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Summary Report

USERS' MANUAL FOR THE SIMULATED LIFE ANALYSIS OF VEHICLE ELEMENTS (SLAVE) MODEL

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SUMMARY REPORT
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USERS' MANUAL FOR THE SIMULATED
LIFE ANALYSIS OF VEHICLE ELEMENTS (SLAVE) MODEL

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Prepared For

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ABSTRACT

The Simulated Life Analysis of Vehicle Elements (SLAVE) Model described in this report was designed to perform statistical simulation studies for any constant loss rate. The outputs of the model consist of the total number of stages required, stages successfully completing their lifetime, and average stage flight life.

This report contains a complete description of the SLAVE Model. Users' instructions and interpretation of input and output data are presented such that a user with little or no prior programming knowledge can successfully implement the program.

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DEFINITION OF SYMBOLS

CPU	Central Processing Unit
N	Number of simulations to be performed
SLAVE	Simulated Life Analysis of Vehicle Elements
URAND	Pseudo Random Number Generator
\bar{X}	Mean (average) value
X_i	Parameter obtained from a single simulation of one program life
σ	One standard deviation

SECTION I. INTRODUCTION

This report contains a complete description of the Simulated Life Analysis of Vehicle Elements (SLAVE) computer model. The SLAVE Model is written in Fortran and was developed to provide data for the Shuttle booster concept selection. A detailed report of previous SLAVE Model usage is contained in Reference 1.

The primary use of the SLAVE Model is anticipated to be related to the Shuttle program, therefore the technical terms used in this report are associated with that program. The SLAVE Model described in this report may be used to obtain statistics for any piece of equipment that has a constant probability of loss. It should be noted that the equipment need not be restricted to the Shuttle program.

The SLAVE Model performs statistical simulation studies that require as input the following parameters:

- Random number generator seed
- Constant percentage loss rate
- Maximum stage lifetime.

The SLAVE Model generates the following output information:

- Total number of stages required
- Number of stages successfully completing their lifetime
- Number of stages failing to complete their lifetime
- Average flight life of all stages.

The above parameters are output as average values. The parameters also appear in histograms as data points which represent each program simulated. These histograms can be used to determine the range over which the output parameters may vary.

SECTION II. GUIDELINES AND ASSUMPTIONS

The guidelines and assumptions that were necessary to develop and utilize the SLAVE Model are as follows:

- The probability of loss for each flight is independent of previous flights
- One stage is used until it is lost or has completed its designed lifetime
- A new stage is immediately available when needed.
- The probability of losing a stage on any individual flight is a constant
- Each new stage performs at least one flight
- The mean (average) values referred to in this report are calculated by use of:

$$\bar{X} = \frac{\sum_{i=1}^N X_i}{N}, \quad (1)$$

where

N = number of simulations to be performed

X_i = parameter obtained from a single simulation of one program life

\bar{X} = mean (average) value

- The two sigma (σ) value is the number of stages necessary to accomplish approximately 97 percent of the flight program.

Program modifications and additional guidelines and assumptions are required when the SLAVE Model is used for distributions that do not have a constant probability of loss. However, the required changes are not included in the context of this report.

The statistical equations and tests used in this report were obtained from Reference 2.

SECTION III. INPUT DATA REQUIREMENTS

A. General Input Information

The SLAVE Model is written for use on a UNIVAC 1108 Digital Computer and requires the standard control cards for that machine. Explanations in this section will be given only for the input parameters and control cards necessary to run a case study. For a detailed explanation of the SLAVE Model see Section VI (Program Definition).

The SLAVE Model requires one data card with five parameter values for each case study. The model is designed to run multiple case studies with one submittal of the job to the UNIVAC 1108 by stacking data cards. The last data card on the stack is a stop control and should contain -999 ending in column 10.

Detailed descriptions of the input parameters required for the SLAVE Model are given below and a brief summary of the input requirements is contained in Table I.

- Parameter No. 1--Random Number Generator Seed

This input parameter is used to start the Pseudo Random Number Generator (URAND). This subroutine generates a uniformly distributed sequence of random numbers in the range of 0.0 to 1.0. The random numbers are used to determine when a stage is lost by comparing a random number with the input parameter that designates the loss rate. The sequence of random numbers generated will always be the same for a particular seed. Therefore, a comparison of different input parameters for identical conditions can be made by using the same seed for each case study in the set. The parameter is located on the data card in columns 1 through 10, with the number required to end in column 10. The number used must be an odd integer not evenly divisible by 5 in the range of 1 to 3435973833, and must not contain a decimal point.

- Parameter No. 2--Constant Percentage Loss Rate

This input parameter designates the stage loss rate to be used throughout the case study. The value used on the data card is to be the exact percentage value desired (not the corresponding decimal equivalent). This input parameter is

TABLE I. DATA CARD SUMMARY

Parameter No.	Description	Data Card Columns	Allowable Values	Ending Column	Decimal Point Required
1	Random Number Generator Seed	1 to 10	1 to 3435973833	10	No
2	Constant Percentage Loss Rate	11 to 20	0.0 or 100.0 or 0.00000001 to 99.999999	20	Yes
3	Maximum Stage Lifetime	21 to 30	1 to value of Parameter No. 5; >Parameter No. 5; <3435973833	30	No
4	Number of Simulations to be Performed	31 to 40	1 to 3435973833 (usually 100)	40	No
5	Number of Missions in One Complete Program	41 to 50	1 to 3435973833	50	No
	Stop Control	7 to 10	-999	10	No

used to determine when a stage is lost by comparing it with a random number. The parameter is located on the data card in columns 11 through 20, with the number ending in column 20. The range can be from 0 to 100 percent with a maximum of 9 significant digits. This parameter should contain a decimal point.

- Parameter No. 3--Maximum Stage Lifetime

This input parameter is used to define the maximum number of flights a stage can make. When a stage has successfully completed the number of flights specified by this input parameter, it is designated as worn out, and a new stage is entered into the system. The number used for a finite maximum flight lifetime must be an integer in the range from one to the value of the fifth parameter on the data card. An infinite flight lifetime can be specified by any integer greater than the fifth parameter on the data card. The maximum stage lifetime parameter is located on the data card in columns 21 through 30, with the number ending in column 30. This parameter must not contain a decimal point.

- Parameter No. 4--Number of Simulations to be Performed

This input parameter is used to establish the number of complete programs to simulate. This parameter should be sufficiently large, usually 100 or greater, to ensure valid statistical output. Each 100 simulations requires approximately 3.6 sec of UNIVAC 1108 Central Processing Unit (CPU) time. This parameter is located on the data card in columns 31 through 40, with the number ending in column 40. This number should be an integer in the range of 1 to 3435973833; however, because of the time required, care should be used in determining the actual size of this parameter. This parameter must not contain a decimal point.

- Parameter No. 5--Number of Missions in One Complete Program

This number should be an integer in the range of 1 to 3435973833. The parameter is located on the data card in columns 41 through 50, with the number ending in column 50. This parameter must not contain a decimal point.

B. Program Deck Instructions

The complete UNIVAC 1108 program deck required to run case studies with the SLAVE Model is described in this section. All cards should be punched exactly as shown, except where otherwise stated. Figure 1 contains a complete listing of the program required to run a

```
@RUN, /PJOBNAME, JOBNUM, NAMExxB1Nxx, T, PAGE  
@ASSG, T TAPE, T, REELNO  
@REWI ND TAPE.  
@COPIN TAPE.  
@XQT SLAVEC  
    11221      20.0      20      100      445  
- 999  
@FIN  
@FIN
```

FIGURE 1. PROGRAM LISTING FOR A SINGLE CASE STUDY UTILIZING THE SLAVE MODEL

single case study that has a 20.0 percent loss rate, a program life of 445 flights, and a maximum vehicle element lifetime of 20 flights. The required substitutions and a brief explanation of each card shown in Figure 1 are as follows:

- @RUN, //P JOBNAM, JOBNUM, NAMExxBINxxx, T, PAGE
This card is an executive control card that tells the computer to schedule your run for initiation, and provide necessary accounting information. The following substitutions to the run card must be made:
 - JOBNAM: A six character name to be assigned to this job
 - JOBNUM: Your UNIVAC 1108 account number
 - NAMExxBINxxx: Your name in six characters and the bin number you want your output returned to in three numerals
 - T: The CPU time you expect your job to require in minutes. This value can be determined by multiplying the number of case studies by 4 sec per 100 simulations and converting to minutes. The number used should be the smallest integer value greater than the above calculation. This number is usually one, two, or three
 - PAGE: The maximum number of output pages your job is allowed to have. This number is usually 200.
- @ASG, T TAPE, T, REELNO
This card is an executive control card that tells the computer which tape is required for this job. The following substitution to the ASG card must be made:
 - REELNO: The current SLAVE tape number. This number may be obtained by contacting Daryl D. Paul, Jr. at Teledyne Brown Engineering Company, telephone 532-1202.
- @REWIND TAPE.
This card is an executive control card that winds the specified tape to the proper starting point. This is done in preparation to copying the SLAVE Model from the tape to the computer.
- @COPIN TAPE.
This card is an executive control card that copies the SLAVE Model from the specified tape to the computer.
- @XQT SLAVEC
This card is an executive control card that tells the computer to begin execution of the SLAVE Model.
- 1 1 2 2 1 2 0 . 0 2 0 1 0 0 4 4 5
This card is a data card that contains the five parameters designated for this case study. If multiple case studies are desired there will be one data card of this type for each case study, located at this point in the deck.

- - 9 9 9

This card is a stop control used by the SLAVE Model to terminate this job submittal.

- @FIN

@FIN

These two cards are executive control cards that signify the end of this control deck.

SECTION IV. OUTPUT DATA INTERPRETATION

An explanation of the output data obtained from a typical case study that utilizes the SLAVE Model is contained in this section. The results of each case study are presented by two basic output formats. The first output format contains the study conditions and the average value of five parameters. The second output format appears four times per case study. This format contains a histogram and information associated with the histogram.

The example output presented in this section is the result of the input deck shown in Figure 1. The first output format is presented in Figure 2 and is interpreted as follows:

- RANDOM NUMBER SEED 11221
When several case studies are to be compared this number should be the same for each case study. This ensures that the parameters being tested are operating under identical conditions.
- NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM 445
The number of flights defined for the NASA Shuttle Traffic Model. This model is currently defined as 445 flights.
- NUMBER OF COMPLETE PROGRAMS SIMULATED 100
This example problem makes 100 simulations of a 445 flight program.
- MAXIMUM STAGE LIFETIME 20
Defines the maximum number of flights one stage may make before being discarded as worn-out. If this number is greater than the number of flights in one complete program, the maximum stage lifetime is infinite for that program. This program allows a stage to fly a maximum of 20 times.
- LOSS RATE (PERCENT) 20.000
The probability of losing a stage on each flight--the probability of losing a stage in this case study is 20 percent per flight.
- AVERAGE NUMBER OF STAGES REQUIRED 90.14000
The average number of stages required to complete the 445 flight program. This value is the average obtained from 100 individual simulations of the 445 flight program.

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	445
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	20
LOSS RATE (PERCENT)	20.000
AVERAGE NUMBER OF STAGES REQUIRED	90.14000
AVERAGE STAGE LIFE	4.98430
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	1.08000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	88.31000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.75000

FIGURE 2. CASE STUDY CONDITIONS AND AVERAGE DATA

- AVERAGE STAGE LIFE 4.98430
The average number of flights each stage performed. This value is obtained by determining the average flight life for each program and then averaging over the number of simulations performed.
- AVERAGE NUMBER OF STAGES WHICH WEAR OUT 1.08000
The number of stages that wear out and are discarded is determined for each program. The average is then calculated from these values.
- AVERAGE NUMBER OF STAGES WHICH ARE LOST 88.31000
The number of stages that are lost is determined for each program. The average is then calculated from these values.
- AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM .75000
This value is the percent probability of having an operational vehicle left at the end of the program.

For the conditions of this case study there is a 75 percent chance that a stage will be operational at the end of the flight program. This will allow a 446th flight if desired.

The histogram output formats presented in this section are the result of the input deck shown in Figure 1. These output formats appear after the format that specifies the study conditions and parameter averages. Four histograms are generated for each case study defined by the input deck. The titles of the histograms and their corresponding average parameter titles are shown in Table II. The histogram outputs for the example deck are shown in Figures 3 through 5.

The histograms contain the full range of data points generated during the 100 simulations specified by the input deck. Each histogram defines the number of data points it contains, the width of each cell and the number of points above or below the histogram's range. The histogram is output in three columns. The UPPER CELL LIMIT column defines the maximum value that can be contained in the cell. The CELL FREQ column contains the number of data points that are in each cell. The CUMULATIVE PROBABILITY column is the percentage of data points that fall equal to or below the cell.

The histogram of the total number of stages required per 445 flight program is presented in Figure 3 and is interpreted as follows:

- NUMBER OF DATA POINTS IN HISTOGRAM 100
Each data point in the histogram represents the total number of stages required to complete one 445 flight program. The

TABLE II. TITLES OF HISTOGRAMS AND CORRESPONDING AVERAGE PARAMETER TITLES

Title of Parameter Average	Title of Corresponding Histogram
Average Number of Stages Required	Histogram of Total Number of Stages Required Per xxx Flight Program
Average Stage Life	Histogram of Average Stage Life
Average Number of Stages Which Wear Out	Histogram of Worn Out Stages
Average Number of Stages Which Are Lost	Histogram of Lost Stages
Average Number of Stages Which Are Still Operational at the End of the Flight Program	No Corresponding Histogram

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 445 FLIGHT PROGRAM
 NUMBER OF DATA POINTS IN HISTOGRAM 100
 CELL WIDTH = 1.000
 NUMBER OF DATA POINTS EQUAL TO OR BELOW 67.00= 0
 NUMBER OF DATA POINTS EQUAL TO OR ABOVE 114.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
67.000	0	.000
68.000	1	.010
69.000	1	.020
70.000	0	.020
71.000	0	.020
72.000	0	.020
73.000	0	.020
74.000	1	.030
75.000	1	.040
76.000	2	.060
77.000	0	.060
78.000	3	.090
79.000	2	.110
80.000	3	.140
81.000	2	.160
82.000	4	.200
83.000	3	.230
84.000	7	.300
85.000	4	.340
86.000	3	.370
87.000	4	.410
88.000	2	.430
89.000	1	.440
90.000	6	.500
91.000	2	.520
92.000	2	.540
93.000	5	.590
94.000	8	.670
95.000	5	.720
96.000	4	.760
97.000	5	.810
98.000	4	.850
99.000	3	.880
100.000	3	.910
101.000	2	.930
102.000	1	.940
103.000	0	.940
104.000	1	.950
105.000	1	.960
106.000	1	.970
107.000	0	.970
108.000	1	.980
109.000	0	.980
110.000	1	.990
111.000	0	.990
112.000	0	.990
113.000	1	1.000
114.000	0	1.000

FIGURE 3. HISTOGRAM OF TOTAL STAGES REQUIRED

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW

3.50= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE

7.50= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
3.500	0	.000
4.000	1	.010
4.500	14	.150
5.000	42	.570
5.500	29	.860
6.000	11	.970
6.500	2	.990
7.000	1	1.000
7.500	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW

.00= 29

NUMBER OF DATA POINTS EQUAL TO OR ABOVE

7.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
.000	29	.290
1.000	46	.750
2.000	19	.940
3.000	3	.970
4.000	1	.980
5.000	1	.990
6.000	1	1.000
7.000	0	1.000

FIGURE 4. HISTOGRAMS OF AVERAGE STAGE LIFE AND WORNOUT STAGES

HISTOGRAM OF LOST STAGES
 NUMBER OF DATA POINTS IN HISTOGRAM 100
 CELL WIDTH = 1.000
 NUMBER OF DATA POINTS EQUAL TO OR BELOW . 64.00= 0
 NUMBER OF DATA POINTS EQUAL TO OR ABOVE 113.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
64.000	0	.000
65.000	1	.010
66.000	1	.020
67.000	0	.020
68.000	0	.020
69.000	0	.020
70.000	0	.020
71.000	1	.030
72.000	3	.060
73.000	0	.060
74.000	2	.080
75.000	0	.080
76.000	2	.100
77.000	3	.130
78.000	2	.150
79.000	2	.170
80.000	2	.190
81.000	6	.250
82.000	2	.270
83.000	6	.330
84.000	4	.370
85.000	0	.370
86.000	5	.420
87.000	2	.440
88.000	4	.480
89.000	3	.510
90.000	3	.540
91.000	4	.580
92.000	7	.650
93.000	6	.710
94.000	5	.760
95.000	3	.790
96.000	2	.810
97.000	4	.850
98.000	4	.890
99.000	3	.920
100.000	0	.920
101.000	2	.940
102.000	0	.940
103.000	1	.950
104.000	1	.960
105.000	1	.970
106.000	1	.980
107.000	0	.980
108.000	0	.980
109.000	1	.990
110.000	0	.990
111.000	0	.990
112.000	1	1.000
113.000	0	1.000

FIGURE 5. HISTOGRAM OF LOST STAGES

results for 100 of these 445 flight programs are contained in this histogram.

- CELL WIDTH = 1.000
The width of each cell in this histogram is one unit.
- NUMBER OF DATA POINTS EQUAL TO OR BELOW 67.000 = 0
The minimum number of stages required to complete one 445 flight program is 68. The percent probability of 68 stages completing the entire 445 flight program can be determined by referring to the cumulative probability column of the histogram corresponding to an upper cell limit of 68.000. It can be seen that the probability of completing the entire program with 68 stages is 1 percent.
- NUMBER OF DATA POINTS EQUAL TO OR ABOVE 114.000 = 0
The maximum number of stages required to complete one 445 flight program is 113.000. The results of the simulation under the present set of specified conditions indicate that there is a 100 percent probability of completing the entire 445 flight program with 113 stages. However, care must be used when making unequivocal statements of this type. It is recommended when stating maximums that a positive 2σ limit (≈ 97 percent) be used in lieu of a 100 percent quote. The closest probability that is larger than or equal to the positive 2σ limit in the example histogram is 97 percent. Therefore, 106 stages are required to have a 2σ probability of completing the entire program.

The interpretation of the remaining three histograms generated by the SLAVE Model can be made in a manner similar to the detailed explanation presented above.

SECTION V. EXAMPLE PROBLEM

This section presents a hypothetical set of parametric case studies for which the statistics generated by the SLAVE Model are desired. The user needs to study information on a 580 flight program, and desires to know how many stages will be required to successfully complete the program. The analyst estimates that the probability of losing a stage could be 5, 10, or 20 percent. He also knows that the stage designers are considering a maximum flight life of 20 or 30 flights per stage.

In order to obtain statistically valid results the user decides 100 simulations are sufficient. In order to compare the results all the case studies should operate under the same conditions, therefore, the random number seed is identical for all the desired case studies. The listing of the required input deck appears in Figure 6. The results of this input deck are presented in Appendix A. A detailed report utilizing results from the SLAVE Model is presented in Reference 1.

@ RUN, / / P CASE01, 567383 , DDPAULBIN22 5 , 1 , 200

@ ASG, T TAPE, T, 13654

@ REWIND TAPE.

@ COPIN TAPE.

@ XQT SLAVEC

11 22 1	5 . 0	2 0	1 0 0	5 8 0
11 22 1	5 . 0	3 0	1 0 0	5 8 0
11 22 1	1 0 . 0	2 0	1 0 0	5 8 0
11 22 1	1 0 . 0	3 0	1 0 0	5 8 0
11 22 1	2 0 . 0	2 0	1 0 0	5 8 0
11 22 1	2 0 . 0	3 0	1 0 0	5 8 0
		- 9 9 9		

@ FIN

@ FIN

FIGURE 6. EXAMPLE PROBLEM INPUT DECK

SECTION VI. PROGRAM DEFINITION

A. Program Description

The SLAVE Model requires approximately 20,000 words of UNIVAC 1108 core space. The program consists of a mainline and four subroutines. The read and write unit designators are designed to be easily adaptable to computers other than the UNIVAC 1108. The program has 8 subscripted variables with a total array size of 10,040 words. The program places data in 4 histograms of which 3 have 1000 cells of width 1. The fourth histogram has 2000 cells of width 0.5. The program operates by placing a stage in the system and using it until it is lost or has reached its maximum flight life. Variables are used to accumulate the data of each flight. When one complete flight program is finished the appropriate values are entered into histograms. This process is repeated for each simulation until all simulations requested are completed. The cumulative probability of obtaining each data point in all histograms is calculated. Mathematical manipulations are then performed to make the data suitable for printout and the output subroutines are initiated. At the completion of the output, a check is made to determine if another case study is desired; if so, the entire process is repeated. The narrative flow chart of the mainline is presented in Appendix B and a complete program listing is contained in Appendix C.

B. Individual Subroutine Descriptions

1. HISTO. This subroutine is used to compile a histogram of the data produced by the main program. Inputs to the subroutine consist of the upper and lower limit of the histogram, the cell width, and an initial entry indicator. The output of the subroutine is a histogram that contains the frequency of occurrence in each cell. The subroutine also outputs the total number of data points contained in the histogram. A narrative flow chart of subroutine HISTO is presented in Appendix B and a complete program listing in Appendix C.

2. CUMPF. This subroutine is used to calculate the cumulative probability function for the data generated by the histogram subroutine. The inputs to this subroutine are the number of data points in the histogram, the number of cells, and the frequency in each cell. The output is the cumulative probability of obtaining a value between the lower limit of the histogram and the upper limit of each cell. A narrative flow chart of subroutine CUMPF is presented in Appendix B and a complete program listing in Appendix C.

3. WHIST. This subroutine is used to write the information generated by the histogram and cumulative probability subroutines. This subroutine writes the number of data points in the histogram, the cell width, the number of data points below the lower limit of the histogram, and the number of data points above the upper limit of the histogram in sentence form. The upper cell limit, cell frequency, and cumulative probability are written in tabular form. The printed histogram consists only of the cells between the lowest and highest occupied cell. A narrative flow chart of subroutine WHIST is presented in Appendix B and a complete program listing in Appendix C.

4. URAND. This subroutine generates a uniformly distributed sequence of pseudo random numbers in the range of zero to one. The narrative flow chart is presented in Appendix B and a complete program listing in Appendix C.

REFERENCES

1. Paul, Daryl Jr.: Booster Fleet Size Studies Considering Different Loss Rate Distributions and Probabilities of Loss. Technical Letter ASD-ASTN-15331, Teledyne Brown Engineering Company, Huntsville, Alabama, February 22, 1972.
2. Miller, Irwin and Freund, John: Probability and Statistics for Engineers. Prentice-Hall, Inc., Englewood Cliffs, New Jersey, 1965.

APPENDIX A. EXAMPLE PROBLEM RESULTS

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	20
LOSS RATE (PERCENT)	5.000
AVERAGE NUMBER OF STAGES REQUIRED	45.61000
AVERAGE STAGE LIFE	12.81811
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	15.94000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	28.77000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.90000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 580 FLIGHT PROGRAM

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 36.00= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 56.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
36.000	0	.000
37.000	1	.010
38.000	2	.030
39.000	2	.050
40.000	4	.090
41.000	5	.140
42.000	11	.250
43.000	9	.340
44.000	10	.440
45.000	8	.520
46.000	11	.630
47.000	5	.680
48.000	7	.750
49.000	9	.840
50.000	4	.880
51.000	2	.900
52.000	1	.910
53.000	5	.960
54.000	1	.970
55.000	3	1.000
56.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW 10.50= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 16.50= 0

UPPER CELL LIMIT	CELL FREN	CUMULATIVE PROBABILITY
10.500	0	.000
11.000	9	.090

11.500	3	.120
12.000	13	.250
12.500	12	.370
13.000	19	.560
13.500	19	.750
14.000	11	.860
14.500	9	.950
15.000	2	.970
15.500	2	.990
16.000	1	1.000
16.500	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 7.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 24.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
7.000	0	.000
8.000	1	.010
9.000	0	.010
10.000	0	.010
11.000	1	.020
12.000	5	.070
13.000	9	.160
14.000	10	.260
15.000	17	.430
16.000	17	.600
17.000	15	.750
18.000	13	.880
19.000	5	.930
20.000	3	.960
21.000	2	.980
22.000	1	.990
23.000	1	1.000
24.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 14.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 43.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
14.000	0	.000
15.000	1	.010
16.000	0	.010
17.000	1	.020
18.000	2	.040

19.000	3	.070
20.000	0	.070
21.000	4	.110
22.000	5	.160
23.000	1	.170
24.000	5	.220
25.000	9	.310
26.000	6	.370
27.000	5	.420
28.000	3	.450
29.000	9	.540
30.000	10	.640
31.000	8	.720
32.000	5	.770
33.000	4	.810
34.000	3	.840
35.000	1	.850
36.000	5	.900
37.000	1	.910
38.000	2	.930
39.000	1	.940
40.000	2	.960
41.000	3	.990
42.000	1	1.000
43.000	0	1.000

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	30
LOSS RATE (PERCENT)	5.000
AVERAGE NUMBER OF STAGES REQUIRED	37.2000
AVERAGE STAGE LIFE	15.82921
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	7.51000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	28.77000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.92000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PFR 580 FLIGHT PROGRAM
NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 27.00= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 52.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
27.000	0	.000
28.000	1	.010
29.000	4	.050
30.000	0	.050
31.000	4	.090
32.000	4	.130
33.000	10	.230
34.000	7	.300
35.000	10	.400
36.000	10	.500
37.000	9	.590
38.000	3	.620
39.000	6	.680
40.000	9	.770
41.000	5	.820
42.000	4	.860
43.000	4	.900
44.000	3	.930
45.000	3	.960
46.000	0	.960
47.000	2	.980
48.000	1	.990
49.000	0	.990
50.000	0	.990
51.000	1	1.000
52.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW 11.00= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 21.50= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
11.000	0	.000
11.500	1	.010
12.000	0	.010
12.500	3	.040
13.000	3	.070
13.500	7	.140
14.000	4	.180
14.500	14	.320
15.000	6	.380
15.500	3	.410
16.000	9	.500
16.500	10	.600
17.000	10	.700
17.500	7	.770
18.000	10	.870
18.500	4	.910
19.000	4	.950
19.500	0	.950
20.000	4	.990
20.500	0	.990
21.000	1	1.000
21.500	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 1.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 13.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
1.000	0	.000
2.000	1	.010
3.000	0	.010
4.000	5	.060
5.000	6	.120
6.000	20	.320
7.000	24	.560
8.000	14	.700
9.000	13	.830
10.000	7	.900
11.000	8	.980
12.000	2	1.000
13.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 14.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 43.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
14.000	0	.000
15.000	1	.010
16.000	0	.010
17.000	1	.020
18.000	2	.040
19.000	3	.070
20.000	0	.070
21.000	4	.110
22.000	5	.160
23.000	1	.170
24.000	5	.220
25.000	9	.310
26.000	6	.370
27.000	5	.420
28.000	3	.450
29.000	9	.540
30.000	10	.640
31.000	8	.720
32.000	5	.770
33.000	4	.810
34.000	3	.840
35.000	1	.850
36.000	5	.900
37.000	1	.910
38.000	2	.930
39.000	1	.940
40.000	2	.960
41.000	3	.990
42.000	1	1.000
43.000	0	1.000

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	20
LOSS RATE (PERCENT)	10.000
AVERAGE NUMBER OF STAGES REQUIRED	66.68000
AVERAGE STAGE LIFE	8.77390
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	7.80000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	58.06000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.82000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 580 FLIGHT PROGRAM
 NUMBER OF DATA POINTS IN HISTOGRAM 100
 CELL WIDTH = 1.000
 NUMBER OF DATA POINTS EQUAL TO OR BELOW 52.000= 0
 NUMBER OF DATA POINTS EQUAL TO OR ABOVE 84.000= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
52.000	0	.000
53.000	1	.010
54.000	0	.010
55.000	1	.020
56.000	3	.050
57.000	2	.070
58.000	4	.110
59.000	2	.130
60.000	4	.170
61.000	2	.190
62.000	6	.250
63.000	7	.320
64.000	8	.400
65.000	4	.440
66.000	8	.520
67.000	6	.580
68.000	4	.620
69.000	4	.660
70.000	5	.710
71.000	5	.760
72.000	6	.820
73.000	3	.850
74.000	6	.910
75.000	2	.930
76.000	2	.950
77.000	1	.960
78.000	0	.960
79.000	1	.970
80.000	1	.980
81.000	0	.980
82.000	1	.990
83.000	1	1.000
84.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW 6.50= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 11.50= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
6.500	0	.000
7.000	1	.010
7.500	3	.040
8.000	14	.180
8.500	20	.380
9.000	22	.600
9.500	21	.810
10.000	12	.930
10.500	5	.980
11.000	2	1.000
11.500	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 2.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 16.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
2.000	0	.000
3.000	1	.010
4.000	8	.090
5.000	5	.140
6.000	18	.320
7.000	19	.510
8.000	15	.660
9.000	9	.750
10.000	10	.850
11.000	6	.910
12.000	7	.980
13.000	1	.990
14.000	0	.990
15.000	1	1.000
16.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 39.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 76.00= 0

UPPER CELL	CELL FREQ	CUMULATIVE PROBABILITY

LIMIT

39.000	0	.000
40.000	1	.010
41.000	0	.010
42.000	1	.020
43.000	0	.020
44.000	1	.030
45.000	4	.070
46.000	1	.080
47.000	2	.100
48.000	2	.120
49.000	3	.150
50.000	3	.180
51.000	4	.220
52.000	2	.240
53.000	3	.270
54.000	5	.320
55.000	4	.360
56.000	2	.380
57.000	4	.420
58.000	10	.520
59.000	6	.580
60.000	2	.600
61.000	4	.640
62.000	9	.730
63.000	3	.760
64.000	5	.810
65.000	2	.830
66.000	4	.870
67.000	2	.890
68.000	2	.910
69.000	3	.940
70.000	1	.950
71.000	2	.970
72.000	1	.980
73.000	0	.980
74.000	0	.980
75.000	2	1.000
76.000	0	1.000

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	30
LOSS RATE (PERCENT)	10.000
AVERAGE NUMBER OF STAGES REQUIRED	61.19000
AVERAGE STAGE LIFE	9.60096
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	2.31000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	58.06000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.82000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 580 FLIGHT PROGRAM
 NUMBER OF DATA POINTS IN HISTOGRAM 100
 CELL WIDTH = 1.000
 NUMBER OF DATA POINTS EQUAL TO OR BELOW 44.00= 0
 NUMBER OF DATA POINTS EQUAL TO OR ABOVE 79.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
44.000	0	.000
45.000	1	.010
46.000	1	.020
47.000	0	.020
48.000	0	.020
49.000	2	.040
50.000	4	.080
51.000	1	.090
52.000	3	.120
53.000	4	.160
54.000	1	.170
55.000	3	.200
56.000	5	.250
57.000	6	.310
58.000	3	.340
59.000	3	.370
60.000	8	.450
61.000	5	.500
62.000	6	.560
63.000	3	.590
64.000	8	.670
65.000	8	.750
66.000	7	.820
67.000	1	.830
68.000	2	.850
69.000	5	.900
70.000	2	.920
71.000	2	.940
72.000	0	.940
73.000	2	.960
74.000	2	.980
75.000	0	.980
76.000	0	.980
77.000	1	.990

78.000	1	1.000
79.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW 7.00= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 13.50= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
7.000	0	.000
7.500	1	.010
8.000	5	.060
8.500	9	.150
9.000	18	.330
9.500	17	.500
10.000	19	.690
10.500	11	.800
11.000	8	.880
11.500	4	.920
12.000	6	.980
12.500	0	.980
13.000	2	1.000
13.500	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW .00= 9
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 6.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
.000	9	.090
1.000	24	.330
2.000	25	.580
3.000	19	.770
4.000	15	.920
5.000	8	1.000
6.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 39.00= 0
NUMBER OF DATA POINTS EQUAL TO OR ABOVE 76.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
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39.000	0	.000
40.000	1	.010
41.000	0	.010
42.000	1	.020
43.000	0	.020
44.000	1	.030
45.000	4	.070
46.000	1	.080
47.000	2	.100
48.000	2	.120
49.000	3	.150
50.000	3	.180
51.000	4	.220
52.000	2	.240
53.000	3	.270
54.000	5	.320
55.000	4	.360
56.000	2	.380
57.000	4	.420
58.000	10	.520
59.000	6	.580
60.000	2	.600
61.000	4	.640
62.000	9	.730
63.000	3	.760
64.000	5	.810
65.000	2	.830
66.000	4	.870
67.000	2	.890
68.000	2	.910
69.000	3	.940
70.000	1	.950
71.000	2	.970
72.000	1	.980
73.000	0	.980
74.000	0	.980
75.000	2	1.000
76.000	0	1.000

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	20
LOSS RATE (PERCENT)	20.000
AVERAGE NUMBER OF STAGES REQUIRED	118.09000
AVERAGE STAGE LIFE	4.95310
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	1.37000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	115.95000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.77000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 580 FLIGHT PROGRAM
 NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 91.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 141.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
91.000	0	.000
92.000	1	.010
93.000	0	.010
94.000	1	.020
95.000	1	.030
96.000	0	.030
97.000	2	.050
98.000	0	.050
99.000	0	.050
100.000	1	.060
101.000	0	.060
102.000	2	.080
103.000	0	.080
104.000	1	.090
105.000	4	.130
106.000	1	.140
107.000	4	.180
108.000	1	.190
109.000	2	.210
110.000	4	.250
111.000	5	.300
112.000	1	.310
113.000	4	.350
114.000	5	.400
115.000	2	.420
116.000	1	.430
117.000	1	.440
118.000	5	.490
119.000	3	.520
120.000	1	.530
121.000	5	.580
122.000	5	.630
123.000	3	.660
124.000	7	.730

125.000	2	.750
126.000	0	.750
127.000	2	.770
128.000	2	.790
129.000	5	.840
130.000	3	.870
131.000	2	.890
132.000	3	.920
133.000	1	.930
134.000	3	.960
135.000	2	.980
136.000	0	.980
137.000	1	.990
138.000	0	.990
139.000	0	.990
140.000	1	1.000
141.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW 4.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 7.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
4.000	0	.000
4.500	21	.210
5.000	37	.580
5.500	29	.870
6.000	10	.970
6.500	3	1.000
7.000	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW .00= 27

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 8.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
0.000	27	.270
1.000	35	.620
2.000	25	.870
3.000	7	.940
4.000	2	.960
5.000	2	.980
6.000	1	.990
7.000	1	1.000
8.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 87.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 139.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
87.000	0	.000
88.000	1	.010
89.000	1	.020
90.000	0	.020
91.000	1	.030
92.000	0	.030
93.000	0	.030
94.000	1	.040
95.000	2	.060
96.000	1	.070
97.000	0	.070
98.000	0	.070
99.000	1	.080
100.000	1	.090
101.000	1	.100
102.000	1	.110
103.000	4	.150
104.000	3	.180
105.000	0	.180
106.000	3	.210
107.000	1	.220
108.000	5	.270
109.000	2	.290
110.000	4	.330
111.000	3	.360
112.000	2	.380
113.000	4	.420
114.000	1	.430
115.000	1	.440
116.000	3	.470
117.000	4	.510
118.000	3	.540
119.000	3	.570
120.000	4	.610
121.000	7	.680
122.000	4	.720
123.000	3	.750
124.000	0	.750
125.000	0	.750
126.000	3	.780
127.000	4	.820
128.000	3	.850
129.000	3	.880
130.000	3	.910
131.000	3	.940
132.000	0	.940
133.000	1	.950

134.000	3	.980
135.000	0	.980
136.000	1	.990
137.000	0	.990
138.000	1	1.000
139.000	0	1.000

RANDOM NUMBER SEED	11221
NUMBER OF FLIGHTS IN 1 COMPLETE PROGRAM	580
NUMBER OF COMPLETE PROGRAMS SIMULATED	100
MAXIMUM STAGE LIFETIME	30
LOSS RATE (PERCENT)	20.000
AVERAGE NUMBER OF STAGES REQUIRED	116.87000
AVERAGE STAGE LIFE	5.01075
AVERAGE NUMBER OF STAGES WHICH WEAR OUT	.15000
AVERAGE NUMBER OF STAGES WHICH ARE LOST	115.95000
AVERAGE NUMBER OF STAGES WHICH ARE STILL OPERATIONAL AT THE END OF THE FLIGHT PROGRAM	.77000

HISTOGRAM OF TOTAL NUMBER OF STAGES REQUIRED PER 580 FLIGHT PROGRAM

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW 89.00= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE 139.00= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
89.000	0	.000
90.000	1	.010
91.000	1	.020
92.000	1	.030
93.000	0	.030
94.000	0	.030
95.000	1	.040
96.000	2	.060
97.000	1	.070
98.000	0	.070
99.000	0	.070
100.000	0	.070
101.000	2	.090
102.000	1	.100
103.000	1	.110
104.000	5	.160
105.000	2	.180
106.000	0	.180
107.000	3	.210
108.000	3	.240
109.000	4	.280
110.000	2	.300
111.000	3	.330
112.000	3	.360
113.000	1	.370
114.000	5	.420
115.000	1	.430
116.000	1	.440
117.000	3	.470
118.000	4	.510
119.000	3	.540
120.000	3	.570
121.000	5	.620
122.000	6	.680

123.000	4	.720
124.000	2	.740
125.000	1	.750
126.000	0	.750
127.000	3	.780
128.000	5	.830
129.000	4	.870
130.000	2	.890
131.000	2	.910
132.000	3	.940
133.000	0	.940
134.000	2	.960
135.000	2	.980
136.000	1	.990
137.000	0	.990
138.000	1	1.000
139.000	0	1.000

HISTOGRAM OF AVERAGE STAGE LIFE

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = .500

NUMBER OF DATA POINTS EQUAL TO OR BELOW

4.000= 0

NUMBER OF DATA POINTS EQUAL TO OR ABOVE

7.000= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
4.000	0	.000
4.500	17	.170
5.000	40	.570
5.500	25	.820
6.000	12	.940
6.500	6	1.000
7.000	0	1.000

HISTOGRAM OF WORN OUT STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW

.000= 85

NUMBER OF DATA POINTS EQUAL TO OR ABOVE

2.000= 0

UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
.000	85	.850
1.000	15	1.000
2.000	0	1.000

HISTOGRAM OF LOST STAGES

NUMBER OF DATA POINTS IN HISTOGRAM 100

CELL WIDTH = 1.000

NUMBER OF DATA POINTS EQUAL TO OR BELOW

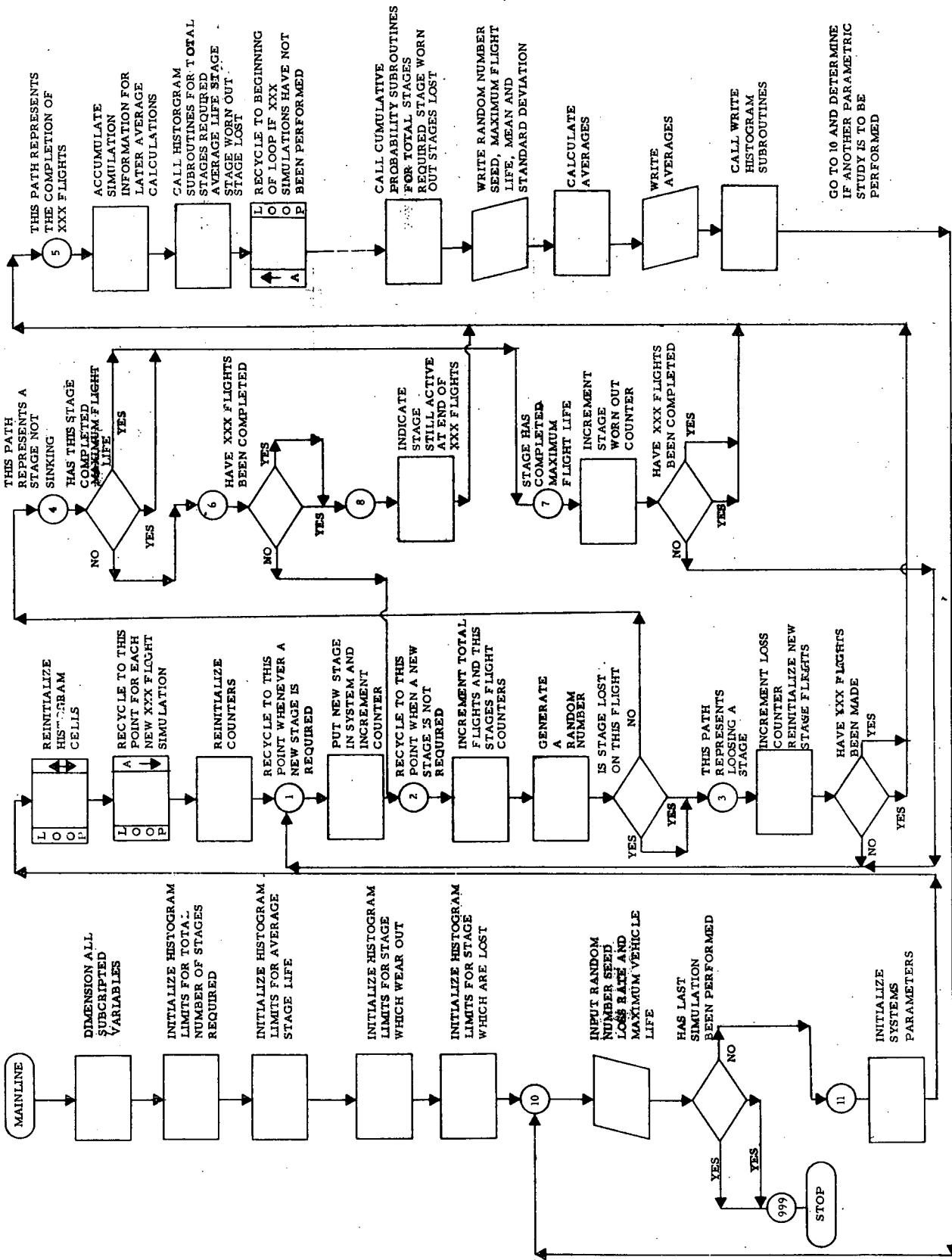
87.000= 0

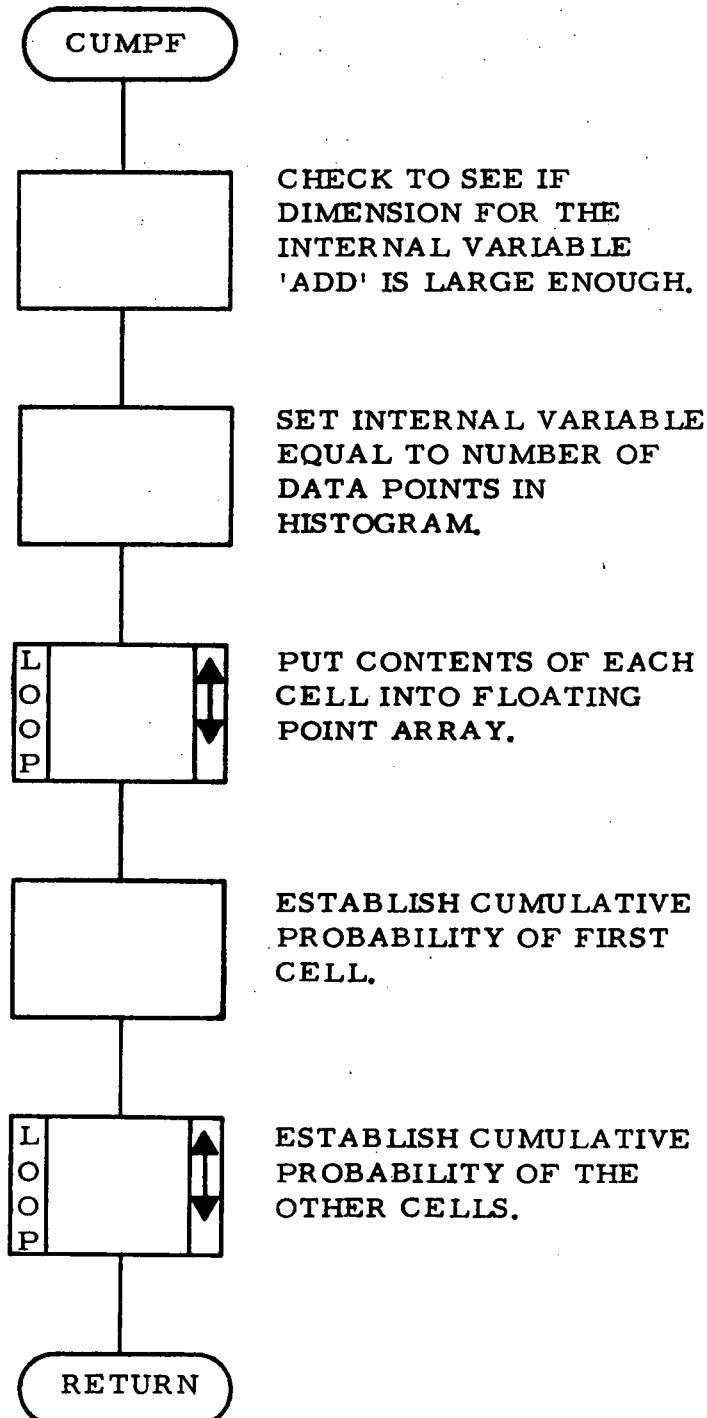
NUMBER OF DATA POINTS EQUAL TO OR ABOVE

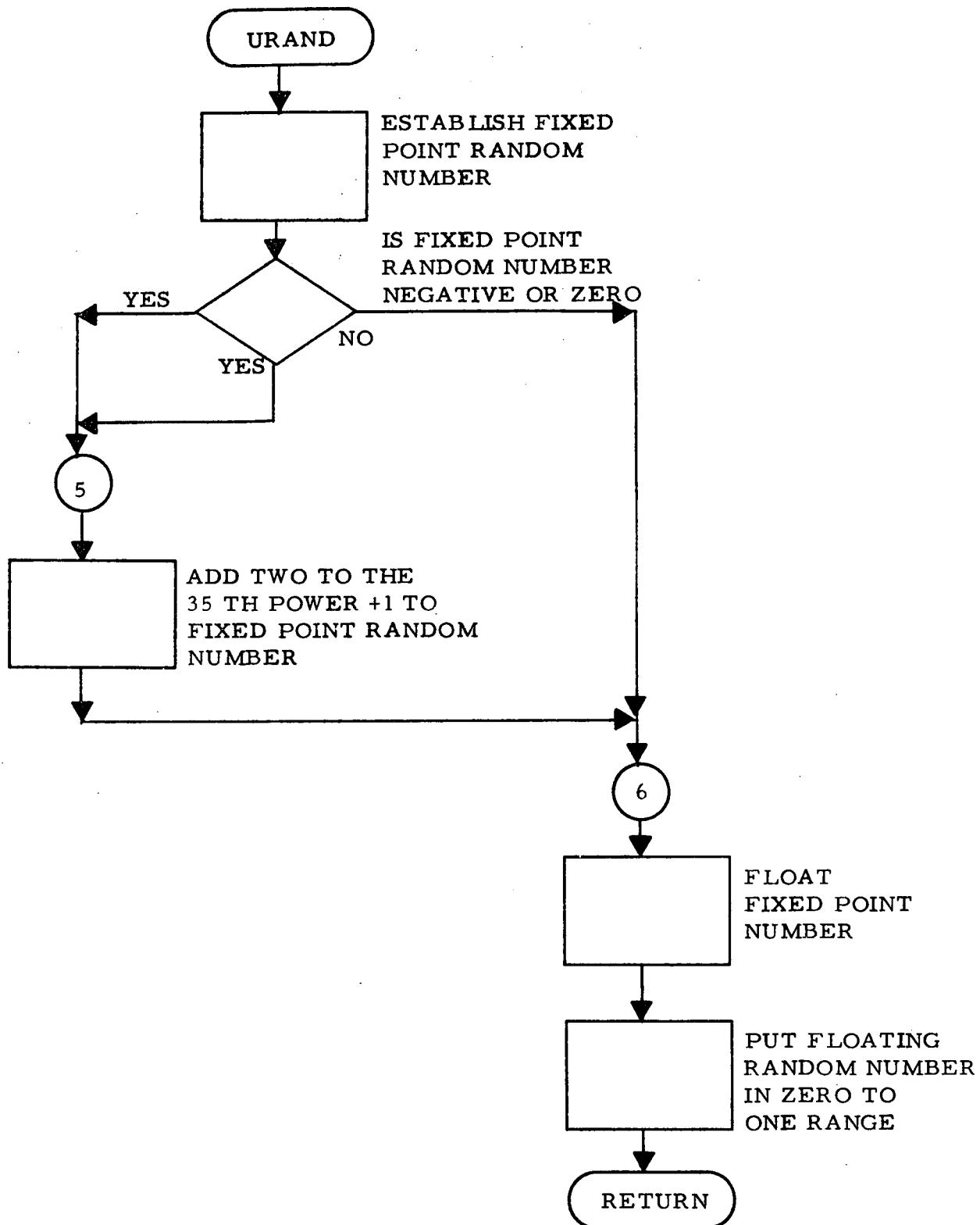
139.000= 0

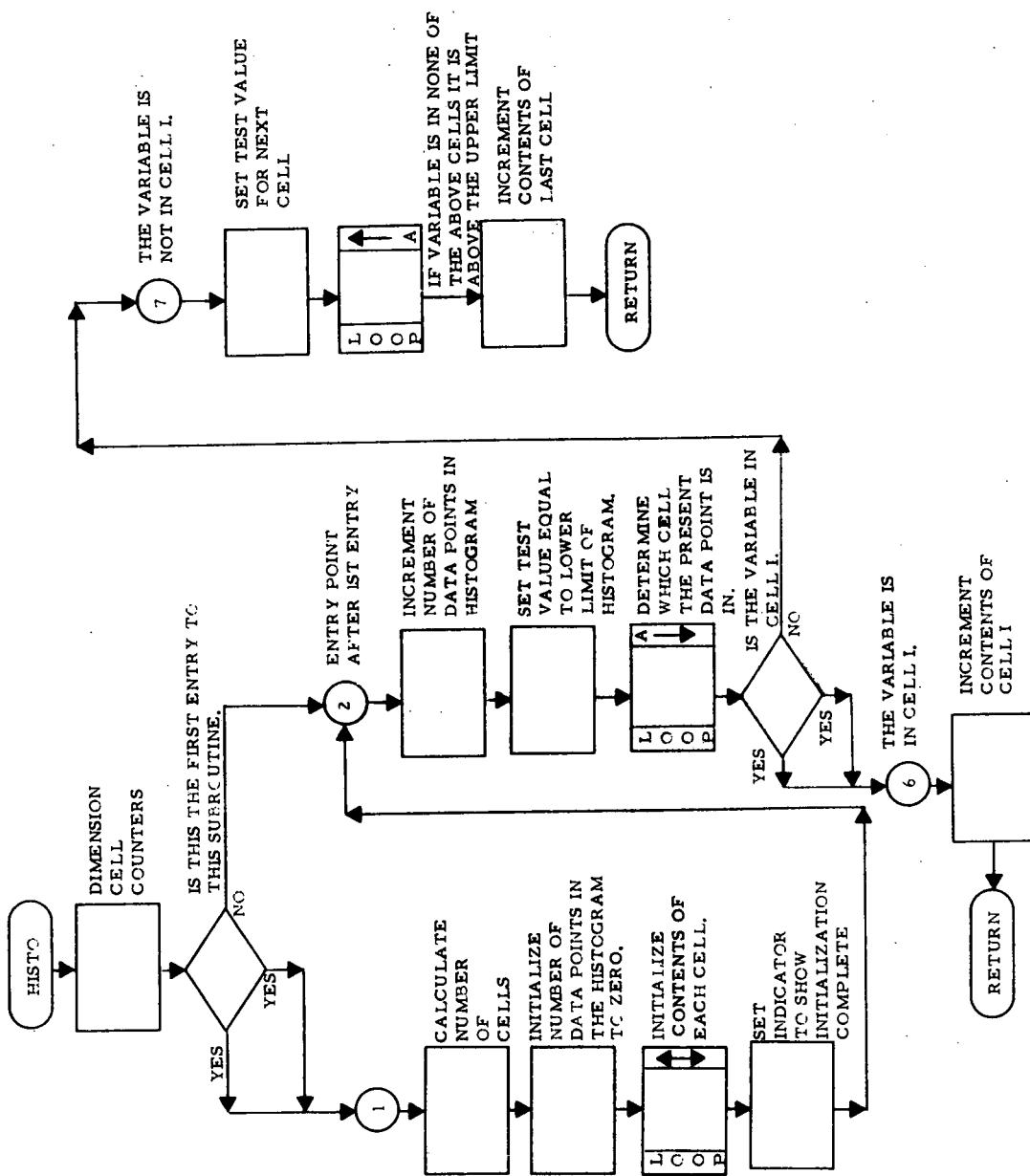
UPPER CELL LIMIT	CELL FREQ	CUMULATIVE PROBABILITY
87.000	0	.000
88.000	1	.010
89.000	1	.020
90.000	0	.020
91.000	1	.030
92.000	0	.030
93.000	0	.030
94.000	1	.040
95.000	2	.060
96.000	1	.070
97.000	0	.070
98.000	0	.070
99.000	1	.080
100.000	1	.090
101.000	1	.100
102.000	1	.110
103.000	4	.150
104.000	3	.180
105.000	0	.180
106.000	3	.210
107.000	1	.220
108.000	5	.270
109.000	2	.290
110.000	4	.330
111.000	3	.360
112.000	2	.380
113.000	4	.420
114.000	1	.430
115.000	1	.440
116.000	3	.470
117.000	4	.510
118.000	3	.540
119.000	3	.570
120.000	4	.610
121.000	7	.680
122.000	4	.720
123.000	3	.750
124.000	0	.750
125.000	0	.750
126.000	3	.780
127.000	4	.820
128.000	3	.850
129.000	3	.880
130.000	3	.910
131.000	3	.940
132.000	0	.940
133.000	1	.950
134.000	3	.980
135.000	0	.980
136.000	1	.990
137.000	0	.990
138.000	1	1.000
139.000	0	1.000

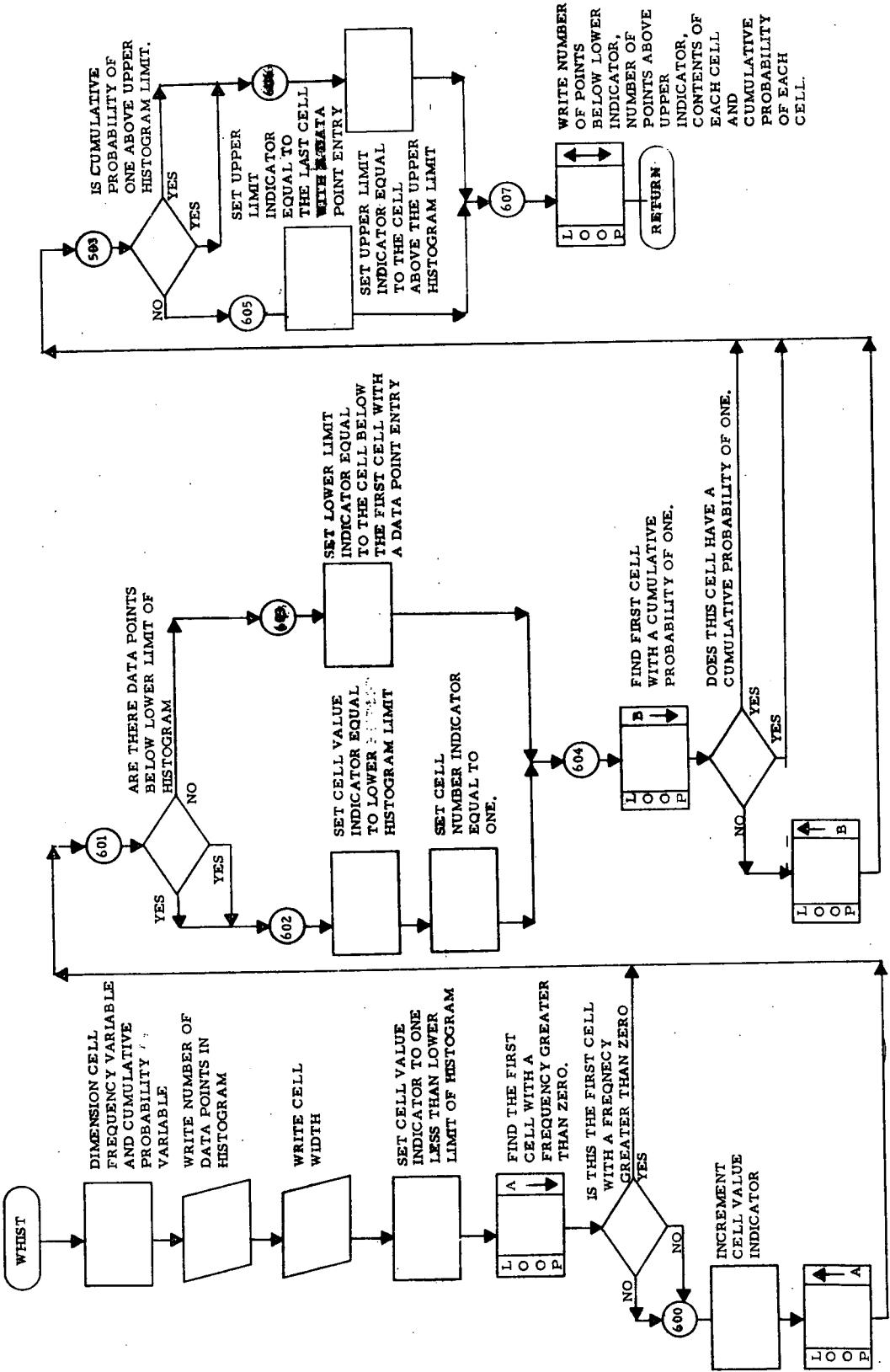
APPENDIX B. SLAVE MODEL NARRATIVE PROGRAM FLOW CHARTS











APPENDIX C. SLAVE MODEL FORTRAN LISTINGS

l RUN//T SLAVE1,420025,DUPAULBIN225,3,150

l ASG,T TAPE,T,SAVEU2

l FOR,IS MAIN,MAIN

SLAVU0000

SLAVU0010

SLAVU0020

DARYL D. PAUL, JR.
TELEDYNE BROWN ENGINEERING
JANUARY 28, 1972

SLAVU0030

SLAVU0040

SLAVU0050

SLAVU0060

SLAVU0070

PROGRAM TO DETERMINE THE NUMBER OF STAGES REQUIRED TO COMPLETE
ALL MISSIONS IN THE PROGRAM LIFE. THE NUMBER OF STAGES REQUIRED
VARIES ACCORDING TO THE ESTIMATED LOSS RATE PER FLIGHT AND MAXIMUM
FLIGHTS A STAGE MAY PERFORM. THIS PROGRAM MAY BE USED TO CALCULATE
THE REQUIRED STATISTICS FOR ANY ELEMENT OF HARDWARE WHICH IS USED
REPEATEDLY FOR WHICH A LOSS RATE MAY BE ESTABLISHED.

SLAVU0080

SLAVU0090

SLAVU0100

SLAVU0110

SLAVU0120

SLAVU0130

SLAVU0140

SLAVU0150

SLAVU0160

SLAVU0170

SLAVU0180

SLAVU0190

VARIABLE IDENTIFICATION

SLAVU200

SLAVU210

SLAVU220

SLAVU230

SLAVU240

SLAVU250

SLAVU260

SLAVU270

SLAVU280

SLAVU290

SLAVU300

SLAVU310

SLAVU320

SLAVU330

SLAVU340

SLAVU350

SLAVU360

SLAVU370

SLAVU380

SLAVU390

SLAVU400

SLAVU410

SLAVU420

SLAVU430

SLAVU440

SLAVU450

SLAVU460

SLAVU470

SLAVU480

SLAVU490

SLAVU500

SLAVU510

SLAVU520

SLAVU530

SLAVU540

SLAVU550

SLAVU560

SLAVU570

SLAVU580

SLAVU590

SLAVU600

ABUST= AVERAGE NUMBER OF STAGES REQUIRED

SLAVU200

ALEFT= AVERAGE NUMBER OF STAGES STILL OPERATIONAL
AT THE END OF EACH PROGRAM SIMULATION

SLAVU210

ALIFE= AVERAGE STAGE LIFE

SLAVU220

ALIVEE= AVERAGE STAGE LIFE ACCUMULATOR

SLAVU230

AMANE= MEAN LOSS RATE PERCENTAGE

SLAVU240

ASINK= AVERAGE NUMBER OF STAGES LOST

SLAVU250

AWEAR= AVERAGE NUMBER OF STAGES WHICH WEAR OUT AND ARE DISCARDED

SLAVU260

BOUT= FLOATING POINT REPRESENTATION OF NUMBER OF STAGES REQUIRED

SLAVU270

CELLW= CELL WIDTH FOR TOTAL NUMBER OF STAGES REQUIRED HISTOGRAM

SLAVU280

CELL1= CELL WIDTH IN AVERAGE STAGE LIFE HISTOGRAM

SLAVU290

CELL2= CELL WIDTH FOR WORN OUT STAGE HISTOGRAM

SLAVU300

CELL3= CELL WIDTH FOR LOST STAGE HISTOGRAM

SLAVU310

FLITE= THE NUMBER OF FLIGHTS A STAGE MADE BEFORE BEING LOST

SLAVU320

INIT= INDICATOR TO THE TOTAL REQUIRED HISTOGRAM SUBROUTINE

SLAVU330

TO INITIALIZE ITSELF

SLAVU340

INIT2= INDICATOR FOR INITIALIZATION OF TOTAL REQUIRED

STAGES HISTOGRAM

IRAND= USED TO RETAIN THE INITIAL RANDOM NUMBER SEE

FOR SUBSEQUENT PRINTOUT

IX= RANDOM NUMBER GENERATOR SEED

SLAVU350

I1ST= INDICATOR TO AVERAGE STAGE LIFE HISTOGRAM SUBROUTINE

TO INITIALIZE ITSELF

C		12ND= INDICATOR TO THE WORN OUT STAGE HISTOGRAM SUBROUTINE C TO INITIALIZE ITSELF	SLAVU62U
C		13RD= INDICATOR TO THE LOST STAGE HISTOGRAM SUBROUTINE C TO INITIALIZE ITSELF	SLAVU63U
C		JHOST= NUMBER OF STAGES REQUIRED ACCUMULATOR	SLAVU64U
C		JSINK= NUMBER OF STAGES WHICH ARE LOST ACCUMULATOR	SLAVU65U
C		JWEAR= NUMBER OF STAGES WHICH WEAR OUT AND ARE DISCARDED	SLAVU66U
C		KKK= INDICATOR FOR NUMBER OF PROGRAM SIMULATIONS REQUIRED	SLAVU67U
C		KREAD= THE READ UNIT OF THE COMPUTER BEING C USED TO RUN THIS PROGRAM	SLAVU68U
C		KRITE= THE WRITE UNIT OF THE COMPUTER BEING C USED TO RUN THIS PROGRAM	SLAVU69U
C		LCELL= NUMBER OF CELLS IN THE TOTAL REQUIRED STAGE HISTOGRAM	SLAVU70U
C		LCEL1= NUMBER OF CELLS IN AVERAGE STAGE LIFE HISTOGRAM	SLAVU71U
C		LCEL2= NUMBER OF CELLS IN WORN OUT STAGE HISTOGRAM	SLAVU72U
C		LCEL3= NUMBER OF CELLS IN LOST STAGE HISTOGRAM	SLAVU73U
C		LEFT= ACCUMULATOR OF STAGES STILL ACTIVE AT THE END C OF A PROGRAM SIMULATION	SLAVU74U
C		LIAUD= AN ARRAY WHICH CONTAINS THE HISTOGRAM OF STAGES REQUIRED C PER 'NSIM' PROGRAM SIMULATIONS	SLAVU75U
C		LIAU1= AN ARRAY WHICH CONTAINS THE HISTOGRAM OF C AVERAGE STAGE LIFE	SLAVU76U
C		LIAU2= AN ARRAY WHICH CONTAINS THE WORN OUT STAGE HISTOGRAM	SLAVU77U
C		LIAU3= AN ARRAY WHICH CONTAINS THE LOST STAGE HISTOGRAM	SLAVU78U
C		LTRY= THE NUMBER OF DATA POINTS IN THE TOTAL C STAGE REQUIRED HISTOGRAM	SLAVU79U
C		MAXLF= MAXIMUM NUMBER OF FLIGHTS A STAGE CAN MAKE BEFORE BEING C DISCARDED AS WORN OUT	SLAVU80U
C		NHOST= NUMBER OF STAGES REQUIRED PER PROGRAM SIMULATION	SLAVU81U
C		NFLIT= NUMBER OF FLIGHTS EACH STAGES MAKES BEFORE BEING C LOST OR DISCARDED AS WORN OUT	SLAVU82U
C		NMISS= NUMBER OF FLIGHTS IN ONE PROGRAM	SLAVU83U
C		NSIME= NUMBER OF PROGRAM SIMULATIONS TO BE MADE	SLAVU84U
C		NSINK= NUMBER OF STAGES WHICH ARE LOST	SLAVU85U
C		NTFLT= NUMBER OF FLIGHTS ACCUMULATOR USED TO CHECK FOR END C OF EACH PROGRAM SIMULATION	SLAVU86U
C		NTRY1= THE NUMBER OF DATA POINTS IN THE AVERAGE C STAGE LIFE HISTOGRAM	SLAVU87U

NTRY2=	THE NUMBER OF DATA POINTS IN THE WORN OUT STAGE HISTOGRAM	SLAV128U
NTRY3=	THE NUMBER OF DATA POINTS IN THE LOST STAGE HISTOGRAM	SLAV129U
NWEAR=	NUMBER OF STAGES WHICH ARE WORN OUT AND DISCARDED	SLAV130U
PERDS=	AN ARRAY WHICH CONTAINS THE CUMULATIVE PROBABILITY FUNCTION OF STAGES REQUIRED	SLAV131U
PERD1=	AN ARRAY WHICH CONTAINS THE CUMULATIVE PROBABILITY FUNCTION OF AVERAGE STAGE LIFE	SLAV132U
PERD2=	AN ARRAY WHICH CONTAINS THE CUMULATIVE PROBABILITY FUNCTION OF WORN OUT STAGES	SLAV133U
PERD3=	AN ARRAY WHICH CONTAINS THE CUMULATIVE PROBABILITY FUNCTION OF LOST STAGES	SLAV134U
PLSS=	LOSS RATE(PERCENT)	SLAV135U
PLSS		SLAV136U
PROGRAM=	A TERM USED ON COMMENT CARDS ONLY. THIS TERM REPRESENTS A COMPLETE PROGRAM LIFE OF NMISS FLIGHTS	SLAV137U
SIM=	FLOATING POINT EQUIVALENT OF NSIM	SLAV138U
STDEV=	STANDARD DEVIATION FROM THE MEAN LOSS RATE	SLAV139U
TLOST=	NUMBER OF STAGES LOST PER PROGRAM SIMULATION	SLAV140U
UP=	UPPER LIMIT OF CELLS IN THE TOTAL STAGES REQUIRED HISTOGRAM	SLAV141U
UP1=	UPPER LIMIT OF CELLS IN AVERAGE STAGE LIFE HISTOGRAM	SLAV142U
UP2=	UPPER LIMIT OF CELLS IN WORN OUT STAGE HISTOGRAM	SLAV143U
UP3=	UPPER LIMIT OF CELLS IN LOST STAGE HISTOGRAM	SLAV144U
URAND=	THE NAME OF A FUNCTION USED TO CALCULATE A UNIFORM RANDOM NUMBER IN THE RANGE 0 TO 1	SLAV145U
WEAR=	THE NUMBER OF WORN OUT STAGES PER PROGRAM SIMULATION	SLAV146U
XLOW=	THE LOWER LIMIT OF CELL VALUE IN THE TOTAL STAGES REQUIRED HISTOGRAM	SLAV147U
XLOW1=	LOWER LIMIT OF CELLS IN AVERAGE STAGE LIFE HISTOGRAM	SLAV148U
XLOW2=	LOWER LIMIT OF CELLS IN THE WORN OUT STAGE HISTOGRAM	SLAV149U
XLOW3=	LOWER LIMIT OF CELLS IN THE LOST STAGE HISTOGRAM	SLAV150U
YFL=	THE VALUE OF THE RANDOM NUMBER GENERATED BY URAND	SLAV151U
KREAD=5		SLAV152U
KRITE=6		SLAV153U
		SLAV154U
DIMENSION LIADU(1005),PERDS(1005)		SLAV155U
DIMENSION LIAD1(2005),PERD1(2005)		SLAV156U
DIMENSION LIAD2(1005),PERD2(1005)		SLAV157U
DIMENSION LIADS(1005),PERD3(1005)		SLAV158U
INITIALIZE UPPER AND LOWER LIMITS AND CELL WIDTH FOR		SLAV159U


```

-----+
      NTRY3=0          SLAV2600
      IRAND=1X          SLAV2610
-----+
C
C
-----+
C   INITIALIZE HISTOGRAM CELLS          SLAV2620
DO 30 INIT2=1,1005          SLAV2630
LIADD(INIT2)=0          SLAV2640
LIAD1(INIT2)=0          SLAV2650
LIAD2(INIT2)=0          SLAV2660
LIAD3(INIT2)=0          SLAV2670
30 CONTINUE          SLAV2680
DO 40 INIT2=1006,2005          SLAV2690
LIAD1(INIT2)=0          SLAV2700
40 CONTINUE          SLAV2710
-----+
C
C
-----+
C   RECYCLE TO THIS POINT FOR EACH NEW PROGRAM SIMULATION          SLAV2720
-----+
C
C
C
C
-----+
C   DO 130 KKK=1,NSIM          SLAV2730
-----+
C
C
C
C
-----+
C   REINITIALIZE COUNT VARIABLES FOR EACH NEW PROGRAM          SLAV2740
-----+
C
NFLIT=0          SLAV2750
NTFLT=0          SLAV2760
NSINK=0          SLAV2770
NBUST=0          SLAV2780
NWEAR=0          SLAV2790
-----+
C
C
C
C
-----+
C   RECYCLE TO THIS POINT WHENEVER A NEW STAGE IS REQUIRED          SLAV2800
-----+
C
50 CONTINUE          SLAV2810
NBUST=NBUST+1          SLAV2820
-----+
C
C
C
C
-----+
C   RECYCLE TO THIS POINT WHEN A NEW STAGE IS NOT REQUIRED          SLAV2830
-----+
60 CONTINUE          SLAV2840
NFLIT=NFLIT+1          SLAV2850
NTFLT=NTFLT+1          SLAV2860
-----+
C
C
C
C
-----+
C   GENERATE A RANDOM NUMBER          SLAV2870
YFL=URAND(1X)          SLAV2880
-----+
C
C
C
C
-----+
C   IS THE RANDOM NUMBER SMALL ENOUGH TO CAUSE THE LOSS OF THIS STAGE          SLAV2890
IF (YFL-AMEAN)>0,70,80          SLAV2900
-----+
C
C
C
C
-----+

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C THIS PATH REPRESENTS A SINKING STAGE SLAV326U
70 CONTINUE SLAV327U
NSINK=NSINK+1 SLAV328U
FLITE=NFLIT SLAV329U
NFLIT=0 SLAV330U
C HAS THE COMPLETE PROGRAM OF 'NMISS' FLIGHTS BEEN COMPLETED SLAV331U
IF(NFLT-NMISS)50,120,120 SLAV332U
C----- SLAV333U
C----- SLAV334U
C----- SLAV335U
C----- SLAV336U
C THIS PATH REPRESENTS A STAGE NOT SINKING SLAV337U
80 CONTINUE SLAV338U
C HAS THIS STAGE COMPLETED MAXIMUM FLIGHT LIFE SLAV339U
IF(NFLIT-MAXLF) 90,110,110 SLAV340U
C NO THIS STAGE HAS NOT COMPLETED MAXIMUM FLIGHT LIFE SLAV341U
90 CONTINUE SLAV342U
C HAS THE COMPLETE PROGRAM OF 'NMISS' FLIGHTS BEEN COMPLETED SLAV343U
IF(NFLT-NMISS)60,100,100 SLAV344U
100 CONTINUE SLAV345U
LEFT=LEFT+1 SLAV346U
GO TO 120 SLAV347U
C YES THIS STAGE HAS COMPLETED MAXIMUM FLIGHT LIFE SLAV348U
110 CONTINUE SLAV349U
NWEAR=NWEAR+1 SLAV350U
NFLIT=0 SLAV351U
C HAS THE COMPLETE PROGRAM OF 'NMISS' FLIGHTS BEEN COMPLETED SLAV352U
IF(NFLT-NMISS)50,120,120 SLAV353U
C----- SLAV354U
C----- SLAV355U
C----- SLAV356U
C----- SLAV357U
C THIS PATH REPRESENTS THE COMPLETION OF THE COMPLETE 'NMISS' SLAV358U
C FLIGHT PROGRAM SLAV359U
C CALCULATE AVERAGE STAGE LIFE SLAV360U
C AND INCREMENT TOTAL NUMBER OF SLAV361U
C STAGES REQUIRED,STAGES WORN OUT,STAGES LOST SLAV362U
120 CONTINUE SLAV363U
BOOST=NBOOST SLAV364U
ALIFE= FLOAT(NMISS)/BOOST SLAV365U
JBUST=JBUST+NBUST SLAV366U
ALIVE=ALIVE+ALIFE SLAV367U
JWEAR=JWEAR+NWEAR SLAV368U
JSINK=JSINK+NSINK SLAV369U
WEAR=NWEAR SLAV370U
TLUST=NSINK SLAV371U
C CALL HISTOGRAM SUBROUTINE TO ACCUMULATE CELL DATA FOR SLAV372U
C SLAV373U
C TOTAL NUMBER OF STAGES REQUIRED HISTOGRAM SLAV374U
C AVERAGE STAGE LIFE HISTOGRAM SLAV375U
C WORN OUT STAGE HISTOGRAM SLAV376U
C LOST STAGE HISTOGRAM SLAV377U
C SLAV378U
C SLAV379U
CALL HISTO(UP,XLOW,CELLW,INIT,BOOST,LIAUD,LCELL,LNTR1) SLAV380U
CALL HISTO(UP1,XLOW1,CELL1,I1ST,ALIFE,LIAD1,LCEL1,NTR1) SLAV381U
CALL HISTO(UP2,XLOW2,CELL2,I2ND,WEAR,LIAD2,LCEL2,NTR2) SLAV382U
CALL HISTO(UP3,XLOW3,CELL3,I3RD,TLUST,LIAD3,LCEL3,NTR3) SLAV383U
C 130 CONTINUE SLAV384U
C----- SLAV385U
C----- SLAV386U
C----- SLAV387U
C----- SLAV388U
C----- SLAV389U
C----- SLAV390U
C----- SLAV391U

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C THIS PATH REPRESENTS THE COMPLETION OF 'NSIM' PROGRAM. SIMULATIONS SLAV392U
C FINAL STATISTICS FOR THE INPUT PARAMETERS ARE CALCULATED AND SLAV393U
C OUTPUT FROM THIS SECTION SLAV394U
C SLAV395U
C SLAV396U
C SLAV397U
C SLAV398U
C SLAV399U
C SLAV400U
C SLAV401U
C SLAV402U
C SLAV403U
C SLAV404U
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C SLAV409U
C SLAV410U
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C SLAV456U
C SLAV457U
C CALL CUMPF(LNTRY,LIAUD,LCELL,PERDS)
C CALL CUMPF(NTRY1,LIAU1,LCEL1,PERD1)
C CALL CUMPF(NTRY2,LIAU2,LCEL2,PERD2)
C CALL CUMPF(NTRY3,LIAU3,LCEL3,PERD3)

C WRITE(KRITE,19U)
C WRITE(KRITE,25U) IRAND
C WRITE(KRITE,32U) NMISS
C WRITE(KRITE,33U) NSIM
C -----
C
C ----- IF(MAXLF-NMISS)160,140,140
140 CONTINUE
WRITE(KRITE,15U)
150 FORMAT(' MAXIMUM STAGE LIFETIME',26X,'INFINITE')
GO TO 170
160 CONTINUE
WRITE(KRITE,24U) MAXLF
170 CONTINUE
C -----
C
C ----- WRITE(KRITE,31U) PLOSS
ABUST=UBUSI
ALEFT=LEFT
AWEAR=UWEAR
ASINK=USINK
ABUST=ABUST/SIM
ALIVE=ALIVE/SIM
AWEAR=AWEAR/SIM
ASINK=ASINK/SIM
ALEFT=ALEFT/SIM
WRITE(KRITE,20U) ABUST
WRITE(KRITE,21U) ALIVE
WRITE(KRITE,22U) AWEAR
WRITE(KRITE,23U) ASINK
WRITE(KRITE,30U) ALEFT
C -----
C ----- WRITE(KRITE,26U) NMISS
CALL WHIST(XLOW,UP,LCELL,PERDS,CELLW,LIAUD,LNTRY,KRITE)
WRITE(KRITE,27U)
CALL WHIST(XLOW1,UP1,LCEL1,PERD1,CELL1,LIAU1,NTRY1,KRITE)
WRITE(KRITE,28U)
CALL WHIST(XLOW2,UP2,LCEL2,PERD2,CELL2,LIAU2,NTRY2,KRITE)
WRITE(KRITE,29U)
CALL WHIST(XLOW3,UP3,LCEL3,PERD3,CELL3,LIAU3,NTRY3,KRITE)

```



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FOR,IS HISTO,HISTO
    SUBROUTINE HISTO (UPLIM,XLOWL,CELLW,I1ST,VAR,IADD,NCELL,INRY)      HIST0000
                                                                HIST0010
                                                                HIST0020
                                                                HIST0030
                                                                HIST0040
                                                                HIST0050
                                                                HIST0060
                                                                HIST0070
                                                                HIST0080
                                                                HIST0090
                                                                HIST0100
                                                                HIST0110
                                                                HIST0120
                                                                HIST0130
                                                                HIST0140
                                                                HIST0150
                                                                HIST0160
                                                                HIST0170
                                                                HIST0180
                                                                HIST0190
                                                                HIST0200
                                                                HIST0210
                                                                HIST0220
                                                                HIST0230
                                                                HIST0240
                                                                HIST0250
                                                                HIST0260
                                                                HIST0270
                                                                HIST0280
                                                                HIST0290
                                                                HIST0300
                                                                HIST0310
                                                                HIST0320
                                                                HIST0330
                                                                HIST0340
                                                                HIST0350
                                                                HIST0360
                                                                HIST0370
                                                                HIST0380
                                                                HIST0390
                                                                HIST0400
                                                                HIST0410
                                                                HIST0420
                                                                HIST0430
                                                                HIST0440
                                                                HIST0450
                                                                HIST0460
                                                                HIST0470
                                                                HIST0480
                                                                HIST0490
                                                                HIST0500
                                                                HIST0510
                                                                HIST0520
                                                                HIST0530
                                                                HIST0540
                                                                HIST0550
                                                                HIST0560
                                                                HIST0570
                                                                HIST0580
                                                                HIST0590
                                                                HIST0600
                                                                HIST0610
                                                                HIST0620
                                                                HIST0630

DARYL D. PAUL JR.
TELEDYNE BROWN ENGINEERING
JANUARY, 1971
MARCH, 1972 (REV. A)

THIS SUBROUTINE IS USED TO ESTABLISH A HISTOGRAM OF INDIVIDUAL
DATA POINTS. SUBROUTINES WHICH SHOULD BE USED IN CONJUNCTION
WITH THIS SUBROUTINE ARE CUMULATIVE PROBABILITY (CUMPF) AND
WRITE HISTOGRAM (WHIST).

DEFINITIONS

CELLW-      WIDTH OF EACH CELL. ESTABLISHED OUTSIDE OF THE          HIST0220
SUBROUTINE                                         HIST0230
I-          CELL NUMBER                                         HIST0240
HIST0250
HIST0260
IADD(I)-    NUMBER OF POINTS OF VAR WHICH FALL IN CELL I.           HIST0270
IADD MUST BE DIMENSIONED IN THE MAINLINE WITH A VALUE          HIST0280
AT LEAST EQUAL TO THE FOLLOWING EQUATION                      HIST0290
NUMBER OF CELLS=((UPLIM-LOWLM)/CELLW)+2.0                  HIST0300
HIST0310
IADD(1)-    ALL VALUES FOR VAR WHICH FALL BELOW LOWLM.          HIST0320
HIST0330
IADD(NCELL)- ALL VALUES OF VAR WHICH FALL ABOVE UPLIM.        HIST0340
HIST0350
HIST0360
HIST0370
HIST0380
HIST0390
HIST0400
HIST0410
HIST0420
HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

I1ST-       NEEDED FOR INITIALIZATION. THIS TERM MUST BE SET TO      HIST0360
ZERO IN THE MAINLINE INITIALIZATION.                           HIST0370
HIST0380
HIST0390
HIST0400
HIST0410
HIST0420
HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

INRY-       THE NUMBER OF POINTS IN THE HISTOGRAM.                   HIST0390
HIST0400
HIST0410
HIST0420
HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

NCELL-     TOTAL NUMBER OF CELLS GENERATED BY THIS SUBROUTINE      HIST0400
HIST0410
HIST0420
HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

UPLIM-     UPPER LIMIT OF HISTOGRAM                                HIST0420
HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

VAR-       VARIABLE FOR WHICH HISTOGRAM IS TO BE OBTAINED.        HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

XLOWL-    LOWER LIMIT OF HISTOGRAM                                HIST0430
HIST0440
HIST0450
HIST0460
HIST0470
HIST0480
HIST0490
HIST0500
HIST0510
HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

DIMENSION IADD(1)                                              HIST0520
HIST0530
HIST0540
HIST0550
HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

INITIALIZE THE SUBROUTINE IF I1ST IS EQUAL TO ZERO
IF (I1ST) 10,10,30                                              HIST0560
HIST0570
HIST0580
HIST0590
HIST0600
HIST0610
HIST0620
HIST0630

10 CONTINUE
CALCULATE NUMBER OF CELLS
NCELL=((UPLIM-XLOWL)/CELLW)+2.0
INITIALIZE NUMBER OF POINTS IN HISTOGRAM.                         HIST0630

```



```

C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

C      FLOAT EACH POINT IN THE HISTOGRAM ARRAY
DO 40 I = 1,NCELL
ADU(I) = IADU(I)
40 CONTINUE
C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

C      ESTABLISH CUMULATIVE PROBABILITY OF THE FIRST CELL
PERDS(1) = ADD(1) / ENTRY
C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

C      INITIALIZE ACCUMULATOR
TEMP = ADD(1)
C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

C      CALCULATE THE CUMULATIVE PROBABILITY OF THE OTHER CELLS
DO 50 J = 2,NCELL
TEMP = TEMP + ADU(J)
PERDS(J) = TEMP / ENTRY
50 CONTINUE
C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

C      RETURN
END
C----- CUMP0640
C----- CUMP0650
C----- CUMP0660
C----- CUMP0670
C----- CUMP0680
C----- CUMP0690
C----- CUMP0700
C----- CUMP0710
C----- CUMP0720
C----- CUMP0730
C----- CUMP0740
C----- CUMP0750
C----- CUMP0760
C----- CUMP0770
C----- CUMP0780
C----- CUMP0790
C----- CUMP0800
C----- CUMP0810
C----- CUMP0820
C----- CUMP0830
C----- CUMP0840
C----- CUMP0850
C----- CUMP0860
C----- CUMP0870
C----- CUMP0880
C----- CUMP0890
C----- CUMP0900
C----- CUMP0910
C----- CUMP0920
C----- CUMP0930
C----- CUMP0940
C----- CUMP0950
C----- CUMP0960
C----- CUMP0970

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LFOR,IS WHIST,WHIST
    SUBROUTINE WHIST(XLOW,UP,LCELL,PERUS,CELLW,LIAUD,LTRY,KRITE)      WHIS0000
C
C-----WHIS0010
C-----WHIS0020
C-----WHIS0030
C-----TELEDYNE BROWN ENGINEERING
C-----DARYL D. PAUL JR.
C-----FEBRUARY, 1972
C-----WHIS0040
C-----WHIS0050
C-----WHIS0060
C-----WHIS0070
C-----WHIS0080
C-----HISTOGRAM(HISTO) AND CUMMULATIVE PROBABILITY (CUMPF) MUST      WHIS0090
C-----BE USED IN CONJUNCTION WITH THIS SUBROUTINE
C-----THIS SUBROUTINE WRITES THE INFORMATION OBTAINED BY HISTO      WHIS0100
C-----AND CUMPF IN A FORM WHICH CONTAINS ONLY THE VALUES BETWEEN THE      WHIS0110
C-----FIRST NON-ZERO CUMMULATIVE PROBABILITY AND THE FIRST CUMMULATIVE      WHIS0120
C-----PROBABILITY OF ONE.      WHIS0130
C-----WHIS0140
C-----WHIS0150
C-----WHIS0160
C-----WHIS0170
C-----WHIS0180
C-----WHIS0190
C-----WHIS0200
C-----DEFINITIONS
C-----CELLW= WIDTH OF EACH CELL. ESTABLISHED OUTSIDE OF THE SUBROUTINE      WHIS0210
C-----JJ= USED TO DETERMINE NUMBER OF LOWEST NONZERO CELL.      WHIS0220
C-----KCELL= NUMBER OF CELL IMMEDIATELY ABOVE THE FIRST CELL      WHIS0230
C-----WITH A CUMMULATIVE PROBABILITY OF ONE      WHIS0240
C-----WHIS0250
C-----WHIS0260
C-----KK= USED TO DETERMINE NUMBER OF THE FIRST CELL      WHIS0270
C-----WITH A CUMMULATIVE PROBABILITY OF ONE      WHIS0280
C-----WHIS0290
C-----WHIS0300
C-----LCELL= NUMBER OF CELLS IN HISTOGRAM.      WHIS0310
C-----WHIS0320
C-----LIAUD= FREQUENCY OF VAR IN CELL      WHIS0330
C-----LTRY= THE NUMBER OF DATA POINTS IN THE HISTOGRAM      WHIS0340
C-----WHIS0350
C-----LOWLM= NUMBER OF CELL IMMEDIATELY BELOW THE FIRST      WHIS0360
C-----NONZERO CELL IN THE HISTOGRAM      WHIS0370
C-----WHIS0380
C-----WHIS0390
C-----N= INDICY FOR WRITING HISTOGRAM      WHIS0400
C-----WHIS0410
C-----PERUS= PERCENT OF CUMMULATIVE PROBABILITY FUNCTION TO CELL      WHIS0420
C-----WHIS0430
C-----TUP= VALUE OF CELL IMMEDIATELY ABOVE THE FIRST CELL      WHIS0440
C-----WITH A CUMMULATIVE PROBABILITY OF ONE      WHIS0450
C-----WHIS0460
C-----WHIS0470
C-----WHIS0480
C-----UP= UPPER LIMIT OF CELL VALUES FOR HISTOGRAM      WHIS0490
C-----WHIS0500
C-----XLOW= LOWER LIMIT OF CELL VALUES FOR HISTOGRAM      WHIS0510
C-----WHIS0520
C-----WHIS0530
C-----WHIS0540
C-----WHIS0550
C-----WHIS0560
C-----WHIS0570
C-----DIMENSION PERDS(1),LIAUD(1)
C-----WHIS0580
C-----WHIS0590
C-----WHIS0600
C-----WHIS0610
C-----WRITE NUMBER OF DATA POINTS IN HISTOGRAM AND THE CELL WIDTH      WHIS0620
C-----WRITE(KRITL,1301) LTRY      WHIS0630

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```

----- WRITE(KRITE+16U) CELLW -----
C
C
C----- SET CELL VALUE INDICATOR TO ONE CELL WIDTH LESS THAN LOWER LIMIT
C TXLOW=XLOW-CELLW
C TUP=UP
C----- FIND THE FIRST CELL WITH A FREQUENCY GREATER THAN ZERO
DO 20 JJ=1,LCELL
IF(PERUS(JJ))10,10,30
10 CONTINUE
TXLOW=TXLOW+CELLW
20 CONTINUE
C----- ESTABLISH AND SET LOWER LIMIT CELL NUMBER INDICATOR
30 CONTINUE
IF(JJ-1) 40,40,50
40 CONTINUE
TXLOW=TXLOW+CELLW
LOWLM=JJ
GO TO 60
50 CONTINUE
LOWLM=JJ-1
60 CONTINUE
C----- FIND FIRST CELL WITH A CUMMULATIVE PROBABILITY OF ONE
DO 70 KK=1,LCELL
IF(PERUS(KK)-1.00) 70,80,80
70 CONTINUE
C----- ESTABLISH AND SET UPPER CELL NUMBER INDICATOR
80 CONTINUE
IF(KK-LCELL)90,100,100
90 CONTINUE
KCELL=KK+1
KK=(LCELL-2)-KK
TUP=TUP-KK*CELLW
GO TO 110
100 CONTINUE
KCELL=KK
TUP=UP+CELLW
C----- WRITE THE NUMBER OF DATA POINTS ABOVE AND BELOW THE UPPER
C AND LOWER LIMITS OF THE PRINTED OUTPUT OF THE HISTOGRAM
110 CONTINUE
WRITE(KRITE+14U) TXLOW,LIADU(LOWLM)
WRITE(KRITE+17U) TUP,LIADU(KCELL)
WRITE(KRITE+18U)

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```

C-----WHIS1300
C-----WHIS1310
C-----WHIS1320
C-----WHIS1330
C-----WHIS1340
C-----WHIS1350
C-----WHIS1360
C-----WHIS1370
C-----WHIS1380
C-----WHIS1390
C-----WHIS1400
C-----WHIS1410
C-----WHIS1420
C-----WHIS1430
C-----WHIS1440
C-----WHIS1450
C-----WHIS1460
C-----WHIS1470
C-----WHIS1480
C-----WHIS1490
C-----WHIS1500
C-----WHIS1510
C-----WHIS1520
C-----WHIS1530

C----- WRITE THE HISTOGRAM
      DO 120 N=LOWLM,KCELL
      WRITE(KRITE,150) TXLOW,LIADD(N),PERUS(N)
      TXLOW=TXLOW+CELLW
120  CONTINUE
C-----WHIS1300
C-----WHIS1310
C-----WHIS1320
C-----WHIS1330
C-----WHIS1340
C-----WHIS1350
C-----WHIS1360
C-----WHIS1370
C-----WHIS1380
C-----WHIS1390
C-----WHIS1400
C-----WHIS1410
C-----WHIS1420
C-----WHIS1430
C-----WHIS1440
C-----WHIS1450
C-----WHIS1460
C-----WHIS1470
C-----WHIS1480
C-----WHIS1490
C-----WHIS1500
C-----WHIS1510
C-----WHIS1520
C-----WHIS1530

130 FORMAT(' NUMBER OF DATA POINTS IN HISTOGRAM',I5)
140 FORMAT(' NUMBER OF DATA POINTS EQUAL TO OR BELOW',F8.2,'=',I3)
150 FORMAT(1X,F10.3,5X,I5,5X,F10.3)
160 FORMAT(' CELL WIDTH =',F7.3)
170 FORMAT(' NUMBER OF DATA POINTS EQUAL TO OR ABOVE',F8.2,'=',I3)
180 FORMAT(7X,'UPPER',8X,'CELL',7X,'CUMULATIVE',5X,'CELL ',8X,'FREQ',WHIS1470
     17X,'PROBABILITY',5X,'LIMIT')
C-----WHIS1480
C-----WHIS1490
C-----WHIS1500
C-----WHIS1510
C-----WHIS1520
C-----WHIS1530

C----- RETURN
      END

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```
IFNR,IS URAND,URAND  
FUNCTION URAND(NR)  
NR=NR*316227  
C THE VALUE IS(2 TO THE 35 POWER)+I  
IF(NR) 10,10,20  
10 NR=NR+34359738367  
20 RN=NR  
URAND=RN/343597384.E2  
RETURN  
END
```

```
URAN000U  
URAN001U  
URAN002U  
URAN003U  
URAN004U  
URAN005U  
URAN006U  
URAN007U  
URAN008U
```