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# COMPUTER RECOMMENDATIONS FOR AN AUTOMATIC APPROACH AND LANDING SYSTEM FOR V/STOL AIRCRAFT

# **VOLUME II: EQUATIONS**

## By Harry T. Gaines, Robert J. Kell, Avery A. Morgan, Leo J. Mueller, James R. Peterson, Edward R. Rang, J. Patrick Redmond and E. David Skelley

# June 1968

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Prepared under Contract No. NAS 12-615 by

# HONEYWELL INC.

Aerospace and Defense Group Minneapolis, Minnesota and St. Petersburg, Florida

**Electronics Research Center** 

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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#### FOREWORD

This computer recommendation report is submitted in accordance with Contract NAS 12-615 with the NASA Electronics Research Center (ERC), Cambridge, Massachusetts. Specifically, this report is intended to satisfy item 7C2 of Phase II, Part II of the contract statement of work.

This report is published in two volumes:

Volume I - Computer Recommendations

Volume II - Equations

Volume I contains an analysis of candidate computers for use in the Automatic Approach and Landing System (AALS) plus a recommendation of suitable computers. This volume defines a baseline AALS which is representative, in terms of complexity, of systems appropriate to the NASA-ERC flight evaluation program. Review and agreement on these equations was accomplished at NASA-ERC during a technical coordination meeting on 23, 24 May 1968.

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### COMPUTER RECOMMENDATIONS FOR AN AUTOMATIC APPROACH AND LANDING SYSTEM FOR V/STOL AIRCRAFT

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#### SUMMARY

A preliminary automatic approach and landing system (AALS) definition has been completed. It is considered to be a configuration typical of that which would be suitable for V/STOL use. It is designed specifically for the designated flight test vehicle, the NASA/LRC YHC-1A helicopter, and is intended to have sufficient flexibility to evaluate a variety of technology concepts.

Design details and requirements are discussed. Included are functional and mode requirements for navigation, guidance, control, and displays, and an evaluation of analog attitude rate gyros for an alternate analog inner-loop stabilization mechanization.

Results given are in terms of applicable equation and computation requirements for each subsystem. Navigation computations are based on the use of a strap-down inertial reference unit.

Attitude rate output from the single-axis gyros is in the form of pulserate; accelerometer output is frequency modulated. Position update methods are included. Linear control laws are used to obtain automatic control equations. Tustin's method is used to obtain the difference equations to be used in programming the digital computer. Several levels of operation or modes are defined, including both attitude control and velocity command control.

Guidance requirements are established and guidance laws are defined for the generalized V/STOL approach situation. Numerical values selected for each of the various parameters are based on the designated flight test vehicle. Guidance equations include the derivation of velocity commands. The baseline guidance subsystem is discussed relative to optimum path control. Display requirements suitable to the baseline AALS also are defined. Display needs for both manual and automatic control are included. Display equations defined are suitable to a CRT-type display mechanization. (Display generation such as symbols, etc., was not part of the task.)

A "down link" (or telemetry system) is considered as part of the instrumentation. The discussion included herein is based entirely on information supplied by NASA/ERC.

Conclusions and recommendations are made as part of each subsystem discussion. All are pertinent to continued AALS development. Particular emphasis is placed on areas where simplifications might be made.

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## SYSTEM DESIGN AND FUNCTIONAL REQUIREMENTS

As treated herein, the V/STOL automatic approach and landing system includes the functions of:

- Navigation: Determination of aircraft position
- Guidance: Computation of desired path to destination
- Control: Closed-loop automatic flight control modes
- Display: Generation of typical AALS display functions

Functional requirements are limited to those specifically applicable to the automatic approach and landing problem. Specific constraints on the design and mechanization are:

- Designed for the YHC-1A helicopter
- Use of strapped-down sensors for navigation
- Use of strapped-down gyros for stability augmentation
- Use of available air data sensors
- Use of existing electrical input servo system
- Use of existing electric stick installation
- Use of GSN-5 and Loran-C to update navigation subsystem
- Use of display functions suitable to CRT-type display
- Use of an all-digital mechanization
- Inclusion of an alternate analog inner-loop stabilization system.

To obtain a system definition adequate for computer sizing purposes, a specific baseline system design was established. Figure 1 is a functional block diagram of the baseline system. In are provided by the navigational up-link receiver, strapped-down se on , air data and radar sensors, electric stick, rate gyros, and a pilot's s i control panel (PSCP). Outputs from the system will be navigation and s stem control information on the PSCP, guidance information and aircraft flight data to the display mechanization, and automatic flight control commands. Table 1 summarizes system input/output signals.

Computation for navigation, guidance, control, and displays will be performed in the central digital computer. Mechanization and signal flow is shown in a simplified manner in Figure 2.

Additional mechanization needs are included in Figure 2. A radar altimeter (sensor block) is required for guidance. Both on-board and telemetry instrumentation are needed for flight test. An analog attitude rate gyro and





# TABLE IAUTOMATIC APPROACH AND LANDING SYSTEMINPUT/OUTPUT SIGNAL DESCRIPTION

ierm	16/ (711	Denr - ption	Unite	Accuracy	Renge	Reenlution	Remple rate per second	Mli num dynamie range	Туре	Uaan hylamera
н,	0	Bearing to apend 1d location	44		160 con' 1	01	14	1800	digital (D/A)	guidenr e
r <sub>G</sub>	1	Pilot selected glide angle	100	0.05	0 10 20	0.01	NA	2000	ist D code wheeld	Curtone .
CISN 5 COM	10	Clora polara to digital command avalam			· • •	· · · ·		· · · .	(24) ; O yaer pulses	narigation
âh	0	Allitude command error	n		+ 200	0.5	•	400	digital (1)/A)	diepteya
* <sub>11</sub>	1	Darimatric atting	n	1	1000 10 15000	100/15	•	18000	analog (A/D)	RAY JOY
hen	1	Command altitude	n			1	NA	18000	HE D code wheels	Pap
h	0	Altitude rate command	ft/00*		±60	0.1	16	1200	digital	tioplays
hμ	1	Film-notected hover altitude	n		-1000, +10000	1	NA	11000	BCD node wheels	Pric Jr
<sup>ь</sup> нун	0	Aititude from altitude sensing system	n		-1000 to 15000	01	32	1 6000	digital (D/A)	pritr is no trapiliant
<sup>h</sup> iryn	0	Aititude rate from altitude annaing ayatem	ft/##c		+80, -170	0.1	32	1400	digital (D/A)	affe hia stopillof
h <sub>NAV</sub>	0	Altitude above sen level	n	10/1.0	-1000 10 18000	1	32	18000	Bigital	nevigetion
hNAV.	1	Pilot setting of initial altitude	n	1			NA		BCD role wheels	navigation
h <sub>NAV</sub> CP	T	Pilot setting of checkpoint altitude	n						RE D code wheeld	nevigetion
hNAV,	1	Pilot enting of landing site altitude	n						BFD code wheels	nevigation
h <sub>R</sub>	I	Reiler altimeter eltitude	n		-20 10 +200	0 5	32 .	440	- analog	
h <sub>R</sub>	•	Rodar altimotor altitude rate	ft/sec		140	0.1	37	1200	analog	800 407 8
L.	0	Longitude	108		2	0 1 600	A.	108000	digitul	nevigation
L	1	Filet acting of initial longitude	deg				NA		BCD code wheels	nevigetion
Larp	1	Pilot setting of checkpoint longitude	deg				NA		BCD code wheels	nevigation
L. fL	I	Pilot setting of landing site longitude	deg				. · i		BCD code wheels	nevigation
L	0	Latitude					44		digital	nevigation
L'to	ĩ	Pilos setting of initial latitude	deg				NA		BCD code wheels	nevigation
L	1	Pilot setting of checkpoint latitude	deg				NA		BCD code wheels	navigation
L	1	Pilot setting of landing site latitude	deg				NA		BCD code wheels	nevigation
Mode logic	1	From pilot's system control panel (PSCP)							18 discrotos	PSC P
RGO	0	Range to turn	n	110	9 to 120000	5	•	24000	digital (D/A)	guidance
-ORH	0	Horizontal range	n	±10	0 to 120000	5	•	24000	digital (D/A)	guidence
1	1	Time		0. 01		0. 01	each update	•••	digitai	nevigation
10 <sub>0</sub>	o	Time to turn		<b>0</b> , 1	0 to 2000	0. 1	16	20000	digital (D/A)	guidence
u	1	Sum of incremental changes in x-axis velocity	ft/ 00 c		-108, +380	0, 1	1624	4000	digital ctr	nevigation
5 <sub>AP</sub>	1	Pilot setting of sizepsed command	ft/sec			0.1	NA	6000		PSCP
ΨD	0	Forward velocity command	ft/sec		•	9.1	•	4980	digital (D/A)	di <b>splays</b>
•	1	Sum of incremental changes in y-axis velocity.	ft/ 99C		*100	9.5	9474	2000	digital ctr	nevigation
*0	0	Ground speed	R/sec	1	0 to 300	۰ م <sup>۱</sup>	•	3000	digital (D/A)	nevigation

Sand good by

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# TABLE I AUTOMATIC APPROACH AND LANDING SYSTEM INPUT/OUTPUT SIGNAL DESCRIPTION (CONCLUDED)

Term	In/ oui	Description	Unite	Accuracy	itange	Repolution	Sample rate per second	Minimum dynamic range	Туре	Veed by/enurce
VIAS		Indicated air openi	ft/arc		0 to 300	0.1	32	3000	analog (A/D)	pitch autopitot
v_	0	Local wind speed	ft/sec		0 to 100	0, 2	8	500	digital (D/A)	displays
U U	1	Sum of incremental changes in z-axis	R/aec		+00, -100	0. 1	1024	1600	digital etr.	navigation
x	I	Update downrange distance to landing	n	15/24	12000 10 150000	10 1		[ <sup>15000</sup> ]	f digital	navigation
×Q	0	Predicted downrange position	n	10/1\$	0 to 12000	1 }	{ <sub>16</sub> }	{ <sub>12000</sub> }	digital (D/A)	diaplaya
Y	1	Update cross-range distance to innding	rı 🛛	15/25	±12000 to ±15000	2 ]	[ <sup>68</sup> ]	∫ 15000 ]	( digital	navigation
Υ <sub>O</sub>	0	Predicted cross-range position	n	10/1\$	0 to ±12000	· }	1 10 5	24000	digital (D/A)	displays
Υ <sub>D</sub>	0	Lateral velocity command	n/aec		±100	0, 1	18	1000	digital (D/A)	displays
z	1	Update sititude above landing point	n	1	0 to 7509	1	58	7500	digital	navigation
v,	1	Ground wind apred	ft/aeu		0 to 1 <b>00</b>	0, 2	NA	500	digital	nevigation
p	1	Vehicle sideslip angle	deg		±50	0, 1	32	500	analog (A/D)	pitch autopilot
γ <sub>0</sub>	I	Ground wind direction	deg		360 con <sup>4</sup> t.	0.1	NA.	3600	digital	navigation
7	ı	Desired landing approach angle w. r. i. true north	deg	1	360 con <sup>e</sup> t	0, 1	NA	3600	digital	navigation
Ben	1	Pilot-selected checkpoint bearing	deg		360 con <sup>s</sup> t	0. 1	NA	3600	BCD code wheels	PSCP
•LC	0	Total longitudinal differential collective	in,		2, 6	0, 0007	32	4080	digital (D/A)	pitch autopilot
¢ <sub>RC</sub>	0	Cyclic yaw command	10.		3	0, 0005	32	4000	(ligital (D/A)	lateral autopilot
0 <sub>SC</sub>	0	Cyclic roll command	tn.		3	0, 000 <b>n</b>		4000	digital (D/A)	Interni autopilot
•COL	I	Electric collective stick	in.		13.8	0, 014		1000	analog (A/D)	collective autopilot
۴L	I	Electric stick input-spitch	In,		±6.1	0, 012		1000	analog (A/D)	pitch autopilot
• <sub>R</sub>	L	Electric pedal inputyaw	in.		± 2. 6	0, 005		1000	analog (A/D)	isteral sutopilot
۰ <sub>8</sub>	1	Electric stick inputroll	1n.		±0, 7	0. 01 s	32	1000	analog (A/D)	lateral autopilot
0	1	Sum of incremental changes in pitch	deg		±48 800	12 5ec	1024	8	digital ctr.	navigation
A	υ	Vehicle elevation an <mark>gle w, r, t, local</mark> horizontal	deg	0, 5	± 35	0. 06	32	1170	digital (D/A)	nevigation
<sup>e</sup> col <sub>e</sub>	υ	Collective command	in,		J. 3	0. 0009	32	4000	digital (D/A)	collective autopilot
•	1	Sum of incremental changes in roll	deg		1.*' več	18 890	1024		digital ctr.	navigation
+	0	Vehicle roll angle	dog	0, 0	±60	0, 06	32	1670	digital (D/A)	navigation
٧	L	Sum of incremental changes in yaw	deg		146 aec	12 5ec	1024		digital ctr.	nevigation
۲	0	Vehicleheading w.r.t. true north	deg	1	360 con't	0, 1	16	3800	digital	navigation
с <b>т</b> 1	0	Checkpoint heading error	deg		20	0. 01	16	2000	digital	guidance
Y <sub>c</sub>	•	Pilot-selected heading	døg		380 con' t	0. 1	NA	3800	BCD code wheels	PSCP
۳ <sub>D</sub>	0	Heading command	deg		360 con't	0, 1		3800	digital (D/A)	displays
Mode logic	1	Stick force switches					]		8 discretes	electric stick
Mode logic	-	Beep trim							4 discretes	electric stick

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analog compensation is included for the alternate inner-loop stabilization mechanization. (Appendix A contains an analog rate gyro recommendation.) Since both the strapped-down gyros and accelerometers output a pulse rate signal form, a method of converting to a whole word digital format is needed; this is labeled a "preprocessor". A "signal conditioner" is included to provide electrical signal matching between system imput (sensor output, etc.) and computer subsystem input.

Complete in-flight control is provided by the PSCP. The baseline system definition includes the following functions in the panel:

• <u>Navigation</u>

Alignment start

Navigation engaged

Automatic update on/off

Initial position input (latitude, longitude, altitude)

Manual update input (latitude, longitude, altitude)

Automatic update (GSN-5/Loran-C)

Landing location input (latitude, longitude, altitude) Readout of current position or any input

• <u>Guidance</u>

Guidance mode selection

Input of pilot selectable quantities

Readout of selected input

• <u>Control</u>

Electric stick on/off Stability augmentation on/off Attitude hold engage Velocity command engage Automatic guidance engage Mode status

System Status

Power on Instrumentation

On-board on Telemetry on Computer ready Servos aligned Baseline panel functions are defined as a result of subsystem requirements (input, control, and status indication).

Because of the need for safety-of-flight assurance, system design is based on use of a safety pilot. The YHC-1A is normally dual-control. The right side has an electric stick installed for AALS evaluation pilot use. Normal controls exist on the left side for use by the safety pilot. Whenever the electric stick is activated (or automatic control modes are engaged), the left hand stick will follow all control motions. The safety pilot will be able to use the motion of his stick as a primary indication of safe automatic control system performance. Emergency electric stick and automatic control disengagement is provided to both pilots with switches mounted on each stick. Electric stick status (on/off) presented to the safety pilot will help provide control coordination between the pilots.

Baseline AALS requirements are given as part of each subsystem discussion in the sections that follow. Prior to further development, firm system requirements should be established in terms of both performance and mechanization.

Ground support concepts and equipment requirements also must be established to assure a compatible system mechanization.

#### NAVIGATION

This section describes inertial navigation equations. Navigation simply means maintaining a knowledge of vehicle position, velocity, and attitude based on the output of the inertial sensors, accelerometers and gyros, and altimeter. These equations were adapted largely from material supplied by NASA-ERC. Although useful to the baseline definition, considerable simplification can probably be made for flight test use.

The navigation equations are divided into 19 computation sections. Each section describes the equations and the frequency and precision with which they should be evaluated, and lists explanatory and critical remarks where appropriate. An attempt is made to keep the notation consistant with the material supplied by NASA- $\Sigma$ RC, insofar as possible.

The calculations described by these equations begin (logically) after introduction into the computer of all initial conditions, constants, inertial sensor pulse counts, and the altimeter output. They carry the calculations through the point of computing the values of the position, velocity, and attitude variables.

1.	Accelerometer	Bias and	Scale	Factor	Computation
----	---------------	----------	-------	--------	-------------

$$K_{0i} = K_{0i} + \Delta K_{0i} \Delta t$$
$$K_{1i} = K_{1i} + \Delta K_{1i} \Delta t$$

Input:

 $K_{0i}$  = accelerometer bias

 $K_{1i}$  = accelerometer scale factor

Constants:  $\Delta K_{0i} = (DR_{K_0})_i$  bias rate (constant)

$$\Delta K_{1i} = \left( \frac{DR}{\Delta K_i/K_1} \right)_i$$
 scale factor rate (constant)

Output:

K<sub>0i</sub> = accelerometer bias

 $K_{1i}$  = accelerometer scale factor

Frequency: Very slow; ∆t could be as large as several seconds
Precision: 20-bit accuracy

# 2. Accelerometer Bias and Scale Factor Compensation

$$C'_{0i} = C_{0i}/K_{1i} - K_{0i}$$

where i = 1, 2, 3.

Input:	$C_{0i}$ i = 1, 2, 3 = uncompensated acceleration
	$K_{0i}$ i = 1, 2, 3 = bias (from 1)
	$K_{1i}^{i}$ i = 1, 2, 3 = scale factor (from 1)
Output:	$C'_{0i}$ i = 1, 2, 3 = compensated acceleration
Frequency:	128 times per second
Precision:	20-bit accuracy

3. Accelerometer Cross-Axis Compensation

$$Q_{1} = C'_{01} - K_{41}C'_{02} - K_{61}C'_{03}$$
$$Q_{2} = -K_{62}C'_{01} + C'_{02} - K_{42}C'_{03}$$
$$Q_{3} = -K_{43}C'_{01} - K_{63}C'_{02} + C'_{03}$$

Input:  $C'_{0i}$  i=1,2,3 = uncompensated acceleration (from 2) Constants:  $K_{4i}$ ,  $K_{6i}$  = cross-axis compensation constants Output:  $Q_i$  i=1,2,3 = compensated acceleration

Frequency: 128 times per second

Precision: 20-bit accuracy. Since the K's are small, single-precision products should suffice.

## 4. Accelerometer Nonlinearity Compensation

$$\Delta \mathbf{v}_{i} = \mathbf{Q}_{i} \left[ 1 - \mathbf{Q}_{i} (\mathbf{K}_{2i} + \mathbf{Q}_{i} \mathbf{K}'_{3i}) \right] \Delta t_{c}$$

where i = 1, 2, 3.

Input:  $Q_i i=1, 2, 3$  = uncompensated acceleration (from 3) Constants:  $K_{2i} i=1, 2, 3$  = nonlinear compensation constants  $K'_{3i} = K_{3i} - 2K^2_{2i}$  = nonlinear compensation constants Output:  $\Delta v_i$  = incremental velocity (accelerometer axis components)

Frequency: 128 times per second

Precision: 20 bits. Since both constants are small, single-precision products should suffice.

5. Angular Environmental Compensation

 $\Delta \mathbf{v}_{c1} = \Delta \mathbf{v}_{1} - \left[\Delta \hat{\theta}_{1} \Delta \hat{\theta}_{2} \mathbf{p}_{2} - (\Delta \hat{\theta}_{2}^{2} + \Delta \hat{\theta}_{2}^{2})\mathbf{p}_{1} - \Delta \hat{\theta}_{1} \Delta \hat{\theta}_{2} \mathbf{p}_{3}\right] / \Delta t$  $+ \Delta \omega_{2} \mathbf{p}_{3} + \Delta \omega_{3} \mathbf{p}_{2}$  $\Delta \mathbf{v}_{c2} = \Delta \mathbf{v}_{2} - \left[\Delta \hat{\theta}_{3} \Delta \hat{\theta}_{2} \mathbf{p}_{3} + \Delta \hat{\theta}_{1} \Delta \hat{\theta}_{2} \mathbf{p}_{1} - (\Delta \hat{\theta}_{3}^{2} + \Delta \hat{\theta}_{1}^{2})\mathbf{p}_{2}\right] / \Delta t$  $+ \Delta \omega_{3} \mathbf{p}_{1} + \Delta \omega_{1} \mathbf{p}_{3}$  $\Delta \mathbf{v}_{c3} = \Delta \mathbf{v}_{3} - \left[\Delta \hat{\theta}_{1} \Delta \hat{\theta}_{3} \mathbf{p}_{1} + \Delta \hat{\theta}_{2} \Delta \hat{\theta}_{3} \mathbf{p}_{2} - (\Delta \hat{\theta}_{1}^{2} + \Delta \hat{\theta}_{2}^{2})\mathbf{p}_{3}\right] \Delta t$  $- \Delta \omega_{1} \mathbf{p}_{2} + \Delta \omega_{2} \mathbf{p}_{1}$ 

Input:

.

 $\Delta v_i$  i=1, 2, 3 = uncompensated velocity increment (from 4)  $\Delta \hat{\theta}_i$  i=1, 2, 3 = angular increment (from 7)

 $\Delta \omega_i$  i=1, 2, 3 = angular velocity increment (from 7)

Constants:  $p_i$  i =1, 2, 3 = accelerometer offset constants Output:  $\Delta v_{ci}$  i=1, 2, 3 = compensated velocity increments Frequency: 128 times per second

Precision: 20 bits. Since compensation will be small, single-precision products should suffice.

Remarks: These are the equations supplied by ERC. If all three accelerometers are assumed offset from the vehicle-fixed reference point, then nine constants should be used;  $p_1, p_2, r_3$  of the first equation describing the location of the first accelerometer;  $p_1, p_2, p_3$  of the second equation describing the location of the second accelerometer;  $p_1, p_2, p_3$  of the third equation describing the location of the third accelerometer. Since selection of the reference point is entirely arbitrary, one of the equations can be completely eliminated by choosing it to be the c.g. of the sensitive element of one of the accelerometers in the block and the orientation of the block relative to the body axes, up to four of the remaining six constants may be eliminated by judicious choice.

## 6. Accelerometer-to-Body Axis Transformation



Frequency: 128 times per second

Precision: 20 bits

Remarks: Assuming the accelerometer axes to be nominally aligned with the body axes, equations of the form of section 3 may be used. In point of fact, these calculations could be accomplished in section 3 by suitably redefining the constants used there and this section completely eliminated. 7. Angular Increment, Rate and Acceleration Computation

$$\Delta \hat{\theta}_{i} = \sum_{k=1}^{8} (\Delta \theta_{i})k$$

$$\omega_{i}(t) = \sum_{k=1}^{8} W_{1k} (\Delta \theta_{i})k$$

$$\omega_{i}(t+\Delta t) = \sum_{k=1}^{8} W_{2k} (\Delta \theta_{i})k$$

$$\Delta \omega_{i} = \omega_{i}(t + \Delta t) - \omega_{i}(t)$$

k =1

Input:  $(\Delta \theta_i) k \ k=1,2,...8$  = angular increment over 1/1024 sec Constants:  $W_{1k}, W_{2k}, k=1,2,...8$  = rate filter weights (constants) Output:  $\Delta \hat{\theta_i}$  = angular increments over 1/128 sec  $\omega_i(t), \omega_i(t+\Delta t)$  = angular rate at beginning and end of 1/128-sec interval

 $\Delta \omega_i$  = angular acceleration over 1/128-sec interval (times  $\Delta t$ )

Frequency: 128 times per second

Precision: 24 bits for  $\omega$ . Only about 8 bits for  $\Delta \hat{\theta}$ .

Remarks: It is felt that calculation of the rates is not only unnecessary but error producing. See section 11. 8. Gyro Drift Computation

$$\begin{bmatrix} D_{1} \\ D_{2} \\ D_{3} \end{bmatrix} = \begin{bmatrix} R_{1} \\ R_{2} \\ R_{3} \end{bmatrix} + \begin{bmatrix} B_{11} & -B_{31} & B_{21} \\ B_{22} & B_{12} & -B_{32} \\ B_{23} & B_{33} & B_{13} \end{bmatrix} \begin{bmatrix} C'_{01} \\ C'_{02} \\ C'_{03} \end{bmatrix} + \\ \begin{bmatrix} 0 & -M'_{31} & M'_{21} \\ M'_{22} & 0 & -M'_{32} \\ M'_{23} & M'_{33} & 0 \end{bmatrix} \begin{bmatrix} \Delta \hat{\theta}_{1} \\ \Delta \hat{\theta}_{2} \\ \Delta \hat{\theta}_{3} \end{bmatrix} + \begin{bmatrix} J'_{1} & 0 & 0 \\ 0 & J'_{2} & 0 \\ 0 & 0 & J'_{3} \end{bmatrix} \begin{bmatrix} \Delta \omega_{1} \\ \Delta \omega_{2} \\ \Delta \omega_{3} \end{bmatrix} + \\ \begin{bmatrix} C_{11} & -C_{31} & 0 \\ 0 & C_{12} & C_{32} \\ 0 & C_{33} & C_{13} \end{bmatrix} \begin{bmatrix} C'_{01}^{2} \\ C'_{02}^{2} \\ C'_{02}^{2} \\ C'_{03}^{2} \end{bmatrix} + \begin{bmatrix} -C_{51} & 0 & -C_{41} \\ -C_{42} & -C_{52} & 0 \\ C_{43} & 0 & C_{53} \end{bmatrix} \begin{bmatrix} C'_{02} & C'_{03} \\ C_{01} & C'_{02} \end{bmatrix} + \\ \begin{bmatrix} Q'_{11} & Q'_{31} & 0 \\ 0 & Q'_{12} & Q'_{32} \\ 0 & Q'_{33} & Q'_{11} \end{bmatrix} \begin{bmatrix} \Delta \hat{\theta}_{1}^{2} \\ \Delta \hat{\theta}_{2}^{2} \\ \Delta \hat{\theta}_{3}^{2} \end{bmatrix} + \\ \begin{bmatrix} 0 & 0 & -Q'_{41} \\ -Q'_{42} & 0 & 0 \\ Q'_{43} & 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta \hat{\theta}_{2} & \Delta \hat{\theta}_{3} \\ \Delta \hat{\theta}_{2} & \Delta \hat{\theta}_{3} \end{bmatrix}$$

Input: 
$$C'_{0i}$$
 = acceleration (from 2)  
 $\Delta \hat{\theta}_{i}$  = angular increment (from 7)  
 $\Delta \omega_{i}$  = angular acceleration (from 7)  
Constants:  $B_{1i}$ ,  $B_{2i}$ ,  $B_{3i}$ ,  $M'_{2i}$  =  $M_{2i}/\Delta t$ ,  $M'_{3i}$  =  $M_{3i}/\Delta t$   
 $J'_{i}$  =  $J_{i}/\Delta t$ ,  $C_{1i}$ ,  $C_{5i}$ ,  $C_{4i}$ ,  $C_{5i}$ ,  $Q'_{1i}$  =  $Q_{1i}/\Delta t^{2}$   
 $Q'_{3i}$  =  $Q_{3i}/\Delta t^{2}$ ,  $Q'_{4i}$  =  $Q_{4i}/\Delta t^{2}$   
Output:  $D_{i}$  i=1, 2, 3 = gyro drift rate

Output:  $D_i = 1, 2, 3 = gyro drift rate$ Frequency: 128 times per secondPrecision: 10 bits

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## 9. Gyro Drift Compensation

$$\omega_{ci}(t) = \omega_{i}(t) - D_{i}$$
$$\omega_{ci}(t+\Delta t) = \omega_{i}(t+\Delta t) - D_{i}$$

where i=1, 2, 3.

Input:

 $\omega_i(t), \omega_i(t+\Delta t) =$  uncompensated angular velocity (from 7)

 $D_i = gyro drift rate (from 8)$ 

Output:  $\omega_{ci}(t)$  = compensated angular velocity

Frequency: 128 times per second

Precision: 24 bits

Remarks: It is felt that gyro drift compensation could be performed at 1/4 to 1/8 of the above frequency with no loss of accuracy. This is based only on the assumption of gross rates of no more than 60 deg/sec and vibration that causes reasonable drift rates (say 10 deg/hr). The pulse counts and their products on which the compensation is based can be accumulated over a longer period than indicated above, and the compensation can be calculated and applied at the angular level rather than the angular rate level.

10. Gyro-to-Body Axis Transformation

$$\underline{\omega}^{B}(t) = T^{BG} \underline{\omega}^{G}(t)$$

Input:

$$\underline{\omega}^{\mathbf{B}(t+\Delta t)} = \mathbf{T}^{\mathbf{B}\mathbf{G}} \, \omega^{\mathbf{G}(t+\Delta t)}$$

$$\underline{\omega}^{\mathbf{G}(t)} = \begin{bmatrix} \omega_{c1}(t) \\ \omega_{c2}(t) \\ \omega_{c3}(t) \end{bmatrix}$$
angular v
frame
$$\underline{\omega}^{\mathbf{G}(t+\Delta t)} = \begin{bmatrix} \omega_{c1}(t+\Delta t) \\ \omega_{c2}(t+\Delta t) \\ \omega_{c3}(t+\Delta t) \end{bmatrix}$$

angular velocity in gyro input axis frame

Constants: 
$$T^{BG} = gyro \text{ axis-to-body axis transformation matrix}$$
  
Output:  $\underline{\omega}^{B}(t) = \begin{bmatrix} \omega_{1} \\ \omega_{2} \\ \omega_{3} \end{bmatrix}$  angular velocity in body axes  
 $\underline{\omega}^{B}(t+\Delta t) = \begin{bmatrix} \omega_{1} \\ \omega_{2} \\ \omega_{3} \end{bmatrix}$ 

Precision: 24 bits

Remarks:

Assuming the gyro axes are nominally aligned with the body axes, this function can be accomplished by suitably redefining the constants in the third term of the equation of section 8, and this calculation eliminated entirely.

11. Attitude Matrix Algorithm

$$\text{TEMP} \leftarrow \begin{bmatrix} -\Delta t [\omega_2 \omega_2' + \omega_3 \omega_3'] & -(\omega_3 + \omega_3') + \Delta t \omega_2 \omega_1' & (\omega_2 + \omega_2') + \Delta t \omega_3 \omega_1' \\ (\omega_3 + \omega_3') + \Delta t \omega_1 \omega_2' & -\Delta t [\omega_3 \omega_3' + \omega_1 \omega_1'] & -(\omega_1 + \omega_1') + \Delta t \omega_3 \omega_2' \\ -(\omega_2 + \omega_2') + \Delta t \omega_1 \omega_3' & (\omega_1 + \omega_1') + \Delta t \omega_2 \omega_3' & -\Delta t [\omega_1 \omega_1' + \omega_2 \omega_2'] \end{bmatrix}$$

$$TEMP = \frac{1}{2} \Delta t T^{IB}(TEMP)$$
$$T^{IB} = T^{IB} + TEMP$$

Input:

 $\mathbf{T}^{\mathbf{IB}}$ 

= body-to-inertial transformation matrix, last
value (from 11 or 12)

$$\frac{\omega^{B}(t)}{\omega_{2}} = \begin{bmatrix} \omega_{1} \\ \omega_{2} \\ \omega_{3} \end{bmatrix}^{2}$$
angular velocity at beginning and end of interval (from 10)

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Output:  $T^{IB}$  = body-to-inertial transformation matrix, new value Frequency: 128 times per second

Precision: 24 bits

Remarks: It is strongly felt that basing the attitude algorithm on numerical integration of the numerically differentiated output of integrating devices (pulse rebalanced gyros) is not only unnecessarily complicated but a potential source of serious error. The basic truncation error of this algorithm is no better (and is in fact slightly worse) than that of the conventional secondorder attitude algorithm described by

$$\mathbf{T} = \mathbf{T} + \mathbf{T} \left[ \Delta \Theta - 1/2 \Delta \Theta^2 \right],$$
$$\Delta \Theta = -\Delta \Theta^{\mathbf{T}} = \begin{bmatrix} 0 & -\Delta \hat{\theta}_3 & \Delta \hat{\theta}_2 \\ \cdot & 0 & -\Delta \hat{\theta}_1 \\ \cdot & \cdot & 0 \end{bmatrix}$$

This algorithm has, in addition, the inevitable error associated with differentiating quantized data by whatever method. Rate errors that are acceptable for compensation or control can easily be accumulated into attitude errors that are entirely unacceptable. The more severe the angular environment, the more serious the problem. The derivation of rates is <u>not</u> necessary for maintaining attitude reference and is therefore not desirable for that purpose.

12. Attitude Matrix Orthonormalization

TEMP <sub>11</sub>	-	T <sup>IB</sup> <sub>22</sub>	$\mathtt{T}^{\mathrm{IB}}_{33}$	-	$\mathtt{T}_{23}^{\mathrm{IB}}$	$\mathtt{T}^{\mathrm{IB}}_{32}$
TEMP <sub>12</sub>	-	$T_{23}^{\mathrm{IB}}$	$\mathtt{T}^{\mathrm{IB}}_{31}$	-	$\mathtt{T}_{21}^{\mathrm{IB}}$	$\mathtt{T}_{33}^{\mathbf{IB}}$
TEMP <sub>13</sub>		$T_{21}^{\mathrm{IB}}$	$T^{\mathrm{IB}}_{32}$	-	$\mathtt{T}_{22}^{\mathrm{IB}}$	$T_{31}^{IB}$
TEMP <sub>21</sub>		T <sup>IB</sup> <sub>32</sub>	$T_{13}^{IB}$	-	$\mathtt{T}^{\mathbf{IB}}_{32}$	T <sup>IB</sup> <sub>11</sub>
TEMP22	2	$T_{33}^{IB}$	${\tt T}_{11}^{\rm IB}$	-	$\mathbf{T_{31}^{IB}}$	$T_{13}^{IB}$
TEMP <sub>23</sub>		$T_{31}^{IB}$	$\mathbf{T_{12}^{IB}}$	•	$\mathbf{T}_{32}^{\mathbf{IB}}$	$\mathbf{T}_{11}^{\mathrm{IB}}$

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TEMP <sub>31</sub>		T <sup>JB</sup> <sub>12</sub>	$T_{23}^{IB}$	-	$_{1}^{\mathrm{IB}}$	$\mathbf{T}_{22}^{\mathbf{IB}}$
TEMP <sub>32</sub>	=	T <sup>IB</sup> <sub>13</sub>	${\rm T}_{21}^{\rm IB}$	-	$\mathtt{T}_{11}^{\mathrm{IB}}$	т <mark>ІВ</mark> 23
TEMP <sub>33</sub>		T <sup>IB</sup> <sub>11</sub>	$T_{22}^{\mathbf{IB}}$	-	$T_{12}^{\mathrm{IB}}$	$T_{21}^{IB}$

$$\text{TEMP} = 1/2 [\text{T}^{\text{IB}} + \text{TEMP}]$$

T <sup>IB</sup> <sub>11</sub>		temp <sub>i1</sub>		TEMP <sub>i1</sub>
$T_{i2}^{IB}$	=	temp <sub>i2</sub>	+ $1/2 (1 - \text{TEMP}_{i1}^2 - \text{TEMP}_{i2}^2 - \text{TEMP}_{i3}^2)$ .	TEMP <sub>i2</sub>
T <sup>IB</sup> i3		temp <sub>i3</sub>		TEMP <sub>i3</sub>

where i=1, 2, 3.

Input:  $T^{IB}$  = body-to-inertial transformation matrix (from 11) Output:  $T^{IB}$  = body-to-inertial transformation matrix (from 11)

Frequency: 16 times per second

Precision: 24 bits

Remarks:

Since the second term of the last equation is a small correction, single-precision products will suffice for that equation.

The frequency of 16 times per second is much higher than necessary. Orthonormalization once every several seconds should be entirely sufficient.

The final equation above results from replacing the inverse of a square root of a quantity nominally unity by the first-order Taylor series of this function. Use of a first-order expansion is justified by the fact that the orthonormalization algorithm itself is first order. It is of interest to note that all three rows have the same scale factor error (to within first-order terms). It can be shown that any nonsingular matrix T can be expressed as

$$T = (I + \Phi)R$$

where  $\Phi$  is symmetric and K is a rotation matrix, the one closest to T in the sense of least squares. Applying the first three equations of this orthonormalization algorithm to T produces

$$TEMP = [1 + 1/2 tr(\Phi)]R + 1/4 \Psi R$$

where  $\Psi$  is a symmetric matrix depending on  $\Phi$  only and secondorder in  $\Phi$ . It is given in tensor notation by

6)

$${}^{\Psi}$$
ij =  ${}^{\varepsilon}$ imn  ${}^{\varepsilon}$ jrs  ${}^{\Phi}$ mr  ${}^{\Phi}$ ns

so that, for example,

$$\Psi_{11} = 2(\Phi_{22} \Phi_{33} - \Phi_{23}^2)$$

and

$$\Psi_{12} = 2(\Phi_{23} \Phi_{12} - \Phi_{21} \Phi_{33})$$

13. Velocity Increment Resolution

Input: 
$$\Delta \mathbf{y}^{\mathbf{B}} = \begin{bmatrix} \Delta \mathbf{v}_{c1}^{\mathbf{B}} \\ \Delta \mathbf{v}_{c2}^{\mathbf{B}} \\ \Delta \mathbf{v}_{c3}^{\mathbf{B}} \end{bmatrix}^{\mathbf{z}} = \text{velocity increment in body axes (from 1)}$$
$$\mathbf{T}^{\mathbf{IB}} = \text{body-to-inertial transformation matrix (from 1)}$$
$$\mathbf{Output:} \quad \Delta \mathbf{y}^{\mathbf{I}} = \begin{bmatrix} \Delta \mathbf{v}_{1}^{\mathbf{I}} \\ \Delta \mathbf{v}_{2}^{\mathbf{I}} \\ \Delta \mathbf{v}_{3}^{\mathbf{I}} \end{bmatrix}^{\mathbf{z}} = \text{velocity increment in inertial axes}$$

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Frequency: 128 times per second

Precision: 20 bits

Remarks: Better error characteristics result if the time intervals over which  $\Delta v^B$  is accumulated and  $T^{IB}$  is updated are staggered. In that way, the incremental velocity is transformed by the matrix associated with the midpoint of the interval over which it was accumulated.

14. Inertial Position, Velocity Computation

 $r_{i} = r_{i} + \frac{1}{2} \Delta t v_{i}$   $v_{i} = v_{i} + \Delta t G_{i} + \Delta v_{i}^{I}$   $r_{i} = r_{i} + \frac{1}{2} \Delta t v_{i}$ 

where i=1, 2, 3

Input:

 $r_i = inertial cartesian components of position$ 

= inertial cartesian components of inertial velocity

 $G_i$  = components of gravitaticnal acceleration (from 15)  $\Delta v_i^J$  = inertial components of incremental velocity (from 13)

Output:

v<sub>i</sub>

r<sub>i</sub>

v<sub>i</sub>

Frequency: 64 times per second

Precision: 30 to 32 bits

Remarks: Updating position twice with first-order formulas is equivalent to updating it with second-order formulas.

Performing basic navigation in inertial coordinates has the disadvantage of a large dynamic range for the state variables and more complicated output transformations. Navigating in local vertical coordinates should be considered as an alternative.

			·
			15. Gravity Computations
			$r_{o} = r_{e} + (r_{ee}) (S2)$
			$r_{G} = r_{o} + h_{a}$
			$RI = 1/r_G$
			RI2 = (RI) (RI)
			RI3 = (RI2) (RI)
			$P_{0} = (G) (RI3)$
			$\lambda_{0} = (KJ) (RI2)$
			$\mu_0 = (5) (S2)$
			$P_{xy} = 1 + \lambda_0 (1 - \mu_0)$
			$P_{z} = P_{xy} + (2) (\lambda_{o})$
			$Temp = (P_0) (P_{xy})$
	·		$G_1 = (Temp)(r_1)$
			$G_2 = (Temp)(r_2)$
			$G_3 = (P_0) (P_2) (r_3)$
Input:	r <sub>i</sub>	=	inertial position (from 14)
	ha	8	altitude above geoid (from altimeter)
	S2	H	square of sine of latitude (from 17)
Constants:	re	8	equatorial radius
	r <sub>ee</sub>	2	geoid flattening parameter
	G, KJ	=	gravitational parameters
Cutput:	G <sub>i</sub>	3	gravitational acceleration components
	ro	2	local earth radius
	<sup>r</sup> G	=	gravitational radius (based on position and altimeter)
Frequency:	16 tin	nes	per second

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#### **Precision**: 19 to 24 bits

#### Remarks:

These equations embody one approach to the problem of altitude divergence control. By basing gravity on the altimeter value of altitude rather than the inertial value of altitude, the vertical channel is given the same characteristics as the horizontal channels, that is, conditional stability and the Schuler frequency.

An alternative approach which should be considered is to treat the altimeter data as augmentation in the same way that radar or Loran data is treated. Gravity is based on the inertial position, but the altimeter altitude and the inertial altitude are compared. The discrepancy is fed back at the acceleration level for restoring and at the velocity level for damping. This approach has the advantage that a stable filter can be designed which takes altimeter error characteristics into consideration.

16. Geographic Computer

R2 xy	=	$r_1^2 + r_2^2$
r <sub>xy</sub>	ŧ	$1/2 (r_{xy} + R2_{xy}/r_{xy})$
tan λ	=	$r_{2}/r_{1}$
tan L g	=	r <sub>3</sub> /r <sub>xy</sub>
D	=	(2e) r <sub>3</sub> r <sub>xy</sub> /R2
λ	=	$\tan^{-1}(\tan \lambda)$
Lg	=	tan <sup>-1</sup> (tan L <sub>g</sub> )
L <sub>t</sub>	#	$L_{g} + D$
r	=	$\lambda + \ell_o - \omega_e t$
h	=	r - r <sub>o</sub>
<b>ນ</b> ໍ	=	$(r_1 v_2 - r_2 v_1)/R2_{xy}$
i	=	$\dot{\lambda} - \omega_{e}$
v	=	$(r_1 v_1 + r_2 v_2 + r_3 v_3)/r$
i,	=	$(v_3/r_{xy}) - (v/r) (tan Lg)$

r

	$\dot{D} = (2e) \dot{L}_{g} [1 - 2 (S2)]$		
	$\dot{L}_{t} = \dot{L}_{g} + \dot{D}$		
	$\dot{h} = v$		
Input:	$r_i = inertial position (from 14)$		
	v <sub>i</sub> = inertial velocity (from 14)		
	r = magnitude of position vector (from 17)		
	R2 = square of r (from 17)		
	$r_{xy} = \sqrt{r_1^2 + r_2^2} $ (from 16)		
	S2 = square of sine of latitude (from 17)		
	t = time		
Constants:	(2e) = geoid flattening parameter		
	$\omega_{e}$ = earth angular velocity		
	$\ell_{o}$ = reference longitude		
Output:	r		
	l = longitude		
	L <sub>t</sub> = geodetic latitude		
	h = inertial altitude from geoid		
	h = altitude rate		
	L <sub>g</sub> = geocentric latitude		
	L <sub>g</sub> = geocentric latitude rate		
	L <sub>t</sub> = geodetic latitude rate		
Frequency:	16 times per second		
Precision;	requirements unknown		
Remarks:	Precision requirements are governed principally by resolution requirements of guidance and display functions		

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The second equation embodies a method of bypassing the extraction of a square root.

17. Euler Angle Computation  $R2 = \sum_{i=1}^{3} r_i^2$  $r = 1/2 (r + \frac{R2}{r})$  $W_{i} = r_{i}/r$ , where i=1, 2, 3  $= W_3^2$ **S2**  $\cos L = 1/2 \left( \cos L + \frac{1 - S2}{\cos L} \right)$  $V_i = W_i / \cos L$ , where i=1, 2  $U_i = W_3 V_i$ , where i=1,2  $n_{j} = T_{ij}^{IB} W_{i}$ , where i=1, 2, 3 and j=1, 2, 3  $\cos\theta\sin\psi = -T_{11}^{IB}V_2 + T_{21}^{IB}V_1$  $\cos \theta \cos \psi = -T_{11}^{IB} U_1 - T_{21}^{IB} U_2 + T_{31}^{IB} \cos L$  $\theta = \sin^{-1} \left( n_1 \right) \quad -90^\circ < \theta < +90^\circ$  $\phi = \tan^{-1}\left(\frac{n_2}{n_2}\right) -90^\circ < \phi < +90^\circ$  $\psi = \tan^{-1} \left( \frac{\cos \theta \sin \psi}{\cos \theta \cos \psi} \right) \quad 0 \le \psi \le 360^{\circ}$ = inertial position (from 14) r, TIB = attitude matrix (from 11) = magnitude of position vector (from 17)  $\cos L = \cos ine of (geocentric) latitude (from 17)$ 

Input:

Output:  $\theta$  = elevation angle

- $\phi$  = roll angle
- $\psi$  = azimuth angle

S2 = square of sine of latitude

R2 = square of r

r = magnitude of position vector

 $\cos L = \cos n \theta$  of latitude

Frequency: Roll, elevation, 32 times per second

Azimuth, 16 times per second

Precision: 16 to 18 bits

**Remarks:** The second equation bypasses the extraction of a square root. Similarly, the fifth equation calculates a cosine as the square root of the square of the cosine.

> If navigation were performed in local vertical coordinates, the attitude algorithm would be arranged to produce the body-tolocal vertical transformation which would then contain all the desired attitude information.

#### 18. Preflight Attitude Alignment

The alignment scheme outlined here is self-contained. A scheme using optical input for azimuth alignment would entail a more complicated interface with the computer and would involve somewhat more calculation. It would, however, reduce alignment error and probably require less time to accomplish. In spite of these facts, the scheme below is recommended for the first stages of AALS development.

The scheme consists of two parts, an initial alignment and a final alignment. During the initial alignment, body motion is ignored and sensor data is collected on which a body-to-local vertical transformation is based. During the final alignment, body motion is accounted for by attempting to maintain attitude reference to the local vertical. Level error is detected by measuring the acceleration in the nominally level channels, and azimuth error is detected by measuring the vehicle's secular rotation rate about the nominally east direction, the strap-down form of gyro compassing.

Initial alignment. -

1) Sum  $\Delta \theta$ 's and  $\Delta V$ 's over time  $t_1$ :

$$V_{i} = V_{i} + \Delta V_{i}^{B}$$
  
$$\theta_{i} = \theta_{i} + \Delta \theta_{i}^{B}$$
  
$$i=1, 2, 3$$

2) When complete, compute

$$g_i = V_i/t_1$$
  
 $\omega_i = \theta_i/t_1$   
 $i=1, 2, 3$ 

- 3) Compute direction cosine matrix, T:
  - $T_{3i} = -k_g g_i$  i=1,2,3

$$T_{2i} = \omega_{(i+1)} T_{3(i+2)} - \omega_{(i+2)} T_{3(i+1)}$$
   
  $i=1, 2, 3$ 

$$T_{2i} \in k_{\omega} T_{2i}$$
 i=1,2,3

$$T_{1i} = T_{2(i+1)} T_{3(i+2)} - T_{2(i+2)} T_{3(i+1)}$$
 i=1, 2, 3

Orthonoralize T. - This procedure is described in section 12. Final alignment. -

1) Initialize k=0.

- 2) Update T with gyros as when navigating.
- 3) Maintain local vertical over a  $\Delta t$  time by computing

$$\theta_{E} = 0$$

$$\theta_{N} = \omega_{N} \cdot \Delta t$$

$$\theta_{D} = \omega_{D} \Delta t$$

$$\Phi = \begin{bmatrix} 0 & -\phi_{D} & \phi_{E} \\ \phi_{D} & 0 & -\phi_{N} \\ -\phi_{E} & \phi_{N} & 0 \end{bmatrix}$$

$$T \in T - \Phi T$$

4) Sum  $\Delta V$ 's in local vertical

$$\begin{pmatrix} \mathbf{v}_{\mathbf{N}} \in \mathbf{v}_{\mathbf{N}} + \sum_{j} \mathbf{T}_{1j} \Delta \mathbf{v}_{j}^{\mathbf{B}} \\ \mathbf{v}_{\mathbf{E}} \in \mathbf{v}_{\mathbf{E}} + \sum_{j} \mathbf{T}_{2j} \Delta \mathbf{v}_{j}^{\mathbf{B}} \end{pmatrix}$$

5) Every  $t_2$  seconds compute:

$$\theta_{E} = \sum_{j} T_{3j} T_{1j}$$

$$k = k + 1$$

$$Y_{1} \in Y_{1} + \theta_{E}$$

$$Y_{2} \in Y_{2} + k\theta_{E}$$

$$Y_{3} \in Y_{3} + V_{N}$$

$$Y_{4} \in Y_{4} + kV_{N}$$

$$Y_{5} \in Y_{5} + V_{E}$$

$$Y_{6} \in Y_{6} + kV_{E}$$

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6) When k=n, compute:

$$\begin{cases} \varphi_{\rm D} = k_{\rm D1} (k_{\rm D2} Y_2 - Y_1) \\ \varphi_{\rm E} = k_{\rm V1} (k_{\rm V2} Y_4 - Y_3) \\ \varphi_{\rm N} = k_{\rm V1} (k_{\rm V2} Y_6 - Y_5) \end{cases}$$

7) Correct the alignment

$$T = T - \Phi T$$

8) Convert to space stable

$$T \in T^{IV} T$$

9) Initialize position, velocity, orthonormalize and navigate.

Remarks: The equations involving the running index k,  $k=1, 2, \dots n$ , produce the least-squares estimate of the (assumed constant) horizontal acceleration and angular rate about East.

 $\mathbf{T}^{\mathbf{LV}}$  is the precalculated local vertical-to-inertial transformation based on the vehicle position.

19. Guidance Input Calculations

 $S_{IE} = S_{IE} + \Delta t \quad \omega_e C_{IE}$   $C_{IE} = C_{IE} - \Delta t \quad \omega_e S_{IE}$   $r_1' = C_{IE} r_1 + S_{IE} r_2$   $r_2' = -S_{IE} r_1 + C_{IE} r_2$   $\Delta r_1 = r_1' - R_1$   $\Delta r_2 = r_2' - R_2$   $\Delta r_3 = r_3' - R_3$ 

$$\begin{pmatrix} N_{A} \\ E_{A} \\ h_{UD} \end{pmatrix} = \begin{pmatrix} T^{RN, E} \\ T^{RN, E} \end{pmatrix} \begin{pmatrix} \Delta r_{1} \\ \Delta r_{2} \\ \Delta r_{3} \end{pmatrix}$$
$$v_{R1} = v_{1} + \omega_{e} r_{2}$$
$$v_{R2} = v_{2} - \omega_{e} r_{1}$$
$$v_{R1}' = C_{IE} v_{R1} + S_{IE} v_{R2}$$
$$v_{R2}' = -S_{IE} v_{R1} + C_{IE} v_{R2}$$
$$\begin{pmatrix} \tilde{u}_{G} \\ \tilde{v}_{i,j} \\ h_{UD} \end{pmatrix} = \begin{pmatrix} T^{RA, E} \\ T^{RA, E} \\ V = \frac{1}{2} \left[ V + \frac{(\tilde{u}_{G})^{2} + (\tilde{v}_{G})^{2}}{V} \right]$$

Input:  $S_{IE} = sine (inertial-to-earth-fixed equatorial coordinate system angle)$  $<math>C_{IE} = cosine (inertial-to-earth-fixed equatorial coordinate system angle)$  $<math>r_1$   $r_2$   $r_3$  = inertial position coordinates  $r_3$  = inertial position coordinates  $v_1$   $v_2$  $v_3$  = inertial velocity coordinates
$\begin{array}{l} \omega_{c} &= \mbox{ earth angular velocity} \\ R_{1} \\ R_{2} \\ R_{2} \\ R_{3} \\ \end{array} = \mbox{ radar position in earth-fixed coordinates} \\ R_{3} \\ \end{array} \\ \begin{array}{l} T^{RN, E} \\ T^{RA, E} \\ \end{array} = \mbox{ Transformation from earth-fixed equatorial to radar local vertical north, and down-range coordinate systems} \end{array}$ 

Output: NA



Frequency: 2 times per second

Precision: 12 to 30 bits

Remarks: The first two equations are used to bypass calculation of high precision sin/cos and should occasionally be replaced by actual sin/cos calculations. Similarly, the last equation bypasses the extraction of a square root.

Description of Variables for Radar Input

 $\begin{vmatrix} m_{x} \\ m_{y} \\ m_{z} \end{vmatrix} = radar \text{ position measurements}$   $\begin{vmatrix} m_{z} \\ m_{z} \end{vmatrix} = local earth radius$   $t_{r} = time \text{ associated with radar measurement}$ 

# Constants:



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# UPDATE

This section contains preliminary equations for updating the inertial navigator by means of external data. Two sets of equations are presented as typical of the kind of external data which might be available. The first set is based on the reception of position data of the form available from a GSN-5 radar receiver. The second set is based on the reception of time difference data of the form available from a Loran receiver.

Preliminary interface data for VORTAC, GSN-5, Loran-C, and DECCA navigation aids are given in Appendix B.

In addition to the data itself, the computer needs an indication of when valid data is available.

 $h_{r} = m_{x}$   $Y_{r} = (m_{y})C_{r} + (m_{z})S_{r}$   $Z_{r} = (m_{z})C_{r} - (m_{y})S_{r}$   $L_{r} = \ell t_{r} + Y_{r}/r_{o}$   $\ell_{r} = Z_{r}/r_{o}$   $r_{r} = r_{o} + h_{r}$   $r_{K} = r_{r} \cos L_{r}$   $\ell g_{r} = Lg_{o} + \ell_{r} + \omega_{e}t_{r}$   $r_{r1} = r_{K} \sin \ell g_{r}$   $r_{r2} = r_{K} \cos \ell g_{r}$   $r_{r3} = r_{r} \sin L_{r}$ 

**Radar Position Calculation** 

Input:

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$$\mathbf{m}_{\mathbf{x}}, \mathbf{m}_{\mathbf{y}}, \mathbf{m}_{\mathbf{z}}, \mathbf{r}_{\mathbf{o}}, \mathbf{t}_{\mathbf{y}}$$

Output: r<sub>r1</sub>, r<sub>r2</sub>, r<sub>r3</sub>

Constants:  $C_r$ ,  $S_r$ ,  $\ell t_r$ ,  $Lg_o$ ,  $\omega_e$ 

# Timing: 1 per second

Radar position extrapolation. -

If

-

$$\Delta m_{z} = m_{z} - m_{z}^{p}$$

$$(|\Delta m_{x}| + |\Delta m_{y}| + |\Delta m_{z}| < \varepsilon^{2})$$

$$t^{p} = t$$

$$m_{x}^{p} = m_{x}$$

$$m_{y}^{p} = m_{y}$$

$$m_{z}^{p} = m_{z}$$

$$\Delta r_{r} = \Delta m_{x}$$

$$\Delta Y_{r} = (\Delta m_{y}) C_{r} + (\Delta m_{z}) S_{r}$$

$$\Delta Z_{r} = (\Delta m_{z}) C_{r} - (\Delta m_{y}) S_{r}$$

$$\Delta L_{r} = \Delta Y_{r}/r_{o}$$

$$\Delta cos L_{r} = -\Delta L_{r} sin L_{r}$$

$$\Delta sin L_{r} = \Delta L_{r} cos L_{r}$$

 $\Delta t = t - t^p$ 

 $\Delta m_x = m_x - m_x^p$ 

 $\Delta m_y = m_y - m_y^p$ 

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$$\Delta \cos \iota g_{\mathbf{r}} = -\Delta^{\iota} g_{\mathbf{r}} \sin \iota g_{\mathbf{r}}$$

$$\Delta \sin \iota g_{\mathbf{r}} = \Delta^{\iota} g_{\mathbf{r}} \cos \iota g_{\mathbf{r}}$$

$$\Delta \mathbf{r}_{\mathbf{K}} = \Delta \mathbf{r}_{\mathbf{r}} (\cos \mathbf{L}_{\mathbf{r}}) + \mathbf{r}_{\mathbf{r}} (\Delta \cos \mathbf{L}_{\mathbf{r}})$$

$$\mathbf{r}_{\mathbf{r}1} = \mathbf{r}_{\mathbf{r}1} + \Delta \mathbf{r}_{\mathbf{K}} (\sin \iota g_{\mathbf{r}}) + \mathbf{r}_{\mathbf{K}} (\Delta \sin \iota g_{\mathbf{r}})$$

$$\mathbf{r}_{\mathbf{r}2} = \mathbf{r}_{\mathbf{r}2} + \Delta \mathbf{r}_{\mathbf{K}} (\cos \iota g_{\mathbf{r}}) + \mathbf{r}_{\mathbf{K}} (\Delta \cos \iota g_{\mathbf{r}})$$

$$\mathbf{r}_{\mathbf{r}3} = \mathbf{r}_{\mathbf{r}3} + \Delta \mathbf{r}_{\mathbf{r}} (\sin \mathbf{L}_{\mathbf{r}}) + \mathbf{r}_{\mathbf{r}} (\Delta \sin \mathbf{L}_{\mathbf{r}})$$

$$\sin \mathbf{L}_{\mathbf{r}} = \sin \mathbf{L}_{\mathbf{r}} + \Delta \sin \mathbf{L}_{\mathbf{r}}$$

$$\cos \mathbf{L}_{\mathbf{r}} = \cos \mathbf{L}_{\mathbf{r}} + \Delta \cos \mathbf{L}_{\mathbf{r}}$$

$$\sin \iota g_{\mathbf{r}} = \sin 4g_{\mathbf{r}} + \Delta \sin \iota g_{\mathbf{r}}$$

$$\cos \iota g_{\mathbf{r}} = \cos 4g_{\mathbf{r}} + \Delta \cos \iota \xi_{\mathbf{r}}$$

$$\mathbf{r}_{\mathbf{K}} = \mathbf{r}_{\mathbf{K}} + \Delta \mathbf{r}_{\mathbf{K}}$$

$$\mathbf{r}_{\mathbf{r}} = \mathbf{r}_{\mathbf{r}} + \Delta \mathbf{r}_{\mathbf{r}}$$
Input:
$$\mathbf{m}_{\mathbf{x}}, \mathbf{m}_{\mathbf{y}}, \mathbf{m}_{\mathbf{z}}, \mathbf{r}_{\mathbf{o}}, \mathbf{m}_{\mathbf{x}}^{\mathbf{p}}, \mathbf{m}_{\mathbf{y}}^{\mathbf{p}}, \mathbf{m}_{\mathbf{z}}^{\mathbf{p}}, t^{\mathbf{p}}, \sin \mathbf{L}_{\mathbf{r}}, \cos \mathbf{L}_{\mathbf{r}},$$

$$\sin \iota g_{\mathbf{r}}, \cos \iota g_{\mathbf{r}}, \mathbf{r}_{\mathbf{r}}, \mathbf{r}_{\mathbf{K}}, \mathbf{r}_{\mathbf{r}1}, \mathbf{r}_{\mathbf{r}2}, \mathbf{r}_{\mathbf{r}3}$$
Output:
$$\mathbf{r}_{\mathbf{r}1}, \mathbf{r}_{\mathbf{r}2}, \mathbf{r}_{\mathbf{r}3}, \mathbf{m}_{\mathbf{y}}^{\mathbf{p}}, \mathbf{m}_{\mathbf{y}}^{\mathbf{p}}, \mathbf{m}_{\mathbf{z}}^{\mathbf{p}}, t^{\mathbf{p}}, \mathbf{r}_{\mathbf{r}}, \mathbf{r}_{\mathbf{K}}, \sin \mathbf{L}_{\mathbf{r}}, \cos \mathbf{L}_{\mathbf{r}},$$

$$\sin \iota g_{\mathbf{r}}, \cot \iota g_{\mathbf{r}}$$
Constants:
$$\mathbf{C}_{\mathbf{r}}, \mathbf{S}_{\mathbf{r}}, \iota t_{\mathbf{r}}, \mathbf{L}g_{\mathbf{0}}, \omega_{\mathbf{e}}$$
Timing:
$$16 \text{ per second}$$

$$\frac{Radar and inertial combining.}{Radar and inertial combining.} - i = 1, 2, 3$$

$$\Delta t_{\mathbf{r}} = t - t_{\mathbf{r}}$$

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Input:

Output:

Timing:

If

$$\left(\sum_{i=1,2,3} |\Delta r_i| < \epsilon^2\right)$$
$$\Delta t_{rp} = t_r - t_{rp}$$
$$\dot{r}_{ri} = (r_{ri} - r_{ri}^p)/\Delta t_{rp}$$
$$\Delta \dot{r}_i = \dot{r}_{ri} - \dot{r}_i$$
$$r_i = r_i + k_r \Delta r_i$$
$$\dot{r}_i = \dot{r}_i + k_r \Delta \dot{r}_i$$

Inputs:

 $\mathbf{r}_{i}$ ,  $\dot{\mathbf{r}}_{i}$ ,  $\mathbf{r}_{ri}$ ,  $\dot{\mathbf{r}}_{ri}$ ,  $\mathbf{t}$ ,  $\mathbf{t}_{r}$ ,  $\mathbf{t}_{rp}$ ,  $\mathbf{r}_{ri}^{p}$ ,  $\mathbf{k}_{r}$ ,  $\mathbf{k}_{r}^{*}$ r<sub>i</sub>, r<sub>i</sub>

Outputs:

Constants:  $\epsilon^2$ 

Radar and inertial combining definitions. -

t	2	present time
<sup>t</sup> r	=	time at which radar data was obtained
r ri	=	components of radar-derived position in inertial coordinates
t <sub>rp</sub>	=	time of previous radar data
r p ri	=	components of previous radar position
k <sub>r</sub> ,	k• =	combining gains either constant or slowly varying constants (generation equations are unknown)

Loran Computation

 $R_e = R_{eo} - Ref(U_3)(U_3)$ 

$$\cos \sigma_{1} = U_{i} U_{1i}$$

$$\Delta U_{1i} = U_{i} - U_{1i}$$

$$TEMP = U_{i} \Delta U_{1i}$$

$$\sin^{2} \sigma_{1} = TEMP (2 - TEMP)$$

$$\sin \sigma_{1} = \frac{1}{2} (\sin \sigma_{1} + \sin^{2} \sigma_{1} / \sin \sigma_{1})$$

$$\sigma_{1} = \sin \sigma_{1} \left[ 1 + \sin^{2} \sigma_{1} \left[ \frac{1}{6} + \sin^{2} \sigma_{1} \left[ \frac{3}{40} + \left( \frac{15}{336} \right) \sin^{2} \sigma_{1} \right] \right] \right]$$

$$A_{1} = U_{3} + U_{13}$$

$$A_{2} = U_{3} - U_{13}$$

$$A_{12} = (A_{1}) (A_{1})$$

$$A_{22} = (A_{2}) (A_{2})$$

$$A_{3} = \sigma_{1} + \sin \sigma_{1}$$

$$A_{4} = \sigma_{1} - \sin \sigma_{1}$$

$$A_{5} = 1 + \cos \sigma_{1}$$

$$A_{6} = 1 - \cos \sigma_{1}$$

$$A_{7} = (A_{3}) (A_{12})$$

$$A_{8} = (A_{4}) (A_{22})$$

$$\delta \sigma_{1} = \left[ \frac{f}{4} \right] (-A_{7}/A_{5} - A_{8}/A_{6})$$

$$R_{1} = R_{e} (\sigma_{1} + \delta \sigma_{1}) + \frac{h}{2} \sigma_{1}$$

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Repeat bracketed equations for second station, obtaining  $R_2$ , sin  $\sigma_2$ ,  $R_3$  and sin  $\sigma_3$ .

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$$T_{c2} = K_{c1} (R_2 - R_1) + K_{c2}$$

$$T_{c3} = K_{c3} (R_3 - R_1) + K_{c4}$$

$$\Delta T_2 = T_{c2} - T_{m2}$$

$$\Delta T_3 = T_{c3} - T_{m3}$$

$$B_{i1} = -RI_{i1} \sin \sigma_1 \quad i = 1, 2, 3$$

$$B_{i2} = -RI_{i2} \sin \sigma_2 \quad i = 1, 2, 3$$

$$B_{i3} = -RI_{i3} \sin \sigma_3 \quad i = 1, 2, 3$$

$$UTB_i = U_j B_{ji} \quad i = 1, 2, 3 \quad j = 1, 2, 3$$

$$UTB_i = UTB_1 + UTB_2 + UTB_3$$

$$UTB_i = UTB_i / TEMP \quad i = 2, 3$$

$$BS_i = B_{i1} + B_{i2} + B_{i3} \quad i = 1, 2, 3 \quad j = 2, 3$$

$$E_i = K_0 \Delta T_i \quad i = 2, 3$$

$$U_i = U_i + \Delta U_i$$

$$U^2 = U_i U_i$$

$$\Delta \left(\frac{1}{U}\right) = \frac{1}{2} (1 - U^2)$$

$$U_i = U_i + \Delta \left(\frac{1}{U}\right) U_i$$

$$\phi' = \omega_e (t - t_{pr})$$

$$t_{pr} = t$$

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$$\sin \phi = \sin \phi + \phi' \cos \phi$$
$$\cos \phi = \cos \phi - \phi' \sin \phi$$
$$v_1 = U_1 \cos \phi + U_2 \sin \phi$$
$$v_2 = U_2 \cos \phi - U_1 \sin \phi$$
$$r_{L1} = r_G v_1$$
$$r_{L2} = r_G v_2$$
$$r_{L3} = r_G U_3$$

The Loran position can now be combined with the inertial position as in the radar description.

Input: h, T<sub>m2</sub>, T<sub>m3</sub>, r<sub>G</sub>

Outputs: r<sub>L1</sub>, r<sub>L2</sub>, r<sub>L3</sub>

Constants: station-dependent (U<sub>ij</sub>, RI<sub>ij</sub>, K<sub>c1</sub>, K<sub>c2</sub>, K<sub>c3</sub>, K<sub>c4</sub>) nonstation-dependent (R<sub>eo</sub>, R<sub>ef</sub>, K<sub>o</sub>, f/4)

Loran Computation Definitions

U <sub>i</sub>	Ξ	direction cosines of vehicle in earth-fixed cartesian frame referred to here as the Loran frame
U <sub>ij</sub>	×	direction cosines of the ith station in the Loran frame, where station 1 is the master and stations 2 and 3 are the slaves
$\sigma_i$	Ŧ	the spherical range angles to the three stations
R <sub>i</sub>	2	the ranges to the stations
R <sub>e</sub>	2	earth radius corrected for flattening
f	=	flatteni <sup>-</sup> g correction coefficient in the oblateness compensation equations
K., K.	H	coefficients to convert range to time

к <sub>с2</sub> ,	K <sub>c4</sub>	=	coefficients to account for fixed time delays
к <sub>о</sub>		3	coefficient to convert time to range angle
RI <sub>ij</sub>		=	elements of matrix which is inverse of matrix whose elements are U <sub>ij</sub> . These elements are station-dependent stored constants.
r		=	Lorandonized position components in the incur

<sup>r</sup>Li = Loran-derived position components in the inertial frame

# GUIDANCE

#### Requirements

Definition of guidance laws appropriate to the NASA/ERC AALS must recognize many factors. These factors include aircraft flight capability, pilot manual control capability, environmental constraints such as imposed by geography, air traffic, buildings, etc., and operational needs such as minimizing flight time and fuel required.

There is probably no area that requires more pilot judgement than the landing phase. The word judgement implies an intelligent choice and assumes an optimum response. When the same functions are proposed in an automatic control system, the terms are often misused.

Any automatic control system that is to duplicate pilot functions must do so in a reasonably optimum marner. But what is an optimum manner? A pilot weighs many factors and then acts in the most optimum manner. A control system only weighs the factors that are built into the system and then only in a fixed manner. There is no judgement as such in a control system and the result is always predictable.

Optimum must be built in, and every possible choice must be included. The only reason systems can be called automatic now is that the choices have been greatly reduced and the weighting factor is constant. Most of the time this is adequate.

The automatic guidance system devised as the AALS baseline is also restricted. The choices have been reduced to the point wher "ney will fit physically (as logic statements) into a digital computer. The weighting factors are constant for the most part and the results are predictable. By providing suitable displays, we still rely on the pilot for judgement to reset the automatic system. The pilot is still the most optimum controller.

Guidance laws are defined herein which are suitable for use in CRT-type displays, as well as in closed-loop automatic modes. Detailed discussions of the various computations required are included.

#### Approach Pattern

The guidance system as defined for the baseline AALS has the following features:

- Rectangular approach pattern
- Automatic glideslope
- Standard turns
- Automatic flare

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A rectangular approach pattern was selected for the automatic guidance system. The rectangular pattern is orientated so that the landings are made into the wind. A bearing to the nearest checkpoint is computed after the guidance system is activated and when the helicopter is within the radar range. Altitude, position, speed, and heading are controlled to fly the desired path. Suitable anticipation is provided to initiate turns prior to reaching the checkpoints. Bank angles are limited to avoid stalling at the lower approach speeds.

Final approach is started at a distance of about two miles from the landing site. Speed is reduced and a constant altitude (selected by pilot) is maintained. The glideslope path (glide angle is selected by pilot) is computed on the basis of relative wind and typical helicopter performance. Speed is gradually reduced after glide-path intercept, but sufficient airspeed is maintained to avoid control problems normally associated with helicopters at low speeds.

The helicopter begins a vertical descent at an altitude preselected by the pilot. Radar altimeter signals are used during the final flare to provide the precise control needed. The system is flexible enough so that only minor changes are necessary to evaluate alternate approaches. The automatic system has been patterned after a typical pilot approach so that the entire system can be maintained or interrupted by the pilot at any time. This feature should also simplify the display system to make it more nearly like the actual flight situation.

Several approach paths were considered for this system. A spiral path in which the helicopter descends vertically in a circular path was one of those considered. At first, this spiral descent looks promising because it is conservative of airspace in the vicinity of the landing site. However, the spiral path is extremely difficult to fly for a V/STOL since the V/STOL has more cross coupling and flies closer to the stall point. The spiral descent also involves precise control in all six degrees of freedom and would be difficult to display. Extended flight in a spiral approach without visual reference is also conducive to air sickness.

A curvilinear path tangent to the straight-line final approach was also considered. The curvilinear path can be described by a suitable mathematical expression and could be modified to provide numerous interception points. This system was discarded because of the severe requirements on bank angle. If an intercept is made close to the touchdown area, the curvilinear path is too short and requires very high bank angles. The short distance also requires high decelerations in order to enter the final glide path with the proper speed.

The rectangular pattern offered the most flexibility, safety, and simplicity of all those considered. It even provides the opportunity for a straightin approach if the vehicle is making an intercept in the proper area. This approach is shown in Figure 3, with both a left-hand and right-hand approach shown. The pattern is dimensioned such that the final and downwind legs are 12,000-foot segments. The (N, E) origin is at the landing site.



Figure 3. Rectangular Approach Pattern

The cross-course legs are 6000 feet, with the relative orientation in a north and east direction. The checkpoints at the corners are labeled, as are the headings between checkpoints. These checkpoints retain this identification regardless of which wind orientation is used. Wind direction as referenced to north determines the orientation of the final approach, crosscourse, and down-wind legs. These dimensions are defined to be compatible with the test helicopter. The north and east coordinate system was chosen to conform to typical flight headings and navigation. Unfortunately, this is contrary to the practice of trigonometry, where angles are measured counterclockwise. The additional logic required to convert from one system to another is small, and it is better to stay in a coordinate system familiar to the pilot.

The coordinates are determined by the following equations:

• North coordinates in feet

$$N_0 = 0$$
  
 $N_1 = 12000 \cos \gamma$   
 $N_2 = [12000 \cos \gamma + 6000 \sin \gamma]$ 

$$N_3 = +6000 \sin \gamma$$
  
 $N_4 = [12000 \cos \gamma - 6000 \sin \gamma]$   
 $N_5 = -6000 \sin \gamma$ 

• East coordinates in feet

$$E_{0} = 0$$

$$E_{1} = 12000 \sin \gamma$$

$$E_{2} = [12000 \sin \gamma - 6000 \cos \gamma]$$

$$E_{3} = -6000 \cos \gamma$$

$$E_{4} = [12000 \sin \gamma + 6000 \cos \gamma]$$

$$E_{5} = +6000 \cos \gamma$$

where  $\psi_1$  = approach direction, and

 $\gamma = \psi_1 + 180$ 

These coordinates are stored in the computer and will be available for heading computations and other functions.

A sine and cosine routine will be used in the computer. This routine measures angles positive from a positive "X"-axis in a counterclockwise manner. The guidance system has angles measured clockwise from north. The additional logic will take the form of:

If $0 < \gamma < 90$	first quadrant sine + cosine +
90 < γ < 180	fourth quadrant sine - cosine +
180 < <b>y</b> < 270	third quadrant sir.e - cosine -
270 < γ < 360	second guadrant sine + cosine -

The quas. ant identifies the sign of the term.

The  $(\gamma)$  angles must also be identified in a different manner:

first quadrant use	90	-	γ		
fourth quadrant use	[360	-	γ]	+	90
third quadrant	[360	-	<b>7</b> ]	+	90
second quadrant use	[360	-	γ]	+	90

# First Checkpoint

The helicopter's present location in terms of north and east coordinates from the landing site is designated as  $N_A$  and  $E_A$ . These coordinates are available at all times from the navigation system.

A groundrule was established not to permit guidance engagement when the helicopter is within five miles of touchdown point. This would prevent unusual maneuvering to get on the desired flight path. Again, should this prove to be a problem, additional logic can be added to permit engagements under five miles. The logic would direct the helicopter to a more distant checkpoint to avoid large bank angles. With this five-mile limit, the present location from the landing site is computed:

$$d = \sqrt{N_A^2 + E_A^2}$$

If this distance d is less than five miles, the system will not engage. The nearest checkpoint is determined by computing the distance to all checkpoints in the rectangular pattern:

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d = 
$$\sqrt{(N_A - N_5)^2 + (E_A - E_5)^2}$$

The checkpoint with the smallest distance is the closest checkpoint. This checkpoint will then determine the desired course from the present location. All bearings are with respect to north and measured clockwise from north:

$$\Delta B = \tan^{-1} \left[ \frac{E_i - E_A}{N_i - N_A} \right]$$

where "i" refers to the nearest checkpoint. This bearing should be expressed with respect to north for the display and for the guidance. To determine the quadrant and bearing, the following logic is used:

If E <sub>i</sub> - E <sub>A</sub> is	If N <sub>i</sub> - N <sub>A</sub> is	Then the bearing is:
+	+	ΔB <sub>i</sub>
+	-	180 - ∆B <sub>i</sub>
-	-	180 + ΔB <sub>i</sub>
-	+	360 - ΔB <sub>i</sub>

The heading from checkpoint to checkpoint i. also determined prior to the first intercept. Since the direction of the wind is known, the respective headings are computed by:

$$\psi_1 = \gamma - 180$$
  

$$\psi_3 = \psi_1 - 180$$
  

$$\psi_4 = \gamma - 90$$
  

$$\psi_5 = \psi_3$$
  

$$\psi_2 = \gamma + 90$$

Again, these are stored for future reference such as the bank-angle command. Prior to the time the helicopter reaches the first intercept, some logic must determine whether a left or a right bank is needed to pick up the first heading:

> If  $[\Delta B_i - \psi_3]$  is positive, use left bank If  $[\Delta B_i - \psi_3]$  is negative, use right bank

It was assumed in these expressions that the heading  $\psi_3$  was the next heading. If the helicopter had been approaching N<sub>2</sub>, E<sub>2</sub>, the heading would have been  $\psi_2$ , and so on.

# Time to Bank

Prior to arriving at the checkpoint, the helicopter must start a bank. The distance to the checkpoint is continuously being computed. As the helicopter approaches the checkpoint, the time to the landing pattern corner is:

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t = 
$$\frac{R_i}{V_G}$$
 =  $\frac{[(N_i - N_A)^2 + (E_i - E_A)^2]^{1/2}}{V_G}$ 

where  $R_i = range$  to checkpoint

 $V_G$  = ground velocity

 $N_i$  = coordinate checkpoint

 $N_A$  = present coordinate

The actual bank is initiated when the time computed previously is equal to the time necessary to complete one half the turn (see following sketch):



$$t_{360} = \frac{2 \pi R}{V_G}$$
$$t_{\Delta \psi} = \frac{2 \pi R}{V_G} \left(\frac{\Delta \psi}{360}\right)$$

The heading change for one half the turn is:

$$\Delta \psi = \frac{\psi_i - B_i}{2}$$

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$$R = \frac{V_G^2}{g \tan \phi}$$

The bank angle  $\phi$  is held constant at 20 degrees to avoid stalling the helicopter:

t (turn) = 
$$\frac{2\pi V_{G}}{g \tan \Phi} \left( \frac{\psi_{i} - B_{i}}{2} \right) \left( \frac{1}{360} \right)$$

The turn is held for an equal period of time before control is relinquished to the heading mode. To avoid abrupt bank angle commands, a two-second first-order lag is added to the 20-degree bank command.

An alternate to "time to turn" to initiate a turn to new course would be a "distance to checkpoint" computation.

The equation to accomplish this is easily obtained by using the previous equation for "time to turn" and combining with the present velocity:

$$t(turn) = \frac{2\pi V_{G}}{g \tan \Phi} \left( \frac{\psi_{1} - B_{i}}{2} \right) \frac{1}{360}$$
  
$$d = V_{G} t$$
  
$$d = V_{G} \left( \frac{2\pi V_{G}}{g \tan \Theta} \right) \left( \frac{\psi_{1} - B_{i}}{2} \right) \frac{1}{360}$$

When the distance to the checkpoint is the same as the "distance to turn" the bank will be initiated.

# **Off-Course** Displacement

The off-course displacement is needed to hold proper ground track. Below some airspeed between 30 and 80 knots, the transition speed, the system controls to lateral velocity error. Under these conditions, the off-course displacement must be converted to the required lateral velocity error. The desired and actual position are continually computed and may be used to obtain the lateral displacement. First the equations of the present ground track are completed.

$$\frac{N - N_1}{E - E_1} = \frac{N_2 - N_1}{E_2 - E_1}$$

where  $N_1$ ,  $E_1$ , and  $N_2$ ,  $E_2$  are end points on the track. This will result in an equation of the form:

AE + BN + C = 0

Here, the A, B, and C are constants.

The perpendicular distance  $\Delta Y$  to course is:

$$\Delta Y = \frac{AE_A + BN_A + C}{\pm \sqrt{A^2 + B^2}}$$

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where  $E_A$ ,  $N_A$  are the present location.

The end points or checkpoints are selected on the basis of the present helicopter location. After the helicopter has passed a checkpoint, an "event marker" keeps a record of what leg is presently being flown.

# Straight-In Approach

There are times where it may be expedient to have a straight-in approach. This should only be possible if this is the shortest path to the landing site. This is the same reasoning the pilot would use.

On this basis, consider Figure 4:



Figure 4. Straight-in Approach Pattern

By drawing a line from the landing site through checkpoints 2 and 4, a feasible straight-in approach area is defined. Lie included angle is 53.12 degrees or  $\pm 26.56$  from the final approach direction  $\psi_1$ .

The actual heading at the time of interrogation is called  $\psi_A$  so that the difference between the true bearing to the landing site and the final approach direction must be within ±26.56 degrees:

+26.56 < 
$$\psi_1$$
 -  $\psi_A$  < -26.56

Under these conditions, the logic will always cause the helicopter to fly to checkpoint one (the final approach) even though it may be closer to checkpoint 4 or 2.

# Vertical Control

The altitude control is used to provide the proper vertical guidance. The control equation needed can be expressed as:

$$\Delta h = \left[\frac{1}{T_1 S}\right] \left[\pm 8 T_1\right]$$

where  $\Delta h = h - h_{c_0}$ 

= present altitude h

h<sub>co</sub> = pilot-selected approach altitude

 $T_1$  = integrator time constant

 $\pm 8 = 8$  ft/sec maximum descent rate (selected as a desirable and comfortable descent rate)

The pilot may select the command altitude h for the downwind and crosswind legs.

# **Altitude Select**

A nominal 800 feet is held on the approach pattern. Since the pilot can select the altitude, certain limits must be applied.

The "event marker" is used to identify the checkpoint that is being approached. The event marker determines the logic:

h (selected)  $\leq$  1500 feet on downwind leg

- h (selected)  $\leq$  1000 feet on base leg
- h (selected)  $\leq$  800 feet on final approach

Once the pilot selects an altitude, the altitude is reduced on each leg until 800 feet is reached on final approach. For example, assume the pilot selected 1500 feet on the downwind leg:

 $\Delta h = 1500 - 1000$ 

The 1000 feet is the desired altitude on the base leg. If the pilot had selected 1000 feet, this altitude would be retained ustil the base leg. The "event marker" also determines the descent rate to command the final altitude.

# Speed Control

It is assumed that a 100-knot speed is used on the downwind leg. This is adequate for suitable control and within the capabilities of the helicopter. If the helicopter is flying at a higher speed, the velocity is reduced through the following equation:

$$\bar{\mathbf{u}}_{c} = \left[\frac{\pm 3, 3 \text{ ft/sec}^{2}}{K}\right] \left[\frac{K}{S}\right] \left[\bar{\mathbf{u}}_{p} - \bar{\mathbf{u}}_{c}\right]$$

where

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 $\overline{\mathbf{u}}_{\mathbf{c}}$ 

= commanded airspeed

K = control gain

 $\pm 3.3 = \text{constant deceleration}$ 

 $\overline{u}_{p}$  = pilot-selected speed

# Final Approach

The final approach distance has been selected as 12,000 feet to be compatible with the helicopter characteristics of the flight test vehicle. This permits adequate distance for deceleration and also descent to 800 feet if the helicopter is at some other altitude. After a short period of level flight, a nominal six-degree glide path is intercepted and followed to the landing site. Glide-path angle is selected by the pilot.

Various research agencies have conducted tests with slopes of 6, 9, and 12 degrees. The recommendations favor the 6- and 7-degree slopes. The steeper angles (12 degrees and more) are very difficult to follow since forward speed and sink rate have to be adjusted rapidly. Also, depending on the forward speed, the steeper angles are too close to the autorotation speed. To keep on these steep paths, the helicopter has to fly very near the autorotation speed or "vortex ring" speed. The vortex-ring speed is when the downwash velocity is equal to the descent rate. This region creates severe roughness and wide variations in descent rate.

The rate of descent will vary as the helicopter flies the glide path. Descent rates are limited by the vortex ring, autorotation, flare capabilities and forward speed. Sufficient altitude must be available so that the helicopter can flare to the final touchdown without exceeding the "g" limits. During this descent the helicopter is operating near or in the region of the back side of the power-required curve. This means that a decrease in forward velocity means an increase in power required. This also means the autopilot will control rate of descent almost entirely by power changes.

The final approach is nominally started at an altitude of 800 feet and a speed of 100 knots. The checkpoint on the final approach is 12,000 feet from the landing site. The 800-foot altitude is maintained while the speed is reduced to 50 knots. At a distance of about 8000 feet from the landing site, ...e helicopter will intercept the six-degree glide path. It will descend along the path as it decreases the speed to 25 knots. At an altitude of 100 feet it will continue to decrease the speed to almost zero. At a pilotselected altitude above the landing site (about six feet), the helicopter will make p vertical descent to touchdown. This is summarized in Figure 5:



Figure 5. Final Approach Flight Profile

Altitude less than 800 feet should not normally be considered for the approach, since certain minimum altitudes are recommended over congested areas. The 800 to 1000 feet altitudes are ideal from the standpoint of the approach. With such an altitude there is some margin for small variations in approach speed, overshoot on the initial entry to the glide path, and some time for update of the inertial reference.

On the final approach, speed is reduced to 50 knots. The equation is then:

$$\bar{u}_{c} = \left[\frac{\left[\pm 3.3 \text{ ft/sec}^{2}\right]}{K}\right] \left[\frac{K}{S}\right] [85 - \bar{u}_{c}]$$

where 85 ft/sec = 50 knots. A switch must be made from airspeed to inertial speed. It is assumed that inertial speed is introduced gradually so that upon transfer there is no transient.

In manual systems, pilots have had difficulty in capturing the glide path. Generally, the overshoot is large since the pilot has insufficient warning that the glideslope intercept is near. With the inertial system some warning should be available so that a descent rate command can be given prior to the intercept. The lead time will depend on the glide path chosen. The effective angle of the glide path in turn will depend on the wind velocity.

To provide proper anticipation of the glide path, a high-passed descent rate command is used. This command is initiated about 1.5 seconds prior to glide-path intercept. The exact time depends on system response, magnitude of the step, the high-pass time constant, and other factors:

$$t = \frac{\pi R}{60 V}$$

where R = radius of maneuver

 $R = \frac{V^2}{A_n}$  $A_n = 0.1g = 3.2 \text{ ft/sec}^2$ 

The descent rate is 8 ft/sec nominal:

$$\frac{1}{h} = \frac{-8 \text{ ft}}{\text{sec}} \frac{20\text{S}}{1+20\text{S}}$$

At a time "t" a step input of 2 ft/3ec through a 20-second high pass should provide the proper anticipation for glidepath intercept and control. The range is simply:

$$R = \frac{800}{\tan E_{g}}$$

where  $E_{g} = glideslope angle.$ 

To follow the glideslope, the system requires an appropriate altitude rate as a command input:

$$h = V \tan E_g$$

where  $E_g = 6$  degrees

V = true ground speed

h = altitude rate

After the glide-pain intercept, the speed is reduced to 25 knots by the following command:

$$\overline{u}_{c} = \left[\frac{\left[\pm 3, 3 \text{ ft/sec}^{2}\right]}{K}\right] \left[\frac{K}{S}\right] \left[\frac{42 - \overline{u}_{c}}{K}\right]$$

where 42 ft/sec = 25 knots.

# Flare

The final flare is assumed to start at an altitude of about 100 feet. At this point the rate of descent and forward speed have been reduced to small values. The final 100 feet is sufficient to flare to a landing without exceeding any "g" limit and is reasonably comfortable for passengers. The last 100 feet may also be used to correct for some deviation in fore and aft position. It is definitely preferable to have a slight forward speed at touchdown, since there is less chance for sideslip. (The helicopter has more directional stability although very small.)

At this time, the radar altimeter is used to provide the necessary altitude (accurately). The required deceleration is 0.25g if the speed is 25 knots at 100 feet. The descent rate is 6 ft/sec or less. The equation:

$$\overline{u}_{c} = \left[\frac{-12 \text{ ft/sec}^{2}}{K}\right] \left[\frac{K}{S}\right] [0 - \overline{u}_{c}]$$

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will reduce forward speed to zero. At an altitude of about 6 feet, as measured by the radar altimeter, the wings-level command is given. Altitude rate is then commanded:

$$h_{c} = -3 \text{ ft/sec}$$

Touchdown will normally occur within two seconds after the time wings level is commanded. The final touchdown command will not be given if:

$$\overline{v} \ge 2-3$$
 ft/sec

where  $\overline{v}$  = lateral speed w.r.t. ground.

This will ensure that the sideload on the landing gear will not be excessive.

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# Go-Around

An additional consideration is the need for an automatic "go-around". A helicopter will have less need for a go-around than a conventional aircrait. With a helicopter, the approach speeds are much less, the deceleration capabilities are greater, and the required landing area is less. With a suitable presentation or display, the pilot should be able to perform instrument go-arounds.

The following information must be considered regardless of the method used to accomplish the go-around.

It will be assumed that the go-around will be initiated only during the approach, where the altitude will be 800 feet or less. The go-around maneuver should not apply to anything at an altitude more than the 800-foot approach. If something is necessary at 800 feet or more, a "loiter" or "standard turn" mode can be provided.

In the event of a go-around, a safe exit heading must be provided. This could take the form of "previously stored" obstructions with respect to the landing site or a clear heading provided by the ground. If the go-around is initiated because of some inertial difficulty, the location of obstructions with respect to the landing site would remain doubtful. If heading is provided, with update from the ground, the system is more reliable. In the go-around suggested, a safe exit heading is provided.

A safe climb angle must also be provided. This safe climb angle must be within the physical capabilities of the helicopter and also provide terrain clearance. It could be provided by the ground station at the same time as the safe heading information.

If a display is provided, the safe heading and climb angle should be shown with the present position of the helicopter. The pilot will be asked to fly above the safe climb angle consistent with the vehicle's potential rate of climb and forward speed. The amount of collective pitch required is dependent on weight, wind velocity, altitude, temperature, and rate of climb. Some of these parameters are related to the helicopter so that a universal solution is out of the question. Applicable performance charts are better stored in the computer with allowable rate of climb as the output. Typically, these charts take the form shown in Figure 6.

The gross weight must be known to determine the allowable rate of climb. Gross weight can be computed if the takeoff gross weight is recorded in the computer and fuel consumption is monitored. The computer could determine the performance via a table lookup or by direct solution of the equations represented by these charts.

As a result of these considerations, no automatic go-around computations are included as part of the baseline system definition. In addition, since a manual go-around probably can be provided with very little added system complexity, it is recommended that functional requirements be defined and mechanization be accomplished during the flight test program.



Figure 6. Typical Performance Chart

# Block Diagrams

Some of the modes have been described in block diagram form (Figures 7 through 11.) These block diagrams are primarily used for sizing of the digital computer. The shaping networks and time constants will have to be determined from subsequent analysis. The block diagrams are intended to command velocities as required by the automatic flight control system. All of the functions shown in the block diagrams have been previously described in the text.



Figure 7. Heading



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Figure 8. Altitude Control



Figure 9. Airspeed Control









# FLIGHT CONTROL

# Scope

This section describes the baseline digital flight control system synthesized for the computer sizing task of the NASA-ERC AALS program.

The equations and diagrams in Appendix C describe the software for the baseline digital flight control system for the YHC-1A helicopter. This digital control system was "flown" on an SDS 9300/PACE 231R hybrid computer in all of its modes of operation. Results of typical flights are shown in Figures 12 and 13.

Underlying the synthesis of the digital controller was a concept of flexibility. To obtain this flexibility, four modes of flight control were synthsized: a rate damper, an attitude/heading hold, an altitude hold, and a velocity command or fully automatic guidance mode. Figures 14 and 15 show vehicle response in each of these modes for a specific input (pilot's pedal/stick or auto guidance command).

Additional studies were also performed in the areas of effects of quantitization of sensor output signals, filtering requirements, sampling rates and multi-sample rate systems, and alternate mechanization of the system using analog rate gyros and an analog inner-loop stabilization system. The results of these studies are presented in the conclusions and recommendations and/or described in the discussion paragraphs.

## System Description

The overall goal of the program is to develop concepts for an automatic approach and landing system for V/STOL aircraft which will utilize a strapdown inertial navigator with radar update and a central digital computer to perform digital flight control computations. The guidance output will be in the form of velocity commands to the flight control system.

The first task was to synthesize a digital flight control system which would enable the vehicle to respond to velocity commands and result in a plausible computer requirements estimate. In addition, an attempt was made to incorporate the greatest possible flight control system flexibility so that system development, ground checkout, and flight testing would be simplified. The overall goal of the system was envisioned as applied research, and therefore a need existed for a flight control system with wide capability.

Also, a goal was established that the automatic flight control system would be operable over the entire flight envelope of the NASA/LRC YHC-1A test vehicles.



Figure 12. AFCS Pitch Axis - Hover







Figure 14. Input/Output, Attitude Rate Damper, and Attitude/ Heading/Altitude Hold Modes



Figure 15. Input/Output Velocity Command Modes

The flight control system which evolved from this study was "flown" on the hybrid simulation. Figures 12 and 13 show typical vehicle responses for the specified inputs. Two flight conditions are shown, although a 60-knot flight condition was also examined. Note that vehicle response to commanded inputs is smooth and overshoots are acceptable.

The system involves four modes of control: rate damping, altitude hold, velocity command, and automatic guidance. Figures 14 and 15 show vehicle response for each of these modes for specified inputs. The rate damping mode is a stability augmentation system and would not be normally used other than to flight check the most basic elements of the system. The attitude/ heading hold mode would normally be used for pitch control with or without altitude hold wnenever the velocity command (or automatic guidance and navigation) system is not used. A unique feature of the attitude, while, at cruise, stick inputs result in a vehicle attitude, while, at cruise, stick inputs result in a vehicle attitude rate. This control feature has been used in other Honeywell VTOL systems, and test pilote have indicated that this type of response, particularly in gust conditions, is most desirable.

The altitude hold mode which is used in conjuntion with the attitude/ heading mode is self-explanatory. Stick inputs result in an altitude rate through use of an input integrator. Altitude control is obtained entirely through collective pitch. No use is made of the cyclic stick for controlling vehicle attitude to obtain altitude changes. This is in keeping with previous Honeywell helicopter studies which indicate that altitude is best controlled by collective at speeds up to about 100 knots. If other types of vehicles which will have speeds in excess of 100 knots are to be studied, then a blending of altitude to attitude control may need to be performed. However, this should not increase the complexity of the computations to any great degree.

The velocity command mode is used in conjunction with the attitude/ heading hold mode and the altitude hold mode. Guidance commands in the form of velocity commands are generated by the guidance equations and input to the flight control system. Also, stick inputs result in a velocity command to the system. At the present time, stick inputs are superimposed upon velocity commands from the guidance equations. However, it may be desirable to inhibit the guidance signals whenever the stick is activated. This question of whether the stick signals should be superimposed upon or inhibit the guidance inputs should be resolved early in future studies.

The method by which various vehicle responses are obtained for various commands is obtained by logic equations and by adjusting certain gains. These gains and logic equations are described in Appendix C, which is a complete software description of the flight control system.

# Difference Equations

The difference equations described in Appendix C were obtained through Tustin's method (Ref. 1). This method was used since it provides the flexibility desired in the system. With this method, the complete flight control system is divided into individual blocks. Difference equations are then

written for these individual blocks. The system can then be mathematically reassembled in any desired order simply by cascading the appropriate difference equations. Hence, logic equations may then be written to exclude or include those blocks which will give the desired response.

# Sampling Frequency

The software description is based on sample rates of up to 30 samples/ sec. This was determined by hybrid simulation of the flight control system. Vehicle attitude and attitude rate loops require 30 samples/sec. Honeywell, in the absence of vehicle bending data, has considered the fundamental rotor frequency (268 rpm) and the third harmonic (3 blade passages/revolution) to possess significant residues in the S domain. This would place underdamped poles at approximately 4.5 and 13 Hz. Since half the sampling frequency should be greater than 13 Hz, the sampling frequency for the attitude control loops was chosen at 30 samples/sec.

The sampling rates of the altitude loop were highly dependent on flight condition. At hover, an altitude loop sample rate of 1 sample/sec would suffice (but not be satisfactory), while at 100 knots a sample rate of 5 samples/sec was required. Consequently, a sample rate of 10 samples/sec for the altitude control loop was selected.

For the velocity command loops, 1 sample/sec was adequate, but a smoother and more satisfactory performance was achieved with a sample rate of 2 samples/sec. In addition, it is envisioned, but not confirmed by computer results (the lateral guidance problem was not simulated), that heading guidance commands should be as high as 10 samples/sec since they would form part of the attitude hold loop. All other velocity command sample rates, as well as the altitude and attitude control system have been verified by hybrid computer simulation. Actual computer sizing was conducted for sample rates which are powers of 2. Thus, a simulation sample rate of 30/sec becomes 32/sec for the sizing model, 10/sec becomes 16/sec, and 2/sec remains the same.

## Bit Weight

The baseline system for this study has no rate gyro signal. Instead, attitude rate is derived from the change of attitude signal by a first-pastdifference equation in the software. The computation of this rate signal from quantitized attitude signals has the same effect as that of resolution in a rate gyro in that it introduces a limit cycle oscillation. The limit cycle can be objectionable depending upon whether or not the pilot detects it. Pilot detection of the oscillation is a function of many factors including vehicle vibration, turbulence, frequency and amplitude of the oscillation and the individual pilot himself. The amplitude of the oscillation obtained in this hybrid study was on the borderline of being objectionable. As the bit weight (attitude change per pulse) is increased, so is the amplitude of the limit cycle. Currently, a bit weight of 0.0035 deg/pulse is used, although a bit weight of 0.00875 degree/pulse is desired. . 94.

Other analog signals quantitized in this study were altitude, altitude rate, and velocity feedback. Bit weights of 0, 25 feet (0, 25 ft/sec) per pulse were used and performance was only acceptable. If the expected in-flight deterioration of these signals takes place, abit weight of 0, 1 feet (0, 1 ft/sec) would be desired.

#### Alternate Inner-Loop Stabilization

In lieu of deriving an attitude rate signal, two alternate mechanizations were examined. These consist of using an analog rate gyro with a digital inner-loop stabilization system and an analog rate gyro with an analog innerloop stabilization system.

The inner-loop stabilization system for the pitch and roll axes consists of the attitude rate signals which are shaped but do not pass through the integrators. For the yaw axis, the inner-loop stabilization system consists of the yaw attitude rate signal, sideslip signal, and roll rate-to-yaw signal. These signals are designated as  $\delta_{L_{C_1}}$ ,  $\delta_{S_{C_1}}$ ,  $\delta_{R_{C_1}}$ ,  $\delta_{R_{C_2}}$ , and  $\delta_{R_{C_3}}$  on the  $C_{C_1}$ 

block diagrams in Appendix B. The rate gyro with digital inner loop reduced limit cycle oscillation by approximately a factor of five but did not reduce the minimum sample rate. With an analog inner-loop stabilization system and an analog rate gyro, the same improvement in limit cycle oscillation was noted as well as a reduction in minimum sampling of 25 percent.

# Filters

The need for filtering was also examined. Previously it was stated that Honeywell, in the absence of vehicle bending data, was assuming significant residues associated with the main rotor frequency and the third harmonic. Based on this assumption, a notch filter at the main rotor frequency was included in the software. A second-order roll-off filter one octave below the third harmonic frequency was also incorporated in the software. This will reduce the gain of the system at the frequency of the third harmonic by 12 dB and in addition will serve as a noise filter.

#### Plant Dynamics

An examination of the analog portion of the plant was also conducted. This consisted of studying the math modeling of the servos and actuators on the CH-46 aircraft. Previous velocity command studies considered the actuators and the rotors as a 20-rad/sec lag plus a 14-rad/sec lag (see Ref. 2).

Previous studies at Honeywell on the CH-46D resulted in an actuator and rotor model of greater lag and complexity. Reference 3 states that the actuator/controls model is a 15-cycle, 0.6-damped, second-order lag. Since this value also seemed optimistic, it was agreed with NASA-ERC that an adequate model for the actuators plus control linkage would be a 15-rad/ sec, 0.6-damped, second-order lag and that the rotor could be modeled by
a 27-rad/sec, 0.67-damped, second-order lag. This is the model which was used in this study.

### Optimal Control

In addition to the baseline system definition studies, an independent control system synthesis was performed using optimal control techniques. This optimal control study is discussed in Appendix D.

### Conclusions

As a result of the control study it was concluded that:

- 1) A digital autopilot can be synthesized for an unstable vehicle such as the YHC-1A and can control the vehicle for an automatic landing.
- An analog rate gyro provides a negligible reduction in sample rate requirements. An analog inner-loop stabilization system reduces sample rate requirements by approximately 25 percent.
- 3) The effects of quantitization of sensor output signals results in the general deterioration of the system in the form of introducing potentially objectionable limit cycle oscillations.
- 4) Tustin's method of mechanizing difference equations has been verified by induction.

Results obtained, however, should be treated as preliminary. Further studies are necessary to define a flightworthy system. In particular, the following should be done:

- In leiu of reducing gyro and accelerometer pulse weight, methods of compensation suitable for software implementation should be studied as a means of minimizing limit cycles.
- 2) Filtering requirements are more stringent than ever with a sample data system due to the frequency folding (aliasing) phenomenon. Therefore, analysis including vehicle structural mode feedback is recommended.
- 3) It should be resolved whether, while in the velocity command mode, stick inputs should inhibit guidance command signals or whether they should be superimposed.
- 4) Optimal control studies should be conducted and the resulting control functions evaluated by simulation and flight test.

### DISPLAYS

Included in the total effort for the definition of the baseline cutomatic approach and landing system is the task of defining relevant navigation/ guidance/flight control parameters to be displayed to the aircraft crew. This task requires specification of parameters to be supplied by the AALS central computer to a display subsystem (display generator and displays). The listing of recommended parameters to be provided by the AALS central computer is fairly long. This is because of the need to retain flexibility of display design (which will depend upon final system design and operational characteristics and which should be developed analytically) at this phase of the AALS development program.

#### Design Considerations

Several system operational and design considerations influence the scope and size of the recommended set of parameters to be provided by the AALS central computer to the display subsystem as part of the baseline system. These considerations are discussed below.

<u>Multi-regime operation of the aircraft</u>. - The AALS is being developed for ultimate use in a V/STOL-type aircraft. This type of aircraft will operate in at least two different flight regimes. In one, it will operate like a conventional aircraft, with the aircraft/local-air-mass relationships being of prime importance. In the other, it will operate as a V/STOL aircraft, with the aircraft/ground relationships being of prime importance. In addition, there will be a transition zone in which the aircraft is changing from one regime to the other.

This multi-regime operational capability requires the aircraft to operate in different reference systems at different times. The relevant parameters for control will differ depending upon the current reference system. Since parameters for display must be compatible with those for control (if the displays are to be meaningful), they will also differ depending upon the current reference system.

<u>Multiple flight-phase operation</u>. - In addition to operating within several different reference frames for different flight regimes, the current reference frame will vary by flight phase. The total flight profile for the aircraft will consist of several phases (e.g., take-off and departure from an initial field, enroute navigation and flight management, initial approach into the landing pattern, final approach, and terminal landing operations). As the relevant reference frame changes, the appropriate parameters for display will also change.

Multiple flight control method. - The flight control method and laws used for the system could be of several types (e.g., command flight path, command attitude/airspeed, command velocity vector, etc.). For different methods of flight control, the resulting reference frame and appropriate parameters for display will vary.

<u>Human operator functions.</u> - Under nominal operating conditions, the pilot's functions may consist primarily of updating and adjusting automatic subsystems, selecting automatic operating modes and functions, and monitoring automatic system operation. However, in the event of automatic system failures or performance degradations, the pilot may be required to assume manual control over one or more functions. In addition, the pilot may desire to operate the system manually even if fully automatic operation is possible. To permit the pilot to "get into the loop" for manual control, he must be provided with sufficient, relevant information regarding system operation and its responses to his control inputs. This information will not necessarily be the same as that he will need for monitoring automatic system operations. For this reason, the capability to provide different displays of information for the manual control and the monitoring of automatic operation may be required.

Basic parameters. - In addition to the special navigation/guidance/flight control parameters which should be displayed for different flight regimes, flight phases, flight control methods, and human operator functions, certain parameters are considered basic by pilots and must be available for display if the system is to be considered adequate. Such parameters as attitude, altitude, altitude rate, and heading fall into the "basic" category.

Special signal conditioning. - Depending upon the flight regime, flight phase, flight control method, human operator functions, and aircraft dynamics existing at a particular time, it may be necessary to provide special conditioning of certain parameters prior to their presentation via displays. Such special conditioning would be required for quickened or predictor displays to provide a "lead" on system responses for the pilot. In general, efficient manual control of high-order control systems is not possible without some "lead". For example, for a V/STOL aircraft, the commanded pitch rate may be proportional to fore-aft stick displacements. If the pilot is attempting to control the aircraft X-position via a pitch rate control, he is operating a fourth-order control system. Unless certain related parameter derivatives (e.g.,  $X, X, \theta$ ) are added to the display of position, it is unlikely that the pilot will be able to control aircraft position. Thus, these parameter derivatives (which would perhaps never be displayed in their "raw" form) need to be combined, with appropriate relative gains, and added to position information.

### Display Formats

Two example display formats are discussed below to illustrate the use of quickened or predictor displays. Both displays are of a plan position indicator (PPI) form. However, related information could be presented via vertical situation indicators or head-up displays.

Figure 16 presents a PPI format referenced to aircraft heading. It displays actual aircraft position  $(X_A, Y_A)$  as a fixed symbol (triangle). Quickened aircraft position  $(X_0, Y_0)$  is presented as a moving symbol (asterisk). Actual landing site location  $(X_0, Y_0)$  is presented as a moving symbol (diamond). Command track is presented as a moving symbol (line intersecting the landing site in this case). Points of interest on the command flight path (e.g., glideslope intercept) are presented as tic marks on the command track. Altitude and altitude error can be presented on the linear scale and pointers at the left margin of the display. It should be noted that the diamond, command track, and tic-mark symbols could represent elements of the approach landing pattern other than landing site location, final approach command track and glideslope intercept location.

Equations for calculating the quickened aircraft position symbol parameters are given below the display drawing.

Figure 17 presents a PPI format which uses predicition. Again, the fixed diamond symbol presents actual aircraft position. The "string" of dots extending from the actual aircraft position represents the predicted X, Y path for the aircraft under present pitch, roll, wind velocity and direction, heading and airspeed conditions. The solid line represents a selected command path (e.g., the base leg of the landing pattern). The display indicates that an overshoot to command path acquisition will occur if aircraft flight conditions remain unchanged.

The equations under the figure define the terms used in calculations. These equations are integrated ahead for differing amounts of time to present the predicted path data on the display. The incremental prediction interval  $\tau$  and the number of intervals n can be varied as a function of range to the selected reference point, altitude, etc.

Helicopter dynamics are assumed in each display such that airspeed is varied by pitch attitude variations and heading is varied by bank angle changes.

#### **Candidate Parameters**

It is recommended that the following navigation/guidance/flight control parameters be provided by the AALS central computer for display. This preliminary selection of recommended parameters is based on the consid-



 $X_{\mathbf{Q}} = X_{\mathbf{A}} + K_{\mathbf{u}} (\mathbf{R}) \, \mathbf{\bar{u}} + K_{\theta} (\mathbf{R}) \, \theta + K_{\theta}^{*} \, \mathbf{\dot{\theta}}$  $Y_{\mathbf{Q}} = Y_{\mathbf{A}} + K_{\phi} \, \mathbf{\dot{Y}}_{\mathbf{A}} + K_{\phi} \phi + K_{\phi}^{*} \, \mathbf{\dot{\phi}}$ 

Figure 16. Example Quickened PPI Format



ASSUME SMALL ANGLES AND CONSTANT PITCH AND ROLL OVER THE PREDICTION TIME

 $u + D = -g\theta$   $\Delta \dot{\Psi} = g\phi/u$   $\dot{X}_{P} = u + V_{w} \cos(\Psi_{o} - \gamma)$  $\dot{Y}_{P} = u\Delta\Psi + V_{w} \sin(\Psi_{o} - \gamma)$ 

u = AIRCRAFT VELOCITY D = AIRCRAFT DRAG g = ACCELERATION OF GRAVITY  $\theta$  = PITCH ATTITUDE  $\phi$  = ROLL ATTITUDE  $\Psi_{o}$  = PRESENT AIRCRAFT HEADING  $X_{A}, Y_{A}$  = PRESENT AIRCRAFT POSITION  $V_{w}$  = WIND VELOCITY  $\gamma$  = WIND DIRECTION

Figure 17. Example Predictor PPI Format

erations discussed above and on the desire to retain display design flexibility at this stage of the AALS development program. Final decisions regarding the appropriate parameters for display will depend upon actual system operational and design characteristics.

The candidate parameters are categorized by the system functions to which they relate;

- 1) <u>AALS operation parameters</u>
  - a. Output to cyclic and differential collective control servos
  - b. Output to collective thrust control servo
- 2) Flight condition parameters
  - a. Heading
  - b. Elevation angle
  - c. Roll angle
  - d. Altitude
  - e. Altitude rate
  - f. Airspeed

### 3) Command error parameters

- a. Longitudinal velocity error in horizontal plane
- b. Velocity error normal to command ground track
- c. Altitude rate error
- d. Heading error (w.r.t. command course)

# .4) Situation parameters

- a. Longitudinal velocity command
- b. Lateral velocity command
- c. Lateral velocity command (w.r.t. command course)
- d. Command heading
- e. Command altitude
- f. Command altitude rate
- g. Landing site location
- h. Present aircraft location
- i. Command course intersection locations
- j. Horizontal range to specified location

- k. Ground speed
- 1. Bearing to specified location
- m. Local cross-track wind velocity
- n. Final approach heading
- o. Predicted aircraft position

## "Eight-Ball" Display

For early AALS evaluation flights it is anticipated that an "eight-ball" display be used to present relevant navigation/guidance/flight control information to the pilot. It is assumed that the "eight-ball" display used will be the Gemini flight director/attitude indicator. This indicator has the following display elements:

- Three-axis ball (used to display vehicle orientation Euler angles for Gemini)
- Roll needle (used to display vehicle roll angle for Gemini)
- Two cross-pointers (used to present pitch and yaw attitude errors or angular rates about the three vehicle axes for Gemini)

At the present time, it is uncertain how the Gemini indicator will be configured to display relevant AALS information for various flight phases. Because of the limited number of display elements available on the Gemini indicator, additional instruments may be required to display sufficient navigation/guidance/flight control information for adequate performance monitoring or manual control.

Also, the particular physical location and orientation of the several display elements on the Gemini indicator, and their resultant direction-ofmotion characteristics, may not be suitable for the display of certain parameters (e.g., displaying altitude error on a horizontally moving crosspointer).

For the reasons stated above, the Gemini indicator above may not be fully adequate (or fully appropriate) as the display device to be used with the AALS.

The preliminary suggested parameters for display for the initial approach, final approach, and terminal landing phases are presented below. It should be noted that, whereas basic parameters are listed, they may have to be presented in combined, quickened, or predictor form to ensure good performance with man-in-the-loop.

The parameters listed are in addition to the following basic parameters which should be displayed at all times (or be available for display at the pilot's descretion):

- Actual heading
- Actual elevation angle
- Actual roll angle
- Actual altitude
- Actual altitude rate
- Actual airspeed

Initial approach phase. - For initial approach (i.e., all operations including acquisition of the initial command track up to the turn onto the final approach), the following parameters should be displayed (or be available for display at the pilot's discretion):

- a. X-deviation from the selected command path (e.g., downwind leg or base leg)
- b. Y-deviation from the selected command path
- c. X-deviation rate
- d. Y-deviation rate
- e. Range to selected command path intersections
- f. Relative bearing to selected command path intersections.
- g. Heading error
- h. Altitude error
- i. Altitude rate error

Final approach phase. - For final approach (i. s., all operations from the turn onto the final approach to near touchdown), the following parameters should be displayed (or be available for display at the pilot's discretion):

- a. X-deviation from the commanded path
- b. Y-deviation from the commanded path
- c. X-deviation rate
- d. Y-deviation rate
- e. Range to "glideslope" intercept
- f. Range to landing site
- g. Altitude error
- h. Altitude rate error

i. Heading error

j. Local wind direction

k. Local wind velocity

<u>Terminal landing phase.</u> - For terminal landing (i. e., operations just prior to touchdown) the following parameters should be displayed:

a. X-deviation from the commanded path

b. Y-deviation from the commanded path

c. X-deviation rate

d. Y-deviation rate

e. Range to landing site

f. Range rate to landing site

g. Altitude error

h. Altitude rate error

i. Heading error

j. Local wind direction

k. Local wind velocity

### Baseline System

Baseline system display functions as defined are intended to be suitable for use with an "eight-ball"-type display, with expansion to a CRT situationtype display as a goal. As such, all functions potentially useful to both the "eight-ball" and the CRT display are defined.

The form of each display function is estimated. Firm quantitative expressions require detailed analysis which is not within the scope of the present effort. It is assumed that normal flight condition information such as airspeed, sideslip, servo command, etc., will be supplied to the pilot in conventional displays. Airspeed, and other appropriate data, may also be incorporated in the CRT display. However, there will be no need for central computer involvement in this type display function.

It is anticipated that all displays will require an analog signal. Therefore, a digital-to-analog converter will be needed for display function outputs. In addition, a display generator (impedance matching, filtering for smoothing sampling ripple, symbol generation for the CRT display, etc.) will be required. The display functions which must be obtained from the central computer or computed digitally are discussed in Appendix E.

### DOWN LINK

Instrumentation provisions include a "down link" (or telemetry system) to the ground. NASA/ERC intends to use modified Gemini equipment for the down link. A description of the equipment and a list of quantities for transmission has been provided by NASA/ERC. Appendix F is based on NASAsupplied information. It can be expected that the quantities transmitted on the down link will change with the purpose of specific flights. The baseline system definition includes the list given in Appendix E. However, instrumentation needs are not specifically included in the design description such as the AALS input/output signals description of Table I.

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### APPENDIX A

## ANALOG RATE GYRO RECOMMENDATION

Mechanization of the alternate analog inner-loop stabilization function requires an analog output attitude rate gyro. The Gemini rate gyro package (Honeywell device GG246B) should be usable in the mechanization. However, there are two areas in which care must be used. They are range available and vibration sensitivity.

Full-scale gyro output occurs at 35 deg/sec minimum. This rate may be marginal in roll and possibly in yaw. Effects should be apparent only when maneuvering at high attitude rates when in the stability augmentation mode. It is not expected that full-scale output would be reached during automatic guidance. If it does occur, it would mean only that some damping would be momentarily lost in most cases. No problem exists for manual control maneuvering, since the gyros can withstand 500-deg/sec inputs.

Vibration tests made on the Gemini rate gyro package (RGP), which NASA-ERC intends to use for instrumentation purposes, disclosed that the gyros have resonant points near the rotor frequencies. (See Honeywell report 20987-TR1, "CH-46 Attitude Control System Design Recommendation and Analysis Summary" dated 20 March 1968.) When output traces from the NASA/LRC YHC-1A test vehicle become available, they should be examined for evidence of resonant responses. The required inner-loop compensation networks will need filters for the resonances if the resonances are present as expected. The one-per-revolution frequency would be the most severe problem. A notch filter probably would be required. Roll-off filters would be satisfactory for the higher frequencies. Whether or not the gyros are usable depends on the amplitude of peaking obtained (and degree of filtering required). Whether or not it is practical to use the gyros will depend on the wear induced by the resonant response and the added complexity needed in the inner-loop compensation circuits.

Substitution of a different rate gyro is an alternate solution. Again, however, particular attention would have to be paid to vibration characteristics. It would be well to impose a vibration acceptance test in the procurement of a substitute gyro. This test should consist of base motion input vibration of  $\pm 0.05$  inch amplitude from 4.0 to 20 Hz and  $\pm 2$  g's amplitude from 20 to 500 Hz. Input should be a 15-minute scan in each axis. No resonances should be permitted at rotor or blade frequencies or harmonics of the blade frequencies or at helicopter structural frequencies. (It is assumed that any gyro procured would be qualified to MIL-E-5400 or equivalent.)

As a result of the above considerations, it is recommended that:

1) The Gemini rate gyro package be flight tested on the NASA/LRC YHC-1A helicopter. Gyro output in all three axes should be continuously monitored during start-up, take-off, cruise, maneuvering, let-down, hover, and shut-down.

- 2) A preliminary analog inner-loop stabilization design be made based on in-flight gyro output characteristics.
- 3) If a complex filter is needed, then the ability of alternate offthe-shelf "autopilot grade" rate gyros to meet the vibration requirements should be established. (Most available rate gyros will meet the functional requirements needed.)
- 4) If an acceptable alternate gyro(s) is found, then a decision can be made for the preferred mechanization: complex filtering versus new gyros.

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### APPENDIX B

### NAVIGATION UPDATE INTERFACES

### VORTAC INTERFACE

The VORTAC radio navigation system is a combination of the VOR (Very High Frequency Omnidirectional Range) system operating in the vhf band ' (around 100 MHz) and the TACAN (Tactical Air Navigation)system operating in the uhf band (around 1000 MHz).

In the VORTAC system, a TACAN station is crected to supplement an existing VOR station. The VOR station provides bearing information using a phase-difference technique, and the TACAN station provides distance information using travel time of radio waves (propagation delay). This system, when interfaced with a central airborne guidance computer, could provide range and bearing information of the aircraft from any of the many VORTAC stations located throughout the world. This will provide bearing information within two degrees and range information to about 0.1 nautical mile. This information could be used either for updating position or application to overall guidance for steering to the target station.

### INTERFACE INFORMATION

The following information can be received from the VORTAC system:

- Range
- Bearing

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• Station identification

Range information on the TACAN airborne system is displayed on a Veeder counter. This is a motor-driven device, and a potentiometer, encoder, or synchro could be added to the shaft to give analog, digital, or synchro information to the computer.

The present system has a variable resistor which might be used to provide a variable dc signal to go into an A/D converter of the computer.

The bearing indicator is also a motor-driven output and could easily be adapted to the outputs listed under the range information. The existing system has a synchro output which could be put into a synchro-to-digital converter of the computer. This would give 360-degree bearing information through one rotation of the synchro. In addition, an output is available in the form of a discrete level which tells whether the aircraft is heading away or toward the VORTAC transmitter. If needed, this signal could be a discrete input to the computer. Station identification is in international morse code transmitted along with distance information. With special equipment, station identification could be converted into an address code and interfaced with the computer. With this input the entire system could be automated to provide nonambiguous position information based on VORTAC inputs.

### GSN-5 INTERFACE

This section is concerned mainly with the airborne digital command system (DCS) interface with the system computer. There is no direct interface of the GSN-5 with the computer; however, the GSN-5 interface with the overall system does have a bearing on the computer interface. Therefore, in this discussion those overall characteristics of the system interface which affect the computer interface will be considered.

### Inputs

<u>DCS ready (DCS to computer)</u>, - This is a discrete signal which sets "true" after the DCS receives a set of up-link data. The total duration will not exceed 110 msec. If the computer fails to reply to this signal within the first 100 msec, the DCS will automatically reset in preparation for receipt of the next transmission.

If the computer does reply to this signal stimulation, the "true" state will prevail for the subsequent transmission of data from DCS to computer. Therefore, in this situation, the duration of "DCS ready" at the computer interface is greater than 5 and less than 10 msec subsequent to receipt by the DCS of the first data clock pulse from the computer.

Data input (DCS to computer). - Data from DCS to computer is transmitted on a serial binary line. One serial word will consist of 24 bits in an NRZ format. Frequency of transmission is 500 kHz, with a bit duration of  $2 \mu sec$ .

The data is transmitted only if a data clock is presented to the DCS, which event is contingent upon computer acceptance of the "DCS ready" discrete described above.

### Outputs

<u>Data clock (computer to DCS)</u>. - If a "DCS ready" discrete is received and accepted by the computer, the computer will issue 24 clocking pulses to the DCS to allow clocking of data into the computer. The clock repetition rate is 500 kHz; pulse duration is 1.0  $\mu$ sec. The computer must provide the first clock pulse to the DCS within 100 msec after receipt of a "DCS ready," or else the "DCS ready" will go low, and a new transmission from the ground will occur.

### LORAN C INTERFACE

This section describes typical interface signals with a Loran C receiver. It is assumed that the receiver processes the rf input and provides to the computer the applicable data in a digital format, and that the computer provides data and control to the receiver in a digital format. The signals and their associated characteristics are described below.

#### Inputs

<u>Time difference (from receiver).</u> - The 10,000- $\mu$ sec-to-0.1- $\mu$ sec time difference information is transmitted in a BCD code on 24 parallel wires. The 0.025- $\mu$ sec time difference information is sent in a standard binary code on two wires. Format is as follows:



This data is available to the computer for the "A" and "B" slaves (assuming a Loran triad consisting of a master and two slaves) in accordance with the receiver-computer timing diagram, Figure B-1.

<u>Time difference identification (from receiver)</u>. - The "A Gate" and "B Gate" waveforms are used to gate the time-difference information as shown on the timing diagram, Figure B-1. These signals are pulse format and require two wires.

<u>Velocity advance (from receiver)</u>. - This is a trigger pulse which instructs the computer to transmit the next word of velocity aid information to the receiver. The velocity aid information is transmitted sequentially in order: Master, Slave A, Slave B. Timing is shown in Figure B-1. This signal requires one wire.

<u>Supply initial M velocity (from receiver).</u> - This discrete signal instructs the computer to insert the M initial velocity information into the receiver. When this data is desired, the signal will switch to the "true" state. When the signal returns to the "false" state, normal M acceleration data is supplied to the receiver. This signal requires one wire.

Loran status (from receiver). - Four alarm signals are generated in the receiver to indicate Loran status. Typical status indications are:

- Transmitter malfunction
- Jammed receiver
- Ground wave available
- Receiver searching



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In the application with which we are familiar, each indication is transmitted on an individual line, requiring a total of four wires. However, the number of indications could be increased or the number of wires decreased by coding the discretes, if desired.

<u>Control inputs (from control panel)</u>. - Because of the variety of modes in which the system is expected to be operated, and to allow versatility in selection of Loran station pairs, allowance should be made for control inputs from the main system control point. These signals would most likely be in the form of coded discrete levels which assume either a "true" or "false" logic state depending on operator preference. Acceptance of these discretes at the computer could efficiently be accomplished on the "sense switch" inputs using an STE- or SKS-type instruction, as typified in the ALERT and SIGN-III computers. Approximately 10 to 15 input discretes should be reserved for these functions. Among the functions to be handled by these discretes are:

- PRR basic select
- PRR specific select
- Slave A or B coding delay select
- Search mode select
- Power control

#### **Outputs**

<u>Basic rate (computer to receiver)</u>. - Provision should be made to allow selection of the basic PRR. These are switched discrete outputs changing under operator control. There are six basic rates possible; therefore, three coded discrete output lines should be reserved for this purpose.

<u>Specific rate (computer to receiver)</u>, - Provision should be made to allow selection of the specific PRR. These are switched discrete outputs changing under operator control. There are eight specific rates possible; therefore, three coded discrete output lines should be reserved for this purpose.

<u>Coding delay (computer to receiver)</u>. - The coding-delay information is transferred to the receiver on 16 wires in a BCD code. These signals will define the 10,000- $\mu$ sec and 1000- $\mu$ sec time difference for slaves A and B. Levels of these signals will be unchanging during the time that a particular station group is being tracked.

<u>Velocity aid (computer to receiver)</u>. - Three kinds of velocity aid information are supplied to the receiver: slave time difference velocity aid, master acceleration aid, and master initial velocity. The information is computed from non-Loran sensors and passed to the receiver on 12 parallel lines in a binary code. The most significant bit is sign, true being positive and false being negative. Normally, these signals are transmitted sequentially to the receiver in a master acceleration aid, slave A velocity aid, and slave B velocity aid order as instructed by the "velocity advance" waveform. During master lock-on, the receiver will request the "master initial velocity" information (see Figure B-1):

- Slave time difference velocity aid The LSB (least significant bit) will have dimension 0.  $025 \mu sec/(32)$  (PRR) with accuracy to one bit.
- Master acceleration aid The LSB will have dimensions  $10 \ \mu \sec/\sec/(1024)(128)$  (PRR) with accuracy of ±5 percent.
- <u>Master initial velocity</u> The LSB will be weighted at 0, 0098 psec/sec with accuracy of ±5 percent. This information is supplied to the receiver when requested by the "supply initial M velocity" signal.

<u>Velocity identification (computer to receiver)</u>. - Velocity identification information should be supplied to the receiver indicating which velocity aid information is being provided. This function could be part of the parallel bus output and would require two lines. Rate of occurrence would be in accordance with the timing diagram of Figure B-1.

<u>Start search (computer to receiver)</u>. - Three discretes (output or two coded output discrete lines) should be made available to allow the receiver to initiate master, slave A, or slave B search.

#### Summary

The following summarizes the expected interface requirements for Loran C:

- 26-bit parallel input bus
- 14-bit parallel output bus
- 4 pulsed discretes (input)
- 20 switched discretes (input)
- 22 switched discretes (output)
- 2 pulsed discretes (output)

### DECCA INTERFACE

The DECCA radio navigation system uses hyperbolic LOPs (lines of position) to determine position fixes. In certain respects, DECCA combines features of both Loran and Omega; however, the application of these features differs in the two cited systems. Very little, if any, applications have been made where DECCA was interfaced with automatic navigation. Normally, the end output is either three visual indicators or a strip-chart-type flight log. For the application under consideration the input from receiver will have to be buffered in the input/output (I/O) to produce digital data for computer processing.

#### Inputs

<u>Phase difference</u>. - These ac inputs will be processed in pairs. Since there are three pairs, a total of six wires will be required. The pairs are designated red, green, and purple. The difference in phase between two wires of a pair represents the position within a lane, and is generated as a result of comparison between transmissions from the master and one of the slaves; i. e., red, green, or purple. One line of each of the pairs is the reference for that pair.

Input frequencies are:

- Green = 255 kHz
- Red = 340 kHz
- Purple = 425 kHz

The phase difference will vary from 0 degree to 360 degrees for each of the pairs as a lane is traversed.

The I/O should be capable of converting this ac phase difference into a digital signal for computer processing. The input to the computer central processor could then be either a serial or parallel binary interface.

<u>Lane identification</u>. - Three input discretes from the receiver are required for lane identification. These discretes occur at the rate of one per minute in the following order (L. I. = lane identification):

- Red L. I. occurs every whole minute
- Green L. I. occurs 15 seconds after red L. I.
- Purple L. I. occurs 15 seconds after green L. I.

<u>Control inputs (from control panel)</u>. - Provision should be made for selection of mode of operation of DECCA. These would be in the form of coded discretes and would operate in conjunction with the control inputs described in the Loran C discussion. Among the functions of these discretes would be:

- Entry into DECCA mode
- DECCA test mode

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• Reset DECCA oscillator

## Outputs

<u>Mode discretes</u>. - These discretes are outputs to the receiver and are used to control the DECCA receiver as necessary to conform with the input controls described above.

## APPENDIX C

## BASELINE AALS AUTOMATIC FLIGHT CONTROL SYSTEM EQUATIONS

- 1) Initialization of the difference equations is implied.
- 2) Bookkeeping terms for the difference equations are implied.
- 3) Two fader subroutines are to be included:

a) 
$$\frac{s+1}{s(2s+1)}$$

b) 
$$\frac{1}{2S+1}$$

4) If a stick signal inhibits velocity commands from the guidance system, two velocity synchronizers will be required.

Input to AFES

	Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
_	JIA,S	Indicated Air Speed from Air Data System	ft/sec			• 1 5thec	30/3ec	
	3	Side Slip Angle form Fir Data System	Rud			. 00 174 jewd	3%; uc	
	hBaro	Baro Altitude from Air Data System	<i>†</i>			·1 <i>5</i> +	19/\$ec	
	E_	Pitch Electric Stick	IN			NI 210 .	30/3ec	
	Es	Roll Electric Stick	in		4	w 1013	30/s'ec	
	ER	Electric Pedul	IN			·005 N	30/see	
	Ecol	Collective Electric Stick	הו			a, 410.	10/3ec	
	Ŭ,	Command from Guidonce	St/see		ţ	•15t/sec	2/3cc	
	'nc	Attitude Rate Command From Guidance	<del>St/sec</del>			144/5ec	10/sec	
	h glide	Glide Path Rate Command From Guidance	St/sec			·1 ft/see	10/5°c	
	ν <sub>c</sub>	Vehicle Side Velocity Command From Guidance	St/sec			.   ft/sec	<sup>2</sup> /sec	
	£y.	CROSS COURSE Velocity Command From Guidance	St/sec			·14+/sec	10/\$0c	

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Input To AFCS

Term	Description	Units	Accuracy	Range	lesolutio	Sample Rate	
Ū	Inectral measurement of component of Vehicle Forward Velocity in the	ft/sec			, 1 <del>51/5</del> 0c	2/3ac	
HOI	plane parallel to cuithe Surface from Nou System 'lehicle Elevation.	Rad			. 00   Rod	3%sec	
⊕ <sub>R</sub> (n-i)	Angle (Earth 11213) Jean New System Vehicle body angle	Rad			.0000 145	30/3ec	
	trom some arbitrony Reference from Not System while i=0=7			•	Kaa		
h <sub>I</sub>	Inential Altitude Rate from Noo System	\$t/s.c			,15t/sec	10/sec	
U <sub>I</sub>	Incetial Component of Vehicle Lateral Velocity in the plane parallel to the conth's surface from Now System	St/sec		,	1 \$+/sec	2/sec	
Φ	Vehicle Roll Angle (Eurth Dxis) from New System	Rad			• 001 Rad	39 sec	
ф(N-с)	ichicle Roll Body Angle Scom some arbitrary Reference from	Rad			• 0000145 Rad	30/sec	
	Now System where i = 0 -> 7						

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Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Ŧ	Vehicle Heading Angle (Earth Aris) From Nav System	Rad			1 00/ Rac	30/3ec	
4 (w-i) a	Vehicle your body angle Srom and arbitrary Reference from Abu System where i= 0 => 7	Rad			• 0000145 Rod	39/5ec	
				•		<b>`</b>	
				-	•		

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Output from AFCS

	Term	Description	Units	Accuracy	Range	Resolutio	Sample Rate	
-	<i>ک</i> ړ د	Differential Collective (Pitch) Command to Pitch EISS	N			, 000 25 vi	30/Sec.	
	O <sub>col</sub>	Collective Commond to Collective EISS	אן			,00025 <sub>M</sub>	10/3ec	
<b>N</b>	N - X	Autopilot Altitude Comman Fredback Signal to Guidan	f ft e			۰ <i>۱                                    </i>	10/sec	
•	SRC	Differential Cyclic (Yaw) Command to Rudder EIS,5	)N	÷	i	• 000 25 <sub>W</sub>	30/Sec	
	Ssc	Cyclic (Roll) Command to Roll EISS	J.N		1	دم <b>، 25 000 .</b>	30/\$ec	
							•	
						•••		

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Pitch Aris A/p

Math Description:

$$G_{\pm} = constant$$

$$K_{\pm} = constant, \quad V_{TM} \leq 50.7 \ f^{\dagger}/sec$$

$$= constant, \quad V_{TM} \leq 50.7 \leq V_{M} \leq 101.4 \ f^{\dagger}/sec$$

$$= constant, \quad V_{TM} \leq 50.7 \leq V_{M} \leq 101.4 \ f^{\dagger}/sec$$

$$K_{\Phi S} = constant, \quad V_{TMS} \leq 50.7 \ f^{\dagger}/sec$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Gé	Pitch Rote damper Gain	IN Stick Rod/Sec				·· ··· •	
kà	Hatopilet Rate Compre Gains	IN Stick Rad /sec	<b></b>			<b></b>	
Ken	Attitude Reference Gain	IN Stick Rod			:	39/se c	
Kos	Fritucia Survinonner Gain	1N Stick Roct			·	30/6¢ c	

Function: Pitch Axis A/P

Math Description:

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$$K_{\Theta_{c}} = Constant$$

$$K_{\delta_{L}} = Constant$$

$$V_{ZAS} < 50.7 \ \text{ft/sec}$$

$$= Constant - (V_{AS} 50.7) \cdot 0.38 \qquad 50.7 < V_{SAS} < 101.4 \ \text{ft/sec}$$

$$= Constant \qquad V_{ZAS} > 101.4 \ \text{ft/sec}$$

$$K_{h} = Constant$$

$$K_{h} = Constant$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Kæ	Velocity Commond Bain	<u>IN. Stick</u> ft/sec.	. –				
KSL	Stick Commond Gain	IN Stick	-	<b>.</b>	-	<i>3%</i> 5ес	
K <sub>h</sub>	Hiltitude Rate Command per Altitude Error Gain	ft/sec ft	-	-		-	
K'n	Collective per Altitude Rate Erron Gain	in pt/sec	-		-	-	
		•					

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Math Description:

$$\mathcal{K} = constant 
\mathcal{K}_{\overline{u}} = 1.0 \qquad \mathbf{Y}_{\overline{ns}} < 67.6 \quad \mathcal{H}_{15c} 
\mathcal{K}_{\overline{u}} = 2.2 - \frac{V_{\overline{sns}}}{V_{\overline{sns}}} \qquad 67.6 < V_{\overline{sns}} < 135.2 \quad \mathcal{H}_{15ec} 
\mathcal{K}_{\overline{u}} = 0.0 \qquad \mathcal{H}_{\overline{sns}} \qquad \mathcal{H}_{\overline{sns}} < V_{\overline{sns}} \\
\mathcal{K}_{\overline{u}} = 0.0 \qquad \mathcal{H}_{\overline{sns}} + \mathcal{H}_{\overline{sns}} < V_{\overline{sns}} = \mathcal{H}_{\overline{sns}}$$

Term	Description	Ünits	Accuracy	Range	Resolutio	n Sample Rate	
x	Stock to Suma and and	in	-	-			
Bre	Indicated to the	st/se:			o   51/soc	3 %'se c	
Kū	Velocitic Bosconne Schert Lessie Gori				• 1 <i>41/3</i> 2	2/ <b>se</b> c	
Kenii	Collection Compression pitch pate	<u>IN</u> Rodite e	· · ·	•	-	-	
K <sub>erold</sub>	Collection Consideration Notes - Consideration	IN Reinja c	-	-		-	•
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Math Description:

Un = Vragi costal cost = K<sub>ii</sub> ũ, + (1.0 - K<sub>ū</sub>; ū<sub>A</sub> Is Novigation Switch ON - No - Oc = 0.0 (CoTo Nort Pare) i le;  $\Theta_c = \overline{u} + \overline{u}_c$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
<i>u</i> <sub>I</sub>	mential mensurrit of concentration derived Forward Velocity (X body axis) inter plane parallel to the cantil during (from Nou Suster)	St/see		•	• 1 <del>\$ 1/2</del> 000	Z/sec	
ū,	AIR NOSS Measurement of component of Vehicle Forward Velocity (x body axis) in the plane poralled to the contra Surface	-5+/3°C	~		- / <del>51</del> /sec	?!/sec	

Pitch Axis F/p

-	Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
	191	Vehicle Elevation Anole from Now System	Red		-	.0001 Ral	30/300	
	د)	Vericle Side din Frair	Red			<b>,0017</b> ''	19 <b>* 4</b> •	
	£	A Hatar of Common for	ft/sec			. 1 [0]	2/5-2	
	<i>ب</i> ر	Velocity Commond from Guidonce	ft/:ec		-	· 1 place	2/3.	
	ū	Volarity Fredlinsk	f1/50.		•		2/sec	
		•			I			
		,			,	1		
							`	
					•			
						•		

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Math Description:

$$\begin{aligned} \Delta e_{A}^{(W)} &= \frac{4}{4} \frac{(W)}{7} \\ \dot{h}_{hyb} &= \dot{h}_{I} \\ \dot{h}_{hyb}^{(I)} &= \begin{cases} h_{A}^{(I)} \left[ b + a_{T}^{2} \right] + h_{Bano}^{(W-1)} \frac{2}{5} + h_{Bano}^{(I)-1} - a_{T}^{2} \right] + \dot{h}_{I}^{(W)} \left[ \frac{2}{7} \right] - \dot{h}_{I}^{(W-2)} \frac{2}{7} \\ - h_{Yb}^{(W-1)} \left[ 2b - 2\frac{4}{7} \right] - h_{hyb}^{(I)-1} \left[ \frac{4}{7^{2}} - a_{T}^{2} + b_{T}^{2} \right] / \left[ \frac{4}{7^{2}} + a_{T}^{2} + b_{T}^{2} \right] \end{aligned}$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate
er	Vehicle Pitch HHitude (ARDI- teary bidy axis) From Nou Systim	Rad	-	•	.00006	S.M.C.
∆ e <sub>r</sub>	Para and the We have to gottek	H and	-		.00006 R.d	corter.
T	Some Permor (Constant)		-	<b></b>	,0001 Sec	30%
$K_{\mu\nu}$	Altotade Pate From Altotic. Soutions objection	St/sec	-	<b>.</b>	.1 ft'sa	19/20 c
h <sub>I</sub>	Attitude Rate From Incontrol Sensing System	ft/de c	-	<b>9</b>	•11 <sup>1</sup> /sc	19/3
H <sub>Baro</sub>	Baxometric Altitude	<u>}</u> +		<b>,</b>	·15+	10/50 c
hiyb	Altitude Form Altitude Grasing System	<i>ft</i>		-	11 f.t	10/sec

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Pitch Axis A/P

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
þ	constant			-	-		
a	constant	-		-	-	-	
<del>\</del>	Vehicle Rate (body axis)	Rod isac		••••	.001 Roffee	20/ toe	
1							
				, i			
	· · .						
				ı			
						``	
		i i					
						Г.	

Pitch Pier rip

Math Description:

 $f(n) = \left\{ \hat{\Theta}(n) \left[ \mathcal{L}_{r} \stackrel{2}{=} + 1.0 \right] + \hat{\Theta}(n, n) \left[ 1.0 - \mathcal{L}_{r} \stackrel{2}{=} - f_{r}(n-n) \left[ 1.0 - \mathcal{L}_{r} \stackrel{2}{=} \right] \right\} / \left[ \mathcal{L}_{r} \stackrel{2}{=} + 1.0 \right]$  $f_{2}(w) = \begin{cases} f_{1}(w) \left[ z_{1}^{2} + 1/\sigma \right] + f_{1}^{2}(w-1) \left[ 1/\sigma - z_{1}^{2} + \frac{1}{2} - f_{2}^{2}(w-1) \left[ 1/\sigma - z_{8}^{2} + \frac{1}{2} - \frac{1}{2} + \frac{1}{2} - \frac{1}{2} + \frac{1}{2} - \frac{1}{2} + \frac{1}{2$  $\frac{1}{3}(w) = \frac{1}{2} \log(w) \left[ \frac{1}{2} + \frac{1}{$ 1 f= 1 = AB,5 [1=]

Term	Description	Ünits	Accuracy	Range	Resolutio	n Sample Rate	
<i>†</i> ,	First F. Sewed Function	Roch	-	-	.001 Kodijse	30/gec	
72	Same Follored Function of 6	Rock	-		. 00 1	3%see	
13	F. Hered Function of 101	R.Y			,000/ Prk	30% Sec	
2 => 20	Conta			-	, <b>6</b> 4 * 1		
<b>f</b> 2	mogertude of fz	Rad/Sec	—	<u> </u>	. 00 / Rod/sec	10/jec	

Pitch firis A/p

 $\left[1.0 + 1.59 \frac{2}{7}\right]$ 

Math Description:

 $S_{C_{1}}^{(1)} = \left\{ G_{*} \left[ \left( 1.0 + .05 - \frac{3}{7} \right) f_{2}(N) + \left( 1.0 - .05 - \frac{3}{7} \right) f_{2}(N-1) \right] - \left( 1.0 - 1.59 - \frac{3}{7} \right) S_{N_{e_{1}}}^{(N-1)} \right\}$ 

δ <sub>1</sub> (ν)	= $\int K_{e} \left[ (1.0+\frac{2}{4}) f_2(\mu) + (1.0-\frac{2}{4}) f_2(\mu-\nu) \right] + K_{eR} \left[ (1.0+\frac{2}{4}) f_3(\mu+\nu) + (1.0-\frac{2}{4}) f_3(\mu-\nu) \right]$
	$-K_{\delta_{L}}\left[(1,0+\frac{2}{7})(2(0)+(1,0-\frac{2}{7})(2(0)-1)\right] + \frac{2}{7} \delta_{L_{\delta_{2}}}(0,-1) \left\{ / \frac{2}{7} \right\}$
I,5	$\begin{bmatrix} Nav & Switch & 0N \end{bmatrix} \xrightarrow{N_{n}} & T_{s} \begin{bmatrix} E_{L} \leq t \\ X \\ Y \\ Y \\ Y \\ Y \\ Y \\ Y \\ S \\ Y \\ S \\ Y \\ S \\ Y \\ S \\ S$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Shei	Filler and x 1 Collection Jen Pitch Rate Domper Ling	IN	-	<b></b> .	,00'025 W	39/50c	•
EL	Electare Stick input	N			. 012 IN	30/5ec	
$\Theta_{\mathcal{B}}$	Synchrowiger Eind	Rad	-	-	. 000 [ Rad	30/sec	
<del>O</del> ,s	Symphony Ortput	Rok	-		.0011 Rad	30/3.c	
SIC2	Differential Collective For Autopilet Rode Lange - Hink Josput	JN		•	.00025 "W	30/ Jec	

Pitch Arris Alp

Nath Description:  $\sum_{k=1}^{N} = \left[ X_{o_{k}} \left[ \left( -\frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} \right) \Theta_{k}(k-1) + \left( 1 + \frac{y}{2k} + \frac{y}{2k} \right) \Theta_{k}(k-1) \right] \\
= K_{o_{k}} \left[ \left( 1 + \frac{y}{2k} \right) \Theta_{k} + \left( \frac{y}{2k} \right) \Theta_{k}(k-1) + \left( 1 + \frac{y}{2k} + \frac{y}{2k} \right) \Theta_{k}(k-1) \right] \\
= \left( -\frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} \right) \left\{ \frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} \right\} \\
= \left( -\frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} + \frac{y}{2k} \right) \left\{ \frac{y}{2k} + \frac{y}{2k}$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Sr. 3	A Constant of Bolton	171		•	, 00025- /N	20 (tor	
	2 mil Velocity Commune						
FELC	Total Triffrend to Mesting	, <i>11</i>	-		, 00025 IN	301	
							ł

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Pitch Aris Alp

Math Description:

$$\begin{split} G_{S_{L_{c}}^{(n)}} &= \left\{ \begin{array}{c} F_{S_{L_{c}}^{(n)}} \left[ \cdot 001375 \frac{y}{\tau_{L}} + \cdot 0037 \frac{x}{T} + 1 \cdot 0 \right] + F_{S_{L_{c}}^{(n)}} \left[ 2 \cdot 0 - \cdot 00275 \frac{y}{T_{L}} \right] + F_{S_{L_{c}}^{(n)}} \left[ \cdot 001375 \frac{y}{T_{L}} - \cdot 0037 \frac{x}{T_{L}} + 0037 \frac{x}{T_{L}} \right] \\ &- G_{S_{L_{c}}^{(n)}} \left[ 2 \cdot 2 - \cdot 027 \frac{y}{T_{L}} \right] - G_{S_{L_{c}}^{(n)}} \left[ \cdot 001375 \frac{y}{T_{L}} - \cdot 0277 \frac{x}{T_{L}} + 1 \cdot 0 \right] \\ &\left[ \cdot 001375 \frac{y}{T_{L}} + \cdot 057 \frac{x}{T_{L}} + 1 \cdot 0 \right] \\ &\left[ \cdot 001375 \frac{y}{T_{L}} + \cdot 057 \frac{x}{T_{L}} + 1 \cdot 0 \right] \\ &\delta_{L_{c}}^{(n)} \right] = \left\{ \begin{array}{c} G_{\delta_{L_{c}}}^{(m)} + 2 \cdot 0 & G_{\delta_{L_{c}}^{(m)}} \right] + G_{\delta_{L_{c}}^{(m)}} \left[ 2 \cdot 0 - \cdot 0277 \frac{y}{T_{L}} \right] - \delta_{L_{c}}^{(m)} \left[ 2 \cdot 0 - \cdot 0277 \frac{y}{T_{L}} \right] \\ &\delta_{L_{c}}^{(n)} \right] \\ &+ 1 \cdot 0 \end{array} \right\} \\ &\left\{ \begin{array}{c} F_{\delta_{L_{c}}}^{(m)} + 2 \cdot 0 & G_{\delta_{L_{c}}^{(m)}} \right] + G_{\delta_{L_{c}}^{(m)}} \left[ 2 \cdot 0 - \cdot 0277 \frac{y}{T_{L}} \right] - \delta_{L_{c}}^{(m)} \left[ 2 \cdot 005575 \frac{y}{T_{L}} - 0277 \frac{y}{T_{L}} \right] \\ &+ 1 \cdot 0 \end{array} \right\} \\ &\left\{ \begin{array}{c} F_{\delta_{L_{c}}}^{(m)} + 2 \cdot 0 & G_{\delta_{L_{c}}^{(m)}} \right\} \\ &\left[ F_{\delta_{L_{c}}}^{(m)} + 1 \cdot 0 & G_{\delta_{L_{c}}^{(m)}} \right] + 0 \\ &\left[ F_{\delta_{L_{c}}}^{(m)} + 1 \cdot 0 & G_{\delta_{L_{c}}^{(m)}} \right] \right\} \\ &\left\{ \begin{array}{c} F_{\delta_{L_{c}}}^{(m)} + 1 \cdot 0 \\ F_{\delta_{L_{c}}}$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
GSLC	First Filterod Function of Total Differential Collective	N	-	•	.000 25 1N	31/	
δLe	Second Filtered Function of Total Differential Collective	JN		. —	, 000 25 IN	30/sec	
		. ·		. •			

Collective Axis

 $\begin{array}{l} \text{Math Description:} \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \left[ \frac{1}{2}, \frac{2}{2} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{2} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{2} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{2} + 1, 0 \right] \right] \right\} \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \right] \right\} \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \right\} \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] + \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} + 1, 0 \right] \\ f_{s}(\lambda) = \left\{ K_{s}_{colo} \left[ \frac{1}{2}, \frac{2}{3} +$ 

Term	Description	Units	Accuracy	Range .	Resolutio	n Sample Rate	·
2,->24	Constant,s	<b></b>	<b></b>	<b></b>		1	
41	2 and filtener Function of g (Absolute Value)	Rod/1 ec	<u> </u>	_	,001. 120/15c	39/sac	
<i>†5</i>	3Bel Filtened Function of ÷	Rodffee	·	-	, 001 Radijec	30/sec	
ţ.	3Rd F. Hencel Function of f.	Rod/jec	-		•001. Pod/sec	39/ Jec.	
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Function: Collective Axis

Math Description: Is [Alt. Hold On] No Yes V Kin = Constant Is [Now Switch On] - No he=0 K=0.0 Kg= Constant JYr: Ki= Constant, Kg = 0.0 he = guidence Input Quill = K E W ke = 0.0  $V_{r,s} = h_{ky_{k}} = 0.0$  $h_{ky_{k}} = h_{ky_{k}} + h_{g_{1}}^{(u)} + h_{g_{1}}$ Is [Glide Slope ON] • •• ·· INO  $I \leq \begin{bmatrix} V \\ F | are Ow \end{bmatrix} \xrightarrow{Ve \leq} h_{nyb} = 0.0$  $| Ne \qquad h_{nyb} = h_{syb} + h_{glide}^{(\omega)}$ Go To Next Page

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
κ <sub>τ</sub>	Feedback Gains of he	Ht/sec fr	_		١	·	
 Ocotec	Initial Condition of Ocol	IN			.014 <sub>10</sub>	10/sec	
h glide	Glide Path Rate	ft/sec	-	-	,1 ft/see	19/sec	
ĥc	Altitude Rete Commond	ft/80 c	-	-	,1 fxfie.	1%sec	
	•						
Eul	Electric Collective Stick	IN		•	:014 1N	14sec	

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Collective Aris

$$\begin{split} & \text{Math Description:} \\ & h_{e}^{(\omega)} = \left\{ \begin{array}{l} \frac{2}{7} h_{h_{Vb}}^{(\omega)} - \frac{2}{7} h_{h_{Vh}}^{(\omega-1)} - h_{e}^{(\omega)} - h_{e}^{(\omega-1)} - \mathcal{E}_{ead}^{(\omega)} - \mathcal{E}_{ead}^{(\mu-1)} - \left[ K_{f} - \frac{2}{7} \right] h_{e}^{(\mu-1)} \right\} / \left[ \frac{2}{7} + K_{f} \right] \\ & h_{e}^{(\omega)} = \int_{1}^{1} \frac{1}{5} \left( \frac{\omega}{5} \right) + \int_{1}^{1} \frac{1}{5} \left( \frac{\omega}{5} \right) + h_{h_{F}}^{(\omega)} + K_{h_{F}} h_{e}^{(\omega)} + \mathcal{O}_{ead}^{(\omega)} \right) \\ & \mathcal{O}_{col} \left[ \frac{\omega}{5} \right] = -K_{h} h_{e}^{(\mu)} \\ & h_{e}^{(\omega)} = \left\{ \mathcal{E}_{col}^{(\omega)} + \mathcal{E}_{col}^{(\omega-1)} + h_{e}^{(\omega)} + h_{e}^{(\omega-1)} + \frac{2}{7} h_{e}^{(\omega-1)} \right\} \right\} / \frac{2}{7} \end{split}$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
he.	Altitude ERRO Signal	ft.		-	.1 \$+	10/\$ec.	
he	Altitude Rate ERROR Signal	ft/sec		•	. 1 <del>{1</del> /gec	10/6°02	
Oole	Collective Command to EIS,5'	jų -	-	-	, 00025 ,N	10/sec	
			•		•		

Math Description:

 $K_{\phi_R} = Constant$   $K_{\phi_R} = Constant - .435(V_{SRS} - 50.7)$   $K_{\phi_R} = Constant$   $K_{\phi_S} = Constant$   $K_{\phi_S} = Constant + .435(V_{SRS} - 50.7)$   $K_{\phi_S} = Constant$ 

$$V_{IAS} < 50.7 ft/sec.$$
  
 $50.7 \leq V_{IAS} \leq 101.4 ft/sec.$   
 $V_{IAS} > 101.4 ft/sec.$   
 $V_{IAS} < 50.7 ft/sec.$   
 $50.7 \leq V_{IAS} \leq 101.4 ft/sec.$   
 $V > 101.4 ft/sec.$ 

Gig	r = Constant					
Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate
K <sub>ér</sub>	Roll Attitude Reference Gain	IN Stick Rad	-	-	1	3%sec
K <sub>¢s</sub>	Roll Attitude Synchronian Gain	in ste Rad	-		_	30/5ec
G <sub>øg<sub>R</sub></sub>	Roll Rate to differential cyclic (Ruddor) Equi	N Pathi Rad/sec	-		•	_
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Lateral A/p

Math Description:

$$G\phi = Constant$$
  
 $K\phi = Constant$   
 $Ks_s = Constant$   
 $V \leq 50.7 \ f^{+}/sec$   
 $= Constant - .0277 (V_{IAS} = 0.7)$   
 $= Constant$   
 $V_{IAS} > 101.4 \ f^{+}/sec$   
 $G_{\psi} = Constant$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Gġ	Roll Rate Damper Gain	IN stick Rad/sec	, <b>1</b>	-	. —	-	
Κġ	Autopilot Roll Rate Gain	in stick Red/sec			_		
K§s	Roll Stick Command Gain	<u>IN stick</u> IN stick	-	ł	-	3%sec	
Gji	Yow Rote Damper Gain	<u>IN Peda</u> l Rad/sec	-	-	-	-	
	·						

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2 stand Alp

Math Description:

Ko Constant Vip 1 - Di Hisa NA = Construct - 19128 (1977 199) (1977 - 197 Vy 19 1944 Viet to 101. " " Bee X= : 0.0

V. ... 2 37.3 - 114 Ky = 0.0

Kup = .37 Viet

Sec. 5 Oak

GA = 124 Vore : Vare : Star 144

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North 2 Carton Contraction

Vine Contraction

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
K.z.	Veloeita Cranad Gans	1) (****) ******		•		2/50-	
K <sub>v.</sub>	Heating Supplies and	era (ment) Tengan	•				
Gr	Englished the deficiency test Cuplie Charles Clements	u Rodal Kad	-	~	•.		
							,

Lateral H/p

Math Description:

VIAS < 50.7 St/See ···· = 0.0 Kye = k VrAs

VIAS > 50.7 ft/see

KSR - Constant Ky = Constant Ky\_ = 0.0  $K_{Ve} = Constant$   $K_{Ve} = 0.0$   $\chi\chi = Constant$ XX

VIAS < 50,7 ft/sec VIAS 2 50.7 ft/Sec Vson < 50.7 Stilsec Vroi 2 507 ft/sec

17 - 20 - 20	= constant						
Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Kyc	Velocity Commond Gains	IN Stick St/Sec		<b>-</b> -	-	10/s'ec.	
Kór	Pedal to differential Collective (Rudder) Gains	in Pedal in Pedal	_	_	_	39/sec	
Ky_	Heading to differential Collective Gain	IN Perlal Rad	<del></del> .	-	-	39/sec	
Wyc	Heading Command to differential Collective Goin	IN Fedal Rock	-		-	10/sec	
XX	Roll Stick to Synchronijer Breakout Logic Scarbank	نمز	<b></b> -		-	-	
XXX	Pedal to Synchemizer Breakout Logic Tiendons	AI	-	-	-	-	
4	Roll Synchro Dead band	Red				-	

Lateral Alp

Math Description:

 $\Delta \phi_{e}(n) = \phi_{e}(n) - \phi_{e}(n-1)$ Pc = 75 - 50

·	Teim	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
	Δ¢	INCROMENTAl Vebuch Kall Hingle (Bady Avis)	Racl	-	<b></b>	. 0.0006 Rad	30/5 cc	
	₹ <sub>R</sub>	Vehicle Roll Plapic Chelitering to de French Fermi Nou System	Rac	-	·	.00 006 Rad	30/ <i>3</i> c c	
	īr	Vehicle Side Velicity W.R.T. earth from Nov System	St/Bec		-	•1 <del>\$</del> 1/se	2/ <sub>Śec</sub>	
	$\overline{\nu}_{c}$	Vehicle Side Velocity command form Guiannes	ft/3 rc	-	4	• 1 ft/sec	2/sec	
	e de la	Kincle Rel Conversed	f#/sec	—		•1ft/sec	2/2'ec	
	Eine	CROSS COURSE Kelseits ERDOR Command	St/sec		-	•1ft/sec	10/ sec	

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# REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR

Function: Lateral A/p

Math Description:  $G(W) = \Delta f(W)' -$ 

• 7

A 4/(N) = 4/(N) - 4/2 (N-1) 4(W) = \$ 4(W)

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	-
ø	Vehicle Roll Rate	Radisce		. Bar a	.00   Rad/tex	30/2cc	
Ý	Vehicle Vaii Ratie	Rod/See			.001 Red/fec	30/Sec	
D K	INCREMENTAL Heading Angle	Rad	-	. <b></b> . *	,00006	30/8rc	
¥.	Vehicle Yow Gruple From Nou System	Red	-		.00006. Mid	37.500	
		·					
		•					

# REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR.

#### Function:

Lateral Alp

 $\begin{aligned} &\text{Math Description:} \\ &\mathcal{L}_{1}(r^{2}) = \left[ \sum_{n=1}^{n} \sum_{i=1}^{n} \frac{1}{r_{i}} \left[ r_{i} \right] + \left[ 1.0 - 2r_{i} \frac{1}{r_{i}} \right] \frac{1}{r_{i}} \left( r_{i} \right) - \left[ 1.0 - 2r_{i} \frac{2}{r_{i}} \right] \frac{1}{r_{i}} \left( r_{i} \right) \right] \right] \left[ 1.0 + 2r_{i} \frac{2}{r_{i}} \right] \\ &\frac{1}{r_{i}} \left[ \frac{1}{r_{i}} \frac{2}{r_{i}} + 1.0 \right] \frac{1}{r_{i}} \left[ \frac{1}{r_{i}} \frac{2}{r_{i}} \frac{2}{r_{i}} \right] \frac{1}{r_{i}} \left[ \frac{1}{r_{i}} \frac{2}{r_{i}} \frac{2}{r_{i}} \right] \frac{1}{r_{i}} \left[ \frac{1}{r_{i}} \frac{2}{r_{i}} \frac{2}{r_{i}} \frac{2}{r_{i}} \frac{2}{r_{i}} \frac{1}{r_{i}} \frac{1}{r_{i$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
i - Z22	Constants'		-		-		
٤	FIRST Follower Transform	No Ary See		-	, 100   Rod/sec	30/ ser	
1,	Second Filtensed Function of d	Rodine		-	. 001 Radify	30/ 5 er	
Ļ	Filtered Investige of \$	Tired			. 0001 Rad	<sup>30</sup> /50c	
↓ <sub>Ţ</sub>	Fultoned Function of W	Rad			.0001	3°/sec.	
₽. I	Vehicle Roll Angle (Egethi Aus) From Nov System	Rod		•	Rod .0001 Rod	30/ju	
Ţ	Vehicle Heading Angle (Eurth Aris) From Nou	Rad	-	-	.000   Rçd	30/sec	

#### ORIGINAL PAGE HE IS

Function:

Lateral 17/12

Math Description:

 $S_{\frac{1}{2}}(N) = S_{\frac{1}{2}}\left[\int_{0}^{1} \frac{1}{2} + \frac{1}{2}\int_{0}^{1} - \frac{1}{2}\int_{0}^{1} \frac{1}{2} + \frac{1}{2}\int_{0}^{1} \frac{1}{2} + \frac{1}{2}\int_{0}^{1} \frac{1}{2}\int_{0}^{1}$ - Ks, [E, (1)] + 1.0] + E, (1) [10-3] + 5, (1-) = ] / [ = ]

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
6:01	Roll Cyclic pra Poll Rate Dampen	טון			, 0 0025 IN	20/3ec	
dec 2	Attractic sen Roll Attracts and Strek	<i>IN</i>		•	.00025 IN	30/3ec	
E.	Election Stick Lamie Doll)	' , <b>13</b>	-		.013 /14	31/3++	

Lateral A/p

Math Description:

fin = { [Z, = +1.0] + (1.0 - 2, = ] + (0.0 - 2, = ] + (0.0 - 2, = ] + (0.0 - 2, = ] / [1.0 + 2, = ] ]  $\frac{1}{8}(N) = \left\{ \left[ z_{3}^{2} + 1.0\right] f_{4}(N) + \left[ 1.0 - z_{3}^{2} + 1.0\right] - \left[ 1.0 - z_{3}^{2} + 1.0\right] \right\} \right\} \left\{ \left[ 1.0 + z_{3}^{2} + 1.0\right] \right\}$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
だっってい	Constant p		<b></b>		<b></b>	<b>40</b> ~0 ** 1	
47	Frast Filtered Function of 4	Rod/sec	-	• •	.001 Rack	30/5'er	
<b>†</b> 8	Second Filtroed Function Of Y	Rod/	-	<b></b>	1001 Ead/sec	70/sec	
				•		•	
				•			

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Latenul Alp

Math Description:

It ENow Switch Vei !	$h  O_{NJ} \xrightarrow{N_{C}} I_{S} \left[ f_{J} \right]$ $J_{S} \left[ \xi_{S} \le 1 \right]$	<pre></pre>	$   \begin{aligned}         I_{s} & \leq t  \gamma \gamma \\         N_{0} & \downarrow \\         P_{0} & = - \{ \eta \}   \end{aligned} $	$\frac{Ye}{2} \phi_{3} = \int_{11}^{1+} \phi_{B}$
di = di,i Um d'inne	<	<b>)</b>		

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Ø.	Synchronger Koll Biasi	Red	-	æ	<b>,000/</b> Ruel	30/54	
Φs	Synchronizen Output Rall	Rad	-		• 000 / Rod	30/5'ec	
		c					
	• • •						

## REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR.

#### Function:

Lateral Fla

#### Math Description:

 $J = [N_{av} \leq u_{v} d - h > D_{v}] \qquad T = \begin{bmatrix} \mathcal{E}_{a} \leq t + v_{v} \text{ and } \mathcal{E}_{R} \leq t + v_{v} \end{bmatrix} \qquad \mathcal{H}_{B} = -f_{q}$   $V_{B} = -f_{q}$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
Y <sub>8</sub>	Heading Synchnewizer. Hund	t an	-	<b>b</b>	0001 12ad	30/irc	
	Hearing Symphon gene Output	Rod	-	<b></b>	, 000 1 Kad	<sup>20</sup> /sec	•
Er	Electric Redat Japut (Jan)		-	-	105N	30%, See	

Function: Lateral A/P

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Math Description:

ð	$\int_{S_{C_3}} (\omega) = \begin{cases} 0 \\ 0 \\ 0 \end{cases}$	Ko [ φω [· 5 ¥· + 1.5 ]+ ···] +Ko [ φω [÷+1.0]+ φω·· ) [2	+ \$.{~-1) { ] + \$	[2.0 - 4 [2.0] [1.0	]+ \$.~. - 7]	)[1.0 - 1.5 + $\delta_{s}(u)$	₹ +.5 ¥ 7) ^4 ] 7)	-
	C .:	$- \delta_{\frac{1}{2}}(\psi, z) \left[ (5 + \frac{1}{2} - \frac{2}{2}) \right]$	15.5	₩ + 27 ₩	-			-7
	ο <sub>≴ςψ</sub> =	$ = K_{y_{a}} \left[ Y_{s}^{(w)} \left[ \cdot 5 \# + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] + \mathcal{E}_{y_{a}}^{(m)} \left[ \frac{2}{2} + 1 \cdot 6 \right] +$	·1·0] + 4 1)[2·0] +	¢, (u - 1)[.?.0) ¢, (u - 2)[0	·- ネ゙! + ·- ネ]+	5 <b>5</b> (N-1) 5 5 (N-1)	,2 -  ,5 ₹, 4 [ <del>4</del> [ <sup>7</sup> 2]	.\$ 42]]
-	Term	$ \begin{array}{c}  5  (v-2) \left[ \cdot 5  \frac{4}{7^2}  -  \frac{2}{7} \\ \end{array} \right] \\ \begin{array}{c} \text{Description} \end{array} $	/ { Unite	¥₂ + ≩] Accuracy	Range	Resolutio	n Sample Rate	
	<i>Б</i> зсу.	Roll Cyclic PER Heading Synchronizer and Velocity Commond	مر		<b>BNN</b> .	, <b>60025</b> JN	30/3ec	
	Sx3	(CROSS COURSE) Roll Cyclic PER Roll Synchronizer	110	•	•	• ●•025 JN	30/ 500	
		ond Velocity Command (body axis' ý)		-				

Lateral A/p

$$\begin{split} & \text{Math Description:} \\ & \mathcal{S}_{k} \begin{pmatrix} \omega \\ i \end{pmatrix} = \left\{ \left[ \mathcal{G}_{i \stackrel{i}{\partial}_{k}} \left[ \mathcal{H}_{k}^{(\omega)} + \mathcal{H}_{k}^{(\omega)} \right] - \mathcal{S}_{R_{c_{i}}^{(\omega)}} \left[ 1.0 - 3 \stackrel{2}{\mp} \right] \right\} / \left[ 1.0 + 3 \stackrel{2}{\mp} \right] \right] \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} = \left\{ \mathcal{G}_{i \stackrel{i}{\partial}_{k}} \left[ \mathcal{H}_{k}^{(\omega)} \left[ 2.91 \stackrel{2}{\mp} \right] - \mathcal{H}_{k_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{2}{\mp} \right] \right] - \mathcal{S}_{k_{c_{i}}^{(\omega)}} \left[ 2.0 - .982 \stackrel{4}{\mp} \right] \\ & -\mathcal{S}_{k_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} - \mathcal{I}_{s} \left[ 2.91 \stackrel{2}{\mp} \right] \right] - \mathcal{S}_{k_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} + 2.51 \stackrel{2}{\mp} + 1.0 \right] \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} = \left\{ \mathcal{G}_{g} \left[ \mathcal{G}_{(\omega)} + \mathcal{G}_{(\omega)} \right] - \left[ 1.0 - .3 \stackrel{2}{\mp} \right] \left[ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \right] \right\} / \left[ 1.0 + .3 \stackrel{2}{\mp} \right] \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} = \left\{ \mathcal{G}_{g} \left[ \mathcal{G}_{(\omega)} + \mathcal{G}_{(\omega)} \right] \right\} - \left[ 1.0 - .3 \stackrel{2}{\mp} \right] \left[ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \right] \right\} = \left\{ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} + 2.51 \stackrel{2}{\mp} + 1.0 \right] \right\} \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} = \left\{ \mathcal{G}_{g} \left[ \mathcal{G}_{(\omega)} + \mathcal{G}_{(\omega)} \right] \right\} = \left\{ 1.0 - .3 \stackrel{2}{\mp} \right\} \left[ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \right] \right\} = \left\{ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} + 2.51 \stackrel{2}{\mp} \right] \right\} \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} = \left\{ \mathcal{S}_{R_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} + 2.51 \stackrel{2}{\mp} \right] \right\} \\ & \mathcal{S}_{R_{c_{i}}^{(\omega)}} \left[ 2.91 \stackrel{4}{\mp} \stackrel{4}{$$

Torm	Description	Unite	Accuracy	Range	Resolutio	n Sample Rate	
ÓRC,	Yaw Cyclic per Roll Rute	N	-	<b>—</b>	.00025 IN	<sup>30/s'ec</sup>	
5 Rez	Yaw Gyclic per Yaw Rate	IN	-		.00025 //	30/yec	,
S <sub>Rc3</sub>	You Cyclic per Side Elip	או			. 00025 IN	30/Sec	
and a construction of the second seco	You Cyclic Peri Pedal Insput	,N	-		. 0002.5 IAI	30/sec.	

Lateral A/p

Math Description:

δ<sub>R(s)</sub> = { Ky [y, (y) [. 5 = +1.0] + y, (m) [1.0-.5 = ]] - Ky [E, (w) + E, (w-1)] - 8, grofto-, still / E. 5 + 1.5]

Term	Description	Unita	Accuracy	Range	Resolutio	n Sample Rate	
SRC 5	Yow Cyclic pez Headiwa Synchronian Ond Headiwa Common Twput	л. 1			.000Z5- 	30/3cz	

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Lateral Alp

Math Description:

י ד גר	$I_{s} [N_{nu} M_{o} M_{o} M_{o} M_{o}] \longrightarrow \delta_{s_{c_{s}}} = 0.0, \delta_{s_{c_{y}}} = 0.0, \delta_{s_{c_{y}}} = 0.0$ $Ve_{s} \downarrow$ $I_{s} [N_{our} Switch O_{N}] \xrightarrow{M_{o}} I_{s} [E_{s} > \pm \chi \chi] \xrightarrow{Ve_{s}} \delta_{k_{c_{3}}} = 0.0, \delta_{s_{c_{y}}} = 0.0$ $Ve_{s} \downarrow$ $I_{s} [ATV M_{o} M_{o} M_{o}] \xrightarrow{N_{o}} \delta_{s_{c_{y}}} = 0.0, \delta_{R_{c_{s}}} = 0.0$ $Ve_{s} \downarrow$ $Ve_{s}$											
F	$\delta_{n_{i}} = -a$	Sec, - SRe - SRes - JRey	- SRC ST									
	Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate					
_	Foic	Total Roll Cyclic Commond	, N	~		.000 25 N	30/sec					
	FSRL	Total Your Cyclic Command	N	—	-	.00025 IN	3% 5 C					
					•							
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Math Description:

$$\begin{split} G_{S_{s_{c}}^{(N)}} &= \left\{ F_{s_{s_{c}}^{(N)}} \left[ \cdot cc_{1375} \frac{4}{7^{2}} + 0037 \frac{2}{7} + 1.0 \right] + F_{s_{s_{c}}^{(N,1)}} \left[ 2.0 - 00275 \frac{4}{7^{2}} \right] \right. \\ &+ \left[ F_{s_{s_{c}}^{(N,2)}} \left[ \cdot cc_{1375} \frac{4}{7^{2}} - 0037 \frac{2}{7} + 1.0 \right] - G_{s_{s_{c}}^{(N-1)}} \left[ 2.0 - 00275 \frac{4}{7^{2}} \right] \right. \\ &- G_{s_{s_{c}}^{(N-2)}} \left[ \cdot 001375 \frac{4}{7^{2}} - 0037 \frac{2}{7} + 1.0 \right] \right\} \left[ \cdot 001375 \frac{4}{7^{2}} + 037 \frac{2}{7} + 1.0 \right] \end{split}$$

$F_{i}$ = $\begin{cases} F_{i} \\ F_{i} \end{cases}$	δR(H) [. 001375 4 +. 0037 + 1	.0] + F.	u-1). [2.0	00275	「纟」		
+ F,	Sat -2) [. 001315 400 37]	· +1,0] -	Gsre W-	) [ 2.0	00275	¥-]	
- 6 Term	$\delta_{R_{c}}^{(W-\varepsilon)} \left[ 00 / 375 \frac{4}{72} - 03 \right]$ Description	7 ≟ +/0 Unite	Accuracy	001375 Range	, +.037 Resolutio	$\frac{2}{7} \neq 1.0$ n Sample Rate	
G <sub>ðşc</sub>	First Filtered Function of Rold Cyclic	· در ا	-	<b></b> -	. 10075 N	30/ <u>5</u> ee	
6 5 <sub>2</sub>	First Filtered Function of Yow Cyclic	) N		-	.00025 .W	30/see	
			-	1.			

Math Description:

$$\begin{split} \delta_{s_{c}}(u) &= \left\{ \begin{array}{l} G_{\delta_{s_{c}}}(u) + 2.0 \ G_{\delta_{s_{c}}}(u-1) + G_{\delta_{s_{c}}}(u-2) - \delta_{s_{c}}(u-1) \left[ 2.0 - .0019 \ \frac{4}{7} \right] \\ &- \delta_{s_{c}}(u-2) \left[ .000595 \ \frac{4}{7} - .0244 \ \frac{2}{7} + 1.0 \right] \right\} \left/ \left[ .000595 \ \frac{4}{7} + .0244 \ \frac{2}{7} + 1.0 \right] \right\} \\ \delta_{R_{c}}(u) &= \left\{ \begin{array}{l} G_{\delta_{R_{c}}}(u) + 2.0 \ G_{\delta_{R_{c}}}(u-1) + G_{\delta_{R_{c}}}(u-2) - \delta_{R_{c}}(u-1) \left[ 2.0 - .0019 \ \frac{4}{7} \right] \\ &- \delta_{R_{c}}(u-2) \left[ .000595 \ \frac{4}{72} - .0244 \ \frac{2}{7} + 1.0 \right] \right\} \right/ \left[ .000595 \ \frac{4}{72} + .0244 \ \frac{1}{7} + 1.0 \right] \end{split}$$

:

. Torm	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
SSC.	Second Filtered Function of Roll Cyclic	ט ו	-		. 000 25 /N	30/30 L	
S <sub>Rc</sub>	Second Filtered Function of Your Cyclic	<b>ט</b> ו		-	.80025 M	39/sec	

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Figure C-1. AFCS Pitch Axis Mechanization Block Dirgram

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Figure C-2. AFCS Roll Aris Mechanization Block Diagram



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#### APPENDIX D

#### QUADRATIC OPTIMAL CONTROL FOR THE NASA LRC YHC-1A HELICOPTER

#### SUMMARY

Quadratic optimization methods were applied to synthesize a velocity control system for the YHC-1A helicopter. The resulting system was found to be tolerant of errors introduced by quantizing pitch angle and velocity signals which simulate measurements from a strapped-down inertial platform with pulse-rebalanced instruments.

#### Equations of Motion

The computer program (RAOPT) used to calculate the quadratic-optimal feedback gains accepts the equations of motion as a system of first-order equations written in the form

$$\hat{\mathbf{X}} = \mathbf{F}\mathbf{X} + \mathbf{G}_1 \mathbf{U} + \mathbf{G}_2 \mathbf{N} \tag{D-1}$$

The feedback control U is found to be linear in the state so that U = KX. The program calculates the gain matrix K. The term  $G_2N$  represents a white-noise disturbance input. It is not used in the problem at hand so we put  $G_2 = 0$ . The response of the system is defined to be

$$\mathbf{R} = \mathbf{H} \mathbf{X} + \mathbf{D} \mathbf{U} \tag{D-2}$$

The matrices H and D must be chosen to give proper meaning to the optimization of the quadratic integral

 $J = \int_0^{\infty} \mathbf{R}' \mathbf{Q} \mathbf{R} \, dt \qquad (D-3)$ 

with suitable choices for elements in the weighting matrix Q. (Note that we may change H, D, and Q in ways which will not alter the performance index J.)

The simplest procedure is to consider the actuators as integrators, and hence their outputs are variables of the state of the system. The method then puts feedbacks around these integrators and converts them into simple lags. Whether the actual actuator dynamics alters the performance in an essential manner must then be determined on the simulation. The vectors for the system state and the system response for the helicopter were taken as

$$\mathbf{X} = \begin{bmatrix} \mathbf{u} \\ \mathbf{w} \\ \dot{\boldsymbol{\theta}} \\ \boldsymbol{\theta} \end{bmatrix}, \quad \mathbf{R} = \begin{bmatrix} \dot{\boldsymbol{\theta}} \\ \boldsymbol{\theta} \\ \dot{\boldsymbol{\theta}} \\ \dot{\boldsymbol{h}} \\ \boldsymbol{\theta}_{\mathbf{LF}} + \boldsymbol{\theta}_{\mathbf{LA}} \\ \boldsymbol{\theta}_{\mathbf{CF}} + \boldsymbol{\theta}_{\mathbf{CA}} \end{bmatrix}$$
(D-4)

where

 $\begin{cases} \dot{x} = u + \theta_0 w \\ \dot{h} = \theta_0 u - w \end{cases}$ (D-5)

and  $\delta_{LF} + \delta_{LA}$ ,  $\theta_{CF} + \theta_{CA}$  represent the total feedbacks split into two parts to isolate the contributions of the dynamical variables u, w,  $\dot{\theta}$ ,  $\theta$  from those of the actuator outputs  $\delta_{L}$  and  $\theta_{C}$ . In detail, the equations of motion are:

The feedback-control vector is then

κ.

$$U = \begin{bmatrix} \delta_{LF} \\ \bullet_{CF} \end{bmatrix} + \begin{bmatrix} \bullet_{LA} \\ \bullet_{CA} \end{bmatrix} = \begin{bmatrix} DU & DW & DTD & DT \\ TU & TW & TTD & TT \end{bmatrix} \begin{bmatrix} u \\ w \\ \bullet \\ \bullet \end{bmatrix} + \begin{bmatrix} DDL & DTC \\ TDL & TTC \end{bmatrix} \begin{bmatrix} \bullet_{L} \\ \bullet_{C} \end{bmatrix}$$
(D-7)

The expressions DU, DW, DTD, etc., are FORTRAN symbols for the gain constants computed by the optimization program. Matrices F and  $G_1$  are displayed in equation (D-6). To get the response vector R, H, and D are taken as

and then Q may be the diagonal matrix:



#### Control Configuration;

The resulting system is diagrammed in Figure D-1. Two notch filters of the form

$$\frac{\mathrm{s}^2 + (30)^2}{\mathrm{s}^2 + 2(0, 3) \ 30 \ \mathrm{s} + (30)^2}$$

were added as shown to see if they reduced the system performance. (They did not, )

For simplicity it was decided to command u and w rather than x and h as called for in the response vector R. This introduced a small discrepancy and it should be removed on further study. Feed-forward terms DWC and TUC shown in Figure D-1 were added to re-establish the proper steady-state values. In spite of this, qualitative conclusions of the study are valid.

#### **Optimal Gains**;

Gains computed for various choices of the elements of the weighting matrix Q are listed in Table D-1. It takes between 10 and 20 seconds for RAOPT to compute a set of gains for this sixth-order system on the Honeywell H1800 computer.

The step size for the difference Quation corresponding to equation (D-1) was taken as 0,05 or 20 steps a second. The simulation was run at 30 steps a second. It was found that the gains computed at 10, 20 and 50 steps did not differ greatly, so this inconsistency is ignored.

The basic weighting of the variables, Cases 1, 9 and 12 in Table D-1, were chosen from the analog scalings (Figure D-2) which seemed to give uniform signal levels in the analog simulation. The gains of these cases were found to be satisfactory. The assumption leading to this choice is that the optimal gains will make all terms of the performance index of the same order of magnitude.

#### The Simulation:

The aircraft was simulated on an analog computer and the control computation was performed on the SDS 9300. Figure D-2, Table D-2 and Figure D-3 record the analog diagram, potentiometer settings used, and the digital FORTRAN program,

The pitch angle was quantized to 0,0035 degree of arc, horizontal and vertical velocities to 0.25 feet per second. Pitch rate, when quantization on pitch was used, was computed as the change in pitch divided by the time for a cycle. In a separate study, Lagrangian polynomials of second, third and fourth orders were used to calculate the derivative of pitch angle. The FORTRAN formulas

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# TABLE D-1 FEEDBACK GAINS

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775	-23	28-	52-	-2.0	-3.0	55-	0:5-	52-	てい	3	à	21/-	27-	87-	-2.0	5.5
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4	-1.5	0.2-	-21	£%-	-~-	シアー	5.5	-2.2	-13	81-	-2.0	-23	- 3	- 86	Si	
P.	- 60	1.1.	en Vi	59-	*	- 2.5	532-	ノンー	- SS	227-	2%-	8 '	*	64	<b>v</b> 1	9
Ŕ	1000.	28:	1.100-	S.	.0 <i>\</i> 3	4.8.1	2	sas.	\$100.	1.85	રેજ-	8X6	2560.	.022	Soo.	Size.
Ŗ	.018	.024	.026	2/0.	120.	.e22	.035	. 026	.018	.025	520.	.0027	. 2065	. 2083	Svo.	Se.
DIC	-54.	-24.	-75.	-62.	-27.	8	- 19.	- 22	<u>30</u>	- 21.	- (3	- 77	-9.9	-7.6	-40	0
720	-5.0	-3.0	-2.3	17-	-6.7	-4.3	-43	1.4-	1-4.7	-2.9	-2.3	-5.0	78-	-3.1	5-	5
ち	-42.	-10.9	本 ジー	12	-35	Ş	ş	-49	-45.6	-45	-77	- 23.	-&-	- 21	2-	-20
210	-37.	-15.7	-10.1	-35.	15-	Ş	-2%.	- 25.	-26	-156	-123	*	-23.	2/-	-40	-40
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ard	<i>8</i> 89	1000	1000	1000	1000	(CORD)	and	2007	000)	2020	8	1200	1800	200	Ś	
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<i>کھ</i> ند	~	~	3	*	5	4	7	60	0	\$	11	2	\$	¥	\$	×

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- Xu/m	РЮ	0252	0325	S-152
5×/m.	PII	2135	3205	3185
(Xom - U. t. ; /100	2:2	0115	:000	occo
- (Xg/ - 4. d.)/100	Pis	0000	2760	0555
9/100	F14	3220	3220	77.2 <b>0</b>
Xselm	Pis	1750	2130	و
Xa/100m		4361	2507	2047
- ICMu/Iyy	P17	0000	0511	0299
10 Mu/Iyy	P13	0437	0000	0000
50 Mus/ Iyy	P19	0888	9000	9160
_ Mis/ 10 Tyy	Q10	0590	1093	1175
Me. Jyy	<i><b>Q</b>11</i>	2950	3140	3305
Mac/10 I'yy	<i>Q12</i>	1520	6260	7290
Zu/m	<i>413</i>	0457	0000	0338
- Zu/m	<i><b>Q14</b></i>	0000	0283	0000
- Zus/m	<i>Q15</i>	2830	5790	7120
( <sup>2</sup> é/m + U.)/500	<i>Q16</i>	0007	2027	3372
90º/100	<i>Q</i> 17	0526	0282	0134
ZSL SM	ହାନ	0101	0738	0420
- 202/500m	<i>Q19</i>	5176	5614	6490

#### TABLE D-2 POTENTIOMETER SETTINGS





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<b>ج بر</b>		CT#CT/16370.						
56		T=TP+CT		1	¥ l			
571		TOFCTAN		CALCU	LATE	THETA	DOT	
581		60 TO (1101)-1101	1012)M	an 6 9 17 92 9 8 - 66 494 4649 5	1			
59	12	"CU-(U-UP)+A+	. Julio 1. Ja		L	· · · · · · · · · · · · · · · · · · ·	an 4 4 1	a 🗰 - a ta second
60	• •	10U=CV		<b>•</b>	۱ 			
611		CUHICU *	C	WANTI	2 5	•		•
691		U=UP+CU/4.		,	Ý	.•		
63		GO 10 (11+11+11+1	1+13)M					
64	13	CW= (W-WP)=4.	ndo, az al milli nindini dini ili nun findul bilad e v	andres a subserve a subserve a	X	ingeneration of the second state where the	martillin an ach bin - ablird y	The Division of the State of th
A state of the second s		ICM=CW	··	Ourser	r act: W/			
1. S. C. S.		CIV≈ICW		WOHE !!		•		
67		W = WP + CW/4,			Y			
58	11	DLF=DU+(U-UG)+DW+	(W-WC)+Di	D+TD+DT	r#T			4
¢⊅r .		TCSSTUA (U-UC)+TN.	(W-WC) +TT	D + TD + TT	Γ#ͳ ,	<b>6 a a a a a a</b>		
701		DLA=DDL+DTC+TC	1			CHLCOL	1971 <u>E.</u> .	I LENDHICKS
71.		TCASTDL * DL + TTC * TC						Ý
72:		GO TO (14+15)MF	CHOO	SE FIL	TFRS	INJ OR.	OUT.	
73:	15	DLB#.9677*(DLBP-C	LFP)+ 806	SA (DLFA	DLFPP)	6130*	OL BPP	
745		DLOPP=DLBP	-			-		ſ
75		DLEP=DLB						
76		DLFPP=DLFP						
777		DLFP=DLF			i i		Lieber	
28 *		DLF×DLB					NOTCH	FILTERS
79		TCB=.9677+(TC8P-1	CFP)+.806	5+(TCF	TCFPP)	6130*	TCBPP	
80		TCBPP=TCBP	v					
811		TCAPATCB			•			
8		TCFPP=TCFP				•		
87		TCFP=TCF						
8.4		TCF=TCB						Ý
851	14	VOUI (,) = DLE ALO.			X ·			
86:	14	VOUT (2) =TCF+1000	•		ľ			
87		VOUT ( ) = DLA + IA ·		OUT PUT		IDIOG		
88		VOUT (A) = TCA + 1000		••••••••		11600		_
89;		CALL DAGLA . VOUT.	)		Ý			<b>^</b>
90:		. <u>ער = ע</u>						
911		WP=W					Retarn	to Start
92		TPHT					of hyd	rid loop
97:		IF (SENSE SWITCH .	1 415 (	HOOSE	OUTPUT	ON LINE	E FRIN	TER
941	5	CALL WAIT						
95.	4	CALL ANALOGIC	natus maasa coluntum - en line e e maa			, , , , , , , , , , , , , , , , , , ,		
96:	• • • • • • • • • • • • • • • • • • •	K.= K + 1	2	OUNT N	NUMBER	ON' L.	P. OUT	PUT
97.		OUTPUT (108) N.K.I	V. DW. DTD.	DT,DDL	, DTC, TU	,TW,TTD	, TT, TI	L, TTC, M
98:		GO TO 1	•	•	•			•
991		END						

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Figure D-3. Digital Program (Concluded)

compared were:

TD = CT \* AN (difference)
TD = (3. \*CT - CTP) \* AN/2. (second)
TD = (11. \* CT - 7. \* CTP + 2. \* CTPP) \* AN/6. (third)
TD = (25. \* CT - 23. \* CTP + 12. \* CTPP - 3. \* CTPPP) \*AN/12. (fourth)

(CT, CTP, etc., represent changes in theta in the current and past cycles. AN is the frequency in cycles per second.)

The higher-order formulas did not improve the performance of the system.

#### Results:

Computer traces are shown in Figures D-4, D-5, and D-6. The system with optimal gains from Case 12 at hover is represented in Figure D-4. The effect of the quantization of all three signals and of the notch filters may be seen by comparing the first and third traces with the second and fourth. The response to a step vertical gust is shown in the fifth trace. The optimal gains of Case 1 were found to give satisfactory results at the 100-knot flight condition. The corresponding traces are omitted.

In Figures D-5 and D-6, the performances of the system with the gains of Case 16 at hover and with the gains of Case 15 at 100 knots are represented. Again, the system without or with quantization and filters may be studied. These gains were found by slightly modifying the 100-knot optimal and then trying to make the gains at hover as close as possible to the 100 dot case. As can be seen from the traces, the 100-knot case has been favored. Only two gains change. These are DTC and TT. The change of DTC most likely can be eliminated on another iteration of the study, and it is possible that the change in TT may be removed, also. However, the transient coupling of the u- and w-commands is somewhat high, particularly at hover, and this may be improved at the expense of more gain changing.

The system is tolerant to the effects of the signal quantization used in the study. It may be too slow in its response to step commands, and a further study with different Q-weightings may be necessary to achieve the system desired.

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Figure D-4. Optimal Control No. 12 at Hover


Figure D-5. Compromised Control No. 16 at Hover



Figure D-6. Compromised Control No. 15 at 100 Knots

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#### APPENDIX E BASELINE DISPLAY EQUATIONS <sup>1</sup>, <sup>2</sup>

Function: Displays

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#### Math Description:

Term	Description	Units	Accuracy	Range	Kesolutic	n Sample Rate
ūc	Longitudinal Velocity Command	Knots				8 Hg
<i>V</i> <sub>c</sub>	Lateral Velocity Command	knots				
Ejc	Lat. Vol. error W.K.t. Course	knots				
hc.	Altitude rate Command	ft/sec				
NA	Aircraft Position-North	feet				
EA	Aircraft Position- East	feet				V
Ni	} North of East Coord.	feet				
Eį	) of Command Course Intersections					

Quantities listed are obtained from navigation, guidance, or AFCS computations.

<sup>&</sup>lt;sup>1</sup>Accuracy, range, and resolution are per navigation, guidance, and control requirements.

<sup>&</sup>lt;sup>2</sup>All outputs are read out at 64 Hz.

Function: Displays

Quantities listed are obtained from navigation, guidance, or AFCS computations.

	Term	Description	Units	Accuracy	Range	Resolutio	Sample Rate
	Ý	Actual Heading	deg				8 Hg
	+01	Elevation Augle	day		1		16 Hz
	ý	Roll Augle	deg				16 Hz
	ha	Altitude	f+				8 Hay
	ha	Altitude Rate	H/sec				16 Hz
	hR	Altitude - Roder	ſt				843
	hR	Altitude Rete - Reder	ft/sec				16 Hz
	ho	Altitude Commendlie,	f+				8 Hz
	Bi	Decrimy	deg	//			
	VS	Ground Speed	Knots				
	Ŧ,	Final Approach Iddy	deg				
	Roo	Raugeto Stort farm	f+				
	too	Time to start turn	See			•	
	f	Londing Site Wind	dag				V
	MAP	Pilot selected airspeed	knots .				Const
İ	he.	Pilot selected approach alt.	feet				
	Es	Filet selected glide augle	dey	0			
1	n <sub>F</sub>	Khot selected hover alt.	feet				
	Jc fc	Pilt selected healing Com.	deg				-

## REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR

Function: Forward velocity error

Math Description:

$$(I, \bar{U}, \bar{U})_{h} = \frac{(T + 2NT_{i})(\bar{U}_{c} - \bar{U}_{h}) + (T - 2VT_{i})(\bar{u}_{c} - \bar{U}_{h-1}) - (T - 2T_{i})(\bar{u}_{c} - \bar{U}_{h-1}) - (T - 2T_{i})}{T - 2T_{i}}$$

$$- K \frac{T(\bar{U}_{h} + \bar{U}_{h-1}) - (T - 2T_{i})(\bar{u}_{c}\bar{U}_{c})_{i-1}}{T + 2T_{i}}$$

Term	Description	Units	Accuracy	Range	Pesolution	Rate	
tre	Command Velucity	filme				8 Hz	
Τ.	Sample period	see					
N	Constant	None					
t.	Constant	sec					
T_	Constant	see					
ū	Horisones ! valueity	fthee					
	- either UA or UI						
Ó	AFCS Pitch Rate	dag fre.				V	

## REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR.

Function: Lateral velocity error

Math Description:

 $\left( S_{3} \right)_{\mu} = \frac{\left( F_{3} \right)_{\mu} + \left( F_{3$ 

1 1 1 2			16. ,	. "
13911	N,	7.	0	(k.);
the then the	1-,:1: 1:	17 VERS	15. 1. 1.	1. Yer.
Adress.	A's	$(T_{i})_{z_{i}}$	(hy)	0

Term	Description	Units	Accuracy	Range	Resolution	Sample Rate	
Eri	Sine water to tweet	11/ce				F. Hg	
T	Sough Berind	14.5				1	
N.	takeda led Contant	15.00					
×.		Fl/sec /der	4				
Fr		re hor forthe					
T,	1 4	100				1	
1/3	leinspace !!!	1º/ce				i 1	
1	127 sersude	des	1.				
4	APCS Not Pate	die/ecc				V	

Function: Altitude rate error

#### Math Description:

(hour (1.57) (he - 1) 1 (T-2117) (he - 1) - (T-57) (ho).

Term	Description	Units	Accuracy	Range	Resolution	Sample Rate	
he, 11 	April Actual Alt. Somple Scried Concernent	rifee Rifee See Nome				16 Hg	
						V	

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Function: Heading error

Math Description:

$$(- \frac{y}{y})_{n} = \frac{(7+2)r_{T}(\underline{x}_{c} - \underline{x}) + (7-2r_{t})(\underline{y}_{c} - \underline{y}) - (7-2r_{t})(\Delta \underline{y}_{b})_{n-1}}{T+2r_{t}}$$
  
-K,  $\frac{T(\underline{y}_{h} + \underline{y}_{h-1}) - (7-2r_{t})(\Delta \underline{y}_{b})_{n-1}}{T+2r_{t}}$ 

$$\frac{V_{SAS}}{L(V_{SAS})}, \frac{N}{N}, \frac{K_{1}}{(K_{1})}, \frac{N}{(K_{2})}, \frac{N}{(K_{2})$$

Term	Description	Units	Accuracy	Range	Resolution	Sample Rate	•
J.c.	Heading Command	deg				SHy	
¥.	Actual Heading	det				;	
T	Saup's Review	gr e.					
~	Scheduler Content	time					
K,	Selectule & Contourt	see	1 de la				
Kin	Auspeed	The fre	No. 2 C		Least and		

Function: Range to course intersection/landing site

Math Description:

$$\Delta N = N_A - N_i \qquad \Delta E = E_A - E_i$$

$$h = h_{c_0} - h_{N_A v}$$

$$R_H = V (\Delta N)^{c_0} + (\Delta E)^{c_0}$$

Term	Description	Units	Accuracy	Range	Resolution	Sample Rate	
NA EA hour Ni Ei heo	Aire Position - N Aire Position - E Aire Altitude Check point Pos - N Check point Pos - E Pilot set altitude					8 Hg	

#### Function: Local wind

Math Description:

$$V_{we} = - i \left( A \quad Si'h \left( \frac{U_A}{U_A} - \frac{U_B}{U_B} \right) \right)$$

$$V_{we} = V_B - i \left( Cos \left( \frac{U_A}{U_A} - \frac{U_B}{U_B} \right) \right)$$

$$V_{we} = i \left( \frac{V_{we}}{V_{we}} \right)^2 + \left( \frac{V_{we}}{V_{we}} \right)^2$$

$$V_{we} = t \operatorname{Res}^{-1} \frac{V_{we}}{V_{we}}$$

$$V_{we} = \frac{U_A}{U_A} = \frac{U_A}{U_A} = \frac{U_A}{U_B}$$

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
U.	Aire. Inorit. Valueity	knows		ti se s		8. Hay	
V.	Arrenoft Honding	dag					
U.	Srowing Track Hodg	den					
Va	Growing Speed	kuuts					

#### Function: Predicted position

Math Description:  $\Delta \overline{X} = + \langle \overline{u}_{n}, \overline{u}_{n} + \langle \overline{y}_{n}, \overline{z} \rangle + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}} \rangle + k_{p} \overline{\mathcal{Q}} + k_{p} \overline{\mathcal{Q}$ 

Term	Description	Units	Accuracy	Range	Resolutio	n Sample Rate	
NA	Attent + l'an Lion-North					16 Hag	
EA	Alterate Van Liou East				ى ب		
$\bar{\nu}_{\varsigma}$	Arrenott Grown & Speed						
HOI.	Elevation Augle						
0 Ø	Roll Aughe						•
Ý.	Aireverty Cross course						
YX RH	Riveratt Heading Hovison tal Konge Gf. or Landing Side						
Kag	Scheduled Constants						
Kija   Kieji							

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#### APPENDIX F

#### DOWN LINK DESCRIPTION

The baseline AALS is defined as using the Gemini PCM programmer as the link with the computer subsystem. It has the capability for operating as a self-contained data-handling unit. Internally it provides the functions of analog data multiplexing, anolog-to-digital conversion, and digital-data multiplexing, including the required timing to perform these functions. The outputs of this programmer consist of two PCM data signals: 51.2 kilobits/second (kbps) data in NRZ-C form and 5.12 kbps data in RZ form. A frame of data from the PCM programmer consists of the following channels:

No. of <u>channels</u>	Type of signal	Sample rate, samples/sec	Bits per sample
6	0-20 mV	640	8
6	0-20 mV	160	8
9	0-20 mV	80	8
3	0-5 V	40	8
3	0-5 V	20	8
6	0-5 V	10	8
32	0-5 V	1, 25	8
40 (corr. to 5 ea. 8- bit words)	Bilevel	10	1997 - 1997 <b>1</b> 997 - 19
24	Digital (compute	r) 0,416	24
1	Time	10	8

The basic sample rate of the commutator is 40 samples per second. The main frame consists of 160 word slots with 8 bits per word. Six of the 160 words are used for frame synchronization; thus 154 word slots are available for data. The complete Gemini DTS system provided for over 300 input channels by using low-speed subcommutation.

The airborne computer and time reference system (TRS) supply the digital data inputs to the programmer. The Gemini computer output is 21 words of 24 bits length each, and the TRS output is 3 words of 24 bits each. These digital data words are transferred serially from the computer into a buffer storage register internal to the programmer. This serial transfer is accomplished as follows. At the proper time for sampling the computer data, the PCM programmer sends a request pulse to the computer for a data word. The computer provides 24 clock pulses to the programmer to transfer into the buffer storage register the 24-bit computer data word available to the programmer. The Gemini computer clocks this data into the programmer at

a 500-kHz rate The programmer unloads the buffer storage register in 8bit groups at a 51. 2-kbps rate. The programmer sends request pulses to the computer for a 24-bit word every 75 milliseconds until 21 computer words have been read into the programmer. The computer clock and data output lines are isolated from the programmer by transformers located in the computer.

The Gemini PCM programmer has some flexibility in the areas of increasing the number of digital channels, increasing the frequency of sampling the digital channels, or increasing the length of the digital words. There are some basic constraints which are applicable to any PCM system used in a vhf transmit link. The most severe limitation is the bit rate for an NRZ code which is 150 kbps maximum. This means the present frame format could be increased by a factor of 3 either in number of word slots or in sampling speed. If the length of the computer words is increased above 24 bits, then the buffer storage register will require additional shift registers, and the format will be changed to 32 bits per digital word (the next multiple of 8). As an example, if the computer word were increased from 24 to 28 bits, the number of computer words were increased from 21 to 40, and the sample rate were increased from 0.416 sample/sec to 40 samples/sec, the computer data words alone would require 160 main frame word slots. This exceeds the 154 words available at 40 samples/sec in the present PCM system. Thus, it is apparent that the number of words in a frame would have to be increased or some other tradeoff between sample rate and the number of computer words read out would be necessary. Another consideration in the computer/PCM programmer interface is the rate at which the computer must clock data into the programmer storage register. The present clock rate of 500 kHz can be increased to 1.0 MHz.

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Based on data requirements known at this time (Table F-1), it does not appear feasible to modify the existing Gemini PCM programmer to satisfy these requirements. The digital and analog data requirements must be defined in light of the constraints cited above. Consideration should be given to supplying the digital data signals to the programmer in serial form rather than parallel form.

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Signal	No. of words	Transmissions · per second
Direction cosine matrix	9	computation rate
Sum of XYZ accelerometer counts	3	1/ <b>∆</b> t
Sum of XYZ gyro counts	3	1/ <b>∆</b> t
Flight time	1	1/ <b>∆</b> t
Computation cycle time	1	computation rate
XYZ position and velocity (radar frame)	6	1
XYZ position and velocity (IMU frame)	6	1
XYZ position and velocity (estimator frame)	6	1
Latitude and longitude	2	1
Gyro scaling (bilevel)	1	1/ <b>∆</b> t
Altimeter output	1	5
XY area/navigation (Z sources)	4 .	1
Euler angles	3	5
Body-axis angular rates	3	5
Guidance velocity commands	3	5

#### TABLE F-1 DIGITAL SIGNALS FOR DATA TRANSMISSION FROM CENTRAL COMPUTER

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#### APPENDIX G

#### NEW TECHNOLOGY

After a diligent review of the work performed under this contract, no new innovation, discovery, improvement, or invention was made.

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#### **REFERENCES**

- Fryer, W. D. and Schultz, W. C.: A Survey of Method for Digital Simulation of Control Systems. Cornell Aero. Lab. No. X4.-1681-E-1, July 1964.
- 2) Anon.: Advanced Flight Control System Concepts for VTOL Aircraft. Phase I Technical Report, TRECOM TR 64-50, October 1964.

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3) Garren, Jr., J.F. and Kelly, J.R.: Description of an Analog Computer Approach to V/STOL Simulations Employing a Variable Stability Helicopter, NASA TN D-1970, January 1964.