C.. IF LAST EQUALS ONE TAPE IS POSITION ALREADY. 160 VOLT(I) = VOLTST + (X-1.0)+DVOLT C .. THERE STILL REMAINS SOME CYCLES. C .. CHECK FOR END OF FILE FIRST. 142 IF (LAST.NE.2) 60 TO 146 146 IF(LAST.EQ.1) G0 T0 16 READ(LTAPE) DUMMY, L THE NEXT RUN NUMBER. READ(LTAPE) LAST D0 160 I=168,16E 00 162 I=IGE, IGE SIG(IA) = SIG(I) SPN(IA) = SPN(I) IGBM1 = IGB - I D0 144 I=1,ID 144 NUMTAB(1) = 0IA = I - IGBM1 REWIND LTAPE C.. RE-ORDER ARRAYS G0 T0 142 60 10 16 T + X = X 150 X = 0 υ 102. 103. 105. 104. 106. 115. 107. 109. 106. 111. 112. 110. 114. 115. 116. 117. 119. 123. 118. 120. 121. 122. 124. 125. 126. 127. 128.

129.	SNOISE(IA) = SNOISE(I)
130.	SIGDN(IA) = SIGDN(I)
131.	volt(IA) = volt(I)
132.	IP(IA) = I
135.	SUMCUR(IA) = SUMCUR(I)
134.	162 CONTINUE
135.	NUMPTS = 16E - 16BM1
136.	KEY = 1
137.	CALL SMT (SIG, SIG1, NUMPTS, OPT2)
138.	KEY = 2
139.	CALL SMT (SPN, SPN1, NUMPTS, OPT2)
140.	IF(CPT3.EQ.0) GO TO 169
.142	WRITE(6,168)
142.	168 FORMAT(1H1+ 12X 5HVOLTS 11X 3H5/I 12X 3H5/I 2X 2(8X 7H(S+N)/I)+
143.	* 6X 11H S/(N*I) • 6X 3HN/I 13X 1HI)
244.	60 TO 1711
145.	169 WKITE(6,170)
146.	170 FURMAT(1H1, 12X 5HVOLTS 12X 1HS 14X 1HS 1X 2(12X 3HS+N), 12X
147.	* 3HS/N 13X 1HN 14X THI)
146.	1711 WRITE(6,171)
149.	171 FORMAT(20X 2(22X, 8H(SMTH 1)) /)
150.	WRITE(6,172) (IP(I), VOLT(I), SIG(I), SIG1(I), SPN(I), SPN1(I),
151.	<pre>1 SIGUN(I) * SNOISE(I) * SUMCUR(I) * I=1 * NUMPTS)</pre>
152.	172 FORMAT(3X, 13, 1P8E15,6)
153.	C PLOT ABOVE ITEMS ON PRINTER.
154.	PCHAR = BLANK
155.	IF(CPT3.NE.0) PCHAR = SLI

156.	WKITE(6,173) PCHAR
157.	173 FORMATE 1H1. 20X SHPLOT OF S. A2)
158.	CALL PLOT (VGLT, SIG, NUMPTS, 100, 46, 6)
159.	WKITE(6,174) PCHAR
160.	174 FORMATIC 1H1, 20X 9HPLOT OF 5, A2, 5X 13HSMOOTHED ONCE)
161.	CALL PLOT (VOLT, SIG1, NUMPTS, 100, 46, 6)
162.	WRITE(6,175) PCHAR
165.	175 FORMAT(1H1, 20X 13HPLOT OF (S+N), A2)
164.	CALL PLOT (VOLT, SPN, NUMPTS, 100, 46, 6)
165.	WRITE(6,176) PCHAR
166.	176 FORMAT(₁ 1H1+ 20X 13HPL _O T OF (S+N)+ A2+ 5X 13HSMOOTHED ONCE)
167.	CALL PLOT (VOLT, SPN1, NUMPTS, 100, 46, 6)
166.	IF(OPT3.EQ.0) 60 TO 1770
169.	WRITE(6,1761)
170.	1761 FORMAT(1H1, 20X, 15HPLOT OF S/(N+1))
171.	60 T0 178
172.	1770 WRITE(6,177)
175.	177 FORMAT(1H1, 20X, 11HPLOT OF S/N)
174.	178 CALL PLOT (VOLT' SIGDN' NUMPTS, 100, 46, 6)
175.	WRITE(6,179) PCHAR
176.	179 FORMAT(1H1, 20X, 9HPLOT OF N, A2)
177.	CALL PLOT (VOLT, SNOISE, NUMPTS, 100, 46, 6)
176.	IF(0PT1.EQ.U) GO TO 260
179.	CALL DIFF(SIG, DSIG, NUMPTS)
180.	CALL DIFF(SIG1, DSIG1, NUMPTS)
181.	KEY = 3
162.	CALL SMT (SIG1, SIG2, NUMPTS, OPT2)

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210.	CALL PLOT (VOLT, DSIG2, NUMPTS, 100, 46, 6)
.115	WRITE(6,241) PCHAR
212.	241 FORMAT(1H1, 20%,19H2ND DERIVATIVE OF S, A2, 15H 5M00THED TWICE)
213.	CALL PLOT (VOLT, D25162, NUMPTS, 100, 46, 6)
214.	WRITE(6,251) PCHAR
215.	251 FORMAT(1H1, 20%,19HUERIVATIVE OF (S+N), A2, 14H SMOOTHED ONCE)
216.	CALL PLOT (VOLT, DSPN1, NUMPTS, 100, 46, 6)
217.	
216.	260 IF(0PT4,EQ.0) GO TO 280
219.	D0 270 J=1,3
220.	PUNCH 261* (TITLE(I),I=1,12)
221.	261 FORMAT(12A6)
222.	PUNCH 262
223.	262 FORMAT(5X, 1H0, 5X, 1H0)
224.	PUNCH 263. VOLT(1), VOLT(NUMPTS), DVOLT
225.	263 FURMAT(3F12.4) .
226.	GO TO (264, 265, 266), J
227.	264 PUNCH 267, (SIG(I), I=1,NUMPTS)
228.	GU TO 270
229.	265 PUNCH 267+ (SPN(I)+ I=1+NUMPTS)
230.	GO TO 270
231.	266 PUNCH 267, (SNOISE(I), I=1,NUMPTS)
232.	267 FORMAT(6F12.4)
233.	270 CONTINUE
234.	260 IF(ILAST.EG.1) 60 TO 10
235.	CALL REWI (LTAPE)
236.	CALL EXIT

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237. END

END OF LISTING. 0 *DIAGNOSTIC* MESSAGE(S).

SHT **M** SMT CH1 SMT SHT F#S YC(L)=Y(I)=8.5714286E=02*(Y(I~>)=4.0*(Y(I=1)+Y(I+1))+6.0*Y,Z)+v(I+SMT SHT SHT YC (NPM1)=0.25*{Y (NPM2)+2.0*Y (NPM1)+Y (NP)) ë fon SMT,SMT Univac 1106 fortran 1º 5,evel 2201 0029 f46148 This completion was dúne un di may 68 at 14;22;13 SUBROUTINE SMT (Y. YC, NP, 10PT) ENTRY POINT 000471 YC(2)=0.25+(Y(1)+2.0+Y(2)+Y(3)) DIMENSION Y(1), YC(1), B(100) ROUTINE TO SMOOTH CURVE IF(IOPT.6T.0) 60 TO 200 ((I)A'NIWJ)TNIWE = NIWJ DO 100 I=3,NPM2 PI = 3.1415926 COMMON DX, KEY NPM1 = NP = 1 NPM2 = NP = 2 YMIN = 1.E+37D0 205 I=1,NP YC (NP)=Y (NP) YC(1)=Y(1) HL, = P+UX 100 CONTINUE 200 P = NP-1 RETURN SUBROUTINE SMT 12)) Ų 11. 14. 15. 16. 17. 18. 19. 20. 21. 22. 4 12. 5 13.

050 060 070 080 090 100 110 120 130

020

	23.	205 CONTINUE
	24.	IF(YMIN.LT.0) GO TO 208
	25.	D0 206 1=1,NP
	26.	YG(I) = Y(I)
	27.	206 CONTINUE
	28.	GO TO 210
	29.	208 DO 209 I=1,NP
	30.	$\gamma C(1) = \gamma (1) - \gamma MIN$
	31.	209 CONTINUE
	32.	210 YI = SQRTK YC(1) }
	33.	YF = (SQRT(YC(NP)) - YI)/HL
	• 1 1	C = X
76	35.	D0 211 1=1,NP
	36.	YC(I) = SQRT(YC(I)) = YI = YFaX
	37.	211 X = X + DX
	38.	CALL FOUR (NP, YC, B)
	39.	NPM = NP-1
	40.	60 TO (212, 214, 216), KEY
	41.	212 WRITE(6,213)
	42.	213 FORMAT(1H1, 20X 46HFOURIER COEFFICIENTS FOR SMOOTHING SIGNAL ANCE
	43.	~*
	• † †	GU TO 218
	45.	214 WRITE(6,215)
	46.	215 FORMAT(1H1, 20X 54HFOURIER COEFFICIENTS FOR SMOOTHING SIGNAL + NO
	47.	*ISE ONCE)

48.	60 TO 218
49.	216 WRITE(6+217)
50.	217 FURMAT(1H1, 20X 47HFOURIER COEFFICIENTS FOR SMOOTHING SIGNAL TW7C
51.	(⊒∗
52.	218 WKITE(6,219) (8(I), I=1,NPM)
53.	219 FORMAT(10X 10E10.3)
0 #•	DO 220 I=1.NPM
55.	CI = I
56.	220 B(I) = B(I)*COS(PI*CI/(2.0*P))**2
57.	WRITE(6,221)
58.	221 FORMAT(/ 20X, 40HFOURIER COEFFICIENTS FILTERED BY COS+*2)
59.	WRITE(6,219) (8(I), I=1,NPM)
60.	IF(10PT.Ea.1) GO TO 230
61.	NMAX = IOPT
62.	60 TO 300
63.	230 BT = 0.0
64.	D0 240 I=1,20
65.	NPI = NP-1
66.	240 BT = 87+8(NPT) ##2
67.	× = 20
68.	242 N = NP-K
•69	BE = B(N-1)**2
70.	CK # K
11.	BET = BT/CK
72.	IF(BE/BET=16.0) 250,250, 280

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73. 250 IF(N-2) 260, 260, 270

74. 260 NMAX = NP/10

75. WRITE(6,261)

76. 261 FORMAT(20X, 11HTEST FAILED)

78. 270 K = K+1

79. BT = 8T + 8E

å1. 200 IF(N-25) 290, 270, 270

82. 290 NMAX = N+2

83. 300 WRITE(6:301) NMAX

84. 3UL FORMAT(/ 20X, 22HSMOOTHING ROUTINE USED 13,13H COEFFICIENT_e

85. CALL FOURI (NMAX, NP, B, YC)

0 II X

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78

67. DO 310 K=1,NP

86. YK = YC(K) + YI + YF+X

89. YC(K) = YK+YK

90. 310 X = X + DX

91. IF(YMIN.LT.0) G0 T0 320

RETURN

92.

93. 320 DO 330 I=1,NP

94. $\gamma C(I) = \gamma C(I) + \gamma MIN$

95. 330 CONTINUE

96. RETURN

97. END

FND OF LISTING. 0 #DIAGNOSTIC* MESSAGE(S).

CMT 140

FOR FOUR FOUR Univec 1105 Fortram IV Level 2201 3029 F46148 This compilation was done on 01 may 68 at 14:22:16 ENTRY POINT 000127 SINI = SINKI*COSK+COSKI*SINK COSI = COSKI*COSK=SINKI*SINK SINKI = SINK*COS2+COSK*SINZ SUBROUTINE FOUR (NP.Y.B) DIMENSION Y(1), B(1) BK = BK + $\gamma(I)$ + SINKI PI = 3,141592653 COSZ = COS(PION) (NOID)NIS = ZNJS 00 22 I = 2,NPM PION = PI/CNPM DO 20 K =1,NPM COSKI = COSK SINKI = SINK SINKI = SINI 22 COSKI = COSI COSK = COSZSINK = SINZ NPM = NP-1 CNPM = NPM CNP = NP BK = 0.0 SUBROUTINE FOUR 12. 13. 16. 4 a, 14. 15. 17. 18. 19. 20. 21. 1 22. ŝ

COSKI = CJSK+COSZ-SINK+SINZ 23.

COSK =COSKI SINK =SINKI

20 B(K)=2.0+BK/CNP 26. 26. 28. 28.

RETURN

ENO

0 *DIAGNOSTIC* MESSAGE(S). END OF LISTING.

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23. 24. 25. 25. 26. 27. 28. 21. 32.	COSKI = COSI	SINKI = SINI	22 CONTINUE	.COSKI = COSK+COSZ-SINK+SIN	SINKI = COSK#SINZ+SINK#COS	COSK = COSKI	SINK = SINKI	20 Y(K) = YK	RETURN	END
	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.

0 #DIAGNOSTIC* MESSAGE(S).

END OF LISTING.

WP FUR DIFF, DIFF UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 THIS COMPILATION WAS DONE ON 01 MAY 68 AT 14:22;18

LFF 020 AIFF 030 BIFF 040 nIFF 050 NIFF 060 ALFF 070 nIFF OAG AIFF 100 DIFF 110 9IFF 120 nIFF 040 0 #DIAGNOSTIC* MESSAGE(S). ENTRY POINT 000031 ROUTINE TO TAKE DIFFERENCES ·YD(1) Yu(I)=(Y(I+1)+Y(I-1))*0*5 SUBROUTINE DIFF (Y, YD, NP) (TMdN) _- (dN) _= (dN) OA DIMENSION 1(1) DO 100 I=2,NPM1 YD(1)=Y(2)-Y(1) I - dN = THAN 100 CONTINUE SUBKOUTINE DIFF RETURN ENO υ u ĥ ~ 11. , 10. 12. ÷ ۍ ف ~ **.** ທີ 6

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END OF LISTING.

WP FGR PLOT,PLGT UNIVAC 1108 FORTRAW IV LEVEL 2201 0029 F46148 This compilation was done on 01 MAY 68 AT 14:22;20

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SUBROUTINE PLOT ENTRY POINT 000510

DIAGNOSTIC THE NAME OR APPEARS IN A DIMENSION OR TYPE STATEMENT BUT IS NEVER REFERENCED.

,			
•		SUBROUTINE PLUT(X+T+N+NL+N2+N013T)	pL0T0010
8 •		DIMENSION X(1),Y(1),IP(150),B(6),A(18),NB(6),NA(18)	PLOTn020
°°		DIMENSION B1(6),82(6),83(6),N81(6),N82(6),N83(6)	pLOT0030
		EWJIVALENCE (A+NA)+(B+NB]+(C+NC)+(D+ND)	PLOT040
5.		EQUIVALENCE (B1,Nb1),(82,Np2),(83,Nb3)	pL0T0050
<u>,</u>	U	X=ABCISSA VALUES TO BE PLOTTED	PLOTN060
7.	υ	Y=ORDINATÉ VALUES TO BE PLOTTEr	PL070070
θ.	U	NENUMBER OF POINTS TO BE PLOTTED (150 OR LESS)	PLOT00A0
6	U	IF N IS NEGATIVE THE Y ARMAY IS IN DESCENDING ORDER	pL0Tr090
10.	U	N1=NUMBER OF PRINT WHEELS TO BE USED (108 OR LESS)	PLOT0100
11.	U	N2=NUMRER OF LINES TO BE USED (RECOMMENU SO)	pL0Tn110
12.	U	NOUT=TAPE NO. OF OUTPUT TAPE	PL070120
13.	U	RESTORATION AND HEADING OF PAGE IS LEFT TO USER	PL070130
14.		***	-pL0T0140
15.	U	ALL BLANKS	PLOT0150
16.	U	ALL NEGATIVE SIGNS - BOTTOM LINE USE	pL070170
17.		DATA C/6H /	pL0T0160
16.		DATA U/6H/	PLOT0140
19.	U	STARS IN VARIOUS POSITIONS - BLANKS FILLED IN (6)	PLOT 0190
20.	U	SUBSTITUTE OCTAL EQUIVALENT OF * IN THIS STATEMENT	pLOT02n0

21.		UATA E/Sh <s05999 .="" shok<294="" shu<9269="" shuqqaqa="" shuqqaqa<="" td=""><td>pL01n210</td></s05999>	pL01n210
22.	U	MASK FOR PICKING OUT SECTOR	oreand la
23.		DATA 81/0770000000000000000000000000000000000	
24.		106000077000•00000000770 0• 00000077.	peulije30
25.	U	MASK FOR COMPARING TO BLANK	Druluz40
26.		BATA B2/44 BBBB2/44B CONSTRACT	pLOTn250
	¢		pLOY ₁₂₆₀
	•	MASK FOR SUBIRACTING ONE	oL0Tn270
28.		0414 83/640 84889,6480 869,6486 889,6486 88,64886 89,648886 8,6488886 7	PL0702A0
29.		DATA LARGE/0001000000000	eLOTo2an
30.		INTEGER AND, OR	of OTotoo
31.0	j		
2			
• 7 •		1.FGS1	PLOT0320
33.		IF (N+LT+3) IFL6=2	pL070330
10		N=IAgS(N)	PLOT0340
35.	U	INITIALIZES FORMAT	PLOT0350
36.		D0 9 LE1.1A	pLOTn3k0
37.	σ	- A(L)=C	bL010370
38.	J	SEARCHES X POINTS FOR HIGHEST AND LOWEST VALUES	of OTATO
39.		XMIN=1.E+3A	ol Orasan
•0+		XMAX=-1.E+38	oLOTokoo
41.		DO IO I=1.N	PLOTA410
42.		XMAX=AMAX1(XMAX,X(I))	
4J.	10	XMIN=AWIN1 (XMIN-X(I))	
44.2	•		pL0T0430
		ULLIAAE (ARRATAMAN// (FLOAT (NL-1))	o t 010440
45.	U	REORDERS Y INTO DESCENDING VALIJES	940T0450

	4ú.	60 TO (20,15),1FLG	PL0Tn460
	47.	15 DU 16 Imin	aL010470
	48.	I=(1)=I	pL0T0490
	+9 •	16 CONTINUE	COT0490
	50.	YMAX=Y(1)	PL0T0500
	51.	YMIN=Y (N)	pL07n510
	52.	GÙ TO 25	pL0T ₀ 520
	53.	20 D6 21 I=1,N	pL076530
	54.	IP(I)=0	pL070540
	55.	21 CONTINUE	oL077550
	\$6 .	D0 23 I=1,N	pL07c560
	57.	YMAX=-1.E3A	PL070570
8	54.	DD 22 J=1.4	pLOT05A0
6	59.	IF(IP(J).6E.LARGE) 60 70 22	p LOT n590
	UIA6NOSTI	C THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.	
	60.	IF(Y(J).LE,YMAX) 60 T0 22	pLOTn6n0
	61.	YMAX=Y (J)	pL070610
	62.	KK=J	nL0T0620
	63.	22 CONTINUE	pLOTn630
,	64.	IP(I)=IP(I)+KK	640T0640
	65 .	IP (KK)=IP (KK)+LARGE	oL070650
	6ó.	23 CONTINUE	aL070660
	67,	D0 24 I=1,N	029u1u7a
	68 .	IP(1)=IP(1)-LARGE	pLOTn640

pLOTn690

24 CONTINUE

69**.**

70,		IXI=IP(1)	PLOTR700
71.		IX2=IP(N)	pL0Tn710
72.		YMAX=Y (IX1)	0L0Tn720
73.		YMIN=Y (IX2)	PL0Tn730
74.		25 DELTAY=(YMAX-YMIN)/(FLOAT(N2-1))	PL070740
75.		DELT=YMAX	PL0T0750
76.	U	PLOTTING SECTION	PL0Tn760
.11.		D0 41 K=1,N	5L010770
78.		I=IP(K)	PLOTO780
.61		J=IP(K+1)	pL070790
30.		IF (K-1) 33, 33, 30	pL076800
81.		30 IF(L)31,31,33	pL010810
82.		JI DELTEDELTAY	pL0T0820
83.		IF(Y(1)-DELT+.001) 32+ 33+ 33	
84.	U	PRINTS BLANK LINES	pL070840
8 5.		32 L=-1	. pL0Tn850
86.		60 TO 37	pL0Tn860
87.	Ų	PRINT WHEEL POSITION (0,1,2,3,.,.N1-1)	pL010870
88.		33 NPWP=(X(I)-XMIN)/UELTAX	pL0T0840
89.	U	SECTOR(1,2,3,4,5N1/6+1)	pL0T0890
90.		NSECT= (NP#P/6) +1	pL0Tn900
91.	Q	POSITION IN SECTOR(1,2,3,4,5,6)	PLOT0910
92.		NF=MOU (NP#P,6)+1	PL0Tn920
93.	U	PLACES * IN FORMAT	PL0T0930
94.	3		0%6v1v7a=======

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* 大学を見ている いたい いたいない

95.			NTST=AND(NA(NSECT) ° NB1(NF))	pL07n950
96.			IF(WTST.EQ.MB2(NF))GO TO 10A	PL070960
97.			NA (NSECT) =NA (NSECT) -NB3 (NF)	PL070970
99.			60 TO 101	PL0T09A0
• 66		100	NA (NSECT) =NA (NSECT) ≠NB (NF)	pL010990
100.		101	CONTINUE	pL071000
101.	ů			
102.			IF (K=N) 34,36,36	pL071020
103.	U		RÉPEATS IF Y(I) AND Y(J) ÂRE CLOSER THAN DELTAY	pL071030
104.		34	IF(Y(J)=OELT+.001) 36, 35, 35	I
105.		35		-
106.			50 TO 41	PL071060
107.		36	L=0	PLOT1070
108.	v		PRINTING ROUTINE	PLOT1080
109.		57	CONTINUE	pL0T1090
110.			#RITE (NOUT,38)DELT,(A(IL),IL=1,18)	PLOT1100
111.		38	FORMAT (1PE10.3, 2H I, 1846)	
112.			lF (L)31,39,39	ot 01. 120
113.	U	-	RESTORES FORMAT	of of the
114.		39	00 40 IL=1,18 .	BLOT-140
115.		0	ر ۱۲۲)=C	
116.		- T+	ONTINUE	-1 0-1 1 120
117.	U	-	HAWS BOTTOM AXIS	
118.		-	0 42 I=1,18	oldino.
119.		124		altitud

120.	WRITE (NOUT,43){A(I),I=1,18)	00232070
121.	43 FORMAT(12X+18A6).	PL071213
122.	C RESTORES A ARRAY TO BLANKS	pL0T1220
123.	D0 44 I=1.18	pL0T1230
124.	++ V(I)=C	011240
125.	C SETS UP + EVERY 10 PLACES FOR LOWER AXIS	°71250
126.	D0 45 1=2,12,5	pL0T1260
127.	NA(I)=NA(I)+NB(4)	pL071270
128.	NA { [+2] =NA (] +2] +NB (2)	CLOT1200
129.	45 NA(I+3)=NA(I+3)+NB(6)	0671Jun
130.	NA(17)=NA(17)+NB(+)	0L0T13n0
131.	NA(1)=NA(1)+NB(1)	PL071310
132.	WRITE (NOUT,43)(A(I),I=1,1A)	PL0T1320
133.	DELTAX=((XMAX-XMIN)/FLOAT(N1))#10.0	pt.0T1330
154.	D0 46 I=1,11	012 JUDA
135.	46 A(I)=XMIN+FLOAT(I-I)*DELTAX	PL0T1350
136.	WRITE (NOUT,47)(A(I),1=2,11)	PL071360
137.	47 FORMAT(16X,1P10E10.4)	pL071370
138.	RETURN	pL011340
139.	END	PL011390
END OF	LISTING. 2 #DIAGNOSTIC* MESSAGE(S).	

SUMMATION LH21 AND LH22 TWO CYCLES RWSULTS NOT DI., BY CURRENT

KEQUESTEU DATA FROM LIBRARY TAPE

RUN LH21 CYCLE 1 REF. POINT 1 RUN LH21 CYCLE 2 REF. POINT 1 RUN LH22 CYCLE 1 REF. POINT 1

RUN LH22 CYCLE 3 REF. POINT

STEP 5: COPY

The COPY program is used to make a backup tape for the data library tape. A backup tape is kept at all times. It is suggested that after every ten experiments, the library tape be copied onto the backup tape.

Below is a complete set of cards that comprise the COPY deck.

Ē					,			•	$\left \cdot \right $	2 2	22	2 2	2255	3	22	č		3		;		ð	- 2	44	5	4 4 6	449	5 5	52	55	55	3	56	6	652	66	6	65	6 7 9 0	77	3		;;;	77	80
	1.1.56	ia	•1	AT	4	LJ	Ø	RA	R	Z.	ιT.	A.C	E.	'n.	Ur	ы	ER.		1.1			4.4	- 4 -	[]	11	1.1	Ι			-						. 1 . 1	1		_	±.1					
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After the backup tape is written, a comparison is made. If the two tapes do not match, the output listing from COPY will so indicate.

No listing is given for this program.

STEP 6: UPDATE

Using the UPDATE program, five types of changes can be made to the data library tape. These fives changes are described below.

Type Number	Description of Change
1	Allows the user to change any word of the data that was on the card for TEDIT
2	Allows the user to delete an entire experiment from the library tape
3	Causes an entire cycle to be deleted from an experiment and remaining cycles to be re- sequenced
4	Allows the signal + noise, noise, and current values for a particular channel number of a cycle to be changed
5	Allows any channel number, along with its signal + noise, noise, and current values, to be deleted from any cycle of an experiment

Card formats for the preceding changes are as follows:

Type 1

7-12

First Card	
Column	
6	Punch one (1)
7-12	Experiment number
Second Card	Identical to that used for TEDIT except for information to be changed
<u>Type 2</u>	· · ·
Column	
6	Punch two (2)

Experiment number

т	vpe	3
T.	ype	5

Column	
6	Punch three (3)
7-12	Experiment number
13-18	Cycle number

Type 4

Column		
6		Punch four (4)
7-12		Experiment number
13-18		Cycle number
19-24		Channel number
25-30	·	Signal + noise value
31-36		Noise value
37-42		Current value

The last three items are always changed together; therefore, if no change is desired, the existing value must be entered.

Type 5	
Column	
6	Punch five (5)
7-12	Experimental number
13-18	Cycle number
19-24	Channel number

The different types of change cards for any one experiment should be in the following sequence: 2, 3, and 4 (in any sequence), 5, and 1. If more than one type 5 change is to be made for any one cycle in any one experiment, cards should be in descending channel-number order, the largest first. This order eliminates the necessity of later change cards that reflect the changes made by previous change cards.

If more than one experiment is to be changed, then the individual groups of change cards must be in the same order as on the library tape (excluding experiments that are not to be changed). Below is an example deck setup, where the data library tape consists of five experiments (I10, I11, I12, I13, and I14) and the following changes are to be made:

- Change the signal + noise value of channel number 50 in cycle 6 of experiment I10. The values of noise and current were originally 34 and 18, respectively.
- 2. Delete cycle 7 of experiment I10.
- 3. Delete experiment I12.
- 4. Change run number from I13 to I13A.
- 5. Delete channel number 45 in cycle 3 of experiment I14.

Ŀ				22222	2 2 2 2				10 2 3 3	555556	66666	4 4 6 7 7 7 1 8 9 0 2	1 2 6 7 2 6 6
v .,	<u>4.56</u>	H=P.A.T.A	LIBRA	RY TAP	F. NUMB	ER.							
Z	<u>a.56</u>	B.=N.EW.	DATA 4	IBRARY	TAPE.	NUMBER							╺╼┷╾┹╼╉╍╉╼┠╾┨╌╻┨╺
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A program listing follows.

G FOR UDATE UPDATE UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 This compilation was done on 21 Jun 68 at 17:09:44

ENTRY POINT 00000 MAIN PROGRAM

- PARAMETER LTAPE = 9. NTAPE = 10
 - INTEGER CHAN, CYCLE
- REAL NOISE
- COMMON IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST, TINT, SIGMIN,
- SIGMAX, CURMIN, CURMAX, DATE(2), CHAN(100,100), SPLUSN(100,00)
- * NOISE(100,100), CURR(100,100), CYCLE(100), L(100), LAST(100) ŝ
- XVWN .
- REWIND LTAPE

•

- REWIND NTAPE

- CALL INRUN (LTAPE) 10.
- C .. READ A CHANGE TYPE CARD .. 11.
- 10 READ(5,11) ITYPE, NRUN, NCYC, NCHAN, XSPN, XN, XCURR 12.
- IL FURMAT(IS, AS, IS, IS, 3F6.0 13.
- IF.(ITYPE.E0.0) 60 TO 80 14.
- 20 IF (NRUN.E4.IRUN) 60 TO 25 15.
- C.. WRITE OUT RUN THAT IS IN MEMORY.. 16.
- CALL OUTRUN(NTAPE) 17.
- C.. WAS THIS THE LAST RUN ON LTAPE? 16.
- IF(LAST(NMAX).EQ.2) 60 TO 110 19.
 - C .. READ IN A NEW RUN .. 20.
 - 21.
- CALL INRUN (LTAPE)

60 TO 20

22.

- 23. C., DETERMINE WHICH TYPE OF CHANGE IS TO BE MADE..
- 24. 25 60 TO (30. 40. 50. 60. 70). ITYPE
- 25. C., MAIN DATA IS TO BE CHANGED. TYPE 1.
- 26. JO READ(5,31) IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST, TINT, SIGUIN,
- 27. * SIGMAX, CURMIN, CURMAX, DATE(1), DATE(2)
- 28. 31 FORMAT(246, F6.0, A6, 8F6.0, A6, A1)
- 29. 60 TO 10
- 30. C
- 31. C., DELETE THE RUN NOW IN MEMORY., TYPE 2.
- 32. 40 IF(LAST(NMAX).EQ.2) 60 TO 100
- 33. C., READ IN ANOTHER RUN FROM TAPE.
- 34. CALL INRUN(LTAPE)
- 60 TO 10

35.

- 36. C., DELETE CYCLE NCYC WHICH IS NOW IN MEMORY. TYPE 3.
- 37. C., CYCLE NUMBERS WILL BE RE-SEQUENCED IN OUTRUN.
- 34. 50 IF (NCYC.LE.0.0R.NCYC.6T.NMAX) 60 TO 130
- 39, CYCLE(NCYC) = 0
 - •
- GU TO 10

£0.

- 41. C., CHANGE DATA OF CYCLE NUMBER NCYC AND CHANNEL NUMBER NCHAN. TYPE 4.
- 42. 60 IF(NCYC.LE.0.0R.NCYC.6T.NMAX) 60 T0 130
- 43. KCHANENCHAN+1
- tt. CHAN(KCHAN, NCYC) = NCHAN
- 45. SPLUSN(KCHAN+NCYC) = XSPN
- 46. NOISE (KCHAN, NCYC) = XN

CURR(KCHAN, NCYC) = XCURR 47.

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- 60 70 10 48**.**
- C .. CHANNEL NUMBER NCHAN IN CYCLE NCYC IS TO BE DELETED. TYPE 5. **#**9.
- 70 IF (NCTC.LE.0.0R.NCTC.6T.NMAX) 60 T0 130 50.
- IF (NCHAN+1.EQ.L(NCYC))60 T0 78 51.
- UM I L(NCYC) 52.
- JP1 = NCHAN + 2 53.
- N0 75 I=JP1,JM 5.
- CHAN(E-1,NCYC) = CHAN(I,NCYC) : 55.
- SPLUSN(I-1,NCYC) = SPLUSN(I,NCYC) 56.
- NDISE(1-1,NCYC) = NOISE(1,NCYC) 57.
- 75 CURR(I-1, NCYC) = CURR(I, NCYC) 58.
- 78 L(NCYC) = L(NCYC) 1 59.
- 60 TO 10

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97

- C .. WRITE OUT THE RUN THAT IS IN MEMORY. 61.
- 86 CALL OUTRUN (NTAPE) 62.
- C .. THERE ARE NO MORE CHANGES TO BE WADE, COPY REST OF LTAPE. 63.
- 90 IF(LAST(NMAX).EQ.2) 60 T0 100 с**н**.
- CALL INRUN(LTAPE) 65.
- CALL OUTRUN (NTAPE) 66.
 - 67.
 - 60 10 90
- 100 BACKSPACE NTAPE 68.
- LAST(NMAX) = 2

69.

- WRITE(NTAPE) LAST(NMAX) 70.
- END FILE NTAPE 71.

- 72. CALL REWI(LTAPE)
- 73. REWIND NTAPE
- 74. CALL EXIT
- 75. 110 WRITE(6,111) NRUN
- 111 FURMATE /, 33H REQUESTED CHANGE FOR RUN NUMBER , A6, 57H IS NOT IN 76.
- 77. * SEQUENCE OR THE RUN NUMBER ITSELF IS IN ERROR. /)
- 78. 60 70 100
- 79. 130 WRITE(6,131) NCYC, NRUN
- 40. 131 FORMAT(/, 14H CYCLE NUMBER , 16,25H IS OUT OF RANGE FOR RUN A4 /)
- 81. 6⁰ TO 100
- END

.82.

END OF LISTING. " 0 *DIAGNOSTIC* MESSAGE(S).

S FUR INRUN'IMRUN UNIVAC 1108 FORTRAM IV LEVEL 2201 0029 F46148 UNIVAC 1108 FORTRAM IV LEVEL 2201 0029 F46148 This compilation was done on **21 Jun 68 at 17:09:46**

SUBROUTINE INRUN ENTRY POINT 400204

- 1. SUBROUTINE INRUN (LTAPE)
- 2. INTEGER CHAN, CYCLE
- 3. REAL NOISE
- COMMON IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST, TINT, SIG4IN,
- * SIGMAX, CURMIN, CURMAX, DATE(2), CHAN(100,100), SPLUSN(100,10Å)
- * / NOISE(100,100), CURR(100,100), CYCLE(100), L(100), LAST(100)
- XVWN + +
- RËAD(LTAPE) IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST,TINT, SIGUIN,
- SIGMAX CURMIN CURMAX DATE(1) DATE(2)
- 10. N =

0

- 11. C
- 12. 10 N = N + 1
- 13. IF(N.6T.100) 60 TO 20
- 14. READ(LTAPE) CYCLE(N), L(N)
- 15. IMAX = L(N)
- 16. READ(LTAPE) (CHAN(I,N), SPLUSN(I,N), NOISE(I,N), CURR(I,N),I=3.
 - + IMAX)

17.

- 18. READ(LTAPE) LAST(N)
- 19. IF(LAST(N).EQ.0) 60 TO 10
- 20. NMAX = N
- 21. RETURN

- 22. C DELETE THE REMAINDER OF THIS EXPERIMENT, IT EXCEEDS 100 CYCLES.
- 23. 20 READ(LTAPE) DUMMY, IDUM
- 24. READ(LTAPE) (DUMMY, DUMMY, DUMMY, DUMMY, I=1,IDUM)
- 25. RÉAD(LTAPE) ILAST
- 26. IF(ILAST.EQ.0) 60 TO 20
- 27. NMAX = 100
- 28. LAST(NMAX) = ILAST
- 29. 30 WRITE(6,31) IRUN
- 30. 31 FORMAT(/, 5X, A6,86H EXCEEDED 100 CYCLES, THE REMAINING CYCLES WA
- 31. *VE BEEN DELETED ### SORRY ABOUT THAT ###.
- 32. RETURN
- END

33.

END OF LISTING, 0 +DIAGNOSTIC+ MESSAGE(S),

B FOR OUTRUN,OUTRUN Univac 1108 Foktran IV Level 2201 0029 F46148 This compilation Was Done on 21 Jun 68 at 17:09:48

SUBROUTINE OUTRUN ENTRY POINT 000142

- 1. SUBROUTINE OUTRUN(NTAPE)
- 2. INTEGËR CHAN, CYCLE
- 3. REAL NOISE
- 1

- COMMON IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST, TINT, SIG_MIN,
- * SIGMAX, CURMIN, CURMAX, DATE(2), CHAN(100,100), SPLUSN(100,106)
 - 6. * NOISE(100,100), CURR(100,100), CYCLE(100), L(100), LAST(100)
- XAMN * *

.

8

- WRITE(NTAPE) IRUN, GAS, VAR, TIME, RES, DVOLT, VOLTST, TINT,
 - 9. * SIGMIN' SIGMAX' CURMIN' CURMAX' DATE(1), DATE(2)
- ICYC = 0

10.

- 11. 10 D0 20 N=1,NMAX
- 12. IF(CYCLE(N),EQ.0) 60 TO 20
- 13. ICYC = ICYC + 1
- 14. WRITE(NTAPE) ICYC, L(N)
- IWAX = L(N)

15.

- 16. WRIFE(NTAPE) (CHAN(I,N), SPLUSN(I,N), NOISE(I,N), CURR(I,N), I=1,
- 17. . : * IMAX)
- 18. WRITE(NTAPE) LAST(N)
- 19. 20 CONTINUE
- 20. BACKSPACE NTAPE
- 21 WRITE(NTAPE) LAST(NMAX)
- 22. RETURN
- END

23.

END. QF_LISTING. 0 +DIAGNOSTIC+ MESSAGE(S).

STEP 7: LEOF (List and End of File)

One input card, in FORTRAN format (A6, I6), is necessary for execution of this program.

Column

1-6	INUM = last valid experiment number
7-12	LCYCLE = last valid cycle number

After LEØF has encountered the last valid cycle number on the library tape, an end of file is written.

A program listing follows.
W FUR LEUF, LEOF UNIVAC 1108 FORTRAN IV LEVEL 2201 0629 F46148 This compilation was Duge un 07 may 68 at 11:58:51

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HAIN PRUSRAM ENTRY POINT 000000

- 4. C.. THE PURPOSE OF THIS ROUTINE IS TO READ THE LIBRARY TAPE AND LIST ALL
- 2. C DATA BY RUN NUMBER AND BY CYCLE NUMBER.
- 3. PARAMETER LTAPE = 10
- INTEGER CHAN
- REAL NOISE
- DIMENSIOW CHAN(100), SPLUSN(100), NOISE(100), CURR(100), DATE(2)
 - REWIND LTAPE
- · READ(5.7) INUM, LCYCLE
- 7 : FUKMAT(A6, 16)

103

- Lú. 8 REÁD(LTAPE) NUM, ITYPE, VAR, TIME, RES, DVOLT, VOLTST, TINT,
- 11. I SIGMIN' SIGMAX' CURMIN' CURMAX' DATE(1), DATE(2)
- 12. WHITE (6,11) NUM
- 15. 11 FORMAT(10X+ 10HRUN NUMBER, 1X, A6, /)
- 14. WAITE(6,12) ITYPE
- 15. 12 FURMAT(10X+ 3HGAS+ 1X+ 46+ /)
- 16. WRITE(6,13) VAR
- 17. 13 FURMAIL 10X, IOHVARIANCE %, 1X, F6.2, /
- 1d. wAITE(6,14) TIME
- 19. 14 FURMATI 10X, 4HTIME, 1X, 46, /
- WRITE(6,15) RES

20.

21. 15 FURMAT(10X, 4HRES, 1X, F6.2, /)

READ(LTAPE) (CHAN(I), SPLUSN(I), NOISE(I), CURR(I), I=1,L) 16 FURMAT(10X, 17HVOLTAGE INCREMENT, 1X, F6.2, /) 17 FURMAT(1UX, 17HSTARTING VOLTAGE , 1X, F6.2, /) IF (NUM.EQ.INUM.AND.KOUNT.EQ.LCYCLE) 60 TO 40 22 FORMAT(10X, 13HMAX, CURRENT , F10.2, / 1 25 FUKMAT (10X, 16HNUMBER OF POINTS, 15, // 21 FURMAT(10X, 13HMIN, CURRENT , F10.2, / 20 FORMAT(10X+ 12HMAX, SIGNAL + F10+2+ /) 19 FORMAT(10X, 12HMIN, SIGNAL , F10.2, /) 18 FURMAT(10X, 14HITIME INTERVAL , F6.2, / 24 FURMAT(10X, 12HCYCLE NUMBER, 1X, 13, / 23 FORMAT(10X+ 4HDATE, 1X+ 246+ /) WAITE(6,23) DATE(1), DATE(2) 10 READ(LTAPE) KOUNT. L WRITE(6,20) SIGMAX WRITE (6,21) CURMIN WRITE(6,22) CURMAX WRITE(6,17) VOLTST WRITE(6,19) SIGMIN WRITE(6,16) DVOLT WRITE(6,24) KOUNT WRITE(6,18) TINT WRITE(6,25) L 31. 24. 25. 27. 28. 29. 30. 37. 39. 4 Ú • ÷1.• 42. 22. ٤ئ. 26. 32. 38. ₽3. ÷ t • 40° 35. • • ч÷. 35. 30. 104

- 31 FORMATC 1H1) sι.
- IF(LAST.E0.1) GO TO 8 51.
- WHITE (6,28) 52.
- 28 FURMAT(/ 12H END OF FILE) 53.
- CALL REWI (LTAPE) •+5
- CALL EXIT 55.
- 40 LAST = 2 56.
- WRITE(LTAPE) LAST 57.
- END FILE LTAPE 58.
- WAITC(6,28) 59.
- CALL REWI (LTAPE) . 90
- CALL EXIT 61.
- END 62.

0 *DIAGNOSTIC* MESSAGE(S). END OF LISTING.

STEP 8: SMØØTH

This program Fourier-smooths data, unfolds a given Gaussian electron energy distribution from the data, and gives the results for the derivative of the function in tabular form. The program is prepared to accept card input. The deck of cards needed is generated as one of the options in ABEAM4.

The normal output of this program, which in its present form was prepared for the study of autoionization in molecular gases, is:

- 1. Input data Fourier-smoothed
- 2. Derivative of Fourier-smoothed square root of the data
- 3. Derivative of Fourier-smoothed data
- 4. Derivative of Fourier-smoothed data with energy distribution unfolded for case 1
- 5. Derivative of Fourier-smoothed data with energy distribution unfolded for case 2
- 6. Derivative of Fourier-smoothed data with energy distribution unfolded for case 3

At present there is one graphic output, which gives the input data Fourier-smoothed once.

The input sequence and card formats are given below.

Title Card: FORTRAN format is (12A6)

Column

1-72 Title (printed at top of first page)

First Data Card: FORTRAN format is (316, 3F6.0, 16)

Column

6	IN = 0: accept Y values as input
	= 1: after reading in Y values below, read YT values
	and compute $Y = Y - YT$
12	ISTOP = 0: last problem
	= 1: read in another title card for a new problem
18	NDEL = number of delta (Δ) values to follow
19-24	DEL (1) = Δ value(s) for unfolding

С	ol	ur	n	r
_	_	_		

25-30 DE	L (2)
----------	-------

31-36 DEL (3)

37-42 NMAX = 0: let program choose number of Fourier coefficients to use

> 0: program is to use this number of Fourier coefficients

Second Data Card: FORTRAN format is (3F12-4)

Column

SI = initial voltage
SF = final voltage
DX = voltage increment

Last Data Card: FORTRAN format is (6F12.4)

6 values per card: Y(i), i = 1, NP NP = total number of values

= [(SF - SI)/DX] + 1

YT(i), i = 1, NP omit if IN = 0 on first data card

If this deck has been punched from the ABEAM4 program, the user must finish punching the second card (first data card) (i.e., NDEL, DEL (1), DEL (2), DEL (3), NMAX).

Below is an example deck setup.

000000000000000000000000000000000000000	1 . I T I I 2 2 2 2 4 5 ¢ 7 € 30 I 2]		1.39444	444444	45555555	55556	666666	666777 789012	7777778 34567890
		SERT STRATH	PREGRA	A HERE)	لمست			
Y XGT SMORTH				لمسبب			المست		
Surdinat		The Card For	EIRST	CASE	mi			1111	<u> </u>
IN ISTOP	NDEL DELU	(PEL (2) DEL(3)	NMAX,	ليتبيد		Lun			
	SF	px			inite	l	لسبين		
Y(2)	Y(2)	Y(3)	Y LLL	(4)	111 Y (5	\mathbf{D}_{11}	Y	(6)	
Y(7)		Y(WP)							
YT(1)	YT (2)	Yπ (3)	<u>, у</u> т	(4)	Y7¦(€	2.11	Y7	(6)	
Y7 (7)		+YTWP)				in			
		I				L			
4	ANOTHER TI	LE CARD FOR	NEXT C	ASE IF	ISTEP	BAVE		1111	

°	12 WKITE(6,124)
•	124 FORMAT(1H1)
7.	READ(5,15) (LABEL(I), I=1,12)
°.	15 FURMAT(1246)
6	KEAD(5,16) IN, ISTOP, NDEL, DEL(1), DEL(2), DEL(3), NMAX
10.	16 FURMATC 316, 3F6.0, IG)
11.	WKITE(6,151) (LABEL(I),I=1,12)
12.	151 FURMAT(4X, 12A6)
13.	READ (5,17)SI,SF,JX
_ 14.	17 FORMAT(3F12.4)
15.	HL = (SF-51)
10.	NPM = HL/UX+.1
17.	T+EdN # AN
16.	KEAD(5,13) (Y(I),[=1,NP)
19.	IS FURMAT(GF12,4)
<i>≿</i> ũ.	LF (IN)20,20,19
21.	19 REAU (5,14) (YT(I),I=1,NP)
22.	DO 14 I = 1.NP
23.	$(1) = \lambda(1) = \lambda(1)$
24.	20 WHITE(6,174)NP,SI,CX,SF
25.	174 FORMAT(/23X+27H=OURIER SMOOTHIME OF SIGNAL / 20X+30HINPUT SIGNAL F

ENTRY POINT 000000 PROGRAM SMOUTHS U

> ; ۰ N

MAIN PROGRAM

& FOK SMUOTH-SMOOTH UNIVAC 1148 FONTRAM IV LEVEL 2201 0429 F46148 THIS COMPLETION WAS DUNE ON 29 APH OR AT 13:17:09

DimENSION Y (300), YT (300), # (300), YD (300), DYS (300, 3), DEL (3), YDS (30^)

DIMENSION LABEL(12) ÷,

DIMENSION VOLT(100) • =

#UIAUWOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL. 142 FURMAT(/20X+42HFOURIER COEFFICIENTS OF SOUARE ROOT SIGNAL /) 10K UATA RANGE... i4,1X,1H(F5.2,1H/F4.2,1H/F5.2,5H)E.V.) WKITE(6,143) (3(K),K=1,NPM) WKITE(6,141)(Y(I),I=1,NP) Y(I) = SonT(Y(I)) - YI - YF + X((I)A "NTKA)TNIWV = NIWA YF = (SQRT(Y(NP)) - YI)/HLIF (YMIN.65.U) 50 TO 210 163 FURMAT(10X,10E10.3) V(I) = Y(I) - YMIH181 FURMAT(10X,10F8.0) CALL FOUR (NP.Y.B) PT = 3.141592655 DU 186 I'= 1,NPM YI = SORT (Y(1)) 00 21 I = 1,NP DU 205 I=1.NP YMIN = 1.6+37 UU 206 I=1,NP 210 KRITE(6,152) CNPH = NPH **2US CONTINUE 206 CUNTINUE** XC+X = X T3 X = 0.0 CI = I20. 32. 27. 28. 29. 30. 33. 37. 31. ・サウ 35. 38. 47. е.њ. 45**.** 46. 35. .55 41. 17 46. 49**.** 50. 4 Ú • 42. 51.

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	52. 53.	<pre>186 B(I) = B(I)*COS(Pl*CI/(2.U*CNPV))**2 WKITE(6*15) 1.4 ECONATIONUTED CONDUNCTE ETITEDED BY CREAND ATTINCTION</pre>	
		.403 FUNMAIL/2019*7/FUNMAEN VOMPUNENIS FALIEREU BT CUS##2 AITUATION #KITE(6,183)(B(K),K=1,0PM)	^
	56.	IF (NMAX.NE.D) GU TO 35	
	57.	B1 = 0.0	
	56.	DU 24 I = 1,20	
	- 26.	NPI = NP-I	
	őů.	24 BT = BT+B(NPI)**2	
	. 61.	K = 20	
	. 62.	201 h = M ^{p-K}	
,	- ó3.	ßt = B(N=1) ≠≠2	
1	64•	CK = K	
10	65.	BLT = DT/CK	
,	66.	IF (BE/BET-16.)27.27.28	
	67.	27 IF (N-2)29,29,33	
	. 68.	29 RMAX = NP/10	
	69.	WKITE(6,291)	
	70.	291 FURNAT(/20X+11HTEST FAILED /)	
	.12	GC TO 35	
	72.	ο3 K = K+1	
	73.	Bī = H1+8č	
	74.	GL TO 261	
	75.	26 IF (N-25)231,33,33	
	76.	261 NMAX = N+2	
	.17	JS CONTINUE	
	. 78.	WAITE(6,36)NMAX	

	uENT							, L	,																	
CALL FOURI (NMAX+NP+B+Y+YD)	36 FURMAT(/2ŭX+24HSMUOTHED SGIJARE ROOT HAS I4+IX+18HFOURIER COMPO	15 /)	×=0.0	DJ 37 K = 1,NP	VK = Y(K) + YI + YF + X	Y(K) = YK+YK		IC* THE TEST FOR EQUALITY RETWEEN NON-INTEGERS MAY NOT BE MEANINGFI	IF(YMIN.6E.U) GO TO 44	D0 43 I=1,NP	NIWA + (T)A = (T)A	43 CONTINUE	44 NPMI = NP - 2	D0 45 I =1,2	45 YUS(I) = 0.0	D0 46 I = 3+14MI	<pre>+6 YLS(I) = 0.10+(-2.0+Y(I-2)-Y(I-1)+Y(I+I)+2.0+Y(I+2))</pre>	dN#WdN = I S9hod	465 YUS(I) = J.G	D0 60 J=1,NDEL	CALL UNFSUR(NMAX,NP,HL,DEL(J),NX,YI,YF,B,YT)	D0 40 I = 1.2	.40 DYS(1,1) = 1.0	DC 41 I = 3,NP4T	41 DYS(I+1) = U+10*(~5*0*YT(1=2)=YT(I=1)+YT(I+1)+2*0*YT(I+2))	G13-MG14 - I 64 DQ
-61	\$0.	.18	82.	кò.	84°.	85.	ă6.	DIAGNOST	a7.	80.	89.	.06	.16	92.	93.	94.	•35•	96.	.76	98.	.99	100.	101.	102.	L03.	104.2

52 FORMAT(/ 2UX 57HDSA = DEMIVATIVE OF (SMOOTHED SQUARE ROOT OF INPU / 184+ 1HX 13X 1HS 11X 3HDSA 9X 6H DT(0) 3(7X 3HDT(WKITE(6,63) X, Y(1), YD(I), YDS(I), (DYS(I,J),J=1,NDEL) 54 FURMAT(/ 20X 37HUT(.XX) = UENIVATIVE OF (IJNFOLDED S). 941 FURMAT(1-1, 33HPLUT OF S SMOOTHED ONCE (FOURIER) 51 FURMAT(/ 20X 26HS = INPUT DATA (SMOOTHED).) 53 FORMAT(/ 20X 26HbT(0) = DERIVATIVE OF (S). CALL PLOT (VOLT, Y, MP, 100, 44, 6 2 #DIAGNOSTIC* MESSAGE(S). WKITE(6,61) (DEL(1), I=1,NDEL) 65 FURMAT(10X, F9.2, 6F14+4 IF (ISTOP) 72, 24, 12 72 CALL EXIT 14, 12, 74 1 F4.2, 1:1)) Dv 70 I = 1.NP 42 DYS(I+J) = 0.0 *T GATA).) WKITE(6,901) VOLT(I) = X WHITE(6+54) WHITE(6+53) WKITE(6,51) WKITE (5,52) 60 CUNTINUE **bi** FCRMAT(XO + X = X O LIS=X **B**ND **D**ND END OF LISTING. 110. 108. 113. 117. 119. 120. 122 124. 125. 126. 127. 128. 129. 107. 109. 111. 115. 116. 118. 121. 106. 112. 114. 123. 130. 105.

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FOR UNFSURFUNFSON Ivac Iiug Fortram IV LEVEL 2201 0029 F46149 Is compilation and Cune on 29 apr 68 at 13:17:12	SUBKOUTINE UNFSER ENTRY POINT GOU440	SUBROUTINE UNFSOR(NC,NP,HL,DL,NX,SI,SF,6,Y)	DIMENSION Y(300), B(300),C(300),S(300),EX(300)	PL = 3,141592653	TLN = 0.69314716	CHI = (PI+DL/HL) **2/(16.*TLN)	Con = SI*SI=(SF*0=) **2/(8*0+L*)	CLOP = 2.0+CHI+HL/PI	56N = -1.0	Sul = 0.0	· SU2 = 0.0	DV 00 K = 1,NC	CA I A	SU1 = SU1 + CK*b(K)	5U2 = 5U2 + 56N*CK*b(K)	60 Seiv H -SGiv	Su1 = -2.0*SF*CLOP*SU1	5U2 = -2.u*5F*CLOP*5U2	Y(1) = CON+SUL	Y (2P) = (5F*HL) **2 +2.0*51*5F*HL+CON+5U2	NPH I NP-I	x = Dx	SINK = SIN(PI*X/HL)
a DH		ਜ	~	64	ŧ	ŗ.	·0	7.	ຕື	0 G	10.	11.	12,	13.	14.	15,	1ó.	17.	18.	19	20,	21	22

CANAL STREET

CUSX = COS(PI*X/HL)	EL = EXP(CHI)	FC = EC*EC	XMIS = ZNTS	CUSZ = COSX	NCM = MC-T	N = NC+NC	EXPZ = 1.0	DC 10 K =1,NT	EAP2 = EC*EXP2	EA(K) = EXPZ	10 EC = FC*EC	00 50 M = 2,NPM	Yid = (SF+X) +*2+2.0*SF*SI*X+CON	SINK = SINX	CUSK = COSX	DU 20 K = 1,NT	S(K) = SINK	C(K) = COSK	SINKP = SINK*COSX+COSK*SINX	CUSKP = CUSK+COSX-SINK+SINX	S. XX = SINKP	20 CUSK = COSKP	TC = 0.0	CO 30 K = 1.NCK
23.	24.	25.	20.	27.	26.	29.	30.	31.	32.	33.		35.	36.	37.	38.	39.	40.	41.	42.	•0 †	• = = =	ħŜ.	-04	47.

Kr = K+1	
DÚ 28 N = KP.KC	
NAK = N-K	
NPK = N+K	
28 DK = BK+B(N) *(EX(NMK) *C(NMK) - EX(NPK) *C(NPK))	
30 TG = TG + B(K) #bK	
Tri = 0.6	
TE = 0.0	
Du 4n K = 1.NC	
BK = ט(K)	
Ki = K+K	
Tú = TG+BK+GK+(TEX(KT)+C(KT))/2.0	
Tr = TH +oK+EX(K)*(X*S(K)+CLOP*CK+C(K))	
+0 T_ = T_ + RK+EX(K)+S(K)	
Y(M) = TG+2.0*SF*TH+2.0*S1*TE+YM	
XC+X = X	
SINK = SI(X*COSZ+COSX*SINZ	
COSA = CG5X*CUSZ=SINX*SINZ	
Surv = Sink	
où CúSi ≡ Cûsk	
kt TURN	
END	
NG. 0 *UIAGNOSTIC* MESSAGE(S).	

W FOR FOUR,FUUR Univac 1108 Fortram IV Level 2201 5029 F46149 This compilation was done on 23 apr 68 at 13:17:14

ENTRY POINT 000127 SUBROUTINE FOUR

SUBROUTINE FOUR (NP, Y, B) • 14

DIMENSION Y (300) + 6 (300)

PL = 3.141592653·,

CivP = NP

÷

t-dN = wdN

CNPM = NPM -

. 9

PION = PI/CWPM

....

в. °5

(NUI4) = CO = ZSOO

(NOID)NIS = ZMTS CUSK = COS

SINK = SINZ

DO 20 K =1,NPM

12.

äK = 0.0.

13.

CUSKI = COSK

14.

SINKI = SINK

15.

DU 22 I = 2,NPM

BK = BK + Y(I) *SINKI

17.

16.

SINI = SINKI*COSK+COSKI*SINK lō.

CUSI = COSKI*COSK-SINKI*SINK 19.

SINKI = SINI 20.

22 CUSKI = CUSI

21.

10. 11.

SINKI = SINK+COSZ+COSK+SINZ	COSKI = CUSK+COSZ-SINK+SINZ	CCSK =COSAI	SINK =SINKI	20 B(K)=2.0*UK/CNP
22.	23.	24.	25.	26.

and other states and be been and a state of the states of

26. 20 B(K)=2.0#UK/CNP 27. Réturn

28. ENU

END UF LISTING. 0 +DIAGNOSTIC* MESSAGE(S).

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G FOR FOURL FOURI UNIVAC 1100 FORTRAM IV LEVEL 2201 0029 F46148 This comptlation was dume on 29 APR 68 at 13:17:15

SUBROUTINE FOURI (NMAX, NP.6, Y, YP) UAMENLIN H(3UU) +Y(300) +YU(300) ENTRY POINT GOUL45 YUK # YDK + PiK+B(I)+COSKI į YK = YK+B(T)*SINK PL = 3.141592653 (M014) 500 = 7500) (WOIDJAIS = ZNIS DO 22 I =1. NMAX PIOA = PI/CNPM DU 20 K = 2.NP SINKI = SINK CUSKÌ = CUSK YU(1) = 0.0SINK = SINZ CUSK = COSZ $h^{\bullet}0 = (T)\lambda$ T-dN = WdN CNPM = NPM YLK = 0.0. PIK = PION YK = 0.0SUBROUTINE FOURI ł 12. 13. 14. 15. 19. 21. 11. 16. 17. 10. 20. 4 Ň ÷ ໍ່ຄ 10. 9 3 æ

Pik = PIK+PIOM	SINI = SINKİ*COSK+COSKI*SINK	CUSI = COSKI*COSK-SINKI*SINK	CUSKI = CUSI	INIS = INNIS	22 CONTINUE	CUSKI = CUSK+COSZ-SINK+SINZ	STNKI = COSK+SINZ+SINK+COSZ	CUSK = COSKI	SINK = SINKI	Y(K) = YK	20 YU(K)= YDK	RETURN	. ENO
22.	23.	24.	ک 5	26.	27.	20.	29.	30.	31.	32.	35.	. 4D	35.

END OF LISTING. 0 #DIAGNOSTIC* MESSAGE(S).

n.

STEP 9: SIMCUR

The program is designed to fold into any given analytic function a Gaussian function with specified full width at half maximum, Δ , in eV units:

$$F(E) = \frac{1}{N} \int_{x_0}^{x_L} f(E') \exp\left[-\ln \frac{2}{(1/2 \Delta)^2} (E - E')^2\right] dE'$$

where the normalization function is

$$N = \int_{x_0}^{x_L} \exp \left[-\ln \frac{2}{(1/2 \Delta)^2} (E - E')^2 \right] dE' .$$

In program notation the function is

$$CS(i) = \frac{\int_{x_0}^{x_L} CS(x) * \exp[-\xi(E - x)^2] dx}{\int_{x_0}^{x_L} \exp[-\xi(E - x)^2] dx}$$

where

$$\xi = \frac{LN(2)}{\left(\frac{1}{2}\Delta/13.605\right)^2}$$

$$E = \frac{EV(i)}{13.605}$$

$$X_0 = E - LIMITS$$

$$X_L = E + LIMITS$$

$$EV(i) = EVMIN + (i - 1) * DELEV$$

The output of this program is in table form giving the energy scale in ∂V and Rydberg units. As an option the output can be given in graphic form.

In the case considered here, the form of the ionization cross section proposed by Omidvar is in the program. This equation can be replaced by any other. In its present form it is possible to obtain as an option the ratio of Omidvar's function to any requested power function. The input card formats are as follows:

First Card: FORTRAN format is (2E12.6, 316)

Column

1-12	COE = coefficient of power function
13-24	POWER = power of the function
25-36	KLAST = 1: return for new run
	= 2: exit; all job completed

Second Card: FORTRAN format is (2E12.6, 316)

Column			
1-12	LIMITS	= i	ntegration interval
13-24	DELTA	= f	ull width at half maximum of Gaussian distribution
25-30	IFOLD	= 1	: do not fold data
		= 2	: fold data
31-36	IPLOT	= 1	: give plot
		= 2	: do not give plot
37-42	ILAST	= 1	: return here for new set of options after
			processing this problem
		= 2	: do not return here

Third Card: FORTRAN format is (3E12.6, I6)

Column

1-12	EVMIN	= 1	the	minimum	value	of	the	electron	energy	(eV)	in
		1	the	domain of	the p	rob	lem	1			

- 13-24 EVMAX = the maximum value of the electron energy (eV) in the problem
- 25-36 DELEV = the step for output starting at EVMIN and going to EVMAX

37-42 LAST = 1: return here for new values after processing

this problem

= 2: do not return here

Below is an example of the deck setup as it stands for the Omidvar equation. In this case we are comparing Omidvar's cross section first with the 1.127 power law and then with a 1.5 power law. A plot is not requested. The energy distributions requested are 0.06 eV and 0.08 eV.

91.9995		322322			1.1.1.1.1	4444	4555555	555556	6666666	556777	
	1-1-1-1-1-1-	. (. IN	GERT. S	IMUR	PREGRA	M HERE		21017101410			212(2)212121212
V XAT	SIMCUR		1.1.1.1.1					1.1.1.1.1		_1_1_1_1_1_1	
	0.1.1	Jun127	لي بيبي		uuu	LILL					
Lui	.0288	 1.06			الاستناسية						
	13.5	 		1.1.105		سأت أحاجه أحاجه				-1-1-1-1-1-	
	0288	 1.10.8				<u></u>					-4-2-2-4-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1
┟┶┵┵┷┷	13.5	 110.7			· · · · · 2		4-1-1-1-1-1-				
	<u> </u>	 <u> </u>							I.L.I. I. I.		╶╶┶╌┺╶┻╌┻╌╇╌╄╌ ╋╌
┝╾╾╌╾╸	0288	 1 4 7	<u></u>					<u></u>			┈┺╼╌┹╌┹╴┛╶┠╌┺╌
μ	1.1.2.2 Dava	 1 Internet	2			- kkkk			┙┛┉┸┉┺╍┺╍┺┙		<u>─┴ ↓ ↓ ↓ ↓ ↓ ↓ ↓</u>
	1.3.5	14.7							• • • • • •		
											
										1.1.1.1.1.1	

A program listing follows.

B FOR SIMCUR'SIMCUR UNIVAC IION FORTRAN IV LEVEL 2201 0029 F4614B THIS COMPILATION WAS DONE UN 27 MAY 68 AT 11:58:03

MAIN PRUGRAM ENTRY POINT 000000

1. C PLOT SIMPLE CURVE AND FOLD SIMPLE CURVE

2. DIMENSION CS(1900), EV(1000), ARRAY(20)

3. COMMON /SIGMA/ COE, POWER

4. COMMON /FUN/ XSEE, XK

5. DATA INIT/ -1/ [PEND/1/

6. REAL LIMITS

7. IP = 2

а. С 9. C... COE IS NOT USED IN OMIDVAR'S FUNCTION, INPUT CARD IS TO BE

10. C... LEFT BLANK IN THIS FIELD.

123

11. 400 READ(5.401) COE, PONER, KLAST

12. 401 FORMAT(2E12.6.316)

13. 410 READ(5,401) LIMITS, DELTA, IFOLD, IPLOT, ILAST

14. C SET LINE COUNTER

15. LC = 60

lo. C

17. XSEE = .69315/(.5*DELTA/13.605) **2

18. C READ INTEGRATION GRID DEFINITIONS.

19. 420 READ(5,421) EVMIN, DELEV, EVMAX, LAST

20. 421 FORMAT(3E12.6' I6)

21. I = 0

22. 60 TO (450, 550), IFOLD

23. C SIMPLE CURVE

	51.	IF(I.6T.1) GO TO 605
	52.	EV(1) = EVMIN
	55.	G0 T0 607
	54.	605 EV(I) = EV(I-I) + DELEV
	55.	607 XK = EV(1)/13.605
	50.	XO = XK = LIMITS
	57.	XL = XK + LIMITS
	56.	NP = 1
	59.	REL = .01
	60.	CALL GAUSS(INIT, XO, XL, Y1, REL, NP, 1)
	• 1 9	NP = 1
	62.	REL = .01
1	63.	CALL GAUSS(INIT, XO, XL, Y2, REL, NP, 2)
25	64.	CS(1) = Y1/Y2
	65.	YMAX = AMAX1(YMAX+CS(I))
	66 .	IF(LC.LT.54) GO TO 620
	67.	610 WRITE(6/611) DELTA/ LIMITS
	68.	611 FORMAT(1H1, 9X, 2SHFOLDED CURVE USING DELTA= , F10.5, 9H, LIMITS
	•69	1 F10.5, 12H - OMIDVAR - // 54X, 2HEV, 19X, 1HK, 18X, 2HCS)
	70.	CALL BCDCON(ARRAY)
	71.	WRITE(0,615) DELTA, LIMITS
	72.	615 FORMAT(25HFOLDED CURVE USING DELTA# , F10.5, 8H LIMITS= , F10.5
	73.	1 12H - OMIDVAR - 31X)
	74.	LC = 3
	75.	620 WRITE(6+521) ÉV(I), XK, CS(I)
	76.	rc = rc + 1
	77.	IF(ABS(EV(I)-EVMAX)001) 700, 700, 600

記書が上たが言うため

C THIS 700 60 TO 710 60 TO 710 60 TO 720 IF(IF 720 IF(IF 720 CALL 1PENC CALL		GRID COMPLETE	(420+ 710)+ LAST	FOLD COMPLETE. CHECK FOR P) (720, 750), IPLOT	540.6T.1) 60 TO 730	SETUP(0.0, 0, 16)) = 2	1	ADF	DGA(123,766,0,900, 13,45,	OUTLIN	DRG(5+7)	SBLIN(5,9)	SLLIN(7,9)	·	DVR(II+1+EV+CS+1)	L GRAPH	CONX (1, XPT)	. CONY (1000+ YPT)	TSP (XPT, YPT, ARRAY, 96)	K FOR NEXT IFOLD	CO (410, 760), ILAST	CURVE COMPLETE	[0 (400, 770)• KLAST	OF JOB	01 0000 0010 10
	с С	C THIS (700 60 10	C THIS	710 60 70	720 IF(IF	CALL	IPEND	= d1	730 CALL	CALL	CALL	CALL	CALL	CALL	1=11	CALL	C LABEL	CALL	CALL	CALL	C CHECI	750 GO T	C THIS	760 60 1	C END	

105. C CLOSE OUT PLOT ROUTINE

106. 740 CALL FINISH

107. 800 STOP

108. 900 WRITE(6,901)

901 FORMAT(113H CHECK INPUT VALUE FOR EVMIN' EVMAX AND DELEV' ONE OF 109.

110. 1HEM IS IN ERROR AND WILL CAUSE RESERVED STORAGE OVERFLOW.

III. IF(IPEND.EQ.I) STOP

112. IP = 2

113. 60 TO 770

114. END

END OF LISTING. 0 *DIAGNOSTIC* MESSAGE(S).

SUBROUTINE GAUSS ENTRY POINT 000317	UTINE GAUSS ENTRY POINT 000317 SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) DIMENSION AA(16), HH(16), YBAR(10), BYB(10) IF(INIT) 1, 1, 2 I INIT = 1 AA(1) = -989400935 AA(1) = -989400935 AA(1) = -98940098 AA(1) = -994457502 AA(4) = -755404408 AA(1) = -994457502 AA(4) = -9561578 AA(4) = -9561578 AA(4) = -9561578 AA(4) = -9501578 AA(4) = -9501578 AA(4) = -950125096E-01 AA(5) = -4A(7) AA(10) = -AA(7) AA(10) = -AA(7) AA(10) = -AA(7) AA(10) = -AA(7) AA(12) = -AA(5) AA(12) = -AA(1) AA(12) = -	N - 0 0 0 0 0 0 0 0 0 0
 SUBROUTINE GAUSSTINIT, XO, XL, Y, REL, MP, IFUN) DIMENSION A(16), HH(16), YBAR(10), BYB(10) IF(INIT) 1, 1, 2 INIT = 1 INIT = 1 A(1) = -969400935 A(2) = -944575023 A(2) = -944575023 A(2) = -944575023 A(3) = -965631202 A(4) = -75540408 A(4) = -75540408 A(4) = -75540408 A(4) = -75540408 A(4) = -75501202 A(1) = -965631202 A(1) = -950125098E-01 A(1) = -950125098E-01 A(1) = -40(6) A(1) = -40(6) A(1) = -40(1) A(1) = -A1(4) A(1) = -A1(4) 	AA(14)= -AA(3)	16.
 SUBROUTINE GAUSSIINITY XOF XL, YFREL MPF IFUN) DIMENSION AA(16)* HH(16)* YBAR(10), BYB(10) IF(INIT) 1, 1, 2 IF(INIT) 1, 1, 2 A(1) =089400335 A(1) =089400335 A(1) =989400335 A(2) =944575023 A(1) =95604008 A(2) =9560408 A(4) =755404408 A(4) =755404408 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =950125096E-01 A(1) =9501	AA(14)= -AA(3)	16.
 SUBROUTINE GAUSSIINITY XOF XL, YFREL MP. IFUN) DIMENSION AA(16), HH(16), YBAR(10), BYB(10) IF(INIT) 1, 1, 2 IF(INIT) 1, 1, 2 A(1) =099400335 A(1) =099400335 A(1) =999400335 A(1) =999400335 A(2) =944575023 A(1) =95601078 A(2) =956016778 A(4) =75504408 A(4) =75504408 A(5) =617376244 A(6) =95016778 A(7) =0103551 A(7) =91003551 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =95016778 A(1) =9103551 A(1) =9103555 A(1) =910555 A(1) =910555 A(1) =910555 A(1) =		•
1. SUBROUTINE GAUSSTINITY XO' REL, MP, IFUN) 2. DIMENSION AA(16)' HH(16)' YBAR(10), BYB(10) 3. IF(INIT) 1. 1. 2 4. 1 INIT = 1 5. DIMENSION AA(16)' HH(16)' YBAR(10), BYB(10) 3. IF(INIT) 1. 1. 2 4. 1 INIT = 1 5. IF(INIT) 1. 1. 2 6. INIT = 1 7. AA(1) =969400935 6. AA(2) =944575023 7. AA(2) =96531202 8. AA(2) =96551202 8. AA(3) =9553102 9. AA(4) =755403406 9. AA(5) =617866244 10. AA(5) =61786244 10. AA(6) =62612609551 11. AA(7) =231603551 12. AA(8) =950126096E-01 13. AA(9) =950126095E-01 14. AA(10) = -AA(7) 15. AA(10) = -AA(17) 16. AA(10) = -AA(17)	AA(13)= -AA(4)	17.
 SUBROUTINE GAUSSTINITY XOF XL, YY RELF MP, IFUN) DIMENSION AA(16)+ HH(16)+ YBAR(10)+ BYB(10) IF(INIT) 1, 1, 2 IF(INIT) 1, 1, 2 A(1) = -+989400935 A(1) = -+989400935 A(2) = -+944575023 A(2) = -+944575023 A(3) = -+944575023 A(3) = -+9501202 A(4) = -,-55040408 A(4) = -,-55040408 A(4) = -,-55016778 A(4) = -,-591603551 A(4) = -,-591603551 A(6) = -,-450016778 A(6) = -,-590125096E-01 A(9) = -A0(6) A(1) = -A0(7) A(1) = -A0(7) A(1) = -A0(7) 		
 SUBROUTINE GAUSSIANTY XO, XL, Y. REL. MP. IFUN) DIMENSION AA(16), HH(16), YBAR(10), BYB(10) IF(INIT) 1, 1, 2 INIT = 1 A(1) =969400355 A(1) =969400355 A(2) =9944575023 A(2) =9944575023 A(2) =95016726244 A(4) =755404408 A(4) =755404408 A(6) =456016778 A(1) =950125098E-01 A(1) =950125098E	AA(12)= -AA(5)	16.
 SUBROUTINE GAUSSIMITY XOF XL, YFRL, MP. JFUN) DIMENSION ALL6)+ HH(L6)+ YBAR(L0) IF(INIT) 1. 1. 2 IF(INIT) 1. 1. 2 1 INIT = 1 AA(1) = -969400935 AA(2) = -944575023 AA(2) = -944575023 AA(2) = -944575023 AA(2) = -944575023 AA(2) = -956531202 AA(4) =75540440B AA(4) =75540440B AA(4) =75540440B AA(4) =9501250946-01 AA(7) =9501250946-01 AA(10) = -AA(7) 	AA(11)= -AA(6)	15.
1. SUBROUTINE GAUSSTANTY XOP, XL, YY, REL, MP, IFUN) 2. DIMENSION AA(16)' HH(16)' YBAR(10)' BYB(10) 3. If(INIT) 1. 1. 2 4. 1 INIT = 1 5. AA(1) = -999400935 6. AA(1) = -999400935 6. AA(1) = -999400935 6. AA(1) = -969400935 7. AA(2) = -9944575023 7. AA(2) = -965631202 8. AA(2) = -965631202 8. AA(2) = -944575023 7. AA(2) = -944575023 8. AA(2) = -944575023 9. AA(2) = -944576244 10. AA(5) = -617876244 10. AA(5) = -612876244 11. AA(5) = -612876244 12. AA(8) = -950125096E-01 12. AA(9) = -AA(8)	AA(10)= -AA(7)	14.
1. SUBROUTINE GAUSS(INIT: X0. XL. Y. REL. NP. IFUN) 2. DIMENSION AA(16). HH(16). YBAR(10) BYB(10) 3. IF(INIT) 1. 1. 2 4. 1 INIT = 1 5. A(1) =96940035 6. A(1) =96940035 7. A(2) =944575023 7. A(2) =944575023 7. A(2) =944575023 8. AA(2) =95631202 8. AA(2) =944575023 10. AA(3) =61787644 10. AA(4) =55016778 11. AA(5) =61806544 12. AA(8) =950125096E-01 13. AA(9) = -AA(8)		
1. SUBROUTINE GAUSSITINTY, XO, XL, Y, REL, NP, IFUN) 2. DIMENSION A(16), HH(16), YBAR(10), BYB(10) 3. IF(INIT) 1, 1, 2 4. 1 INT = 1 5. A(1) =989400935 6. A(1) =989400935 6. A(1) =989400935 6. A(2) =944575023 7. A(2) =944575023 8. A(2) =944575023 8. A(2) =944575023 9. A(2) =944575023 10. A(3) =865651202 8. A(4) =755404408 9. A(5) =617876244 10. A(5) =617876244 11. A(7) =281603551 12. A(6) =950125096E-01	AA(9) = -AA(8)	13.
1. SUBROUTINE GAUSCINITY XOF XL, YF RELF NPF IFUN) 2. DIMENSION AA(16)* HH(16)* YBAR(10) 3. IF(INIT) 1, 1, 2 4. 1 INIT = 1 5. AA(1) = -969400935 6. AA(2) = -944575023 7. AA(2) = -944575023 8. AA(2) = -965631202 8. AA(2) = -965631202 8. AA(3) = -617876244 9. AA(5) = -617876244 10. AA(5) = -617876244 10. AA(5) = -458016778 11. AA(7) = -281603551	AA(8) =950125098E-01	12.
1. SUBROUTINE GAUSS(INIT: X0: XL: Y: REL: NP: IFUN) 2. DIMENSION AA(16): HH(16): YBAR(10): BYB(10) 3. IF(INIT) 1. 1. 2 4. I INIT = 1 5. AA(1) =989400935 6. AA(1) =989400935 6. AA(2) =9944575023 7. AA(2) =9944575023 7. AA(2) =995400935 8. AA(4) =755404408 9. AA(5) =456016778 10. AA(6) =456016778	AA(7) =281603551	-11
1. SUBROUTINE GAUSS(INIT: X0: XL: Y: REL: NP: IFUN) 2. DIMENSION AA(16): HH(16): YBAR(10); BYB(10) 3. IF(INIT) 1: 1: 2 4. 1 INIT = 1 5. AA(1) =969400935 6. AA(1) =969400935 6. AA(1) =969400935 6. AA(2) =944575023 7. AA(2) =944575023 8. AA(3) =955404408 9. AA(5) =617876244	AA(6) =458016778	10.
 SUBROUTINE GAUSS(INIT: X0: XL: Y: REL: NP. IFUN) DIMENSION AA(16): HH(16): YBAR(10). BYB(10) IF(INIT) 1: 1: 2 INIT = 1 AA(1) =969400935 AA(1) =969400935 AA(2) =944575023 AA(2) =944575023 AA(2) =955404408 AA(4) =755404408 	AA(5) =617876244	•6
 I. SUBROUTINE GAUSS(INIT, X0, XL, Y, REL, NP, IFUN) 2. DIMENSION AA(16), HH(16), YBAR(10), BYB(10) 3. IF(INIT) 1, 1, 2 4. 1 INIT = 1 5. AA(1) =989400935 6. AA(2) =944575023 7. AA(3) =865631202 	AA(4) =755404408	8.
 I. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) 2. DIMENSION AA(16), HH(16), YBAR(10), BYB(10) 3. IF(INIT) 1, 1, 2 4. I INIT = 1 5. AA(1) = -,989400935 6. AA(2) = -,944575023 	AA(3) =865631202	7.
 L. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) 2. DIMENSION AA(16), HH(16), YBAR(10), BYB(10) 3. IF(INIT) 1, 1, 2 4. 1 INIT = 1 5. AA(1) =989400935 	AA(2) =944575023	é.
 L. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) C. DIMENSION AA(16), HH(16), YBAR(10), BYB(10) J. IF(INIT) 1, 1, 2 H. IINIT = 1 	AA(1) =969400935	• •1
 I. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) 2. DIMENSION AA(16), HH(16), YBAR(10), BYB(10) 3. IF(INIT) 1, 1, 2 	1 INIT = 1	•
I. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) 2. DIMENSION AA(16), HH(16), YBAR(10), BYB(10)	IF(INIT) 1, 1, 2	, • 17
L. SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN)	DIMENSION AA(16)• HH(16)• YBAR(10)• BYB(10)	°.
	SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN)	•

HH(2) = .62253524E-01	HH(3) = ,95158512E-01	HH(4) = .12462897	HH(5) = .14959599	HH(6) = .16915652	HH(7) = .18260342	HH(8) = ,18945061	HH(6) = HH(8)	HH(10)= HH(7)	HH(11)= HH(6)	HH(12)= HH(5)	HH(13)= HH(4)	HH(14)= HH(3)	HH(15)= HH(2)	HH(16)= HH(1)	NG = 16	U	2 Y = 0.0	XLGTH = XL - XO	IF(XLGTH) 201, 105, 201	201 NPP = NP	00 103 K=1+10	Y = 0.	ENP = NP	00 200 L=1.NP
22.	23.	24.	25.	26.	27.	28.	29.	30.	31.	32.	33.	9.4. 0	35.	3 6.	37.	38.	39.	40.	41.	42.	4.5.4	• = =	45.	46.

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AREA = 0.0	- YF = F	X1PX2 = {2.0+AL - 1.0}+XLGTH/ENP + 2.0+X0	X2MX1 = XLGTH/ENP	D0 100 J=1+NG	X = (X1PX2 + AA(J)*X2MX1)/2.0	CALL FOFX(X, FX, IFUN)	100 AREA = AREA + HH(J)*FX	Y = Y + AREA	200 CONTINUE	Y = XLGTH/(2.0*ENP)*Y	YBAR(K) = Y	IF(K-1) 104, 104, 144	144 BYB(K-1) = ABS(YBAR(K-1) - Y)	IF(BYb(K=1) = REL*ABS(Y)) 105, 105, 104	104 NP = 2*NP	103 CONTINUE	D0 108 L=1/10	REL = 2.0*REL	D0 107 K=2,10	IF(BYB(K-1) - REL*ABS(YBAR(K))) 106, 106, 107	107 CONTINUE	108 CONTINUE	K = 10	106 NP = (2**(K=1))*NPP
47.	48.	+ 6 +	• 0¢	51.	52.	53.	54.	50.	56.	57.	56.	59.	60.	61.	62+	63.	64•	65.	66.	67.	68.	• 69	70.	71.



W FOR FOFX,FOFX UNIVAC 1100 FORTRAN IV LEVEL 2201 0029 F46148 This compilation was done on 27 May 68 at 11:58:11

SUBROUTINE FOFX ENTRY POINT 000033

- 1. SUBROUTINE FOFX(X, FX, IFUN)
- 2. C EVALUATE ONE OF TWO FUNCTIONS FOR GAUSS.
 - 5. COMMON /FUN/ XSEE, E'
- 4. FX = EXP(=XSEE*(E=X)++2)
- 5. 60 TO (100, 200), IFUN
- 0. 100 CALL CROSS(X+ CS)

1

- 7. FX = FX+CS
- 8. 200 RETURN
- 9. END

END OF LISTING. 0 +DIAGNOSTIC+ MESSAGE(S).

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. . .

G FOR CROSS/CROSS UNIVAC 1105 FORTRAN IV LEVEL 2201 0029 F46148 THIS COMPILATION WAS DONE ON 27 MAY 68 AT 11:56:13

ENTRY POINT 000122 SUBROUTINE CROSS

SUBROUTINE CROSS (E, CS) 4

/SIGMA/ COE, POWER COMMON Ň

ن *

OMIDVAR : ;;

u . ئ REAL NU

ò

VALUE = E - 1.0 ř

IF (VALUE) 100, 100, 200 •

100 CS = 0.0 •

RETURN 16.

133

200 NU = 1.0/(SORT(E)+1.0) 11.

F1 = 16.0*NU12.

F2 = 3.0 - F14NU 13. F3 = 2.0*NU#ALOG(4.0*VALUE) 14.

CS = 6.0*NU*(1.0 + 3.0*(F2*CuS(F3) + F1*SIN(F3))/(F2**2 + F1**2)) ;;

*VALUE**1.5/{TANH(3.14159265*NU)*.014) 16.

IF (POWER) 210+ 220+ 210 17.

210 CS = CS/VALUE**POWER 14.

220 RETURN 19.

END 20.

0 *DIAGNOSTIC* MESSAGE(S). END OF LISTING.

STEP 10: SIMTAB

This program is designed to fold a Gaussian function into any given \therefore function which has been prepared in table form. This program is identical to SIMCUR except the term CS(x) is interpolated from tabular data.

It is not necessary that the input be given in equal intervals. Within the program is an interpolation subroutine that can be as much as a ninthorder polynomial.

The input card formats are as follows:

First Card: FORTRAN format is (216)

Column

1-6	NL = number of points in the table (max 100)
7-12	KLAST = 1: return here for new table

= 2: exit; all jobs finished

Table Cards: FORTRAN format is (6E12.6)

Column

1-12	XX(1) = first energy value
13-24	YY(1) = first cross section value
25-36	XX(2)
37-48	YY(2)
49-60	XX(3)
61-72	YY(3)

Continue with three pairs per card.

Next Card after Table: FORTRAN format is (2E12.6, 3I6)

Column	
1-12	LIMITS
13-24	DELTA
25-30	IFOLD
31-36	IPLOT
37-42	ILAST

Next Card: FORTRAN format is (3E12.6, I6)

Column

1-12	EVMIN
13-24	DELEV
25-36	EVMAX
37-42	LAST

The last two cards are identical to cards two and three for the SIMCUR program.

A program listing follows.

G FOR SIMTAB'SIMTAB UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F4G14B This compilation Was Done UN 27 May 68 at 11:58:16

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	ł		
	23.		X5EE = •69315/(•5*DELTA/13.605)**2
	24.	U	READ INTEGRATION GRID DEFINITIONS.
	25.	420	READ(5+421) EVMIN, DELEV, EVMAX, LAST
	2ó.	421	FORMAT(3E12.6' I6)
	27.		I = 0
	28.		60 TO (450, 550), IFULD
	29.	U	SIMPLE CURVE
	30.	450	YMAX = 1.E-37
	31.	500	1 + 1 = 1
	32.		IF(I.GT.1000) 60 TO 900
			IF(I.6T.1) G0 T0 505
	34.		EV(1) = EVMIN
	35.		GO TO 507
137	. 36.	505	EA(I) = EA(I-I) + DELEV
,	37.	507	XK = EV(I)/13.605
	38.		CALL CROSS(XK, CS(I))
	. 6£		YMAX = AMAX1(YMAX, CS(I))
	• 17 /		IF(LC.LT.54) 60 TO 520
	41.	510	WRITE(6,511) ITAB
	42.	511	FORMAT(1H1, 39X 41H SIMPLE CURVE SIGMA = FUNCTION OF TABLE
	43.	•••	I // 54X 2HEV 19X 1HK 18X 2HCS)
	• • •		CALL BCDCON(ARRAY)
	45.		WRITE(0,515) ITAB
	40.	515	FORMAT(40HSIMPLE CURVE SIGMA = FUNCTION OF TABLE 13, 53X)
	47.		LC = 3
	46.	520	WRITE(6+521) EV(1), XK, CS(1)
	•64	521	FORMAT (± 36X+ 3E20+8)

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50.	rc = rc + 1	
51.	IF((EV(I)+DELEV).LT.EVMAX) GO TO 500	
DIAGNOSTIC	THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT HE MEANINGFUL.	
54.	IF(EV(I).6E.EVMAX) GO TO 700	
53.	IF((I+1).6T.1000) 60 TO 900	
54.	1 = 1 + 1	
55.	EV(I) = EVMAX	
56.	G0 T0 507	
57. C	•	
5¢• C	FOLDED CURVE	
59. 550	YMAX = 1.E-37	
60. 600		
61.	IF(1.6T.1000) 60 TO 900	
•29	IF(I.6T.1) GO TO 605	
63.	EV(1) = EVMIN	
64.	G0 T0 607	
6 0 5	EV(I) = EV(I-1) + DELEV	
66. ôU7	XK = EV(I)/13.605	
67.	XO = XK - LIMITS	
68.	XL = XK + LIMITS	
67.	NP = 1	
70.	REL = .01	
71.	CALL GAUSS(INIT' XO, XL, Y1, REL, NP, 1)	
72.	NP = 1	
73.	REL = .01	
74.	CALL GAUSS(INIT, XO, XL, Y2, REL, NP, 2)	
75.	CS(I) = Y1/Y2	
7		
-------------	-------------	---
. .		IMAX = AMAX1(TMAX+CS(I))
.17.		IF(LC.LT.54) G0 T0 620
73.	611	0 WRITE(6,611) DELTA, LIMITS, ITAB
79.	61.	I FORMAT(1H1, 9X, 25HFOLDED CURVE USING DELTA= , F10.5, 9H, LIMITS
86.		1=+ F10.5+ 27H SIGMA = FUNCTION OF TABLE 13 //
61 .		2 54X, 2HEV, 19X, 4HK, 18X, 2HCS)
82.		CALL &CDCON(ARRAY)
ġ3.		MRITE(0,615) DELTA, LIMITS, ITAB
84.	615	5 FORMAT(25HFOLDED CURVE USING DELTA= + F10.5, 8H LIMITS= + F10.5+
65.		1 27H SIGNA = FUNCTION OF TABLE [3])
66.		LC = 3
67.	62 0) WRITE(6,521) EV(1), XK, CS(1)
80.		FC = FC + 1
-88°	·	IF((ËV(I)+DELEV)•LT•EVMAX) G0 T0 600
DIAGN	STIC	THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
90.		IF(EV(I).6E.EVMAX) GO TO 700
•16		IF((I+1).6T.1000) G0 T0 900
92.		I = I + T
93.		EV(I) = EVMAX
94.		G0 T0 607
90.	J	
96.	U	THIS GRID COMPLETE
97.	700	GO TO(420, 710), LAST
96.	U	THIS FOLD COMPLETE. CHECK FOR PLOT.
•66	710	60 TO (720, 750), IPLOT
100.	720	IF(IPEND.6T.1) 60 T0 730
101.		CALL SETUP(0.0, 0, 16)

CALL SETUP(0.0, 0, 16)

								•																		
IPEND = 2	IP = 1	30 CALL ADF	XX1 = XX(1)+13.605	. XXNL = XX(NL)*13.605	CALL DGA(123, 766, 0, 900, XX1, XXNL, YMAX, 0,0)	CALL OUTLIN	CALL DRG(5,7)	CALL SBLIN(5,9)	CALL SLLIN(7,9)	1:=1-T	CALL DVR(II,1,EV,CS,1)	- LABEL GRAPH	CALL CONX (1, XPT)	CALL CONY (1000, YPT)	CALL TSP (XPT, YPT, ARRAY, 96)	CHECK FOR NEXT IFOLD	50 60 TO (410, 760), ILAST	THIS CURVE COMPLETE	0 60 TO (400, 770), KLAST	END OF JOB	70 60 T0 (780, 800), IP	CLOSE OUT PLOT ROUTINE	10 CALL FINISH	0 STOP	0 WKITE(6,901)	1 FORMAT(113H CHECK INPUT VALUE FOR EVMINE EVMAN AND
		el.														υ	75	U	76	U	17	J	781	801) 0 6	905
102.	103.	104	-901.	106.	107.	106.	109.	110.	.111	112.	113.	114.	115.	116.	117.	118.	119.	120.	121.	122.	123.	124.	125.	126.	127.	128.

129. IHEM IS IN ERROR AND WILL CAUSE RESERVED STORAGE OVERFLOW.

130. IF(IPEND.EQ.1) STOP

131. IP = 2

132. 60 T0 770

133. END

END OF LISTING. 2 #DIAGNOSTIC* MESSAGE(S).

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© FOR GAUSS'GAUSS Univac 1108 Fortran IV Level 2201 0029 F4614B This compilation was done on 27 May 68 at 11:58:20

SUBROUTINE GAUSS ENTRY POINT 000317

SUBROUTINE GAUSS(INIT, XO, XL, Y, REL, NP, IFUN) DIMENSION AA(16), HH(16), YBAR(10), BYB(10) AA(8) = -.950125098E-01 •27152459E-01 •62253524E-01 AA(2) = -.944575023 AA(4) = -.755404408 AA(6) = -.458016778 AA(1) = -.989400935AA(3) = -.865631202 A4(5) = -.617876244 A4(7) = -.281603551 IF(INIT) 1. 1. 2 AA(9) = -AA(8) AA(14)= -AA(3) AA(15)= -AA(2) AA(16)= -AA(1) AA(10)= -AA(7) AA(11)= -AA(6) AA(13)= -AA(4) AA(12)= -AA(5) HH(2) = HH(1) = 1 INIT = 1, ÷ 17. 19. 21. 16. 20. 22. 15. 16. ÷ å ÷ 12. 13. 14. ÷ 4 Ň å å ň

HH(3) = +95158512E-01	HH(4) = •12462897	HH(5) = 14959599	HH(6) = .16915652	HH(7) = .18260342	HH(8) = .18945061	HH(6) = HH(8)	HH(10)= HH(7)	HH(11)= HH(6)	HH(12)= HH(5)	HH(13)= HH(4)	HH(14)= HH(3)	HH(15)= HH(2)	HH(16)= HH(1)	NG = 16	U	2 Y = 0.0	XLGTH = XL - XO	IF(XLGTH) 201, 105, 201	201 NPP = NP	D0 103 K=1,10	Y = 0.	ENP = NP	D0 200 L=1,NP	AREA = 0.0	9 1 = T
53 .	24.	25.	26.	27.	26.	29.	30.	31.	32.	33.	34.0	35.	36.	37.	36.	39.	40.	•14	42.	43.	• † †	45.	46.	47.	46.

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X1PX2 = (2.0*AL - 1.0)*XLGTH/ENP + 2.0*X0	X2MX1 = XLGTH/ENP	D0 100 J=1+NG	X = (X1PX2 + AA(J)*X2MX1)/2.0	CALL FOFX(X+ FX+ IFUN)	100 AREA = AREA + HH(J)*FX	Y = Y + AREA	200 CONTINUE	Y = XLGTH/{2.04ENP}#Y	YBAR(K) = Y	IF(K-1) 104, 104, 144	144 BYB(K-1) = ABS(YBAR(K-1) - Y)	IF(BYB(K-1) - REL*ABS(Y)) 105, 105, 104		103 CONTINUE	D0 108 L=1/10	REL = 2.0¥REL	. DC 107 K=2,10	IF(BYB(K-1) - REL*A8S(YBAR(K))) 106+ 106+ 107	107 CONTINUE	108 CONTINUE	K = 10	100 NP = `(2**{K-1))*NPP	Y = YBAR(K)	105 RETURN	END	F LISTING. 0 *DIAGNOSTIC* MESSAGE(S).
• 6 1	5U•	51.	52.	53.	54.	55.	56.	57.	58.	59.	60.	61•	62.	63.	•	65.	ξΰ.	67.	68.	•69•	70.	-12	72.	73.	74.	END O

G FOR FOFX,FOFX UNIVAC 1104 FORTRAN IV LEVEL 2201 0029 F4G148 Tris completion was done on 27 May 68 at 11:58:23

SUBROUTINE FOFX ENTRY POINT 000033

1. SUBROUTINE FOFX(X, FX, IFUN)

2. C EVALUATE ONE OF TWO FUNCTIONS FOR GAUSS.

3. COMMON /FUN/ XSEE' E

4. FX = EXP(-XSEE*(E-X)**2)

5. GO TO (100, 200), IFUN

6. 100 CALL CROSS(X, CS)

7. FX = FX+CS

8. 200 RETURN

9. END

END OF LISTING. 0 *DIAGNOSTIC* MESSAGE(S).

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& FOR CROSS.CROSS UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 THIS COMPILATION WAS DONE ON 27 MAY 68 AT 11:58:26

ENTRY POINT 000034 17 CS = TERP(XX, YY, NL, E, 3) DIMENSION XX(100) YY(100) COMMON /SIGMA/ NL. XX. YY SUBROUTINE CROSS (E.CS) 10 IF(E-XX(2)) 15, 16, 17 IF(YY(1)) 10. 10. 17 16 CS = YY(2) SUBROUTINE CROSS RETURN RETURN 15 CS = 0 10. .-• 2 ŝ 5 : ŝ

12. RETURN

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IF(CS.LT.0.) CS = 0.0

13. END

END OF LISTING. 0 *DIAGNOSTIC* MESSAGE(S).

11.

G FOR TERP,TERP UNIVAC 1108 FORTRAN IV LEVEL 2201 0029 F46148 THIS COMPLLATION WAS DONE ON 27 MAY 68 AT 11:58:29

I

	UNCTION	TERP ENTRY POINT 000267	
+		FUNCTION TERP(X+Y+NL+ARG+IL)	TERPOOLO
\$	l J		-TERP0020
З.	U	THIS FUNCTION DOES LAGRANGIAN INTERPOLATION OR	TERP0030
• •	IJ	EXTRAPOLATION OF ILTH ORDER ON X AND Y FOR ARG	TERP0040
. و	IJ	WHEN THE TABLES ARE EITHER INCREASING OR DECREASING	TERP0050
•0			-TERP0060
- 2	U	X X ARRAY, INDEPENDENT VARIABLE	TERP0070
•0	U	Y Y ARRAY, DEPENDENT VARIABLE	TERPU080
6	IJ	NL . NUMBER OF ENTRIES IN TABLES OF X AND Y	TERP0090
10.	U	ARG INDEPENDENT VARIABLE VALUE	TERP0100
11.	U	IL NUMBER OF POINTS TO USE FOR INTERPOLATION	TERP0110
12.			-TERP0120
13.		DIMENSION X(2) + Y(2)	TERP0130
14.	U	DIMENSION X(2), Y(2)	TERP0140
15+	C		-TERP0150
16.		IF (NL-IL) 97,98,99	TERP0160
17.	<mark>ں</mark>	NOT ENOUGH ENTRIES IN TABLES FOR THIS ORDER INTERPOLATION	TERP0170
18.	97	IL=NL	TERP0180
19.	96	L=1	TERP0190
20.		60 TO 112	TERP0200
21.	66	CONTINUE	TERP0210

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all the second

2 IADD=MOD(IL/2) 2 C CHECK IF TABLES IN INCREASING OR DECREASING SEQUENCE 2 C TIT(X1)-X(ML))100.100.101 2 C NUREASING SEQUENCE 2 C NUREASING SEQUENCE 2 C NUREASING SEQUENCE 2 C NUREASING SEQUENCE 2 INO LOW=1L2+1 3 INI=ML-IL2-IADD 3 INIEML-IL2-IADD 3 INIEML-IL1+1 3 INEEL=1 3 INSEL=1 3 INSEL=1 3 INSEL=1 3 LAST=IRO-IL2+1 3 LAST=IEND-IL2+1 3 LAST=IEND-IL2+1 3 LAST=IEND-IL2+1 3 LAST=IEND-IL2+1 3 LAST=IL2+1ADD+1 3 LAST=IEND-IL2+1 3 LAST=IL2+1ADD+1 3 LAST=IL2+1ADD+1 3 LAST=IL2+1ADD+1 3 IND=-0 4 IND=-0 3 IND=-1L2+1	22.		1r2=1r/2	TERP0220
24. C CHECK IF TABLES IN INCREASING OR DECREASING SEQUENCE 25. IF(X(1)-X(ML))100.100.101 26. INCREASING SEQUENCE 27. 100 ILOWEIL2+1 28. IHI=ML-IL2-IADD 29. IUSEL=1 30. IUSEL=1 31. ISEG=ILOW+1 32. IUSEL=1 33. ISEG=ILOW+1 34. IAST=IEND-IL2+1 35. LAST=IEND-IL2+1 36. IAOE=0 37. IAOE=1 38. LAST=IEND-IL2+1 39. IAST=IEND-IL2+1 31. IBEG=ILOW+1 32. LAST=IEND-IL2+1 34. IAOD=0 35. C 36. IAOD=0 37. JOI ILOW=N-IL2 38. IAOE=1 39. IAOE=0 30. IAOE=0 31. IAOE=0 32. LOI ILOW=N-IL2 34. IAOE=0 35. IAOE=0 36. IAOE=0 37.	23.		IADD=MOD(IL,2)	TERP0230
25. IF(X(1)=X(M_1)100.100101 26. C INCREASING SEQUENCE 27. 100 ILOW=IL2+1 28. IHI=ML-IL2-IADD 29. IHI=ML-IL2-IADD 31. IUSEH=NL-IL1+1 32. IUSEH=NL-IL1+1 33. IUSEH=NL-IL2+1 34. IBEG=ILOW+1 35. LAST=IEND-IL2+1 36. IADD=U 37. IADD=U 38. LAST=IEND-IL2+1 39. LAST=IEND-IL2+1 31. IADD=U 32. LAST=IEND-IL2+1 34. IADD=U 35. LAST=IEND-IL2+1 36. IADD=U 37. JOI ILOW=ML-IL2 38. IADD=U 39. IADD=U 30. IADD=U 31. IADD=U 32. JOI ILOW=ML-IL2 34. IADD=U 36. IADD=U 37. JOI ILOW=ML-IL2 38. IADD=U	24.	J	CHECK IF TABLES IN INCREASING OR DECREASING SEQUENCE	TERP0240
2b. C INCREASING SEQUENCE 27. 100 ILOW=IL2+1 28. IHI=NL-IL2-IADD 29. IUSEL=1 30. IUSEL=1 31. IUSEH=NL-IL+1 32. IUSEH=NL-IL+1 34. ISEG=ILON+1 35. LAST=IEND-IL2+1 36. IADD=0 36. IADD=1 37. IADD=0 36. IADD=1 37. IADD=0 36. IADD=1 37. IADD=0 36. IADD=1 37. IADD=0 38. IADD=0 39. IADD=0 30. IADD=1 31. IADD=1 32. IAD=1-IL+1 40. INSEL=NL-IL+1 40. INSEL=NL-IL+1 40. INSEL=NL-IL+1 40. INSEL=NL-IL+1 40. INSEL=NL-IL+1 40. INSEL=NL-IL+1 41. ISE	25.		IF(X(1)=X(NL))100+100+101	TERP0250
27. 100 ILOW=TL2+1 28. IHI=NL=TL2=IADD 28. IUSEL=1 30. IUSEL=1 31. IDEG=LON+1 32. IUSEH=NL-1L+1 32. IUSEH=NL-1L+1 33. ISEC=LON+1 34. IDEG=LON+1 35. C 36. C 37. IADD=U 38. IADD=U 39. IADD=U 30. INT=LLATADD+1 30. INT=LLATADD+1 30. INT=LLATADD+1 40. IUSEL=NL-1L+1 40. IUSEL=NL-1L+1 40. IUSEL=NL-1L+1 40. IUSEL=NL-1L+1 40. IUSEL=NL-1L+1 40. IUSEL=NL-1L+1 41. ISEE=NL-1L+1 42. IUSEL=NL-1L+1 43. IUSEL=NL-1L+1 44. IUSEL=NL-1L+1 45. C 46. IADD=1-IADD 47. IADD=1-IADD 48. IADD=1-IADD 49. </td <th>20.</th> <td>J</td> <td>INCREASING SEQUENCE</td> <td>TERP0260</td>	20.	J	INCREASING SEQUENCE	TERP0260
28. IHI=NL-IL2-IADD 29. IUSEL=1 30. IUSEH=NL-IL+1 31. IBEG=ILO#+1 32. IUSEH=NL-IL+1 33. ISET=END-IL2+1 34. IAOD=U 35. LAST=IEND-IL2+1 36. IAOD=U 36. IAOD=0 36. IAOD=0 36. IAOD=0 36. IAOD=0 37. IAOD=0 38. IHT=IL2+1ADD+1 39. IHT=IL2+1ADD+1 39. IHT=IL2+1ADD+1 39. IUSEL=NL-IL41 40. IUSEL=NL-IL41 40. IUSEL=NL-IL41 40. IUSEL=NL-IL41 41. IBEG=IH1+1 42. IUSEH=1 43. IASEI=NL-IL41 44. IASEI=NL-IL41 45. C 46. IASEI=IL0#1 47. IASEI=IL41 48. IASEI=IL41 49. IASEI=IL41 44. IASEI=IL41 45. C </td <th>27.</th> <td>100</td> <td>ILOW=JL2+1</td> <td>TERP0270</td>	27.	100	ILOW=JL2+1	TERP0270
29. IUSEL=1 30. IUSEH=NL-IL+1 31. IBEG=ILOW+1 32. IEND=IH1-1 33. IEND=IH1-1 33. LAST=IENO-IL2+1 34. IAOD=U 35. Control 36. Go To 102 37. J01 38. IADD=U 37. J01 38. IMI=IL2+IADD+1 39. IUI ILOW=NL-IL2 39. IUI ILOW=NL-IL2 39. IUI ILOW=NL-IL2 30. IUI ILOW=NL-IL2 31. IUI ILOW=NL-IL2 34. IUI ILOW=NL-IL2 35. IUI ILOW=NL-IL2 36. IUI ILOW=NL-IL2 37. IUI ILOW=NL-IL2 38. IHT=IL2+IADD+1 40. IUSEH=1 41. IBEG=IHI+1 42. ISEG=IHI+1 43. IADE=1 44. IADE=1 45. C 46. IADE=1-IADD 45. C 46. IADE=1	28.		IHI=NF-IFS-IFDD	TERP0280
30. IUSEHENL-IL+1 31. IBEG=ILOW+1 32. IEND=IH1-1 33. LAST=IEND-IL2+1 34. IADD=0 35. LAST=IEND-IL2+1 36. C 36. C 37. JO1 38. IADD=0 39. IADD=0 30. C 31. IADD=0 32. JO1 34. IADD=0 35. IO1 36. ILSELENLIL2 37. JO1 38. IH1=IL2+IADD+I 39. IUSELENLIL2 30. IUSELENLIL2 31. IUSELENLILA 41. IUSELENLILA 42. IUSELENLILA 43. IUSELENLILA 44. IADE=1 45. C 46. IADE=1-IADD 45. C 46. IADE=1-IADD 46. IADE=1-IADD 46. IADE=1-IADD	29.		IUSEL=1	TERP0290
31. IB66=ILOW+1 32. IEND=IHI-1 33. LAST=IEND-IL2+1 34. IA00=U 35. G0 T0 102 36. G T0 102 36. J1 ILOW=NL-IL2+1 37. J01 ILOW=NL-IL2 36. IHI=IL2+IADD+1 36. IHI=IL2+IADD+1 36. IUSEL=NL-IL+1 40. IUSEL=NL-IL+1 41. IUSEL=NL-IL+1 42. IUSEL=NL-IL+1 43. IUSEH=1 44. ISEG=IHI+1 45. IEND=ILOW-1 46. IADD=1-IADD 45. C 46. IADD=1-IADD	30.		IVSEH=NL-IL+1	TERP0300
32. IEND=1HI-1 33. LAST=IEND-1L2+1 34. IADD=0 35. C 0 TO 102 36. G0 TO 102 36. C DECREASING SEQUENCE 36. II ILOW=NL-IL2 36. IN1 ILOW=NL-IL2 36. IN1 ILOW=NL-IL2 36. IN1 ILOW=NL-IL2 36. IN15EL=NL-IL+1 39. IUSEL=NL-IL+1 40. IUSEH=1 41. IUSEH=1 42. IUSEH=1 43. IUSEH=1 44. IADE=1LOW-1 45. C 46. IADD=1-IADD 45. C 46. IADD=1-IADD 46. IADC=1-IADD 46. IADC=1-IADD	31.		IBEG=ILOW+1	TERP0310
33. LAST=IEND-TL2+1 34. IADD=U 35. 60 TO 102 36. 60 TO 102 36. C 36. C 36. C 36. LADD=U 36. LOUENL-IL2 37. J01 38. IHT=IL2+IADD+1 39. IHT=IL2+IADD+1 39. IUSEL=NL-IL4 40. IUSEL=NL-IL4 40. IUSEL=NL-IL4 41. IBEG=IH141 42. IUSEL=N-IL4 43. ISEG=IH141 44. IBEG=IH141 45. IADD=ILOW-1 45. C 46. IADD=1-IADD 45. C 46. IOD=1-IADD 45. C 46. IOD=1-IADD 45. C 46. IOD=1-IADD 46. IOD=1-IADD 46. IOZ IFGaRG-X(ILOW))103>104+105	32.		IEND=IHI-1	TERP0320
34. IADD=0 35. 60 T0 102 36. C DECREASING SEQUENCE 37. 101 ILOW=NL-IL2 38. IHI=IL2+IADD+1 39. IHI=IL2+IADD+1 39. IUSEL=NL-IL+1 40. IUSEL=NL-IL+1 41. IUSEH=1 42. IUSEH=1 43. IAD==1LOW-1 44. IADD=1-IADD 45. C 46. IADD=1-IADD 45. C 46. IOZ IFARGE IS SMALLER THAN TABLE VALUES	33.		LAST=IEND-IL2+1	TERP0330
35. 60 To 102 36. C DECREASING SEQUENCE 37. 101 ILOW=NL-IL2 38. IHI=IL2+IADD+1 39. IHI=IL2+IADD+1 39. IUSEL=NL-IL2 40. IUSEL=NL-IL+1 41. IBEG=IH1+1 42. IBEG=IH1+1 43. IEND=ILOW-1 44. IADD=1-IADD 45. C 46. IADD=1-IADD 45. C 46. IADD=1-IADD 45. C 46. IADD=1-IADD 45. C 46. IADD=1-IADD	94.		IADD=0	TERP0340
30. C DECREASING SEQUENCE 37. 101 ILOW=NL=IL2 39. IHI=IL2+IADD+1 39. IUSEL=NL=IL+1 40. IUSEH=1 41. IUSEH=1 42. IBEG=IHI+1 43. IEND=ILOW-1 44. IADE=1-IADD 45. C 46. IADE=1-IADD 46. IADE=1-IADD 46. IADE=1-IADD 46. IADE=1-IADD 46. IADE=1-IADD	35.		60 TO 102	TERP0350
37. 101 ILOW=NL-IL2 36. IHI=IL2+IADD+1 39. IUSEL=NL-IL+1 40. IUSEL=NL-IL+1 41. IUSEH=1 42. IBEG=IHI+1 43. IEND=ILOW-1 44. IEND=ILOW-1 45. C 46. 102 102 IF(ARG-X(ILOW))103,104,105	36.	U	DECREASING SEQUENCE	TERP0360
36. IHI=IL2+IADD+1 39. IUSEL=NL-IL+1 40. IUSEH=1 41. IBEG=IHI+1 42. IBEG=IHI+1 43. IEND=ILOW-1 44. IADD=1-IADD 44. IADD=1-IADD 45. C 46. 102 102 IF(ARG-X(ILOW))103,104,105	37.	101	ILOW=NL-IL2	TERP0370
39. IUSEL=NL-IL+1 40. IUSEH=1 41. IBEG=IHI+1 42. IBEG=ILOW-1 43. LAST=2 44. IADD=1-IADD 45. C CHECKS IF ARG IS SMALLER THAN TABLE VALUES 46. 102 IF(ARG-X(ILOW))103,104,105	36.		IHI=IL2+IADD+1	TERP0380
40.IUSEH=141.IBEG=IHI+142.IEND=ILOW-142.IEND=ILOW-143.LAST=244.IADD=1-IADD45.C46.IO2 IF(ARG-X(ILOW))103,104,105	- 6£	1	Insel=nL-IL+1	TERP0390
41.IBEG=IHI+142.IEND=ILOW-143.LAST=244.IADD=1-IADD45.CCCHECKS IF ARG IS SMALLER THAN TABLE VALUES46.102 IF(ARG-X(ILOW))103,104,105	40.		ICREHE1	TERP0400
42. IEND=ILOW-1 43. LAST=2 44. IADD=1-IADD 45. C CHECKS IF ARG IS SMALLER THAN TABLE VALUES 46. 102 IF(ARG-X(ILOW))103/104/105	•1•		IBE6=IHI+1	TERPO410
43. LAST=2 44. IADD=1-IADD 45. C CHECKS IF ARG IS SMALLER THAN TABLE VALUES 46. 102 IF(ARG-X(ILOW))103/104/105	42°		IEND=ILOW-1	TERP0420
<pre>44. IADD=1-IADD 45. C CHECKS IF ARG IS SMALLER THAN TABLE VALUES 46. 102 IF(ARG-X(ILOW))103,104,105</pre>	ù3.		LAST=2	TERP0430
45. C CHECKS IF ARG IS SMALLER THAN TABLE VALUES 46. 102 IF(ARG-X(ILOW))103/104/105	• • • •		IADD=1-IADD	TERP0440
46. 102 IF(ARG-X(ILOW))103,104,105	45.	່ ບ	CHECKS IF ARG IS SMALLER THAN TABLE VALUES	TERP0450
	46.	102	IF(ARG-X(ILOW))103,104,105	TERP0460

47.	U	SMALLER THAN SMALLEST TABLE VALUE	TERP0470
43.	103	L=IUSEL	TERP0480
•64		60 TO 112	TERP0490
50.	104	TĔRP=Y(ILOW)	TER-0500
51.		60 T0 117	TERP0510
52.	U	CHECKS IF ARG IS GREATER THAN TABLE VALUES	TERP0520
53.	105	IF(X(IHI)-ARG)106+107+108	TER-0530
54.	U	ARG GREATER THAN TABLE VALUE	TERP0540
55.	106	L=IUSEH	TERP0550
56.		60 T0 112	TERP0560
57.	107	TERP=Y(IHI)	TERP0570
54.		60 T0 117	TERP0580
59°	J	SEARCHES X ARRAY TO BRACKET ARG	TER P0590
•09	106	DO 109 NEIBEG/IEND	TERP0600
61.		IF(IUSEL-1)1080,1080,1081	TERP0610
62•	1060	N=W	TER P0620
63.		60 TO 1082	TERP0630
64.	1081	T+N-TN=W	TERP0640
65 .	1082	IF(X(M)-ARG)109+110+111	TERP0650
66.	109	CONTINUE	TERP0660
67 .		L=LAST	TERP0670
68.		60 TO 112	TERP0580
•69	U	EQUALS ARGUMENT, RETURN OK	TE RP0690
70.	110	TERP=Y (M)	TERP0700
.17	-	Ġ0 T0 117	TERP0710

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TERP0720	TERP0730	TERP0740	TERP0750	TER-0760	TERP0770	TER-0780	TERP0790	TERP0800	TERP0810	TERP0820	TERP0830	TERP0840	TERP0850	TERP0860	TERP0870	TERP0880	TERP0890	TERP0900	TERP0910	
					-															
									5											
	IADD		ATION SECTION		=1,1L				P=1 • IL	113,114,113	7	((dNI)X-	((dNI)X-(NI)		λ4/ (N1) /≠d					
EUREKA	L=M-IL2+;	CONTINUE	INTERPOL	SUM=0.0	D0 115 I	0.1=q	PK=1.0	1-1+1=NI	D0 114 II	IF(I-41)]	INP=L+IP.	P=P*(ARG	Х) +Хd=Хd	CONTINUE	I+WOS=WOS	CONTINUE	TERP=SUM	RETURN	END .	
U	111	112	U			,					113			114		115		117		
72.	73.	74.	75.	76.	.77	78.	79.	60.	61.	82.	83.	84•	85.	86.	67.	88.	8 9.	• 06	•16	

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10. OTHER COMPLEMENTARY ACTIVITIES

To promote a vigorous exchange of information on electron scattering between the theoretical and experimental communities, a city-wide series of colloquia was initiated with the support of Gulf General Atomic. The series has been known as CAMP (Colloquia on Atomic and Molecular Processes). During the contract period, the following CAMP colloquia have been of interest to this program:

March 8, 1967	"Energetic Ions from Diatomic Molecules, " Dr. Lee J. Keiffer, Joint Institute for Lab Astrophysics, University of Colorado, Boulder, Colorado
March 14, 1967	"Theory of Near Adiabatic Collisional Transitions," Professor K. M. Watson, University of California, Berkeley, Physics Department
March 31, 1967	"Atomic Scattering Spectroscopy: Analysis of Scattering of He ⁺ by Ne and Ar, "Dr. Felix T. Smith, Stanford Research Institute, Menlo Park, California
April 28, 1967	"Total Elastic and Inelastic Heavy Particle Collisions in the Energy Range 10 to 1000 eV. A: Elastic Scattering in the Alkali-Rare Gas System; B: Ionization Due to Rare Gas Metastable Collisions, " Dr. Manfred Hollstein, Stanford Research Institute, Menlo Park, California
May 4, 1967	"The Importance of Polarization in Low Energy Electron Molecular Collisions - An Application to H ₂ ," Dr. Neil F. Lane, Department of Physics, Rice University, Houston, Texas
October 16, 1967	"The Excitation and Spectroscopy of H-like Atoms," Dr. Hans Kleinpoppen, Joint Institute for Lab- oratory Astrophysics, University of Colorado, Boulder, Colorado
November 3, 1967	"Low Energy Rotational Excitation Cross Sections Derived from Spectroscopic Data," Dr. Marvin Mittleman, Space Science Laboratory, University

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of California, Berkeley, California

December 11, 1967	"Proton H-Atom Collisions," Professor M. R. C. McDowell, Goddard Space Flight Center, Greenbelt, Maryland
April 4, 1968	"Ionization Processes of Molecules at Low Energies, " Professor R. Stephen Berry, Department of Chemistry, University of Chicago, Chicago, Illinois
May 17, 1968	"Polarization of Scattered Electrons," Professor E. Reichart, Department of Physics, University of Mainz, Mainz, Germany

Probably the most significant activity this year was the Working Session on Electron H-Atom Collisions. The text of the notice and the program for the meeting are presented below.

(- 19 M)

WORKING SESSION ON ELECTRON H-ATOM COLLISIONS

The detailed experimental and theoretical study of electron hydrogen atom collisions has developed to the point where our group at Gulf General Atomic, in conjunction with the group at the University of California, San Diego, plan to spend two days in a "working session" in order to examine what has been done, what is being done, and what can be done to most effectively study (e-H) collisions. The days we have in mind are Monday and Tuesday, April 8 and 9.

In particular, we plan to examine resonance and threshold problems since these areas have received the most extensive study of late. We have invited R. Damburg and A. Temkin to help organize discussion during our first day and to give colloquia on topics of particular interest. We plan to have several other talks by J. C. Y. Chen and ourselves, but for the most part our program will be informal and will stress the broadest possible exchange of ideas. We hope to spend one day together in an informal meeting while the second day (or part of the day) we are setting aside for the exchange of thoughts on a more individual basis. This will occur both here and at the University.

For those who would like to join us, arrangements will be made at a local hotel. We plan to get together for dinner Monday evening. Since time is already short, from those who will join us, we would appreciate word as soon as possible.

> J. William McGowan James F. Williams GULF GENERAL ATOMIC

WORKSHOP ON ELECTRON HYDROGEN-ATOM COLLISIONS

	Monday, April 8, 1968	
AM SESSION:	La Salle Room, La Jolla Beach & Tennis (llub
9:00 - 9:30	Business and Coffee	
9:30 - 12:30	Elastic and Inelastic Electron Scatterin	<u>ng</u>
	Chairman: Edward Gerjuoy	
	Review Experimental Measurements	J. William McGowan Atomic Physics Lab Gulf General Atomic
	Excitation of the Hydrogen Atom by Electron Impact	R. Damburg Latvian Academy of Science
	Solutions of the Faddeev Equation for the (e-H) System	J. C. Y. Chen University of California San Diego
Lunch 12:30 - 1:45	Scripps Institute of Oceanography Cafeteria After lunch, a visit to Scripps Physiological Research Lab	
PM SESSION: 2:00 - 5:00	IGPP Building, University of California, San Diego Ionization Threshold Studies	,
	Chairman; Kenneth M. Watson	
	Black Box Aspects of the Threshold Law for Ionization	G. H. Wannier University of Oregon
3:30	Coffee Break	
	An Approach to the Electron Atom Ionization Threshold Behavior	A. Temkin NASA-Goddard Space Flight Center
Evening:	La Valencia Hotel	

Cocktail hour at 7:00 Dinner at 8:00

WORKSHOP ON ELECTRON HYDROGEN-ATOM COLLISIONS

Tuesday, April 9, 1968

AM SESSION: 9:00 - 12:00

Joint Experimental and Theoretical Workshop

La Salle Room, La Jolla Beach & Tennis Club

Chairman: Marvin Mittleman

Possible Topics:

Polarization of Radiation

Polarized Electron and Atom Beams

Coincidence Experiments

Angular Correlation Experiments

The Application of Born Approximation

Lorentz Decay

San Diego

Removal of Degeneracy

Definition of Threshold

Special Working Sessions

Cascade of Radiation

Potential Resonances

12:00

A STATISTICS AND A STATISTICS

PM SESSION:

2:00

Visits to Gulf General Atomic and the University of California, San Diego

Lunch at La Jolla Beach & Tennis Club Dining Room

IGPP Building, University of California,

NOTE :

At 11:00 a.m. at Gulf General Atomic Professor Gregory H. Wannier will be speaking on "Stark Ladders in Solids?"

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APPENDIX I

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ABSTRACTS OF PAPERS GIVEN AT SCIENTIFIC MEETINGS

LYMAN-ALPHA PRODUCTION AND POLARIZATION IN He⁺ COLLISIONS WITH H AND H₂^{*}

Robin A. Young, R. F. Stebbings,[†] and J. Wm. McGowan

Presented at 20th Annual Gaseous Electronics Conference of the American Physical Society, San Francisco, October 1967.

Measurements of the Lyman-alpha production from $He^+ + H(1s) + He^+ + H(2p)$ collisions have been obtained over the energy range from 0.5 to 30 keV. At the lower ion energies the cross section remains large; this fact reflects the rotational interaction between states of the collision complex HeH⁺. A similar result had been reported by Stebbings <u>et al.</u> (1) for the H⁺-H collision system. Also presented are measurements of the total cross section for Lyman-alpha production from He⁺-H₂ collisions. Some values of the polarization have been obtained for emission of Lyman-alpha from the collisions of He⁺, Ne⁺, and Ar⁺ with atomic hydrogen.

Work supported by the National Aeronautics and Space Administration, Goddard Space Flight Center, Contract NAS 5-11025.

[†]On leave from University College London, London, England.

1. R. F. Stebbings, R. A. Young, C. L. Oxley, and H. Ehrhardt, Phys. Rev. 138, A1312 (1965).

I-1

THRESHOLD BEHAVIOR OF ELECTRON EXCITATION FUNCTIONS IN ATOMIC HYDROGEN*

J. F. Williams, E. K. Curley, and J. Wm. McGowan

Presented at 20th Annual Gaseous Electronics Conference of the American Physical Society, San Francisco, October 1967.

The excitation function, for electron impact, of the (1s - 2p) transition in atomic hydrogen appears to be finite at the threshold. When electron energy distribution functions of from 240 to 100 meV (FWHM) are unfolded from the observed Lyman-alpha radiation versus electron energy curve, it appears that the excitation function reaches a significant value within several tens of meV of the threshold and then drops sharply to about 60% of its peak threshold value. A report is given of attempts made to observe the resonance in the 2p excitation function, which is predicted by Burke et al. (1) to appear just below the n = 3 level.

*Work supported by the National Aeronautics and Space Administration, Goddard Space Flight Center, Contract NAS-5-11025.

^{1.} P. G. Burke, S. Ormonde, and W. Whitaker, Phys. Rev. Letters 17, 800 (1966).

(e-H) COMPOUND STATES REFLECTED IN THE H(2p) CHANNEL IN THE VICINITY OF $n = 3^*$

J. William McGowan and James F. Williams

Presented at American Physical Society Meeting, Los Alamos Scientific Laboratory, June 1968.

High resolution electron impact studies of the 2p excitation cross section of atomic hydrogen have been made in the vicinity of n = 3. Prominent resonance structure has been observed below and above n = 3. The structure below n = 3 qualitatively is in agreement with the predictions of Burke <u>et al.</u>, (1) but in detail there is some difference as to the breadth of the (e-H) resonances. Above n = 3 there is evidence that a shape resonance is present. *Work supported by the National Aeronautics and Space Administration, Goddard Space Flight Center, Contract NAS-5-11025.

¹P. G. Burke, S. Ormonde, and W. Whitaker, <u>Proc. Phys. Soc.</u> 92, 319 (1967).

COMPARISON OF THE CALCULATED AND OBSERVED RESONANCES

IN THE (e-H) ELASTIC SCATTERING CHANNEL

ABOVE 10.0 eV^*

J. William McGowan and S. Ormonde[†]

Submitted to the Arnold Sommerfeld Centennial Memorial Meeting and International Symposium on the Physics of One and Two Electron Atoms, Munich, September 1968.

Recent measurements of the electron hydrogen atom elastic scattering cross section show a rather wide structure immediately below the n = 2 threshold. (1) This structure has been attributed to the ¹D and ³S compound states of H⁻, which have already been partially discussed in the literature. (2-4) Since the observed effect of these states on the differential cross section appears to be considerably larger than expected from what we know of the resonances in the ¹S series, it was decided to compare the experiment with the results of a detailed close-coupling calculation of the resonances just below the n = 2 threshold. Preliminary results for the ¹D resonance place it at an energy of 10. 15 eV with width Γ = 0.0073 eV. When the energy distribution of the electron beam is folded into the calculated cross section, the agreement between theory and experiment is reasonably good. The effects of including higher hydrogenic states as well as taking into account the considerations of Damberg and Geltman⁽⁵⁾ are presently being examined.

*Work supported by DASA and the Air Force Special Weapons Center, Contract AF29601-68-C-0052, and by the National Aeronautics and Space Administration, Contract NAS 5-11025.

[†]Quantum Systems, Incorporated, Albuquerque, New Mexico.

- 1. J. William McGowan, E. M. Clarke, and E. K. Curley, <u>Phys.</u> <u>Rev. Letters 15</u>, 917 (1965); <u>17</u>, 66E (1966).
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A DETAILED COMPARISON OF THE THEORETICAL AND EXPERIMENTAL RESULTS FOR THE 2p ELECTRON-IMPACT EXCITATION CROSS SECTION OF HYDROGEN^{*}

J. William McGowan and J. F. Williams

Submitted to the Arnold Sommerfeld Centennial Memorial Meeting and International Symposium on the Physics of One and Two Electron Atom, Munich, September 1968.

At first glance one is satisfied with the agreement between theory and experiment in the threshold region of the 2p electron-impact excitation cross section of atomic hydrogen. However, when a detailed comparison is made in the region between the onset of the n = 2 level and the n = 4 level, one finds that there is much yet to be done with the theory. The measured value for the total cross section lies below the best theoretical value. For example, if we consider the interval between 0.2 and 1.5 eV above threshold, the measured cross section is only 80% of the value estimated by the correlation method. (1) Similar agreement between theory and experiment for 2s excitation was recently reported by Fite et al.(2) The shape resonance predicted in the ¹P channel just above threshold and the finite threshold of excitation are approximately the magnitude suggested by the theory. However, following the first shape resonance are at least two other small structures which appear to be real and which may be part of a series of such shape resonances. Unfortunately, the calculations that have been performed thus far have not been done on a fine enough grid to identify in which channel these other resonances lie.

As predicted by the six-state approximation, $^{(3)}$ there are a number of resonances just below the onset of the n = 3 level. However, there is not good agreement between the theoretically predicted and the measured resonances. Provided the positions that have been predicted are correct, one is lead to the conclusion that the dominant resonance structure is in the ¹P channel while less prominent structure appears in the ¹S channel. The theory, however, predicts that the principle resonance will be in the ¹D channel.

In our experimental results one of the most prominent features appears at the threshold of n = 3. This no doubt reflects a large shape resonance at the threshold of the n = 3 level. Part of the flux from this resonance will appear directly in the 2p channel while another portion of it will arrive

^{*}Work supported by the National Aeronautics and Space Administration, Contract NAS 5-11025, and by Gulf General Atomic Incorporated private research funds.

there through cascade from the 3s and 3d states of the atom. Although detailed measurements of the resonance structure between n = 3 and n = 4 have not been completed, it is clear from our crude measurements that some measurable resonance structure does exist in this interval. One would hope that the calculations similar to those of Damburg and Geltman⁽⁴⁾ will eventually be able to correct for the incompleteness in the original close-coupling approximation calculations.

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- 2. W. L. Fite, W. E. Kauppila, and W. R. Ott, <u>Phys. Rev. Letters</u> <u>20</u>, 409 (1968).
- 3. P. G. Burke, S. Ormonde, and W. Whitaker, <u>Proc. Phys. Soc.</u> 92, 319 (1967).
- 4. R. J. Damburg and S. Geltman, Phys. Rev. Letters 20, 485 (1968).

APPENDIX II

PAPERS RESULTING THIS YEAR FROM

THE PROGRAM

THE PHYSICAL REVIEW

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Faddeev Equations for Atomic Problems and Solutions for the (e,H) System*

James S. Ball[†] Department of Physics, University of California, Los Angeles, California

and

Joseph C. Y. Chen Department of Physics and Institute for Pure and Applied Physical Sciences, University of California, San Diego, La Jolla, California

and

David Y. Wong Department of Physics, University of California, San Diego, La Jolta, California (Received 1 April 1968)

Solutions of the Faddeev equations for Coulomb potentials are investigated. A method which is of practical use for solving the Faddeev equations below the three-particle breakup threshold is developed. As an example, the method is applied to the (e, H) system in which the H^- bound state and the lowest members of the resonances in both the singlet and the triplet J = 0 series are calculated. The results are in good agreement with the experimental measurements and previous calculations which used conventional methods.

I. INTRODUCTION

The nonrelativistic three-body problem with twobody interactions has been formulated by Faddeev^{1,2} in a way that allows straightforward computations. For short-range forces, the Faddeev equations have been applied successfully to a number of problems.³⁻¹³ It is the purpose of this paper to show that the Faddeev equations are equally applicable to atomic problems as long as the total energy is below the three-body breakup threshold – for example, the calculation of three-body bound states and resonance energies and wave functions below the ionization energy. The significant advantage of the Faddeev equation over conventional methods is that the wave functions are calculated systematically along with the energy levels. No trial wave function is needed in the computation. Although this paper only contains a few illustrative examples all dealing with the e-H problem, we believe that the Faddeev equation has a considerably wider range of applicability. A brief account of this work was presented recently at the Leningrad Conference.¹⁴

In Sec. II, we give a simple derivation of the Faddeev equation, and review the method of reduction with respect to angular momentum. The method of solution is presented in Sec. III and applied to the H⁻ problem in Sec. IV. A discussion of possible extensions is given in Sec. V.

II. THE FADDEEV EQUATIONS

A. Formal Derivation

The scattering matrix T(s) for the three-particle system with two-body interactions is a solution of the equation

$T(s) = V + VG_0(s)T(s),$	(2.1)
with $V = \sum_{i} V_{i} (V_{i} = V_{jk})$,	(2.2)
$G_0(s) = (s - H_0)^{-1},$	 (2.3)

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where the three particles are labeled by i, j, and k, and $G_0(s)$ is the free three-particle Green's function. The "off-shell" scattering matrix $T_i(s)$ arising from the two-body potential V_i above is given by the Lippmann-Schwinger equation

$$T_{i}(s) = V_{i} + V_{i}G_{0}(s)T_{i}(s).$$
(2.4)

Since V_i acts only on two particles, the third particle is therefore left as a spectator in Eq. (2.4). Equation (2.4), in effect, is equivalent to the equation for two-particle scattering matrix; the presence of the spectator particle gives rise to merely a shift in the energy scale.

Now we decompose the three-particle scattering matrix T(s) into three components

$$T(s) = T^{(1)}(s) + T^{(2)}(s) + T^{(3)}(s), \qquad (2,5)$$

where $T^{(i)}(s) = V_i + V_i G_0(s) T(s)$. (2.6)

As it stands, Eq. (2.6) is a set of integral equations with each $T^{(i)}$ coupled to all three operators T(j), j = 1, 2, and 3. The main difference between these equations and the Faddeev equations is that, in the latter, each $T^{(i)}$ is only coupled to two T(j)'s with $j \neq i$, and as a result, the kernel of the integral equation is less singular. We give here a simple derivation of the Faddeev equations:

Define the expression

$$\Omega = T^{(i)}(s) - T_{i}(s) - \sum_{j \neq i} T_{i}(s)G_{0}(s)T^{(j)}(s).$$
(2.7)

One can readily show by utilizing Eqs. (2, 4)-(2, 6) that

$$\Omega = V_i + \sum_{j=1}^{3} V_i G_0 T^{(j)} - V_i - V_i G_0 T_i - \sum_{j \neq i}^{3} V_j G_0 T^{(j)} - \sum_{j \neq i}^{3} V_j G_0 T_i G_0 T^{(j)} = V_i G_0 \Omega.$$
(2.8)

Since $V_i G_0(s)$ is not the identity operator, Eq. (2.8) implies that $\Omega = 0$ for each *i*. We then obtain for $T^{(i)}(s)$ the equations

$$T^{(i)}(s) = T_i(s) + \sum_{j \neq i} T_i(s)G_0(s)T^{(j)}(s), \quad i = 1, 2, 3, \qquad (2.9)$$

which are the well-known Faddeev equations.¹ In the matrix form:

$$\begin{pmatrix} T^{(1)}(s) \\ T^{(2)}(s) \\ T^{(3)}(s) \end{pmatrix} = \begin{pmatrix} T_1(s) \\ T_2(s) \\ T_3(s) \end{pmatrix} + \begin{pmatrix} 0 & T_1(s) & T_1(s) \\ T_2(s) & 0 & T_2(s) \\ T_3(s) & T_3(s) & 0 \end{pmatrix} G_0(s) \begin{pmatrix} T^{(1)}(s) \\ T^{(2)}(s) \\ T^{(3)}(s) \end{pmatrix}.$$

$$(2.10)$$

This is a coupled set of integral equations in five variables. Since no approximation is made on this formal transformation, the solution of Eq. (2.10) yields $T^{(1)}$, $T^{(2)}$, and $T^{(3)}$ whose sum is the exact solution of the original equation (2.1).

The Faddeev equations can also be interpreted diagrammatically. Let us represent T_1 by the sum of the diagrams as shown in Fig. 1 and similarly for T_2 and T_3 . For the T's with a superscript, we use the symbols shown in Fig. 2. The Faddeev equations are then given by Fig. 3. One can easily see that the iterative solution of the three equations in Fig. 3 using the equation in Fig. 1 reproduces all the diagrams in perturbation theory. Our formal derivation given earlier simply shows that the Eqs. in Fig. 3 are valid even if the perturbation series fails to converge. In the diagrammatic representation, it is physically evident that $T^{(1)}$ is that part of the full three-body T matrix where particles 2 and 3 undergo a final-state interaction. Since T_i already represent a complete sequence of two-body interactions, each $T^{(i)}$ can only couple to T(j), $j \neq i$. As mentioned earlier, this decoupling of $T^{(i)}$ from itself results in a less singular kernel as compared to the original equation (2.6). This is due to the fact that each T_i is associated with a δ function corresponding to the momentum conservation of the *i*th particle, and the decoupling removes the repeated δ functions.

B. Three-Body Kinematics

To reduce the Faddeev equations, a suitable set of basis variables must first be chosen. For this purpose, the momentum representation is adopted. Let the masses and asymptotic monienta of the three particles be denoted by m_1 , m_2 , and m_3 , and \tilde{k}_1 , \tilde{k}_2 , and \tilde{k}_3 , respectively. An appropriate set of basis variables may be constructed by taking certain combinations of the momenta in the center-of-mass system of the three particles. For $T^{(1)}$, the suitable basis variables are the pair of independent momentum

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$$T_1 = \frac{2}{3} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2}$$

FIG. 1 Diagrams for the two-body scattering matrix T_i . The wavy lines represent the two-particle potential V_i .

$$\mathsf{T}^{(1)} := \underbrace{\mathsf{T}}_{\mathsf{(3)}} := \underbrace{\mathsf{T}}_{\mathsf$$

FIG. 2 Symbols representing the three-body scattering matrix $T^{(\ell)}$ with a pair of particles undergoes a final-state interaction.

FIG. 3 Diagrammatical representation of the Faddeev equations. The gap between two diagrams represents a a noninteracting three-body Green's function.

variables.³

with

$$\vec{p}_1 = [m_3 \vec{k}_2 - m_2 \vec{k}_3] / [2m_2 m_3 (m_2 + m_3)]^{1/2}, \quad \vec{q}_1 = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_2 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_3 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_1 + m_2 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_3 + m_3)]^{1/2}, \quad (2.11)^{1/2} = [m_1 (\vec{k}_2 + \vec{k}_3) - (m_1 + m_3 + m_3) \vec{k}_1] / [2m_1 (m_2 + m_3) (m_1 + m_3 + m_3)]^{1/2}$$

and their conjugated pairs $\vec{p}_2\vec{q}_2$ and $\vec{p}_3\vec{q}_3$, which are obtained by a cyclic interchange of subscripts in Eqs. (2, 11) are the appropriate sets for $T^{(2)}$ and $T^{(3)}$ respectively.

The nonrelativistic kinetic energy in the center-of-mass frame may be written in any pair of basis variables;

$$H_0 = p_1^2 + q_1^2 = p_2^2 + q_2^2 = p_3^2 + q_3^2.$$
(2.12)

Consequently, the corresponding state vector $|\hat{k}_1\hat{k}_2\hat{k}_2\rangle$ may be represented in several equivalent forms

$$|\vec{\mathbf{k}}_1 \vec{\mathbf{k}}_2 \vec{\mathbf{k}}_3\rangle = |\vec{\mathbf{p}}_1 \vec{\mathbf{q}}_1\rangle_1 = |\vec{\mathbf{p}}_2 \vec{\mathbf{q}}_2\rangle_2 = |\mathbf{p}_3 \mathbf{q}_3\rangle_3 , \qquad (2, 13)$$

where the extra subscript keeps track of the proper pair of basis variables.

These sets of basis momentum variables are linearly dependent on each other. The relations are summarized below.

$$\vec{p}_{1} = v_{12}\vec{p}_{2} - \beta_{12}\vec{q}_{2} = -\alpha_{13}\vec{p}_{3} + \beta_{13}\vec{q}_{3}, \quad \vec{q}_{1} = \beta_{12}\vec{p}_{3} - \alpha_{12}\vec{q}_{2} = -\beta_{13}\vec{p}_{3} - \alpha_{13}\vec{q}_{3}, \quad (2, 14a)$$

$$\vec{p}_{2} = -\alpha_{21}\vec{p}_{1} + \beta_{21}\vec{q}_{1} = -\alpha_{23}\vec{p}_{3} - \beta_{23}\vec{q}_{3}, \quad \vec{q}_{2} = -\beta_{21}\vec{p}_{1} - \alpha_{21}\vec{q}_{1} = \beta_{23}\vec{p}_{3} - \alpha_{23}\vec{q}_{3}, \quad (2.14b)$$

$$\vec{p}_{3} = -\alpha_{32}\vec{p}_{2} + \beta_{32}\vec{q}_{2} = -\alpha_{31}\vec{p}_{1} - \beta_{31}\vec{q}_{1}, \quad \vec{q}_{3} = -\beta_{32}\vec{p}_{2} - \alpha_{32}\vec{q}_{2} = \beta_{31}\vec{p}_{1} - \alpha_{31}\vec{q}_{1}, \quad (2.14c)$$

where
$$\alpha_{ij} = [m_i m_j / (m_i + m_k)(m_j + m_k)]^{1/2}, \ \beta_{ij} = (1 - \alpha_{ij}^2)^{1/2}$$
 (2.15)

We will frequently interchange these basis momentum variables among different sets for convenience.

C. Separation of Angular Momentum

A separation of the angular momentum states in the Faddeev equations can be carried out using the relative angular momentum of two particles, which is combined with the angular momentum of the third particle in the over-all center-of-mass system.^{9,15} In this decoupling scheme, the state vector $[\tilde{p}_{f}, \tilde{q}_{i} \rangle_{i}$ may be expanded in terms of a set of orthonormal partial-wave states $|p_{i} lm_{l}, q_{i} Lm_{L} \rangle_{i}$. Since the total angular momentum J is conserved, we may in general consider the states to be diagonal in J. These states are given by

$$|pqJMlL\rangle_{i} = (-)^{L-l-M} (2J+1)^{\frac{1}{2}} \sum_{m_{l}m_{L}} \begin{pmatrix} J & l & L \\ -M & m_{l} & m_{L} \end{pmatrix} |plm_{l}, qLm_{L}\rangle_{i}, \qquad (2.16)$$

$$|plm_l, qLm_L\rangle_i = Y_{lm_l}(\hat{p})Y_{Lm_L}(\hat{q})|\hat{p}, \hat{Q}_i, \qquad (2.17)$$

$$i^{(plm_l, qLm_L|p'l'm_{l'}, q'L'm_{L'})}_{i} = (pq)^{-2} \delta(p - p') \delta(q - q') \delta_{ll'} \delta_{LL'} \delta_{m_l m_{l'}} \delta_{m_L m_{L'}}, \qquad (2.18)$$

where the Wigner 3j symbol is adopted for the Clebsch-Gordan coefficients.

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The Faddeev equations [Eqs. (2,9)] may be written in this representation as

$$\Psi_{\alpha}^{(i)}(p_{j},q_{j},s) = \Phi_{\alpha}^{(i)}(p_{j},q_{,s}) + \frac{1}{4}\sum_{\alpha_{j}}\sum_{j\neq i}\int_{0}^{\infty}dp_{j}^{2}\int_{0}^{\infty}dq_{j}^{2}\mathcal{K}_{j}^{(i)}(pq\alpha|p_{j}q_{j}\alpha_{j})[p_{j}q_{j}/(p_{j}^{2}+q_{j}^{2}-s)] \times \Psi_{\alpha_{j}}^{(j)}(p_{j},q_{j},s), \qquad (2.19)$$

with
$$\Psi_{\alpha}^{(i)}(p,q,s) = \frac{1}{i} \langle pq\alpha | T^{(i)}(s) | \vec{k}_1 \vec{k}_2 \vec{k}_s \rangle, \qquad (2.20)$$

$$\Phi_{\alpha}^{(i)}(p,q,s) = {}_{i}\langle pq\alpha | T_{i}(s) | \vec{k}_{i}\vec{k}_{2}\vec{k}_{3} \rangle, \qquad (2.21)$$

$$\mathcal{K}_{j}^{(i)}(pq\alpha|p_{j}q_{j}\alpha_{j}) \equiv \langle pq\alpha|T_{i}(s)|p_{j}q_{j}\alpha_{j}\rangle_{j}, \qquad (2.22)$$

where for convenience the discrete quantum numbers (JMLL) are collectively denoted by α . The physical interpretation of the equations is straightforward. The quantity $\Psi_{\alpha i}^{(i)}(b_i q_i s)$ represents the contribution to the three-particle scattering amplitude in which particles j and $k(j \neq k \neq i)$ undergo final-state interaction with relative angular momentum l_i . The quantity $\Phi_{\alpha i}^{(i)}(b_i q_i s)$ represents the scattering amplitude in which particle i acts as a spectator. The initial state which is denoted by $|\vec{k}_1 \vec{k}_2 \vec{k}_3\rangle$ is arbitrary. The quantity p is proportional to the magnitude of the relative momentum between particles j and k, and the quantity q is proportional to the magnitude of the momentum of particle i in the three-particle center-of-mass frame.

Utilizing Eqs. (2.16)-(2.18), we obtain for the kernel $\mathfrak{X}_{i}^{(i)}$ [defined in Eq. (2.22)] the expression

$$\sum_{j}^{(i)} (pq\alpha|p_{j}q_{j}\alpha_{j}) = (-)^{L+L'-l-l'} \sum_{\substack{m_{l}m_{L} \\ -M m_{l}m_{L} \\ m_{l}m_{L}}} \begin{pmatrix} J \ l \ L \\ -M \ m_{l} \ m_{L} \end{pmatrix} \begin{pmatrix} J \ l' \ L' \\ -M \ m_{l} \ m_{L} \end{pmatrix} \\ \times \int d\hat{p}_{j} d\hat{q}_{j} d\hat{p}_{i} d\hat{q}_{i} \ d\hat{q}_{i} \ i \langle \vec{p} \vec{q} | T_{i}(s) | \vec{p}_{j} \vec{q}_{j} \rangle_{j} (2J+1) Y_{lm_{l}}^{*} \langle \hat{p}_{i} \rangle Y_{L}^{*} \\ \times Y_{L'm_{L'}}(\hat{q}_{i}) Y_{l'm_{l}}(\hat{p}_{j})$$

$$(2.23)$$

Since T_i involves only two-body potential V_i [see Eq. (2.4)], the matrix element $i\langle p q | T_i(s) | p_j q_j \rangle_j$ in Eq. (2.23) may be reduced to a two-particle matrix element. According to Eqs. (2.3), (2.12), and (2.13), we have

$$_{i}\langle \vec{p}\vec{q} | T_{i}(s) | \vec{p}_{j}\vec{q}_{j}\rangle_{j} = _{i}\langle \vec{p}\vec{q} | T_{i}(s) | p_{i}q_{i}\rangle_{i} = \delta(\vec{q} - \vec{q}_{i})\langle \vec{p} | \vec{T}_{i}(s - q^{2}) | \vec{p}_{i}\rangle, \qquad (2.24)$$

with
$$\delta(\vec{q} - \vec{q}_i) = 2q^{-1}\delta(q^2 - q_i^2)\delta(\cos\theta\vec{q} - \cos\theta\vec{q}_i)\delta(\varphi_{\vec{q}} - \varphi_{\vec{q}_i}),$$
 (2.25)

where \tilde{T}_i is the two-particle scattering matrix in the Hilbert space of the two-particle states. We may make use of the decomposition

$$\langle \vec{p} | \vec{T}_{i}(s-q^{2}) | \vec{p}_{i} \rangle = -\frac{1}{2\pi^{2}} \sum_{l=0}^{\infty} (2l+1) P_{i}(\cos\theta_{\vec{p}\vec{p}_{i}}) t_{l}^{(i)}(p,p_{i};s-q^{2}), \qquad (2.26)$$

where the scattering amplitude between particles j and k with angular momentum l is normalized according to the equation

$$t_{l}^{(i)}(p,p;p^{*}) = e^{i\delta_{l}}(\sin\delta_{l})/p.$$
(2.27)

Here p^2 is the two-body center-of-mass energy.

When Eqs. (2.24)-(2.26) are utilized, the kernel in the Faddeev equations may be written as

$$\mathfrak{x}_{j}^{(i)}(pq\alpha|p_{j}q_{j}\alpha_{j}) = \int_{-1}^{1} d\cos\theta_{\overline{q}}\overline{p}_{j}A_{\alpha\alpha_{j}}^{(\theta}\overline{p}_{i}\overline{p}_{j}, \theta_{\overline{q}_{j}}\overline{p}_{j}, \theta_{\overline{q}_{j}}\overline{p}_{j})\delta(q^{a}-q_{i}^{2})t_{l}^{(i)}(p,p_{i};s-q^{a})$$

$$(2.28)$$

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with
$$A_{\alpha\alpha'}(\theta_{\bar{q}_{j}}, \bar{p}_{j}) = \frac{(-)^{L+L'-l-l'+1}}{q} 16\pi^{\frac{1}{2}}(2l'+1)^{\frac{1}{2}}\delta_{JJ}, \delta_{MM'}\sum_{\bar{m}_{l},\bar{m}_{L},\bar{m}_{L}} \binom{l \ L \ J}{m_{l} \ m_{L} - m_{L'}} \binom{l' \ L' \ J'}{0 \ \bar{m}_{L}, -\bar{m}_{L'}} \times Y_{l\bar{m}_{l}}^{*}(\theta_{\bar{q}_{j}}, \bar{p}_{j}, 0)Y_{L\bar{m}_{L}}^{*}(\theta_{\bar{q}_{j}}, \bar{p}_{j}, 0)Y_{L'\bar{m}_{L'}}^{*}(\theta_{\bar{q}_{j}}, \bar{p}_{j}, 0), \qquad (2.29)$$

where $\theta_{\vec{q}_j\vec{p}_j}$, for example, is the angle between momentum variables \vec{q}_j and \vec{p}_j . It should be noted that these angles are related through the relations between different sets of pair momentum variables [see Eqs. (2.14)].

The above result was derived for any angular momentum state J of the three-particle system. For convenience, we will consider explicitly only states corresponding to zero total angular momentum. For this J = 0 case, $\alpha = (0011) \equiv 1$, and Eq. (2.29) becomes

$$A_{ll}, (\theta_{\vec{q}_{j}\vec{p}_{j}}) = \frac{2(-)^{l+l'}}{\pi q} (2l+1)^{\frac{1}{2}} (2l'+1)^{\frac{1}{2}} p_{l} (\cos\theta_{\vec{q}_{j}\vec{p}_{j}}) p_{l'} (\cos\theta_{\vec{q}_{j}\vec{p}_{j}}), \qquad (2.30)$$

with $p_i^2 = p_j^2 + q_j^2 - q^2$ and

$$\cos\theta_{\vec{q}_{i}\vec{p}_{i}} = (ij) \frac{\left[\alpha_{ij}^{2}(q_{j}^{2}-q^{2})+\beta_{ij}^{2}(q^{2}-p_{j}^{2})\right]}{2\alpha_{ij}\beta_{ij}qp_{i}}, \qquad (2.31)$$

$$\cos\theta_{\vec{p}_{j}\vec{q}_{j}} = (ij) \frac{[\beta_{ij}^{2} p_{j}^{2} + \alpha_{ij}^{2} q_{j}^{2} - q^{2}]}{2\alpha_{ij}\beta_{ij}p_{j}q_{j}}, \qquad (2.32)$$

where (ij) denotes that (12) = (23) = (31) = 1 and (21) = (32) = (13) = -1.

Substituting Eq. (2.28) with A_{ll} , given by Eq. (2.30) back into Eq. (2.19), and integrating over the angles, we obtain for the Faddeev equations

$$\Psi_{l}^{(i)}(\phi, q, s) = \Phi_{l}^{(i)}(\phi, q, s) + \sum_{j \neq i} \sum_{l'=0}^{\infty} \int_{0}^{\infty} dq_{j}^{2} \int_{L_{ij}}^{U_{ij}} dp_{j}^{2} \\
\times \frac{(-)^{l+l'}[(2l+1)(2l'+1)]^{\frac{1}{2}} P_{l}(\cos\theta_{\vec{p}}, \vec{q}) P_{l'}(\cos\theta_{\vec{p}}, \vec{q})}{4\pi\alpha_{ij}\beta_{ij}q(p_{j}^{2} + q_{j}^{2} - s)} \\
\times t_{l}^{(i)}(\phi, p_{i}; s - q^{2})\Psi_{l'}^{(j)}(p_{j}, q_{j}, s), \quad i = 1, 2, 3 \quad (2.33)$$
Ith $U_{..} = (\alpha_{..}q_{.} + q)^{2}/\beta_{..}^{2}, \quad L_{..} = (\alpha_{..}q_{.} - q)^{2}/\beta_{..}^{2}, \quad (2.34)$

with $U_{ij} = (\alpha_{ij}q_j + q)^2 / \beta_{ij}^2$, $L_{ij} = (\alpha_{ij}q_j - q)^2 / \beta_{ij}^2$.

It is clear that if $t_j^{(i)}(p,p_i;s-q^2)$ is expanded in a sum of terms separable in p and p_i , then the p dependence of $\Psi_l^{(i)}(p,q,s)$ becomes explicit (p does not appear in the kinematic functions or the limits of integrations), and the coupled integral equations in two variables [Eq. (2.33)] can be reduced to equations of one variable.¹⁰,¹² We will consider the application of these equations to three-particle atomic systems in which the interaction proceeds through two-body Coulomb potentials between each pair of particles.

III. THE METHOD OF SOLUTION

A. Eigenfunction Expansion for "Off-Shell" Amplitude

As mentioned before, the partial-wave Faddeev equations of two variables may be reduced to equations of one variable if the "off-shell" two-body scattering amplitudes t_l are represented in sums of separable terms. In general, if the two-body potentials $V_l^{(i)}$ for a system are given, the two-body amplitude $t_l^{(i)}$ can be obtained from the solution of the Lippmann-Schwinger equation

$$t_l^{(i)}(p,p';E) = V_l^{(i)}(p,p') + \pi^{-1} \int_0^\infty dp''^2 p'' V_l^{(i)}(p,p'') t_l^{(i)}(p'',p';E) / (p''^2 - E).$$
(3.1)

Since the argument E is replaced by $(s - q^2)$ in the Faddeev equations, it is negative-definite provided the three-particle energy s is below the three-particle threshold (s=0). For negative values of E, the $(p''^2 - E)^{-1}$ term in Eq. (3.1) is nonsingular, and it is well known that the solution for $t_1^{(1)}$ can be expressed

in terms of eigenfunctions of the homogeneous portion of Eq. (3.1).

The solution $\phi_{nl}^{(i)}$ of the homogeneous Lippmann-Schwinger equation and the corresponding eigenvalues $\lambda_{nl}^{(i)}$ are defined by

$$\lambda_{nl}^{(i)}(E)\phi_{nl}^{(i)}(p,E) = \pi^{-1} \int_0^\infty d_{l}^{h''2} \left[p''V^{(i)}(p,p'')/(p''^2 - E) \right] \phi_{nl}^{(i)}(p'',E), \quad (3.2)$$

with the orthonormality property

$$\pi^{-1} \int_{0}^{\infty} dp''^{2} p'' \phi_{nl}^{(i)}(p'', E) \phi_{ml}^{(i)}(p'', E) / (p''^{2} - E) = \delta_{nm}.$$
(3.3)

Since $\phi_{nl}^{(i)}$ constitutes a complete set, the two-body amplitude $t_l^{(i)}$ can be expanded in the form

$$t_{l}^{(i)}(p,p';E) = \sum_{n=0}^{\infty} C_{nl}^{(i)}(p',E)\phi_{nl}^{(i)}(p,E).$$
(3.4)

Substitution of (3.4) into Eq. (3.1) yields, with the help of Eqs. (3.2) and (3.3),

$$t_{l}^{(i)}(p,p';E) = \sum_{n=0}^{\infty} \left\{ \lambda_{nl}^{(i)}(E) / \left[1 - \lambda_{nl}^{(i)}(E) \right] \right\} \phi_{nl}^{(i)}(p,E) \phi_{nl}^{(i)}(p',E) .$$
(3.5)

This is the desired representation for $t_l^{(i)}$ in the sums of separable terms. In momentum representation, the Coulomb potential is

$$V_l^{(i)}(p,p') = -(Z_i \mu_i^{\frac{1}{2}} / \sqrt{2} p p') Q_l^{(p^2 + p'^2)} / 2p p', \qquad (3.6)$$

where the Q_l 's are the Legendre functions of the second kind, μ_i is the reduced mass, and Z_i is the product of the charges (i.e., $Z_j Z_k$) of the two particles. For this potential the eigenfunction $\phi_{nl}^{(i)}$ and the eigenvalue $\lambda_{nl}^{(i)}$ are both known analytically.¹⁶ We have

$$\phi_{nl}^{(i)}(p,E) = [N_{nl}(E)p^{l}/(p^{2}-E)^{l+1}]C_{n-l-1}^{l+1}[(p^{2}+E)/(p^{2}-E)], \quad n > l$$
(3.7)

and
$$\lambda_{nl}^{(i)}(E) = -Z_i \mu_i^{\frac{1}{2}} / n \sqrt{-2E}$$
, (3.8)

where n > l and the normalization constant is

$$N_{nl}(E) = \left[2^{4l+3}n(n-l-1)!/\Gamma(n+l+1)\right]^{\frac{1}{2}}l!(-E)^{(2l+3)/4}.$$
(3.9)

The $C_{m-1}^{l+1}(x)$'s in Eq. (3.7) are the Gegenhauer polynomials¹⁷

$$C_{m-1}^{l+1}(x) = \frac{\Gamma(m+2l+1)}{\Gamma(m)\Gamma(2l+3)} F\left(m+2l+1, 1-m; l+\frac{3}{2}; \frac{1}{2}(1-x)\right) = \sum_{\gamma=0}^{m-1} a_{\gamma}^{(l+1)}(m)\left(\frac{x-1^{\gamma}}{2}\right), \quad (3.10)$$

with
$$a_{\gamma}^{(l+1)}(m) = [2(m+2l+\gamma)(m-\gamma)/\gamma(2l+2\gamma+1)]a_{\gamma-1}^{(l+1)}(m)$$
, (3.11)

where the recursion relation for the a's starts with

$$a_0^{(l+1)}(m) \equiv (m+2l) \left[\frac{(m-1)}{(m-1)} \right] . \tag{3.12}$$

B. Coupled Single-Variable Integral Equations

Utilizing the separable representation [Eq. (3.5)] for the off-shell two-particle amplitude, the p dependence of $\Psi_{Q}(i)(p,q,s)$ can now be made explicit. Let us return to the Faddeev equations for total J=0. From Eq. (2.33), it is clear with the help of Eq. (3.5) that $\Psi_{l}(i)(p,q,s)$ can be expressed as

$$\Psi_{l}^{(i)}(p,q,s) = \Phi_{l}^{(i)}(p,q,s) + \sum_{n} \{\lambda_{nl}^{(i)}(s-q^{2})/[1-\lambda_{nl}^{(i)}(s-q^{2})]\} \phi_{nl}^{(i)}(p,s-q^{2})\chi_{nl}^{(i)}(q,s).$$
(3.13)

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Substituting Eq. (3.13) into Eq. (2.33), we obtain a set of coupled single-variable integral equations for $\chi_{nl}^{(i)}(q,s)$:

$$\chi_{nl}^{(i)}(q,s) = \eta_{nl}^{(i)}(q,s) + \sum_{n',l';j \neq i} \int_{0}^{\infty} dq_{j}^{2} \mathscr{K}_{nl,nl'}^{(i,j)}(q,q_{j};s) \chi_{n'l'}^{(j)}(q_{j},s), \quad i = 1,2,3$$
(3.14)

with
$$r_{nl}^{(i)}(q,s) = \sum_{l',j \neq i} \int_{0}^{\infty} dq_{j}^{2} \left(\frac{U_{ij}}{L_{ij}} dp_{j}^{2} \frac{(-)^{l+l'} [(2l+1)(2l'+1)]^{\frac{1}{2}}}{4\pi \alpha_{ij} \beta_{ij} q(p_{j}^{2}+q_{j}^{2}-s)} P_{l}(\cos\theta_{\vec{p}_{i}\vec{q}_{i}}) P_{l'}(\cos\theta_{\vec{p}_{j}\vec{q}_{j}}) \times \phi_{nl}^{(i)}(p_{i},s-q^{2})\phi_{ll}^{(j)}(p_{i},q_{i}), \qquad (3.15)$$

$$\frac{3c}{nl,n'l} \stackrel{(i,j)}{(q,q_{j};s)}{=} \int_{L_{ij}}^{U_{ij}} dp_{j}^{2} \frac{(-)^{l+l'} [(2l+1)(2l'+1)]^{\frac{1}{2}} P_{l}(\cos\theta_{\vec{p}_{i}}\vec{q}_{i}) P_{l'}(\cos\theta_{\vec{p}_{i}}\vec{q}_{j})}{4\pi\alpha_{ij}\beta_{ij}q(p_{j}^{2}+q_{j}^{2}-s)[1-\lambda_{n'l}^{(j)}(s-q_{j}^{2})]} \times \phi_{nl}^{(i)}(p_{i},s-q^{2})\lambda_{n'l'}^{(j)}(s-q_{j}^{2})\phi_{n'l'}^{(j)}(P_{j},s-q_{j}^{2}).$$
(3.16)

Equations (3.14) are the basic working equations. We will now examine their physical implications.

Let us first examine the singularities of the kernel \mathcal{X} given by Eq. (2.16). For negative values of s, two-particle bound states of the system (if they exist) play an important role in the analytic structure of the kernel \mathcal{X} . Denote the two-particle bound-state energy by $-\epsilon$. For each such two-particle state, there is a corresponding eigenvalue λ which equals to unity at $-\epsilon$. The denominator $1 - \lambda_{n/l} (j)(s-q^2)$ in the kernel then vanishes at $q^2 = s + \epsilon$ for $s > -\epsilon$, therefore creating a branch point for $\chi_{nl} (i)(q, s)$ at $s = -\epsilon$. Three-particle bound states can only occur below the branch points. The region between the lowest and the next branch points is the energy region for purely elastic scattering of a particle by a two-particle system in its ground state. A single inelastic process occurs above the second threshold, and so forth. By solving the Faddeev equations, we can obtain bound-state and resonance energies and wave functions below the three-particle breakup threshold.

Now if there is no two-particle bound state between any pair of particles in the three-particle system, the behavior of the kernel x becomes less complicated, since in this case the kernel is pure real below s = 0. Again, Eqs. (3.14) can be solved in a straightforward manner for both the energies and wave functions of any possible three-particle bound states.

It should be noted, however, that if the total energy s is positive (i.e., above the three-particle breakup threshold), then there is a region $0 < q^2 < s$ where the two-particle energy $s - q^2$ is positive and the expansion for the off-shell two-particle amplitude [Eq. (3.5)] in general fails to converge. The method discussed above becomes unsuitable. This includes the problems of three-particle breakup such as, for example, the ionization of hydrogen atoms by electron impact.

We remark here that, for the Coulomb interaction, the two-body T matrix $t_l(p,p',E)$ is singular at $p^2 = E$, $p'^2 = E$ or p = p' for all E. The first two regions are inaccessible below the three-particle threshold (ionization energy), because E is negative-definite while p and p' are positive. The region p = p' is accessible but the kernel $\mathcal{K}_{nl,n'l'}(q,q_j;s)$ is already the result of an integration over p_j^2 . Since the singularity at p = p' is only logarithmatic, the kernel no longer contains such a logarithmatic singularity. This, we believe, is the reason why the three particle atomic problem can be handled by the Faddeev equations without further modification, as long as the total energy is below the three-particle breakup threshold.

So far the initial states of the three-particle system are left unspecified. This is possible because the kernel of the integral equation is independent of the initial state, and the energy spectrum of the threebody system is determined entirely by the kernel. The specification of the initial state and the corresponding inhomogeneous terms are, however, of importance for the wave function of the scattering problem. We now show how this term may be calculated.

For a physical scattering process, one usually has an initial state consisting of two interacting subsystems; in the present case, a particle plus a two-particle subsystem in certain bound state. For definiteness, we consider an initial state consisting of particle 1 and a bound state of (2, 3) with energy s_0 and angular momentum l_0 . The corresponding inhomogeneous term takes the form [see Eqs. (2.21), (2.24), and (2.26)]

$$\Phi_{l_0}^{(1)}(p,q,s) = -\frac{4}{\pi q} t_{l_0}^{(1)}(p,p_0,s-q_0^2) \delta(q^2-q_0^2), \qquad (3.17)$$

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where p_0 and q_0 are the p and q of the initial state. Since $t_{l_0}^{(1)}$ has a pole at $s - q_0^2 = s_0$, $\Phi_{l_0}^{(1)}(p,q,s)$ can be rewritten as

$$\Phi_{l_0}^{(1)}(p,q,s) = \frac{4}{\pi q} \left[\delta(q^2 - s + s_0) / \lambda_{n_0 l_0}^{(1)'}(s_0)(s - q_0^2 - s_0) \right] \phi_{n_0 l_0}^{(1)}(p,s_0) \phi_{n_0 l_0}^{(1)}(p_0,s_0) , \qquad (3.18)$$

where λ' is the derivative of λ with respect to s. Now multiply both sides of Eq. (2.33) by $(s - q_0^2 - s_0)/\phi_{n_0l_0}^{(1)}(p_0, s_0)$ and then take the limit $q_0^2 - s - s_0$. It is easily seen that all the inhomogeneous terms vanish except for $\Phi_{I_0}^{(1)}$ and that the wave function of the initial (2,3) bound state $\phi_{n_0l_0}^{(1)}(p_0, s_0)$ is factored out of the equation. Substitution of $\Phi_{I_0}^{(1)}$ from Eq. (3.18) into Eq. (3.15) gives an explicit inhomogeneous term $\eta_{n_0l_0}^{(1)}$. Equation (3.14) can now be solved by standard numerical methods. For s above the lowest branch point the kernel must be taken as the limit of s approaching the real axis from above. One can either use numerical methods for complex arithematics or the Fredholm reduction given by Noyes¹⁸ and by Kowalski,¹⁹

C. Spin and Identical Particles

So far, we have not considered spin in this formulation of the Faddeev equations. For nonrelativistic atomic problems, there is no spin-orbit coupling and the effect of the spin simply appears as a multiplicative factor in the kernel^a:

$$\begin{array}{c} (i,j) & (i,j) \\ \mathcal{K}_{nl,n'l'}(q,q_{j};s) - \mathcal{K}_{nlS,n'l'S'}(q,q_{j};s,S_{0}) = (-1) \\ & & & \\ & &$$

where S_0 is the total spin of the three-particle system; S the spin of the pair (j,k); S' the spin of the pair (k, i); S_i , S_j , and S_k the spins of the individual particles; and $\{ \}$ denotes the 6j symbol. Of course, the *T*-matrix elements $\chi_{nl}(i)$ should now carry an additional spin index S denoting the spin of the pair (j,k).

As for identical particles, the statistics require that the two-body partial wave T matrix $t_{f}^{(i)}(p,p';E,S)$ be identically zero for certain l. In particular, for two spin- $\frac{1}{2}$ identical fermions, t is zero for even l if S = 1 and for odd l if S = 0. As long as all the two-body T-matrix elements satisfy the requirement of statistics, the solution of the Faddeev equations also satisfies the statistic. The number of equations is reduced because some of the kernels become equivalent.

IV. APPLICATION TO THE (e,H) SYSTEM

It is well-known that for the (e, H) system, there exists only one three-particle bound state corresponding to the ground 'S H- state. All the other three-particle states are unstable. They correspond to the resonant states which may be generated in the laboratory in an electron-hydrogen (atom) scattering experiment,^{20,21} Theoretically it can be shown^{22,23} that associated with each excited two-particle threshold (corresponding to the excited states of H atom) there exist a number of resonances supported by a potential which asymptotically goes to zero primarily as r^{-2} . Reasonably accurate determinations of the position and the width of a few of the lower members of the resonances have been recently carried out both theoretically 2^{24-29} and experimentally.²¹ For the bound H⁻ state on the other hand, an accurate value for the H⁻ detachment potential has been known for some time. A calculation of this singlet H- state and the lowest members of the resonances in both the singlet and the triplet J = 0 series would therefore provide some insight into the feasibility of the method outlined in Sec. III.

A. The 'S H⁻ Bound State

Since the 'S H⁻ state has a zero total angular momentum (i.e., J=0), Eq. (3.4) may be used for the calculation of this state. One can readily show for singlet spin multiplicity that the electron-proton interaction amplitudes for electrons 1 and 2 must satisfy the relation

$$\chi_{nl}^{(1)}(q,s) = (-)^{l} \chi_{nl}^{(2)}(q,s),$$

and the electron-electron amplitude the relation

$$\chi_{nl}^{(s)}(q,s) = 0$$
 for odd l.

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(4.1)

(4.2)

Equation (4, 2) is simply the statement of the Pauli principle which excludes the possibility for two electrons in the singlet spin state to have odd parity. Equation (4,1) allows for the reduction of the coupled equations [Eq. (3.14)] into a pair of coupled equations. The spin factor for the kernel is unity in this case.

We write Eq. (3.14) in the matrix notation

$$\chi(q,s) = \underline{\eta}(q,s) + \int_0^\infty dq_j^2 \underline{\mathfrak{K}}(q,q_j;s) \underline{\chi}(q_j,s) , \qquad (4.3)$$

with
$$\underline{\chi}^{\dagger}(q,s) = [\chi_0^{(1)}(q,s), \chi_0^{(3)}(q,s), \chi_1^{(1)}(q,s), \chi_1^{(3)}(q,s), \chi_2^{(1)}(q,s), \chi_2^{(3)}(q,s), \ldots],$$
 (4.4)

where each element $\chi_l^{(i)}(q,s)$ is a row with a dimension which equals the number of terms included in the off-shell two-particle amplitude $t_l^{(i)}$ [see Eq. (3.5)]. Equation (4.3) may be solved for $\chi(s)$ by digitizing the continuous variables q and q_i and inverting the matrix (I - x)

$$\chi(s) = [I - \underline{\mathfrak{x}}(s)]^{-1} \underline{\eta}(s) \,. \tag{4.5}$$

To calculate the bound H⁻ state, we need to determine the pole in the inverse operator $[I - \underline{x}(s)]^{-1}$. The pole may be located by locating the energy s at which the determinant of the $I - \underline{x}$ (s) matrix is zero.

For Coulomb interactions, the matrix elements in X may be obtained analytically since both the eigenfunctions $\phi_{\eta i}$ ⁽ⁱ⁾ and eigenvalues $\lambda_{\eta i}$ ⁽ⁱ⁾ of the homogeneous Lippmann-Schwinger equation [Eq. (3.2)] are known explicitly [see Eqs. (3.7) and (3.8)]. It can be shown that when these explicit expressions are utilized with the help of Eq. (3.10), all the integrals needed for the evaluation of the matrix element in \underline{x} can be expressed in terms of the basic integrals

$$I_{n}(q,q_{i},s) = \int_{(\sqrt{2}q-q_{i})^{2}}^{(\sqrt{2}q+q_{i})^{2}} \frac{dp_{i}^{2}}{(p_{i}^{2}+q_{i}^{2}-s)^{n+1}},$$
(4.6)

where we have made use of the large disparity between the electron and proton masses (i.e., m_1/m_3 $= m_2/m_2 \cong 0$). These integrals satisfy the recursion relation

$$I_{n+1} = [n/(n+1)] \{ [(\xi+\zeta)^{n+1} - (\xi-\zeta)^{n+1}] / [(\xi+\zeta)^n - (\xi-\zeta)^n] \} [I_n/(\xi^2-\zeta^2)], \quad n \ge 1,$$
(4.7)

with
$$\xi = (2q^2 + 2q_i^2 - s), \ \xi = 2\sqrt{2}qq_i$$
, (4.8)

where the recursion relation for the I's starts with

$$I_1 = 4\sqrt{2} q q_i / [(2q^2 + 2q_i^2 - s)^2 - 8q^2 q_i^2].$$
(4.9)

As discussed before, the three-particle bound states can only occur below the branch point corresponding to the elastic threshold. In this energy region s < -1 Ry (-13.605 eV), the matrix $(I - \mathcal{K})$ is pure real. After Eqs. (4.1) and (4.2) are utilized in Eqs. (4.3), the resultant matrix integral equations are then solved by matrix inversion [Eq. (4.5)]. By taking only the first term in the $t_l^{(2)}$ expansion [Eq. (3.5)], we found that the H⁻ state appears at -1.0516 Ry below the three-particle breakup threshold. This corresponds to a detachment potential of -0.0516 Ry (i.e., 0.702 eV) for H⁻ in comparison with the accurate value of -0.0555 Ry of Peheris.³⁰ The agreement is most remarkable in view of the fact that only a single 1s term in the $t_1^{(2)}$ expansion is used in the calculation. This then implies that all the remaining terms contribute less than 7%.

To demonstrate that all the remaining terms in the $t_1^{(i)}$ expansion contribute less than 7% is, however, a somewhat difficult task. The expansion converges in an oscillatory manner and involves large cancellations. For example, the addition of the 2s term pushes the H⁻ state up very close to the elastic threshold. The 2s term effect is cancelled by the 3s term. The net result due to the inclusion of the 2s and 3s terms is to move the H⁻ state down to -1.061 Ry. On the other hand, the addition of 2p and 3p terms would lower further the H⁻ state to - 1.064 Ry, and the addition of a 3d and 4s terms then pushes the H⁻ state up to -1.063 Ry. It is clear from the numerical result that the oscillations become smaller for higher terms in the $t_l^{(i)}$ expansion. However, our results seem to converge to a value lower than the accepted value. This is probably due to systematic errors in our numerical calculations. We will return to the convergence problem in Sec. V. Perhaps it is worthwhile to note that there is a substantial con-tinuum component in each term of the $t_l^{(i)}$ expansion because this is a Stermian function expansion, so that the symbols 1s, 2s, 2p, etc. should be interpreted accordingly.

Recently, a calculation of the H⁻ bound state has been carried out by Vesselova.³¹ In this calculation the two-body interaction amplitude between the electrons $t_l^{(s)}$ was taken to be zero. As a test of our program we have considered the $t_I^{(3)}=0$ case and obtained, as expected, an energy spectrum which is simply the superposition of two sets of hydrogenic levels.

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B. The Resonant H⁻ States

As the total energy s of the system moves above the elastic threshold, we encounter the electron-hydrogen scattering problem. The corresponding matrix $(I - \underline{x})$ now becomes complex and contains branch points arising from bound states of H atom. These branch points must be treated properly in solving Eq. (4.3) for resonant states and in calculating the complex poles in $(I - \underline{x})^{-1}$. As an example, we will determine the two lowest J=0 resonances with singlet and triplet spin states in the elastic region. We choose this example for simplicity since in the elastic energy region the branch point of concern is reduced to just the one associated with the ground hydrogen state.

For the calculation of the singlet J=0 resonances, one may again solve Eq. (4.3) numerically. Due to the presence of the branch points, it is difficult to maintain a desired accuracy by the standard numerical method of complex integration. However, the accuracy may be significantly improved by the Fredholm reduction method^{18,19} in which the branch points are removed from the matrix to be inverted. For the present problem, the only branch point of concern is that associated with the ground H state in $\chi_0^{(1)}(q,s)$ [Eq. (4.4)]. We will now show how such a method may be adopted for the present problem.

Write for $\chi(q,s)$ the expression

$$\chi(q,s) = u(s)\gamma(q,s) \tag{4.10}$$

where $u(s) = \chi(\sqrt{s_0}, s)$ and

$$\underline{\Upsilon}^{\dagger}(s) = \left[\Upsilon_{0}^{(1)\dagger}(q,s), \Upsilon_{0}^{(3)\dagger}(q,s), \Upsilon_{1}^{(1)\dagger}(q,s), \Upsilon_{1}^{(3)\dagger}(q,s), \Upsilon_{2}^{(1)\dagger}(q,s), \Upsilon_{2}^{(3)\dagger}(q,s), \Upsilon_{2}^{(3)\dagger}(q,s), \ldots \right],$$
(4.11)

where $s_0 \equiv s+1$, $u(s_0)$ is a scalar function, and the $\Upsilon_l^{(i)}(q,s)$'s are columns with elements $\Upsilon_{nl}^{(i)}(q,s)$. For the purpose of calculating resonance poles, we may replace Eq. (4.3) by

$$u(s)\underline{\Upsilon}(q,s) = \underline{\mathfrak{K}}_{10}^{(1)}(q,\sqrt{s_0},s) + u(s) \int_0^\infty dq_j^2 \underline{\mathfrak{K}}(q,q_j,s)\underline{\Upsilon}(q_j,s)$$
(4.12)

where we have replaced $\underline{\eta}(q,s)$ [see Eq. (4.3)] by $\underline{\mathfrak{X}}_{10}^{(1)}(q,s_0;s)$ since poles in $\chi(s)$ are independent of the inhomogeneous term $\eta(q,s)$ [see Eq. (4.5)]. The symbol $\underline{\mathfrak{K}}_{10}^{(1)}$ stands for $\underline{\mathfrak{K}}_{10}^{-},\underline{\mathfrak{n}}^{(1,i)}$ where *i*, *n*, and *l* are the suppressed indices of \mathbf{T} . This quantity $_{10}^{(1)}(q,s_0;s)$ in Eq. (4.12) is chosen to make the kernel of the integral equation for Υ nonsingular at $q^2 = s_0$. By definition of u, $\Upsilon_{10}^{(1)}(\sqrt{s_0},s)$ is normalized to unity. Solving Eq. (4.12) for u(s) at $q^2 = s_0$, we obtain

$$u(s) = \mathfrak{R}_{10,10}^{(1,1)}(\sqrt{s_0}, \sqrt{s_0}; s) / \left(1 - \sum_{\substack{j,n,l \\ n > l}} \int_0^\infty dq_j^2 \mathfrak{R}_{10,nl}^{(l,j)}(\sqrt{s_0}, q_j; s) \mathfrak{T}_{nl}^{(j)}(q_j, s)\right).$$
(4.13)

Substitution of u(s) from Eq. (4.13) back into Eq. (4.12) yields

$$\underline{\Upsilon}(q,s) = \frac{\underline{\mathscr{K}}_{10}^{(1)}(q,\sqrt{s_0},s)}{\underline{\mathscr{K}}_{10,10}^{(1,1)}(\sqrt{s_0},\sqrt{s_0};s)} + \int_0^\infty dq_1^2 \left\{ \underline{\mathscr{K}}(q,q_j;s) - \frac{\underline{\mathscr{K}}_{10}^{(1)}(q,\sqrt{s_0};s)}{\underline{\mathscr{K}}_{10,10}^{(1)}(\sqrt{s_0},\sqrt{s_0};s)} \cdot \underline{\mathscr{K}}_{10}^{(1)\dagger}(\sqrt{s_0},q_j;s) \right\} \underline{\Upsilon}(q_j,s).$$
(4.14)

Now, the kernel does not have a pole at $q_j^2 = s_0$, and Eq. (4.14) contains no branch point for s < -0.25 Ry. It may be solved in a straightforward manner for $\Upsilon(q,s)$. Having obtained $\Upsilon(q,s)$, u(s) can be calculated by evaluating the principal part integral in Eq. (4.13), and the poles of u(s) are then poles of χ .

Unlike the case for the bound state, retaining only the 1s term in the $t_1^{(t)}$ expansion [Eq. (3.5)] fails to give any resonance. A resonance pole is found when either the 2s or the 2p term is included in the $t_1^{(t)}$ expansion. This is expected since the H⁻ resonances are closed-channel resonances²² lying very close to the excitation threshold. The positions of the pole obtained in the 1s-2s and 1s-2p expansions are at -0.286 and -0.291 Ry below the three-particle breakup threshold, respectively. The position of the lowest H⁻ resonance in the J=0 singlet series has been found to be at -0.2973 Ry both experimentally²¹ and theoretically.²²⁻²⁹ This seems to indicate that neither the 2s nor the 2p term alone is sufficiently attractive to lower the pole to -0.2973 Ry. From these results one may also conclude that the 2p term is more attractive than the 2s term.

The combined effect of the 2s and 2p terms, on the other hand, is much too attractive. The pole is lowered in the 1s-2s-2p approximation to -0.326 Ry. It requires the 3s term to push the pole up to -0.3004 Ry. The addition of the 3p and 3d terms move the pole further up to -0.298 Ry, which is closer to the value of -0.2973 Ry calculated in the closed-coupling approximation with correlated wave functions. Though there is a definite indication of convergence towards the value of -0.2973 Ry, the convergence is again oscillatory and not rapid. It is perhaps worthwhile to emphasize that the present calculation is term-by-term exact. No variational or stationary parameters were used in the calculation.

The calculated width for the lowest J=0 singlet resonance in the 1s-2s-2p-3s approximation is 0.0025 Ry (0.034 eV) which is in reasonable agreement with previous calculations.^{24,25,29,29} The measured width for this resonance is 0.043 eV.³¹ In Fig. 4 the profile of the elastic scattering cross section in the neigh-

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18.0 16.2 14.4 12.6

² 10.8

CROSS SECTION

9.0

7.2 5.4 3.6

-0.3034

-0.3020

-0.3006

-0.2992

ENERGY s(Ry)

-0.2978



FIG. 4 Energy dependence of the singlet J = 0 elastic scattering cross section in the neighborhood of the resonance in the 1s-2s-2p-3s approximation.

borhood of the J=0 singlet resonance is given. It is seen that the interference between direct and resonance scattering is important. Due to the absence of other channels, the cross section actually dips through zero at s = -0.2997 Ry.

For the triplet case, the electron-proton interaction amplitudes for electrons 1 and 2 must satisfy, instead of Eq. (4.1), the relation

$$\chi_{nl}^{(1)}(q,s) = (-)^{l+1} \chi_{nl}^{(2)}(q,s), \qquad (4.15)$$

and the electron-electron interaction must satisfy, instead of Eq. (4.2), the relation

$$\chi_{nl}^{(S)}(q,s)=0, \text{ for even } l.$$

Equation (4.16) is again the statement of the Pauli principle which excludes the possibility for two electrons in the triplet spin state to have even parity. Equation (4.15) allows for the reduction of Eq. (3.14) into a different pair of coupled equations for the triplet case. The spin factor for the kernel is again unity.

The behavior of the solution for the triplet case is similar in nature to the singlet case. We obtain in the 1s-2s-2p-3s-3p approximation a resonance pole at -0.257 Ry below the three-particle breakup threshold with a width of -2×10^{-5} Ry (2. 72×10^{-4} eV) which are in reasonable agreement with the previously calculated values.^{25,29}

V. CONCLUDING REMARKS

The method presented in Sec. III provides a practical way of solving the Faddeev equation for Coulomb potentials below three-particle breakup threshold. It is seen, from the example in Sec. IV, that by retaining only a few leading terms in the series a reasonably accurate value is obtained. The interesting problem is then to investigate the convergence of the remaining terms in the series. This is, however, a somewhat difficult task, since, as was pointed out in Sec. IV, the expansion converges in an oscillatory manner and involves large cancellations. The net sum of all the terms, considered as a whole, constitutes, nevertheless, a small correction. It is then feasible that a perturbation scheme in which the sum of the contribution of the remaining terms is treated as a perturbation may be developed. In this concluding section, we outline such a perturbative scheme.

Let us consider the problem of determining the poles in the inverse operator in Eq. (4.5) by examining the energy dependence of the determinant Det $\{I - \mathcal{K}(s)\}$. We can partition the matrix as

$$I - \mathcal{K}(s) = B + \underline{\mathcal{S}} = B \{I + B^{-1} \underline{\mathcal{S}}\},\$$

where B is a square matrix consisting of elements obtained in a truncated expansion including the leading terms in the series and \mathcal{S} is the remainder. Utilizing the relation between the determinant and the trace of the logarithm of the corresponding matrix,

$$Det A = \exp\{Tr(\ln A)\},\$$

we have

$$\operatorname{Det}\{I - \mathfrak{X}(s)\} = \operatorname{Det}B \exp\{\operatorname{Tr}[\ln(1+B^{-1}\mathcal{E})]\} = \operatorname{Det}B\{1 + \operatorname{Tr}B^{-1}\mathcal{E} - \frac{1}{2}\operatorname{Tr}(B^{-1}\mathcal{E}B^{-1}\mathcal{E}) + \cdots\},$$
(5.3)

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-0.2950

-0.2964

(4, 16)

(5.1)

(5.2)

173

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Defining $C = B^{-1}$, we have

$$\operatorname{Det}\{I - \underline{\mathfrak{K}}(s)\} = \operatorname{Det}\underline{B}\left[1 \div \sum_{\alpha=m+1}^{n} \epsilon_{\alpha\alpha} - \sum_{\alpha=1}^{m} \sum_{\beta=1}^{m} \sum_{\gamma=m+1}^{n} c_{\alpha\beta} \epsilon_{\beta\gamma} \epsilon_{\gamma\alpha} - \frac{1}{2} \sum_{\alpha=m+1}^{n} \sum_{\lambda=m+1}^{n} \epsilon_{\lambda\alpha} \epsilon_{\alpha\lambda} + \frac{1}{2} \left(\sum_{\alpha=m+1}^{n} \epsilon_{\alpha\alpha}\right)^{2} + \cdots\right], \qquad (5.4)$$

where ϵ_{ij} and c_{ij} are the elements of matrices $\underline{\delta}$ and \underline{C} respectively, n is the order of the matrix while m is the order of the submatrix corresponding to the truncated expansion. This then provides a systematic way of investigating the convergence problem.

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H(2p) EXCITATION RESONANCES IN (e-H) SYSTEM NEAR THRESHOLD*

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High-resolution electron-impact measurements reveal that just above the threshold for excitation of the 2p level of atomic hydrogen there is a complicated resonance structure, part of which had not previously been predicted or observed.

In this note we discuss our recent measurements of the resonance structure found in the total cross section for the production of Lyman- α from the reaction

The observed structure is associated with the temporary formation of one or more H⁻⁻ compound states in the $(2s)^{2}$, $(2p)^{2}$, or (2s, 2p) doubly excited configurations. These "potential" resonances are of the same configurations as the resonances previously studied in the elastic channel below the first inelastic threshold.¹

It has previously been observed, both theoretically³⁻⁴ and experimentally,⁵ that the excitation cross section does not follow what is normally considered Wigner's law. The most recent calcualtions have demonstrated that near threshold there is at least one resonance. However, a major point of this report will be to show that the resonance structure in the threshold region is more complicated than has been suggested thus far by theory. In the paper which follows, a partial explanation of this observation is given by Marriott and Rotenberg.⁶ In a subsequent experimental paper, the details of our experimental technique, our total cross-section measurements, and cur measurements of the resonances below and above the n=3 level will be discussed.

A modulated rectangular beam of H atoms (more than 85% pure) is crossed with a rectangular beam of electrons with an energy distribution (the width of the Gaussian energy distribution at half-maximum) of 0.07 eV. Electrons from a 127° electron-energy selector enter a magneticand electric-field free region. cross the modulated H-atom beam from below, and then pass into a collector in which a crossed electric field can be applied to collect all the electrons in the beam. When this field is removed the electrons pass through the collector region into a second, rotatable, electrostatic energy analyzer which measures the energy and angular distribution of the electrons. Photons from the interaction of the electron and hydrogen atoms are detected at an angle of 54.5° with respect to the direction of the electrons. At this angle the observed signal

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is proportional to the total 2p-excitation cross section.⁷

Ions from the interaction region are accelerated along the atomic-beam axis into a Paul mass filter. As in previous experiments^{1, 8} the linear extrapolation of the ionization efficiency curve to its energy axis is used as a calibration reference point for the electron energy scale. As has already been shown, this point is approximately 0.03 eV above the real ionization threshold.⁸

For each experimental run, data were collected automatically over a period which often exceeded 100 h. The instrument was programmed to step through a prescribed energy interval which in this experiment is usually 0.90 eV taken in 0.015eV steps. The residence time for each energy step was normally 60 sec. The data were collected digitally, i.e., for each energy interval, the signal plus background, the background, and the electron current were recorded on punched tape to be processed later by the computer. Every 12 to 15 h the process was interrupted and an ionization efficiency curve for the collision

 $H(1s) + e = H^+ + 2e$

was taken to make sure that the electron energy scale for excitation remained constant. Through all of our experiments the ionization reference point remained constant to within ± 0.015 eV.

Because particular attention was to be focused upon the details of the structure which appeared in our excitation curves, it was necessary to make certain that none of the structure observed was due to radiation from the collisions of the electrons with He molecules residual in our Hatom beam or with H₂ which formed part of the background gas. It has already been recognized⁷ that the oxygen gas filter which is normally placed in front of the Lyman- α detector, although transparent to Lyman- α , also passes some molecular radiation. However, it has now been verified by our experiments that the electron energy threshold for production of this molecular radiation is in the vicinity of 11.3 eV, well above the range of interest for this report. Consequently, such radiation cannot have affected our results.

In Fig. 1(a), we give a comparison of our data with the earlier low-resolution experimental results of Chamberlain, Smith, and Heddle⁵ and with two calculations on this system, both by Taylor and Burke.⁴ In Fig. 1(b), the results of Taylor and Burke are shown as modified by folding into their correlation calculation our experimental electron energy distribution. The experi-



FIG. 1. (a) Our data for the excitation of H(2p) (this work), together with earlier measurements by Chamberlain, Smith, and Heddle (CSH) of the Lyman- α excitation cross section (for radiation observed at 90° to the direction of the bombarding electrons). Also shown are two theoretical calculations: the three-stage closecoupling calculations of Taylor and Burke (TB (3 state)) and the three-state-plus-correlation calculation of Taylor and Burke [TB (correlation)]. (b) Comparison of our data with the calculated cross section of Taylor and Burke into which has been folded our experimental energy distribution 0.07 eV.

mental data reported here have been normalized to the Born approximation at high energies by a procedure to be discussed in detail in a later paper.⁹ The results of Chamberlain, Smith, and Heddle are also normalized to theory near threshold in the manner given by Burke, Taylor, and Ormonde.⁴

The sharp rise in the excitation cross section at threshold has been predicted by Damburg and Gailitis⁸ from a close-coupling approximation calculation which includes the lowest three states of the H atom, i.e., the 1s, 2s, and 2ρ states. Subsequent three-state close-coupling calculations by Taylor and Burke,³ shown as TB (3state) in Fig. 1(a), have used a finer energy grid to show that within 0.03 eV of the threshold, there is a sharp resonance in the ¹P channel of

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the temporary H^- doubly excited compound state. A modified calculation, in which the interaction potential contains an additional term to describe the electron-electron interaction (correlation), shown as TB (correlation) in Fig. 1(a), lowers the total cross-section value, shifts the position of the resonance closer to threshold, and considerably reduces its width.

The results of Chamberlain, Smith, and Heddle using an electron beam with a resolution of 0.35 eV, and observing Lyman- α emitted at 90° to the direction of the electron beam, show that the cross section near threshold is finite as predicted. By assuming various shapes for the excitation cross section into which they folded their known electron-energy distribution, they were able to suggest that the cross section near threshold contained a peak. Subsequently, Burke, Taylor. and Ormonde⁴ theoretically identified this peak and showed that their calculations were consistent with the measurements. With our measurements, which have been made with an electron-energy resolution of 0.07 eV, the predicted sharp onset at threshold and the ${}^{1}P$ potential resonance near threshold are clearly defined. Now, however, our data reveal the presence of second and third maxima which have not previously been reported. This second maximum is statistically real, its height being approximately twice the rms error, while the third maximum is not yet statistically sound although its presence has been observed in all our data.

In Fig. 1(b) we show our data in comparison with the three-state close-coupling-plus-correlation calculation of Taylor and Burke³ into which we have folded our electron energy distribution. The agreement at threshold and over the first peak is good, thus giving credence to the calculated position of the resonance at 10.214 eV; however, the discrepancy in widths is large enough so that we suggest that the width of their resonance should be slightly in excess of the suggested 0.015 eV.¹⁰ What is the second peak which appears in our data? One possible explanation is that there is more than one potential resonance in the ${}^{1}P$ channel. Another possible explanation, which is discussed in the following paper by Marriott and Rotenberg,⁶ is that the second peak is part of the first resonance and is not really a separate resonance at all.

One possible explanation for the conjectured third peak is that it, too, is part of a series of potential resonances. Another, and perhaps a more reasonable explanation, is that this is structure which appears in some channel other than the ${}^{1}P$.

It is with pleasure that we acknowledge the help of Professor E. M. Clarke who participated in the early stages of this work and of E. K. Curley who has continuously assisted our program.

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