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FINAL REPORT

Contract NAS 9-8869

"Supporting Studies for the Coronagraph Contamination Experiment"

Period: September 1, 1968 to February 28, 1971

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## A. INTRODUCTION

In accordance with the aims specified in the contract, the following tasks were completed by the Contractor in the allotted time period (September 1, 1968, to February 28, 1971):

(1) Calculation of Mie Scattering Functions.

(a) Computation of individual particle scattering functions.

These calculations were done for a range in particle size and a range in the wavelength of incident light. In particular, computations were completed for a  $15\text{\AA}$  particle and for particles subjected to incident light of ultraviolet wavelengths as specified in the contract. A list of computed individual particle scattering functions is given in Appendix A. (Here  $\lambda$  is the wavelength of incident light,  $\alpha$  is  $2\pi$  x the ratio of particle size to the wavelength of incident light.)

(b) Computation of Mie Scattering Functions for a Mixture of Particles.

These have been done for a range in  $\alpha$  of 2 to 240 (as specified in the contract) and for a number of other particle distributions. They are listed in Appendix B.

The calculations cited in (a) and (b) necessitated an assessment as to demands on computer memory, storage and computational time. Though some of the calculations were carried out on a Sigma 7, the vast majority were done on the Univac 1108. A duplicate copy of the appropriate deck written on Fortran 5 can be made available upon request.

- (2) Calculations of Contaminant Atmospheres for Gemini, Apollo and SKYLAB.

These have involved assumptions as to the leakage rates for the respective vehicles and, thus, of the mass column density of the atmospheres surrounding them. Atmospheres for these vehicles have been computed for the two cases specified in the contract; namely,

- (a) a uniform particle size distribution.
- (b) a particle distribution in which size varies as  $r^{-3}$ .

Results of these computations are presented in the body of this report.

#### B. MIE SCATTERING FUNCTION CALCULATIONS

During the contract period, the relative Mie scattering functions,  $\sigma(\theta)$  where  $\theta$  is the scattering angle, were computed for spherical particles having an index of refraction  $m$  and a size distribution  $n(r) \propto r^{-k}$ ,  $r$  being particle size, and  $k$  the distribution function. In the case where  $k=0$ , of course, all particles are of the same size. Results of the calculations of scattering functions for an individual scattering particle are presented first, followed by scattering functions for a distribution of particles of varying size.

- (1) Individual Scattering Functions.

The evaluation of the scattering function involves a series expression consisting of Riccati-Bessel functions, which may have a complex argument, and derivatives of Legendre polynomials. (We have compiled and printed out tables of Riccati-Bessel functions though in our calculation of the scattering function, these are not printed out separately.)

The convergence of the series requires a number of terms slightly greater than  $\alpha$ . This results in computational time increasing rapidly with particle size.

Now, contributions to the contamination atmosphere may be either controlled or continuous. Continuous contributions give rise to scattering by a column of various sized particles. Controlled events such as waste dumps or thruster firings, however, result in light being scattered by individual large particles. Thus, for the spacecraft contamination problem, scattering functions appropriate to scattering by individual spherical ice particles have been calculated. The range in particle size considered is  $15\text{\AA}$  to 1 cm and the wavelength of incident light ranges from  $1000\text{\AA}$  to  $5300\text{\AA}$ .

Figure 1 shows the scattering curve for a  $15\text{\AA}$  particle with an index of refraction  $m = 1.33$  subject to incident light of  $5300\text{\AA}$  (representative of visible light). The ordinate is the log of the scattering function and the abscissa the scattering angle.  $\sigma_1$  is the scattering function for the component of the incident plane wave having its electric vector perpendicular to the plane of vision and  $\sigma_2$  that for the electric vector parallel to the plane of vision.  $\bar{\sigma}$  is the average of the two. Figure 2 is the scattering function for a  $15\text{\AA}$  particle for incident light of  $1200\text{\AA}$ , which is in the vacuum ultraviolet near the Lyman  $\alpha$  line. The index of refraction of ice at this wavelength is complex and equal to  $1.333 - 0.4414 i$ . Note that for both wavelengths, the curves are smooth and  $\sigma_2$  has a pronounced minimum at  $90^\circ$ . This means, of course, that strong polarization occurs at this angle.

Figure 3 gives the scattering curves for a  $1\mu$  size particle for incident light of  $5300\text{\AA}$ , represented by the solid line, and of  $2500\text{\AA}$ , represented by the dashed line. The two curves are similar, consist of many maxima and minima, and differ markedly from those for  $15\text{\AA}$ . For small scattering angles,  $\theta < 10^\circ$ , the values of the scattering function at the two wavelengths differ significantly, but for larger scattering angles, the scattering functions have approximately the same value. The curve for a  $1\mu$  particle at  $1200\text{\AA}$  is shown in Figure 4. Here the index of refraction is complex and the curve differs from those at  $5300\text{\AA}$  and  $2500\text{\AA}$  in that it damps out at about  $90^\circ$ . Figure 4 illustrates a portion of the scattering curve,  $\sigma_1$ , for a  $1000\mu$  particle for incident light of  $5300\text{\AA}$ . The interval of scattering angle shown is  $140^\circ$  to  $140.2^\circ$ . To obtain the exact curve for this size particle, increments in theta must be of the order of 0.002. With such increments, or even smaller ones as for the case of a 1 cm particle where  $\Delta\theta = 0.0002$  is required, machine time becomes prohibitive. Consequently for the larger particles, 10 or more microns, an averaging or sampling technique was devised and the value of the scattering function computed at selected values of the scattering angle. The procedure used was to compute the scattering function at certain specified intervals in theta. Then, at each of these values the scattering function was calculated at a selected number of adjacent angles and the average scattering function computed for the proscribed range in scattering angle. Figure 5 compares the actual and sampled values of  $\bar{\sigma}$  for a  $10\mu$  particle at  $5300\text{\AA}$ . The solid line is for the sampled values, and the x's the actual values as taken

from the detailed scattering curve. The agreement is quite good.

Figure 6 shows the sampled curve for a 100 $\mu$  particle for incident light of 2500 $\text{\AA}$ . The many maxima and minima of the detailed curve have been smoothed out, but the essential shape of the curve has been retained. There are strong secondary maxima at about 120° and 140°. The latter is typical of ice particles. As the next figure (Figure 6) indicates, when the index of refraction becomes complex, as it does for ice at  $\lambda=1200\text{\AA}$ , the scattering curve exhibits a substantially different behavior. The curves in this figure are for a 10 $\mu$  particle.  $\sigma_1$  no longer has a pronounced maximum at 140°, but increases slowly to a maximum at 100°.  $\sigma_2$  has a rather broad maximum from 60° to 90°.

(2) Mie Scattering Functions for Particles Heterogeneous in Size.

The relative Mie scattering functions,  $\sigma'(\theta)$ , for spherical particles having an index of refraction  $m$  and following a size distribution  $n(r) \propto r^{-k}$  were computed. The total scattering function is related to the relative scattering function by

$$\sigma(\theta) = C \int_{\alpha_{\min}}^{\alpha_{\max}} [i_1(\alpha, \theta) + i_2(\alpha, \theta)] \alpha^{-k} d\alpha$$

where  $C$  is normalizing factor and  $i_1$  and  $i_2$  are the individual particle scattering functions discussed in section (1) above.

Figure 7 shows the relative scattering function for a distribution of 12 to 120 in  $\alpha$  with  $m = 1.33$  and  $k$ , the distribution function, equal to 2.5. Increments in alpha,  $\Delta\alpha$ , equal 0.10.

For  $\lambda = 5300 \text{ \AA}$ , this range in  $\alpha$  corresponds to a particle size range of 1 to  $10\mu$ . This particle size interval is an appropriate selection for the spacecraft contamination problem. For particles of size much smaller than  $1\mu$ , the scattering approaches Rayleigh scattering and particles much larger than  $10\mu$  tend to scatter as random individuals and would not appreciably contribute to the general background radiance. Note that the many maxima and minima of the individual scattering functions have been smoothed out leaving a prominent maximum at  $140^\circ$ .

Figure 8 shows the relative scattering function for the same  $k$  and  $m$ , but for a particle distribution function in alpha of 12 to 240. That is,  $r$  ranges from 1 to  $20\mu$  for a wavelength of  $5300 \text{ \AA}$ .

Though the calculations presented are for ice particles, the program is written in a general form and will accommodate any  $m$  or  $\alpha$  within machine capacity.

### C. CONTAMINANT ATMOSPHERE CALCULATIONS

The quantity of interest to be calculated is the radiance of the contaminant cloud,  $B$ . If light scattering is considered to be done by a column of particles, either of uniform size or varying in size, the radiance of the cloud in terms of the Sun's mean surface brightness,  $B_\odot$ , is

$$B/\overline{B}_\odot \approx \Omega_\odot \sigma(\epsilon)M_s$$

where  $\Omega_0$  is the solid angle subtended by the Sun at the spacecraft,  $\sigma(\epsilon)$  is the mass scattering coefficient ( $\epsilon$  is the elongation), and  $M_s$  is the mass column density.

Assuming that a particle of radius  $r$  leaves the spacecraft radially with a velocity  $v_0$ , an expression for the mass loss rate  $dm/dt$  can be derived. Since at the altitudes of interest the most effective mechanism of particle removal is aerodynamic drag, and since even this mechanism is relatively unimportant, the column of material extends out to a distance  $R_1$  from the spacecraft of radius  $R_0$  (where  $R_1 > R_0$ ). If we represent the Gemini and Apollo spacecraft by a sphere of radius  $R_0$  and assume that there is a uniform space density of particles surrounding these spacecraft, then the column mass density of material,  $M_s$ , is

$$M_s = \frac{1}{4\pi R_0 v_0} [dm/dt]_{H_2O} \quad \text{gm/cm}^2$$

The ATM (or Skylab) configuration must be treated in a slightly different manner since it resembles a cylinder of radius  $R_0$  and length  $L$ . If it is assumed that the amount of material outgassed at the ends of the cylinder is small compared to the amount outgassed along its length, then the column mass density associated with ATM can be found using an analysis similar to that used for the spheres of Gemini and Apollo. For ATM

$$M_s = \frac{1}{2\pi L v_0} [dm/dt]_{H_2O} \ln R_1/R_0 \quad \text{gm/cm}^2,$$



where  $R_0$  is the radius of the S-IV B stage and  $L$  is approximately  $3 \times 10^3$  cm.

The total continuous leakage rates as well as the value of  $R_0$  and that of the mass column density for Gemini 3 and 11, Apollo and the ATM cluster are presented in Table I. The leakage rates for the Gemini spacecraft were obtained from the Cape Kennedy Archives and represent the maximum and minimum rates for the Gemini vehicles as experimentally determined prior to the launch of each vehicle. The values adopted for Apollo and the ATM cluster are estimates obtained from the Crew Systems Division of the Manned Spacecraft Center. Of interest, though, is not the total leakage rate but that for water vapor. The percentage water vapor can be estimated from the known temperature and relative humidity of the cabin atmosphere--about 293°K and 60% respectively. In computing the mass column density of particles it was assumed that all of the water vapor leaking out of the spacecraft emerges as ice particles or forms ice particles shortly after exhaust. In order to estimate the velocity of the escaping material, conditions in and around the spacecraft must be examined. Inside the vehicle, gas is under 1/3 atmosphere, while outside a near vacuum exists. Gas flow through leaks in the walls of the spacecraft can be considered to resemble flow through a supersonic wind tunnel. Such an analysis gives for the lower limit for the exhaust velocity that of the speed of sound at the cabin temperature,  $3.3 \times 10^4$  cm/sec. This value was adopted for the computations presented in this report.

It may be that not all the escaping water will condense into micron sized particles but that a large percentage of the resultant particles will be Angstrom sized. Also, the assumption of a smooth distribution of particle radii [ $n(r) = r^{-k}$ ] may not represent the actual situation at all. Some supersonic wind tunnel experiments with humid water, for example, suggest that the ice particles formed in the expansion would be uniform in size and of the order of  $15 \text{ \AA}$ . Figure 9 shows how the radiance of a cloud of  $15 \text{ \AA}$  particles having an index of refraction of 1.33 varies with distance from the Sun for incident light of  $5300 \text{ \AA}$ . The ordinate is the radiance in units of the mean solar radiance and the abscissa is the elongation. The solid line is the  $15 \text{ \AA}$  curve and the dashed line the radiance curve for the outer corona and the zodiacal light as determined by Blackwell and Weinberg, respectively (see references). The distribution function is, of course, equal to zero. As is to be expected, such a cloud would not be very bright and would not hamper coronal or zodiacal light observations.

Figure 10 shows the radiance curves for a cloud of  $10 \mu$  and a cloud of  $100 \mu$  particles surrounding the ATM for light of  $5300 \text{ \AA}$ . The solid line is the  $10 \mu$  curve, the dashed line the  $100 \mu$  curve and the long followed by a short dashed line the zodiacal light. Note that the curve for the  $10 \mu$  particles falls below that for the zodiacal light for small elongations,  $\epsilon \leq 20^\circ$ , where it starts to exceed the brightness of the zodiacal light and continues to do so to about  $60^\circ$  elongation. It then falls well below the zodiacal light except for a small

range in elongation around  $140^\circ$ . The  $100\mu$  curve stays well below that for the zodiacal light except for a narrow range in elongation around  $140^\circ$ .

It is of interest to ascertain the effect of the debris in the ultraviolet. Figure 11 shows the curves for the intensity of scattered light, expressed in Rayleighs, due to a  $10\mu$  and a  $100\mu$  cloud surrounding ATM. Again, the  $10\mu$  cloud is brighter than the  $100\mu$  cloud.

Figure 12 shows the radiance curves for two different types of particle distributions. The radiance of a debris cloud of  $1\mu$  particles surrounding the ATM is given by the dashed line and that of a cloud composed of particles ranging in size from  $0.2$  to  $20\mu$  and having a distribution of 2.5 by the solid line. In both cases an index of refraction equal to 1.33 was assumed. The  $1\mu$  cloud is brighter than the zodiacal light for all elongations larger than about  $5^\circ$ . The situation is even worse for the mixture of particle sizes. Here the radiance curve is above that for the zodiacal light for all elongations and is of the order of  $10^{-9}$  to  $2.4 \times 10^{-12} \bar{B}_\odot$  for all angles larger than  $10^\circ$ , making daylight observations of the zodiacal light impossible.

It is of interest to see how the radiance curve is affected when the scattered earthlight is taken into account. Figure 13 shows the radiance of a debris cloud surrounding Gemini 11 with and without the earthlight contribution. Calculations for scattered earthlight were carried out in this case for the

spacecraft located over the terminator. For elongations less than about  $20^\circ$ , the contribution of scattered earthlight is not important. In the elongation interval  $40^\circ$  to  $180^\circ$ , scattered earthlight sets a background brightness of about  $10^{-10} \bar{B}_\odot$ . Disregarding the angular interval of backscattered earthlight, the background radiance for GT-11 would be about  $10^{-12} \bar{B}_\odot$  for this same range in elongation. The debris cloud both in this figure and in the next was assumed to be composed of particles having a size range of 0.2 to  $10\mu$ , with a distribution function of 3 and an index of refraction of 1.30.

Figure 14 shows the calculation for Apollo and ATM. This figure shows quite graphically that daylight observations will probably not be feasible for ATM (Skylab) unless stringent precautions are taken about waste dumps, thruster firings, cabin leaks, etc. Again, though, the assumptions that have been made must be stressed: the leakage rates are uncertain, the exact size distribution and state of the debris is uncertain, the ejection velocity is uncertain.

The computer program for the calculation of the contaminant atmospheres is written in the format--constant x scattering function x mass column density--and so may be used for other particle distributions and other mass column densities than specified above.

#### D. PUBLICATIONS

Several publications have resulted from the work carried

out under this contract. These have been reported in (and copies of the publications attached to) the monthly progress reports.

References

1. D. E. Blackwell, Mon. Nat. R. Astr. Soc. 115, 629 (1955).
2. N. S. Kovar, "Theory of Light Scattering by Manned Spacecraft Atmospheres," invited paper presented at Symposium for Optical Contamination in Space, August 1969.
3. N. S. Kovar, R. P. Kovar and G. P. Bonner, Planet Space Sci. 17, 143 (1968).
4. R. P. Kovar, "Light Scattering by Large Ice Particles," paper presented at Symposium for Optical Contamination in Space, August 1969.
5. G. Newkirk, Planet Space Sci. 15, 1267 (1967).
6. H. C. Van de Hulst, Light Scattering by Small Particles, Wiley & Sons, New York, (1957).
7. J. L. Weinberg, Annals Astro Phys. 27, 201 (1964).

TABLE I  
SPACECRAFT PARAMETERS

Spacecraft	h (km)	dm/dt (gm/sec)	R <sub>o</sub> (cm)	M <sub>s</sub> (gm/cm <sup>2</sup> )
Gemini 3	160	4.2 x 10 <sup>-3</sup>	2 x 10 <sup>2</sup>	1.5 x 10 <sup>-12</sup>
Gemini 11	300	1.4 x 10 <sup>-2</sup>	2 x 10 <sup>2</sup>	5.1 x 10 <sup>-12</sup>
Apollo	300	3 x 10 <sup>-2</sup>	2 x 10 <sup>2</sup>	1 x 10 <sup>-11</sup>
ATM	400-500	1 x 10 <sup>-1</sup>	3 x 10 <sup>2</sup>	1 x 10 <sup>-10</sup>

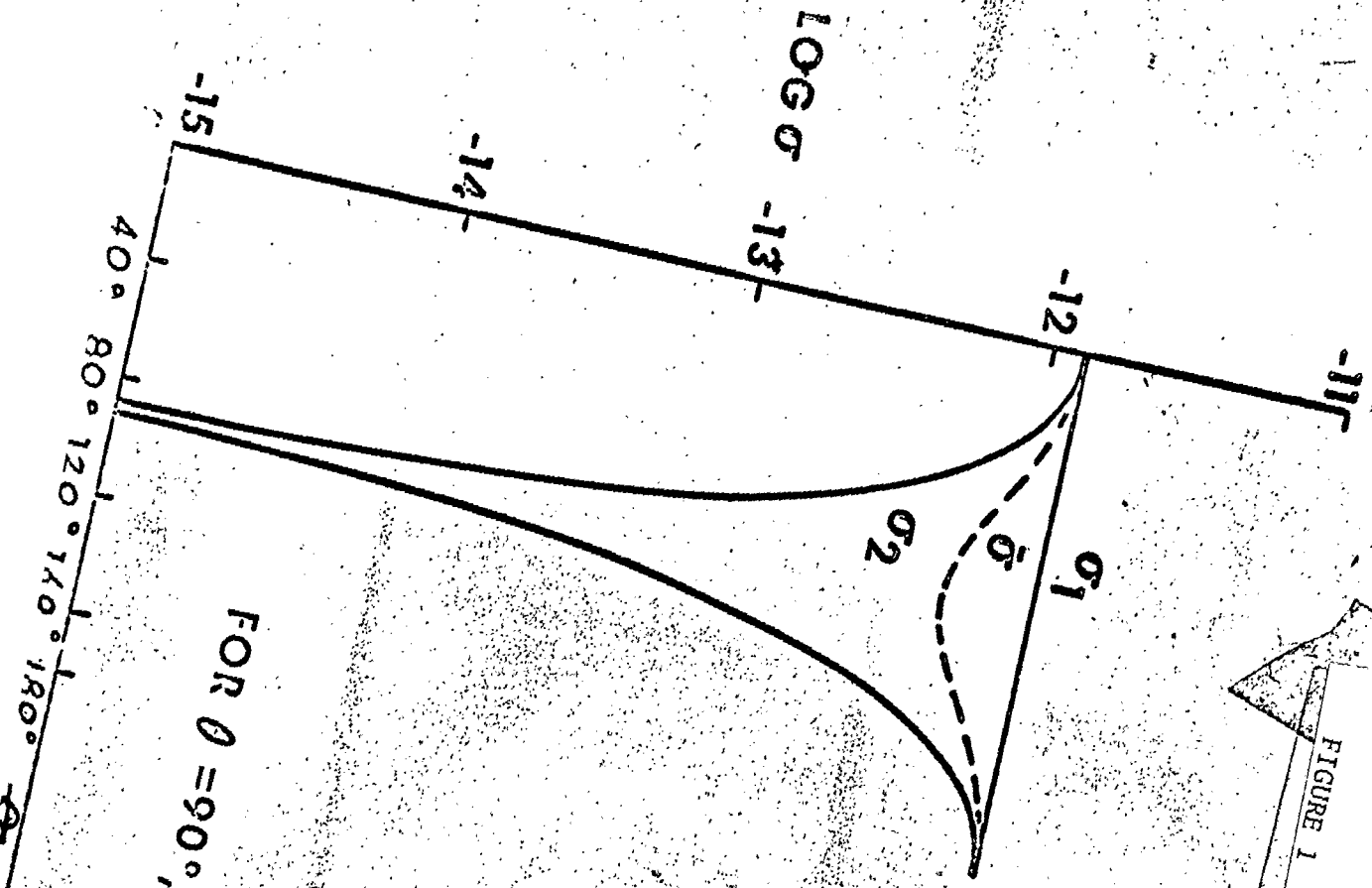
FIGURES





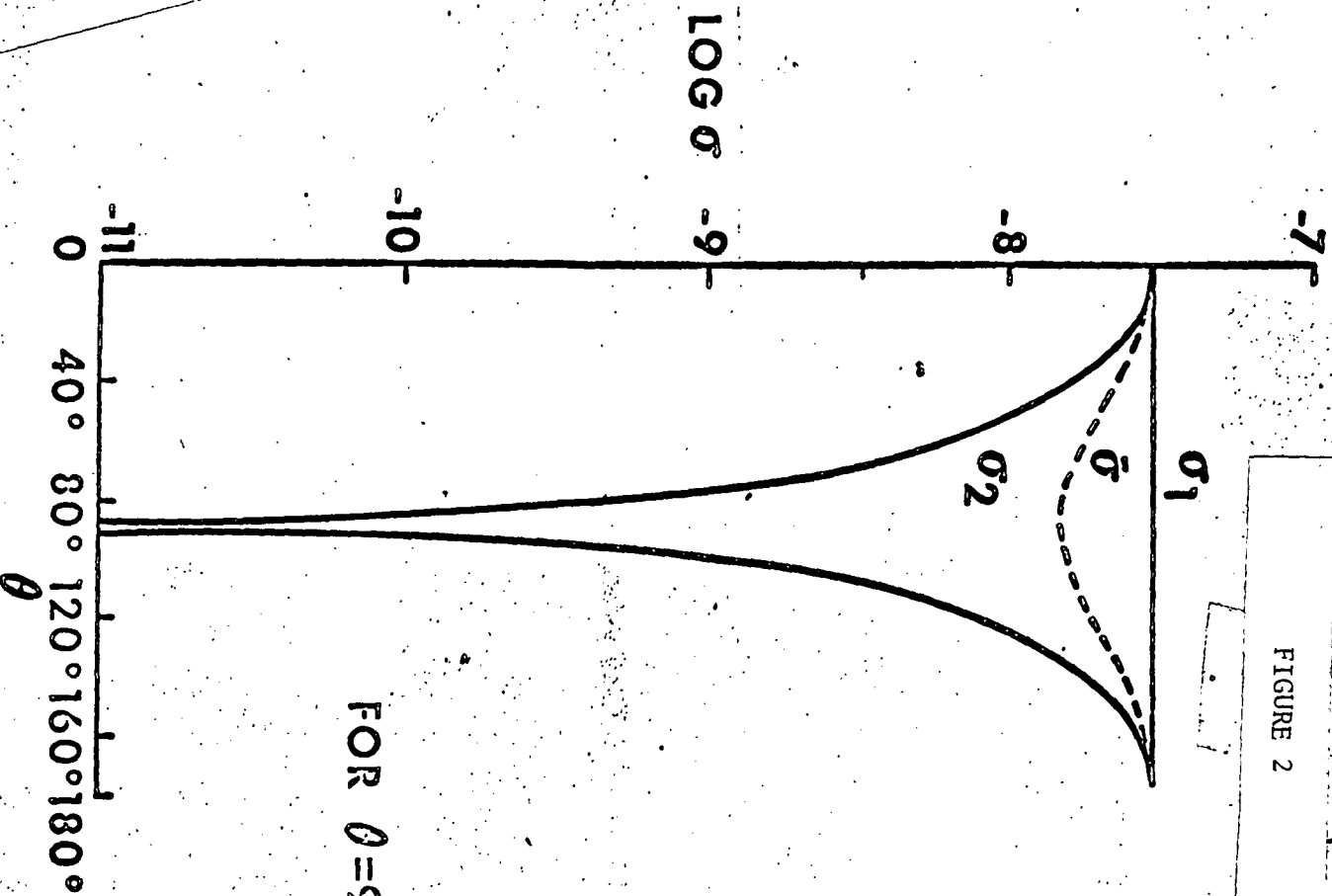
FIGURE 1

$r=15\text{\AA}$   
 $\lambda=5300\text{\AA}$   
 $m=1.33$



FOR  $\theta = 90^\circ$ ,  $\sigma_2 = 0.115 \times 10^{-21}$

FIGURE 2



FOR  $\theta=90^\circ, \sigma_z=0.295 \times 10^{-14}$

$r=15 \text{ \AA}$   
 $\lambda=1200 \text{ \AA}$   
 $m=1.353-0.4414i$

FIGURE 3

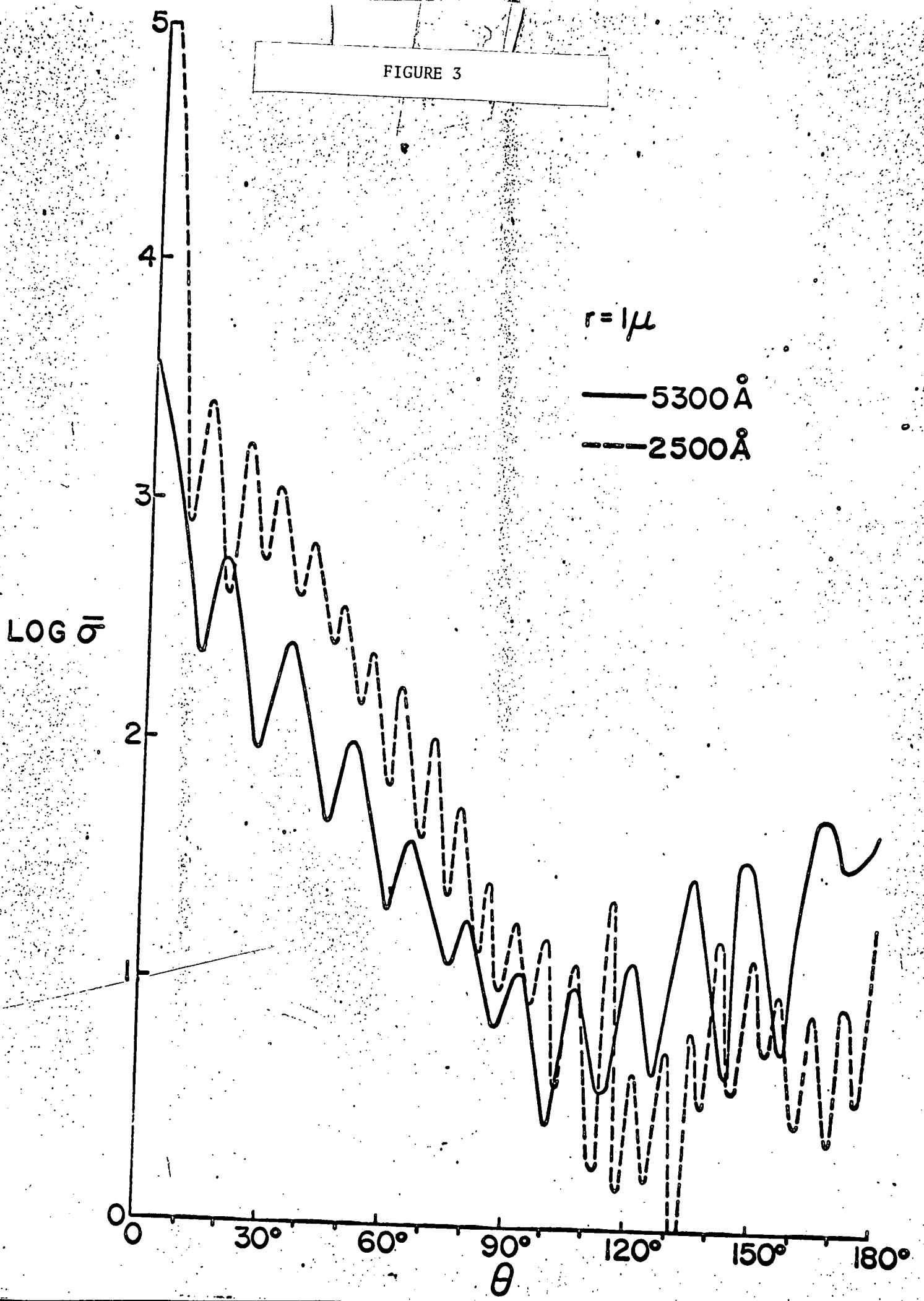
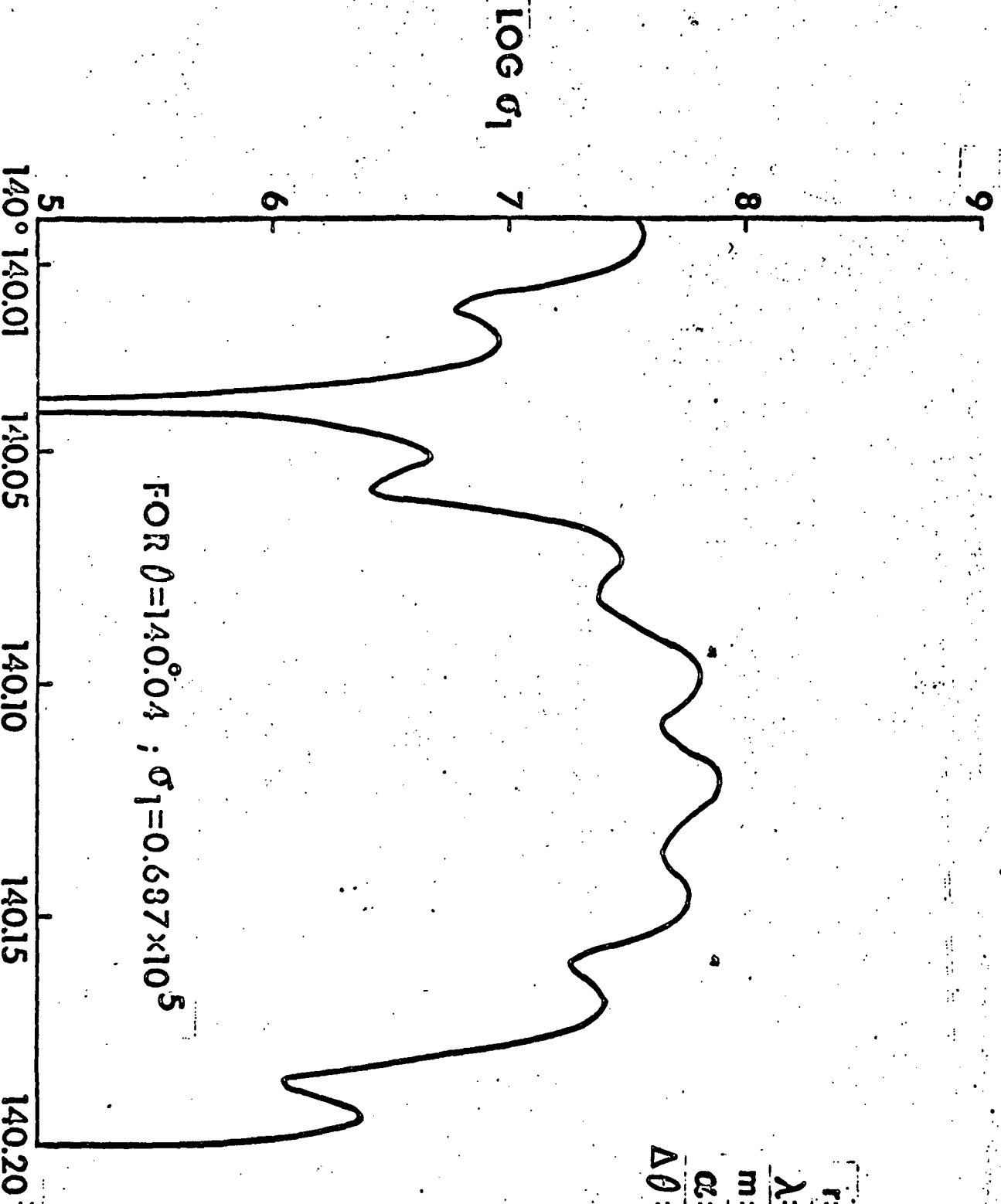


FIGURE 4

# MIE SCATTERING FUNCTION



$r = 1000 \mu$   
 $\lambda = 5300 \text{ \AA}$   
 $m = 1.33$   
 $\alpha = 11,855$   
 $\Delta\theta = 0.002$

FIGURE 5

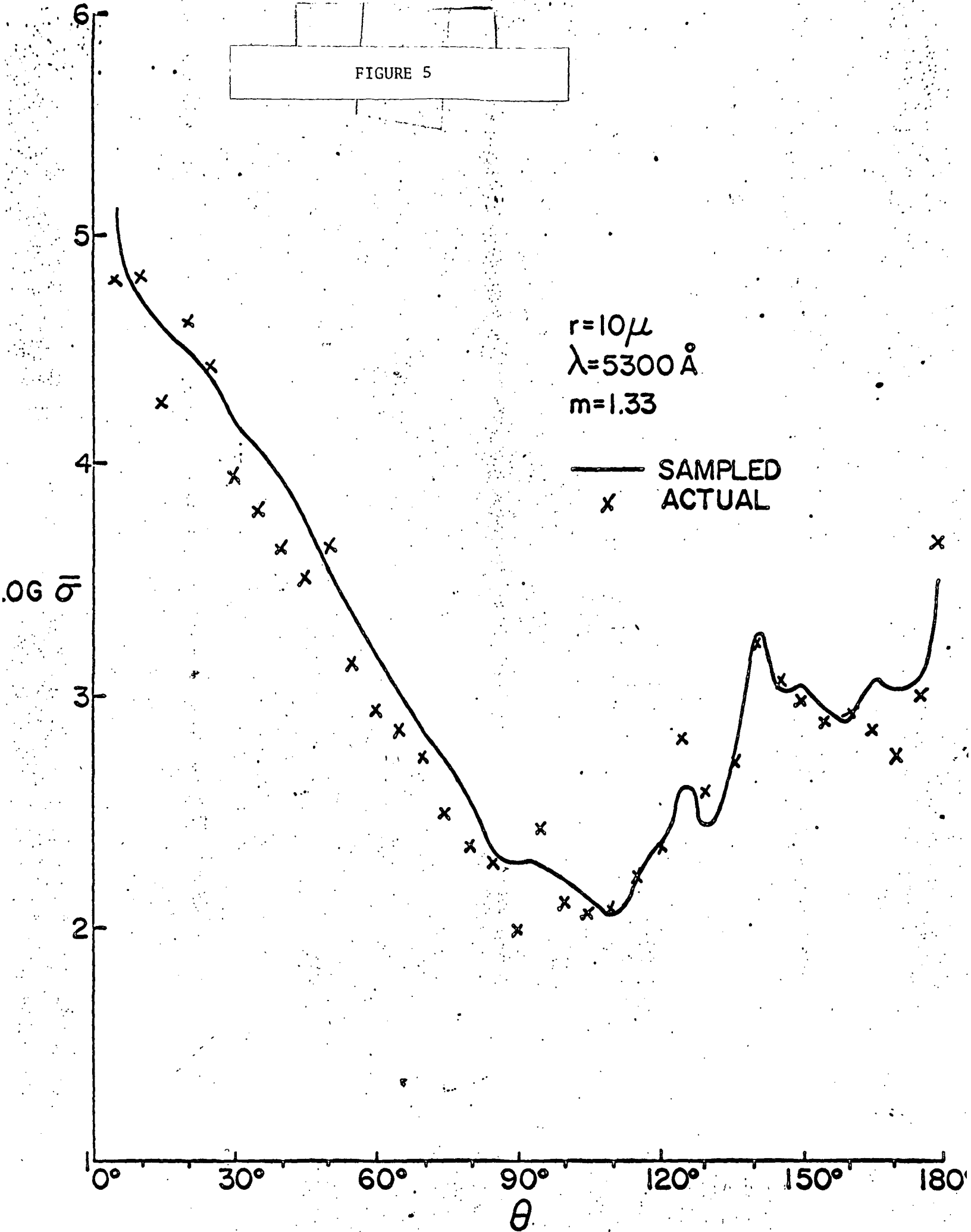


FIGURE 6

$r=10\mu$   
 $\lambda=1200\text{\AA}$   
 $m=1.353 - 0.4414i$   
"AVERAGED" CURVE

—  $\sigma_1$   
- - -  $\sigma_2$

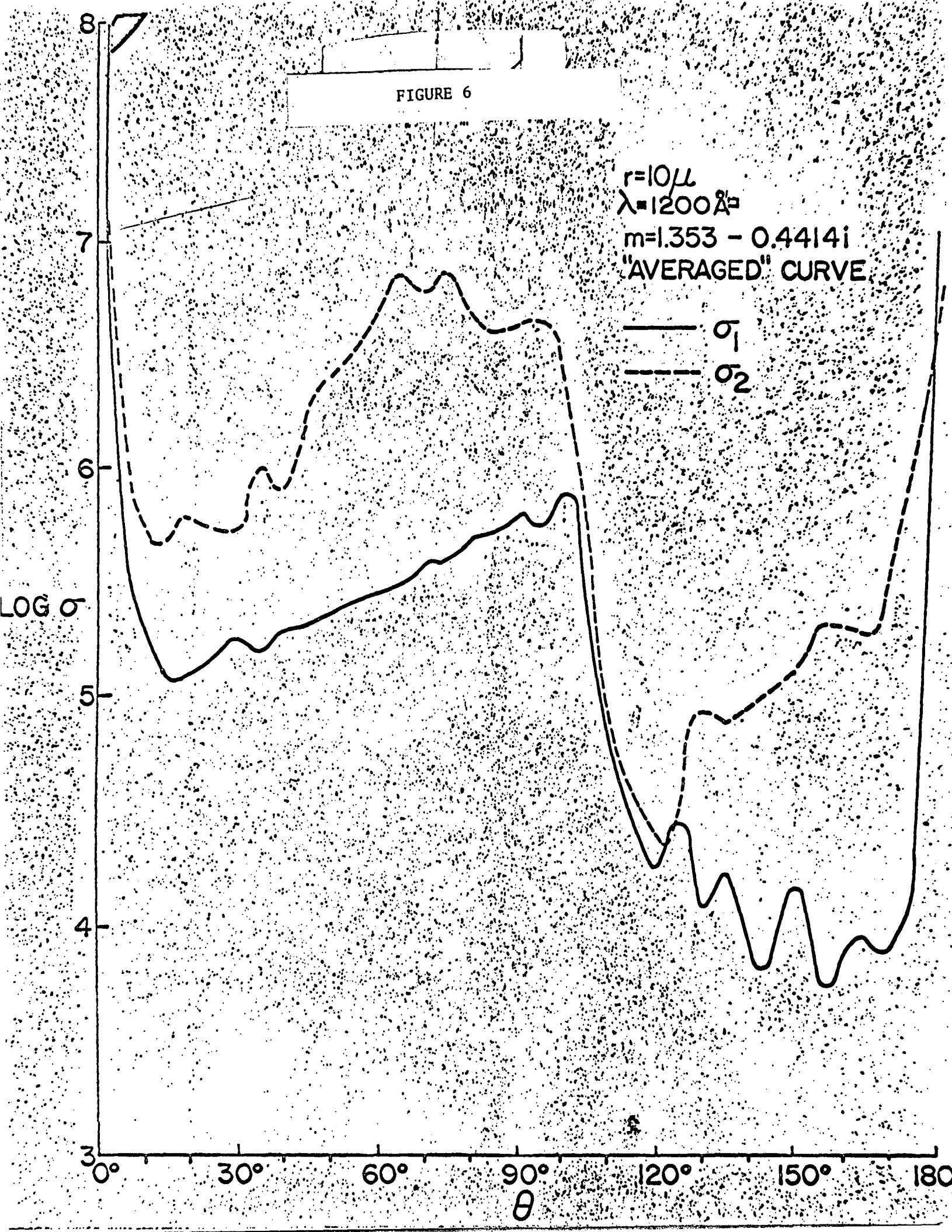


FIGURE 7

$k=2.5, m=1.33$

$12-\alpha-120$

$\Delta\alpha=0.10$

—  $\sigma_1(\theta)$

- - -  $\sigma_2(\theta)$

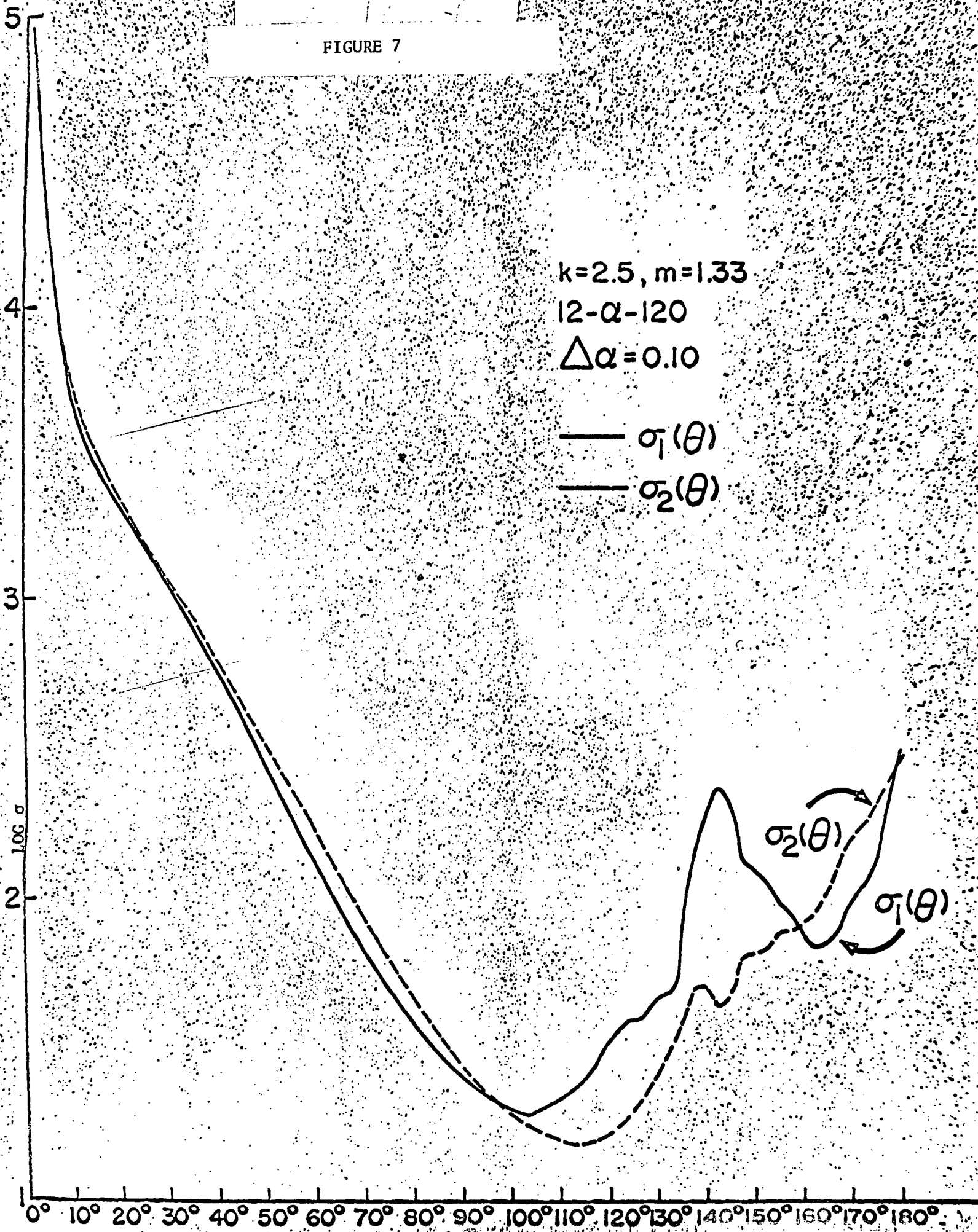


FIGURE 8

$k = 2.5$   
 $m = 1.33$   
 $12 \leq \alpha \leq 240$   
 $\Delta\alpha = 0.20$

LOG  $\sigma$

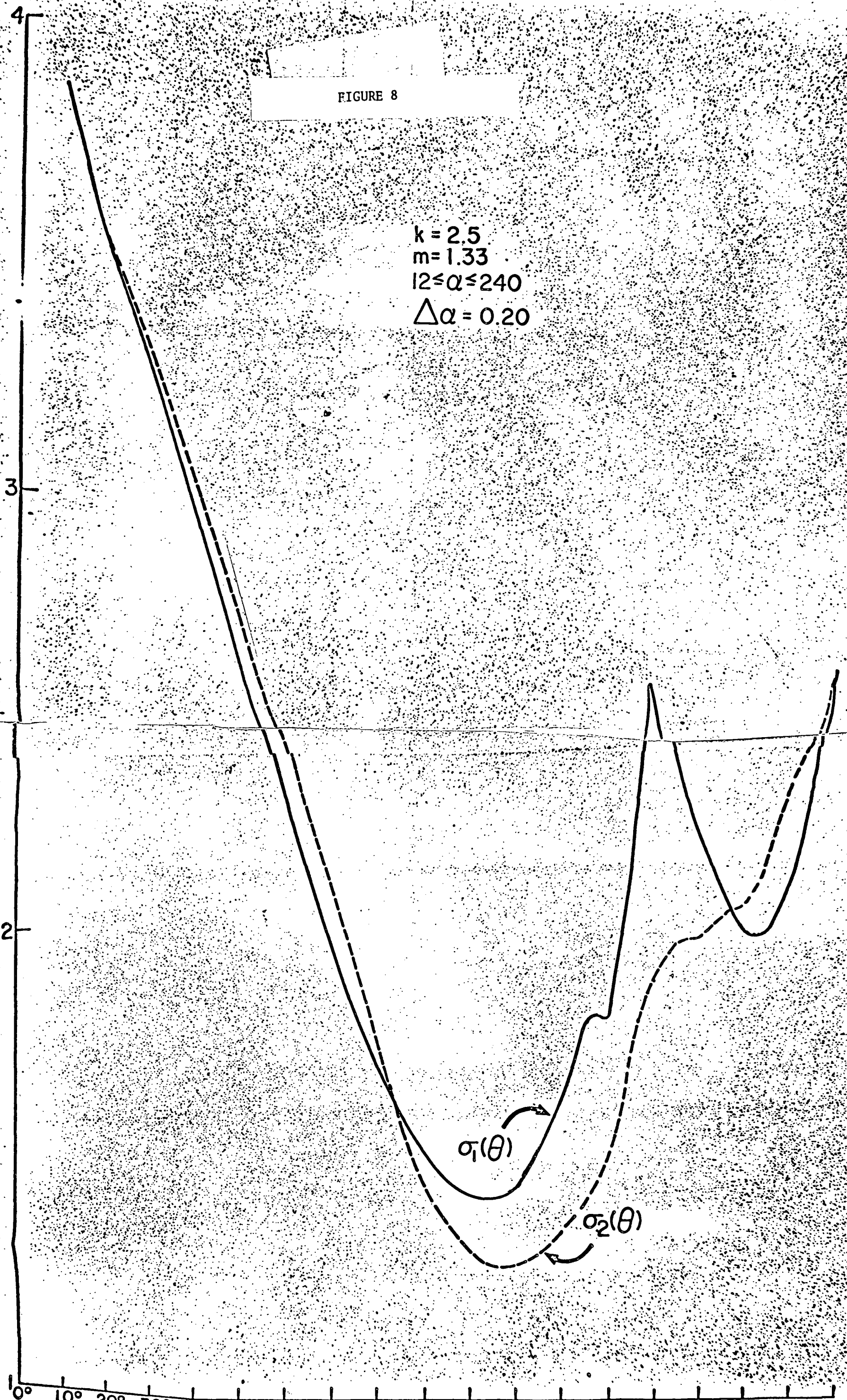




FIGURE 9

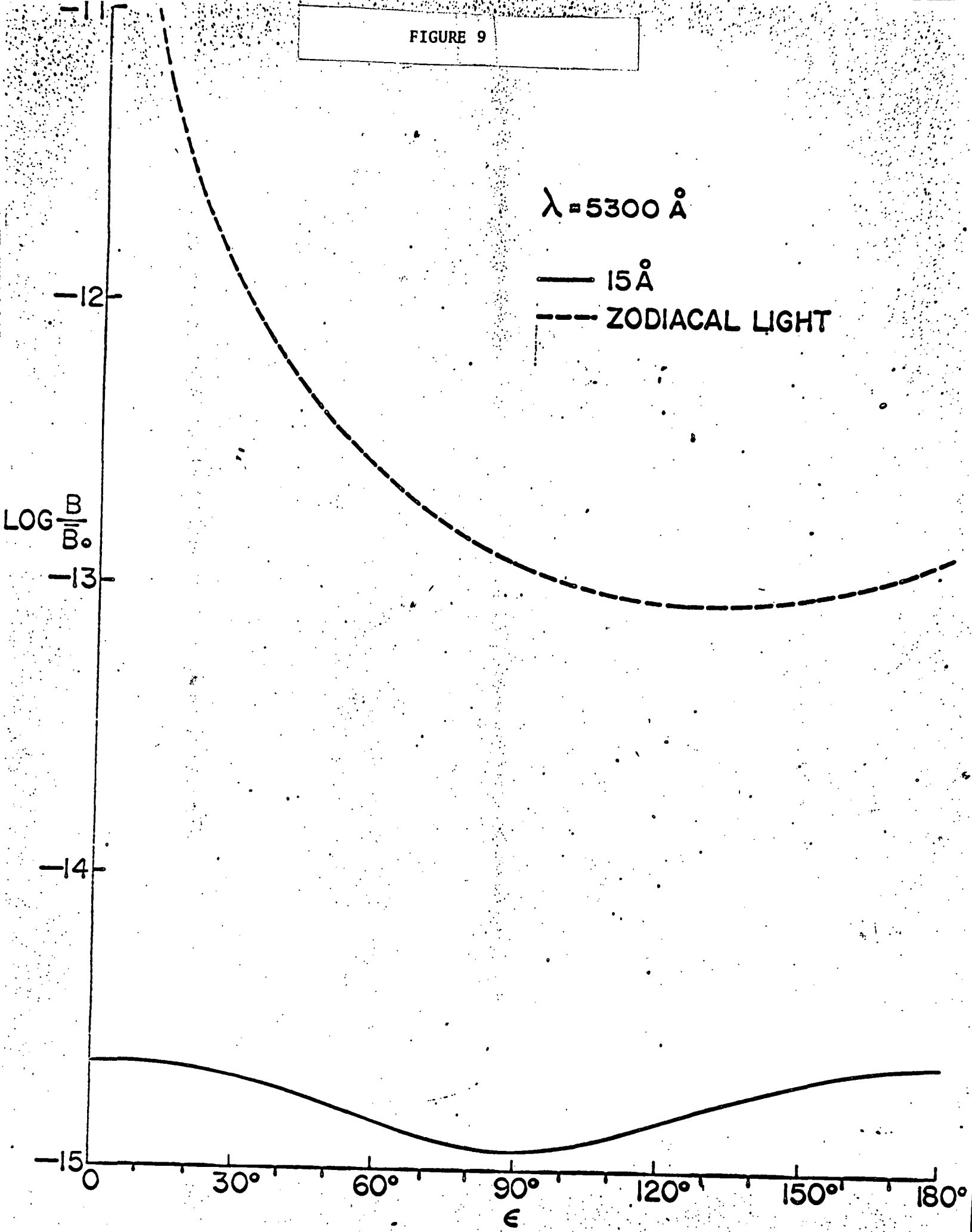
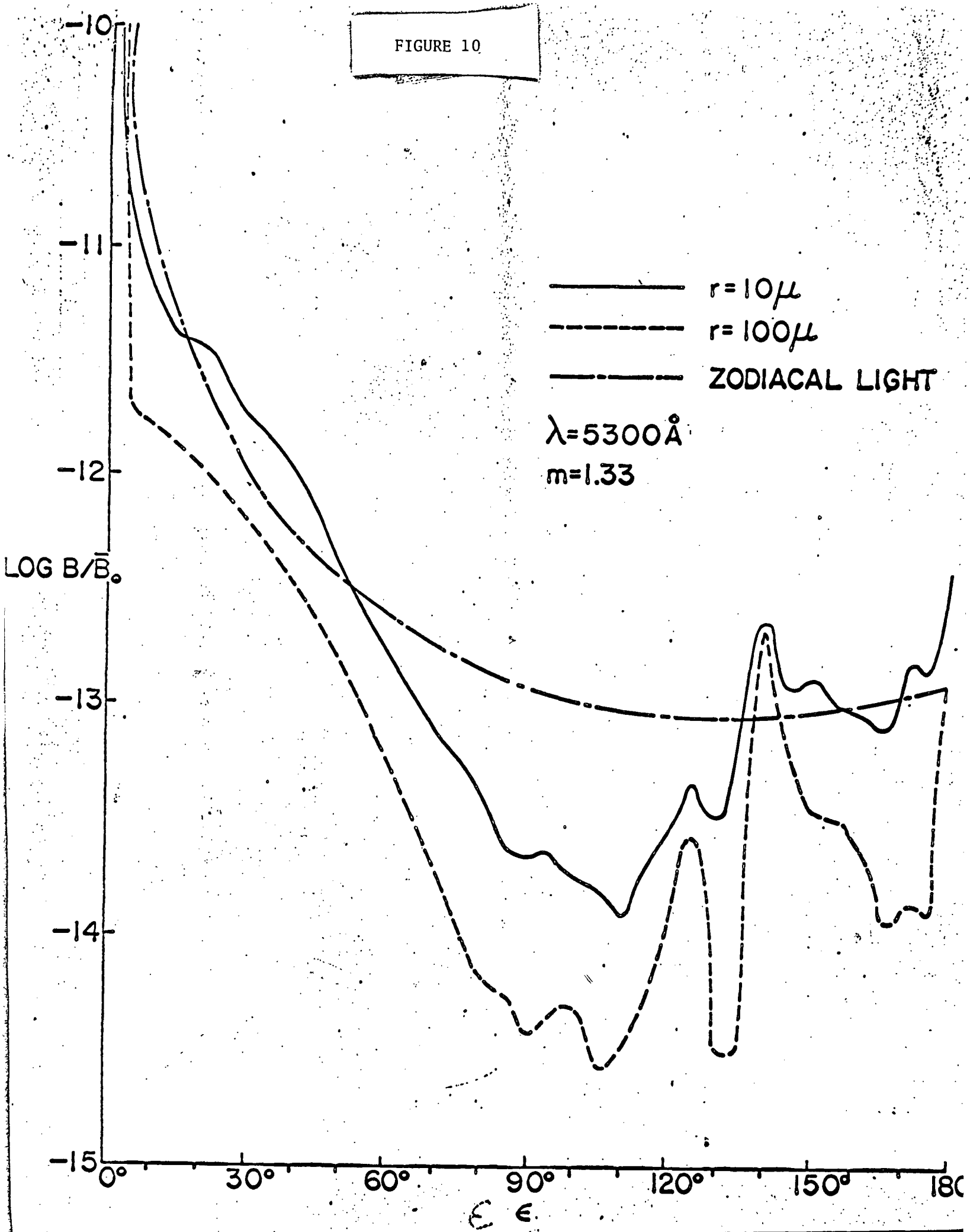


FIGURE 10



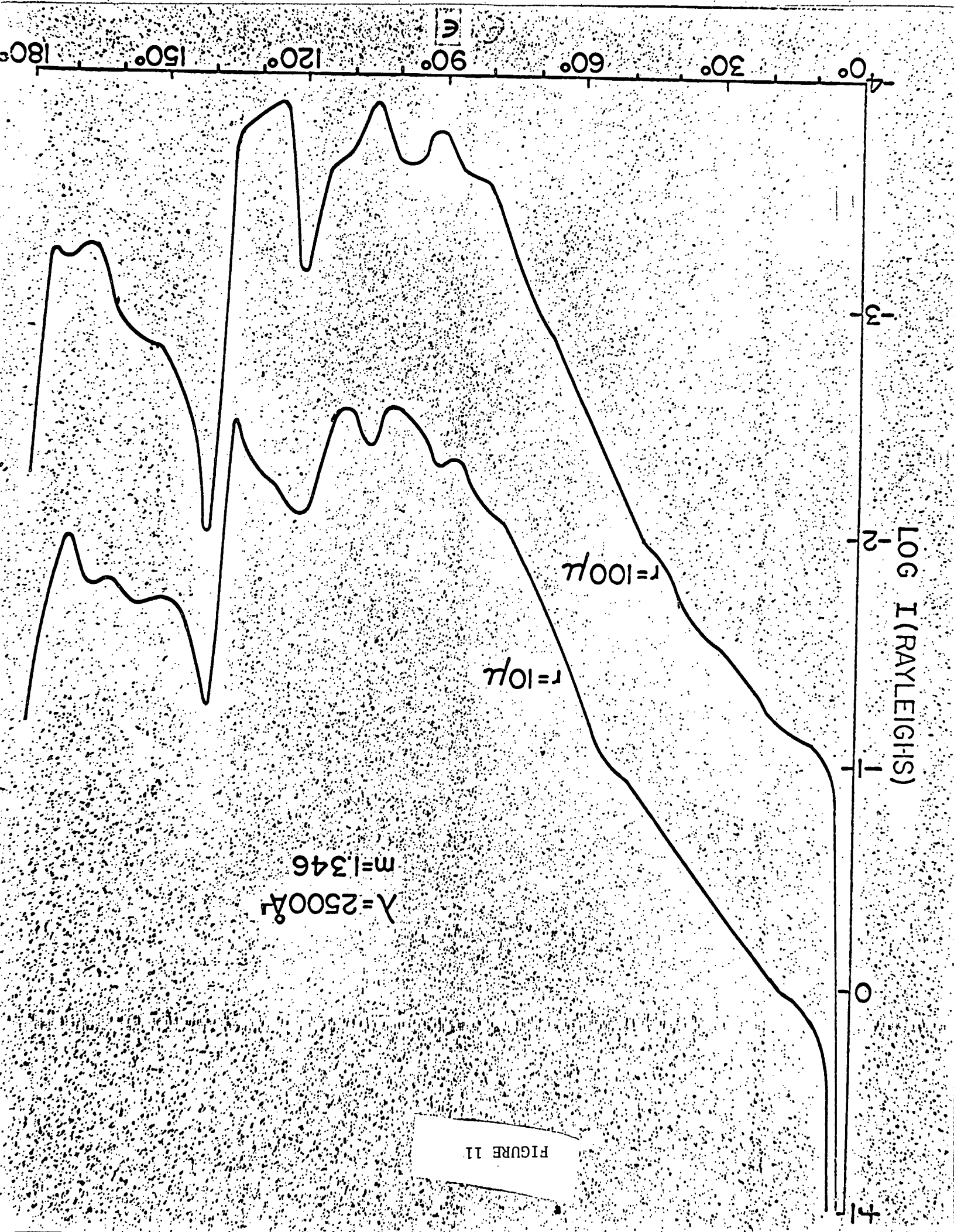


FIGURE 11

FIGURE 12

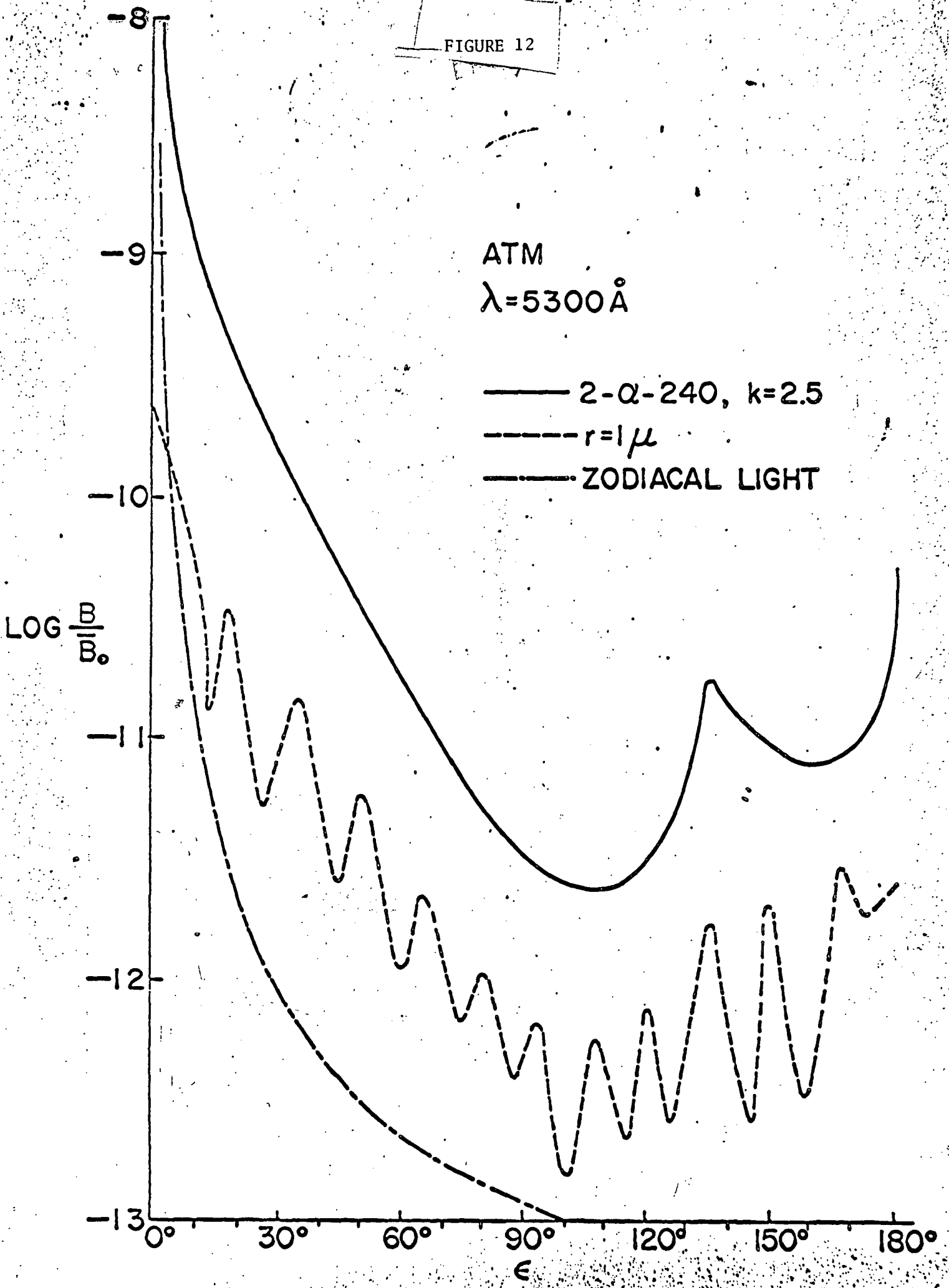


FIGURE 13

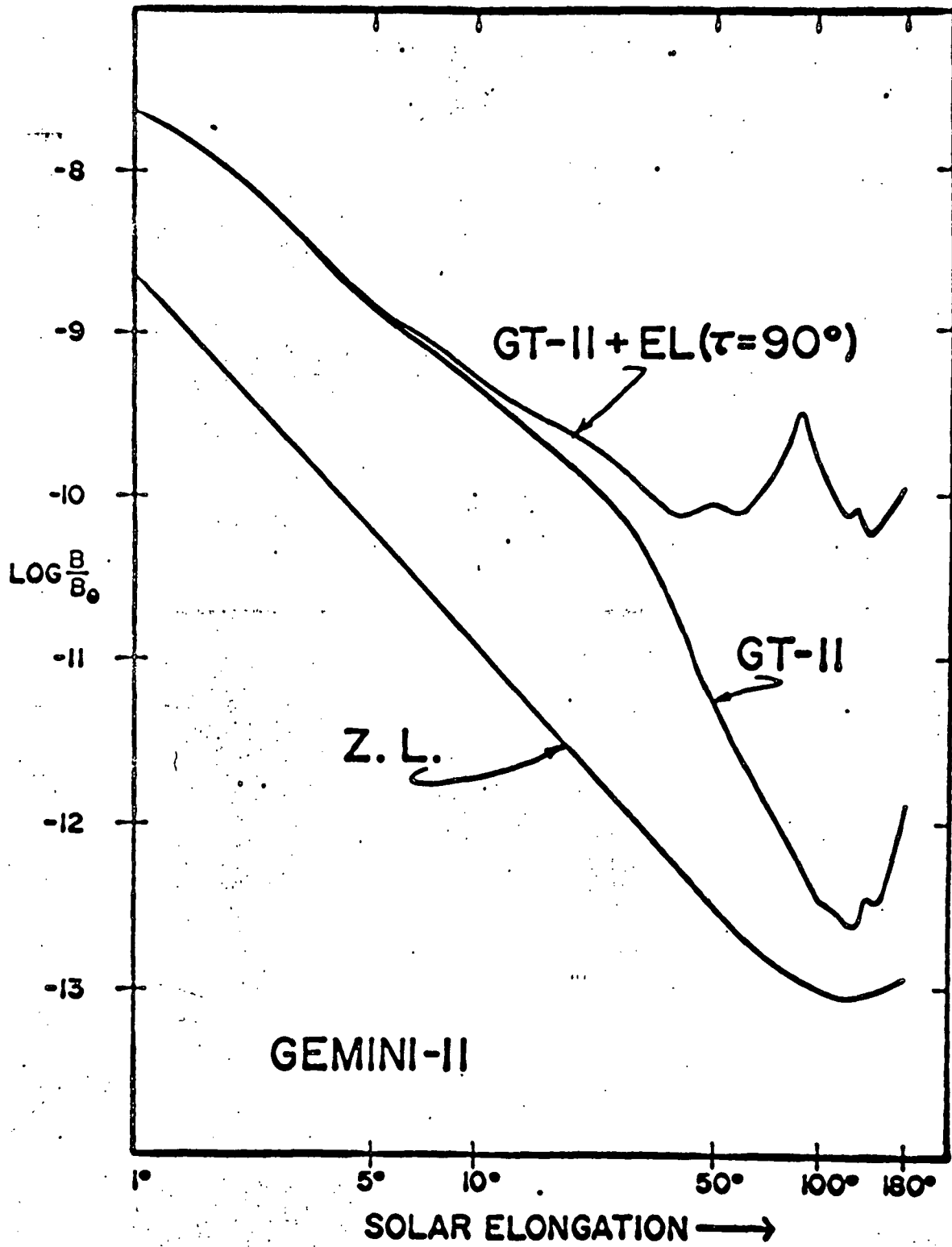
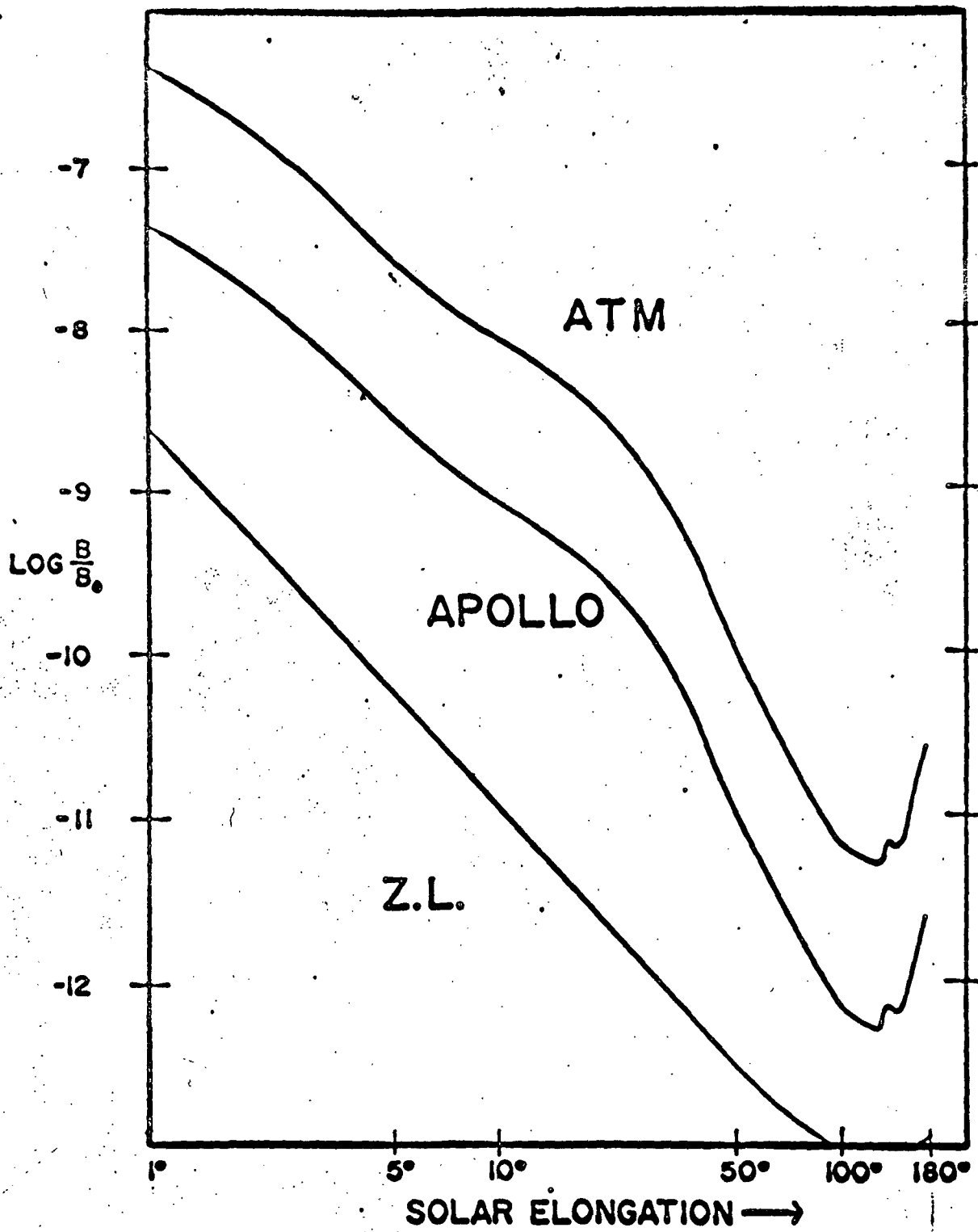


FIGURE 14



APPENDICES

APPENDIX A

Individual Scattering Functions

$\lambda$ (A°)	$r$ ( $\mu$ )
5300	$15 \times 10^{-4}$ , 1, 10, 20, 100, 200, 1000, 10,000
2500	$15 \times 10^{-4}$ , 1, 10, 100, 1000, 10,000
2000	$15 \times 10^{-4}$ , 10
1800	$15 \times 10^{-4}$ , 10
1700	$15 \times 10^{-4}$ , 10, 100, 1000
1600	$15 \times 10^{-4}$ , 10, 100, 1000
1500	$15 \times 10^{-4}$ , 10, 100, 1000
1400	$15 \times 10^{-4}$ , 10, 100, 1000
1300	$15 \times 10^{-4}$ , 10, 100, 1000
1200	$15 \times 10^{-4}$ , 1, 10, 1000
1100	$15 \times 10^{-4}$ , 10, 100, 1000
1000	$15 \times 10^{-4}$ , 10, 100, 1000



APPENDIX B

Selected Scattering Functions for a  
Range of Particle Size\*

<u>m</u>	<u><math>\alpha_1</math></u>	<u><math>\alpha_2</math></u>	<u>k</u>
1.30	1	6	2, 3, 4
	2	12	2.5, 3, 4
	2	240	2.5
	12	30	2.5, 3
	30	60	2.5
	60	90	2.5
	40	120	2.5
	150	180	2.5
1.340	1.396	55.85	4
1.249-0.0472i	0.038	0.077	0
	0.698	1.396	0
	0.077	3.084	4
1.27-1.37i	2	2	2.5
	12	30	2.5
	60	90	2.5

\*These results represent only a limited sampling of the scattering functions computed for a column of material for particles of varying size. Results are available for other indices of refraction and for a wide range in increments of  $\alpha$  and of  $\theta$ . In all cases a particle distribution,  $n(r) \propto r^{-k}$ , was assumed. (The contractor will, upon request, make available any computed data.)