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Measurements of π^+p Elastic Scattering from 1.71 to 5.53 GeV/c²

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ABSTRACT

The π^+p elastic scattering differential cross section has been obtained at eighteen incident momenta from 1.71 to 5.53 GeV/c. The measurements were taken over a limited range of squared four-momentum transfer, t , near the forward direction. The statistical accuracy and resolution of these data are comparable to, or better than, existing data. The parameter b in the expression $d\sigma/dt = Ae^{bt}$ has been determined at each of our incident momenta, and a large (~25%) enhancement in b as a function of momentum is observed at a center of mass energy of ~2200 MeV. The relation of this bump in b with the well established bump in the total π^+p cross section at ~2200 MeV is discussed.

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1. INTRODUCTION

In a recent experiment at the Argonne National Laboratory Zero-Gradient-Synchrotron (ZGS), we measured the differential cross section for the elastic scattering of negative pions from deuterium at 2.01, 3.77, and 5.53 GeV/c.¹ To check the acceptance of our apparatus we made measurements of the process $\pi^+p \rightarrow \pi^+p$ over a similar momentum range and compared them with existing π^+p elastic scattering measurements.²⁻⁴ In this paper we present the π^+p measurements. The measurements were made at twelve incident pion momenta in the range from 1.71 to 2.76 GeV/c and also at 3.01, 3.52, 3.77, 4.02, 5.03, and 5.53 GeV/c. The closely spaced 1.71 to 2.76 GeV/c data were taken to help settle the question of what nucleon resonances are present in the mass region of the $N(2190)$.

Our data are in agreement with previous measurements,²⁻⁴ and in the 1.71 to 2.76 GeV/c region have somewhat superior statistical accuracy than previous results. These data coupled with polarization measurements of the same process⁴ have proved useful in providing additional evidence for a nucleon resonance in the $H_{1/2}$ partial wave at a mass value of 2245 MeV. Our data are confined to a limited angular region; in terms of t , the squared four-momentum transfer, the data cover a t interval of approximately -0.2 to -0.7 (GeV/c)².

Section II gives the details of our experimental method. Section III presents the differential cross sections in tabular form, as well as the momentum variation of the parameter b in the expression $d\sigma/dt = Ae^{bt}$. This exponential slope, b , shows about a 25% increase at center of mass energy of 2290 MeV, significantly higher in mass than the well known bump in the π^+p total cross section near 2200 MeV.^{6,7}

III. EXPERIMENTAL METHOD

The experiment was performed in the 17° beam of the ZGS. The beam transport system determined the momentum of the pions to $\pm 1\%$ and brought the beam to a final focus on a 2.31 in.-long liquid-hydrogen target. The beam intensity varied from $(1 \text{ to } 7) \times 10^5$ pions/pulse depending on the beam momentum, with a pulse repetition rate of 1000 pulses/h. The beam angular divergence was ± 5 mrad horizontally and ± 3 mrad vertically. The experimental apparatus used to detect the elastic events is shown in Fig. 1. The pion beam was detected by a series of scintillation counters labeled S_1 , S_2 , S_3 , and S_4 . Counters S_1 and S_2 are not shown in the figure and are located near the first focus of the 17° beam. The beam size was defined by S_4 , a $\frac{3}{4}$ -in. \times $\frac{3}{4}$ -in. counter.

Elastic events were detected in a double-arm spectrometer consisting of the two bending magnets M1 and M2 and scintillation counter arrays A, B, and P. Each of the A and B arrays consisted of 16 elements; the P array consisted of 30 elements. The dimensions for the A, B, and P elements are shown on Fig. 1. Negative particles traversed M1 and were detected by pairs of corresponding A and B elements. The width of an A array element determined the scattering-angle acceptance for each data point. The 16 pairs of corresponding A and B counters allowed 16 simultaneous differential cross sections to be measured. A single scintillation counter G behind the A-array determined the azimuthal angular acceptance. The recoil protons traversed M2 and were detected by the P array. The V1 and V2 counters were used to veto particles which did not satisfy the angular restrictions of $\pi\pi$ elastic-scattering kinematics. The V3 counter was used as an additional

anticoincidence counter to veto beam pions that did not interact in the target. Events satisfying the following electronic coincidence requirements were selected and stored in a multichannel analyzer: (a) a count in beam counters ($S_1 S_2 S_3 S_4$), (b) no count in veto counters ($\bar{V}_1 \bar{V}_2 \bar{V}_3$), (c) a count in corresponding A and B counters in coincidence with a count in any of the P counters, and (d) a count in G. These events were sorted into 16 different groups corresponding to the 16 AB pairs. For each pair the distribution of events along the P array was obtained.

Figure 2 shows some typical data accumulated for a beam momentum of 2.01 GeV/c. There are 16 separate distributions labelled 1 through 16 corresponding to increasing pion scattering angle. In each of the distributions the elastic-scattering events appear as a peak with a background of less than 1%. Since the acceptance of our apparatus varies slowly with angle, one can roughly see in Fig. 2 the variation in the differential cross section as a function of pion scattering angle. Also one can see the variation in the recoil proton direction. The data were displayed in this manner simultaneously with the running of the experiment so that any trouble that developed would have been readily detected. It took 6 hours to accumulate the data shown in Fig. 2. These particular data are all of the data at 2.01 GeV/c. The positions of the elastic peaks agree with predictions of a Monte Carlo simulation of the experiment.

III. RESULTS

The differential cross section is given by the formula

$$d\sigma/dt = \frac{E}{H_p} N \Delta t ,$$

where E is the number of events, N_{π} is the number of incident pions, N_p is the number/cm² of target protons, and Δt is the interval of the squared four-momentum transfer associated with the instrumental solid angle. The number of events was determined from the counts in the elastic peak, the number of beam pions was determined from the number of beam counts, $S_1 S_2 S_3 S_4$, and the number of protons/cm² was determined from a knowledge of the length of the target and the known density of liquid hydrogen at an operating pressure of 1 atm. The solid angle was determined by a straightforward hand calculation and checked independently by a Monte Carlo computer program.

Corrections were applied to the data for muon and electron contamination of the pion beam, for decay of the scattered pion, for electronic deadtime effects due to V1, V2, and V3, and for absorption of particles in scintillators, liquid hydrogen, and other material. The combined correction due to these effects was typical¹¹ of 20%.

Table I lists the eighteen momenta at which the experiment was performed, the t -range covered⁸ at each momentum, and the statistical accuracy of the differential cross sections. The elastic differential cross sections for the eighteen momenta are tabulated in Table II along with their associated errors. The quoted errors are statistical errors associated with event counts only. The relative normalization error between any two of our data sets at different momenta is less than 2%. In addition there is an over-all absolute uncertainty of $\pm 5\%$ to be uniformly associated with all data points.

The present data have been compared with other measurements²⁻⁴ at the same or nearby momenta and are in good agreement. The extent of this

agreement as well as the quality of our data is illustrated in Fig. 3, where we have plotted our data at two momenta and data from other experiments at similar momenta.

In an effort to arrive at a simplified understanding of these cross section measurements we have fit the differential cross sections at each momentum to an expression of the form

$$d\sigma/dt = A e^{bt},$$

a form suggested by a small angle approximation to an optical model of high energy scattering⁹ and employed extensively to parametrize small angle scattering data. A least-squares fitting procedure determined the coefficients A and b at each of the 18 momenta. In order to arrive at reasonable chi-squares, it was necessary to restrict the fit to data points for which $|t| \leq 0.63$ (GeV/c)². Beyond this value of t the differential cross section has a secondary peak or "shoulder" and deviates drastically from a simple exponential dependence on t . The values of b obtained from this procedure are listed in Table III and plotted in the lower half of Fig. 4.

In the upper half of Fig. 4, we have plotted the π^+p total cross section taken from Carter *et al.*⁷ and Citron *et al.*¹⁰ Note the large bump in b (approximately 25%) in the vicinity of the $\sim 8\%$ bump in the total cross section, usually attributed to the $N(2190)$, $J^P = 7/2^-$. The central position of the bump in b is at a value of $P_{LAB} \approx 2.3$ GeV/c while the position of the bump in σ_T is at a value of $P_{LAB} \approx 2.1$ GeV/c. The corresponding center of mass energies at these momenta are ≈ 2290 MeV and ≈ 2200 MeV, respectively. We would like to make the following two points: First, the bump in b

is due to the presence of direct channel resonances. The evidence for the correlation of variations in b with direct channel resonances has been extensively presented by Lasinski, Levi Setti, and Predazzi.¹¹ Second, the shift in the position of the bump from ~ 2200 MeV in σ_T to ~ 2290 MeV in b can be understood in terms of the simple phenomenological model used in Ref. 11. In this model the scattering amplitude at small angles has two contributions, one due to diffraction scattering and the second due to direct channel resonance formation. As a consequence of this model Lasinski et al. demonstrate that resonances of different spin contribute to structure in b with a relative weight which is different than the relative weight with which they contribute to structure in σ_T . For a given resonance elasticity the weighting factor increases with increasing spin more rapidly for b than for σ_T . Therefore, one qualitative explanation for the mass difference in the positions of the bumps is that there are several resonances of different spin in this mass region, and the higher spin resonances have greater mass. A similar, but more precise, conclusion is reached by the authors of Ref. 5. Their detailed examination of our data and polarization data⁴ provides evidence for two nucleon resonances in this energy region: one at 2245 MeV in the H_{19} partial wave, and one at 2260 MeV in the G_{17} partial wave. This latter resonance is the familiar $N(2190)$. As the authors of Ref. 5 demonstrate, the bump in the total cross section at a mass value of 2200 MeV is due to these two high spin resonances plus the $D_{13}(2040)$ resonance.

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Table I. Summary of experiment.

Incident momentum (GeV/c)	$ t $ range covered (GeV/c) ²	Statistical accuracy of data (%)
1.71	0.17-0.37	5.0-6.0
1.81	0.19-0.41	3.0-5.5
1.91	0.24-0.45	3.5-7.0
2.01	0.24-0.49	3.5-8.0
2.09	0.26-0.53	3.5-8.5
2.16	0.27-0.56	2.0-7.0
2.23	0.29-0.60	3.5-15.0
2.31	0.31-0.64	3.5-11.5
2.41	0.34-0.69	3.5-12.5
2.51	0.36-0.74	4.0-13.0
2.62	0.39-0.80	3.0-10.0
2.76	0.43-0.88	5.0-14.0
3.01	0.51-0.88	6.0-10.0
3.52	0.29-0.57	4.5-12.0
3.77	0.24-0.56	4.0-13.0
4.02	0.27-0.55	4.0-9.5
5.03	0.27-0.63	3.5-10.0
5.53	0.28-0.62	3.5-9.5

Table II. π^-p elastic scattering.

$-t$ (GeV/c) ²	$d\sigma/dt$ mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²	$-t$ (GeV/c) ²	$d\sigma/dt$ mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²
	1.71 GeV/c				
0.177	17.87	0.99	0.289	7.62	0.28
0.188	16.10	0.91	0.303	6.26	0.25
0.199	14.61	0.85	0.317	6.05	0.24
0.211	14.15	0.82	0.332	5.06	0.22
0.235	11.88	0.73	0.346	4.78	0.21
0.259	9.36	0.34	0.361	4.14	0.20
0.285	7.29	0.29	0.376	3.73	0.19
0.299	6.63	0.28	0.392	3.54	0.18
0.312	5.95	0.26	0.407	3.09	0.17
0.325	5.64	0.26			
0.339	4.98	0.24		1.91 GeV/c	
0.367	4.16	0.23	0.247	10.12	0.35
			0.260	9.00	0.32
			0.275	7.60	0.29
	1.81 GeV/c		0.290	7.01	0.28
0.197	13.61	0.42	0.304	6.18	0.25
0.210	12.78	0.40	0.320	5.51	0.24
0.222	12.47	0.39	0.335	4.68	0.21
0.235	11.03	0.36	0.351	4.36	0.20
0.248	9.52	0.33	0.367	4.00	0.19
0.262	8.35	0.30	0.383	3.49	0.18
0.275	7.52	0.28	0.400	3.16	0.17

MORE

Table II. (continued)

$-t$ (GeV/c) ²	d_2/dt mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²	$-t$ (GeV/c) ²	d_3/dt mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²
0.587	0.349	0.039	0.444	2.12	0.05
0.611	0.376	0.040	0.468	1.64	0.07
0.637	0.352	0.039	0.494	1.26	0.06
0.661	0.272	0.035	0.520	1.02	0.05
0.685	0.287	0.036	0.546	0.784	0.047
	2.51 GeV/c		0.572	0.680	0.043
0.367	3.66	0.14	0.598	0.548	0.038
0.390	3.03	0.13	0.626	0.435	0.033
0.413	2.44	0.11	0.653	0.407	0.032
0.435	2.02	0.10	0.681	0.297	0.027
0.459	1.60	0.09	0.708	0.262	0.026
0.482	1.28	0.08	0.736	0.287	0.027
0.506	1.10	0.07	0.764	0.276	0.027
0.531	0.839	0.060	0.792	0.285	0.028
0.556	0.600	0.049		2.76 GeV/c	
0.581	0.554	0.047	0.439	1.98	0.10
0.607	0.518	0.045	0.466	1.71	0.09
0.632	0.389	0.039	0.493	1.35	0.08
0.659	0.347	0.037	0.520	0.965	0.063
0.685	0.268	0.033	0.547	0.863	0.059
0.711	0.235	0.031	0.576	0.758	0.054
0.738	0.249	0.032	0.605	0.582	0.047
	2.62 GeV/c		0.633	0.467	0.041
0.39 ^b	3.11	0.10	0.663	0.394	0.037
0.420	2.46	0.09	0.692	0.339	0.034

MORE

Table II. (continued)

$-t$ (GeV/c) ²	d_2/dt mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²	$-t$ (GeV/c) ²	d_3/dt mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²
0.723	0.339	0.034	0.421	2.00	0.14
0.753	0.291	0.032	0.456	1.38	0.11
0.783	0.340	0.034	0.491	1.02	0.10
0.813	0.241	0.029	0.527	0.734	0.078
0.844	0.219	0.028	0.563	0.675	0.076
0.875	0.196	0.027		3.77 GeV/c	
	3.01 GeV/c		0.240	7.60	0.30
0.515	1.20	0.07	0.270	6.45	0.27
0.545	1.00	0.06	0.302	5.52	0.24
0.577	0.755	0.052	0.335	4.13	0.20
0.608	0.611	0.046	0.369	3.26	0.17
0.639	0.496	0.041	0.404	2.47	0.15
0.672	0.435	0.038	0.441	2.01	0.13
0.706	0.364	0.034	0.479	1.17	0.10
0.739	0.334	0.032	0.517	0.757	0.077
0.773	0.283	0.029	0.557	0.536	0.065
0.808	0.266	0.028		4.02 GeV/c	
0.842	0.259	0.027	0.273	6.54	0.26
0.876	0.275	0.028	0.306	4.88	0.22
	3.52 GeV/c		0.342	4.20	0.19
0.294	5.92	0.26	0.379	2.89	0.16
0.324	4.66	0.22	0.417	2.25	0.13
0.355	3.20	0.18	0.457	1.82	0.12
0.388	2.60	0.16	0.499	1.02	0.09
			0.541	0.736	0.074

Table I'. (continued)

$-t$ (GeV/c) ²	dg/dt mb/(GeV/c) ²	Statistical error mb/(GeV/c) ²
5.03 GeV/c		
0.274	5.73	0.18
0.316	4.67	0.15
0.363	3.03	0.12
0.410	2.04	0.09
0.461	1.38	0.08
0.514	0.804	0.055
0.570	0.635	0.048
0.627	0.354	0.035
5.53 GeV/c		
0.281	5.28	0.16
0.328	4.11	0.14
0.379	2.62	0.11
0.434	1.94	0.09
0.492	1.16	0.07
0.553	0.692	0.049
0.614	0.385	0.036

Table III. Parameter b in $dg/dt = Ae^{bt}$, from a fit to the present data for t values $|t| \leq 0.63$ (GeV/c)²

Beam momentum (GeV/c)	Number of data points	χ^2	b (GeV/c) ⁻²
1.71	12	6.2	7.91 ± 0.25
1.81	16	16.5	7.30 ± 0.16
1.91	14	7.0	7.76 ± 0.21
2.01	16	23.2	8.02 ± 0.16
2.09	16	21.6	8.55 ± 0.16
2.16	16	17.2	9.08 ± 0.11
2.23	15	4.9	9.24 ± 0.21
2.31	15	6.7	9.06 ± 0.18
2.41	13	11.6	9.63 ± 0.21
2.51	11	7.2	8.81 ± 0.24
2.62	10	4.4	8.73 ± 0.22
2.76	7	5.1	7.53 ± 0.44
3.01	4	0.3	7.40 ± 0.96
3.52	9	5.4	8.64 ± 0.28
3.77	10	28.6	7.77 ± 0.21
4.02	8	12.0	7.70 ± 0.25
5.03	8	12.9	7.93 ± 0.17
5.53	7	13.2	7.50 ± 0.18

FIGURE CAPTIONS

Fig. 1. Plan view of experimental apparatus. The pion beam is incident from the left on a hydrogen target. The scattered pions pass through magnet M1, and counter arrays A and B and are detected in coincidence with recoil protons in the side array P.

Fig. 2. A typical raw data run. The beam momentum is 2.01 GeV/c and the total number of incident pions is 20×10^8 . There are 16 event distributions shown in the figure; increasing number means increasing pion scattering angle. The elastic events form a well-defined peak with a background of less than 1%.

Fig. 3. Comparison of our data with data from other experiments near 2.5 GeV/c and 2.1 GeV/c.

Fig. 4. In the lower portion: slope parameter b versus laboratory beam momentum; in the upper portion: total π^+p cross section versus laboratory beam momentum. The values of b plotted are taken exclusively from this experiment. The values of σ_T plotted are taken from Carter *et al.*, Ref. 7; and Citron *et al.*, Ref. 10.

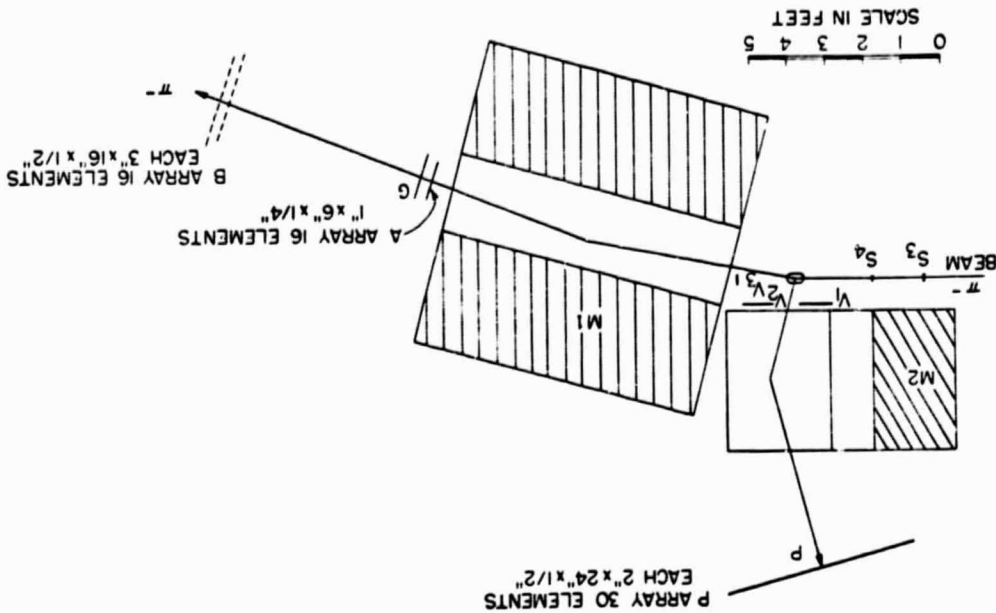


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π -P \rightarrow π -P
 2.0 GeV/c
 $\pi = 20.0 \times 10^8$

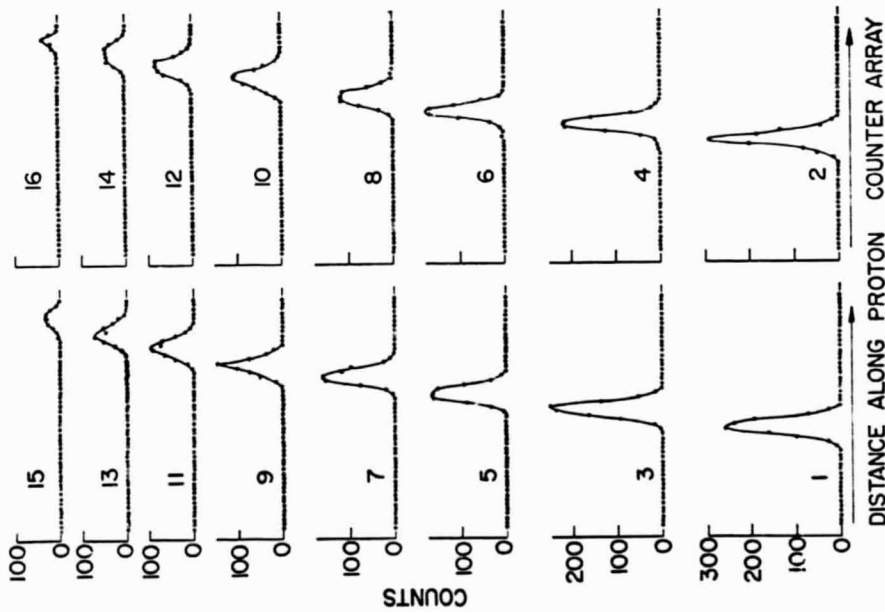


Fig. 2. A typical raw data run. The beam momentum is 2.0 GeV/c and the total number of incident pions is 20×10^8 . There are 16 event distributions shown in the figure; increasing number means increasing pion scattering angle. The elastic events form a well-defined peak with a background of less than 1%.

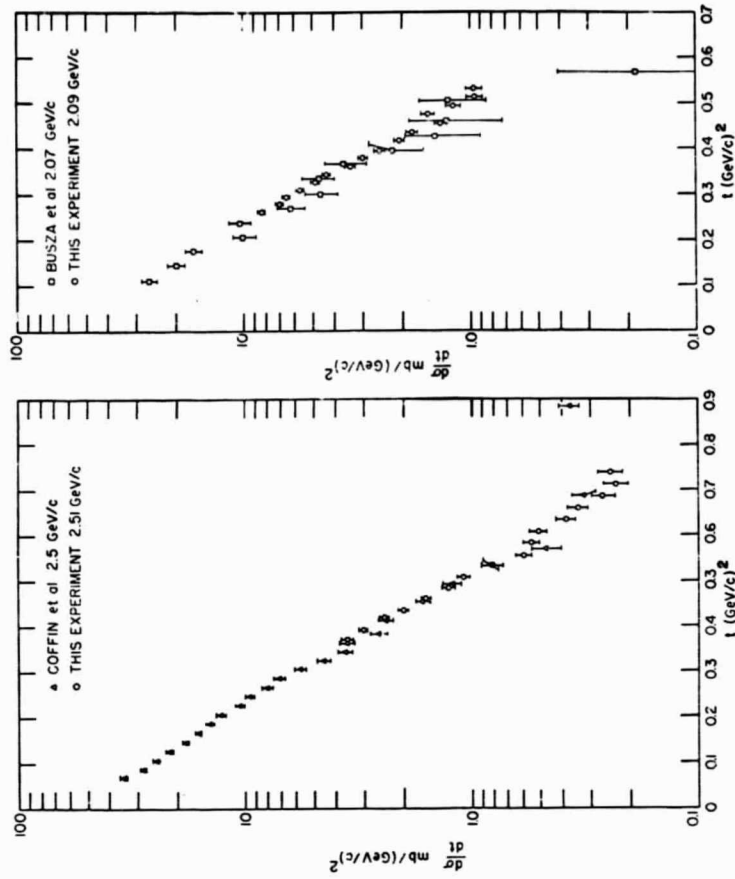


Fig. 3. Comparison of our data with data from other experiments near 2.5 GeV/c and 2.1 GeV/c.

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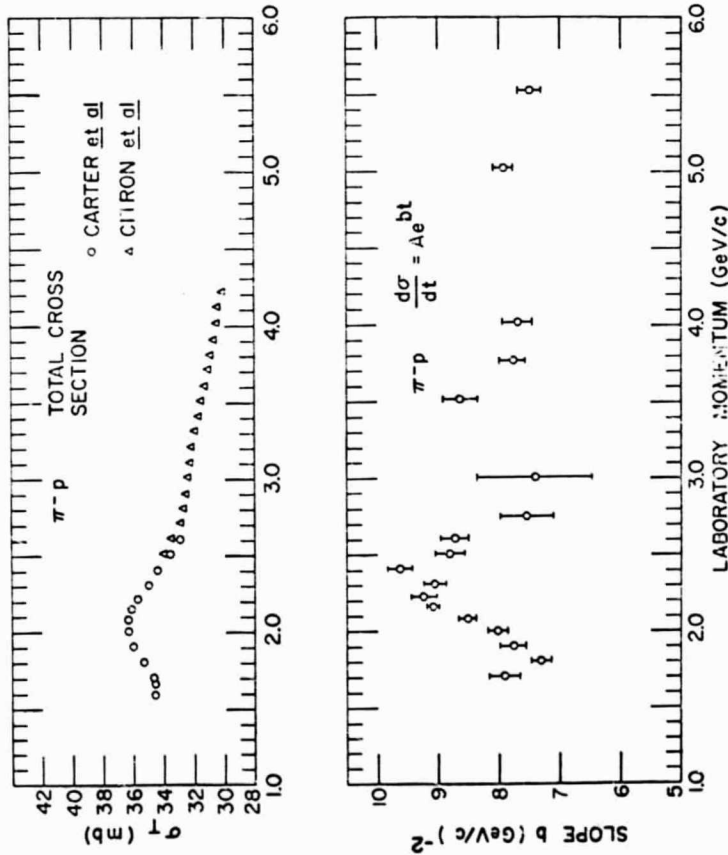


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