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INVESTIGATION OF CHARACTERISTICS OF FEED SYSTEM INSTABILITIES

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FOREWORD

This final report is submitted in accordance with the requirements of the Statement of Work for Contract NAS8-26266, and documents the work accomplished during the contract period 1 July 1970 through 1 June 1972. This study was performed for the George C. Marshall Space Flight Center of the National Aeronautics and Space Administration, and was administered technically by Mr. Raymond Spink of the Science and Engineering Directorate, Astronautics Laboratory.

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ABSTRACT

In the investigation of structure-propulsion system coupled longitudinal oscillations (POGO), the relationship between the structural and feed system natural frequencies is of major importance. The structural frequencies can be adequately defined by existing analytical techniques. The feed system frequencies are usually very dependent upon the compressibility (compliance) of cavitation bubbles that exist to some extent in all operating turbopumps. The lack of an accurate analytical prediction method for determining cavitation compliance has delayed the completion of POGO stability analyses until after turbopumps have been built and tested.

This document includes: a complete review of cavitation mechanisms; development of a turbopump cavitation compliance model; an accumulation and analysis of all available cavitation compliance test data; and a correlation of empirical-analytical results. The analytical model is based on the analysis of flow relative to a set of cascaded blades, having any described shape, and assumes phase changes occur under conditions of isentropic equilibrium. The model is restricted to incipient blade cavitation and does not include the effects of blade tip clearance or back flow.

Analytical cavitation compliance predictions for the J-2 LOX, F-1 LOX, H-1 LOX and LR87 oxidizer turbopump inducers do not compare favorably with test data. The model predicts much less cavitation than is derived from the test data. This implies that mechanisms other than blade cavitation contribute significantly to the total amount of turbopump cavitation. A current related technology contract (NAS8-27731) is extending the empirical evaluation of test data presented in this document. •

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1. Introduction

1. INTRODUCTION

1.1 <u>Purpose</u> - Longitudinal oscillation instabilities (POGO) due to closed loop coupling between structural modes and propulsion feed system modes have been encountered on most liquid propellant launch vehicles (Reference 1). Experimental evaluation of feed system dynamics in these vehicles has shown that turbopump cavitation is usually the major source of feed system compliance which, along with the effective fluid mass, determines the feed system resonant frequencies. Compliance (C) is defined as the rate of change of fluid mass (W) with respect to pressure (P) for a constant volume; i.e.,

$$C = \frac{\partial W}{\partial P} \qquad \frac{lb_{m} in.^{2}}{lb_{f}} \quad \text{or in.}^{2} \qquad (1.1)$$

Cavitation bubble compliance (C_b) is given by the rate of change of the mass of propellant stored in the turbopump (W_p) with respect to inlet pressure (P_s) . Changes in W_p can be related to changes in cavitation vapor volume (V_v) by

$$C_{b} = \frac{\partial W_{p}}{\partial P_{s}} \approx -\frac{\rho \frac{\partial V_{v}}{\partial P_{s}}}{\partial P_{s}}$$
(1.2)

where ρ is the liquid density and the mass of vapor is small relative to the mass of liquid.* Some previous analytical and semi-empirical attempts (Section 2.3) have been made, usually using average geometry parameters and flow conditions through the turbopump, to predict the amount of cavitation. Confidence in these methods has never been sufficient to eliminate the requirement to perform dynamic response tests on new turbopump

^{*} In some of the literature C_b is defined as $\partial V_v / \partial P_s$ which can be related to the values presented in this report by multiplying by the appropriate propellant density.

configurations. The lack of available test hardware during design phases is one of the major reasons that POGO suppression has been worked as a post flight effort on all past launch vehicles. The technology effort documented in this report is aimed at producing increased confidence in pre-test POGO stability analysis on future launch vehicle programs like the Space Shuttle Vehicle. This study is closely related to three other current Space Shuttle Technology programs: contract NAS8-26250, "Research on Cavitating Pump Instabilities", Hydronautics Incorporated; contract NAS8-25919, "Analysis of Propellant Feedline Dynamics", South West Research Institute; and contract NAS8-27731, "Empirical Evaluation of Pump Inlet Compliance", Aerospace Corporation.

1.2 <u>Objectives</u> - The intent of this investigation is to establish the relationships between turbopump inlet compliance and the pump parameters and fluid properties that control or define the compliance mechanism. The correlation is to be established with an analytical and/or semi-empirical model which is verified with existing test data. It is desired that the correlations be formulated and presented such that the frequency response characteristics of a cryogenic feed system can be evaluated for a given vehicle configuration. It is desired that the deviation in feed system resonant frequency between analytical and empirical results not exceed ±10%.

1.3 <u>Scope</u> - This study deals primarily with the determination of turbopump cavitation compliance, the largest element of uncertainty in dynamic modeling of feed systems. Feed system models, incorporating cavitation compliance, are well understood and range from very simple models (Paragraph 4.1.3) to fairly complicated models (References 2 and 3). A general feed system computer model was provided to NASA under contract NAS8-23511. Also, detailed feed system modeling is currently being performed under contract NAS8-25919. For these reasons, no complex feed system models are presented in this report.

1.3.1 Since cavitation compliance is required for determination of feed system frequency response characteristics for use in POGO stability analysis, only linear response characteristics are of interest. Also, only the normal flight operating range of a turbopump is considered. These two conditions permit the analysis of turbopump cavitation to be restricted to the region of incipient cavitation, and does not consider the region of gross cavitation where turbopump operating performance is significantly reduced. The analytical model developed deals with thermal vapor cavitation between the turbopump blades. It does not include gaseous cavitation, or cavitation resulting from back flow or blade tip clearance flow, although these effects are discussed.

1.4 <u>General Approach</u> - The general approach taken to meet the study objectives within the scope specified was to:

- a. Review all literature relative to turboyump cavitation;
- b. Develop an analytical model to predict cavitation compliance;
- c. Analyze all available cavitation compliance test data;
- d. Perform an evaluation of the test data;

e. Correlate the analytical and test results.

The model development portion of this study is a continuation of a portion of a general POGO technology contract conducted for the Air Force Rocket Propulsion Lab (References 4 and 5). The analytical cavitation model is a fluid dynamic/thermodynamic model which employs the compressible flow equations in finite difference form and solves them iteratively. Isentropic conditions of thermodynamic equilibrium between the vapor (cavitation) and liquid phases are assumed. The solution yields the amount of vapor at many grid points in a turbopump streamsheet of revolution (an annulus between two blades). A combination of several streamsheets at different blade radii gives the total turbopump cavitation, which when related to a change in inlet pressure, results in cavitation compliance. This approach accounts for varying conditions of fluid flow and blade geometry throughout the turbopump.

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2. Review of Cavitation Mechanism

2. REVIEW OF CAVITATION MECHANISM

2.1 Turbopump Operation - Turbopumps used in present rocket propulsion systems are generally of the mixed flow design. The pump fluid while in the impeller has, in addition to angular velocities, both axial and radial velocity components as opposed to the predominantly radial velocities associated with centrifugal water pumps. In most cases, the turbopump will have an inducer section upstream of the main impeller that improves fluid angle of attack and increases the pressure at the inlet to the impeller. This allows further reduction in NPSH before blade stall and a loss in head rise (pressure increase from inlet to discharge) occurs. In some configurations, the impeller and inducer are of one piece construction, the inducer blades transitioning into impeller blades with additional impeller blades starting at some distance into the turbopump. The pressure rise through the inducer makes it probable that the majority of the turbopump cavitation occurs in the inducer. This is because the average pressure at the impeller inlet is generally too high for any local blade surface pressure to be reduced to the vapor pressure.

2.1.1 Shrouded blades of proper design, operating at the design point and free of vapor represent an analytical idealization in that channel type flow exists between the blades. Most turbopumps, however, are not designed with completely shrouded blades, and the channel flow idealization cannot be realized. In this situation, the flow picture is complicated by a tip clearance flow between the moving blades and the stationary shroud. The tip clearance flow, which is from the pressure side of a blade to the suction side, often induces a vortex 5

near the outer edge of the blades on the section side. If the blades are improperly designed or arc being operated off the design conditions, a liquid-filled separation cavity may be attached to the leadung edge. This is more likely when the blade leading edges are quite sharp. Although the impeller will still pump fluid with an associated pressure rise, it is accomplished at a reduced efficiency.

2.1.2 The complexity of the flow situation increases with the appearance of vapor phases. If the velocity gradients are not large and the inducer blades have large radii of curvature associated with the leading edge region, the vapor phases, which consist of dissolved gas coming out of solution and/or a change in phase of the pump fluid, will appear as a region of bubbles moving with the fluid. On the other hand, it a liquid-filled separation cavity exists before the appearance of vapor, the cavity may fill with vapor when it evolves and expand with further reduction in suction pressure. Such covidies that originate near the leading edge of the blade may reattach on the downstream side of the blade or, if severely low pressures exist, extend downstream into the discharge portion of the pump. Although separation cavities may not exist before the appearance of vapor, the density change and disturbances associated with the evolution of vapor may induce separation of the boundary layer and create a cavity. In both types of two-phase flow, the variations of density add considerable complexity to the analysis problem.

2.2 <u>Sources of Cavitation</u> - Cavities may exist in the turbopump liquid propellant due to the presence of either vapor bubbles produced by liquid boiling, hereafter referred to as thermal cavitation; or contaminant gas bubbles, hereafter referred to as gaseous cavitation.

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2.2.1 Thermal Cavitation - Thermal cavitation results when the ambient pressure drops below the saturation pressure, or the fluid temperature rises above the saturation temperature. Pressure changes may be associated with quasi-steady fluid motion, transient fluid motion, or acoustic excitation. Temperature changes can result from heat transfer across the boundaries of the system, fluid motion, and phase changes of the fluid (latent heat of vaporization and condensation). For an isentropic process, a change in pressure produces a phase change, which results in a change in fluid temperature, which in turn tends to impede the phase change. With sufficient time, thermodynamic equilibrium is reached and there exists a given amount of vapor for a given pressure. For bubble growth and decay under conditions of non-thermodynamic equilibrium, the mathematics defining the rate of change of bubble size are given in Appendix A.

2.2.2 <u>Gaseous Cavitation</u> - Gaseous cavitation can occur from the following sources:

- a. Dissolved gases coming out of solution;
- b. Undissolved gases mixed with the propellant;
- c. Chemical reaction (corrosion) between the propellant and the turbopump.

Substantial concentrations of both dissolved and undissolved foreign gases, such as atmospheric air or blanket gases used to hold the fluid under pressure before entrance to the pump, may also be present in propellants which have been stored for either long periods of time or under very low gravity conditions. Changes in the ratio of dissolved to undissolved gas can result from changes in fluid velocity, acoustic excitation, or heat transfer. Undissolved gas may also exist as a result of a Gas Bubbling POGO Suppression Device (References 6 and 7). The problem of corrosion is not normally encountered in current propulsion systems. Even if storage and utilization of propellants are controlled so that an insignificant amount of gaseous cavitation occurs, small amounts of dissolved gases may be instrumental in the initial formation of a thermal cavitation vapor bubble (Paragraph 2.3.2).

2.3 <u>Previous Cavitation Analyses</u> - Analysis of turbopump cavitation compliance was initiated with a review of existing knowledge on cavitation. Discussion of this review and the conclusions derived follow.

2.3.1 <u>Turbopump vs Other Types of Cavitation - Considerable</u> investigation has been performed in the field of cavitation. Areas that have received the most attention have been pump cavitation, hydrofoil and hydrodynamic propeller cavitation, cavitation on such underwater vehicles as submarines and torpedos, and cavitation induced by sound waves. The majority of investigations associated with pumps have been experimental or semiempirical with the objective of preventing cavitation damage by determination of incipient cavitation conditions (References 8 and 9). Investigations of hydrofoils, propellers, and underwater vehicles have been aimed at predicting lift and drag coefficients and reducing noise associated with cavitation bubble collapse. Ultrasonic cavitation research has been directed primarily toward assessing sound energy and frequency requirements to induce cavitation, and examining the attenuation and distortion of sound waves caused by the cavitation bubbles.

2.3.2 Nucleation - If gas-filled voids exist in a fluid (References 10 and 11), changes in the concentration of dissolved gases and changes in phase within the fluid will take place at the boundary of the voids as well as at the fluid surface. The presence of voids in a fluid is suggested by the cohesive strength of water. Predictions of cohesive strength based on breaking the van der Waals intermolecular bonds exceed experimental observations by several orders of magnitude. The source of this large discrepancy is attributed to the presence of contaminants in the water that form voids of nuclei on the order of 10^{-5} to 10^{-2} cm in diameter. Since it is known that large amounts of air can be dissolved in water, it is hypothesized that the voids of nuclei are filled with contaminant gases such as air or mixtures of gas and fluid vapor. This hypothesis only partially explains the observed fracture strength of water. A nucleus containing contaminant gas and vapor will be in static equilibrium in the fluid if

$$P_{v} + P_{G} - P_{\infty} = 2\sigma/R \qquad (2.1)$$

(0 1)

where

 $P_v = vapor pressure$ $P_G = sum of partial pressures of contaminant gases$ $P_{\infty} = ambient pressure$ $\sigma = surface tension constant$ R = radius of nucleus

If the nucleus contains only vapor and its radius is given by Equation (2.1), it is in a condition of unstable equilibrium and will either grow or collapse upon being disturbed.

2.3.2.1 Gas-filled nuclei on the order of 10^{-5} to 10^{-2} cm in diameter present in an undersaturated or saturated solution of

water (saturation in this context refers to the concentration of dissolved gas) dissolve in a few minutes or beconds depending on the radius of the nuclei and the dissolved gas concentration. The dissolving process is assisted by the surface tension force $2\sigma/R$. A nucleus of this size, if present in a supersaturated solution of water, grows by diffusion of gas into the nucleus and floats to the surface of the water where it escapes. The rate of rise of a nucleus of 10^{-5} cm in diameter is very slow and may take several hundred hours to escape from the liquid. Water that has been allowed to set a long time still fails to demonstrate the expected cohesive strength. A mechanism or mechanisms, therefore, that prevents the diffusion of gas out of the nuclei and/or prevents nuclei from rising to the surface of the fluid must be acting. Two hypotheses advanced are:

- a. Surface films composed of algae or other contaminants form around the nuclei and act as barriers to the diffusion process;
- b. The nuclei are held in surface cracks of the fluid
 container or on dust particles suspended in the fluid.

The first hypothesis has been demonstrated by Bernd (Reference 12) in experiments where the cohesive strength of various fluids has been manipulated by control of the algae content. Rosenberg (Reference 13) has shown analytically and experimentally that the walls of the fluid containers can have cracks in which nuclei can be attached in a stable condition. In the same work, it was shown that dust particles or colloidal matter in the fluid can have cracks upon which the nuclei can be stabilized. An aspect of Rosenberg's investigation that will require further attention is the observed difference in susceptibility of various liquids to contamination by dust. 2.3.2.2 The nuclei are the focal points that govern changes in dissolved gas concentration and changes in phase (Reference 14). Regarding changes in phases, nucleation action occurs not only for the growth of vapor bubbles, but also for their collapse. The presence of contaminant dust particles in the bubble and on its surface serve as nuclei upon which additional condensation can take place.

2.3.2.3 The preceding discussion shows that cavitation in a turbopump will depend on the number of nuclei present in the fluid, their size, and conditions that will affect their dynamic behavior. It is important, therefore, that methods be developed for assessing the effects of fluid characteristics on nucleation.

2.3.3 Diffusion - A decrease in the concentration of dissolved gas in the pump fluid will result from diffusion of dissolved gas into nuclei present in the fluid. If the diffusion process continues, the nuclei will grow into gas bubbles and the phenomenon of gaseous cavitation will be observed. The diffusion process in a pump can be driven by changes in either pressure or temperature. Once the temperature and pressure conditions have been altered to a condition that favors diffusion of gas out of the cavitation bubble, the bubble will decrease in size. Although conditions return to those existing at inception of bubble growth, the contracting bubble may reach an equilibrium volume substantially greater than that of the original nucleus. This phenomenon is demonstrated by tests of the cohesive strength of water. Water that has been subjected to gaseous cavitation has a fracture strength considerably less than it had before cavitation. This results from the presence of nuclei after cavitation that are larger than those that existed before cavitation. Plesset and Epstein (Reference 15),

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ignoring the effects of the motion of the bubble boundary on the concentration gradient in the liquid, have derived the equation governing the diffusion of gas into and out of a static bubble. Their results, if applied directly to turbopumps, show that the characteristic time for bubble growth is too large to cause cavitation. The boundary conditions for the derivation, however, differ considerably from those that will exist in a turbopump. The effects of bubble boundary motion and turbulence on the gaseous concentration gradient serve to accelerate the bubble growth. Future work, therefore, should incorporate these effects into a more accurate description of the diffusion process.

2.3.4 Acoustic Cavitation - As previously stated, changes in the ratio of dissolved to undissolved gas in a fluid can occur due to acoustic excitation. The generation of sound in a fluid results in an oscillatory pressure throughout the fluid. The pressure disturbances in turn result in an oscillation of the boundary of nuclei in the fluid. With a fluid saturated or supersaturated with dissolved gas, the nuclei may grow into gas bubbles given the proper amplitude and frequency of acoustic excitation. The growth is achieved through the rectified diffusion of gas into the bubble. During the low-pressure or expansion phase of bubble oscillation, conditions result in diffusion of gas into the bubble. During compression of the bubble, gas diffuses out; however, due to the large time surface area associated with the bubble expansion, a net inflow of gas occurs. Because of the extreme noises associated with rocket engines, this type of cavitation should not be ignored when analyzing rocket turbopumps.

2.3.5 <u>Thermodynamics</u> - The cavitation problem requires consideration of many thermodynamic effects. Literature on the subject of thermal cavitation may be divided into two areas. The first of these deals with the effect of heat transfer on cavitation bubble growth. The nonsteady heat diffusion problem with moving boundaries has been solved by Plesset and Zwick (Reference 16). The same authors have combined the results of the heat diffusion problem with the equations of motion for bubble growth to obtain a solution for the case of constant ambient pressure (Reference 17). Skinner and Bankoff (Reference 18) as well as Forster and Zuber (Reference 19) have taken slightly different approaches and obtained similar results. The bubble growth problem with variable ambient pressure and inclusion of terms containing P_{tr} is still unsolved.

2.3.5.1 Other investigators such as Stepanoff (References 20 and 21) and Jakobsen (Reference 22), rather than examine thermal cavitation on a microscopic basis, choose to derive semiempirical macroscopic descriptions. The results of this approach suffer from inability to correlate a particular value of pump head dropoff with volume of vapor present over a wide range of operating conditions. Furthermore, the results cannot justifiably be used to predict the vapor volume, because a number of assumptions and empirical factors do not accurately describe the vapor formation process.

2.3.5.2 Future work on thermal cavitation should take two directions. The first, referred to as the equilibrium approach, should examine the thermal cavitation phenomenon assuming thermal equilibrium phase changes. For pumps that have gradual changes in pressure through the system and low fluid velocities, the equilibrium approach may give entirely satisfactory results; and, thereby, negate the need for a microscopic examination. The second method should be a microscopic examination of cavitation in which large pressure gradients and velocities produce metastable changes of phase. For cryogenic fluids, the effects of heat transfer across the boundaries of the system should be included in both methods of analysis. The thermodynamic properties of the fluid should be examined clouely to determine whether certain characteristics simplify or complicate the solution of the thermal cavitation equations.

2.3.6 Fluid Mechanics - Like thermodynamics, there are many branches of fluid mechanics drawn on for examination of turbopump cavitation. The flow of liquid through a turbopump to the inception of cavitation can be examined with the incompressible flow equations. In the pump, cavitation may appear in a number of forms. If the leading edges of the impeller blades are very sharp, a separation cavity may be attached to the suction side of the blade. Depending on the fluid velocity, pressure, and boundary layer conditions, the cavity may close on the downstream suction side of the blade or may extend through the pump in a condition known as supercavitation. Examinations of separation cavities as related to turbopump cavitation have been made by Stripling and Acosta (References 23 and 24). This method predicts the geometry of the cavity up to the point of maximum height based on fluid momentum considerations; however, the reattachment or cavity closure conditions remain arbitrary. The work of Wade (Reference 25) applies to the conditions of cavities closing on the blade. The most recent and most elegant application of the Stripling and Acosta method is that developed by Davis, Coons and Scheer (Reference 26). This application

couples the Stripling-Acosta model to a two dimensional impeller flow field including boundary layer displacement effects. The primary objective of this model was to predict blade loading under cavitating conditions. Comparing its results with test data showed that it accomplished this purpose very well. Its use for predicting cavitation compliance is much more questionable due to a greater sensitivity to the assumed closure conditions. After documentation of the Stripling and Acosta work, different investigators have claimed that various pieces of experimental data (mostly photographic data, e.g., Reference 32) support either the separation cavity theory or the thermal equilibrium mixed flow concept. Our own review of this data suggests that it is inconclusive for the most part in offering substantial supporting evidence for either theory.

2.3.6.1 Unfortunately, the assumptions for the mathematical models, such as a blade leading edge radius of curvature equal to zero are seldom if ever physically realizable. If the blade is very thick and has a large leading edge radius of curvature, the flow may remain attached, and cavitation will appear as a mixture of vapor bubbles and liquid that demonstrates compressible flow characteristics. In this type of cavitation, the growth and collapse of vapor bubbles require fluid-mechanic examination. Plesset (References 17, 27 and 28) has examined the growth phenomena under conditions of constant ambient pressure and bubble vapor density. Both Gilmore (Reference 29) and Hunter (Reference 30) have taken into account compressibility and shock effects encountered during bubble collapse.

2.3.6.2 The effect of gas bubbles on the sonic velocity in a fluid represents another area that has received attention in

cavitation investigations. Figure 2.1 shows the variation in sonic velocity as a function of gas content for a mixture of water and air. It is seen that the sonic velocity can drop to a very low value that may result in sonic choking in the turbopump. Ghahremani (Reference 31) uses the work of Jakobsen (Reference 22) and assumes that fully choked flow exists at head breakdown (no pressure rise through the turbopump). Somewhat arbitrary assumptions, requiring empirical correlation, are then made to relate the fully choked conditions to normal operating conditions of unchoked or partially choked flow. The Ghahremani approach is unique in that the theory includes the effects of blade tip clearance backflow which, according to his results, produce more cavitation than occurs on the blade suction surface.

2.3.6.3 Attention in future fluid-mechanic investigations of cavitation should be given to determination of the conditions necessary for and which influence the geometry of separation cavities; and development of the flow equations for a vaporliquid mixture in a turbopump. Incorporated into these equations should be the effects of bubble growth and collapse on the surrounding fluid. Also, the approach related to sonic choking at head breakdown should be refined.

2.4 <u>A General Cavitation Analysis</u> - From the preceding review of existing investigations of cavitation, it is possible to construct a plan for solution to the general cavitation compliance problem. This plan, which itemizes the various areas of investigation and integrates these areas into a completely general analysis, is outlined in the following paragraphs. The analytical investigations conducted during this program were restricted to fluid-mechanics with thermodynamic cavitation, which occurs on an equilibrium basis.

2.4.1 Nucleation

- a. Number of nuclei;
- b. Size distribution of nuclei;
- c. Conditions in fluid or vapor that affect the dynamic behavior of nuclei.

2.4.2 Acoustic Cavitation

- a. Identification of sound sources;
- Assessment of power and frequency characteristics of each source;
- c. Wave transmission in the fluid mechanic system.

2.4.3 Diffusion

- a. Identification of dissolved gas species and assessment of their relative concentrations;
- Evaluation of diffusion rates into nuclei or out of gas bubbles under both laminar and turbulent flow conditions;
- c. Determine effects of contaminants on diffusion rates.

2.4.4 Thermodynamics

- a. Examination of thermal cavitation on a microscopic or dynamic basis;
- b. Examination of thermal cavitation on a thermal equilibrium basis;
- c. Thermodynamic properties of fluids;
- d. Heat transfer across system boundaries.

2.4.5 Fluid Mechanics

- a. Hydrodynamics of turbomachinery without cavitation;
- Hydrodynamics of turbomachinery with cavitation, but without separation cavities;
- c. Bubble hydrodynamics;
- Hydrodynamics of turbomachinery with separation cavities attached to blades;
- Compressibility effects in fluid including shock phenomena;
- f. Effects of tip clearance flow and backflow.

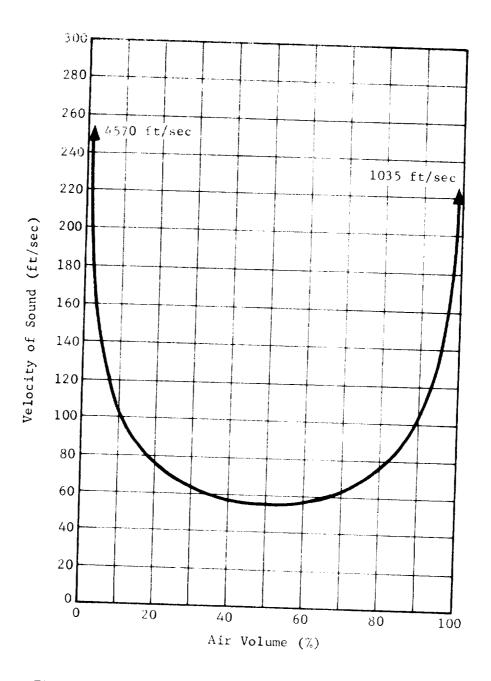


Figure 2.1 Variation of Isothermal Velocity of Sound in Water Containing Air Bubbles

3. Turbopump Cavitation Model

3. TURBOPUMP CAVITATION MODEL

3.1 <u>Model Requirements</u> - As outlined in Section 2.4, a complete analysis of turbopump cavitation compliance will require a complex model of the turbopump based upon the physical equations describing the fluid mechanic and thermodynamic phenomena occuring in the pump. The purpose of this program was to develop such a model; but, on a very fundamental basis, in order to evaluate the validity of such a model and identify the associated programming and numerical analysis problems. If the feasibility and engineering usefulness of a basic program could be demonstrated the more complex effects of fluid viscosity, gas diffusion, and nonequilibrium thermodynamics could be added to the program with considerably more confidence of success.

3.1.1 A prime objective of the cavitation compliance model development was to derive mathematical descriptions that could be related directly to the physical situation in a turbopump. Semiempirical approaches were discarded because of their inability to account for all the different design considerations. This is particularly true considering the lack of any empirical data which relates changes in cavitation compliance to changes in specific turbopump geometry parameters. The required mathematical descriptions, which are consistent with the objectives and scope of this study, are:

- a. Basic turbopump flow equations into which two-phase flow phenomena can be incorporated and which could later be expanded to include more complex flow situations;
- b. A thermal cavitation model which is independent of time and conditions of nucleation and which can be

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combined with the flow equations to give a description of turbopump cavitation compliance;

c. A finite difference iteration algorithm which allows solution of the flow and cavitation equations for any given blade geometry and flow conditions.

3.2 <u>Model Assumptions</u> - The assumptions made in the development of the turbopump model pertain to the cavitation process, the fluid-mechanics, and the turbopump configuration. The assumptions were required in order to obtain a solution for cavitation compliance within the scope of this study. The first two assumptions related to the cavitation process determine the basic approach of the analytical effort.

3.2.1 <u>Channel Flow</u> - The fundamental assumption of the turbopump model is that channel flow exists approximately between the pump inducer and impeller blades. This assumption can be used to separate the three-dimensional flow problems into two-dimensional problems. The first problem is that of defining the flow stream-lines in the meridional plane. This can be accomplished by the method described in Appendix A, or by a more approximate method wherein the streamlines and associated streamtube width (b in Figure 3.2) is related to the inducer or impeller hub and shroud geometry by a suitable function. With a meridional plane description of the streamlines, one can proceed with the development of the blade to blade flow equations along a surface generated by rotating a meridional plane streamline about the impeller axis. This development is presented below in Section 3.3.

3.2.2 <u>Thermal and Velocity Equilibrium</u> - The liquid-vapor phase change is assumed to occur under isentropic conditions of thermodynamic equilibrium with both phases in velocity equilibrium. An equation that deals with nonequilibrium changes of phase (vapor bubble growth) for a single bubble is presented in Appendix B. This derivation includes the effects of heat transfer at the bubble wall, varying ambient pressure, and variable density of the vapor within the bubble. Unfortunately, a complete solution to the resulting integro-differential equation was not obtained. Solutions were found in the literature for simplified versions of the equation; however, the solutions sacrificed the inertial effects to gain a description of the thermodynamic effects or vice versa. The assumed condition of equilibrium applies to the bubble growth and decay both as the fluid passes through the turbopump encountering different local pressures, and as the local pressures change as a result of changes in the turbopump inlet pressure. Some test results (Reference 4) at very low static inlet pressure (6 to 10 psi) and large pressure oscillation amplitudes (10 to 20 psi peak to peak) indicate that the cavitation process is not in equilibrium, and that the amount of compliance is a function of the frequency of the pressure oscillations. The extrapolation of this data to small amplitudes and flight pressures is not possible. Since this model is more concerned with cavitation compliance (rate of change of cavitation with respect to pressure) than with the amount of cavitation, the equilibrium assumption should be more valid because the period of pressure oscillation is greater than the average bubble life (Paragraph 3.2.5).

3.2.3 <u>Tip Clearance and Backflow</u> - An additional restriction which is implied by the channel flow assumption is that there is no tip clearance flow or backflow within the pump. The model only computes envitation as a result or channel flow between cascaded blades and does not consider cavitation which may occur from either blade tip clearance flow or from backflow into the suction line (backflow is produced by tip clearance flow). These other sources may have a significant effect when considering unshrouded blades. Based on analysis, Ghahremani (Reference 31) theorizes that tip flow cavitation is much larger than blade cavitation. The only tests concerned with tip clearance flow evaluated the effect on performance for a gas medium (Reference 33) instead of a liquid, and for a variation in the axial clearance of the impeller tip (Reference 34) instead of a radial clearance of the inducer tip. A test program to investigate the effect of tip clearance flow and backflow would be very beneficial to the understanding of the complete turbopump cavitation process.

3.2.4 <u>Incipient Cavitation</u> - The model is developed for conditions of incipient cavitation only. This restriction is necessary because in deep cavitation local fluid velocities may approach the local speed of sound, whereupon the finite difference solution scheme becomes invalid. Since turbopumps do not usually operate in the region of deep cavitation, this is not considered to be a severe restriction.

3.2.5 <u>Steady Flow</u> - Since cavitation compliance is related to an oscillatory change in inlet pressure, unsteady flow conditions are implied. However, since the period of oscillation is typically 50 times greater than the time required for a fluid element to pass through the cavitation region, it is valid to assume quasi-steady flow; i.e., cavitation compliance can be obtained from a steady state solution at different turbopump inlet pressures. 3.2.6 <u>Inviscid Flow</u> - A further assumption which must be used is that the flow is inviscid. A solution of the complete viscous flow equations would compound the overall computational problems and is not warranted until the usefulness of the basic inviscid approach is demonstrated.

3.2.7 <u>Separation Cavities</u> - The computer model of turbopump cavitation was developed on the basis that no separation cavities were present in the blade system. This restriction is actually necessary only when the vapor phase is present in the pump. Solutions can be obtained with separation cavities for incompressible or non-cavitating flow; however, diverging solutions appear whenever two phase flow is encountered.

3.2.8 <u>Identical Blades</u> - The final assumption of the model development requires that all blades within the pump inducer or impeller are identical. This restriction was necessary in order to simplify the computer programming and to meet core limitations on the computer. In most pumps, the inducer section where most cavitation occurs is made up of identical blades. In the impeller section, however, partial blades are quite often placed between the main blades. The capability of treating non-identical blade systems can be added to the program, but would require an overlay technique and, consequently, some re-programming.

3.3 Equation Development - The development of the nonseparated, thermal equilibrium cavitation flow equations for a blade-to-blade analysis are discussed below along with the pump blade coordinate transformations used to simplify the numerical solutions. Figure A.1 shows the coordinate system used for derivation of the flow equations. The coordinate system is rotating about the Z axis with angular velocity ω . The velocities shown, therefore, are relative to the pump blades. The equation development derives two basic equations: a fluid flow equation, and an energy equation. The flow equation is derived from potential theory utilizing a continuity equation and the condition of irrotational flow. The energy equation is derived by relating the fluid energy to the inlet energy and the work done by the turbopump. Changes in thermal energy are obtained from the assumed condition of thermal equilibrium. The final form of the two equations is written in terms of the stream function, ψ , and the density ρ .

3.3.1 <u>Flow Equation</u> - From a solution to the flow problem in the meridional plane (Appendix A), a streamline and its associated streamtube can be defined as shown graphically in Figure 3.1. Rotation of the streamtube about the impeller axis results in a streamtube of revolution while a stream surface is generated by the meridional streamline. With reference to Figure 3.2, which shows a segment of the streamtube, the flow continuity equation is derived as follows. Using the segment of the streamtube as a control volume, the conservation of mass is expressed by

$$\sum \left(\dot{W}_{in} - \dot{W}_{out} \right) = \frac{d}{dt} (W) = 0$$
(3.1)

where \dot{W} is the flowrate. $\frac{d}{dt}$ (W) is the time rate of change of the weight of fluid in the control volume, which is zero for steady flow. In the M direction,

$$\begin{split} \mathbf{\hat{w}}_{\text{in}} - \mathbf{\hat{w}}_{\text{out}} &= (\rho \mathbf{V}_{\text{M}} \mathbf{b}) \mathbf{r} \, d\theta - \left[\rho \mathbf{V}_{\text{M}} \mathbf{b} + \frac{\partial}{\partial \mathbf{r}} (\rho \mathbf{V}_{\text{M}} \mathbf{b}) \, d\mathbf{r} \right] (\mathbf{r} + d\mathbf{r}) \, d\theta \\ &= - \left[\rho \mathbf{V}_{\text{M}} \mathbf{b} \, d\mathbf{r} \, d\theta + \frac{\partial}{\partial \mathbf{r}} (\rho \mathbf{V}_{\text{M}} \mathbf{b}) d\mathbf{r} \, \mathbf{r} \, d\theta + \frac{\partial}{\partial \mathbf{r}} (\rho \mathbf{V}_{\text{M}} \mathbf{b}) d\mathbf{r}^2 \, d\theta \right] (3.2) \end{split}$$

In the θ direction,

$$\dot{W}_{in} - \dot{W}_{out} = \rho V_{\theta} \ b \ \frac{dr}{\sin \alpha} - \left[\rho V_{\theta} + \frac{\partial}{\partial \theta} \left(\rho V_{\theta} \right) d\theta \right] b \ \frac{dr}{\sin \alpha}$$
$$= - \frac{\partial}{\partial \theta} \left(\frac{\rho V_{\theta} \ b}{\sin \alpha} \right) d\theta \ dr \qquad (3.3)$$

Using the above relationship, Equation (3.1) becomes:

$$\rho V_{M} b dr d\theta + \frac{\partial}{\partial r} (\rho V_{M} b) dr r d\theta + \frac{\partial}{\partial r} (\rho V_{M} b) dr^{2} d\theta$$
$$+ \frac{\partial}{\partial \theta} \left(\frac{\rho V_{\theta} b}{\sin \alpha} \right) dr d\theta = 0 \qquad (3.4)$$

Dividing through by $r d\theta b \frac{r}{\sin \alpha}$, and taking the limit as dr and $d\theta$ approach zero, Equation (3.4) becomes

$$\frac{\partial}{\partial \mathbf{r}} \left(\rho \mathbf{V}_{\mathrm{M}} \mathbf{b} \mathbf{r} \right) + \frac{\partial}{\partial \theta} \left(\frac{\rho \mathbf{V}_{\theta} \mathbf{b}}{\sin \alpha} \right) = 0$$
(3.5)

A stream function ψ that satisfies Equation (3.5) is then defined by

$$\frac{\partial \Psi}{\partial \theta} = \rho V_{\rm M} \, b \, r \tag{3.6}$$

$$\frac{\partial \Psi}{\partial \mathbf{r}} = -\frac{\rho V_{\theta} \mathbf{b}}{\sin \alpha}$$
(3.7)

With the further assumptions that the fluid is inviscid and that its absolute motion is irrotational, another equation for fluid motion can be derived. For absolute irrotational flow the circulation, Γ , around the fluid segment (Figure 3.3) must be zero.

If $\Gamma = 0$, then $d\Gamma = 0$, or

$$d\Gamma = 0 = \left[\frac{\partial}{\partial r}\left(r\omega + V_{\theta}\right)r\theta\right]dr - \frac{\partial}{\partial\theta}\left(\frac{V_{M}dr}{\sin\alpha}\right)d\theta \qquad (3.8)$$

Differentiating:

$$2\mathbf{r} + \mathbf{V}_{\theta} + \mathbf{r} \frac{\partial \mathbf{V}_{\theta}}{\partial \mathbf{r}} - \frac{\partial \mathbf{V}_{M}}{\partial \theta} \frac{1}{\sin \alpha} = 0$$
(3.9)

At this point, a transformation of the pump blade coordinates facilitates programming of the problem for computer solution. The transformation will depend on the blade shape. However, the objective of the transformation is to straighten the blade such that the leading edge becomes the maximum of the blade angular coordinates and the trailing edge the minimum. For an inducer a transformation such as dE = dZ and $dF = d\theta$ may be the most appropriate. For an impeller having logarithmic spiral blades, the following transformation is most convenient.

$$dE = \frac{1}{\sin \alpha} \frac{dr}{r}$$
(3.10)

$$dF = d\theta \tag{3.11}$$

Carrying the equation development through, using this last transformation, Equation (3.9) becomes

$$2r_{\Theta} + V_{\theta} + \frac{1}{\sin \alpha} \left[\frac{\partial}{\partial E} \left(V_{\theta} \right) - \frac{\partial}{\partial F} \left(V_{M} \right) \right] = 0$$
(3.12)

Combining Equations (3.6), (3.7) and (3.12) results in

4

$$2r \omega \sin \alpha - \frac{\sin \alpha}{\rho br} \frac{\partial \psi}{\partial E} + \frac{1}{\rho^2 r b} \frac{\partial \rho}{\partial E} \frac{\partial \psi}{\partial E} + \frac{\sin \alpha}{b \rho r} \frac{\partial \psi}{\partial E} + \frac{1}{\frac{\partial \rho}{\partial E}} + \frac{1}{\rho^2 r b} \frac{\partial \phi}{\partial E} \frac{\partial \psi}{\partial E} - \frac{1}{\rho br} \frac{\partial^2 \psi}{\partial E^2} - \frac{1}{\rho br} \frac{\partial^2 \psi}{\partial F^2} + \frac{1}{\rho^2 r b} \frac{\partial \psi}{\partial F} \frac{\partial \rho}{\partial F} = 0$$
(3.13)

which in turn reduces to

$$2r^{2}_{\omega b\rho} \sin \alpha + \frac{\partial \Psi}{\partial E} \left[\frac{\partial}{\partial E} \left(\ell n \rho \right) \right] + \frac{\partial \Psi}{\partial E} \left[\frac{\partial}{\partial E} \left(\ell n b \right) \right] - \frac{\partial^{2} \Psi}{\partial E^{2}} - \frac{\partial^{2} \Psi}{\partial F^{2}} + \frac{\partial \Psi}{\partial F} \left[\frac{\partial}{\partial F} \left(\ell n \rho \right) \right] = 0$$
(3.14)

From the meridional plane solution a relationship between α , b, and r can be defined. Equation (3.10) can then be integrated to give E as a function of r with the condition that E = 0 at $r = r_t$. Also, from Equation (3.11) $F = \theta$. The relationship between the stream surface on which E and F lie and the r, θ, Z coordinate system is shown for the general case in Figure 3.4. In the E,F plane, the pump blades are as shown in Figure 3.5. With a relationship between fluid density, stream function, and known inlet conditions, Equation (3.14) can be solved numerically in the E,F plane.

3.3.2 Energy Equation - The completion of the solution to Equation (3.14) depends on a relationship between the fluid density, ρ , the streamfunction, ψ , and known pump inlet conditions. The energy equation for a steady flow fluid system such as a turbopump is given by

2

$$h + \frac{v'^2}{2g} = h_{o_{H}} + W$$
 (3.15)

where

h = static enthalpy/lb
V' = absolute fluid velocity
h
o_u = total enthalpy/lb at the pump inlet
W = work done on the fluid per pound of fluid/unit time

Equation (3.15) expressed in terms of components of the absolute velocity is

h +
$$\frac{1}{2g}\left[\left(\sigma \mathbf{r} + V_{\theta}\right)^2 + V_M^2\right] = h_{o_u} + W$$
 (3.16)

But the rate of work addition between a station, u, upstream (where all flow properties are known) and the station being considered is equal to the rate of change in moment of angular momentum between the stations or

$$W = \frac{\omega}{g} \left[r \left(r \omega + V_{\theta} \right) - r_{u} \left(r_{u}^{\omega} + V_{\theta}_{u} \right) \right]$$
(3.17)

The quantity $r_u \begin{pmatrix} r_u^{\omega} + V_{\theta_u} \end{pmatrix}$ is commonly referred to as the pump prewhirl, which is either specified for the problem or is obtained from a viscous flow solution to the upstream flow problem. If it is assumed that the flow in the impeller undergoes isentropic changes of state and that for cavitation conditions the vapor and liquid phases are in thermal and velocity equilibrium, a relationship between pressure and average fluid density, ρ , can be obtained from a state diagram for the working fluid. Referring to Figure 3.6, which represents a temperature-entropy diagram for a typical pump fluid, the isentropic compression process might be represented by the vertical line CAB. Assuming the inlet properties of the fluid correspond to Point A, the fluid experiences a decreasing pressure as it enters the pump and ultimately reaches conditions corresponding to Point B in the vicinity of the blade leading edge. Cavitation is fully developed at this point. Downstream of the blade leading edge region, the work input to the pump goes into compressing the fluid that exists from the pump having properties corresponding to Point C. Using oxygen as the pump fluid and assuming that the flow process in the pump is isentropic and that velocity and thermal equilibrium exist throughout, the variation of density with pressure is shown in Figure 3.7. The data of the figure is based on a saturation temperature corresponding to 15 psia. The data from which the curve was derived were taken from Reference 35. Similar relationships can be obtained for different saturation temperatures as well as different fluids. Combining Equations (3.16), (3.17), and relating h to P/ρ yields

h (P/
$$\rho$$
) - $\frac{(\omega r)^2}{2g} + \frac{1}{2g} \left(v_{\theta}^2 + v_M^2 \right) = \text{CONST}$ (3.18)

where CONST = inlet energy conditions. Upon application of Equation (3.6), (3.7), (3.10) and (3.11), Equation (3.18) is transformed to its final form

h
$$(\mathbf{p}/\rho) + \frac{1}{2g} \left(\frac{1}{\rho br}\right) \left[\left(\frac{\partial \psi}{\partial F}\right)^2 + \left(\frac{\partial \psi}{\partial E}\right)^2 \right] - \frac{(r\omega)^2}{2g} = \text{CONST}$$
 (3.19)

3.4 <u>Solution Technique</u> - In order to define the turbopump cavitation flow field, Equations (3.14) and (3.19) must be solved throughout the field between two blades of the pump and for a number of streamtubes selected from the meridional plane.

The results are then integrated throughout the pump to obtain the total cavitation compliance. The solution of Equations (3.14) and (3.19) is accomplished in a finite difference form on the CDC 6000 series computer. The problem is initiated by transforming the pump blades from the physical plane (Figure 3.4) to the E, F plane (Figure 3.5) through Equations (3.10) and (3.11). Next, a gridwork is established between the blades as shown in Figure 3.5. Equations (3.14) and (3.19) are written in finite difference form at each grid point and a relaxation method of solution employed. Solution of the problem is accomplished by specifying the upstream and downstream boundary conditions, assuming values of ψ at each grid point within the boundaries, and checked to see if Equations (3.14) and (3.19) are satisfied at each point. If it is not, the left hand side of Equation (3.14) will be equal to a residual R. Then, values of ψ at each grid point are systematically adjusted until the residuals are reduced to an acceptable level. Once this condition is reached, a solution is achieved. This initial solution may not correspond to the correct angular velocity on the upstream boundary. A scheme is included in the program for adjusting the upstream boundary and reapplying the relaxation solution until the correct value of angular velocity is obtained. A complete discussion of the relaxation method of solving systems of partial differential equations is given in Reference 36. The equations and solution technique described above have been developed into a computer program known as the turbopump cavitation flow program. User instructions for the computer model are given in Appendix D, and program listings are given in Appendix E. The analysis of the computer results required to obtain the cavitation compliance of the total turbopump is given in Section 5.1.

3.5 <u>Model Applications</u> - In addition to cavitation compliance, the turbopump model is capable of generating other information which is of interest in the analysis of turbopump response and the design of turbopump blades. Turbopump discharge dynamic pressure gain can be determined as a function of inlet pressure (pump gain, $\partial Pd/\partial Ps$), exit flow (pump resistance, $\partial Pd/\partial wd$), and blade speed (speed gain, $\partial Pd/\partial N$). These parameters are also important in POGO stability analysis. Unlike cavitation compliance, there are currently methods available for estimating these parameters; however, the use of a cavitating turbopump model may result in a significant improvement. This model can also be used for design analysis of turbopump blades. This could include blade pressure loading, and the influence of blade shape on cavitation, separation, etc.

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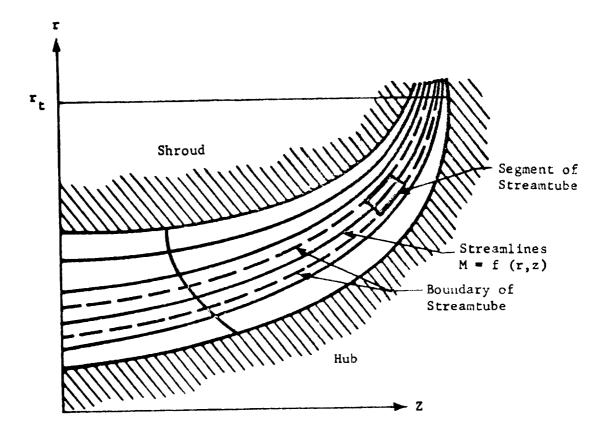


Figure 3.1 Meridional Plane of Pump Impeller

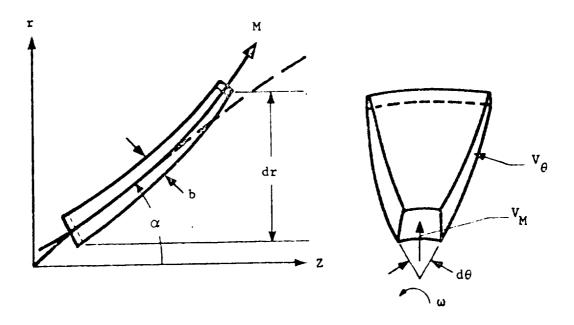


Figure 3.2 Segment Streamtube of Revolution for Continuity Equation

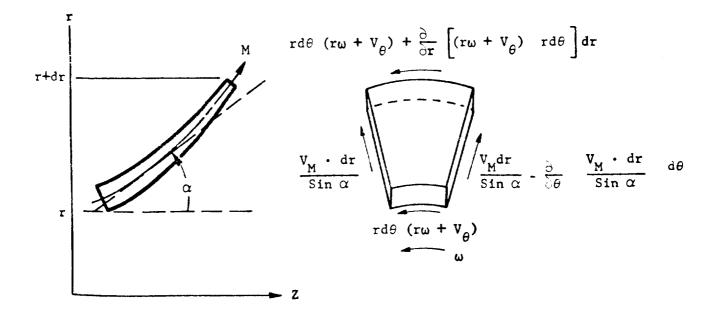


Figure 3.3 Segment Streamtube of Revolution for Irrotational Flow

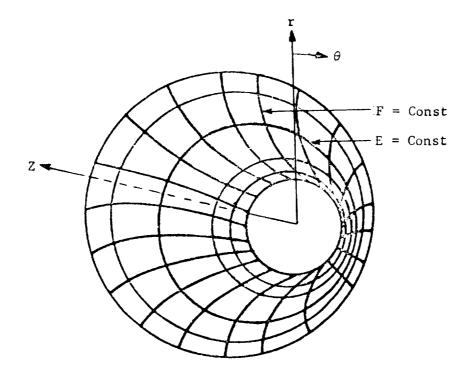


Figure 3.4 E,F Surface Relative to r, Z and $\boldsymbol{\theta}$ Coordinates

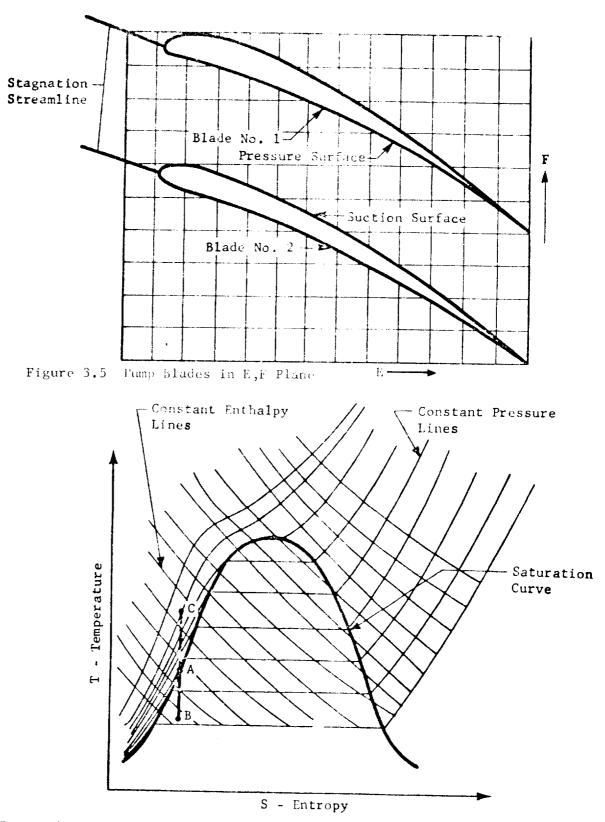
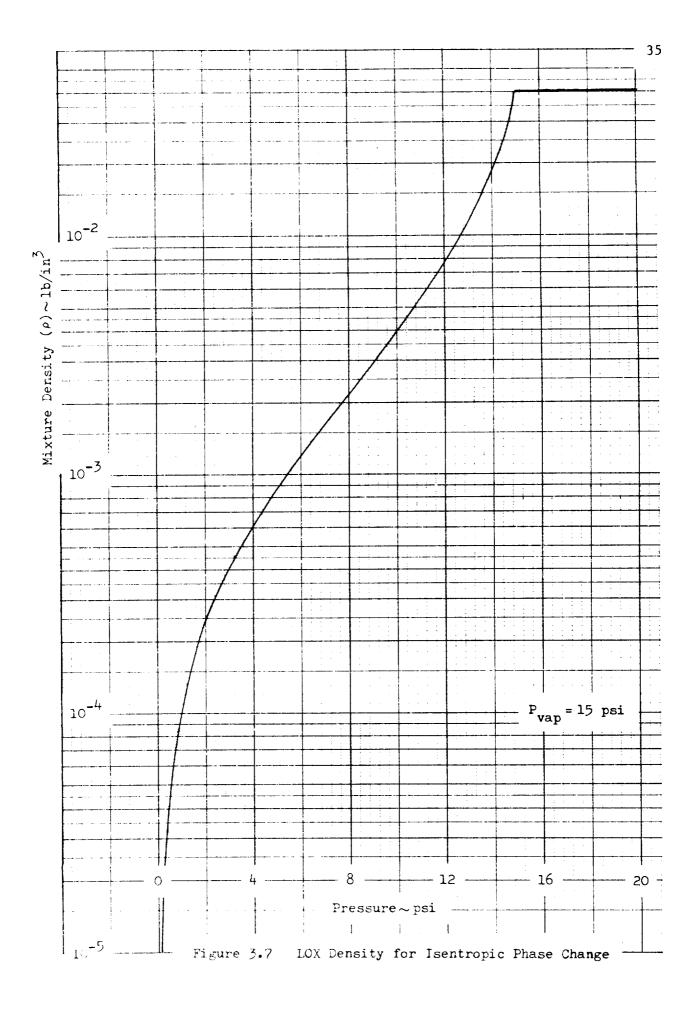


Figure 3.6 Pump Fluid Property Diagram



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4. Empirical Cavitation Data

4. EMPIRICAL CAVITATION DATA

4.1 Test Data Analysis

4.1.1 <u>Objectives</u> - The objectives of the test data analysis are:

- a. Determine the true cavitation compliance from all available test data on as many different turbopump configurations as possible;
- b. Considering turbopump and propellant parameters which influence cavitation, attempt to present all the test data in a nondimensional correlated form;
- c. Provide test results of specific turbopump configurations for verification of the analytical model.

Completion of the first objective will provide all currently available turbopump cavitation data in a single document. An empirical evaluation of the data, in terms of nondimensional parameters, is a parallel approach to the purely analytical turbopump cavitation model. The pump configurations selected for verification of the analytical model should meet the following requirements:

- Accurate determination of cavitation compliance from test data;
- b. Controlled and known test conditions;
- c. The turbopump should be typical of those of interest in POGO analysis;

d. The curbopump should be consistent with the assumptions of the analytical model.

Considering these requirements, the J-2 LOX and F-1 LOX turbopumps were originally selected for model verification. In addition, the H-1 LOX and LR87 oxidizer pumps were selected for less detailed study. These selections were based on both compatibility with the analytical model and confidence in existing test data, as discussed in the following sections.

4.1.2 <u>Data Sources</u> - Table 4.1 shows all the different turbopump configurations for which cavitation data is known to exist. In all of these cases, cavitation data was derived from tests whose objectives were to determine the natural frequencies of the propulsion feed system for use in POGO analysis. Although turbopump cavitation usually has an important influence on feed system frequency, testing and data reduction was only concerned with determining an equivalent cavitation compliance. For determination of feed system frequency it was not required to separate the true cavitation compliance from other sources of mechanical compliance in the vicinity of the turbopump.

Table 4.1 Turbopump Configurations

| <u>Vehicle</u> | Stage | Engine | <u>Oxidizer</u> | <u>Fuel</u> |
|----------------------------|----------------------------|-------------------|-------------------------------|---------------------|
| Saturn Saturn Saturn | S-1E S-1C S-11/S-1VB | H-1 F-1 J-2 | LOX LOX LOX | RP-1 RP-1 LH2 |
| Titan | 1 | LR87 | N204 | 4 Aerozine 50* |
| Titan | 11 | LR91 | N ₂ 0 ₄ | Aerozine 50* |
| Thor | 1 | MB - 3 | LOX | RP-1 |
| * | 50% Hydrazine a | and 50% UDMH | | |

Test data related to this study comes from one of the following sources:

- a. System tests with flowing propellant and an operating turbopump;
- Feed system tests with non-flow propellant in the absence of an operating turbopump;
- c. Feed line component tests on segments whose compliance can not be accurately calculated;
- d. Flight data.

Almost all of the available ground system test data is pulsed; i.e., the system response is measured relative to some known forcing function. The only test results which include the effects of turbopump cavitation are the flow system tests and the flight data. These test results required separation of the cavitation effects from other compliance effects. Some flow system tests have flight feed systems while others have facility feed systems; and some have hot firing engines while others are "bobtailed" (turbopump is driven in normal mode of operation but propellants are not mixed and burned in the main thrust chamber).

4.1.3 <u>Determination of Cavitation Compliance From Natural</u> <u>Frequency</u> - Cavitation compliance cannot be measured directly during a turbopump test and must be determined through use of analysis. A typical procedure for this determination is as follows:

- a. Run a flow systems test;
- b. Assume an analytical model of the test configuration;
- Calculate, estimate, or determine from separate tests all model inputs except cavitation compliance;
- d. Determine value of cavitation compliance for which model best fits test data.

Since cavitation compliance has its strongest influence on feed system natural frequency (as opposed to gain, damping, etc.) the above procedure is normally reduced to a correlation between test and analytical natural frequencies. These frequencies are a function of the inertance and compliance of the total system. For those unfamiliar with these hydraulic terms an analogy with a spring mass system is given in Figure 4.1. Inertance can be accurately calculated from the geometry of the feed line. The system compliance includes the distributed compressibility of the fluid and the radial flexibility of the suction line, axial flexibility due to a feed line area change, local flexibility of a line joint or bellows, and the compressibility of the cavitation vapor bubbles in the turbopump. Only the combined effect of all the system compliances can be determined from a dynamic systems test; thus, the line and fluid compliance must be known before cavitation compliance can be accurately determined. The distributed fluid and line compliance can be calculated fairly accurately. Local flexibilities can be determined from analysis, component tests, and/ or system tests without the turbopump operating. Suction line bellows are local flexibilities which often represent a significant portion of the feed system compliance but cannot be determined accurately due to insufficient test data and a lack of analytical methods. A current technology contract (NAS8-25919) should result in improved analytical methods for determination of all suction line elements. The exact equations relating cavitation compliance to natural frequency are a function of the analytical model used. The more representative the model the more accurate the derived cavitation compliance. Two computer programs which were developed for Titan and Saturn V POGO analysis were modified for general test analysis in this study. These programs consist of: 1) a modal analysis program (Reference 37) for determination of natural frequencies for any distribution of line inertance and compliance; and 2) a transfer function program (unpublished) which utilizes the modal data to generate the transfer function of suction pressure per excitation as a function of excitation frequency. For a lightly damped system with negligible feed line and fluid compliance the cavitation bubble compliance, C_b, can be approximated by

$$C_{b} = 1/(I\omega_{1}^{2})$$
 (4.1)

where I is the feed system inertance and ω_1 is the first natural frequency of the feed system. For a uniformly distributed suction line and fluid compliance, which yields an open-closed organ pipe frequency (ω_0), and a lumped duct compliance near the pump inlet (C_d), the cavitation bubble compliance can be approximated by

$$C_{\rm b} = \frac{1}{1 \omega_1^2} \left[\frac{(\omega_1 / \omega_0)^2 - 1}{(\omega_1 / 2 \omega_0)^2 - 1} \right] - C_{\rm d}$$
(4.2)

4.1.4 <u>Determination of Natural Frequency From Test Data</u> - A fairly standard procedure for determining feed system natural frequency from test data is as follows:

- a. Configure a test set up which resembles the flight feed system as closely as possible;
- Excite the feed system dynamic response with a measured forcing function;
- Generate trequency domain perturbation transfer function (amplitude ratio and phase) of response per excitation from the measured results;
- d. Natural frequency occurs near frequency of maximum amplitude ratio and phase shift of 90°.

For most of the test results analyzed herein, the excitation has been some type of near sinusoidal wave pulsing of suction flowrate. In this case the pulser frequency has been changed in steps (or in very slow ramp) and the resulting pressure oscillations recorded at each frequency increment. This, together with the measured excitation, yields a perturbative transfer function of turbopump inlet pressure per excitation. Another type of excitation which has been successfully used (Reference 38) is the random noise associated with the engine combustion process. In this case auto- and/or cross-spectral analysis is required to determine the frequency domain response of the system. In most feed system configurations the first natural frequency is very near the frequency at which the amplitude ratio is maximum simultaneous with a phase shift of 90° for an appropriate feed system transfer function. In POGO analysis the most important transfer function is turbopump inlet pressure oscillation per turbopump acceleration perturbation $(\partial P_s/\partial g_p)$. Any transfer function which has the same natural frequency as $\partial P_s/\partial g_p$ is an appropriate transfer function. Pulser acceleration and flow acceleration are legitimate excitations whereas transfer functions with respect to pulser pressure can yield significant errors in natural frequency. This effect is shown in the analysis of the J-2 test results. If additional information besides natural frequency (e.g. static gain and damping) are desired from the test results, it is required that a best fit between an analytical and test transfer function be obtained.

4.1.4.1 Test Frequency Correction - In reviewing test data two possible situations were recognized which could cause small errors in the test results. First is the determination of the system natural frequency from a transfer function of suction pressure per pulser pressure $(\partial P_s / \partial P_p)$ in lieu of suction pressure per pulser flow $(\partial P_s / \partial \dot{W}_p)$. Second is the presence of facility lines which do not exist in the flight configuration. Both of these conditions existed on the S-II LOX line tests and each represents an error in frequency determination of about 5% in opposite directions. The effect of using the $\partial P_s/\partial P_p$ transfer function is shown in Appendix C for a simplified system and results in a frequency which is 5% too high. The S-II LOX line test set up had a facility line running from the sump to the facility tank. This line was isolated from the suction line by a large accumulator at the sump; however, the residual effect of the facility line yields a system

natural frequency which is 5% too low. A model of the test and flight configuration is shown in Figure 4.2. A comparison of the $\partial P_s / \partial P_p$ transfer function for the test set up with the correct $\partial P_s / \partial g_p$ transfer function for the flight configuration is shown in Figure 4.3. Neither of the two possible discrepancies are known to exist in any other test data.

4.1.5 <u>Test Results</u> - No attempt has been made to duplicate previous analysis of pertinent test results. However, in many cases the analysis had to be extended in order to separate cavitation compliance from other sources of compliance. Also, in several instances independent tests on the same configuration produced conflicting results. In these cases, if a review of both results could not favor one over the other, the discrepancy was carried through the analysis and yields a tolerance on the results. Cavitation compliance is a function of many propellant and turbopump parameters; however, for a given configuration at a fixed operating point the only significant parameter which undergoes a planned variation during tests is turbopump inlet static pressure (P_s). Thus, the cavitation results presented in the following paragraphs are given as either a function of P_s or a non-dimensional form of P_s defined by

$$K = \frac{P_{s} - P_{v}}{1/2 \rho v_{r}^{2}}$$
(4.3)

where K = cavitation index

P_v = propellant vapor pressure ρ = propellant mass density V_r = inducer relative tip velocity This is a convenient parameter since it has been found that for most turbopump configurations cavitation compliance is a linear function of a constant raised to a power which is proportional to K, i.e., a straight line on semi-log graph paper. Whenever the scatter in the test data allows, this functional relationship will be observed in the presentation of the following test data. The data necessary for calculation of cavitation index is presented in Table 4.2.

4.1.5.1 <u>F-1 LOX Cavitation Compliance</u> - The F-1 LOX turbopump was tested with a S-IC outboard feed line and an outboard Arrowhead PVC (Pressure-Volume Compensator) duct. The feed line properties were taken from Reference 39. A LOX compressibility of .135 x 10^6 psi (T = -296° F) was calculated from velocity of sound data given in Reference 40. The compliance of the main line area change (above the prevalve) was investigated and found to be negligible. The PVC compliance was calculated from component test by Aerrowhead, MSFC and Boeing; and from non-flow system dynamic tests by MSFC and Boeing. These data were then used in a model in which cavitation compliance was varied to match Bobtail (Reference 41) and Single Engine (Reference 42) tests results.

4.1.5.1.1 <u>F-1 LOX PVC Component Test Results</u> - The total PVC compliance, C_{PVC} , includes the combined effect of the fluid compressibility and radial expansion (C_f) and axial flexibility of the upper and lower annulus area (C_x).

$$\frac{C_{PVC}}{dP} = \frac{dW}{dP} = \frac{d(PV)}{dP} = \frac{C_x}{x} + C_y$$
(4.4)

where

С

$$x = \rho A \frac{dx}{dP} = \rho A^2 / K$$
(4.5)

and

$$C_{\rm F} = \rho \int \frac{\mathrm{d}A}{\mathrm{d}P} + A \int \frac{\mathrm{d}\rho}{\mathrm{d}P}$$
(4.6)

 ${f C}_{{f f}}$ was calculated to be .011 in 2 and is included as part of the distributed compliance of the feed line addel. The results of the component test are summarized in Table 4.3, and discussed below. Figures 4.4 and 4.5 contain unpublished results, supplied by MSFC, of PVC component tests run by Aerrowhead. From Figure 4.4 total PVC compliance can be calculated from dV/dP; however, this result is considerably too large compared with all other data. This can only be explained by the presence of air in the system. Two observations can still be made from these results. 1) dV/dP appears to be nonlinear with respect to pressure, and 2) dV/dP is approximately the same whether or not the PVC ends are restrained (this agrees with an analysis of the areas and spring rates). A more reliable estimate of PVC compliance can be made using Equation (4.5) and the results given in Figure 4.5. This result is independent of the amount of trapped air in the system. Component tests run at MSFC (Reference 43) gave a value of dX/dP of .0056 (2 x .0028 for both the upper and lower annulus) for an Aerrowhead inboard PVC, and .007 for Flexonics outboard PVC. The results were very linear over the pressure range of 40 to 130 psig. The corresponding values of C are .060 $_{\rm X}$ and .075 in respectively. An equivalent FVC spring rate of K = 34250 lb/in was determined from Boeing component tests on a Aerrowhead outboard PVC (Reference 39), and this was also

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fairly linear over the pressure range of 50 to 125 psia. This yields (Equation 4.5) a C_x value of .081 in². An analysis of the flexibility of supporting structure used in the Boeing water tests (Reference 39) showed that for the PVC installed in the line C_x could increase to .096 in²; however, it could never decrease below .081 (a completely rigid mounting of the uppor spool and lower flange). Component tests ($\Delta X/\Delta P$) show that the outboard Aerrowhead and Flexonics PVC's have approximately the same compliance while inboard Aerrowhead PVC has about 25% less compliance.

4.1.5.1.2 F-1 LOX PVC Systems Test Results - Analytical feed system natural frequencies as a function of the sum of the cavitation bubble compliance $(C_{\rm b})$ and the PVC annulus compliance (C_{ij}) are given in Figure 4.6. Since these two compliances are located fairly close together, the frequencies are practically independent of the distribution between C_{b} and C_{v} . The second resonance of a pressure/pulser flow transfer function is shown to be a function of the location of the pulser line. Figure 4.7 gives MSFC dynamic test data with the turbopump isolated from the feedline. Some non-flow tests were run with a Flexonics outboard PVC and some with an Aerrowhead PVC; however, since the component tests indicate they have essentially the same compliance no attempt was made to differentiate between the two. A similar method of obtaining C_x from the Boeing Water Tests (Reference 39) yielded a C_x of .125 in² at 80 psia and .086 at 140 psia. This compliance is high enough to suspect that there may be some air trapped in the system, which is always a possibility in non-flow tests.

4.1.5.1.3 F-1 LOX Cavitation Compliance - Figure 4.8 shows MSFC dynamic test results (References 41 and 42) with the turbopump running. Also shown is the sum of the cavitation and PVC annulus compliance, $\rm C_{b}$ and $\rm C_{x},$ required to make the analytical results match the test results. The resulting cavitation compliance is shown in Figure 4.9 for two different C_v functions. One is the maximum C_v variation as derived from a best fit of the MSFC non-flow tests (Figure 4.7). This variation is much more than can be justified by any component tests, and also results in a cavitation compliance which shows less variation with pressure than is expected. The other C_{x} function used is a constant value of $.081 \text{ in}^2$, as derived from some of the component tests. Since some of the component tests indicate some variation in ${\rm C}_{_{\rm \! V}}$ with pressure, a constant value is probably conservative. The true cavitation compliance should lie between the limits shown in Figure 4.9.

4.1.5.2 <u>F-1 Fuel Cavitation Compliance</u> - The Rocketdyne evaluation of fuel pump inlet compliance (Reference 44) from the F-1 Bobtail Test results (Reference 41) are presented in Figure 4.10. Also shown are cavitation data derived from feed system frequencies obtained from the F-1 Bobtail tests and the S-IC Single Engine Test (Reference 42). The results of this analysis yield higher values of pump inlet compliance than were obtained by Rocketdyne. The variation in test frequency data presented in Figure 4.11 accounts for the lower values of pump inlet compliance analytically derived from the S-IC Single Engine Tests. The only differences between the Bobtail and Single Engine Test are that the Bobtail Test configuration had an outboard PVC and used discharge pulsing, whereas the Single Engine Test configuration had an inboard PVC and used suction pulsing. Discharge pulsing should yield the same results as suction pulsing; however, obtaining good reliable feed system frequencies by discharge pulsing usually presents severe data reduction problems. The differences in results are larger than the anticipated differences due to changing PVC ducts. It was concluded that the S-IC Engine Test data was more reliable because it was derived from suction line pulsing, it is more recent data, and it showed less scatter. Since compliance derived from the S-IC Engine Test is less than that derived from the F-1 Bobtail Tests it should contain less PVC duct compliance. Since no PVC duct compliance was available it is assumed that turbopump inlet compliance derived from the F-1 Engine Tests is equal to cavitation compliance.

4.1.5.3 J-2 LOX Cavitation Compliance - Dynamic test data exists for four different J-2 LOX feed systems. They are the S-II inboard test facility feed system, the S-II outboard test facility feed system, the S-IVB test facility feed system, and the Rocketdyne turbopump test facility feed system. These tests were run for a range of turbopump inlet pressures and three different PU (propellant utilization) settings. As expected, the feed system natural frequencies (and thus turbopump cavitation) varied greatly with inlet pressure; however, the effect of PU setting was within the scatter of the data. Thus, for a given inlet pressure, reduced test results from all the different J-2 LOX feed systems should yield the same cavitation compliance. Two independent detailed analyses of test results have been performed. Brown Engineering analyzed the results of the S-II and S-IVB feed system tests (Reference 45) and Rocketdyne analyzed their test facility results

(References 46 and 47). Both analyses yield approximately the same predecticate reconnects when related to common feed systems. This is shown in Figure 4.12 for the fill and S-IVB flight feed systems (which is somewhat different than the test facility feed systems). Brown Engineering assured a single compliance turbopump model whereas Rocketdyne derived a turbopump flow impedance transfer function, G(S), from their test data which implies a dual compliance turbopump model. For the same test results (i.e., the same predominate feed system frequency) the two different turbopump models will yield different values of cavitation compliance.

4.1.5.3.1 J-2 LOX Duct Compliance - Also of importance is the amount of fluid and duct compliance present in the suction line. The Brown Engineering analysis derived a lumped compliance from dynamic tests which had the suction line isolated from the pump. Pocketdyne, on the other hand, coupled their test derived turbopump impedance function to flight suction line models and added suction line compliance until the analytical frequencies agreed with flight observed resonances. These results are compared in Table 4.4 and in both cases represent equivalent lumped values at, or near, the turbopump inlet. Both of these approaches are valid and should yield approximately the same results, whereas, the differences shown represent a very significant portion of the total feed system compliance. 4.1.5.3.2 <u>J-2 LOX Turbopump Model</u> - The single compliance model (see Figure 4.13a) used in the Brown Engineering analysis has a flow impedance given by

$$G(S)_{1} = \frac{P_{o}}{W_{o}} = \frac{R}{K_{p}} \frac{\left[\frac{L}{R} S + 1\right]}{\left[\frac{CL}{K_{p}} S^{2} + \frac{CR}{K_{p}} S + 1\right]}$$
(4.7)

In this case the resistance, R, and inertance, L, were calculated; and the pump gain, K, and the cavitation compliance, C, were derived from test data. This impedance function and Brown Engineering duct compliance shown in Table 4.4 yield cavitation compliances shown in Figure 4.14.

The Rocketdyne analysis fit an impedance function to test data. The form required to give good correlation is given by

$$G(S)_{2} = \frac{P_{o}}{W_{o}} = \frac{K\left[\left(\frac{S}{\omega_{2}}\right)^{2} + \left(\frac{2\zeta_{2}}{\omega_{2}}\right)S + 1\right]}{\left(\frac{S}{\omega_{1}} + 1\right)\left[\left(\frac{S}{\omega_{3}}\right)^{2} + \left(\frac{2\zeta_{3}}{\omega_{3}}\right)S + 1\right]}$$
(4.8)

One possible physical representation which gives this type of response is given in Figure 4.13b. In terms of the physical parameters, the impedance functions become

$$G(S)_{2} = \frac{P_{0}}{W_{0}} = \frac{R}{K_{p}} \left[\left(\frac{LC_{2}R_{2}}{R} \right) S^{2} + \left(\frac{L + R_{1}R_{2}R_{2}}{R} \right) S + 1 \right]$$
(4.9)
$$K_{p} \left[\left(\frac{LC_{1}C_{2}R_{2}}{K_{p}} \right) S^{3} + \frac{C_{1}}{K_{p}} \left(L + R_{1}R_{2}C_{2} \right) S^{2} + \left(\frac{C_{1}R}{K_{p}} + C_{2}R_{2} \right) S + 1 \right]$$

Equating coefficients of Equations (4.8) and (4.9) will yield the physical model parameters in terms of the frequency and damping parameters. Table 4.5 gives these results for the latest frequency and damping data given in Reference 47. In this model, C_1 is the main inlet cavitation compliance. It is the most important turbopump parameter in determining the predominate feed system frequency and is independent of pump gain (K_p). To illustrate the effect of the other turbopump parameters consider the case where the impedance beyond the cavitation compliance is very high. Then both of the above turbopump models approach an impedance function given by

$$G(S)_3 = \frac{1}{CS}$$

where C is the cavitation compliance. Using Rocketdyne feed system frequencies (Figure 4.12) and duct compliances (Table 4.4) cavitation compliances for both $G(S)_2$ and $G(S)_3$ are shown in Figure 4.15. Although $G(S)_3$ is not a good pump model, the effect of different turbopump models is illustrated.

4.1.5.3.3 <u>J-2 LOX Test Cavitation Compliance</u> - The difference in the Brown Engineering and the Rocketdyne derived cavitation compliance can be attributed to different suction duct compliances and different pump impedance functions. There is considerable test data which indicates that a double compliance model, $G(S)_2$, is a better representation of the turbopump than a single compliance model, $G(S)_1$. From this point of view the Rocketdyne data should be more accurate; however, the Brown Engineering analysis is a more conventional approach which has been used on several other turbopump configurations. For purposes of this study, both of these results (as shown in Figure 4.16) are considered to be equally valid. It is thus assumed that the true inlet cavitation compliance can be any-where between these limits.

4.1.5.3.4 S-II Flight Data - AS-509 S-II Stage flight data (Reference 48) were reviewed and the observed LOX feed system oscillations compared with test results. Two things were evident from the flight data. First, the observed S-II outboard feed system contourgram frequency was higher than anticipated; and, second, there was an observed frequency change at engine mixture ratio (EMR) shift. Prior to EMR shift, the observed outboard frequency was approximately 33% higher than the predicted value which was based on S-II "bobtail" and J-2 test results for inlet NPSH in the vicinity of 60 ft. Furthermore, if the 65 to 75 Hz inboard suction pressure oscillation, observed during and after accumulator fill, represents a response of the second inboard line ("short stack") mode, this result is approximately 28% higher than would be analytically predicted. The following theories have been advanced by different Saturn V POGO analysts as to the reason for these apparent frequency discrepancies:

a. The observed oscillation is not a natural frequency of the feed system but a 1/3 subharmonic of a 90 Hz turbopump self-induced oscillation;

- b. The section line structure is such that the properiod pass in the horizontal section does not affect the feed system frequency on the tlight configuration;
- c. For some unknown reason less tarropump cavitation exists in the flight vehicle than in the ground test.

The true cause remains unreactived; however, if it is due to reduced cavitation compliance $(C_{\tilde{b}})$, the right results for both the S-II inhoard and outboard feed systems imply that C_{b} is at least 70% lower than predicted from test data. This possible discrepance must be considered man atilizing the test results. In the later portion of S-II burn, the engine mixture ratio (EMR) changed from 5.5 to 4.8. This results in a predicted decrease in the flux coefficient (ϕ) of 10%. A reduced flow coefficient results in the turbopump inlet flow entering the inducer blades with a larger angle of attack. This should produce increased cavitation compliance and result in a lower feed system frequency. The observed flight results were just the opposite. When the EMR changed from 5.5 to 4.8 the S-11 outboard LON contourgram frequency appeared to increase from 26. to 33. Hz. The reason for this contradiction is unknown.

4.1.5.4 J-2 Fuel Cavitation Compliance - Turbopump cavitation compliance for the J-2 axial flow fuel pump is shown in Figure 4.17. This data was derived from a Rocketdyne single compliance math model (Reference 46). Since these tests were run at a Rocketdyne test facility it is assumed that rigid suction lines were used, and thus the results do not contain any pump inlet duct compliance. An analytical model of the S-II outboard feed system was used to determine J-2 fuel pump inlet compliance from a frequency data point (9.5 H_z) supplied by MSFC for Saturn POGO analysis. Although present available data on fuel bellows compliance is incomplete, a value of .004 in² was assumed after a review of the J-2 oxidizer configuration and inlet duct compliance test values. The resulting pump inlet compliance derived from this datum falls within the scatter of pump compliance data derived by Rocketdyne as shown in Figure 4.17.

4.1.5.5 H-1 LOX and Fuel Cavitation Compliance - Brown Engineering and Rocketdyne derived values of pump inlet compliance (Reference 49) based on S-IB Bobtail Tests (Reference 50) are shown in Figure 4.18. The mathematical models differed only in the suction line representation while turbopump and discharge line representation were comparable. The characteristic resonant frequencies derived from the test data by Brown Engineering and Rocketdyne also differed since the method employed by each in the interpretation of the test data varied. Both suction line and discharge line pulsing data were available. The use of spectral analysis of the test results by Brown Engineering has shown that discharge line pulsing did not give the correct characteristic frequencies (Reference 51). Lack of data points for the fuel pump inlet compliance in the Brown Engineering analysis is due to the inability of their data reduction procedure to always determine values of feed

system frequencies. Since Rocketdyne did not indicate this to be a problem, their procedure was considered more reliable and will be used exclusively in this analysis. The Bobtail test configuration does not have any suction line bellows located at the pump inlet. Since there are small line bellows located at several points in the fuel and oxidizer lines, it is assumed that their compliance is accounted for in the distributed compliance of the suction lines. Thus, for the H-1 feed systems, the derived pump inlet compliance shown in Figure 4.18 is assumed to result exclusively from turbopump cavitation.

4.1.5.6 <u>MB-3 LOX and Fuel Cavitation Compliance</u> - MB-3 cavitation compliance data was obtained from an Aerospace Corporation evaluation of feed system frequencies on the THOR vehicle (Reference 52). These data are shown in Figure 4.19 as a function of cavitation index (K). They are presented in this report for reference only, as MB-3 turbopump geometry and operating parameters were not available to permit evaluation of the data.

4.1.5.7 <u>LR87 and LR91 Oxidizer and Fuel Cavitation Compliance</u> -Cavitation compliance of the Titan Stage 1 and 11 turbopumps is shown in Figure 4.20. This data was determined by combined Martin Marietta Corporation and Aerospace Corporation analysis of pulsed and/or non-pulsed hot firing engine tests, bobtailed turbopump tests, suction line non-flow tests, and flight data. The final results have evolved over several evaluations (particularly in the case of the LR87 data) and no concise documentation exists. The Martin results, presented here, agree closely (except for a density scale factor) with the Aerospace results given in Reference 31. The LR87 oxidizer feed system contains the largest amount of non-cavitation compliance. In this case the suction line distributed compliance was calculated and compared with non-flow test results (unpublished results of Martin Marietta Corporation tests). These results indicated that the line bellows located near the pump inlet contain very little compliance. This is assumed to be true for the other Titan lines which use similar line bellows.

4.1.6 <u>General Test Data Assessment</u> - The preceding cavitation compliance test data generally have large uncertainties associated with the results. In most cases this can be related to the fact that the objective of these tests was to determine feed system frequency, not cavitation compliance. In several cases the results even show large dispersions in feed system frequency for a given test series and unexplained disagreement between results of different tests of the same feed system. Assuming the feed system frequency is accurately known the following error sources exist for determining cavitation compliance.

- a. Unknown feed line compliance;
- b. Frequency insensitive to cavitation compliance, conversely cavitation compliance is very sensitive to frequency dispersions;
- c. Unknown turbopump model (test data will not fit a physical model).

In addition to dispersions in the results there are unknowns associated with parameters which affect the amount of cavitation which occurs. Some of these unknown factors are:

- H. Aslocity distribution at the turbopump inlet;
- 5. Propellant back flow into the suction line;
- e. Propoliant preswir) at the inlet;
- d. Amount of absorbed gas in the propellant;
- Start propellant temporature at the turbopump infect;
- F. Effect of PU (Propellant Utilization) recirculation flow.

The accumulated effect of all the unknowns must be carefully considered when judging the merits of either an empirical or analytical prediction technique.

4.2 Empirical Data Evaluation

4.2.1 <u>Influential Parameters</u> - In order to evaluate all the different turbopump cavitation compliance test data one has to postulate as to what are the important variables, and attempt to group these into non-dimensional parameters which will yield the same cavitation compliance for all existing turbopump configurations. If this could be accomplished with some degree of success, it would provide a method for predicting the amount of cavitation compliance that will occur on a new turbopump design. The turbopump operating and geometry parameters, and propellant variables which could affect the amount of turbopump cavitation are:

- $P_s = pump inlet static pressure$
- \dot{W} = propellant flow rate
- $H_i = inducer head rise$
- N = inducer speed
- α_i = inducer angle of attack

- $n_i = number of inducer blades$
- $D_i = inducer tip diameter$
- D_{h} = inducer hub diameter
- ℓ_{i} = inducer tip radial clearance
- $P_{v} = propellant vapor pressure$
- ρ = propellant density
- h = propellant latent heat of vaporization

The ideal method of assessing the effect of these variables is to conduct cavitation tests where only one parameter is varied at a time. The available test results are for different turbopump configurations (all geometry parameters changed together), each run with a single propellant, at normal operating conditions (usually only inlet pressure is varied). This approach does not give specific empirical dependence of cavitation compliance on parameters other than P_s . The other parameters do vary for different turbopump configurations, but the effects cannot be separated. Thus, only a qualitative empirical evaluation of the results can be performed. This is accomplished by comparing non-dimensional cavitation compliance against non-dimensional turbopump and propellant parameters.

4.2.2 <u>Non-Dimensional Parameters</u> - Ideally there exists a nondimensional combination of parameters which uniquely describes a cavitation parameter as a function of operating and configuration parameters for all conditions and configurations. The most generally used non-dimensional cavitation parameter is cavitation index, K (Equation 4.3), which combines P_s , P_v , and V_r . The data required to compute cavitation index is given in Table 4.2 for several turbopump configurations. All of the available cavitation compliance data is shown in Figure 4.21 vs cavitation index. When two sources of equally valid data exist, an average of the two values was assumed for comparison with other data. Although all of thes data exhibits the same trend and lies within an order of magnitude band, the variation is much too large to eliminate the need for obtaining cavitation test data on a new turbopume configuration. Turbopump size can be easily accounted for by non-dimensionalizing cavitation compliance (C_b) with respect to size variables. $C_b/n_i D_i^2$ vs K is shown in Figure 4.22. This in general narrows the band of data encept for the LR-91 oxidizer data. The inducer leading edge angle of attack, assuming no propellant preswirl at the pump inlet, can be calculated by

$$\alpha_{i} = \beta_{i} - \tan^{-1}\phi \tag{4.4}$$

where β_i is the inducer blade angle and \emptyset is the flow coefficient. Comparing the values of α_i given in Table 4.2 with the cavitation data given in Figure 4.21 and 4.22 shows no particular correlation. This may be partly due to the fact that all of the LR series turbopumps have cambered inducers which operate at near zero leading edge angle of attacks. All the other turbopumps have flat inducer blades which require a leading edge angle of attack to generate a pressure rise. Thus, α_i is not a good universal cavitation measurement parameter. A turbopump performance parameter, pump specific speed (SS), defined in non-dimensional form as

$$SS = 8136 \left[\frac{1}{2} - \frac{D_{h}^{2}}{D_{i}^{2}} \right]^{\frac{1}{2}} \qquad \emptyset^{\frac{1}{2}} \left[\frac{K}{K} \right]^{\frac{3}{4}}$$

(Reference 31), was considered as a means for correlating cavitation compliance. Figure 4.23 shows non-dimensional cavitation compliance (related to inducer inlet area $D_i^2 - D_b^2$) as a function of 1/SS. Comparison of Figures 4.22 and 4.23 shows that 1/SS is not significantly better than K. Thor(MB-3) data is not shown because the necessary geometry parameters were not known. Information on other influential parameters given in the preceding paragraph was not obtained for enough turbopump configurations to permit non-dimensional evaluation of their affect. However, it is doubtful if the existing spread in data shown in Figures 4.22 and 4.23 can be significantly reduced. Simple non-dimensional parameters cannot account for such important affects as blade shape, flow separation, and propellant phase change. The non-dimensional data presented here could be used to predict an order of magnitude cavitation compliance on a new turbopump configuration.

4.2.3 Effect of Inlet Pressure - It is of interest to note what the functional relationship is between inlet pressure (P_s) and cavitation compliance (C_b) as observed from the test data. Assuming that

$$C_b = Constant/P_s^n$$

$$n = -\frac{P_s}{C_b} \quad \frac{\partial C_b}{\partial P_s} = -\frac{(K + \frac{P_v}{q})}{C_b} \quad \frac{\partial C_b}{\partial K}$$

where $K = (P_s - P_v)/q$

and
$$q = p V_r^{-2}/2g$$

Measuring average values of K, C , and $\exists c_b^{-}/\exists K$ from the test results (Figure 4.21), values of "n" were calculated (see Table 4.6). The results show that for the Aerojet turbopumps, "n" fall in the range of 2 to 4. For several other turbopumps, "n" falls in the range of .5 to 1. Due to scatter in the test data, there is a fairly large tolerance associated with $\partial C_{\rm b} / \partial K$; however, if the trend is correct, these results imply that cavitation compliance, in different turbopumps, is proportional to different powers of P_s . This indicates that an analytical derivation of cavitation compliance, in terms of average flow field parameters, cannot yield good agreement with test results for all configurations. The work of F. Ghahremani (Reference 31) indicates that blade cavitation is inversely proportional to P_s^2 , while backflow cavitation is inversely proportional to P_s^3 . For the Aerojet turbopumps, this formulation should show good slope agreement (which it does) with test results; however, poor slope agreement could result for some of the other pumps. Current studies are being performed under Contract NAS8-27731 to evaluate this approach with respect to additional turbopump configurations (Reference 56).

| | | ~ | FUEL | | | RP-1 | ,029 | | | 6.12 | 2.00 | 26.3 | | 4 | 13.75 | 10.4 | | 6750 | 180 | 26.6 | 32943。 | 243 ° | .1475 | 3.1 |
|----------------|---------|---------------|--------------------------|-----------------------|---------------|-----------------|--------------------------------|-----------------------------------|-----------------------------|------------------------------|-------------------------------|------------------------------------|-------------------------|------------------------------|----------------------------|-------------------------------------|-----------------------------|--------------------|----------------------------------|--------------------------------|--|----------------------|-----------------------------------|--|
| Turbopump Data | | S-IB | OXID | Η | 2.41 | XOI | .041 | | | 7.60 | 2.0 | 42.3 | | 4 | 11.0 | 11.3 | | 6750 | 224 | 24.7 | 50787. | 514.4 | .110 | 6.5 |
| | SATURN | S-II/S-IVB | FUEL | | J2 4.95 | LH ₂ | .00255 | 49.6 | | 7.80 | 2. 93 | 41.0 | | 4 | Axial | 7.0 | | 25800 | 876 | 62.3 | 771257. | 78. | .071 | 3.7 |
| | | | OXID | J2 | | LOX | .041 | 49 . 6 | | 6.75 | 1.375 | 34.3 | | 3 | 10.20 | 6.9 | | 8050 | 237 | 22.9 | 56693. | 386. | .097 | 5.1 |
| | | S-IC | FUEL | | F1 2.22 | RP-1 | . 029 | 226 | | 15.71 | 6.61 | 159.6 | | 4 | 23.42 | 8.6 | | 5550 | 380 | 30.6 | 145336. | 1697. | .081 | 6. 0 |
| | | | OXID | UXLD F1 2 22 | | LOX | .041 | 227 | | 15.75 | 3.51 | 185.0 | | £ | 19.50 | 0.0 | | 5550 | 381 | 41°4 | 146875. | 3765. | . 109 | 3.6 |
| | TITAN | STAGE II | FUEL | | | A-50 | 。033 | 12.2 | | 3.80 | 0.84 | 10.8 | .045 | Э | 4.93 | 5.7 | | 23576 | 390 | 27.3 | 152845. | 116.9 | .070 | 1.7 |
| | | | OXID | LR-91 | 1.67 | N,0, | د ۲ 0525 ° | 27.1 | | 5.10 | 1.73 | 18.0 | .045 | ۴ | 8.75 | 5.7 | | 8366 | 186 | 17.2 | 34892. | 195.05 | .093 | 0.4 |
| | | ы | FUEL | 7 | 7 | A-50 | .033 | 27.2 | | 6.64 | 2 .24 | 30.7 | 0 45 | e | 10.75 | 5.7 | | 9175 | 266 | 22.4 | 71258. | 272.57 | •084 | 6•0 |
| | | STAGE | STAGE OXID F LR-87 | LR-87 1.917 | N,0, | 2 4 .0525 | 37.2 | | 7.10 | 2.15 | 36.0 | . 045 | ŝ | 9.42 | 5.7 | | 8350 | 258 | 23.0 | 67093. | 522.55 | 089 | ·8.0.6 | |
| | Vehicle | Vehicle Stage | | Envine Identification | Mixture Ratio | Propellant | Density (p) lb/in ³ | Suction Line Area in ² | Pump Dimensional Parameters | Diameter-Inducer Eye (D.) in | Diameter-Inducer Hub (D,) in | Area Inducer Inlet in ² | Design Clearance (0) in | Number of Inducer Blades (n) | Diameter of Impellertip in | Blade Angle ($m{eta}$) deg.at tip | Pump Performance Parameters | Pump Speed (N) RPM | Inducer Tip Velocity (V.) ft/sec | Propellant Velocity (U) ft/sec | Relative Velocity ² (V ²) ft ² /sec ² | Flow Bare (W) lb/sec | Flow Coefficient (ϕ = U/Vi) | Inducer Tip Angle of Attack (α_i) deg.0.6 |

Table 4.2

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Pable 4.3

PVC Annulus Compliance ($C_{\rm x} \simeq {\rm in}^2$)

| Test Conductor | Source | Press=80psia | Press=140psia | | | | | | |
|---------------------------|-----------------------|--------------|---------------|--|--|--|--|--|--|
| (Aerrowhead Inboard P | VC) | | | | | | | | |
| Aerrowhead | $\Delta X / \Delta P$ | .073 | .046 | | | | | | |
| MSFC | $\Delta X / \Delta P$ | .060 | .060 | | | | | | |
| MSFC | 1 | .062 | .060 | | | | | | |
| (Aerrowhead Outboard PVC) | | | | | | | | | |
| Aerrowhead | $\Delta X / \Delta P$ | .085 | .060 | | | | | | |
| Boeing | $\Delta X / \Delta P$ | .081 | .081 | | | | | | |
| Boeing | 2 | .096 | .096 | | | | | | |
| Boeing | 1 3 | .125 | .086 | | | | | | |
| MSFC | 1 | .068 | .025 | | | | | | |
| (Flexonics Outboard PV | VC) | | | | | | | | |
| MSFC | ΔΧ/ΔΡ | •075 | •0 7 5 | | | | | | |

1 2 Match to no flow dynamic test results.

 $\Delta X / \Delta P$ results plus mounting flexibility.

3 Possibility of air in the system.

Table 4.4

J-2 LOX Suction Duct and Fluid Compliance

Feed SystemCompliance (in²)Brown Eng*
(Reference 45)Rocketdyne**
(Reference 47)S-II Inboard.0112.0031S-II Outboard.0077.0055S-IVB.0055.0015

Located approximately 10" above turbopump inlet

** Located at turbopump inlet

Table 4.5

J-2 LOX Physical Model Parameters For G(S)2

| NPSH | Ps | c ₁ | С ₂ Кр | R ₁ /Kp | R ₂ /Kp | L/Kp |
|------------------|------|----------------|-------------------|--------------------|--------------------|------|
| 40 | 33.7 | .0189 | .0158 | .418 | 3.47 | .016 |
| 40 45 | 36.2 | .0175 | .0173 | .371 | 3.18 | .014 |
| 4 <i>5</i> 50 | 38.1 | .0142 | .0163 | .376 | 3.29 | .014 |
| 55 | 41.1 | .0134 | .0140 | .346 | 3.22 | .014 |
| 60 | 43.6 | .0123 | .0119 | .318 | 3.15 | .015 |
| 65 | 46.0 | .0102 | .0112 | .304 | 3.23 | .014 |
| 70 | 48.4 | .00813 | .0105 | .327 | 3.22 | .014 |
| , 5 | | | | | | |

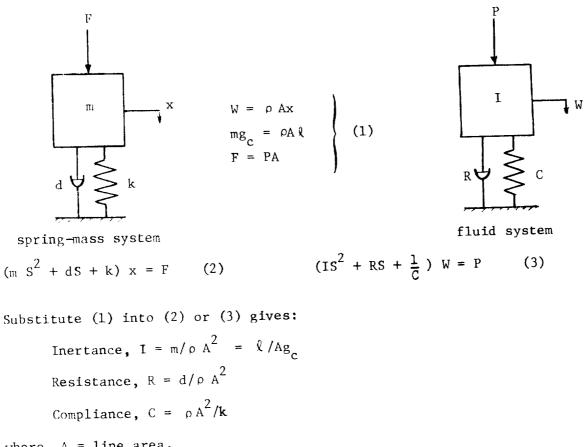
Table 4.6

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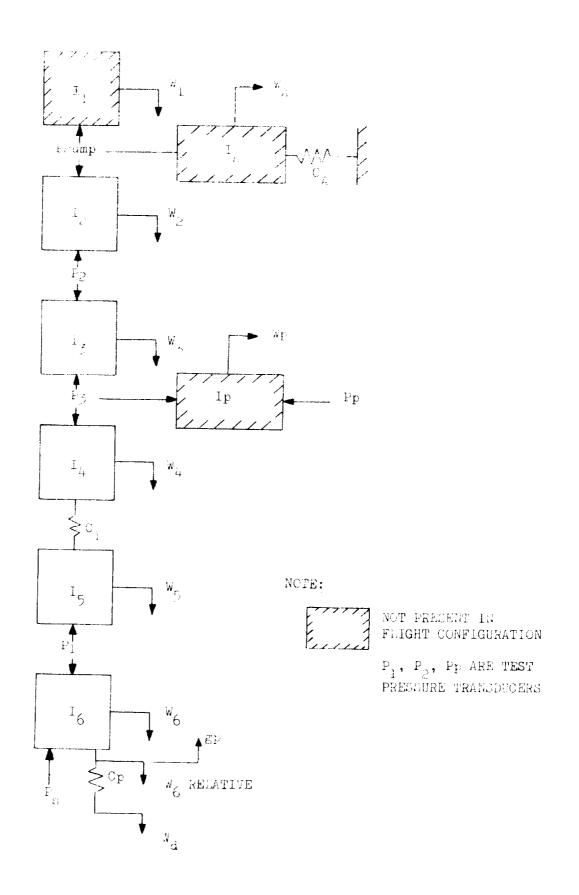
Suction Pressure Power

| Turbopump Configuration | С _ь | Aver. k | age Test ∂C _b /∂k | Parameters P _v /q | n |
|----------------------------|----------------|------------|---------------------------------|---------------------------------|--------------|
| LR87 Fuel LR87 Ox | .019 .014 | .08 .07 | 54 37 | .004 | 2.37 |
| LR91 Ox | . 027 | .10 | 90 | .035 | 2.33 4.44 |
| F-1 Fuel | .088 | .06 | 94 | .000 | .64 |
| F-1 Ox | .095 | .07 | 95 | | .83 |
| J-2 Fuel | .019 | .036 | 40 | .041 | 1.62 |
| J-2 Ox | .011 | .044 | 30 | .035 | 2.10 |
| H-1 Fuel | .012 | .26 | 023 | .000 | .49 |
| H-1 Ox | .014 | .13 | 075 | .039 | .92 |
| MB-3 Fuel | . 9023 | .21 | 011 | .000 | 1.01 |
| MB-3 Ox | . 027 | .048 | 60 | .02 | 1.50 |

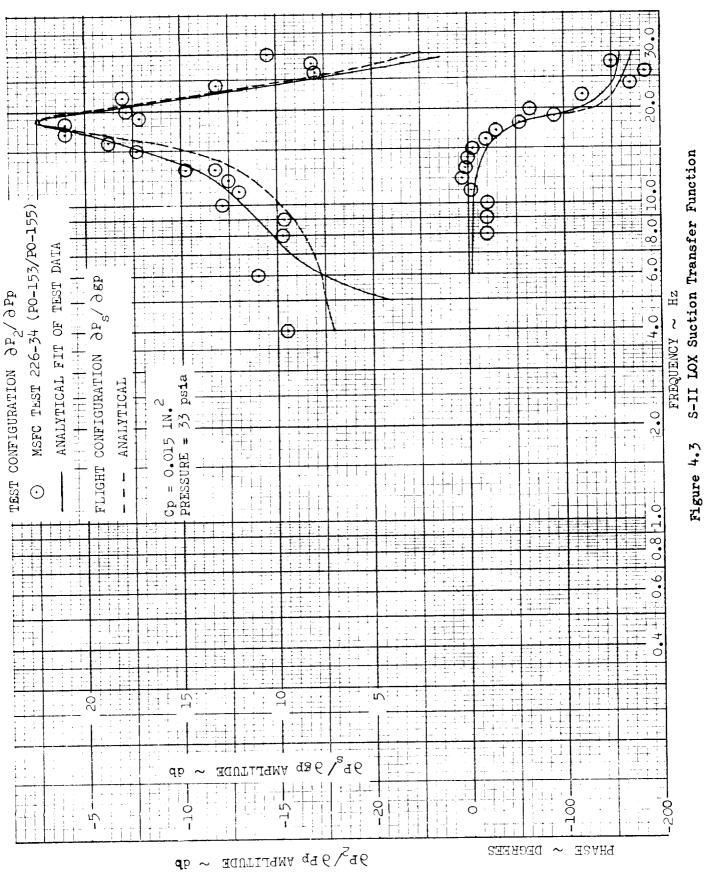


where A = line area, χ = line length, g_c = gravitational constant, ρ = fluid density.

Figure 4.1 Comparison of Spring-Mass and Fluid Systems



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S-II LOX Suction Transfer Function

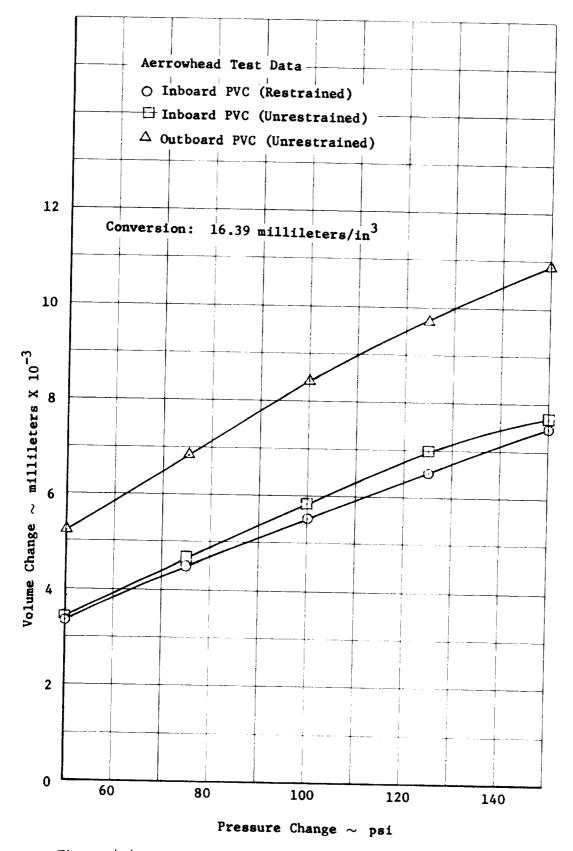


Figure 4.4 S-IC LOX PVC Volume Change With Pressure

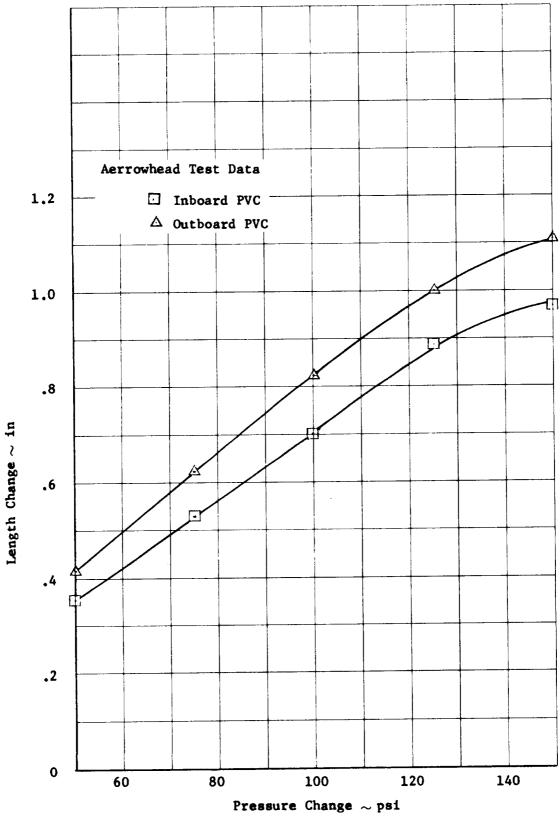
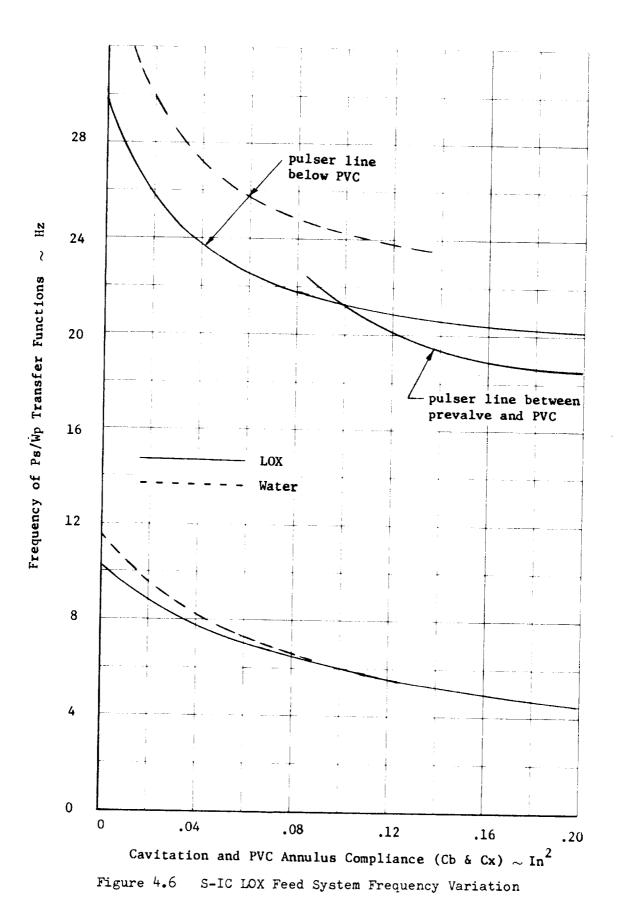


Figure 4.5 S-IC LOX PVC Length Change With Pressure



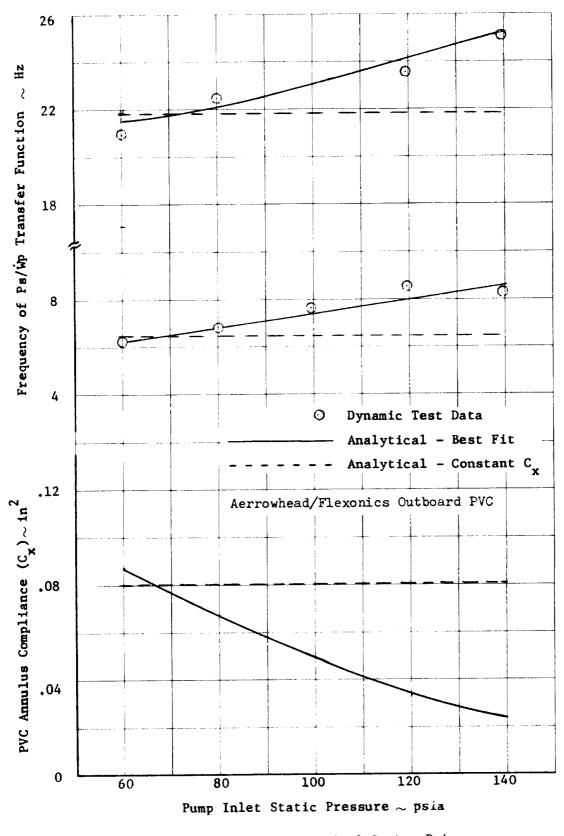
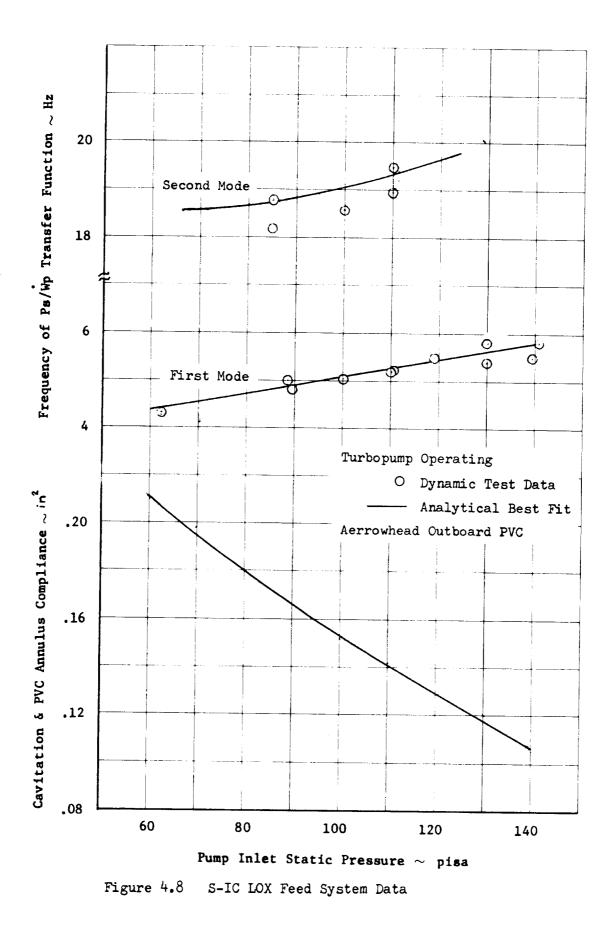


Figure 4.7 S-IC LOX Non-Flow Feed System Data



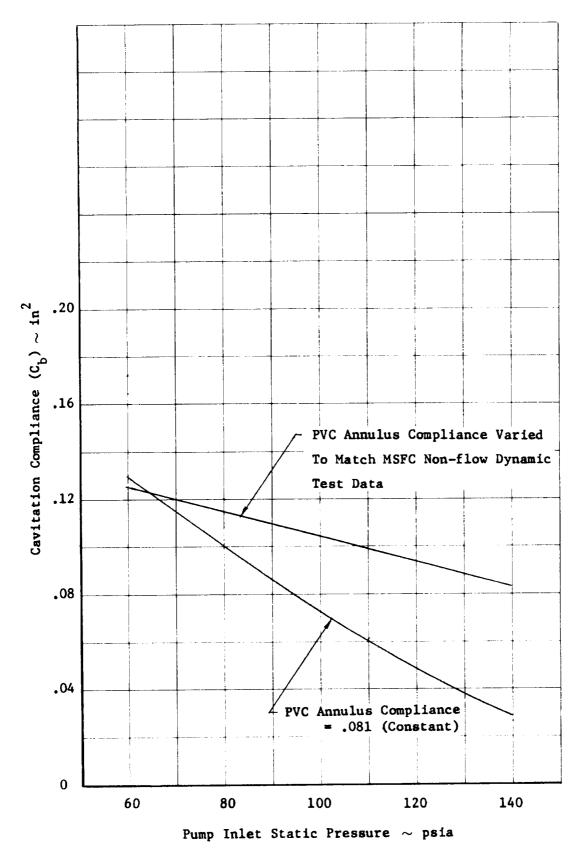
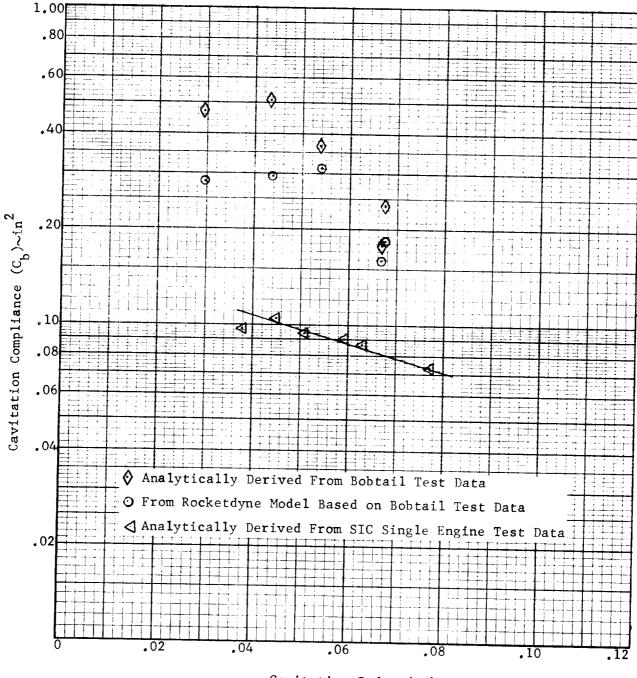


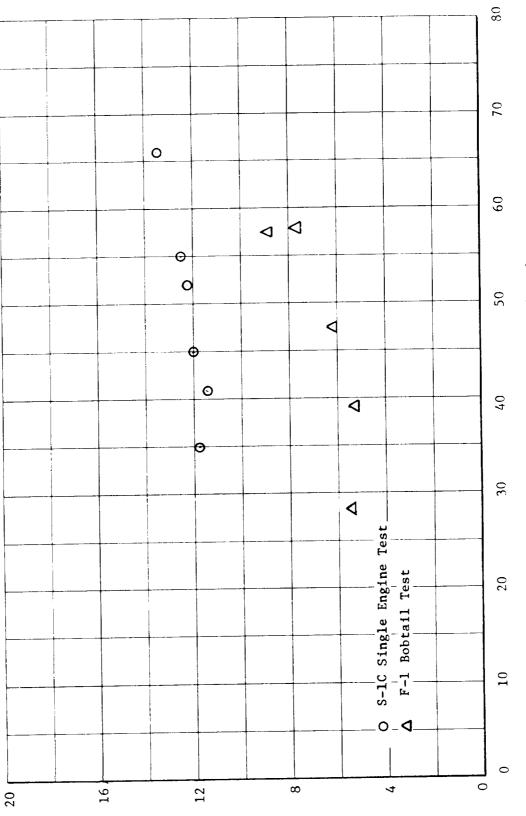
Figure 4.9 F-1 LOX Turbopump Cavitation Compliance



Cavitation Index (ND)

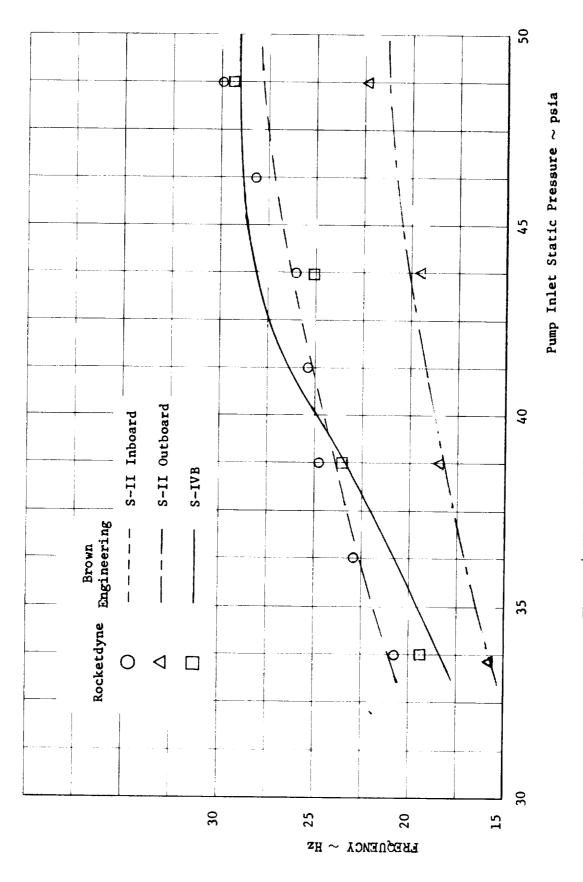
Figure 4.10 F-1 Fuel Turbopump Cavitation Compliance

Figure 4.11 F-1 Fuel Feed System Frequency Data

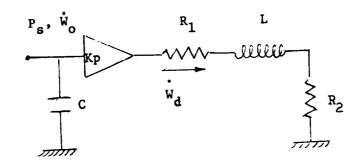


Fuel Pump Inlet Pressure (psia)

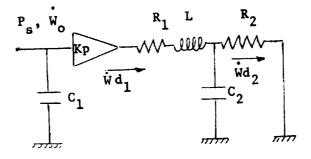
Fuel System Resonant Frequency (Hz)



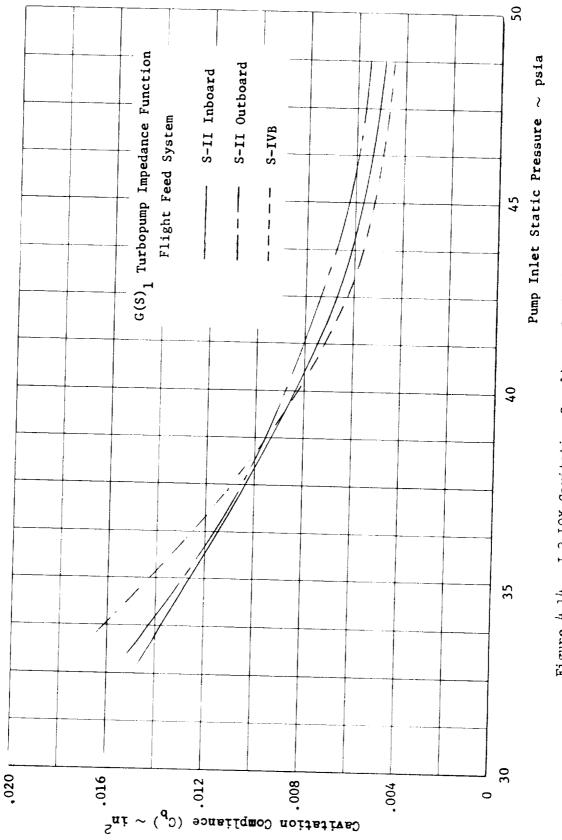




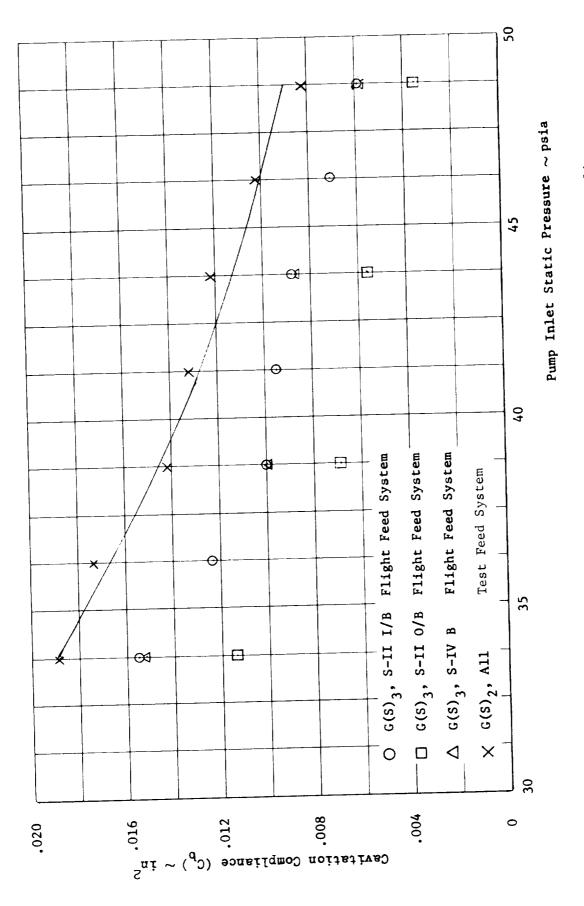
a. Single Compliance Model



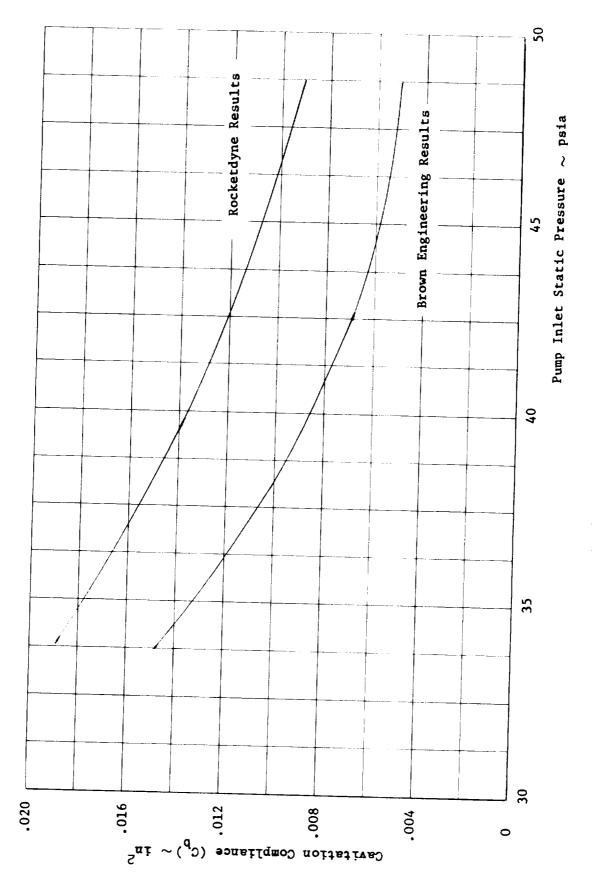
b. Double Compliance Model















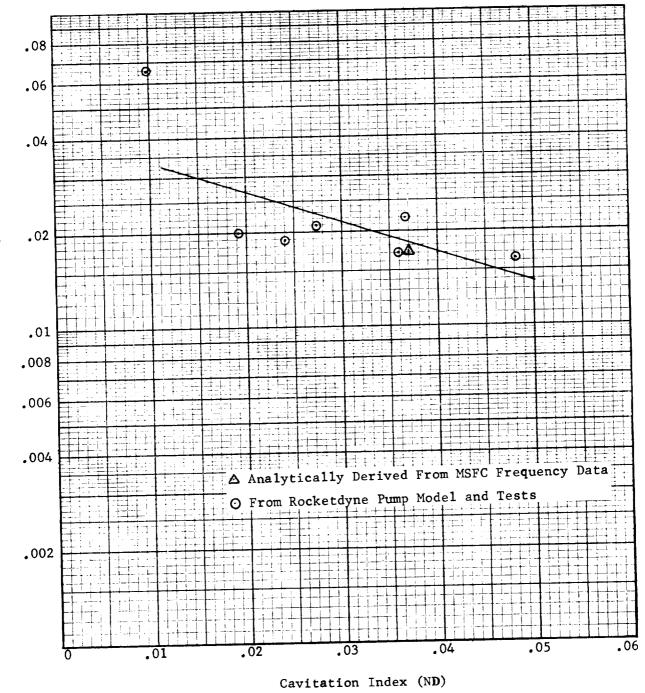
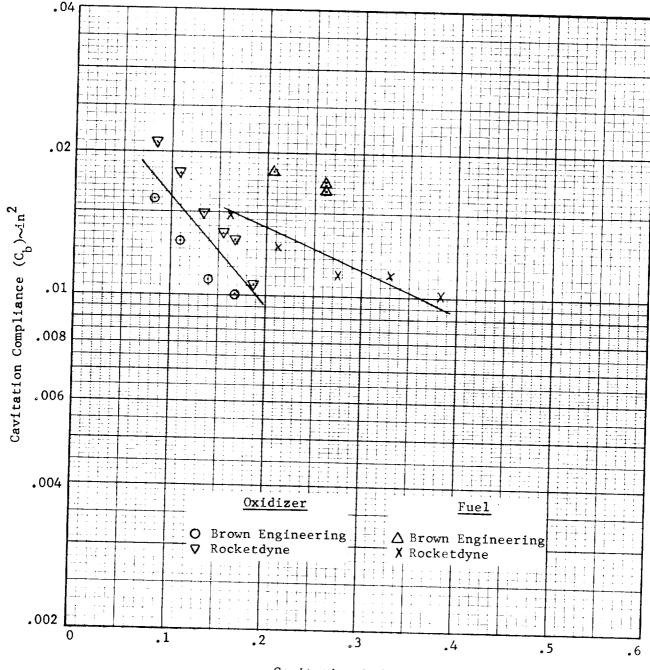


Figure 4.17 J-2 Fuel Turbopump Cavitation Compliance



Cavitation Index (ND)

Figure 4.18 H-1 Oxidizer and Fuel Turbopump Cavitation Compliance

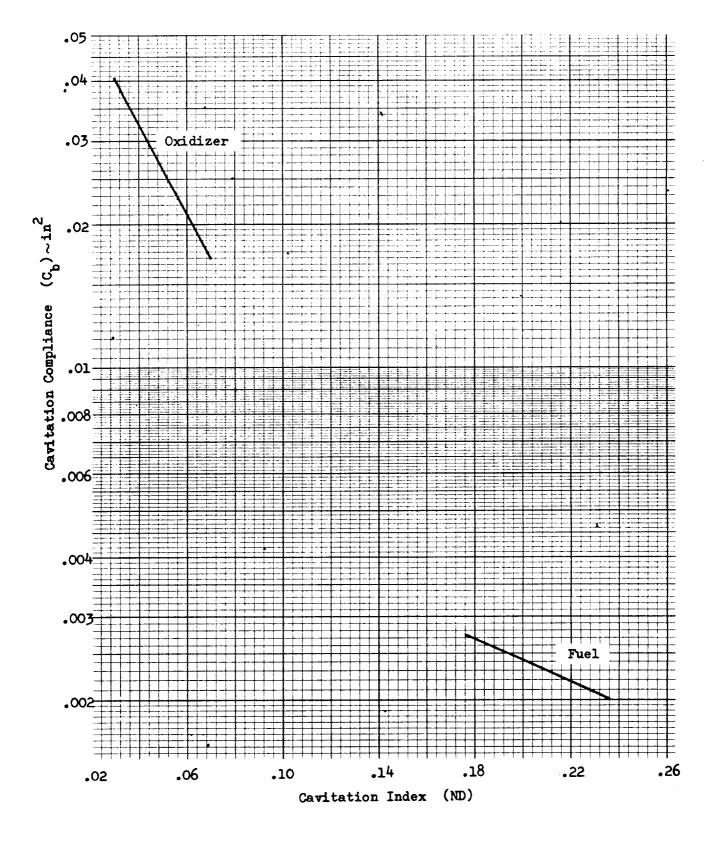


Figure 4.19 MB-3 Cavitation Compliance

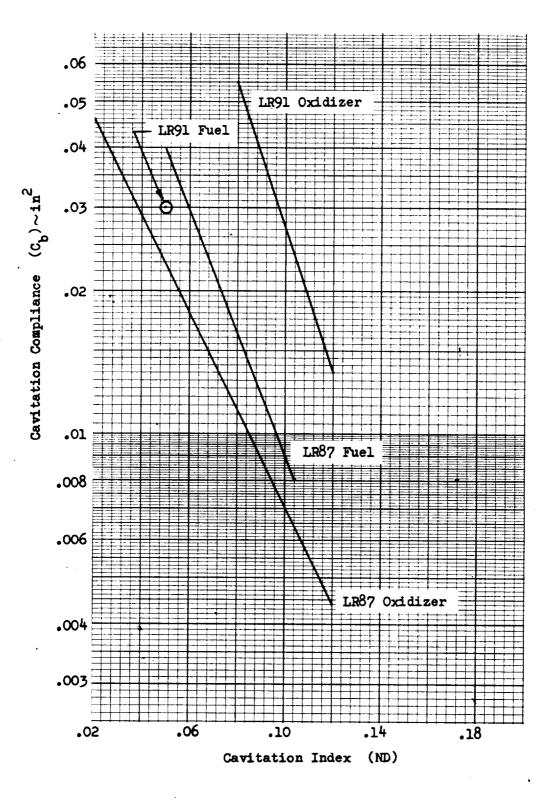


Figure 4.20 Titan Turbopump Cavitation Compliance

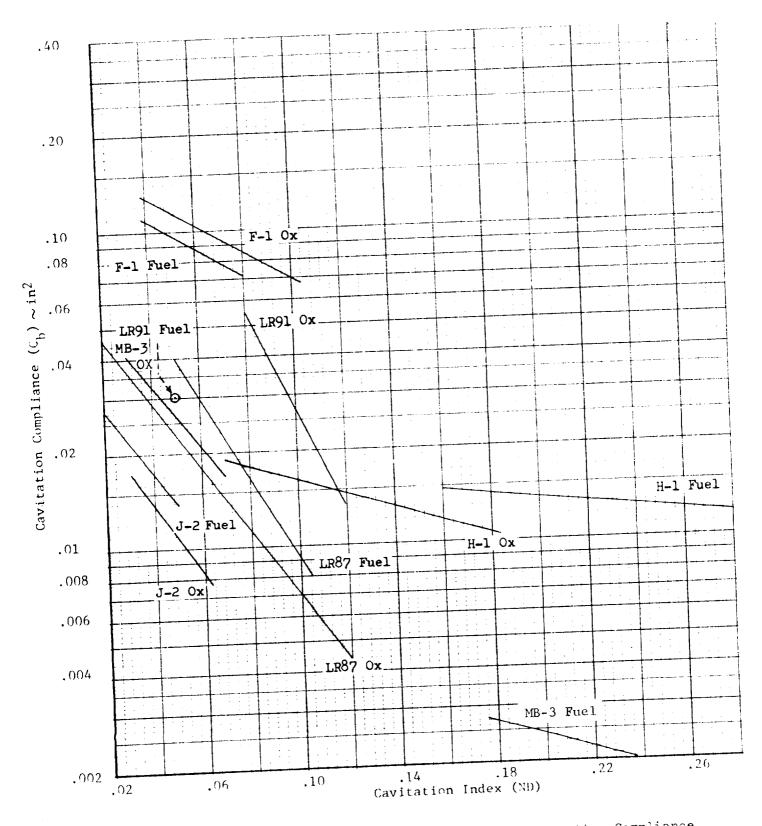


Figure 4.21 Oxidizer and Fuel Turbopump Cavitation Compliance

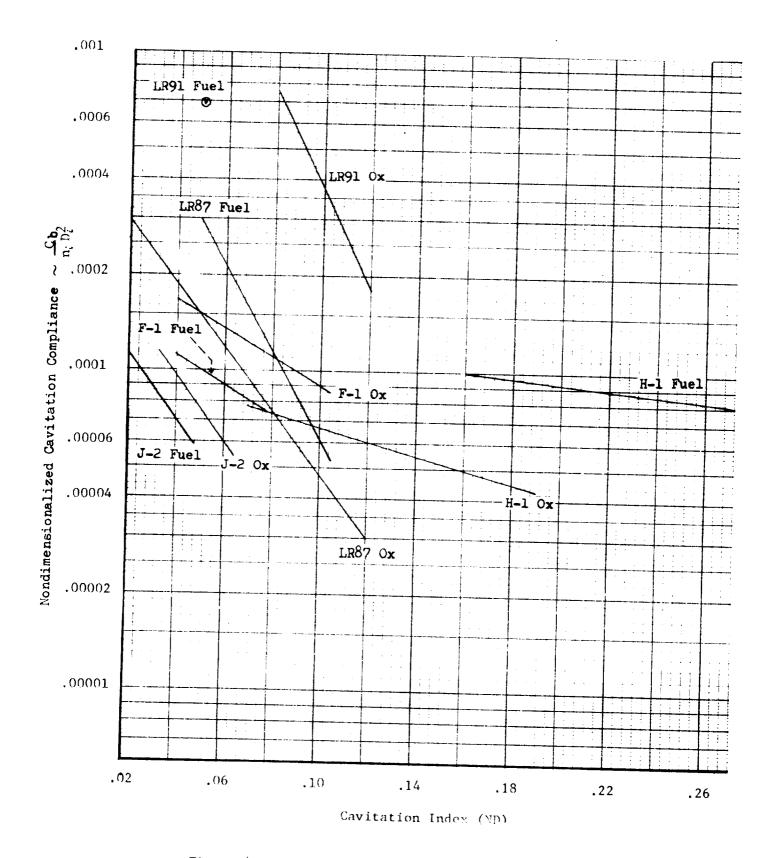


Figure 4.22 Nondimensionalized Turbopump Cavitation Compliance

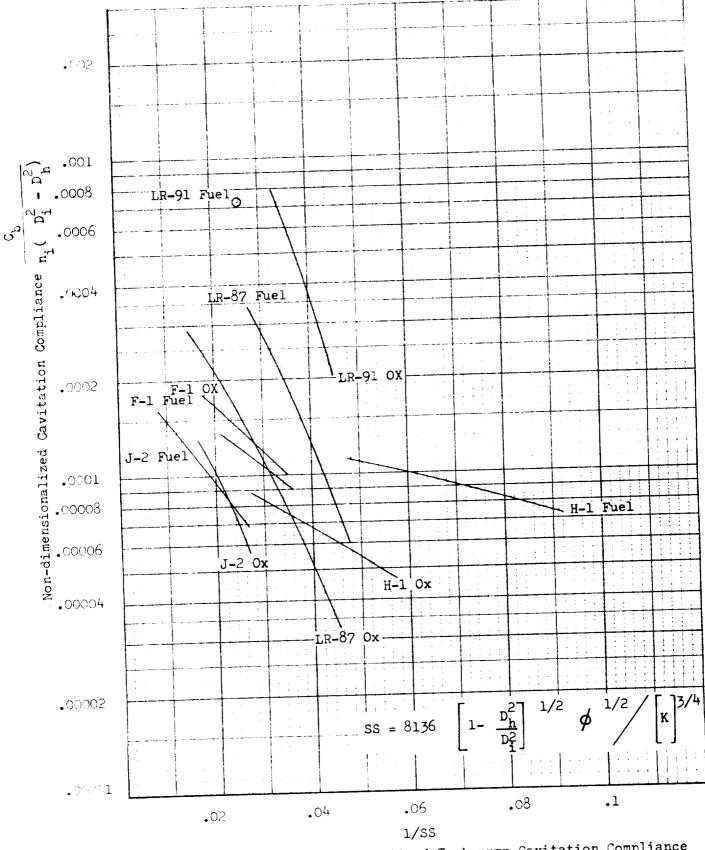


Figure 4.23 Nondimensionalized Turbopump Cavitation Compliance

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5. Empirical-Analytical Correlation

5. EMPIRICAL - ANALYTICAL CORRELATION

5.1 <u>Analytical Results</u> - The turbopump cavitation model described in Section 3. was used to analyze the J-2 LOX, F-1 LOX, H-1 LOX, and LR87 oxidizer turbopumps. These four configurations were selected because they are typical of those of interest in the determination of cavitation compliance for POGO analysis. Also, considerable test data exists for these configurations and their geometry and operation are in reasonable agreement with the assumptions of the analytical model. Because of the large pressure rise which occurs through the inducers (for example, 100 psi through the J-2 inducer and 300 psi through the F-1 inducer) it is assumed that any mismatch between the inducer exit flow and the impeller blades is not sufficient to produce a significant amount of cavitation in the impeller. For this reason only the inducers were analyzed.

5.1.1 Blade Section Analysis - The complete analysis of an inducer requires that the computer model be run for different streamsheets corresponding to different blade cross sections at different inducer radii. These results are then interpolated and integrated to yield the total cavitation compliance for all the inducer blades from the hub to the tip. Initial analyses performed for the J-2 and F-1 inducers employed the blade sectional data as tabulated on the inducer design drawings (Figures 5.1 and 5.2, respectively). This data defines the blade geometry for a constant distance off the inducer hub, and is normally only given for a few blade sections. The turbopump cavitation compliance program was thus restricted by both the limited amount of input data and the fact that the data supplied for a given blade section was associated with a constant distance off the inducer hub, and not a fixed percent of the distance between the hub and the feedline wall. The results of these

analyses indicated significantly different behavior of the cavitation phenomenon between the hub and blade tip, and did not agree favorably with test data. Recent analyses performed for all four inducers have utilized a different form of input blade geometrical data. A computer program was written to interpolate the supplied data and calculate blade geometrical data for five blade sections located at 10%, 30%, 50%, 70%, and 90% of the blade span. Details of this computer program are given in Appendix F. This simulation improvement resulted in an order of magnitude reduction in predicted cavitation.

5.1.1.1 Figures 5.5 through 5.8 show the blade sectional data derived from the inducer design drawings (Figures 5.1 through 5.4) for the J-2 LOX, F-1 LOX, H-1 LOX, and LR87 oxidizer turbopumps. It is noted that this data has been normalized to the trailing edge. Figures 5.9 through 5.12 show the results of interpolating this data to five blade sections, each at a constant percent of blade span. As shown by these figures, $\Delta Z/\Delta \Theta$ is constant and independent of r for the J-2, F-1, and H-1 inducers. These inducers are a constant pitch helical screw design and are symmetrical about the chord. In contrast, the LR87 inducer is a twisted flat plate cambered in the vicinity of the leading edge.

5.1.2 <u>Calculation Procedure</u> - Because most of the inducers analyzed exhibit a linear relationship between blade coordinates Z and Θ , the most suitable transformation from the inducer coordinates (r, Θ , Z) to the streamsheet coordinates (E, Z) is simply

- E = Z (5.1)
- $F = \Theta \tag{5.2}$

This transformation is used in lieu of the logarithmic spiral transformation, Equations (3.10), which is more suitable for the impeller portions of a turbopump. For channel flow the streamsheet width varies as a function of Z and is defined by

$$b(Z) = b(Z_0)(r_t(Z) - r_h(Z))/C$$
 (5.3)

where:

 r_t = the blade tip radius r_h = the hub radius $b(Z_o)$ = selected streamsheet width at Z_o $C = (r_t(Z_o) - r_h(Z_o))$

The feedline axial velocity, U, can have any radial distribution provided that continuity is satisfied, i.e.,

$$\dot{W} = 2 \pi \rho_{l} \int_{r_{h}}^{r_{t}} U r dr \qquad (5.4)$$

where p_{ℓ} is the inlet fluid density. For a uniform inlet fluid velocity distribution the flow in a streamsheet annulus is given by

$$W_{ss} = 2 \pm r(Z_0) b(Z_0) \rho_{l} U$$
(5.5)

For this analysis, a constant value of $b(Z_0)$ was used for all streamsheets in each inducer, causing \dot{W}_{ss} to vary as a function of radius. Other local angles such as the blade angle, β , the inlet flow angle, ϕ , and the angle of attack relative to the upstream undistrubed flow, α , are defined by

$$\beta = \tan^{-1} \left(\frac{1}{r} \quad \frac{\Delta Z}{\Delta \Theta} \right)$$
 (5.6)

$$\phi = \tan^{-1} \left(\frac{1}{r} \frac{U}{\omega} \right)$$
 (5.7)

$$\alpha = \beta - \phi \tag{5.8}$$

In the (E, F) coordinate system the blade angle is $\Delta Z/\Delta \theta$ and the flow angle is U/ω , both of which tend to be independent of the radius or of which streamsheet is under consideration. All of these parameters are given in Table 5.1. Each pump inducer was analyzed for two inlet flow angles, U/ω , and a range of inlet pressures, P_s , for the streamsheets described above. Each calculation produced a description of the flow field in the particular streamsheet in terms of the streamfunction, ψ , pressure field, P, and the weight of propellant in the streamsheet, W_{ss} . Figure 5.13 shows a computer output plot of the streamlines in a J-2 LOX inducer streamsheet which corresponds to a 30% blade section. For the purpose of calculating cavitation compliance the prime model output is W_{ss} , which is computed by

$$W_{ss} = \sum_{i} \rho_{i} A_{i} b_{i}$$
(5.9)

where

 p_i = density of the two phase fluid at grid point i A_i = area between grid points b_i = streamsheat width at and

$$i = \text{streamsneet width at grid point i}$$

From Equation (1.2) the cavitation compliance in a streamsheet

between two blades is given by

$$C_{ss} = \frac{\Delta W}{\Delta P_{s}}$$
(5.10)

An example of C derived from computer output is shown in Table 5.2. The total turbopump cavitation compliance for N blades is given by

$$C_{b} = N \int_{r_{b}}^{r_{t}} \frac{\partial C_{ss}}{\partial r} dr$$
 (5.11)

where $\frac{\partial C_{ss}}{\partial r} = \frac{C_{ss}}{b}$ (5.12)

Since most of the cavitation occurs near the inlet; $b = b(Z_0)$ which was chosen to be the same at each radius section. Equation (5.11) thus becomes

$$C_{b} = \frac{N}{b(Z_{o})} \int_{r_{h}}^{r_{t}} C_{ss} dr$$
(5.13)

5.1.3 <u>J-2 Results</u> - Analytical values of W_{ss} were obtained from the computer model for inlet pressures from 32 to 50 psia, values of U/ ω (inlet flow direction) of .33 and .20, and five blade sections. The resulting streamsheet compliance is shown in Figure 5.14 for five inlet pressures and the nominal flow direction of U/ ω = .33. These results are relatively well behaved and exhibit the expected trend with variations in inlet pressure. Also, the variation along the blade appears to be reasonable in view of the following factors:

- a. For constant streamsheet inlet thickness the tip streamsheet has a larger fluid flow (Equation 5.5);
- b. The blades are thinner at the tip which results in a sharper leading edge;
- c. The blades are thinner at the tip which also results in less venturi effect between the blades;
- d. The angle of attack at the tip is lower than at the hub (Equations 5.6, 5.7, and 5.8).

The first two factors would tend to produce higher streamsheet compliance at the tip than at the hub while the last two factors have the opposite effect. The graphical integration of these results (Figure 5.14), along with similar results for an inlet flow direction of $U/\omega = .20$, according to Equation (5.13) give the following values of cavitation compliance.

| U/o (in/rad) | .33 | .20 | Inlet Press (psia) |
|------------------------|-------|-------|--------------------|
| | .0044 | .0063 | 33. |
| Cavitation | .0033 | .0053 | 36. |
| Compliance $\sim in^2$ | .0023 | .0039 | 40. |
| | .0012 | .0023 | 44. |
| | .0005 | .0014 | 48. |

5.1.3.1 The sensitivity to inlet flow direction requires consideration of the factors involved. The actual analytical inlet flow direction is determined from the slope of the computed streamlines upstream of the blades. The upstream boundary conditions are then automatically adjusted until the computed slope matches the desired slope calculated with respect to the undisturbed flow. Computation of the potential flow solution at different distances into the suction line (Figure 5.18) showed that propogation of blade disturbances extend approximately one inch upstream. This was found to be true for all the inducers analyzed. The pressure field upstream of this point remains essentially constant (+1 psi). An additional error source, not included in the model, is fluid prerotation produced by fluid viscosity (Figure 5.19). As stated previously, all flow was assumed to be inviscid. An upper bound of viscous produced prerotation of 67% of the turbopump speed ($\omega_r = 2/3\omega$) was assumed for analytical evaluation. This yielded a new inlet flow direction of $U/(\omega + \omega_r)$, or 60% of the nominal U/ω computed without considering prerotation. This effect is not intended to be representative of actual prerotation values, but is only used to demonstrate the influence on cavitation results.

5.1.4 F-1 Results - Analytical values of streamsheet fluid weight, W_{ss} , were obtained from the computer model for inlet pressures from 60 to 140 psia, U/ω values of .86 and .52, and five blade sections. For the nominal value of inlet flow direction (U/ ω = .86), computed without consideration for viscous induced prerotation, the model predicted no cavitation at any of the blade sections for the range of inlet pressures considered. That is, the minimum pressure predicted by the potential flow solution was always greater than the LOX vapor pressure. Reducing the flow direction to 60% of nominal to account for neglected prerotation resulted in small amounts of blade cavitation for inlet pressures below 100 psia. As shown in Figure 5.15 cavitation was observed at the 30%, 50%, and 70% blade sections. Reasons for variations at different blade sections are the same as discussed in Paragraph 5.1.3. Initial predictions, based only on the two blade sections

defined on the drawing (Figure 5.2), assumed that the amount of cavitation increased toward the blade tip. These results indicate that was a bad assumption. Local conditions can produce cavitation at a mid section, while for the same inlet conditions none occurs at either the hub or the blade tip. Applying Equation (5.13) to the results in Figure 5.15, and to the computed results for U/w = .86, gives the following values of cavitation compliance.

| U/o (in/rad) | .86 | .52 | Inlet Press. (psia) |
|--|-----|-------|---------------------|
| | 0 | .0020 | 65 |
| ${}^{ m Cavitation} \sim { m in}^2$ Compliance | 0 | .0009 | 75 |
| | 0 | .0005 | 85 |
| | 0 | .0002 | 95 |
| | 0 | 0 | 105 |

5.1.5 <u>H-1 Results</u> - Analytical values of streamsheet fluid weight, W_{ss} , were computed for inlet pressures from 40 to 90 psia, U/ω values of .42 and .25, and five blade sections. The results showed that essentially no cavitation was predicted for the nominal flow direction of $U/\omega = .42$, and very little cavitation for the flow direction reduced to account for possible viscous pre-rotation effects. Figure 5.16 shows the minimum pressure obtained in the H-1 LOX inducer which occurs at a grid point near the blade leading edge of the 30% section. For non-cavitating conditions the pressure increment between the inlet static pressure and the minimum pressure grid point is essentially constant for fixed flow conditions. This is reasonable since compressibility effects should be minimal if there is no cavitation vapor present. Figure 5.16 shows that cavitation starts at an inlet pressure of 46 psia for nominal U/ω and 59 psia for U/ω reduced to 60% of nominal. However, even for pressures below these values, so few grid points reach vapor pressure that no significant cavitation is produced. At blade sections other than the 30% sections no cavitation was predicted.

5.1.6 <u>LR87 Oxidizer Results</u> - The computer model generated values of streamsheet fluid weight, W_{ss} , for inlet pressures from 40 to 90 psia, U/ $_{\odot}$ values of .32 (nominal) and .19, and five blade sections. The results showed no measurable change in W_{ss} implying no blade cavitation. For the nominal inlet flow direction the potential flow solution predicts that the minimum pressure grid point is only 17 psi below the inlet pressure (Figure 5.17). This means that the inlet pressure would have to be reduced to 31 psia before the minimum pressure reaches the vapor pressure resulting in cavitation. This computed pressure reduction from the inlet to the minimum pressure point is considerably less for the LR87 than the other inducers. These values, along with some of the influential parameters,

These values, drong way are shown in Table 5.3 for comparison. Not all of the parameters are in the right direction (lower angle of attack, thinner blade, and lower dynamic pressure); however, the combination could justify the smaller pressure increment for the LR87. For the inlet flow direction reduced by 60% (U/ ω = .19) to simulate a worst case viscous pre-rotation, the minimum pressure point is 36 psi lower than the inlet pressure (Figure 5.17). In this case cavitation just begins for an inlet pressure of 49 psia. For the lowest pressure case analyzed, 40 psia, no significant cavitation had developed.

5.2 Comparison With Test Data - The first task performed in the comparison of the analytical and test results was to compare the predicted inducer pressure rise with available test data. Figure 5.20 shows J-2 LOX inducer head rise test data (Reference 53) using water as the test fluid. This indicates a head rise of 172 ft (75 psi for water) for the nominal operating flow rate of 2540 gal/min $(U/\omega = .33 \text{ in/rad})$. Figure 5.21 shows the corresponding pressure profiles predicted by the computer model at the 50% blade section for an inlet pressure of 100 psia (230 ft NPSH). This shows a predicted pressure rise of greater than 60 psi, and it could easily be 75 psi depending on where the measurement is taken. The model predicts slightly greater pressure rises at a hub blade section (10%) and slightly less pressure rises at a tip blade section (90%). In the actual case, radial mixing will occur and tend to give a uniform pressure rise (in the radial direction) through the inducer. Thus the 50% blade section is felt to be most representative even though the pressure measurement is assumed to be taken on the pump housing nearest to a tip blade section. The J-2 LOX inducer head rise test data was the only pressure data available for comparison with analytical predictions. This single point comparison tends to confirm the overall accuracy of the potential flow equations used to compute pressures through the inducer blades. Analytical-empirical correlation of the cavitation compliance is obviously not as good as the pressure correlation since little or no cavitation was predicted in three out of the four inducers analyzed. On the other hand, test data (Figure 4.21) indicates that a significant amount of cavitation occurs in all turbopumps. Figures 5.22 and 5.23 present a comparison between test data and the cavitation compliance predicted by the analytical model for the J-2 and F-1 LOX inducers, respectively. Since no cavitation was predicted for either the H-1 or LR87 inducers, comparative plots are not presented. Plots of test data for these inducers were presented in Figures 4.18 and 4.20, respectively.

No model assumptions have been identified which could account for the lack of correlation observed. Beasonable variations in inlet flow direction to simulate viscous prerotation tended to improve predictions but failed to yield adequate correlation. Also, since no cavitation was predicted in some inducers, the analytical results can not be simply scaled to agree with test data. The entire results of this analysis indicate that some other mechanism besides blade cavitation contributes significantly to total turbopump compliance. Other mechanisms presented (Section 2.) as having potential significance are: blade tip clearance flow, circulation flow within the turbopump, and circulation flow back into the feedline.

5.2.1 Since the effect of cavitation compliance on feed system natural frequency is of prime interest, it is important to determine how uncertainties in one propagate into uncertainties in the other. The first feed system natural frequency, ω_1 , can be defined by

$$\omega_{1} = \sqrt{\frac{1}{I (C_{b} + C_{l})}}$$
(5.14)

where

. . .

 C_{b} = cavitation compliance

I = suction line fluid inertance

 C_{ℓ} = equivalent total suction line and fluid compliance (except pump cavitation) related to the pump inlet.

Differentiating Equation (5.14) yields

$$\frac{d\omega_{1}}{\omega_{1}} = -\frac{c_{b}}{2(c_{\ell} + c_{b})} - \frac{dc_{b}}{c_{b}}$$
(5.15)

which shows that the percentage change in ω_1 is at most 1/2 the percentage change in C_b , and may be much less if C_l is large relative to C_b . For the S-II/J-2 LOX feed system, C_l is .003 to .005 in.² (Rocketdyne results, Table 4.4). Using these values of C_{p} and test values of C_{b} in Equation (5.15), it may be concluded that for a maximum uncertainty of 10% in S-II feed system natural frequency cavitation compliance must be known to within 25%. A similar evaluation on the other systems of concern results in the following required accuracies in cavitation compliance for a 10% accuracy in frequency: 70% for S-IC/F-1 LOX; 25% for S-IB/H-1 LOX; and 35% for Titan/LR87 Ox. As previously stated, an objective of the cavitation model development is that it be capable of predicting feed system frequency to within a 10% accuracy. The results predicted by the current model clearly do not meet this objective. Although additional refinements and extensions to the existing model framework could be recommended, it is felt that none of them have a high probability of resulting in adequate correlation with test data.

| Inducer | J-2 LOX | F-1 LOX | H-1 LOX | LR-870X |
|--------------------------------------|---------|---------|---------|-----------|
| No. of Blades | 3 | 3 | ۷. | 3 |
| Flow Rate (W) lb/sec | 386. | 3765. | 514. | 522. |
| Pump Speed (0) rad/sec | 841. | 581. | 706. | 874. |
| Inlet Velocity (U) in/sec | 275. | 497. | 294. | 276. |
| U/ω in | .33 | .86 | .42 | . 32 |
| Chord کے/Zد in | .59 | 1.25 | .76 | Fig. 5.12 |
| Inlet Thickness $(b(Z_0))$ in | .323 | .331 | .317 | .294 |
| Tip Radius (r,) in | 3.375 | 7.875 | 3,80 | 3.55 |
| Tip Blade Angle (β) deg | 9.0 | 9.9 | 11.3 | 5.7 |
| Tip Flow Angle (Ø) deg | 5.6 | 6.2 | 6.3 | 5.2 |
| Tip Angle of Attack (α) deg | 3.4 | 3.7 | 5.0 | 0.5 |
| | | | | |

Table 5.1 Inducer Streamsheet Parameters

Table 5.2 Streamsheet Cavitation Compliance J-2 LOX Inducer, 50% Section, U/ω = .33

| P s | Wss | 7M 7M | 7 b | Css |
|--------|--------|----------|-----|--------|
| 50 | .17938 | | | |
| 48 | | .00015 | 4 | .00004 |
| 46 | .17923 | | | |
| 44 | | .00026 | 4 | .00007 |
| 42 | .17897 | | | |
| 40 | | .00042 | 4 | .00011 |
| 38 | .17855 | | | |
| 36 | | .00056 | 4 | .00014 |
| 34 | .17799 | | | |
| 33 | | .00038 | 2 | .00019 |
| 32 | .17761 | | | |

| Inducer | "tip (deg) | "hub (deg) | Blade Thickness ⁽¹⁾ (% of channel) | $1/2\rho V_r^2$ (psi) | $P_{s}-P_{min}^{(2)}$ (psi) |
|---------|---------------|---------------|--|-----------------------|--------------------------------|
| J-2 LOX | 3.4 | 15.1 | 32 | 433. | (3) |
| F-1 LOX | 3.7 | 9.4 | 18 | 1120. | 59 |
| H-1 LOX | 5.0 | 14.5 | 26 | 388. | 30 |
| LR87 Ox | .5 | 8.9 | 19 | 655. | 17 |

Table 5.3 Factors Affecting Minimum Inducer Pressure

- (1) At the 50% blade section
- (2) Nominal inlet flow direction
- (3) $P_{min} = vapor pressure$

| | А◄ |
|--|-----|
| | A C |
| (B) 6 SLOTS EQUALLY SPACED WITHIN OID FILLET R.020 SLOTS MAY BE ROTATED AT RANDOM | AS |

BLADE SURFACE COORDINATES ALL R & & VALUES ARE GAGE DIMENSIONS REFER TO MD-MISC-48-270 FOR ADDITIONAL WFORMATION

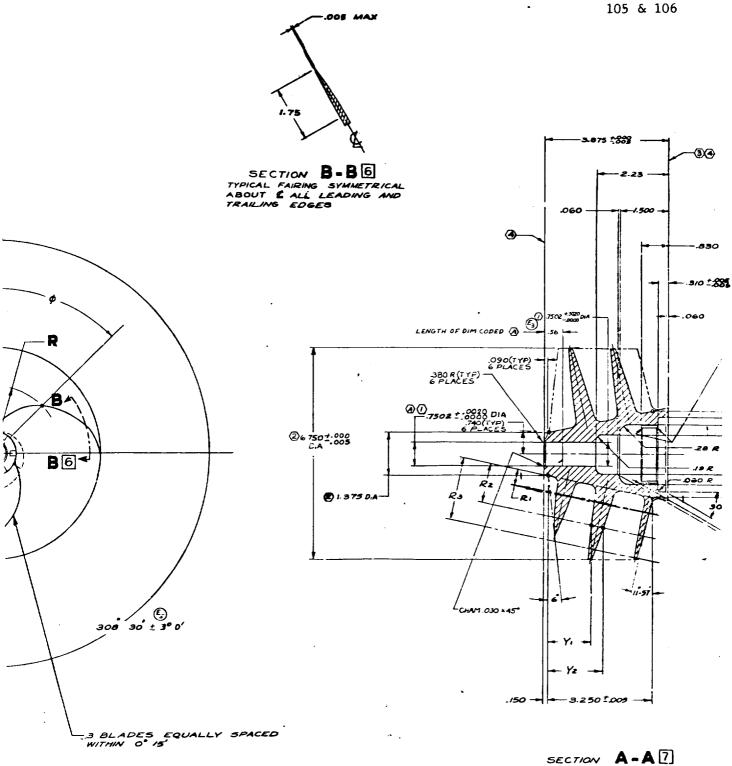
| | R1=.500 | | R2= 1.250 | | R3= 2.000 | | |
|------|---------|-----------|-----------|---------|-----------|----------|-----|
| Ø | Y11.000 | Y2 1.0100 | | 12:0100 | Y.:0100 | Y22.0100 | 1(4 |
| 20 | .0668 | .1179 | | | | | 1 |
| 30' | .1042 | 2073 | | | | | |
| 40' | .1477 | .4441 | | | | | j |
| 45' | | | .1469 | 2118 | | | I |
| 50' | .1984 | -5885 | 1613 | .2960 | | | |
| 55 | | | .1787 | .3793 | | | |
| 60' | 2972 | .7208 | .1995 | 4559 | | | 1 |
| 65' | | | 2239 | .5277 | | | L |
| 70" | 3253 | .84// | 2521 | .5940 | .2395 | .3000 | 1 |
| 75 | | 1 | 2644 | -657Z | .2625 | . 3755 | Ł |
| 80* | 4042 | 9495 | 5156. | .7/49 | 2689 | .4462 | ł |
| 85' | | | .3627 | .76 79 | .3/92 | 3/ZZ | Ł |
| 90* | .4940 | 1.0485 . | .4096 | 8173 | -3558 | .5733 | 1 |
| 95 | .5461 - | 1.0979 | 4620 | 8665 | .3932 | -6296 | |
| 100 | 5984 | 1.1474 | .5/46 | .9/60 | .4373 | -6811 | 1 |
| 105 | -6508 | 1.1971 | 5671 | 9656 | 4900 | .7307 | |
| 120 | -8083 | 1.3474 | 72.54 | 1.1155 | .6484 | .8806 | |
| 135 | .9668 | 1.4992 | -8844 | 1.2671 | .8076 | 1.0321 | 1 |
| 1500 | 1.1262 | 1.6527 | 1.0444 | 1.4204 | .9678 | 1.1853 | |
| 165' | 1 2867 | 1.8079 | 1.2054 | 1.5754 | 1.1289 | 1.3402 | |
| 180* | 1. 4485 | 1.9648 | 1.3677 | 1.7321 | 1.2913 | 1.4968 | |
| 195' | 1.6116 | 1.1234 | 1.5312 | 1.8905 | 1.4550 | 1.6553 | |
| 210. | 1.7769 | 4.2039 | 1.6963 | 2.0508 | 1.6202- | 1.8/55 |] |
| 225' | / 9427 | 2.4463 | 1.8690 | 2.2130 | 1. 7870 | 1.9776 | |
| 240 | 2.1108 | 1.6106 | 2.0315 | 2.3771 | 1.9595 | 2.1417 | |
| 295 | 2.2807 | 2.7763 | 2.2017 | 2.5432 | 2 1259 | 2.3077 | |
| 269 | 2.3995 | 2.8765 | 2.3163 | 2.6551 | 2.2405 | 2.4196 | 1 |
| 270" | | | 2. 9737 | 2.7/13 | 2.2981 | 2.4759 | 1 |
| 279 | 2.3358 | 2.9625 | 2.4330 | 2.7643 | 2.3559 | 2.5324 | 1 |
| 280' | | 1 | 2.4996 | 2 0/23 | 2.4/43 | 2.5889 | |
| 285' | 2.6917 | 3.0342 | 2.5713 | 2.8554 | 2.4771 | 2.6421 | 1 |
| 290 | | | 14.6490 | 2.8935 | 2.5447 | 2.6912 | 1 |
| 295 | 2.869/ | 3.09/6 | 2 7329 | 29266 | 2.6171 | 2.7360 | 1 |
| 300 | | | 2.8231 | 2.9540 | 2.6942 | 2.7767 | 1 |
| 505" | 3.0702 | 3.1348 | 2.9/97 | 2.9780 | 2.7760 | 28/31 | 1 |

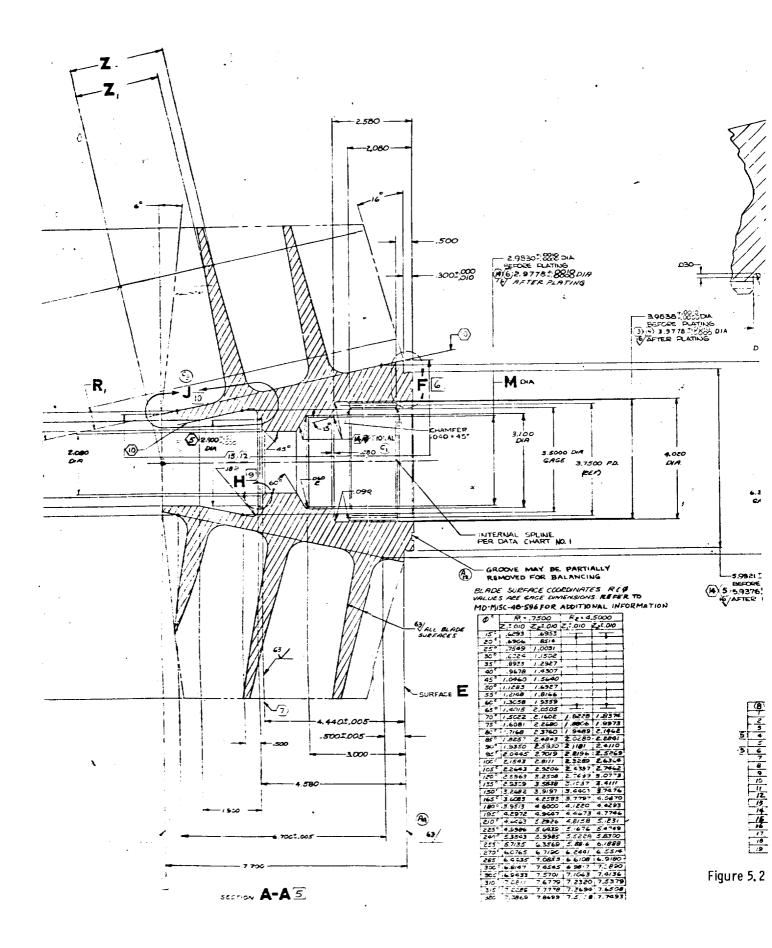
LEADING EDGE TRIM COORDINATES FAIR SMOOTHLY BETWEEN COORDINATE POINTS

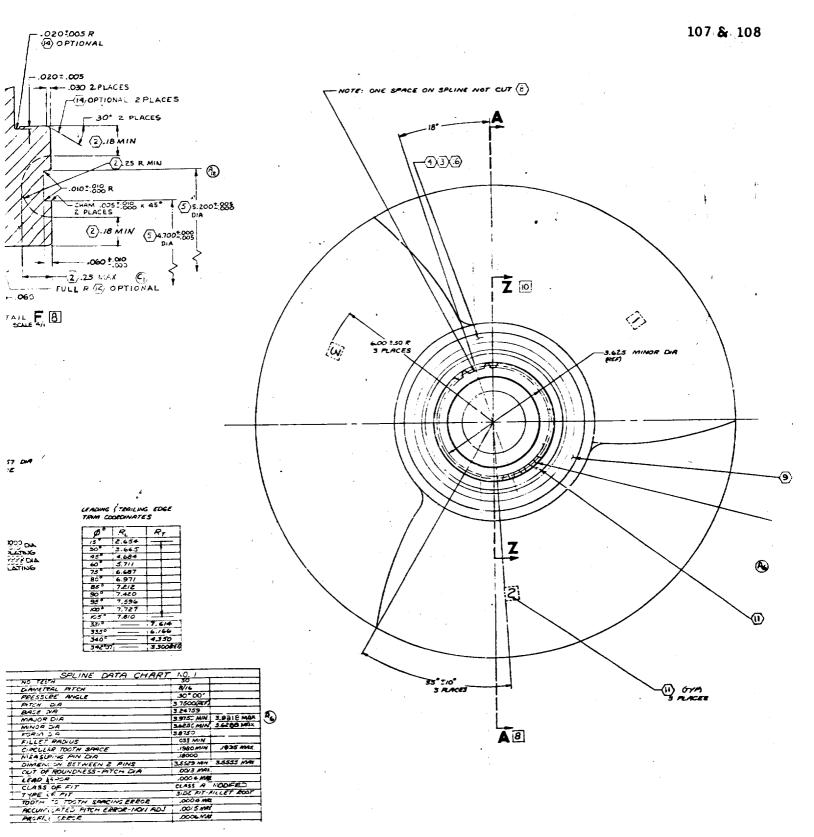
| oc | RDINA | IE POINTS | |
|----|----------------------|---------------|---|
| | MALE ØGAGE | R ±.03 | 3 |
| - | Q, | -600(RDF) | |
| | 15 | 1.162 | |
| | 30' | 1.644 | |
| | 45° | 2128 | |
| | 60 | 12.620 | |
| | 75* | 9.090 | |
| | 30. | 3.348 | |
| | | | |

.

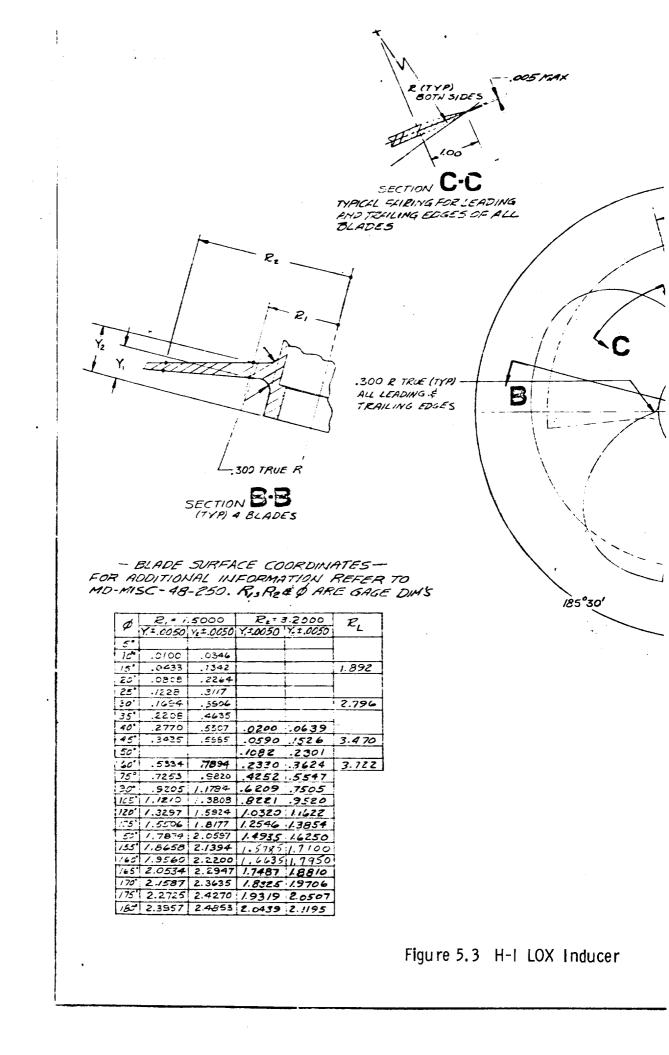
105 & 106

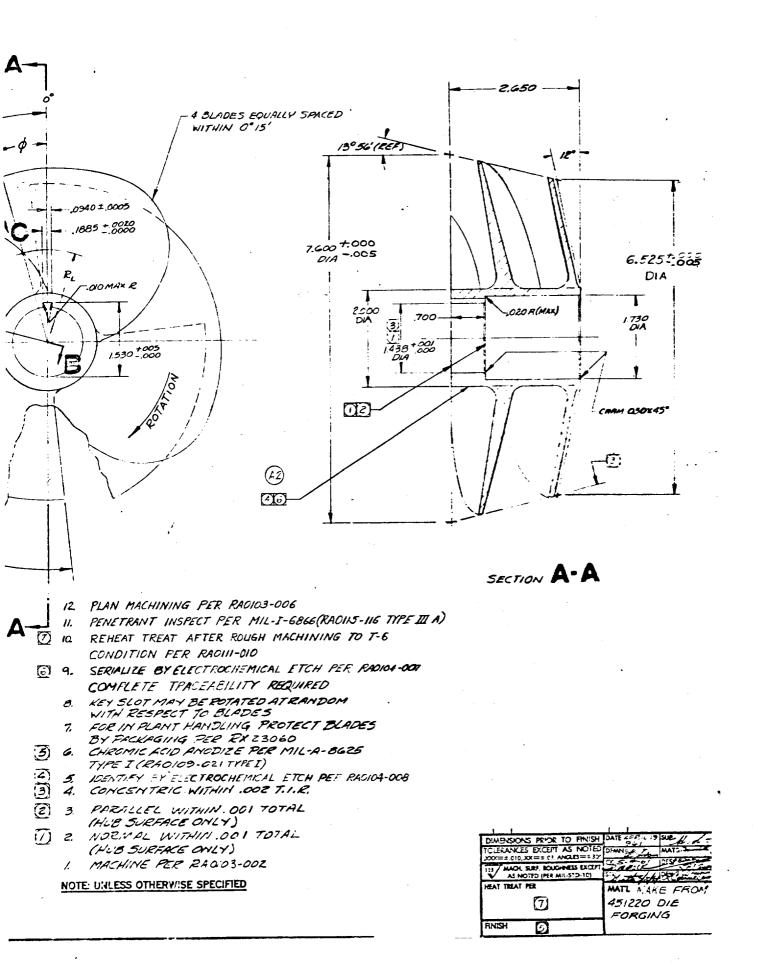


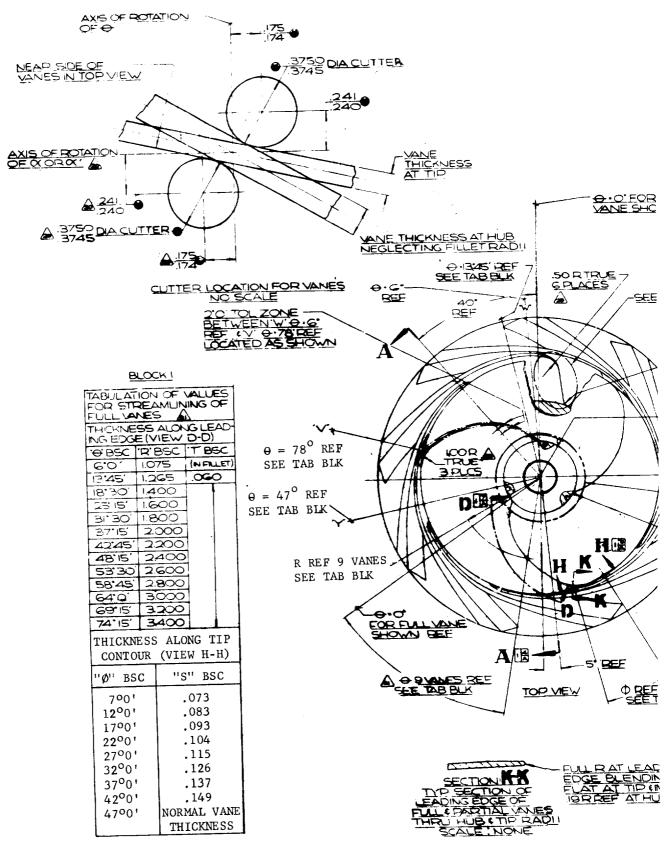




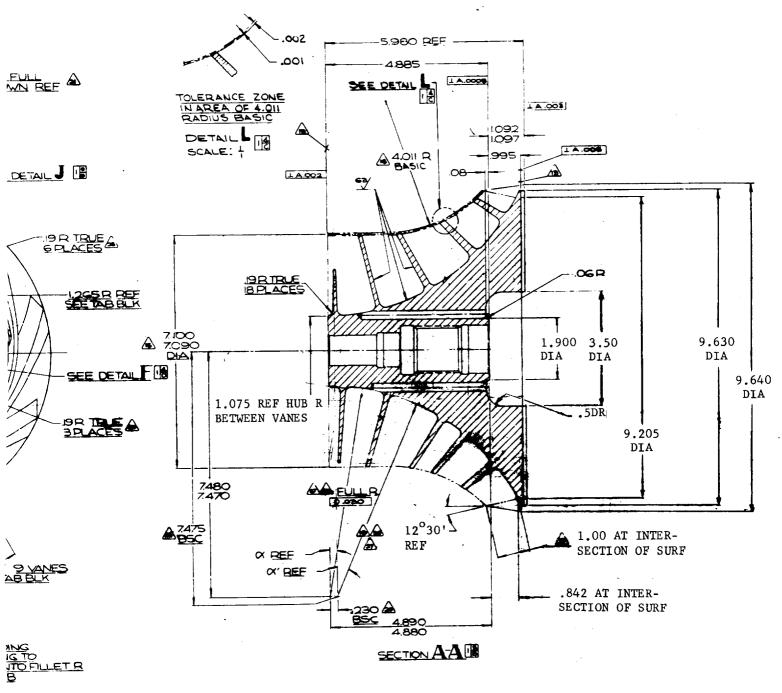
F-1 LOX Inducer





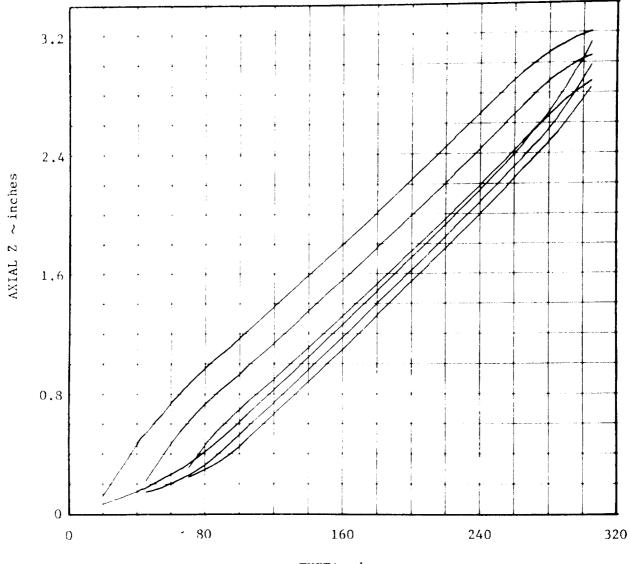


Figu re



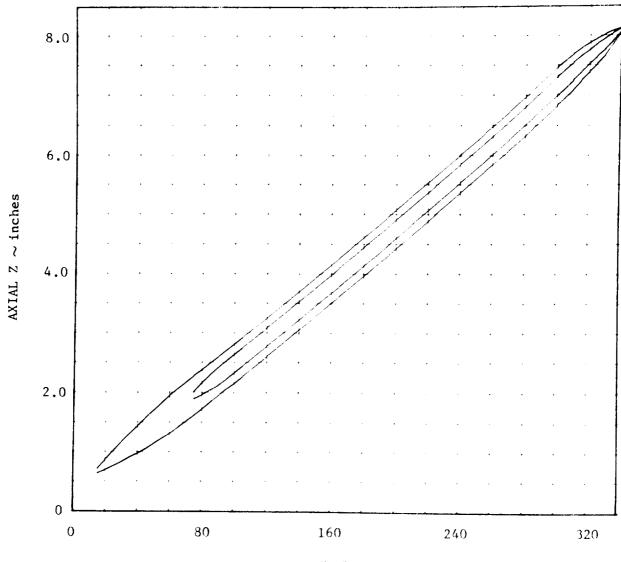
18. ALL DIM ARE FINAL & APPLY AT 68" F ONLY.

5.4 LR87 Oxidizer Inducer

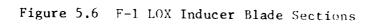


THETA $\sim degrees$

Figure 5.5 J-2 LOX Inducer Blade Sections



THETA~degrees



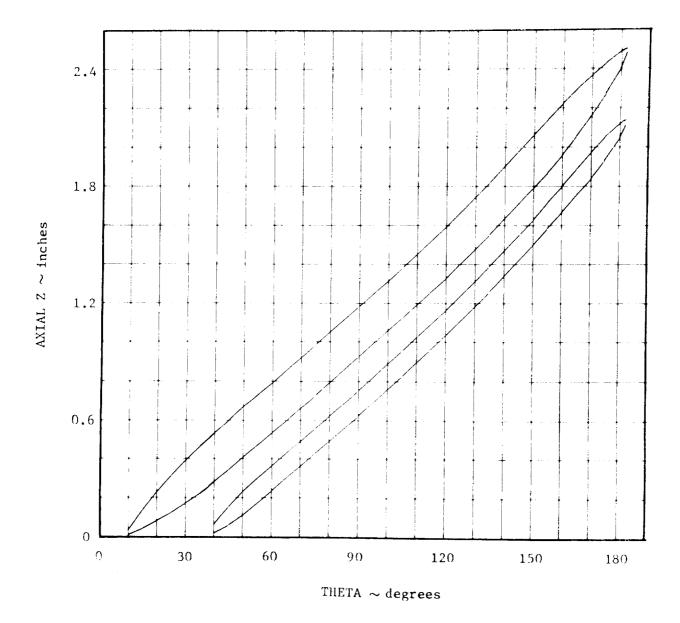
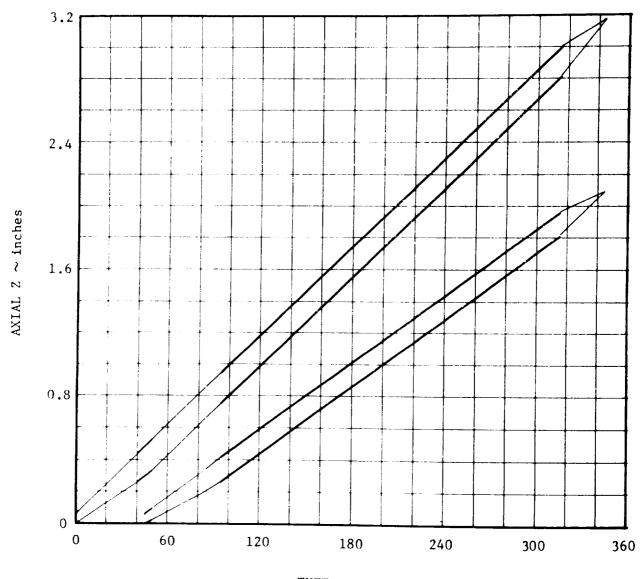


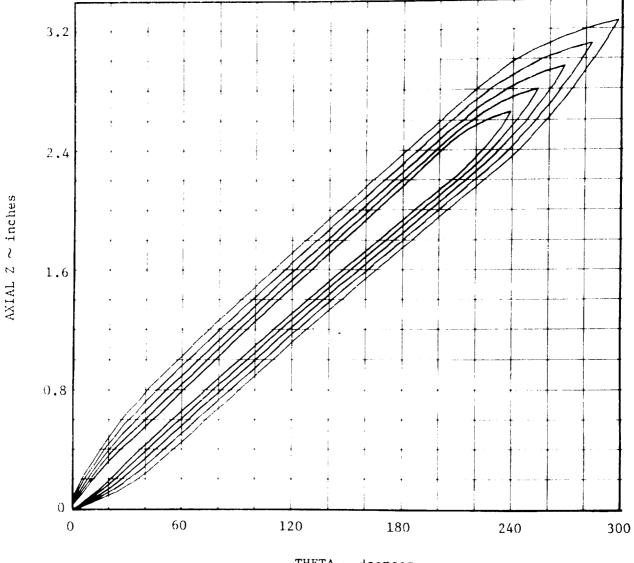
Figure 5.7 H-1 LOX Inducer Blade Sections



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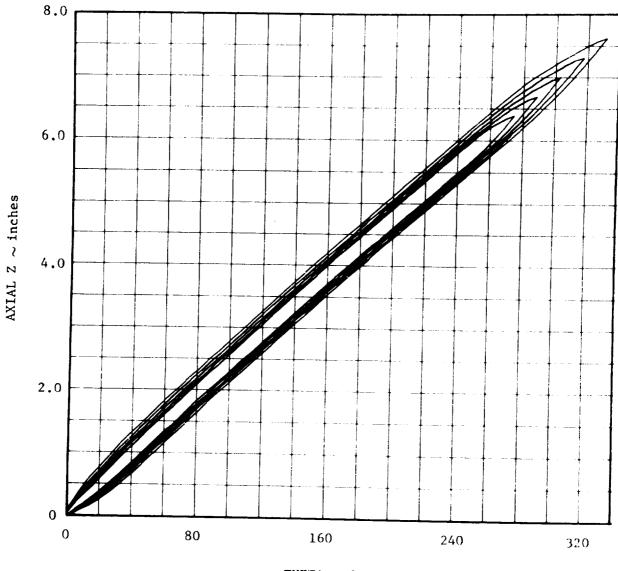
THETA \sim degrees

Figure 5.8 LR87 Oxidizer Inducer Blade Sections



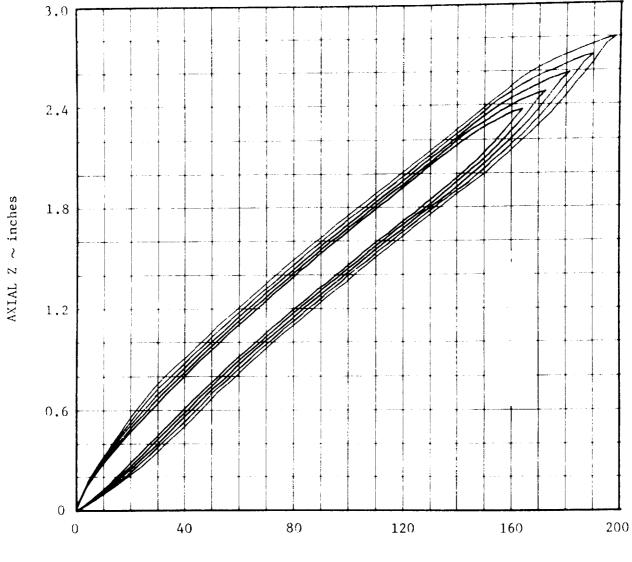
THETA \sim degrees

Figure 5.9 J-2 LOX Inducer Interpolated Blade Sections



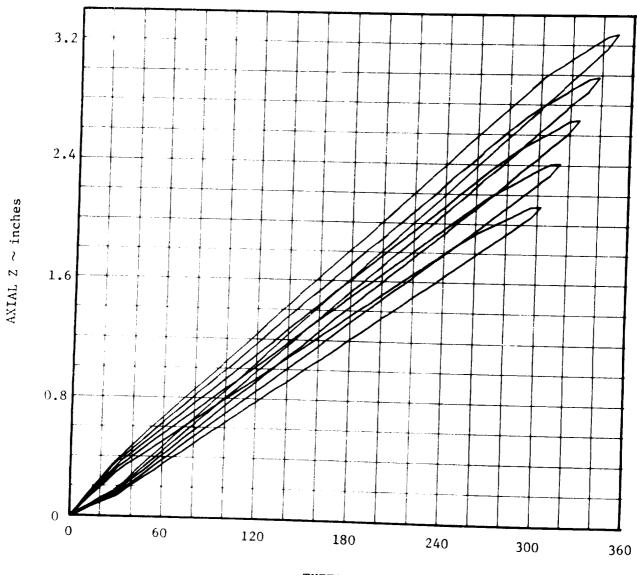
THETA \sim degrees

Figure 5.10 F-1 LOX Inducer Interpolated Blade Sections



THETA \sim degrees

Figure 5.11 H-1 LOX Inducer Interpolated Blade Sections



THETA \sim degrees

Figure 5.12 LR87 Oxidizer Inducer Interpolated Blade Sections

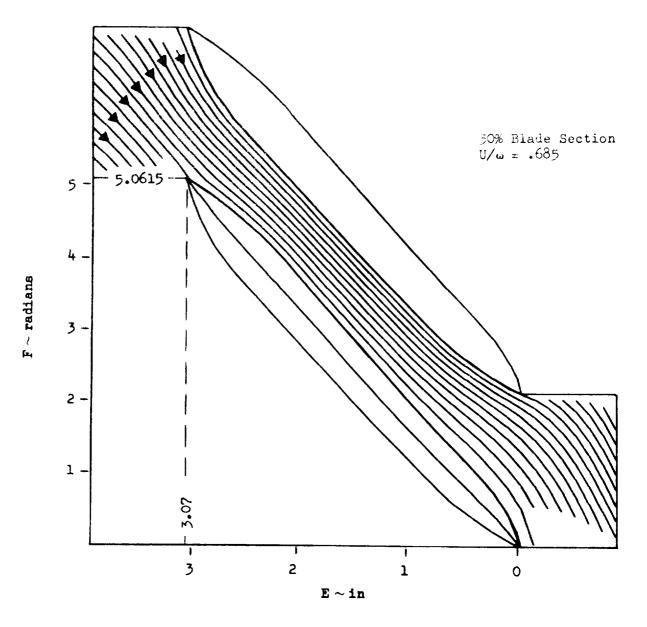
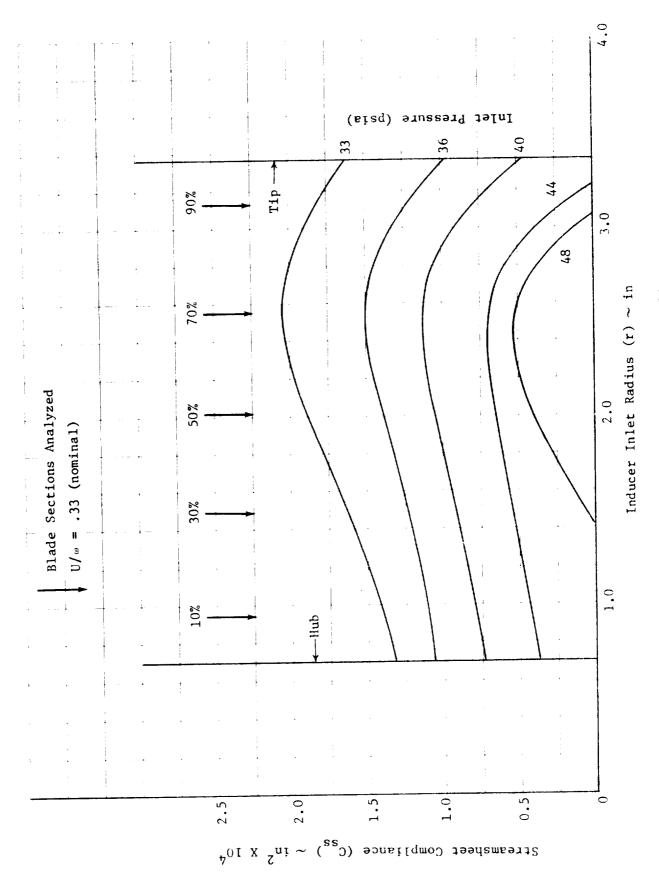


Figure 5.13 J-2 LOX Inducer Streamlines



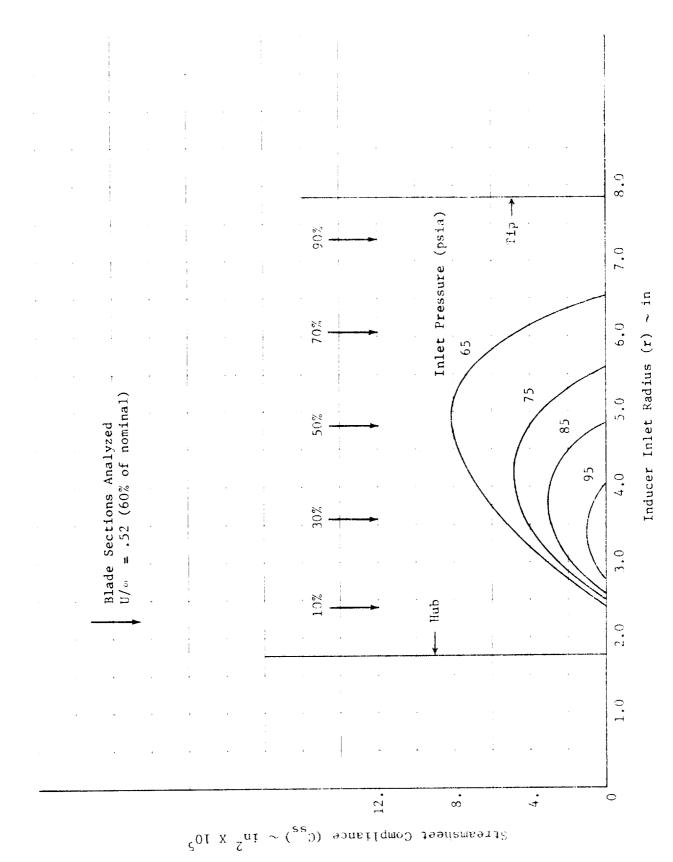
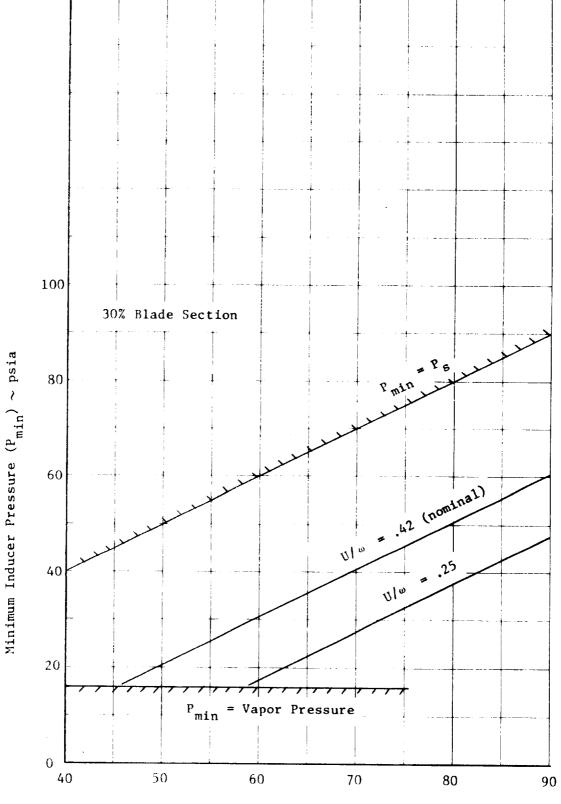


Figure 5.15 F-1 LOX Inducer Streamsheet Compliance



Pump Inlet Static Pressure (P $_{s}$) ~ psia

Figure 5.16 H-1 LOX Minimum Predicted Inducer Pressure

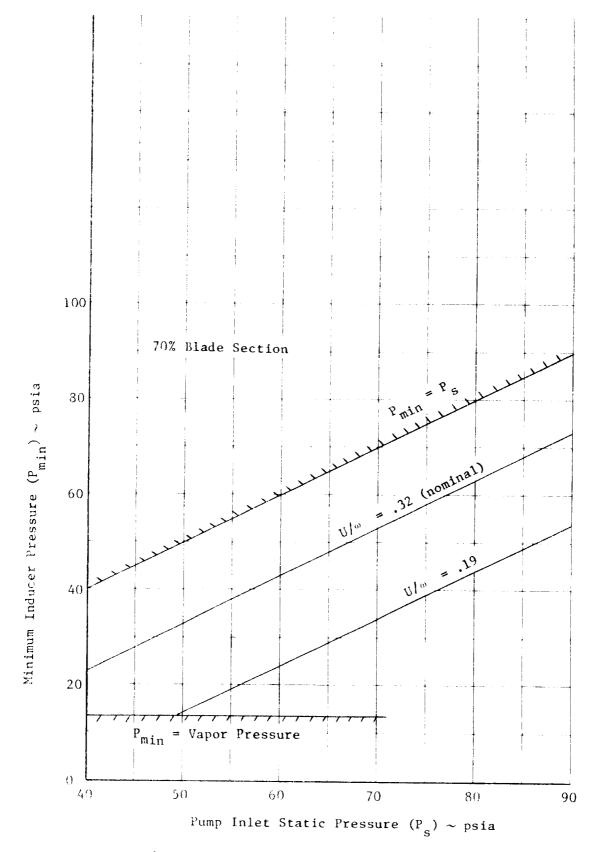
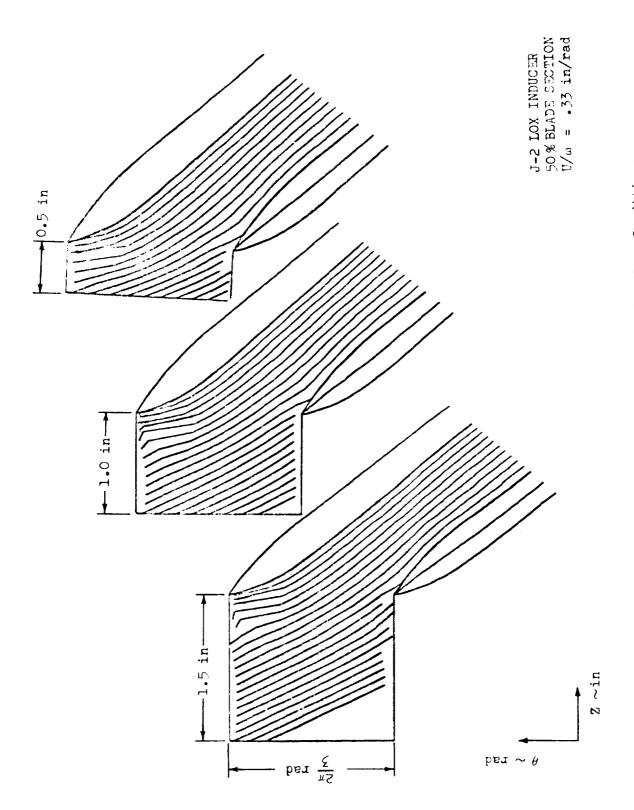


Figure 5.17 LRS7 Oxidizer Minimum Predicted Inducer Pressure



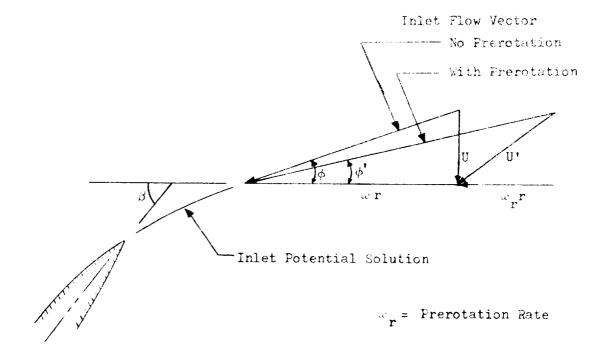


Figure 5.19 Effect of Prerotation on Inlet Flow Vector

Jeel ~ beeH lead ~ feet

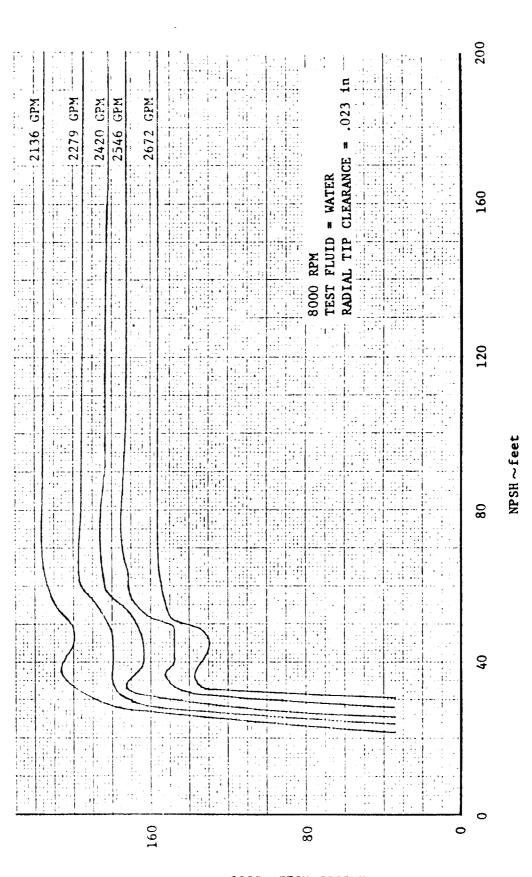


Figure 5.20 J-2 LOX Inducer Suction Performance

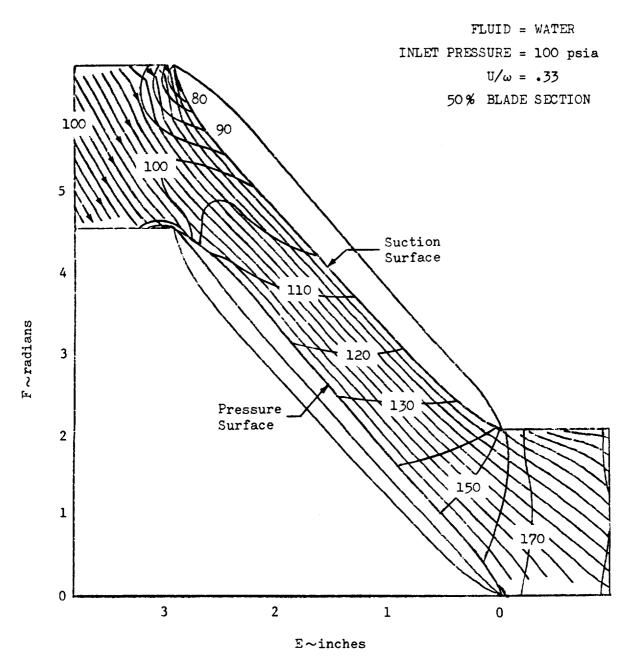


Figure 5.21 J-2 Inducer Pressure Profiles

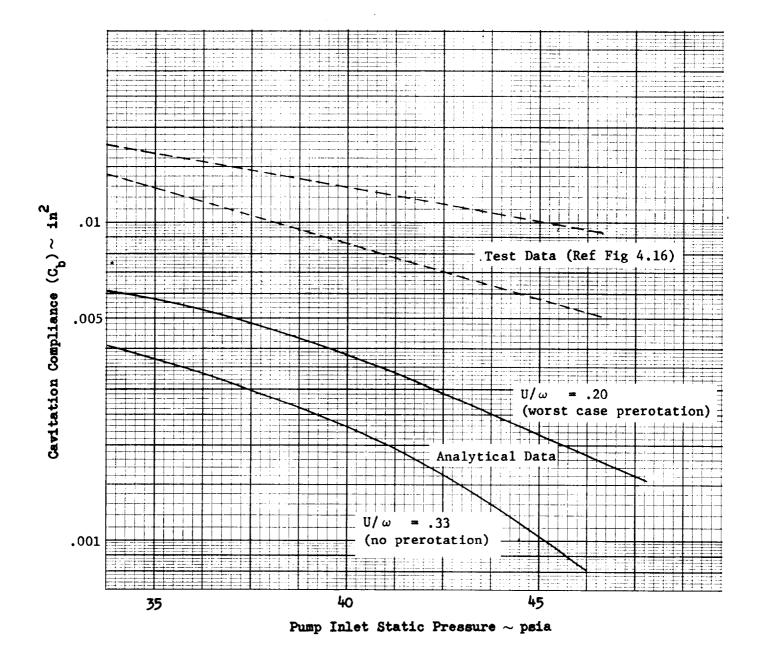
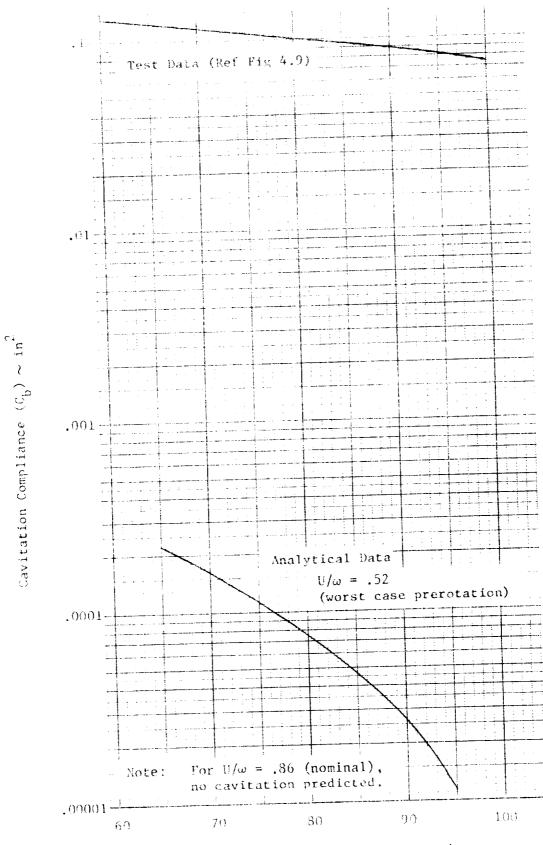


Figure 5.22 J-2 Lox Analytical-Empirical Comparison



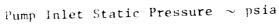


Figure 5.23 F-1 LOX Analytical-Empirical Comparison

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6. Conclusions and Recommendations

6. CONCLUSIONS AND RECOMMENDATIONS

The following conclusions and recommendations are based on the analysis of available test data, the turbopump cavitation model development, the analysis of the model results, and the correlation between test data and model predictions.

- a. Large uncertainties exist in most cavitation compliance values derived from test data. This is because the objective of the tests was to dedetermine natural frequency, and cavitation compliance must usually be derived from an assumed relationship.
- b. Cavitation compliance test results for all available turbopump configurations do not correlate with any simple nondimensional combination of turbopumps and fluid parameters.
- c. Compliance derived from a phase change process is a function of the local flow conditions and, unlike compressibility of a gas, is not necessarily directly proportional to the vapor volume.
- d. The turbopump pressure field, derived from a potential solution, will not predict a large enough blade surface cavitation region to yield agreement with test results.
- e. Mechanisms other than blade cavitation contribute the major amount of total turbopump compliance.
- f. Turbopump pulse tests, using accurate inlet and outlet dynamic flow meters, should be conducted for the purpose of investigating cavitation compliance. These tests should vary the following parameters

one at a time: test fluid, dissolved gas, operating conditions (pressure, speed, and flow), tip clearance, natural frequency and oscillation amplitude (effect of nonequilibrium phase changes), etc.

g. Precise analytical simulation of the cavitation process can not be obtained until a dedicated test program (item f.) is performed.

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Appendixes

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APPENDIX A

Equations of Motion in Impeller Meridional Plane

For a (r, θ, z) coordinate system (Figure A.1), the equations of relative motion for a turbopump impeller rotating with angular velocity ω about z (Reference 53) are:

$$\begin{split} & \left[\frac{\partial V_{\mathbf{r}}}{\partial \mathbf{t}} + V_{\mathbf{r}} \frac{\partial V_{\mathbf{r}}}{\partial \mathbf{r}} + \frac{V_{\theta}}{\mathbf{r}} \frac{\partial V_{\mathbf{r}}}{\partial \theta} + V_{z} \frac{\partial V_{\mathbf{r}}}{\partial z} - \frac{\left(V_{\theta} + \omega\mathbf{r}\right)^{2}}{\mathbf{r}} \right] \\ &= -\frac{\partial P}{\partial \mathbf{r}} - \left[\frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r} + \tau_{\mathbf{rr}}\right) + \frac{1}{\mathbf{r}} \frac{\partial \tau_{\mathbf{r}\theta}}{\partial \theta} - \frac{1}{\mathbf{r}} \tau_{\theta\theta} + \frac{\partial \tau_{\mathbf{r}z}}{\partial z} \right] + \partial g_{\mathbf{r}} \qquad (A.1) \\ & \left[\rho \left(\frac{\partial V_{\theta}}{\partial \mathbf{t}} + V_{\mathbf{r}} \frac{\partial V_{\theta}}{\partial \mathbf{r}} + \frac{V_{\theta}}{\mathbf{r}} \frac{\partial V_{\theta}}{\partial \theta} + V_{z} \frac{\partial V_{\theta}}{\partial z} + \frac{V_{\mathbf{R}}V_{\theta}}{\mathbf{r}} + 2\omega V_{\mathbf{r}} \right) \right] \\ &= -\frac{1}{\mathbf{r}} \frac{\partial P}{\partial \theta} - \left[\frac{1}{\mathbf{r}^{2}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r}^{2}\tau_{\mathbf{r}\theta} + \frac{1}{\mathbf{r}} \frac{\partial^{2}\theta}{\partial \theta} + \frac{\partial^{2}\tau_{\mathbf{r}}}{\partial z} \right) \right] + \rho g_{\theta} \qquad (A.2) \\ & \left[\partial \left(\frac{\partial V_{z}}{\partial \mathbf{t}} + V_{\mathbf{r}} \frac{\partial V_{z}}{\partial \mathbf{r}} + \frac{V_{\theta}}{\mathbf{r}} \frac{\partial V_{z}}{\partial \theta} + V_{z} \frac{\partial V_{z}}{\partial z} \right] \right] \\ &= -\frac{1}{\mathbf{r}} \frac{\partial P}{\partial \theta} - \left[\frac{1}{\mathbf{r}^{2}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r}^{2}\tau_{\mathbf{r}\theta} + \frac{1}{\mathbf{r}} \frac{\partial^{2}\tau_{\theta\theta}}{\partial \theta} + \frac{\partial^{2}\tau_{\thetaz}}{\partial z} \right) \right] + \rho g_{\theta} \qquad (A.2) \\ & \left[\partial \left(\frac{\partial V_{z}}{\partial \mathbf{t}} + V_{\mathbf{r}} \frac{\partial V_{z}}{\partial \mathbf{r}} + \frac{V_{\theta}}{\mathbf{r}} \frac{\partial V_{z}}{\partial \theta} + V_{z} \frac{\partial V_{z}}{\partial z} \right] \right] \\ & = -\frac{\partial P}{\partial z} - \left[\frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r}\tau_{\mathbf{r}z}\right) + \frac{1}{\mathbf{r}} \frac{\partial^{2}\tau_{\theta}}{\partial \theta} + \frac{\partial^{2}\tau_{zz}}{\partial z} \right] + \rho g_{z} \qquad (A.3) \end{aligned}$$

where $\rho \cdot V_{\theta}^2 / r$ is the centrifugal force. It gives the effective force in the r direction due to fluid motion in the v direction. The term $\rho \cdot V_r \cdot V_{\theta} / r$ is the coriolis force. It is the effective force in the θ direction when there is flow in both the r and θ directions. For steady inviscid flow in the absence of gravity equations (A.1) through (A.3) can be written

$$\frac{\mathrm{d}\mathbf{V}_{\mathbf{r}}}{\mathrm{d}\mathbf{r}} - \frac{\left(\mathbf{V}_{\theta} + \omega\mathbf{r}\right)^{2}}{\mathbf{r}} = -\frac{1}{\rho}\frac{\partial\mathbf{P}}{\partial\mathbf{r}} = \mathbf{V}_{\mathbf{r}}\frac{\partial\mathbf{V}_{\mathbf{r}}}{\partial\mathbf{r}} + \frac{\mathbf{V}_{\theta}}{\mathbf{r}}\frac{\partial\mathbf{V}_{\mathbf{r}}}{\partial\theta} + \mathbf{V}_{\mathbf{z}}\frac{\partial\mathbf{V}_{\mathbf{r}}}{\partial\mathbf{z}} - \frac{\left(\mathbf{V}_{\theta} + \omega\mathbf{r}\right)^{2}}{\mathbf{r}} \quad (A.4)$$

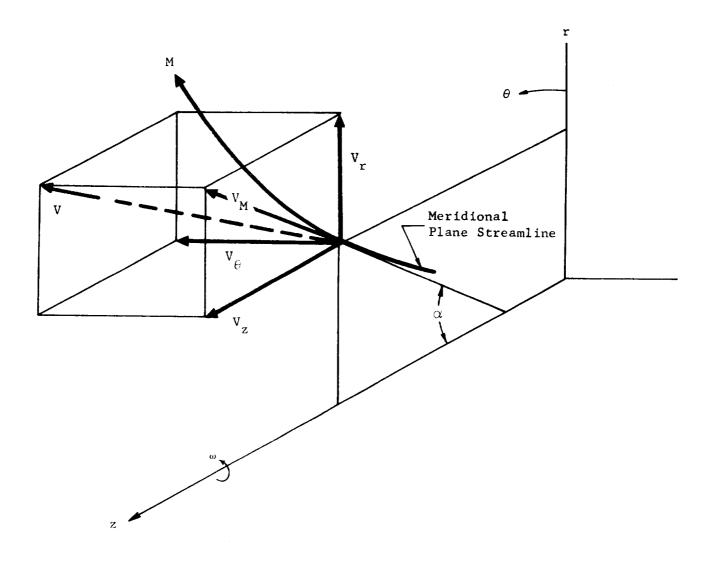


Figure A.1 Fluid Element Coordinates

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$$\frac{dV_{0}}{dc} + \frac{V_{r}V_{0}}{r} + 2\omega V_{r} = -\frac{1}{\omega r}\frac{\partial P}{\partial \theta}$$

$$= V_{r}\frac{\partial V_{\theta}}{\partial r} + \frac{V_{\theta}}{r}\frac{\partial V_{\theta}}{\partial \theta} + V_{z}\frac{\partial V_{\theta}}{\partial z} + \frac{V_{r}V_{\theta}}{r} + 2\omega V_{r} \qquad (A.5)$$

$$\frac{dV_{r}}{dV_{r}} = \frac{1}{2}\frac{\partial V_{r}}{\partial r} + \frac{V_{r}}{2}\frac{\partial V$$

$$\frac{\mathrm{d}V}{\mathrm{d}t} = -\frac{1}{\rho} \frac{\mathrm{d}P}{\mathrm{d}z} = V_{\mathrm{r}} \frac{\mathrm{d}V_{\mathrm{z}}}{\mathrm{d}r} + \frac{V_{\mathrm{d}}}{\mathrm{r}} \frac{\mathrm{d}V_{\mathrm{z}}}{\mathrm{d}\theta} + V_{\mathrm{z}} \frac{\mathrm{d}V_{\mathrm{z}}}{\mathrm{d}z}$$
(A.6)

Assuming the values of the impetter guide the fluid or that channel flew exists approximately, a stream surface may be constructed half way between blades (Figure A.2). The stream surface S can be described by

$$S = S(r, \theta, z)$$
 (A.7)

Solving for m,

$$\forall = \forall (r, z) \tag{A.8}$$

The static pressure in a turbopump is generally a function of r, ε and z:

$$P = P(r, \theta, z).$$
 (A.9)

On S

$$P^* = P(r, \theta (r, z), z)$$
 (A.10)

since 6 on the surface is specified by Equation (A.8). The relation between the partial derivatives of static pressure in the three-dimensional field to that on the stream surface "S" is:

$$\frac{\partial \mathbf{P}^{\star}}{\partial \mathbf{r}} = \frac{\partial \mathbf{P}}{\partial \mathbf{r}} + \frac{\partial \mathbf{P}}{\partial \theta} \frac{\partial \theta}{\partial \mathbf{r}}$$
(A.11)

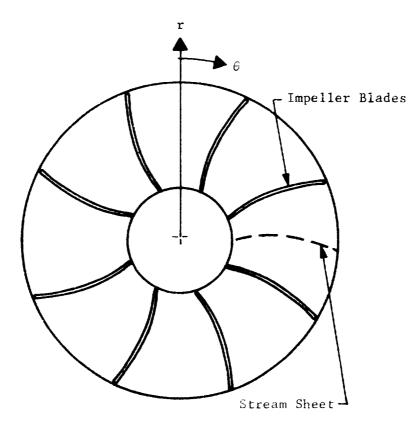
$$\frac{\partial \mathbf{P}^{*}}{\partial z} = \frac{\partial \mathbf{P}}{\partial z} + \frac{\partial \mathbf{P}}{\partial \theta} \frac{\partial \theta}{\partial z}$$
(A.12)

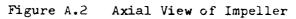
Substituting Equations (A.11) and (A.12) into (A.4) and (A.6),

$$\frac{\mathrm{d}\mathbf{V}_{\mathbf{r}}}{\mathrm{d}\mathbf{t}} - \frac{\left(\mathbf{V}_{\theta} + \mathbf{r}\omega\right)^{2}}{\mathbf{r}} = -\frac{1}{\varphi}\left(\frac{\partial\mathbf{P}^{*}}{\partial\mathbf{r}} - \mathbf{r}\frac{\partial\theta}{\partial\mathbf{r}} + \frac{1}{\mathbf{r}}\frac{\partial\mathbf{P}}{\partial\theta}\right) \tag{A.13}$$

$$\frac{\mathrm{d}V}{\mathrm{d}t} + \frac{V_{\mathbf{r}}V_{\theta}}{\mathbf{r}} + 2\omega V_{\mathbf{r}} = -\frac{1}{\rho r}\frac{\partial P}{\partial \theta}$$
(A.14)

$$\frac{\mathrm{d}V}{\mathrm{d}t} = -\frac{1}{\rho} \left(\frac{\partial \mathbf{P}^{\star}}{\partial z} - \mathbf{r} \frac{\partial \theta}{\partial z} + \frac{1}{\mathbf{r}} \frac{\partial \mathbf{P}}{\partial \theta} \right)$$
(A.15)





The circumferential pressure gradient $\frac{1}{r} \frac{\partial P}{\partial \theta}$ can be eliminated from Equations (A.13) and (A.15) by (A.14)

$$\frac{\mathrm{d}\mathbf{V}_{\mathbf{r}}}{\mathrm{d}\mathbf{t}} - \frac{\left(\mathbf{V}_{\theta} + \omega\mathbf{r}\right)^{2}}{\mathbf{r}} = -\frac{1}{\rho} \left[\frac{\partial \mathbf{P}^{\star}}{\partial \mathbf{r}} + \mathbf{r}^{\rho} \frac{\partial \theta}{\partial \mathbf{r}} \left(\frac{\mathrm{d}\mathbf{V}_{\theta}}{\mathrm{d}\mathbf{t}} + \frac{\mathbf{V}_{\mathbf{r}}\mathbf{V}_{\theta}}{\mathbf{r}} + 2\omega\mathbf{V}_{\mathbf{r}} \right) \right]$$
$$\frac{\mathrm{d}\mathbf{V}_{\mathbf{r}}}{\mathrm{d}\mathbf{t}} - \frac{\mathbf{V}_{\theta}^{\dagger 2}}{\mathbf{r}} = -\frac{1}{\rho} \left[\frac{\partial \mathbf{P}^{\star}}{\partial \mathbf{r}} + \mathbf{r}^{\rho} \frac{\partial \theta}{\partial \mathbf{r}} \left(\frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{t}} \left(\mathbf{r} \mathbf{V}_{\theta}^{\dagger} \right) \right) \right]$$
(A.16)

where $V_{\theta}' = V_{\theta} + \omega r$ and $dr/dt = V_r$.

$$\frac{dV_{z}}{dt} = -\frac{1}{\rho} \left[\frac{\partial P^{*}}{\partial z} + r \frac{\rho}{\partial z} \frac{\partial \theta}{\partial t} + \frac{V V}{r} + \frac{\rho}{\rho} \frac{\partial \theta}{\partial t} \right]$$

$$\frac{dV_{z}}{dt} = -\frac{1}{\rho} \left[\frac{\partial P^{*}}{\partial z} + r \frac{\rho}{\partial z} \frac{\partial \theta}{\partial t} \left(\frac{1}{r} \frac{d}{dt} \left(r V_{\theta}^{+} \right) \right) \right]$$
(A.17)

If the flow is restricted to a streamline on the stream sheet and the streamline is projected on the meridional plane (Figures A.3 and A.4), the tangent to the projected streamline at any point makes an angle α with the impeller axis.

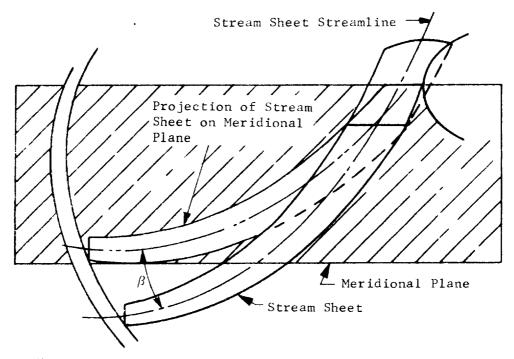


Figure A.3 Projection of Stream Sheet on Meridional Plane

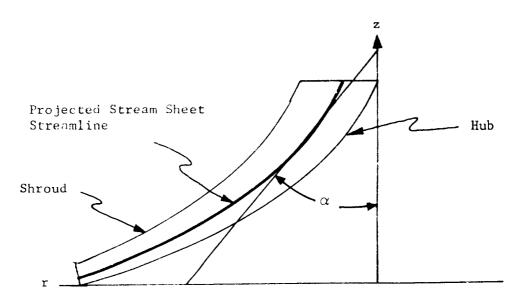


Figure A.4 Meridional Plane of Impeller

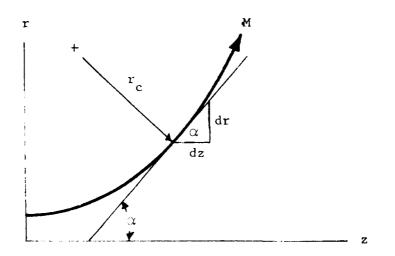


Figure A.5 Meridional Streamline

The velocity components V_r and V_z of the stream sheet streamline lead to a velocity V_M in the meridional plane where:

$$v_m^2 = v_r^2 + v_z^2$$
 (A.18)

$$V_r = V_m \sin \alpha$$
 (A.19)

$$V_z = V_m \cos \alpha$$
 (A.20)

Differentiating,

$$\frac{dV}{dt} = \frac{dV_{M}}{dt} \sin \omega + V_{M} \frac{d\alpha}{dt} \cos \alpha$$
 (A.21)

$$\frac{dV_z}{dt} = \frac{dV_M}{dt} \cos \alpha - V_M \frac{d\alpha}{dt} \sin \alpha$$
 (A.22)

to is related to the radius of curvature of the projected streamline by

$$dM = r_c d\omega$$
 (A.23)

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$$\frac{1}{r_{c}} = \frac{d_{M}}{dM} = \frac{\frac{d\alpha}{dt}}{\frac{dM}{dt}} = \frac{1}{V_{M}} \frac{d\alpha}{dt}$$
(A.24)

$$\therefore \frac{d\alpha}{dt} = \frac{V_{\rm M}}{r_{\rm c}}$$
 (4.25)

Combining Equations (A.16) through (A.25),

$$\frac{dV_{M}}{dt}\cos \omega - \frac{V_{M}^{2}}{r_{c}}\sin \omega = -\frac{1}{\rho} \left\{ \frac{\partial P^{*}}{\partial z} + r^{\rho} \frac{\partial \theta}{\partial z} \left[\frac{1}{r} \frac{d(rV_{\theta})}{dt} \right] \right\}$$
(A.26)

$$\frac{\mathrm{d}\mathbf{V}_{\mathrm{M}}}{\mathrm{d}\mathbf{t}}\sin\varphi + \frac{\mathrm{V}_{\mathrm{M}}^{2}}{\mathrm{r}_{\mathrm{c}}}\cos\varphi = \frac{\mathrm{V}_{\theta}^{\prime 2}}{\mathrm{r}} - \frac{1}{\mathrm{e}}\left\{\frac{\mathrm{d}\mathbf{P}^{*}}{\mathrm{d}\mathbf{r}} + \mathrm{r}\frac{\mathrm{\rho}_{\Theta}\theta}{\mathrm{d}\mathbf{r}}\left[\frac{1}{\mathrm{r}}\frac{\mathrm{d}(\mathbf{r}\mathrm{V}_{\theta}^{\prime})}{\mathrm{d}\mathbf{r}}\right]\right\}$$
(A.27)

$$\frac{\mathrm{d}\mathbf{P}^*}{\mathrm{d}\mathbf{N}} = \frac{\partial \mathbf{P}^*}{\partial \mathbf{r}} \frac{\partial \mathbf{r}}{\partial \mathbf{N}} + \frac{\partial \mathbf{P}^*}{\partial z} \frac{\partial z}{\partial \mathbf{N}}$$
(A.28)

$$\frac{\partial \mathbf{r}}{\partial \mathbf{N}} = \cos \phi$$
 and $\frac{\partial \mathbf{z}}{\partial \mathbf{N}} = -\sin \phi$ (A.29)

$$\therefore \frac{\mathrm{d}P^*}{\mathrm{d}N} = \frac{\mathrm{d}P^*}{\mathrm{d}r} \cos \varphi - \frac{\mathrm{d}P^*}{\mathrm{d}z} \sin \varphi \qquad (A.30)$$

where $\frac{d}{dN}$ is the derivative with respect to the normal to the streamline.

Multiplying Equation (A.26) by $\sin \alpha$ and substituting Equation (A.30)

$$\frac{dV_{M}}{dt}\sin\alpha + \cos\varphi - \frac{\left(V_{M}\sin\alpha\right)^{2}}{r_{c}} = -\frac{1}{2}\left[\frac{\partial P^{*}}{\partial r}\cos\alpha - \frac{\partial P^{*}}{\partial N} + r^{\rho}\frac{\partial \theta}{\partial z}\left(\frac{1}{r}\frac{d(rV_{\theta}^{\dagger})}{dt}\right)\sin\varphi\right] \quad (A.31)$$

Multiplying Equation (A.27) by $\cos \alpha$

$$\frac{dV_{M}}{dt} \sin \alpha + \cos \alpha + \frac{\left(\frac{V_{M} \cos \alpha}{r_{c}}\right)^{2}}{r_{c}} - \frac{V_{0}^{\prime 2}}{r} \cos \alpha = -\frac{1}{\rho} \left[\frac{\partial P^{*}}{\partial r} \cos \alpha + r^{\rho} \frac{\partial \theta}{\partial r} \left(\frac{1}{r} - \frac{\partial (rV_{0}^{\prime})}{\partial t} \right) \cos \alpha \right]$$
(A.32)

Subtracting Equation (A.31) from (A.32)

$$\frac{v_{M}^{2}}{r_{c}} - \frac{v_{\theta}^{2}}{r} \cos \alpha = -\frac{1}{\rho} \frac{\partial P^{*}}{\partial N} + \frac{1}{\rho r} \left(r^{\rho} \frac{\partial \theta}{\partial z} \sin \alpha - r^{\rho} \frac{\partial \theta}{\partial r} \cos \alpha \right) \left(\frac{d(rV_{\theta})}{dt} \right) \quad (A.33)$$

From Figure A.3 the velocity along the stream sheet streamline V is related to the projected velocity V_M and the velocity V[']_{\theta} by

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$$V_{\rm M} = V \cos \beta \qquad (A.34)$$

$$V_{\theta} = V \sin \beta \text{ or } V_{\theta}' = V \sin \beta + \omega r$$
 (A.35)

Equation (A.33) becomes

$$\frac{\left(V\cos\beta\right)^{2}}{r_{c}} = \frac{\left(V\sin\beta + \omega r\right)^{2}}{r}\cos\alpha = -\frac{1}{\rho}\frac{\partial P}{\partial N} + \left\{\frac{V\cos\beta}{\rho}\right\} \cdot \left[\left(r^{\rho}\frac{\partial\theta}{\partial z}\sin\alpha - r^{\rho}\frac{\partial\theta}{\partial r}\cos\phi\right)\left(\frac{dV_{\theta}}{dM} + \frac{V\sin\beta + \sin\beta}{r} + 2\cos\alpha\phi\right)\right] \quad (A.36)$$
Multiplying Equation (A.4) by $V_{r} = \frac{dr}{dt}$, Equation (A.5) by $V_{\theta} = r\frac{d\theta}{dt}$, and Equation (A.6) by $V_{z} = \frac{dz}{dt}$ yields:

$$V_{r} \frac{dV_{r}}{dt} - \frac{V_{r} \left(V_{\theta} + \omega r\right)^{2}}{r} = -\frac{1}{\rho} \frac{\partial P}{\partial t}$$
(A.37)

$$V_{\theta} \frac{dV_{\theta}}{dt} + \frac{V_{r}V_{\theta}^{2}}{r} + 2\omega V_{r}V_{\theta} = -\frac{1}{\rho}\frac{\partial P}{\partial t}$$
(A.38)

$$V_{z} \frac{\partial V_{z}}{\partial t} = -\frac{1}{p} \frac{\partial P}{\partial t}$$
(A.39)

Adding the above three equations,

$$V_{r} \frac{dV_{r}}{dt} - \frac{V_{r} \omega^{2} r^{2}}{r} + V_{\theta} \frac{dV_{\theta}}{dt} + V_{z} \frac{dV_{z}}{dt} = -\frac{3}{\rho} \frac{\partial P}{\partial t}$$
(A.40)

$$\mathbf{v}^2 = \mathbf{v}_{\mathbf{r}}^2 + \mathbf{v}_{\theta}^2 + \mathbf{v}_{\mathbf{z}}^2 \tag{A.41}$$

and

$$\frac{dV^2}{dt} = 2V_r \frac{dV_r}{dt} + 2V_\theta \frac{dV_\theta}{dt} + 2V_z \frac{dV_z}{dt}$$
(A.42)

$$\therefore \frac{1}{2} \frac{\mathrm{d}V^2}{\mathrm{d}t} - V_r \omega^2 r = -\frac{3}{\rho} \frac{\mathrm{d}P}{\mathrm{d}t}$$
 (A.43)

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Integrating Equations (A.42) and (A.43) along a streamline between a station in the pump inlet, i, and a point in the pump

• • •

$$\frac{1}{2}\left(\mathbf{v}^2 - \mathbf{v}_i^2\right) - \frac{\omega^2}{2}\left(\mathbf{r}^2 - \mathbf{r}_i^2\right) = -3\int_i \frac{d\mathbf{P}}{\rho} \qquad (A.44)$$

But

$$v^{+2} = v_{\theta}^{+2} + v_{r}^{2} + v_{z}^{2}$$
 (A.45)

$$V'_{t} = V_{t} + \omega r$$
 (A.46)

$$\therefore \mathbf{V'}^2 = \mathbf{V}_{\theta}^2 + \mathbf{V}_{\mathbf{r}}^2 + \mathbf{V}_{\mathbf{r}}^2 + 2\omega \mathbf{r} \mathbf{V}_{\theta} + \omega^2 \mathbf{r}^2$$
 (A.47)

$$V^{2} = V^{2} + 2\omega r V_{\theta} + \omega^{2} r^{2}$$
 (A.48)

$$V^{\prime 2} = V^{2} + 2\omega r V_{\theta}^{\prime} - \omega^{2} r^{2}$$
 (A.49)

and along a streamline Bernoulli's equation is

$$P_{t} = P + \frac{1}{2} \rho V^{2}$$
 (A.50)

If $\omega = \text{const:}$ Equation (A.44) can be written

$$\frac{\mathbf{V}^2}{2} - \frac{\mathbf{a}^2 \mathbf{r}^2}{2} + \frac{2\mathbf{b}\mathbf{r}\mathbf{V}_{\theta}}{2} - \frac{\mathbf{3P}_{\mathbf{t}}}{\rho} = -\frac{\mathbf{3P}}{\rho}$$
(A.51)

Taking the derivative of Equation (A.51) with respect to ${\tt N}$

$$V \frac{dV}{dN} - \omega^2 r \frac{dr}{dN} + \omega \frac{d}{dN} \left(r V_{\theta_i}^{\dagger} \right) - \frac{3}{\rho} \frac{\partial P_{t_i}}{\partial N} = -\frac{3}{\rho} \frac{\partial P}{\partial N}$$
(A.52)

Substituting Equation (A.52) into Equation (A.36)

$$V \frac{dV}{dN} = -\frac{1}{r} \frac{dv}{dN} - -\frac{1}{2} \frac{\partial}{\partial N} \left(r V_{\theta_{i}}^{\dagger} \right) + \frac{3}{\rho} \frac{\partial^{P} t_{i}}{\partial N} + \frac{3 \left(V \cos \beta \right)^{2}}{r_{c}} - 3 \frac{\left(V \sin \beta + \omega r \right)^{2}}{r} \cos \alpha$$

$$-3\frac{V\cos\beta}{\omega}\left(r\frac{\rho\partial\theta}{\partial z}\sin\phi - r\frac{\rho\partial\theta}{\partial r}\cos\phi\right)\left(\frac{dV_{\theta}}{dM} + \frac{V\sin\beta\sin\phi}{r} + 2\omega\sin\alpha\right)$$
(A.53)

Equation (A.53) combined with hub and shroud boundary conditions, inlet conditions, and the continuity equation in the form:

$$\frac{1}{N_{b}} = \int_{N_{1}}^{N_{2}} \int_{\theta_{s}}^{\theta_{P}} V \cdot r \cdot d\theta \cdot dN$$
(A.54)

where: \dot{W} = total pump flow rate

 N_1, N_2 = streamline numbers Θ_P = Θ on pressure surface of blade ψ_s = Θ on suction surface of adjacent blade N_L = number of blades

provides a solution to the incompressible flow problem in the meridional plane. The solution involves the numerical integration of Equations (A.53) and (A.54) from streamline to streamline in the meridional plane.

APPENDIX B

Growth of a Thermal Cavitation Bubble

A thermal cavitation bubble appears in a turbopump when the local static pressure drops below the vapor pressure of the liquid. The bubble growth begins either on a small gas nucleus lodged in the walls of the fluid container, on dust and colloidal matter suspended in the media, or on a small bubble of contaminant gas free in the fluid. Bubble growth is due to essentially three mechanisms. First, additional contaminant gas can diffuse into the bubble; second the bubble grows because of a decrease in ambient pressure; and third, growth results from a phase change occurring at the bubble wall.

The initial nucleus is composed solely of contaminant gases or a mixture of contaminant gas and liquid vapor. The effect of the initial contaminant gas and the additional contaminant gas that diffuses into the nucleus during its growth is important only during the initial stages of growth. Due to the large surface tension force, the initial growth of the bubble is slow. However, once the bubble radius has increased by an order of magnitude, the presence of the contaminant gases is relatively unimportant.

The flow of fluid surrounding a single bubble can be treated as incompressible and irrotational and, hence, can be described by a potential function, ϕ

$$-\frac{\partial F}{\partial \mathbf{r}} = \dot{\mathbf{r}}$$
(B.1)

where r is the radius from the center of the bubble to any point in the fluid and \dot{r} is the velocity of the fluid at that point. The boundary conditions $\dot{r} = \dot{R}$ at r = R, where R is the bubble radius, and $\dot{r} = 0$ at $r = \infty$ establish the potential function to be

$$\psi = \frac{\mathbf{R}^2 \cdot \dot{\mathbf{R}}}{r} \tag{B.2}$$

Since the fluid is considered incompressible with gravitational effects negligible, the work done by a growing pubble appears only as a change in kinetic energy of the thild surrounding the bubble. The increment of work done by the bubble in expanding from R to R + Δ R is

$$\Delta W = \Delta P \cdot 4\pi \cdot R^2 \cdot \Delta R \qquad (B.3)$$

where

$$\angle P = P_R - P_{\infty}$$

In terms of the rate of change of work with respect to R

$$\frac{\mathrm{dW}}{\mathrm{dR}} = \left(\mathbf{P}_{\mathrm{R}} - \mathbf{P}_{\infty}\right) + 4\pi \mathrm{R}^{2} \tag{B.4}$$

The kinetic energy of the fluid between R and r is

$$KE = \frac{1}{2} mv^{2} = \frac{1}{2} \int_{R}^{r} 4\pi \rho_{L} r^{2} \dot{r}^{2} dr \qquad (B.5)$$

where $\rho_{\rm L}$ is the mass density of the liquid.

But from Equation (B.2)

$$\dot{\mathbf{r}} = -\frac{\partial \varphi}{\partial \mathbf{r}} = \frac{\mathbf{R}^2 \dot{\mathbf{R}}}{\mathbf{r}^2}$$
(B.6)

$$\therefore KE = 2\pi \omega_L R^4 \dot{R}^2 \int_R^r \frac{dr}{r^2}$$
(B.7)

or

$$KE = 2\pi\rho_{L}R^{4}\dot{R}^{2}\left(\frac{1}{R} - \frac{1}{r}\right)$$
(B.8)

letting $r \rightarrow \infty$

$$KE = 2\pi \rho_L R^3 \dot{R}^2$$
(3.9)

The rate of change of kinetic energy with respect to R is:

$$\frac{d}{dR} (KE) = 2\pi \rho_L \frac{d}{dR} (R^3 R^2)$$
(B.10)

Setting Equation (B.4) equal to Equation (B.10)

$$\left(\mathbf{P}_{\mathbf{R}} - \mathbf{P}_{\infty}\right) 4\pi \mathbf{R}^{2} = 2\pi \mu_{\mathbf{L}} \frac{\mathrm{d}}{\mathrm{d}\mathbf{R}} \left(\mathbf{R}^{3} \dot{\mathbf{R}}^{2}\right)$$
(B.11)

But

$$\frac{d}{dR} = \frac{dt}{dR} \cdot \frac{d}{dt} = \frac{1}{\dot{R}} \frac{d}{dt}$$

$$\therefore \frac{P_{R} - P_{co}}{L} = \frac{1}{2R^{2}\dot{R}} \frac{d}{dt} (R^{3}\dot{R}^{2})$$
(B.12)

Equation (B.12) therefore, is the equation of motion governing bubble growth. The same results can be obtained starting with the Bernoulli equation

$$\frac{\mathbf{P} - \mathbf{P}_{\infty}}{\mathbf{P}_{\mathrm{L}}} = \frac{1}{2} \dot{\mathbf{r}}^{2} + \frac{\partial \varphi}{\partial \mathbf{t}}$$
(B.13)

The temperature at the bubble wall will be controlled by the evaporation process. If it is assumed that the pressure in the bubble is uniform and at the vapor pressure, P_v , of the liquid corresponding to the temperature at the bubble wall, then P_R is related to P_v by:

$$P_{R} = P_{V} - 2 \frac{\sigma}{R}$$
(B.14)

where σ is the surface tension of the fluid

$$\therefore \frac{1}{2R^{2}\dot{R}} \frac{d}{dt} \left(R^{3}\dot{R}^{2} \right) = \frac{1}{\mu_{L}} \left(P_{v} - P_{\infty} - \frac{2\sigma}{R} \right)$$
(B.15)

If the boiling curve of a fluid is linear or nearly so over the region in which bubble growth takes place, the saturation pressure P can be related to the saturation temperature T by s

$$P_{s} = A + T_{s} + B$$
 (B.16)

 $F_{\rm c} \sim P_{\rm c}$ can be expressed as

$$P_{v} - P_{\infty} = A(T_{R} - T_{o}) + A(T_{o} - T_{P_{\infty}})$$
(B.17)

where $\frac{1}{0}$ is the fluid temperature a great distance from the babble and T is the saturation temperature corresponding to $\frac{P_{x}}{P_{x}}$ the time-dependent ambient pressure.

Equation (B.15) then becomes

$$\frac{1}{2R^{2}\dot{R}}\frac{d}{dt}\left(R^{3}+\dot{R}^{2}\right) = \frac{A}{\rho_{L}}\left[\left(T_{R}-T_{O}\right)+\left(T_{O}-T_{P_{\infty}}\right)\right] - \frac{2\sigma}{\rho_{L}R}$$
(B.18)

If it is assumed that the temperature a great distance from the bubble, $T_{_{O}}$, remains constant during bubble growth the quantity $T_{_{R}} - T_{_{O}}$ can be obtained from the solution to the problem of non-steady heat diffusion with boundary motion of Plesset and Zwick (Reference 16). The equations will not be derived here. However, the final results can be expressed by the following equation:

$$T_{R} - T_{O} = -\left(\frac{D}{\pi}\right)^{\frac{L}{2}} \int_{0}^{t} \frac{R^{2}(x) + (\partial T/\partial r)_{r=R(x)}}{\left[\int_{x}^{t} R^{4}(y) dy\right]^{\frac{L}{2}}} dx \qquad (B.19)$$

where D is the thermal diffusivity of the fluid and the variable y is associated with a translation of the time axis. The derivative $(\partial T/\partial r)$ is the temperature gradient at the bubble wall. Equation (B.18) is then

$$\frac{1}{2R^{2}\dot{R}}\frac{d}{dt}\left(R^{3}\dot{R}^{2}\right) = \frac{A}{\rho_{L}}\left(T_{o} - T_{p_{o}}\right) - \frac{A}{\rho_{L}}\left(\frac{b}{dt}\right)^{\frac{1}{2}}\int_{0}^{t}\frac{R^{2}(x) \cdot (\partial T/\partial r)_{r=R(x)}}{\left[\int_{x}^{t}R^{4}(y) \cdot dy\right]^{\frac{1}{2}}} dx - \frac{2\sigma}{\rho_{L}R} \quad (B.20)$$

The temperature gradient at the bubble wall can be obtained from a mass and heat balance as follows. The heat transfer at the bubble wall per unit time is:

$$\dot{Q} = 4\pi R^2 k \left(\frac{\Theta T}{\Theta r}\right)_{r=R}$$
 (B.21)

where k is the thermal conductivity.

This heat goes into vaporizing liquid at a rate

$$\frac{\mathrm{dm}_{\mathrm{L}}}{\mathrm{dt}} = \frac{\dot{Q}}{\mathrm{L}} \tag{B.22}$$

where L is the latent heat of vaporization.

The rate at which liquid is evaporated is equal to the rate of mass addition to the bubble:

$$\frac{dm_{L}}{dt} = \frac{dm_{v}}{dt}$$
(B.23)

where $m_{y} = mass of vapor$

but

$$m_v = (4/3)\pi R^3 \rho_v$$
 (B.24)

and

$$\frac{\mathrm{dm}}{\mathrm{dt}} = (4/3)\pi \frac{\mathrm{d}}{\mathrm{dt}} \left(R^3 \rho_{\rm v} \right) = (4/3)\pi \left(3R^2 \cdot \dot{R} \cdot \rho_{\rm v} + R^3 \dot{\rho}_{\rm v} \right) \qquad (B.25)$$

$$\cdot \cdot \frac{4\pi R^2 k}{L} \left(\frac{\Theta T}{\Theta r} \right)_{r=R} = (4/3)\pi \left(3R^2 \cdot \dot{R} \cdot \rho_v + R^3 \dot{\rho}_v \right)$$
 (B.26)

or

$$\left(\frac{\Delta T}{\Delta r}\right)_{r=R} = \frac{L}{k} \rho_{v} + \dot{R} + \frac{LR}{3k} \dot{\rho}_{v}$$
(B.27)

The growth of a vapor bubble under conditions of variable ambient pressure and variable vapor density is described by a solution to Equations (B.20) and (B.27).

APPENDIX C

Simplified Test Food System Transfer Functions

A simplified analytical model of the S-II inboard LOX suction line with the by-pass pulser line is shown in Figure C.1. Solution of these equations give the following transfer functions:

$$\frac{\partial Ps}{\partial Wp} = \frac{-I_1}{\left(1 + 2\zeta \frac{S}{\omega} + \frac{S^2}{\omega^2}\right)}$$
(C.1)

$$\frac{\partial P_{s}}{\partial P_{p}} = \frac{(I_{1p}/I_{p})}{\left(1 + 2\zeta_{1}\frac{S}{\omega_{1}} + \frac{S^{2}}{\omega_{1}^{2}}\right)}$$
(C.2)

$$\frac{\partial P_1}{\partial P_P} = \frac{\partial P_S}{\partial P_P} \left(1 + \frac{S^2}{\omega_0^2} \right)$$
(C.3)

where I =
$$\ell / \text{Agc}$$

 $\omega^2 = 1/[C (I_1 + I_2)]$
 $\omega_1^2 = 1/[C (I_{1p} + I_2)]$
 $\omega_0^2 = 1/CI_2$
 $I_{1p} = I_1 I_p / (I_1 + I_p)$
 $\zeta = 1/2 \omega (I_1 + I_2) \frac{\partial \dot{W} d}{\partial Ps}$

.

$$\tilde{\zeta}_1 = 1/2 \omega_1 (I_{1p} + I_2) \frac{\partial \dot{W} d}{\partial Ps}$$

 $\frac{\partial \dot{W} d}{\partial Ps} = \text{engine flow transfer function}$

The true system transfer function of suction pressure with respect to pump acceleration is:

$$\frac{\partial Ps}{\partial gp} = \frac{-(1_1 + 1_2) \rho Agc}{\left(1 + 2\zeta \frac{S}{\omega} + \frac{S^2}{\omega^2}\right)}$$
(C.4)

and, therefore, the only test transfer function that has the right dynamics (correct natural frequency) is $\partial Ps/\partial \dot{W}p$. However, since pulser flow acceleration is not easy to measure accurately, frequency can also be determined from $\partial Ps/\partial Pp$ if the proper correction is applied. For the S-II inboard LOX line, the natural resonance of the $\partial Ps/\partial Pp$ transfer function will be approximately 5% too high. This is independent of where the line pressure is measured except as the pressure transducer moves up the line an anti-resonance will approach the resonance from above.

For other test configurations, the $\partial Ps/\partial Pp$ transfer function will give approximately the correct natural frequency provided that the pulser line inertance (from the suction line to the pressure transducer) is large relative to the inertance in the suction line between the tank and pulser line.

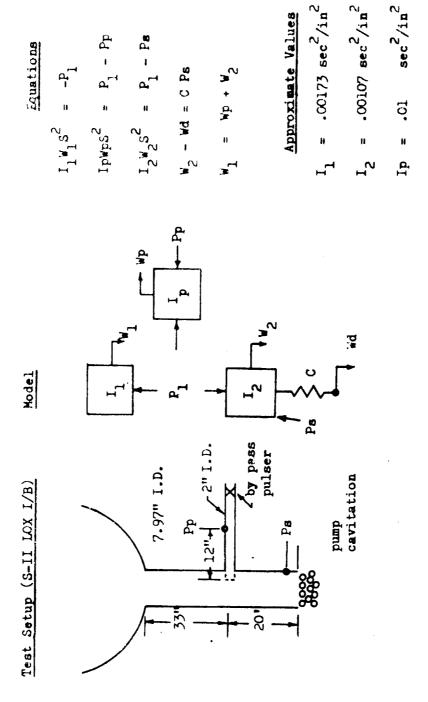


FIGURE C.1 Simplified Suction Line Model for Pulse Test

APPENDIX D

Turbopump Program Users Instructions

The turbopump cavitation flow program has been written in the Fortran IV program language for the CDC 6000 series computer. The program is made up of a main controlling program and seven subroutines. The main program controls the sequence of solution steps and the adjustment of boundary conditions to meet proper inlet and exit flow conditions.

The first subroutine employed (PEER) reads in the input data, sets up the grid system, and establishes initial estimates of the streamfunction at each grid point. Subroutine RELAX is used next to solve the flow and energy equations throughout the field. This solution is accomplished by applying relaxation techniques to a finite difference form of the equations. The first series of relaxation solutions is done with the density throughout the field set equal to the liquid density. This solution is referred to as the incompressible or uncoupled solution. The relaxation solution is then continued with the completely coupled two phase flow equations. Following this solution, boundary conditions are checked, adjusted, and the relaxation solution repeated uptil the proper inlet and exit conditions are satisfied. The last operation of the program prepares and prints out the output data.

Subroutine TABL is an interpolation subroutine used by the main program and many of the subrountines. Subroutine PREWRT prepares the output data for printing while subroutine SETUP prepares the output data for computer plotting. Subroutines WRTOUT and PLOTT respectively do the criting and plotting of the output.

A flow diagram for the program is given in Figure D.1. With the exception of the plotting capabilities, this program should be compatible with any computer which has a FORTRAN IV compiler. The plotting routines are documented in Reference 55. The routine ALTFILE is required on the CDC 6000 computer so that the TAPE9 buffer area may also be used for TAPE10 through TAPE99.

The problem solution is initiated by plotting the inducer or impeller blade sections (Figures 5.3 and 5.4) and the relationship between density and pressure for equilibrium phase changes (Figure 3.7). All input variables are defined in the program listing of subroutine PEER (Appendix E). Input dimensions and internal program variables are shown in Figures D.2 through D.4.

Parts of a sample output from the turbopump cavitation flow program are presented at the end of this Appendix. The first data printed is the input data. Next is a tabulation of the iterations required for solution along with the value of the maximum residual (RESIM) throughout the field for each iteration. Following the last iteration, which corresponds to the uncoupled solution, the pressure and density is printed out at each grid point in the system. The next item to be printed (volume) is the weight of propellant in the streamsheet analyzed. Finally, for the uncoupled solution the values of the streamfunction, ψ , theta, θ , potential function, ϕ , circumfrential velocity, V, and meridional velocity, U, are printed for increments along the E axis. At this point the solution is continued on a coupled basis and the pressure data printed out for each iteration. After the final iteration of the coupled solution the pressure field, the weight of fluid in the streamsheet, and the streamfunction - velocity fields are printed out.

| N = 51 | L = 51 | K = 51 | NN = 1 | LL = 1 | MNM = 51 |
|--------------|------------------|--------------------|------------------|----------------|------------------|
| 8 = | 2 • 09 4 4 | 0 = 60. | 0000 RT | = 6 | .7500 |
| RS = | 0. | THETS # | 0. | ES1 = | 0. |
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| RS ≠ | .0650 | THETS = | .1874 | ES1 = | .0650 |
| RS = | .1050 | THETS 🛎 | .2812 | ES1 = | .1050 |
| RS = | •1480 | THETS = | .3749 | ES1 = | •1480 •1970 |
| RS = | .1970 | THETS = | •4686 | ES1 = ES1 = | • 2500 |
| RS = | .2500 | THETS = | •5624 •6561 | ESI = | .3050 |
| RS = | .3050 | THETS # | .7498 | ES1 = | .3630 |
| RS = | •3630 | THETS ₽ THETS ₽ | .8436 | ES1 = | .4210 |
| RS = | .4210 | THETS = | .9373 | ES1 = | .4810 |
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| RS = | .8880 | THETS = | 1.5934 | ES1 = | .8880 |
| RS ≠ | .9450 | THETS = | 1.6871 | ES1 = | . 945 0 |
| RS = | 1.0020 | THETS = | 1.7808 | ES1 = | 1.0020 |
| RS = | 1.0590 | THETS # | 1.8746 | ES1 = | 1.0590 |
| RS = | 1.1160 | THETS $=$ | 1.9683 | ES1 = | 1.1160 |
| RS = | 1.1720 | THETS ≠ | 2.0620 | ES1 = | 1.1720 |
| RS = | 1.2280 | THETS = | 2.1557 | ES1 = | 1.2280 |
| R S = | 1.2840 | THETS = | 2.2494 | ES1 = | 1.2840 |
| RS = | 1.3390 | THETS * | 2.3432 | ES1 = | 1.3390 1.3950 |
| RS = | 1.3950 | THETS ≠ | 2.4369 | ES1 = ES1 = | 1.4500 |
| RS = | 1.4500 | THETS = | 2•5306 2•6244 | ESI = | 1.5050 |
| RS = | 1.5050 | THETS ≠ THETS = | 2.7181 | ES1 = | 1.5600 |
| RS ≖ | 1.5600 | THETS = | 2.8118 | ES1 = | 1.6150 |
| RS = | 1.6150 1.6690 | THETS = | 2.9056 | ES1 = | 1.6690 |
| RS = | 1.7230 | THETS = | 2.9993 | ES1 = | 1.7230 |
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| RS ≠ | 1.9380 | THETS = | 3.3742 | ESi = | 1.9380 |
| RS = | 1.9910 | THETS = | 3.4679 | ES1 = | 1.9910 |
| RS = | 2.0430 | THETS ≠ | 3.5616 | E\$1 = | 2.0430 |
| RS = | 2.0960 | THETS ₽ | 3.6554 | ES1 = | 2.0960 |
| RS = | 2.1490 | THETS = | 3.7491 | ES1 = | 2.1490 |
| RS = | 2 .2 060 | THETS $=$ | 3.8428 | ES1 = | 2.2060 |
| RS = | 2.2640 | THETS = | 3.9366 | ES1 = | 2.2640 |
| RS = | 2.3240 | THETS = | 4.0303 | ES1 = | 2.3240 2.3890 |
| RS = | 2.3890 | THETS # | 4.1240 | ES1 = ES1 = | 2.4560 |
| RS = | 2.4560 | THETS = | 4.2177 | ES1 = | 2.5290 |
| RS = | 2.5290 | THETS = | 4.3115 4.4052 | ES1 = | 2.6090 |
| RS = | 2.6090 | THETS = THETS = | 4.4989 | ES1 = | 2.6920 |
| RS = | 2.6920 2.7800 | THETS = | 4.5926 | ES1 = | 2.7800 |
| RS = RS = | 2.8880 | THETS = | 4.6864 | ES1 = | 2.8880 |
| K2 - | 200000 | | | | |

| RP = | 0. | THETP = | 2.0944 | EP2 = | 0. |
|--------------|------------------|--------------------|------------------|----------------|------------------|
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| RP = | .2430 | THETP = | 2.2818 | EP2 = | .2430 |
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| RP = | •4840 | THETP = | 2.5630 | EP2 = | • 4840 |
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| RP = | .6180 | THETP = | 2.7505 | EP2 = | .6180 |
| RP = | .6810 | THETP = | 2.8442 | EP2 = | .6810 |
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| RP = | .9890 | THETP = | 3.3128 | EP2 = | .9890 |
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| RP = | 2.8010 | THETP = | 6.4058 | EP2 = | |
| <u>RP</u> = | 2.8270 | THETP ≠ | 6.4996 | EP2 = | 2.8270 |
| RP = | 2.8510 | THETP = | 6.5933 | EP2 = | 2.8510 |
| RP = | 2.8710 2.8880 | THETP = THETP = | 6.6870 6.7808 | EP2 = EP2 = | 2.8710 2.8880 |
| 8P = | | | 5 . (5 0 5 | FF/ | L . 000U |

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| RC = | 2.8260 | THETC = | 4.5926 | EC1 = | 2.8260 |
| RC = | 2.8880 | THETC # | 4.6864 | EC1 = | 2.8860 |
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| RD = | 2.4920 | . 8D | Ħ | •1818 | SIAD = | •1057 | ED | = | -1.0830 |
|------|--------|------------|----------|-------|--------|-------|----|----|---------|
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| RD = | 2.4640 | 8D | = | .1874 | SIAD = | .1057 | ED | = | 8233 |
| RD = | 2.4500 | BD | * | .1903 | SIAD = | .1057 | ED | | 6933 |
| RD = | 2.4370 | 80 | # | .1931 | SIAD = | .1057 | ED | u. | 5633 |
| RD = | 2.4230 | 8 D | # | •1960 | SIAD = | •1057 | ED | = | 4333 |
| RD = | 2.4090 | 8D | # | .1988 | SIAD = | •1057 | ED | = | 3033 |
| RD = | 2.3950 | 60 | ÷ | .2017 | SIAD = | •1057 | ED | = | 1733 |
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| RD = | 2.3670 | 8D | Ξ | •2074 | SIAD = | •1057 | ED | = | .0867 |
| RD = | 2.3540 | 8D | # | .2102 | SIAD = | .1057 | ED | = | .2167 |
| RJ = | 2.3400 | 80 | te: | .2130 | SIAD = | .1057 | ΕO | Ξ | • 3467 |
| RD = | 2.3260 | BD | = | .2159 | SIAD = | .1057 | ED | 3 | .4767 |
| RD = | 2.3120 | 8D | # | .2187 | SIAD = | .1057 | ED | 4 | .6067 |
| RD = | 2.2980 | 80 | * | .2216 | SIAJ = | .1057 | ED | z | .7367 |
| RD = | 2.2850 | BD | # | .2244 | SIAD = | .1057 | ED | = | .8667 |
| RD = | 2.2710 | BD | = | .2273 | SIAD = | .1057 | ED | = | .9967 |
| RD = | 2.2570 | 80 | = | •2301 | SIAD = | .1057 | ED | = | 1.1270 |
| RD = | 2.2430 | BD | # | .2329 | SIAD = | .1057 | ED | = | 1.2570 |
| RD = | 2.2290 | 80 | = | .2358 | SIAD = | .1057 | ED | = | 1.3870 |
| RD = | 2.2150 | BD | ÷ | .2386 | SIAD = | .1057 | ED | = | 1.5170 |
| RD = | 2.2020 | 80 | × | .2415 | SIAD = | .1057 | ED | Ŧ | 1.6470 |
| RD = | 2.1880 | BD | = | .2443 | SIAD = | .1057 | ED | = | 1.7770 |
| RD = | 2.1740 | 8D | æ | .2472 | SIAD = | .1057 | ED | = | 1.9070 |
| RD = | 2.1600 | PD | Ξ | .2500 | SIAD = | .1057 | ED | ÷ | 2.0370 |
| R0 = | 2.1460 | 8D | Ħ | .2528 | SIAD = | .1057 | ED | = | 2.1670 |
| RD = | 2.1330 | 8 D | Ħ | .2557 | SIAD = | •1057 | ED | = | 2.2970 |
| RD = | 2.1190 | BD | 늄 | .2585 | SIAD = | .1057 | ED | = | 2.4270 |
| RD = | 2.1050 | BD | I | •2614 | SIAJ = | •1057 | ED | = | 2.5570 |
| RD = | 2.0910 | 8D | Ħ | •2642 | SIAD = | •1057 | ED | Ξ | 2.6870 |
| R0 = | 2.0770 | 80 | = | .2671 | SIAD = | .1057 | ED | : | 2.8170 |
| RD = | 2.0630 | 8D | = | .2699 | SIAD = | •1057 | ED | 3 | 2.9470 |
| RD = | 2.0500 | 80 | 3 | .2727 | SIAD = | .1057 | ED | = | 3.0770 |
| RD = | 2.0360 | 8D | Ħ | .2756 | SIAD = | .1057 | ED | 3 | 3.2070 |
| RD = | 2.0220 | BD | Ť. | .2784 | SIAD = | .1057 | ED | 2 | 3.3370 |
| RD = | 2.0080 | 80 | = | .2813 | SIA) = | .1057 | ED | = | 3.4670 |
| RD = | 1.9940 | 80 | # | .2841 | SIAD = | .1057 | ED | = | 3.5970 |
| RD ≠ | 1.9810 | 80 | = | .2870 | SIAD = | .1057 | ED | # | 3.7270 |
| RD = | 1.9670 | 8D | # | .2898 | SIAD = | 1057 | ED | Ξ | 3.8570 |
| RD = | 1.9530 | 80 | × | .2926 | SIAD = | .1057 | ED | 11 | 3.9870 |
| RD = | 1.9390 | BD | Ħ | •2955 | SIAD = | .1057 | ED | = | 4.1170 |
| RD = | 1.9250 | 8D | | •2983 | SIAD = | .1057 | ED | = | 4.2470 |
| RD = | 1.9120 | 80 | Ħ | .3012 | SIAD = | •1057 | ED | = | 4.3770 |
| RD = | 1.8980 | 80 | = | .3040 | SIAD = | .1057 | ED | 3 | 4.5070 |
| RD = | 1.8840 | BD | ≇ | .3069 | SIAD = | .1057 | ED | = | 4.6370 |
| RD = | 1.8700 | 8D | Ŧ | .3097 | SIAD = | .1057 | ED | 3 | 4.7670 |
| RD = | 1.8560 | BD | * | .3126 | SIAD = | .1057 | ED | = | 4.8970 |
| R) = | 1.8420 | 80 | Ŧ | .3154 | SIAD = | .1057 | ED | = | 5.0270 |
| RD = | 1.8290 | BD | Ħ | .3182 | SIAD = | .1057 | ED | = | 5.1570 |
| RD = | 1.8150 | 8D | = | .3211 | SIAD = | .1057 | ED | = | 5.2870 |
| RD = | 1.8010 | 8D | = | .3239 | SIAD = | .1057 | ED | = | 5.4170 |
| | | | | | | | | | |

| KKL = 27 | INPUF = | 0 8N | = | 3.0000 W | W = 842.0000 |
|----------|-----------|--------------|------|-----------|--------------|
| VTHIN = | 1000.0000 | VNDIN | = 27 | 74.8000 P | S = 15.0000 |
| RHOT = | .0000 | HT = | 0. | PT = | .0150 |
| RHOT = | .0000 | HT = | 0. | PT = | • 0 3 0 0 |
| RHOT = | .0000 | HT = | 0. | PT = | .0740 |
| RHOT = | .0000 | HT = | 0. | PT = | 1 32 0 |
| RHOT = | .0000 | HT = | 0. | PT = | .2650 |
| RHOT = | .0001 | HT = | 0. | PT = | •4700 |
| RHOT = | .0001 | HT = | 0. | PT = | .8090 |
| RHOT = | .0002 | HT = | 0. | PT = | 1.3380 |
| RHOT = | .0003 | HT = | 0. | PT = | 2.1020 |
| RHOT = | .0005 | HT = | 0. | PT = | 3.1900 |
| RHOT = | .0008 | HT = | 0. | PT = | 4.7040 |
| RHOT = | .0015 | HT = | 0. | PT = | 6.7330 |
| RHOT = | .0032 | HT = | 0. | PT = | 9.3930 |
| RHOT = | •0105 | HT = | 0. | PT = | 12.8120 |
| RHOT = | • 04 0 9 | H T = | 0. | PT = | 17.1260 |
| RHOT = | .0409 | HT = | 0. | PT = | 25.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 30.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 36.0000 |
| RHOT = | .0409 | HT = | 0. | PT = | 57.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 100.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 150.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 175.0000 |
| RHOT = | • 04 0 9 | HT = | 0. | PT = | 200.0000 |
| RHOT = | • 04 09 | HT = | 0. | PT = | 300.0000 |
| RHOT = | .0409 | HT = | 0. | PT = | 500.0000 |
| RHOT = | . 04 0 9 | HT = | 0. | PT = | 700.0000 |
| RHOT = | • 04 09 | HT = | 0. | PT = | 1000.0000 |

.

| BEGIN NAI | | TNORFHEN | T THETA AND | THEN E |
|-----------|-------------|----------|-------------|------------|
| | ONE COMPLET | | MENT E AND | THEN THETA |
| ITERATION | NUMBER = | 1 | RESIM = | 11.5183 |
| ITERATION | NUMBER = | 2 | RESIM = | 2.6713 |
| ITERATION | NUMBER = | 3 | RESIN = | •9615 |
| ITERATION | | 4 | RESIM = | •6371 |
| ITERATION | NUMBER = | 5 | RESIM = | .4649 |
| ITERATION | NUMBER = | 6 | RESIM = | .3882 |
| ITERATION | NUMBER = | 7 | RESIM = | .3439 |
| ITERATION | NUMBER = | 8 | RESIM = | •3052 |
| ITERATION | NUMBER = | 9 | RESIM = | •2712 |
| ITERATION | NUMBER = | 10 | RESIM = | .2415 |
| ITERATION | NUMBER = | 11 | RESIM = | •2154 |
| ITERATION | NUMBER = | 12 | RESIM = | •1925 |
| | VTHTA = | 440.59 | | • 1 7 4 2 |
| ITERATION | NUMBER = | 13 | RESIM = | .2308 |
| ITERATION | NUMBER = | 14 | RESIM = | .2106 |
| ITERATION | NUMBER = | 15 | RESIM = | •1729 |
| | VTHT2 = | 477.00 | ļ | |
| ITERATION | NUMBER = | 16 | RESIM = | 1.9332 |
| ITERATION | NUMBER = | 17 | RESIM = | 1.2643 |
| ITERATION | NUMBER = | 18 | RESIM = | .8813 |
| ITERATION | NUMBER = | 19 | RESIM = | •6690 |
| ITERATION | NUMBER = | 20 | RESIM = | •5466 |
| ITERATION | NUMBER = | 21 | RESIM = | •4789 |
| ITERATION | NUMBER = | 22 | RESIM = | •4181 |
| ITERATION | NUMBER = | 23 | RESIM = | •3659 |
| ITERATION | NUMBER = | 24 | RESIM = | •3219 |
| ITERATION | NUMBER = | 25 | RESIM = | •2852 |
| ITERATION | NUMBER = | 26 | RESIM = | .2607 |
| ITERATION | NUMBER = | 27 | RESIM = | •2377 |
| ITERATION | NUMBER = | 28 | RESIM = | •2166 |
| ITERATION | NUMBER = | 29 | RESIM = | •1974 |
| ITERATION | NUMBER = | 30 | RESIM = | .1801 |
| | VTHT2 = | 683.58 | | |
| ITERATION | NUMBER = | 31 | RESIM = | 1.4799 |
| ITERATION | NUMBER = | 32 | RESIM = | •9777 |
| ITERATION | NUMBER = | 33 | RESIM = | •6876 |
| ITERATION | NUMBER = | 34 | RESIM = | •5268 |
| ITERATION | NUMBER = | 35 | RESIM = | •4431 |
| ITERATION | NUMBER = | 36 | RESIM = | .3907 |
| ITERATION | NUMBER = | 37 | RESIM = | • 3433 |
| ITERATION | NUMBER = | 38 | RESIM = | •3025 |
| ITERATION | NUMBER = | 39 | RESIM = | .2680 |
| ITERATION | NUMBER = | 40 | RESIN = | •2430 |
| ITERATION | NUMBER = | 41 | RESIM = | .2230 |
| ITERATION | NUMBER = | 42 | RESIM = | .2043 |
| ITERATION | NUMBER = | 43 | RESIM = | •1871 |

| Ρ= | 4.6675702E+01 | IN = | 55 | 5 JC | - | 23 | RHO | = | 4.1000000E-02 |
|-----|-----------------|------|-----|--------|---|----|------|---|---------------|
| ρ = | -3.4023753E+02 | IN = | | | = | 24 | RH 0 | | 4.1000000E-02 |
| P = | -3.4023753E+02 | IN = | | | = | 24 | | = | 4.1000000E-02 |
| P = | -3.4023753E+02 | IN = | - | | Ŧ | 24 | | = | 6.0000000E-06 |
| P = | 3.0468643E+01 | IN = | _ | | = | 24 | | 4 | 4.1000000E-02 |
| P = | 3.0468643E+01 | IN = | | | = | 24 | | = | 4.1000000E-02 |
| P = | 6.4769333E+01 | IN = | | | Ξ | 24 | | Ξ | 4.1000000E-02 |
| P = | 6.1914359E+01 | IN = | - | | = | 24 | | = | 4.1000000E-02 |
| P = | 5.5674399E+01 | IN = | | - | ÷ | 24 | | I | 4.1000000E-02 |
| P = | 5.2196954E+01 | IN = | · | | = | 24 | RHO | = | 4.1000000E-02 |
| P = | 5.2196954E+01 | IN = | | | z | 24 | | = | 4.1000000E-02 |
| P = | -3.6635503E+02 | IN = | | | Ξ | 25 | | Ξ | 4.1000000E+02 |
| P = | -3.6635503E+02 | IN = | - | | = | 25 | RHO | = | 4.1000000E-02 |
| P = | -3.6635503E+02 | IN = | : 5 | | Ŧ | 25 | RHO | # | 6.0000000E-06 |
| Р= | 7.1561888E+01 | IN = | | | Ξ | 25 | | = | 4.1000000E-02 |
| Р ± | 8.8397838E+01 | IN = | · _ | | = | 25 | | = | 4.1000000E-02 |
| P = | 7.2384835E+01 | IN = | _ | | = | 25 | | = | 4.1000000E-02 |
| P≠ | 6.0701382E+01 | IN = | | | - | 25 | | = | 4.1000000E-02 |
| P = | 5.5440809E+01 | IN = | | | ± | 25 | RHO | Ξ | 4.1000000E-02 |
| Р = | 5.5440809E+01 | IN = | | | Ξ | 25 | RH O | I | 4.1000000E-02 |
| P = | -1.0906847E+03 | IN = | = 5 | O JC | = | 26 | RHO | = | 4.1000000E-02 |
| P = | -1.0906847E+03 | IN = | = 5 | D JC | = | 26 | RHO | = | 4.1000000E-02 |
| P = | -1.0906847E+03 | IN = | = 5 | OL O | = | 26 | RH 0 | = | 6.0000000E-06 |
| P = | 1.4466197E+01 | IN = | = 5 | 1 JC | = | 26 | RH 0 | = | 4.1000000E-02 |
| P = | 1.4466197E+01 | IN = | = 5 | 1 JC | Ξ | 26 | RH 0 | = | 4.1000000E-02 |
| P = | 1.4466197E+01 | IN = | = 5 | 1 JC | = | 26 | RH O | Ξ | 2.2156833E-02 |
| P = | 7.5372255E+01 | IN = | = 5 | 2 JC | = | 26 | RH 0 | = | 4.1000000E-02 |
| P = | 6.7070811E+01 | IN : | = 5 | 3 JC | z | 26 | RHO | Ξ | 4.1000000E-02 |
| Ρ = | 5.8513096E+01 | IN = | = 5 | 4 JC | = | 26 | RHO | Ξ | 4.1000000E-02 |
| P = | 5.4855696E+01 | IN = | = 5 | 5 JC | = | 26 | RH O | = | 4.100000E-02 |
| P = | 5.4855696E+01 | IN = | = 5 | 5 JC | = | 26 | RH 0 | = | 4.1000000E-02 |
| P = | -1.3379538E+03 | IN = | = 5 | 0 JC | = | 27 | | Ξ | 4.1000000E-02 |
| P = | -1.3379538E+03 | IN = | = 5 | O JC | Ξ | 27 | | = | 4.1000000E-02 |
| P = | -1.3379538E+03 | IN = | = 5 | 0 JC | Ξ | 27 | | Ξ | 6.000000E-06 |
| P = | -7.7274892E+01 | IN : | = 5 | 1 JC | = | 27 | RH 0 | Ξ | 4.1000000E-02 |
| Ρ = | -7.7274892E+01 | IN : | = 5 | | | 27 | | = | 4.1000000E-02 |
| Ρ= | -7.7274892E+01 | IN : | = 5 | 1 JC | = | 27 | RHO | Ξ | 6.000000E-06 |
| P = | 3.2876837E+01 | | = 5 | | | 27 | RHO | | 4.1000000E-02 |
| P = | 3.2876837E+01 | | = 5 | | | 27 | RHO | | 4.1000000E-02 |
| Ρ= | 4.8862768E+01 | | = 5 | | | 27 | RHO | | 4.1000000E-02 |
| P = | 4.8862768E+01 | - | = 5 | | | 27 | RHO | | 4.100000E-02 |
| Ρ= | 5.0418879E+01 | | = 5 | | | 27 | RHO | | 4.1000000E-02 |
| Ρ= | 5.0983057E+01 | | = 5 | | | 27 | RH O | | 4.1000000E-02 |
| Ρ= | 5.0983057E+01 | | = 5 | | | 27 | RHO | Ξ | 4.1000000E-02 |
| ITE | RATION NUMBER = | 44 | R | ESIM = | | 0. | | | |
| | | | | | | | | | |

++++++ VOLUME = 1.55393E-01

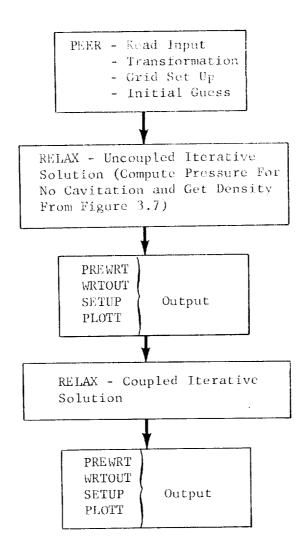


Figure D.1 Turbopump Program Computation Sequence

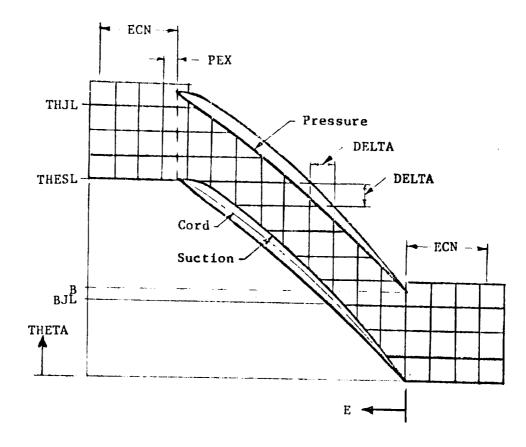
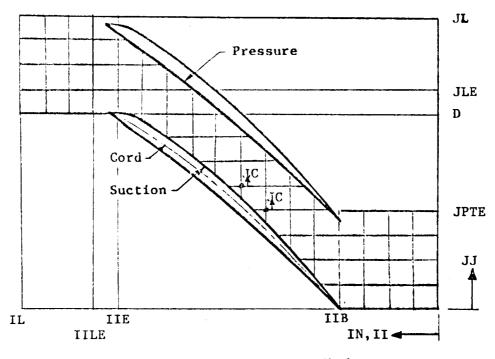
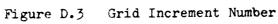


Figure D.2 THETA, E Dimensions





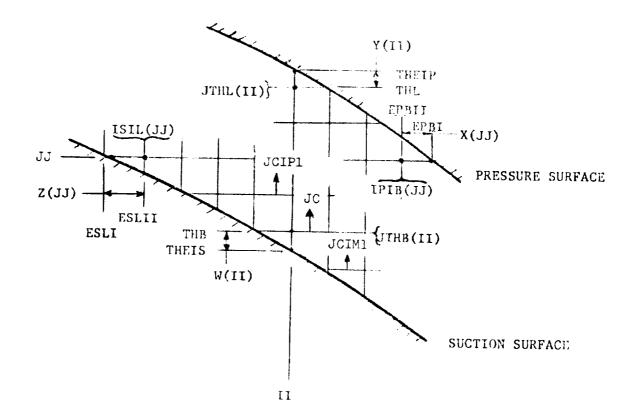


Figure D.4 Grid Increment For Extrapolation to Blade Surfaces

APPENDIX E

Turbopump Program Listing

```
PROGRAM MAIN ( INPUT, OUTPUT, TAPE5 = INPUT, TAFE6 = OUTPUT,
                       TAPES, FILMPL )
     *
С
          COMPRESSIBLE - INCOMPRESSIBLE FLOW TURBO PUMF PROGRAM
С
С
                ISIL(150), IPI8(150), W(150), X(150), Y(150), Z(150),
      COMMON
     #
                JTHL(150), JTHB(150), PSI(100,100),
     #
                RS(100), RP(100), ES1(100), RC(100),
                ED(150), RD(150), BD(150), SIAD(150), MNM, IL, JL, IIB,
     #
                IIE, B, DELTA, RESIN, OPSIP, KK, DEX, ACC, JLE, BN,
                PSIPR, RHO(100,100), G, WDOT, WW, KKL, RHOIN, POIN, HOIN,
                RCIN, VTHIN, VMOIN, PS, RR(150), BZ(150), SIA(150), RT,
     #
                INPUF, RRL, ITRIP, PDEL, JOPL
C
          ZERO OUT ARRAYS
C
      ITRIP=0
      00 \ 100 \ JJ = 1, \ 150
      W(JJ)
                 = 0.
      Y(JJ)
                 = 0.
  100 CONTINUE
С
      00 \ 150 \ II = 1, \ 150
      X(II)
                 = 0.
      Z(II)
                 = 0.
  150 CONTINUE
С
      00 \ 250 \ JJ = 1, \ 100
      DO 200 II = 1, 100
      PSI(II, JJ) = 0.
  200 CONTINUE
  250 CONTINUE
Ĉ
          CALL PEER TO READ INPUT DATA AND SET UP GRID
С
С
                 = 386.4
      G
      CALL PEER
 300
                 = PSIPR / 70.
      ER
      ACC
                 = ER
С
С
          OBTAIN FIRST RELAXATION
С
      CALL RELAX
С
      JEPSI = -PSIPR/50.
       ILMI=IL-I
       VTHTA=(PSI(ILMI,1)-PSI(IL,1))/DELTA
       VTHTA=VTHTA/(RHOIN*BZ(IL)*RR(IL))
       WRITE(6,399) VTHTA
      FORMAT(10X_{*} VTHTA = * F10.2)
 399
 400
      IF (ABS(VTHTA-WW).LT.15.0) GO TO 900
       JT8=JTH8(IL)
       JTL=JTHL(IL)
       JJ = 0
      DO BOD JN=JTB, JTL
       JJ = JJ+1
```

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```
PSI(IL, JJ) = PSI(IL, JJ) + DEPSI
 800 CONTINUE
      CALL RELAX
      IL MI=IL-1
      VTHT2=(PSI(ILMI,1)-PSI(IL,1))/DELTA
      VTHT2=VTHT2/(RHOIN*BZ(IL)*RR(IL))
      WRITE(6,899) VTHT2
 899 FORMAT(10X, * VTHT2 = *, F10.2)
      DVTHD=(VTHT2-VTHTA)/DEPSI
      DE PSI= (WW-VTHT2)/DVTHD
      VTHTA=VTHT2
      GO TO 400
С
         WRITE OUT FIRST RELAXATION
С
 90.0
      ITRIP=1
      DO 1000 JDELP=1,JDPL
      POIN=PCIN-PDEL
      WRITE(6,989) POIN
 989 FORMAT(10X, * POIN = *F10.3)
      CALL RELAX
      CALL PREWRT
      CALL WRTOUT
 1000 CONTINUE
      GO TO 300
      END
```

.

SUBROUTINE TABL (AI, BD, CI, DD, M, J, K) С С. MONO-VARIANT TABLE LOOK UP ROUTINE С. EXTRAPOLATION = LINEAR BASED ON FIRST OR LAST TWO POINTS **C** . INTERPOLATION = LINEAR, QUADRATIC, OR CUBIC С SUBROUTINE ARGUNENTS С. AI = GIVEN INDEPENDENT VARIABLE С. BD = DESIRED DEPENDENT VARIABLE С. **CI = SET OF INDEPENDENT VARIABLES** С. DD = SET OF DEPENDENT VARIABLES С. M = ORDER OF INTERPOLATION (1,2,3)C. = FIRST POINT IN TABLE (USUALLY 1) C. J K = LAST POINT IN TABLE С. C CI(1), DD(1)DIMENSION С 8001 FORMAT (* UNSUCCESFUL TABLE LCCK UP *) С C. IS AI INSIDE RANGE OF TABLE C IF (AI .GT. CI(K)) GO TO 100 GO TO 200 IF (AI .LT. CI(J)) GO TO 300 С EXTRAPOLATE IF AI OUTSIDE TABLE RANGE С. C = DD(K) + (DD(K) - DD(K-1)) + (AI - CI(K)) / (CI(K))100 BD - CI(K-1)) # GO TO 1700 = 30(J) + (30(J+1) - 30(J)) + (AI - CI(J)) /200 80 (CI(J+1) - CI(J))GO TO 1700 С DOES AI = POINT IN TABLE С. С 300 D0 400 IN = J, KI = IN IF ((ABS (AI - CI(I))) .LT. 0.00001) GO TO 500 400 CONTINUE GC TO 600 = DD(I)500 BD GO TO 1700 С C. LOCATE POSITION IN TABLE С $600 \ 0 700 \ IO = J, K$ I = IO IF (CI(I) .GT. AI) GO TO 800 700 CONTINUE WRITE (668001) CALL EXIT С 800 GO TO (900, 1000, 1300), M

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С

```
C. LINEAR INTERPOLATION
С
  900 Y1
                 = DD (I-1)
      Y2
                 = 00(I)
      X1
                 = CI (I-1)
                 = CI(I)
      X2
      DE X
                 = X2 - X1
                 = Y2 - Y1
      DY 1
                 = Y1 + ( AI - X1 ) + DY1 / DEX
      BD
       GC TC 1700
С
   GUADRATIC INTERPOLATION
C.
C
 1000 IF ( I .EQ. K )
                                           GO TO 1100
      ¥1
                 = 00(I-1)
      ¥2
                 = DD(I)
                 = DD(I+1)
      Y3
      X1
                 = CI(I-1)
                 = CI(I)
      X2
      X3
                 = CI(I+1)
       GO TO 1200
 1100 Y1
                 = 00(I-2)
      Y2
                 = DD(I-1)
      Y3
                 = 00(I)
      X1
                 = CI(I-2)
      X2
                 = CI(I-1)
      X3
                 = CI(I)
 1200 B1
                 = Y1 * ( AI - X2 ) * ( AI - X3 ) / ( ( X1 - X2 ) *
     #
                   ( X1 - X3 ) )
      82
                 = Y2 * ( AI - X1 ) * ( AI - X3 ) / ( ( X2 - X1 ) *
                   ( X2 - X3 ) )
     #
                 = Y3 * ( AI - X1 ) * ( AI - X2 ) / ( ( X3 - X1 ) *
      83
     *
                   ( X3 - X2 ) )
      BD
                 = 81 + 82 + 83
       GO TO 1700
С
    CUBIC INTERPOLATION
С.
С
 1300 IF ( I .EQ. K )
                                           GO TO 1400
      IF ((I - 1) \cdot EQ \cdot J)
                                            GO TO 1500
                 = DD(I-2)
      Y1
                 = 33(I-1)
      ¥2
      ¥3
                 = DD(I)
      ¥4
                 = DD(I+1)
      X1
                 = CI(I-2)
      X2
                 = CI(I-1)
                 = CI(I)
      X3
      X4
                 = CI(I+1)
       GO TO 1600
C
 1400 Y1
                 = 00(I-3)
      Y2
                 = 00(I-2)
      Y3
                = 00(I-1)
      ¥4
                = 00(I)
                = CI(I-3)
      X1
```

X2 = CI(1-2)X3 = CI(I-1) = CI(I) X4 GC TC 1698 С 1500 Y1 = 00(1-1)Y2 = 00(1)= JJ(I+1) **Y3** ¥4 = DD(I+2) X1 = CI(I-1) X2 = CI(I)= CI(I+1)X3 X4 = CI(I+2) С 1600 80 = Y1 * (AI - X2) * (AI - X3) * (AI - X4) / ((X1 - X2) + (X1 - X3) + (X1 - X4))# + Y2 + (AI - X1) + (AI - X3) + (AI - X4) / ($(x_2 - x_1) + (x_2 - x_3) + (x_2 - x_4))$ ¥ + Y3 * (AI - X1) * (AI - X2) * (AI - X4) / ((X3 - X1) * (X3 - X2) * (X3 - X4)) + Y4 * (AI - X1) * (AI - X2) * (AI - X3) / ((x4 - x1) * (x4 - x2) * (x4 - x3)) 1700 RETURN EN D

SUBROUTINE PEER

С

| Ų. | | | |
|----------|------------------|--------|---|
| | INPUT AND S | | |
| С. | SETUP IN | CLI | UDES INITIALIZATION, TRANSFORMATION, GRID SET UP, AND |
| С. | FIRST GU | E S | S AT STREAM FUNCTION AND JENSITY VALUES |
| C | | | |
| C. | INPUT DEFIN | | |
| с. | N | 1 | NO. OF INPUT BLADE COORDINATES (SUCTION SURFACE) |
| С. | L | 1 | NO. OF INPUT BLADE COORDINATES (PRESSURE SURFACE) |
| С. | K | | NO. OF INPUT BLADE COORDINATES (CORD LINE) |
| с. | NN | Ξ | NOT USED |
| С. | | - - | NOT USED |
| C. | חאח | = | NO. OF INPUT STREAM TUBE COORDINATES ANGLE BETWEEN BLADES (RAD) = 6.28/BN NO. OF F (THETA) GRID INCREMENTS FROM TRAILING TO |
| C. | 8 | = | ANGLE BETWEEN BLADES (RAD) = $6.287BN$ |
| C. C. | U | Ξ | NUO UP F UTHETAJ GRIU INGREMENTS FROM TRAILING TO |
| C. | D T | - | LEADING EDGE OF BLADE BLADE TIP RADIUS (IN) |
| C. | ENC | - | LENGTH OF FLOW FIELD INFRONT AND BEHINE BLADE (IN) |
| C. | RP(I) | _ | P OP 7 COOPDINATE OF ODESCUDE SUDFACE (IN) |
| C. | RS(I) | - | R OR Z COORDINATE OF PRESSURE SURFACE (I=1,L) (IN) |
| Č. | | - | R OR Z COORDINATE OF SUCTION SURFACE (I=1,N) (IN) |
| Č. | THETS(T) | - | R OR Z COORDINATE OF CORD LINE (I=1,K) (IN) THETA COORDINATE OF SUCTION SURFACE (I=1,N) (DEG) |
| č. | THETPITA | = | THETA COORDINATE OF PRESSURE SURFACE (I=1,N) (DEG) |
| č. | THETCIT | = | THETA COORDINATE OF CORD LINE (I=1,K) (DEG) |
| Č. | RD(I) | Ξ | RADIUS COORD. OF STREAM TUBE CENTER LINE(I=1, MNM) (IN) |
| Ċ. | | = | WIDTH COORD. OF STREAM TUBE RADIAL DIR. (I=1, MNH) (IN) |
| C. | SLAD(I) | = | SIN(A) COORD. OF STREAM TUBE CENTER LINE(I=1, MNH) (ND) |
| Ċ. | | | A = ANGLE BETHEEN IMPELLER C.L. AND STREAM TUBE C. |
| c. | ED(I) | = | AXIAL COORD. OF STREAM TUBE CENTER LINE(I=1, MNH) (IN) |
| C. | | ## | ALL BLADE AND STREAM TUBE COORDINATE DATA STARTS AT |
| C. | | | AT BLADE TRAILING EDGE AND GOES +VE IN UPSTREAM DIR. |
| C. | KKL | ≖ | NO. OF POINTS IN RHO-H-P TABLE |
| C. | | | CONDITIONS OR INTERIOR POINTS DEPENDING ON FLAG (INPUF |
| С. | INPUF | z | FLAG FOR DIFFERENT INLET AND EXIT BOUNDARY CONDITIONS |
| С. | | | 0 FOR STREAM LINES PARALLEL TO BLADE CORD LINE |
| C . | | | 1 EQUIVALENT TO 2 AT INLET AND 0 AT EXIT |
| С. | | | 2 INPUT STREAM FUNCTION AT ALL GRID POINTS |
| С. | | | 3 INPUT BOTTOM STREAM FUNCTION VALUE |
| С. | _ | | 4 EQUIVALENT TO |
| C. | BN | | NO. OF IMPELLER BLADES |
| С. | WW | | PUMP SPEED (RAD/SEC) |
| С. | WDOT | = | FLOW RATE IN STREAM TUBE ANULUS (LB/SEC) |
| C. | ROHIN | | PROPELLANT DENSITY AT INLET (LB/IN**3) |
| C. C. | PCIN | | STATIC FRESSURE AT INLET (LB/IN**2) |
| C. | HOIN | | ENTHALPY AT INLET (FT/SEC) |
| C. | V THIN V MOIN | - | CIRCUMFERENTIAL FLUID VELOCITY AT INLET (IN/SEC) |
| C. | PS | - | PROPELLANT LINE VELOCITY AT INLET (IN/SEC) |
| C. | RCIN | - | PROPELLANT VAPOR PRESSURE (LB/IN++2) |
| C. | IN U LIN | | RADIUS OF CENTER OF STREAM TUBE ANULUS AT INLET (IN) RD(MNM) |
| C. | RHOT(I) | | PROP. DENSITY VALUES NEAR SATURATION (I=1,KKL) (LB/IN3 |
| | 1111111111 | - | TROUT DENSITY THEORS NEAR SATURATION (1=1, KKE) (LB/INS) |
| C. | HT(T) | - | PROP. ENTHALPY VALUES DEE. TO HOTH 17-4 VVILLET 1000 |
| C. C. | HŤ(I) PT(I) | - | PROP. ENTHALPY VALUES REF. TO HOIN (I=1,KKL) (FT/SEC |
| C. | PT(I) | = | PROP. ENTHALPY VALUES REF. TO HOIN (I=1,KKL) (FT/SEC PROP. PRESSURE VALUES NEAR SATURATION (I=1,KKL) (LB/IN2 |
| | PT(I) | = | PROP. ENTHALPY VALUES REF. TO HOIN (I=1,KKL) (FT/SEC |

.

```
С
 7997 FORMAT(8A10)
 7998 FORMAT(1H1,10X,8A10)
 7999 FORMAT(19X,8A10)
 8000 FORMAT(615.5F10.4)
 8001 FORMAT(4E10.3)
 8002 FORMAT(3E10.3)
 8003 FORMAT(315,/,(10E8.3))
 8004 FORMAT(10F8.3)
                                   THETS = F10.4,8H
                                                      ES1 = F10.4
 80.09 \text{ FORMAT}(1 \times 5 \text{ HRS} = F10.4, 10 \text{ H})
                                                      EP2 = F10.4)
 8010 \text{ FORMAT(1X5HRP} = F10.4,10H)
                                   \mathsf{THETP} = \mathsf{F10.4.8H}
                                   THETC = F10.4,8H
                                                      EC1 = F10.4)
 8012 \text{ FORMAT}(1 \times 5 \text{ MRC} = F10.4, 10 \text{ H})
 8011 FORMAT(5HON = 12,7H
                            L = I2,7H
                                          K = I2,8H
                                                       NN = I2.8H
                                                                     LL = ,
     1 I_{2,8H} NNM = ,I_{2,7/5H} B = F_{10,4,7H}
                                               D = F10.4,8H
                                                               RT = F10.4,
     2 8H ENC = ,F10.4,8H ENC = ,F10.4 //)
 8013 FORMAT(1X 5HR) = F10.4,10H
                                          = F10.4,10H
                                                         SIAD = F10.4,
                                     80
                    ED
                         = F10.4)
              10H
 8014 FORMAT(1X8HDELTA = F10.4,9H THESL = F10.4,5H E = F10.4,8H THUL = F
     110.4,6H JL = I4,6H IL = I4,7H IIB = I4/7H IIE = I4,7H JLE = I4)
 8015 FORMAT(8E10.4)
 8016 FORMAT(1X8H KKL = ,12,10H INPUF = ,12,8H
                                                      BN = ,F10.4,7H
                                                                       WW =
     1 F10.4,9H WOOT = ,F10.4,10H RHOIN = ,F10.4,9H POIN = ,F10.4,9H
     2 HOIN = 4F10.4,//,11H VTHIN = ,F10.4,10H VMOIN = ,F10.4,7H PS
     3 = ,F10.4,9H ROIN = ,F10.4,10H PSINU = ,F10.4,10H PSIND = ,
     4 F10.4)
 8017 FORMAT(1K9H RHOT = ,F10.4,7H HT = ,F10.4,7H PT = ,F10.4)
 8018 FORMAT(//)
 8019 FORMAT(1X46HBEGIN MAIN PRCGRAM INCREMENT THETA AND THEN E)
 8020 FORMAT (1X49HSTEP NO. ONE COMPLETE INCREMENT E AND THEN THETA)
 8030 FORMAT(1X5HII = I4,7H JN = I4/EH W = F10.4,6H X = F10.4,
          Y = F10.4, 6H Z = F10.4)
     16H
 8035 FORMAT(1X5HJJ = 14,9H IPIB = 14,9H ISIL = 14/9H
                                                             ESLI = F10.4,
     1 9H ESLII= F10.4,9H EPBI = F10.4,10H EPBII = F10.4)
 8040 FORMAT(1X5HJJ = 14,9H IPIB = 14,9H ISIL = 14/9H ESLI = F10.4,
     110H ESLII = F10.4)
С
      COMMON
                /ABC/
                RHOT(100), HT(100), PT(100)
      COMMON
                / C8 A/
     #
                ENC
      COMMON
                / NO G/
      ¥
                NNDG, LNDG, KNDG, ILNDG, THETMIN, THETMAX, EMIN,
     *
                EMAX, ICNT(99), THETS(100), THETC(100), THETP(100),
     ¥
                EC1(100), EP2(100), ESS1(100), KNT1, KNT2
                ISIL(150), IPI8(150), W(150), X(150), Y(150), Z(150),
      COMMON
     ¥
                JTHL(150), JTHB(150), PSI(100,100),
     ¥
                RS(100), RP(100), ES1(100), RC(100),
                ED(150), RD(150), BJ(150), SIAJ(150), MNM, IL, JL, IIB,
     ¥
     ¥
                IIE, B, DELTA, RESIM, DPSIP, KK, DEX, ACC, JLE, BN,
                PSIPR, RHO(100,100), G, HDOT, WW, KKL, RHOIN, POIN, HOIN,
     ¥
     ¥
                ROIN, VTHIN, VMOIN, PS, RR(150), BZ(150), SIA(150), RT,
     ¥
                INPUF, RRL, ITRIP, POEL, JOPL
С
```

```
C
C
```

READ INPUT DATA

```
READ(5,7997) 11,12,13,14,15,16,17,18
      IF (EOF, 5) 50,60
50
      CALL EXIT
      WRITE(6,7998)11,12,13,14,15,16,17,18
60
      READ(5,7997) 11,12,13,14,15,16,17,18
      WRITE(6,7999)11,12,13,14,15,16,17,18
      READ (5,8000)
                        N, L, K, NN, LL, MNM, B, D, RT, ENC, BNG
                           Ny Ly Ky NNy LL, MNM, B, D, RT, ENC, BNC
      WRITE (6+8011)
      READ (5,8004)
                         (RP(I), I=1, L)
      READ (5,8004)
                         (RS(I), I=1, N)
                         (RC(I),I=1,K)
      READ (5,8004)
      READ (5,8004)
                         (THETS(I), I=1, N)
      READ (5,8004)
                         (THETP(I), I=1, L)
      READ (5,8004)
                         (THETC(I), I=1, K)
С
                         (RD(I), BD(I), SIAD(I), ED(I), I=1, MNM)
      READ (5,8001)
                        KKL, INPUF, JOPL, BN, WW, WOOT, RHOIN, POIN,
      READ (5,8003)
     ¥
                        HOIN, VTHIN, VMOIN, PS, ROIN, PSINU, PSIND, PDEL
                         (RHOT (I), HT(I), PT(I), I=1, KKL)
      READ (5,8002)
С
    TRANSFORM FRCM R, THETA PLANE TO E, THETA PLANE
С.
       FOR THIS CASE BOTH ARE LINEAR TRANSFORMATIONS
C .
С
      DO 100 I = 1, N
                 = RS(I)
      ES1(I)
                 = THETS(I) / 57.2958
      THETS(I)
  100 CONTINUE
      200 I = 1, L
      EP2(I)
                 = RP(I)
                 = THETP(I) / 57.2958
      THETP(I)
  200 CONTINUE
      20
         300 I = 1, K
      EC1(I)
                 = RC(I)
                 = THETC(I) / 57.2958
      THETC(I)
  300 CONTINUE
С
       OVER RIDE BD INPUT
С.
С
      CALL TABL ( ES1(N), RRL, ED, RD, 1, 1, MNM )
                 = THETC(K) / D
      DELTA
C
         WRITE OUT INPUT DATA AND VALUES CALCULATED FROM INFUT
С
С
      WRITE (6,8009)
                           ((RS(I), THETS(I), ES1(I)), I=1, N)
      WRITE (6,8018)
                           ((RP(I), THETP(I), EP2(I)), I=1,L)
      WRITE (6,8010)
      WRITE (6,8018)
                           ((RC(I), THETC(I), EC1(I)), I=1,K)
      WRITE (6,8012)
      WRITE (6,8018)
                           ((RD(I), BD(I), SIAD(I), ED(I)), I=1, MNM)
      WRITE (6,8013)
      WRITE (6,8018)
                           KKL, INPUF, BN, WW, WDOT, RHOIN, PCIN, HOIN,
      WRITE (6,8016)
                           VTHIN, VMOIN, PS, ROIN, PSINU, PSIND
                           (RHOT(I), HT(I), PT(I), I=1, KKL)
      WRITE (6,8017)
```

```
THESL
               🛫 🖸 🥙 DELTA
                = IFIX ( THETP(L) / DELTA ) + 1
      JL
                = FLOAT ( JL - 1 ) + DELTA
      THUL
                = - FLOAT ( IFIX ( ENC / DELTA ) + 1 ) * DELTA
      E
                = IFIX ( ( EC1(K) + ENC ) / DELTA ) + IFIX ( BNC /
      IL
                  DELTA ) + 1
                = N
      NN OG
      LNDG
                = L
      KNDG
                = K
                = IL
      IL NDG
      THETMIN
                = AMIN1 ( THETS(1), THETP(1), THETC(1) )
                = AMAX1 ( THETS(N), THETP(L), THETC(K) )
      THETMAX
                = WDOT / BN
      PS IPR
                = PSIPR * DELTA / B
      DELPS
С
      DO 500 IJK= 1, N
      ESS1(IJK) = ES1(IJK)
  500 CONTINUE
C
                = IFIX ( ENC / DELTA ) + 1
      IIB
                = IFIX ( EC1(K) / DELTA ) + IFIX ( ENC / DELTA ) + 1
      IIE
      RESIM
                = 0.
                = PSIPR / 20.
      DPSIP
      JP TE
                = IFIX ( B / JELTA ) + 1
                = IFIX(D) + 1
      JLE
                = ( FLOAT ( IFIX ( EC1(K) / DELTA ) ) + DELTA ) +
      PE X
                   DELTA - EC1(K)
                = IIE + 1
      IILE
      IF ( PEX .EQ. 0. )
                                         GO TO 600
       GC TC 700
C
  600 PEX
                = JELTA
  700 DEX
                = PEX / DELTA
      IF ( THUE .EQ. THETP(L) )
                                     GO TO 800
       GO TO 908
Ć
  800 JL
                = JL - 1
      THUL
                = THJL - DELTA
                = -DELTA
  900 THETA
                        DELTA, THESL, E, THJL, JL, IL, IIB, IIE, JLE
      WRITE (6,8014)
      WRITE (6:8019)
С
    INCREMENT THETA AND CALCULATE E DIMENSION BETWEEN GRID POINTS AND
С.
    BLADE SURFACES
С.
С
      DO 2100 JJ = 1, JL
      THETA
               = THETA + DELTA
      IF ( ABS ( 1. - ( THETA / THESL ) ) - .0001 ) 1300, 1300, 1000
 1000 IF ( THETA .GT. THESL )
                                          GO TO 1300
Ĉ
       E INCREMENT NEXT TO SUCTION SURFACE = Z(JJ)
С.
С
 1100 CALL TABL ( THETA, ESLI, THETS, ES1, 2, 1, N )
      ISIL(JJ) = IFIX ( ESLI / DELTA ) + IFIX ( ENC / DELTA ) + 1
                = FLOAT ( IFIX ( ESLI / DELTA ) ) * DELTA
      ESLII
```

```
16 ( ESUIT .EQ. ESUI ) 50 TO 1200
      GO TO 1400
С
1200 \text{ ISIL(JJ)} = \text{ISIL(JJ)} - 1
     ESLII = ESLII - DELTA
      GC TO 1400
G
 1300 ISIL(UU) = IL = 1
               = O.
      ESLII
                = DELTA
      ESLI
С
                                       GO TO 1500
 1400 IF ( THETA .GT. 8 )
      IPIB(JJ) = 2
      GO TO 1600
С
      E INCREMENT NEXT TO PRESSURE SURFACE = X(JJ)
С.
С
 1500 CALL TABL ( THETA, EPBI, THETP, EP2, 2, 1, L )
      IPIB(JJ) = IFIX ( EPBI / JELTA ) + IFIX ( ENC / JELTA ) + 2
                = ( FLOAT ( IFIX ( EPBI / DELTA ) + 1 ) ) + DELTA
      EPBII
                = IPIB(JJ)
 1600 IPB
                = ISIL(JJ)
      ISL
                = 1.
      X(JJ)
               = 1.
      Z(JJ)
      DO 2000 IN= IPB, ISL
                                 GO TO 1700
      IF ( IN .EQ. ISIL(JJ) )
      GO TO 1800
С
             = ( ESLI - ESLII ) / DELTA
 1700 Z(JJ)
      GO TO 2000
 1800 IF ( ( THETA .GT. B ) .AND. ( IN .EQ. IPIB(JJ) ) ) GO TO 1900
       GC TC 2000
С
               = ( EPBII - EPBI ) / DELTA
 1900 X(JJ)
 2000 CONTINUE
 2100 CONTINUE
      WRITE (6,8020)
С
   INCREMENT E AND 1) LOOK UP STREAM TUBE DIMENSIONS, 2) CALCULATE THET
С.
    DIMENSION BETHEEN GRID POINTS AND BLADE SURFACES, AND 3) PROVIDE
С.
    FIRST GUESS OF STREAM FUNCTION AND DENSITY AT GRID POINTS
С.
С
      00 3800 II=1, IL
               = 1.
      W(II)
      Y(II)
                = 1.
      Ε
                = E + DELTA
      CALL TABL ( E, RRR, ED, RD, 1, 1, MNM )
                = RRR
      RR(II)
      CALL TABE ( E, BZZ, ED, BD, 1, 1, MNM )
      87 (II)
                = 822
                = (BD(MNM)/(RRR**2.))*(RD(MNM)**2.)
С
      8Z(II)
С
      CALL TARE ( E, SIDD, ED, SIAD, 1, 1, MNM )
      SIA(II) = SIDD
                                         GO TO 2800
      IF ( E .GT. 0.)
```

```
С
       REGION DOWN STREAK OF BLADES
С.
С
                = -DELTA
      THETA
С
       EXTRAPOLATE BACK ALONG BLADE CORD LINE
С.
С
      CALL TABL ( E, THEC, ECI, THETC, 1, 1, K )
      JTHL(II) = IFIX ( B / DELTA ) + 1
                = FLOAT ( JTHL(II) - 1 ) * DELTA
      BJL
      JTHB(II)
               = 1
                                          GO TO 2200
      IF ( BJL .EQ. 8 )
       GO TO 2300
С
 2200 \text{ JTHL(II)} = \text{JTHL(II)} - 1
                = 8 - JELTA
      BJL
 2300 IF ( ( ABS(E) ) .LT. 0.0001 ) GO TO 2400
       GC TO 2500
С
 2400 THETA
                = 0.
      JTHB(II) = 2
                = JTHB(II)
 2500 JTB
                 = JTHL(II)
      JTL
                = 0
      JJ
С
      DO 2700 JN=JTB, JTL
      JJ
                 = JJ + 1
                = THETA + JELTA
      THETA
      PSI(II,JJ) = ( THETA - THEC ) + PSIPR / B
      RHO(II,JJ) = RHOIN
                                          GO TO 2600
      IF ( JN .EQ. JTHL(II) )
       GO TO 2700
С
 2600 Y(II) = ( B - BJL ) / DELTA
 2700 CONTINUE
       GC TO 3800
С
                                         GO TO 3500
 2800 IF ( E .GT. EC1(K) )
С
       REGION BEWEEN BLADES
C.
С
       CALL TABE ( E, THEIS, ES1, THETS, 2, 1, N )
C
       THETA INCREMENT NEXT TO PRESSURE SURFACE = Y(II)
C.
C
       CALL TABL ( E, THEIP, EP2, THETP, 2, 1, L )
       JTHL(II) = IFIX ( THEIP / DELTA ) + 1
                 = FLOAT ( JTHL(II) - 1 ) * DELTA
       THL
                                           GO TO 2900
       IF ( THL .EQ. THEIP )
       GO TO 3000
С
                 = THL - DELTA
 2900 THL
       JTHL(II) = JTHL(II) - 1
С
       THETA INCREMENT NEXT TO SUCTION SURFACE = W(II)
С.
```

```
С
                 = IFIX ( THEIS / DELTA ) + 2
 3000 JTHB(II)
                 = FLOAT ( JTHB(II) - 1 ) + DELTA
      THB
                 = THR - DELTA
      THETA
                 = THEIP - THEIS
      DELTH
                 = JTHB(II)
      JT B
                 = JTHL(II)
      JTL
                 = 0
      JJ
С
      DO 3400 JN= JTB, JTL
                 = JJ + 1
      JJ
                 = THETA + DELTA
      THETA
      PSI(II,JJ) = ( THETA - THEIS ) * PSIPR / DELTH
      RHO(II, JJ) = RHOIN
                                           GO TO 3100
      IF ( JN .EQ. JTHB(II) )
       GO TO 3200
С
             = ( THB - THEIS ) / DELTA
 3100 W(II)
                                            GO TO 3300
 3200 IF ( JN .EG. JTHL(II) )
       GO TO 3400
С
                 = ( THEIP - THL ) / DELTA
 3300 Y(II)
 3400 CONTINUE
       GO TO 3800
С
        REGION OP STREAM OF BLADES
С.
C
 3500 \text{ JTHL}(II) = \text{JL}
С
        EXTRAPOLATE FORWARD ALONG BLADE CORD LINE
С.
С
       CALL TABL ( E, THEC, EC1, THETC, 1, 1, K )
       J2 BLADE AND INLET FLOW SLOPE
С
       0TDE = 1.7
       DWDU = 3.0
       DELD = DWDU - DTDE
       IF ( E.LT. (EC1(K) + .5)) THEC = THEC + 1.*DELD*(E - EC1(K))**2
       IF ( E.GE. (EC1(K)+.5)) THEC = THEC +.25*DELD + DELD*(E -EC1(K)-.5)
       JTHB(II) = IFIX(0) + 1
                  = ( D - 1. ) * DELTA
       THETA
                  = JTHB(II)
       JT B
                 = JTHL(II)
       JTL
                 = 0
       JJ
 С
       DO 3700 JN= JTB, JTL
                  = JJ + 1
       JJ
                  = THETA + DELTA
       THETA
       PSI(II,JJ) = ( THETA - THEC ) * PSIPR / B
       RHO(II,JJ) = RHOIN
                                            GO TO 3600
       IF ( JN .EQ. JTHL(II) )
        GO TO 3700
 С
                  = ( THETP(L) - THUL ) / DELTA
  3600 Y(II)
  3700 CONTINUE
                  = JTL - JTB + 1
       JLIM
```

```
IF ( INPUF .EQ. 1 ) READ (5,8015) ( PSI(II,JJ), JJ = 1, JLIM )
 3800 CONTINUE
C
      IF ( INPUF .GT. 1 .ANG. INPUF .LT. 4 ) GO TO 4000
 3900 IF ( INPUF .GE, 3 )
                                         GO TO 4200
      GO TO 4400
 4000 PSIUP = PSINU
С
      DO 4100 JJ = 1, JLIM
      PSIUP = PSIUP + JELPS
      PSI(IL,JJ) = PSIUP
 4100 CONTINUE
      GO TO 3900
С
 4200 PSIDN = PSIND
      DO 4300 JJ= 1, JPTE
      PSIDN = PSIDN + DELPS
      PSI(1,JJ) = PSIDN
 4300 CONTINUE
С
 4400 00 4600 I = 1, 110
      DO 4500 J = 1, 55
      RHO(I,J) = RHOIN
4500 CONTINUE
 4600 CONTINUE
С
      RETURN
     EN D
```

```
SUPROUTINE RELAX
                                                   ∕
С
С
         RELAXATION SUBROUTINE
С
 8001 FORMAT ( 20H ITERATION NUMBER = , I4, 14H
                                                       RESIM = , F10.4 )
                                    IN = *, I4, *
                                                     JC = *, I4, *
                                                                       RHO
 8002 FORMAT ( * P = *, E15.7, *
                       PCAL = ", E12.5)
     1- *, 615.7,*
                                             P = *, E12.5, * \vee IN = *, I5,
                     RHOCM = *, E12.5, *
 8003 FORMAT ( *
                       JC = +, I5 )
C
                / PL T/
      COMMON
                R(100,100), RESID(100)
                ISIL(150), IPIB(150), W(150), X(150), Y(150), Z(150),
      COMMON
                JTHL(150), JTHB(150), PSI(100,100),
     #
                RS(100), RP(100), ES1(100), RC(100),
                ED(150), RD(150), BD(150), SIAD(150), MNM, IL, JL, IIB,
                IIE, 8, DELTA, RESIM, DPSIP, KK, DEX, ACC, JLE, BN,
                PSIFR, RHO(100,100), G, WDOT, WW, KKL, RHOIN, POIN, HOIN,
                ROIN, VTHIN, VHOIN, PS, RR(150), BZ(150), SIA(150), RT,
     4
                INPUF, RRL, ITRIP, PDEL, JDPL
                /ABC/
      COMMON
                RHOT(100), HT(100), PT(100)
     *
                NUM
                      101
      DATA
С
          ARITHMETIC STATEMENT FUNCTIONS FOR INTERPOLATION
С
С
                 = ( ( DEX / 3. ) + ( 0.5 * DEX ** 2 ) + ( ( DEX ** 3 )
      AA (DEX)
                     6.)) + (-1.)
                   1
                   ( ( 3. * DEX / 2. ) + ( 2. * DEX ** 2 ) + ( ( DEX **
      BB (DEX)
                 Ξ
                   3)/2.))
      ¥
                 = ( 3. * DEX + ( ( 5. * DEX ** 2. ) / 2. ) + ( ( DEX
      CC (DEX)
                   ** 3. ) / 2. ) ) * ( -1. )
                 = ( 1. + ( 11. * DEX / 6. ) + ( DEX ** 2. ) + ( ( DEX
      DO (DEX)
                   ** 3. ) / 6. ))
С
      RESI2 = 10000.
       ILMI = IL - 1
                 = 1.
      CKK
                 = 1.
       CC C
                   (-11. # PSI(IL,1) + 18. * PSI(IL-1,1) -9.
   100 DPSI1
                 =
                   * PSI(IL-2,1) + 2. * PSI(IL-3,1) ) / DELTA
      4
                 = - CCC * DPSI1 / ( RHO(IL,1) * BZ(IL) * RR(IL) * 6. )
       VT HC
       JENO = 1./(RHOIN*BZ(IL)*RR(IL))**2.
                 = DENO * ( ( 01+ D2) / DELTA ) ** 2 + ( ( E1+ E2)
       BOIN
                    / DELTA ) ** 2 )
      ¥
С
       00 3400 JJ= 1, JL
                 = IPIB(JJ)
       TP B
                 = ISIL(JJ)
       ISL
                 = 0
       II
С
       DO 3300 TN= IP8, ISL
                 = II + 1
       II
                  = JJ - JTHB(IN) + 1
       XC.
                 = JJ - JTHB(IN+1) + 1
       JUIP1
```

```
JCIM1 = JJ - JTHB(IN-1) + 1
С
      IF ( ( IN .LT. IIB ) .OR. ( IN .GT. IIE ) ) GC TO 1100
  200 IF ( JJ .EQ. JTHB(IN) )
                                       GO TO 300
       GO TO 500
С
  300 PSIJ
           = 0.
                = RHO(IN,JC) + ( 1. + W(IN) ) - RHO(IN,JC+1) + W(IN)
      RHIJ
      IF ( IN .EQ. ISIL(JJ) )
                                      GO TO 400
       GO TO 2100
С
  400 PSII
               = 0.
               = RHO(IN,JC) + ( 1. + Z(JJ) ) - RHO(IN-1,JCIM1) + Z(JJ)
      RHII
      BIJ
                = \theta Z(IN)
      BII
               = (1 - Z(JJ)) + BZ(IN) + Z(JJ) + BZ(IN+1)
       GO TO 2200
C
  500 IF ( IN .EQ. IPI9(JJ) )
                                GO TO 600
       GO TO 700
С
  600 PSI(IN-1, JCIM1) = PSIPR
      BII
               = 87(IN+1)
      BIJ
               = 8Z(IN)
      RHO(IN-1, JCIM1) = ( 1. + X(JJ) ) * RHO(IN, JC) - X(JJ) *
                  RHO(IN+1, JCIP1)
      PSIJ
               = PSI(IN, JC-1)
      RHIJ
              = RHO(IN, JC-1)
      PSII
              = PSI(IN+1, JCIP1)
              = RHO(IN+1, JCIP1)
      RHII
      IF ( IN .GT. IIE )
                                        GO TO 2100
С
  700 IF ( JJ .EG. JTHL(IN) )
                                        GO TO 800
       GO TO 900
  800 PSI(IN, JC+1) = PSIPR
      RHO(IN, JC+1) = RHO(IN, JC) + (1 + Y(IN)) - RHO(IN, JC-1) + Y(IN)
 900 IF ( IN .EQ. ISIL(JJ) )
                                        GO TO 1000
      IF ( IN .EQ. IPIB(JJ) )
                                        GO TO 2200
      GO TO 2000
С
 1000 IF ( IN .GT. IIE )
                                        GO TO 2000
      PSII
             = 0.
      BII
               = (1 - Z(JJ)) + BZ(IN) + Z(JJ) + BZ(IN+1)
               = 8Z(IN)
      BIJ
               = RHO(IN, JC) + (1 + Z(JJ)) - RHO(IN-1, JCIM1) + Z(JJ)
      RHII
               = RHO(IN, JC) + (1. + W(IN)) - RHO(IN, JC+1) + W(IN)
     RHIJ
     PSIJ
               = PSI(IN, JC-1)
      GO TO 2200
C
 1100 IF ( JJ .EQ. JTHB(IN) )
                                        GO TO 1200
      GO TO 1600
 1200 JJL
               = JTHL(IN) - JTHB(IN) + 1
     PSIJ
               = PSI(IN,JJL) - PSIPR
     RHIJ
               = RHO(IN,JJL)
     W(IN)
              = Y(1)
     IF ( IN .LT. IIB )
                                   GO TO 1300
```

```
GC TC 1480
С
 1300 DEX
                 = 1.0
                 = 4. * PSI(IN, JC+1) - 6. * PSI(IN, JC+2) + 4. *
      PSIJ
                   PSI(IN, JC+3) - PSI(IN, JC+4)
     #
                 = 4. * RHO(IN, JC+1) - 6. * RHO(IN, JC+2) + 4. *
      RHIJ
                   RHO(IN, JC+3) - RHO(IN, JC+4)
 1400 IF ( ( IN .EG. ISL ) .AND. ( IN .LT. IIB ) ) GO TO 1500
       GO TO 2100
С
 1500 PSII
                 = 0.
                 = RHO(IN,JC) * ( 1. + Z(JJ) ) - RHO(IN-1,JCIM1) * Z(JJ)
      RHII
                 = (1 - Z(JJ)) + BZ(IN) + Z(JJ) + BZ(IN+1)
      BII
                 = BZ(IN)
      BIJ
       GO TO 2200
                                            GO TO 1700
 1600 IF ( JJ .EG. JTHL (IN) )
       GO TO 2000
С
 1700 PSI(IN, JC+1) = PSI(IN, 1) + PSIPR
      RHO(IN, JC+1) = RHO(IN, 1)
                                            GO TO 1800
       IF ( IN .LT. IIB )
       GO TO 1900
C
                 = Y(1)
 1800 DEX
       PSI(IN, JC+1) = AA(DEX) + PSI(IN, JC-3) + BB(DEX) + PSI(IN,
                   JC-2) + CC(DEX) * PSI(IN, JC-1) + DD(DEX) * PSI(
                    IN,JC)
       RHO(IN, JC+1) = AA(DEX) * RHO(IN, JC-3) + BB(DEX) * RHO(IN, JC-2) +
                   CC(DEX) * RHO(IN, JC-1) + DD(DEX) * RHO(IN, JC)
      .
С
 1900 IF ( ( IN .EQ. IPIB(JJ) ) .AND. ( IN .GT. IIE ) ) GO TO 200
                 = PSI(IN, JC-1)
 2000 PSIJ
                 = RHO(IN, JC-1)
       RHIJ
                 = PSI(IN+1, JCIP1)
 2100 PSII
                 = BZ(IN+1)
       BII
                 = BZ(IN)
       BIJ
                 = RHO(IN+1, JCIP1)
       RHII
С
  2200 WWW
                  = 1.0
       XXX
                  = 1.0
                  = 1.0
       YYY
                  = 1.0
       ZZZ
                                            YYY = Y(IN)
       IF ( JJ .EQ. JTHL(IN) )
                                            WWW = W(IN)
       IF ( JJ .EQ. JTHB(IN) )
                                            XXX = X(JJ)
       IF ( IN .EC. IPIB(JJ) )
                                            ZZZ = Z(JJ)
       IF ( IN .EQ. ISIL(JJ) )
 С
                  = ZZZ + ( PSI(IN-1,JCIM1) - PSI(IN,JC) ) /
       01
                    ( XXX + ( XXX + ZZZ ) )
      ¥
                  = XXX * ( PSI(IN, JC) - PSII ) / ( ZZZ * ( XXX +
       D2
                    ZZZ ) )
      #
                  = YYY * ( PSIJ - PSI(IN, JC) ) / ( WWW * ( YYY +
       E1
                    HMM ) )
      #
                  = WWW + ( PSI(IN, JC) - PSI(IN, JC+1) ) /
       E2
                    ( YYY + ( YYY + WWW ) )
      *
```

```
Ĉ
С
       IF ((IN.EQ.ISL).AND. (ISL.EQ.ILM1).AND. (JC.EQ.3)) GO TO 2210
С
       GO TO 2220
C2210 BOIN = DENC* (((D1+D2)/DELTA) ++2+((E1+E2)/DELTA) ++2)
 2220 IF ( ITRIP .EG. 0 )
                                            GO TO 2600
       WR SO
                 = ( WH + RR(IN) ) ++ 2
       DENO
                 = 1. / ( RHOIN * BZ(IN) * RR(IN)) ** 2.
       IF(IN.LT.IIE) GO TO 2300
       COIN = BOIN - ((RR(IN) + WW) + 2_{*})
       GO TO 2400
С
 2300 COIN
                 = BOIN - ( ( RRL * WW ) ** 2. )
 2400 JOIN
                 = COIN + ( POIN * 2. * G / RHOIN )
       Ρ
                 = RHOIN * ( DENO * ( ( C D1 + D2 ) / DELTA ) ** 2 +
                   ( ( E1 + E2 ) / DELTA ) ** 2 ) - WRSQ - DOIN ) * ( -1.
      *
                   ) / ( 2. + G )
       WRITE(6,8002)P, IN, JC, RHO(IN, JC)
       IF ((IN.EQ.ISL) .AND. (ISL.EQ.ILM1))GO TO 2510
       IF (P.LT.POIN) GO TO 2510
      GO TO 2500
 2510 WRITE (6,8002) P, IN, JC, RHO (IN, JC)
С
 2500 IF ( P .LT. PS )
                                           GO TO 2700
      GO TO 3300
 2600 RHIJ
                 = AMAX1 ( RHIJ, 0.000006 )
      RHO(IN, JC+1) = AMAX1 ( RHO(IN, JC+1), 0.000006 )
                 = AMAX1 ( RHII, 0.000006 )
      RHII
      RHO(IN-1, JCIM1) = AMAX1 ( RHO(IN-1, JCIM1), 0.000006 )
C
                 = ( 2. * ( RR(IN) ** 2 ) * WW * BZ(IN) * RHO(IN,JC)
      A1
                    * SIA(IN) ) * DELTA * DELTA
                 = ZZZ * ( ALOG ( RHO(IN-1,JCIM1) * BIJ ) - ALOG ( RHO(IN
      Ci
                   ,JC) * BZ(IN) ) ) / ( XXX * ( XXX + ZZZ ) )
      C2
                 = XXX * ( ALOG ( RHO(IN, JC) * BZ(IN) ) - ALOG ( RHII *
     ¥
                   EII ) ) / ( ZZZ + ( XXX + ZZZ ) )
      R1
                 = ( PSI(IN-1,JCIM1) - PSI(IN,JC) ) / ( XXX * (
                   XXX + ZZZ ) )
                 = ( PSI(IN,JC) - PSII ) / ( ZZZ + ( ZZZ + XXX ) )
      R2
      R3
                 = ( PSI(IN, JC+1) - PSI(IN, JC) ) / ( YYY + ( YYY +
                   WWW ) )
      R4
                 = ( PSI(IN, JC) - PSIJ ) / ( WWW + ( WWW + YYY ) )
      C3
                 = WHW + ( ALOG (RHIJ) - ALOG ( RHO(IN,JC) ) ) / ( YYY +
     *
                   ( YYY + WWW ) )
                 = YYY + ( ALOG (RHO(IN,JC) ) - ALOG ( RHO(IN,JC+1) ) ) /
      C4
                   ( HMM * ( YYY + MMM ) )
С
                 = -(A1 + (D1 + D2) + (C1 + C2) + CCC - 2. + ((R1))
      R(IN,JC)
                   - R2 ) * CCC + ( R3 - R4 ) * CKK ) + ( E1 + E2 ) * (
                   C3 + C4 ) * CKK )
С
      IF ( ITRIP .EQ. 0 )
                                           GO TO 3300
      IF (P.GT.POIN ) GO TO 3300
С
      WRITE (6;8002)
                       P, IN, JC, RHC(IN, JC)
       GO TO 3300
С
```

```
2700 CALL TABL ( P, RHIP, PT, RHOT, 1, 1, KKL )
       IF (RHIP.L (.. 000006) RHIP=.000006
       WRITE(6.8002) P, IN, JC, RHIP
       RHO(IN, JG) = RHIP
       GO TO 3300
       GO TO 2710
 ин анниккочкичкички не ВЕГОХ
 27.20 IF (ABS((RH1P/RHO(IN,JC))-1.0).LT..001) GO TO 2710
       RHO(IN, JC) = .5 + (RHO(IN, JC) + RHIP)
       RHOCM=RHO(IN,JC)
       DE NO=1 / (RHOCM*BZ(IN) *RR(IN)) **2
                 = RHOCH * ( DENO * ( ( C D1 + D2 ) / DELTA ) ** 2 + ( (
       Ρ
                    E1 + E2 ) / DELTA ) ** 2 ) - WRSQ - DOIN ) * ( -1. )
      4
                    / (2. * G)
       GO TO 2700
 2705 WRITE(6,8002) P, IN, JC, RHIP
       GO TO 2600
  2710 WRITE(6,8002) P, IN, JC, RHO(IN, JC)
       GO TO 2600
       IF ( RHIP .LE. 0. )
                                            RHIP = 0.000006
С
**** ***** *** *** *** *** RELAX
  2800 RHOCM
                 = RHIP
       IF ( ITRIP .EQ. 1 )
                                            RHO(IN, JC) = RHOCM
       WRITE (6,8003) RHOCM, P, IN, JC
                                            GO TO 3300
       IF ( ITRIP • EQ. 1 )
С
                 = 1. / ( RHOCH + BZ(IN) + RR(IN) ) ++ 2.
       DE NO
                  = RHOCM + ( DENO + ( ( 01 + D2 ) / DELTA ) ++ 2 + ( (
       PCAL
                    E1 + E2 ) / DELTA ) ** 2 ) - WRSQ - DOIN ) * ( -1. )
                    / (2. * G)
                                             GO TO 2900
       IF ( ITRIP .EQ. 0 )
       WRITE (6,8002) P, IN, JC, RHO(IN, JC), PCAL
C
  2900 IF ( ( ABS ( PCAL / P ) - 1. ) .LT. 0.0001 )
                                                          GO TO 3100
       IF ( PCAL .LT. PSAV )
                                             GO TO 3000
       RHO(IN, JC) = RHOCH
        GC TO 3100
  3000 RHO(IN, JC) = RHOIN - 0.05 * ( RHO(IN, JC) - RHOCM )
       IF ( RHC(IN, JC) .LT. 0.00002 ) RHO(IN, JC) = RHOIN
       GO TO 2600
 C
  3100 IF ( RHOCM .LE. 0. )
                                             RHOCM = 0.000006
  3200 \text{ RHO}(IN, JC) = \text{RHOCM}
        GO TO 2600
  3300 CONTINUE
  3400 CONTINUE
       IF (ITRIP.NE.0) GO TO 4800
  3500 DO 4308 JJ= 1, JL
       IPB
                 = IPIB(JJ)
       ISL
                  = ISIL(JJ)
                 = 0
       II
C
       DO 4200 IN= IPB, ISL
                = II + 1
       II
```

```
WW W
                = 1+0
                = 1.0
      XXX
      YYY
                 = 1.0
      ZZZ
                 = 1.0
      IF ( JJ .EG. JTHL(IN) )
                                            YYY = Y(IN)
      IF ( JJ .EQ. JTHB(IN) )
                                            WWW = W(IN)
      IF ( IN .EQ. IPIB(JJ) )
                                            XXX = X(JJ)
      IF ( IN .EQ. ISIL(JJ) )
                                            ZZZ = Z(JJ)
С
      JC
                 = JJ - JTHB(IN) + 1
      JC IP1
                 = JJ - JTHB(IN+1) + 1
                 = JJ - JTHB(IN-1) + 1
      JCIM1
      DPSI
                 = R(IN, JC) / ( ( 1. / WWW ) + ( 1. / XXX ) + ( 1. / YYY
                   ) + (1 \cdot / ZZZ))
      R(IN, JC)
               = 0.
      PSI(IN, JC) = PSI(IN, JC) + DPSI
С
      IF ( ( IN .LT. IIB ) .OR. ( IN .GT. IIE ) ) GO TO 3600
      IF ( ( JJ .EQ. JTHB(IN) ) .AND. ( IN .EQ. ISIL(JJ) ) ) GO TO 4100
      IF ( JJ .EQ. JTHR(IN) )
                                            GO TO 4000
      IF ( IN .EQ. ISIL(JJ) )
                                            GO TO 4100
       GC TO 3900
С
 3600 IF ( JTHB(IN) .EQ. JJ )
                                             GO TO 3700
      IF ( JTHE(IN) .EQ. JJ )
                                             GO TO 3800
       GO TO 3900
 3700 JJL
                 = JTHL(IN) - JTHB(IN) + 1
      JB
                 = JTHL(IN)
      R(IN, JJL) = R(IN, JJL) + DPSI + (1. / YYY)
      IF ( IN .EQ. ISIL(JJ) )
                                             GO TO 4100
       GO TO 4000
С
 3800 JJ8
                 = JTHB(II)
      R(IN, 1) = R(IN, 1) + DPSI
      R(IN, JC-1) = R(IN, JC-1) + DPSI* (1./WWW)
       GO TO 4000
С
 3900 R(IN, JC-1) = R(IN, JC-1) + DPSI + (1, / WWW)
 4000 R(IN+1, JGIP1) = R(IN+1, JCIP1) + DPSI + ( 1. / ZZZ )
 4100 R(IN, JC+1) = R(IN, JC+1) + DPSI + ( 1. / YYY )
      R(IN-1,JCIM1)= R(IN-1,JCIM1) + DPSI + ( 1. / XXX )
 4200 CONTINUE
 4300 CONTINUE
С
      IL M1
                = IL - 1
      DO 4500 II= 2, IL M1
      RESID(II) = 0.
      JJ
                 = 0
      JT B
                = JTHB(II)
      JTL
                = JTHL(II)
С
      DO 4400 JN= JTB, JTL
                = JJ + 1
      JJ.
      IF ( ( ABS (R(II,JJ) ) ) .GT. RESID(II) ) RESID(II)=ABS(R(II,JJ))
 4400 CONTINUE
```

```
4500 CONTINUE
С
     DO 4600 II= 2, ILM1
     IF ( RESID(II) .GT. RESIM ) RESIM = RESID(II)
 4608 CONTINUE
     IF (RESIM.GT.RESI2) STOP
     RESI2=2.0*RESIM
     IF ( RESIM .GT. ACC )
                                     GO TO 4700
     GO TO 4880
С
4700 NUM
          = NUM + 1
     WRITE (6,8001) NUM, RESIM
     RESIM = 0.
     IF (NUM.EQ.50) GO TO 4710
     GO TO 100
4710 CALL PREWRT
     CALL WRTOUT
      GC TC 100
С
 4800 NUM
             = NUM + 1
     WRITE (6,8001) NUM, RESIM
     RESIN
             = 0.
     RETURN
     END
```

```
SUBROUTINE PREWRT
С
          ROUTINE TO CALCULATE OPSIDD, DPSIDU, AND PHI VALUES BEFORE
C
С
               GOING INTO WRTOUT
С
 80 01 FORMAT ( ////* ++++++ VOLUME = *, E12.5 )
C
               ISIL(150), IPI8(150), W(150), X(150), Y(150), Z(150),
      COMMON
               JTHL(150), JTHB(150), PSI(100,100),
     #
     ¥
               RS(100), RP(100), ES1(100), RC(100),
     #
               ED(150), RD(150), BD(150), SIAD(150), MNM, IL, JL, IIB,
               IIE, B, DELTA, RESIM, DPSIP, KK, DEX, ACC, JLE, BN,
               PSIPR, RHO(100,100), G, WDOT, WW, KKL, RHOIN, POIN, HOIN,
     #
               ROIN, VTHIN, VMOIN, PS, RR(150), BZ(150), SIA(150), RT,
     ¥
               INPUF, RRL, ITRIP, PDEL, JOPL
      COMMON / CEA /
               ENC
      COMMON
               /NDG/
               NNDG, LNDG, KNDG, ILNDG, THETHIN, THETHAX, EMIN,
     #
               EMAX, ICNT(99), THETS(100), THETC(100), THETP(100),
     #
     #
               EC1(100), EP2(100), ESS1(100), KNT1, KNT2
С
                = DELTA + 0.5
      HOELTA
      SU M
                = 0.
      ILL
                = IL - 1
                = -( FLOAT ( IFIX ( ENC / DELTA ) ) * DELTA ) - DELTA
      E
С
      00 3000 II= 1, ILL
                = E + DELTA
      Ε
                = JTHB(II)
      JT 8
      JTL
                = JTHL(II)
      JJ
                = 0
С
      00 2900 JN= JTB, JTL
      JJ
                = JJ + 1
С
                = \cos(ASIN(SIA(II)))
 2100 COSA
      THETA
                = FLOAT (JN-1) + DELTA
                                           GO TO 2200
      IF ( II .LE. IIB )
      IF ( JN .EG. JTB )
                                           GO TO 2400
      IF ( JN .EQ. JTL )
                                           GO TO 2600
С
               = DELTA / COSA * DELTA * RR(II) * BZ(II)
      VOLUME
       GO TO 2800
С
 2200 DELT
                = DELTA
                = DELTA
      DELE
                                           DELE = HDELTA
      IF ( II .EQ. 1 )
      IF ( JN .EQ. JTL )
                                           DELT = HDELTA + DELTA + Y(1)
      IF ( JN .EQ. 1 )
                                           DELT = HDELTA
               = DELE / COSA + RR(II) + DELT + BZ(II)
      VOLUME
       GO TO 2800
С
 2300 DELE = DELTA
      IF ( II \cdot EQ. ISIL(1) )
                                           DELE = HDELTA + DELTA + Z(1)
```

```
VOLUME = DELE / COSA * RR(II) * HDELTA * BZ(II)
      GO TO 2800
С
                                          GO TO 2500
2400 IF ( II .GT. IIE )
      EU 1
                = E + HDELTA
                = E - HDELTA
      EL A
      CALL TABE ( EU1, THETU1, ESS1, THETS, 2, 1, NNDG )
      CALL TABL ( EL1, THETL1, ESS1, THETS, 2, 1, NNDG )
С
                = THETA + HJELTA
      THETU2
                = THETA - HDELTA
      THETL2
      CALL TABL ( THETU2, EU2, THETS, ESS1, 2, 1, NNDG )
      CALL TABE ( THETL2, EL2, THETS, ESS1, 2, 1, NNDG )
С
                = AMIN1 (EU1, EU2)
      EULC
                = AMIN1 ( THETU1, THETU2 )
      THETLC
                = ( EULC - EL1 ) / COSA
      EHGT
                = (( THETU2 - THETLC ) + ( THETU2 - THETL1 )) / 2.0
      TL NGTH
                = EHGT + RR(II) + BZ(II) + TLNGTH
      VOLUME
       GO TO 2800
С
 2500 VOLUME = DELTA / COSA * RR(II) * HDELTA * BZ(II)
       GO TO 2800
С
 2600 IF ( II .GT. IIE )
                                          GO TO 2700
                = E + HDELTA
      EU1
                = E - HDELTA
      EL 1
      CALL TABL ( EU1, THETU1, EP2, THETP, 2, 1, LNDG )
      CALL TABE ( EL1, THETL1, EP2, THETP, 2, 1, LNDG )
С
                = THETA + HDELTA
      THETU2
      THETL 2
                = THETA - HDELTA
      CALL TABL ( THETU2, EU2, THETP, EP2, 2, 1, LNDG )
      CALL TABL ( THETL2, EL2, THETP, EP2, 2, 1, LNDG )
C
                = AMAX1 (EL1, EL2)
      EULC
                 = AMAX1 ( THETL1, THETL2 )
      THETLC
                = ( EU1 - EULC ) / COSA
      EHGT
                = (( THETU1 - THETL2 ) + ( THETLC - THETL2 )) / 2.0
      TL NGTH
                 = EHGT + RR(II) + TLNGTH + BZ(II)
      VOLUME
       GO TO 2800
С
                = HDELTA + DELTA + Y(II)
 27 0 0 DELT
                = DELTA / COSA + RR(II) + DELT + BZ(II)
      VOLUME
C
 2800 VOLUME
                = VOLUME * RHO(II,JJ)
                 = SUM + VOLUME
      SUM
 2900 CONTINUE
 3000 CONTINUE
      WRITE (6;8001)
                           SUM
      RETURN
      END
```

```
SUBROUTINE WRTOUT
С
С
          ROUTINE TO PROCESS AND PRINT OUTPUT
C
 8001 \text{ FORMAT} ( 5H \text{ E} = ,F10.4,7H)
                                     I = , I4, 7H R = , F10, 4, 7H
                                                                    B = ,F10.
              SIA = F10.4
     *4,9H
 8002 \text{ FORMAT}(1 \times 6 \text{ MPSI} = F10.4, 10 \text{ M})
                                    THETA = F10.4,8H PHI = F10.4,6H
                                                                          V ¥
     +F10.4,6H U = F10.4)
 8003 FORMAT( # IJK IS GREATER THAN 25 # )
С
                ISIL(150), IPIB(150), W(150), X(150), Y(150), Z(150),
      COMMON
     ¥
                JTHL(150), JTHB(150), PSI(100,100),
     ¥
                RS(100), RP(100), ES1(100), RC(100),
     #
                ED(150), RD(150), BD(150), SIAD(150), MNH, IL, JL, IIB,
                IIE, B, DELTA, RESIM, DPSIP, KK, DEX, ACC, JLE, BN,
     ¥
     #
                PSIPR, RHO(100,100), G, WDOT, WW, KKL, RHOIN, POIN, HOIN,
     ¥
                RCIN, VTHIN, VMOIN, PS, RR(150), BZ(150), SIA(150), RT,
     ¥
                INPUF, RRL, ITRIP, PDEL, JOPL
      COMMON
                /FL T/
                THTA(100)
      COMMON
                / CB A/
     *
                ENC
                /NDG/
      COMMON
     ¥
                NNDG, LNDG, KNDG, ILNDG, THETMIN, THETMAX, EMIN,
                EMAX, ICNT(99), THETS(100), THETC(100), THETP(100),
     ¥
     *
                EC1(100), EP2(100), ESS1(100), KNT1, KNT2
С
С
          ARITHMETIC STATEMENT FUNCTIONS FOR INTERPOLATION
С
                 = ( ( DEX / 3. ) + ( 0.5 * DEX ** 2 ) + ( ( DEX ** 3 ) /
      AA (DEX)
                    6.)) + (-1.)
      BB (DEX)
                 = ( ( 3. * DEX / 2. ) + ( 2. * DEX ** 2 ) + ( ( DEX ** 3
                    ) / 2. ) )
                 = ( 3. * DEX + ( ( 5. * DEX ** 2. ) / 2. ) + ( ( DEX **
      CC (DEX)
                    3. ) / 2. ) ) * ( -1. )
      DD (DE X)
                 = ( 1. + ( 11. * DEX / 6. ) + ( DEX ** 2. ) + ( ( DEX **
                    3.)/6.))
С
                 = -( FLOAT ( IFIX ( ENC / DELTA ) ) * DELTA ) - DELTA
      Ε
      ENIN
                 = E + DELTA
                 = EC1(KNDG)
      ECC1
      THETCC
                 = THETC(KNJG)
      THETPP
                 = THETP(LNDG)
С
      IJKNDG
                 = 160
                 = -1.05 * PSIPR
      SIMIN
                 = 0
      KNT1
      KNT2
                 = 0
      LF ILE
                 = 9
                 = IL -1
      ILL
C
      00 700 II = 1, ILL
                 = E + DELTA
      E
      CALL TABL ( E, RPRNT, ED, RD, 3, 1, MNM )
      CALL TABLE ( E, BPRNT, ED, BD, 3, 1, HNM )
```

```
CALL TABL ( E, STAPRT, ED, STAD, 3, 1, MNN )
С
                = 0
      KKK
                = 0
      LLL
                = JTHB(II)
      JT B
                = JTHL(II)
      JTL
                = 1)
      JJ
                = 0
      MM
С
         500 JN= JTB, JTL
      00
                = II - IPIB(JN) + 1
      IC
                = JJ + 1
      JJ -
                = NM + 1
      MM
      IF ( ( II .LT. IIB ) .OR. ( II .GT. IIE ) ) GO TO 300
                                          GO TO 100
      IF ( JN .EQ. JTB )
       GO TO 300
С
                = ( ( FLOAT(JN-1) ) - W(II) ) * DELTA
  100 THTA(MM)
                = W(II)
      DEX
                = AA(DEX) * PSI(II,JJ+3) + BB(DEX) * PSI(II,JJ+2) +
      RC (HM)
                  CC(DEX) * PSI(II,JJ+1) + DD(DEX) * PSI(II,JJ)
     *
                = MM + 1
      MM
       GO TO 300
С
                = MM + 1
  200 MM
                = ( (FLOAT(JN-1)) + Y(II)) + DELTA
      THTA(MM)
                 = Y(II)
      DE X
                 = AA(DEX) * PSI(II,JJ-3) + BB(DEX) * PSI(II,JJ-2) +
      RC (MH)
                   CC(DEX) * PSI(II,JJ-1) + DD(DEX) * PSI(II,JJ)
       GO TO 400
С
  300 THTA(MM) = ( FLOAT(JN-1) ) * DELTA
               = PSI(II, JJ)
      RC (MM)
                                        GO TO 200
      IF ( JN .EG. JTL )
  400 K
                = MM
  500 CONTINUE
С
                = SIMIN
       PSIP
       JJK
                = 0
С
       DO 600 IJK= 1, IJKNDG
              = PSIP + DPSIP
       PSIP
                                                      GO TO 600
       IF ( PSIP .LT. -0.0001 .AND. E .LT. ECC1 )
                                                         GO TC 700
       IF ( FSIP .GT. PSIPR .AND. E .GT. 0. )
 С
       CALL TABL ( PSIP, THETA, RG, THTA, 3, 1, K )
       IF ( THETA .LT. 0. .OR. THETA .GT. THETPP )
                                                         GO TO 600
       IF ( E .GE. ECC1 .AND. THETA .LT. THETCC )
                                                         GO TO 600
       IF ( E .LE. ESS1(1) .AND. THETA .GT. THETP(1) ) GO TO 600
 С
                                           GO TO 600
       IF ( MOD(IJK,2) .EQ. 0 )
 С
                 = IFIX ( ( PSIP + PSIPR ) / ( DPSIP * 2.0 ) + 9.25 )
       IFILE
       ICNT(IFILE) = ICNT(IFILE) + 1
                                           IFILE = 2
       IF ( IFILE .EQ. 44 )
```

```
CALL ALTFILE ( LFILE, IFILE, NDUM )

LFILE = IFILE

WRITE (IFILE) E, THETA, PSIP

600 CONTINUE

700 CONTINUE

C

C

CALL ALTFILE (LFILE, 9, NDUM )

EMAX = E

CALL PLOTT

KK = 1

RETURN

END
```

•

```
SUBROUTINE PLOTT
С
C
       SUBROUTINE TO PLOT OUTPUT DATA
С
               / PL 1/
      COMMON
               E(200), THETA(200), PSI(200)
      COMMON
                2 NO 67
                NNDG, LNDG, KNDG, ILNDG, THETMIN, THETMAX, EMIN,
     3
               ENAX, ICNT(99), THETS(100), THETC(100), THETP(100),
     #
                EC1(100), EP2(100), ES1(100), KNT1, KNT2
C
               KNTO / 0 /
      DATA
                                           GO TO 100
      IF ( KNTO .NE. 0 )
      CALL INIT 280
      KNTO
                = 1
  100 CONTINUE
C
                 = AMIN1 ( EMIN, ES1(1), EP2(1), EC1(1) )
      ENIN
                 # AMAX1 ( EMAX, ES1(NNDG), EP2(LNDG), EC1(KNDG) )
      EMAX
      THETPP
                 = THETP(1)
      CALL SETUP
С
      00 \ 200 \ I = 1, NNDG
                = THETS(I) + THETPP
      E(I)
  200 E(I+100) = EMAX - ( ES1(I) - EMIN )
          300 I = 1, LNDG
      DO
      THETA(I) = THETP(I) - THETPP
  300 THETA(I+100) = EMAX - ( EP2(I) - EMIN )
      20 400 I = 1, KNOG
                = EMAX - ( EC1(I) - EMIN )
  400 PSI(I)
С
      DO 500 I = 1, 2
      CALL LINES ( E(101), THETS(1), NNDG )
      CALL LINES ( THETA(101), THETP(1), LNDG )
      CALL LINES ( PSI(1), THETC(1), KNDG )
      CALL LINES ( E(101), E(1), NNDG )
      CALL LINES ( THETA(101), THETA(1), LNOG )
      CALL LINE ( E(101), THETPP, EMAX, THETPP )
      CALL LINE ( EMAX, THETFP, EMAX, THETMIN )
      CALL LINE ( EMIN, THETP(LNDG), THETA(LNDG+100), THETP(LNDG) )
      CALL LINE ( EMIN, THETC(KNDG), PSI(KNDG), THETC(KNDG) )
  500 CONTINUE
С
      LFILE
                 = 9
      30 800 T = 9, 99
                 = ICNT(I)
      IJK
      ICNT(I)
                 = 0
                                           GO TO 800
      IF ( IJK .EQ. 0 )
                 = I
      II
                                           II = 2
      IF ( I .EQ. 44 )
      CALL ALTFILE ( LFILE, II, NOUM )
                 = II
      LFILE
      REWIND II
                                           GO TO 800
      IF ( IJK .EQ. 1 )
С
```

```
DO 600 J = 1, IJK

READ (II) E(J), THETA(J), FSI(J)

E(J) = EMAX - (E(J) - EMIN)

600 CONTINUE

REWIND II

C

DO 700 J = 1, 2

CALL LINES (E(1), THETA(1), IJK)

700 CONTINUE

CALL ALTFILE (LFILE, 9, NDUM)

CALL FRAME

RETURN

END
```

SUBROUTINE SETUP

```
С
       SUBROUTINE TO SETUP GRID FOR PLOTS
С
С
               /NDG/
      COMMON
               NNDG, LNDG, KNDG, ILNDG, THETMIN, THETMAX, EMIN,
     #
               ENAX, ICNT(99), THETS(100), THETC(100), THETP(100),
     #
               EC1(100), EP2(100), ES1(100), KNT1, KNT2
     ¥
С
      CALL CHAROPT ( 0, 0, 1, 0, 0 )
      CALL LINEOPT ( 0, 1 )
      CALL ABSBEAM ( .15, .993 )
      CALL ABSVECT ( .15, .214 )
      CALL ABSVECT ( .930, .214 )
С
      CALL LINEOPT ( 0, 0 )
      CALL MAP ( EMIN, EMAX, THETMIN, THETMAX, .15, .930, .214, .993 )
      DO 100 K = 1, 2
      CALL ABSBEAM ( .5, .15 )
      CALL SYMBOL ( 3HES. )
      CALL ABSBEAM ( .05, .6 )
      CALL SYMBOL ( 3HFS. )
      CALL ABSBEAM ( .4, .08 )
  100 CALL SYMBOL ( 27 HCOORDINATES IN E, F PLANES. )
      RETURN
```

4

EN D

APPENDIX F

Input Data Interpolation Program

For all of the turbopump inducers analyzed in this study, blade geometrical data was derived from inducer design drawings. This data is normally tabulated on the drawing for only a few blade sections at a constant distance off the inducer hub. A computer program was written to provide input data for additional blade sections located at a constant percent of blade span. Figure F.1 illustrates this procedure. Sections R_1 and R_2 represent typical blade sections for which blade geometrical data is supplied. This data is linearized to yield associated geometry for blade sections at 10%, 30%, 50%, 70%, and 90% of the blade span, shown as dashed lines in this figure.

Figures F.2 through F.6 show a typical sequence of data manipulation for the J-2 LOX inducer. Figure F.2 is a plot of the tabulated data given on the inducer design drawing (Figure 5.1). This data is normalized to the blade leading edge (Figure F.3), non-dimensionalized (Figure F.4), and linearly interpolated (Figure F.5) to yield the required input data for the five blade sections (Figure F.6). The final form of the data is then punched on computer cards for input to the turbopump cavitation compliance program.

The following pages of this appendix present a listing of the input data interpolation program. The liberal use of comment cards makes the program operation self-explanatory. Sample input/output listings are also provided.

PROGRAM BLADE2(INPUT, OUTPUT, TAPE5=INPUT, TAPE5=OUTPUT, FILMPL, PUNCH) BD2 2 С. PROGRAM TO INFERPOLATE BLADE INPUT DATA FOR TWO SECTIONS 802 4 国家工作 合業日本所以回答「OPA 802 Ê 010EUSION TITL143), FITL218), X(50), Y11(50), Y12(50), Y21(50), Y2002 8 12(30), Y10UM(30), Y20UH(30), Y3DUY(30), Y4DUY(50), X1(50), X2(50),BD2 10 2 TEY(5), XLEOG(5), X33(5,31), YLEDG(5), XT(51), Y(11(51), YT12(51)BD2 12 3, YT21(51), YT22(51), TEP(5,50), RSTREAM(3), XLSQ(3), YLSQ(3), RADBD2 14 4(3), YR1(3), YR2(3), Y1(5,51), Y2(5,51), YCC(51), TPAC(51), AX(51)BD2 16 5, RX(51), RD(51), BD(51), YZER1(51), YSLP1(51), YZER2(51), YSLP2(5BD2 18 611 802 2.0 DEFINITION OF INPUT DATA BD2 22 û e С. CARO 1 TITLE = TITLE COMMON TO ALL CASES (BA1J FORMAT) 3D2 24 CAR9 2 TITLE = FITLE PECULIAR TO EACH DASE (8A10 FORMAT) 802 С. 26 GARS 3 IPJNCH, INTERP (1015 FURMAT) BD2 8.5 С. IPUNCH= FLAG TO CONTROL PUNCHING OF OUTPUT DATA 302 С. 30 INTERP= FLAG TO CONTROL INTERPOLATION OF INPUT DATA С. BD2 32 ALF1, ALF2, FSR, HL, HX (SF10.4 FORMAT) C . CARD 4 BD2 34 = HALF-CONE ANGLE OF HJB ALFI (DEG) 802 36 С. ALF 2 = ANGLE OF BLADE LEADING EDGE LOCUS BD2 3. (DEG) 38 С. FSR. = FEEDLINE UPSTREAM RADIUS (IN)BD2 40 = FORWARD HUB RADIUS (IN) 8 D 2 42 С. HL С. НΧ = HJB EQUIVALENT LENGTH (IN)8D2 44 Ο. CARD 5 S1,32,KSOLFO (5F10.4 FORMAT) 802 46 S1 = LOCATION OF INNERMOST BLADE SECTION 802 Ο. (IN)48 = LOCATION OF OUTERMOST BLADE SECTION 802 S2 (IN)50 С. XSCLFC= FLAG FO CORRECT INPUT DATA IF Z MEASURED 8D2 52 С. PARALLEL TO CENTERLINE (ND) BD2 54 С. CARD 6 С. BNJM, DGINC, ENC, BNC, STWNOM (5F10.4 FORMAT) BD2 56 С. BNUM = NUMBER OF BLADES BD2 58 С. DGINC = NUMBER OF GRID INCREMENTS BD2 6 J Ο. = UPSTREAM EXTENSION OF FLOWFIELD SOLUTION BD2 ENC 62 = DOWNSFREAM EXTENSION OF FLOWFIELD SOLUTION BD2 BNC. 64 Ĉ. STWNOM= NOMINAL WIDTH OF STREAMTUBE BD2 С. 66 CARD I X,Y11,Y12,Y21,Y22 (5F1J.4 FORMAT) 302 ö8 с. READ (5,255) IIT_1 BD2 70 BD2 READ (5,255) TIT_2 72 10 BD2 IF (TITL2.EQ.STOP) GO TO 205 74 802 READ (5,280) IPUNCH, INTERP 76 802 С. READ IN INDUCER GEOMETRY DATA 78 READ (5,260) ALFL, ALF2, FSR, HL, HX 802 8.0 BD2 RAD=57.29578 82 ANGL1 = ALF1/RAD B D 2 84 8D2 ANGL2=ALF2/RAD 86 802 88 [MLTAN=ABS(TAN(ANGL1)) TMLCSN=ABS(COS(ANGL1)) BD2 90 FSL=FSR-HL 802 92 BD2 HI=HX*TMLTAN+HL 94 FST=FSR-HT BD2 96 BD2 READ (5,260) S1,S2,XSOLFC 98 BD2 100 ο. READ IN INDUCER ANALYSIS DATA READ (5,26) BNU4, JGING, ENC, BNC, STWNOM BD2 102 BD2 104 DO 15 I=1,50 READ (5,260) X(I), Y11(I), Y12(I), Y21(I), Y22(I) BD2 106 IF (x(I).LT.0.) 50 TO 20 BD2 1J8 CONTINUE BD2 110 15 20 BD2 112 VPTS = [-1]ALE INPUT COMPLETE - PRODUCE ECHO PRINTOUT BD2 114 Û . ARITE (6,265) TITL1, TIT_2 BD2 116 WRIT: (6,27)) S1,S2 BD2 118

```
204
       WRITE (6,260) (X(I),/11(I),Y12(I),Y21(I),Y22(I),I=1,NPTS)
                                                                                8D2
       IF (XSCLFC.LE.O.) GO TO 30
                                                                                BD2
          CORRECT INPUT DATA FOR Z MEASURED PARALLEL TO CENTERLINE
С.
                                                                                802
       30 25 I=1.NPTS
                                                                                802
       Y11(I)=Y11(I)/TH_C34
                                                                                802
       Y12(I)=Y12(I)/TH_CSN
                                                                                802
       Y21(I) = Y21(I) /TM_CSN
                                                                                802
       Y22(I)=Y22(I)/TH_GSN
                                                                                BD2
25
       CONTINUE
                                                                                802
       ARITE (6,265) TITL1,TITL2
                                                                                8 D 2
       WRITE (6,21J)
                                                                                8 D 2
       WRITE (6,270) S1,52
                                                                                802
       WRITE (6,260) (X(I), Y11(I), Y12(I), Y21(I), Y22(I), I=1, NPTS)
                                                                                802
30
       CONTINUE
                                                                                802
       TP1=X(NPTS)
                                                                                PD2
       IY1=Y12(NPTS)
                                                                                802
       TP2=X(NPTS)
                                                                                BD2
       TY2=Y22(NPTS)
                                                                                802
       WRITE (6,275) TP1, TY1, TP2, TY2
                                                                                802
С.
          ECHO DE INPUT COMPLETE
                                                                                892
С.
                                                                                3 D 2
С.
          LINEARIZE R/Z VERSUS ANGULAR DISPLACEMENT
                                                                                802
       RMAX=FSL/THLCSN
                                                                                802
       RMIN=FST/TMLCSN
                                                                                BD2
       XLSQ(1) = X(1)
                                                                                BD2
       XLSQ(2) = X(NPTS)
                                                                                BD2
       YLSQ(1) = RMAX
                                                                                BD2
       YLSQ(2) = RMIN
                                                                                BD2
       SALL LSQ1 (2,XLSQ,YLSQ,RNAUT,RSLOPE,PE,SRSQ)
                                                                                BD2
С.
          LINEARIZATION COMPLETE *** R(PHI) = RNAUT + RSLOPE*PHI
                                                                                BD2
С.
                                                                                BD2
С.
          PLOT INPUT DATA NON-NORMALIZED
                                                                                SD8
       SALL PLOTRI (X, Y11, Y12, Y21, Y22, NPTS, TITL1, TITL2, 1)
                                                                                BD2
С.
                                                                                BD2
С.
          NORMALIZE ALL INPUT TO TRAILING EDGE COURDINATES
                                                                                802
       00 35 I=1,NPTS
                                                                                BD2
       JEND=NPTS+1-I
                                                                                8 D 2
       X1(I) = X(NPTS) - X(JEND)
                                                                                802
       Y10U4(I)=Y12(NPTS)-Y11(JEND)
                                                                                BD2
       Y20U4(I)=Y12(NPTS)-Y12(JEND)
                                                                                302
       Y3DUY(I) = Y22(NPTS) - Y21(JEND)
                                                                                BD2
       Y40UM(I)=Y22(NPTS)-Y22(JEND)
                                                                                BD2
35
       CONTINUE
                                                                                SC 8
       00 40 I=1,NPTS
                                                                                802
       X(I) = X1(I)
                                                                                8D2
       Y11(I) = Y1DUM(I)
                                                                                BD2
      Y12(I) = Y2DJM(I)
                                                                                SCB
      Y21(I) = Y3DUM(I)
                                                                                802
      Y22(I) = Y40UM(I)
                                                                               202
40
      CONTINUE
                                                                               802
          WRITE NORMALIZED INPUT DATA
С.
                                                                               BD2
      WRITE (6,265) TITL1, TITL2
                                                                               BD2
      WRITE (6,215)
                                                                               BD2
      WRITE (6,260) (X(I),Y11(I),Y12(I),Y21(I),Y22(I),I=1,NPTS)
                                                                               BD2
С.
          NORMALIZATION COMPLETE
                                                                               BDS
С.
                                                                               BD2
С.
          PLOT NORMALIZED INPUT DATA
                                                                               208
      CALL PLOTR1 (X, ¥11, ¥12, ¥21, ¥22, NPTS, TITL1, TITL2, 2)
                                                                               ED2
      IF (INTERP.LE.0) GD TD 150
                                                                               802
С.
                                                                               802
```

| | | 205 | |
|-------------|---|-------------|------------|
| З. | NON-DIMENSIONALIZE ALL INPUT DATA WITH RESPECT TO CHORD LENGTH | | |
| | DO 45 I=2,NPTS | BD2 | |
| | IF (Y11(I).EQ.Y12(I)) GD TD 50 | | 244 |
| 45 | CONTINUE | 905 | |
| 50 | NPAIRS1=I | 802 | |
| 20 | | 802 | |
| | 00 55 I=2,NPTS | | |
| | IF (Y21(I).EQ.Y22(I)) GO TO 50 | | 252 |
| 55 | CONTINUE | 802 | |
| 60 | NPAIRS2=I | 802 | |
| | DO 65 I=1,NPTS | 602 | S |
| | X1(I)=X(I)/X(NPAIRS1) | 802 | 24.5 |
| | X2(I) = X(I) / X(NPAIRS2) | BDZ | 262 |
| | IF (X2(I).GT.1.) X2(I)=1.0 | 802 | 264 |
| 65 | CONTINUE | 802 | 266 |
| Ο. | STURE LEADING EDGE AXIAL COORDINATES FOR LATER CURVE FIT | BD2 | 268 |
| | YLDG1=Y11(NPAIRS1) | BDS | |
| | $Y \perp DG2 = Y 21 (NPAIRS2)$ | BD2 | |
| С. | NON-DIMENSIONALIZE ALL INPUT DATA WITH RESPECT TO AXIAL COORD | BD2 | |
| U • | DO 70 I=1,NPTS | 802 | |
| | · | | |
| | $Y_{11}(I) = Y_{11}(I) / Y_{11}(N^2 A I R S_1)$ | | 278 290 |
| | Y12(I) = Y12(I) / Y12(NPAIRS1) | 902 | |
| | Y21(I) = Y21(I) / Y21(NPAIRS2) | BD2 | |
| | Y22(I)=Y22(I)/Y22(NPAIRS2) | 802 | |
| | IF (Y21(I)+GT+1+) Y21(I)=1+ | 602 | |
| | IF (Y22(I).GT.1.) Y22(I)=1. | 8 D2 | 288 |
| 70 | CONTINUE | BDS | 293 |
| С. | WRITE NON-DIMENSIONALIZED INPUT DATA | BD2 | 292 |
| | WRITE (6,265) TITL1,TITL2 | BD2 | 294 |
| | WRITE (6,220) | 802 | 296 |
| | WRITE (6,225) (X1(I), Y11(I), Y12(I), X2(I), Y21(I), Y22(I), I=1, NPTS) | BDZ | |
| С. | PLOT NON-DIMENSIONALIZED DATA | BD2 | |
| | CALL PLOTR2 (X1, V11, V12, X2, V21, V22, NPAIRS1, NPAIRS2, TITL1, TITL2, 1) | | |
| С. | NON-DIMENSIONALIZATION IS NOW COMPLETE | BD2 | |
| | MON-DIBENDIONALISHINA IQ NON OQUUECIC | | 336 |
| С. | | 8D2 | |
| С. | BEGIN INTERPOLATION SCHEME | | |
| | YT11(1)=Y11(1) | BD2 | |
| | YT12(1)=Y12(1) | | 312 |
| | YT21(1) = Y21(1) | 802 | |
| | YT22(1)=Y22(1) | | 316 |
| | NSEX=51 | | 318 |
| | D0 95 J=2,NSEX | 6D2 | |
| | XINC=J-1 | 9D2 | 322 |
| | XT(J)=.0+.02*XINC | 802 | 324 |
| | DO 75 I=1,NPAIRSL | 8 D 2 | 326 |
| | IF (X1(I).GE.XT(J)) GJ TO 80 | 802 | 328 |
| 75 | CONTINUE | 802 | |
| 8.5 | YI11(J) = Y11(I-1) + (Y11(I) + Y11(I-1)) + (XT(J) - X1(I-1)) / (X1(I) - X1(I-1)) | | |
| | $Y\Gamma_{12}(J) = Y_{12}(I-1) + (Y_{12}(I) - Y_{12}(I-1)) + (XT(J) - X1(I-1)) / (X1(I) - X1(I-1))$ | | |
| | DO 85 $I \neq 1$, NPAIRS? | 802 | |
| | IF (X2(I).GE.XT(J)) 30 TO 90 | 302 | |
| 45 | CONTINUE | BD2 | |
| 85 | YT21(J)=Y21(I-1)+{Y21(I)-Y21(I-1))*(XT(J)-X2(I-1))/(X2(I)-X2(I-1)) | | |
| 90 | | | |
| a .: | YT22(J) = Y22(I-1) + IY22(I) - Y22(I-1)) + (XT(J) - X2(I-1)) / (X2(I) - X2(I-1)) | | |
| 95 | CONTINUE | 802 | |
| | WRITE (6,265) TIFL1,FITL2 | BD2 | |
| | WRITE (6,230) | 8D2 | |
| | WRITE (6,260) (XF(I),YT11(I),YT12(I),YT21(I),YT22(I),I=1,NSEX) | 802 | |
| | CALL PLOTR2 (XT, TT11, YT12, XT, YT21, YT22, NSEX, NSEX, TITL1, TITL2, 2) | | 354 |
| | 00 105 I=1,NSEX | 802 | 356 |
| | RSTREAM(1)=RNAUT+RSLOPE+XT(I)+X(NPAIRS1) | 602 | 353 |
| | | | |

| 206 | | | |
|------------|---|-------|------------|
| 200 | RSTREAM(2)=RNAUT+RSLOPE*XT(I)*X(NPAIRS2) | | 763 |
| | RAD(1) = S1/RSTREAM(1) | | 36J 362 |
| | RAD(2) = S2/RSTREAM(2) | | 364 |
| | YLSQ(1) = YT11(1) | | 366 |
| | YLSQ(2)=YT21(I) | | 368 |
| | CALL LSQ1 (2, RAD, YLS1, YZER1, YSLP1, PE, SRSQ) | | 370 |
| | YLSQ(1) = YT12(I) | | 372 |
| | YLSQ(2) = YT22(1) | | 374 |
| | CALL LSQ1 (2,RAD, 1_SQ, YZER2, YSLP2, PE, SRSQ) | | 376 |
| | 00 100 J=1,5 | | 378 |
| | RINC=J-1 | | 380 |
| | RADIJS=.1J+.20*RINC | | 382 |
| | Y1(J,I)=YZER1+YSLP1*RADIUS | | 384 |
| | Y2(J,I)=YZER2+YSLP2*RADIUS | | 386 |
| 100 | CONTINUE | | 388 |
| 1] 5 | CONTINUE | | 390 |
| | WRITE (6,265) TIFL1,FITL2 | | 392 |
| | WRITE (6,235) | | 394 |
| | DD 110 I=1,NSEX | | 396 |
| | WRIIE (6,243) (XT(I),Y1(J,I),Y2(J,I),J=1,5) | | 398 |
| 110 | CONTINUE | 8.02 | 400 |
| С. | PLOT NON-DIMENSIONALIZED DATA FOR INTERPOLATED BLADE SECTIONS | | 402 |
| С. | | | 402 |
| _ | CALL PLOTR3 (XT,Y1,Y2,NSEX,TITL1,TITL2,1) | | 406 |
| C. | LSR FIT TO LEADING EDGE COORDINATES | | 408 |
| С. | | | 410 |
| | YLSQ(1) = X(NPAIRS1) | | 412 |
| | YLSQ(2) = X(NPAIRS2) | | 414 |
| | RSTREAM(1) = RNAUT+RSLOPE*X(NPAIRS1) | | 416 |
| | RSTREAM(2)=RNAJTERSLOPE*X(NPAIRS2) | | 418 |
| | XLSQ(1) = S1/RSTREAM(1) | | 42 J |
| | XLSQ(2) = S2/RSTREAM(2) | | 422 |
| | GALL LSQ1 (2, XLSQ, YLSQ, YLEZ, YLES, PE, SRSQ) | | 424 |
| | 00 115 J=1,5 | | 426 |
| | | 8D2 | 428 |
| | XINC=.10+.20*XM | 8 D 2 | 430 |
| 442 | XLEDG(J)=YLEZ+YLES*XINC | | 432 |
| 115 C. | CONTINUE | BD2 | 434 |
| U • | LSQ FIT TO LEADING EDGE AXIAL COORDINATES YLSQ(1)=YLDG1 | BD2 | 436 |
| | YLSQ(2)=YLDG2 | | 438 |
| | | | 440 |
| | CALL LSQ1 (2,XLSQ,YLSQ,YLDZ,YLDS,PE,SRSQ) D0 120 J=1,5 | | 442 |
| | XM=J-1 | | 444 |
| | XINC=.10+.20*XM | | 446 |
| | ATHC-TTATTCATTCATTCATTCATTCATTCATTCATTCATTC | | 448 |
| 120 | CONTINUE | | 450 |
| C. | COMPUTE INTERPOLATED BLADE SECTIONS | | 452 |
| | $\frac{30}{130} J=1.5$ | | 454 |
| | DO 125 I=1,NSEX | | 456 |
| | XUS(J,I)=XF(I) *XLEDG(J) | | 458 |
| 125 | CONTINUE | BD2 | |
| 130 | CONTINUE | BD2 | |
| | 00 140 J=1,5 | BD2 | |
| | DO 135 I=1,NSEX | BD2 | |
| | Y1(J, I) = Y1(J, I) + YLEOG(J) | BD2 | |
| | Y2(J, I) = Y2(J, I) + YLEDG(J) | BD2 | |
| 135 | CONTINUÉ | BD2 | |
| 140 | CONFINUE | BD2 | |
| - | WRITE (6,255) TIFL1,TITL2 | BD2 | |
| | | 802 | 478 |

```
207
     WRITE (0,245)
                                                                              BD2 480
     00 145 I=1,NSEX
                                                                              BD2 482
     WRITE (6,250) (XBS(J,I),Y1(J,I),Y2(J,I),J=1,5)
                                                                              802 484
     COMELARIE
4 2
                                                                              8 n 2 -
                                                                                  486
        PLUT NORMALIZED INTERPOLATED DATA
e.
                                                                              PD2 488
     CALL PLOTR4 (XBS, Y1, Y2, NSEX, TITL1, TITL2, 1)
                                                                              802 490
50
     CONTINUE
                                                                              802 492
     IF (IPUNCHLEGIJ) GO TO 10
                                                                              802 494
     NSEX=NPTS
                                                                              BD2 496
        SET UP STREAMFUBE COORDINATES
                                                                              BD2 498
a
$
                                                                              802 500
        LINEARIZE RAZ VERSUS AXIAL DISPLACEMENT
                                                                              302 532
     X \subseteq SQ(1) = 0.
                                                                              BD2 504
     XLSQ(2) = HX
                                                                              8D2 506
     YLSQ(1) = FST
                                                                              802 538
     YLSQ(2) =FSU
                                                                              BD2 510
     GALL LSQ1 (2,XLSQ,YLSQ,RAXZ,RAXS,PE,SRSQ)
                                                                              BD2 512
        LINEARIZATION COMPLETE *** R(AX)=RAXZ+RAXS*AX
                                                                              BD2 514
٠
٠
                                                                              BD2 516
        SET UP AX MATRIX OF AXIAL DISPLACEMENTS
.
                                                                              BD2 518
                   (-33 PRONT TO +66 PRONT SECTIONAL SPAN)
                                                                              BD2 520
     AX(1)=-HX/3.
                                                                              BD2 522
     AX(NSEX)=5.*HX/3.
                                                                              BD2 524
     XNPT=NSEX-1
                                                                              802 526
     AXDE_T=(AX(NSEX)-AX(1))/(XNPT)
                                                                              BD2 528
     00 155 I=2.NSEX
                                                                              BD2 530
     AX(I) = AX(I-1) + AXDELT
                                                                              BD2 532
55
     CONFINUE
                                                                              BD2 534
                                                                              BD2 536
.
        COMPUTE RX MATRIX OF FREESTREAM RADIAL DIMENSIONS AS F(AX)
.
                                                                              BD2 538
     00 160 I=1,NSEX
                                                                              802 540
     RX(I)=RAXZ+RAXS*AX(I)
                                                                              802 542
     CONTINUE
50
                                                                              BD2 544
.
                                                                              BD2 546
        PUNCH INPUT FOR CAVITATION PROGRAM *** Y1=PRESSURE, Y2=SUCTION
                                                                              802 548
     BRAD=2.*FSR
                                                                              BD2 550
     NDUM=1
                                                                              BD2 552
     BANG=6.28318/BNU4
                                                                              BD2 554
     PUNCH255,TITL1
                                                                              802 556
     PUNCH255,TITL2
                                                                              BD2 558
     KSTPRI=5
                                                                              BD2 560
     IF (INTERP.GT.0) GO TO 170
                                                                              BD2 562
     KSTPRI=2
                                                                              B02 564
     K=1
                                                                              802 566
     03 165 I=1,NP1S
                                                                              8D2 568
     Y1(K, 1) = Y11(1)
                                                                              802 570
     Y2(K, I) = Y12(I)
                                                                              BD2 572
     XBS(K,I) = X(I)
                                                                              802 574
55
     CONTINUE
                                                                              BD2 576
     K=2
                                                                              BD2 578
     00 173 Ist, NPTS
                                                                              B02 580
     Y1(K, I) = Y21(I)
                                                                              BD2 582
     Y2(K,I) =<22(I)
                                                                              802 584
' D
     CONTINUE
                                                                              BD2 586
     JO 200 MaiskSIPRI
                                                                              BD2 588
     INC=10+(K-1)*20
                                                                              BD2 590
     PUNGH235,1NC
                                                                              BD2 592
     PUNCHESSI, NSEX, NSEX, NSEX, NDUM, NDUM, NSEX, BANG, DGINC, BRAD, ENC, BNC
                                                                              BD2 594
        PUNCH PRESSURE R, Z COORDINATES
                                                                              BD2 596
     PUNCH295, (Y1(K,I),I=1,NSEX)
                                                                              BD2 598
```

| 2.09 | | | |
|--------------|--|--------------|---|
| 208 C. | PUNCH SUCTION R,Z COORDINATES | 8D2 | r |
| | PJNCH295, (Y2(K,I),I=1,NSEX) | BD2 | |
| С. | COMPUTE CHORD COURDINATES | | |
| •• | DU 175 I=1,NSEX | BD2 | |
| | Y = (Y + (K, 1) + Y + (K, 1)) / 2. | 802 | |
| 475 | | 802 | |
| 175 | CONFINUE | 802 | |
| С. | PUNCH CHORD R,Z COORDINATES | 8 02 | |
| | PJNCH295, (YCC(I), I=1, NSEX) | 802 | |
| С. | PUNCH SUCTION THEFA COORDINATES | 802 | |
| _ | PUNCH295, (XBS(K, I), I=1, NSEX) | 802 | |
| C. | COMPUTE PRESSURE ANGULAR COORDINATES | 8D2 | e |
| | DD 180 I=1,NSEX | 802 | 6 |
| | TPAC(I) = XBS(K, I) + 35J. / BNUM | 802 | Ē |
| 180 | CONTINUE | 802 | 6 |
| G. | PUNCH PRESSURE THEFA COORDINATES | BD2 | € |
| | PUNCH295, (TPAC(I), I=1, NSEX) | SDS | E |
| Ο. | PUNCH CHORD FHEFA COORDINATES | 8 D 2 | ٤ |
| | PUNCH295,(XBS(K,I),I=1,NSEX) | 802 | ć |
| С. | COMPUTE RD MATRIX OF STREAMTUBE RADII FOR PRONT BLADE SECTION | BD2 | |
| | XJ=K-1 | 802 | |
| | XINC=.10+.20*XJ | 802 | |
| | DO 185 I=1,NSEX | 802 | |
| | RD(I)=RX(I)*XING+H_+(HX+AX(I))*TMLTAN | B D 2 | |
| 185 | CONTINUE | BD2 | |
| C. | COMPUTE BD(I) = STREAMTUBE WIUTH AS F(AX) | 802 | |
| | NMID=NSEX/2 | BD2 | |
| | RMID=RX(NMID) | 802 | |
| | DO 190 I=1,NSEX | 802 | |
| | BD(I)=STWNOM*RX(I)/R4ID | BD2 | |
| 190 | CONTINUE | BDZ | |
| 2 7 4 | DYBETA=RD(1)-RD(NSEX) | BD2 | |
| | DXBEFA=2.*HX | 802 | |
| | BETA=ATAN2(DYBETA, DXBETA) | 8D2 | |
| | SIAD=SIN(BETA) | BD2 | |
| | DO 195 I=1,NSEX | | |
| | PUNCH3JJ,RD(I),BJ(I),SIAD,AX(I) | B 02 | |
| 195 | CONTINUE | 802 | |
| 200 | CONTINUE | 8D2 | |
| 200 | GO TO 1J | 6D2 | |
| 235 | STOP | BDZ | |
| C 2 3 9 | | 802 | |
| 210 | EDDNAT (/)VEAUCODDECTED INDUT DATA FOD 7 M(A) DEC DADAL TO A | BD2 | £ |
| 610 | FORMAT (72X51HCORRECTED INPUT DATA FOR Z MEASURED PARALLEL TO C7L. 1) | | |
| 215 | | BD2 | |
| 610 | FORMAT (2X4JHNORMALIZED INPUT DATA FOR SECTIONAL DATA,/6X2HX ,2(8) | | |
| 7 7 0 | 12HY1,8X2HY2)/) | BD2 | |
| 220 | FORMAT (2X78HNON-DIMENSIONALIZED INPUT DATA NORMALIZED TO TRAILING | | |
| 22- | 1 EDGE FOR SECTIONAL INPUT, /2(8X2HX ,8X2HY1,8X2HY2)/) | BD2 | |
| 225 | FORMAT (5F10.4) | BD2 | |
| 230 | FORMAT (2X45HINCREMENTAL PERCENT CHORD DERIVED DATA POINTS, /8X2HX | | |
| | 1,2(8x2HY1,8x2HY2)/) | 6 D 2 | £ |
| 235 | FORMAT (2X48HBLADE SECTIONAL DATA EXTRAPOLATED FOR 5 SECTIONS, /5(: | | |
| | 1X2HXT, 5X2HY1, 6X2HY2)/) | BD2 | |
| 240 | FORMAT (15F8.4) | BD2 | 7 |
| 245 | FORMAT (2X53HNORMALIZED INPUT DATA FOR INTERPOLATED BLADE SECTIONS | SBD2 | 7 |
| | 1,/5(6X2HX ,6X2HY1,5X2HY2)/) | 802 | 7 |
| 250 | FORMAT (5(F8.2,2F8.4)) | 8 D 2 | 7 |
| 255 | FORMAT (6A10) | B D 2 | |
| 260 | FORMAT (5F10.4) | 8D2 | |
| 205 | FORMAT (1H1,8A1J//BA1J//) | 802 | 7 |
| 270 | FORMAT (4X53HINPJT DATA FOR CONTINUOUS BLADE SECTIONS AT LOCATIONS | | |
| | | | |

| | TENTOYOHKT — ELDEDETENYOUVE — ELDEDENOYOHI HETENOVEHLETOKEHLEN I — — — — | 72 0 |
|-----|--|-------------|
| 175 | FORMAT (4x31HINPUT TRAILING EDGE COORDINATES, /F10.4.F15.4./F10.4.2802 | 120 |
| | 1CX+F15-4) BD2 | 724 |
| '8D | FORMAT (1015) 802 | 726 |
| 285 | THE THE THE TAR THE TAR START FEATING AT 17 181000000000000000000000000000000000 | 728 |
| | | 730 |
| 290 | 80.2 | 732 |
| 295 | | 734 |
| 300 | | 736 |
| 500 | | 740* |

| | SUBROUTINE LSQ1 (N.X.Y.A.B.PE.SRSQ) | L 91 | 1 |
|-----|---|-------|------|
| | LINEAR LEAST SQUARES SUBROUTINE FIT | L01 | 2 |
| | R A ZEHNLENOVEMBER 1968 | L 01 | 3 |
| | EQUATION Y = A+BX | L 0 1 | 4 |
| | PROGRAM VARIABLES | L Q1 | 5 |
| | N NUMBER OF PAIRS OF DATA POINTS (X+Y) | L Q 1 | 6 |
| | X ARRAY OF INDEPENDENT VARIABLES | L 01 | 7 |
| | Y ARRAY OF DEPENDENT VARIABLES | L Q 1 | 8 |
| | A, B CONSTANTS OF STANDARD FIRST ORDER EQUATION | L 91 | 9 |
| | PE PROBABLE ERROR OF FIT OF DATA TO CURVE | LQ1 | 10 |
| | SRSQ SUM OF THE RESIDUALS SQUARED | L Q1 | 11 |
| | DIMENSION X(1), Y(1) | LQ1 | 12 |
| | IF (N.LE.1) GO TO 15 | L Q 1 | 13 |
| | | LQ1 | 14 |
| | SX=0. | L Q1 | 15 |
| | SXSQ=0. | LQ1 | 16 |
| | SY=0. | L Q1 | 17 |
| | SXY=D. | LQ1 | 18 |
| | SRSQ=D. | L 0 1 | 19 |
| | DO 5 I=1.N | LQ1 | 20 |
| | SY=SY+Y(I) | LQI | 21 |
| | SXY=SXY+X(I)+Y(I) | LQ1 | 22 |
| | SX=SX+X(I) | L 01 | 23 |
| | SXSQ=SXSQ+X(I)++2 | LQ1 | 24 |
| | D=N+SXSQ+SX+SX A=(SXSQ+SY-SX+SXY)/D | L Q 1 | 25 |
| | A=(SxSQ+SY+SX+SX)/D B=(N+SXY+SX+SX)/D | L01 | 26 |
| | | L Q 1 | 27 |
| • • | DO 10 I=1+N SRSQ=SRSQ+(Y(I)-A-B+X(I))++2 | LQ1 | 28 |
| 10 | | L Q1 | 29 |
| | PE=.675+SQRT(SRSQ/(N-2)) | LQ1 | 30 |
| | RETURN | L 01 | 31 |
| | ERROR MESSHOE PROPORTION | L01 | 32 |
| | WRITE (6+20) N | L 01 | 33 |
| | RETURN | LQI | 34 |
| | FORMAT (1X36HERROR IN INPUT TO LSQ1 N INPUT AS .IS) | LQI | 35 |
| | FURHAL (INSCREAMON IN IN TO COUL | LQ1 | 36 * |
| | END LSQ1 | | |

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210 SUBROUTINE PLOTR1(X, Y11, Y12, Y21, Y22, N, TITL1, TITL2, IS) PLT1 | DIMENSION X(1), Y11(1), Y12(1), Y21(1), Y22(1), PLT1 | \$TITL1(8) +TITL2(8) +T(1(9) +TL2(9) PLT1 DATA 111191, 112(9)/285.,285./ PLT1 : DATA XSYHB. YSYHE/IDHTHEIA \$...IDHAXIAL Z \$./ PL T1 CALL INIT280 PLT1 | DO 1 1=1.8 PL T1 TL1(I)=TITL1(I) PLT1 | 1 TL2(I) = TITL2(I)PLT1 : XMIN=0. PLT1 YMIN=D. PL T1 XHAX=X(1) PLT1 YMAX=Y12(1) PLT1 DO 2 I=2+N PLT1 IF(X(I).GT.XMAX) MMAX=X(I) PL T1 IF(Y12(I).GT.YMAX) YMAX=Y12(I) PLT1 2 CONTINUE PL T1 CALL MAPS (XMIN+XMAX+YMIN+YMAX+-1+-9+-15+-9) PLT1 CALL LINEOPT(C+1) PL T1 CALL CHAROPT(0,C,1,0,0) PLT1 CALL ABSBEAM(.01,.98) PLT1 CALL SYMBOL(TL1) PLT1 CALL ABSBEAM(.01..94) PLT1 CALL SYMBOL(TL2) PLT1 CALL ABSBEAM(.5..07) PLT1 CALL SYMBOL(XSYMB) PET1 CALL ABSEEAM (.10+.02) PL T1 IF (IS.EQ.1) CALL SYMBOL (36HECHO PLOT OF INPT DATA SECTIONS \$.)PLT1 IF (IS.EG.2) CALL SYMBOL (36HDATA NORMALIZED TO TRING EDGE \$. JPL T1 CALL CHAROPT(0,0,1,1,0) PLT1 CALL ABSBEAM(.01,.5) PL T1 CALL SYMBOL(YSYMB) PLT1 NST=N-1 PLT1 DO 45 I=1.NST PLT1 $IF((Y11(I), EQ, O_{*}), OR, (Y11(I+1), EQ, O_{*})) GO TO 44$ PL T1 IF(Y11(I).EQ.Y12(I)) GO TO 44 PLT1 CALL LINE(X(I)+Y11(I)+X(I+1)+Y11(I+1)) PL T1 CALL LINE(X(I)+ Y12(I)+X(I+1)+Y12(I+1)) PLT1 44 CONTINUE PLT1 **45 CONTINUE** PLT1 DO 47 T=1.NST PL T1 IF((Y21(I).EQ. 0.). OR.(Y21(I+1).EQ.0.)) GO TO 45 PLT1 IF(Y21(I).EQ.Y22(1)) GO TO 46 PL T1 CALL LINE(X(I), Y21(I), X(I+1), Y21(I+1)) PLT1 CALL LINE(X(I), Y22(I), X(I+1), Y22(I+1)) PL 11 **46 CONTINUE** PLT1 47 CONTINUE PLT1 CALL FRAME PLT1 RETURN PL T1 END PLT1

| SUBROUTINE PLOTR2(X1+Y11+Y12+X2+Y21+Y22+N1+N2+T1+T2+IS) PLT2 DIMENSION X1(1)+Y11(1)+Y12(1)+X2(1)+Y21(1)+Y22(1)+T1(8)+T2(8)+ PLT2 \$111(9)+T(2(9) PLT2 PLT2 \$111(9)+T(2(9) PLT3 PLT3 \$111(9)+T(2(9) PLT3 PLT3 | | 12 13 14 15 |
|--|------------------|----------------------|
| DIMENSION X1(1)+Y11(1)+Y12(1)+X2(1)+Y21(1)+Y22(1)+T1(8)+T2(8)+ \$11(9)+T(2(9) DATA 1L1(9)+TL2(9)/2H\$++2H\$+/ PLT3 | | 3 4 15 |
| \$111(9) + T(2(9)) PLT DATA TL1(9) + T(2(9)) / 2H\$ + 2H\$ + / PLT | 0 0 0 0 | 4 |
| DATA (1119). TL2(9)/2H\$.,2H\$./ PLT | 2 0 2 0 | 5 |
| | 0 0 | |
| DATA XSYMB.YSYMB/10HTHETA \$10HAXIAL 2 \$ PLT | 2 0 | 6 |
| CALL INIT280 PLT2 | | ~ |
| D(-1 151+B PLT. | 0 | 17 |
| TL1(I)=T1(I) PLT2 | | 8 |
| 1 YL2(I)=12(I) PLT | 2 0 | 19 |
| WHITE PLT: PLT: | | |
| VMTNUTT. PLT | | - |
| YMAY:X1(1) PLT | | |
| YKAX=Y12(1) PLT | | |
| DO 2 I=2+N1 PLT. | | |
| IF(X1(I).GT.XMAX) XMAX=X1(I) PLT | | |
| IF (Y12(I).GT.YMAX) YMAX=Y12(I) PLT | | |
| 2 CONTINUE PLT | | |
| CALL MAPS (XMIN, XMAX, YMIN, YMAX, 1, 9, 15, 9) PLT | | |
| CALL LINEOPT(C+1) | | |
| CALL CHAROPT(0,0,1,0,0) PLT | | |
| CALL ABSBEAM(.01+.98) PLT | | |
| CALL STROULIELD | | |
| CALL ABSDEAM(SUITEST) | | |
| | | |
| | | |
| UALL SIMBULIXSIMDI | | |
| CALL ABSBEAH (.10,.02) IF (IS.EQ.1) CALL SYMBOL (36HNON-DIMEN DATA FOR INPUT DATA PTS \$.)PLT | | |
| IF (IS.EQ.2) CALL SYMBOL (36HNON-DIMEN DATA FOR 51 DATA POINTS \$.)PLT | 2 2 | 29 |
| CALL CHAROPT(0+0+1+1+0) | 2 3 | 30 |
| CALL ADSBEAM(.01+.5) | 2 3 | 31 |
| CALL SYMBOL(YSYMB) | 2 3 | 32 |
| $PLT \qquad \qquad PLT$ | | |
| $PLT \qquad PLT$ | | |
| CALL 1 TNES(Y2+Y21+N2) PLT | | |
| PLT = PLT | | |
| CALL FRAME PLI | | |
| PETHON PLT | | |
| END PLT | ۷. | 22* |

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SUBROUTINE PLOIR3 (X.Y1.Y2.N.TITL1.TITL2.IS)
                                                                         PLT3
   DIMENSION X(1)+Y1(5+1)+Y2(5+1)+XP(51)+YP1(51)+YP2(51)+
                                                                         PLT3
  $TITL1(8), TITL2(8), TL1(9), TL2(9)
                                                                         PLT3
   DATA TL1(9) + TL2(9) / 2H$ + 2H$ - /
                                                                         PL 13
   DATA XSYMB, YSYMB/10HTHETA S. . 10HAXIAL Z S./
                                                                         PLT3
   CALL INIT280
                                                                         PLT3
   DO 1 I=1.8
                                                                         PLT3
   TL1(I)=TITL1(I)
                                                                         PLT3
 1 TL2(I)=TITL2(I)
                                                                         PLT3
   XMIN=0.
                                                                         PLT3
   YMIN=0.
                                                                         PLT3
   XMAX=X(1)
                                                                         PLT3
   YMAX=Y1(1+1)
                                                                         PLT3
   D0 2 I=1.N
                                                                         PLT3
   IF(X(I).GT.XMAX) XMAX=X(I)
                                                                         PLT3
   IF(Y1(1,I).GT.YMAX) YMAX=Y1(1,I)
                                                                         PLT3
 2 CONTINUE
                                                                         PLT3
   CALL MAPS (XMIN+XMAX+YMIN/+YMAX++1++9++15++9)
                                                                         PL T3
   CALL LINEOPT(0.1)
                                                                         PLT3
   CALL CHAROPT(0.0.1.0.0)
                                                                         PLT3
   CALL ABSBEAM(.01+.98)
                                                                         PLT3
   CALL SYMBOL(TL1)
                                                                         PLT3
   CALL ABSBEAM(.01.94)
                                                                         PLT3
   CALL SYMBOL(TL2)
                                                                         PL13
   CALL ABSBEAM(.5..07)
                                                                         PLT3
   CALL SYMBOL (XSYMB)
                                                                         PLT3
   CALL ABSBEAM (.10,.02)
                                                                         PLT3
   IF (IS.EQ.1) CALL SYMBOL (36HNON-DIMEN DATA FOR INTERP SECTIONS .)PLT3
   IF (IS.EQ.2) CALL SYMBOL (36H
                                                                      $.)PLT3
   CALL CHAROPT(0,0,1,1,C)
                                                                         PLT3
   CALL ABSBEAM(.01..5)
                                                                         PLT3
   CALL SYMBOL(YSYMB)
                                                                         PLT3
   DO 60 J=1.5
                                                                         PLT3
   DO 44 I=1.N
                                                                         PLT3
   XP(I) = X(I)
                                                                         PLT3
   YP1(I)=Y1(J,I)
                                                                         PL13
   YP2(I)=Y2(J,I)
                                                                        PLT3
44 CONTINUE
                                                                        PLT3
   CALL LINES(XP, YP1, N)
                                                                        PLT3
   CALL LINES(XP+YP2+N)
                                                                        PL13
60 CONTINUE
                                                                        PLT3
   CALL FRAME
                                                                        PLT3
   RETURN
                                                                        PLT3
   END
                                                                        PL 13
```

| | | 213 | |
|-------|---|--------------|-------|
| | SUBROUTINE PLOTR4 (X+Y1+Y2+N+TITL1+TITL2+IS) | PLT4 | 01 |
| | DIMENSION X(5+1)+Y1(5+1)+Y2(5+1)+XP(51)+YP1(51)+YP2(51)+ | PLT4 | |
| 4 | 5TITL1(8),TITL2(8),TL1(9),TL2(9) | PLT4 | |
| • | DATA TL1(9)+TL2(9)/2H%++2H8+/ | FLIG | |
| | DATA XSYMB.YSYMB/10HTHETA SICHAXIAL Z S./ | PLT4 | 65 |
| | CALL INIT280 | PLT4 | 06 |
| | DO 1 I=1+8 | PLT4 | |
| | TL1(I)=TITL1(I) | PLT4 | |
| 1 | TL2(I)=TITL2(I) | PLT4 | |
| | XMIN=0. | PL14 PL14 | |
| | YMIN=0. | PLT4 | |
| | XMAX=X(1+1) YMAX=Y1(1+1) | PLT4 | |
| | $DO 2 T=1 \cdot N$ | PLT4 | |
| | IF(X(1+I).GT.XMAX) XMAX=X(1+I) | PLT4 | 15 |
| | IF(Y1(1+I).GT.YMAX) YMAX=Y1(1+I) | PLT4 | |
| 2 | CONTINUE | PLT4 | |
| | CALL MAPG (XMIN+XMAX+YMIN+YMAX++1++9++15++9) | PLT4 | |
| | CALL LINEOPT(0.1) | PLT4 PLT4 | |
| | CALL CHAROPT(0,0,1,0,0) | PL14 PL14 | |
| | CALL ABSBEAM(=01+=98) CALL SYMBOL(TL1) | PL14 | |
| | CALL ABSBEAM(.0194) | PLT4 | |
| | CALL SYMBOL(TL2) | PLT4 | 24 |
| | CALL ABSBEAM(.5+.07) | PLT4 | |
| | CALL SYMBOL(XSYMB) | PLT4 | |
| | CALL ABSBEAM (.10,.02) | PLT4 | |
| | IF (IS.EQ.1) CALL SYMBOL (36HNRMLZD DATA FOR 5 INTRPLTD SECTS | PLT4 | |
| | CALL CHAROPT(0+0+1+1+0) CALL ABSBEAM(+01++5) | PLT4 | |
| | CALL SYMBOL(YSYMB) | PLT4 | |
| | DO 60 J=1+5 | PLT4 | 32 |
| | DO 44 I=1.N | PLT4 | |
| | XP(I)=X(J+I) | PLT4 | |
| | YP1(I)=Y1(J,I) | PLT4 PLT4 | |
| 11 11 | YP2(I)=Y2(J.I) CONTINUI | PLT4 | |
| 44 | JL=1 | PLT4 | |
| 45 | K=JL+1 | PLT4 | |
| | IF((YP1(K)-YP1(JL)).GT.D.) GO TO 48 | PLT4 | 40 |
| | JL=JL+1 | PLT4 | |
| | GO TO 45 . | PLT4 | |
| 48 | CONTINUE | PLT4 PLT4 | |
| | NP=N IF(JL.Eg.1) GO TO 50 | PLT4 | |
| 49 | IK=I+JL-1 | PLT4 | |
| | XP(I)=XP(IK) | PLT4 | 47 |
| | YP1(I)=YP1(IK) | PLT4 | |
| | YP2(I)=YP2(IK) | PLT4 | |
| | NP=I | PLT4 | |
| | | PLT4 PLT4 | |
| E 0 | IF(IK.LT.N) GO TO 49 Continue | PL 14 | |
| ЪU | CALL LINES(XP+YP1+NP) | PLT4 | |
| | CALL LINES(XP+YPZ+NP) | PLT4 | |
| 60 | CONTINUE | PLT4 | |
| - | CALL FRAME | PLT4 | |
| | RETURN | PLT4 | |
| | END | PLT4 | 2,7,4 |

TURBOPUMP INDUCER CAVITATION ANALYSIS FOR NASS-26266 F/0, 17 JAN 1972

F-1 LOX, 2 INPUT BLADE DECTIONS INTERPOLATED TO 10,30,50,70,90 PRONT SECTION

| INPUT DA | TA FOR CONT R1 = . | TNUOUS B | | DNS AT LOCATIONS |
|-------------------------------|-----------------------|--------------------------|------------------|------------------|
| PHI | Y1 - • | ¥2 | 92 = 4 Y1 | +•500 ¥2 |
| 13.0000 15.0000 | • 5250 • 6293 | • 6250 • 6 953 | 0 • 0 • | 0 • 0 • |
| 20.0000 25.0000 | •6905 •7549 | .8514 1.0031 | 0 • 0 • | 0.0. |
| 30.0000 | •8224 | 1.1502 | 0• | 0. |
| 35.0000 40.0000 | •3333 •9578 | 1•2927 1•4307 | 0 . 0 . | 0 • 0 • |
| 45.0000 50.0000 | 1.0460 1.1283 | 1.5640 1.6927 | 0 . 0 . | 0. 0. |
| 55.0000 | 1.2143 | 1.8166 | 0. | 0. |
| 65.0000 | 1.3058 1.4015 | 2.0505 | | 0 • 0 • |
| 70.0000 75.0000 | 1.5022 1.6081 | | 1.8300 1.8806 | 1.8300 1.9973 |
| 80.0000 85.0000 | 1.7158 | 2.3760 | 1.9489 | 2.1462 |
| 90.0000 | 1.9350 | | 2.1181 | 2•2841 2•4110 |
| | 2.0445 2.1543 | | 2.2196 2.3289 | 2•5269 2•6364 |
| 105.0000 | 2.2543 2.5963 | | 2.4397 | 2.7462 |
| 135 • 0000 | 2.9309 | 3.5838 | 3.1037 | |
| 150.0000 165.0000 | 3.2582 3.6083 | 3•9197 4•2583 | | 3•7476 4•0870 |
| 180.0000 195.0000 | 3.)513 4.2972 | 4•6000 4•9447 | 4.1220 | 4.4293 |
| 210.0000 | 4.6463 | 5,2926 | 4.8158 | 5.1231 |
| | 4•9986 5•3543 | | 5•1676 5•5228 | |
| 255.0000 2 70. 0000 | 5.7135 6.J765 | 5.3569 5.7190 | 5.8816 6.2441 | |
| 285.0000 | 6 • 4435 | 7.0853 | 6.6108 | 6.9180 |
| 300.0009 305.0000 | 6.3147 6.3433 | 7.4545 7.5701 | 6.9817 7.1063 | 7•2890 7•4136 |
| | 7.0811 7.2286 | 7.6779 7.7778 | 7.2320 7.3694 | 7•5379 7•6508 |
| 320.0000 | 7.3700 | 7.8699 | 7.5100 | 7.7493 |
| 330.0000 | 7.5150 7.6350 | 8.0150 | 7.6350 7.7600 | 7•8550 7•9500 |
| | 7.8500 8.0500 | 8.0750 8.1250 | 7.9000 8.0600 | 8.0300 8.1150 |
| INPUT TRA | ILING EDGE | COORDINA | | O • T T > O |
| 340.0000 340.0000 | 8.129 | 9 U | 8.1 | 150 |

TURGORIME INDUCER CAVITATION ANALYSIS FOR NAS6-26266 F/O+ 17 JAN 1972 1 LOX+ 7 IMPUT BLADE SECTIONS INTERPOLATED TO 10+30+50+70+90 PRENT SECTIONS IMPORT MATA FOR SECTION AT THE PERCENT RADIAL

| 11221 | | 5 F.) | | : Stat1105 | | | | | | |
|--------------------------|----------------------|----------------------------------|--|--|---------------------------------------|--------------|---------|---|----------|---------|
| ÷ (| | 51 | 1 | 1 | 1.1144 | 44.304 | 18 15.0 | 1008 1 | •3000 | 1.0000 |
| .176 | | 747 | | 761 | . <u>95</u>] | 1.142 | 1.317 | 1.482 | 1.647 | 1.810 |
| .973 | | 135 | | 35 2.456 | | | | 3,090 | | 3 4 0 3 |
| | | | | | | | | | | |
| .559 | | 113 | á a Al | | | | 4.479 | 4.631 | | 4.932 |
| .331 | S. | 231 | î | 9 5.528 | 3 7.675 | 5.922 | 5.969 | 5.11 5 | 6.261 | 6.406 |
| .591 | ĩ | 693 | 1 . P | ng Ginn. | 7.060 | 7.178 | 7.279 | 7.374 | 7.464 | 7.549 |
| | • | U 1. | | | · · · · · · · · · · · · · · · · · · · | | 16412 | 8 8 64 8 3 | 13701 | 10010 |
| 450 Q | | | | | | | | | | |
| P | • | 8.5.0 | • 17 | ie .249 | .371 | .503 | •653 | .823 | .983 | 1.145 |
| , 307 | 1. | 439 | 1.51 | 15 1.731 | 1.348 | 2.106 | 2.263 | 2.420 | 2.576 | 2.731 |
| .837 | | 940 | 5.1 | | | 3.651 | 3.802 | 3.952 | 4.102 | 4.252 |
| | | | | | | | | | | |
| ,400 | | 54C | H. 51 | | | | 5.231 | 5.420 | 3.571 | 5.715 |
| , 353 | ε. | 0 fi 1 | () | i 6 - 0 - 253 | 0.462 | 6.632 | 6.812 | 6.999 | 7.193 | 7.395 |
| .673 | | | | | | | | | | |
| .031 | | 285 | • 31 | .90. | | .825 | .987 | 1.151 | 1.315 | 1.479 |
| | | | | | | 2.440 | 2.598 | 2.755 | 2.912 | 3.067 |
| ,G43 | | a 92 | | | | | | | | |
| .273 | 3. | 377 | 3.5. | (1 J.CA) | 4 3.337 | 3,969 | 4.140 | 4.292 | 4.442 | 4.592 |
| ,741 | 4. | 3 90 | 5.3. | 5.179 | . 5.333 | 5.479 | 5.625 | 5.771 | 5.916 | 6.061 |
| ,284 | | 347 | 6.4 | | | 6.905 | 7.045 | 7.185 | 7.329 | 7.472 |
| | () 4 | . 1 | 0.01 | | | 0.00 | 1.40.10 | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | | |
| .603 | | | | | | | | | | |
| | Γ. | 643 | 13.2 | s5 1 0+920 | | 33.214 | | | | 59.785 |
| . 427 | 73. | 075 | 73.7. | .3 36.351 | 5 92.993 | 99.641 | 105.284 | 112.927 | 113.569 | 126.212 |
| 855 | 130. | 499 | 146.1 | 48 152.78 | 3 159.426 | 156.068 | 172.711 | 179.354 | 185.997 | 192.639 |
| .232 | | | 212.5 | | | | | 245.781 | | |
| | | | | | | | | | | |
| | 272. | 352 | 276.9 | 05 285+635 | 3 252.281 | 238.923 | 305.560 | 312.209 | 210-021 | 325.494 |
| .137 | | | | | | | | | | |
| 010 | 125. | 647 | 133-2 | 15 139.020 | 3 146.571 | 153.214 | 159.856 | 166.493 | 173.142 | 179.785 |
| .427 | | | | 2223.35 | | | | | | |
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| 292 | 325. | 025 | 337.5 | 18 339.21: | 345.953 | 352.435 | 359.139 | 365.731 | 372.424 | 379.067 |
| 710 | 392 | 75.2 | 703.3 | 35 405.03. | 9 412.281 | 413.923 | 425.566 | 432.209 | 438.851 | 445.494 |
| 137 | 0.24. | . | e | | | | | | | |
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| 427 | | . 07 G | | | 1 85.903 | | | | | |
| 855 | 139. | 4 2 8 | 146.1 | 10 152.78 | 3 150.426 | 166.065 | 172.711 | 173.354 | 185.997 | 192.639 |
| 232 | 205- | 325 | 212.5 | 59 213.21: | 0.005.453 | 232.406 | 239.139 | 245.761 | 252.424 | 259.057 |
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| 35+ | UD 2 | . 131 | 1-01 1 | . 3701-01 | 2.3335-01 | | | | | |
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| 60+ 20+ 90+ 00+ | 60 ? 00 ? 00 ? | • 275 • 231 • 317 • 344 | 0 = 0 1 1 1 = 0 1 1 5 = 0 1 1 - 3 1 1 | •0736-01 •3720-01 •3736-01 •3736-01 | 2.5095+13 2.0775+80 1.775+80 | | | | | |
| 60+ 20+ 90+ 00+ | 60 ? 00 ? 00 ? | • 275 • 231 • 317 • 344 | 0 = 0 1 1 1 = 0 1 1 5 = 0 1 1 - 3 1 1 | •0736-01 •3730-01 •3730-01 | 2.5095+13 2.0775+80 1.775+80 | | | | | |

| 2.9032+30 | 2.4385-31 | 1.9792-01 | 4.2038+00 |
|---------------|-----------|-----------|-----------|
| 2.8445+60 | 2.4690-61 | 1.4790-31 | 4.5170+00 |
| 2.7855+30 | 2.5362-01 | 1.3792-81 | |
| 2.7265+00 | | | 4.3235+00 |
| | 2.531E-01 | 1.6795-01 | 5.1338+60 |
| 2.667 2 + 0 0 | 2.5622-01 | 1.3732-01 | 5.4418+00 |
| 2.6085+60 | 2.5942-01 | 1.07BE-U1 | 5.7495+00 |
| 2.5491+80 | 2.5252-01 | 1.3731-01 | 6.057E+00 |
| 2.4902+00 | 2.6565-01 | 1.879E-01 | G.J65E+00 |
| 2.431_+00 | 2.6376-01 | 1.8795-31 | 5.6730+01 |
| 2.372E+00 | 2.7195-01 | 1.8798-01 | 6.9818+00 |
| 2.3141+00 | 7.7502-01 | 1.3732-01 | 7.2096+00 |
| 2.2555+60 | 2.731E-01 | 1.8790-01 | 7.5976+00 |
| 2.1952+00 | 2.8128-31 | 1.9792-31 | |
| 2.1375+00 | | | 7.9352+73 |
| | 2.8442-01 | 1.6791-01 | 8.213E+00 |
| 2.3793+00 | 3.8752-31 | 1.8731-01 | 9.521E+00 |
| 2.0195+00 | 2.90CE-01 | 1.879E-01 | 8.82SE+00 |
| 1.9603+30 | 2.337E-01 | 1.3730-01 | 3.1375+00 |
| 1.9015+00 | 2.9698-01 | 1.8795-01 | 0.4455+00 |
| 1.3425+00 | 3.0005-01 | 1.3702-31 | 3.7535+02 |
| 1.7835+60 | 3.0316-01 | 1.8706-01 | 1.508[+01 |
| 1.7242+30 | 3.3628-01 | 1.3702-31 | 1.037E+01 |
| 1.6652+00 | 3.0946-01 | 1.5702-01 | 1.008E+01 |
| 1.6072+00 | 3.1252-01 | 1.3701-01 | 1.099E+01 |
| 1.5485+60 | 3.1562-01 | 1.8796-01 | 1.125E+01 |
| 1.4895+00 | 3.1976-01 | | |
| | | 1.8792-31 | 1.16JE+01 |
| 1.430E+60 | 3.2196-01 | 1.8732-01 | 1.1916+01 |
| 1.3712+00 | 3.2502-01 | 1.3797-01 | 1.2228+01 |
| 1.312E+00 | 3.2810-01 | 1.8791-01 | 1.2536+01 |
| 1.2535+00 | 3.3128-01 | 1.3702-01 | 1.2815+91 |

÷.

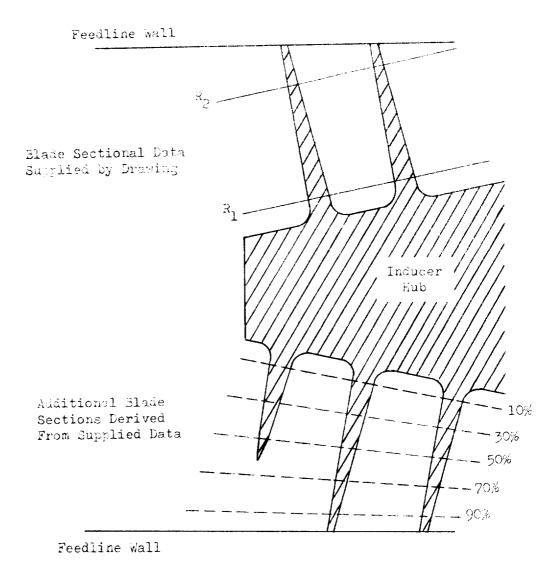
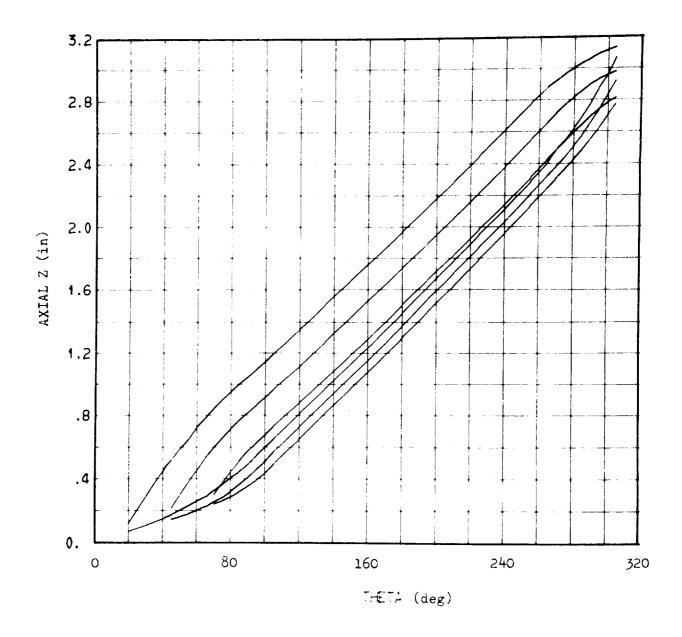


Figure F.1 Typical Inducer Showing Blade Sections



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Figure F.2 Input Blade Sectional Data

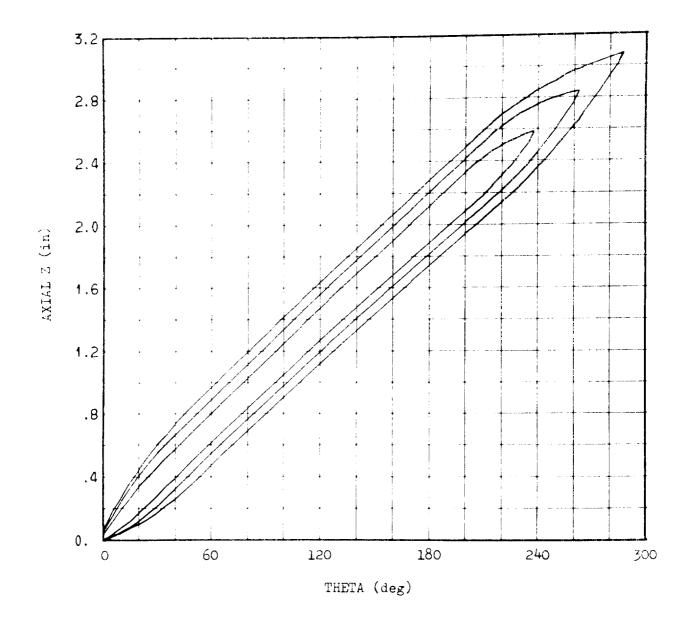


Figure F.3 Input Data Normalized To Trailing Edge

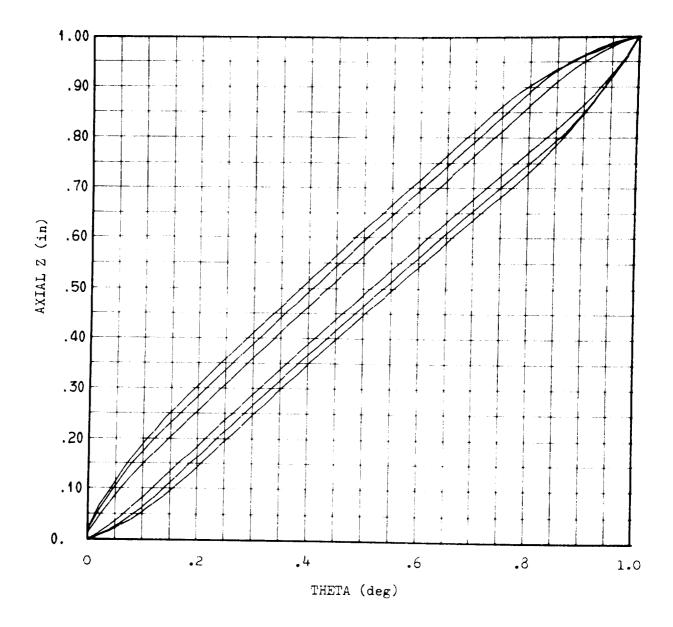


Figure F.4 Non-Dimensionalized Input Data

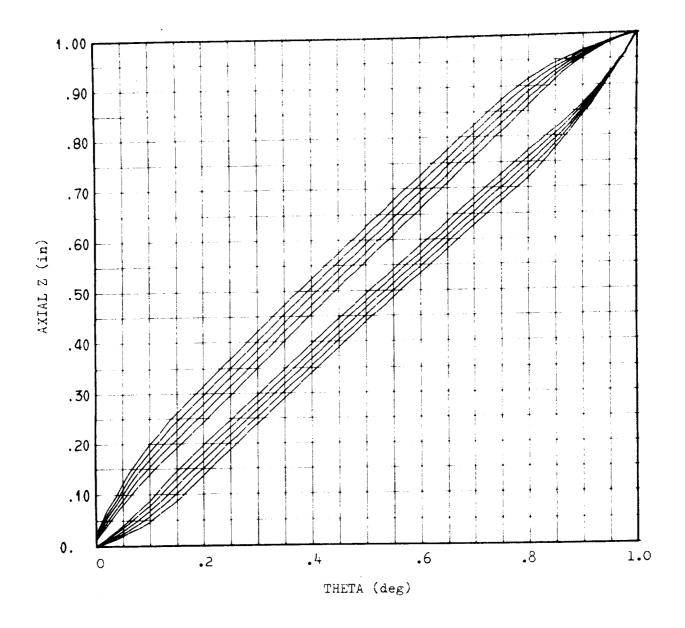


Figure F.5 Non-Dimensionalized Data For 5 Blade Sections

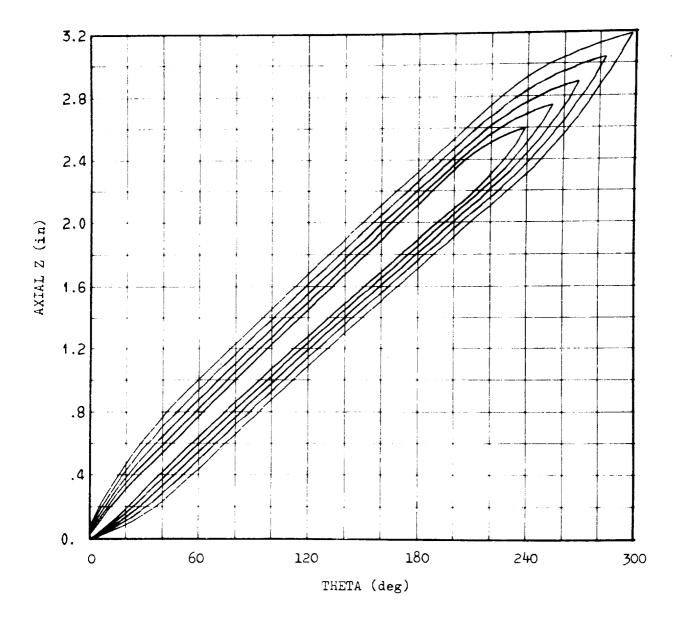


Figure F.6 J-2 LOX Data For 5 Blade Sections Normalized To Trailing Edge