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**SAMMSOR II - A FINITE ELEMENT
PROGRAM TO DETERMINE STIFFNESS AND
MASS MATRICES OF SHELLS OF REVOLUTION**

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ABSTRACT

A user's guide for the SAMMSOR II (Stiffness And Mass Matrices for Shells Of Revolution) computer code is presented in this report. The finite element method of analysis is employed using a curved shell of revolution element to determine structural stiffness and mass matrices. Documentation of the analysis technique is included along with user hints and a discussion of the program limitations. Instructions for preparing the input data is included along with procedures for modifying the code. This program has the capability of internally generating the geometry of a number of important classes of shell configurations (such as shallow caps, cylinders, cones, hemispheres, etc.). Several example problems are presented to aid the user.

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SOR - Shell Of Revolution

Computer Programs

A family of compatible computer codes for the analysis of the shell of revolution (SOR) structures has been developed by researchers at Texas A&M University. These analyses employ the matrix displacement method of structural analysis utilizing a curved shell element. Geometrically nonlinear static and dynamic analyses can be conducted using these codes. The important natural frequencies and mode shapes can also be determined by employing another of the codes. Efficient programming provides codes capable of performing these desired analyses in relatively small amounts of computer time.

Each of these programs has been extensively tested using problems the solutions to which have been reported by other researchers in order to establish the validity of the codes. In addition, the capabilities of the codes have been demonstrated in a number of publications by presenting solutions to problems which were unsolved by other researchers.

SAMMSOR II - Stiffness And Mass Matrices for Shells Of Revolution are generated utilizing the first member of this family. This program accepts a description of the structure in terms of the coordinates and slopes of the nodes and the properties of the elements joining the nodes. For shells with simple geometries (such as cylinders, shallow caps, hemispheres, etc.) the shell geometry can be internally generated. Utilizing the element properties, the structural stiffness and mass matrices are generated for as many as twenty harmonics and stored on magnetic tape. Each of the other SOR programs utilizes the output tape generated by SAMMSOR as input

data for the respective analyses. One advantage of creating the stiffness and mass matrices in a separate program is that a variety of analyses can be performed on the same shell configuration without having to create the matrices more than once. Obviously, a variety of boundary and loading conditions can be employed without having to create new mass and stiffness matrices for each case.

SNASOR II - The Static Nonlinear Analysis of Shells Of Revolution subjected to arbitrary mechanical and thermal loading is performed using the second computer code. Utilizing the stiffness matrices generated by SAMMSOR and the loading conditions and boundary conditions input to SNASOR II, the equilibrium equations for the structure are generated. The nonlinear strain energy terms result in pseudo generalized forces (as functions of the displacements) which are combined with the applied generalized forces. The resulting set of nonlinear algebraic equilibrium equations is solved by one of several methods: Newton-Raphson type iteration, incremental stiffness method, or a modified incremental stiffness method. In general, the Newton-Raphson procedure is the best and yields accurate results for highly nonlinear problems.

DYNASOR II - The third code is used for the Dynamic Nonlinear Analysis of Shells Of Revolution. The equations of motion of the shell are solved using Houbolt's numerical procedure with the nonlinear terms being moved to the right-hand side of the equilibrium equations and again treated as generalized loads. The displacements and stress resultants can be determined for both symmetrical and asymmetrical loading conditions. Asymmetrical dynamic buckling can be investigated using this program. Solutions can be obtained for highly nonlinear problems in reasonable periods of time on the computer utilizing as many as five of the harmonics generated

in SAMMSOR. A restart capability is incorporated in this code which allows the user to restart the program at a specified time without having to expend the computer time necessary to regenerate the prior response.

FAMSOR - Frequencies And Modes for Shells Of Revolution can be determined using the fourth code. Using the stiffness matrix generated by SAMMSOR and a lumped mass representation developed from the consistent mass matrix generated by SAMMSOR, a specified number of natural frequencies (beginning with the lowest or fundamental frequency) are obtained using the inverse iteration method. The mode shapes for each of the frequencies are also obtained.

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NOMENCLATURE

Variable

a_1, a_2, a_3 = coefficients in the expansion for shell slope representation

$$C_1 = E_s t / (1 - \nu_{s\theta} \nu_{\theta s})$$

$$C_2 = E_\theta t / (1 - \nu_{s\theta} \nu_{\theta s})$$

$$D_1 = E_s t^3 / [12(1 - \nu_{s\theta} \nu_{\theta s})]$$

$$D_2 = E t^3 / [12(1 - \nu_{s\theta} \nu_{\theta s})]$$

E = modulus of elasticity

e = linear strains and rotations of shell middle surface

G = shear modulus

$$G_1 = Gt$$

$$G_2 = Gt^3 / 12$$

IA = number of Fourier cosine harmonics

[K] = structural stiffness matrix

[M] = structural mass matrix

q = generalized nodal displacement (cylindrical coordinates)

r = radial coordinate normal to the axis of revolution

s = meridional coordinate

T = kinetic energy

U = strain energy

u, v, w = meridional, tangential, and normal displacements, respectively

z = axial coordinate

α = generalized coefficient of a displacement function

θ = circumferential angular coordinate

ν = Poisson's ratio

ϕ = angle between meridian and axis of revolution in the unde-formed shell

x = changes in curvature

σ = stress component

INTRODUCTION

The SAMMSOR (Stiffness And Mass Matrices for Shells Of Revolution) II code has been developed as the basic code used by the three SOR family analysis programs --- SNASOR II, DYNASOR II, and FAMSOR. This report is a user's guide for the SAMMSOR II code and is divided into four self-contained sections with an extended appendix.

The first section of the report describes the method of analysis used to obtain the output matrices. This documentation is not intended to be a detailed derivation of the element and structural properties but is intended to show the basic sets of equations employed in calculating the element and structural properties.

A section providing guidelines for the user and enumerating many of the limitations of the code is then presented. The hints contained in this second section concern mainly the selection of an element idealization for the shell. The limitations presented result partly from the method of analysis and partly from the programming procedures and storage capacity utilized.

A description of the input data required by the code is presented in the third section. Limitations placed upon the input parameters are once again presented and examples are provided in cases where the wording might, at first glance, seem to be unclear or insufficient.

A final section containing a number of example problems follows the description of the input data. Copies of the input data required for each case are presented along with selected output that may be scrutinized by a user who desires to check his output. The user should study and understand the example problems before attempting to input to the code.

While the appendix which follows the main report may seem to be quite extensive, it is believed that the user will find the various sections extremely useful, especially if a thorough understanding of the program is desired. A description of the various subroutines, a glossary defining the significant FORTRAN variables, a subroutine call map and a flow chart of the basic operations are included in this appendix. A discussion of the program output is also included. Since undoubtedly some users will find it necessary to modify the element capacity of the code, a section in the appendix describes this procedure. A sample coding sheet for use in preparing input data is provided to aid the user.

An extended effort has been made to anticipate the questions which a user might ask before running the program. In particular, the report attempts to provide guidelines and hints for the successful use of the options for inputting the shell geometry and for the selection of the element idealization.

SECTION I
METHOD OF ANALYSIS

Introduction

The purpose of this section is to provide theoretical documentation of the equations and procedures employed in the SAMMSOR II code to calculate the mass and stiffness matrices used by the Shell Of Revolution (SOR) analysis programs. This program uses the curved shell element of Stricklin, Navaratna, and Pian¹ and the displacement function investigated by Mebane.² Since the nonlinear terms are treated as pseudo generalized forces in both the static³ and dynamic⁴ nonlinear analyses, the stiffness and mass matrices remain the same as in the linear analysis of shells of revolution. Detailed presentations of the methods of linear analysis can be found in Refs. 1, 2, and 5.

Structural Idealization

The shell of revolution is idealized as a sequence of consecutively numbered curved elements. The slope of each element (Fig. 1) is represented by a second-order polynomial in the meridional distance s :

$$\phi = a_1 + a_2 s + a_3 s^2 \quad (1)$$

where ϕ is the slope between the vertical axis and a tangent to the shell in the meridional direction, s is the meridional distance along the element, and a_1 , a_2 , and a_3 are coefficients that are evaluated by requiring the slopes of the structural idealization and the actual shell to be the same at the nodal points.

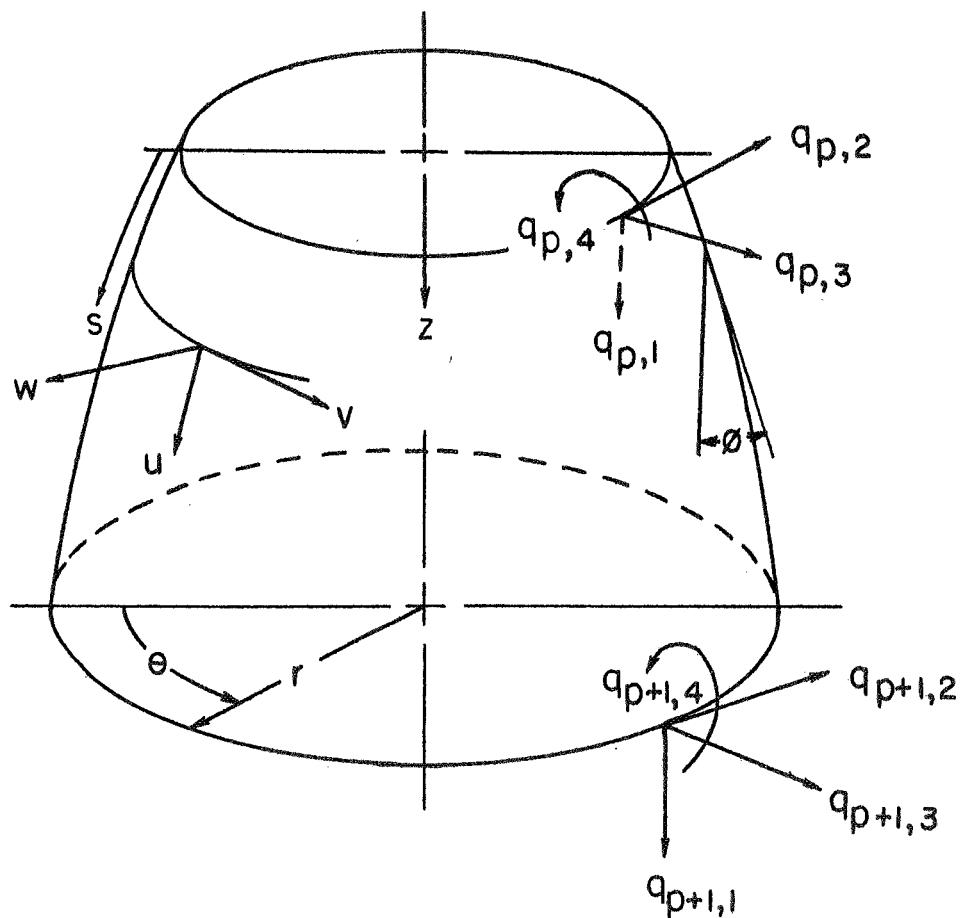


Fig. I GENERALIZED COORDINATES
OF SHELL ELEMENT

Displacement Functions

The displacements of an element in the normal, meridional, and circumferential directions are represented by cubic polynomials in the meridional distance s and by a Fourier expansion in the circumferential angle θ :

$$\begin{aligned} w &= \sum_{i=0}^{IA} [\alpha_1^i + \alpha_2^i s + \alpha_3^i s^2 + \alpha_4^i s^3] \cos i\theta \\ u &= \sum_{i=0}^{IA} [\alpha_5^i + \alpha_6^i s + \alpha_9^i s(s-\ell) + \alpha_{10}^i s^2(s-\ell)] \cos i\theta \\ v &= \sum_{i=0}^{IA} [\alpha_7^i + \alpha_8^i s + \alpha_{11}^i s(s-\ell) + \alpha_{12}^i s^2(s-\ell)] \sin i\theta \end{aligned} \quad (2)$$

In these expressions, the α 's are the generalized coefficients; ℓ is the length of an element in the meridional direction; and i is the harmonic number.

Four degrees of freedom of the element are eliminated using the technique of static condensation.⁶ After condensation each element has an 8×8 element stiffness matrix. The net result is therefore a stiffness matrix based upon higher order displacement functions without requiring additional geometrical data about the elements.

Linear expressions for u and v are used in the SAMMSOR I code,⁴ but it has been recently shown² that the cubic polynomials better represent rigid-body motion and converge somewhat faster than the linear displacement fields. The input data for the SAMMSOR I and II codes is identical.

In both the SNASOR II and DYNASOR II codes, linear displacement functions are used for evaluating the nonlinear terms; justification for this is provided in Ref. 4.

The generalized coordinates, q_i , of the shell are defined as the displacements and rotations at the nodes in cylindrical coordinates for each harmonic (Fig. 1). The shell generalized coordinates are related to the generalized coefficients, α , through the relation

$$\{\alpha\} = [A]\{q\} \quad (3)$$

where

$$[A] = [B]^{-1}[\Psi]^t$$

The matrices $[B]^{-1}$ and $[\Psi]^t$ are presented as expressions (5) and (6) in Ref. 3.

Strain-Displacement Relations

While the nonlinear shell theory of Novozhilov⁷ is applied in the SNASOR and DYNASOR codes the method of treating the nonlinear terms allows calculation of the stiffness matrix for each harmonic based upon the following linear strain-displacement relations for the midsurface strains:

$$\begin{aligned} e_s &= (\partial u / \partial s) - \phi^* w \\ e_\theta &= (1/r)[(\partial v / \partial \theta) + u \sin \phi + w \cos \phi] \\ e_{s\theta} &= (1/r)(\partial u / \partial \theta) - (v/r) \sin \phi + \partial v / \partial s \end{aligned} \quad (4)$$

where

$$\phi^* = \frac{\partial \phi}{\partial s}$$

The changes in curvature of the shell element are given by:

$$\begin{aligned} x_s &= -\hat{\partial e}_{13} / \partial s \\ x_\theta &= -(1/r)(\hat{\partial e}_{23} / \partial \theta) - (1/r) \sin \phi \hat{e}_{13} \\ x_{s\theta} &= -(1/r)(\hat{\partial e}_{13} / \partial \theta) + (1/r) \sin \phi \hat{e}_{23} - \hat{\partial e}_{23} / \partial s \end{aligned} \quad (5)$$

where

$$\hat{e}_{13} = (\partial w / \partial s) + u \phi'$$

$$\hat{e}_{23} = (1/r)(\partial w / \partial \theta) - (v \cos \phi) / r$$

The strains at any point through the thickness of the shell can be written as

$$\begin{aligned}\epsilon_s &= e_s + x_s z \\ \epsilon_\theta &= e_\theta + x_\theta z \\ \epsilon_{s\theta} &= e_{s\theta} + x_{s\theta} z\end{aligned}\tag{6}$$

Stress-Strain Relations

The stress-strain relationships used in this analysis are valid for an orthotropic material whose principal lines of orthotropy are the s and θ directions. These expressions can be written as:

$$\begin{aligned}\sigma_s &= \frac{E_s}{1-v_{s\theta} v_{\theta s}} (\epsilon_s + v_{s\theta} \epsilon_\theta) \\ \sigma_\theta &= \frac{E_\theta}{1-v_{s\theta} v_{\theta s}} (\epsilon_\theta + v_{\theta s} \epsilon_s) \\ \sigma_{s\theta} &= G \epsilon_{s\theta}\end{aligned}\tag{7}$$

Strain Energy

The strain energy expression for orthotropic shells is given by

$$U = \frac{1}{2} \iiint [\sigma_s \epsilon_s + \sigma_\theta \epsilon_\theta + \sigma_{s\theta} \epsilon_{s\theta}] r d\theta ds dz \tag{8}$$

Substituting Eqs. 7 into Eqs. 8 and integrating through the thickness,

the strain energy can be expressed in the following form

$$U = \frac{1}{2} \int \int (C_1 \epsilon_s^2 + C_2 \epsilon_\theta^2 + 2\nu_{s\theta} C_1 \epsilon_s \epsilon_\theta + G_1 \epsilon_{s\theta}^2 + D_1 x_s^2 + D_2 x_\theta^2 + 2\nu_{s\theta} D_1 x_s x_\theta + G_2 x_{s\theta}^2) r d\theta ds \quad (9)$$

The strain energy can also be written as a quadratic form and the element stiffness matrix calculated using

$$U^i = [q^i] [k^i] \{q^i\} \quad (10)$$

where i denotes the harmonic number. This procedure has been explained in detail in Refs. 1 and 3.

Mass Matrix

The element mass matrices, which include the effects of rotary inertia, can be obtained by considering the expression for the kinetic energy:

$$T = \frac{1}{2} \int_{V_0} (\dot{u}^2 + \dot{v}^2 + \dot{w}^2) dm \quad (11)$$

Substituting the proper derivatives of the displacement functions, the kinetic energy can be written as a quadratic form in the generalized velocity coefficients.

$$T = \frac{1}{2} [\dot{\alpha}] [\bar{M}] \{\dot{\alpha}\} \quad (12)$$

The $\{\dot{\alpha}\}$ matrix is related to the velocities of the generalized structural coordinates, $\{\dot{q}\}$, by the transformation

$$\{\dot{\alpha}\} = [A] \{\dot{q}\} \quad (13)$$

The terms in $[\bar{M}]$ are listed in the appendix of Ref. 4. Because of the inclusion of the effects of rotary inertia, the mass matrix is a function of

the harmonics being used. The mass matrix in structural coordinates is then obtained from

$$[M^e] = [A]^T [\bar{M}] [A] \quad (14)$$

The mass matrices for the individual elements are then combined (in the same way as for element stiffness matrices) to obtain the structural mass matrix.

SECTION II

Guidelines and Program Limitations

Guidelines for the use of the SAMMSOR II code along with the limitations placed on the analysis are enumerated in this section. Some of these limitations result from the method of analysis utilized while others result from the programming procedures which are used. Most of these limitations are minor in nature and hence this code, when coupled with the other compatible SOR programs, can be used to analyze a large number of practical shell of revolution problems.

First of all, the shell must be idealized as a sequence of curved elements. As is the case with most computer codes using the finite element method, the selection of the element breakdown of the structure requires the application of engineering judgement. The following considerations should prove most helpful in the selection of the idealization:

- (1) Elements should be closely spaced in regions where rapid variations of the displacements and stresses are anticipated.
- (2) Elements should be concentrated in regions of rapidly varying material properties.
- (3) The change in slope over an element should, in general, be kept less than about 10° .

Examples of judicious choices of element breakdown can be seen by considering the example problems presented in Section IV. If doubt still exists about how many elements to use, it is recommended that the maximum number of elements allowed by the program (50) be employed.

The material used in the shell may be isotropic or orthotropic. For an orthotropic material, the principal directions of orthotropy must be in

the meridional and circumferential directions. It is also assumed that the material properties for any given element are constant in the two directions, but these properties may vary from element to element. The properties of an element must be constant through the thickness of the element. The thickness of an individual element is constant, but thickness variations from element to element are allowed.

Slope discontinuities are not allowed between elements, i.e. the slope at the end of element i must equal the initial slope of element $i + 1$.

The code requires that the units for the input, and hence output, data be given in inch-pound-seconds. A different set of consistent units may be utilized if the value of the FORTRAN variable GRAVITY is changed in subroutines AZERO and NONAB.

The integrals which are required for the calculation of the element stiffness and mass matrices are evaluated exactly in the circumferential direction, but Simpson's rule is applied at twenty-nine (29) equally spaced stations along the element in the meridional direction. Fewer stations could probably be used for most problems, but good results have been obtained in all cases using 29 stations.

Stiffness and mass matrices may be generated for the first 20 Fourier harmonics. In general, it has been found that few problems require more than 3-5 of the harmonics. Unless the exact number of harmonics to be used by the solution programs is known, it is better to generate a relatively large number of harmonics say (6-8) in SAMMSOR so that they will be available if needed.

Utilizing only the cosine harmonics necessitates that the meridional line traced by $\theta = 0$ be selected so that the displacements, u and w , of the shell will be symmetrical about this line in the θ - direction.

A maximum of fifty (50) elements are allowed in the SAMMSOR code. It is believed that 50 elements is sufficient for a very large number of shell of revolution problems. More elements may be needed for analyzing geometrically complex structures such as the shell with negative Gaussian curvature depicted in Fig. 2-d of Ref. 3. Since undoubtedly some users will find it necessary to change the maximum allowable number of elements in the program, instructions for changing the capacity are given in Appendix 6.

A different output tape unit number (NT - Card III) must be specified for each of the cases of a particular run. Logical units 5 and 6 are used for the card reader and printer. Three scratch tapes are used by the code.

Utilizing FORTRAN IV language, it has been noted that double-precision arithmetic is necessary for operation on an IBM 360/65 computer. This additional word length is not believed necessary when the program is employed on machines with a longer built-in word length (such as a CDC 6600 machine).

The following limitation is placed upon the values of the Poisson's ratios of the materials:

$$\nu_{s\theta} \nu_{\theta s} < 1$$

If this criterion is violated, the stiffness matrix is no longer positive definite.

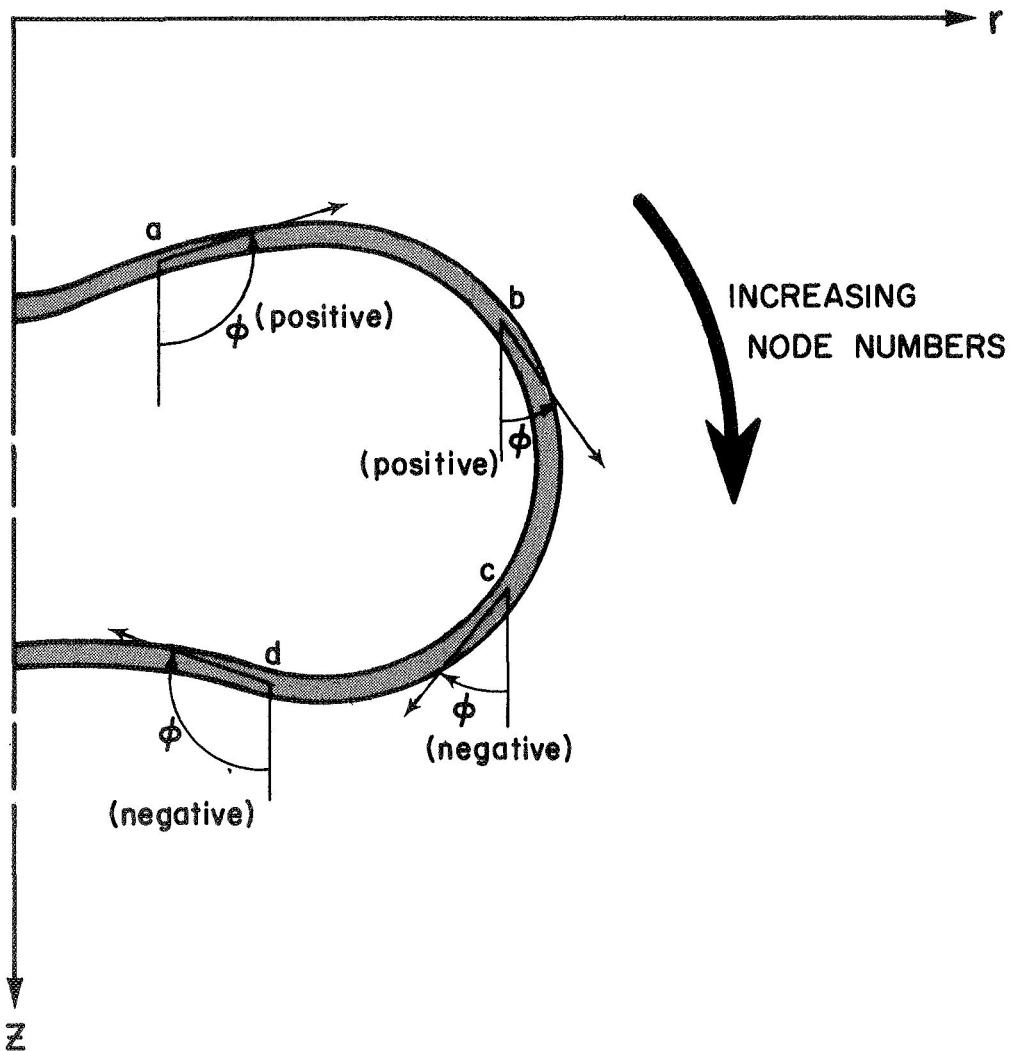
The slope, ϕ , at a node is considered positive if the tangent drawn in the direction of increasing node numbers is rotated counterclockwise from the positive z-axis. A negative slope exists if the tangent is

rotated clockwise from the positive z-axis. The magnitude of ϕ is thus limited to the range $-180^\circ \leq \phi \leq 180^\circ$. Considering Fig. 2 it should be noted that at nodes a and b the value of ϕ is positive while nodes c and d give rise to negative values of ϕ . Reversing the direction of node numbering therefore changes both the sign and the magnitude of the slope at a node.

Restrictions or limitations placed upon input geometry are:

1. The magnitude of ϕ must be in the range $-180^\circ \leq \phi \leq 180^\circ$.
2. A generating segment cannot have a change in slope greater than 180° (this restriction is easily circumvented by using a greater number of segments to generate the element data).
3. The generating segments must always be placed in the r - z coordinate system so that r and z are always positive (first quadrant).
4. The circular and parabolic segments cannot be degenerated to flat elements (linear segments).
5. A segment cannot contain, except at an end point, the "discontinuity" in slope at $\pm 180^\circ$. To circumvent this restriction use one segment whose slope is -180° at its final node and a second segment whose initial slope is $+180^\circ$.
6. Only elements which are consecutively numbered may intersect. This restriction is imposed to maintain the banding which is present in the stiffness and mass matrices.

In addition to the major limitations presented here, the section describing the input to the code enumerates a number of minor requirements which are necessary for valid input data. Other limitations and guidelines are also presented in the user's manuals for the solution programs: SNASOR II, DYNASOR II, and FAMSOR.



Axis of Revolution

FIG. 2 SIGN CONVENTION FOR SLOPE SPECIFICATION

SECTION III

Program Input

The SAMMSOR code has been written so that the program can readily be utilized by investigators who are not familiar with the inner workings of the program. Using the hints and adherring to the limitations presented in the previous section, it is believed that a user with only a superficial knowledge of the finite element method can effectively employ the SAMMSOR II code.

The double-precision version of the code requires a storage space of about 190K bytes on the IBM 360/65. The single-precision code requires approximately 110K bytes. The code is written in the FORTRAN IV language.

The input data for the program consists of one card I (card types will be explained on the following pages) followed by a complete data set for each of the cases to be run. A final card VIII is added at the end of the last data set. A case consists of cards of type II through VII and is all the input data required to generate the desired stiffness and mass matrices for a particular shell. The set of cards II - VII for a case is also referred to as a data set. There is no limit on the number of cases which can be included per run, but the logical unit number of the output tape (NT from Card II) must be different for each case of a run.

I. RUN CONTROL CARD

This card is used to identify the number of cases to be run and the logical unit numbers of the scratch tapes used in the run. (ONLY ONE CARD I IS USED PER RUN.)

Card Type I Format (4I5)		
Columns	Variable	Description
1-5	NCASES	The number of different data sets utilized for this run.
6-10	ND	Logical unit number for scratch tape. All the input data for the run is read onto this unit at the start of the run and is stored here until needed in the program.
11-15	NS	Logical unit number for scratch tape used by the program.
16-20	NS2	Logical unit number of a second scratch tape used by the code.

II. CASE IDENTIFICATION CARDS

These cards allow the user to print out comments which identify the problem being run.

A. Control Card (ONE CARD II-A PER DATA SET)

Card Type II-A Format (2I5)		
Columns	Variable	Description
1-5	NCARDS	Number of comment cards (Type II-B) which follow.
6-10	NT	Unit number of the tape on which stiffness and mass will be stored. The value of NT must be different for each case of a run.

B. Identification Cards

The information printed on these cards is printed as output for the SOR programs and should identify the particular shell being analyzed.
(IF NCARDS=0, OMIT CARDS II-B, OTHERWISE INCLUDE NCARDS OF TYPE II-B.)

Card Type II-B Format (20A4)		
Columns	Variable	Description
1-80	COMENT	Any desired alphanumeric information may be printed on these cards.

III. CASE CONTROL CARD

Identifies the number of elements and harmonics used and gives the unit number for the output tape. (ONE CARD III PER DATA SET)

Card Type III Format (3I5)		
Columns	Variable	Description
1-5	NELEMS	Total number of elements used to idealize the shell (NELEMS \leq 50).
6-10	IA	Total number of harmonics for which mass and stiffness matrices are to be calculated ($1 \leq IA \leq 20$).
11-15	NPRNMS	If the mass and stiffness matrices are to be printed, set NPRNMS = 1. If not, set NPRNMS = 0.

IV. MATERIAL PROPERTIES

The elastic and mass properties in the meridional and circumferential directions are constant over an element, but the properties can vary from element to element. (THE NUMBER OF CARDS OF TYPE IV < NELEMS (CARD III) PER DATA SET.)

Card Type IV Format (2I5, 5F10.0)		
Columns	Variable	Description
1-5	IELM1	Number of the first element to which the properties on this card apply.
6-10	IELM2	Number of the last element to which the properties on this card apply.
11-20	EE1	Young's Modulus of elasticity in the meridional direction (psi).
21-30	EE2	Young's Modulus of elasticity in the circumferential direction (psi).
31-40	GG	Shear modulus (psi). For an isotropic material, $GG=E/2(1+\nu)$
41-50	FFNU1	Poisson's ratio. The contraction in the meridional direction due to stress in the circumferential direction.
51-60	RHO	Density of the material (lb./in. ³).

NOTE: The elastic and mass properties can be read in for each individual element using NELEMS cards of type IV. If the properties of a consecutively numbered group of elements are the same, the input data can be simplified considerably by using only one card to describe the properties of this group of elements. In particular, if the elastic and mass properties of all the elements are the same, only one card of type IV is necessary per data set.

EXAMPLE: Consider a shell that is idealized using 20 elements. Assuming that the elastic properties of elements 1 through 10 are the same, different properties exist for the eleventh element and elements 12 through 20 have the same properties as the first group. Three cards should be

used to input the properties of the shell. The following values for IELM1 and IELM2 should be used.

Card 1:	IELM1 = 1	IELM2 = 10
Card 2:	IELM1 = 11	IELM2 = 11
Card 3:	IELM1 = 12	IELM2 = 20

A less sophisticated procedure would be to use one card for each element. Note that the properties for the elements 12-20 must be read in on a different card from those of elements 1-10.

V. THICKNESS

It is assumed that the thickness is a constant over the element in the meridional and the circumferential directions. Essentially the same procedure is used here as is employed with cards IV for the material properties. (THE NUMBER OF CARDS OF TYPE V MUST BE ≤ NELEMS FOR ANY GIVEN DATA SET.)

Card Type V Format (2I5, F10.0)		
Columns	Variable	Description
1-5	IELM1	Number of the first element to which thickness properties on this card apply.
6-10	IELM2	Number of the last element to which thickness properties on this card apply.
11-20	TT	Thickness of the shell element or group of elements (in).

VI. SHELL GEOMETRY

A most important part of any shell of revolution analysis is the generation of the geometry and the element idealization of the shell. For this reason, an extended discussion follows which describes in detail the procedure used to generate the geometry of the idealized shell. Slope discontinuities between elements are not allowed.

The shell nodal coordinates and slopes can be generated using either of two options available (or a combination of the two):

OPTION 1: The user may specify the coordinates and slopes of the nodes by inputting the values of these parameters at each of the nodes.

OPTION 2: For shells of relatively simple geometry (shallow caps, hemispheres, cylinders, etc.) the program has the capability of generating internally the desired nodal point data.

The shell is considered as being composed of one or more segments, with the segments being divided, in turn, into one or more sub-segments. The sub-segments are then divided into the desired number of finite elements. A segment may contain only one element or the entire shell may in some cases be considered as a single segment. The choice of the segment breakdown depends upon the option selected for inputting the shell geometry as well as the geometry of the shell itself.

If the geometry for a particular segment is to be generated internally, the profile of the segment must be linear, circular or parabolic. A segment is divided into a maximum of five sub-segments with each sub-segment being divided, in turn, into a specified number of equally spaced elements. Obviously, if the segment consists of only one element, no division into sub-segments is necessary. A set of cards (type VI) is required for each segment, with a set consisting of one card of types VI-A, VI-B, and VI-C --- in that order.

In order to generate the required nodal point data for a given shell, the following procedure must be used:

1. Select a breakdown of the shell into segments.
2. Establish the desired breakdown of the segments into sub-segments and determine the number of elements to be used for each sub-segment.
3. Input the required three data cards for each segment until the data for all the segments has been input.

The total number of data cards necessary for establishing the geometry of the entire shell is equal to three times the number of segments. If the first option is used for generating the geometry, the user will find that the total number of cards required will equal ($3 * \text{NELEMS}$) where NELEMS was defined on card III. However, only ($\text{NELEMS} + 1$) of these cards will be different since duplicate cards and blank cards are used. The procedure may therefore seem somewhat cumbersome when the user desires to specify the slopes and coordinates of each node. The procedure is, however, extremely simple when the nodal point data is to be internally generated. In addition, it has been found that fewer input errors arise when using this simple but repetitious procedure. It is for these reasons that the procedure is used in the code. An example of the effective use of this scheme can be seen by considering the first example problem presented where only three cards are required to generate the desired nodal data.

A. Segment initial node data

The data furnished by this card provides the node number, slope and coordinates of the initial node of a given segment.

Card Type VI-A Format (I5, 3F10.0)

Columns	Variable	Description
1-5	NN1	Number of the node at the beginning of this shell segment.
6-15	Z1C	Axial coordinate of node NN1.
16-25	R1	Radial coordinate of node NN1.
26-35	PHI1	Slope of the shell in the meridional direction at node NN1 (degrees).

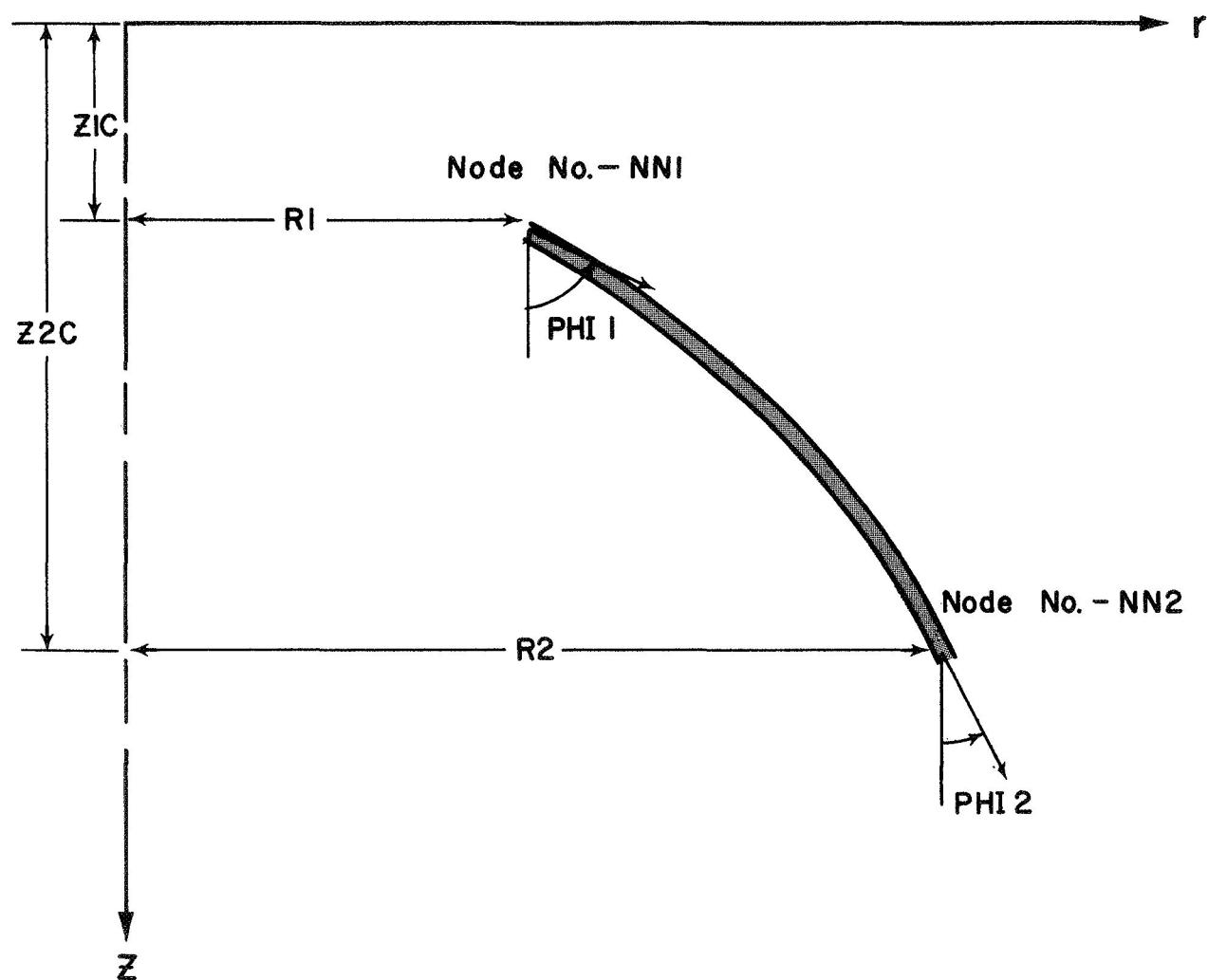
***The slopes PHI1 and PHI2 are measured from the positive axis of revolution to the tangent to the meridian (see Fig. 2). Refer to Fig. 3 for an explanation of the input parameters.

B. Segment terminal node data

The data furnished by this card provides the node number, slope, and coordinates of the final node of a given segment.

Card Type VI-B Format (I5, 3F10.0)

Columns	Variable	Description
1-5	NN2	Number of the node at the end of the segment (<u>NN2 must be > NN1</u>).
6-15	Z2C	Axial coordinate of node NN2.
16-25	R2	Radial coordinate of node NN2.
26-35	PHI2	Slope of the shell in the meridional direction at node NN2 (degrees).



Axis of Revolution

FIG. 3 INPUT VARIABLES SPECIFYING THE GEOMETRY OF A SHELL SEGMENT

C. Coordinate generation control card

This card controls the internal generation of data for the shell segment whose end coordinates are described on cards III-A and III-B of this set by describing the type of shell profile and the element breakdown to be used in the idealization of the segment. Each segment can be divided into a maximum of five sub-segments.

If ($NN2 = NN1 + 1$), obviously, the segment under consideration consists of only one element and the coordinates and slopes at the two adjacent nodes completely define the geometry of the shell segment. If this is the case, the user must include a card III-C in the set; but it must be blank.

Card Type VI-C Format (I5, 5(I5, F10.0))

Columns	Variable	Description
1-5	ICLASS	Control parameter which defines the shell profile ICLASS = 1 - linear profile ICLASS = 2 - circular profile ICLASS = 3 - parabolic profile
6-10	NERAT (1)	This data specifies the number of elements
11-20	RA (1)	and the relative lengths (decimal fractions) into which the sub-segments of the
21-25	NERAT (2)	shell segment are divided. <u>The sum of the</u>
26-35	RA (2)	<u>RA (I)'s must equal 1.0.</u>
36-40	NERAT (3)	
41-50	RA (3)	
51-55	NERAT (4)	
56-65	RA (4)	
66-70	NERAT (5)	
71-80	RA (5)

An understanding of the use of this card can be obtained by studying the input data for the example problems and by considering the following example. Consider a circular segment to be divided into four sub-segments which are each divided into five elements. Sub-segment lengths are

given as 1/10, 2/10, 1/2, and 2/10 respectively of the length of the segment. The following values would be used on card VI-C for this segment:

ICLASS = 2 (circular profile)

NERAT(1) = 5	RA(1) = 0.10
NERAT(2) = 5	RA(2) = 0.20
NERAT(3) = 5	RA(3) = 0.50
NERAT(4) = 5	RA(4) = 0.20
NERAT(5) = 0	RA(5) = 0.00
	$\Sigma = \underline{1.0}$

If the segment was divided instead into 20 equally spaced elements, then the data would be:

ICLASS = 2

NERAT(1) = 20	RA(1) = 1.0
NERAT(2) = 0	RA(2) = 0.0
NERAT(3) = 0	RA(3) = 0.0
NERAT(4) = 0	RA(4) = 0.0
NERAT(5) = 0	RA(5) = <u>0.0</u>
	$\Sigma = 1.0$

VII. FINAL DATA CARD FOR A CASE

Place this card after the last card VI-C of each data set. This signifies the end of the input data for a case. (USE ONE CARD VII PER DATA SET.)

Card Type VII	
Columns	Punch
1-11	END OF CASE

VIII. FINAL DATA CARD FOR A RUN

This card must be placed after the card VII of the last case to be run. This card denotes the end of the input data for a run. (ONLY ONE CARD VIII IS USED PER RUN.)

Card Type VIII	
Columns	Punch
1-10	END OF RUN

SECTION IV

EXAMPLE PROBLEMS

The example problems which follow were chosen to demonstrate the various facets of the input data required to run a given case and to acquaint the user with typical problems which have been analyzed using the SOR programs. As stated in a prior section, the choice of the element idealization must be judiciously selected. The example problems should provide the user with a "feel" for the selection of the element idealization for an analysis. The input data for the various shell geometries should answer any questions the user might have concerning the input procedure for cards VI of the input section.

Stiffness and mass matrices for selected harmonics are presented as output for the example problems. The output was generated using double-precision arithmetic on an IBM 360/65 system.

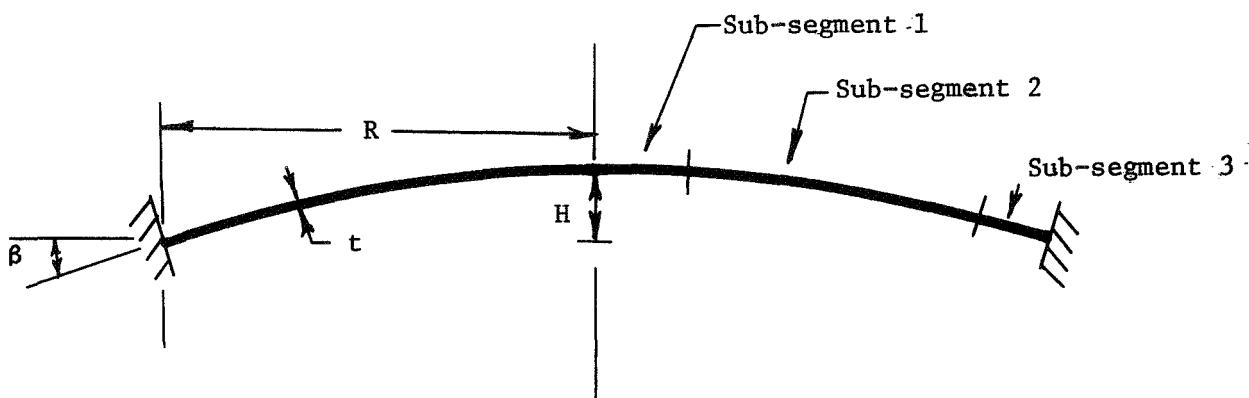
Example Problem 1

The first example problem is a shallow spherical cap ($\lambda = 6$) that has been analyzed extensively using the SNASOR II, DYNASOR II and the FAMSOR codes. The geometric and material properties for the shell are presented in Fig. 4.

The selection of the element breakdown and the number of harmonics to be generated depends not only upon the geometry of the shell, but also upon the loading to be applied to the shell. In order to be certain that the data for a sufficient number of harmonics will be generated, six (6) cosine harmonics will be used. The static and dynamic analyses previously conducted on this shell have shown that thirty (30) elements provide a good idealization for the loadings used providing these elements are concentrated near the apex of the shell, where a singularity obviously exists, and near the clamped edge.

A set of input data for this case is presented in Fig. 5. The geometry is input using the second option for inputting the data and the shell is considered as a single segment with a circular profile. Obviously, the geometry could have been input for each node, but the process would have been tedious.

A selected portion of the output generated for this case is presented in Figs. 6-10.



SHELL DESCRIPTION

$R = 0.9$ in.
 $H = 0.0859$ in.
 $t = 0.01576$ in.
 $\lambda = 6.0$
 $\beta = 10.9^\circ$

MATERIAL PROPERTIES

ALUMINUM

$E = 10.0 \times 10^6$ psi
 $G = 3.85 \times 10^6$ psi
 $\nu = 0.30$
 $\rho = 0.0942$ lb./in.³

ELEMENT BREAKDOWN

Sub-segment 1 - 6 elements
 Sub-segment 2 - 12 elements
 Sub-segment 3 - 12 elements

Fig. 4 SHALLOW SPHERICAL CAP

Fig. 5 INPUT DATA - EXAMPLE PROBLEM 1

GEOMETRIC AND ELASTIC PROPERTIES OF STRUCTURE

ELEM. NO.	NODE NOS.	Z	COORDINATES R	SLOPE	S	THICKNESS	ELASTIC CONSTANTS		NU1	RHO
							E1	E2		
1	1	0.0	0.10000D-05	0.90000D 02	0.1509D-01	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	2	0.95697D-04	0.30182D-01	0.89637D 02						
2	2	0.95697D-04	0.30182D-01	0.89637D 02	0.4527D-01	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	3	0.38278D-03	0.60362D-01	0.89273D 02						
3	3	0.38278D-03	0.60362D-01	0.89273D 02	0.7545D-01	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	4	0.86125D-C3	C.90540D-01	C.8891CD 02						
4	4	0.86125D-C3	0.90540D-01	C.88910D 02	0.1056D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	5	0.15311D-C2	0.12071D 00	0.88547D 02						
5	5	0.15311D-C2	0.12071D 00	0.88547D 02	0.1358D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	6	0.23922D-02	C.15088D 00	0.88183D 02						
6	6	0.23922D-02	C.15088D 00	0.88183D 02	0.1660D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	7	0.34447D-C2	0.18105D 00	0.87820D 02						
7	7	0.34447D-C2	0.181C5D 00	0.8782CD 02	0.2056D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	8	0.55628D-C2	C.230C5D 00	0.87230D 02						
8	8	0.55628D-02	C.230C5D 00	0.87230D 02	0.2547D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	9	0.81857D-C2	0.27902D 0C	0.86639D 02						
9	9	0.81857D-02	C.27902D 0C	0.86639D 02	0.3037D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	10	0.11313D-01	C.32797D 00	0.86049D 02						
10	10	0.11313D-01	C.32797D 00	C.86049D 02	0.3527D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	11	0.14945D-01	0.37688D 00	0.85458D 02						
11	11	0.14945D-01	0.37688D 00	0.85458D 02	0.4018D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	12	0.19080D-01	0.42575D 00	0.84868D 02						
12	12	0.19080D-01	C.42575D 00	0.84868D 02	0.45C8D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	13	0.23719D-01	0.47457D 00	0.84277D 02						
13	13	0.23719D-01	C.47457D 00	0.84277D 02	0.4999D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	14	0.28861D-01	0.52335D 00	0.83687D 02						
14	14	0.28861D-01	C.52335D 00	0.83687D 02	0.5489D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	15	0.34505D-01	0.57207D 00	0.83097D 02						
15	15	0.34505D-01	C.57207D 00	C.83097D C2	0.5980D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	16	0.40651D-01	0.62C73D 00	0.82506D 02						
16	16	0.40651D-01	C.62C73D 00	0.82506D 02	0.6470D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	17	0.47297D-C1	C.66932D 00	0.81916D 02						
17	17	0.47297D-C1	C.66932D 00	0.81916D 02	0.6961D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	18	0.54445D-C1	0.71784D 00	0.81325D 02						
18	18	0.54445D-C1	0.71784D 00	0.81325D 02	0.7451D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	19	0.62091D-01	0.76629D 00	0.80735D 02						
19	19	0.62091D-01	C.76629D 00	0.80735D 02	0.7753D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	20	0.63927D-01	C.77746D 00	0.80599D 02						
20	20	0.63927D-01	C.77746D 00	C.80599D 02	0.7866D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	21	0.65789D-01	0.78862D 00	0.80462D 02						
21	21	0.65789D-01	0.78862D 00	0.80462D 02	0.7979D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	22	0.67678D-01	0.79578D 00	0.80326D 02						
22	22	0.67678D-01	C.79578D 00	0.80326D 02	0.8092D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	23	0.69593D-01	0.81093D 00	0.80190D 02						
23	23	0.69593D-01	C.81093D 00	0.80190D 02	0.8206D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	24	0.71534D-01	0.82208D 00	0.80054D 02						
24	24	0.71534D-C1	0.82208D 00	C.80054D 02	0.8319D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	25	0.73503D-01	0.83323D 00	0.79917D 02						
25	25	0.73503D-01	C.83323D 00	0.79917D 02	0.8432D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	26	0.75497D-01	0.84437D 00	0.79781D 02						
26	26	0.75497D-01	C.84437D 00	0.79781D 02	0.8545D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	27	0.77519D-C1	C.85551D 00	0.79645D 02						
27	27	0.77519D-C1	C.85551D 00	0.79645D 02	0.8658D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	28	0.79566D-01	0.86664D 00	0.79509D 02						
28	28	0.79566D-01	C.86664D 00	0.79509D 02	0.8772D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	29	0.81640D-01	0.87776D 00	0.79372D 02						
29	29	0.81640D-01	0.87776D 00	0.79372D 02	0.8885D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	30	0.83741D-01	0.88889D 00	0.79236D 02						
30	30	0.83741D-01	C.88889D 00	0.79236D 02	0.8998D 00	0.1576D-01	0.100D 08	0.100D 08	0.385D 07	0.300 0.09420
	31	0.85868D-01	0.90000D 00	0.79100D 02						

Fig. 6 ELEMENT PROPERTIES (OUTPUT) EXAMPLE PROBLEM 1

		HARMONIC NUMBER	O	HAS THE FOLLOWING STIFFNESS MATRIX	
0.222543330	06	U..0			
-0.85592700	02	U..0	0.392402210	D9	
-0.117313360	04	U..0	0.22653560	D1	0.81e16195D 04
-0.222543330	06	U..0	0.85492720	C2	0.110731336D 04
0.0	0.0	U..0	0.0	0.0	0.0
-0.198572570	04	U..0	-0.130447000	C5	0.14330393u 02
-0.335820300	04	U..0	0.213229180	C1	0.17432026D 02
-0.465254340	06	U..0	0.91153e23D	C4	0.60013619D 04
0.0	0.0	U..0	0.0	0.0	0.0
-0.126611500	05	U..0	0.1145056480	C7	-0.135422860 02
-0.152790220	04	U..0	0.920976300	C2	-0.67023339D 02
-0.754148090	06	U..0	-0.38232E730	C5	0.167021910L C6
0.0	0.0	U..0	0.0	0.0	0.0
-0.133748280	05	U..0	-0.261101500	C7	-0.92327899D 02
-0.119726450	05	U..0	0.233705930	C3	0.91004613D 05
-0.104822410	07	U..L	-0.57325785D	C5	0.149395993D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.647659730	05	U..0	-C372915940	C7	-0.24202080D 03
-0.164343690	05	U..0	0.431e0727D	C3	0.15742666D 03
-0.134446390	07	U..0	-0.96424C890	C5	0.19409551u 03
0.0	0.0	U..0	0.0	0.0	0.0
-0.105887370	06	U..0	-0.483273107	C7	-0.441660u7D 03
-0.208987180	05	U..0	0.686e080770	C3	0.20250637D 03
-0.164220110	07	U..L	-0.1455C798D	C6	0.238773120
0.0	0.0	U..0	0.0	0.0	0.0
-0.157013360	06	U..0	-0.59289735D	C7	-0.98090558D 03
-0.253617910	05	U..0	0.99716493D	C3	0.24755995D 03
-0.481209690	06	U..0	-0.1696232CD	C6	0.11096966D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.183019040	06	U..0	-0.44808059D	C7	-0.26470430D 03
-0.119686840	05	U..0	0.741194840	C3	0.18858314D 03
-0.599774420	06	U..0	-0.22C97C72D	C6	0.13849561D 01
0.0	0.0	U..0	0.0	0.0	0.0
-0.278665850	06	U..0	-0.5560eC550	C7	-0.40654608D 03
-0.147303410	05	U..0	0.101714547D	C6	0.23586159D 03
-0.721657860	06	U..0	-0.373125C0	C6	0.16598679D 03
0.0	0.0	U..0	0.0	0.0	0.0
-0.394143230	06	U..0	-0.666503040	C7	-0.66504780D 03
-0.174574960	05	U..0	0.14579232D	C3	0.27859232D 03
-0.84738860	06	U..0	-0.50479595D	C6	0.19325781D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.129325140	06	U..0	-0.17743101D	C7	-0.9800752D 03
-0.201766200	05	U..0	0.19050533A0	C1	0.3235e242D 03
-0.97752593D	06	U..C	-0.656492110	C6	0.22050609D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.848070510	06	U..0	-0.88141651D	C7	-0.13516825D 04
-0.228863160	05	U..0	0.2397191450	C4	0.36845339D 04
-0.111263970	07	U..C	-0.82720060	C6	0.2477181290
0.0	0.0	U..0	0.0	0.0	0.0
-0.858212360	06	U..C	-0.98782375D	C7	-0.17791042D 04
-0.25953853610	05	U..0	0.29534343D	C6	0.41332351D 04
-0.1253302ED	07	U..L	-0.10172213D	C7	-0.27499096D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.105156740	07	U..C	-0.109349110	C8	-0.22627545D 05
-0.282725910	05	U..0	0.35632e42D	C3	0.4516721D 03
-0.140008610	07	U..0	-0.12262525D	C7	0.30193325D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.12839313D	07	U..C	-0.11963e76D	C8	-0.20022284D 04
-0.305467640	05	U..0	0.42239356D	C6	0.502920800
-0.15535569D	07	U..0	-0.145407C7D	C7	0.3288eC53D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.149507940	07	U..0	-0.13023943D	C8	-0.3397e284D 04
-0.33805740D	05	U..0	0.49438327D	C6	0.54761398D 03
-0.17142767D	07	U..0	-0.17004304D	C7	0.355619R0D 03
0.0	0.0	U..0	0.0	0.0	0.0
-0.20127299D	07	U..C	-0.14051512D	C8	-0.404767900
-0.38879519D	05	U..L	-0.1570230262	C6	0.32253998D 03
-0.18827999D	07	U..0	-0.19686049D	C7	0.38225591D 05
0.0	0.0	U..0	0.0	0.0	0.0
-0.20127299D	07	U..C	-0.15076620D	C8	-0.47531315D 04
-0.38879519D	05	U..L	-0.15520580D	C6	0.363689651D 03
-0.22586814D	07	U..C	-0.11477C390	C7	0.40874916D 05
-0.41900561D	05	U..0	-0.16088771D	C8	-0.5513e341D 04
-0.22586814D	07	U..C	-0.14579264D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.65595208D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12477218D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.11123950D	08	U..C	-0.74038664D	C8	-0.13151684D 09
-0.20539561D	06	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.11123950D	08	U..C	-0.71192597D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.22621663D 08
-0.21669571D	06	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.11123950D	08	U..C	-0.71192597D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.22621663D 08
-0.21669571D	06	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	09	U..C	-0.74038664D	C8	-0.22621663D 09
-0.21669571D	07	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.22621663D 08
-0.21669571D	06	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	09	U..C	-0.74038664D	C8	-0.22621663D 09
-0.21669571D	07	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	09	U..C	-0.74038664D	C8	-0.22621663D 09
-0.21669571D	07	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.13535930D 08
-0.21669571D	06	U..0	0.13649381D	C6	0.31164e42D 04
-0.14405857D	09	U..C	-0.11176e89D	C8	-0.80159046D 06
-0.22586814D	07	U..C	-0.16088771D	C8	-0.88782153D 07
-0.41900561D	05	U..0	0.74505770D	C6	0.68142488D 03
-0.22477C390	07	U..0	-0.12405742D	C6	0.82418247D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	-0.22621663D 08
-0.21669571D	06	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	09	U..C	-0.74038664D	C8	-0.22621663D 09
-0.21669571D	07	U..0	0.13258237D	C6	0.30720018D 04
-0.144058210	09	U..0	-0.114977C4D	C6	0.81289567D 06
0.0	0.0	U..0	0.0	0.0	0.0
-0.1123950D	08	U..C	-0.74038664D	C8	

		HARMONIC NUMBER	U	MAS HAS THE FOLLOWING MASS MATRIX
0.218659390-08		0..C	0.183411410-08	
-0.327737370-11		J..C	0.183300980-13 0.8678C194U-13	
-0.125800010-10		J..C	0.102850870-10 -0.956096160-11 0.175483560-07	
0..0		0..0	0..0	
-0.602677640-11		0..0	0..0	
0..9+885922D-11		0..0	0.1833959570-C8 0.503735130-13 C.247972890-1C 0..0	
0..334+3960-08		J..C	-0.150438790-13 -0.718522890-13 -0.251594710-10 0..0	
0..0		J..C	0..44778E520-10 -0.260497460-10 0.090559564-07	
-0.46617450-11		0..0	0..0	
0..293379850-10		0..C	0..350161970-08 0.4273U445U-12 -0.795157840-10 0..0	
-0.221316250-12		0..0	-0.237566730-12 -0.251535720-10 0..0	
0..557434490-C8		0..C	0..7574362450-10 -0.476526260-10 0.526398460-07	
0..0		J..C	0..0 0..0 0..0	
0..161300440-10		J..C	0..916954200-08 0.545788860-12 -0.170689700-09 0..0	
0..475829280-10		J..C	-0..069160800-12 -0.395933940-12 -0.25156670-10 0..0	
0..780498330-08		0..6	0..168512G7D-C9 -0.466876760-10 0.701799310-07	
0..0		0..0	0..0	
0..554575700-19		0..0	0..128142280-07 0.160574420-11 -0.298281850-09 0..0	
0..66220660-10		0..0	-0..1565850460-11 -0.554285220-12 -0.251346020-10 0..0	
0..100365220-07		0..C	0..257683670-09 -0.457115450-10 C.877144200-07	
0..0		0..0	0..0	
0..111166260-09		0..C	0..164981850-07 0.260704810-11 -0.462240920-09 0..0	
0..856481180-10		0..C	-0..228952360-11 -0.1261642420-12 -0.251203790-10 0..0	
0..122692160-U7		J..C	0..365021C9D-C9 -0.164721910-09 0.137587450-06	
0..0		J..C	0..0 0..0 0..0	
0..185950250-09		0..0	0..201599180-07 0.384953960-11 -0.812566470-09 0..0	
0..104662240-09		0..0	-0..346120790-11 -0.8709142460-12 -0.404559710-09 0..0	
0..288204860-07		J..C	0..800925910-09 -0.361240750-09 C.200A55960-06	
0..0		J..C	0..0 0..0 0..0	
0..215317800-09		J..C	0..405656460-07 0.166597450-10 -0.129729220-08 0..0	
0..357002810-09		J..C	-0..142432040-10 -0.3525273820-11 -0.95978650-10 0..0	
0..357037010-U7		J..C	0..1141746450-C8 -0.44659146U-C9 0.252314130-06	
0..0		J..C	0..0 0..0 0..0	
0..416585580-09		0..0	0..502063950-C7 -0.252068520-10 -0.186955990-08 0..0	
0..4423950-09		0..0	-0..22438120-10 -0.539010160-11 -0.937344940-10 0..0	
0..4525923910-U7		J..C	0..153972050-08 -0.53172790-09 0.296525210-08	
0..0		J..C	0..0 0..0 0..0	
0..675051770-09		0..C	0..598636930-07 0.355108420-10 -0.260979790-08 0..0	
0..52760600-09		0..0	-0..322119560-10 -0.442651060-11 -0.916849930-10 0..0	
0..4944875910-U7		0..C	0..159944150-C8 -0.61664392D-09 0.340680970-06	
0..0		0..C	0..0 0..0 0..0	
0..900375130-09		0..0	0..6944860010-07 0.75673400-10 -0.343625420-08 0..0	
0..12593520-C9		0..0	-0..437353420-10 -0.74+362081D-11 -0.949315840-10 0..0	
0..563903230-07		0..C	0..250551210-C8 -0.701293450-09 0.384773250-06	
0..0		0..C	0..0 0..0 0..0	
0..134215350-09		0..C	0..179088130-07 0.51712250-10 -0.37504640-08 0..0	
0..97923780-09		0..0	-0..570157520-10 -0.849835320-11 -0.986603230-10 0..0	
0..43301570-U7		J..C	0..307245460-08 -0.785640520-09 0.428793880-06	
0..0		J..C	0..0 0..0 0..0	
0..178992640-08		0..C	0..866673560-C7 0.769166320-10 -0.5245217340-08 0..0	
0..78176960-09		0..C	-0..720355290-10 -0.953277590-11 -0.93563260-10 0..0	
0..702224070-C7		C..0	0..369473320-C8 -0.869649330-C9 -0.472734750-06	
0..0		C..0	0..0 0..0 0..0	
0..227317130-08		0..C	0..982209000-C7 0.941969610-10 -0.658585230-08 0..0	
0..86588440-09		0..C	-0..887923010-10 -0.105661660-10 -0.980197210-10 0..0	
0..711537310-U7		J..C	0..43717520-C8 -0.953284180-09 0.516587780-06	
0..0		J..C	0..0 0..0 0..0	
0..281130810-08		0..0	0..107746460-C6 -0.113204947U-09 -0.785846170-08 0..0	
0..949636050-09		0..0	-0..107276890-09 -0.115984750-10 -0.978506520-10 0..0	
0..80965620-U8		0..C	0..510285580-C8 -0.103650960-08 C.563044950-06	
0..0		0..C	0..0 0..0 0..0	
0..340365790-08		0..0	0..117242C8D-06 0.139322920-C9 -0.923183670-08 0..0	
0..103298890-08		0..0	-0..12748760-09 -0.126295320-10 -0.972492760-10 0..0	
0..910517360-U7		C..0	0..588734250-C8 -0.111929010-09 0.603998280-06	
0..0		C..0	0..0 0..0 0..0	
0..404984390-08		0..0	0..1267CC320-C6 0.156370410-09 -0.1071324930-07 0..0	
0..11159070-08		0..0	-0..149047640-09 -0.130572470-10 -0.980157620-10 0..0	
0..980202790-07		J..C	0..672443220-C6 -0.12015907D-09 0.647539840-06	
0..0		J..C	0..0 0..0 0..0	
0..174839200-08		0..0	0..180509710-09 -0.123027720-07 0..0	
0..11935670-08		0..0	-0..173035980-C9 -0.14867513D-10 -0.963502950-10 0..0	
0..105003040-06		0..C	0..761130370-C8 -0.128337630-09 0.458171710-06	
0..0		0..C	0..0 0..0 0..0	
0..549913180-05		0..C	0..145056810-C6 0.2063349920-C9 -0.142604870-07 0..0	
0..120803180-08		0..0	-0..1980536320-C9 -0.157171219U-10 -0.213059310-08 0..0	
0..980202790-07		J..C	0..672443220-C6 -0.12015907D-09 0.647539840-06	
0..0		J..C	0..0 0..0 0..0	
0..11159070-08		0..0	-0..173035980-C9 -0.14867513D-10 -0.963502950-10 0..0	
0..105003040-06		C..0	0..761130370-C8 -0.128337630-09 0.458171710-06	
0..0		C..0	0..0 0..0 0..0	
0..549913180-05		C..0	0..145056810-C6 0.2063349920-C9 -0.142604870-07 0..0	
0..120803180-08		C..0	-0..1980536320-C9 -0.157171219U-10 -0.213059310-08 0..0	
0..980202790-07		J..C	0..672443220-C6 -0.12015907D-09 0.647539840-06	
0..0		J..C	0..0 0..0 0..0	
0..11159070-08		0..0	-0..173035980-C9 -0.14867513D-10 -0.963502950-10 0..0	
0..105003040-06		C..0	0..761130370-C8 -0.128337630-09 0.458171710-06	
0..0		C..0	0..0 0..0 0..0	
0..549913180-05		C..0	0..145056810-C6 0.2063349920-C9 -0.142604870-07 0..0	
0..120803180-08		C..0	-0..1980536320-C9 -0.157171219U-10 -0.213059310-08 0..0	
0..128418520-U7		J..C	0..812010180-C8 -0.351204420-10 0.241065380-06	
0..0		J..C	0..0 0..0 0..0	
0..822857590-C8		0..C	0..3479142400-C7 0.590685740-11 -0.163496449D-07 0..0	
0..306059520-10		0..C	-0..605939380-11 -0.346292790-11 -0.220257370-11 0..0	
0..-129222320-U7		C..0	0..858639936GD-C8 -0.360900560-10 0.247724370-06	
0..0		C..0	0..0 0..0 0..0	
0..84588010-U8		J..C	0..352201200-C7 0.628748730-11 -0.172739220-07 0..0	
0..365845010-10		J..C	-0..623096010-11 -0.352425550-12 -0.219700730-11 0..0	
0..-13059520-U7		C..0	0..E1515E240-C8 -0.3659717350-10 0.251046760-06	
0..0		C..0	0..0 0..0 0..0	
0..869195830-08		J..C	0..35646727D-07 0.6421964610-11 -0.177448470-07 0..0	
0..3070726610-10		J..C	-0..646048501D-11 -0.356319840-10 -0.219461760-11 0..0	
0..-1311956520-U7		C..0	0..905361000B-08 -0.37074380D-08 0.254364340-06	
0..0		C..0	0..0 0..0 0..0	
0..892603460-08		J..C	0..361313340-07 0.659086020-11 -0.182219590-07 0..0	
0..375595980-10		J..C	-0..6363212100-12 -0.219129040-11 0..0	
0..-13132969D-C7		C..0	0..92942823D-08 -0.37560780D-08 0.257677030-06	
0..0		C..0	0..0 0..0 0..0	
0..916701590-08		J..C	0..3574382U-C7 0.67771570-11 -0.187041410-07 0..0	
0..308044710-10		J..C	-0..675958520-11 -0.364610230U-12 -0.218837560-11 0..0	
0..-133461934D-C7		C..0	0..9537846560-C8 -0.380463250-10 0.260984790-06	
0..0		C..0	0..0 0..0 0..0	
0..0+0868930-08		J..C	0..37015292D-07 0.65982150-11 -0.191945550-07 0..0	
0..35231000-10		J..C	-0..694042420-11 -0.37299043U-12 -0.218542340-11 0..0	
0..-133952450-07		C..0	0..97842620-C8 -0.38593103U-11 0.264287540-06	
0..0		C..0	0..0 0..0 0..0	
0..-135952450-07		J..C	0..37454262D-07 0.716158460-11 -0.196865110-07 0..0	
0..-136534660-04		J..C	-0..712355472D-11 -0.377876460-12 -0.218243380-11 0..0	
0..-138474570-07		C..0	0..10033590L-07 -0.390148040-10 0.267585240-06	
0..0		C..0	0..0 0..0 0..0	
0..-13901250-08		J..C	0..37812070-07 0.73272575-11 -0.21868280D-07 0..0	
0..-139901520-10		J..C	-0..7309011530-11 -0.36276053D-12 -0.217634280-11 0..0	
0..-13972396D-C7		C..0	0..10540731D-07 -0.397997280-10 0.136570740-06	
0..0		C..0	0..0 0..0 0..0	
0..-140450220-07		J..C	0..38750939D-07 0.770549590-11 -0.104642310-07 0..0	
0..-1404658500-10		J..C	-0..7688053D-11 -0.3925121550-12 -0.186376880-09 0..0	

Fig. 8 ZEROTH (0) HARMONIC MASS MATRIX

HARMONIC NUMBER 1 HAS THE FOLLOWING STIFFNESS MATRIX

0.9971657016	0	0.2664691060	05	0.2648471656	09	0.9738755650	04	0.3744737930	06	0.7692387970	06	0.1122572007	00	0.9935821500	02		
0.5992636000	0	0.2647597500	05	0.2648471656	09	0.9738755650	04	0.3744737930	06	0.7692387970	06	0.1122572007	00	0.9935821500	02		
0.5992520570	09	0.2647597500	05	0.2648471656	09	0.9738755650	04	0.3744737930	06	0.7692387970	06	0.1122572007	00	0.9935821500	02		
0.8391245070	03	0.2613013490	C3	0.54-058467C0	02	0.1111436500	04	0.3744737930	06	0.7692387970	06	0.1122572007	00	0.9935821500	02		
0.160723080	C3	-0.1705e+5595	C0	0.1344059090	02	0.2287740400	04	0.4665603400	02	0.2919680800	05	0.3543609700	04	0.1193144900	01	0.719265100	01
0.1023625000	05	0.1045342320	C5	-0.7093324600	04	0.4560052720	02	0.4621592700	04	0.3543609700	04	0.1193144900	01	0.719265100	01		
0.2542950000	05	0.1847253590	C6	-0.0574553300	04	0.3042547500	02	0.6578913100	04	0.3543609700	04	0.1193144900	01	0.719265100	01		
0.2542950000	04	0.1847253590	C6	-0.0574553300	04	0.3042547500	02	0.6578913100	04	0.3543609700	04	0.1193144900	01	0.719265100	01		
0.5990978700	04	0.1317120500	C0	0.6867853200	04	0.4967847400	01	0.1997440800	05	0.230491960	02	0.282877070	07	0.041297230	01	0.362170290	01
0.3842492900	04	0.1317120500	C0	0.6867853200	04	0.4967847400	01	0.1997440800	05	0.230491960	02	0.282877070	07	0.041297230	01	0.362170290	01
0.3893236360	08	0.2072611000	04	0.1349576100	05	0.5260870200	04	0.9205457900	06	0.2121011600	07	0.1252931100	00	0.362170290	01		
0.2353941600	08	0.2072611000	04	0.1349576100	05	0.5260870200	04	0.9205457900	06	0.2121011600	07	0.1252931100	00	0.362170290	01		
0.1614502000	05	0.1349576100	05	0.5260870200	04	0.9205457900	06	0.2121011600	07	0.1252931100	00	0.362170290	01	0.362170290	01		
0.15002000	05	0.1523303000	C1	0.1166407300	04	0.5359386800	02	0.1166407300	04	0.1645870400	04	0.1645870400	04	0.1645870400	04		
0.5327171600	09	0.2424712400	C0	0.2424712400	09	0.2424712400	C0	0.2424712400	09	0.2424712400	09	0.2424712400	09	0.2424712400	09		
0.1494105000	09	0.2424712400	C0	0.2424712400	09	0.2424712400	C0	0.2424712400	09	0.2424712400	09	0.2424712400	09	0.2424712400	09		
0.3105043000	05	0.1209+414100	C0	-0.1414618670	02	0.1252931100	03	0.1252931100	03	0.1252931100	03	0.1252931100	03	0.1252931100	03		
0.8422393240	04	0.559+459410	C0	0.2156845400	03	0.7805121300	02	0.1748384400	04	0.128516700	C1	0.486676760	01	0.362170290	01		
0.4788744100	04	0.5365597700	C0	-0.4735277800	05	0.9711434600	04	0.1509151000	07	0.1997440800	05	0.163464330	07	0.163464330	07		
0.4605713000	04	0.5223913100	C0	-0.146551580	02	0.5817272700	01	0.4735277800	05	0.1997440800	05	0.163464330	07	0.163464330	07		
0.521721420	05	0.199689150	C0	-0.239620290	02	0.221973700	04	0.1252931100	03	0.278748000	05	0.9722402400	05	0.549175890	07		
0.104618180	C5	-0.559+897020	C1	0.343021930	03	0.1010742700	03	0.1010742700	03	0.1010742700	03	0.1010742700	03	0.1010742700	03		
0.2865060000	05	0.1551c+1310	C6	-0.726264600	05	0.1195116100	05	0.106936470	07	0.1997440800	05	0.162463950	06	0.162463950	06		
0.573016870	07	0.1911c+195900	C7	-0.1524604000	05	0.366830250	01	0.366830250	01	0.366830250	01	0.366830250	01	0.366830250	01		
0.7774404000	05	0.196209370	C0	0.294924590	07	0.3509+442930	03	0.162720010	06	0.102463950	06	0.532833180	07	0.162463950	06		
0.1269595210	05	0.161624050	C1	0.498673590	03	0.1233+34340	02	0.713688900	04	0.713688900	04	0.713688900	04	0.713688900	04		
0.4232474500	06	0.1715178400	05	0.393327320	03	0.555931530	02	0.555931530	02	0.554262460	06	0.554262460	06	0.554262460	06		
0.6950673000	05	0.167261600	C0	0.144703450	02	0.427343630	02	0.427343630	02	0.427343630	02	0.427343630	02	0.427343630	02		
0.040564600	05	0.192509870	C0	0.259587950	06	0.2224748210	C0	0.105242700	03	0.221877110	06	0.103460490	06	0.515234880	07		
0.1469394920	05	0.174353870	C0	0.259587950	06	0.2224748210	C0	0.105242700	03	0.221877110	06	0.103460490	06	0.515234880	07		
0.3035680000	04	0.130400140	C0	0.259587950	06	0.2224748210	C0	0.105242700	03	0.221877110	06	0.103460490	06	0.515234880	07		
0.138286260	05	0.1570+5150	C0	0.277422000	05	0.205088100	03	0.221877110	06	0.103460490	06	0.515234880	07	0.162463950	06		
0.737507320	04	0.164+747870	C0	0.353522720	03	0.116659090	03	0.9262+53410	03	0.137840970	01	0.422075780	03	0.202957890	03		
0.2625951170	C6	0.118+1615230	05	0.154-1615230	05	0.8011616200	04	0.781868170	06	0.162463950	06	0.242574760	07	0.162463950	06		
0.161219210	05	0.115+420400	C0	0.1550+5110	05	0.144+86460	02	0.6452+86460	03	0.6452+86460	03	0.261209350	07	0.162463950	06		
0.190630700	05	0.194+05360	C0	0.3319306150	03	0.334403040	03	0.4494+05150	03	0.4494+05150	03	0.728787070	05	0.72877700	03		
0.87389054	05	0.14-19452370	C0	0.372581570	03	0.139175290	03	0.432008020	03	0.157244670	01	0.603825790	03	0.1603825790	03		
0.425190500	05	0.136+649500	C0	0.251251320	05	0.968+80770	04	0.913+80770	04	0.242574760	07	0.162463950	06	0.242574760	07		
0.124374270	05	0.154-1781290	C0	0.1488+8950	02	0.5927+85340	03	0.45297+85340	03	0.298405450	07	0.162463950	06	0.298405450	07		
0.236326810	05	0.1918+333D	C0	0.3859+8010	04	0.479+514050	03	0.221877110	06	0.162463950	06	0.835+41650	07	0.162463950	06		
0.100953230	05	0.14-1535230	C0	0.9506002610	02	0.161+67020	02	0.938000230	03	0.137457470	01	0.719265100	01	0.137457470	01		
0.4908065270	05	0.154+561690	C0	0.272322120	00	0.110323230	05	0.104766200	07	0.199744080	05	0.162463950	06	0.162463950	06		
0.142596780	05	0.15+086960	C0	0.16-1603524B	07	0.1451+52920	05	0.648711900	03	0.648711900	03	0.335759870	03	0.335759870	03		
0.051402970	05	0.1896+3560	C0	0.34-0367360	03	0.677030590	03	0.755566680	06	0.562085170	05	0.941077860	07	0.162463950	06		
0.114491500	05	0.15+1495210	C0	0.1841+3520	03	0.9445+93470	03	0.9445+93470	03	0.120091920	01	0.35422180	01	0.35422180	01		
0.9574529400	05	0.1713+70176	C0	0.14-1623120	05	0.8118230750	03	0.118852630	03	0.118852630	03	0.118852630	03	0.118852630	03		
0.160797500	05	0.1713+70176	C0	0.14-1623120	05	0.8118230750	03	0.118852630	03	0.118852630	03	0.118852630	03	0.118852630	03		
0.4280774400	05	0.15+086960	C0	0.272322120	03	0.8118230750	03	0.118852630	03	0.118852630	03	0.118852630	03	0.118852630	03		
0.354750000	05	0.15+086960	C0	0.272322120	03	0.8118230750	03	0.118852630	03	0.118852630	03	0.118852630	03	0.118852630	03		
0.1500247700	05	0.15+086960	C0	0.272322120	03	0.8118230750	03	0.118852630	03	0.118852630	03	0.118852630	03	0.118852630	03		
0.777578100	05	0.227521250	C0	0.16-1603524B	07	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05		
0.17124830	05	0.15+086960	C0	0.16-1603524B	07	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05		
0.630943070	05	0.15+086960	C0	0.16-1603524B	07	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05	0.1455912100	05		
0.154777330	05	0.14-013700	C0	0.21+1417120	02	0.124+672970	04	0.221877110	06	0.146071950	05	0.146071950	05	0.146071950	05		
0.767575700	05	0.2265+92400	C0	0.14-1603524B	07	0.1778+248200	03	0.18+00770	05	0.18+00770	05	0.18+00770	05	0.18+00770	05		
0.2513042300	07	0.1875+87620	C0	0.14-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.266477070	05	0.15+0873050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.074482000	05	0.15+0873050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.2321529400	05	0.15+0873050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.604904260	05	0.17+0604050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.174492600	05	0.15+0873050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.703203820	05	0.15+0873050	C0	0.16-1623120	05	0.20+4428298	05	0.172062300	08	0.1450956240	08	0.265952640	08	0.265952640	08		
0.230410300	05	0.15+0873050</td															

Fig. 9 FIRST (1) HARMONIC STIFFNESS MATRIX

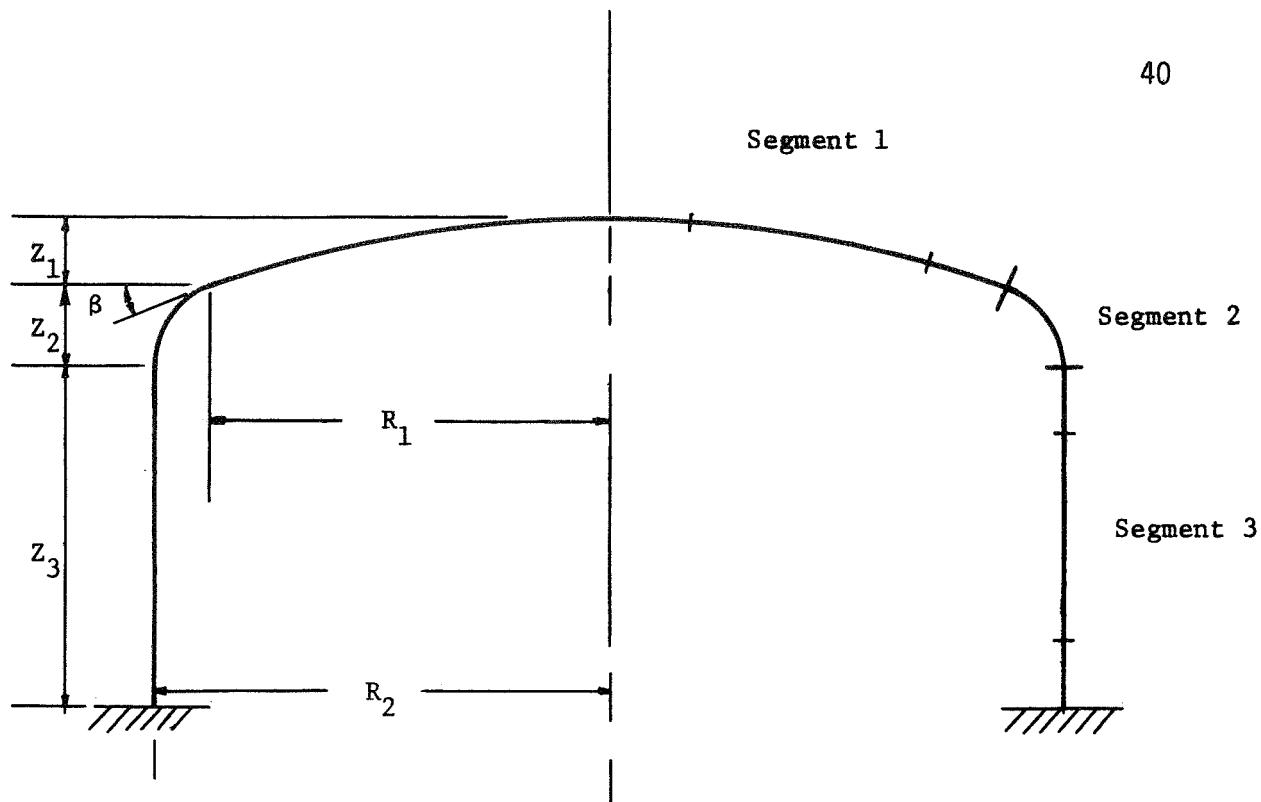
HARMONIC NUMBER- I HAS THE FOLLOWING MASS MATRIX

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-0.237815560-12 0.916992820-05 0.339168700-15 0.159503030-16 -0.110982420-11 0.733583750-08
-0.159503030-16 0.110982420-11 0.224316030-15 0.159503030-16 -0.110982420-11 0.733583750-08
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0.169393970-C8 -0.237813220-12 C.222190780-10 -0.144595960-19 0.176426320-07
-0.237821190-12 0.27504160-08 0.184328390-13 0.159513610-14 -0.110977060-11 0.146715020-07
-0.227506900-11 0.269110800-14 0.270508170-12 0.165327800-12 -0.409470250-10 C.140756710-13 0.146720780-07
0.144311940-10 -0.159513610-14 -0.1195513610-14 -0.1195513610-14 0.259401903-22 0.248963220-12 0.505599080-12
0.280009916-C8 -0.237791440-12 0.464567430-10 +0.2393187610-10 0.263823780-07
-0.237804720-12 0.458477970-08 0.335134730-14 0.159513620-14 -0.110950950-11 0.220065150-07
0.783911500-11 +0.18451C30-14 0.445842740-08 0.424951601-02 0.865272780-10 0.211127950-13 0.220082470-07
0.23886910-14 -0.159513620-14 -0.335927230-14 -0.198602660-12 0.125513900-10 0.112828770-22 0.373704720-12 0.756447540-12
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-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-14 -0.1122229750-14 -0.217739570-11 -0.4975952090-10 0.111930000-22 0.378113750-11 0.699950280-11
0.213017340-07 -0.3855162730-12 0.273015470-09 -0.105657730-09 0.141290300-06
-0.385576200-12 0.215336670-07 0.159513620-13 0.4212123560-14 -0.17923510-11 0.908612590-07
0.107350690-09 0.177597310-13 0.202296400-07 0.159513620-13 -0.4212123560-14 0.871715440-13 0.908935640-07
0.178592690-09 -0.4212123560-1

Example Problem 2

The second example problem, a little more geometrically involved than the first problem, is the cap-torus-cylinder configuration shown in Fig. 11. To generate the required geometry, the shell is considered to be the combination of a spherical cap, a torus, and a cylinder. Hence, three segments are used for inputting the shell geometry. The profiles of the first two segments are circular and obviously, the profile of the cylinder is linear. The elements are concentrated in the area of the apex of the shell, close to the cap-torus intersection, around the torus, and near the clamped end of the cylinder with the maximum number of elements (50) being utilized. Obviously, for this case the advantage of using the segmentized procedure for inputting the geometry is quite evident since only nine cards are required to input the geometry for this complex configuration.

Since the thickness is constant for the shell, only one card is necessary for this data. The same is true for the mass and elastic properties. Again, a set of input data (Fig. 12) is presented and a portion of the output is included (Fig. 13).



SHELL DESCRIPTION

$$R_1 = 3.00 \text{ in.}$$

$$R_2 = 5.44 \text{ in.}$$

$$z_1 = 0.0755 \text{ in.}$$

$$z_2 = 2.5495 \text{ in.}$$

$$z_3 = 3.00 \text{ in.}$$

$$\beta = 2.88 \text{ deg.}$$

$$t = 0.125 \text{ in.}$$

MATERIAL PROPERTIES
ALUMINUM

$$E = 10.0 \times 10^6 \text{ psi}$$

$$G = 3.75 \times 10^6 \text{ psi}$$

$$\nu = 0.333$$

$$\rho = 0.0942 \text{ lb/in}^3$$

ELEMENT BREAKDOWN

Segment 1 - Sub-segment 1 4 elements

Sub-segment 2 8 elements

Sub-segment 3 8 elements

Segment 2 - Sub-segment 1 18 elements

Segment 3 - Sub-segment 1 4 elements

Sub-segment 2 4 elements

Sub-segment 3 4 elements

Fig. 11 CAP-TORUS - CYLINDER CONFIGURATION

```

NCASE=1

PRINTOUT OF INPUT DATA

      10      20      30      40      50      60      70      80
123456789012345678901234567890123456789012345678901234567890

      5      4
***** EXAMPLE PROBLEM NO. 2 *****

***** CAP-TORUS-CYLINDER CONFIGURATION *****

***** ALL ELEMENTS HAVE THE SAME MATERIAL PROPERTIES AND THICKNESS *****

      50      6      1
      1  50 10000000. 10000000. 37500000. 0.333  0.0942
      1  50 0.125
      1  0.0  0.0  0.0  90.00
     21  0.0755  3.00  87.12
      2  4    0.2   8   0.6   8   0.2   0   0.0   0
     21  0.0755  3.00  87.12
     39  2.625   5.44   0.0   0.0   0.0   0   0.0   0
      2  18   1.0   0   0.0   0   0.0   0   0.0   0
     39  2.625   5.44   0.0   0.0   0.0   0   0.0   0
     51  5.625   5.4400  0.00  0.6   4   0.2   0   0.0   0
      1  4    0.2   4
END OF CASE

```

Fig. 12 INPUT DATA - EXAMPLE PROBLEM 2

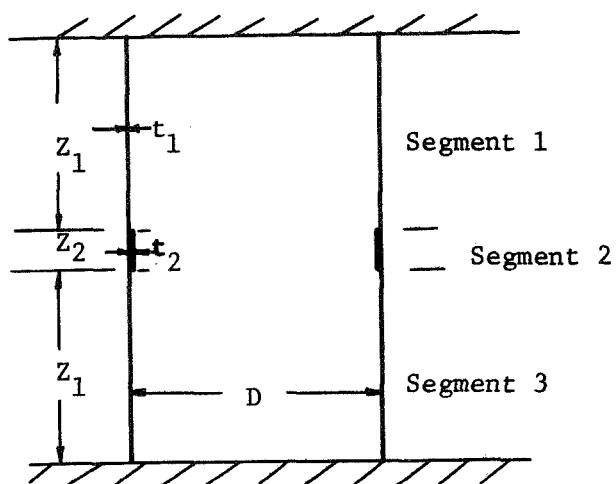
GEOMETRIC AND ELASTIC PROPERTIES OF STRUCTURE												
ELEM. NO.	NODE NOS.	Z	COORDINATES R	SLOPE	S	THICKNESS	E1	E2	ELASTIC CONSTANTS G	NUL	RHO	
1	1	0.0	0.10000D-05	0.900000 02	0.75030D-01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	2	0.188570-03	0.15006D 00	0.898560 02								
2	2	0.188570-03	0.15006D 00	0.898560 02	0.22510 00	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	3	0.754300-03	0.30013D 00	0.897120 02								
3	3	0.754300-03	0.30013D 00	0.897120 02	0.37520 00	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	4	0.169720-02	0.45019D 00	0.895680 02								
4	4	0.169720-02	C.45019D 00	0.895680 02	0.52520 00	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	5	0.301720-02	0.60024D 00	0.894240 02								
5	5	0.301720-02	0.60024D 00	0.894240 02	0.71280 00	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	6	0.970430-02	0.82532D 00	0.892080 02								
6	6	0.970430-02	0.82532D 00	0.892080 02	0.93790 00	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	7	0.923990-02	0.10504D 01	0.889920 02								
7	7	0.923990-02	0.10504D 01	0.889920 02	0.111630 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	8	0.136240-01	0.12754D 01	0.887760 02								
8	8	0.136240-01	0.12754D 01	0.887760 02	0.13880D 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	9	0.188570-01	0.15005D 01	0.885600 02								
9	9	0.188570-01	0.15005D 01	0.885600 02	0.16130 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	10	0.249370-01	0.17250D 01	0.883440 02								
10	10	0.249370-01	0.17250D 01	0.883440 02	0.181380 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	11	0.318660-01	0.19505D 01	0.881280 02								
11	11	0.318660-01	0.19505D 01	0.881280 02	0.20630D 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	12	0.396440-01	0.21754D 01	0.879120 02								
12	12	0.396440-01	0.21754D 01	0.879120 02	0.22880D 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	13	0.482690-01	0.24004D 01	0.876960 02								
13	13	0.482690-01	0.24004D 01	0.876960 02	0.24390 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	14	0.513320-01	0.24753D 01	0.876240 02								
14	14	0.513320-01	0.24753D 01	0.876240 02	0.25140 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	15	0.544900-01	0.25503D 01	0.875520 02								
15	15	0.544900-01	0.25503C 01	0.875520 02	0.25890 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	16	0.577420-01	0.26253D 01	0.874800 02								
16	16	0.577420-01	0.26253D 01	0.874800 02	0.26640 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	17	0.610880-01	0.27002D 01	0.874080 02								
17	17	0.610880-01	0.27002D 01	0.874080 02	0.27390 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	18	0.645280-01	0.27752D 01	0.873360 02								
18	18	0.645280-01	0.27752D 01	0.873360 02	0.28140 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	19	0.680630-01	0.28501D 01	0.872640 02								
19	19	0.680630-01	0.28501D 01	0.872640 02	0.28890 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	20	0.716910-01	0.29251D 01	0.871920 02								
20	20	0.716910-01	0.29251D 01	0.871920 02	0.29640 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	21	0.754140-01	0.30000D 01	0.871200 02								
21	21	0.754140-01	0.30000D 01	0.871200 02	0.31090 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	22	0.954730-01	0.32153D 01	0.82280D 02								
22	22	0.954730-01	0.32153D 01	0.82280D 02	0.33260 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	23	0.133540 00	0.34282D 01	0.77440D 02								
23	23	0.133540 00	0.34282D 01	0.77440D 02	0.35420 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	24	0.189430 00	0.36370D 01	0.726000 02								
24	24	0.189430 00	0.36370D 01	0.726000 02	0.37580 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	25	0.262750 00	0.38405D 01	0.677600 02								
25	25	0.262750 00	0.38405D 01	0.677600 02	0.39750 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	26	0.352970 00	0.404370D 01	0.629200 02								
26	26	0.352970 00	0.404370D 01	0.629200 02	0.41910 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	27	0.459450 00	0.42252D 01	0.580830 02								
27	27	0.459450 00	0.42252D 01	0.580830 02	0.44070 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	28	0.581420 00	0.44037D 01	0.53240D 02								
28	28	0.581420 00	0.44037D 01	0.53240D 02	0.46230 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	29	0.718030 00	0.45713D 01	0.48400D 02								
29	29	0.718030 00	0.45713D 01	0.48400D 02	0.48400 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	30	0.868290 00	0.47268D 01	0.43564D 02								
30	30	0.868290 00	0.47268D 01	0.43564D 02	0.50560 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	31	0.103110 01	0.48691D 01	0.387200 02								
31	31	0.103110 01	0.48691D 01	0.387200 02	0.52720 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	32	0.120540 01	0.49971D 01	0.338800 02								
32	32	0.120540 01	0.49971D 01	0.338800 02	0.54890 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	33	0.138990 01	0.51100D 01	0.29040D 02								
33	33	0.138990 01	0.51100D 01	0.29040D 02	0.57050 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	34	0.158320 01	0.52068D 01	0.242400 02								
34	34	0.158320 01	0.52068D 01	0.242400 02	0.59210 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	35	0.17840D 01	0.528710 01	0.19360D 02								
35	35	0.17840D 01	0.528710 01	0.19360D 02	0.61380 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	36	0.199080 01	0.53501D 01	0.14520D 02								
36	36	0.199080 01	0.53501D 01	0.14520D 02	0.63540 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	37	0.22022D 01	0.53954D 01	0.968000 01								
37	37	0.22022D 01	0.53954D 01	0.968000 01	0.65700 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	38	0.24167D 01	0.54227D 01	0.484000 01								
38	38	0.24167D 01	0.54227D 01	0.484000 01	0.67860 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	39	0.26328D 01	0.54319D 01	0.-222640-13								
39	39	0.26328D 01	0.54319D 01	0.-222640-13	0.69700 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	40	0.27750D 01	0.54400D 01	0.0								
40	40	0.27750D 01	0.54400D 01	0.0	0.69700 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	41	0.29250D 01	0.54440D 01	0.0								
41	41	0.29250D 01	0.54440D 01	0.0	0.72700 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	42	0.30750D 01	0.54440D 01	0.0								
42	42	0.30750D 01	0.54440D 01	0.0	0.74200 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	43	0.32250D 01	0.54440D 01	0.0								
43	43	0.32250D 01	0.54440D 01	0.0	0.77200 01	0.12500 00	0.1000 08	0.1000 08	0.375D 07	0.333	0.09420	
	44	0.36750D 01	0.54440D 01	0.0								
44	44	0.36750D 01										

Example Problem 3

For illustrative purposes, a cylindrical shell (Fig. 14) with a stiffening ring at its midpoint has been selected as the third example. The input data for this shell should serve to illustrate many of the features of the code. In particular, the procedure used for a variable thickness shell will be demonstrated along with the option for inputting the nodal point geometry at each individual node.

To demonstrate these input procedures the cylinder will be idealized using nine elements: four on each side of the ring, and one containing the ring. If this shell were to actually be analyzed, many more elements would obviously be necessary. The elements on each side of the ring are considered to be five inches in length (s-direction) and one-eighth inch thick while the element for the stiffener is three inches long and one-fourth inch thick.

Two sets of input data are presented in Figures 15 and 16. The first set inputs separately the thickness of each element and the geometry for each node. The second data set effectively employs the program capabilities and inputs the thickness and geometry for the three segments of the cylinder.



SHELL DESCRIPTION

$D = 10$ in.
 $z_1 = 20$ in.
 $z_2 = 3$ in.
 $t_1 = 0.125$ in.
 $t_2 = 0.250$ in.

MATERIAL PROPERTIES
STEEL

$E = 30.0 \times 10^6$ psi
 $G = 11.55 \times 10^6$ psi
 $\nu = 0.3$
 $\rho = 0.289$ lb/in.³

ELEMENT BREAKDOWN

Segment 1 - 4 elements
 Segment 2 - 1 element
 Segment 3 - 4 elements

Fig. 14 STIFFENED CYLINDRICAL SHELL

NCASE= 3

PRINTOUT OF INPUT DATA

CARD	TYPE	10	20	30	40	50	60	70	80
II - A	6	4							
- B	*****	EXAMPLE PROBLEM NO. 3 *****	SAMSOR	USER'S	MANUAL				
- B	*****	THIS EXAMPLE DEMONSTRATES THE PROCEDURE USED TO SPECIFY VARIABLE							
- B	*****	THICKNESSES AND ALSO SHOWS THE PROCEDURE FOR SPECIFYING THE GEOMETRY OF							
- B	*****	EACH NODE OF THE IDEALIZED SHELL							
- B	*****	*****							
III	9	5	1						
IV	1	9	3000000.	30000000.	11550000.	0.3	0.289		
V	1	4	0.125						
V	5	5	0.250						
V	6	9	0.125						
VI - A	1	0.0	5.0	0.0	0.0				
- B	2	5.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	2	5.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	3	10.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	3	10.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	4	15.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	4	15.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	5	20.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	5	20.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	6	23.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	6	23.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	7	28.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	7	28.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	8	33.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	8	33.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	9	38.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0.0	0.0	0.0	0.0	0.0	0.0
- A	9	38.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- B	10	43.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0
- C	1	1	1.0	0	0.0	0	0.0	0	0.0
VII	END OF CASE								

Fig. 15 INPUT DATA (SET #1) EXAMPLE PROBLEM 3

NCASE= 4

CARD

CARD	TYPE	10	20	30	40	50	60	70	80
III - A	6	4							
- B	*****	*****	*****	*****	*****	*****	*****	*****	*****
- B	EXAMPLE PROBLEM NO.	3	SAMMSON USER'S MANUAL						
- B	THIS EXAMPLE DEMONSTRATES THE PROCEDURE USED TO SPECIFY VARIABLE								
- B	THICKNESSES AND SHOWS THE MOST EFFICIENT PROCEDURE FOR SPECIFYING THE								
- B	GEOOMETRY OF THE IDEALIZED SHELL								
- B	*****	*****	*****	*****	*****	*****	*****	*****	*****

III	9	5	1	9	30000000.	30000000.	11550000.	0.3	0.289
IV	1	4	0	125					
V	1	5	0	250					
V	5	5	0	250					
V	6	9	0	125					
VI	A	1	0	0	5.0	0.0			
- B	5	20.0	5.0	0.0					
- C	1	4	1.0	0	0.0	0			
- A	5	20.0	5.0	0.0					
- B	6	23.0	5.0	0.0					
- C	1	1	1.0	0	0.0	0			
- A	6	23.0	5.0	0.0					
- B	10	43.0	5.0	0.0					
- C	1	4	1.0	0	0.0	0			
VII	END OF CASE								

Fig. 16 INPUT DATA (SET #2) EXAMPLE PROBLEM 3

REFERENCES

1. Stricklin, J. A., Navaratna, D. R., and Pian, T. H. H., "Improvements on the Analysis of Shells of Revolution by the Matrix Displacement Method," AIAA Journal, Vol. 4, No. 11, Nov. 1966, pp. 2069-2072.
2. Mebane, P. M., "An Improved Shell of Revolution Element Utilizing Cubic Displacement Functions," Masters Thesis, Texas A&M University, Aug. 1970.
3. Stricklin, J. A., Haisler, W. E., MacDougall, H. R., and Stebbins, F. J., "Nonlinear Analysis of Shells of Revolution by the Matrix Displacement Method," AIAA Journal, Vol. 6, No. 12, Dec. 1968, pp. 2306-2312.
4. Stricklin, J. A., Martinez, J. E., Tillerson, J. R., Hong, H. H., and Haisler, W. E., "Nonlinear Dynamic Analysis of Shells of Revolution by Matrix Displacement Method," Report 69-77, Aerospace Engineering Department, Texas A&M University, Feb. 1970.
5. Percy, J. H., Pian, T. H. H., Klein, S., and Navaratna, D. R., "Application of Matrix Displacement Method to Linear Elastic Analysis of Shells of Revolution," AIAA Journal, Vol. 3, No. 11, Nov. 1965, pp. 2138-2145.
6. Pian, T. H. H., "Derivation of Element Stiffness Matrices," AIAA Journal, Vol. 2, No. 3, March 1964, pp. 576-577.
7. Novozhilov, V. V. Foundations of the Nonlinear Theory of Elasticity, Graylock Press, Rochester, N. Y., 1956.

APPENDIX

Appendix 1 Description of SAMMSOR II Subroutines

Subroutine	Description
MAIN	Controls the flow of the program by calling the other subroutines to both obtain the structural stiffness and mass matrices for the shell and prepare the input tape for use in the other compatible programs.
INPUT	Reads input data and program control parameters and prints a description of the idealized structure.
SLOCOR	Reads coordinates of shell segments and controls the calculation of the z, r, ϕ coordinates for the specified element breakdown.
FLAT	Calculates the z, r, ϕ nodal coordinates for a shell segment with a linear profile.
CIRCUL	Calculates the z, r, ϕ nodal coordinates for shell segment with a circular profile.
PARABO	Calculates the z, r, ϕ nodal coordinates for a shell segment with a parabolic profile.
FUS	Used by subroutine PARABO to calculate arc lengths for the elements of the segment.
ELEMCA	Calculates geometrical parameters i.e., $r, \phi, \phi', \phi'', \sin\phi, \cos\phi$, etc. for each element between the nodal points. In addition, this subroutine calculates the transformation matrix $[A]$ which relates the shell generalized coordinates, q_i , to the generalized coefficients, α_i , of the displacement functions.
CRETAL	Calculates the values of integrals in the meridional direction which are to be used in calculating the terms in the mass and stiffness matrices.

Appendix 1 Continued

Subroutines	Description
CREATL	Evaluates the element stiffness matrices based on generalized coefficients. The element stiffness matrices are condensed in this subroutine.
CREMAS	Controls the calculation of the element mass matrices according to harmonic number.
AZERO	Generates the element mass matrices based on generalized coefficients for the zero harmonic only.
NONAB	Generates the element mass matrices based on generalized coefficients for harmonics other than zero.
MMPLT3	Premultiplies the element mass and stiffness matrices based on generalized coefficients by $[A]^t$ and post-multiplies by $[A]$ to form the element stiffness and mass matrices $[k]$ and $[m]$
SIMP	Evaluates the integral of a given function using Simpson's integration.
ASEMBL	Assembles element stiffness and mass matrices to form structural stiffness and mass matrices, $[K]$ and $[M]$, for each harmonic.

Appendix 2 Glossary of Significant FORTRAN Variables in SAMMSOR II

Variable	Subroutine where variable is defined or calculated	Description
AK	MMPLT3	Element stiffness matrix [k]
AKK	MMPLT3	Element mass matrix, [m]
AL	CRETAL	Integral of functions used in the [L] and [EMASS] matrices.
AM	ELEMCA	Matrix $[B]^{-1}$ which relates the generalized α coordinates to the generalized shell co-ordinates.
AR	ELEMCA	Matrix of the radial coordinates, r, of the NET stations between the nodes of an element.
ARCL	ELEMCA	Arc length of an element (s-direction).
AS	ELEMCA	Matrix of the meridional distances, s, of the NET stations between the nodes of an element.
CHECK	ELEMCA	Matrix [A], which relates the shell generalized coordinates to the generalized coefficients of the displacement functions.
COMENT	INPUT	Alphanumeric data printed as output for problem identification.
COSINE	ELEMCA	Matrix whose elements are the cosine of ϕ for NET stations along the element.
E1	INPUT	Matrix of Young's Moduli in the meridional direction, E_s
E2	INPUT	Matrix of Young's Moduli in the circumferential direction, E_θ
EMASS	CREMAS	Element mass matrix based on generalized coefficients.

Appendix 2 Continued

Variable	Subroutine where variable is defined or calculated	Description
F	CREATL	Element stiffness matrix based on generalized coefficients.
FNU1	INPUT	Poisson's Ratio, $\nu_{S\theta}$
FNU2	INPUT	Poisson's Ratio, $\nu_{\theta S}$
G	INPUT	Shear Modulus, G [for an isotropic material G = E/2(1+ν)].
IA	INPUT	Total number of harmonics for which the mass and stiffness matrices are to be determined.
ICLASS	SLOCOR	Designates the type of profile for a given segment of the shell.
NCARDS	INPUT	Number of comment cards used for problem identification.
ND	MAIN	Logical unit number of the binary scratch tape on which the input data is stored.
NELEMS	INPUT	Total number of elements used to idealize the structure.
NELEMT	SLOCOR	Element number of the first element of a segment.
NEQ	INPUT	Number of equilibrium equations (degrees of freedom) per harmonic.

Appendix 2 Continued

Variable	Subroutine where variable is defined or calculated	Description
NET	INPUT	Number of Simpson's integration stations used over the meridional length of the shell elements. NET is set equal to 29 in the program.
NH	INPUT	Total number of harmonics for which the mass and stiffness matrices are to be determined.
NNODES	INPUT	Total number of nodes, equal to NELEMS + 1.
NS	MAIN	Logical unit number of a binary scratch tape.
NSIZE	INPUT	The number of terms in the structural stiffness or mass matrix (in vector form) for a particular harmonic.
NT	INPUT	Logical unit number of the tape on which stiffness and mass matrices will be stored.
PHI1	SLOCOR	Slope of the shell at the first node of a segment.
PHI2	SLOCOR	Slope of the shell at the last node of a segment.
PHIMAT	ELEMCA	Matrix [Ψ] which relates the generalized shell coordinates for an element to the global or cylindrical coordinates of the structure.
PHP	ELEMCA	$d\phi/ds$ for NET stations along an element.
PHPP	ELEMCA	$d^2\phi/ds^2$ for NET stations along the element (constant).
PHPRIM	ELEMCA	$d\phi/ds$ at the middle of an element.

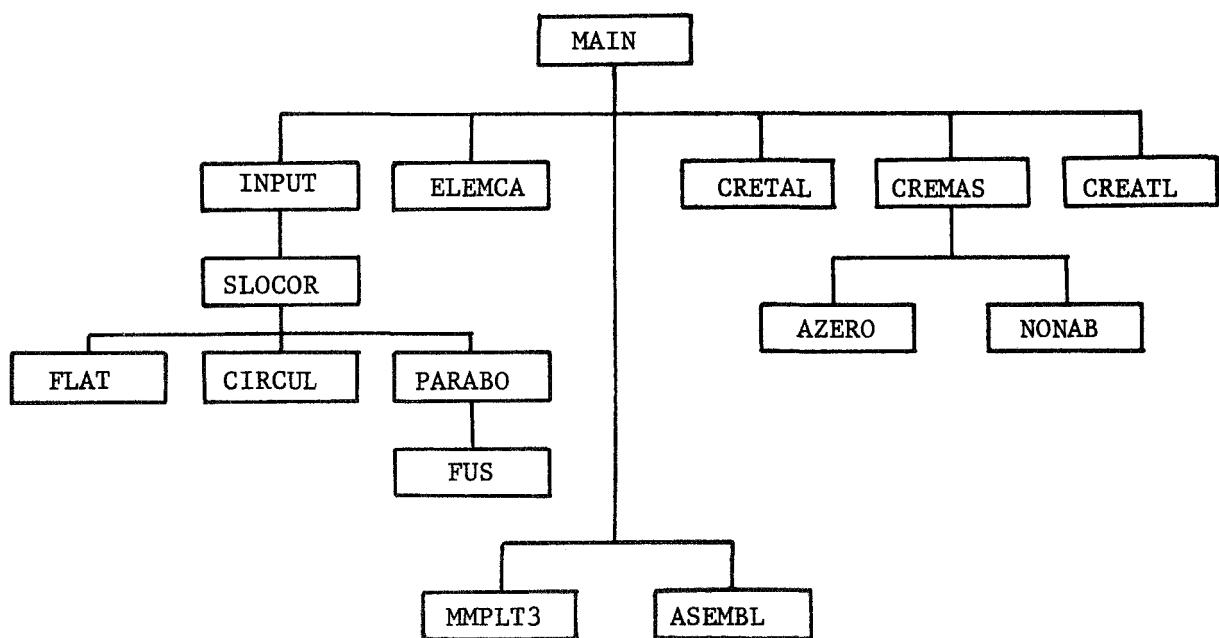
Appendix 2 Continued

Variable	Subroutine where variable is defined or calculated	Description
PHY1	INPUT	Slope at node i of element i.
PHY2	INPUT	Slope at node (i + 1) of element i.
R1	SLOCOR	Radial coordinate of the first node of a segment.
R2	SLOCOR	Radial coordinate of the last node of a segment.
RA	SLOCOR	Decimal fraction corresponding to the lengths of the sub-segments into which a segment is being divided.
RHOS	INPUT	Matrix of the material densities of the elements, lbs/in ³
R01	INPUT	Radial coordinate of node i for element i.
R02	INPUT	Radial coordinate of node (i+1) for element i.
SINE	ELEMCA	Matrix whose elements i are the sine of ϕ for the NET stations along the element.
STIFM	ASEMBL	Structural stiffness matrix, [K], for a given harmonic.
THICK	INPUT	Matrix of element thicknesses.
TMASS	ASEMBL	Structural mass matrix, [M], for a given harmonic.
Z1	INPUT	Axial coordinate of node i for element i.
Z2	INPUT	Axial coordinate of node (i+1) for element i.
Z1C	SLOCOR	Axial coordinate of the first node of a segment.

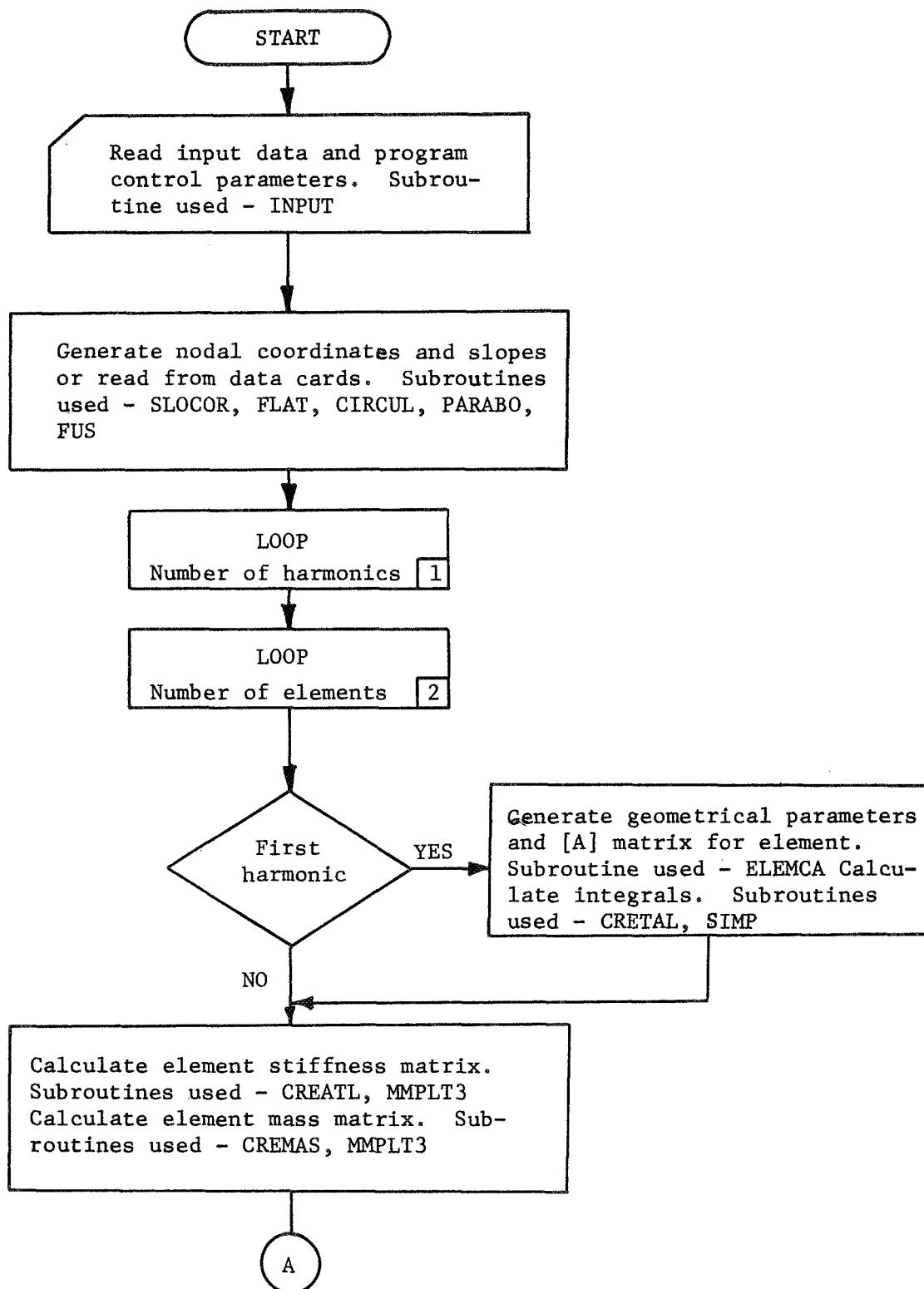
Appendix 2 Continued

Variable	Subroutine where variable is defined or calculated	Description
Z2C	SLOCOR	Axial coordinate of the last node of a segment.

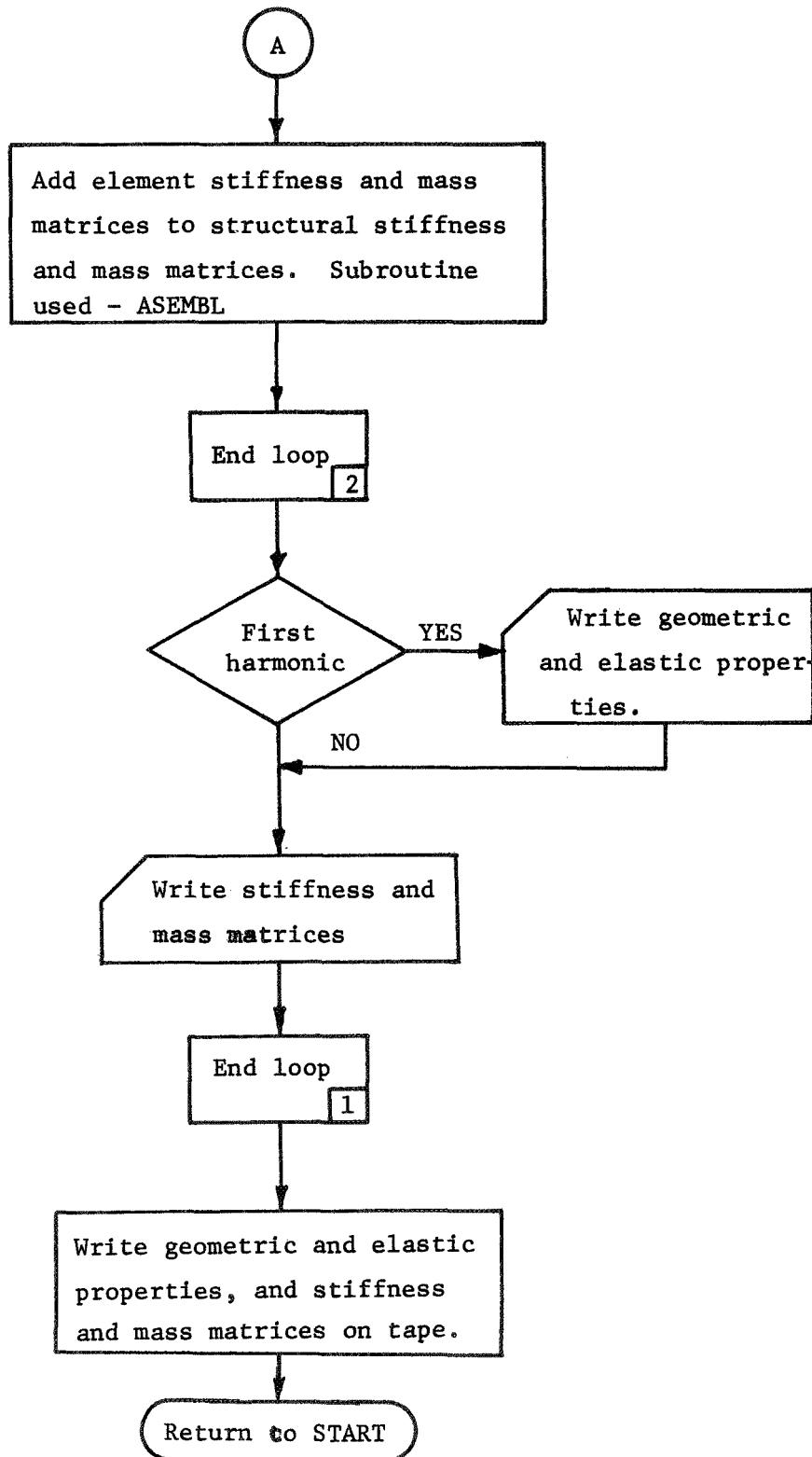
Appendix 3 Subroutine Call Map SAMMSOR II



Appendix 4 Flow Chart of Basic Operations SAMMSOR II



Appendix 4 Continued



Appendix 5 Program Output

The output for the SAMMSOR code consists basically of four parts:

1. The input data for all cases comprising the run.
2. Alphanumeric data used for case identification.
3. Listing of the element properties and nodal point geometry.
4. The upper half of the diagonal band of the stiffness and mass matrices for each harmonic (if desired).

Section 2-4 are repeated for each of the cases of the run.

The output of part 1 is extremely helpful to the user since the input data for all cases is printed at the start of a run. If an error occurs in the program as a result of an error in the input data, then this printout should readily show the source of the error.

The comments of the user which describe or identify the case or problem considered are printed in the second section of the output. This information is stored on the output tape and is also printed as identifying data in the other SOR programs.

The fourth part of the output lists the lower half of the diagonal band of the structural stiffness and mass matrices. The program output and the vector form of storage used in the program contain only those terms within the band of the matrix which are on or above the diagonal. One line of output is printed for each degree of freedom when writing the stiffness and mass matrices. The last term on a particular line of output is the diagonal term corresponding to the degree of freedom. The terms which appear to the left of this diagonal term are the terms on the row (corresponding to the degree of freedom) which are within the

band of the matrix. In other words, the terms for the stiffness matrix of a particular harmonic with N degrees of freedom would appear as shown in Fig. A5-1. As is shown in Fig. A5-1, the maximum number of nonzero terms which appears in any row of the banded matrix is eight (8).

Terms whose value is zero will appear on the diagonals in the printout of the stiffness and mass matrices for harmonic zero. These terms correspond to the V-direction displacements which are identically zero for this harmonic. Since diagonal terms of zero value cause problems when solving a system of equations, these diagonal terms are set equal to one in the analysis programs to provide equations of the form

$$(1.0)q_n = 0.0$$

In addition to the four major parts of the printout, several checks have been included which generate output remarks if an error is encountered.

K_{11}								
K_{21}	K_{22}							
K_{31}	K_{32}	K_{33}						
K_{41}	K_{42}	K_{43}	K_{44}					
K_{51}	K_{52}	K_{53}	K_{54}	K_{55}				
K_{61}	K_{62}	K_{63}	K_{64}	K_{65}	K_{66}			
K_{71}	K_{72}	K_{73}	K_{74}	K_{75}	K_{76}	K_{77}		
K_{81}	K_{82}	K_{83}	K_{84}	K_{85}	K_{86}	K_{87}	K_{88}	
K_{95}	K_{96}	K_{97}	K_{98}	K_{99}				
$K_{10,5}$	$K_{10,6}$	$K_{10,7}$	$K_{10,8}$	$K_{10,9}$	$K_{10,10}$			
-	-	-	-	-	-	-	-	
$K_{12,5}$	-	-	-	-	-	-	-	$K_{12,12}$
$K_{13,9}$	$K_{13,10}$	$K_{13,11}$	$K_{13,12}$	$K_{13,13}$				
-								
-								
-								
-								
-								
$K_{N,N-7}$	$K_{N,N-6}$	-	-	-	-	-	-	$K_{N,N}$

Fig. A5-1 Banded Stiffness Matrix Output Format

Appendix 6 Modification of Program Capacity

The procedure for modifying the maximum number of elements which can be utilized in the SAMMSOR code is presented in this section. With only one exception, the modifications consist of changing only DIMENSION and COMMON statements. The following terms are defined to facilitate the modifications:

NE = Maximum number of elements

N1 = (26 * NE) + 10

N2 = 6 * NE

Having calculated these constants for the desired maximum number of elements, the following cards in the specified subroutines must be changed by substituting the values of the above constants.

Main Program

```
COMMON /B2/ R01(NE), R02(NE), Z1(NE), Z2(NE), PHY1(NE), PHY2(NE)
COMMON /B3/ E1(NE), E2(NE), FNU1(NE), FNU2(NE), G(NE), THICK(NE),
RHOS(NE)
COMMON /B21/ F(8,8), AK(8,8), STIFM(N1)
COMMON /B30/ EMASS(8,8), AKK(8,8), TMASS(N1)
DIMENSION XZ(N2), COMENT(20), JUNK(20), CARD(20), SL(NE)
```

Subroutine INPUT

```
*COMMON /B2/
*COMMON /B3/
COMMON /B13/ SS(NE)
```

*Elements in this block are previously shown.

**NELMAX = NE

Subroutine SLØCØR

DIMENSION RA(5), NERAT(5), RØ1(NE), RØ2(NE), Z1(NE), Z2(NE),
PHII1(NE), PHII2(NE)

Subroutines FLAT, CIRCUL, and PARABØ

DIMENSION RØ1(NE), RØ2(NE), Z1(NE), Z2(NE), PHII1(NE), PHII2(NE)

Subroutine ELEMCA

*CØMMØN /B2/

*CØMMØN /B3/

*CØMMØN /B13/

Subroutine CRETAL

***CØMMØN /B3/

Subroutine AZERØ and NONAB

*CØMMØN /B3/

*CØMMØN /B30/

Subroutines MMPLT3 and ASEMBL

DIMENSIØN F(8,8), AK(8,8), STIFM(N1)

** This is the only card that must be changed which is not a CØMMØN or
DIMENSIØN statement.

***Replace G(NE) by GG(NE) in this block.

Appendix 7 Coding Sheet for Input Data

SHELL DESCRIPTION and comments	Status: Operational Deleted To be deleted on _____, _____
	DATA SET NAME/NUMBER _____ DATE CREATED _____ CREATED BY _____
	SAMMSOR VERSION DOUBLE/SINGLE PREC. _____
CARD TYPE	INPUT DATA
II - A NCARDS NT (2I5)	_____
- B DESCRIPTIVE COMMENTS (20A4)	_____ _____ _____ _____
III NELEMS IA NPRNMS (3I5)	_____
IV IELM1 IELM2 EE1 EE2 GG FFNU1 RHO (2I5,5F10.0)	_____ _____ _____
V IELM1 IELM2 THICKNESS (2I5, F10.0)	_____ _____ _____

Appendix 7 Continued

VI SHELL GEOMETRY

- A NN1 Z R ϕ (I5, 3F10.0)

- B NN2 Z R ϕ

- C ICLASS NERAT RA NERAT RA NERAT RA NERAT RA NERAT RA
1 1 2 2 3 3 4 4 5 5

A
B
C
A
B
C
A
B
C
A
B
C
A
B
C
A
B
C

VII END OF CASE

***** Add an END OF RUN card at the end of the final case

***** Add a Card I at the start of the first data set: This card contains NCASES,
ND, NS, and NS2 -- in that order