

NASA CR-72491 WRL 8962-18-F

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MEASUREMENT OF TEMPERATURE PROFILES IN HOT GASES BY EMISSION-ABSORPTION SPECTROSCOPY

by F. S. Simmons, H. Y. Yamada, and C. B. Arnold

INFRARED AND OPTICS LABORATORY WILLOW RUN LABORATORIES THE UNIVERSITY OF MICHIGAN

prepared for NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

NASA Lewis Research Center Contract NAS3-9419 Carl B. Norgren, Project Manager Air Breathing Engines Division Donald R. Buchele, Research Advisor Instrument and Computing Division

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FINAL REPORT

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by F. S. Simmons, H. Y. Yamada, and C. B. Arnold

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April 1969

CONTRACT NAS3-9419

NASA Lewis Research Center Cleveland, Ohio Carl B. Norgren, Project Manager Air Breathing Engines Division Donald R. Buchele, Research Advisor Instrument and Computing Division

ABSTRACT

Measurements of spectral radiances and absorptances in the 2-3- μ m region are presented for several samples of H₂O, CO₂, and HF, and a mixture of H₂O, CO₂, and N₂ in a 60-cm cell heated in a furnace such that various temperature profiles could be imposed along the optical path. The spectral data were converted into apparent temperatures corresponding to the ratio of spectral radiance to absorptance as a function of frequency. Temperature profiles in the sample gases were deduced from the variation of apparent temperature with absorptance, using molecular bandmodel calculations and assuming knowledge of the profile shape. The deduced temperature profiles are shown to agree quite well with direct measurements by thermocouples attached to the cell.

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MEASUREMENT OF TEMPERATURE PROFILES IN HOT GASES BY EMISSION-ABSORPTION SPECTROSCOPY Final Report

SUMMARY

This study was undertaken to explore the application of infrared emissionabsorption spectroscopy as a means of determining temperature profiles in nonuniform hot gases such as the exhaust jets of advanced air-breathing engines. Experimental measurements were made using a double-beam ratio-recording spectrometer which could accommodate long sample cells heated in a segmented furnace so that various temperature profiles could be maintained in the gas sample. Spectral radiances and absorptances in the 2-3- μ m region were obtained for various pressures and temperature profiles in H₂O vapor, CO₂, HF, and a mixture of CO₂, H₂O, and N₂ in a 60-cm cell. The spectral data were reduced to apparent temperatures, which are defined as those temperatures the Planck functions of which are the observed ratios of spectral radiance to absorptance, as a function of frequency throughout the various vibration-rotation bands.

A general computer program was written for the calculation of molecular radiative transfer. For the case of polyatomic molecules, the calculation was based on a band model consisting of a random array of lines of nearly equal intensity; for diatomic molecules exhibiting nonoverlapping lines, the calculation was based on expressions for the total radiances and equivalent widths of Lorentz lines for nonisothermal paths. Calculations based on the temperature profile in the cell measured by thermocouples were shown to agree well with the observed spectra.

The inversion of the observed radiance and absorptance measurements proceeded in the following manner. The general shape of the temperature profile in the sample was assumed to be known, and was approximated in terms of simple geometric forms so that the profile could be characterized in terms of a few parameters. These parameters were then adjusted in straightforward calculations using the appropriate radiative-transfer expression until a best fit was obtained with the observed spectra. It was found to be most convenient and reliable to fit the band-model calculations to plots of apparent temperature vs. absorptance, and the isolated-line calculations to plots of apparent temperature vs. a generalized rotational quantum number. The resultant temperature profiles so deduced showed satisfactory agreement with the thermocouple measurements in all cases except those in which an inappropriate profile shape was assumed. It was therefore concluded that infrared emission-absorption spectroscopy applied in this manner shows excellent promise as a fairly simple and reliable means of determining temperature profiles in hot gas streams such as the exhausts of jet or rocket engines for which a priori knowledge of the general shape of the temperature profile is available. However, some further development of the method would be requisite; in particular, it would be most appropriate to carry out an investigation exploring combustion products in a laboratory apparatus before proceeding to applications involving full-size jet or rocket engines.

1 INTRODUCTION

Since the turn of the century, spectroscopy has seen wide use as the means for determining temperatures in hot gaseous sources ranging from stellar atmospheres to the flame of a bunsen burner. The basic principles involved and the many experimental techniques that have been employed are well documented in the literature, and have been reviewed in a number of textbooks [1-3] and in the proceedings of periodic symposia on temperature measurements [4]. However, most of this work has been based on the simplifying assumption that the gas is a completely equilibrated isothermal source, and much of it on the further assumption that the gas is optically thin. For the latter case, measurements of the spectral distribution of emission (or absorption) alone is sufficient, in principle, for the determination of temperature. However, when appreciable self-absorption of emitted radiation must be accounted for, then measurements of both emission and absorption are required; hence the term emissionabsorption pyrometry.

For nonisothermal gases in local thermodynamic equilibrium, the application of either spectral distribution or absorption-emission techniques to determine a single "effective temperature" can be shown to produce a result with little meaning: the value of the resultant "temperature" would be wavelength dependent, hence not a parameter useful for characterizing the physical state of the gas.

For the case in which thermal equilibrium does not prevail even locally, there are difficulties in even defining temperature; hence, measurements in either optically thin or dense gases lack meaning in correspondence with the extent of the disequilibrium.

The present study has been restricted to gases of appreciable optical depths in local thermodynamic equilibrium, and is concerned with the measurement of temperature profiles using infrared emission-absorption spectroscopy. The specific objective of the work is to explore the utility of this experimental technique as a possible diagnostic tool for the performance evaluation of advanced air-breathing engines.

Previous studies at The University of Michigan were concerned with the problem of calculating infrared radiation from highly nonuniform hot gaseous sources. In the course of that work, expressions were derived for the integrated radiances and equivalent widths of isolated spectral lines [5-7], and applied in band-model expressions for the more general case [8]. Calculated values of the net spectral radiances from hot sources, in which the temperature profiles were known, were then shown to compare well with direct observations [9].

In this work, the inverse problem is considered: given the observed emission and absorption spectra, how well can the temperature profile within a nonisothermal source be deduced?

THEORETICAL BACKGROUND

2.1. DEFINITIONS AND BASIC RELATIONS

Throughout this report, the radiometric symbols and nomenclature are those approved by the Commission on Symbols, Units, and Nomenclature of the International Union of Pure and Applied Physics. All symbols are defined in appendix E.

The governing equation for emission-absorption pyrometry derives from Kirchhoff's law of radiation, and is given by

$$\mathbf{L}_{\nu}^{*}(\mathbf{T}^{*}) = \mathbf{L}_{\nu}^{\prime} \alpha(\nu) \tag{1}$$

where L_{ν} is the observed spectral radiance (specific intensity) at a frequency ν along a particular line of sight through the gas and $\alpha(\nu)$ is the corresponding spectral absorptance; their ratio, L_{ν}^{*} , is designated as the Planck function of an apparent temperature, T^{*} . For uniform isothermal systems, T^{*} can be identified as the true thermodynamic temperature, T, and equation (1) can be directly applied. For all other cases, T^{*} is an apparent temperature which is nothing but a convenient alternative expression of an effective blackbody spectral radiance.

A distinction should be noted between T^* and a quantity often referred to as an "apparent temperature," T_{br} , which is more appropriately termed the "brightness temperature," and is defined by

$$\mathbf{L}_{\nu} \equiv \mathbf{L}_{\nu}^{*}(\mathbf{T}_{br}) \tag{2}$$

Thus T_{br} is seen to be an alternative expression of spectral radiance; i.e., it is that temperature at which the Planck function gives the observed radiance. Correspondingly, T^* is an alternative expression of the ratio of spectral radiance to spectral absorptance; both are therefore functions of wavelength in general. It might be noted that spectral radiance can also be expressed in terms of a spectral emissivity, $\epsilon(\nu)$, defined by

$$\mathbf{L}_{\mu} \equiv \epsilon(\nu) \mathbf{L}_{\mu}^{*}(\mathbf{T}) \tag{3}$$

The quantity $\epsilon(\nu)$ is equal to the spectral absorptance in an isothermal gas, by virtue of Kirchhoff's law, but of course loses its meaning in a nonisothermal gas.

The spectral radiance and absorptance in equation 1, in the strictest sense, refer to radiation in a spectral interval between ν and $\nu + d\nu$; actually, of course, measurements are always made of the average radiant power in a finite interval $\delta\nu$. For isothermal gases, it is easy to prove that the ratio of observed radiance to absorptance is independent of the spectral interval $\delta \nu$, represented by the response function of the measuring instrument, provided only that it remain the same for both the emission and the absorption measurement [10], hence justifying the identification of T^* as T in equation 1. For the nonisothermal case, this is not generally so, and equation 1 in its simple form is of little use; more of the details of the origin of the radiation are required, as outlined in the sections to follow.

2.2. NONISOTHERMAL GROWTH

Consider an isolated spectral line of a gas in local thermodynamic equilibrium, as observed with an instrument of moderate resolution, having a slit function $g(\nu)$ whose effective width $\delta \nu$ is much greater than the line width. The indication of a well-behaved instrument, linear in response, would be proportional to the total radiance, L, of the spectral line:

$$\mathbf{L} = \int_{0}^{\infty} \mathbf{g}(\nu) \mathbf{L}_{\nu} \, \mathrm{d}\nu \tag{4}$$

Infrared lines at ordinary pressures and temperatures exhibit contours well described by the Lorentz dispersion formula, giving for the spectral absorption coefficient, $k(\nu, T)$,

$$k(\nu, T) = \frac{S(T)}{\pi} \frac{\gamma(P, T)}{\gamma^2 + (\nu - \nu_0)^2}$$
(5)

where S(T) is the line strength, ν_0 is the line center frequency, and $\gamma [= \gamma(\mathbf{P}, T)]$ is the pressureand temperature-dependent half-width.

If equation 5 is substituted into the equation of radiative transfer in integral form, an appropriate transformation introduced, and integration made over frequency, the resultant relation is [5]

$$\mathbf{L} = 2\pi\gamma_{\rm e} \int_0^{\mathbf{f}(\mathbf{x}_{\rm L})} \mathbf{L}_{\nu}^*(\mathbf{f}) \, \mathrm{d}\mathbf{f}$$
(6)

where γ_e is an effective (mass-weighted) average line width, and f[= f(x)] is the Ladenburg-Reiche function

$$f(x) = xe^{-x}[J_0(ix) - iJ_1(ix)]$$
(7)

 J_0 and J_1 being Bessel functions of the first kind with the argument, the dimensionless optical depth x, defined by

$$x = (2\pi\gamma_{e})^{-1} \int_{0}^{X} S(X')F(X')dX'$$
(8)

in which X is the ordinary optical depth (cm-atm), S(X) is the temperature-dependent line strength, and F(X) = 1 or $\gamma(X)/\gamma_e$, respectively, for nearly weak or nearly strong lines. Use of a function $F(X) = [\gamma(X)/\gamma_e]^{\eta}$, where $0 < \eta < 1$ is an empirical factor, provides a

convenient means of interpolation between the two [5]. The prime in equation 8 simply indicates the quantity as a variable of integration; the quantity x_L in equation 6 is the value of x for the entire path through the nonisothermal gas.

In this case, the integrated absorptance, usually termed the equivalent width, W, is given by

$$W = 2\pi\gamma_{e}f(x_{L})$$
(9)

(The corresponding relations for Doppler lines are given in reference 6.)

Although collision theory can in some cases provide Lorentz half-widths, values are more generally taken from semi-empirical expressions such as

$$\gamma(\mathbf{P}, \mathbf{T}) = \gamma_0(\mathbf{P}_0, \mathbf{T}_0) \frac{\mathbf{P}}{\mathbf{P}_0} \left(\frac{\mathbf{T}_0}{\mathbf{T}}\right)^n \tag{10}$$

in which γ_0 , the line width at reference pressure P_0 and reference temperature T_0 , and the exponent n are experimentally determined. Acceptance of a value n = 1/2, which follows from simple kinetic theory, and neglect of the dependence of half-width on rotational quantum number, are usually considered justifiable for engineering purposes.

2.3. BAND-MODEL FORMULATIONS

Equation 6 can easily be extended to a molecular band consisting of nonoverlapping spectral lines. In this case, the quantities of interest are the average spectral radiance and absorptance in the interval $\delta \nu$, which are given by

$$\overline{\mathbf{L}}_{\nu} = \beta_{\mathbf{e}} \int_{0}^{f(\overline{\mathbf{x}}_{\mathbf{L}})} \mathbf{L}_{\nu}^{*}(\overline{\mathbf{f}}) \, \mathrm{d}\overline{\mathbf{f}}$$
(11)

and

$$\overline{\alpha}(\nu) = \beta_{\mathbf{e}} \mathbf{f}(\overline{\mathbf{x}}_{\mathbf{L}}) \tag{12}$$

in which β_e is the effective value of a factor characterizing the extent of line overlapping:

$$\beta = 2\pi \overline{\nu}/d \tag{12a}$$

where $\overline{\gamma}$ is the average line half-width and d is the average spacing between lines. In this case, $\overline{f} = f(\overline{x})$, in which the dimensionless optical depth \overline{x} is defined by

$$\overline{\mathbf{x}} = \beta_{\mathbf{e}}^{-1} \int_{0}^{\mathbf{X}} \overline{\mathbf{k}}(\mathbf{X}') \mathbf{F}(\mathbf{X}') d\mathbf{X}'$$
(13)

where

$$\overline{\mathbf{k}} = \overline{\mathbf{S}}/\mathbf{d} \tag{13a}$$

is the average spectral absorption coefficient, the ratio of average line strength to average spacing, and $F(\mathbf{X}) = (\beta/\beta_{c})^{\eta}$ in analogy to the single-line case.

Equation 11 can be further extended to handle molecular bands in which line overlapping is appreciable [8]; the resultant expressions for average spectral radiance and absorptance are:

$$\overline{\mathbf{L}}_{\nu} = \beta_{\mathbf{e}} \int_{0}^{\mathbf{f}(\mathbf{x}_{\mathbf{L}})} \mathbf{L}_{\nu}^{*}(\mathbf{f}) \exp\left[-\beta_{\mathbf{e}} \overline{\mathbf{f}}\right] d\overline{\mathbf{f}}$$
(14)

and

$$\overline{\alpha}_{L} = 1 - \exp\left[-\beta_{e}f(\overline{x}_{L})\right]$$
(15)

If an average transmittance, $\overline{\tau}$, is defined by

$$\overline{\tau} = 1 - \overline{\alpha} = \exp\left[-\beta_{\alpha} f(\overline{x})\right] \tag{16}$$

equation 14 can be rewritten simply as

$$\overline{\mathbf{L}}_{\nu} = \int_{\overline{\tau}}^{1} \mathbf{L}_{\nu}^{*}(\overline{\tau}) \, \mathrm{d}\overline{\tau}$$
⁽¹⁷⁾

Equation 17 is in form the radiative-transfer expression used in experimental studies at Warner and Swasey [11], General Dynamics [12], and in calculations carried out at NASA MSFC [13]; equation 14 is the form used in previous studies at this laboratory [14]. The derivation of a comparable expression in a slightly different form, and examples of its use in some hypothetical flames in which neither line strengths nor widths varied with temperature, have also recently been reported [15].

Equations 11, 12, 14, and 15 reduce to more familiar forms for the strong- and weak-line limits [9]; however, there is little advantage in using such approximations for nonisothermal calculations. A machine calculation would be used in any event, and the above equations are about as easy to program. There is some advantage, however, in using a simple analytical approximation to the Ladenburg-Reiche function [16]; this will be discussed in more detail in section 2.4.

Equation 17 can also be extended to handle mixtures of gases. Since the spectral line positions in the vibration-rotation bands of different gases would be uncorrelated, the incremental transmittances would be multiplicative. In this case, $\overline{\tau}$ would represent the product incremental transmittance, which would be used in the summation to yield the observed radiance.

2.4. EVALUATION OF BAND-MODEL PARAMETERS

In principle, there are two methods by which the band-model parameters, equations 12a and 13a (or any other pair formed from the three basic variables: the line strengths, widths,

and positions) can be evaluated. Detailed information on these line parameters can be appropriately averaged, or the lumped quantities can be determined directly by experiment. The former approach has been applied in calculations of atmospheric transmission in the infrared [17]; however, for hot gases, the population of higher rotational and vibrational states results in an increase in the numbers of lines and in the appearance of hot bands of uncertain strengths. Hence, for polyatomic molecules with their various degrees of freedom, such an approach is not practical at the present time for most engineering purposes. (A line-by-line calculation of the opacity of hot water vapor in cool stars has been made recently [18]; a total of 2.3 million lines were included in the calculation, which required 40 hours of IBM 7094 computer time.) On the other hand, for some diatomic molecules, e.g., HF, there is sufficient and reliable information on strengths and widths with which one could proceed in such a manner. However, the need for a band-model diminishes and line-by-line calculations become more feasible as the number of lines requiring consideration becomes smaller.

The alternative method for evaluating band-model parameters is by direct experimental observations using isothermal samples of the emitting-absorbing gas. The average spectral absorption coefficient, equation 13a, is obtained from observations for path lengths and pressures low enough that the gas is optically thin; i.e., all lines are weak and hence their growth is linear. This condition is specified by $x \rightarrow 0$, for which equation 12 reduces to

$$\overline{k}(\nu, T) = \overline{\alpha}(\nu, T) / X_{T}, \ \alpha(\nu, T) << 1$$
(18)

where X_L is the optical depth in cm-atm and $\overline{\alpha}(\nu, T)$ is the observed average spectral absorptance in the interval $\delta\nu$. Note that the necessary condition is that $\alpha(\nu, T) \ll 1$, not $\overline{\alpha}(\nu, T) \ll 1$. The latter condition can and very often does only signify that the resolution of the observing instrument is low (i.e., the slit function is much greater than line widths); this situation could therefore be encountered with the lines themselves being strong. Accordingly, in practice, observations using a number of path lengths are required to establish that the growth is linear. Note also that reduction in pressure alone is not sufficient; although the optical depth X = PL will decrease, since the line width varies directly with pressure (cf. eq. 10), the absorptance will not decrease at the line center as rapidly as elsewhere, so that the required condition of linear growth cannot be readily observed for arbitrary values of path length.

Evaluation of the other band-model parameter requires measurements in which all lines are strong; i.e., the growth varies as the square root of the optical depth. These conditions permit the evaluation of the quantity

$$\left[(\overline{S}/d)(\overline{\gamma}/d)\right]^{1/2} = \frac{\overline{\alpha}(\nu, T)}{2x^{1/2}}, \quad \alpha(\nu_0, T) \sim 1$$
(19)

from which the line overlap factor (eq. 12a) can be extracted. This evaluation is more difficult than the other for several reasons. The long path lengths required for most of the lines in the $\delta\nu$ to become strong, especially in the wings and troughs of bands, create experimental difficulties; for the large amounts of absorber required, line overlapping cannot be completely eliminated; and the unavoidable presence of some weak lines compromises to some extent the validity of the results.

Again, variation of pressure alone is not sufficient; increasing concentrations of absorbers for a given path length do increase the optical depth, but the concomitant broadening of the lines tends to lower absorptances at the line center, thus obviating square-root growth.

In practice, both band-model parameters are evaluated by experiments in which a sufficient range of path lengths can be achieved so that the variation from linear to square-root growth can be observed. The extent to which this can be accomplished is the principal factor limiting the accurate evaluation of band-model parameters and hence the utility of band models for radiating gases.

An important and often overlooked fact is that band models, although based on theoretical principles, in effect are empirical formulations requiring as input experimentally determined parameters. Hence, it is not imperative that the parameters \overline{k} and β truly represent the ratios of mean line strength to spacing and mean line width to spacing; there is an arbitrary character to these quantities in the first place, since one must prescribe a lower limit to the strengths of lines to be considered in a detailed analysis. Therefore, the question of how realistically a particular band model represents an actual molecule is not of prime importance. The significant question is how well it functions in its capacity as an interpolation device to utilize isothermal laboratory measurements for calculations of radiative transfer in inhomogeneous gases. In this light, the use of more complex band models based on more realistic assumptions regarding properties of the lines in a molecular band is not necessarily desirable. In fact, as illustrated below, the advantage can be largely illusory.

Equations 11, 12, 14, and 15 were derived for a molecular band consisting of Lorentz lines of nearly equal strengths randomly positioned. In order to illustrate the fact that more realistic line-intensity distributions do not necessarily improve the model, consider equation 12 for the case of identical nonoverlapping Lorentz lines in an isothermal gas. In the interval $\delta \nu$

$$\overline{\alpha}(\nu, \mathbf{T}) = \beta \mathbf{f}(\mathbf{x}) \tag{20}$$

where β is defined by equation 12a and $x = SX/2\pi\gamma$. Consider now an array of nonoverlapping Lorentz lines with a probability distribution of strength $p(S) = \overline{S}^{-1} \exp[-S/\overline{S}]$ where p(S) is the probability of finding a line of strength S in the interval S, S + dS and \overline{S} is the mean line strength in the interval $\delta\nu$. It is easy to show that in this case [19]

$$\overline{\alpha}_{\mathbf{p}}(\nu, \mathbf{T}) = \frac{2\pi(\overline{\gamma}/\mathbf{d}_{\mathbf{p}})\mathbf{x}_{\mathbf{p}}}{\sqrt{1 + 2\mathbf{x}_{\mathbf{p}}}}$$
(21)

where $x_p = \overline{S}X/2\pi\overline{\gamma}$. The subscript p in this case denotes a probability strength distribution.

These nonoverlapping models are the special cases of the two corresponding general models, which are appropriate to the evaluation of the two band-model parameters. In the weak-line limit, equations 20 and 21 reduce to

$$\mathbf{x} \neq \mathbf{0}, \quad \overline{\alpha} \neq 2\pi(\overline{\gamma}/\mathbf{d})\mathbf{x}$$
 (22)

$$\mathbf{x}_{\mathbf{p}} \neq \mathbf{0}, \quad \overline{\alpha}_{\mathbf{p}} \neq 2\pi(\overline{\gamma}/\mathbf{d}_{\mathbf{p}})\mathbf{x}_{\mathbf{p}}$$
 (23)

and in the strong-line limit to:

$$\mathbf{x} \to \infty, \quad \overline{\alpha} \to 2(\overline{\gamma}/\mathrm{d})\sqrt{2\pi \mathrm{x}}$$
 (24)

$$x_p - \infty, \quad \overline{\alpha}_p - \pi(\overline{\gamma}/d_p)\sqrt{2x_p}$$
 (25)

Since the values of \overline{S} and d_p will depend on an arbitrary lower limit of intensity below which one could identify large numbers of very low intensity lines not worthy of considering in a particular problem, these quantities are not precisely defined, and may be chosen to suit convenience. Consider the consequences of equating (22) with (23), and (24) with (25):

$$\overline{S}/d_{n} = \overline{S}/d \tag{26}$$

$$\overline{\gamma}/d_{\rm p} = (4/\pi)(\overline{\gamma}/d)$$
 (27)

and

$$\mathbf{x}_{\mathbf{p}} = (\pi/4)\mathbf{x} \tag{28}$$

Substituting (27) and (28) into (21):

$$\overline{\alpha}_{p} = \frac{2\pi(\overline{\gamma}/d)x}{\sqrt{1+(\pi/2)x}}$$
(29)

in which the quantity $x/\sqrt{1 + (\pi/2)x}$ is the approximation to the Ladenburg-Reiche function $xe^{-x}[J_0(ix) -iJ_1(ix)]$ that has been recently proposed [16]. Hence, the two band models yield essentially the same results, and by virtue of (26) and (27), band-model parameters obtained through the use of one model may be used with the other. The above result illustrates the more general fact that calculations with band models are not particularly sensitive to the line strength distribution function that is assumed in the formulation. This fact is best illustrated in figure 3 of reference 19, in which the experimental data of several investigators are fitted equally well by the Ladenburg-Reiche curve of growth, representing the band-model formulation used in the present study, as by one based on a more realistic distribution of line strengths. An analysis of errors to be expected in the application of various band-model approximations to inhomogeneous gases is given in reference 20.

2.5. EMISSION-ABSORPTION PYROMETRY

Consider now the application of emission-absorption spectroscopy to the case of an inhomogeneous nonisothermal gas in local thermodynamic equilibrium. For this case, the ratio of observed spectral radiance to spectral absorptance will vary with optical depth, hence in general with wavelength. At a particular wavelength, the value of the spectral absorptance will depend primarily on the absorber concentration profile; the value of spectral radiance depends on both the concentration and the temperature profiles. For observations at moderate resolution, at a particular wavelength the indicated values of both quantities will depend on the instrument slit opening, but their ratio will not. Therefore, while in principle spectral radiance and absorptance distributions could be analyzed to determine temperature and concentration profiles, the analysis of the emission-absorption ratio offers the considerable advantage of eliminating the uncertainties introduced by inexact knowledge of the shape and width of the instrument slit function.

Consider first the case of isolated Lorentz spectral lines treated individually. Upon substitution of equations 6 and 9, equation 1 becomes [5]

$$L_{\nu}^{*}(T^{*}) = \frac{1}{f(x_{L})} \int_{0}^{f(x_{L})} L_{\nu}^{*}(f) df$$
(30)

where f(x) and x are defined by equations 7 and 8. Equation 30 indicates the manner in which the blackbody radiance of the local temperature within the nonisothermal body of gas is averaged along the line of sight; in essence it represents the appropriate weighting of the blackbody radiance function of the local temperatures by concentration and line-strength variations.

Equation 30 also represents the emission-absorption expression for the case of a molecular band consisting of nonoverlapping Lorentz lines, if x is replaced with \overline{x} as defined by equation 13.

For the case of a molecular band with some line overlapping, substitution of equations 16 and 17 into equation 1 yields

$$\mathbf{L}_{\nu}^{*}(\mathbf{T}^{*}) = (\mathbf{1} - \overline{\tau}_{\mathbf{L}})^{-1} \int_{\overline{\tau}_{\mathbf{L}}}^{1} \mathbf{L}_{\nu}^{*}(\overline{\tau}) \, \mathrm{d}\overline{\tau}$$
(31)

There are basically two approaches through which temperature profiles can be deduced from a set of measurements of spectral radiances and absorptances at various wavelengths. Given a set of T^* , the values of T can in principle be obtained by an appropriate inverse transformation, i.e., a mathematical inversion of (30) or (31). This inversion could in principle be accomplished analytically as, for example, in the case of the Abel transform applied to the expression for the observed transverse radiance of an optically thin axisymmetric source. In practice, such inversions must generally be handled numerically. The problem in essence is the solution of a set of n radiance equations to obtain a temperature profile approximated by n isothermal zones. The n equations must represent n substantially different optical depths; this can be achieved either by n observations at a particular frequency but different path lengths (as in the transverse scan of an axisymmetric source) or by observations at n frequencies for the same path. The latter case is more generally applicable, but also more difficult in that the n equations must be solved simultaneously rather than sequentially. Generally, moderateresolution molecular-band radiation is utilized in such studies; however the same principle applies to high-resolution observations of the contour of an isolated spectral line. This method appears to be straightforward: spectral data are obtained at n frequencies and used to solve n simultaneous radiance equations for n unknown local temperatures along the line of sight. However, the problem is not so simple because of the nonlinearity of the Planck function and the factors governing the growth of spectral lines, in particular the strongly nonlinear variation of line strengths with temperature. The main difficulties encountered are the mathematical instabilities and nonuniqueness of solutions which result primarily from the imprecision of the input data. Further discussions of these problems are to be found in the recent literature, much of which is concerned with the deduction of atmospheric temperature profiles from satellite observations [21-26].

The alternative approach, and the one employed in this investigation, in essence consists of a set of straightforward calculations using equations 30 or 31 and a model by which the temperature profile within the nonuniform body of gas is characterized by a very few parameters which are adjusted until the best agreement is obtained between calculated and observed values of T^* . This approach, which can also be characterized as an inversion in the broadest sense, does, of course, presume some prior knowledge of the shape of the temperature profile. However, this requirement is not much of a constraint for many engineering applications in which the general pattern of a high-temperature flow field can easily be specified. Likewise the argument that, mathematically, the minimization of differences between observed and calculated T^* does not necessarily imply a corresponding minimum between actual and calculated T [27] need not be a deterrent to this approach. Under the imposed constraint of a known shape to the temperature profile, it is difficult to see how large errors could be engendered by this approach. On this pragmatic basis, then, the present investigation was carried out, the objective being to determine how well temperature profiles could be so deduced, and thereby to assess the utility of emission-absorption spectroscopy so applied.

3 EXPERIMENTAL PROGRAM

3.1. APPARATUS AND PROCEDURES

The apparatus used in this investigation is shown in figure 1. In essence, it consists of a segmented combustion-tube furnace, housing a sample cell 60 cm in length, and positioned in one beam of a double-beam ratio-recording spectrometer which had been designed specifically for the study of emission and absorption in nonisothermal gases [28].

Figure 2 is a schematic of the optical arrangement. Light from a graphite-tube blackbody source [29] is split into two beams by a pair of diagonals and redirected into a pair of spherical mirrors. One beam passes through the sample cell in the furnace; the two beams are collected by another pair of spherical mirrors which reimage the blackbody aperture onto the slit of the monochromator. Iris diaphragms at each of the second pair of spheres serve to limit the angular field and to balance the beams.

Each chopper is made with two rows of holes differing in number so that the two beams are chopped at different frequencies, 420 and 780 Hz, which were chosen to facilitate signal separation. For absorption measurements, the chopper next to the blackbody is used; thus emission from the hot gas is not sensed. For emission measurements, the chopper next to the monochromator is used with the upstream shutter in the sample beam closed after the beams are balanced; thus the ratio of emission from the furnace to that of the blackbody is obtained.

The monochromator is equipped with a 300 lines/mm grating blazed at 3 μ m. A germanium filter in front of the entrance slit cuts off the radiation below 1.8 μ m to eliminate second-order light. An elliptical mirror images the exit slit onto a PbS detector, a 0.25×2.0 -mm Type P Kodak Ektron cell installed in a Dewar and cooled with liquid nitrogen.

The entire optical path outside the sample cell is thoroughly flushed by dry nitrogen in order to minimize absorption due to H_2O and CO_2 present in the atmosphere.

The electronic circuit is illustrated in figure 3. The signal from the detector is amplified, separated into two components by a filter network, and synchronously rectified by a demodulation circuit which is controlled by the signals of two photodiodes facing a pair of small lamps across the chopper. The intermodulation between beams was determined to be less than 1%, and through the use of a set of sectored discs rotated at high speed in the sample beam, the linearity of the entire system was established to be within 1%.



FIGURE 1. EXPERIMENTAL APPARATUS



- () BLACKBODY
- CHOPPER
 SPHERICAL MIRROR
 SHUTTER
- (6) IRIS DIAPHRAGM
 (7) GRATING MONOCHROMATOR
 (8) TEST CELL

(5) 7-SECTION FURNACE

FIGURE 2. OPTICAL ARRANGEMENT

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The output signals were displayed on a recording potentiometer. The reference beam signal was placed across the slide wire and the sample signal across the slider, so that the ratio of radiances in the two beams was indicated. A multiple-turn potentiometer connected to the shaft of the slider provided a signal which was passed through an analog-to-digital converter and recorded on punched cards; the readout command signal for the card punch was provided by a photodiode facing a lamp across a slotted disc on the monochromator wavelength drive.

Two types of sample cells were used in the present study; both were 60 cm in length and approximately 25 mm in diameter. The data for H_2O and CO_2 were obtained using a cell fabricated from fused silica; for the HF measurements, a Monel cell with bonded sapphire windows was fabricated. Carbon dioxide and hydrogen fluoride samples were admitted to the evacuated cell from supply cylinders through appropriate plumbing; the amount was monitored and measured with a bonded strain-gage absolute-pressure transducer. A liquid-nitrogen cold-trap and a mechanical pump comprised the vacuum system for disposing of the samples. Water vapor samples were introduced and measured by the arrangement shown in figure 4. The cell was evacuated and maintained at a uniform temperature. Distilled water was heated in a flask to a temperature at which the vapor pressure had the desired value. Since the sample cell and connecting tubes were maintained at a higher temperature than that of the flask, no condensation could occur during loading. Hence, the optical depth of the sample could be specified by the temperature of the cell and the vapor pressure in the flask. The CO₂ was of a purity commercially available. However, in order to eliminate H₂O from the HF samples, additional purification was carried out by the procedure described in reference 30.

Charges of H_2O and CO_2 could be contained in the quartz sample cell indefinitely with no long-term change in partial pressure detectable either by direct measurement or by observation of absorption. However, in spite of thorough presoaking, charges of HF would gradually diminish, presumably as the consequence of adsorption on the Monel cell walls. During the course of a run involving emission and absorption scans, decreases on the order of several percent were encountered. Therefore, data were collected in the following sequence: absorption, emission, absorption; the two absorption scans were then averaged prior to combination with the emission data for the evaluation of apparent temperatures. The partial pressures indicated in table I for these runs accordingly represent the average of the initial and final values.

The temperature distribution in the sample cell was measured by 10 chromel-alumel thermocouples equally spaced with one at the plane of each window. For the H_2O and CO_2 measurements, the thermocouples were welded to a thin stainless-steel sleeve which fitted closely over the quartz sample cell; for the HF measurements, the thermocouples were welded directly to the Monel cell. In an earlier study [31], in order to ascertain whether the temperature profile in the gas sample within the cell could be reliably assumed to be that measured along the outside wall of the cell, a test was made as illustrated in figure 5. The sample cell was simulated



FIGURE 4. METHOD FOR LOADING CELL WITH WATER VAPOR

TABLE I. SUMMARY OF EXPERIMENTAL CONDITIONS

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- -	2	1148	389	387	1153	1152	424	374	536	497	489	485	644	643		383			1153		1150	
nator)	מ	1146	558	541	1061	1059	637	541 97)	1114	725	725	729	1093	1074		555			1057		1061	
nochron	0	1147	751	737	994	993	873	812 (11	1160	908	908	913	1182	1178		752			066		994	
t to moi	_	1146	066	619	914	918	1147	1136	777	1090	1092	1100	1206	1209		066			915		918	
1 closes	٥	1146	1160	1160	824	835	1149	871 135)	1062	1189 224)	1189 234)	1199	934	934		1158			833		831	
Station	ი	1143	1128	1130	715	745	1147	855 (1:	1060	1184 (15	1186 (12	1192	1056	1060		1127			744		729	
(⁰ K) (41	1146	953	953	641	671	1147	1136	781	1105	1107	1112	1209	1212		958			673		639	
eratures	o	1144	723	719	537	593	884	813 93)*	1160	892	896	868	1189	1194		723			594		554	
Tempe	V	1147	537	528	464	513	649	535 (11)	1132	723	723	725	1073	1046		537			517		485	
•	1	1146	382	386	390	392	424	368	518	498	494	488	645	643		378			395		388	
Ч	(mm Hg)	1520	670	160	760	692	760	760	760	397	751	191	367	760	57	28	675	54	28	619	1520	
C	Gas	c_{0}^{0}	н ₂ о	co_2	c_{0_2}	$^{\rm H_2O}$	co_2	co_2	co_2	НF	HF	ΗF	НF	ΗF	H_2O	co_2^2	$^{\rm N}_2$	$\rm H_2O$	co_2	N_2	co	
ſ	Run	10216803	10216811	10216812	10246808	10246813	10286811	10286816	10286821	12056804	12056808	12056812	12276804	12276807		10216807			10246812		10246818	

*Values in parentheses obtained between stations using movable thermocouple.



FIGURE 5. VERIFICATION OF TEMPERATURE-PROFILE MEASUREMENT

by a fused silica tube 1 ft long and 1 in. in diameter, mounted in the furnace between two refractory discs. The outside temperature was measured with chronel-alumel thermocouples looped about the tube; the air temperature within the tube was measured by a small-gauge platinum-platinum 10% rhodium thermocouple. Negligible differences were observed between the outside and inside temperatures at any station; hence it was concluded that the radial gradient would be insignificant at any plane for a sample gas whose thermal conductivity was comparable to that of air at a pressure of 1 atm.

The wavelength calibration of the spectrometer followed from the observed spectrum of HF. The line positions for HF are very well known, so that this gas represents perhaps the best available calibration source for infrared spectrometers operating in the region 2.3 to 3.5 μ m. The slit function of the spectrometer was deduced from the observations of the weaker lines in the HF bands; its shape was very nearly triangular, and the half-width was approximately constant with wavelength, hence varied with frequency. Most of the data were obtained at a slit opening such that the effective slit width varied from about 2.5 cm⁻¹ at 3000 cm⁻¹ to 5.0 cm⁻¹ at 4000 cm⁻¹.

The intensity calibration of the spectrometer could be made in one of two fashions. With a mirror on the back side of one of the downstream shutters, the temperature of the blackbody could be observed using an optical pyrometer. However, this procedure required a correction for the fact that the mirror reflectances and window transmittances varied from 0.65 μ m, where the optical pyrometer bandpass was centered, to 2.5 μ m, where the measurements were made: and the magnitudes of these corrections were difficult to accurately evaluate in situ. Therefore, an alternative calibration procedure was adopted: a blackbody source whose emission in the 2.7- μ m region could be accurately evaluated was positioned in the sample beam. The most convenient source for this method was a 2-atm charge of CO₂ in the sample cell itself, which was then maintained at a temperature as close as possible to isothermal. The center of the $2.7-\mu m$ CO₂ band was black under these conditions; hence its emission could be obtained from the Planck function of the measured cell temperature. Under the above isothermal conditions with an optically dense charge in the cell, the emission from the cell window, being at the same temperature as the gas in the cell, did not influence the observed radiation. However, in general, a correction for window emission was required; the manner in which this was incorporated into the data reduction procedure is detailed in appendix A.

The raw data recorded on punched cards were processed using the University's IBM 360 computer; the reduced data were provided on punched cards from which an automatic curve plotter could in convenient format produce the spectra in terms of spectral radiance or absorptance, plotted against wavelength or frequency as desired.

3.2. PRESENTATION OF SPECTRA

Spectral radiances and absorptances in the 2.7- μ m region were measured for a number of temperature profiles using pure samples of H₂O vapor and CO₂. Measurements were also obtained for two of the profiles using a mixture of these gases with nitrogen in a proportion simulating the products of combustion of CH₄ with air at a fuel/air weight ratio of 0.02 (except that the surplus oxygen was replaced with nitrogen). Finally, a number of observations were made of the 2.3- μ m overtone band of CO and the 2.5- μ m fundamental band of HF. Table I summarizes the data collected and the conditions of the measurements.

A complete set of radiance and absorptance spectra are presented in appendix B. The data for CO_2 , H_2O , and CO were collected using the automatic card-punching output of the spectrometer; hence, the reduced data are displayed. The resultant spectra for the CO_2 and H_2O runs are quite faithful to the original chart recordings that were also obtained. On the other hand, the strength of the 2.3- μ m overtone band of CO is so weak that, even with the high cell loadings, the reduced spectra were considerably altered in appearance because of the uncertainties in the very low values of the observed absorptances. The data for HF were collected only by chart recording, since punched-card recording of the widely separated intense lines with fidelity would have required very long scan times which were not desirable for several reasons. Accordingly, the radiance and absorptance spectra for HF are reproductions of the original recordings; the full-scale lines for emission were traced in by superimposing the appropriate prerun or postrun scans with the cell evacuated.

3.3. COMPARISONS WITH PREDICTED SPECTRA

The deduction of temperature profiles from observed spectra is a much more uncertain process than the calculation of nonisothermal spectra given the temperature profile. Accordingly, it is in order to examine first how well nonisothermal spectra can be calculated using a band-model expression. Therefore, a number of the spectra obtained in this study were compared with radiances and absorptances predicted as follows.

Equations 16 and 17, as combined in equation 31, were programmed, using a trapezoidal approximation, in Fortran IV language for computation by University's IBM 360 computer. Equation 31 not only encompasses the nonoverlapping band-model approximation but also the isolated line expression as given by equation 30. The General Dynamics tabulations of band-model parameters for H_2O and CO_2 were used in the present investigation [12, 32]: a sample calculation is shown in appendix C. Figures 6 through 9 are typical of the observed values of spectral radiance, absorptance, and apparent temperatures for H_2O and CO_2 in comparison with the predicted values. In general, the agreement is satisfactory.

For HF, computed values of line strengths and widths [33, 34] were used in equation 30. Since the large charges of HF in the 60-cm cell produced considerable overlapping in the wings



(a) Radiance vs. Frequency

FIGURE 6. COMPARISON OF ISOTHERMAL CO₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216803)





FIGURE 6. COMPARISON OF ISOTHERMAL CO₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216803) (Continued)









(a) Radiance vs. Frequency

FIGURE 7. COMPARISON OF NONISOTHERMAL H₂O SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216811)





FIGURE 7. COMPARISON OF NONISOTHERMAL H₂O SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216811) (Continued)









FIGURE 8. COMPARISON OF NONISOTHERMAL CO₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216812)


(b) Absorptance vs. Frequency

FIGURE 8. COMPARISON OF NONISOTHERMAL CO₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216812) (Continued)





FIGURE 8. COMPARISON OF NONISOTHERMAL CO₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216812) (Concluded)



FIGURE 9. COMPARISON OF NONISOTHERMAL $\rm H_2O/\rm CO_2/N_2$ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216807)



FIGURE 9. COMPARISON OF NONISOTHERMAL H₂O/CO₂/N₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216807) (Continued)





FIGURE 9. COMPARISON OF NONISOTHERMAL H₂O/CO₂/N₂ SPECTRA WITH BAND-MODEL CALCULATIONS (RUN 10216807) (Concluded)

of the lines, total radiances and equivalent widths could not be readily evaluated from the observed spectra. Hence, comparisons were made only of the apparent temperatures, representing the ratio of observed peak radiances and absorptances, thus obviating the need for measuring areas under lines and estimating corrections for overlapping. Typical results are shown in figure 10, in which apparent temperatures are plotted against a generalized rotational quantum number for the v = 0 = 1 and v = 1 = 2 bands of HF, where the number designates vibrational state.

Figures 6 through 10 are indicative of the accuracy to which spectra can be calculated using the currently available knowledge of molecular band-model parameters (or in the case of HF the knowledge of the line strengths and widths). There are a number of anomalies in the band-model calculations which must be attributed to errors in the tabulations of the parameters. The most obvious of these is the glaring feature near 3660 cm^{-1} in the isothermal CO₂ spectra (fig. 6); it is not quite so evident but also present in the nonisothermal CO₂ spectra (fig. 8). It would, of course, be a simple matter to insert an appropriate false value into the tabulations in lieu of a reevaluation using original absorptance spectra. However, for the present study, no particular purpose would have been served by correcting these errors, which were simply ignored in the following analyses.

3.4. TEMPERATURE PROFILE DETERMINATIONS

In this investigation it was found to be more convenient to work with plots of apparent temperature vs. absorptance rather than vs. wavelength for successive comparisons of band-model predictions based on temperature-profile models. This result was consistent with the conclusion reached in an earlier study of H₂-F₂ flames [34], in which the final comparisons of theory and experiment were made in terms of apparent temperature vs. rotational quantum number. The convenience obtains from the rather simple shape of such plots, which were all quite similar. Physically, this similarity is easy to understand. At lower values of absorptance (or higher rotational quantum numbers for the case of HF), the hot gas is much more transparent, and the apparent temperature will approach a constant value corresponding to the optically thin gas and representing the average radiance along the entire optical paths. Conversely, as the absorptance approaches unity, the apparent temperature should approach the value corresponding to radiances at the near boundary, and in the limit would reach the actual temperature at that location. Thus, regardless of the shape of the actual profile, one would expect all the curves of apparent temperature vs. absorptance to be much alike and that, for a particular profile, the value of T^{*} should be a function mainly of absorptance and not very dependent on wavelength.

Using these curves of apparent temperatures vs. absorptance, temperature profiles were determined for the H_2O and CO_2 runs by successive calculations with the band-model program.



FIGURE 10. COMPARISON OF NONISOTHERMAL HF SPECTRUM WITH ISOLATED-LINE CALCULATIONS (RUN 12056804). R and P are branch designations.

Since this was an exploratory study, the parameters characterizing the temperature profiles were adjusted in simple sequences until a best fit between calculations and observations was obtained. This procedure is illustrated in complete detail in appendix D. The results of these inversions are shown in figures 11 through 17, in which the inferred temperature profiles are compared with the values measured directly by the thermocouples, as indicated by the crosses.

A variety of options were exercised in regard to the specification of the number of parameters characterizing the temperature profile. For example, linear and symmetrical triangular profiles can always be characterized by two parameters, the maximum and minimum temperatures. However, if one has the further constraint that the lower temperature is known, then these profiles can be characterized by only one parameter. Similarly, the number of parameters for the other profiles can vary; in the case of the truncated triangle, the width of the isothermal region at the higher temperature can be included as a parameter, or taken to be a known fixed value implicit in the a priori knowledge of the shape of the profile. Such specifications are not as arbitrary as they might seem at first glance. In many practical applications involving propulsion devices, the geometry of the system will clearly indicate the location and extent of temperature maxima and minima, and the lower temperature at the boundary of the gas stream can be related to a value easily measured on a duct or exhaust nozzle wall.

The corresponding comparisons of deduced and observed temperature profiles for the HF runs are shown in figures 18 through 22. For these comparisons, the profile models were again taken to consist of linear segments. However, in these runs, the shapes of actual profiles imposed on the sample were not so well approximated by linear segments as they would have been by curves consisting of parabolic segments. Figure 23 shows the results for a single maximum profile approximated with a parabola specified by one or two parameters.



FIGURE 11. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10216811)



FIGURE 12. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10216812)



FIGURE 13. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10246808)



FIGURE 14. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10246813)



FIGURE 15. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10286811)



FIGURE 16. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10286816)



FIGURE 17. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 10286821)



FIGURE 18. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 12056804)



FIGURE 19. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 12056808)



FIGURE 20. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 12056812)



FIGURE 21. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 12276804)



FIGURE 22. TEMPERATURE PROFILES EXTRACTED FROM EMISSION AND ABSORP-TION SPECTRA (RUN 12276807)



FIGURE 23. TEMPERATURE PROFILES USING PARABOLAS EXTRACTED FROM EMISSION AND ABSORPTION SPECTRA (RUN 12056804)

4 DISCUSSION OF RESULTS

The results of this investigation, as presented in the comparisons of the temperature profiles deduced from the emission and absorption spectra with the directly measured profiles (figs. 13 through 23), clearly validate the present approach in the application of infrared emission-absorption spectroscopy to temperature-profile determination. In all cases the agreement between the inferred and the directly measured temperature profiles was satisfactory in view of the quality and quantity of the information available on the spectral properties of the emitting and absorbing gases, the experimental errors in the measurements of temperatures and radiances, and the representation of the temperature profiles by linear segments. The principal conclusion to be drawn from this work, therefore, is that infrared emission-absorption spectroscopy offers considerable promise as a means for determining temperature profiles in nonisothermal radiating gases. However, further development of this approach would be requisite to the successful extension of the method from the controlled conditions in the furnaceheated cell in the present study to those encountered in the testing of full-size engines. Along these lines, it would be especially appropriate to apply it to an intermediate case of a nonisothermal source created in an appropriate combustion apparatus in the laboratory, in which the temperature profiles could be independently determined.

Further analyses of the mathematical methods for inversion of spectra might also be in order. In this regard it could be expected that the problem of nonuniqueness of the solutions could largely be avoided in an approach which could be characterized as intermediate between the method of the present study based on successive calculations using a profile model, and true inversion calculations which assume no knowledge whatsoever of the profile. One approach would be an inversion calculation involving a trial solution based on a priori knowledge of the shape of the profile, with numerical values obtained by the present method. Another approach, applicable to axisymmetric flow fields, would be to deduce the general shape of the temperature profiles from transverse spatial scans at particular frequencies, thus providing the initial guesses for the inversion. In order to assess the advantages of one approach over another thoroughly, or the possible combination of the two, more complete experimental data representing a greater variety of temperature profiles would be required.

In considering the application of infrared spectroscopy to propulsion studies, it should be kept in mind that, for most combustion systems, the principal products which radiate in the infrared are CO_2 and H_2O , which are also present in the atmosphere. In the present experiment,

the optical path outside of the sample cell was thoroughly flushed with dry nitrogen to eliminate the atmospheric absorption. However, it is not always possible to do this with an instrument viewing a jet or rocket engine; an unflushed path of even a few centimeters will result in appreciable absorption which must be taken into account. The method for doing this is straightforward; the radiative-transfer calculation is simply set up for the entire optical path, not just that through the hot gas stream.

The ultimate accuracy of the temperature profiles deduced by emission-absorption spectroscopy is difficult to establish from the present results alone. Obviously, errors in the radiance and absorptance measurements could be further reduced by more meticulous attention to the calibration method. Using an optically dense charge of gas with a uniform temperature appears to be a preferable means of calibration rather than using a blackbody and evaluating corrections for mirror reflectance changes with wavelength. However, considerable improvement would result in the use of a windowless absorption cell to eliminate corrections for emission, absorption, and reflection by the window materials, the properties of which vary both with temperature and wavelength. Further accuracy could be gained through the use of a precision temperature controller to better equalize the temperatures along the length of the sample cell.

The use of a two-sided instrument is recommended; that is, the reference source for absorption should be located on the opposite side of the hot gas from the detector. One-sided systems utilizing a passive element on the far side of the hot gas, e.g., a flat or spherical mirror or a corner-cube reflector, offer some advantages: convenience in packaging an instrument for installation in a test cell, and, in the case of a corner-cube, resisting the effects of highlevel acoustic environment. However, for the most precise measurements, this convenience would be outweighed by the difficulties accounting for the reflectance losses of the mirror, and in treating the more complex profile represented by the apparent doubling of the source.

Finally, the reliability of the inferred temperature profiles could be enhanced by the use of an appropriate calculation, programmed for a computer, for fitting the band-model predictions to the observed variation of apparent temperatures with absorptance.

5 SUMMARY OF RESULTS

Emission-absorption spectroscopy has been shown to provide a means for determining temperature profiles within bodies of hot gases which are nonuniform and optically dense in regions of molecular-band radiation. In review, the approach explored in the present study is based on the following premises.

- 1. Local thermodynamic equilibrium prevails throughout the gas.
- 2. The general character of the temperature and density profiles are known so that their shapes can be specified in terms of a very few parameters.
- 3. The spectral properties of the emitting-absorbing species are known. For polyatomic molecules, the required properties are two band-model parameters characterizing the positions, strengths, and spacings of the lines, as functions of frequency and temperature. For diatomic molecules exhibiting nonoverlapping lines, the alternative requirement is knowledge of line positions, and strengths and widths as functions of temperature.

The recommended procedure for deducing temperature profiles from emission and absorption spectra consists of:

- 1. Quantitative measurements of emission and absorption to yield values of spectral radiances and absorptances throughout a molecular band.
- 2. Evaluation of apparent temperature as a function of frequency from the ratio of the spectral radiances and absorptances.
- 3. Deduction of the temperature profile from the observed variation of apparent temperature, with absorptance (or rotational quantum number) by means of a best fit of bandmodel calculations (or isolated-line calculations) obtained by appropriately adjusting the profile-shape parameters.

This procedure has been shown to yield satisfactory agreement with direct measurements of temperature profiles of various shapes in water vapor, carbon dioxide, hydrogen fluoride, and a mixture of water vapor, carbon dioxide, and nitrogen.

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Appendix A DATA REDUCTION PROCEDURE

The raw data on the emission and absorption were processed by a digital computer to yield spectral radiances, absorptances, and apparent temperatures. In accordance with the requirements outlined in section 3 (Apparatus and Procedures), the computer program was set up to utilize emission-absorption measurements in an isothermal charge of CO_2 as the fundamental calibration source. Since the output of the instrument, as deflections on the chart recorder or voltages recorded on punched cards, was proportional to the radiance of the blackbody built into the spectrometer, it was necessary to deduce from the observed output of the isothermal CO_2 charge the effective radiation temperature of the blackbody. Furthermore, in order to account for the emission from the cell windows, an in situ measurement of the absorptance spectrum of the window at the operating temperature was a required part of the data collection.

Spectral data were gathered in an appropriate sequence.

- 1. Absorption, background (cell empty)
- 2. Absorption, isothermal (CO_{9})
- 3. Absorption, nonisothermal (gas sample)
- 4. Emission, beam balance (cell empty)
- 5. Emission, window (cell empty)
- 6. Emission, isothermal (CO₂)
- 7. Emission, nonisothermal (gas sample)

In addition, zero energy levels were checked during each scan. Note that, in the absorption mode, the zero energy level represented full scale, whereas the zero absorptance was given by scan 1, the background scan with the cell empty. On the other hand, in the emission mode, zero energy level corresponded to zero radiance, whereas full scale corresponded to the effective radiance of the blackbody as given by scan 4. The two modes of operation are illustrated in figure A1, a schematic representation of the various scans.

The calculations proceeded stepwise as indicated below; the quantity D refers to the signal voltage i.e., the deflection on the chart recorder.

I. Isothermal Absorption

Input:

- 1. Absorption, zero, $D_{a,0}$
- 2. Absorption, background D_{a,bk}
- 3. Absorption, CO_2 sample, $D_{a,s}$



FIGURE A1. SCHEMATIC REPRESENTATION OF VARIOUS SCANS

Output:

1. Absorptance, $\alpha_{iso}(\nu)$

Equations used:

$$\alpha_{iso}(\nu) = 1 - R_{a,iso}$$
$$R_{a,iso} = \frac{D_{a,s} - D_{a,o}}{D_{a,s} - D_{a,o}}$$

II. Isothermal Emission

Input:

- 1. Emission, cell windows, D_{e,w}
- 2. Emission, beam balance, De,b
- 3. Emission, CO_2 sample, $D_{e,s}$
- 4. Temperature, average of thermocouple indications, T_{t.c.}
- 5. Window reflectance, $\rho_w vs. v$
- 6. Isothermal absorptance, $\alpha_{iso}(\nu)$

Output:

- 1. Effective blackbody temperature $T_{bb}(\nu)$
- 2. Radiance, $L_{\nu,iso}$
- 3. Apparent temperature, T^{*}_{iso}
- Average effective blackbody temperature, T_{bb}
 Equations used:

$$L_{\nu,bb}^{*} = \frac{\alpha_{iso}(\nu)L_{\nu}^{*}(T_{t.c.})}{R_{e,iso}(1 - \rho_{w})^{2}}$$

$$R_{e,iso} = \frac{D_{e,s} - D_{e,w}}{D_{e,b} - D_{e,w}}$$

$$T_{bb}(\nu) = c_{1}\nu^{3} \ell n \left(\frac{c_{2}\nu}{L_{\nu,bb}^{*}} + 1\right)$$

$$\overline{T}_{bb} = \frac{1}{n} \sum_{i=1}^{n} T_{bb}(\nu_{i})$$

$$L_{\nu,iso} = R_{e,iso}(1 - \rho_{w})^{2} L_{\nu}^{*}(\overline{T}_{bb})$$

$$T_{iso}^{*} = c_{2}\nu / \ell n \left\{ c_{1}\nu^{3}\alpha_{iso}(\nu) / L_{\nu,iso} \right] + 1 \right\}$$

Input:

- 1. Emission, zero, D_{e,o}
- 2. Emission, beam balance, D_{e,b}
- 3. Emission, cell window, $D_{e,w}$
- 4. Temperature of window 2, T_{w2}
- 5. Average effective blackbody temperature, \overline{T}_{bb}

Output:

1. Window 2 absorptance, $\alpha_2(\nu, T)$ Equations used:

$$\begin{aligned} \alpha_{2}(\nu, \mathbf{T}) &= \left[1 + \left(\frac{1 - \mathbf{R}_{w}}{\mathbf{R}_{w}} \right) \frac{\mathbf{L}_{\nu}^{*}(\mathbf{T}_{w2})}{\mathbf{L}_{\nu}^{*}(\mathbf{T}_{bb})} \frac{1}{(1 - \rho_{w})^{2}} \right]^{-1} \\ \mathbf{R}_{w} &= \frac{\mathbf{D}_{e,w} - \mathbf{D}_{e,o}}{\mathbf{D}_{e,b} - \mathbf{D}_{e,o}} \end{aligned}$$

IV. Nonisothermal Absorption

Input:

- 1. Absorption, zero, D_{a,o}
- 2. Absorption, background, D_{a,bk}
- 3. Absorption, sample gas, $D_{a,s}$

Output:

1. Spectral absorptance, sample gas, $\alpha(\nu)$

Equations used:

$$\alpha(\nu) = 1 - R_{a}$$
$$R_{a} = \frac{D_{a,s} - D_{a,o}}{D_{a,bk} - D_{a,o}}$$

V. Nonisothermal Emission

Input:

- 1. Emission, cell windows, $D_{e,w}$
- 2. Emission, beam balance, D_{e,b}
- 3. Emission, sample gas, $D_{e,s}$
- 4. Blackbody temperature, \overline{T}_{bb}

- 5. Window reflectance, $\rho_{\rm W}$
- 6. Window 2 absorptance, $\alpha_2(\nu, T)$
- 7. Window 2 temperature, T_{w2}
- 8. Spectral absorptance, sample gas, $\alpha(\nu)$

Output:

- 1. Spectral radiance, sample gas, $\mathbf{L}_{\boldsymbol{\nu}}$
- 2. Apparent temperature, sample gas, $T^*(\nu)$

Equations used:

$$\mathbf{L}_{\nu} = \mathbf{R}_{e} \mathbf{L}_{\nu}^{*} (\overline{\mathbf{T}}_{bb}) (1 - \rho_{w})^{2} (1 - \alpha_{2}) + \mathbf{L}_{\nu}^{*} (\mathbf{T}_{w2}) \alpha_{2} \alpha(\nu)$$

$$R_{e} = \frac{D_{e,s} - D_{e,w}}{D_{e,b} - D_{e,w}}$$

Appendix B EMISSION AND ABSORPTION SPECTRA

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FIGURE B23. EMISSION AND ABSORPTION SPECTRA, RUN 12056808. Gas: HF. P = 751 mm. Temperature (^OK) = 494, 723, 896, 1107, 1186, 1189, 1092, 908, 725, 489.







FIGURE B25. EMISSION AND ABSORPTION SPECTRA, RUN 12056812. Gas: HF. P = 191 mm. Temperature (^oK) = 488, 725, 898, 1112, 1192, 1199, 1100, 913, 729, 485.







FIGURE B27. ABSORPTION SPECTRA, RUN 12276804 (REPEAT) AND RUN 12276807 (REPEAT). For Run 12276804, gas: HF. P = 367 mm. Temperature (⁰K) = 645, 1073, 1189, 1209, 1056, 934, 1206, 1182, 1093, 644. For Run 12276807, gas: HF. P = 760 mm. Temperature (⁰K) = 643, 1046, 1194, 1212, 1060, 934, 1209, 1178, 1074, 643.





Appendix C SAMPLE BAND MODEL RADIATION CALCULATION

The programming of equations 16, 17, and 31 for the computation of spectral transmittances, radiances, and apparent temperatures was done in Fortran IV language for The University of Michigan's IBM 360/67 computer. The equations are collected, and steps in the procedure are presented below, along with the printout of a sample calculation at $\nu = 3500 \text{ cm}^{-1}$ for run 10246808.

The spectral radiance at the boundary, \overline{L}_{ν} , is calculated by equations 17, approximated using the trapezoidal rule:

$$\overline{\mathbf{L}}_{\nu} = \sum_{i=1}^{n} \mathbf{L}_{\nu}^{*}(\overline{\tau}_{i}) \left(\Delta \overline{\tau} \right)_{i}$$

in which the spectral transmittance difference $(\Delta \tau)_i = \tau_{i-1} - \tau_i$ is obtained from equation 15:

$$\overline{\tau}_{i} = \exp\left[-\beta_{e}f(\overline{x}_{i})\right]$$

and

$$\overline{\tau}_0 \equiv 1$$

For a mixture of m absorbing gases:

$$\overline{\tau}_{i} = \iint_{k=1}^{m} \overline{\tau}_{i,k}$$

The function f(x) is the Ladenburg-Reiche expression:

$$f(\mathbf{x}) = \mathbf{x} e^{-\mathbf{x}} [\mathbf{J}_0(\mathbf{i}\mathbf{x}) - \mathbf{i}\mathbf{J}_1(\mathbf{i}\mathbf{x})]$$

The argument \overline{x} is the dimensionless optical depth defined by equation 13:

$$\widetilde{\mathbf{x}}_{i} = \beta_{e}^{-1} \sum_{j=1}^{i} \widetilde{\mathbf{k}}(\mathbf{T}_{j}) [\beta(\mathbf{T}_{j})/\beta_{e}]^{\eta} (\Delta \mathbf{X})_{j}$$

in which $\overline{k}(T_j)$ is the local value of the first band-model parameter, the average absorption coefficient, corresponding to the average line strength to spacing ratio:

$$\overline{\mathbf{k}}(\mathbf{T}) = \overline{\mathbf{S}}(\mathbf{T})/\mathbf{d}$$

 $\beta(T_j)$ is the local value of the second band-model parameter, the line-overlap factor, corresponding to the average line width to spacing ratio:

$$\beta(\mathbf{T}) = 2\pi \overline{\gamma} (\mathbf{T})/d$$

The optical depth increment is given by

$$(\Delta X)_i = P_i(\Delta L)_i$$

where P_i is the local value of the partial pressure of the radiating species, and $(\Delta L)_i$ is the geometrical path increment. The exponent η is an empirically derived factor given by [5]:

$$\eta = f(0.05\overline{x}_{L,e}) \sqrt{\pi/(0.1\overline{x}_{L,e})}$$

where the total dimensionless optical depth $\overline{x}_{L,e}$ is the mean between the strong- and weakline approximations.

The band-model parameters were extracted from the General Dynamics tabulations [12, 32] and entered into the program as two-dimensional tables: \overline{k}_0 vs. ν , T and β_0 vs. ν , T with appropriate interpolation subroutines. The tabulated values, k_0 , represented the normalization of the experimentally derived values to standard conditions of pressure and temperature to account for the dependency on gas density; accordingly, denormalization consisted of:

$$\overline{\mathbf{k}}(\nu, \mathbf{T}) = \overline{\mathbf{k}}_{0}(\nu, \mathbf{T})\sqrt{273/\mathrm{T}}$$

The pressure dependency is accounted for in the optical depth definition. The tabulated values of the line-overlap factor, β_0 , are normalized to a unit effective broadening pressure, defined by

$$\mathbf{P}_{\mathbf{e}} = \sum_{k=1}^{m} \alpha_k \mathbf{P}_k$$

where $P_{k=1}$ is the value P_i in the optical depth definition; $P_{k>1}$ are the partial pressures of the foreign broadening gases (other species which may or may not be radiating at frequency ν); $\alpha_{k=1} \equiv 1$, and $\alpha_{k>1}$ are the broadening coefficients derived from experimental line-broadening studies. The values of α used in this investigation were extracted from data in the literature [35]:

$$\alpha = 0.20$$
, N₂ broadening H₂O
 $\alpha = 0.77$, N₂ broadening CO₂

Thus

$$\beta(\nu, T) = \beta_0(\nu, T)P_e$$

The effective value, β_{e} , was taken to be the mass-weighted average along the entire path:

$$\beta_{e} = \frac{\sum_{i=1}^{n} \beta_{0}(T_{i}) P_{e,i}(P_{i}/T_{i})(\Delta L)_{i}}{\sum_{i=1}^{n} (P_{i}/T_{i})(\Delta L)_{i}}$$

The computation proceeded according to the following steps:

- 1. Read in:
 - (a) Names and number (m) of component gases.
 - (b) Frequencies ν_{ℓ} , $\ell = 1 \dots q$ (or $\nu_{\text{initial}}, \Delta \nu$, and number q).
 - (c) Incremental lengths $(\Delta L)_i$, $i = 1 \dots n$ (or total length L and number n).
 - (d) Partial pressures, $P_{i,k}$, $i = 1 \dots n$, $k = 1 \dots m$.
 - (e) Broadening coefficients, α_{k} , k = 1 . . . m.
 - (f) Temperature profile, T_i , $i = 1 \dots n$.

2. For absorbing gas k = 1:

- (a) Store Program Table I: $k_0(\nu, T)$ vs. ν , T; and Program Table II: $\beta_0(\nu, T)$ vs. ν , T.
- (b) For frequency ν_1 :
 - (1) Calculate $P_{e,i}$
 - (2) Calculate β_{e}
 - (3) Calculate $\overline{\mathbf{x}}_{\mathbf{L},\mathbf{W}} (\overline{\mathbf{x}}_{\mathbf{L}} \text{ for } \eta = 0)$
 - (4) Calculate $\overline{\mathbf{x}}_{\mathbf{L},\mathbf{s}}^{-,\cdots}$ ($\overline{\mathbf{x}}_{\mathbf{L}}^{-}$ for $\eta = 1$)
 - (5) Calculate $\eta = \eta [(x_{L,W} + x_{L,s})/2]$, using function subprogram in which Program Table III, f(x) vs. x, is stored.
 - (6) Calculate $\overline{\tau}_{i}$, k = 1, ℓ = 1 using Program Tables I, II, and Subprogram Table III, and store $\overline{\tau}_{i,1,1}$, i = 1 . . . n
- (c) Repeat 2(b) for all other ν_{ℓ} , $\ell = 1 \dots q$
- 3. Repeat 2 for next absorbing gas, etc.
- 4. For ν_1 :

(a) Calculate
$$\overline{\tau}_{i,1} = \iint_{k=1}^{m} \overline{\tau}_{i,k,\ell}, \ \ell = 1$$

- (b) Calculate and store \overline{I}_{ν_1}
- (c) Calculate and store $(1 \overline{\tau}_{L,1})$
- (d) Calculate $I_{\nu_1}^{*}(T^*)$

(e) Calculate and store T_1^* using Planck function.

- 5. Repeat 4 for all ν_{ℓ} , $\ell = 2 \dots q$.
- 6. Print out $\overline{L}_{\nu_{\rho}}$, $(1 \overline{\tau}_{L,\ell})$, T_{i}^{*} , ν_{ℓ} .
- 7. Go back to 1 and repeat calculation for other conditions: P_i , T_i , etc.

The following printout for the sample calculation contains, in addition to the normally requested quantities, \overline{L}_{ν} , $1 - \overline{\tau}_{L}$, T^* , and ν , for ν_{ℓ} , $\ell = 1 \dots q$, the intermediate quantities, $\beta(T_i)$, $\overline{k}(T_i)$, x_i , T_i , $f(x_i)$ and $\overline{\tau}_i$ for $i = 1 \dots 100$.

PLEASE ENTER NAMELIST IN.

```
AIN GAS= 'CO2 ',NT= 10, TEMP=390., 464., 537., 641., 715., 824., 914., 994.,
1061.,1153.,LENGTH=60.,INU=-10,NU=3500.,MON=10,DAY=24,YEAR=65,
RUN=8, ALPHA=1., PTAB=1., NG=1, EXP0=-5., ITYPE=1.NFREQ=1.NDIV=-100.
TODAY='06/25/69' 4END
> INTERPOLATED VALUES OF TEMPERATURE
                                      419.97
                                              426.63
                                                       433.29
                                                                439.95
    393.33 399.99
                     406.65
                             413.31
>
    446.61
            453.27
                     459.93
                             466.55
                                      473 . 12
                                               479.69
                                                       486.26
                                                                492+83
>
            505.97
                     512-54
                             519-11
                                      525-68
                                               532-25
                                                       539-60
                                                                548.96
    499.40
>
            567+68
                                      595.76
                                               605-12
                                                       614-48
                                                                623.84
    558.32
                     577.04
                             556.40
>
                     648.77
                             655+43
                                      662.09
                                               668.75
                                                       675-41
                                                                652.07
    633-80
            642.11
>
                     702.05
                             708 - 71
                                      715+54
                                               725.35
                                                                744.97
    655.73
            695.39
                                                       735-16
>
                                                                823+45
    754+78
            764.59
                     774.40
                             784+21
                                      794.02
                                               803.83
                                                       813 . 64
>
                     847.85
                                              872.15
                                                       880.25
                                                                555-35
    831.65
            839.75
                             855+95
                                      864-05
>
                                              934-40
                                                       941.60
                                                                945.79
    896.45
            904-55
                     912.65
                             920-00
                                      927.20
            963.19
                   970-39
                            977.59
                                     984-79
                                              991.99
                                                       995-35 1004-35
    955.99
   1010-41 1016-44 1022-47 1028-50 1034-53 1040-56 1046-59
                                                              1052+62
>
   1058-65 1066-05 1074-33 1082-61 1090-89 1099-17 1107-45 1115-73
>
   1124.01 1132.29 1140.57 1148.85
> PATHLENGTH INCREMENT =
                            0.60 CM.
                                              PAGE
> 06/25/69
                                                      1
        NONISOTHERMAL BAND MODEL CALCULATIONS
                 (OVERLAPPING LINES)
        5,0N 10/24/65, L=
                             60.00 CM, TMP(1)= 393.3
> RUN
> DEG K, TMP( 100) = 1148.9 DEG K, P(CO2 )= 1.000 ATM
  FREQUENCY
              RADIANCE
                             T STAR
                                             ABSORP.
   (1/CM)
            (W/(CM+STR))
                              (DEG K)
   3500.0
              1.4205E-04
                             9.0339E 02
                                            0.73046
>
```

> EFFECTIV		597.27 DEG K.				
> EFFECTIV	E PRESSURE = 1 + 00	/ AIM+				
> EFFECTIV	> EFFECTIVE BETA = 0.1061E 02.					
. BETA/EFF	ECTIVE BETA ABS	SORPTION COEFFICIENT				
> 0.27	750E 00	0•3592E-02				
> 0.56	591E 00	0-4100E-02				
> 0+30	03E 00	0.4301E-02				
> 0.31	14E 00	0•4496E-08				
> 0.32	225E 00	0.4684E-08				
> 0.33	37E 00	0.4866E-02				
> 0.34	145E UU	0.5043E-02				
> 0.3:		0.5814E-08				
> 0.30	0/12 UU	0.5351E-02				
> 0.31		0.53422-02				
> 0.40	9942 00 10AF 00	0.55515-02				
> 0.41	1AF 00	0.50075-00				
> 0.49	945 00	0.61385-02				
> 0.43	1345 00	0-49775-00				
> 0.44		0.6411E-02				
> 0.44	54E 00	0.45425-02				
> 0.4	63E 00	0-66708-02				
> 0.47	73E 00	0.67845-09				
> 0.45	152 00	0.69165-02				
> 0.49	93E 00	0.70345-09				
> 0.51	03E 00	0.7149E-08				
. 0.58	186E 00	0.7274E-02				
> 0.53	52E 00	0.7429E-08				
> 0.55	539E 00	0.7579E-02				
> 0.56	95E 00	0.7724E-02				
> 0+58	52E 00	0.7864E-02				
> 0.60	08E 00	0.5000E-02				
> 0+61	64E 00	0.8132E-02				
> 0+64	134E 00	0 • 5767E-02				
> 0.67	96E 00	0+9796E-02				
> 0.71	58E 00	0+1079E-01				
> 0.75	520E 00	0-1176E-01				
> 0.78	165E 00	0•12 66E- 01				
> 0.81	23E 00	0+1331E-01				
> 0+83	181E 00	0+1395E-01				
> 0.56	38E 00	0+1458E-01				
> 0.88	96E 00	0+1520E-01				
> 0.91	54E 00	0+1580E-01				
> 0.94	112E 00	0+1639E-01				
> 0.96	67E 00	0-1697E-01				
> U•99	272 00	0+1754E-01				
> 0.10	NICE UI	0.1810E-01				
> 0+10	718 A1	U+ 15642*U1				
■ U•10	DAE OI	0.19205-01				
> 0.11	478 01	U• 177 / E= U1				
	475 UI	0.21455-01				
> 0.10	9995 A1	0+21432-01 0-99175-01				
> 0.12	695 UI 615 A1					
- 0+18	WIE VI	A+55005-A1				

>	0.1299E 01	0-2354E-01
>	0.1336E 01	0.2420E-01
>	0.1374E 01	0.2454E-01
>	0-1412E 01	0.2547E-01
>	0-1450E 01	0-2609E-01
>	0-1466E 01	0-8669E-01
>	0.1520E 01	0-2718E-01
>	0.1551E 01	0-2765E-01
>	0+1583E 01	0-2511E-01
>	0.1614E 01	0+2857E-01
>	0+1645E 01	0-2902E-01
>	0.1677E 01	0.2946E-01
>	0.1708E 01	0+2959E-01
>	0.1739E 01	0-3031E-01
>	0.1771E 01	0-3073E-01
>	0.1802E 01	0-3114E-01
>	0+1834E 01	0-3154E-01
>	0.1562E 01	0-3190E-01
>	0.1890E 01	0-3224E-01
>	0+1918E 01	0.3258E-01
>	0-1946E 01	0+3292E-01
>	0.1973E 01	0.3325E-01
>	0+2001E 01	0•3357E-01
>	0.2029E 01	0•33 59E- 01
>	0-2057E 01	0•3421E-01
>	0.2085E 01	0+3452E-01
>	0.2113E 01	0-3452E-01
>	0.2141E 01	0.3512E-01
>	0-2165E 01	0-3539E-01
	0-2159E 01	0-3563E-01
>	0.2212E 01	0+35882-01
>	0.2235E 01	0+36122-01
>	0-2259E 01	0.3635E-01
>	0.55655 01	0.36592-01
>		0.32055-01
>	0.0250E 01	0-37032-01
<u>.</u>	0.93755 01	0.37505-01
Ś	0.23995 01	0.37725-01
5	0.94975 01	0.37995-01
5	0.94598 01	0.3898F-01
5	0.2491F 01	0.38578-01
\$	0.25235 01	0+3556F=01
\$	0.25558 01	0.3914F-01
>	0+2587E 01	0.3942E-01
>	0.2620E 01	0.3970E-01
>	0.2652E 01	0.3997E-01
>	0.2654E 01	0.4023E-01
>	0.2716E 01	0.4049E-01
>	0.2748E 01	0.4075E-01

> EFFECTIVE MODIFIED OPTICAL DEPTH XE = 0.8699F-02.

> L-R FUNCTION OF XE = 0.8654E-02.

> ETA = 0.1163E 00.

>	MODIFIED OPTICAL	DEPTH	L-R FUNCTION	TRANSMITTANCE
Ś	0.1897F-03	w	0.1895F-03	0.9980F 00
5	0-39045-03		0.39005-03	0.99595 00
5	0.60195-03		0.60115-03	0.99365 00
Ĵ	0.89395-03		0.80085-03	0.99125 00
5	0.10565-09		0.10555-00	0.99132 00
1	0.19985-02		0.10045-02	0.0072 00
2	0+12982-02		0.15485-02	0.96032 00
2	0+15502-02		0.13462-02	0.96372 00
2	0.10122-02		0.19035-05	0.981UE 00
2	0.2083E-02		0.20792-02	0.97522 00
2	U-2363E-02		0.23581-02	0.97532 00
2	0.26521-02		0.2645E-02	0.9723E 00
>	0.2949E-02		0.2942E-02	0.9693E 00
>	0.3255E-02		0.3246E-02	0+9661E 00
>	0.3569E-02		0.3559E-02	0.9629E 00
>	0.3891E-02		0-3880E-02	0•9597E 00
>	0.4221E-02		0.4205E-02	0•9563E 00
>	0.4559E-02		0•4544E-02	0.9529E 00
>	0.4904E-02		0•4887E-02	0•9495E 00
>	0 • 5257E-02		0•5238E-02	0•9459E 00
>	0•5616E-02		0•5595E-02	0•9424E 00
>	0+5983E+02		0•5960E-02	0 •9387E 00
>	0+6357E-02		0.6331E-02	0.9350E 00
>	0.6739E-02		0.6710E-02	0.9313E 00
>	0.7130E-02		0.7098E-02	0.9275E 00
>	0.7530E-02		0•7495E-02	0.9236E 00
>	0.7939E-02		0.7900E-02	0•9196E 00
>	0.8357E-02		0+8315E-02	0.9156E 00
>	0.8783E-02		0.8737E-02	0+9115E 00
>	0.9218E-02		0.9167E-02	0.9073E 00
>	0•968 9 E-02		0•9634E-02	0.9025E 00
>	0.1022E-01		0.1016E-01	0.8978E 00
>	0+1081E-01		0.1074E-01	0.5923E 00
>	0.1145E-01		0•1137E-01	0+5563E 00
≥	0+1215E-01		0 • 1206E-01	0+8799E 00
>	0+1268E-01		0.1279E-01	0.5731E 00
>	0.1365E-01		0+1355E-01	0+8661E 00
>	0.1446E-01		0+1435E-01	0.8588E 00
>	0.1531E-01		0+1518E-01	0.8512E 00
>	0+1620E-01		0+1605E-01	0.8434E 00
>	0.1712E-01		0.1696E-01	0.8353E 00
>	0.1807E-01		0.1790E-01	0.8271E 00
>	0-1906E-01		0.1887E-01	0.5156E 00
>	0.2009E-01		0.1957E-01	0+8099E 00
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>	0.43942-01	0.4297E-01	0.6339E 00
>	0.4565E-01	0.4463E-01	0.6228E 00
>	0.4745E-01	0.4632E-01	0+6118E 00
>	0.49252-01	0+4803E-01	0.6007E 00
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>	0.5293E-01	0+5154E-01	0.5788E 00
>	0-5482E-01	0.5332E-01	0.5680E 00
>	0.5673E-01	0.5514E-01	0.5571E 00
>	0.5867E-01	0-5697E-01	0.5464E 00
•	0.6064E-01	0+5882E-01	0.5358E 00
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2	0.1200E 00	0.10125 00	0.07405 00
>	0.1318F 00	0.1026F 00	0.040EF 00
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Appendix D ILLUSTRATION OF METHOD FOR TEMPERATURE PROFILE DETERMINATION

A typical calculation for the extraction of a temperature profile from observed spectra using a band-model radiative-transfer expression proceeded as follows. From the radiance and absorptance spectra, such as figures B7 and B8 for this example, the apparent temperatures T^* were extracted and plotted as a function of absorptances, as in figure D1. The resultant curves of T^* vs. α were all quite similar (a fact which itself suggests the need for a priori information on the profile shape for reliable analysis) and at first glance simple in shape, approaching asymptotically a constant value for the optically thin extreme, and rapidly decreasing towards a value representing the boundary temperature in the optically dense extreme. However, the shape of the T^* vs. α curves show two salient features: a complex pattern of behavior, quite repeatable, at absorptances between 0.9 and 1.0, and an apparent "hysteresis" in the lowabsorptance data between values obtained for the short- and long-wavelength wings of the band. Both of these features are explicable. The first can be accounted for by the fact that apparent temperatures are not functions only of absorptance; at substantial optical depths, the variation of the Planck function and the temperature dependence of the band-model parameters with wavelength appreciably influence the values of the observed radiances, hence apparent temperatures.

The low-absorptance discrepancy, on the other hand, is attributable to an imperfection in the apparatus: the presence of a small amount of light scattered from the grating onto the exit slit of the monochromator. This scattered light appeared only when the continuous blackbody radiance passed through the sample cell during the absorption scans or the beam-balance scans for setting the emission scale. Since this scattered light became completely negligible at frequencies greater than 4000 cm⁻¹, the shorter wavelength data, (the lower sequence of points on the T^{*} vs. α plots) were therefore weighted more heavily in the fitting of the band-model calculations.

The deduction of the temperature profile was then a simple and straightforward matter. An initial temperature profile was assumed, based on the a priori knowledge of the profile shape. The simplest shape, linear with temperature and increasing along the line of sight from the monochromator, was selected for this illustration. A reasonable initial set of values could be obtained by inspection of the T^* vs. α plot: the initial minimum temperature could be based on the extrapolation to $\alpha = 1$, and an initial maximum temperature taken as the intercept at $\alpha = 0$. The former could be a very realistic estimate; the latter, however, is bound to be



FIGURE D1. FITTING OF BAND-MODEL CALCULATIONS TO OBSERVED VARIATION IN APPARENT TEMPERATURE

considerably lower than the actual maximum temperature, but provided a convenient starting point. Using the band-model expression given by equation (31) in the main text, values of T^* were calculated throughout the band and plotted against absorptance. The assumed temperature profile was then adjusted and the calculation repeated until an optimum fit with the observed data was obtained. In this example, a one-parameter fit was chosen for purposes of illustration; with the minimum temperature taken to be known, the three profiles could be specified by three maximum temperatures. These profiles, shown in figure D3, provided the three curves of calculated T^* vs. α shown in figure C1. (The actual graphical fitting was done on larger scale plots in which the band-model calculations also showed nonuniform variations in the $0.9 < \alpha < 1.0$ region; for purposes of this illustration only the mean curves are shown.) Clearly, the intermediate curve represents the best fit in figure C1; this profile also showed the best agreement with the observed temperatures, as shown in figure C2. For the purposes of this study, such fits were made by inspection; obviously, future analyses programmed for routine applications should include an appropriate mathematical fitting procedure.

For the fits involving adjustments of two or more parameters, many more calculations were required, but the basic approach was the same. The example above illustrated the deduction of a temperature profile in a sample of CO_2 . For the case of water vapor, the very same procedure was used. There was, however, an appreciable difference in the appearance of the T^{*} vs. α plots, namely, a great deal more scatter in the data. This was attributed to the fact that the H₂O line overlapping was not as great as for CO₂. Hence the spectra showed much more rotational line detail; this structure appeared also in the T^{*} vs. ν plots (cf. figure 7c), as the consequence of an imperfect register of the L_{ν} vs. ν and $\alpha(\nu)$ vs. ν data in the calculation of L^{*}_{ν} = L_{ν}/ $\alpha(\nu)$ and hence T^{*}. This scatter, however, did not introduce any particular difficulty in the judgment of the best fit.

For the case of the isolated line spectra of HF, an exactly analogous procedure was used. In this case, apparent temperatures were calculated using equation 30 and plotted against the generalized rotational quantum number. Again the assumed profiles were adjusted until a best fit was determined by inspection.



FIGURE D2. TEMPERATURE PROFILE ASSUMED FOR FITTING BAND-MODEL CALCU-LATIONS TO OBSERVED DATA
Appendix E SYMBOLS

d average line spacing

F = $(\gamma/\gamma_e)^{\eta}$ or $(\beta/\beta_e)^{\eta}$, function characterizing variation of line half-width with temperature and pressure

f = f(x), Ladenburg-Reiche function for line growth

g slit function of spectrometer

k spectral absorption coefficient $(cm^{-1}-atm^{-1})$

L integrated line radiance (W/cm^2-sr)

 $L_{,,}$ spectral radiance (W/cm²-sr-cm⁻¹)

 L_{ν}^{*} ratio of L_{ν} to $\alpha(\nu)$ (Planck function of T^{*})

m generalized rotational quantum number (-J for P-branch, J + 1 for R-branch transitions)

P pressure (atm)

S line strength $(cm^{-2}-atm^{-1})$

T temperature (°K)

 T^* apparent temperature (^OK) [inverse Planck function of $L_{\nu}/\alpha(\nu)$]

W equivalent width of spectral line (cm^{-1})

X optical depth (cm-atm)

x dimensionless optical depth

 α spectral absorptance

 $\beta = 2\pi \overline{\gamma}/d$, line overlap factor

 γ half-width of Lorentz spectral line (cm⁻¹)

 $\delta \nu$ spectral interval (cm⁻¹)

ε spectral emissivity

 ν frequency (cm⁻¹)

 ρ reflectance

au spectral transmittance

Subscripts

e effective value (mass-weight average along line of sight)

L value appropriate for entire path along line of sight

o reference value

p value for probability line strength distribution

0 line center

Superscripts

- ' variable of integration
- average over spectral interval δv
- * reference to Planck function
- η empirically determined parameter, $0 < \eta < 1$

REFERENCES

- 1. S. S. Penner, Quantitative Molecular Spectroscopy and Gas Emissivities, Addison-Wesley (1959).
- 2. R. W. Ladenburg et al. (eds.), Physical Measurements in Gas Dynamics and Combustion, Princeton University Press (1954).
- 3. R. H. Tourin, Spectroscopic Gas Temperature Measurement, Elsevier (1966).
- 4. Temperature, Its Measurement and Control in Science and Industry, Reinhold, Vol. I (1941); Vol. II (1954); Vol. III (1962).
- 5. F. S. Simmons, Radiances and Equivalent Widths of Lorentz Lines for Nonisothermal Paths, J. Quant. Spectros. Rad. Trans., 7, 111 (1967).
- 6. H. Y. Yamada, Total Radiances and Equivalent Widths of Doppler Lines for Nonisothermal Paths, J. Quant. Spectros. Rad. Trans., 7, 997 (1967).
- H. Y. Yamada, Total Radiances and Equivalent Widths of Isolated Lines with Combined Doppler and Collision Broadened Profiles, J. Quant. Spectros. Rad. Trans., 8, 1463 (1968).
- 8. F. S. Simmons and H. Y. Yamada, Relations for Molecular Radiative Transfer Based on a Random-Line Band Model, Rept. 4613-150-T, Willow Run Laboratories of the Institute of Science and Technology, The University of Michigan, Ann Arbor, February 1967.
- 9. F. S. Simmons, Application of Band Models to Inhomogeneous Gases, Specialist Conference on Molecular Radiation, NASA TMX 53711 (October 1967).
- 10. H. Babrov, Instrumental Effects in Infrared Gas Spectra and Spectroscopic Temperature Measurements, J. Opt. Soc. Am., 51, 171 (1961).
- 11. B. Krakow, H. J. Babrov, G. J. Maclay, and A. L. Shabott, Use of the Curtis-Godson Approximation in Calculations of Radiant Heating by Inhomogeneous Gases, NASA TMX 53411 (1966).
- 12. C. B. Ludwig et al., Study on Exhaust Plume Radiation Predictions, General Dynamics Corp., NASA CR-61233 (1968).
- 13. R. M. Huffaker and M. J. Dash, A General Program for the Calculation of Radiation from a Inhomogeneous, Nonisobaric, Nonisothermal Rocket Exhaust Plume, NASA TM-53622 (1967).
- 14. F. S. Simmons, Further Notes on Band Models for Nonisothermal Radiating Gases, Appl. Opt., 6, 1423 (1967).
- 15. G. N. Plass, Radiation from Nonisothermal Gases, Appl. Opt., 6, 1995 (1967).
- 16. A. Goldman, On Simple Approximations to the Equivalent Width of a Lorentz Line, J. Quant. Spectros. Rad. Trans., 8, 829 (1968).
- 17. D. M. Gates, R. F. Calfee, D. W. Hansen, and W. S. Benedict, Line Parameters and Computed Spectra for Water Vapor Bands at 2.7 μ , NBS Monograph 71 (1964).
- 18. J. R. Auman, Jr., The Infrared Opacity of Hot Water Vapor, Proceedings of a Conference on Molecular Radiation, NASA TMX 53711 (October 1967).

- 19. C. B. Ludwig and W. Malkmus, Band Model Representatives for High Temperature Water Vapor and Carbon Dioxide, Specialist Conference on Molecular Radiation, NASA TMX 53711 (October 1967).
- 20. J. A. L. Thomson, Radiation Model for Nonscattering Rocket Exhaust Gases, Specialist Conference on Molecular Radiation, NASA TMX 53711 (October 1967).
- 21. B. Krakow, Spectroscopic Temperature Profile Measurements in Inhomogeneous Hot Gases, Appl. Opt., Vol. 5, 201 (1966).
- 22. L. D. Kaplan, Inference of Atmospheric Structure from Remote Radiation Measurements, J. Opt. Soc. Am., Vol. 49, 1004 (1959).
- 23. D. T. Hilleary, D. Q. Wark, and D. G. James, An Experimental Determination of the Atmospheric Temperature Profile by Indirect Means, Nature (January 30, 1965).
- 24. R. A. McClatchey, Sensing of the Earth from Satellites, R. Zirkind (ed.), Polytechnic Press (1965).
- D. Q. Wark and H. E. Fleming, Indirect Measurements of Atmospheric Temperature Profiles from Satellites, Monthly Weather Rev., Vol. 94, 351 (1966).
- 26. M. T. Chahine, Determination of the Temperature Profile in an Atmosphere from Its Outgoing Radiation, California Institute of Technology, Jet Propulsion Laboratory, paper submitted to J. Opt. Soc. Am. (1969).
- S. Twomey, The Application of Numerical Filtering to the Solution of Integral Equations Encountered in Indirect Sensing Measurements, J. Franklin Inst., 279, 95 (1965).
- F. S. Simmons, An Analytic and Experimental Study of Molecular Radiative Transfer in Nonisothermal Gases, Tenth Symposium on Combustion, The Combustion Institute, Pittsburgh, Pa. (1965).
- 29. F. S. Simmons, A. G. DeBell, and Q. S. Anderson, A 2000^OC Slit-Aperture Blackbody Source, Rev. Sci. Instr., 32, 1265 (1961).
- 30. R. L. Jarry and W. Davis, Jr., The Vapor Pressure, Association, and Heat of Vaporization of Hydrogen Fluoride, J. Phys. Chem., 57, 600 (1953).
- 31. F. S. Simmons, C. B. Arnold, and D. H. Smith, Studies of Infrared Radiative Transfer in Hot Gases; I. Spectral Absorptance Measurements in the 2.7 μ H₂O Bands, Rept. 4613-91-T, Willow Run Laboratories of the Institute of Science and Technology, The University of Michigan, Ann Arbor, August 1965.
- 32. C. B. Ludwig et al., Study on Exhaust Plume Radiation Predictions, General Dynamics/Convair, Repts. DBE 66-017, -001a (1966).
- 33. R. E. Meredith and N. F. Kent, Line Strength Calculations for the 0 1, 0 2, 0 3, and 1 2 Vibration Rotation Bands of HF, Rept. 4613-125-T, Willow Run Laboratories of the Institute of Science and Technology, The University of Michigan, Ann Arbor, April 1966.
- 34. F. S. Simmons, Infrared Spectroscopic Study of Hydrogen-Fluorine Flames, AIAA J., 5, 778 (1967).
- 35. D. E. Burch, E. B. Singleton, and D. Williams, Absorption Line Broadening in the Infrared. Applied Optics 1, 359 (1962).

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