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*The Thermodynamic Properties of Solid Mercury at Temperature
Intervals of from 0 deg. K to Melting Point at Normal Pressure*

ТЕРМОДИНАМИЧЕСКИЕ СВОЙСТВА ТВЕРДОЙ РТУТИ В ИНТЕРВАЛЕ ТЕМПЕРАТУР
ОТ 0 К ДО ТОЧКИ ПЛАВЛЕНИЯ ПРИ НОРМАЛЬНОМ ДАВЛЕНИИ

Termodinamicheskiye Svoystva Tverdoy Rtuti v Intervale Temper-
atur ot 0 K do Tochki Plavleniya pri Normal'nom Davlenii

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The Thermodynamic Properties of Solid Mercury at Temperature Intervals of from 0 deg K to Melting point at Normal Pressure

In all branches of knowledge a great flow of information (or the lack of it) gives the work of sorting, identifying, and preparing standard reference data a special set.

The Department of Theoretical Foundations of Thermotechnics at the MEI* has prepared thermotechnical tables of mercury characteristics. The properties of saturated and burned out gas are considered up to 1000 degC and 800 bar, and an ζ -s diagram is constructed. (Ref. 1). The results of the experiment, which relate to viscosity and heat transfer are thoroughly analyzed. The possibility of the interaction potential are considered as well as the possibility of error in determining its parameter in relation to viscosity (Ref.2).

The reference table (Ref.3) presents a fairly complete bibliography about the properties of mercury, which were published before 1955.

Two modifications of solid mercury are known: α and β given various crystalline structures. α -mercury is a crystal and has a simple rhomboid nuclear mesh structure with the following parameters: $a=2.993\text{\AA}$, $\alpha=70\text{ deg } 45\text{ min}$ given 78 deg K Ref. 4. β -mercury has a tetragonal volumetrically centralized mesh structure ($a=3.995\text{\AA}$, $c=2.825\text{\AA}$, $a/c\approx\sqrt{2}$ given 77 deg K Ref. 5). In the lower temperature zone ($T<79\text{ deg K}$) the thermodynamically stable phase is the β mercury; however, this transformation occurs only when there is plastic deformation or high pressure.

When α -mercury cools below 79 deg K and atmospheric pressure is α - β the transformation does not occur under normal conditions Ref. 6. Beyond this the thermophysical properties of β -mercury remain unexplored and it is only possible to create a table of physical heat properties for α -mercury only.

Translator's Note: MEI = Moscow Institute of Energetics

Both modifications of mercury have super conductive powers, given low temperatures. The transitional temperature T_c of α and β mercury into a super conductive state is 4, 15, and 3, 95 deg K respectively Ref. 7.

In principle, the modern theory of solid matter allows for a thermal and caloric equation of the state of solid matter, if the potential energy of the interrelationships of atoms in the crystalline mesh structure is known. A series of simplifications are introduced with the equation: e.g., - a harmony of atomic oscillation is assumed, thus allowing the problem to be considered from the point of view of determining the spectrum of particles of harmonic vibration of the crystal.

Slutsky and Jelinek (Ref. 8) calculated this vibrative of α -mercury in such a fashion when they took into consideration the fixed intensity of mercury established by Gruneisen and Sckell (Ref. 9). In view of the fact that the fixed intensity was determined for only one temperature ($t = -190^\circ C$) and in the inadequate precision, the determined spectrum corresponds poorly with experiments regarding the thermal capacity of mercury.

Several complicated interrelated phenomena harshly stand out in the properties of solid substances - unharmonic oscillation of the mesh structure (thermal expansion), influence of distant neighbors with the possibility of non-additivity of interaction (mesh structure and emission of X-rays and neutron streams) an electron-phonon interaction (heat conductivity) formation of defects, etc. In spite of progress in the solid state physics, there are currently no equalizations which transmit data with experimental precision, even regarding equilibrium in wide intervals of parameters. That is why in considering the properties of solid matter the decisive meaning, as a rule, is only experimentally valid.

As a whole the problem of creating correlated tables of physical heat properties with the aid of theoretical equations should include the determination of certain constants, related to parameters of interrelated potentials; different types of experimental data must be utilized in the process (compression, caloric properties, intensity of radiation, heat conductivity, auto diffusions, etc.). However, at the present time this problem can only be solved for gaseous substances of moderate density.

Therefore the adjustment factor of these various experimental data, about thermodynamic properties of solid mercury was negligible in this work and was mainly qualitative in character.

In the process the International System of units was utilized. The atomic weight was 200.59 (1965 data) attributed to mercury. The thermodynamic scale is used in the table in regards to temperature. The difference between

the practical temperature scale and the thermodynamic one is included in the percentage of error.

The point of liquefaction of mercury in normal pressure is 38.87 deg C, according to the International Temperature Scale or 234.28 deg K allowing a magnitude of error, according to a thermodynamic scale of ± 0.005 deg.

Thermal Capacity of Solid Mercury(According to Given Experiments)

The measuring of thermal capacity is taken into consideration when calculating the caloric properties of solid substances that have been experimntally determined. The heat capacity of α -mercury has been adequately studied, but for β -mercury data are lacking. That is why it is only possible to provide tables for α -mercury.

In the reference material (10), the table indicates the properties of mercury that are based on the data provided by Busey (Ref. 3) and Giauque (Ref. 1). The appearance of more recent experimental data, especially in the sphere of the lowest temperature ranges, allows us to receive more detailed meanings of caloric function - entropy and enthalpy.

In Table 1, the basic knowledge of experiemnts determening the thermal capacity of solid mercury is presented. In all experiemnts the method of direct heating of the calorimeter exposed to changing temperatures, existing in the isothermal film in conditions close to adiabatic is used. This data embraces temperature intervals ranging from 0.1 deg K to the melting point; with their aid we can determine the caloric function of solid mercury.

The experimental data received from the works of Kammerling-Onnes and Holst (Ref. 12), Dewar (Ref. 13), Børschall (Ref. 14) and Koref (Ref. 15) about the average meaning of thermal capacity C_p in different intervals of temperature, is not exact and is, therefore, not examined in detail.

First, the experimental devices were analyzed and the error in calculating the thermal capacity of mercury was evaluated. According to our observations, the estimated degree of error of Pollitzer (Refs. 16 and 17) and Simon (Refs. 18 and 19) is not less than $\pm(2-2.5)\%$. The estimated error for Pickard and Simon (Ref. 20), Smith and Wolcott (Ref. 21) is $\pm 2\%$.

A thorough analysis of Busey and Giauque's method for measuring the thermal capacity of solid mercury (and other works by Giauque) has indicated that their evaluation of the degree of error is basically correct if the given temperature is higher than 35 deg K, then the degree

of error is close to $\pm 0.1\%$ if temperature is 20 deg K it reaches $\pm 1\%$ and if 15 deg K thus it approaches $\pm 3\%$.

When various data were compared they showed that the early works of the German authors (Ref.16,19) gave results that were in accord, within the limit of measured error; however, in the interval of temperature 25 - 80 deg K they exceeded the value calculated by Buge and Jacques by approximately 2,5% (Ref.11).

In the region between 4 and 10 deg K the data of Pecard and Simon (Ref.20) are excessive by comparison to the results of Smith and Wolcott and have an anomalous character, but in intervals from 10 to 20 deg K they are insufficient by comparison to those of Simon (Ref.19). Smiths' and Wolcott's data correspond with those of Simon in this temperature interval. On the other hand, the calculations of Smith and Wolcott correspond sufficiently with those of Van der Hoeven and P. Keesom (Ref.23) when the temperature is lower than 4,2 deg K (in the region beyond mercury's heat capacity).

The results of Phillips' and his co-workers (Ref.24) basically correspond with those of Van der Hoeven and Keesom. The data of Phillips are presented in graphic form and are not taken into consideration in our processing.

In this regard, the more accurate and more agreeable data are taken to be those of Simon, Smith and Wolcott, Van der Hoeven and P. Keesom, and Busey and Giauque. Preference is given to Busey and Giauque in the area between 20 deg K to the melting point of mercury because of greater exactness, even though these data don't correspond with the others (Ref.16-18) of $T = 25-80$ deg K .

It is important to indicate that the analysis of this experimental data, by the authors of the experiments or by those who created the tables, was not able to reveal experimental errors close to the numerical value of the sensitivity of the apparatus, and only repeated measuring could verify a high degree of accuracy. That is why it is imperative to conduct additional measuring experiments of mercury's heat capacity in the interval between 25-80 deg K within the limit of error $< 0.1\%$.

In analyzing data regarding heat capacity of solid substances the character of heat activity near the melting point is important.

According to special experiments with mercury by Kostriukov and Strelkov (Ref.25) it has been demonstrated that great pre-melting effects, that are expressed in increase of heat capacity (C_p) up to tens and hundreds of percents, are not necessarily present. The results in (Ref.11) show that even a small amount of additives varies heat capacity sharply if the temperature is 3-4 degrees below the melting point. A similar effect can be observed if

temperature is not even throughout a given substance.

Carpenter and Oakley also measured heat capacity of mercury near the melting point. The mercury was thoroughly purified beforehand. The dispersion of points in relation to a curve medium lay within the limit 1%. On the basis of the curves from the authors of the work (Ref.22) concluded there is an anomaly of heat capacity of solid mercury near the melting point, where it increases to a degree not greater than the dispersion of experimental data.

The points do not disperse systematically near the melting point and, therefore, such a conclusion by the authors is difficult to explain. Apparently, a correct manipulation of Carpenter's and Stoodley's data would give us a smooth curve without twists which would approximate a straight line, even to the melting point.

The values of mercury heat capacity found by Carpenter and Stoodley are 1% lower in the average to those of Busey and Giauque (Ref.11) and are not processed by us.

It should be noted that the sources of systematic error in measuring heat capacity with low temperature, may be due to gas absorption, the appearance of thermal pressure in the substance and in resistance within the thermometer. If heat capacity is insignificant and temperature is low the smallest vibration limits increased heating of the specimen. That is why it is important to perform additional experiments that will agree with previous ones.

Let us note, that a more detailed analysis of experimental settings, tables of resulting data, etc. is presented by the authors in tables (Ref.26).

Calculation of caloric functions of solid mercury

In order to calculate entropy, enthalpy, isobaric and isothermal potential; and to create a heat-capacity table, it is necessary to choose a function that describes best the experimental data regarding the heat capacity of solid mercury.

Usually in describing the isochoric heat capacity of solid mercury Debay's formula is used:

$$C_v = 9Nk \left(\frac{T}{\theta} \right)^3 \int_0^{\frac{\theta T}{T}} \frac{x^3 e^{-x}}{e^x - 1} dx, \quad (1)$$

(1) where θ is the characteristic temperature.

However, C_v calculated according to equation (1) cannot be greater than $3R$ - this does not correspond to our data. That is why we must correct elements relating to disharmony, formation of holes (gaps), and the term that considers the difference between C_v and the value of C_p determined in our experiments.

$$C_p - C_v = \frac{\alpha^2 VT}{\kappa_T}, \quad (2)$$

$$\alpha = \frac{1}{V} \left(\frac{\partial V}{\partial T} \right)_p \text{ и } \kappa_T = - \frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_T.$$

(2) All this complicates the equation that is useful in approximating our data.

In order to describe the dependency of heat capacity on temperature, we can utilize the equation based on a more definite dynamic theory of crystalline mesh structure

$$C_v = 3Nk \int_0^{\infty} E \left(\frac{h\nu}{kT} \right) \rho(\nu) d\nu, \quad (3)$$

where

$$E(x) = \frac{x^2 e^x}{(e^x - 1)^2}$$

Einstein's formation for harmonic oscillators and

$$\rho(\nu) =$$

is the function of mesh oscillation depending on frequency. The function $\rho(\nu)$ for mercury was calculated by Slutsky and Jelinek (Ref.8); however, the heat capacity C_v , calculated with the aid of equation (3) poorly coincides with experimental dependency $C_v(T)$ of mercury, even with low temperatures (up to 50 deg K).

In principle (Ref.27-29) it is possible to discover function $\rho(\nu)$ by referring to experimental data regarding heat capacity with the aid of integral transformative functions (3). In this way we can find an analytic dependence $C_v(T)$ which, however, will not be free of limitations existing in equation (1).

With all this in mind we decided to approximate the experimental data regarding isobaric heat capacity of simple analytical dependency in terms of multiple algebraic terms, which allow us to get simple correlations for calculating caloric function

$$\left. \begin{aligned} I - I_0 &= \int_0^T C_p dT \\ S - S_0 &= \int_0^T \frac{C_p}{T} dT \\ \Phi &= I - TS \end{aligned} \right\} \quad (4)$$

where I -enthalpy; S -entropy and Φ -the isobaric-isothermal potential.

In so far as it was difficult to approximate C_p by one multiple term, in the entire temperature interval 0 deg K to melting point, we broke up the interval into several parts; for each of these we selected a multiple term by the method of minimum squares, which described the experimental data with derration not exceeding the experimental degree of error. All calculations were made with the aid of an M-20 computer.

In the multiple-term selection process the areas overlapped, with the exception of joint with T_0 , where there is a jump in heat capacity. Experimental points were included in the calculation with weight $W=V_0^2$, where σ is the absolute limit of error assigned experimental value. We also took into consideration relative errors δC_p , which are the results of data described above. We selected polynomials of different degrees, beginning with the smallest. We increased the ratio until the quantity of atomic numbers, last in transforming the matriax system of normal equations did not exceed the quantity of atomic figures of mechanical numbers.

We chose polynomials of the needed degree and based our considerations on the following:

- 1) the sum of squares of deviation of experimental points from the approximating curve must be close to $n-m$ (n is the number of experimental points; m is the quantity of unknown parameters, in this case the quantity of unknown coefficients of polynomials).
- 2) the absolute measure of deviation must not exceed the limit of error of experimental points.
- 3) the calculated errors of coefficients must be at least one order of magnitude less than the value of the coefficients.

After a series of efforts experimental dats, C_p , were approximated to the curve, which consisted of three areas, each of which was represented by its own multiple term. At the joints the coincidence of heat capacity value was guaranteed up to five known digits. The products of joints

were disturbed, first according to the final differential C_p (table 6). The degree of error of caloric function stipulated by the inaccuracy of the jointed areas is less than their common degree of error by one to two orders of magnitude.

In the transition of α -mercury to a condition of superconductivity and back we observed a jump in heat capacity ΔC about 0,019 J/(mole · deg) (Ref.23) in magnitude. The value of the transitional temperature T_0 , in various sources, oscillated from 4,153 (Ref.7) to 4,167 deg K (Ref.30). We took the average value of $T_0 = (4.16 \pm 0.01)$ deg K.

Here are the approximating multiple terms

$$C_p(T) = \sum_{i=1}^m a_i T^i. \quad (5)$$

Coefficients a_i are presented in table 2.

The caloric functions are calculated by formula (4) containing corrections leading the function to standard pressure $p_0 = 760 \text{ mm Hg}$.

$$\left. \begin{aligned} I - I_0^0 &\approx I - I_0 + V(p_0 - p_s)(1 - T_2) - V_0(p_0 - p_s) \\ S^0 - S_0^0 &\approx S - S_0 - V_2(p_0 - p_s) \end{aligned} \right\} \quad (6)$$

The corrections do not exceed the degree of error of calculated functions.

The crystalline formation of the α -mercury mesh structure is not stable in relation to β -mercury, where $T < 79$ deg K but it is stable in relation to small deflections from a state of equilibrium - the α -mercury condition can be realized in a regulated structure by one method. With such a system, given absolute zero, we can accept $S_{0,\alpha} = S_{0,\beta} = 0$ (Ref.31).

In Fig. 1 we show the durations of the experimental value of mercury's heat capacity from the calculated ones; these durations do not exceed calculated ones, for the most part. We do not show on our graphs the data of Pichard and Simon (Ref.20), whose systematic deviations reach up to 30%, and the experimental points of Pollitzer (Ref.16,17) and Simon (Ref.18), whose deviations reach 6-7%, when temperature ranges from 30-70 deg K.

The degree of error of enthalpy and entropy are related to relative error of heat capacity C_p ; which is approximately 3% when $T < 15$ deg K: $\pm 1\%$ when $T = 15-35$ deg K and $\pm 0.1\%$ when $T > 35$ deg K.

Errors of integration in interval 0-15 deg K are $\delta(S-S_0) = \delta(I-I_0) \approx 3\%$, in interval 15-35 deg K $\sim 1\%$, and in interval 35 - melting point $\sim 0.1\%$. The calculated errors indicate the limit in so far as it is assumed that all experimental points C_p are displaced systematically to one side relative to real values.

The absolute limits of error thus calculated, determining entropy ΔS and enthalpy $\Delta(I^0-I_0^0)$, are presented in table 3.

In this way the limiting relative degree of error of determining entropy with melting point $\sim 0.5\%$, and consequently the degree of error of entropy $\sim 0.1\%$ calculated by Busey and Giauque is decreased.

According to our calculations, S^0 (melting point) = 59,349 J/(mole · deg), which is 0,134 J(mole · deg) less than the value achieved by Busey and Giauque (Ref.11).

According to (Ref.11) the entropy of mercury is 76.11 J/(mole · deg) at 298.15 deg K while according to Douglas, Ball, and Giueiys (Ref.32) it is $S_{298.15}^0 = 75.81$ J/(mole · deg) for the pressure of condensed gases.

Our calculation $S_{298.15}^0 = (75.98 \pm 0.3)$ J/(mole · deg) lies between the given results and agrees with them, within the limit of possible errors.

The values of errors $\Delta\phi$ in table 3, calculated according to equation, $\Delta\phi = \Delta I - T\Delta s$, do not define the limit.

The caloric characteristics β -mercury are difficult to determine when data regarding heat-capacity of C_p is missing.

From Swenson's experiments determining the parameters of transition α - β , we only know that the generation should be ~ 122 J/mole where $p=1$ atm with the formation of β -phase from α -mercury. We took $S_{0,\alpha} = S_{0,\beta} = 0$. This allowed us to determine the effectual values of characteristic temperatures (in the Debye approximation) of α and β -mercury in the interval 0-79 deg K corresponding to $\bar{\theta}_\alpha = 97$ deg K and $\bar{\theta}_\beta = 118$ deg K. However, the function $\theta_\beta(T)$ and the energy of the crystalline structure of β -mercury with 0 deg K, $I_{0,\beta}$ remain unknown.

The Thermal Properties of Solid Mercury

The Contractability of Solid Mercury

$$\kappa_T = - \frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_T$$

Swenson obtained more complete data about contractibility of solid mercury in 1958 when he experimented with the substance under high pressure. The experiment was conducted, utilizing the method of a mobile plunger (pecton) developed

by Bridgman (Ref.34) and adapted for low temperature measurement.

By extrapolating isotherms $V(p)$, Swenson obtained data about isometric contractibility

$$\alpha_T = -\frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_T$$

in conditions of atmospheric pressure (Fig.2). Swenson evaluated the degree of error of determination K_T as equal to 5%. However, we can consider the degree of error to be close to $\pm 10\%$ because of the dispersion of data and possible system error. Swenson's experimental data relate primarily to temperatures between 78-200 deg K. At 4.2 deg K we have another experimental point. This is why Swenson's function $K_T(T)$ needs experimental verification.

Note that Gruneisen and Sckell (Ref.9) recommended earlier that the value of the contractile coefficient is $\alpha_T = 3.16 \cdot 10^{-11} \text{ m}^2/\text{n}$ when $T=82 \text{ deg K}$ and in the given reference material there was an extrapolation of data regarding liquid mercury.

In sorting the analytical dependence $K_T(T)$, when $p=1 \text{ atm}$, the following are considered.

- 1) when $T \rightarrow 0 \frac{dK_T}{dT} \rightarrow 0$;
- 2) a correspondence of derivatives must be realized resulting from conditions of phase equilibrium

$$\frac{d^2 p}{dT^2} \Delta V = \frac{\Delta C_p}{T} - 2 \left(\frac{\partial \Delta V}{\partial T} \right)_p \frac{dp}{dT} - \left(\frac{\partial \Delta V}{\partial p} \right)_T \left(\frac{dp}{dT} \right)^2, \quad (7)$$

here, ΔV and ΔC_p is an adhesion of specific volume and heat capacity during fusion.

It follows from the works of Busey and Giauque (Ref. 11), Kostryukov and Strelkov (Ref. 25) that the calculations $\Delta C_p = C_p^J - C_p^{TB} = 0$ are within the limit of error.

In extrapolating the data of Bigg (Ref. 35), at the melting point of mercury, we get $V^J = 14.65064 + 0.0020 \text{ cm}^3/\text{mole}$.

The density of solid mercury has not been satisfactorily investigated. We can discover the specific density of solid mercury at the melting point on the basis of Bridgman's data (Ref. 36), when the volume of mercury is modified during fusion: $\Delta V = 0.5083 \text{ cm}^3/\text{mole}$ with a degree of error of $\pm 0.0015 \text{ cm}^3/\text{mole}$. Then the specific density of solid mercury at the melting point will equal $14.1423 \pm 0.0035 \text{ cm}^3/\text{mole}$.

The preliminary development of the test data concerning the thermal expansion of solid mercury (Refs. 37 and 38) gives us $\alpha_{2,4,3} = (18.1 \pm 0.02) \cdot 10^{-5} \text{ deg}^{-1}$.

On the basis of an extrapolation of Pena's data (Ref. 40) concerning the contractibility of liquid mercury at the melting point, we find: $K_T^J = (3.88 \pm 0.05) \cdot 10^{-11} \text{ m}^2/\text{N}$.

The equation for mercury's melting curve was provided by Babb in the form given by Simon's equation

$$\frac{p-p_0}{a} = \left(\frac{T}{T_0}\right)^c - 1, \quad (8)$$

where T_0 is the melting temperature with p_0 for atmospheric pressure; $a=38215 \pm 817$ bar, $c=1.177 \pm 0.023$ when $p < 10^4$ bar.

By utilizing the listed data with the help of Eq. 8, we can find $K_{2,3,4}^{TB} = (3.66 \pm 0.4) \cdot 10^{-11} \text{ m}^2/\text{N}$.

We prefer this value of contractibility even though it makes many assumptions recommended by Swenson (Ref 33) who found $K_{2,3,4}^{TB} = (3.82 \pm 0.02) \cdot 10^{-11} \text{ m}^2/\text{N}$ in extrapolating his data to the melting point - this is close to $K_{2,3,4}^J$ and is excessive.

However, Swenson's data gives us some idea about the general progress of $K_T(T)$ and, therefore, its processing together with the above point $K_{2,3,4}^{TB}$ gives us an acceptable dependability within a limit of error of $\pm 10\%$

$$K_T = 2,807 \cdot 10^{-11} + 1,556 \cdot 10^{-16} T^2, \text{ m}^2/\text{N}. \quad (9)$$

The resulting dependency is shown in Fig. 2 by means of a solid line.

Swenson also measured the contractibility of β -mercury when the temperature varies from 4 to 78 deg K, which turned out to be 20% lower than the contractibility of α -mercury (Ref. 33).

The Thermal Coefficient of Expansion

$$\alpha = 1/V(dV/dT)_p.$$

Experimental data about the actual coefficient of expansion was used in creating the tables regarding the value of thermal mercury expansion.

In 1931, Carpenter and Oakley, and Hull in 1965 performed similar calculations. Carpenter and Oakley (Ref. 37) measured the volumetric coefficient of solid mercury expansion in temperature intervals between 183 - 234 deg K with the aid of a glass dilatometer which consisted of a retort and capillary. The retort (flask) was filled mostly by mercury with the remaining space filled with alcohol. The change in the level of alcohol in the capillary in accordance with a rise in the temperature made it possible to measure the coefficient of mercury expansion. The authors concluded that the error in measurement was $\delta\alpha < 3\%$.

The precision of the experimental method and the additional research for evaluating the degree of error systematically verifies the work of Carpenter and Oakley; the degree of error of the data apparently does not exceed $\pm 3\%$.

Let us note that the anisotropic quality of mercury monocrystal elicits various expansions of mercury according to different axis. When mercury cools, crystallization can occur with a preeminent orientation, which is the chief source of systematic errors relating to the measurement of mercury's coefficient of expansion. Further on we shall consider α to be the "thermodynamic" coefficient of thermic expansion for polycrystals without preeminent orientation.

In this connection, the work of Hill (Ref. 38) is interesting with regards to measuring the coefficients of linear expansion along the main axis of monocrystalline mercury when $T=113 - 160$ deg K.

Experiments were performed with monocrystalline mercury, grown in rod shapes, with various orientations of the central axis of the crystal being relative to the end axis. We found the coefficient of linear expansion along the main axis $\alpha_{||}$ and in the perpendicular direction α_{\perp} according to the dependency of the coefficient of linear expansion on the angle of orientation at a given temperature. The volumetric coefficient of expansion was computed by the equation

$$\alpha = \alpha_{||} + 2\alpha_{\perp}$$

Hill's error of measurement of α was not evaluated; the dispersion of experimental points of the leveling curve does not exceed 1%. The available data only allow for dependency $\alpha(T)$ in intervals from 110 deg K to the melting point.

$$\alpha = (13,631 - 0,047636T + 2,5973 \cdot 10^{-4}T^2) \cdot 10^{-5} \text{ град}^{-1}. \quad (10)$$

Gruneisen's rule is used in extrapolating α from 110 deg K to absolute zero

$$\Gamma = \frac{\alpha V}{\kappa_T C_p} = \text{idem}, \quad (11)$$

which is approximately executed for most solid substances.

In order to compute the value of Gruneisen's constant we must utilize the dependence C_p , κ_T , and α and also the equation for the mole volume of mercury recommended by Swenson (Ref. 33)

$$V = (13,7873 + 7,6473 \cdot 10^{-3}T + 1,2498 \cdot 10^{-5}T^2 - 2,9021 \cdot 10^{-8}T^3) \cdot 10^{-3} \text{ м}^3/\text{кмоль при } T = 0 + 234^\circ\text{K}. \quad (12)$$

We obtain $\Gamma = 2.22$ with 110 deg K, 2.15 at 130, 2.13 with 150 and 170, 2.17 with 190, 2.24 with 210, and 2.06 at 230.

From these values we can see that Gruneisen's rule for solid mercury is executed with sufficient accuracy. The greatest deviations occur near the melting temperature and are probably due to the formation of "gaps" unused bundles in the crystalline mesh

structure. The value of Γ at 110 and 170 deg K differs by about 4%. With temperatures below 110 deg K, the deviation from the rule for $\Gamma = \text{idem}$ for mercury, apparently does not exceed 10 - 15%. In further calculations we utilize the value $\Gamma = \Gamma_{T=110} \approx 2.22$.

We calculated the thermal coefficient of mercury expansion with temperatures below 110 deg K with the aid of the relationship resulting from equation (11)

$$\alpha = 2 \cdot \alpha_T \cdot C_p / V^{-1} [1 + (1 + 4\alpha_T C_p T^2 V^{-1})^{1/2}]^{-1}. \quad (13)$$

In this area, the error of determination for α reaches 15 - 10%. The general passage of $\alpha(T)$ is shown in Fig. 3.

The following indicates the comparison between the true calculated value of α and the calculation for the average magnitude of α . Grummach's values (Ref. 42) are too low: $\bar{\alpha}(195 \div 234 \text{ deg K}) = 12.3 \cdot 10^{-5} \text{ deg}^{-1}$. So are these by about 10%: $(78 \div 194 \text{ deg K}) = 12 \cdot 10^{-5} \text{ deg}^{-1}$ (Ref. 43). The magnitude $\alpha = 12.8 \cdot 10^{-5}$, according to Gruneisen and Sckell (Ref. 9) coincides with the value $\alpha(80 \div 190 \text{ deg K}) = 13.1 \cdot 10^{-5} \text{ deg}^{-1}$ from Table 5, within the limit of error.

The electron heat capacity is lower than the crystal lattice in the superconductive condition of mercury ($T < 4.16 \text{ deg K}$); we don't have to take into account the influence of the electrons on the coefficient of expansion. When $T < 4.16 \text{ deg K}$ in the normal state (in the magnetic field), the electron heat capacity becomes greater than the lattice, and the influence of electron gas on the coefficient of expansion can predominate.

Specific Volume of Solid Mercury

Swenson's data regarding specific volumes of mercury under atmospheric pressure is adequately described by equation (12). However, we are not able to determine the true magnitude of the specimen with various temperatures and pressures by using Swenson's methodology; we only measured the changes in the lengths of the sample. That is why Swenson used the data of other efforts on the capacity of capacity of data points to interpret his own calculations of volumetric changes of mercury.

Swenson took the results of Denitz's calculations executed together with Gruneisen and Sckell as the main data points with an 82 deg K temperature: $V(82) = 13.865 \text{ cm}^3/\text{mole}$.

Swenson's resulting dependency $V(T)$ agreed satisfactorily with the small amounts of other data about the direct changes in density of solid mercury.

In determining analogous dependencies $V(T)$ for solid mercury, Grosse (Ref. 44) used primarily the basic data regarding density by means of X-ray analysis of mercury crystal and also the data about thermal expansion of solid mercury (Refs. 37 and 38). As data points, he accepted Barrett's data regarding the density of mercury (Ref. 4) that were obtained by X-ray analyses with temperatures of 5 and 78 deg K. Barrett's data corresponded poorly with those of Denitz's measurements, and Grosse's results measure substantially

higher than those of direct calculation of mercury's density. Barrett himself acknowledges that this points to a systematic deviation of the data subjected to X-ray analyses. That is only why we may consider Swenson's data (Ref. 33) regarding molar volume of mercury to be more reliable

Conducting a correspondence of Swenson's data on the molar volume of mercury with data concerning thermal expansion and with the value $V(T_{\text{boiling point}})$, it is possible to substantially specify the dependence $V(T)$ by means of the equation

$$V(T) = V(T_{\text{m}}) \exp \left(\int_{T_{\text{m}}}^T \alpha dT \right). \quad (14)$$

Utilizing the values we obtained for $\alpha(T)$ and the molar volume of mercury at boiling point, and also $V(T_{\text{boiling point}}) = 14.1423 \pm 0.0035 \text{ cm}^3/\text{mole}$, according to Equation (14) we computed the dependence $V(T)$ of solid mercury at all temperature intervals. The integral is taken graphically. We determine the error V_0 :

$$\Delta V(T) \approx V_{\text{m}} \Delta \left(\int_{T_{\text{m}}}^T \alpha dT \right) + \Delta V_{\text{m}}(T_{\text{m}}). \quad (15)$$

In as much as $\int_{T_{\text{m}}}^0 \alpha dT \approx -0.025 \pm 0.0025$ (the error $\alpha(T)$ is discussed above) we find that the limit of error of the calculated volume when 0 deg K $\Delta V_0 \approx \pm 0.04 \text{ cm}^3/\text{mole}$ or $\delta V_0 \approx \pm 0.3\%$. The experimental data 0 V calculated directly are similarly dispersed. The final molar volume of mercury is $V_0 = 13.786 \pm 0.04 \text{ cm}^3/\text{mole}$ at 0 deg K .

By these calculations we can determine heat capacity with a constant volume C_v , according to Equation (2)

The relative error

$$\delta C_v \approx \delta C_p + \frac{C_p - C_v}{C_p} \delta(C_p - C_v), \quad (16)$$

where

$$\delta(C_p - C_v) \approx 2\delta\alpha + \delta V + \delta x_T.$$

Errors in obtaining C_p, α, K, V were indicated earlier. From Table 4 we can see how errors δC_p and $\delta(C_p - C_v)$ influence the degree of error δC_v given various temperatures.

Table 4 shows the calculated limit of error; the probable error would be smaller.

The adiabatic curve of contractibility of solid mercury is determined by

$$K_s = x_T \frac{C_v}{C_p}. \quad (17)$$

Here we show the obtained values for the characteristic properties of solid mercury of α -phase when $p=1$ atm with the indicated accuracy of the determination:

Temperature of melting, T_{BP}(234.28 \pm 0.005) deg K
Molar volume, $V^B(T_{BP})$(14.1423 \pm 0.0035) cc/mole
Coefficient of thermal expansion, $\alpha(T_{BP})$(16.728 \pm 0.5 \cdot 10⁻⁵ deg⁻¹
Coefficient of isothermal contractibility

$$K_S = -1/V(\partial V/\partial p)_S \text{ when } T_{BP} \dots\dots (3.336 \pm 0.4) \cdot 10^{-11} \text{ m}^2/\text{N}$$

Thermal capacity, $C_p(T_{BP})$(28.484 \pm 0.05) J/(mole \cdot deg)
Thermal capacity, $C_v(T_{BP})$(25.95 \pm 0.5) J/(mole \cdot deg)
Entropy, $S_{234.28}^0$ (59.353 \pm 0.3) J/(mole \cdot deg)
Enthalpy, $|I_{234.28}^0 - I_{0.1atm}^0|$(5245.1 \pm 10) J/mole
Temperature of the transition of T_c from
a normal state to superconductive..(4.16 \pm 0.01) deg K
Change in thermal capacity ΔC_p when T_{BP} ..(0.19 \pm 0.02) \cdot 10⁻³ J/(mole \cdot deg)
Molar volume when 0 deg K.....(13.786 \pm 0.04) cc/mole
Gruneisen's constant, $\Gamma = \alpha V/K_T C_v$2.22 \pm 0.4
Parameters for a rhombohedral lattice
at 78 deg K..... $a=2.993 \text{ \AA}$, $\alpha=70$ deg 45 min
Temperature of the α - β transition.....(79 \pm 2) deg K

It is expedient to compare the data on the properties of mercury to the results like efforts. The values of heat capacity and enthalpy the the MEI determined are compared with the computed results of Busey, Giauque (Ref. 11) and those in the reference manual (Ref. 10).

The values of enthalpy coincide within the limit of estimated error. In structuring Busey's and Giauque's dependency $C_p(T)$ in areas of low temperature, Pickards and Simon's data (Ref. 20) which are noticeably incorrect, were used, that is why the discrepancy in the values for C_p when the temp is 15 deg K is understandable.

The coefficient for thermal expansion of mercury in interval of 0 to 234 deg K in presented in Grosse's work (Ref. 44) and in the NBE monograph (Ref. 45); a comparison is presented in Table 6.

The NBE data conform adequately in the entire temperature interval. There is considerable disagreement with Grosse's data in the area of extrapolation ($T=0$ to 100 deg K).

In so far as various data were used as points of departure, our computed molar volumes differed considerably from Grosse's results.

Grosse did not analyze the experimental works critically. On the one hand he probably overestimated the accuracy of the X-ray analysis of solid mercury. On the other hand, in computing the changes of mercury's volume during the liquifaction, Grosse simply averaged the experimental data; however, the work of Bridgman is more reliable. That is why Grosse's data points on the volume of solid mercury at the melting point and at $T=0$ deg K

are doubtful. Table 7 compares the molar volume of mercury that we got from our work and from Grosse's work.

In Table 8 we present the values of heat capacity C_p , the caloric properties of solid mercury determined at 1 deg K spacing and their initial differences. Table 9 shows the value of thermal properties of solid mercury V, α, K_T, K_S and heat capacity C_v mainly distributed by a 10 deg K pace.

Let us make some comment regarding the completion of Tables 8 and 9. We did not level out the values according to differences, but rounded them out by the usual rules of the nine-scale table determined for M-20. Although the table of caloric functions were joined only according to C_p , the initial differences in heat capacity C_p change regularly only at the joints except in the area of 189 - 193 deg K. There is a noticeable jump of the curved line $\alpha(T)$ (Table 5) in the transition to the extrapolation area according to Gruneisen's rule ($T < 110$ deg K)

The recurvature points of heat capacity C_p and C_v are noticeably displaced. Strangely, the curve of thermal capacity C_p and $C_v(T)$ (Tables 8 and 9) diminishes near the melting point. In this area the behaviour of the C_p and C_v line, the aharmonic oscillations of the mesh structure and the effect of vacancy formation is determined. At the melting point, the value of aharmonic insertion into the thermal capacity of mercury is 0.5-1%; they correspond exactly to the mark (sign) in computing different works (Refs. 46 and 47). The effect of gap formations should increase the curvature. It seems natural that, taken as a whole, the curvature near the melting point should increase, at least for the isobaric thermal capacity. We can achieve this by changing the value C_p from Table 8. within the limit of error of Busey's and Gianque's experiments $\sim 0.1\%$.

The analysis performed indicates that it is necessary to explore anew the properties of solid mercury with greater precision.

We need precise thermal capacity data for α -phase where $T=10-30$ deg K, to explore thermal capacity of β -phase to determine the coefficient of volumetric expansion of mercury when $T < 111$ deg K, to investigate the velocity of sound in solid mercury, to establish critical experiments to determine the contractibility at $T \rightarrow 0$, and to determine exactly (with a degree of error less than $\pm 0.2\%$) the change of volume of mercury when melting. For the sake of expediency, we must also investigate the dispersion of neutrons in solid mercury to determine the spectrum of mesh-structure oscillations.

The authors continue their work toward completing tables of mercury's properties and will gratefully accept any comments concerning this problem

Table 1. Data on basic experimental efforts regarding thermal capacity of solid mercury by the caloric method.

Author	Year	Laboratory	Temp Interval, deg K	No. of Points	Relative error, ΔC_p , %
Pollitser (16)	1911	Physico-Chem. Institute, U of Berlin, Ger.	61-233	17	1.0
Pollitser (17)	1913	ditto	31-168	5	1.0
Simon (18)	1922	ditto	19-232	15	0.5-1.5
Simon (19)	1923	ditto	10-13.4	7	-
Carpenter, Studli (22)	1930	U. of Southampton, G.B.	197-234	21	
Pichard, Simon (20)	1948	Clarendon Lab., Oxford	3.5-95		0.5-1.5
Busey, Giaque, (11)	1953	U. of Calif. Berkely	15-234	65	3 at 15 deg K 1 at 20 deg K 0.1 at T 35>deg K
Smith, Wolcott, (21)	1956	Clarendon Lab., Oxford	1.3-21		-
Van der Hoeven (23)	1964	Purdue Univ, USA	0.35-4.27	54	3.0
Phillips, Lambert, Gardner, (24)	1964	U. of Calif. Berkely	0.1-1.0		3.0

Table 2. Coefficients a_i of polynomials describing the dependency

$$C_p(T) = \sum a_i T^i$$

i	$\frac{H}{T}$ При $0 < T < 4.16$	$\frac{C_p}{T}$ При $4.16 < T < 60.598$	$\frac{C_p}{T}$ При $60.598 < T < 234.28$
-1	0	0	-776.081718
0	0	-1.97926752	47.3651931
1	0	0.750133661	-0.403512788
2	0	-0.118245093 · 10 ⁻¹	0.439216578 · 10 ⁻²
3	0.275692589 · 10 ⁻²	0.486966166 · 10 ⁻³	-0.258008613 · 10 ⁻⁴
4	0.202139136 · 10 ⁻¹	-0.158416718 · 10 ⁻⁴	0.780989701 · 10 ⁻⁷
5	-0.578127214 · 10 ⁻¹	0.222021301 · 10 ⁻⁶	-0.929902517 · 10 ⁻¹⁰
6	0.749918233 · 10 ⁻¹	-0.110524244 · 10 ⁻⁸	0
7	-0.482081354 · 10 ⁻¹	0	0
8	0.173531546 · 10 ⁻¹	0	0
9	-0.359854892 · 10 ⁻²	0	0
10	0.403751347 · 10 ⁻³	0	0
11	-0.190657737 · 10 ⁻⁴	0	0

Table 3. Errors in determining the caloric function of solid mercury

T, °K	$\epsilon C_p, \%$	S°	ΔS°	$I^\circ - I_0^\circ$	$\Delta(I^\circ - I_0^\circ)$	$(I^\circ - I_0^\circ)$	$\Delta(I^\circ - I_0^\circ)$
		Дж/моль·град		Дж/моль			
15	3	5.07	0.15	48.6	1.5	27.4	0.8
35	1	15.11	0.25	298.5	4.0	230.5	4.8
234,28	0.1	59.35	0.29	5245.1	8.9	8660.1	59.1

Table 4.

$$\delta C_p = f(\delta C_p, \delta a, \delta x_T, \delta T)$$

T, °K	$\epsilon C_p, \%$	$\delta(C_p - C_v), \%$	$\frac{C_p - C_v}{C_p}$	$\frac{C_p - C_v}{C_p} \delta(C_p - C_v), \%$	$\epsilon C_v, \%$
4-15	3	50	0.001	0.05	3
15-35	1	50	0.006	0.3	1.3
35-110	0.1	50	0.024	1.2	1.3
110-170	0.1	16	0.017	0.8	0.9
170-234	0.1	20	0.090	1.8	1.9

Table 5. A comparison of the caloric function of solid mercury

$$C_p, \text{ кДж/(кмоль·град)} (I - I_0^\circ), \text{ кДж/(кмоль)}$$

T, °K	C_p в кДж/(кмоль·град), по данным [11]			C_p в кДж/(кмоль), по данным [10]		
	[11]	[11]	[10]	[11]	[11]	[10]
15	7.61	7.34	7.63	48.6	45.1	—
100	24.26	24.25	24.3	1704	1702	1705
234,28	28.48	24.48	25.5	5245	5240	5230

Table 6. A comparison of the coefficients of thermal expansion

α

T, °K	$\alpha \cdot 10^{-5}, \text{град}^{-1}$, по данным		
	МЭИ МЭИ	Гроссе [11]	НБС НБС [12]
0	0	0	0
10	2,13	0,82	2,1
20	4,65	4,00	4,5
50	9,04	8,70	8,7
100	11,22	11,05	11,1
150	12,33	12,28	12,33
200	14,49	14,00	14,34
234,28	16,73	17,10	17,16

Table 7. A comparison of the molar volume of mercury

$V, \text{cm}^3/\text{mole}$

T, °K	V, см ³ /моль, по данным	
	Гроссе [11]	МЭИ МЭИ
0	13,8479	13,786
78	13,9314	13,859
100	13,9312	13,892
150	14,0096	13,974
200	14,0930	14,067
234,28	14,1725	14,142

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Таблица 7

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МЭИ
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13,892
13,974
14,067
14,142

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Таблица 8

Table 8. The caloric properties of solid mercury (α -phase) at atmospheric pressure

T, °K	t, °C	c_p kJ/(kmole·deg)	kJ/(kmole·deg)			
			$\rho - \rho_0$ kJ/kmole	$\rho - \rho_0$ кДж/(кмоль·град)	$-\rho - \rho_0$ kJ/kmole	$-\rho - \rho_0$ kJ/kmole
0	-273,15	0	0	0	0	0
1	-272,15	0,006	0,002	0,002	0,000	0,000
2	-271,15	0,099	0,010	0,025	0,010	0,010
3	-270,15	0,397	0,270	0,114	0,072	0,072
4	-269,15	0,898	0,903	0,293	0,268	0,268
4,16 ^(s)	-268,99	0,988	1,054	0,330	0,318	0,318
4,16 ⁽ⁿ⁾	-268,99	0,968	1,054	0,330	0,318	0,318
5	-268,15	1,529	2,101	0,558	0,686	0,686
6	-267,15	2,184	3,962	0,895	1,407	1,407
7	-266,15	2,827	6,468	1,280	2,491	2,491
8	-265,15	3,459	9,612	1,699	3,978	3,978
9	-264,15	4,080	13,383	2,142	5,897	5,897
10	-263,15	4,692	17,770	2,601	8,268	8,268
11	-262,15	5,295	22,761	3,079	11,108	11,108
12	-261,15	5,888	28,356	3,565	14,430	14,430
13	-260,15	6,472	34,538	4,060	18,242	18,242
14	-259,15	7,048	41,298	4,561	22,552	22,552
15	-258,15	7,614	48,630	5,067	27,365	27,365
16	-257,15	8,171	56,524	5,576	32,686	32,686
17	-256,15	8,718	64,969	6,087	38,517	38,517
18	-255,15	9,256	73,957	6,601	44,861	44,861
19	-254,15	9,783	83,478	7,116	51,719	51,719
20	-253,15	10,300	93,521	7,631	59,092	59,092
21	-252,15	10,806	104,07	8,146	66,980	66,980
22	-251,15	11,300	115,13	8,660	75,382	75,382
23	-250,15	11,782	126,67	9,173	84,295	84,295
24	-249,15	12,252	138,69	9,684	93,727	93,727

s-superconductive state; n-normal state

Продолжение

$T, ^\circ K$	$t, ^\circ C$	C_p^0 кДж/(кмоль·град)	$P - P_0^0$ кДж/кмоль	S^0 кДж/(кмоль·град)	$-(P - P_0^0) / T_0^0$ кДж/кмоль
25	-248,15	12,709	151,17	10,193	103,66
26	-247,15	13,153	161,10	10,700	114,11
27	-246,15	13,581	177,47	11,205	125,06
28	-245,15	14,002	191,26	11,707	136,52
29	-244,15	14,405	205,47	12,205	148,48
30	-243,15	14,797	220,07	12,700	160,93
31	-242,15	15,170	235,05	13,191	173,88
32	-241,15	15,532	250,41	13,679	187,31
33	-240,15	15,879	266,11	14,162	201,23
34	-239,15	16,212	282,16	14,641	215,63
35	-238,15	16,532	298,54	15,116	230,51
36	-237,15	16,838	315,22	15,586	245,86
37	-236,15	17,130	332,21	16,051	261,68
38	-235,15	17,409	349,43	16,512	277,96
39	-234,15	17,676	367,02	16,967	294,70
40	-233,15	17,920	384,82	17,418	311,90
41	-232,15	18,173	402,88	17,864	329,54
42	-231,15	18,405	421,17	18,305	347,62
43	-230,15	18,626	439,68	18,740	366,15
44	-229,15	18,837	458,41	19,171	385,10
45	-228,15	19,039	477,35	19,596	404,48
46	-227,15	19,232	496,49	20,017	424,29
47	-226,15	19,418	515,82	20,433	444,52
48	-225,15	19,596	535,32	20,843	465,16
49	-224,15	19,769	555,00	21,249	486,20
50	-223,15	19,935	574,86	21,650	507,65
51	-222,15	20,097	594,87	22,046	529,50
52	-221,15	20,253	615,05	22,438	551,74
53	-220,15	20,406	635,38	22,825	574,37
54	-219,15	20,555	655,86	23,208	597,39

$T, ^\circ K$	$t, ^\circ C$
55	-218,15
56	-217,15
57	-216,15
58	-215,15
59	-214,15
60	-213,15
61	-212,15
62	-211,15
63	-210,15
64	-209,15
65	-208,15
66	-207,15
67	-206,15
68	-205,15
69	-204,15
70	-203,15
71	-202,15
72	-201,15
73	-200,15
74	-199,15
75	-198,15
76	-197,15
77	-196,15
78	-195,15
79	-194,15
80	-193,15
81	-192,15
82	-191,15
83	-190,15
84	-189,15

Продолжение

Т. °К	t. °С	C_p кДж/(кмоль·град)	$\rho - \rho_0$ кДж/кмоль	S кДж/(кмоль·град)	$-(\rho - \rho_0)$ кДж/кмоль
55	-218,15	20,702 147	676,49 2063	23,587 379	620,79 2310
56	-217,15	20,816 144	697,26 2077	23,961 374	644,57 2378
57	-216,15	20,987 141	718,18 2092	24,331 370	668,71 2444
58	-215,15	21,125 138	739,24 2106	24,698 367	693,23 2452
59	-214,15	21,261 136	760,43 2119	25,060 362	718,11 2488
60	-213,15	21,394 133	781,76 2133	25,418 358	743,35 2524
61	-212,15	21,519 125	803,21 2145	25,773 355	768,94 2559
62	-211,15	21,635 116	824,79 2158	26,124 351	794,89 2595
63	-210,15	21,746 111	846,48 2169	26,471 347	821,19 2630
64	-209,15	21,853 107	868,28 2180	26,814 343	847,83 2664
65	-208,15	21,956 103	890,19 2191	27,154 340	874,82 2699
66	-207,15	22,056 100	912,19 2200	27,490 336	902,14 2732
67	-206,15	22,153 97	934,30 2211	27,822 332	929,79 2765
68	-205,15	22,246 93	956,50 2220	28,151 329	957,78 2799
69	-204,15	22,337 91	978,79 2229	28,477 326	986,10 2832
70	-203,15	22,425 88	1001,2 224	28,799 322	1014,7 286
71	-202,15	22,510 85	1023,6 224	29,117 318	1043,7 290
72	-201,15	22,593 83	1046,2 226	29,433 316	1073,0 293
73	-200,15	22,673 80	1068,8 226	29,745 312	1102,6 296
74	-199,15	22,752 79	1091,5 227	30,054 309	1132,5 299
75	-198,15	22,828 76	1114,3 228	30,360 306	1162,7 302
76	-197,15	22,902 74	1137,2 229	30,663 303	1193,2 305
77	-196,15	22,974 72	1160,1 229	30,963 300	1224,0 308
78	-195,15	23,044 70	1183,1 230	31,259 296	1255,1 311
79	-194,15	23,112 68	1206,2 231	31,553 294	1286,5 314
80	-193,15	23,179 67	1229,4 232	31,844 291	1318,2 317
81	-192,15	24,245 66	1252,6 232	32,132 288	1350,2 320
82	-191,15	23,309 64	1275,9 233	32,418 286	1382,5 323
83	-190,15	23,371 62	1299,2 233	32,701 283	1415,0 325
84	-189,15	23,432 61	1322,6 234	32,981 280	1447,9 329

Продолжение

Т. °К	t. °С	C_p кДж/(кмоль·град)	$\rho - \rho_0$ кДж/кмоль	S^0 кДж/(кмоль·град)	$-(\rho^0 - \rho_0)$ кДж/кмоль
85	-188,15	23,491	1316,1	33,259	1481,0
86	-187,15	23,550	1369,6	33,534	1514,4
87	-186,15	23,607	1393,2	33,807	1548,1
88	-185,15	23,663	1416,8	34,077	1582,0
89	-184,15	23,718	1440,5	34,345	1616,2
90	-183,15	23,771	1464,2	34,610	1650,7
91	-182,15	23,824	1488,0	34,873	1685,4
92	-181,15	23,876	1511,9	35,134	1720,4
93	-180,15	23,926	1535,8	35,392	1755,7
94	-179,15	23,976	1559,7	35,648	1791,2
95	-178,15	24,025	1583,7	35,902	1827,0
96	-177,15	24,073	1607,8	36,154	1863,0
97	-176,15	24,120	1631,9	36,404	1899,3
98	-175,15	24,167	1656,0	36,651	1935,8
99	-174,15	24,212	1680,2	36,897	1972,6
100	-173,15	24,257	1704,4	37,141	2009,6
101	-172,15	24,301	1728,7	37,382	2046,9
102	-171,15	24,345	1753,0	37,622	2084,4
103	-170,15	24,387	1777,4	37,860	2122,1
104	-169,15	24,429	1801,8	38,095	2160,1
105	-168,15	24,471	1826,3	38,329	2198,3
106	-167,15	24,512	1850,8	38,562	2236,8
107	-166,15	24,552	1875,3	38,792	2275,4
108	-165,15	24,591	1899,9	39,020	2314,3
109	-164,15	24,630	1924,5	39,247	2353,5
110	-163,15	24,668	1949,1	39,472	2392,8
111	-162,15	24,706	1973,8	39,696	2432,4
112	-161,15	24,744	1998,5	39,918	2472,2
113	-160,15	24,781	2023,3	40,138	2512,3
114	-159,15	24,817	2048,1	40,356	2552,5

Т. °К	t. °С
115	-155,15
116	-157,15
117	-159,15
118	-155,15
119	-151,15
120	-147,15
121	-143,15
122	-139,15
123	-135,15
124	-131,15
125	-127,15
126	-123,15
127	-119,15
128	-115,15
129	-111,15
130	-107,15
131	-103,15
132	-99,15
133	-95,15
134	-91,15
135	-87,15
136	-83,15
137	-79,15
138	-75,15
139	-71,15
140	-67,15
141	-63,15
142	-59,15
143	-55,15
144	-51,15

Продолжение

$\frac{t - t_0}{\rho}$
 км/моль
 331
 334
 337
 339
 342
 345
 347
 350
 353
 355
 358
 360
 363
 365
 368
 370
 373
 375
 377
 380
 382
 385
 386
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 396
 398
 401
 402
 405

$T, ^\circ K$	$t, ^\circ C$	C_p кДж/(кмоль·град)	$\rho - \rho_0$ кДж/кмоль	S^0 кДж/(кмоль·град)	$-(\Phi^0 - I_0^0)$ кДж/кмоль
115	-158,15	24,853 36	2072,9 248	40,573 217	2593,0 405
116	-157,15	24,888 35	2097,8 249	40,788 215	2633,7 407
117	-156,15	24,923 35	2122,7 249	41,002 214	2674,5 408
118	-155,15	24,957 31	2147,6 249	41,214 212	2715,6 411
119	-154,15	24,991 31	2172,6 250	41,425 211	2757,0 414
120	-153,15	25,025 34	2197,6 250	41,631 209	2798,5 415
121	-152,15	25,058 33	2222,6 250	41,842 208	2840,2 417
122	-151,15	25,091 33	2247,7 251	42,049 207	2882,1 419
123	-150,15	25,123 32	2272,8 251	42,254 205	2924,3 422
124	-149,15	25,155 32	2298,0 252	42,457 203	2966,7 424
125	-148,15	25,187 32	2323,2 252	42,659 202	3009,3 426
126	-147,15	25,218 31	2348,4 252	42,860 201	3052,0 427
127	-146,15	25,249 31	2373,6 252	43,060 200	3095,0 430
128	-145,15	25,280 31	2398,9 253	43,258 198	3095,0 431
129	-144,15	25,310 30	2424,2 253	43,455 197	3138,1 431
130	-143,15	25,310 30	2449,5 253	43,455 195	3181,5 435
131	-142,15	25,370 30	2474,8 253	43,650 194	3225,0 438
132	-141,15	25,400 30	2499,2 254	43,844 194	3268,8 439
133	-140,15	25,429 29	2525,6 254	44,038 194	3312,7 442
134	-139,15	25,458 29	2551,0 254	44,229 191	3356,9 443
135	-138,15	25,487 29	2576,5 254	44,420 191	3401,2 445
136	-137,15	25,515 28	2602,0 255	44,609 189	3445,7 447
137	-136,15	25,543 28	2627,5 255	44,797 188	3490,4 449
138	-135,15	25,571 28	2653,1 256	44,984 187	3535,3 451
139	-134,15	25,599 28	2678,7 256	45,170 186	3580,4 452
140	-133,15	25,627 27	2704,3 256	45,355 185	3625,6 455
141	-132,15	25,654 27	2729,9 256	45,539 184	3671,1 456
142	-131,15	25,681 27	2755,6 257	45,721 182	3716,7 458
143	-130,15	25,708 27	2781,3 257	45,903 182	3762,5 460
144	-129,15	25,735 27	2807,0 257	46,083 180	3803,5 462
				46,262 179	3854,7

Продолжение

Т, °К	t, °С	C_p^0 кДж/(кмоль·град)	$R-T_0^0$ кДж/кмоль	S^0 кДж/(кмоль·град)	$-(\psi^0 - T_0^0)$ кДж/кмоль
145	-123,15	25,762	2832,8	46,410	3901,0
146	-127,15	25,789	2858,6	46,617	3917,6
147	-126,15	25,815	2881,4	46,791	3991,3
148	-125,15	25,841	2910,2	46,969	4011,2
149	-124,15	25,867	2936,0	47,143	4088,2
150	-123,15	25,893	2951,9	47,316	4135,4
151	-122,15	25,920	2987,8	47,488	4182,8
152	-121,15	25,945	3013,7	47,659	4230,4
153	-120,15	25,971	3039,7	47,829	4278,2
154	-119,15	25,997	3065,7	47,999	4326,1
155	-118,15	26,023	3091,7	48,167	4374,2
156	-117,15	26,049	3117,7	48,334	4422,4
157	-116,15	26,075	3143,8	48,501	4470,8
158	-115,15	26,100	3169,9	48,666	4519,4
159	-114,15	26,126	3196,0	48,831	4568,2
160	-113,15	26,152	3222,1	48,995	4617,1
161	-112,15	26,178	3248,3	49,158	4666,2
162	-111,15	26,203	3274,5	49,320	4715,4
163	-110,15	26,229	3300,7	49,482	4764,8
164	-109,15	26,255	3326,9	49,642	4814,4
165	-108,15	26,281	3353,2	49,802	4864,1
166	-107,15	26,307	3379,5	49,961	4914,0
167	-106,15	26,333	3405,8	50,119	4964,0
168	-105,15	26,359	3432,2	50,276	5014,2
169	-104,15	26,385	3458,6	50,433	5064,6
170	-103,15	26,412	3485,0	50,589	5115,1
171	-102,15	26,438	3511,4	50,744	5165,7
172	-101,15	26,464	3537,8	50,898	5216,5
173	-100,15	26,491	3564,3	51,051	5267,5
174	-99,15	26,518	3590,8	51,204	5318,6

Т, °К	t, °С
175	-98,15
176	-97,15
177	-96,15
178	-95,15
179	-94,15
180	-93,15
181	-92,15
182	-91,15
183	-90,15
184	-89,15
185	-88,15
186	-87,15
187	-86,15
188	-85,15
189	-84,15
190	-83,15
191	-82,15
192	-81,15
193	-80,15
194	-79,15
195	-78,15
196	-77,15
197	-76,15
198	-75,15
199	-74,15
200	-73,15
201	-72,15
202	-71,15
203	-70,15
204	-69,15

Продолжение

$-(t^* - t_0^0)$
кДж/кмоль

$T, ^\circ K$	$t, ^\circ C$	C_p^* кДж/(кмоль·град)	$r - t_0^0$ кДж/кмоль	S^* кДж/(кмоль·град)	$-(t^* - t_0^0)$ кДж/кмоль
3991.0	463				
3997.6	466				
3994.3	467				
4011.2	469				
4088.2	470				
4135.4	472				
4182.8	474				
4230.4	476				
4278.2	478				
4326.1	479				
4374.2	481				
4422.4	482				
4470.8	484				
4519.4	486				
4568.2	488				
4617.1	489				
4666.2	491				
4715.4	492				
4764.8	494				
4814.4	496				
4864.1	497				
4914.0	499				
4964.0	500				
5014.2	502				
5064.6	504				
5115.1	505				
5165.7	506				
5216.5	508				
5267.5	510				
5318.6	511				
175	-98.15	26,511	3617.3	51,356	5369.9
176	-97.15	26,571	3613.9	51,507	5421.4
177	-96.15	26,699	3670.5	51,658	5473.0
178	-95.15	26,626	3697.1	51,808	5524.7
179	-94.15	26,653	3723.7	51,957	5576.6
180	-93.15	26,681	3750.4	52,106	5628.6
181	-92.15	26,709	3777.1	52,254	5680.8
182	-91.15	26,737	3803.8	52,401	5733.1
183	-90.15	26,765	3830.6	52,547	5785.6
184	-89.15	26,793	3857.4	52,693	5838.2
185	-88.15	26,821	3884.2	52,838	5891.0
186	-87.15	26,850	3911.0	52,983	5943.9
187	-86.15	26,879	3937.9	53,127	5996.9
188	-85.15	26,908	3964.8	53,271	6050.1
189	-84.15	26,937	3991.7	53,414	6103.4
190	-83.15	26,967	4018.7	53,556	6156.9
191	-82.15	26,997	4045.7	53,698	6210.5
192	-81.15	27,027	4072.7	53,839	6264.3
193	-80.15	27,057	4099.7	53,979	6318.2
194	-79.15	27,088	4126.8	54,119	6372.3
195	-78.15	27,119	4153.9	54,258	6426.5
196	-77.15	27,150	4181.0	54,397	6480.8
197	-76.15	27,181	4208.2	54,535	6535.3
198	-75.15	27,212	4235.4	54,673	6589.9
199	-74.15	27,244	4262.6	54,810	6644.6
200	-73.15	27,276	4289.8	54,947	6699.5
201	-72.15	27,308	4317.1	55,083	6754.5
202	-71.15	27,340	4344.4	55,219	6809.7
203	-70.15	27,373	4371.8	55,354	6865.0
204	-69.15	27,406	4399.2	55,488	6920.4

6*

83

Продолжение

$T, ^\circ K$	$t, ^\circ C$	C_p кДж/(кмоль·град)	$\rho - \rho_0$ кДж/кмоль	S_p кДж/(кмоль·град)	$-(\rho - \rho_0)$ кДж/кмоль
205	-68,15	27,439 33	4126,6 274	55,622 134	6975,9 555
206	-67,15	27,472 33	4151,1 275	55,756 134	7031,6 557
207	-66,15	27,506 34	4181,6 275	55,889 133	7087,4 558
208	-65,15	27,540 34	4509,1 275	56,022 133	7143,4 560
209	-64,15	27,574 34	4536,7 276	56,154 132	7199,5 561
210	-63,15	27,608 34	4564,3 276	56,286 132	7255,7 562
211	-62,15	27,642 34	4591,9 276	56,417 131	7312,1 564
212	-61,15	27,677 35	4619,5 276	56,548 131	7368,6 565
213	-60,15	27,712 35	4647,2 277	56,678 130	7425,2 566
214	-59,15	27,747 35	4674,9 277	56,808 130	7481,9 567
215	-58,15	27,782 35	4702,7 278	56,937 129	7538,8 569
216	-57,15	27,817 35	4730,5 278	57,066 129	7595,8 570
217	-56,15	27,853 36	4758,3 278	57,195 129	7652,9 571
218	-55,15	27,889 36	4786,2 279	57,323 128	7710,2 573
219	-54,15	27,925 36	4814,1 279	57,451 128	7767,6 574
220	-53,15	27,961 36	4842,0 279	57,578 127	7825,1 575
221	-52,15	27,997 36	4870,0 280	57,705 127	7882,7 576
222	-51,15	28,033 36	4898,0 280	57,831 126	7940,5 578
223	-50,15	28,070 37	4926,1 281	57,957 126	7998,4 579
224	-49,15	28,106 36	4954,2 281	58,083 126	8056,4 580
225	-48,15	28,143 37	4982,3 281	58,208 125	8114,5 581
226	-47,15	28,179 36	5010,5 282	58,333 125	8172,8 583
227	-46,15	28,216 37	5038,7 282	58,458 125	8231,2 584
228	-45,14	28,253 37	5066,9 282	58,582 124	8289,7 585
229	-44,15	28,290 37	5095,2 283	58,706 124	8348,3 586
230	-43,15	28,327 37	5123,5 283	58,829 123	8407,1 588
231	-42,15	28,364 37	5151,8 283	58,952 123	8466,0 589
232	-41,15	28,401 37	5180,2 284	59,074 122	8525,0 590
233	-40,15	28,437 36	5208,6 284	59,196 122	8584,1 591
234	-39,15	28,474 37	5237,1 285	59,318 122	8643,4 593
234,28	-38,87	28,484 10	5245,1 80	59,353 35	8660,1 167

табл. 9) уменьшаются
линий C_p и C_p опре-
шетки и эффектом
оценки вклада

Термодинамические свойства
от 0°K до точки плавления

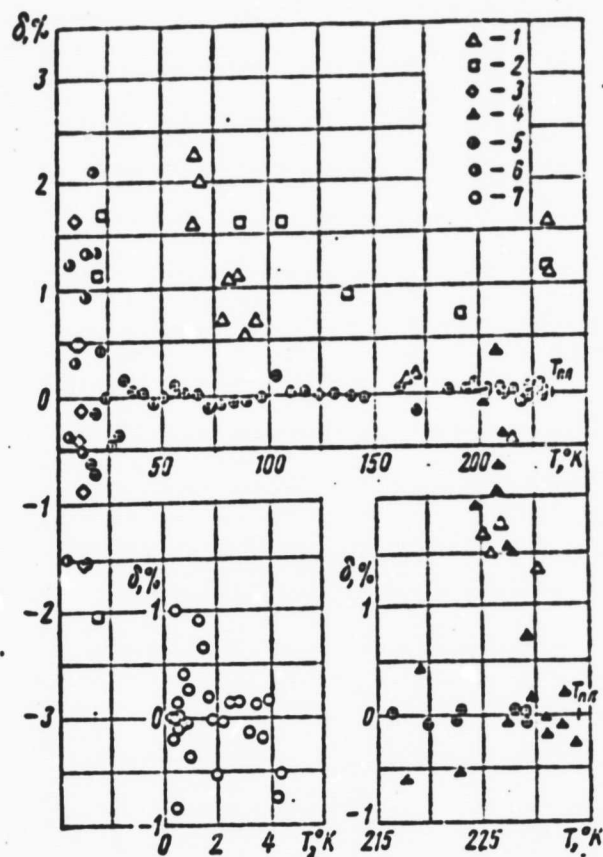
$T, ^\circ K$	$\rho - \rho_0$ кДж/кмоль	S_p кДж/(кмоль·град)
0	13,786	2,87
5	13,786	2,87
10	13,787	2,87
20	13,791	2,87
30	13,799	2,87
40	13,809	2,87
50	13,821	2,87
60	13,831	2,87
70	13,848	2,87
80	13,862	2,87
90	13,877	2,87
100	13,892	2,87
110	13,908	2,87
120	13,924	2,87
130	13,940	2,87
140	13,957	2,87
150	13,974	2,87
160	13,992	2,87
170	14,010	2,87
180	14,028	2,87
190	14,047	2,87
200	14,067	2,87
210	14,088	2,87
220	14,110	2,87
230	14,132	2,87
234,28	14,142	2,87

$\pm 0,2\%$) измене-
довать рассеяние
колебаний решетки
Авторы про-
с благодарности

И. Вукалов
1000°С и давлением

Table 9. Thermodynamic properties of solid mercury (alpha-phase) from 0 deg K to melting point at atmospheric pressure

T, °K	$V \cdot 10^3$ м ³ /моль	$\alpha_T \cdot 10^4$ м ² /м	$\alpha \cdot 10^{-5}$, град ⁻¹	C_p ккал/(кмоль · град)	$\alpha_s \cdot 10^4$ м ² /м
0	13.786	2.807	0	0	2.807
5	13.786	2.807	0.692	1.529	2.807
10	13.787	2.809	2.123	4.690	2.807
20	13.791	2.813	4.660	10.279	2.803
30	13.799	2.821	6.693	14.729	2.808
40	13.809	2.832	8.115	17.802	2.812
50	13.821	2.846	9.035	19.737	2.818
60	13.831	2.863	9.718	21.120	2.826
70	13.848	2.883	10.219	22.074	2.838
80	13.862	2.907	10.606	22.750	2.853
90	13.877	2.933	10.931	23.263	2.871
100	13.892	2.963	11.220	23.667	2.891
110	13.908	2.995	11.486	23.995	2.915
120	13.924	3.031	11.656	24.276	2.910
130	13.940	3.070	11.829	24.514	2.970
140	13.957	3.112	12.054	24.714	3.001
150	13.974	3.157	12.330	24.883	3.034
160	13.992	3.205	12.659	25.032	3.068
170	14.010	3.257	13.040	25.167	3.103
180	14.028	3.311	13.473	25.296	3.139
190	14.047	3.369	13.957	25.423	3.175
200	14.067	3.429	14.494	25.552	3.212
210	14.088	3.493	15.082	25.681	3.249
220	14.110	3.560	15.723	25.806	3.286
230	14.132	3.630	16.415	25.917	3.322
234.28	14.142	3.661	16.728	25.956	3.336



$$\delta = \frac{C_p^{on} - C_p^{pacu}}{C_p^{pacu}} \cdot 100\%$$

Fig. 1. Deviation of the experimental data obtained by various authors from an approximated dependence $C_p(T)$: 1-Pollitser's data (16 and 17), 2-Simon 1922 (18), 3-Simon, 1923 (19), 4-Carpenter and Studli (22), 5-Busey and Guaugua (11), 6-Smith and Wolcott (21), 7 Van der Hoven and P. Keezom (23)

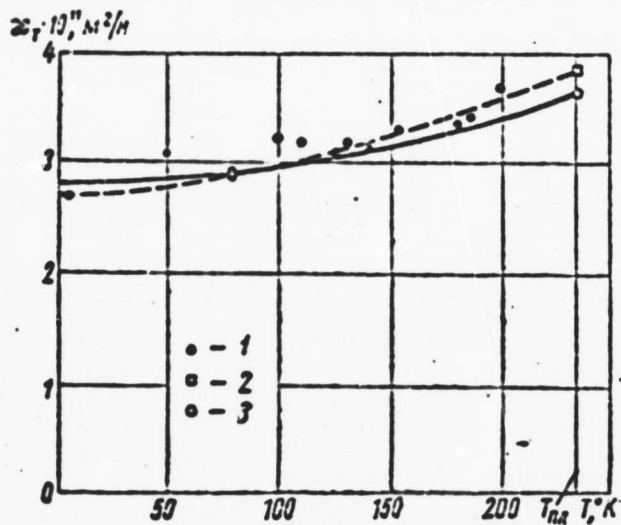


Fig. 2. Dependence of isothermiccontractibility K_T on temperature at normal pressure $p=1$ atm: 1-Swenson's test data (33), 2-the value K_T^J at T_{BP} obtained by extrapolation of Pena's test data (40), the value K_T^{TB} at T_{BP} computed by equation 7, dashed - dependence described by Swenson's data.

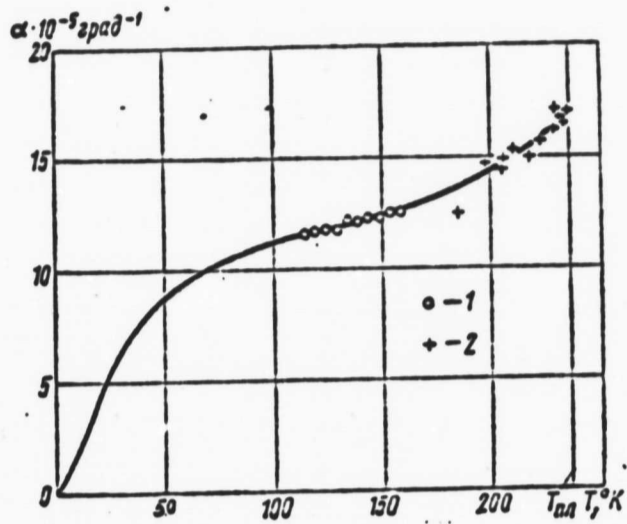
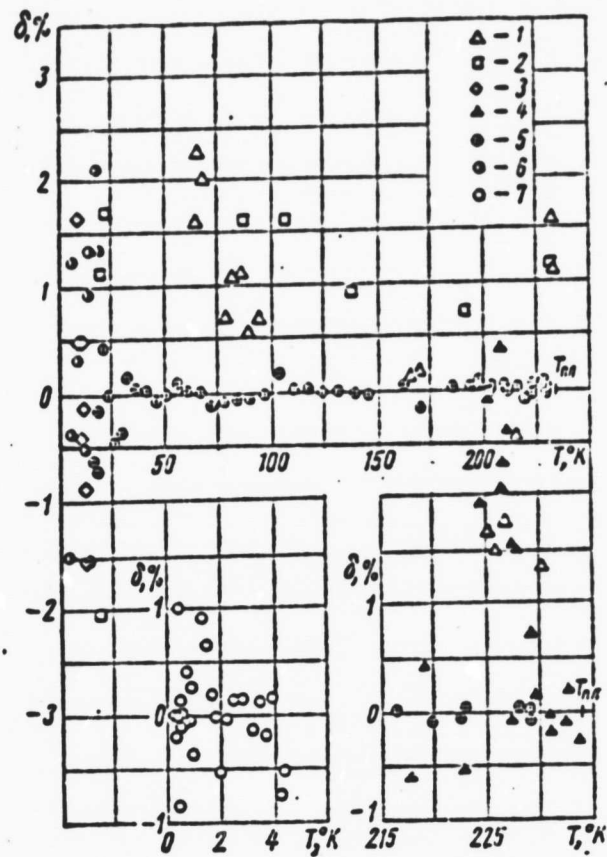


Fig. 3. The dependence of the coefficient for thermal expansion α on temperature at normal pressure $p=1$ atm. 1-Carpenter and Oukli's test data, 2- Hill's (38)



$$\delta = \frac{C_p^{on} - C_p^{pacu}}{C_p^{pacu}} \cdot 100\%$$

Fig. 1. Deviation of the experimental data obtained by various authors from an approximated dependence $C_p(T)$: 1-Pollitser's data (16 and 17), 2-Simon 1922 (18), 3-Simon, 1923 (19), 4-Carpenter and Studli (22), 5-Busey and Guaugua (11), 6-Smith and Wolcott (21), 7 Van der Hoven and P. Keezom (23)

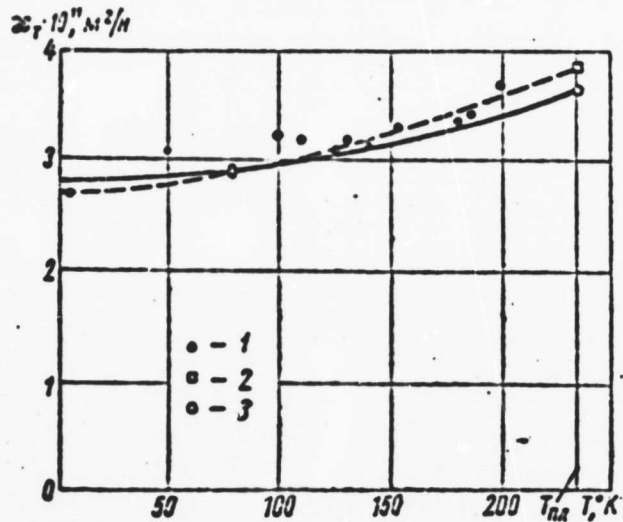


Fig. 2. Dependence of isothermiccontractibility K_T on temperature at normal pressure $p=1$ atm: 1-Swenson's test data (33), 2-the value K_T^J at T_{BP} obtained by extrapolation of Pena's test data (40), the value K_T^{TB} at T_{BP} computed by equation 7, dashed - dependence described by Swenson's data.

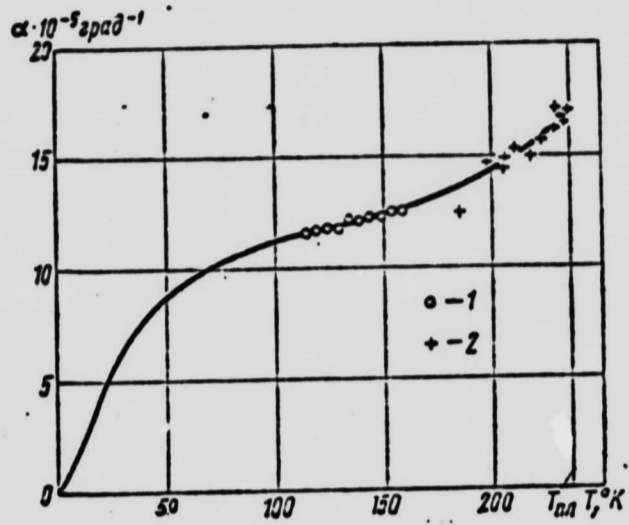


Fig. 3. The dependence of the coefficient for thermal expansion α on temperature at normal pressure $p=1$ atm. 1-Carpenter and Oukli's test data, 2- Hill's (38)

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