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INTEGRATED DYNAMIC ANALYSIS SIMULATION OF SPACE STATIONS WITH CONTROLLABLE SOLAR ARRAYS (SUPPLEMENTAL DATA AND ANALYSES)

By

Joseph A. Heinrichs Fairchild Industries, Inc.

Joseph J. Fee Wolf Research and Development Corp.

Prepared Under Contract No. NAS1-10155

By



Fairchild Industries Germantown, Maryland 20767

For

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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Vibration Mode Data

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1.0 INTRODUCTION

This volume of the final report presents space station and solar array data and the analyses which were performed in support of the integrated dynamic analysis study. It is intended to supplement the information included in NASA CR-112118.

The presented analysis methods and the formulated digital simulation were developed by the combined efforts of Fairchild Industries and its associate, Wolf Research and Development Corporation.

Section 2 of this volume presents the space station and solar array configurations which were considered during the course of this study. These are resulting configurations from studies performed by various aerospace companies. Control systems for space station altitude control and solar array orientation control (Report Section 3) include generic type control systems. These systems have been digitally coded and included in the simulation.

Report Section 4 presents the detailed analytical formulations which were derived and digitally simulated to provide an automated method of dynamic analysis. These formulations and corresponding simulations were derived for two study phases. The first study phase considered only the rigid body dynamics of the space station; while the second study phase included the flexible body dynamics of space station as well as the rigid and flexible dynamics of spinning space stations. Required input to the simulation includes the vibration mode data associated with the controllable and non-controllable appendages, and the space station. Therefore, extensive structural analyses were performed on the structures in support of the study work and analyses results are presented in Report Section 5. Appendix A presents detailed information and structural analyses data associated with the models utilized.

Verification analyses performed with the simulation are presented in Report Section 6. These analyses used simple structural configurations for the subsequent comparison with the simulation. Numerous documents were written during the course of this study which present interim study results and user information for the simulations.

1-1 .

2. SPACE STATION/SOLAR ARRAY STRUCTURAL CONFIGURATIONS

The formulation of an interaction analysis method for the determination of solar array structural requirement required structural concept definitions for purposes of providing analytical baselines. By direction from NASA/LRC, two solar array configurations were specified as analytical baselines for this study. One configuration consisted of the flexible rollup array studied by the Lockheed Missile and Space Company (Reference 2. 1) and is sized to meet a 100 kilowatt power requirement. An initial version of the fully extended array and space station configurations is shown in Figure 2-1. The other solar array configuration which was used in this study was the foldout panel concept shown in Figure 2-2. The structural configuration of this array is based upon a Boeing Aircraft Corporation design which was proposed for a Mars mission vehicle. This design was updated to meet the 100 kw power requirement and to meet the geometrical constraints of the space station's shroud for the launch phase of powered flight. These two array configurations were utilized to derive structural vibration mode data which are required in the implementation of the dynamic interactions analysis.

A space station configuration concept utilized was that presented by the North American Rockwell Corporation (NAR) in Reference 2.2. The configuration is comprised of one or more modules which can be assembled in space in "cruciform" and "bar bell" arrangements. Typical arrangements are depicted in Figure 2-3. The specific arrangement of modules analyzed for vibration mode properties, is that given in Figure 2-4. It is comprised of a power boom, a core module, and eight attached modules arranged in a cruciform configuration. An artificial "G" space station configuration was also chosen and analyzed and is shown in Figure 2-5.

An updated version of the rollup solar array configuration was also analyzed. This design was configured by Lockheed under Contract NAS9-11039. A review of their study is given in Reference 2.3 and a sketch of the array is shown in

Figure 2-6. It is comprised of a series of 10 flexible solar cell substrates deployed with a center boom and tensioned between an inner and outer boom. During a proposed artificial "G" mode of operation, the roll up array configuration is changed to that shown in Figure 2-7. All array configurations were analyzed for cantilever vibration mode properties.

REFERENCES

Reference 2.1 - "Space Station Solar Array Technology Program Mid-Term Review", Lockheed Missile and Space Company, May 1971.

Reference 2.2 - "Modular Space Station - Phase B Extension, First Quarterly Review", North American Rockwell, Space Division, PDS-71-2, May 1971.

Reference 2.3 - "Space Array Technology Evaluation Program, Second Topical Report", Lockheed Missile and Space Company (LMSC-A981486), November 1971.



Figure 2-1. Space Station/Rollup Flexible Array



Figure 2-2. Space Station/Foldout Panel Array



Figure 2-3. Space Station - Modular Concept







Figure 2-6

Zero "G" Roll-Up Solar Array Configuration 2-8



Figure 2-7 Artificial "G" Rollup Solar Array Configuration

3. GUIDANCE AND CONTROL SYSTEM CONSIDERATIONS

3.1 SPACE STATION ATTITUDE CONTROL SYSTEM

The guidance and control system for the North American space station incorporates two generic types of control laws/torquers for attitude control. A control moment gyro (CMG) control system is used for precision attitude stabilization without the need for propellant expenditure. A reaction jet control system (RCS) is used for reference attitude acquisition maneuvers and for momentum desaturation, as required, for the CMG system.

The attitude control requirements as given in Reference 3.1 during zero G operations are as follows:

- Stabilization of the Station, prior to manning, to an accuracy of ±5 degrees
- Stabilization during initial docking to an accuracy of ±1 degree
- Stabilization during routine experiment operations to a ±0.25 degree attitude tolerance, and with angular rate excursions below 0.05 degree per second.
- 3.1.1 CMG CONTROL SYSTEM

The CMG control system has been designed by the General · Electric Company for North American.

A simulation model has been developed and is based upon a number of reports provided by G.E. A block diagram of this simulation model as given in Reference 3.2 is presented in Figure 3-1. The detailed equations for the control law are in accordance with the system selected by GE, which can be characterized as follows. It consists of three two-degree-of-freedom⁴ control moment gyros with parallel outer gimbals and with their momentum vectors initially equally spaced in the orbit plane. This configuration permits simpler steering laws and a planar, rather than three dimensional, anti-hangup law.

Reference 3.1 indicates that this control system has a natural frequency of 1.414 Hz and a damping ratio of 0.707. It was found that during the performance of various digital simulations, that a relatively small numerical integration interval ($\Delta t = .005$ second) was required to stabilize solutions to motion equations when the CMG was chosen as the active control system. This was due to high frequencies of inner control loops. Since small integration time steps were required for stability of solution with the CMG of Reference 3.2, a simpler system for the control structural motions was also derived to represent CMG controlling torques. This system which was suggested by NAR, produces a more efficient computer simulation time to real time ratio when the CMG is chosen as the active control. It is programmed in the simulation as represented by the diagram shown in Figure 3-2. It is comprised of a lead-lag compensator, a constant multiplying the moment of inertia properties of the spacecraft under investigation and an output torque limiter. The time constants of the lead-lag compensator, the constant multiplying spacecraft inertia and the limiting torque are allowed as input quantities to the control subroutine in the simulation. This simplified representation thus allows a certain degree of flexibility when analyzing general space station configurations. The commanded position angle is obtained from parameters calculated within the computer program (Reference 3. 3). The actual angle is calculated within the program logic and is comprised of rigid plus flexible spacecraft body structural motions. Since space station structural flexibility is considered in the feedback control loop, the position of angle sensors and angular rate within the structural system is allowed to be specified. In like manner, the position of the control torque is specified so that generalized modal torques produced by the control system can be considered as input to modal degrees of freedom.

A simple wobble damper control representation is included in the simulation for control of spinning structural configurations. It consists of a single degree-of-freedom control moment gyro with its gimbal axis along the nominal spin axis and its momentum vector normal to that axis. With reference to Figure 3-3, the spinning structural system is considered to be about the X axis. The control moment gyro is torqued so that its momentum

vector \bar{h} always lags the wobble rate, ω_{T} , by 90°. A correction torque is applied to the space station which is equal to the following.

$$T_{C} = (\omega_{S} + \dot{\alpha}) \times \ddot{h}$$

An increase in the nominal spin rate also occurs to the correction wobble torque and is given as

$$\bar{T}_{S} = - \bar{\omega}_{T} \times \bar{h}$$

The magnitudes of parameters associated with the wobble damper control system are an option when performing the simulation of a spinning space station.

3.1.2 REACTION JET CONTROL SYSTEM (RCS)

The reaction jet control system (RCS) is used for reference attitude acquisition maneuvers, momentum unloading of the control moment gyro, and as an alternate to the CMG for controlling the attitude of the space station. A RCS is composed of four thruster modules and each module has four thrusters. The modules are located at the periphery of a space station, as shown in Figure 3-4. All sixteen thrusters compose a fully redundant three axes attitude control system.

A jet thrust level is indicated in Reference 3.1 to be 10 pounds in order to provide the same torque magnitude with the RCS as with the CMG control system. Reference 3.1 further states that this small jet size requires significant pulse durations for most maneuvers and thus should minimize the need for a minimum impulse provision which was a major problem area for Apollo. Expected orbit makeup (correction) firing times are indicated to range from 7 to 14 seconds. Reference 3.1 indicates that the preprocessing electronics for the RCS sums the outer loop attitude and rate signals with any attitude maneuver command signals. It also includes the phase-plane deadband logic which then feeds the jet drive electronics.

Based upon the foregoing information, a suitable model of the RCS for the North American space station should be as depicted in Figure 3-5. Because of the indicated comparable torque levels of the CMG control system

and the RCS (and the low thrust levels and relatively long firing times) the former will represent a dynamic excitation element for the space station/array that is comparable to the latter. All maneuvers using the RCS are performed by firing two thrusters as a couple. The primary thrusters for each maneuver are selected by choosing the pair of thrusters with the longest lever arm.

The torque equations in the simulation of a rigid space station, and based upon the block diagram in Figure 3-5, are

$$\begin{bmatrix} \mathbf{T}_{\mathbf{R}} \\ \mathbf{T}_{\mathbf{P}} \\ \mathbf{T}_{\mathbf{Y}} \end{bmatrix} = \begin{bmatrix} \mathbf{B}_{\mathbf{R}} \\ \mathbf{B}_{\mathbf{P}} \\ \mathbf{B}_{\mathbf{Y}} \end{bmatrix} \begin{bmatrix} \mathbf{K}_{\Theta} \quad \phi_{\mathbf{e}} + \mathbf{K}_{\Theta} \quad \dot{\varphi} \\ \mathbf{K}_{\Theta} \quad \Theta_{\mathbf{e}} + \mathbf{K}_{\Theta} \quad \dot{\varphi} \\ \mathbf{K}_{\Theta} \quad \psi_{\mathbf{e}} + \mathbf{K}_{\Theta} \quad \dot{\psi} \end{bmatrix}$$

where

 T_R , T_P , T_Y are the torques applied to the space station about the roll, pitch and yaw axes respectively.

 $B_R^{}, B_P^{}, B_Y^{}$ are the torque dead bands for each axis $K_{\Theta}^{}$ is the gain proportional to the space station angle error $K_{\Theta}^{}$ is the gain proportional to the space station rate about each axis $\phi_{\epsilon}, \theta_{\epsilon}, \psi_{\epsilon}^{}$ are the angle errors in roll, pitch and yaw respectively $\dot{\phi}, \dot{\Theta}, \dot{\psi}^{}$ are the space station rates in roll, pitch and yaw.

These equations are used in the RCS digital subroutine

in the simulation to develop the control torques for the thruster system. This proportional control system, when used as an alternate to the CMG control system, will permit more economical computation of the interaction dynamics. Since the computerized method of simulating space station motions was modified in Phase II study efforts to account for space station flexibility, the reaction jet control system in the simulation consists of six individual constant-thrust-magnitude thrusters at specified structural locations to control the three angular rigid body motions. Location of each thruster, thrust magnitude and thrust direction, are allowed to be specified prior to performing a simulation. Program logic computes the generalized forces into space station modal degrees of freedom using other appropriate input structural mode constants. The typical applied torque equation is

$$T = K \bullet 1 (E_C - E_{DB})$$

where

T = output torque of the reaction jets at any given time for which the computed "error" is E_C.

K = torque capability of the reaction jets

- unit step function having the value zero for negative or zero arguments and the value unity for positive arguments.
- E_C⁼ computed equivalent attitude/rate error of the space station determined by

$$E_{C} = K_{1}(K_{2} \phi - \omega)$$

where K_1 and K_2 are input constants and ϕ and ω are attitude and rate errors of the space station respectively.

E_{DB} = deadband threshold level for equivalent attitude/rate error which determines when the reaction jets are active.

3.2 SOLAR ARRAY ORIENTATION CONTROL SYSTEM (OCS)

The operating characteristics of the Orientation Control System (OCS) for the solar arrays being considered in this study effort can have a major impact on the latter's design requirements. Hence, in developing an analysis method to evaluate the design of such arrays, the significant dynamic characteristics of the OCS must be properly modeled. Two generic types of OCS drive systems have been considered and are characterized by the following:

- The continuous array drive system
- The non-linear (bang-bang) drive system.

3.2.1 CONTINUOUS ARRAY DRIVE SYSTEM

A block diagram of the continuous OCS is shown in Figure 3-6. The difference between the commanded array angle and actual array angle are used to generate the angle error signal. This error signal is then filtered by the provided compensation in the control loop. The array angular rate $\dot{\theta}$ is multiplied by the back EMF coefficient K_B and added (negatively) to the filtered error signal. This gives the effective drive signal for the motor. The drive motor is modeled as a first order lag with K_M as the torque gain of the motor and τ_M as the motor time constant. The output torque of the motor is reduced by the friction in the reduction gear unit as shown by the K_F feedback loop. The effective torque of the motor is increased by the ratio of the reduction gear and delivered to the solar array. To determine the stability of the OCS, the solar array is assumed to be rigid and have an inertia I_A about is axis of rotation.

To assess the effects of the two rate feedback loops in Figure 3-6 the value of $K_F \dot{\Theta}$ and T_M were compared for $\dot{\Theta}$ equal to orbital rate. The results showed $K_F \dot{\Theta}$ to be significantly smaller than T_M and hence the K_F feedback loop can be dropped from the simulation without any loss of generality. This is generally expected to occur for this class of control systems. With one of the feedback loops removed, the OCS continuous drive model can be simplified. The drive mechanism can then be modeled by two first order

filters to smooth the array angle error and rate signals. The two signals are weighted by the appropriate gains and added together. The sum is then filtered by a third first order filter (i.e., the motor) where the gain of the filter is the product of the torque gain of the motor and the gear ratio of the drive system. This is shown schematically in Figure 3-7.

To evaluate the stability of the continuous drive OCS, the T-2170 Inland torque motor is assumed as the prime mover in the system. The characteristics of this motor are generally representative of the class of DC torque motors that would be suitable for the array drive system. These characteristics are:

=	3×10^{-3} Henrys
=	18.9 oz-in/amp
=	3.3 ohms
=	1.3 volts/rad/sec

The motor gain and time constant are defined as

$$K_{M} = K_{T} / R_{T} = 5.727 \text{ oz-in/volt}$$
$$\gamma_{M} = M / R_{T} = 0.00091 \text{ sec.}$$

A larger torque motor than required was chosen to allow the motor to operate near its rated speed without an unusually high gear reduction ratio. The chosen motor requires the use of a 6800:1 reduction gear.

The open loop transfer function of the simplified continuous drive OCS is given by equation 1.

$$\frac{\Theta}{\Theta_{c}} = \frac{G(S)}{S} = \frac{K_{\Theta} K_{M} K_{G}}{S \left\{ \gamma_{\Theta} \gamma_{M} I_{A} S^{3} + I_{A} (\gamma_{\Theta} + \gamma_{M}) S^{2} + (K_{M} K_{G}^{2} K \gamma_{\Theta} + I_{A}) S + K_{M} K_{G}^{2} K \gamma_{\Theta} + I_{A} \right\}}$$

The steady state hang off error for the system when following a velocity input (orbit rate) is given by equation 2.

(Equation 2)

 $\frac{\dot{\Theta}_{c}}{\lim S G (S)}$ e_{ss} =

Hence, by selecting a suitable steady state following error, the value of K_{Θ} can be determined. The steady state error is chosen to be 1 degree for the determination of K_{Θ} . This is somewhat tighter than required but it allows for other components in the system to contribute to the steady state error without exceeding the desired overall system value. Substituting equation 1 into equation 2 gives an expression for K_{Θ} in terms of known quantities.

$$K_{\Theta} = \frac{K_B K_G \Theta}{\frac{e_{ss}}{e_{ss}}}$$

(Equation 3)

Using the values for K_B , K_G , and e_{ss} previously given and assuming an orbit period of 100 minutes, the gain of the loop compensation is

$$K_{\Theta} = 530$$

The time constant for the loop compensation is selected by restricting the maximum overshoot to be less than 1 db. Using the characteristics of the T-2170 torque motor and an array inertia of 77,000 slug ft², Equation 1 reduces to

$$G(s) = \frac{\frac{1}{166.8 \text{ T}}}{\frac{1}{S} (S + \frac{1}{T_{\Theta}})}$$

(Equation 4)

when all small terms are neglected. An appropriate time constant for equation 4 is

 $T_{\Theta} \approx 0.01$ sec.

The values presented in this section are considered representative of the continuous drive control system. If other values are desired, provisions are available to include them in the digital simulation.

3.2.2 NON-LINEAR DRIVE SYSTEM

The non-linear drive OCS is similar to the continuous drive system with the exception that the control logic is operated in an on-off manner. When the error signal exceeds some pre-selected threshold value, the motor is turned on until the array is driven to the null position at which point the motor is switched off. The time that the motor takes to reach its running speed when switched on is very small compared to the total time that the motor is operated to drive the array back to the null position. Similarly, the time the motor takes to coast to a stop when the power is turned off is small compared to its total on-time. This would allow the motor to be modeled as a square wave rate generator, i.e., when the motor is commanded on, the array begins rotating at a constant velocity and when the motor is commanded off the array stops rotating.

A non-linear orientation control drive system has been formulated by the Ball Brothers Research Corporation (Reference 3. 4), and this system is included as a control subroutine in the simulation. It is represented by the diagram shown in Figure 3-8. Values of the various constants shown are those received as representative of the BBRC system. In order that simulations could be performed with the many constants varied as parameters, the following were allowed to be input variables to the program subroutine representing this system.

- Deadband angle
- Bus Voltage Generator time constant,
- Bus Voltage Generator amplification constant, A
- Motor Gain ($K_T N/R$)
- Coulomb Friction
- Scaling constant, G

- Gear Ratio, K_G
- Back EMF

The relative velocity vector and angular error are computed by the simulation program for the space station rigid body and flexible degrees of freedom and the solar array degrees of freedom.

3.3 **REFERENCES**

Reference 3.1. "Solar-Powered Space Station Preliminary Design," Vol. III, Guidance and Control Subsystem, North American Rockwell, July 1970.

Reference 3.2. "Preliminary Synthesis and Simulation of the Selected CMG Attitude Control System, "G.E. Report EL-506-D, 5 March 1970.

Reference 3.3. "Small Eccentricities or Inclinations in the Brower Theory of the Artificial Satellite," R.H. Lyddane, Astronomical Journal, Vol. 68, No. 8, Octiber 1963, pg. 555.

Reference 3.4. "Space Station Solar Array Technology Evaluation Program," Second Topical Report, Lockheed Missile and Space Company (LMSC-A981486), November 1971.



CMG CONTROL SYSTEM

(Simplified)



FIGURE 3-2



$\overset{ullet}{lpha}$	- Gimbal Rate of CMG
h	- Momentum Vector
ω _S	- Spin Axis Component of Spin Rate
ωΤ	- Transverse Component of Spin Rate

 $\frac{\text{Applied Torques}}{\overline{T}_{c} = (\overline{\omega \, s} + \overline{\alpha}) \times \overline{h} \text{ (opposes } \overline{\omega}_{T})}$ $\overline{T}s = -\overline{\omega}_{T} \times \overline{h} \text{ (increases spin rate)}$

FIGURE 3-3 Wobble Damper Control Torques

•] •



Figure 3-4 RCS Jet Location/Function





Model for Continuous Drive OCS for Solar Arrays (one continuous motion axis)

Figure 3-6.









•**•**°

θ_Ŕ = θ Α



4. DYNAMIC INTERACTIONS ANALYSIS FORMULATION AND DIGITAL SIMULATION

Three phases of interaction analysis formulations and corresponding simulations resulted during the study period. Separate digital simulations and the associated user information were derived on the basis of each analytical formulation. The formulations are categorized by the following:

- Rigid space station with two flexible controllable appendages in a zero "G" orbit environment
- Flexible space station with two flexible controllable appendages and four flexible non-controllable appendages in a zero "G" orbital environment
- Flexible space station with four flexible non-controllable appendages in an artificial "G" orbital environment.

A detailed description and derivation of each of the formulations that were digitally programmed are contained in the following report subsections.

4.1 RIGID SPACE STATION/FLEXIBLE CONTROLLED APPENDAGES

The interaction dynamics study simulation is designed to determine the effects of important solar array structural characteristics on the motion of an orbiting space station. Two flexible solar arrays are connected to the space station by means of rigid driver assemblies which are totally constrained in translation and allowed two rotational degrees of freedom for each driver about the attachment point. The array drivers are rotated to obtain the desired sun/solar array aspect. The space station is attitude stabilized by a Control Moment Gyro System (CMG) which is augmented by a reaction control system to provide maneuver capability and "momentum dumping". The simulation model utilized for this system is described below:

- The space station and the two rigid array drivers are each modeled as rigid bodies with each of the rigid drivers permitted to rotate about the spacecraft attachment points along an axis parallel to the spacecraft roll axis and an axis normal to that in the plane of the solar array. The rigid array driver rotation may be additionally constrained in rotational freedom by user input to the digital simulation.
 - The flexible array is modeled by the synthetic modes technique of Likins (Reference 4.1), i.e., the array is modeled in terms of a finite number of orthogonal cantilever modes suitably augmented by six synthetic modes to assure that the steady state (rigid) conditions for constant acceleration are met. The appendage equation is an exact formulation which includes all accelerations of the appendage base. In accord with the synthetic modes approach, the effect of the two flexible arrays upon the rigid body system is obtained in the form of the equivalent force and torque exerted by the flexible arrays upon the system by the modal accelerations. The effects of the rigid system motion upon the flexible arrays is accounted for by system acceleration in the appendage equation of each array.
 - Maneuver and attitude control of the space station together with the solar array orientation control are modeled in terms of the appropriate time varying forces and torques produced by closed loop guidance equations. The guidance and steering commands are computed external to the dynamics section and provide the space station with a fixed orientation relative to orbit coordinates.

Formulation of these equations is given in the Command and Control description.

• The array driver gear train for the axis parallel to the space station roll axis is modeled as an ideal mechanical transformer referenced to the spacecraft side of the gear train. The other driver axis is directly driven. Either axis of both drivers may be locked.

The simulation orbit generator uses Lyddane's method for near earth orbits which may be circular. (Ref. 4.2).

A block diagram representation of the simulation program is presented in the following where important logical switches and function interconnection have been delineated (Figures 4-1 thru 4-5).

4.1.1 CONVENTIONS AND COORDINATE SYSTEMS

The coordinate systems given below represent the main computational frames utilized in the simulation.



Figure 4-1 Overall Flow Chart


Figure 4-2 Blk 1 Edit Routine Flow Chart



Figure 4-3 Blk 2 - Major Cycle Flow Chart





4-3d



Figure 4-5 Blk 4 - Integration Package Flow Chart

4.1.1.1 COORDINATE FRAME 1



I - In equatorial plane pointing at Aries

- $\mathbf{Z}_{\mathbf{I}}$ Points to geocentric north pole
- Y₁ Provides right handed set in order X₁, Y₁, Z₁

4.1.1.2 COORDINATE FRAME 2

Local Level (RTN) Coordinate

R		Cθ	Sθ	0	1	0	0		ິດລ	SΩ	0	xI
Т	= .	-S0	Cθ	0	0	Ci	Si		- SΩ	CΩ	0	Υ _I
א		0.	0	1	0	-Si	Ci		0	0	1	Z _I
					ς.		1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 - 1997 -	•				

R - directed along geocenter to space station radius vector

N - normal to orbit plane

T - completes right handed set (R, T, N)

where

 Ω - longitude of ascending node

i - orbital inclination

 θ - sum of argument of perigee (ω), plus the true anomaly (ν)

C,S - cosine and sine functions

As indicated above, the Euler rotations are about the Z_{I} , the X_{I} and the N axis where X_{I} is the X_{I} axis after rotation through Ω .

4.1.1.3 COORDINATE FRAME 3

Commanded Space Station Coordinates

The desired space station orientation X_c , Y_c , Z_c represent, in order,

the commanded orientation of the space station roll, pitch and yaw axes. The vehicle command orientation is related to the R, T, N set by means of three Euler rotations:



4.1.1.4 COORDINATE FRAME 4

Actual Space Station Coordinates

The actual orientation of the space station is similarly related to the RTN frame by a set of Euler angles α , β , γ . The order of rotations is the same as for the command angles and the resultant direction cosine matrix is given below in expanded form

 X_{s}, Y_{s}, Z_{s} - actual roll, pitch, and yaw axes of the space station

α , β , γ - Euler angles

in more condensed form



4.1.1.5 COORDINATE FRAME 5

Solar Array Driver Coordinates

Each rigid solar array driver is constrained to rotate about an axis parallel to the space station roll (X_s) axis and about the array vane (Z_A) axis where the resultant set of axes for the first driver are X_{A_1} , Y_{A_1} and Z_{A_1} as shown below. The resultant direction cosine relation is in expanded form

				•	· · ·	· · · ·					
x _c		[1	0	٢٥	Г ^{СВ} с	SBc	0	ΓCαc	0	-Sac	R
Y _c	=	0	CY _c	Sγ _c	-Sβ _c	C ^β c	0	0	1	0	Т
^z c_		0	- ^{Sγ} c	СŶс	0	0	1	^{Sα} c	0	^{Cα} c	N

Sec. 18 Same

 X_{c} - commanded roll axis

 Y_c - commanded pitch axis

^Z_c - commanded yaw axis

 $\alpha_{c}^{\beta}, \beta_{c}^{\gamma}, \gamma_{c}$ - commanded Euler angles

or in more condensed fashion



4-6**-A**



In condensed form



The second rigid driver nominally has the same Y_A axis as the first and the remaining axes are reversed.

$$\begin{bmatrix} x_{A_2} \\ Y_{A_2} \\ Z_{A_2} \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} C_1 \\ C_1 \end{bmatrix} \begin{bmatrix} x_s \\ Y_s \\ Z_s \end{bmatrix}$$

$$\begin{bmatrix} C_2 \\ C_2 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} C_1 \\ C_1 \end{bmatrix}$$

$$\begin{bmatrix} x_{A_2} \\ Y_{A_2} \\ Z_{A_2} \end{bmatrix} = \begin{bmatrix} C_2 \\ C_2 \\ Y_s \\ Z_s \end{bmatrix}$$

where

 $Y_{A(1,2)}$ is normal to the plane of the (1,2) array and is pointed to the sun. $Z_{A(1,2)}$ is normal to the space station roll axis and in the plane of the array. The Z_A axis provides the seasonal adjustment and is referred to as

 $X_{A(1,2)}$ makes X_A , Y_A , Z_A a right handed set.

the vane axis.

4.1.1.6 COORDINATE FRAME 6

Control Moment Gyro Orientation

The Control Moment Gyro is oriented with respect to the spacecraft axes in the following manner:

or

$$\begin{bmatrix} x_{G} \\ Y_{G} \\ Z_{G} \end{bmatrix} = \begin{bmatrix} c_{G} \\ Y_{s} \\ Z_{s} \end{bmatrix}$$

Transformation from outer gimbal axes to inner gimbal axes is treated in the discussion of CMG dynamics.

Direction Cosine Identities



1,2 - driver bases w_i = rotation of iTH rigid body about its C of G.

.1.2 INITIALIZATION PROCEDURES

4.1.2.1 GENERAL INITIALIZATION PROCEDURES

The program is capable of initializing the simulation with any of the integrals or key parameters to user specified values. The input will utilize the Namelist feature of FORTRAN IV and the default (no input data) will be to use the values given in the Data Statements. Such a procedure will assure that any run will not fail because of omitted data and is at the same time extremely flexible.

4.1.2.2 DIRECTION COSINE INITIALIZATION

Space Station Commanded Attitude (C)

The basic philosophy used for space station orientation is "belly down" or earth pointing attitude control. Therefore the desired orientation can be specified in terms of the three Euler angles given in Section 1, α_c about T, β_c about N' and γ_c about R" (or yaw). Specification of these three commanded angles will give any desired space station attitude with respect to the (R, T, N) orbit unit vector set. The steps in computing (C_c), the direction cosine matrix of desired space station orientation are as follows:

Α.

Computation of Inertial to RTN Direction Cosine Matrix (C_{c})



where \overline{R} is the vector position of the orbiting space station in ECl coordinates and \overline{V} is the vector velocity.

$$\begin{bmatrix} C_{s} \\ Initial \end{bmatrix} = \begin{bmatrix} \hat{R}_{1} & \hat{R}_{2} & \hat{R}_{3} \\ \hat{T}_{1} & \hat{T}_{2} & \hat{T}_{3} \\ \hat{N}_{1} & \hat{N}_{2} & \hat{N}_{3} \end{bmatrix}$$
Initial
(RTN + ECI)
Note that $\begin{bmatrix} C_{s} \end{bmatrix}$ is computed throughout the simulation.

B. Computation of the Commanded Attitude Matrix (C_{Ac})

Performing the multiplications in the order indicated in Section 4.1.3 we find:

$$\begin{bmatrix} C\beta_{c} C\alpha_{c} & S\beta_{c} & -S\alpha_{c} C\beta_{c} \\ S\gamma_{c} S\alpha_{c} & & & \\ C\gamma_{c} S\beta_{c} C\alpha_{c} & C\gamma_{c} C\beta_{c} & C\gamma_{c} S\beta_{c} S\alpha_{c} \\ & & + C\alpha_{c} S\gamma_{c} \\ S\gamma_{c} S\beta_{c} C\alpha_{c} & -S\gamma_{c} S\beta_{c} S\alpha_{c} \\ C\gamma_{c} S\alpha_{c} & -S\gamma_{c} C\beta_{c} & C\gamma_{c} C\alpha_{c} \end{bmatrix}$$

(Command S/S + RTN)

where

C and S imply cosine and sine respectively. (C_{Ac}) is computed once, at the start of the simulation.

Computation of the Command Direction Cosine Matrix (C_c)

 $\begin{vmatrix} C_c \end{vmatrix} = \begin{vmatrix} C_{Ac} \end{vmatrix} \begin{vmatrix} C_s \end{vmatrix}$

([C_c] is computed throughout the simulation) in which the commanded roll axis unit vector and commanded pitch axis unit vector are respectively:

$$\begin{split} \overline{R}_{o}_{c} \Big|_{ECI} &= (C_{c}(11), C_{c}(12), C_{c}(13)) \\ \overline{P}_{i}_{c} \Big|_{ECI} &= (C_{c}(21), C_{c}(22), C_{c}(23)) \\ \\ \underline{Space Station Attitude}_{ECI} (C_{o}) \\ \hline \Big|_{C_{o}} \Big|_{Initial}^{T} &= \left[C_{A}^{i} \right] \left[C_{s} \right]_{Initial} \end{split}$$

where $[C_A]$ is the direction cosine matrix of actual space station attitude relative to the RTN set. This matrix is identical in structure to the $[C_{Ac}]$ matrix except that α , β and γ are used in place of α_c , β_c , and γ_c respectively. $[C_0]^T$ is defined as the transpose of $[C_0]$ matrix.

SOLAR ARRAY

The solar array drivers are allowed to rotate about an axis parallel to the roll axis and about the array vane axis. In addition, the two vane axes are 180 degrees apart and the two axes normal to the arrays are parallel. Therefore only two angles are needed to specify the direction cosines of both arrays relative to the spacecraft. \emptyset_{A_0} is the rotation of the vane axis of Driver 1 about the space station roll axis. ${}^{\psi}A_0$ is the rotation of the solar array about the vane axis.

$$\begin{bmatrix} X_{A1} \\ Y_{A1} \\ Z_{A1} \end{bmatrix} = \begin{bmatrix} C\psi_{A_{0}} & S\psi_{A_{0}} & 0 \\ S\psi_{A_{0}} & C\psi_{A_{0}} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\phi_{A_{0}} & S\phi_{A_{0}} \\ 0 & -S\phi_{A_{0}} & C\phi_{A_{0}} \end{bmatrix} \begin{bmatrix} x_{s} \\ Y_{s} \\ z_{s} \end{bmatrix}$$

or

$$\begin{bmatrix} x_{A1} \\ y_{A1} \\ z_{A1} \end{bmatrix} = \begin{bmatrix} c_1 \\ Initial \end{bmatrix} \begin{bmatrix} x_s \\ y_s \\ z_s \end{bmatrix}$$

and

$$\begin{array}{c} X_{A2} \\ Y_{A2} \\ z_{A2} \end{array} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix} \begin{array}{c} X_{A1} \\ Y_{A1} \\ z_{A1} \end{bmatrix}$$

Γ	-c ₁₍₁₁₎	-C ₁₍₁₂₎	-C ₁₍₁₃₎
C ₂ = Initial	C ₁₍₂₁₎	C ₁₍₂₂₎	^C 1(23)
	-C ₁₍₃₁₎	-C ₁₍₃₂₎	-C ₁₍₃₃₎

4.1.3 RIGID BODY EQUATIONS OF MOTION

4.1.3.1 GENERAL RIGID BODY DYNAMICS FORMULATION

The space station and the rigid array drivers are modeled as a subsystem of interconnected rigid bodies whose motion is described by the Newton-Euler equations of motion. This is shown in Figure 4.6. As stated earlier the effect of appendage dynamics is modeled as an external force and torque. The pertinent equations are given below:

System Force

$$m_{T} = \frac{d^{2}(\overline{R}_{0} + \overline{C})}{dt^{2}} = \overline{F}_{A_{J}} + \overline{F}_{F}$$

Space Station Moment

$$\frac{d}{dt} (\overline{L}_{0} (CG_{ss})) \bigg|_{I} = (\overline{C} - \overline{L}_{R}) \times \overline{F}_{R} - \sum_{J} \overline{r}_{J} \times \overline{F}_{H_{J}} - \sum_{T} \overline{T}_{J} + \overline{T}_{AC} + \overline{T}_{CMG}$$

Hinged Body Moment

$$\frac{d}{dt} (\overline{L}_{J} (CG_{J})) = \overline{T}_{AJ} + T_{J} + \overline{T}_{J} \times \overline{F}_{H_{J}}$$

J	-	Index of solar array. J is equal to 1 or 2
F _{AJ} , T _{AJ}	. .	are the force and torque exerted by the flexible array on each rigid driver
τ _Α _C	-	torque exerted on spacecraft by rigid driver along constrained axes
^m T	-	total system mass
0 _N	-	Newtonian reference point
0 _B	-	Spacecraft reference point
^{CG} s.s.	-	Space Station center of gravity
CG _{SYS}	-	Center of gravity for the entire rigid body system
ccj	-	Center of gravity for the J TH rigid driver
R ₀	-	Distance space station has moved from unperturbed orbital position
F _R	-	External force annlied by reaction control system
ĽJ	-	Angular Momentum of J TH rigid body
I = 0 1 2		



4-1**6**a

.

հ _յ	 Vector from space station reference point to hinge point for rigid drivers and CMG package
ī,	- vector from the respective hinge point to the J TH rigid body (on space station)
₽ _R	 vector from space station reference point to rocket location
כ	 vector from space station reference to rigid system CG
\overline{T}_J	 hinge torque on JTH driver produced by control system
r _J	- $(\overline{r}_{o} - \overline{h}_{J})$ hinge force moment arm
F _H J	 hinge force exerted by space station on JTH body
$\frac{d}{dt}$ ()	- implies differentiation w.r.t. an inertial reference frame
T _{C_MG}	- control torque exerted by the control moment gyros

Before proceeding further, it is instructive to present the principal coordinate frames and direction cosine identities to be utilized in the matrix formulation of these equations.

$$\left\{ \begin{array}{c} x_{s} \\ \end{array} \right\} = \begin{bmatrix} c_{0} \\ \end{array} \right]^{T} \left\{ \begin{array}{c} x_{I} \\ \end{array} \right\}$$
$$\left\{ \begin{array}{c} x_{A_{1}} \\ \end{array} \right\} = \begin{bmatrix} c_{1} \\ \end{array} \right]^{T} \left\{ \begin{array}{c} x_{s} \\ \end{array} \right\}$$
$$\left\{ \begin{array}{c} x_{A_{2}} \\ \end{array} \right\} = \begin{bmatrix} c_{2} \\ \end{array} \right]^{T} \left\{ \begin{array}{c} x_{s} \\ \end{array} \right\}$$

where



 $\left\{ x_{s} \right\}$



is the vector basis defined by unit vectors along X_s , Y_s and Z_s directions

 $\left\{ x_{A_{i}} \right\}$

is the vector basis for the iTH solar array

indicates that the transpose of the matrix is required.

We have previously shown how the C_0 , C_1 and C_2 matrices are initialized in terms of Euler angles. The updating of these time varying matrices during the course of the simulation will be performed by the following equation.

 $\begin{bmatrix} \dot{c}_i \end{bmatrix} = \begin{bmatrix} c_i \end{bmatrix} \begin{bmatrix} 0 & -w_{i3} & w_{i2} \\ w_{i3} & 0 & -w_{i1} \\ -w_{i2} & w_{i1} & 0 \end{bmatrix}$ $= \begin{bmatrix} c_1 \end{bmatrix} \begin{bmatrix} \tilde{w}_1 \end{bmatrix}$

where

w₁₁

 w_{i2}

are the rotational rates about iTH coordinate frame axes (i = 0, 1, 2). For i equals zero, these rates are the spacecraft roll, pitch and yaw rates. ^wi3 .

This equation is derived in Section 4.1.7. The four vector equations presented may now be formulated as a matrix equation in a convenient coordinate frame. In the equations that follow the space station frame was chosen for the system force and space station moment equations. Each driver moment equation is written in terms of driver coordinates.

In the following formulation the square brackets used to denote a matrix are dropped and it is assumed that all quantities given are in matrix format. A few useful identities are given below.

$$A \times B + \tilde{A}B$$

$$\tilde{A}B = -\tilde{B}A$$

$$m_{T} \begin{bmatrix} \ddot{R}_{0} + 2 \tilde{w}_{0} \dot{R}_{0} + (\tilde{w}_{0} \tilde{w}_{0} + \dot{\tilde{w}}_{0}) R_{0} \\ + (\tilde{w}_{0} \tilde{w}_{0} + \dot{\tilde{w}}_{0}) (\mu_{0} r_{0} + \sum_{J} \mu_{J} (h_{J} + C_{J} r_{J})) \\ + \sum_{J} \mu_{J} \begin{pmatrix} C_{J} (\tilde{w}_{J} \tilde{w}_{J} + \dot{\tilde{w}}_{J}) r_{J} \\ + 2 \tilde{w}_{0} C_{J} \tilde{w}_{J} r_{J} \end{pmatrix} \\ (SYSTEM FORCE)$$

$$\tilde{I}_{0} w_{0} + \tilde{w}_{0} \tilde{I}_{0} w_{0} = k_{R} F_{R} - \sum_{J=1}^{2} T_{J} + T_{CMG}$$

$$(SPACE STATION MOMENT) - \frac{2}{J=1}^{2} \tilde{r}_{J} F_{HJ} + T_{AC}$$

$$\frac{\pi}{I}_{J} (C_{J}^{T} \dot{w}_{0} + \dot{w}_{J} + (C_{J}^{T} w_{0}) \tilde{w}_{J}) \\ + (C_{J}^{T} w_{0} + w_{J}) \tilde{I}_{J} (w_{J} + C_{J}^{T} w_{0}) + \tilde{r}_{J} C_{J}^{T} F_{HJ}$$

$$J = 1,2$$

$$(RIGID DRIVER MOMENT)$$
where
$$F_{HJ} = m_{J} \begin{bmatrix} (\tilde{w}_{0} \tilde{w}_{0} + \dot{w}_{0}) (R_{0} + h_{J}) + 2\tilde{w}_{0} \dot{R}_{0} + \tilde{R}_{0} \\ + (2\tilde{w}_{0} C_{J} \tilde{w}_{J} + \dot{w}_{J}) r_{J} \\ + C_{J} (\tilde{w}_{J} \tilde{w}_{J} + \dot{w}_{J}) r_{J} \end{bmatrix}$$

$$(HINGE FORCE)$$

$$-C_{J} F_{AJ}$$

$$4-20$$

4-20

Æ

where

R ₀ , R ₀ and R ₀ - (3x1 matrix)	The "apparent" (space station referenced) acceleration of the space station reference point and its first two integrals.
μ _J (scalar) -	^m J/m _T
= I _J - (3x3 matrices)	Inertia tensor of the J TH rigid driver referenced to the driver basis and center of gravity.
= I ₀ (3x3 matrix)	Space station inertia tensor referenced to the space station basis and center of gravity.
W ₀ , W ₀ (3x1 matrix)	Space station angular accelera- tion and rate.
w_1, w_1 (3x1 matrix)	Driver angular accelerations and rates.
(3x1 matrix)	

4.1.3.2 MATRIX FORMULATION OF RIGID BODY DYNAMICS

The equations developed must now be rearranged in a form suitable for solution. This involves formulating the problem in terms of coefficients of \hat{R}_0 , \hat{w}_0 , \hat{w}_1 and \hat{w}_2 and then inverting the coefficient matrix to obtain these derivatives.

In addition some changes are required in the form of the equations to obtain the following model requirements:

- The rotational motion of the rigid solar array drivers is constrained to motion about an axis parallel to the spacecraft roll axis and an axis in the plane of the solar array normal to the space station roll axis.
- The gear ratio for the array rotation in the roll direction is explicitly incorporated into the moment equations by considering all array driver rotation on the space station side of the gear train.

In effect, this reduces the three equations for each rigid driver to two, the first of which is solved for the scalar variable \widehat{w}_{Ai} which is the driver rotation referred to the space station side of the gear box. The roll axis rotation of the driver is taken to be the orbit adjustment while the rotation about the array axis of symmetry is considered nominally to be the seasonal adjustment.

In addition the effect of the constrained axis of driver rotation (rotation about an axis normal to the roll axis and the vane or Z_A axis) must be included in the Space Station Moment Equation. This is done by solving for the constraint torque in terms of R_0 and w_0 and adding the terms in these variables to the equation of space station moment to obtain the set of ten scalar equations presented on the following page in matrix form.



Definitions -

c₁, c₂

 h_1, h_2

- Direction cosine matrix (3x3) relating driver bases to space station basis



direction cosines relating array basis to normally unconstrained axes

- direction cosines relating array basis to normally constrained axes

 3xl vectors in space station basis giving hinge position from reference point

I₀, I₁, I₂ - inertia matrices of space station, driver 1 and driver 2 respectively. Each is expressed in its own basis

K_G - gear ratio for array driver orbit adjust mechanism

1₁, 1₂ - vector from driver CG to appendage connection point given in the driver basis

m1, m2, mT - masses of array drivers and total
system respectively

· · ·		
	- vector from Newtonian reference to	
U .	space station reference point in	
•	space station basis	
0	- vector from reference point to spa	ce
•	station CG in space station basis	
r, r,	- vectors from hinge point to driver	
1 6	CG in the driver basis	
', r ₂ '	- vectors from hinge point to space	
1 2	station CG	
v 0	- rotation rate of space station	
∀ 1, ₩ ₂	- rotation rate of rigid driver (on	
1 2	array side of gear train)	
NAI, WAZ	- rotation rate of rigid driver on	
	space station side of gear box	
ົ້ງ	- matrix equivalent of vector cross	
	product	
μ ₁ , μ ₂	- mass fractions m ₁	^m 2
	$\mu_1 = \frac{1}{m_2} \mu_2 = \frac{1}{m_2}$	
	4	

Equation Set I - System Translation

$$[A_1] \ R_0] + [A_5] \ w_0] + [A_9] \ w_{A1}] + [A_{13}] \ w_{A2}] = F_1]$$

$$\begin{bmatrix} A_1 \end{bmatrix} = m_T \begin{bmatrix} I \end{bmatrix}$$

$$\begin{bmatrix} A_{5} \end{bmatrix} = -m_{T} \begin{pmatrix} \tilde{R}_{0} \end{bmatrix} + \mu_{0} \quad \tilde{r}_{0} \end{bmatrix} + \mu_{1} \quad \begin{pmatrix} h_{1} \end{bmatrix} + \begin{bmatrix} C_{1} \end{bmatrix} \quad r_{1} \end{bmatrix} \end{pmatrix}$$

$$+ \mu_{2} \quad \begin{pmatrix} h_{2} \end{bmatrix} + \begin{bmatrix} C_{2} \end{bmatrix} \quad r_{2} \end{bmatrix} \end{pmatrix}$$

$$\begin{bmatrix} A_{9} \end{bmatrix} = -m_{T} \quad \mu_{1} \quad \begin{bmatrix} C_{1} \end{bmatrix} \quad \tilde{r}_{1} \end{bmatrix} \quad \begin{bmatrix} C_{1} * \end{bmatrix}^{T} \quad \begin{bmatrix} \frac{1}{KG} & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} A_{13} \end{bmatrix} = -m_{T} \quad \mu_{2} \quad \begin{bmatrix} C_{2} \end{bmatrix} \quad [\tilde{r}_{2} \end{bmatrix} \quad \begin{bmatrix} C_{2} * \end{bmatrix}^{T} \quad \begin{bmatrix} \frac{1}{KG} & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{aligned} \mathbf{F}_{1} &= & \mathbf{F}_{R} \mathbf{J} + [\mathbf{C}_{1}] \mathbf{F}_{A1} \mathbf{J} + [\mathbf{C}_{2}] \mathbf{F}_{A2} \mathbf{J} \\ & 2 \quad [\tilde{w}_{0}] \quad \dot{k}_{0} \mathbf{J} + [\tilde{w}_{0}] \quad [\tilde{w}_{0}] \quad (\tilde{w}_{0}] \quad (\tilde{w}_{0}] + [u_{0} \quad \mathbf{r}_{0}]) \\ & + \quad [\tilde{w}_{0}] \quad [\tilde{w}_{0}] \quad ((h_{1}] + [\mathbf{C}_{1}] \quad \mathbf{r}_{1}) \mathbf{J} \quad \mu_{1} + (h_{2}] + [\mathbf{C}_{2}] \quad \mathbf{r}_{2} \mathbf{J}) \mu_{2}) \\ & + \quad \mu_{1} \quad ([\mathbf{C}_{1}] \quad [\tilde{w}_{1}] \quad [\tilde{w}_{1}] \quad \mathbf{r}_{1}] \quad + \quad 2 \quad [\tilde{w}_{0}] \quad [\mathbf{C}_{1}] \quad [\tilde{w}_{1}] \quad \mathbf{r}_{1}]) \\ & + \quad \mu_{2} \quad ([\mathbf{C}_{2}] \quad [\tilde{w}_{2}] \quad [\tilde{w}_{2}] \quad \mathbf{r}_{2}] \quad + \quad 2 \quad [\tilde{w}_{0}] \quad [\mathbf{C}_{2}] \quad [\tilde{w}_{2}] \quad \mathbf{r}_{2}]) \end{aligned}$$

where

[I] is the identity matrix,

[] and () indicate that the cross product form is required

$$\begin{bmatrix} \tilde{x}_{1} \\ x_{2} \\ x_{3} \end{bmatrix} \begin{bmatrix} 0 & -x_{3} & x_{2} \\ x_{3} & 0 & -x_{1} \\ -x_{2} & x_{1} & 0 \end{bmatrix}$$

KG is the gear ratio for the array driver

 $[C_i^*]^T$ = transforms \hat{w}_{Ai} to array basis $(X_{Ai}, Y'_{Ai}, Z_{Ai})$

 $\begin{bmatrix} C_{i}^{*} \end{bmatrix}^{T} = \begin{bmatrix} C_{i1} & 0 \\ C_{i2} & 0 \\ 0 & 1 \end{bmatrix}$

 C_{i1} is the direction cosine between the X_s space station axis (roll) and X_{Ai}

 C_{i2} is the direction cosine relating X_s and Y_{Ai}

$$w_{i} = \begin{bmatrix} C_{i1} & 0 \\ C_{i2} & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \\ \end{bmatrix} \hat{w}_{Ai2}$$

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Equation Set II - Space Station Rotation

$$\begin{bmatrix} A_{2} & \ddot{R}_{0} \end{bmatrix} + \begin{bmatrix} A_{6} & \dot{w}_{0} \end{bmatrix} + \begin{bmatrix} A_{10} & \dot{w}_{A1} \end{bmatrix} + \begin{bmatrix} A_{14} & \dot{w}_{A2} \end{bmatrix} = F_{2} \end{bmatrix}$$

$$\begin{bmatrix} A_{2} & = m_{1} & \left(- [\tilde{r}_{1}] + [C_{1}^{**}] & [\tilde{r}_{1}] & [C_{1}]^{T} \right) + m_{2} & \left(- [\tilde{r}_{2}] + [C_{2}^{**}] & [\tilde{r}_{2}] & [C_{2}]^{T} \right) \end{bmatrix}$$

$$\begin{bmatrix} A_{6} & = [I_{0}] + m_{1} & [\tilde{r}_{1}] & (R_{0}] + h_{1} \end{bmatrix} + \begin{bmatrix} C_{1} & r_{1} \end{bmatrix} \right)$$

$$+ m_{2} & [\tilde{r}_{2}] & (R_{0}] + h_{2} \end{bmatrix} + \begin{bmatrix} C_{2} & r_{2} \end{bmatrix} \right)$$

$$+ \begin{bmatrix} C_{1}^{**} & [I_{1}] & [C_{1}]^{T} & -m_{1} & [\tilde{r}_{1}] & [C_{1}]^{T} & (R_{0}] + h_{1} \end{bmatrix} + \begin{bmatrix} C_{1} & r_{1} \end{bmatrix} \right)$$

$$+ \begin{bmatrix} C_{2}^{**} & [I_{2}] & [C_{2}]^{T} & -m_{2} & [\tilde{r}_{2}] & [C_{2}]^{T} & (R_{0}] + h_{2} \end{bmatrix} + \begin{bmatrix} C_{2} & r_{2} \end{bmatrix} \right)$$

$$\begin{bmatrix} A_{10} & = + m_{1} & [\tilde{r}_{1}] & [C_{1}] & [\tilde{r}_{1}] & [C_{1}^{*}]^{T} & \begin{bmatrix} 1/KG^{2} & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} A_{14} & = + m_{2} & [r_{2}'] & [C_{2}] & [\tilde{r}_{2}] & [C_{2}']^{T} & \begin{bmatrix} 1/KG^{2} & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} F_{2} \end{bmatrix} = - \begin{bmatrix} \tilde{k}_{r} \end{bmatrix} F_{R} \end{bmatrix} - T_{1} \end{bmatrix} - T_{2} \end{bmatrix}$$

$$= \begin{bmatrix} \tilde{w}_{0} \end{bmatrix} \begin{bmatrix} I_{0} \end{bmatrix} w_{0} \end{bmatrix} + \begin{bmatrix} 1/KG & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/KG & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/KG & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/KG & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/KG & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} T_{1} \end{bmatrix} \begin{bmatrix} T_{2} \end{bmatrix} F_{H2}^{T} + T_{CMG}^{T} \end{bmatrix}$$

$$= \begin{bmatrix} T_{1} \end{bmatrix} \begin{bmatrix}$$

where $r_1 = r_0 - h_1$ $F_{H1} = F_{H2} - are the hinge force equations less$ $the linear terms in <math>R_0$, w_0 , and w_1

The terms in C_i^{**} represent the effect of the normally constrained rigid driver axis moment on the space station moment equation

 $C_{i}^{**} = \begin{bmatrix} C_{i} \end{bmatrix} \begin{bmatrix} +C_{i12} \\ -C_{i11} \end{bmatrix} \begin{bmatrix} C_{i12} - C_{i11} \\ 0 \end{bmatrix}$

i = 1,2 gives the projection of constrained axis component of the iTH driver variables onto the space station-axes. Equation Set III - Rigid Driver 1 Dynamics

The dynamics of the X_{A1} and Y_{A1} axes are restricted to rotation about the X_s direction.

$$[A_3] \ddot{R}_0] + [A_7] \ddot{w}_0] + [A_{11}] \ddot{w}_{A1}] + [A_{15}] \ddot{w}_{A2}] = F_3$$

$$[A_3] = + [C_1^*] [m_1] [r_1] [C_1]^T$$

$$\begin{bmatrix} A_{7} \end{bmatrix} = \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} C_{1}^{*} \end{bmatrix} \begin{bmatrix} I_{1} \end{bmatrix} \begin{bmatrix} C_{1} \end{bmatrix}^{T} - m_{1} \begin{bmatrix} \tilde{r}_{1} \end{bmatrix} \begin{bmatrix} C_{1} \end{bmatrix}^{T} \begin{pmatrix} R_{0} \end{bmatrix} + h_{1} \end{bmatrix} + \begin{bmatrix} C_{1} \end{bmatrix} \begin{bmatrix} r_{1} \end{bmatrix} \tilde{r}_{1} \end{bmatrix} \tilde{r}_{1}$$

$$\begin{bmatrix} A_{11} \end{bmatrix} = \begin{bmatrix} 1/KG^2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} C_1^* \end{bmatrix} (\begin{bmatrix} I_1 \end{bmatrix} - m_1 \begin{bmatrix} \tilde{r}_1 \end{bmatrix} \begin{bmatrix} \tilde{r}_1 \end{bmatrix}) \begin{bmatrix} C_1^* \end{bmatrix}^T$$

 $[A_{15}] = 0$

$$\begin{aligned} \mathbf{F}_{3} \end{bmatrix} &= \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{C}_{1}^{*} \end{bmatrix} \begin{bmatrix} \mathbf{T}_{A1} \end{bmatrix} + \left(\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{T}_{1} \end{bmatrix} \right) KG \\ &- \begin{bmatrix} \mathbf{I}_{1} \end{bmatrix} \left(\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{w}_{0} \end{bmatrix} \right) \tilde{\mathbf{w}}_{1} \end{bmatrix} \\ &- \left(\begin{bmatrix} \mathbf{I}_{1} \end{bmatrix} \left(\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{w}_{0} \end{bmatrix} \right) \tilde{\mathbf{w}}_{1} \end{bmatrix} \\ &- \left(\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{w}_{0} \end{bmatrix} \right) \tilde{\mathbf{w}}_{1} \end{bmatrix} \\ &- \left(\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{w}_{0} \end{bmatrix} \right) \tilde{\mathbf{w}}_{1} \end{bmatrix} \\ &- \left[\begin{bmatrix} \mathbf{v}_{1} \end{bmatrix} \left[\begin{bmatrix} \mathbf{C}_{1} \end{bmatrix}^{T} & \mathbf{F}_{H1} \end{bmatrix} \right] \end{aligned}$$

Equation Set IV - Rigid Driver 2 Dynamics

$$\begin{bmatrix} A_{4} \end{bmatrix} \quad \ddot{R}_{0} \end{bmatrix} + \begin{bmatrix} A_{8} \end{bmatrix} \quad \dot{w}_{0} \end{bmatrix} + \begin{bmatrix} A_{12} \end{bmatrix} \quad \dot{w}_{A1} \end{bmatrix} + \begin{bmatrix} A_{16} \end{bmatrix} \quad \dot{w}_{A2} \end{bmatrix} = F_{4} \end{bmatrix}$$

$$\begin{bmatrix} A_{4} \end{bmatrix} = + \begin{bmatrix} C_{2}^{*} \end{bmatrix} \quad m_{2} \begin{bmatrix} \tilde{r}_{2} \end{bmatrix} \quad [C_{2}]^{T}$$

$$\begin{bmatrix} A_{8} \end{bmatrix} = \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} C_{2}^{*} \end{bmatrix} \quad [C_{2}]^{T} - m_{2} \begin{bmatrix} \tilde{r}_{2} \end{bmatrix} \quad [C_{2}]^{T} \quad (R_{0}] + h_{2} \end{bmatrix} + \begin{bmatrix} C_{2} \end{bmatrix} \quad r_{2} \end{bmatrix})^{T}$$

$$\begin{bmatrix} A_{16} \end{bmatrix} = \begin{bmatrix} 1/KG^{2} & 0 \\ 0 & 1 \end{bmatrix} \quad \begin{bmatrix} C_{2}^{*} \end{bmatrix} \quad ([I_{2}] - m_{2} \begin{bmatrix} \tilde{r}_{2} \end{bmatrix} \begin{bmatrix} \tilde{r}_{2} \end{bmatrix} \quad [C_{2}]^{T} \\ F_{4} \end{bmatrix} = \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \quad \begin{bmatrix} C_{2}^{*} \end{bmatrix} \quad ([C_{2}^{*}] + ([C_{2}]^{T} \quad T_{2}]) \\ \begin{bmatrix} T_{A2} \end{bmatrix} + ([C_{2}]^{T} \quad w_{0}])^{*} \quad w_{2} \end{bmatrix} - \begin{bmatrix} \tilde{r}_{2} \end{bmatrix} \begin{bmatrix} C_{2} \end{bmatrix}^{T} \quad F_{H2} \end{bmatrix} \\ - ([C_{2}]^{T} \quad w_{0}])^{*} + [\tilde{w}_{2}]) \quad \cdot \quad [I_{2}] \quad (w_{2}] + [C_{2}]^{T} \quad w_{0}]_{1} \end{bmatrix}$$

where

$$w_{1}^{T} = \begin{bmatrix} C_{1}^{*} \end{bmatrix}^{T} \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \hat{w}_{A11}^{T}$$
$$w_{2}^{T} = \begin{bmatrix} C_{2}^{*} \end{bmatrix}^{T} \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \hat{w}_{A21}^{T}$$
$$w_{A22}^{T}$$

and

$$[\dot{c}_1] = [C_1] [\tilde{w}_1]$$

 $[\dot{c}_2] = [C_2] [\tilde{w}_2]$
4.1.3.3 APPLICATION OF ADDITIONAL CONSTRAINTS

The constraint torque imposed by the rigid driver axis simultaneously normal to the roll axis and the array vane axis has been incorporated into simulation by:

Solving the driver equations for the constraint torque about the locked axis.

 $T_{Con} = f (R_0, w_0, w_0, T_{A_i}, F_{H_i})$

The moment applied to the space station is the negative of this constraint torque which is applied by combining the terms in R_0 and w_0 with those of A_2 and A_6 for the unconstrained case and adding the remaining terms to F_2 .

This results, as we have previously noted, in the addition of a set of terms preceded by C_i^{**} which is the direction cosine matrix relating the normally constrained driver axis to the space station axes.

We could perform the same procedure for additional constraints imposed by the user and solve a further reduced matrix. However, since the values of these constraints are of real interest for engineering analysis an alternative scheme is utilized:

The matrix equation for the affected axis is changed from an equation in R_0 , w_0 and w_A to an equation in R_0 , w_0 and T_C , the constraint torque. In other words, we now solve for the constraint torque instead of the rotational acceleration.

In terms of matrix changes the appropriate row of matrix A_{11} and A_{16} is changed to (-10) if the axis parallel to the roll axis is constrained or (0-1) if the vane axis is constrained.

Since the affected matrix variable is now constraint torque, the columns of A_{10} and A_{14} are changed to give the projection of the negative of constraint torque in space station coordinates. If the vane axis is constrained,

the second column of these matrices become

1

0



If the other axis is constrained the first column is changed to

and both are changed accordingly if the drivers are completly locked.

4.1.4 FLEXIBLE ARRAY DYNAMICS

4.1.4.1 GENERAL FORMULATION OF A FLEXIBLE APPENDAGE EQUATION

The model for the flexible array dynamics is adapted from the synthetic modes approach developed by Likens in Reference 4.1. The utilization of orthogonal modes augmented by a set of synthetic modes is an attractive approach for simulating the dynamics of large, driven, flexible structures from both a modeling and a computational efficiency viewpoint. The geometry of the system considered is shown in Figure 4-7.

Major Assumptions and Conventions

- Each flexible array utilizes the basis associated with the rigid driver to which it is fixed. This is the basis in which the equations are solved.
- The particle masses have negligible inertias about their respective CG's
 - The appendage deflections are sufficiently small that conventional structural analysis is valid; i.e., the system is linear.

Force on iTH Particle

$$\overline{t}_{i} = m_{i} \frac{d^{2}}{dt^{2}} (\overline{R}_{0} + \overline{h}_{J} + \overline{u}_{J} + \overline{r}_{i} + U_{i})$$



In order to simplify the notation in the following list:

$$\frac{R_{0}}{M_{0}} = C_{J}^{T} R_{0}$$

$$\frac{W_{0}}{M_{0}} = C_{J}^{T} W_{0} C_{J}$$

$$\begin{bmatrix} \frac{\ddot{R}_{0}}{H_{0}} + 2\tilde{W}_{0} & \frac{\dot{R}_{0}}{H_{0}} + (\frac{\ddot{W}_{0}}{H_{0}} + \frac{\ddot{W}_{0}}{H_{0}}) & (R_{0} + \frac{\dot{H}_{J}}{H_{J}} + R_{J} + r_{i} + U_{i}) \\
+ (\tilde{W}_{J} + \tilde{W}_{J} \tilde{W}_{J}) & (R_{J} + r_{i} + U_{i}) + 2\tilde{W}_{0} \tilde{W}_{J} & (R_{J} + r_{i} + U_{i}) \\
+ 2 & (\tilde{W}_{0} + W_{J}) & U_{i} + U_{i}$$

$$J=1, 2, \quad i=1, 2, \dots, n$$

Because of the linear elastic properties of the flexible array the force F_J is also related to the deformation of the array and the applied loads:

$$[M] q + [K] q = - [G] q - [B] q + L$$

where

$$q = [U_1^{1} U_2^{1} U_3^{1} U_1^{2} U_2^{2} U_3^{2} - - U_1^{N} U_2^{N} U_3^{N}]$$

K is the symmetric stiffness matrix

L is the matrix of applied loads and rigid body forcing functions.

^m1 0. ^m2 ^m3 (0 ^m4 · 0

M

3n x 3n



3n x 3n

 $w_{\rm T} = w_0 + w_{\rm J}$

$$= \begin{bmatrix} m_{1} & \hat{\Omega} & 0 & 0 & 0 & 0 \\ 3x3 & & & & \\ 0 & m_{2} & \hat{\Omega} & 0 & 0 & 0 \\ 3x3 & & & & \\ 0 & 0 & m_{3} & \hat{\Omega} & 0 & 0 \\ & & & \ddots & \end{bmatrix}$$
$$\frac{\hat{\Omega}}{\hat{\Omega}} = \tilde{w}_{T} + \tilde{w}_{0} & \tilde{w}_{0} + \tilde{w}_{J} & \tilde{w}_{J} + 2 & \tilde{w}_{0} & \tilde{w}_{J}$$
$$= \tilde{w}_{T} + \tilde{w}_{T} & \tilde{w}_{T}$$

B

Before formulating the expression for the L term the following identities are useful

Т

.. E

$$\sum_{E} = \begin{bmatrix} E & \vdots & E \\ 3x3 & \vdots & 3x3 & \vdots \\ \end{bmatrix}^{T}$$
$$\hat{\sum}_{EO} \begin{bmatrix} E & \vdots & O \\ 3x3 & \vdots & 3x3 \end{bmatrix}^{T}$$
$$\hat{\sum}_{OE} \begin{bmatrix} O & \vdots & E \\ 3x3 & \vdots & 3x3 \end{bmatrix}^{T}$$

where



where





$$\begin{bmatrix} C \end{bmatrix} = 2 \underbrace{w_0}_{E} \frac{\dot{R}_0 + \tilde{w}_0}{Q} \underbrace{w_0}_{E} (\underline{R}_0 + h_J) + \tilde{w}_T w_T \hat{x}_J + \tilde{r}_J \dot{w}_T$$

$$\begin{bmatrix} D \\ 3nx3n \end{bmatrix} = \begin{bmatrix} \left(\sum_{E} \frac{w_0}{Q} \right)^{\tilde{r}} \left(\sum_{E} \frac{w_0}{Q} \right)^{\tilde{r}} + \left(\sum_{E} w_J \right)^{\tilde{r}} \left(\sum_{E} w_J \right)^{\tilde{r}} \end{bmatrix}$$

$$+ 2 \left(\sum_{E} \frac{w_0}{Q} \right)^{\tilde{r}} \left(\sum_{E} w_J \right)^{\tilde{r}}$$

$$\begin{bmatrix} \sum_{E} w \right)^{\tilde{r}} = \begin{bmatrix} \tilde{w} & 0 & 0 & 0 \\ 0 & \tilde{w} & 0 & 0 \\ 0 & 0 & \tilde{w} & 0 \end{bmatrix}$$

0

w.__

0

Let

Ü

=

$$\hat{\mathbf{w}}_{\mathrm{T}} \int \mathbf{L} = -\mathbf{M} \left(\sum_{\mathrm{E}} \hat{\boldsymbol{\Sigma}}_{\mathrm{EO}}^{\mathrm{T}} - \left(\sum_{\mathrm{E}} \tilde{\boldsymbol{\ell}}_{\mathrm{J}} - \tilde{\mathbf{r}} \right) \hat{\boldsymbol{\Sigma}}_{\mathrm{OE}}^{\mathrm{T}} \right) \frac{\mathbf{u}}{\mathbf{U}}$$

0

0

. 0

$$- M\left(\sum_{E} C + D \overline{r}\right) + \lambda$$

where

$$\ell_J = \ell_J - r_J$$

Conversion to Normal Coordinates

There exists a unique orthogonal transformation which has the following properties:

a.
$$\phi^{T} M \phi = [E]$$

b. $\phi^{T} K \phi = \begin{bmatrix} \sigma_{1}^{2} & \sigma_{2}^{2} & \sigma_{N}^{2} \end{bmatrix} = \overline{\sigma^{2}}$

such that

 $q(R,t) = \phi(R) \eta(t)$

A finite number of cantilever modes $(\overline{\phi})$ satisfying (a) and (b) are utilized to transform the appendage equation:

Mon + Kon = -Gon - Bon + L

Premultiplying by $\overline{\phi}^T$ we have

 $\ddot{\vec{n}} + 2\xi \overline{\sigma} \dot{\vec{n}} + \overline{\sigma}^2 \eta = \overline{\phi}^T G \overline{\phi} \dot{\vec{n}} - \phi^T B \overline{\phi} \eta + \overline{\phi}^T L$

$\overline{\eta}, \overline{\eta}, \overline{\eta}$ are N x 1 matrices where

N is the number of cantilevered modes utilized. Note that a modal damping term has been arbitrarily inserted in the classic manner of structural analysis.

Now since the appendage mass, mode shape, and geometry are all known a priori and remain invariant, the appendage equation can be reformulated to reduce the required computational effort

$$\ddot{\overline{n}} + 2\xi \overline{\sigma} \overline{\overline{n}} + \overline{\sigma}^2 n = -A_1 \dot{\overline{n}} - A_3 \overline{n}$$
$$-A_4 C - A_5$$
$$-\Delta^2 \ddot{U} + \phi^T L$$

where

4.1.4.2 ADDITION OF SYNTHETIC MODES

A particularly important term in the Appendage Equation is the next to the last term $\Delta' U$ where

$$\Delta^{\prime} = -\overline{\phi}^{T} M \left(\sum_{E} \hat{\Sigma}_{EO}^{T} - \sum_{E} \hat{\Sigma}_{OE}^{T} - \hat{r} \hat{\Sigma}_{OE} \right)$$

If we define $\Delta = \lim \Delta'$ it can be shown that

$$\Delta^{T} \Delta = \begin{bmatrix} M_{A} & P_{A} & M_{A} \\ 3x3 & 3x3 \\ P_{A} & M_{A} & I_{A} \end{bmatrix}$$

where

M_A - Appendage mass

I_A - Apendage inertia

 P_A - Centroid vector for appendage relative to attachment point.

Since $\Delta^{T}\Delta' \neq \Delta^{T}\Delta$, the rigid or steady state representation of the appendage is inaccurate. In order to circumvent this difficulty, synthetic modes may be added in terms of additional rows for Δ' .

Let
$$\Delta = \Delta^{\prime\prime}$$

The synthetic modes are then defined as

$$\ddot{\overline{n}}_{s} + 2 \, \overline{\xi}_{s} \overline{\sigma}_{s} \dot{\overline{n}}_{s} + \overline{\sigma}_{s}^{2} n_{s} = \Delta^{--} \ddot{U}_{J}$$

To avoid impacting the frequency range of interest the following procedures is utilized: $(\sigma_s)_{MIN} >> \sigma_{MAX}$

ξ > • 71

The synthetic modes are computed in terms of a difference equation to avoid potential integration instability:

$$\eta_{s}(NT) = a\Delta^{-1}U(NT) + b\Delta^{-1}U(NT-T)$$

 $-d n_s(NT-T) - e n_s(NT-2T)$

for each synthetic mode.

Six synthetic modes will be employed, each one will be chosen to satisfy the constraints for a given column and thus the first synthetic mode will have six co-efficients, the second will have five and so forth, until the sixth mode which has only q^{-1} coefficient.

The capability of using a steady state mode function is also included in this case

$$\eta_{s}(NT) = K\Delta^{\prime}U(NT)$$

where

$$\zeta = \frac{a+b}{1+d+e}$$

 $\Lambda^{\prime} = \mathbf{f}^{\prime}$

Forces and Torques Induced by the Flexible Appendage (from Likins)

$$f' = \sum_{E}^{T} M\phi\sigma^{2} \eta$$

$$1' = \left(\sum_{E}^{T} \tilde{r} + \tilde{\ell}_{J} \sum_{E}^{T}\right) M\phi\sigma^{2} \eta$$

where f ' and 1 ' are respectively, the force and torque upon the rigid driver Let

$$\Lambda^{T} = \left(\sum_{EO} \sum_{E} + \sum_{E} \left(\sum_{E} \tilde{r} + \tilde{\ell}_{J} \sum_{E}\right)\right) M \phi \sigma^{2} \eta$$

 $\Lambda^{\prime} = -\Delta^{T} \sigma^{2} \eta$ (for ideal Δ^{T})

'or the case where Δ is approximated by a finite number of cantilever modes augmented by the synthetic modes as discussed earlier

$$\Lambda^{-} = - \overline{\Delta}^{T} \overline{\sigma}^{2} \overline{\eta}$$

$$\overline{\Delta}^{\mathrm{T}} = [\overline{\Delta}_{1} \ \overline{\Delta}_{2}]^{\mathrm{T}}$$

where

$$\overline{\sigma^2 \eta}$$
 - external force impressed upon JTH rigid driver (F_{AJ})

 $\overline{\Delta}_2^T \overline{\sigma}^2 \overline{\eta}$ - external torque impressed upon JTH rigid driver (T_J) Difference Equation Formulation for Synthetic Modes

Given an equation of the form q + a q + b q = F (t),

 $\overline{\Delta}_1^{\mathrm{T}}$

A difference equation formulation utilizing a staircase step representation of F(t) can be readily obtained by the use of Z transform theory. The equivalent block diagram corresponding to this approach is shown in the following figure.



C(NT) - Output of system to staircase step representation of F(t) at t = NT

T - Sampling interval

S - LaPlace transform variable

In terms of the sampled data Z transform:

$$\frac{C(Z)}{F(Z)} = \frac{Z-1}{Z} \frac{3}{2} \left(\frac{1}{S(S^2 + aS + b)} \right)$$

Let





Laplace Transform Z Transform 1/SZ/Z-1 $-(S+\alpha)/[(S+\alpha)^2 + \beta^2] = \frac{(Z^2 - Ze^{-\alpha T} \cos \beta T)}{(Z^2 - 2Ze^{-\alpha T} \cos \beta T + e^{-2\alpha T})}$ $- \alpha / [(S+\alpha)^2 + \beta^2]$ $-\frac{\alpha}{\beta(7^2-27e^{-\alpha T}\cos\beta T)}$ $\frac{C(Z)}{F(Z)} = \frac{Z-1}{Z} \frac{1}{b} \begin{bmatrix} z^3 - 2Z^2 e^{-\alpha T} \cos \beta T + e^{-2\alpha T} Z \\ -Z^3 + Z^2 (e^{-\alpha T} \cos \beta T - \frac{\alpha}{\beta} e^{-\alpha T} \sin \beta T) \\ \frac{+Z^2 - Ze^{-\alpha T} \cos \beta T + \frac{\alpha}{\beta} Ze^{-\alpha T} \sin \beta T}{(Z-1) (Z^2 - 2Ze^{-\alpha T} \cos \beta T + e^{-2\alpha T})} \end{bmatrix}$ $= \frac{1}{b} \begin{bmatrix} z (1 - e^{-\alpha T} \cos \beta T - \alpha / \beta e^{-\alpha T} \sin \beta T) \\ + (e^{-2\alpha T} - e^{\alpha T} \cos \beta T + \frac{\alpha}{\beta} e^{-\alpha T} \sin \beta T) \\ \hline z^2 - 2z e^{-\alpha T} \cos \beta T + e^{-2\alpha T} \end{bmatrix}$

The equivalent difference equation is:

$$C(NT) = a_1 F (NT-T) + a_2 F (NT-2T)$$

- $a_3 C (NT-T) - a_4 C (NT-2T)$

1

where

$$a_{1} = (1 - e^{-\alpha T} \cos \beta T - \alpha/\beta e^{-\alpha T} \sin \beta T)$$

$$a_{2} = (e^{-2\alpha T} - e^{-\alpha T} \cos \beta T + \alpha/\beta e^{-\alpha T} \sin \beta T)$$

$$a_{3} = -2e^{-\alpha T} \cos \beta T$$

$$a_{4} = e^{-2\alpha T}$$

X(NT) - present sampled value of X

X(NT-T) - previous sampled value of X

4.1.4.3 PRESIMULATION COMPUTATIONS

The form of the appendage equation given in the preceding section is:

$$\ddot{n}$$
 + 25 σ \ddot{n} + σ^2 \bar{n} = $-A_1\dot{n}$ - $A_3\bar{n}$ - A_4C - A_5 - $\Delta \ddot{U}$

In their most general form these equations require the multiplication of 3nx3n matrices where n is the number of mass points used to define the appendage. The form of the mass matrix employed allows considerable simplification of the computation and permits the calculation of a set of coefficients of much reduced order prior to the actual simulation.

Computation of A₂, A₄, A₆

From the preceding equation we can define the A_1 and A_3 matrices in terms of rigid body rotation parameters and A_2 , a constant matrix:

$$A_{1_{\ell m}} = \sum_{i=1}^{3} \sum_{J=1}^{3} 2 \widetilde{w}_{T_{iJ}} A_{2_{iJ\ell m}}$$
$$A_{3_{\ell m}} = \sum_{i=1}^{3} \sum_{J=1}^{3} \widetilde{\alpha}_{iJ} A_{2_{iJ\ell m}}$$

where

k

mk

$$A_{2_{IJ\ellm}} = \sum_{k=1}^{n} \phi_{kJ}^{m} \phi_{ki}^{\ell} m_{k}$$

 ℓ , m - cantilever mode numbers (0 < ℓ , m \leq N)

- mass point number $(0 < k \le n)$

i, J - identify the three components of the n mode shape displacements (0 < i, J < 3)

 k^{TH} mass element (0 < $k \leq n$)

 A_4 is an Nx3 matrix which multiplies the 3x1 C matrix which is a summation of rigid acceleration terms

$$A_{4_{li}} = \sum_{k=1}^{n} \phi_{ki}^{l} m_{k}$$

 ℓ - cantilever mode number (0 < $\ell \leq N$)

i - component identifier (0 < i < 3)

The A_5 matrix can be reduced to the product of a constant matrix and a matrix of rigid angular accelerations:

$$A_{5_{\ell}} = \sum_{J=1}^{3} \sum_{i=1}^{3} d_{Ji} A_{6_{Ji}}$$

where

$$A_{6_{Jil}} = \sum_{k=1}^{n} m_{k} \phi_{ki}^{l} r_{ki}$$

where

- d_{Ji} are
 - are rigid acceleration terms
- r_{ki} are the coordinates of the undeflected mass points relative to the attachment point.

Computation of the Δ Matrix

The Δ matrix is an (N+6x6) matrix which is composed entirely of constant parameters. It is formed by calculating the unaugmented Δ matrix Δ' (Nx6) shown below and augmenting this matrix to obtain the desired $\Delta^T \Delta$ product.

$$\Delta^{-} = -\phi^{T} M \begin{pmatrix} \Sigma & \widehat{\Sigma}^{T} - \widetilde{b}_{i} & \Sigma & \widehat{\Sigma}^{T} \\ E & EO & E & OE \end{pmatrix}$$

where each \tilde{b}_i is a 3 x 3 matrix formed by $\tilde{b}_i = (r_i + 1_j)$

The matrix multiplication may be performed yielding the general formula for Δ , an (Nx6) matrix shown below:

a)
$$\Delta_{1m}^{-} = \sum_{i=1}^{n} m_{i} \phi_{im}^{1}$$

for l and m such that $1 \le l \le N$ and $1 \le m \le 3$

b)
$$\Delta_{1m} = \sum_{i=1}^{n} m_i \left(\phi_{ik}^1 b_{ij} - \phi_{ij}^1 b_{ik} \right)$$

for l and m such that $1 \le l \le N$ and $4 \le m \le 6$ where the J's and k's are related to m by:

Six rows will be added to the \triangle matrix to form the \triangle matrix. These rows will be added in such a manner so that the new \triangle matrix will represent the real world. This is accomplished by performing the multiplication $\triangle^T \triangle$. This multiplication should equal.

	MA	0	0	0	P _{A3} M _A	-P _{A2} M _A
	0 .	MA	0	-P _{A3} M _A	0	PAIMA
$\Delta^{T}\Delta =$	0	0	MA	PA2 ^M A	-P _{A1} M _A	0
(ideal)	. 0	-P _{A3} ^M A	P _{A2} M _A	IA11	I _{A12}	I _{A13}
	P _{A3} M _A	0	-P _{A1} M _A	I _{A21}	I _{A22}	I _{A23}
•	-P _{A2} M _A	P _{A1} ^M A	- O	- ^I A31	I _{A32}	I _{A33}

where

 $\dot{1}$

 M_A is the total mass of the flexible appendage



a .

 $P_{A_{1,2,3}}$ is the coordinates of the appendage mass centroid, with respect to the attachment

point.		<u>n</u>				
	P _{Ai}	$=\sum_{k=1}$	(r _{ki}	+ 1,)	^m k	/M _A
			· · ·	· · · ·	. L	

I_A is the moment of inertia with respect to the attachment point.

$$I_{A} = -\sum_{k=1}^{n} m_{k} \tilde{b}_{k}^{2}$$

Since every element of the $\Delta^{T}\Delta$ product has the form:

$$(\Delta^{T}\Delta)_{iJ} = \Delta_{1i} \Delta_{1J} + \Delta_{2i} \Delta_{2y} - \dots - \Delta_{Ni} + \Delta_{NJ}$$

We can add a row of augmenting Δ 's to obtain a perfect row in the $\Delta^T \Delta$ matrix; e.g., add

 $\Delta_{N+1,1}$ $\Delta_{N+1,1}$ to idealize 1, 1 element $\Delta_{N+1,1}$ $\Delta_{N+1,2}$ to idealize 1, 2 element and so forth.

We can perform the same function for the second row and by making its first entry zero, avoid changing the previously obtained result. This process continues until six rows of augmenting Δ 's have been developed. (The last row is a single element.)

The six augmenting Δ rows are defined by the following set of equations:

$$\Delta_{(N+1)1} = \left[M_{A} - \sum_{i=1}^{N} \Delta_{i1} \Delta_{i1} \right]^{1/2}$$
$$\Delta_{(N+1)j} = -\left(\sum_{i=1}^{N} \Delta_{ij} \Delta_{i1} \right) / \Delta_{(N+1)1} \quad j = 2, 3, 4$$

$$\Delta_{(N+1)5} = \left(P_{A3}M_A - \sum_{i=1}^N \Delta_{i5} \Delta_{i1} \right) / \Delta_{(N+1)1}$$

$$\Delta_{(N+1)6} = \left(-P_{A2}M_A - \sum_{i=1}^N \Delta_{i6} \Delta_{i1}\right) / \Delta_{(N+1)1}$$

$$\Delta_{ij} = 0$$
 $i = N+k$
 $j = 1,2,...k-1$
 $k = 2,3,4,5,6$

$$\Delta_{(N+2)2} = \left[M_{A} - \sum_{i=1}^{N+1} \Delta_{i2} \Delta_{i2} \right]^{1/2}$$

$$\Delta_{(N+2)j} = -\left(\sum_{i=1}^{N+1} \Delta_{ij} \Delta_{i2}\right) / \Delta_{(N+2)2} \quad J = 3,5$$

$$\Delta_{(N+2)4} = -P_{A3}M_A \sum_{i=1}^{N+1} \Delta_{i4} \Delta_{i2} / \Delta_{(N+2)2}$$

$$\Delta_{(N+2)6} = P_{A1}M_{A} - \sum_{i=1}^{N+1} \Delta_{i4} \Delta_{i2} / \Delta_{(N+2)2}$$

$$\Delta_{(N+3)3} = \left[M_{A} - \sum_{i=1}^{N+2} \Delta_{i3} \Delta_{i3} \right]^{1/2}$$

$$\Delta_{(N+3)4} = P_{A2}M_A - \sum_{i=1}^{N+2} \Delta_{14} \Delta_{i3} / \Delta_{(N+3)3}$$

$$\Delta_{(N+3)5} = P_{A2}M_{A} - \sum_{i=1}^{N+2} \Delta_{i5} \Delta_{i3} / \Delta_{(N+3)3}$$

$$\Delta_{(N+3)6} = P_{A2}M_A - \sum_{i=1}^{N+2} \Delta_{i6} \Delta_{i3} / \Delta_{(N+3)3}$$

$$\Delta_{(N+4)4} = \left[I_{A11} - \sum_{i=1}^{N+3} \Delta_{i4} \Delta_{i4} \right]^{1/2}$$

$$\Delta_{(N+4)5} = I_{A21} - \sum_{i=1}^{N+3} \Delta_{i5} \Delta_{14} / \Delta_{(N+4)4}$$

$$\Delta_{(N+4)5} = I_{A21} - \sum_{i=1}^{N+3} \Delta_{i5} \Delta_{14} / \Delta_{(N+4)4}$$

$$\Delta_{(N+4)6} = I_{A31} - \sum_{i=1}^{N+3} \Delta_{i6} \Delta_{i4} / \Delta_{(N+4)6}$$

$$\Delta_{(N+5)5} = \left[I_{A22} - \sum_{i=1}^{N+4} \Delta_{i5} \Delta_{i5} \right]^{1/2}$$

$$\Delta_{(N+5)6} = I_{A23} - \sum_{i=1}^{N+4} \Delta_{i6} \Delta_{i5} / \Delta_{(N+5)5}$$

$$\Delta_{(N+6)6} = \left[I_{A33} - \sum_{i=1}^{N+5} \Delta_{i6} \Delta_{i6} \right]^{1/2}$$

As we have shown the equations, the inertial quantities not absorbed by the modal representation are accounted for by the synthetic modes representation. For the specific case which we are considering, the allocation of some of the mass and inertia to the rigid body driver is advisable. This requires that biased values of mass, moment of inertia and centroid location be used in lieu of the values now used.

4.1.5 GUIDANCE AND CONTROL

The STRISS simulation has two principal guidance and control functions:

- The space station is to be oriented with the roll axis normal to the orbit plane and yaw axis along the negative of the radius vector from the geocenter to the spacecraft.
- The two solar arrays are driven normal to the space station to sun line within the limits of permissible array motion.

4, 1.5.1 SPACE STATION GUIDANCE

Since the commanded attitude is fixed relative to the R, T, N frame, computation of the space station commands consist of updating the (C_s) matrix as a function of orbit position and then multiplying by the constant (C_{Ac}) matrix to obtain the current value of \overline{R}_0 and \overline{P}_i .

$$[C_c] = [C_{Ac}] [C_s]$$

 $\overline{R}_{0_{c}}$ = row 1 of [C_c] (Commanded roll axis)

 $\overline{P}_{i_c} = row 2 \text{ of } [C_c]$ (Commanded pitch axis)

where the vectors given above are expressed in inertial coordinates. For the nominal case where the roll axis is normal to the orbit plane and yaw is along the $-\overline{R}$ direction, the required Euler angle commands are:

$$\alpha_{c} = -90^{\circ}$$
$$\beta_{c} = \gamma_{c} = 0$$

4.1.5.2 SOLAR ARRAY GUIDANCE

Orientation commands for the solar array drivers are obtained by using the cross product of the array Y_A axis and the earth-to-sun unit vector as an

error signal. When the Y_A axis, which is normal to the plane of the solar array, is pointing toward the sun the error is null. Other orientations result in an error signal of proper sign being generated. The components of the error signal along the permitted axes of notation are then input to the array driver control equations.

Earth-to-Sun Unit Vector

$$\hat{s} = Cr EC1 Sr C\Delta Sr S\Delta$$

 Γ - rotation of sun in ecliptic plane

 Δ - deflection of ecliptic

$$\hat{\mathbf{S}} = [\mathbf{C}_0]^T \hat{\mathbf{S}}_{EC}$$

Cross Product Law

$$\hat{E}1 = \hat{Y}_{A1} \times \hat{S} \Big|_{SS}$$
$$\hat{E}2 = \hat{Y}_{A2} \times \hat{S} \Big|_{SS}$$

 $\phi_{AE1} = \hat{E}1(1)$

 $\phi_{AE2} = -\hat{E}^2(1)$

 $\psi_{AE1} = \hat{1}_{\psi 1} \cdot \hat{E}_{1}$

 $\Psi_{AE2} = \hat{1}_{\psi 2} \cdot E_2$



 ϕ_{AEi} and ψ_{AEi} are the solar array error components along the axes of allowable rotation for the iTH driver.

4.1.5.3 SPACE STATION CONTROL

The space station attitude controls are affected by one of two methods:

- Control Moment Gyro (CMG)
- Reaction Control System

The program permits the selection of one or the other by setting a logical flag.

4. 1. 5. 3. 1 Control Moment Gyro (CMG) Dynamics

The CMG modelled in the simulation is the Three Parallel Mount (3 PM) configuration shown in Figure 4-8. This CMG and the mathematical description utilized were developed by the General Electric Company Defense Electronics Division (References 4.3 through 4.5) and utilizes three individual two degree of freedom CMG's mounted with their outer gimbal axes parallel. The CMG is mounted in the spacecraft with the parallel outer gimbal axes aligned with the space station axis of minimum moment of inertia which is, in the present case, the roll axis.

CMG COORDINATE FRAMES

The CMG will be mounted in the space station with the following orientation of the Outer Gimbal basis relative to the space station axes.

٦				Г	
X _G	- - 	0	1	0	Xs
Y _G	=	0	0	1	Ys
ZG	· · · · · · · · · · · · · · · · · · ·	_ 1	0	0	Zs
		L		ا ل	

This orientation assumes that minimum momentum requirement is along the X_s (roll) spacecraft axis where

$$\begin{bmatrix} x_{s} \\ Y_{s} \\ z_{s} \end{bmatrix} \begin{bmatrix} roll \\ pitch \\ yaw \end{bmatrix} \begin{bmatrix} w_{ro} \\ w_{pi} \\ w_{ya} \end{bmatrix} \begin{pmatrix} \phi \\ \theta \\ \psi \end{bmatrix}$$





In the parallel mount configuration employed there are three individual CMG gyros.



The I^{TH} CMG wheel momentum vector, $\overline{h},$ in the inner gimbal space is

$$h_{x_{i}} = 0 \qquad h - magnitude of each
CMG momentum
$$h_{y_{i}} = h \cos \gamma_{i}$$

$$h_{z_{i}} = h \sin \gamma_{i} \qquad \gamma_{i} - inner gimbal angle
of ITH CMG$$$$



The CMG momentum wheel vector is, in Outer Gimbal space:

h _{xo}		-	h	cos	Υi	sin	θ _i
h _{yo}	=		h	cos	Υi	cos	$^{\theta}\mathbf{i}$
hzo			h	sin	γ _i		* 1
	•						



In the parallel mount configuration employed there are three individual CMG gyros.

CMG TORQUE EQUATIONS

$$\overline{T}_g = \dot{\overline{H}}_g = H + \overline{w}_g \times H$$
 (Torque Equation)

where

T_g - external torque exerted <u>on</u> CMG

 change in magnitude of momentum vector in CMG coordinates

wg

o H_g

rotation rate of CMG in inertial space

H - CMG momentum vector -

$$H = \overline{h}_{wheel} + \overline{I}_{Gimbal} \overline{w}_{g}$$

$$H = \overline{h} + \overline{I}_{Gimbal} \overline{w}_{g}$$

$$\overline{W}_{g} \times \overline{H} \approx \overline{w}_{g} \times \overline{h}$$

where

I _{Gimbal}	is the CMG moment of inertia matrix (inertia tensor)
	 implies the derivative with respect to inertial 'coordinates
	<pre>o implies the derivative with respect to CMG coordinates</pre>

Initial Conditions

Initially the CMG's have, for the nominal case, zero inner and outer gimbal angles. Thus we have

 $\theta_1 = 0^{\circ}$ $\theta_2 = 120^{\circ}$ $\theta_3 = 240^{\circ}$

and the net momentum of the system is identically zero.

The torque on the space station is equal to $-\overline{T}_{G}$

$$T_{out} = -\left(\begin{bmatrix} - & 0 \\ I_{Gimbal} & \frac{0}{w_g} + \overline{w}_g & \overline{h} \end{bmatrix} \right)$$

Performing all computations in the Inner Gimbal space we have

$$T_{out_{xi}} = -I_{Gi} \dot{\gamma}_{i} + w_{zi} h \cos \gamma - w_{yi} h \sin \gamma$$
$$T_{out_{yi}} = w_{xi} h \sin \gamma$$

$$\Gamma_{out_{zi}} = -I_{Go} \ddot{\alpha} - w_{xi} h \cos \gamma$$

where

w_i is the total inertial rate of the iTH CMG gyro with respect to inertial space

$$w_{xi} = \dot{\gamma} + \Omega_{xi}$$
$$w_{yi} = \Omega_{yi}$$
$$w_{zi} = \dot{\alpha} + \Omega_{zi}$$

where Ω is defined as:



and

 α , γ ; α , γ are the scalar derivatives of outer and inner gimbal angles and gimbal rates, respectively.

Therefore,

 $\begin{bmatrix} x_{i} = I_{Gi} \dot{\gamma} + (\dot{\alpha} + w_{ro}) h \cos \gamma - \Omega_{yi} h \sin \gamma \\ y_{i} = (\dot{\gamma} + \Omega_{xi}) h \sin \gamma \\ \vdots & \vdots & \vdots \\ z_{i} = I_{Go} \dot{\alpha} - (\dot{\gamma} + \Omega_{xi}) h \cos \gamma \end{bmatrix}$
$$I_{Gi} = J_{Gi}$$

$$I_{Go} = J_{Go} + J_{Gi(Z)} \cos^2 \gamma + J_{Gi(Y)} \sin^2 \gamma$$

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let

$$\alpha_{I} = \alpha + w_{ro}$$

$$\gamma_{\rm I} = \gamma + \Omega_{\rm xi}$$

$$\begin{bmatrix} T_{out} \\ (i^{TH}CMG) \end{bmatrix} \begin{bmatrix} x_i & I_{G1} \dot{\gamma} + \dot{\alpha}_I h \cos \gamma - \Omega_{yi} h \sin \gamma \\ \dot{\gamma}_i &= \dot{\gamma}_I h \sin \gamma \\ z_i & I_{G0} \ddot{\alpha} - \dot{\gamma}_I h \cos \gamma \end{bmatrix}$$

where

- I_{Gi} inertia tensor of inner gimbal expressed in the inner gimbal coordinate frame
- J_{Gi} inertia matrix of inner gimbal in inner gimbal coordinate
- I_{Go} inertia tensor of outer gimbal plus inner gimbal (suitably transformed) expressed in inner gimbal coordinates
- J_{GO} inertia matrix of outer gimbal in inner gimbal coordinates

CMG MOTOR TORQUE CONTROL LAW

$$T_{M1} = \left(\dot{\gamma}_{pi} - \dot{\gamma}_{i} - \frac{\dot{\alpha}_{i} + \cos \gamma}{K_{M1}} + \gamma_{Ai}\right) K_{M1}$$
$$T_{M2} = \left(\dot{\alpha}_{pi} - \dot{\alpha}_{i} + \frac{\dot{\gamma} + \cos \gamma}{K_{M2}}\right) K_{M2}$$

are the equations for the motor torque for inner and outer gimbals respectively, where the terms divided by KM1 and KM2 are used to decouple the torque motor dynamics between gimbals in a given CMG. KM1 and KM2 are, respectively, the inner and outer torque motor gains. If the motor torque exceeds the stiction torque plus the reaction torque produced by the CMG motion, the gimbal accelerates

$$\overline{T}_{GIMBAL} = \overline{T}_{M1_i} - \overline{T}_{REACT1} - \overline{T}_{RUN1}$$

if

$$(\overline{T}_{M1_{i}} - \overline{T}_{REACT1} - \overline{T}_{STICK1}) > 0$$

otherwise

T = 0 GIMBAL = 0 (INNER)

Similarly for

T_{GIMBAL} (OUTER)

where

$$\overline{T}_{REACT1} = T_{OUT_{xi}} - I_{Gi} \gamma$$

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in other words, T_{REACT} is the torque exerted by the gyro about the inner gimbal axis when the gimbal is not accelerated.

$$T_{REACT2} = T_{OUT_{3i}} - I_{Go} \alpha$$

^TSTICK is the stiction torque

^TRUN is the running torque



If $T_{GIMBAL} = 0$, it is necessary to set the gimbal rates about the affected axes to the component of body rate on the axis, e.g.

 $T_{\text{GIMBAL}} = 0 \quad \dot{\gamma}_{\text{I}} = \Omega_{\text{Xi}}, \quad \dot{\gamma} = 0$ (INNER)

 $T_{GIMBAL} = 0 \quad \alpha_1 = \Omega_{zi}, \quad \alpha = 0$ (OUTER)

COMPUTATION OF CMG GIMBAL COMMAND RATES

The terms γ_{pi} and α_{pi} represent the commanded gimbal rates and are obtained from the following computation:

$$T_{xc} = \int (T_{xe} - T_{xv}) dt$$
$$T_{yc} = \int (T_{ye} - T_{yv}) dt$$
$$T_{zc} = \int (T_{ze} - T_{zv}) dt$$

where

T₍₎e is the disturbance torque applied to the CMG by the control law. T₍₎v is the torque presently applied by the gyro to the vehicle $\dot{\gamma}_{pi} = -T_{zc}/3h \cos \gamma$ $\dot{\alpha}_{pi} = T_{xc} \cos \theta_i + T_{yc} \sin \theta_i + T_{AH_i}$

The last term in the second equation represents the torque term to eliminate "hang-up" or antiparallelism.

Another term

$$\gamma_{A1} = [(\gamma_1 + \gamma_2 + \gamma_3)/3 - \gamma_i] \cdot K_p$$

is added to the inner gimbal commanded angle to assure an equal distribution of orientation and reduce the possibility of gimbal limits being encountered

$$\begin{array}{c} \mathbf{T}_{\mathbf{x}\mathbf{e}} \\ \mathbf{T}_{\mathbf{y}\mathbf{e}} \\ \mathbf{T}_{\mathbf{z}\mathbf{e}} \end{array} = \begin{bmatrix} \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{1} \\ \mathbf{1} & \mathbf{0} & \mathbf{0} \end{bmatrix} \quad \begin{array}{c} (\mathbf{K}_{\mathbf{D}} \ \boldsymbol{\theta}_{\mathbf{\varepsilon}} \ - \ \mathbf{K}_{\mathbf{R}} \ \mathbf{w}_{\mathbf{p}\mathbf{i}}) \\ (\mathbf{K}_{\mathbf{D}} \ \boldsymbol{\theta}_{\mathbf{\varepsilon}} \ - \ \mathbf{K}_{\mathbf{R}} \ \mathbf{w}_{\mathbf{p}\mathbf{i}}) \\ (\mathbf{K}_{\mathbf{D}} \ \boldsymbol{\psi}_{\mathbf{\varepsilon}} \ - \ \mathbf{K}_{\mathbf{R}} \ \mathbf{w}_{\mathbf{y}\mathbf{a}}) \end{array}$$

where ϕ_{ϵ} , θ_{ϵ} , and ψ_{ϵ} are the space station attitude errors.

ATTITUDE ERROR EQUATIONS

$$EI = R_0 \times R_{0C}$$

$$\theta_{\varepsilon} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} C_0 \end{bmatrix}^T = E_1$$

$$EZ = P_i \times P_{iC}$$

where

R ₀ , P _i	-	unit vectors of roll and pitch axes in inertial coordinates
R _{oc} , P _{ic}		unit vectors of roll and pitch axes in in inertial coordinates
Ē ₁ , Ē ₂	-	error vectors in inertial coordinates
E ₁], E ₂]	-	3xl matrix representation of \mathbb{E}_1 and \mathbb{E}_2

and $[C_0^T]$ is used to transform the attitude errors into the space station frame.

CMG CONTROL TORQUE

The computation of the CMG control torque involves the transformation of the output torque of each CMG to the space station basis followed by the summation of the three torque terms:



To $\begin{bmatrix} To \\ TOTAL \end{bmatrix} = To_1 + To_2 + To_3$ $\end{bmatrix} ss = \end{bmatrix} ss = backstarter between the second seco$

4.1.5.3.2 Reaction Control System

A perfect proportional control system is modelled as an alternative to the Control Moment Gyro. The utilization of this alternative control system will permit more economical computation of the interaction dynamics.

$$To = \begin{bmatrix} I_{o(11)} \\ I_{o(22)} \\ I_{o(33)} \end{bmatrix} \begin{bmatrix} (K\theta \ \phi_{\varepsilon} + K\theta \ w_{ro}) \\ (K\theta \ \theta_{\varepsilon} + K\theta \ w_{pi}) \\ (K\theta \ \psi_{\varepsilon} + K\theta \ w_{ya}) \end{bmatrix}$$

Kθ, Kθ are control gains chosen to satisfy frequency and damping characteristics.

 ϕ_{ϵ} , θ_{ϵ} , and ψ_{ϵ} are computed in identical fashion to that presented in the previous section.

4.1.5.4 SOLAR ARRAY CONTROL EQUATIONS

The solar array drive controller mechanism consists of two first order filters which smooth the attitude error and driver rate signals. The two signals are weighted by appropriate gains, added together and then the sum is filtered by a third first order lag filter. The control system equations are adaptive with respect to driver inertia and roll axis gear ratio.

Filter Input Signals

\hat{w}_{11}	=	$b_{11} w_{11} + a_{11} \hat{w}_{11}_{-1}$
ŵ ₁₂	=	$b_{12} w_{12} + a_{12} w_{12}_{-1}$
w ₂₁		$b_{21} \hat{w}_{21} + a_{21} \hat{w}_{21}_{-1}$
w ₂₂	z ·	$b_{22} w_{22} + a_{22} \hat{w}_{22}_{-1}$
φ _{AE1}	=	$b_{11} \phi_{AE1} + a_{11} \hat{\phi}_{AE1} - 1$
ΨÂE1	=	$b_{12} \psi_{AE1} + a_{12} \psi_{AE1} - 1$
AE2	2	$b_{21} \phi_{AE2} + a_{21} \phi_{AE2}$
ΨAE2	8	$b_{22} \psi_{AE2} + a_{22} \psi_{AE2} - 1$

where

^w iJ	-	J^{TH} component of i TH driver rotation rate
[¢] AEi	-	roll axis error of i TH driver
^ψ ΑΕi	-	vane axis error of i TH driver
x	-	implies "smoothed" or filtered value of X
x1	-	implies immediately previous value of X
a _{iJ}	-	difference equation coefficient $a_{iJ} = exp\left(\frac{INT.STEP}{\tau_{iJ}}\right)$
^b iJ	-	$1 - a_{iJ}$
τ _i J	- ·	filter time constant

Computatio	on of Hinge Torque
^T C11 ⁼	$K\theta_{A} \cdot I_{1(R0)} \cdot \hat{\phi}_{AE1} + K\theta_{A} \cdot I_{1(R0)} \cdot \hat{w}_{11}$
T _{C12} =	$\hat{W}_{A} \cdot I_{1(33)} \cdot \hat{\psi}_{AE1} + K\dot{\theta}_{A} \cdot I_{1(33)} \cdot \hat{w}_{12}$
T _{C21} =	$\hat{\kappa}_{\theta_{A}} \cdot I_{2(R0)} \cdot \hat{\phi}_{AE2} + \hat{\kappa}_{\theta_{A}} \cdot I_{2(R0)} \cdot \hat{w}_{21}$
T _{C22} =	$\hat{W}_{A} \cdot I_{2(33)} \cdot \hat{\psi}_{AE2} + K \hat{\theta}_{A} \cdot I_{2(33)} \cdot \hat{W}_{22}$
Filtered	Hinge Torque
T _{C11} =	$b_{13} T_{C11} + a_{13} T_{C11} - 1$
$\hat{T}_{C12} =$	$b_{13} T_{C12} + a_{13} T_{C12}$
$\hat{T}_{C21} =$	$b_{13} T_{C21} + a_{13} T_{C21} - 1$
$\hat{T}_{C22} =$	$b_{13} T_{C22} + a_{13} T_{C22}$
• •	
Ke _A . Kė _A	- displacement and rate gains
^I J(R0)	- root sum square (RSS) of 11 and 22 elements of the J TH inertia matrix
	divided by KG
^I J(33) -	vane axis moment of inertia for J TH rigid driver
^a 13 -	$\exp\left(\frac{\text{Integration Step}}{\tau_{13}}\right)$
^b 13 -	$1 - a_{13}$

^b13

where

 $\hat{\boldsymbol{\zeta}}$

4.1.6 ORBIT GENERATOR

The calculation of the space station orbit is required to perform the previously specified guidance functions. Lyddane's method is employed in this simulation to obtain the desired orbital state vector. This method provides a closed form of solution and is much more efficient and economical than numerical integration techniques. WOLF R & D has developed a standardized Lyddane's method subroutine which will be utilized in the simulation. A complete analytic treatment is presented in Reference 4.2 and will not be repeated here. Lyddane's method is an extension of Brouwer's theory which provides closed form solution of orbits from mean orbital elements. A brief exposition of the method is given below.

Brouwer/Lyddane Theory

wosc_{t-to}

W¹¹

Brouwer's theory utilizes the standard elliptic elements a, e, I, w, M. The end product is typified by

 $= w'' + (t-t_0) f_1 (a'', e'', I'') + f_2 (a'', e'', I'', '', w'', M'')$

w_{osc}t-t

where

= ''real world'' or ''osculating'' value of the argument of perigee at time t-t.

"mean" value of the argument of perigee at time to
 These "mean" values are related to the constants of
 integration of the differential equations of motion.
 They do not represent real world values, but are
 required for the prediction of osculating elements.

The difficulty with Brouwer's theory is that the function f_2 involves terms with e" and sin I" in the denominator, and for very small values of e" and/or I", these terms present a situation which violates the basic foundations of "small perturbation" theory.

In order to overcome these difficulties, Lyddane used a different set of parameters, which were first suggested in the 1800's by Poincare'. These variables, which do not produce divisions by e or sin I, are:

a e (sin M) e (cos M) (sin I) (sin Ω) (sin I) (cos Ω) w + Ω + M

With these parameters, numerical values are computed for each of the above six quantities from equations similar to those given by Brouwer. Then the individual values for e and M are obtained from

 $e^2 = (e \sin M)^2 + (e \cos M)^2$

Tan M = $\frac{e (\sin M)}{e (\cos M)}$

Similar Procedures are performed for I and

, and finally, w is computed from

 $w = (w + \Omega + M) - \Omega - M$

4.1.7 EQUATIONS OF CONSTRAINED MOTION FOR A SYSTEM OF THREE RIGID BODIES





Consider the three body system presented above in which bodies one and two have unconstrained rotation about the two hinge points and neither of the two bodies can have translational motion with respect to the central (zero) body.

Definitions:

0 _N	- Newtonian reference point
0 _B	- Zero body reference point
R ₀	- Distance of body reference point from Newtonian reference
r _o	- Distance of zero body CG from body reference point
h _i i=1,2	- Distance between body reference point and i TH hinge point
r _i i=1,2	 distance between iTH hinge point and iTH body center of gravity
Ϝ ₀ , Τ ₀	- Vector force and torque applied to body zero
F ₁ , T ₁	- Vector force and torque applied to body one
F ₂ , T ₂	- Vector force and torque applied to body two

Coordinate Frames and Relationships

{I} -	Inertially	fixed	coordinate basis		
{X} -	Coordinate	basis	fixed	to body zero	
{x ₁ } -	Coordinate	basis	fixed	to body one	
${x_2} -$	Coordinate	basis	fixed	to body two	

where $\{I\}$ can be represented as the unity matrix and each of the others as a triad of or hogonal unit vectors in the form of a 3x3 matrix.

> {I} = $C_0 \{X\}$; {I}^T = {X}^T C_0^T {X} = $C_1 \{x_1\}$; {X}^T = {x_1}^T C_1^T {X} = $C_2 \{x_2\}$; {X}^T = {x_2}^T C_2^T

where

 C_i are the direction cosine matrices i=0,1,2

Vector Representation of Variables

Each of the variables defined as distances represent the scalar magnitude of the related vector quantity. Each of the vectors defined below is given in a "convenient" frame and choice of basis is, of course, arbitrary.

$$\mathbf{\overline{R}}_{0} = \{\mathbf{X}\}^{T} \mathbf{R}_{0}$$
$$\mathbf{\overline{r}}_{o} = \{\mathbf{X}\}^{T} \mathbf{r}_{0}$$
$$\mathbf{\overline{h}}_{i} = \{\mathbf{X}\}^{T} \mathbf{h}_{i}$$
$$\mathbf{\overline{r}}_{i} = \{\mathbf{x}_{i}\} \mathbf{r}_{i}$$

where the bars designate a vector quantity.

The following identity is offered

$$\dot{C}_{i} = C_{i} \tilde{w}_{i}$$
 $i = 0, 1, 2$

where



EQUATIONS OF MOTION

1.

Acceleration of the System Mass Center

$$m_{T} \frac{d^{2}}{dt^{2}} \left(\left(\overline{R}_{0} + \overline{C} \right) \right|_{I} = \overline{F}_{1} + \overline{F}_{2} \left(\begin{array}{c} \text{Forces external to the} \\ \text{System} \end{array} \right)$$

$$m_{T} = \text{ total system mass}$$

$$m_{0} = \text{ mass of body zero}$$

$$m_{1} = \text{ mass of body one}$$

$$m_{2} = \text{ mass of body two}$$

$$\overline{C} = \frac{m_{0} \overline{r}_{0} + m_{1} (\overline{R}_{1} + \overline{r}_{1}) + m_{2} (\overline{R}_{2} + \overline{r}_{2})}{m_{T}}$$

C is the system mass center relative to $O_{\mathbf{B}}$

Noting that F_1 is in body one coordinates and F_2 in those of body two, we have in the inertial basis $(\frac{d}{d\tau}(1) \equiv 0)$:

$$\begin{split} & \widetilde{m}_{\widetilde{T}} \quad \frac{d^{2}}{dt^{2}} \quad (\{\widetilde{I}\}^{\widetilde{T}} \ \widehat{c}_{0} \ \widetilde{R}_{0}) \\ & + \ \widetilde{m}_{0} \quad \frac{d^{2}}{dt^{2}} \quad (\{\widetilde{I}\}^{\widetilde{T}} \ \widehat{c}_{0} \ \widetilde{r}_{0}) \\ & + \ \widetilde{m}_{1} \quad \frac{d^{2}}{dt^{2}} \quad (\{\widetilde{I}\}^{\widetilde{T}} \ (\widetilde{c}_{0} \ h_{1} \ + \ \widetilde{c}_{0} \ \widetilde{c}_{1} \ \widetilde{r}_{1})) \\ & + \ \widetilde{m}_{2} \quad \frac{d^{2}}{dt^{2}} \quad (\{\widetilde{I}\}^{\widetilde{T}} \ (\widetilde{c}_{0} \ h_{2} \ + \ \widetilde{c}_{0} \ \widetilde{c}_{2} \ \widetilde{r}_{1})) \end{split}$$

where

$$\frac{d}{dt} (\{I\}^{T} : G_{\hat{0}} : R_{\hat{0}}\}) = \{I\}^{T} : G_{\hat{0}} : (\dot{R}_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : R_{\hat{0}})$$

$$\frac{d^{\hat{2}}}{dt^{2}} : (\{I\} : G_{\hat{0}} : R_{\hat{0}}\}) = \{I\}^{T} : G_{\hat{0}} : (\ddot{R}_{\hat{0}} + 2\ddot{\tilde{w}}_{\hat{0}} : \dot{R}_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : \ddot{\tilde{w}}_{\hat{0}} : R_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : \dot{\tilde{w}}_{\hat{0}} : R_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : R_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : R_{\hat{0}} + \ddot{\tilde{w}}_{\hat{0}} : R_{\hat{0}} : R$$

ŝ

and

$$\frac{d}{dt} \quad ((1) \ c_0 \ c_1 \ r_1) = (1)^{T} \ (c_1 \ c_1 \ r_1 + c_0 \ \tilde{w}_0 \ c_1 \ r_1 + c_0 \ c_1 \ \tilde{w}_1 \ r_1$$

 $\frac{d^2}{dt^2} (\{I\} C_0 C_1 r_1) = \{I\}^T \left[C_0 \tilde{w}_0 \tilde{w}_0 C_1 r_1 + C_0 \tilde{w}_0 C_1 \tilde{w}_1 r_1 \right]$ + $C_0 \tilde{w}_0 C_1 \tilde{w}_1 r_1 + C_0 C_1 \tilde{w}_1 \tilde{w}_1 r_1$ + $C_0 \tilde{w}_0 C_1 r_1 + C_0 C_1 \tilde{w}_1 r_1$ $= \{X\}^{T} \begin{pmatrix} \tilde{w}_{0} \ \tilde{w}_{0} \ C_{1} \ r_{1} + 2\tilde{w}_{0} \ C_{1} \ \tilde{w}_{1} \ r_{1} \\ + C_{1} \ \tilde{w}_{1} \ \tilde{w}_{1} \ r_{1} \\ \tilde{w}_{0} \ C_{1} \ r_{1} + C_{1} \ \tilde{w}_{1} \ r_{1} \end{pmatrix}$

This gives us, in the body zero basis

$$m_{T} \{X\}^{T} \begin{bmatrix} \ddot{R}_{0} + 2\tilde{w}_{0} \dot{R}_{0} + \tilde{w}_{0} \tilde{w}_{0} + \tilde{w}_{0} \hat{w}_{0} + \tilde{w}_{0} \hat{w}_{0$$

F

F₂

0

 $\mu_{0} = \frac{m_{0}}{m_{T}}$ $\mu_{1} = \frac{m_{1}}{m_{T}}$ $\mu_{2} = \frac{m_{2}}{m_{T}}$

2. Hinge Force Applied To The iTH Body

(i = 1, 2)



 \overline{F}_{Hi} , the hinge force, is given in the body zero, {X}, basis

.....

$$m_{i} \{I\}^{T} \frac{d^{2}}{dt} \left(C_{0} (R_{0} + h_{i}) + C_{0} C_{i} r_{i} \right) = \{I\}^{T} C_{0} (F_{Hi} + C_{i} F_{i})$$

$$\{x\}^{T} F_{Hi} = \{x\}^{T} m_{i} + \tilde{w}_{0} \tilde{w}_{0} + \tilde{w}_{0} (R_{0} + h_{i} + C_{i} r_{i}) + 2\tilde{w}_{0} C_{i} \tilde{w}_{i} r_{i} - C_{i} F_{i} + C_{i} (\tilde{w}_{i} \tilde{w}_{i} + \tilde{w}_{i}) r_{i}$$

Torque Equation For The iTH Body $\frac{d}{dt} \frac{\overline{L}_{i}}{t} = \overline{T}_{i} + \tilde{\ell}_{i} \overline{F}_{i}$ $-\widetilde{\mathbf{r}}_{i} \widetilde{\mathbf{F}}_{Hi} + \widetilde{\mathbf{T}}_{Hi}$ \overline{L}_i - Angular momentum about CG of iTH Body $\overline{L}_{i} - \{x_{i}\}^{T} \begin{bmatrix} I_{i} \end{bmatrix} \{x_{i}\} \cdot \begin{bmatrix} \{x_{i}\}^{T} w_{i} + \{x\}^{T} w_{0} \end{bmatrix}$ T_{Hi} - hinge torque $\frac{d}{dt} \left[\overline{L}_{i} \right]_{T} = \frac{d}{dt} \{I\}^{T} C_{0} C_{i} [I_{i}] C_{i}^{T} C_{0}^{T} \{I\} \left(\{I\}^{T} (C_{0} C_{i} w_{i}^{+} C_{0} w_{0}) \right)$ = {I}^T (C₀ \tilde{w}_0 C_i+C₀ C_i \tilde{w}_i) [I_i] {x_i}.{x_i}^T (w_i+C_i^T w₀) + $\{\mathbf{x}_{i}\}^{T}$ $[\mathbf{I}_{i}]$ $\left(\tilde{\mathbf{w}}_{i}^{T} \mathbf{C}_{i}^{T} \mathbf{C}_{0}^{T} + \mathbf{C}_{i}^{T} \tilde{\mathbf{w}}_{0}^{T} \mathbf{C}_{0}^{T}\right)$ $\{\mathbf{I}\}$. $\{\mathbf{I}\}^{T} \left(\mathbf{C}_{0} \mathbf{C}_{i} \mathbf{w}_{i}\right)$ $+ C_0 w_0$ + $\{x_i\}^T [I_i] \{x_i\} \cdot \{I\}^T / C_0 \tilde{w}_0 C_i w_i + C_0 C_i \tilde{w}_i w_i$ + $C_0 \tilde{w}_0 w_0$ + $C_0 C_i \dot{w}_i + C_0 \dot{w}_0$

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3.

noting that $\{x\} \cdot \{x\}^T$ equals the identity matrix

$$\frac{d}{dt} L_{i} \Big|_{I} = \{x_{i}\}^{T} \left(C_{i}^{T} \tilde{w}_{0} C_{i} + \tilde{w}_{i} \right) [I_{i}] \left(w_{i} + C_{i}^{T} w_{0} \right)$$

$$+ \{x_{i}\}^{T} [I_{i}] \left(\tilde{w}_{i}^{T} - C_{i}^{T} \tilde{w}_{0} C_{i} \right) \left(w_{i} + C_{i}^{T} w_{0} \right)$$

$$+ \{x_{i}\}^{T} [I_{i}] \left(C_{i}^{T} \tilde{w}_{0} C_{i} w_{i} + \dot{w}_{i} + C_{i}^{T} \dot{w}_{0} \right)$$

$$\{x_{i}\}^{T} \left(C_{i}^{T} \tilde{w}_{0} C_{i} + \tilde{w}_{i} \right) [I_{i}] \left(w_{i} + C_{i}^{T} w_{0} \right)$$

$$+ \{x_{i}\}^{T} [I_{i}] \left(\dot{w}_{i} + C_{i}^{T} \dot{w}_{0} \right)$$

$$+ \{x_{i}\}^{T} [I_{i}] \left(\tilde{w}_{i}^{T} C_{i}^{T} w_{0} - C_{i}^{T} \tilde{w}_{0} C_{i} w_{i} \right)$$

$$+ C_{i}^{T} \tilde{w}_{0} C_{i} w_{i}$$

We note that

$$(C_{i} w_{0})^{\tilde{}} = C_{i} \tilde{w}_{0} C_{i}^{T}$$

$$\tilde{A} B = -\tilde{B} A$$

$$\tilde{A}^{T} = -\tilde{A}$$

$$\tilde{A}^{T} = -\tilde{A}$$

$$\tilde{v}_{i}^{T} C_{i}^{T} w_{0} = -\tilde{w}_{i} C_{i}^{T} w_{0} = C_{i}^{T} \tilde{w}_{0} C_{i} w_{i}$$

: Two of the terms cancel giving

$$(\mathbf{x_{i}})^{T} \begin{pmatrix} \left(\mathbf{c_{i}}^{T} \mathbf{w_{0}} \right)^{T} + \tilde{\mathbf{w}_{i}} \right) [\mathbf{I_{i}}] \begin{pmatrix} \mathbf{w_{i}}^{T} \mathbf{c_{i}}^{T} \mathbf{w_{0}} \\ \mathbf{w_{i}}^{T} \mathbf{c_{i}}^{T} \mathbf{w_{0}} \end{pmatrix} = \{\mathbf{x_{i}}\}^{T} \begin{bmatrix} \mathbf{c_{i}}^{T} \mathbf{T}_{Hi} \\ -\tilde{\mathbf{r}_{i}} \mathbf{c_{i}}^{T} \mathbf{F}_{Hi} \\ -\tilde{\mathbf{r}_{i}} \mathbf{c_{i}}^{T} \mathbf{F}_{Hi} \\ + [\mathbf{I_{i}}] \mathbf{c_{i}}^{T} \tilde{\mathbf{w}_{0}} \mathbf{c_{i}} \mathbf{w_{i}} \end{bmatrix} = \{\mathbf{x_{i}}\}^{T} \begin{bmatrix} \mathbf{c_{i}}^{T} \mathbf{T}_{Hi} \\ -\tilde{\mathbf{r}_{i}} \mathbf{c_{i}}^{T} \mathbf{F}_{Hi} \\ \tilde{\mathbf{z}_{i}} \mathbf{F_{i}} + \mathbf{T}_{i} \end{bmatrix}$$

where T_{Hi} and F_{Hi} are given in the zero body basis and T_{i} , F_{i} are in the iTH body basis.

4.



External Moments on Body Zero

 $(-r_0 + h_1)^{\tilde{F}} - \overline{F}_{H1}$ -T_{H1} $(-r_0 + h_2)^{-F_{H2}}$ -T_{H2} $(-r_0 + \ell_0)^{-1} F_0 + T_0$

Reaction Torque

$$\frac{d \overline{L}_{0}}{dt} \bigg|_{I} = \{X\}^{T} \begin{bmatrix} \tilde{w}_{0} [I_{0}] w_{0} \\ \vdots \\ \vdots \\ \vdots \end{bmatrix}$$

$$\{x\}^{T} \begin{bmatrix} \tilde{w}_{0} & [I_{0}] & w_{0} \\ [I_{0}] & w_{0} \end{bmatrix} = \begin{bmatrix} (r_{0} + h_{1})^{2} & F_{H1} \\ (-r_{0} + h_{2})^{2} & F_{H2} \\ (-r_{0} + \ell_{0})^{2} & F_{0} \end{bmatrix} + T_{0} - T_{H1} - T_{H2}$$

Matrix Equations

Since $\{x\} \cdot \{x\}^T$ is equal to the identity matrix we can obtain a set of scalar matrix equations from the preceding by formally taking this product on both sides of the equation. For purposes of computer solution we shall also require a formulation of the form

$$[A] \quad X] = -I$$

$$[X]^{T} = [R_{0}, w_{0}, w_{1}, w_{2}]$$

and B is a function of external forces and terms in w_0 , w_1 , w_2 , \dot{R}_0 and R_0 . Noting the identity

$$X\tilde{Y} = -\tilde{Y}X$$

System Acceleration Equation
L.H.S.

$$m_T \ddot{R}_0] -m_T (R_0) \ddot{r} + N_0 r_0 \ddot{r} + N_1 (h_1] + C_1 r_1]) \ddot{r} + N_2 (h_2] + C_2 r_2]) \ddot{r}) \dot{w}_0$$

 $-m_1 C_1 \ddot{r}_1 \dot{w}_1 - m_2 C_2 \ddot{r}_2 \dot{w}_2$
R.H.S.
 $-m_T (2 \tilde{w}_0 \dot{R}_0 + \tilde{w}_0 \tilde{w}_0 R_0)$
 $-m_0 \tilde{w}_0 \tilde{w}_0 r_0 - m_1 \tilde{w}_0 \tilde{w}_0 (h_1 + C_1 r_1)$
 $-m_1 (2 \tilde{w}_0 C_1 \tilde{w}_1 r_1 + C_1 \tilde{w}_1 \tilde{w}_1 r_1)$
 $-m_2 (\tilde{w}_0 \tilde{w}_0 (h_2 + C_2 r_2) - 2 \tilde{w}_0 C_2 \tilde{w}_2 r_2)$
 $-m_2 (C_2 \tilde{w}_2 \tilde{w}_2 r_2)$
 $+ C_1 F_1 + C_2 F_2 + F_0$

NOTE: L.H.S. - implies "lefthand side" R.H.S. - implies "righthand side"

ITH Body Torque Equation L.H.S $\mathbf{m}_{i} \tilde{\mathbf{r}}_{i} C_{i}^{T} \tilde{\mathbf{R}}_{0} + \begin{bmatrix} \mathbf{I}_{i} \end{bmatrix} C_{i}^{T} - \mathbf{m}_{i} \tilde{\mathbf{r}}_{i} C_{i}^{T} (\mathbf{R}_{0} + \mathbf{h}_{i} + C_{i} \mathbf{r}_{i})^{T} \end{bmatrix} \mathbf{w}_{0}$ + ([I_i] - $m_i \tilde{r}_i \tilde{r}_i$) \dot{w}_i R.H.S. $\begin{array}{c} -m_{i} \tilde{r}_{i} C_{i}^{T} \\ + 2\tilde{w}_{0} C_{i} \tilde{w}_{i} r_{i} + C_{i} \tilde{w}_{0} \tilde{w}_{0} (R_{0} + h_{i} + C_{i} r_{i}) \\ + 2\tilde{w}_{0} C_{i} \tilde{w}_{i} r_{i} + C_{i} \tilde{w}_{i} \tilde{w}_{i} r_{i} \end{array} \right)$ $-\left[\begin{pmatrix} c_{i}^{T} w_{0} \end{pmatrix}^{\tilde{}} + \tilde{w}_{i} \end{bmatrix} [I_{i}] \begin{pmatrix} w_{i} + c_{i}^{T} w_{0} \end{pmatrix}$ - $[I_i] \left(C_i^T \tilde{w}_0 C_i w_i \right) + C_i^T T_{Hi}$ + $\tilde{l}_{i}F_{i} + T_{i}$ + m_i r_i F_i

Body Zero Torque Equation

L.H.S.

Terms in R₀

$$\left(m_{1}(-r_{0}+h_{1})^{+}+m_{2}(-r_{0}+h_{2})^{-}\right)$$

Terms in $\dot{w_0}$

$$\begin{pmatrix} -m_{1} (-r_{0} + h_{1})^{\tilde{}} (R_{0} + h_{1} + C_{1} r_{1})^{\tilde{}} \\ + [I_{0}] \\ -m_{2} (-r_{0} + h_{2})^{\tilde{}} (R_{0} + h_{2} + C_{2} r_{2})^{\tilde{}} \end{pmatrix}$$

Terms in $\dot{w}_{1} + \dot{w}_{2}$ $\left(-m_{1}(-r_{0} + h_{1}) \tilde{c}_{1} \tilde{r}_{1}\right) \dot{w}_{1} \left(-m_{2}(-r_{0} + h_{2}) \tilde{c}_{2} \tilde{r}_{2}\right) \dot{w}_{2}$

$$-m_{1} (-r_{0}+h_{1}) \left[\begin{array}{cccc} 2\tilde{w}_{0} & 0 & \tilde{w}_{0} (R_{0}+h_{1}+C_{1} r_{1}) \\ + & 2\tilde{w}_{0} C_{1} & \tilde{w}_{1} r_{1} + C_{1} & \tilde{w}_{1} & \tilde{w}_{1} r_{1} \end{array} \right]$$

$$-m_{2} (-r_{0}+h_{2}) \left[\begin{array}{ccccc} 2\tilde{w}_{0} & \dot{R}_{0} + \tilde{w}_{0} & \tilde{w}_{0} (R_{0}+h_{2}+C_{2} r_{2}) \\ + & 2\tilde{w}_{0} C_{1} & \tilde{w}_{1} r_{1} + C_{1} & \tilde{w}_{1} & \tilde{w}_{1} r_{1} \end{array} \right]$$

$$- (-r_{0} + k_{0}) \tilde{F}_{0} - \tilde{w}_{0} [I_{0}] w_{0}$$

$$-T_{H1} - T_{H2} + T_{0}$$

$$+ m_{1} (-r_{0} + h_{1}) \tilde{C}_{1} F_{1}$$

$$+ m_{2} (-r_{0} + h_{1}) \tilde{C}_{2} F_{2}$$

R.H.S.

Case B - Constrained Rotation

In the previous case the hinge torques were assumed to be arbitrary functions which completely accounted for the rotational interaction between the bodies 1 and 2 and the central element. In general, one or more axes of rotation may be constrained and the equations given previously must be modified to handle the rotational constraints.

Modification to the Driver Moment Equation

If we consider the constrained axes in terms of unit vectors, the modification procedure is easily visualized:



Consider the unit vector of constraint shown above. The remaining two degrees of rotation must be about mutually orthogonal axes lying in the plane normal to \hat{l}_c . An additional constraint, if it exists, must lie within the plane and for this case the single degree of rotational freedom is about the unit vector normal to both of the constraint axes. The moment equation is altered by the elimination of constrained degree of freedom. This can most easily be done by taking the dot product of the unconstrained equations with unit vectors along the axes of allowable rotation. The reduction in dimension may be utilized advantageously by then reformulating the equations in terms of the new driver rotational acceleration components thereby eliminating a variable for each constraint.

Modification of the Zero Body Moment Equation

The constraint application effects this equation in two ways:

- 1. The negative of the constraint torque which nulls the outer body rotation about the axis of constraint must be applied to body zero.
- 2. If the driver moment equations are written in terms of the reduced set of variables the zero body moment equation must be modified appropriately.

Computation of the constraint torque is simply the reaction torque of the outer body minus the external outer body torque; this difference projected onto the constrained axis. The implementation of this computation can be done in either of two ways.

.

- 1. The constraint torque can be solved for formally and the terms in R_0 and w_0 added to the L.H.S. of the zero body moment equation while all other terms are added to the R.H.S. of the equation.
- 2. The scalar equation of the outer body rotational acceleration about the constrained axis can be changed to an equation in terms of constraint torque (with suitable coupling to the zero body moment equation).

The former is recommended for constraints which are always applied while the latter is useful if the application of constraints is optional.

4.2 <u>FLEXIBLE SPACE STATION/FLEXIBLE APPENDAGE</u>, ZERO "G" CONDITION

The flexible body considerations used in the initial study phase have been extended to include the space station as a non-rigid structure and in addition, the capability of simulating the flexible dynamics of four non-controlled appendages has also been included. Extension of the initial digital simulation to include the capability of modeling the space station as a flexible structure necessitated a major revision of the systems dynamic equations which had been previously derived. Basically, appendage and array base motion must now include translation and rotation due to space station flexibility. Likewise, space station flexible modes must be excited by external forces and torques, and appendage and array interaction forces and torques. However, much of the philosophy and equation development techniques established in Section 4.1 are still applicable. Space station guidance and orbital motion, solar array guidance, ability to constrain solar array motions and so forth remain essentially unchanged from those descriptions given in Section 4.1.
The equation derivations logically fall into four separate categories:

- 1. Modal analysis of a freely translating and rotating space station.
- 2. Modal analysis of an appendage rigidly fixed to a base which is arbitrarily moving in space.
- 3. Modal analysis of appendage hinged to a base which is moving arbitrarily in space.
- 4. Total system equation which can be simultaneously solved for both rigid and flexible motions of a flexible space station with a maximum of two hinged arrays and up to four rigidly attached appendages.

4.2.1 MODAL ANALYSIS OF A FREELY TRANSLATING AND ROTATING SPACE STATION*

The space station, taken as a rigid body, rotates with an angular velocity $\overline{\omega}_{0}$ with respect to inertial space. Its translation is measured by \overline{R}_{0} , a vector from O_{N} , the origin of an inertial coordinate frame, to point O_{B} , a point fixed on the space station. This "rigid body" motion is conveniently described by a coordinate frame X_{S} fixed in the space station with origin at point O_{B} .

Determination of the flexible motion of the space station assumes that the station may be described by a collection of a discrete rigid bodies interconnected by massless elastic constraints. This system is idealized as initially undamped. The flexible motion of each discrete rigid body is measured relative to the X_s coordinate frame defined in the preceding paragraph. Thus, for example, the ith rigid body's center of mass is located by the vector

$$\frac{\Delta}{p_i} = \frac{\Delta}{q_i} + \frac{\Delta}{x_i}$$

where

 \vec{p}_i - center of mass of ith rigid body P_i

 \dot{q}_i - vector fixed in X_s ; it accommodates in its changes of orientation the motion of P_i due to "rigid body" motion of the space station (Figure 4-9).

 \dot{x}_i - describes small deformations of system at P_i Likewise, the ith rigid body's angular velocity - measured in its own principal axes frame - is \dot{w}_b with respect to the X_s coordinate system. Thus flexible motion of the ith body may be represented by the variables x_i , x_i , x_i , θ_i , θ_{i_2} , θ_{i_3} , and their respective derivatives.

*See Reference 4.6.



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4.2.1.1 Coordinate Frames and Relationships

- [I] inertially fixed coordinates
- $[X_s]$ coordinate basis fixed to and moving with the space station taken as a rigid body (origin at O_B, angular velocity $\overline{\omega}_o$ with respect to inertial space)
- $\begin{bmatrix} B_{i} \end{bmatrix} \begin{array}{c} \text{coordinate basis with origin at the center of mass of} \\ \text{the i}^{\text{th}} \text{ elastically connected rigid body used to define} \\ \text{space station flexible motion (angular velocity } \Omega^{i} \\ \text{with respect to inertial space}). \\ \text{This basis is initially} \\ \text{oriented along } [X_{s}]. \end{array}$

The relationships between these frames are defined by the following direction cosine matrices:

$$\begin{bmatrix} I \end{bmatrix} = C_{O} \begin{bmatrix} X_{s} \\ s \end{bmatrix}$$
$$\begin{bmatrix} X_{s} \end{bmatrix} = C_{B_{i}} \begin{bmatrix} B_{i} \end{bmatrix} \qquad i = 1, 2, --, n$$
$$\cong \begin{bmatrix} 1 & \theta_{i} & -\theta_{i} \\ -\theta_{i} & 1 & \theta_{i} \end{bmatrix} = E - \tilde{\theta}_{i}$$

1

where

B,

E is the identity matrix. The
$$\sim$$
 operation is basically used in cross product calculations and is defined by

$$\widetilde{\mathbf{y}} = \begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \mathbf{y}_3 \end{bmatrix} = \begin{bmatrix} 0 & -\mathbf{y}_3 & \mathbf{y}_2 \\ \mathbf{y}_3 & 0 & -\mathbf{y}_1 \\ -\mathbf{y}_2 & \mathbf{y}_1 & 0 \end{bmatrix}$$

As shown in Section 4.1

4.2.1.2 Equation Derivation

Using D'Alembert's principle, the total external force acting on the ith rigid body is

$$F_{i} = m_{i} \frac{d^{2}}{dt^{2}} \left[\dot{\vec{R}}_{o} + \dot{\vec{q}}_{i} + \dot{\vec{x}}_{i} \right]_{I}$$

Defining $\stackrel{\checkmark}{R}_{0}$, $\stackrel{\checkmark}{q}_{i}$, and $\stackrel{\checkmark}{x}_{i}$, in the X_s frame, and derivation in Reference 4.1, representative calculations are

$$\frac{d}{dt} \left(\stackrel{\rightarrow}{R}_{o} \right)_{I} = \frac{d}{dt} \left[I^{T} C_{o} R_{o} \right] = I^{T} (C_{o} \widetilde{\omega}_{o} R_{o} + C_{o} \dot{R}_{o})$$

$$\frac{d^{2}}{dt^{2}} \left(\stackrel{\rightarrow}{R}_{o} \right)_{I} = I^{T} \left[C_{o} \widetilde{\omega}_{o} \dot{R}_{o} + C_{o} \dot{R}_{o} + C_{o} \widetilde{\omega}_{o} \dot{\omega}_{o} R_{o} \right]$$

$$+ C_{o} \dot{\widetilde{\omega}}_{o} R_{o} + C_{o} \widetilde{\omega}_{o} \dot{R}_{o} \right]$$

$$= X_{s}^{T} \left[\widetilde{\omega}_{o} \widetilde{\omega}_{o} R_{o} + 2 \widetilde{\omega}_{o} \dot{R}_{o} + \widetilde{\omega}_{o} R_{o} + \dot{R}_{o} \right]$$

Therefore, remembering that \overline{q}_i does not vary with respect to time in the X s frame, the translational equation of motion for the ith rigid body becomes

$$\left\{ F_{i} \right\} = m_{i} X_{S}^{T} \left[\widetilde{\omega}_{o} \widetilde{\omega}_{o} (R_{o} + q_{i} - x_{i}) + 2 \widetilde{\omega}_{o} (R_{o} + x_{i}) + \widetilde{\omega}_{o} (R_{o} + q_{i} + x_{i}) + R_{o} + x_{i} \right]$$

$$+ \widetilde{\widetilde{\omega}}_{o} (R_{o} + q_{i} + x_{i}) + R_{o} + x_{i} \right]$$

$$(4.1)$$

Thus F_i must be expressed in $\{X_s\}$ frame.

Rotational motion of the rigid body in the $\begin{bmatrix} B_i \end{bmatrix}$ frame is expressed by Euler's equation for principal axes

$$\left\{\mathbf{T}_{i}\right\}_{\mathbf{B}} = \begin{bmatrix}\mathbf{I}\\\mathbf{I}\end{bmatrix} \quad \left\{\stackrel{\cdot}{\Omega}{}^{i}\right\} \quad + \quad \widetilde{\boldsymbol{\Omega}}^{i} \quad \begin{bmatrix}\mathbf{I}\\\mathbf{I}\end{bmatrix} \quad \left\{\stackrel{i}{\Omega}{}^{i}\right\} \tag{4.2}$$

where

$$\begin{bmatrix} I^{i} \end{bmatrix} = \begin{bmatrix} I^{i}_{1} & 0 & 0 \\ 0 & I^{i}_{2} & 0 \\ 0 & 0 & I^{i}_{3} \end{bmatrix} \equiv \text{ inertia matrix for } i^{\text{th}} \text{ rigid body}$$

 $\begin{cases} \Omega^{i} \\ \Omega^{i} \\ R^{i} \\ R^$

$$\left\{ T_{i} \right\}_{B} = \left[I^{i} \right] \left\{ \dot{\omega}_{bi} \right\} - \left[I^{i} \right] \widetilde{\omega}_{b_{i}} C_{b_{i}}^{T} \left\{ \omega_{o} \right\} + \left[I^{i} \right] C_{bi}^{T} \left\{ \dot{\omega}_{o} \right\}$$

$$+ \widetilde{\omega}_{bi} \left[I^{i} \right] \left\{ \omega_{bi} \right\} + \widetilde{\omega}_{bi} \left[I^{i} \right] C_{bi}^{T} \left\{ \omega_{o} \right\} + \left[\widetilde{C}_{bi}^{T} \left\{ \omega_{o} \right\} \right] \left[I^{i} \right] \left\{ \omega_{bi} \right\}^{(4.3)}$$

$$+ \left[C_{bi} \widetilde{T} \left\{ \omega_{o} \right\} \right] \left[I^{i} \right] C_{bi}^{T} \left\{ \omega_{o} \right\}$$

For small flexible rotations of the ith rigid body $C_{bi}^{T} \cong E + \tilde{\theta}_{i}$ as shown above. Substituting this along with the simplification

$$\begin{bmatrix} \widetilde{C}_{\mathrm{bi}} & \{\omega_{\mathrm{o}}\} \end{bmatrix} \cong \widetilde{\omega}_{\mathrm{o}} + \begin{bmatrix} \widetilde{\theta}^{\mathrm{i}} & \{\omega_{\mathrm{o}}\} \end{bmatrix}$$

into equation (4.3) gives

$$\left\{ T_{i} \right\}_{B} = \left[I^{i} \right] \left\{ \dot{\omega}_{bi} \right\} - \left[I^{i} \right] \widetilde{\omega}_{bi} \left\{ \omega_{o} \right\} - \left[I^{i} \right] \widetilde{\theta}^{i} \widetilde{\omega}_{bi} \left\{ \omega_{o} \right\}$$

$$+ \left[I^{i} \right] \left\{ \dot{\omega}_{o} \right\} + \left[I^{i} \right] \widetilde{\theta}^{i} \left\{ \dot{\omega}_{o} \right\} + \widetilde{\omega}_{bi} \left[I^{i} \right] \left\{ \omega_{bi} \right\} + \widetilde{\omega}_{bi} \left[I^{i} \right] \left\{ \omega_{o} \right\}$$

$$+ \widetilde{\omega}_{bi} \left[I^{i} \right] \widetilde{\theta}^{i} \left\{ \omega_{o} \right\} + \widetilde{\omega}_{o} \left[I^{i} \right] \left\{ \omega_{bi} \right\} - \left[\widetilde{\theta}^{i} \left[\widetilde{\omega}_{o} \right] \right] \left[I^{i} \right] \left\{ \omega_{bi} \right\}$$

$$+ \widetilde{\omega}_{o} \left[I^{i} \right] \left\{ \omega_{o} \right\} - \widetilde{\omega}_{o} \left[I^{i} \right] \widetilde{\theta}^{i} \left\{ \omega_{o} \right\} + \left[\widetilde{\theta}^{i} \left\{ \omega_{o} \right\} \right] \left[I^{i} \right] \left\{ \omega_{o} \right\}$$

$$+ \left[\widetilde{\theta}^{i} \left\{ \omega_{o} \right\} \right] \left[I^{i} \right] \widetilde{\theta}^{i} \left\{ \omega_{o} \right\}$$

4)

Note that linearization of the above equation has been assumed since terms containing products of small variables have been neglected.

The force equation is written in the X_s coordinate basis. Transforming Equation 4.4 to the X_s frame involves multiplication by $C_{b_i}^T \cong E - \tilde{\theta}^i$. This procedure results in Equation 4.5.

Using the following identity

$$\widetilde{\mathbf{u}} \{\mathbf{v}\} = - \widetilde{\mathbf{v}} \setminus \{\mathbf{u}\}$$

and defining

$$\{h_i\} = [I^i] \{\omega_o\}$$

Therefore

$$\widetilde{\mathbf{h}}_{\mathbf{i}} = \left[\begin{bmatrix} \mathbf{I}^{\mathbf{i}} \end{bmatrix} \left\{ \boldsymbol{\omega}_{\mathbf{o}} \right\} \right]$$

$$\widetilde{\left[\boldsymbol{\Theta}^{\mathbf{i}} \quad \left\{ \boldsymbol{\widetilde{\omega}}_{\mathbf{o}} \right\} \right]} \left[\begin{bmatrix} \mathbf{I}^{\mathbf{i}} \end{bmatrix} \left\{ \boldsymbol{\omega}_{\mathbf{o}} \right\} = - \widetilde{\mathbf{h}}_{\mathbf{i}} \quad \widetilde{\boldsymbol{\Theta}^{\mathbf{i}}} \left\{ \boldsymbol{\omega}_{\mathbf{o}} \right\} = - \widetilde{\mathbf{h}}_{\mathbf{i}} \quad \widetilde{\boldsymbol{\omega}}_{\mathbf{o}} \left\{ \boldsymbol{\Theta^{\mathbf{i}}} \right\}$$

Substitution of these identities into Equation 4.5, yields the rotational equation of motion for the i^{th} rigid body of the space station.

$$\left\{ T_{i} \right\} = \left[I^{i} \right] \left\{ \dot{\omega}_{bi} \right\} + \left[I^{i} \right] \widetilde{\omega}_{o} \left\{ \omega_{bi} \right\} + \left[I^{i} \right] \left\{ \dot{\omega}_{o} \right\}$$

$$\left\{ \widetilde{\mu}_{i}^{i} \left\{ \widetilde{\Theta}_{i} \right\} - \left[I^{i} \right] \left\{ \dot{\omega}_{o}^{i} \right\} - \widetilde{\mu}_{i}^{i} \left\{ \omega_{bi} \right\} + \widetilde{\omega}_{o}^{i} \left[I^{i} \right] \left\{ \omega_{bi} \right\} + \widetilde{\omega}_{o}^{i} \left\{ h^{i} \right\}$$

$$\left\{ \widetilde{\mu}_{o}^{i} \left[I^{i} \right] \left\{ \omega_{2} \right\} \right\} \left\{ \Theta_{i} \right\} - \widetilde{\omega}_{o}^{i} \left[I^{i} \right] \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} + \widetilde{\mu}_{i}^{i} \left\{ \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} \right\}$$

$$\left\{ \widetilde{\mu}_{o}^{i} \left\{ I^{i} \right\} - \widetilde{\omega}_{o}^{i} \left[I^{i} \right] \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} + \widetilde{\mu}_{i}^{i} \left\{ \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} \right\}$$

$$\left\{ \widetilde{\mu}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} - \widetilde{\omega}_{o}^{i} \left[I^{i} \right] \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} + \widetilde{\mu}_{i}^{i} \left\{ \widetilde{\omega}_{o}^{i} \left\{ \Theta_{i}^{i} \right\} \right\}$$

Combining Equations 4.1 and 4.6 for all n rigid bodies into one large matrix equation of column dimension 6 n yields

$$\begin{bmatrix} m \\ q \end{bmatrix} \{ q \} + \begin{bmatrix} K \\ q \end{bmatrix} \{ q \} = -\begin{bmatrix} G \\ q \end{bmatrix} \{ q \} - \begin{bmatrix} B \\ q \end{bmatrix} \{ q \} + \begin{bmatrix} R \\ R \end{bmatrix} \{ RB \}$$
(4.7)
+ { F¹} + { L}

 ${F^1}$ - discretely applied forces and torques on those elastically connected rigid bodies which define the space station to which either

- (a) fixed appendange is attached
- (b) rotating array is hinged
- (c) external force is applied (\overline{F}_{R})
- (d) external torque is applied $(\tilde{T}_R \tilde{\lambda}_R)$

The applied forces and torques include those resulting from appendage base constraints.



F_D)



where

q = $\begin{bmatrix} x_{11}, x_{12}, x_{13}, \theta_{13}, \dots, \theta_{n2}, \theta_{n3} \end{bmatrix}^T$







$$\left\{ RB \right\} = \begin{bmatrix} \vdots \\ R_{o} \\ \vdots \\ \omega_{o} \end{bmatrix}$$

R

4.2.1.3 Modal Analysis

Subjecting Equation 4.7 to the orthogonal transformation

$$\{q\} = [\gamma] \{n_s\}$$

and premultiplying by $\begin{bmatrix} \gamma \end{bmatrix}^T$ yields, if $\begin{bmatrix} \gamma \end{bmatrix}$ is a matrix whose columns are eigenvectors of the system, $\begin{bmatrix} \gamma \end{bmatrix}^T \begin{bmatrix} m \end{bmatrix} \begin{bmatrix} \gamma \end{bmatrix}^T = I$,

$$\dot{\mathbf{n}}_{\mathbf{s}} + \begin{bmatrix} 2 \xi_{\mathbf{s}} & \omega_{\mathbf{s}} \end{bmatrix} \dot{\mathbf{n}}_{\mathbf{s}} + \begin{bmatrix} \omega_{\mathbf{s}}^{2} \end{bmatrix} \mathbf{n}_{\mathbf{s}} = -\begin{bmatrix} \gamma \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{G} \end{bmatrix} \begin{bmatrix} \gamma \end{bmatrix} \dot{\mathbf{n}}_{\mathbf{s}}$$

$$+ \begin{bmatrix} \gamma \end{bmatrix}^{\mathrm{T}} \quad \left\{ \mathbf{L} \right\} - \begin{bmatrix} \gamma \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{B} \end{bmatrix} \begin{bmatrix} \gamma \end{bmatrix} \mathbf{n}_{\mathbf{s}}$$

$$+ \begin{bmatrix} \gamma \end{bmatrix}^{\mathrm{T}} \quad \left\{ \mathbf{R} \right\} \quad \left\{ \mathbf{RB} \right\} + \begin{bmatrix} \gamma \end{bmatrix}^{\mathrm{T}} \quad \left\{ \mathbf{F}^{1} \right\}$$

$$(4.8)$$

Note that modal damping has been added in the classical manner of structural analysis.

For this simulation, space station "rigid body" motion is considered to be small. Thus, Equation 4.8 may be linearized to the following form

$$\dot{n}_{s} + \left[2 \xi_{s} \cdot \omega_{s}\right] \dot{n}_{s} + \left[\omega_{s}^{2}\right]n_{s}^{=} \left[\gamma\right]^{T} \left\{F^{1}\right\} + \left[\gamma\right]^{T} \left[R\right] \left\{RB\right\} (4.9)$$

Derivations in Section 4.2.5 lalso show that $[\gamma]^T$ [R] {RB} = 0. Thus Equation 4.9 becomes

The above equation in diamond brackets is the equation modeled in the simulation. The diamond bracket will hence forth be utilized solely for indicating equations to be programmed.

In summary, the above equation was derived assuming:

- (a) linearization of equations because of
 - 1. small flexible motions of system
 - 2. small space station angular velocity, and translation with respect to osculating orbit position
- (b) free-free modes of space station are available for generation of $[\gamma]$ modal matrix
- (c) moments of inertia for each of the n discrete rigid bodies are initially defined along axes parallel to the X_s coordinate basis
- (d) external forces and torques acting on the space station to be expressed in the space station axes system

4.2.2 <u>RIGIDLY ATTACHED APPENDAGES</u>

Appendages, as in previous derivations, are modeled as elastically connected masses. Cantilevered mode shapes are used to represent the fixed appendage flexibility. The base of a fixed appendage must be rigidly attached to one of those rigid bodies which comprise the space station. Therefore base motion of the appendage includes translational and rotational motion of that rigid body to which it is attached plus translational and rotational motion of the entire space station with respect to inertial space.



FIGURE 4-10 FIXED APPENDAGE COORDINATE SYSTEM

4.2.2.1 Coordinate Frames and Relationships

previously defined inertial basis

[B] previously defined basis fixed to ith rigid body of space station

$$\begin{bmatrix} X_F \end{bmatrix} - & \text{coordinate basis defined with origin at attachment point} \\ & \text{of appendage and axes directed along principal axes of} \\ & \text{the appendage} \end{bmatrix}$$

$$\begin{bmatrix} C_F \end{bmatrix}$$
 - direction cosine matrix relating coordinate frames $\begin{bmatrix} B_i \end{bmatrix}$
and $\begin{bmatrix} X_F \end{bmatrix}$
 $\begin{bmatrix} B_i \end{bmatrix} = \begin{bmatrix} C_F \end{bmatrix} \begin{bmatrix} X_F \end{bmatrix}$

Equation Derivation 4.2.2.2

The total force acting on the j^{th} mass particle m_J of the appendage is, by D'Alembert's principle

$$\mathbf{F}_{J} = \mathbf{m}_{J} \frac{\mathrm{d}^{2}}{\mathrm{dt}^{2}} \left[\frac{\dot{\mathbf{x}}}{\mathbf{R}_{o}} + \frac{\dot{\mathbf{x}}}{\mathbf{q}_{i}} + \frac{\dot{\mathbf{x}}}{\mathbf{x}_{i}} + \frac{\dot{\mathbf{x}}}{\mathbf{h}_{F}} + \frac{\dot{\mathbf{x}}}{\mathbf{r}_{J}} + \frac{\dot{\mathbf{x}}}{\mathbf{u}_{J}} \right] \mathbf{I}$$

where

 \dot{h}_{F} - location of attachment point of appendage with respect to the center of mass of the ith rigid body of the space station to which the appendage is rigidly attached.

$$\vec{r}_J$$
 - undeformed location of j^{th} particle m_J of appendage.
 u_J - location of m_J with respect to undeformed position.

Representative calculations, assuming \vec{h}_{F} is defined in the $\begin{bmatrix} B_{i} \end{bmatrix}$ basis and \vec{r}_J and \vec{u}_J are defined in the $\begin{bmatrix} X \\ F \end{bmatrix}$ basis, and noting that $C_F = 0$ are $\frac{d}{dt} \overrightarrow{u}_{J} = \frac{d}{dt} \left[I^{T} C_{o} C_{bi} C_{F} u_{J} \right] =$ $I^{T} \begin{bmatrix} C_{o} & \widetilde{\omega}_{o} & C_{bi} & C_{F} & u_{J} + C_{o} & C_{bi} & \widetilde{\omega}_{bi} & C_{F} & u_{J} + C_{o} & C_{bi} & C_{F} & u_{J} \end{bmatrix}$ $\frac{d^2}{dt^2} \begin{bmatrix} u_J \end{bmatrix}_{I} = I^T \begin{bmatrix} C_0 \widetilde{\omega}_0 \widetilde{\omega}_0 C_{bi} C_F u_J + C_0 \dot{\widetilde{\omega}}_0 C_{bi} C_F u_J \end{bmatrix}$ + $C_{o} \widetilde{\omega}_{o} C_{bi} \widetilde{\omega}_{bi} C_{F} u_{J} + C_{o} \widetilde{\omega}_{o} C_{bi} u_{J} + C_{o} \widetilde{\omega}_{o} C_{bi} \widetilde{\omega}_{bi} C_{G} u_{J}$ + $C_{o}C_{bi}\widetilde{\omega}_{bi}\widetilde{\omega}_{bi}C_{F}u_{J}$ + $C_{o}C_{bi}\widetilde{\omega}_{bi}C_{F}u_{J}$ + $C_{o}C_{bi}\widetilde{\omega}_{bi}C_{F}u_{J}$ + $C_o \approx C_{bi} C_F u_J + C_o C_{bi} \approx C_F u_J + C_o C_{bi} C_F u_J$ $= \mathbf{X}^{\mathrm{T}} \left[\widetilde{\omega}_{\mathrm{o}} \quad \widetilde{\omega}_{\mathrm{o}} \quad \mathbf{C}_{\mathrm{bi}} \quad \mathbf{C}_{\mathrm{F}} \quad \mathbf{u}_{\mathrm{J}} + \dot{\widetilde{\omega}}_{\mathrm{o}} \quad \mathbf{C}_{\mathrm{bi}} \quad \mathbf{C}_{\mathrm{F}} \quad \mathbf{u}_{\mathrm{J}} + 2 \quad \widetilde{\omega}_{\mathrm{o}} \quad \mathbf{C}_{\mathrm{bi}} \quad \widetilde{\omega}_{\mathrm{bi}} \quad \mathbf{C}_{\mathrm{F}} \quad \mathbf{u}_{\mathrm{J}} \right]$ + 2 \mathfrak{T}_{O} C_{bi} C_F u_J + C_{bi} \mathfrak{T}_{bi} \mathfrak{T}_{bi} \mathfrak{T}_{F} u_J + C_{bi} \mathfrak{T}_{bi} C_F u_J + 2 C_{bi} \mathfrak{T}_{bi} C_F u_J + C_{bi} C_F u_J $\vec{q}_1, \vec{h}_F, \vec{r}_T$ do not vary with time in their respective frames.

$$\begin{cases} \mathbf{F}_{\mathbf{J}} \end{bmatrix} = \mathbf{m}_{\mathbf{J}} \mathbf{X}_{\mathbf{F}}^{\mathbf{T}} \left[(\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + 2 \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{x}_{i}) \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{0} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{0} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{C}_{bi} + \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \widetilde{\mathbf{u}}_{bi} + \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi}) + \mathbf{r}_{i} + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{C}_{F} + \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \mathbf{C}_{F} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{C}_{\mathbf{F}} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \widetilde{\mathbf{c}}_{F} + \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \mathbf{C}_{F} + \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} \mathbf{C}_{F} \right] \\ = \mathbf{m}_{\mathbf{J}} \mathbf{x}_{\mathbf{F}}^{\mathbf{T}} \left[\left\{ \mathbf{C}_{\mathbf{F}}^{\mathbf{T}} \mathbf{C}_{bi}^{\mathbf{T}} \right\} (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} + \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{0} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \widetilde{\mathbf{u}}_{bi} + \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{0} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{c}_{i} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{u}_{bi} \right] \\ + \widetilde{\mathbf{u}}_{0} (\mathbf{R}_{0} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{0} + \mathbf{x}_{i}) + (\widetilde{\mathbf{u}}_{0} \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{C}_{bi} + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{c}_{bi} \mathbf{c}_{bi} \mathbf{c}_{bi} \right] \\ + 2 \widetilde{\mathbf{u}}_{0} \mathbf{C}_{bi} \mathbf{u}_{bi} + \mathbf{C}_{bi} \mathbf{u}_{bi} \mathbf{u}_{bi} \mathbf{c}_{i} \mathbf{c}_{i}$$

For small translational and rotational motion of the rigid body to which the appendage is attached $C_{bi}^T \cong E + \tilde{\theta}^i$

$$\left\{ F_{J} \right\} = m_{J} X_{F}^{T} \left[\left\{ C_{F}^{T} \right\} \cdot \left\{ \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} \left(R_{0} + q_{i} + x_{i} \right) + 2 \, \widetilde{\omega}_{0} \left(R_{0} + x_{i} \right) \right. \right. \right. \right. \right. \right.$$

$$+ \widetilde{\widetilde{\omega}}_{0} \left(R_{0} + q_{i} + x_{i} \right) + R_{0} + x_{i} \right) + \widetilde{\theta}_{i} \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} \left(R_{0} + q_{i} \right) + 2 \, \widetilde{\omega}_{0} R_{0} \right. \right.$$

$$+ \widetilde{\widetilde{\omega}}_{0} \left(R_{0} + q_{i} \right) + R_{0} \right) + \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} + \theta_{i} \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{0} \right) - \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{0} \right) \overline{\theta}^{i} \right.$$

$$+ \widetilde{\widetilde{\omega}}_{0} + 2 \, \widetilde{\omega}_{0} \, \widetilde{\omega}_{bi} + \frac{2}{\omega_{bi}} \, \widetilde{\widetilde{\omega}}_{bi}^{0} + \widetilde{\widetilde{\omega}}_{bi} \right) h_{F}^{i} + \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{0} \right) \left. \left(\widetilde{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{0} \right) \right. \right.$$

$$- \left(\left(\overline{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{0} \right) \overline{\theta}^{i} + \left(\overline{\omega}_{0} + 2 \, \widetilde{\omega}_{0} \, \widetilde{\omega}_{bi} + \frac{1}{\omega}_{bi} \right) R_{F}^{i} + \left(\overline{\omega}_{0} \, \widetilde{\omega}_{0} + \frac{1}{\omega}_{bi} \right) C_{F} \left(r_{J} + u_{J} \right) \right.$$

$$+ \left(2 \, \widetilde{\omega}_{0} + 2 \, \overline{\theta}^{i} \, \widetilde{\omega}_{0} - 2 \, \widetilde{\omega}_{0} \, \overline{\theta}^{i} + \left(\overline{\omega}_{bi} \right) C_{F} \, u_{J} \right]$$

The space station motion is assumed to be small, thus, the above equation reduces to

$$\{\mathbf{F}_{J}\} = \mathbf{m}_{J} \mathbf{X}_{F}^{T} \left[\mathbf{C}_{F}^{T} \left(\dot{\widetilde{\omega}}_{o} \mathbf{q}_{i} + \mathbf{R}_{o} + \mathbf{x}_{i} + \left(\dot{\widetilde{\omega}}_{o} + \dot{\widetilde{\omega}}_{bi} \right) \mathbf{h}_{F}^{\prime} \right] + \left(\dot{\widetilde{\omega}}_{o} + \dot{\widetilde{\omega}}_{bi} \right) (\mathbf{C}_{F} \mathbf{r}_{J} + \mathbf{u}_{J}$$

$$(4.10)$$

Combining the above equation for all n particles of the appendage into one large matrix equation of column size 3 n yields

$$[m] \{q\} + [K] \{q\} = -[G] \{\dot{q}\} - [B] \{q\}$$
(4.11)
+ [R] {RB} + [s₂] {s} + {L}

where

$$3n \times 3n$$

t

 $\begin{bmatrix} G \end{bmatrix} = \begin{bmatrix} B \end{bmatrix} = 0$

$$\left\{ \mathbf{RB} \right\} = \begin{bmatrix} \mathbf{R}_{0} \\ \mathbf{L}_{0} \\ \mathbf{L}_{0} \end{bmatrix}$$

used to define coupling of the rigid body modes of space station with cantilever modes of fixed appendages.

$$\begin{bmatrix} R \end{bmatrix} = \begin{bmatrix} -\overline{m}_{1} & C_{F}^{T} & \overline{m}_{1} & C_{F}^{T} & ((q_{i} + h_{F}^{\prime}) + (C_{F} - r_{1})) \\ -\overline{m}_{2} & C_{F}^{T} & \overline{m}_{2} & C_{F}^{T} & ((q_{i} + h_{F}^{\prime}) + (C_{F} - r_{2})) \\ \hline -\overline{m}_{2} & C_{F}^{T} & \overline{m}_{2} & C_{F}^{T} & ((q_{i} + h_{F}^{\prime}) + (C_{F} - r_{2})) \\ \hline & & \cdot & \cdot \\ \hline -\overline{m}_{n} & C_{F}^{T} & \overline{m}_{n} & C_{F}^{T} & ((q_{i} + h_{F}^{\prime}) + (C_{F} - r_{n})) \\ \hline & & 3n \times 6 \\ \hline & 4-120 \end{bmatrix}$$

$$\begin{array}{c} \cdot \cdot \\ \mathbf{s} \\ \end{array} = \begin{bmatrix} \cdot \cdot \\ \mathbf{x} \\ \cdot \\ \cdot \\ \omega \mathrm{bi} \end{bmatrix}$$

6 x 1

- used to define coupling of the space station flexible modes with the cantilever modes of the fixed appendage.

 ${L} =$

 $|\mathbf{s}_2|$

(no external forces are applied to appendages)

4.2.2.3 <u>Modal Analysis</u> $q = [\tau]^n$

where $[\tau]$ - modal matrix of dimension $3 n \times N_{Fi}$

0

n – normal modes of which there are N_{Fi}

N_{Fi} - number of normal cantilever modes used to simulate fixed appendage #i.

Assuming $\begin{bmatrix} \tau^{T} \end{bmatrix} \begin{bmatrix} m \end{bmatrix} \begin{bmatrix} \tau \end{bmatrix} = I$, equation (2) becomes $-\tau^{T} \begin{bmatrix} R \end{bmatrix} \left\{ RB \right\} - \tau^{T} \begin{bmatrix} s_{2} \end{bmatrix} \begin{bmatrix} \gamma_{F} \end{bmatrix} \left\{ \ddot{n}_{s} \right\}$ $+ \left\{ \ddot{n}_{F} \right\} + \left[2 \xi_{F} \omega_{F} \right] \left\{ \dot{n}_{F} \right\} + \left[\omega_{F}^{2} \right] \left\{ n_{F} \right\} = 0$ (4.12) where $\left\{ \begin{matrix} \cdots \\ s \end{matrix} \right\} = \begin{pmatrix} \begin{matrix} \cdots \\ \vdots \\ \vdots \\ bi \end{pmatrix} = \begin{bmatrix} \gamma_{F} \end{bmatrix} \quad \left\{ \begin{matrix} \cdots \\ n_{s} \right\} \\ is \\ 6 \ge N_{c} \end{bmatrix}$ is

the relationship between the translational and rotational motion of the rigid body to which the appendage is attached and the normal mode accelerations of the space station.

In summary, Equation 4.12 above is generated via the following assumptions:

- (a) base motion of the fixed appendage must include translations and rotations due to both rigid body motion of the space station and flexible modes of the space station,
- (b) the fixed appendage is modeled by discrete masses; cantilever modes are used to define its modal motion,
- (c) the above equations are derived in the coordinate frame of the fixed appendage
- (d) moments of inertia of the fixed appendage are defined with respect to principal axes with origin at base of appendage
- (e) linearization of equations has resulted because of
 - (1) small flexible motions of space station
 - (2) small flexible motions of fixed array
 - (3) small rigid body motion of space station

4.2.3 ROTATING ARRAYS

Rotating arrays are modeled exactly as fixed appendages, except that the base of the rotating array may have rotational motion with respect to the rigid body of the space station to which it is attached.



FIGURE 4-11 FLEXIBLE APPENDAGE COORDINATE SYSTEM

4.2.3.1 Coordinate Frames and Relationships

[1]	-	previously defined
[x _s]	-	previously defined
[B _i]	-	previously defined
$\begin{bmatrix} x \end{bmatrix}$	-	coordinate basis wh
-		with regreat to the i

coordinate basis which rotates with angular velocity ω_J with respect to the rigid body of the space station to which it is attached with origin at the attachment point of the rotating array.

The relationship between $[x_J]$ and $[B_i]$ is defined by the direction cosine relationship

$$[B_i] = [C_J] [X_J]$$

Likewise, as shown in Reference 4.1

$$[c_J] = [c_J] \widetilde{\omega}_J$$

4.2.3.2 Equation Derivations

Again using D'Alembert's principle, the total force acting on the p^{th} mass particle of the rotating array equals

$$\mathbf{F}_{\ell} = \mathbf{m}_{\ell} \frac{d^2}{dt^2} \begin{bmatrix} \overrightarrow{\mathbf{R}}_{0} + \overrightarrow{\mathbf{q}}_{1} + \overrightarrow{\mathbf{x}}_{1} + \overrightarrow{\mathbf{h}}_{J} + \overrightarrow{\mathbf{r}}_{\ell} + \overrightarrow{\mathbf{u}}_{\ell} \end{bmatrix}_{\mathbf{I}}$$

where

 \vec{h}'_J .

location of attachment point of appendage with respect to the center of mass of the ith rigid body of the space station to which the appendage is attached

- undeformed location of m_{ℓ} of array
- ⊥ u
- time dependent location of m_{j} with respect to undeformed location

Representative calculations, assuming \vec{h}'_{J} is defined in the $[B_i]$ and $\vec{u}_{\mathcal{L}}$ are defined in the $[X_{J}]$ basis, are basis and r_d $\frac{d}{dt} \begin{bmatrix} \vec{u}_{\ell} \end{bmatrix}_{I} = \frac{d}{dt} \begin{bmatrix} I^{T} & C_{O} & C_{D} & U_{\ell} \end{bmatrix}$ $= \mathbf{I}^{\mathrm{T}} \left[\mathbf{C}_{\mathrm{o}} \widetilde{\boldsymbol{\omega}}_{\mathrm{o}} \mathbf{C}_{\mathrm{bi}} \mathbf{C}_{\mathrm{J}} \mathbf{u}_{\ell} + \mathbf{C}_{\mathrm{o}} \mathbf{C}_{\mathrm{bi}} \widetilde{\boldsymbol{\omega}}_{\mathrm{bi}} \mathbf{C}_{\mathrm{J}} \mathbf{u}_{\ell} + \mathbf{C}_{\mathrm{o}} \mathbf{C}_{\mathrm{bi}} \mathbf{C}_{\mathrm{J}} \widetilde{\boldsymbol{\omega}}_{\mathrm{J}} \mathbf{u}_{\ell} \right]$ + $C_{0}C_{bi}C_{J}u_{\ell}$ $\frac{d^{2}}{u^{2}} \left[\widehat{u}_{\mathcal{L}} \right]_{I} = I^{T} C_{O} \left[\widetilde{\omega}_{O} \widetilde{\omega}_{O} C_{Di} C_{J} u_{\mathcal{L}} + \widetilde{\widetilde{\omega}}_{O} C_{Di} C_{J} u_{\mathcal{L}} + 2 \widetilde{\omega}_{O} C_{Di} \widetilde{\omega}_{Di} C_{J} u_{\mathcal{L}} \right]$ + $2\widetilde{\omega}_{0}C_{bi}C_{J}\widetilde{\omega}_{J}u_{\mathcal{L}}$ + $2\widetilde{\omega}_{0}C_{bi}C_{J}u_{\mathcal{L}}$ + $C_{bi}\widetilde{\omega}_{bi}\widetilde{\omega}_{bi}C_{J}u_{\mathcal{L}}$ + 2 $C_{bi} \widetilde{\omega}_{bi} C_J u_{\ell}$ + $C_{bi} \widetilde{\widetilde{\omega}}_{bi} C_J u_{\ell}$ + 2 $C_{bi} \widetilde{\widetilde{\omega}}_{bi} C_J \widetilde{\omega}_{j}$ u_{ℓ} + $C_{bi} C_{J} \widetilde{\omega}_{J} \widetilde{\omega}_{J} u_{\ell}$ + $2 C_{bi} C_{J} \widetilde{\omega}_{J} u_{\ell}$ + $C_{bi} C_{J} \widetilde{\widetilde{\omega}}_{J} u_{\ell}$ + $C_{bi} C_{J} u_{\ell}$ $\therefore \left\{ F_{\mathcal{L}} \right\} = m_{\mathcal{L}} x_{J}^{T} \left[(C_{J}^{T} C_{bi}^{T}) \left(\left\{ \widetilde{\omega}_{o} \widetilde{\omega}_{o} (R_{o} + q_{i} + x_{i}) + 2\widetilde{\omega}_{o} (R_{o} + x_{i}) \right\} \right] \right]$ $\cdot \\ + \widetilde{\widetilde{\omega}}_{o} (\mathbf{R}_{o} + \mathbf{q}_{i} + \mathbf{x}_{i}) + \mathbf{R}_{o} + \mathbf{x}_{i} + \{ \widetilde{\omega}_{o} \widetilde{\omega}_{o} C_{bi} + \widetilde{\widetilde{\omega}}_{o} C_{bi} + 2 \widetilde{\widetilde{\omega}}_{o} C_{bi} \widetilde{\omega}_{bi}$ + $C_{bi} \widetilde{\omega}_{bi} + C_{bi} \widetilde{\widetilde{\omega}}_{bi} +$ + $2\widetilde{\omega}_{0}C_{bi}\widetilde{\omega}_{bi}C_{J}$ + $2\widetilde{\omega}_{0}C_{bi}C_{J}\widetilde{\omega}_{J}$ + $C_{bi}\widetilde{\omega}_{bi}C_{J}$ + $C_{bi}\widetilde{\omega}_{bi}C_{J}$ + $C_{bi}\widetilde{\omega}_{bi}C_{J}$ + 2 $C_{bi} \widetilde{\omega}_{bi} C_{J} \widetilde{\omega}_{J}$ + $C_{bi} C_{J} \widetilde{\omega}_{J} \widetilde{\omega}_{J}$ + $C_{bi} C_{J} \widetilde{\omega}_{J}$ + $C_{bi} C_{J} \dot{\widetilde{\omega}}_{J}$ (r_{ℓ} + u_{ℓ}) + $\left\{ 2\widetilde{\omega}_{0}C_{bi}C_{J} + 2C_{bi}\widetilde{c}_{bi}C_{J} \right\} \left[u_{l} \right] + 2\widetilde{\omega}_{J}u_{l} + u_{l}$

C_{bi} ~ E

Again, ignoring products of small variables and recalling that – $\widetilde{\theta}^i$

$$\begin{split} & \ddots \left\{ \mathbf{F}_{\boldsymbol{\ell}} \right\} = \mathbf{m}_{\boldsymbol{\ell}} \mathbf{x}_{\mathbf{J}}^{\mathrm{T}} \left[(\mathbf{C}_{\mathbf{J}}^{\mathrm{T}} (\mathbf{E} + \widetilde{\theta}^{\mathrm{I}}) (\{\widetilde{\omega}_{0} \ \widetilde{\omega}_{0} (\mathbf{R}_{0} + \mathbf{q}_{1} + \mathbf{x}_{1}) + \widetilde{\omega}_{0} (\mathbf{R}_{0} + \mathbf{q}_{1} + \mathbf{x}_{1}) + \widetilde{\mathbf{R}}_{0} + \widetilde{\mathbf{x}}_{1} \} + \{\widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \\ & - \widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} + \widetilde{\omega}_{0} - \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} + 2 \ \widetilde{\omega}_{0} \ \widetilde{\omega}_{\mathrm{bi}} + \widetilde{\omega}_{\mathrm{bi}} \} \mathbf{h}_{\mathrm{J}}^{\mathrm{I}} \\ & + \{\widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \ \mathbf{C}_{\mathbf{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) - \widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} + \widetilde{\omega}_{0} \ \mathbf{C}_{\mathbf{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) - \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} \\ & + 2 \ \widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \ \mathbf{C}_{\mathbf{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) - \widetilde{\omega}_{0} \ \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} + \widetilde{\omega}_{0} \ \mathbf{C}_{\mathbf{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) - \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} \\ & + 2 \ \widetilde{\omega}_{0} \ \widetilde{\omega}_{\mathrm{bi}} \ \mathbf{C}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} + 2 \ \widetilde{\omega}_{0} \ \mathbf{C}_{\mathbf{J}} \ \widetilde{\omega}_{\mathbf{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) - 2 \ \widetilde{\omega}_{0} \ \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \ \widetilde{\omega}_{\mathbf{J}} \mathbf{r}_{\boldsymbol{\ell}} \\ & + 2 \ \widetilde{\omega}_{0} \ \widetilde{\omega}_{\mathrm{bi}} \ \mathbf{C}_{\mathrm{J}} \mathbf{r}_{\boldsymbol{\ell}} + 2 \ \widetilde{\omega}_{0} \ \mathbf{C}_{\mathrm{J}} \ \widetilde{\omega}_{\mathrm{J}} (\mathbf{r}_{\boldsymbol{\ell}} + \mathbf{u}_{\boldsymbol{\ell}}) \\ & - \widetilde{\theta}^{\mathrm{I}} \ \mathbf{C}_{\mathbf{J}} \ \widetilde{\omega}_{\mathbf{J}} \mathbf{\omega}_{\mathbf{J}} \mathbf{r}_{\mathbf{\ell}} + \mathbf{C}_{\mathbf{J}} \ \widetilde{\omega}_{\mathbf{J}} \ \mathbf{U}_{\mathbf{J}} \mathbf{U} \\ & + 2 \ \widetilde{\omega}_{\mathrm{o}} \ \widetilde{\omega}_{0} \ \mathbf{U}_{\mathrm{J}} \mathbf{r}_{\mathrm{J}} + \mathbf{C}_{\mathrm{J}} \ \widetilde{\omega}_{\mathrm{J}} \mathbf{U}_{\mathrm{J}} \mathbf{U} \\ & + 2 \ \widetilde{\omega}_{\mathrm{o}} \ \mathbf{U}_{\mathrm{J}} \mathbf{U}_{\mathrm{J}} + \ \widetilde{u}_{\mathrm{J}} \right \right \right \right \right \right \right \right$$

$$\begin{aligned} &+\widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{o} (R_{o} + q_{i} + x_{j}) + \widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{o} + \widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{i} + \theta^{i} \stackrel{i}{\widetilde{\omega}}_{o} \stackrel{i}{\widetilde{\omega}}_{o} h_{j}^{i} + \widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{o} h_{j}^{i} + \widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{o} c_{j} x_{\ell} + \widetilde{\theta}^{i} \stackrel{i}{\widetilde{\omega}}_{o} c_{j} \frac{i}{\widetilde{\omega}}_{j} x_{\ell} + \widetilde{\theta}^{i} \frac{i}{\widetilde{\omega}}_{o} c_{j} \frac{i}{\widetilde{\omega}}_{j} x_{\ell} + \widetilde{\theta}^{i} \frac{i}{\widetilde{\omega}}_{j} x_{\ell} + \widetilde{\theta}^{i} \frac{i}{\widetilde{\omega}}_{j} x_{\ell} + \widetilde{\theta}^{i} \frac{i}{\widetilde{\omega}}_{j} x_{j} x_{\ell} + \widetilde{\omega}^{i} \frac{i}{\widetilde{\omega}}_{j} x_{j} x_{j} x_{\ell} + \widetilde{\omega}^{i} \frac{i}{\widetilde{\omega}}_{j} x_{j}$$

where

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Letting

$$\begin{bmatrix} G \end{bmatrix} = \text{Diag} (2 \overline{m}_1 \widetilde{\omega}_J, 2 \overline{m}_2 \widetilde{\omega}_J, \dots, 2 m_n \widetilde{\omega}_J)$$

3n x 3n

$$\begin{bmatrix} B \\ 3n \times 3n \end{bmatrix} = \text{Diag} (\overline{m}_1 (\widetilde{\omega}_J + \widetilde{\omega}_J \widetilde{\omega}_J), \dots, \overline{m}_n (\widetilde{\omega}_J + \widetilde{\omega}_J \widetilde{\omega}_J))$$

$$\left\{ RB \right\} = \begin{bmatrix} \ddots \\ R_{0} \\ \dot{\omega}_{0} \\ \dot{\omega}_{A1} \\ \dot{\omega}_{A2} \\ 10 \times 1 \end{bmatrix}$$

$$\begin{cases} \langle \omega_{J} \rangle = \begin{bmatrix} * \\ C_{J} \end{bmatrix}^{T} \begin{bmatrix} KG & 0 \\ 0 & 1 \end{bmatrix} \begin{cases} \omega_{AJ} \rangle \\ 2 \times 1 \end{cases}$$

NOTE: Motion of rotating arrays is exactly as defined in Section 4.1 with only two rotation degrees of freedom allowed.

$$\left\{ \begin{array}{c} \cdot \\ \mathbf{s} \end{array} \right\} = \left(\begin{array}{c} \cdot \\ \cdot \\ \cdot \\ \omega_{\mathrm{bi}} \end{array} \right)$$





$$\left\{ \begin{array}{c} L \\ S \\ 3n \\ x \\ 1 \end{array} \right\} = - \left[\begin{array}{c} m \\ \end{array} \right] \cdot \operatorname{Diag} \left(C_J^T \left(2 \\ \widetilde{\omega}_0 \\ C_J \\ \widetilde{\omega}_J \\ \end{array} \right)_J + C_J \\ \widetilde{\omega}_J \\ \widetilde{\omega}_J \\ \widetilde{\omega}_J \right)_J, \dots \right] \overline{r}$$

$$\overline{r} = \left[\begin{array}{c} r_{11}, r_{12}, r_{13}, \\ s_{11} \\ s_{12} \\ s_{13} \\ \end{array} \right]$$

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4.2.3.3 Modal Analysis

$$q = \phi_{\eta}$$

$$\Phi^{T} [m] \Phi = I$$

$$-\Phi^{T} [R] \{RB\} - \Phi^{T} [s_{2}] [\ell_{R}] \{\eta_{s}\}$$

$$+ \{\eta_{R}\} + [2 \varsigma \omega_{s}] \{\eta_{R}\} + [\omega_{s}^{2}] \{\eta_{R}\}$$

$$= -\Phi^{T} [G] \Phi \{\eta_{R}\} - \Phi^{T} [B] \Phi\{\eta_{R}\} + \Phi^{T} \{L\}$$

In summary, the above equation was derived assuming

- (a) base motion of the rotating array includes translations and rotations due to both space station rigid body motion and space station flexible motion
- (b) the rotating array is modeled by discrete masses; cantilever modes are used to define its modal motion
- (c) rotational motions of the array may be constrained as previously derived in Section 4.1.
- (d) the above equations are derived in the coordinate frame of the rotating array
- (e) small motion of the rotating arrays is not assumed to further linearize the above equation

4.2.4 TOTAL SYSTEM EQUATION

The above derived equations, along with the rigid body equations of Reference 4.1 can be combined into one large matrix ordinary differential equation of the form

where

$$\begin{bmatrix} M \end{bmatrix} \stackrel{\cdots}{x} + \begin{bmatrix} C \end{bmatrix} \stackrel{\cdot}{x} + \begin{bmatrix} K \end{bmatrix} x = P \qquad (4.16)$$

$$\stackrel{\cdots}{x} = \begin{bmatrix} \vdots \\ R \\ \vdots \\ n \\ s \\ \vdots \\ n \\ F \end{bmatrix}$$

The column dimensional size of Equation 4.16 is equal to $N_{TT} = 10 + N_s + N_R + N_F \le 70$.

 N_s - total number of simulated flexible space station modes

 N_R - total number of flexible cantilever modes associated with 0, 1, or 2 rotating arrays (= $N_{R1} + N_{R2}$)

 N_{F} - total number of flexible cantilever modes associated with 0, 1, 2, 3, or 4 fixed appendages (= $N_{F1} + N_{F2} + N_{F3} + N_{F4}$) Before preceding with the make up of the [M], [C], [K], [X], & [P] matrices it should again be made very clear that rotational motion of the two rotating arrays is exactly as defined in Section 4.1. Only two rotational degrees of freedom are allowed. Likewise, either axis of both drivers may be locked. No attempt has been made here to recount these equation derivations, or those involving array driver gear trains, etc.

The only departure from the equations derived in Sections 4.2, 4.3 and 4.4 has been to assume that the distances from the attachment points of rotating arrays $(\overline{h'}_J)$ and fixed appendages $(\overline{h'}_F)$ to the center of mass is negligible. This assumption has been made since the space station will be modeled as a collection of particle masses, with moments of inertia possible for each. This places the base of each array and appendage at a mass grid pt. of the space station. Therefore:



Submatrices of $\{x\}$

$$\{ \stackrel{\cdot}{\mathbf{R}} \} = \begin{bmatrix} \stackrel{\cdot}{\mathbf{R}} \\ \stackrel{\circ}{\mathbf{O}} \\ \stackrel{\cdot}{\mathbf{O}} \\ \stackrel{\omega}{\mathbf{O}} \\ \stackrel{\omega}{\mathbf{O}} \\ \stackrel{\omega}{\mathbf{A1}} \\ \stackrel{\omega}{\mathbf{A2}} \end{bmatrix}$$

rigid modes of space and two rotating arrays.

$$\left\{ \begin{matrix} \ddots \\ n \\ R \end{matrix} \right\} = \begin{bmatrix} \ddots \\ n \\ R \end{matrix} \right\}$$

$$\begin{cases} \vdots \\ n_{s} \\ s \\ s \end{cases} = \begin{bmatrix} \vdots \\ n_{s} \end{bmatrix} \qquad N_{s} \times 1$$

$$\begin{bmatrix} M \end{bmatrix} = \begin{bmatrix} \frac{M_{11}}{M_{11}} & \frac{M_{12}}{M_{21}} & \frac{M_{13}}{M_{23}} & \frac{M_{14}}{M_{24}} \\ \\ \frac{M_{21}}{M_{31}} & \frac{M_{22}}{M_{32}} & \frac{M_{23}}{M_{24}} \\ \\ \frac{M_{31}}{M_{41}} & \frac{M_{32}}{M_{42}} & 0 & I \end{bmatrix}$$

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 $= \begin{bmatrix} P_{1} & & \\ 10 \times 1 \\ P_{2} & N_{5} \times 1 \\ P_{3} & N_{R} \times 1 \\ P_{3} & N_{R} \times 1 \\ P_{4} & N_{F} \times 1 \end{bmatrix}$

P



As the above partitioning implies, Equation 4.16 is generated via four coupled matrix equations:

$$\begin{bmatrix} M_{11} \end{bmatrix} \stackrel{"}{R} + \begin{bmatrix} M_{12} \end{bmatrix} \stackrel{"}{n}_{S} + \begin{bmatrix} M_{13} \end{bmatrix} \stackrel{"}{n}_{R} + \begin{bmatrix} M_{14} \end{bmatrix} \stackrel{"}{n}_{F} = P_{1} \qquad (4.17)$$

$$\begin{bmatrix} M_{21} \end{bmatrix} \stackrel{"}{R} + \begin{bmatrix} M_{22} \end{bmatrix} \stackrel{"}{n}_{S} + \begin{bmatrix} M_{23} \end{bmatrix} \stackrel{"}{n}_{R} + \begin{bmatrix} M_{24} \end{bmatrix} \stackrel{"}{n}_{F} \qquad (4.18)$$

$$+ \begin{bmatrix} 2 \zeta_{g} \ \omega_{g} \end{bmatrix} \stackrel{"}{n}_{g} + \begin{bmatrix} \omega_{24} \end{bmatrix} \stackrel{"}{n}_{g} = P_{2} \qquad (4.18)$$

$$+ \begin{bmatrix} 2 \zeta_{g} \ \omega_{g} \end{bmatrix} \stackrel{"}{n}_{g} + \begin{bmatrix} \omega_{2} \\ \beta \end{bmatrix} n_{g} = P_{2} \qquad (4.19)$$

$$+ \begin{bmatrix} 2 \zeta_{R} \ \omega_{R} \end{bmatrix} \stackrel{"}{n}_{R} + \begin{bmatrix} \omega_{2} \\ \beta \end{bmatrix} n_{R} = P_{3} \qquad (4.19)$$

$$\begin{bmatrix} M_{41} \end{bmatrix} \stackrel{"}{R} + \begin{bmatrix} M_{42} \end{bmatrix} \stackrel{"}{n}_{g} + 0 + [1] \stackrel{"}{n}_{F} \qquad (4.20)$$

d.

Discussing each equation in detail:

Equation 4.17 is the basic rigid body system equation of Section 4.1 with only slight modification

(1) Forces and Torques on the system induced by the flexible appendage transient response are, in their own basis

 $\widehat{F}_{J} = -\sum_{E}^{T} M_{RJ} \Phi_{RJ} n_{RJ}$ $\widehat{T}_{J} = -\sum_{E}^{T} \widehat{r}_{RJ} M_{RJ} \Phi_{RJ} n_{RJ}$ $\widehat{F}_{FJ} = -\sum_{E}^{T} M_{FJ} \Phi_{FJ} n_{FJ}$ $\widehat{F}_{FJ} = -\sum_{E}^{T} M_{FJ} \Phi_{FJ} n_{FJ}$ $\widehat{f}_{FJ} = -\sum_{E}^{T} M_{FJ} \Phi_{FJ} n_{FJ}$ $\widehat{f}_{FJ} = -\sum_{E}^{T} \widehat{r}_{FJ} M_{FJ} \Phi_{FJ} n_{FJ}$ fixed appendages J = 1, 2, 3, 4

(2) Addition of applied external torque \overline{T}_R if desired

(3) Mass and moment of inertia of space station includes that do to any fixed appendages.

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 (4) Inclusion of terms dependent upon modal acceleration of space station at attachment points of appendages, (see 4.6.3).

Partitioning equation 4.17 into four equations:

$$A_{1} R_{0} + A_{5} \omega_{0} + A_{9} \omega_{A1} + A_{13} \omega_{A2}$$

$$- \sum_{J}^{2} C_{J} \hat{F}_{J} - \sum_{J}^{4} C_{FJ} \hat{F}_{FJ}$$

$$- \sum_{J}^{2} F_{J}' - \sum_{J}^{4} F_{FJ}' = F_{1}$$

$$\begin{bmatrix} M_{11} \end{bmatrix}_{10 \times 10}^{2} = \begin{bmatrix} M_{11} \end{bmatrix}_{10 \times 10}^{2} + A_{12} \end{bmatrix}_{A_{11}}^{2} + A_{13} \end{bmatrix}_{A_{2}}^{2} + A_{10} \end{bmatrix}_{A_{11}}^{2} + A_{13} \end{bmatrix}_{A_{2}}^{2} + A_{10} \end{bmatrix}_{A_{11}}^{2} + A_{13} \end{bmatrix}_{A_{2}}^{2} + A_{11} = A_{13} \end{bmatrix}_{A_{2}}^{2} + A_{10} + A_{10} = A_{10} + A_{10} + A_{10} = A_{10} + A_{$$

previously defined rigid body matrix A of Section 4.1.




where

 $\begin{bmatrix} D_{RJ} \\ 3 \times N_{RJ} \end{bmatrix} = \sum_{E}^{T} M_{RJ} \Phi_{RJ} \qquad J = 1,2$ $\begin{bmatrix} R_{RJ} \\ 3 \times N_{RJ} \end{bmatrix} = \sum_{E}^{T} \sum_{RJ}^{T} M_{RJ} \Phi_{RJ} \qquad J = 1,2$ $3 \times N_{RJ}$



 $\mathbf{D}_{\mathbf{F}J}$ where

ЕJ

MFJ

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$$\left[\mathbf{R}_{\mathbf{F}J} \right] = \sum_{\mathbf{r}}^{\mathbf{T}} \sum_{\mathbf{F}J}^{\mathbf{T}} \mathbf{M}_{\mathbf{F}J}$$

 Φ_{FJ}

3 x N_{FJ}

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as previously defined in Section 4.1 except for addition of external torque T_R

Equation 4.18 is the flexible modal equation for the space station. These flexible modes are excited by external forces and torques on the space station, including those which act at the attachment points of the rotating and fixed arrays.

Equations for the various hinge forces and torques are shown in Section 4.2.5.3. The above excluded linear terms in R_0 , $\dot{\omega}_0$, $\dot{\omega}_{A1}$, $\dot{\omega}_{A2}$ are regrouped on the left-hand side of Equation 4.16 for proper coupling with the rigid body modes (forming M_{21}). Linear terms in \ddot{n}_s are regrouped on the left-hand side of Equation 4.16 for proper coupling with the space station modes (M_{22}). Likewise, linear terms in \ddot{n}_R , and \ddot{n}_F form M_{23} and M_{24} , respectively.





0 1/KG 0 1/KG 11/KG = $-(I_2 - m_2 \widetilde{r}_2 \widetilde{r}_2) C_2^{*!}$ $a_2 = -(I_1 - m_1 \widetilde{r}_1 \widetilde{r}_1) C_1^*$ $a_1 = \tilde{m}_1 c_1 \tilde{r}_1 c_1^{T}$ $a_3 = \overline{m}_2 C_2 \overline{r}_2 C_2^{*T}$ а 4 0 = 11 = а₂ ື່ອ ຮ່ if J=2 if J=1

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(1)





10 x 6



where

$$\begin{bmatrix} G_{RJ} \\ \end{bmatrix}$$

the transpose of those rows of the modal space station matrix which define the total flexural 3-dimensional displacement of the rigid body of the space station to which the jth rotating appendage is attached.

- $\begin{bmatrix} G_{RJ}^{\ \prime\prime} \end{bmatrix}$ (N_s x 3)
- the transpose of those rows of the modal space station matrix which define the total flexural 3-dimensional rotation of the rigid body of the space station to which the jth rotating appendage is attached.

Like definitions are also true for submatrices G_{F_i} and G_{F_i} at the attachment points of each fixed appendage.

$$\begin{bmatrix} P_{2} \\ P_{2} \end{bmatrix} = \sum_{i=1}^{2} \begin{bmatrix} G_{E_{i}} \end{bmatrix} F_{R_{i}} + \sum_{i=1}^{2} \begin{bmatrix} G_{E_{i}} \end{bmatrix} T_{R_{i}} + \sum_{i=1}^{2} \begin{bmatrix} G_{R_{i}} \end{bmatrix} (-F_{H_{i}})$$

$$+ \sum_{i=1}^{2} \begin{bmatrix} G_{R_{i}} \end{bmatrix} (-T_{i} + T_{AC_{i}}) + \begin{bmatrix} G_{CMG} \end{bmatrix} T_{CMG}$$

$$+ \sum_{i=1}^{4} \begin{bmatrix} G_{R_{i}} \end{bmatrix} (-F_{H_{F_{i}}}) + \sum_{i=1}^{4} \begin{bmatrix} G_{F_{i}} \end{bmatrix} (-T_{H_{F_{i}}})$$

where

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hinge force on the jth rotating array due to rigid body motion of the array, excluding linear terms in \ddot{R}_{0} , $\dot{\omega}_{0}$, $\dot{\omega}_{A1}$, $\dot{\omega}_{A2}$, \dot{n}_{s}



т.ј

Gx

constraint torque exerted on spacecraft by rigid driver along constrained axis, excluding linear terms, (contains hinge torque).

hinge torque on jth driver produced by control system. hinge force on ith fixed appendage excluding linear terms.

hinge torque on ith fixed appendage excluding linear terms.

modal columns (eigenvectors) associated with modal displacements at grid point to which "x" array is attached or external force or torque acts.

modal columns associated with modal rotations at grid point to which "x" array is attached or external force or torque acts. Equation 4.19 is the rotating appendage modal equation in which

$$\begin{bmatrix} M_{31} \\ N_{R} \times 10 \end{bmatrix} = \begin{bmatrix} -\Phi_{R1}^{T} & [R_{1}] \\ -\Phi_{R2}^{T} & [R_{2}] \end{bmatrix}$$

$$\begin{bmatrix} -\Phi_{R1}^{T} & \begin{bmatrix} m_{R1} \end{bmatrix} \begin{bmatrix} -\Sigma_{E} C_{1}^{T} & \begin{bmatrix} \Sigma_{E} C_{1}^{T} & \tilde{q}_{R1} + \tilde{\tilde{r}}_{R1} & \Sigma_{E} C_{1}^{T} & \begin{bmatrix} \tilde{r}_{R1} & \Sigma_{E} C_{1}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & \end{bmatrix} & \begin{bmatrix} 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix}$$
$$-\Phi_{R2}^{T} & \begin{bmatrix} m_{R2} \end{bmatrix} \begin{bmatrix} -\Sigma_{E} C_{2}^{T} & \begin{bmatrix} \Sigma_{E} C_{2}^{T} & \tilde{q}_{R2} + \tilde{\tilde{r}}_{R2} & \Sigma_{E} C_{2}^{T} & 0 & \begin{bmatrix} \tilde{r}_{R2} & \Sigma_{E} C_{2}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix}$$
$$\begin{bmatrix} D_{R1}^{T} & C_{1}^{T} & -D_{R1}^{T} & C_{1}^{T} & \tilde{q}_{R1} + R_{R1}^{T} & C_{1}^{T} & R_{R1}^{T} & C_{1}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix}$$
$$\begin{bmatrix} D_{R2}^{T} & C_{2}^{T} & -D_{R2}^{T} & C_{2}^{T} & \tilde{q}_{R2}^{*T} + R_{R2}^{T} & C_{2}^{T} & 0 & \begin{bmatrix} R_{R2} & C_{2}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix} \end{bmatrix}$$
$$\begin{bmatrix} D_{R2}^{T} & C_{2}^{T} & -D_{R2}^{T} & C_{2}^{T} & \tilde{q}_{R2}^{*T} + R_{R2}^{T} & C_{2}^{T} & 0 & \begin{bmatrix} R_{R2} & C_{2}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix}$$
$$\begin{bmatrix} D_{R2}^{T} & C_{2}^{T} & -D_{R2}^{T} & C_{2}^{T} & \tilde{q}_{R2}^{*T} + R_{R2}^{T} & C_{2}^{T} & 0 & \begin{bmatrix} R_{R2} & C_{2}^{*T} & \begin{bmatrix} 1/KG & 0 \\ 0 & 1 \end{bmatrix} \end{bmatrix}$$
$$\begin{bmatrix} D_{R2}^{T} & C_{2}^{T} & 0 & R_{R2}^{*T} & C_{2}^{*T} & R_{R2}^{*T} & R_{R2}^{$$

$$\begin{bmatrix} M_{32} \end{bmatrix} = \begin{bmatrix} -\Phi_{R1}^{T} & S_{2}^{1} & \gamma_{R}^{1} \\ -\Phi_{R2}^{T} & S_{2}^{2} & \gamma_{R}^{2} \end{bmatrix}$$
$$= \begin{bmatrix} -\Phi_{R1}^{T} \begin{bmatrix} m_{R1} \end{bmatrix} \begin{bmatrix} -\Sigma_{E} & c_{1}^{T} & \frac{\widetilde{r}}{r_{R1}} & \Sigma_{E} & c_{1}^{T} \end{bmatrix} \begin{bmatrix} \gamma_{R}^{1} \\ R \end{bmatrix}$$
$$= \begin{bmatrix} -\Phi_{R1}^{T} \begin{bmatrix} m_{R1} \end{bmatrix} \begin{bmatrix} -\Sigma_{E} & c_{1}^{T} & \frac{\widetilde{r}}{r_{R1}} & \Sigma_{E} & c_{1}^{T} \end{bmatrix} \begin{bmatrix} \gamma_{R}^{1} \\ R \end{bmatrix}$$
$$= \begin{bmatrix} -\Phi_{R2}^{T} \begin{bmatrix} m_{R2} \end{bmatrix} \begin{bmatrix} -\Sigma_{E} & c_{2}^{T} & \frac{\widetilde{r}}{r_{R2}} & \Sigma_{E} & c_{2}^{T} \end{bmatrix} \begin{bmatrix} \gamma_{R}^{2} \end{bmatrix}$$

 ${}^{\mathrm{N}}_{\mathrm{R}} \times {}^{\mathrm{N}}_{\mathrm{s}}$

N. B.

 $\begin{bmatrix} M_{32} \end{bmatrix} = + \begin{bmatrix} M_{23} \end{bmatrix}^{T}$



Τ Φ F1 $\left[{}^{R}_{F1} \right]$ T F2 [R_{F2}] M41 = T N_F x 10 R_{F3} F3 Т R_{F4} ф F4

Equation 4.20 is the modal equation for the fixed appendages

$\begin{vmatrix} \mathbf{D}_{F1}^{T} \mathbf{C}_{F1}^{T} \\ - \mathbf{D}_{F1}^{T} \mathbf{C}_{F1}^{T} \\ - \mathbf{Q}_{F1}^{T} \mathbf{Q}_{F1}^{T} + \mathbf{R}_{F1}^{T} \mathbf{C}_{F1}^{T} \end{vmatrix}$	0
$D_{F2}^{T} C_{F2}^{T} - D_{F2}^{T} C_{F2}^{T} \widetilde{q}_{F2} + R_{F2}^{T} C_{F2}^{T}$	0
$\begin{bmatrix} - & - & - & - & - & - & - & - & - & - $	0
$D_{F4}^{T}C_{F4}^{T} - D_{F4}^{T}C_{F4}^{T}\widehat{q}_{F4} + R_{F4}^{T}C_{F4}^{T}$	0

N_F x 10

 $\begin{bmatrix} - \Phi_{F1}^{T} & \begin{bmatrix} S_{2}^{F1} \end{bmatrix} & \begin{bmatrix} \gamma_{F1} \end{bmatrix} \\ - \Phi_{F2}^{T} & \begin{bmatrix} S_{2}^{F2} \end{bmatrix} & \begin{bmatrix} \gamma_{F2} \end{bmatrix} \\ - \Phi_{F3}^{T} & \begin{bmatrix} S_{2}^{F3} \end{bmatrix} & \begin{bmatrix} \gamma_{F3} \end{bmatrix} \\ - \Phi_{F3}^{T} & \begin{bmatrix} S_{2}^{F3} \end{bmatrix} & \begin{bmatrix} \gamma_{F3} \end{bmatrix} \\ - \Phi_{F4}^{T} & \begin{bmatrix} S_{2}^{F4} \end{bmatrix} & \begin{bmatrix} \gamma_{F4} \end{bmatrix} \end{bmatrix}$

 $\mathbf{D}_{\mathbf{F1}}^{\mathbf{T}} \mathbf{C}_{\mathbf{F1}}^{\mathbf{T}} \mathbf{G'}_{\mathbf{F1}}^{\mathbf{T}} + \mathbf{R}_{\mathbf{F1}}^{\mathbf{T}} \mathbf{C}_{\mathbf{F1}}^{\mathbf{T}} \mathbf{G''_{\mathbf{F1}}}^{\mathbf{T}}$ (N_{F1} × N_s) $\overline{\mathbf{D}_{F2}^{T} \mathbf{C}_{F2}^{T} \mathbf{G}_{F2}^{\prime T} + \mathbf{R}_{F2}^{T} \mathbf{C}_{F2}^{T} \mathbf{G}_{F2}^{\prime \prime T}}$ $(N_{F2} \times N_s)$ $\mathbf{D}_{\mathbf{F3}}^{\mathbf{T}} \mathbf{C}_{\mathbf{F3}}^{\mathbf{T}} \mathbf{G}_{\mathbf{F3}}^{\mathbf{T}} + \mathbf{R}_{\mathbf{F3}}^{\mathbf{T}} \mathbf{C}_{\mathbf{F3}}^{\mathbf{T}} \mathbf{G}_{\mathbf{F3}}^{\mathbf{T}}$ $(N_{F3} \times N_s)$ $\overline{D_{F4}^{T} C_{F4}^{T} G_{F4}^{'T} + R_{F4}^{T} C_{F4}^{T} G_{F4}^{'T}}$ $(N_{F4} \times N_s)$

N_F × N_s

 $\begin{bmatrix} P_4 \\ N_F \times 1 \end{bmatrix} = 0$ $N.B. \begin{bmatrix} M_{42} \end{bmatrix} = + \begin{bmatrix} M_{24} \end{bmatrix}^T$ 4-150

[M₄₂]

4.2.5 AUXILIARY EQUATIONS

4.2.5.1 When free-free modes are utilized in the definition of spacecraft

flexibility it can be shown that



Considering the first term of the product,





Since for the free-free case, the spacecraft structure is in dynamic equilibrium with respect to all forces such that

This equilibrium condition also applies to torques.

Rearranging the remaining terms $m_i (R_0 + q_i)$ by letting

$$R_0^1 = R_0 + \overline{q}$$
$$q_i^1 = q_i - \overline{q}$$

where \overline{q} is the constant vector from point O_B to the center of gravity of the undeformed system.

$$\gamma^{T} \begin{bmatrix} \frac{\overline{m}_{1} (R_{0}^{1} + q_{1}^{1})}{0} \\ \frac{\overline{m}_{2} (R_{0}^{1} + q_{2}^{1})}{0} \\ 0 \\ \vdots \end{bmatrix} = \begin{bmatrix} \overline{m}_{1} \\ 0 \\ \overline{m}_{2} \\ 0 \\ \vdots \end{bmatrix} (\sum_{E} R_{0}^{1}) + \gamma^{T} \begin{bmatrix} \overline{m}_{1} q_{1}^{1} \\ 0 \\ \overline{m}_{2} q_{2}^{1} \\ 0 \\ \vdots \\ 0 \\ \vdots \end{bmatrix} = 0$$

The first term is zero as shown previously. The second term is also zero since

 $\sum_{J} \gamma_{iJ} m_{J} q_{J}^{1}$

represents the moment about the center of mass which equals zero in the free-free case.

4.2.5.2 Nastran Algorithm

The integration of the system equation developed in Section 4.2.4 will be accomplished by use of the Nastran algorithm.

$$\begin{bmatrix} \frac{M}{\Delta t^2} + \frac{C}{2\Delta t} + \frac{K}{3} \\ + \begin{bmatrix} \frac{2M}{\Delta t^2} - \frac{K}{3} \\ \end{bmatrix} \left\{ X_{\eta+2} \right\} = \frac{1}{3} \qquad \begin{bmatrix} P_{\eta+2} + P_{\eta+1} + P_{\eta} \\ + \begin{bmatrix} \frac{2M}{\Delta t^2} - \frac{K}{3} \\ \end{bmatrix} \left\{ X_{\eta+1} \right\} + \begin{bmatrix} -\frac{M}{\Delta t^2} + \frac{C}{2\Delta t} - \frac{K}{3} \\ - \frac{K}{3} \end{bmatrix} \left\{ X_{\eta} \right\}$$
$$\left\{ \frac{\cdot}{X_{\eta}} \right\} = \frac{1}{2\Delta t} \qquad \begin{bmatrix} X_{\eta+1} \\ - \frac{X_{\eta-1}} \\ - \frac{X_{\eta-1}} \end{bmatrix}$$
$$\left\{ \frac{\cdot\cdot}{X_{\eta}} \right\} = \frac{1}{\Delta t^2} \qquad \begin{bmatrix} X_{\eta+1} \\ - 2 \\ - 2 \end{bmatrix} \left\{ X_{\eta} \right\} - \left\{ X_{\eta-1} \\ - 2 \\ - 2 \end{bmatrix}$$

* See Reference 4.7

4.2.5.3 Interaction Forces and Torques

The interaction forces (torques) which exist at the attachment points of the various arrays are calculated by summing the hinge force (torque) due to rigid body motion of the system at the attachment point and the flexible appendage transient response.

Hinge force for rotating array*:

$$\mathbf{F}_{H_{i}} = \mathbf{m}_{i} \left[\begin{array}{c} \mathbf{\ddot{R}}_{o} + 2 \ \widetilde{\omega}_{o} \ \mathbf{\ddot{R}}_{o} + (\dot{\widetilde{\omega}}_{o} + \widetilde{\omega}_{o} \ \widetilde{\omega}_{o}) \ (\mathbf{R}_{o} + \mathbf{h}_{i} + \mathbf{C}_{i} \ \mathbf{r}_{i}) \right] + 2 \ \widetilde{\omega}_{o} \ \mathbf{C}_{i} \ \widetilde{\omega}_{i} \ \mathbf{r}_{i} + \mathbf{C}_{i} \ (\widetilde{\omega}_{i} \ \widetilde{\omega}_{i} + \dot{\widetilde{\omega}}_{i}) \ \mathbf{r}_{i} \right] + \mathbf{F}_{i}^{\prime}$$

Hinge torque for rotating array*:

$$T_{H_{i}} = C_{i} \left[((C_{i}^{T} \omega_{o})^{+} \widetilde{\omega}_{i}) [I_{i}] (\omega_{i} + C_{i}^{T} \omega_{o}) + [I_{i}] (\omega_{i} + C_{i}^{T} \dot{\omega}_{o}) + [I_{i}] (C_{i}^{T} \widetilde{\omega}_{o} C_{i} \omega_{i}) \right]$$
$$+ C_{i} \widetilde{r}_{i} C_{i}^{T} F_{H_{i}} + T_{i}^{+}$$

Force induced by flexible appendage transient response $\stackrel{\wedge}{F}_{i} = -\left(\sum_{E}^{T} M_{i} \phi_{i}\right) \stackrel{\cdot}{n}_{i}$

Torque induced by flexible appendage transient response

$$\hat{\mathbf{T}}_{\mathbf{i}} = -\sum_{\mathbf{F}}^{\mathbf{T}} \quad \tilde{\tilde{\mathbf{r}}}_{\mathbf{i}} \quad \mathbf{M}_{\mathbf{i}} \quad \boldsymbol{\phi}_{\mathbf{i}} \quad \mathbf{n}_{\mathbf{i}}$$

* Equations for hinge forces and torques for fixed appendages are identical except that $\omega_i=0$ (the negative of these hinge forces and torques acts on the space station). Admittedly, for the rotating case, some products have been neglected which couple ω_i with modal variables and ω_o , basically assuming that ω_i will also be small.

Hinge force for rotating array due to space station modal accelerations of attachment point:

Hinge torque for rotating array due to space station modal accelerations of attachment point:

$$T_{i}' = \left[\tilde{m}_{i}(\tilde{C}_{i}r_{i}) \middle| C_{i}I_{i}C_{i}^{T} - \tilde{m}_{i}(\tilde{C}_{i}r_{i})^{2} \right] \left[-\frac{G_{i}^{T}}{G_{i}} \right] \frac{n}{s}$$

$$3 \times 6 \qquad 6 \times N_{s}$$

The total interaction force at the attachment point of an array is

$$\mathbf{F}_{\mathbf{iNT}_{\mathbf{i}}} = -\mathbf{F}_{\mathbf{H}_{\mathbf{i}}} + \mathbf{F}_{\mathbf{i}}$$

Likewise, the total interaction torque acting on the space station due to the attachment of a flexible array is

$$T_{iNT_i} = -T_{H_i} + T_i$$

4.3 FLEXIBLE SPINNING SPACE STATION

4.3.1 MODAL EQUATIONS

(1)
$$\left[\begin{array}{c} m \end{array} \right] \left[\begin{array}{c} \ddot{q} \end{array} \right] + \left[\begin{array}{c} K \end{array} \right] \left\{ q \right\} = - \left[\begin{array}{c} G \end{array} \right] \left\{ \begin{array}{c} \dot{q} \end{array} \right\} - \left[\begin{array}{c} B \end{array} \right] \left\{ q \right\} + \left[\begin{array}{c} R \end{array} \right] \left\{ \begin{array}{c} RB \end{array} \right\} \\ + \left\{ F' \right\} + \left\{ \begin{array}{c} L \end{array} \right\} \end{array}$$

where [R] and {L} are rigid body terms. If we choose $u = R_0 + q_i + x_i$ we can form the following set of equations of motion

(2)
$$[m] \{ \ddot{u} \} + [G] \{ \ddot{u} \} + [K'] \{ u \} \neq \{ F' \}$$

where [m]is mass matrix of the space station,

[G] is skew symmetric matrix of coriolis acceleration terms
and [K'] = [K_e] + [K_c] + [B]
[K_e] = elastic stiffness matrix
[K_c] = symmetric matrix of centrifugal acceleration terms

[B] = geometric stiffness matrix

The second-order matrix equation (2) can be reduced to a first order state equation (3) by introducing the following matrices

 $\mathbf{U} = \begin{bmatrix} \mathbf{u} \\ \mathbf{u} \end{bmatrix} \quad \text{and} \quad \mathbf{\dot{U}} = \begin{bmatrix} \mathbf{\ddot{u}} \\ \mathbf{\dot{u}} \end{bmatrix}$

(3) $[D]\{\dot{U}\} + [E]\{U\} = \{F\}$

where

$$\begin{bmatrix} D \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} 0 \\ m \end{bmatrix}^{-1} - \begin{bmatrix} m \\ m \end{bmatrix}^{-1} \\ \begin{bmatrix} G \end{bmatrix}^{-1} \end{bmatrix}, \quad \begin{bmatrix} E \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} m \\ 0 \end{bmatrix}^{-1} - \begin{bmatrix} 0 \\ 0 \end{bmatrix}^{-1} \\ \begin{bmatrix} K \end{bmatrix}^{-1} \end{bmatrix}$$
and

$$\{F\} = \begin{bmatrix} \frac{10}{F} \\ \frac{10}{F} \end{bmatrix}$$

The reduced equation of motion (3) can be uncoupled by the transforma-

tion

(4)
$$\{\mathbf{U}\} = \begin{bmatrix} \mathbf{\Phi} \end{bmatrix} \{\mathbf{Y}\}$$
, where $\begin{bmatrix} \mathbf{\Phi} \end{bmatrix} = \begin{bmatrix} \lambda_{\mathbf{n}} \end{bmatrix} \begin{bmatrix} \phi^{(\mathbf{n})} \end{bmatrix}$

and the transformation matrix $[\Phi]$ consists of complex eigenvectors and their conjugates pairs.

$$\begin{bmatrix} \phi^{(n)} \end{bmatrix} = \begin{bmatrix} \phi^1 \\ \phi^2 \end{bmatrix} - - \begin{bmatrix} \phi^N \\ \phi^1 \end{bmatrix} \begin{bmatrix} \phi^{2*} \\ \phi^{2*} \end{bmatrix} - - \begin{bmatrix} \phi^{N*} \\ \phi^n \end{bmatrix} = DIAG(-jw_1, -, -jw_n)$$

$$\begin{cases} \phi^* \\ \phi^* \end{bmatrix} = complex conjugate of \{\phi\},$$

 $Y \equiv \begin{bmatrix} Y_1 Y_2 & \cdots & Y_N & Y_1 Y_2 & \cdots & Y_N \\ Y_1 x_2 & \cdots & Y_N & y_1 & y_2 & \cdots & y_N \end{bmatrix}^{T}$ we winter eigenvalues and ϕ^i are eignevectors.

where w_i are eigenvalues and ϕ^i are eignevectors. In terms of the new coordinates Y, Equation (3) becomes

(5) $\left[D\right]\left[\Phi\right]\left\{Y\right\} + \left[E\right]\left[\Phi\right]\left\{Y\right\} = \left\{F\right\}$

Premultiplication of Equation (5) by $\begin{bmatrix} \phi^* \end{bmatrix}^T$

(6)
$$\left[\boldsymbol{\Phi}^{*} \right]^{\mathrm{T}} \left[\mathbf{D} \right] \boldsymbol{\Phi} \left\{ \dot{\mathbf{Y}} \right\} + \left[\boldsymbol{\Phi}^{*} \right] \left[\mathbf{E} \right] \left[\boldsymbol{\Phi} \right] \left\{ \mathbf{Y} \right\} = \left[\boldsymbol{\Phi}^{*} \right]^{\mathrm{T}} \left\{ \mathbf{F} \right\}$$

Since [E] is symmetric and [D] skew symmetric, $[\Phi^*]^T [\Phi] = diagonal matrix.⁽²⁾$ Writing equation (6) in simplier form

(7) $\left[D'\right]\left\{\dot{\mathbf{Y}}\right\} + \left[\mathbf{E'}\right]\left\{\mathbf{Y}\right\} = \left[\boldsymbol{\Phi}^{*}\right]^{T}\left\{\mathbf{F}\right\}$

where

 $\begin{bmatrix} D' \end{bmatrix} = \begin{bmatrix} \phi \\ \phi \end{bmatrix}^{T} \begin{bmatrix} D \end{bmatrix} \begin{bmatrix} \phi \end{bmatrix} = \text{diagonal matrix}$ $\begin{bmatrix} E' \end{bmatrix} = \begin{bmatrix} \phi \\ \phi \end{bmatrix}^{T} \begin{bmatrix} E \end{bmatrix} \begin{bmatrix} \phi \end{bmatrix} = \text{diagonal matrix}$

If $[\Lambda]$ is the matrix of the complex eigenvalues of the operator in Equation (7), then upon premultiplication by $[D']^{-1}$ we obtain

(8)
$$\left\{ \begin{array}{c} \cdot \\ Y \end{array} \right\} = -\left[- \wedge \right] \left\{ Y \right\} + \left\{ \begin{array}{c} - \\ F \end{array} \right\}$$

where $\left\{ \begin{array}{c} - \\ F \end{array} \right\} = \left[D' \right]^{-1} \left[\Phi * \right]^{T} \left\{ F \right\}$



N is the number of modes of the space station to be preserved in the simulation.

Equation (8) can be written as:

$$(9) \begin{bmatrix} \frac{\mathbf{i}}{\mathbf{Y}} \\ \frac{\mathbf{i}}{\mathbf{Y}} \end{bmatrix} = -\begin{bmatrix} \overline{\mathbf{A}} & \mathbf{0} \\ \mathbf{0} & \overline{\mathbf{A}}^* \end{bmatrix} \begin{bmatrix} \overline{\mathbf{Y}} \\ \overline{\mathbf{Y}}^* \end{bmatrix} + \{\overline{\mathbf{F}}\}$$
where $\overline{\mathbf{Y}} \equiv \begin{bmatrix} \mathbf{Y}_1 & \mathbf{Y}_2 & \cdots & \mathbf{Y}_N \\ \mathbf{Y}^* \equiv \begin{bmatrix} \mathbf{Y}_1^* & \mathbf{Y}_2^* & \cdots & \mathbf{Y}_N^* \end{bmatrix}^T$

$$\overline{\mathbf{A}} \equiv \begin{bmatrix} \mathbf{A}_1 \\ \mathbf{A}_2 & \mathbf{0} \\ \mathbf{0} & \mathbf{A}_N \end{bmatrix}$$

$$\overline{\mathbf{A}}^* \equiv \begin{bmatrix} \mathbf{A}_1^* & \mathbf{0} \\ \mathbf{A}_2^* & \mathbf{0} \\ \mathbf{A}_N \end{bmatrix}$$

Multiply both sides of Equation (9) by

$$\frac{1/2}{\begin{array}{c} I & I \\ J & J \end{array}}$$

I = unity matrix
J =
$$\sqrt{-1}$$
 I

and let

$$Z_{i}^{(1)} = (1/2)(Y_{i} + Y_{i}^{*})$$

$$Z_{i}^{(2)} = (1/2)J(Y_{i} - Y_{i}^{*})$$

$$(10) \quad \left(\begin{array}{c} \overline{Z}^{(1)} \\ \overline{Z}^{(2)} \end{array} \right) = \left[\begin{array}{c} 0 & | \wedge | \\ | \wedge | & 0 \end{array} \right] \quad \left[\begin{array}{c} \overline{Z}^{(1)} \\ \overline{Z}^{(2)} \end{array} \right] + \left[V \right] \left[F_{i}^{T} \right]$$

where

$$\begin{bmatrix} V \end{bmatrix} = \frac{1}{2} \begin{bmatrix} I & | & I \\ J & | & -J \end{bmatrix} \begin{bmatrix} D \end{bmatrix}^{-1} \begin{bmatrix} \phi^* \end{bmatrix}^T$$

when N modes are retained

$$\vec{z}^{(1)} \equiv \begin{bmatrix} z_1^{(1)} \\ \vdots \\ z_1^{(1)} \\ \vdots \\ z_N^{(2)} \end{bmatrix}$$
$$\vec{z}^{(2)} \equiv \begin{bmatrix} z_1^{(2)} \\ \vdots \\ z_N^{(2)} \\ \vdots \\ z_N^{(2)} \end{bmatrix}$$

Modal damping may be introduced in Equation (1) by the matrix $-2\xi^{|\Lambda|}$

$$\begin{array}{c} (11) \\ \left[\frac{\cdot}{Z} (1) \\ \frac{\cdot}{Z} (2) \end{array} \right] + \left[\begin{array}{c} 0 & -1 & \overline{-1} \\ 1 & \overline{-1} & 2\xi & \overline{-1} \end{array} \right] \left[\begin{array}{c} \overline{z} (1) \\ \overline{z} (2) \end{array} \right] = \left[V \right] \left[F' \right]$$

where ξ = arbitrary chosen damping factor.

** See Section 4.3.6.

In terms of the new coordinates \overline{Z} , Equation (4) may be written as

(12) $\{U\} = \begin{bmatrix} \Phi \end{bmatrix} \{Y\} = \begin{bmatrix} \Phi \end{bmatrix} \begin{bmatrix} I & J \\ J & J \end{bmatrix} \begin{bmatrix} \overline{Z} & (1) \\ \overline{Z} & (2) \end{bmatrix}$

or

(13)
$$\{U\} = \begin{bmatrix} w \end{bmatrix} \begin{bmatrix} \overline{z} \end{bmatrix}$$

where $\begin{bmatrix} w \end{bmatrix} = \begin{bmatrix} \phi \end{bmatrix} \begin{bmatrix} \\ - \end{bmatrix} \begin{bmatrix} - \end{bmatrix} = \begin{bmatrix} 1 \end{bmatrix}$

$$\begin{bmatrix} \mathbf{w} \end{bmatrix} \equiv \begin{bmatrix} \mathbf{\Phi} \end{bmatrix} \begin{bmatrix} \mathbf{I} & \mathbf{J} \\ -\mathbf{I} & \mathbf{J} \end{bmatrix}$$
$$\begin{bmatrix} \mathbf{\bar{z}} \end{bmatrix} \equiv \begin{bmatrix} \mathbf{\bar{z}} & (1) \\ \mathbf{\bar{z}} & (2) \end{bmatrix}$$

Equations (11) and (13) are to be implemented in the simulation.

N.B. If desired, the variation of ω_0 about the nominal can be accommodated by setting

(14) $G' = \frac{\partial [G]}{\partial \omega}$ (15) $B' = \frac{\partial [B]}{\partial \omega}$

(16)
$$\Delta \omega = (\omega_{o} - \omega_{nom})$$

For this case(10) is modified to give

(10a)
$$\begin{bmatrix} \frac{i}{Z}(1) \\ \frac{i}{Z}(2) \end{bmatrix} + \begin{bmatrix} 0 & -i\overline{A}i \\ i\overline{A}i & 0 \end{bmatrix} \begin{bmatrix} \overline{Z}^{(1)} \\ \overline{Z}^{(2)} \end{bmatrix} = \begin{bmatrix} V \end{bmatrix} \begin{bmatrix} F' \end{bmatrix} - \begin{bmatrix} V \end{bmatrix} \begin{pmatrix} G' \end{bmatrix} + \begin{bmatrix} B' \end{bmatrix} \Delta \omega$$

4.3.2 RIGID BODY EQUATIONS

The equations developed in Section 4.3.1 will be used to simulate N complex flexible modes for the space station. The rigid body modes will not be used. Instead, the rigid body motion will be given by the Newton-Euler equations for the rotating space station taken as a rigid body.

The rigid body system given in Figure 4-12 describes the force and torque relationships which exist for two rigid appendages and a rigid body_space station.

Newton's and Euler's vector equations of motion for the space station can be written as

(17)
$$M_T \frac{d^2}{dt^2} \Big|_{I} (R_o + C) = F_E$$

 $\tilde{\mathbf{C}}$

r F_J

Space station moment equation

(18)
$$\frac{d}{dt} \Big|_{I} (\bar{\tilde{I}}_{T} \cdot \bar{\omega}_{O}) = \bar{T}_{E}$$

where M_{T} = total system mass.

= vector from space station reference to system rigid body CG.

 \bar{R}_{o} = location of space station reference point with respect to inertial space

$$\vec{I}_T$$
 = inertia dyadics of the space station about its center of mass.

 $\bar{\omega}_{0}$ = angular velocity vector of the space station, with respect to inertial space

= location of attachment point of appendage with respect to space station reference point

$$4 - 162$$



FIGURE 4-12. RIGID BODY SYSTEM CONFIGURATION

 \overline{F}_{Ext} = external forces applied to space station \overline{T}_{Fxt} = external torques applied to space station

Defining \overline{R}_{0} and \overline{C} in the X_S frame (coordinate basis fixed to and moving with the space station taken as rigid body) and carrying out the differentiation w.r.t.time we obtain (see Section 4.2 for the following derivation conventions)

(19)
$$\overrightarrow{R}_{o} = \overrightarrow{I}^{T} \overrightarrow{C}_{o} \overrightarrow{R}_{o}$$
, $\overrightarrow{C} = \overrightarrow{I}^{T} \overrightarrow{C}_{o} \overrightarrow{C}$

(20)
$$\frac{d}{dt}\Big|_{I} (\dot{\vec{R}}_{o} + \dot{\vec{C}}) = I^{T} \left[C_{o} \widetilde{\omega}_{o} R_{o} + C_{o} R_{o} + C_{o} \widetilde{\omega}_{o} C\right]$$

$$(21) \qquad \frac{d^{2}}{dt^{2}}\Big|_{I} (\vec{R}_{o} + \vec{C}) = I^{T} \left[C_{o}\widetilde{\omega}_{o}\widetilde{\omega}_{o}R_{o} + C_{o}\widetilde{\omega}_{o}R_{o} + 2C_{o}\widetilde{\omega}_{o}R_{o} + C_{o}R_{o} + C_{o}R_{o} + C_{o}\widetilde{\omega}_{o}C\right] + C_{o}\widetilde{\omega}_{o}\widetilde{\omega}_{o}C + C_{o}\widetilde{\omega}_{o}C\right] = X_{S}^{T} \left[\left(\widetilde{\omega}_{o}\widetilde{\omega}_{o} + \widetilde{\omega}_{o}\right)\left(R_{o} + C\right) + 2\widetilde{\omega}_{o}R_{o} + \vec{R}_{o}\right] (22) \qquad \frac{d}{dt}\Big|_{I} \left(\vec{\bar{I}}_{T}, \vec{\omega}_{o}\right) = I_{T}\dot{\omega}_{o} + \widetilde{\omega}_{o}I_{T}\omega_{o}$$

Substituting equation (21) and (22) in equation (17) and (18), we obtain rigid body equations of motion for the space station

(23)
$$M_{T}\left(R_{o} + (\tilde{\omega}_{o} + \tilde{\omega}_{o}\tilde{\omega}_{o}) (R_{o} + C) + 2\tilde{\omega}_{o}R_{o}\right) = F_{E}$$

(24)
$$I_{T}\dot{\omega}_{O} + \widetilde{\omega}_{O}I_{T}\omega_{O} = T_{E}$$

where

$$M_{T} = M_{o} + \sum_{i=1}^{4} m_{Fi}$$

$$\overline{C} = \underbrace{M_{o}\overline{r} + \underbrace{\Sigma}_{i=1}^{4} m_{Fi} (\overline{h}_{Fi} + C_{Fi} \overline{r}_{Fi})}_{M_{T}}$$

$$I_{T} = I_{o} - M_{o} \left(\vec{r}_{o} - \vec{C} \right)^{2} + \sum_{i=1}^{4} C_{Fi} \left[I_{Fi}^{\prime} \right] C_{Fi}^{T}$$
$$I_{Fi}^{\prime} = I_{Fi} - m_{Fi} \left(C_{Fi}^{T} \vec{h}_{Fi} + \vec{r}_{Fi} C_{Fi}^{T} \vec{C}_{Fi}^{T} \vec{C} \right)^{2}$$

$$F_{E} = \text{external forces } (F_{R_{J}}) + \text{force due to flexible appendage motion } (F_{A_{J}}) + \text{force due to flexible motion of base point of appendage} (F_{A'_{J}}) + \text{force due to flexible motion of base point of appendage} (F_{A'_{J}}) = F_{R1} + F_{R2} + \sum_{J=1}^{2} C_{F_{J}}(F_{A_{J}} + F_{A'_{J}}) + F_{A_{J}} = -\sum_{E}^{T} M_{F_{J}} W_{F_{J}} \dot{z}_{F_{J}}$$

$$F_{A_{J}} = -\sum_{E}^{T} M_{F_{J}} W_{F_{J}} \dot{z}_{F_{J}}$$

$$F_{A'_{J}} = m_{F_{i}} W_{S_{i}} Z_{S}$$
 see section 2.5.1
$$F_{E} = \text{external torques} + \text{torque due to flexible appendage motion} + \text{torque due to flexible motion of base point of appendage}$$

$$T_{E} = T_{R1} + T_{R2} - (\tilde{1}_{R1}) F_{1} - (\tilde{1}_{R2}) F_{2}$$

-
$$\sum_{i=1}^{4} C_{F_{i}} T_{A_{i}} + \sum_{i=1}^{4} F_{F_{i}} C_{F_{i}} (F_{A_{i}} + F_{A_{i}})$$

-
$$\sum_{i=1}^{4} C_{F_{i}} I_{F_{i}} C_{F_{i}} W_{S_{b_{i}}} \dot{z}_{S}$$

. -

 $T_{A_{i}} = \sum_{E}^{T} \widetilde{R}_{F_{i}} M_{F_{i}} W_{F_{i}} \dot{z}_{F_{i}}$ $T_{R_{J}} = \text{externally applied torque (J = 1, 2)}$ $F_{R_{J}} = \text{externally applied forces (J = 1, 2)}$ $M_{F_{i}} = \text{mass of } i^{\text{th}} \text{ appendage}$ $M_{o} = \text{mass of space station}$ $I_{R_{i}} = \text{location of application point of } i^{\text{th}} \text{ external force with respect to system center of mass (negative of)}$ $I_{F_{i}} = \text{inertia matrix of } i^{\text{th}} \text{ appendage}$

R = location of space station center of mass with respect to space station reference point

 $r_{F'_i} = (r - h_{F_i})$

Equation (23) and (24) may be expressed in matrix form

$$\begin{array}{l} (25) \qquad \left[\frac{M_{T}+M_{T}\widetilde{C}}{0}+\widetilde{L}_{T}^{T}\right]\left[\frac{\widetilde{R}}{\omega_{O}}\right]+\left[0\right]\left[\frac{\widetilde{R}}{\omega_{O}}\right]+\left[0\right]\left[\frac{\widetilde{R}}{0}\right]+\left[0\right]\left[\frac{\widetilde{R}}{0}\right]\\ = \left[\frac{F_{E}-M_{T}}{0}\left(\widetilde{\omega}+\widetilde{\omega}_{O}+\widetilde{\omega}_{O}\widetilde{\omega}\right)R_{O}+\widetilde{\omega}_{O}\widetilde{\omega}_{O}\widetilde{C}+2\widetilde{\omega}_{O}\dot{R}_{O}\right]\\ T_{E}-\widetilde{\omega}_{O}I_{T}\omega_{O} \end{array} \right]$$

4.3.3 EQUATIONS OF FLEXIBLE APPENDAGES ATTACHED TO THE SPINNING SPACE STATION

The motion of a fixed flexible appendage is modeled as in previous derivations . Cantilevered mode shapes are used to represent the flexible appendage, whose fixed base is excited by the translational and rotational motion of the rigid body of the spinning space station, and the modal motions of the flexible space station at that point.

4.3.3.1 COORDINATE FRAMES AND RELATIONSHIPS

- [I] = inertially fixed coordinates
- $[X_S]$ = coordinate basis fixed and moving with the space station taken as rigid body, origin at reference point O_B . (See Figure 4-13).
- $[X_{F}]$ = coordinate basis defined with origin at attachment point of appendage and axes directed along principal axes of the appendage.

The relationship between $\begin{bmatrix} I \end{bmatrix}$ and $\begin{bmatrix} X \\ F \end{bmatrix}$ is defined by the direction cosine relationship

 $[I] = C_{O}C_{F}[X_{F}]$

4.3.3.2 EQUATION DERIVATIONS

Using D'Alembert's principle, the total force acting on the jth particle of the ith appendage equals

(26)
$$\left\{F_{j}\right\} = m_{j} \frac{d^{2}}{dt^{2}} \left[\overrightarrow{a}_{i} + \overrightarrow{r}_{j} + \overrightarrow{u}_{j}\right]_{I}$$

where $\overline{a_i}$ is the position vector of the hinge point of ith fixed appendage w.r.t. inertial space

$$\vec{\mathbf{a}}_{i}^{\lambda} = \mathbf{I}^{T} \mathbf{a}_{i}^{\lambda}$$
$$\vec{\mathbf{r}}_{j}^{\lambda} = \mathbf{I}^{T} \mathbf{C}_{o} \mathbf{C}_{F} \mathbf{r}_{j}^{\lambda}$$
$$\vec{\mathbf{u}}_{j}^{\lambda} = \mathbf{I}^{T} \mathbf{C}_{o} \mathbf{C}_{F} \mathbf{u}_{j}^{\lambda}$$



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$$\frac{d}{dt} \stackrel{\dot{r}_{j}}{r} = \frac{d}{dt} \left[I^{T}C_{o}C_{F}r_{j} \right] = I^{T} \left[C_{o}\omega_{o}C_{F}r_{j} \right]$$

$$\frac{d^{2}}{dt^{2}} \stackrel{\dot{r}_{j}}{r} = \frac{d}{dt} \left[I^{T}C_{o}\overset{\omega}{}_{o}C_{F}r_{j} \right]$$

$$= I^{T}C_{o}\overset{\omega}{}_{o}\overset{\omega}{}_{o}C_{F}r_{j} + I^{T}C_{o}\overset{\omega}{}_{o}C_{F}r_{j}$$

$$\frac{d}{dt} \stackrel{\dot{u}_{j}}{u} = \frac{d}{dt} \left[I^{T}C_{o}C_{F}u_{j} \right] = I^{T}C_{o}\overset{\omega}{}_{o}C_{F}u_{j} + I^{T}C_{o}C_{F}u_{j}$$

$$\frac{d^{2}}{dt^{2}} \stackrel{\dot{u}_{j}}{u} = \frac{d}{dt} \left[I^{T}C_{o}\overset{\omega}{}_{o}C_{F}u_{j} + I^{T}C_{o}C_{F}u_{j} \right]$$

$$= I^{T} \left[C_{o}\overset{\omega}{}_{o}C_{F}u_{j} + I^{T}C_{o}C_{F}u_{j} + I^{T}C_{o}C_{F}u_{j} \right]$$

Substituting the above equations in equation (26), we obtain

$$(27) \quad \left\{ F_{j} \right\}^{=} \qquad m_{j} I^{T} \left\{ \ddot{a}_{i} + C_{o} \left[\left(\widetilde{\omega}_{o} \widetilde{\omega}_{o} + \widetilde{\omega}_{o} \right) C_{F} r_{j} \right] \\ + \left(\widetilde{\omega}_{o} \widetilde{\omega}_{o} + \widetilde{\omega}_{o} \right) C_{F} u_{j} + 2 \widetilde{\omega}_{o} C_{F} u_{j} + C_{F} u_{j} \right] \right\} \\ = m_{j} I^{T} C_{o} C_{F} \left\{ C_{F}^{T} C_{o}^{T} \ddot{a}_{i} + C_{F}^{T} \left[\left(\widetilde{\omega}_{o} \widetilde{\omega}_{o} + \widetilde{\omega}_{o} \right) C_{F} r_{j} \right] \\ + \left(\widetilde{\omega}_{o} \widetilde{\omega}_{o} + \widetilde{\omega}_{o} \right) C_{F} u_{j} + 2 \widetilde{\omega}_{o} C_{F} u_{j} \right] + u_{j} \right\}$$

where $C_0^{T_{a_i}}$ is sum of rigid body and space station modal accelerations at the attached point of ith appendage

(28)
$$C_0^T \ddot{a}_i = (\ddot{R}_i)' + U_{S_i}$$

 $(\ddot{R}_i)' \sim rigid body acceleration of the ith appendage attachment point $(\ddot{U}_{S_i}) \sim space station modal acceleration of the ith appendage attachment point$$

(29)
$$I^{T}C_{o}(\ddot{R})' = \frac{d^{2}}{dt^{2}} \left[\vec{h}_{o} + \vec{h}_{F_{i}} \right]_{I} = \frac{d^{2}}{dt^{2}} \left[I^{T}C_{o}(R_{o} + h_{F_{i}}) \right]$$
$$= I^{T}C_{o} \left[\widetilde{\omega}_{o}\widetilde{\omega}_{o}(R_{o} + h_{F_{i}}) + \widetilde{\omega}_{o}(R_{o} + h_{F_{i}}) + 2\widetilde{\omega}_{o}\dot{R}_{o} + \ddot{R}_{o} \right]$$

Combining the above equations for all n particles of the appendage yields in matrix form

(30) $[m] \{\ddot{q}\} + [K] \{q\} = -[G] \{\dot{q}\} - [B] \{q\} + [R] \{RB\} + \{L\} + [S_2] \{S\}$ 3nx3n 3nx1

where

$$\begin{bmatrix} G \end{bmatrix} = \begin{bmatrix} 2\overline{m}_{1}C_{F}^{T} \widetilde{\omega}_{0}C_{F} & 0 \\ 2\overline{m}_{2}C_{F}^{T}\widetilde{\omega}_{0}C_{F} & 0 \\ 0 & 2\overline{m}_{n}C_{F}^{T}\widetilde{\omega}_{0}C_{F} \end{bmatrix}$$
$$\begin{bmatrix} B \end{bmatrix} = \begin{bmatrix} \overline{m}_{1}C_{F}^{T}(\widetilde{\omega}_{0}\widetilde{\omega}_{0} + \widetilde{\omega}_{0})C_{F} & 0 \\ (3n \times 3n) & 0 & 0 \end{bmatrix}$$
$$\begin{bmatrix} B \end{bmatrix} = \begin{bmatrix} \overline{m}_{0}C_{F}^{T}(\widetilde{\omega}_{0}\widetilde{\omega}_{0} + \widetilde{\omega}_{0})C_{F} & 0 \\ (3n \times 3n) & 0 & 0 \end{bmatrix}$$
$$\{RB\} = \begin{bmatrix} \overline{n}_{0}\\ \widetilde{\omega}_{0} \end{bmatrix}$$
$$(6 \times 1)$$
$$\begin{bmatrix} -\overline{m}_{1}C_{F}^{T} & \overline{m}_{1}C_{F}^{T}(n_{F} + C_{F}r_{1}) \\ -\overline{m}_{n}C_{F}^{T} & \overline{m}_{n}C_{F}^{T}(n_{F} + C_{F}r_{n}) \\ -\overline{m}_{n}C_{F}^{T} & \overline{m}_{n}C_{F}^{T}(n_{F} + C_{F}r_{n}) \\ (3n \times 6) \end{bmatrix}$$

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 $\left[-\widetilde{\mathbf{m}}_{1}\mathbf{C}_{F}^{T}\left[\widetilde{\omega}_{0}\widetilde{\omega}_{0}\left(\mathbf{R}_{0}+\mathbf{h}_{F_{i}}+\mathbf{C}_{F}\mathbf{r}_{1}\right)+\widetilde{\omega}_{0}\mathbf{R}_{0}+2\widetilde{\omega}_{0}\mathbf{R}_{0}\right]\right]$ [L]= $-\widetilde{m}_{n}C_{F}^{T} \left[\widetilde{\omega}_{o}\widetilde{\omega}_{o} \left(R_{o}^{+}h_{F_{i}}^{+}+C_{F}r_{n} \right) + \widetilde{\omega}_{o}R_{o}^{+} + 2\widetilde{\omega}_{o}\dot{R}_{o}^{+} \right]$





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Choosing $Q = \begin{bmatrix} \dot{q} \\ q \end{bmatrix}$, we reformulate equation (30) as follows (31) $[D_F] \{\dot{Q}\} + [E_F] \{Q\} = [R] \{RB\} + [S_2] \{\ddot{S}\} + \{L\}$ where

$$\begin{bmatrix} D_{\mathbf{F}} \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} 0 \\ - \end{bmatrix} & \begin{bmatrix} -\mathbf{M} \\ \mathbf{M} \end{bmatrix} & \begin{bmatrix} \mathbf{G} \\ \mathbf{G} \end{bmatrix} & \mathbf{E}_{\mathbf{F}} \end{bmatrix} = \begin{bmatrix} \begin{bmatrix} \mathbf{M} \\ -\mathbf{M} \\ \mathbf{G} \end{bmatrix} & \begin{bmatrix} 0 \\ \mathbf{K} \end{bmatrix}$$

By the same reasoning as in Section 2.1.

$$(32) \begin{bmatrix} \dot{\bar{z}}^{(1)} \\ \dot{\bar{z}}^{(2)} \end{bmatrix}_{F} + \begin{bmatrix} 0 & -| \wedge | \\ | \wedge | & 2 \xi | \wedge | \\ \bar{z} & | \rangle \end{bmatrix}_{F} \begin{bmatrix} \bar{z}^{(1)} \\ \bar{z}^{(2)} \end{bmatrix}_{F}$$
$$= \begin{bmatrix} V_{F} \end{bmatrix} \begin{bmatrix} R \end{bmatrix} \{ RB \} + \begin{bmatrix} V_{F} \end{bmatrix} \begin{bmatrix} S \end{bmatrix} \{ \dot{S} \} + \begin{bmatrix} V_{F} \end{bmatrix} \{ L \}$$

We can express $\{Q\}$ and $\{\ddot{S}\}$ in terms of the new coordinates \bar{Z}

$$\begin{cases} (33) & \{Q\} = \begin{bmatrix} \dot{q} \\ q \end{bmatrix} = \begin{bmatrix} W_F \end{bmatrix} \begin{bmatrix} \bar{z} \end{bmatrix}_F \\ (34) & \{\bar{s}\} = \begin{bmatrix} W_S \end{bmatrix} \begin{bmatrix} \bar{z} \end{bmatrix}_S$$

4.3.4 INTERACTION FORCES AND TORQUES

4.3.4.1 INTERACTION FORCES OF RIGID APPENDAGE

Using D'Alembert's principle in Figure 14 the interaction force of ith appendage is 2

(35)
$$\vec{F}_{H_i} = -m_{F_i \frac{d}{dt^2}} \left[\vec{a}_i + \vec{r}_i\right]_{I}$$

where

r_i

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 $\vec{r}_i = I^T C_0 C_{F_i} r_i$

 $C_{o}^{T} \overset{\cdot}{a}_{i} = \overset{\cdot}{R}_{i}' + \overset{\cdot}{u}_{S}$

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(36)
$$\mathbf{F}_{\mathrm{H}_{i}} = -\mathbf{m}_{\mathrm{F}_{i}}\mathbf{I}^{\mathrm{T}}\mathbf{C}_{\mathrm{o}}\left[\mathbf{C}_{\mathrm{o}}\overset{\mathrm{T.i.}}{\mathbf{a}_{i}} + \left(\widetilde{\omega}_{\mathrm{o}}\widetilde{\omega}_{\mathrm{o}} + \widetilde{\omega}_{\mathrm{o}}\right)\mathbf{C}_{\mathrm{F}}\mathbf{r}_{\mathrm{F}_{i}}\right]$$

but

where

space station rigid body acceleration at attachment point i.

$$= \left[\widetilde{\omega}_{O}\widetilde{\omega}_{O}\left(R_{O}+h_{F_{i}}\right)+\widetilde{\omega}_{O}\left(R_{O}+h_{F_{i}}\right)+2\widetilde{\omega}_{O}\dot{R}_{O}+\ddot{R}_{O}\right]$$

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space station modal acceleration at point i (measured relative to rigid body space station motion).

*Approximation


Figure 4-14 Interaction Force of Rigid Appendage to S/S

Therefore, the interaction force of a rigid appendage on the space station can be written as

(37)
$$F_{H_i} = \left[F'_{H_i} - m_{F_i}\left(\dot{R}_o - \left(h_{F_i} + C_F r_{F_i}\right) \dot{\omega}_o\right)\right] + F_{A'_i}$$

where

$$F_{H_{i}} = -m_{F_{i}} \left[\widetilde{\omega}_{o} \widetilde{\omega}_{o} \left(R_{o} + h_{F_{i}} + C_{F} r_{F_{i}} \right) + \widetilde{\omega}_{o} R_{o} + 2\widetilde{\omega}_{o} R_{o} \right]$$

$$F_{A'_{i}} = -m_{F_{i}} W_{j_{i}} \dot{z}_{s}$$

4.3.4.2 INTERACTION TORQUES OF RIGID APPENDAGE

(38) $\frac{d}{dt}L_{i} = -\tilde{r}_{i}F_{H_{i}} - T_{H_{i}}$

where

$$\begin{split} \mathbf{L}_{\mathbf{i}} &= (\mathbf{X}_{\mathbf{i}})^{\mathrm{T}}\mathbf{I}_{\mathbf{i}} (\mathbf{X}_{\mathbf{i}}) \left[(\mathbf{X}_{\mathbf{i}})^{\mathrm{T}} \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) \right] \\ &= \left[\left(\mathbf{I}^{\mathrm{T}} \mathbf{C}_{\mathrm{o}} \right) \mathbf{C}_{\mathbf{i}} \mathbf{I}_{\mathbf{i}} \mathbf{C}_{\mathbf{i}}^{\mathrm{T}} \left(\mathbf{C}_{\mathrm{o}}^{\mathrm{T}} \mathbf{I} \right) \right] \left[\left(\mathbf{I}^{\mathrm{T}} \mathbf{C}_{\mathrm{o}} \right) \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) \right] \\ &= \mathbf{I}^{\mathrm{T}} \mathbf{C}_{\mathrm{o}} \mathbf{C}_{\mathbf{i}} \mathbf{I}_{\mathbf{i}} \mathbf{C}_{\mathbf{i}}^{\mathrm{T}} \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) \\ \frac{\mathrm{d} \mathbf{L}_{\mathbf{i}}}{\mathrm{dt}} &= \mathbf{I}^{\mathrm{T}} \left[\mathbf{C}_{\mathrm{o}} \widetilde{\boldsymbol{\omega}}_{\mathrm{o}} \mathbf{C}_{\mathbf{i}} \mathbf{I}_{\mathrm{c}} \mathbf{C}_{\mathbf{i}}^{\mathrm{T}} \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) + \mathbf{C}_{\mathrm{o}} \left(\mathbf{C}_{\mathbf{i}} \mathbf{I}_{\mathrm{i}} \mathbf{C}_{\mathbf{i}}^{\mathrm{T}} \right) \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) \right] \\ &= \mathbf{X}^{\mathrm{T}} \left[\widetilde{\boldsymbol{\omega}}_{\mathrm{o}} \mathbf{C}_{\mathbf{i}} \mathbf{I}_{\mathrm{c}} \mathbf{C}_{\mathrm{i}}^{\mathrm{T}} \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) + \mathbf{C}_{\mathrm{i}} \mathbf{I}_{\mathrm{c}} \mathbf{C}_{\mathrm{i}}^{\mathrm{T}} \left(\boldsymbol{\omega}_{\mathrm{o}} + \boldsymbol{\omega}_{\mathrm{b}_{\mathbf{i}}} \right) \right] \end{split}$$

where

 $I_i = inertia matrix of i^{th} appendage$

 $\dot{\mathbf{w}}_{b_{i}} \equiv \text{modal angular acceleration at attachment point of i}^{\text{th}} \text{ appendage}$ $\dot{\mathbf{w}}_{b_{i}} = \begin{bmatrix} \mathbf{W}_{S_{b_{i}}} \end{bmatrix} \dot{\mathbf{z}}_{S}^{*}$ $(3 \times N_{i})$

Therefore, the interaction torque of ith appendage of rigid motion on space station is

(39)
$$T_{H_{i}} = \left(\widetilde{C}_{F_{i}r_{F_{i}}} \right)^{F_{H_{i}}} - C_{i}I_{i}C_{i}^{T}W_{S_{b_{i}}}\dot{Z}_{S} - C_{i}I_{i}\mathfrak{C}_{i}^{T}\dot{\omega}_{O} - \left(\widetilde{\omega}_{O}C_{i}I_{i}C_{i}^{T} \right) \left(\omega_{O} + W_{S_{b_{i}}}Z_{S} \right)$$

*Approximation

$$T_{H_{i}} = -\left(\widetilde{C_{F_{i}}}^{T} F_{i} \right) \widetilde{F}_{H_{i}} - (E + \omega_{o}) (C_{i} I_{i} C_{i}^{T}) W_{S_{b_{i}}} \dot{z}_{S}$$
$$- \left(C_{i} I_{i} C_{i}^{T} \right) \dot{\omega}_{o} - \widetilde{\omega}_{o} \left(C_{i} I_{i} C_{i}^{T} \right) \omega_{o}$$

where

or

E is the identity matrix.

4.3.4.3 INTERACTION FORCES AND TORQUES OF FLEXIBLE APPENDAGE

(40)
$$F_{A_i} = -C_{F_i} \Sigma_E^T M_{F_i} W_{F_i} Z_{F_i}$$

See Section 4.3.7 for computational considerations

(41)
$$T_{A_i} = -C_{F_i} \Sigma_E^T \widetilde{R}_{F_i} M_{F_i} W_{F_i} \dot{Z}_{F_i}$$

4.3.4.4 TOTAL INTERACTION FORCES AND TORQUES

The total interaction forces and torques at the attachment point of the appendages can be obtained by summing the interaction forces (torques) of the rigid and the flexible appendages at the attachment point.

(42)
$$\begin{array}{ccc} \mathbf{F}_{t_{i}} &=& \mathbf{F}_{H_{i}} + \mathbf{F}_{A_{i}} \\ (43) & \mathbf{F}_{t_{i}} &=& -\left[\mathbf{F}_{H_{i}} + \mathbf{m}_{F_{i}} \left(\mathbf{R}_{o} - \left(\mathbf{h}_{F_{i}} + \mathbf{C}_{F} \mathbf{r}_{F_{i}} \right) \dot{\omega}_{o} \right) + \mathbf{m}_{F_{i}} \mathbf{W}_{S_{i}} \dot{z}_{S} \right] \\ & & -\mathbf{C}_{F_{i}} \boldsymbol{\Sigma}_{E}^{T} \mathbf{M}_{F_{i}} \mathbf{W}_{F_{i}} \dot{z}_{F_{i}} \end{array}$$

T_ti $T_{H_i} + T_{A_i}$ (44) $-\left[\left(\widetilde{C_{F_{i}}}^{r}_{F_{i}}\right)_{F_{H_{i}}} + \left(E + \widetilde{\omega}_{o}\right)\left(C_{i} I_{i} C_{i}^{T}\right) w_{S_{b_{i}}}^{\dagger} \widetilde{Z}_{S}\right]$ 2 $+ \left(C_{i} I_{i} C_{i}^{T} \right) \dot{\omega}_{o} + \widetilde{\omega}_{o} \left(C_{i} I_{i} C_{i}^{T} \omega_{o} \right) \right]$ $- \mathbf{C}_{\mathbf{F}_{i}} \mathbf{\tilde{\Sigma}}_{\mathbf{E}}^{\mathrm{T}} \mathbf{\tilde{\tilde{R}}}_{\mathbf{F}_{i}}^{\mathrm{M}} \mathbf{W}_{\mathbf{F}_{i}}^{\mathrm{W}} \mathbf{W}_{\mathbf{F}_{i}}^{\mathrm{T}} \mathbf{z}_{\mathbf{F}_{i}}^{\mathrm{T}}$

4.3.5 TOTAL SYSTEM EQUATION

The above derived equations of motion of spinning space station with the attached appendages can be written in matrix notation as

(45)
$$[M] \{ \ddot{x} \} + [C] \{ \dot{x} \} + [K] \{ x \} = \{ P \}$$

where

$$M = \begin{cases} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \\ \end{bmatrix} \leftarrow \text{Rigid Body} \\ \leftarrow \text{Space Station} \\ \leftarrow \text{Appendages} \\ C = \begin{cases} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \\ \end{bmatrix} \\ K = \begin{cases} K_{11} & K_{12} & K_{13} \\ K_{21} & K_{22} & K_{23} \\ K_{31} & K_{32} & K_{33} \\ \end{bmatrix} \\ K = \begin{cases} K_{11} & K_{12} & K_{13} \\ K_{21} & K_{22} & K_{23} \\ K_{31} & K_{32} & K_{33} \\ \end{bmatrix} \\ K = \begin{cases} K_{0} \\ K_{$$

For the previously derived state equations, we find that M = O.

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Thus, the rigid body equations (25) lead to the first equation of the total system, which is

(46)
$$\begin{bmatrix} C_{11} \\ \dot{\omega}_{o} \end{bmatrix} + \begin{bmatrix} C_{12} \\ \dot{\omega}_{o} \end{bmatrix} \dot{z}_{S} + \begin{bmatrix} C_{13} \\ \dot{z}_{F} \end{bmatrix} \dot{z}_{F} = \{P_{1}\}$$

(6x6) (6x1) (6x2N_S) (6x2N_F) (6x1)

where

$$\begin{cases} C_{11} &= \left(\begin{array}{c} M_{T} & -M_{T}C \\ \hline 0 & -- & T_{T} \end{array} \right) \\ & \left[C_{12} \right] &= \left(\begin{array}{c} A_{2} & 0 \\ -\Sigma_{i=1} & 0 \\ \hline -M_{F_{i}}(C_{F_{i}}\tilde{r}_{F_{i}}) & -C_{i}I_{i}C_{i} \end{array} \right) \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S_{b_{i}}} \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}(\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}(\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}(\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}(\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}(\begin{array}{c} W_{S}T \end{array} \right] \\ & \left[\begin{array}[\begin{array}{c} W_{S}T \\ -W_{S}T \end{array} \right] \\ & \left[\begin{array}[\begin{array}{c} W_{S}T \end{array} \right]$$

(6x2 N_F)

$$\mathbf{P}_{1} = \left[\frac{\mathbf{F}_{R1} + \mathbf{F}_{R2} - \mathbf{M}_{T} \left[\left(\widetilde{\widetilde{\omega}}_{o} + \widetilde{\omega}_{o} \widetilde{\omega}_{o} \right) \mathbf{R}_{o} + \widetilde{\omega}_{o} \widetilde{\omega}_{o} \mathbf{C} + 2 \widetilde{\omega}_{o} \widetilde{\mathbf{R}}_{o} \right]}{\mathbf{T}_{R1} + \mathbf{T}_{R2} - \widetilde{\mathbf{I}}_{R1} \mathbf{F}_{R1} - \widetilde{\mathbf{I}}_{R2} \mathbf{F}_{R2} - \widetilde{\omega}_{o} \mathbf{I}_{T} \omega_{o}} \right]$$

 $\begin{bmatrix} K_{11} \end{bmatrix} = \begin{bmatrix} K_{12} \end{bmatrix} = \begin{bmatrix} K_{13} \end{bmatrix} = 0$

The flexible spinning space station equation (11) leads to the second equation of the total system which is

$$(47) \qquad [C_{21}] \begin{pmatrix} R \\ 0 \\ \omega_0 \end{pmatrix} + [C_{22}] \{ z_S \} + [C_{23}] \{ z_F \} + [K_{22}] \{ z_S \}^{=} \{ P_2 \}$$

where

$$\begin{bmatrix} C_{21} \end{bmatrix} = -\frac{4}{\sum_{i=1}^{4} \begin{bmatrix} V_{F} \end{bmatrix}} \begin{bmatrix} -m_{F_{i}} & M_{F_{i}} & M_{F_{i}} \end{bmatrix} \begin{bmatrix} M_{F_{i}} & M_{F_{i}} & M_{F_{i}} \end{bmatrix}$$

$$= -\frac{2}{\sum_{i=1}^{4} \left[V_{Fi}' | V_{Fi}' \right]} \begin{bmatrix} -m_{Fi}' | m_{Fi}' | m_{Fi}$$

(6 x 6)

$$\begin{bmatrix} 22 \end{bmatrix} = -\frac{4}{2} \begin{bmatrix} v'_{Fi} & v''_{Fi} \end{bmatrix} \begin{bmatrix} -m_{Fi} & 0 & 0 \\ -m_{Fi} & -m_$$

Forces and torques acting on space station and exciting flexible motion include:

- 1. 2 external forces
 - 2. 2 external torques
 - up to 4 hinge forces and torques due to 4 attached rigid appendages
 - 4. up to 4 forces and torques due to flexible motion of 4 fixed appendages
 - 5. wobble damper control torque

$$\begin{bmatrix} P_2 \end{bmatrix} = \sum_{i=1}^{4} V'_{Fi} \begin{bmatrix} m_{Fi} (2\omega_0 \dot{R}_0 + \tilde{\omega}_0 \tilde{\omega}_0 (R_0 + h_{Fi} + C_{Fi} r_{Fi}) + \dot{\omega}_0 R_0 \end{bmatrix}$$

$$+ \frac{4}{\Sigma} V_{Fi}'' \left\{ C_{Fi} (C_{Fi}^{T} \omega_{o}) I_{Fi} C_{Fi}^{T} \omega_{o} + (C_{Fi} r_{Fi})(m_{Fi}) \left[2 \omega_{o} R_{o} + \frac{1}{\omega_{o}} \alpha_{o} (R_{o} + h_{Fi} + C_{Fi} r_{Fi}) \right] \right\}$$

$$+ \sum_{i=1}^{2} V_{Ri}^{'} F_{Ri} + \sum_{i=1}^{2} V_{Ri}^{''} T_{Ri} + V_{WOB}^{''} WOB$$

$$\begin{bmatrix} \mathbf{K}_{22} \end{bmatrix} = \begin{bmatrix} \mathbf{0} & |-|\bar{\mathbf{A}}| \\ |\bar{\mathbf{A}}| & |2\xi_{S}|\bar{\mathbf{A}}| \end{bmatrix}$$

$\begin{bmatrix} K_{21} \end{bmatrix} = \begin{bmatrix} K_{23} \end{bmatrix} = 0$

The flexible appendage equations (22) lead to the third equation of the total system, which is

$$\begin{bmatrix} (48) \\ \begin{bmatrix} C_{31} \end{bmatrix} \begin{pmatrix} \mathbf{R} \\ \mathbf{\omega} \\ \mathbf{\omega} \\ \mathbf{0} \end{pmatrix} + \begin{bmatrix} C_{32} \end{bmatrix} \begin{pmatrix} \mathbf{Z} \\ \mathbf{Z} \\ \mathbf{S} \end{pmatrix} + \begin{bmatrix} C_{33} \end{bmatrix} \begin{pmatrix} \mathbf{Z} \\ \mathbf{F} \end{pmatrix}^{0} + \begin{bmatrix} K_{33} \end{bmatrix} \begin{pmatrix} \mathbf{Z} \\ \mathbf{F} \end{pmatrix}^{1} = \begin{pmatrix} \mathbf{P}_{3} \end{pmatrix}$$

where

here

$$\begin{bmatrix} M_{31} \end{bmatrix} = \begin{bmatrix} V_{F1}^{''} R_{F1} \\ V_{F2}^{R} R_{F2} \\ V_{F3}^{R} R_{F3} \\ V_{F4}^{R} R_{F4} \end{bmatrix} - M_{32} = \begin{bmatrix} V_{F1}^{''} S_{1} \\ V_{F1}^{S} S_{1} \\ V_{F2}^{S} S_{2} \\ V_{F3}^{S} S_{3} \\ V_{F4}^{S} S_{4} \end{bmatrix}$$

$$\begin{bmatrix} K_{33} \end{bmatrix} = \begin{bmatrix} 0 & -|\bar{A}_{\rm F}] \\ |\bar{A}_{\rm F} & 2\xi_{\rm F}|\bar{A}_{\rm F} \end{bmatrix}$$

(for each appendage)

$$\begin{bmatrix} K_{31} \end{bmatrix} = \begin{bmatrix} K_{32} \end{bmatrix} = 0$$

$$P_3 = \begin{bmatrix} V_{F1}^{''} L_1 \\ \vdots \\ \vdots \\ V_{F4} L_4 \end{bmatrix}$$

In order to evaluate the coefficient matrices in equation (48) the transformation matrix $\begin{bmatrix} V_F \end{bmatrix}$ derived in Section 4.3.6 may be used.

For computational speed and storage considerations, the elements of $\begin{bmatrix} C_{31} \end{bmatrix}$ may be obtained as follows:

Define:

 $d_{RE} = \sum_{E}^{T} [m] R_{E} (\Phi_{B})$ $d_{Im} = \sum_{E}^{T} [m] I_{m} (\Phi_{B})$ $thus, d_{RE}^{T} = R_{E} (\Phi_{B}^{T}) [m] \sum_{E}$ $d_{Im}^{T} = I_{m} (\Phi_{B}^{T}) [m] \sum_{E}$

Also define:

 $r_{RE} = \sum_{E}^{T} \tilde{r} [m] R_{E} (\Phi_{B})$ $r_{Im} = \sum_{E}^{T} \tilde{r} [m] I_{m} (\Phi_{B})$

then

$$\mathbf{r}_{\mathrm{RE}}^{\mathrm{T}} = -\mathbf{R}_{\mathrm{E}}(\mathbf{\Phi}_{\mathrm{B}}^{\mathrm{T}}) [m] \widetilde{\mathbf{r}} \sum_{\mathrm{E}}$$
$$\mathbf{r}_{\mathrm{Im}}^{\mathrm{T}} = -\mathbf{I}_{\mathrm{m}}(\mathbf{\Phi}_{\mathrm{B}}^{\mathrm{T}}) [m] \widetilde{\mathbf{r}} \sum_{\mathrm{E}}$$

In terms of the above definitions equation (49) can be written as

$$(50) \quad \left[V_{F} \right] \left\{ \begin{matrix} 0 \\ R \end{matrix} \right\} = \left[\begin{matrix} d'd_{I}^{T} C_{F}^{T} & d'd_{I}^{T} C_{F}^{T} & h_{F} + d'r_{I}^{T} C_{F}^{T} \\ - & m \end{matrix} \right] - \left[\begin{matrix} d'd_{I}^{T} C_{F}^{T} & h_{F} + d'r_{I}^{T} C_{F}^{T} \\ - & d'd_{R_{E}}^{T} C_{F}^{T} & h_{F} + d'r_{R_{E}}^{T} C_{F}^{T} \end{matrix} \right]$$

Similarly, we have the elements of the matrix $\begin{bmatrix} M_{32} \end{bmatrix}$ as

(51)
$$\begin{bmatrix} V_F \end{bmatrix} \begin{cases} 0 \\ S \end{cases} = \begin{bmatrix} V''_F \end{bmatrix} \begin{bmatrix} S \end{bmatrix} = \begin{bmatrix} V''_F \end{bmatrix} \begin{bmatrix} -m_1 C_F^T & | & 0 \\ -m_1 C_F^T & | & 0 \\ -m_1 C_F^T & | & 0 \end{bmatrix} \begin{bmatrix} W_{si} \\ -m_1 C_F^T & | & 0 \end{bmatrix} \begin{bmatrix} W_{si} \\ W_{sbi} \end{bmatrix}$$

(3n x 6) (b x N_s)

$$= - \left[\mathbf{V}_{\mathbf{F}}^{"} \right] \left[\mathbf{m} \right] \sum_{\mathbf{E}} \mathbf{C}_{\mathbf{F}}^{\mathbf{T}} \mathbf{W}_{\mathbf{s}\mathbf{i}}$$
$$(2\mathbf{N}_{\mathbf{F}} \times 3 \mathbf{n}) \quad (3\mathbf{n} \times \mathbf{N}_{\mathbf{s}})$$

Finally, we can write equation (51) as

(52)

$$-\left[V_{F}^{''}\right][S] \quad \left[\begin{matrix} d_{Im}^{'} & (\Phi_{B}^{T}) \\ \vdots & \vdots \\ d_{R_{E}}^{'} & (\Phi_{B}^{T}) \end{matrix}\right] [m] \Sigma_{E} C_{F}^{T} W_{si}$$

$$(2N_{F} \times 3n) \qquad (3n \times N_{s})$$

$$= \begin{bmatrix} d'd_{I_{m}}^{T} C_{F}^{T} W_{si} \\ -d'd_{R_{E}}^{T} C_{F}^{T} W_{si} \end{bmatrix}$$

$$(2N_{F} \times N_{s})$$

The matrix $[P_3]$ is equation (48) can similarly be evaluated as (53) $[V_F] \begin{cases} 0 \\ L \end{cases} = [V_F''][L]$ $= \begin{bmatrix} v_F'' \end{bmatrix} \begin{bmatrix} -m_1 C_F^T \begin{bmatrix} \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ (R_0 + h_{Fi} + C_F r_1) + \widetilde{\omega}_0 R_0 + 2 \widetilde{\omega}_0 \dot{R}_0 \end{bmatrix}$ $= \begin{bmatrix} u_F'' \end{bmatrix} \begin{bmatrix} -m_1 C_F^T \begin{bmatrix} \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ (R_0 + h_{Fi} + C_F r_n) + \widetilde{\omega}_0 R_0 + 2 \widetilde{\omega}_0 \dot{R}_0 \end{bmatrix}$ $= \begin{bmatrix} d' d_{IM} C_F T \begin{bmatrix} \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ (R_0 + h_{Fi}) + \dot{\widetilde{\omega}}_0 R_0 + 2 \ \widetilde{\omega}_0 \dot{R}_0 \end{bmatrix}$ $= \begin{bmatrix} d' d_{IM} C_F T \begin{bmatrix} \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ (R_0 + h_{Fi}) + \dot{\widetilde{\omega}}_0 R_0 + 2 \ \widetilde{\omega}_0 \dot{R}_0 \end{bmatrix}$ $-V_F'' [m] DIAG (C_F^T \ \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ C_F^{-1}, \dots, C_F^{-1} \widetilde{\omega}_0 \ \widetilde{\omega}_0 \ C_F^{-1}, \end{pmatrix}$ 4.3.6 Transformation Matrix [V]

By Definition

(54)
$$\mathbf{V} = \frac{1/2}{\left[-\frac{\mathbf{I}}{\mathbf{J}} + \frac{\mathbf{I}}{\mathbf{J}}\right]} \left[\mathbf{\Phi}^{*} \mathbf{D} \mathbf{\Phi} \right]^{-1} \mathbf{\Phi}^{*}$$

where D is askew symmetric matrix defined in equation (3)

(55)
$$D \equiv \begin{bmatrix} -\begin{bmatrix} 0 \\ -\end{bmatrix} & -\begin{bmatrix} m \\ -\end{bmatrix} & \begin{bmatrix} m \\ &$$

where

 $\overline{\lambda}$

$$\Phi_{\mathrm{T}} = \Phi_{\mathrm{B}} \overline{\lambda} \qquad \Phi_{\mathrm{B}} = \left[\left\{ \phi^{(1)} \right\} \left\{ \phi^{(2)} \right\} \cdots \left\{ \phi^{(N)} \right\} \right]$$

$$\Phi_{\mathrm{B}}^{*} = \left[\left\{ \phi^{(1)} \right\} \left\{ \phi^{(2)} \right\} \cdots \left\{ \phi^{(N)} \right\} \right]$$

$$\left\{ \phi^{*} \right\} \text{ is complex conjugate of } \left\{ \phi \right\}$$

Using the above defined matrices, we may formulate the following equation

$$(57) \quad \Phi^{*T} D \Phi = \begin{bmatrix} *^{T} & *^{T} \\ \Phi_{T} & | & \Phi_{B} \\ -\frac{T}{\Phi_{T}} & | & \Phi_{B} \\ -\frac{T}{\Phi_{B}} & | & \Phi_{B} \\ -\frac{T}{\Phi_{B}} & | & \Phi_{B} \\ -\frac{T}{\Phi_{B}} & | & \Phi_{T} \\ -\frac{T}{\Phi_{T}} &$$

 $= \begin{array}{c} \Phi_{B}^{*}{}^{T}[m]\Phi_{T}^{-} \Phi_{T}^{*}{}^{T}[m]\Phi_{B}^{+}\Phi_{B}^{*}[G]\Phi_{B}^{-} & \Phi_{B}^{*}{}^{T}[m]\Phi_{T}^{*} - \Phi_{T}^{*}[m]\Phi_{B}^{*} + \Phi_{B}^{*}[G]\Phi_{B}^{*} \\ \Phi_{B}^{T}[m]\Phi_{T}^{-} \Phi_{T}^{T}[m]\Phi_{B}^{+} + \Phi_{B}^{T}[G]\Phi_{B}^{-} & \Phi_{B}^{T}[m]\Phi_{T}^{*} - \Phi_{T}^{T}[m]\Phi_{B}^{*} + \Phi_{B}^{T}[G]\Phi_{B}^{*} \end{array}$

(Note that the cross terms are the complex conjugate of each other)

In order to evaluate the matrices in equation (57) we introduce the following method.

(58.) Let
$$\Psi = (1/2)\Phi\left[-\frac{I}{I} - \frac{I}{J} - \frac{J}{J}\right]$$

$$= (1/2)\left[\frac{\Phi_{T}}{\Phi_{B}} + \frac{\Phi_{T}}{\Phi_{B}}\right]\left[\frac{I}{I} - \frac{I}{J} - \frac{J}{J}\right] = (1/2\left[\frac{\Phi_{T}}{\Phi_{B}} + \frac{\Phi_{T}}{\Phi_{B}} + \frac{J(\Phi_{T}}{\Phi_{B}} - \frac{\Phi_{T}}{\Phi_{B}}\right]\right]$$

$$= \left[\frac{R_{E}}{R_{E}} + \frac{(\Phi_{T})}{\Phi_{B}} + \frac{I}{M} + \frac{(\Phi_{T})}{I} + \frac{I}{M} + \frac{(\Phi_{T})}{\Phi_{B}}\right]$$

The transpose of Ψ may be written as

$$(59) \quad \psi^{\mathrm{T}} = 1/2 \begin{bmatrix} I & I & I \\ -J & I & J \end{bmatrix} \Phi^{\mathrm{T}}$$
$$= 1/2 \begin{bmatrix} I & J & I \\ -J & I & J \end{bmatrix} \begin{bmatrix} \Phi^{\mathrm{T}} & \Phi^{\mathrm{T}} \\ \Phi^{\mathrm{T}} & \Phi^{\mathrm{T}} \\ \Phi^{\mathrm{T}} & \Phi^{\mathrm{T}} \\ \Phi^{\mathrm{T}} & \Phi^{\mathrm{T}} \end{bmatrix}$$

and the conjugate transpose of ψ as (60) $\psi^{*T} = (1/2) \begin{bmatrix} -\frac{I}{J} & \frac{I}{J} & \frac{I}{J} \\ -\frac{J}{J} & -\frac{J}{J} \end{bmatrix} \begin{bmatrix} \Phi^{*T} & \Phi^{*T} \\ -\frac{T}{\Phi} & \Phi^{T} \\ -\frac{T}{\Phi} & -\frac{T}{\Phi} & -\frac{T}{\Phi} \end{bmatrix}$ $= (1/2) \begin{bmatrix} \Phi^{*T} + \Phi^{T} & \Phi^{*T} + \Phi^{T} \\ -\frac{T}{J} & \Phi^{*T} + \Phi^{T} \\ -\frac{T}{J} & -\frac{T}{\Phi} & -\frac{T}{T} \end{bmatrix}$ $= \begin{bmatrix} R_{E} (\Phi_{T}^{T}) & R_{E} (\Phi_{B}^{T}) \\ -\frac{T}{I} & -\frac{T}{I} & -\frac{T}{I} & -\frac{T}{I} \end{bmatrix}$ Defining Φ in terms of ψ

(61;)

$$\Phi = \Psi \begin{bmatrix} I & I \\ J & I & J \end{bmatrix} (1/2)$$
$$= \begin{bmatrix} R_{E} (\Phi_{T}) & I & (\Phi_{T}) \\ R_{E} (\Phi_{B}) & I & (\Phi_{B}) \end{bmatrix} \begin{bmatrix} I & I \\ J & J \end{bmatrix}$$

and the conjugate transpose of Φ as

$$(62) \Phi^{*T} = \begin{bmatrix} \underline{I} & \underline{J} \\ \overline{I} & \overline{J} \end{bmatrix} \begin{bmatrix} \underline{R}_{E} (\Phi_{T}^{T}) & \underline{R}_{E} (\Phi_{B}^{T}) \\ \overline{I}_{m} (\Phi_{T}^{T}) & \overline{I}_{m} (\Phi_{B}^{T}) \end{bmatrix}$$

Combining equation (2), (3), and (8), we can formulate equation (63)

Substituting the following relations in equation (62)

 $\Phi_{T} = \Phi_{B} \overline{\lambda} = \phi_{B} \lambda (-j)$

and $R_E(\Phi_T) = {}^{+}I_m(\Phi_B) \lambda_{A} R_E(\Phi_T^T) = {}^{+}\lambda I_m(\Phi_B^T)$ $I_m(\Phi_T) = {}^{-}R_E(\Phi_B) \lambda_{A} I_m(\Phi_T^T) = {}^{-}\lambda R_E(\Phi_B^T)$

we obtain

$$(64) \quad \Phi^{*T} D \Phi = \begin{bmatrix} I & J \\ -J \\ I & J \end{bmatrix} \begin{bmatrix} a & c \\ b & d \end{bmatrix} \begin{bmatrix} I & J \\ J & -J \end{bmatrix}$$

where

$$a = -\lambda I_{m}(\Phi_{B}^{T}) [m] R_{E}(\Phi_{B}) + R_{R}(\Phi_{B}^{T}) (+ [m] I_{m}(\Phi_{B}) \lambda + [G] R_{E}(\Phi_{B}))$$

$$b = +\lambda R_{E}(\Phi_{B}^{T}) [m] R_{E}(\Phi_{B}) + I_{m}(\Phi_{B}^{T}) (+ [m] I_{m}(\Phi_{B}) \lambda + [G] R_{E}(\Phi_{B}))$$

$$c = -\lambda I_{m}(\Phi_{B}^{T}) [m] I_{m}(\Phi_{B}) + R_{E}(\Phi_{B}^{T}) (m] R_{E}(\Phi_{B}) \lambda + [G] I_{m}(\Phi_{B}))$$

$$d = +\lambda R_{E}(\Phi_{B}^{T}) [m] I_{m}(\Phi_{B}) + I_{m}(\Phi_{B}^{T}) (m] R_{E}(\Phi_{B}) \lambda + [G] I_{m}(\Phi_{B}))$$

Let

$$(65) \Phi^{*}^{T} D \Phi = \begin{bmatrix} e & g \\ f & h \end{bmatrix}$$

where

(66,)	е	=	(a+d) - (b+c)J
	f	=	(a-d) + (b+c)J
	g	2	(a-d) - (b+c)J
	h	2.	(a+d) + (b-c)J

From the orthogonality relation of eigenvectors $\Phi^{*}D\Phi$ should be diagonal matrix,⁽³⁾ hence,

f = g = 0, e and h are diagonal matrices.

Applying the above conditions in equation (66) , we have the following set of equations

$$(67) \begin{cases} e = 2 (a-bj) \\ h = 2 (a+bj) \\ c = -b \\ and a = d \end{cases}$$

Then equation (64) becomes

$$(68) \Phi^* D \Phi = 2 \begin{bmatrix} a - b & 0 \\ 0 & a + b \end{bmatrix}$$

It can be shown that the diagonal terms of equation (57) are purely imaginary; 4 therefore, a in equation (68) must vanish, and hence

$$(69) \quad \Phi^*^{\mathrm{T}} \mathrm{D} \Phi = \begin{bmatrix} -2\mathrm{bj} & 0\\ 0 & -\overline{0} & -\overline{2}\mathrm{bj} \end{bmatrix}$$

where

$$2^{bj} = 2^{j} \left[\lambda_{B_{E}}(\Phi_{B}^{T}) [m] R_{E}(\Phi_{B}) + I_{M}(\Phi_{B}^{T}) (+[m] I_{m}(\Phi_{B}) + [G] R_{E}(\Phi_{B})) \right]$$
$$= \Phi_{B}^{*T} [m] \Phi_{T}^{-} \Phi_{T}^{*T} [m] \Phi_{B}^{-} + \Phi_{B}^{*T} [G] \Phi_{B}$$

Substituting equation (69) in equation (54), we obtain

$$V = \frac{1/2 \left[\frac{I}{J} \cdot \frac{I}{J} - \frac{I}{J} \right] \left[\frac{2 \text{bj}}{0} \cdot \frac{0}{1 + 2 \text{bj}} \right]^{-1} \Phi^{*T}}{\left[\frac{1}{J} \cdot \frac{I}{J} - \frac{I}{J} \right] \left[\frac{2 \text{bj}}{0} \cdot \frac{1}{1 + 2 \text{bj}} \right]^{-1} \Phi^{*T}}$$

$$= \frac{1/2 \left[\frac{I}{J} \cdot \frac{I}{J} - \frac{I}{J} \right] \left[\frac{d'j}{0} \cdot \frac{0}{1 - d'j} \right] \Phi^{*T}}{\left[\frac{d'j}{0} \cdot \frac{1}{1 - d'j} \right] \Phi^{*T}}$$

 $\frac{1}{2} \begin{bmatrix} 0 & d' \\ -d' & 0 \end{bmatrix} \begin{bmatrix} I & -I \\ J & -J \end{bmatrix} \Phi^{*T}$ = $= 1/2 \begin{bmatrix} -\mathbf{0} & \mathbf{i} & \mathbf{a}' \\ -\mathbf{d}' & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{I} & \mathbf{i} & \mathbf{I} \\ \mathbf{J} & \mathbf{i} & \mathbf{J} \end{bmatrix} \begin{bmatrix} \mathbf{\Phi}_{\mathrm{T}}^{*\mathrm{T}} & \mathbf{\Phi}_{\mathrm{B}}^{*\mathrm{T}} \\ \mathbf{\Phi}_{\mathrm{T}}^{\mathrm{T}} & \mathbf{\Phi}_{\mathrm{B}}^{*\mathrm{T}} \end{bmatrix}$ $\begin{bmatrix} 0 & | & d' \\ -d' & 0 \end{bmatrix} \begin{bmatrix} R_{E}(\Phi_{T}^{T}) & R_{E}(\Phi_{B}^{T}) \\ I_{m}(\Phi_{T}^{T}) & I_{m}(\Phi_{B}^{T}) \end{bmatrix}$ =

where

 $\begin{bmatrix} -\frac{2\mathbf{b}\mathbf{j}}{\mathbf{0}} & \mathbf{0} \\ -\frac{2\mathbf{b}\mathbf{j}}{\mathbf{0}} & 2\mathbf{b}\mathbf{j} \end{bmatrix}^{-1} = \begin{bmatrix} \mathbf{d}'\mathbf{j} & \mathbf{0} \\ \mathbf{0} & -\mathbf{d}\mathbf{j} \end{bmatrix}$ is used.

$$\begin{split} \mathbf{F}_{\mathbf{A}_{\mathbf{i}}} &= \sum_{\mathbf{E}}^{\mathbf{T}} \mathbf{M}_{\mathbf{F}_{\mathbf{i}}} \mathbf{W}_{\mathbf{F}_{\mathbf{i}}} \dot{\mathbf{z}}_{\mathbf{F}_{\mathbf{i}}} \\ &= [\mathbf{E}\mathbf{E}....\mathbf{E}] \left[\frac{\mathbf{m} \mid \mathbf{o}}{\mathbf{o} \mid \mathbf{o}} \right] \left[\frac{\boldsymbol{\Phi}_{\mathbf{T}} \mid \boldsymbol{\Phi}_{\mathbf{T}}^{*}}{\boldsymbol{\Phi}_{\mathbf{B}} \mid \boldsymbol{\Phi}_{\mathbf{B}}} \right] \left[\frac{\mathbf{I} \mid -\mathbf{J}}{\mathbf{I} \mid \mathbf{J}} \right] \dot{\mathbf{z}}_{\mathbf{F}_{\mathbf{i}}} \\ &= [\mathbf{E}....\mathbf{E}] \left[\frac{\mathbf{m} \mid \mathbf{o}}{\mathbf{o} \mid \mathbf{o}} \right] \left[\frac{2\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{T}}) \mid 2\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{T}})}{2\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{B}}) \mid 2\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{B}})} \right] \dot{\mathbf{z}}_{\mathbf{F}_{\mathbf{i}}} \\ &= [\mathbf{E}....\mathbf{E}] \left[\frac{2\mathbf{m}\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{T}}) \mid 2\mathbf{m}\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{T}})}{\mathbf{O}} \right] \dot{\mathbf{z}}_{\mathbf{F}_{\mathbf{i}}} \\ &= \left[\mathbf{E}....\mathbf{E} \right] \left[\frac{2\mathbf{m}\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{T}}) \mid 2\mathbf{m}\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{T}})}{\mathbf{O}} \right] \dot{\mathbf{z}}_{\mathbf{F}_{\mathbf{i}}} \\ &= \left[\sum_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{B}j\mathbf{x}}) \dots \right]_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{B}j\mathbf{x}}) \dots \\ &= \sum_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{B}j\mathbf{x}}) \dots \right]_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{I}_{\mathbf{m}}(\boldsymbol{\Phi}_{\mathbf{B}j\mathbf{x}}) \dots \\ &= \sum_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{R}_{\mathbf{E}}(\boldsymbol{\Phi}_{\mathbf{B}j\mathbf{x}}) \dots \\ &= \sum_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{R}_{\mathbf{E}}(\mathbf{M}_{\mathbf{B}j\mathbf{x}}) \dots \\ &= \sum_{j=1}^{n} 2\mathbf{m}_{j}\mathbf{R}_{\mathbf{E}}(\mathbf{M}_{\mathbf{B}j\mathbf{x}})$$

(3 x 2N)

Likewise -

 $T_{A_{i}} = \sum_{E}^{T} \widetilde{\widetilde{R}}_{F_{i}} M_{F_{i}} W_{F_{i}} \dot{z}_{F_{i}}$ $= [E....E] \left[\frac{\widetilde{\widetilde{R}}_{F_{i}} | O}{O | O} \right] \left[\frac{m | O}{O | O} \right] \left[\frac{\Phi_{T} | \Phi_{T}^{*}}{\Phi_{B} | \Phi_{B}^{*}} \right] \left[\frac{1 | -J}{1 | J} \right] \dot{z}_{F_{i}}$ $= [E...E] \left[\frac{2\widetilde{\widetilde{R}}_{F_{i}} mR_{E}(\Phi_{T}) | 2\widetilde{\widetilde{R}}_{F_{i}} mI_{m}(\Phi_{T})}{O | O} \right] \vec{z}_{F_{i}}$ $= 2 \begin{bmatrix} \widetilde{m}_{1} \widetilde{F}_{1} \\ O \\ \vdots \\ \vdots \\ O \end{bmatrix} \begin{bmatrix} R_{E}(\Phi_{T}) | I_{m}(\Phi_{T}) \\ \vdots \\ I_{m}(\Phi_{T}) \end{bmatrix} \dot{z}_{F_{i}}$

4.4 REFERENCES

- Ref. 4.1 "Dynamics and Control of Flexible Space Vehicles", P. W. Likens, NASA CR 105592.
- Ref. 4.2 "Small Eccentricities or Inclinations in the Brouwer Theory of the Artificial Satellite", R. H. Lyddane, Astronomical Journal, Volume 68, No. 8, October 1963, P. 555.
- Ref. 4.3 Space Station Study (Phase B), Selected Control Moment Gyro Configuration Report 505, General Electric Company Avionic Controls Department, Binghamton, New York.
- Ref. 4.4 Space Station Study (Phase B), Control Moment Gyro Assembly Candidate CMG Assemblies Report 504, General Electric Company Avionic Controls Department, Binghamton, New York.
- Ref. 4.5 Space Station Study (Phase B), Control Moment Gyro Assembly
 Report EL 506-D, "Preliminary Synthesis and Simulation of
 Selected CMG Attitude Control System," General Electric Co.
 Avionic Controls Department, Binghamton, New York.
- Ref. 4.6 Likens, P. W., "Modal Method for Analysis of Free Rotations of Spacecraft," AIAA Journal, Vol. 5, #7, July 1967.
- Ref. 4.7 MacNeal, R. H., "The NASTRAN Theoretical Manual," SP-221, pg. 11.3-1 to 11.3-13, Office of Technology Utilization, NASA, Washington, D. C.

5. SOLAR ARRAY AND SPACE STATION STRUCTURAL DYNAMIC ANALYSES AND DATA

Structural dynamic analyses were performed on various solar array and space station configurations to compliment the formulation of the dynamic interactions methodology. The results of these analyses in terms of modal property definitions are required as basic input to the simulation program. Described in this report section are the performed structural analyses for two phases of the interactions study. The first study phase considered only the derivation of solar array modal properties since the space station was considered to be a rigid body. The second study phase considered the influence of space station flexibility in the dynamic interactions methodology and therefore structural mode analyses are also presented for a space station conceptual design.

5.1 PHASE I STUDY ANALYSES

The structural analyses described in this report section were performed to obtain the necessary solar array vibration mode data for use as input to the dynamic interaction analysis simulation. By direction from NASA/LRC, two solar array configurations were considered in the structural analyses; these being a rollup flexible array, configured by the Lockheed Missile and Space Corporation, and a fold out panel array, configured from a Boeing Aircraft Corporation design concept. Both arrays meet the 100 KW power requirement for the North American Rockwell Space Station. In addition, the stowage configuration of both arrays for the launch phase of flight are compatible with the present geometrical constraints imposed by the space station shroud. It is noted, however, that the design criteria for the rollup array includes the loading environment associated with an artificial "G" environment while the fold out panel array is configured for the zero "G" mode of operation only.

A discrete structural element and mass representation of the solar arrays was utilized in the analysis method of deriving the required modal data. This technical approach required the generation of large-order stiffness and mass matrices for subsequent use in a matrix displacement method of modal analysis (Reference 5.1). Details of the modal analyses and analytical results are given in the following report subsections for both the rollup and foldout panel arrays.

5.1.1 FLEXIBLE ROLLUP ARRAY

The stiffness and mass characteristics used to model the flexible array for the determination of vibration modes are based upon information received from LMSC for the North American space station flexible array concept. The array wing section (Figure 5-1) consists of a central extendible boom with inner and outer array support members attached perpendicular to the boom (Reference 5.2). Ten kapton membrane strips are tensioned between the inner and outer support members to which the solar cells are attached. Primary structural member sizes are dictated by the loading associated with the artificial "G" mode of operation which presents the most severe design condition. If the array were designed only for the zero "G" environment, a lighter weight structure would result.

The total array area (2 wing sections) is approximately 10,000 sq. ft. and the electrical power output is rated as 10 watts per sq. ft. A six inch spacing is assumed to exist between the membrane strips and each strip carries a preset tension force of 2 pounds per foot of width. The main boom and support member are specified as frames. However, they are modeled for the discrete element method of analysis as equivalent stiffness beams. The stiffness properties of the structural members are given below.



Figure 5-1. Flexible Array Wing Section Dimensions

	AE	Elxi ₁ *	EIxi ² *	EIxi ₃ *	JG
Member	(lbs.)	$(lbin.^2)$	$(lb in.^2)$	$(lbin.^2)$	<u>(lbin.</u> ²)
Boom	11.45×10^{6}		1489×10^6	1585×10^{6}	23.1×10^{6}
Inner and Outer Support	23.4×10^{6}	160×10^{6}		840×10^6	è

*EIxi refers to moments about the Xi axis where the axis designation is shown on Figure 5-1.

The weight distribution used for each of the structural elements are as follows:

Running Weight
0.133 lb/in
0.958 lb/in
0.565 lb/in
2.45 (10^{-3}) lbs/in ²

5.1.1.1 Out of Plane Motion - Array Vibration Model

In solving for the out of plane array vibration modes, advantage was taken of the structural and mass symmetry of the rollup array wing section. This enables utilizing a structural model of only one half of the wing section. By suitable adjustment of the boundary conditions along the boom centerline, the symmetric and antisymmetric modes about the boom axes were obtained. Figure 5-2 is a sketch of the finite element model similar to that used for the mathematical representation of the continuous structure.

The out of plane motion degree of freedom given the membrane nodes was an X_3 translation. The support member nodes



a) Symmetric Model

· ·



b) Antisymmetric Model

Figure 5-2 Finite Element Model Rollup Array

were allowed degrees of freedom in X_3 translation and X_1 rotation. The boom nodes were allowed to translate in the X_3 direction and rotate about the X_2 axis for the symmetrical condition, and rotate about the X_1 axis only for the antisymmetrical condition.

The discrete element model used for computing the out of plane modes is shown in Figure 5-3. A one-hundred node model was used with the boom rigidly constrained at node 100 as shown. The discrete weights derived for each of the various nodes are tabulated in Table 5-1. The weight associated with this model does not include equipment weight located on the space station tunnel.

TABLE 5-1.	NODAL WEIGHTS ASSOCIATED WITH ROLLUP	
	ARRAY DYNAMIC MODEL	

Node	Weight (lbs.)
1	26.22
2-8, 11-17, 20-26, 29-35, 28-44, 47-53	11.63
56-62, 65-71, 74-80, 83-89	11.63
10,19,28,37,46,55,64,73,82	27.92
9	40.32
18,27,36,45,54,63,72,81,90	43.22
91	10.5
92,93,94,95,96,97,98	17.6
99	14.87
100	3.2

Ross' rectangular membrane finite element

representation (Reference 5.3) was used to model the membrane strips. A pictorial sketch of this element with the forces and degrees of freedom associated with the element nodes is shown in Figure 5-4a together with the corresponding formulation of the stiffness matrix.



Figure 5 - 3 Dynamic Model, Rollup Array, Out of Plane Modes



Figure 5-4a Rectangular Membrane Finite Element

$$K = \frac{2 \text{ EI}}{1^{3}} \begin{bmatrix} 6 & & & \\ 3 1 & 2 1^{2} & & \\ -6 & -3 1_{2} & 6 & \\ 3 1 & 1^{2} & -3 1 & 2 1^{2} \end{bmatrix} + \frac{\mu_{1}}{1/2} \begin{bmatrix} 6/1 & & & \\ 1/2 & 21/3 & & \\ -6/1 & -1/2 & 6/1 & \\ 1/2 & -1/6 & -1/2 & 21/3 \end{bmatrix}$$



Figure 5 -4b Beam Column Finite Element

Figure 5-4. Stiffness Matrices

An axial compression load due to the tensioning

of the membrane strips causes a decrease in the lateral stiffness of the boom. This beam column effect was accounted for in the stiffness matrix representing the boom, although for the values of bending and torsional stiffnesses used, the effect is small. The beam columning effect on the stiffness matrix (References 5.3 and 5.4) is shown in Figure 5-4b.

5.1.1.2 In-Plane Motion - Array Vibration Model

The in-plane rollup array model had the same nodes, mass properties and geometry as the out of plane model. Only one half of the wing section was modeled since the wing section is symmetric about the boom axis. Adjustments in the boundary conditions of the boom were made to obtain both the symmetrical and antisymmetrical modes. The model is shown in Figure 5-5. The membrane finite element representation utilized triangular plate elements which are described in Reference 5.1. These elements resist in-plane forces only. The effect of membrane tension upon the elemental in-plane stiffness representation was found to be negligible by use of the stiffness derivation method given in Reference 5.5. All nodes were allowed in-plane motion degrees of freedom only. The symmetrical modes were produced by allowing the boom to deflect only in the X_1 direction, and the antisymmetrical modes were produced by allowing the boom modes to deflect only in the X_2 direction and rotate about the X_3 axis. The symmetric modes induce axial forces into the boom while the antisymmetric modes produce in-plane shear forces and bending moments. The physical characteristics of the Kapton membrane substrate that were utilized for the analysis were:

> thickness = 0.004 inch Youngs Modulus = 450,000 psi Poisson's ratio = 0.5



Figure 5 - 5 In-Plane Rollup Array Model

5.1.1.3 Rollup Array Vibration Modes

From the rollup array out of plane modal analysis, 60 symmetric and 99 antisymmetric eigenvalues were obtained with the corresponding sets of eigenvectors. It was necessary to obtain a large number of modes in order to determine those of importance to the interactions study. Many of the modes are local torsion or bending of the individual membrane strips and do not contribute significantly as external loadings upon the space station.

The first forty-one frequencies for the out of plane modes are tabulated in Tables 5-2 and 5-3 with a description of the modes. Pictorial presentations of each of the lower symmetric and antisymmetric modes along with other higher modes which are considered to be important for inclusion in the interactions study are shown in Figures 5-6 to 5-22. In determining which modes to be used for interaction computer program runs (a total of 12 modes can presently be used for both in- plane and out of plane motion), use was made to modal participation factors. For the symmetric modes, the percent participation is based on the shear at the point of structural constraint due to a base translational acceleration when the value is equal to:

% participation =
$$\frac{(\Sigma m_i \phi_{in})^2}{R_n M}$$
 x 100

For the antisymmetric modes, the participation is based on the moment at the point of structural constraint due to a base rotational acceleration. The percent participation is equal to:

% participation =
$$\frac{(\Sigma m_i \mathcal{Q}_{in} r_i)^2}{\frac{R_n I_{x1}}{R_n x_{x1}}} \times 100$$

TABLE 5 - 2LIST OF OUT OF PLANE SYMMETRIC MODEFREQUENCIES FOR ROLLUP ARRAY

Mode	Frequency (Hz)	Description
ì	.0441	First torsion modes of
2	.0441	membrane strips
3	.0441	
4	.0441	
5	.0441	
6	.0734	
7	.0762	First bending modes of
8	.0763	membrane strips
9	.0763	
10	.0763	· · ·
11	.0864	
12	.0864	Second torsion modes of
13	.0864	membrane strips.
14	.0864	
15	.0864	
16	. 1255	
17	. 1255	Third torsion modes of
18	1255	membrane strips.
19	1255	
20	1255	· ·
21	. 1429	
22	. 1495	Second bending modes of
23	1497	membrane strins
24	1497	memorane strips
25	1497	
26	1507	
2 ₀ 0 97	1507	Fourth torgion modes of
29	1507	rout in tor sion modes of
20	1507	membrane scrips.
30	1507	
31	1979	
32	1070	Fifth tonsion modes of
33	1070	r nun tor sion modes of
34	1070	memorane strips
35	1272	
36	· 10/0]	First boom handing made
37	2020 -	r itst boom bending mode
38	2000	Sixth tongion meder of
20 20	.2000	Sixin torsion modes of
39 40		memorane strips
±v .11	.2080	
71	. 2085	

TABLE 5 - 3LIST OF OUT OF PLANE ANTISYMMETRICMODE FREQUENCIES FOR ROLLUP ARRAY

Mode	Frequency (Hz)	Description
1 2 3 4	.0439 .0441 .0441 .0441	First torsion modes of membrane strips
5 6 7 8 9 10	.0441) .0557 - .0763 .0763 .0763 .0763	First torsion mode of boom First bending modes of membrane strips
10 11 12 13 14 15	.0863 .0864 .0864 .0864 .0864	Second torsion modes of membrane strips
16 17 18 19 20 21	. 1082 - . 1255 . 1255 . 1255 . 1255 . 1255 . 1256	First bending mode of outer support Third torsion modes of membrane strips
22 23 24 25 26	.1497 .1497 .1497 .1497 .1497 .1595	Second bending modes of membrane strips
27 28 29 30 31	.1597 .1597 .1597 .1597 .1597 .1620 -	Fourth torsion modes of membrane strips Second torsion mode of
32 33 34 35 36	. 1878 . 1878 . 1878 . 1878 . 1878 . 1878	boom Fifth torsion modes of membrane strips
37 38 39 40 51	. 2086 . 2086 . 2086 . 2086 . 2086	Sixth torsion modes of membrane strips







Figure 5-7 Mode 2, Rollup Array, Out of Plane, Symmetric


f = .0441 Hz $\% \approx 0$

Figure 5-8. Mode 3, Rollup Array, Out of Plane, Symmetric







f = .0441 Hz

Figure 5-10 Mode 5, Rollup Array, Out of Plane, Symmetric



Figure 5-11 Mode 6, Rollup Array, Out of Plane, Symmetric 5-19



Figure 5-12 Mode 36, Rollup Array, Out of Plane, Symmetric



Figure 5-13 Mode 56, Rollup Array, Out of Plane, Symmetric



Figure 5-14 Mode 1, Rollup Array, Out of Plane, Antisymmetric



Figure 5-15 Mode 2, Rollup Array, Out of Plane, Antisymmetric



Figure 5-16 Mode 3, Rollup Array, Out of Plane, Antisymmetric





Figure 5-18 N

Mode 5, Rollup Array, Out of Plane, Antisymmetric



Figure 5-19 Mode 6, Rollup Array, Out of Plane, Antisymmetric



Figure 5-20

Mode 31, Rollup Array, Out of Plane, Antisymmetric



Figure 5-21

Mode 57, Rollup Array, Out of Plane, Antisymmetric



Figure 5-22. Mode 62, Rollup Array, Out of Plane, Antisymmetric

where

 $m_i - mass of discrete node i (lb.-sec. ²/in.)$ $<math>\emptyset$ in - deflection of node i for mode n $R_n - generalized inertia of mode n (lb.-sec. ²/in.)$ M - mass of dynamic model (lb.-sec. ²/in.) $r_i - distance along X₂ axis of mass i. (in.) (Ref. Fig. 5.1-3)$ $I_{x1} - moment of inertia of dynamic model about the X₁ axis (lb.-in.-sec. ²)$

The participation factors for the full wing section are shown on the mode shape plots along with the frequencies. The modes which were chosen to be important for subsequent interaction analyses were antisymmetric modes 6, 31, 57 and 62 and symmetric modes 6, 36, and 56.

From the rollup array in-plane modal analysis, eigenvalues and corresponding eigenvectors were computed up to 5 Hz. Frequencies within this range should be sufficient to determine the effects of the array flexibility on the spacecraft control system. Six symmetric and eight antisymmetric modes were obtained for these cases. The frequencies for these modes are listed in Table 5-4.

Frequency (Hz)			· · · · · · · · · · · · · · · · · · ·
Mode	· · · · ·	Symmetric	Antisymmetric
1		2.1199	. 2911
2		2.2604	1.939
3		2.3825	2.177
4		2.4486	2.4139
5		2.4895	2.4757
6		2.5038	2.4999
7			2.7056
8			4.1198

TABLE 5 - 4FREQUENCIES OF IN-PLANE MODESFOR ROLLUP ARRAY

The modal participation factors for these cases

are based on axial load due to a base translational acceleration for the symmetric modes and shear load due to a base translational acceleration for the antisymmetric case. The mode shapes for the full wing section and percent modal participations are shown in Figures 5-23 to 5-29. On these figures, the solid lines are the deflected shapes while the dashed lines are the the undeflected outline of the wing section. The modes which were chosen to be important for interaction analyses are symmetric mode 2 and antisymmetric modes 1, 2, 7 and 8. The complete list of frequencies and modal participation factors for the modes selected for use in the interaction program for the rollup array are listed in Table 5-5.

TABLE 5 ----5 FREQUENCIES AND MODAL PARTICIPATION FACTORS OF ROLLUP ARRAY MODES USED IN INTERACTION ANALYSIS

Out of Plane					
	Symmetric			Antisymmet	ric
Mode	Frequency (Hz)	Percent Participation	Mode	Frequency (Hz)	Percent Participation
6 36 56	.0734 .2026 .2873	50.4 12.5 3.5	6 31 57 62	.0557 .1620 .3182 .3404	67.7 5.35 7.3 7.73
		In-P	lane		- <u> </u>
Symmetric		Antisymmetric			
Modé	Frequency (Hz)	Percent Participation	Mode	Frequency (Hz)	Percent Participation
2	2.2604	57	1 2 7 8	.2911 1.939 2.7056 4.1198	55 3.1 6.5 2.7







Figure 5-24. Mode 2, Rollup Array, Inplane, Symmetric





[•] 5−35







Figure 5-27 Mode 2, Rollup Array, Inplane, Antisymmetric







Figure 5-29. Mode 8, Rollup Array, Inplane, Antisymmetric

5.1.2 FOLDOUT PANEL ARRAY

The foldout panel array is a multipanel array consisting of a beryllium framework with a tape substrate. The array is based on a Boeing concept (Reference 5.6) for a lightweight rigid array designed for an unmanned Mars mission. The overall dimensions of one wing section of the array as modified for the space station are shown in Figure 5-30. The wing section consists of thirty panels which were required in varying lengths so as to meet the internal shroud geometry constraints for stowage during the flight launch phase. Panels 1 through 6 are hinged together and are the main load carrying members of the array. Attached to each main panel are four subpanels (such as 1A, 1B, 1C and 1D) hinged at the long side only. The entire wing section is attached to the spacecraft tunnel through members attached to main panel 1.

Each panel consists of a beryllium rectangular x-braced frame with lateral and longitudinal stiffeners as shown in Figure 5-31. Corresponding section properties are given in Figure 5-32. The overall dimensions shown are for panels 1 through 1D. The stiffeners and outer frame members are split in a horizontal plane to hold a tape membrane substrate to which the solar cells are bonded. Details of this frame construction are discussed in Reference 5.6.

Ten mill cells with six mill coverglas were used in determining the solar stack weight. The remaining weight of the array was formulated by ratioing the weight breakdown listed in Reference 5.6 by the respective areas of the 100 and 50 KW arrays. The weight breakdown and total weight of the foldout panel array used for the structural analysis is tabulated in Table 5-6.



CENTER -LONGITUD/NAL SPAR END FRAME -LONGITLIDINAL INTERCOSTAL DIAGONAL BRACE 100" LATERAL SPAR LATERAL INTERCOSTAL OLITBO**ARD** SPAR -296 "

Figure 5-31. Foldout Panel Construction



Figure 5-32. Member Properties

TABLE 5-6 WEIGHT BREAKDOWN FOR FOLDOUT PANEL ARRAY

.

Cell Stack, Substrate and Thermal Coating	Weight (lbs)	
Cover Glass	674	
Cover Glass Adhesive	38	
Cells	938	
Connectors	116	
Solder	8	
Substrate Adhesive	130	
Substrate	156	
Thermal Coating Total	190	2250
Mechanisms	· · · · · · · · · · · · · · · · · · ·	
Main Hinges and Latches	60	
Auxiliary Hinges, Latches and Dampers	72	
Quadrants and Sequencers	56	
Strut Assemblies	30	
Solar Curtains	28	
Boost Tie-down System	144	
Cable, Drive and Miscellaneous	84	
Total		474
Electrical Connectors		· .
Busses and Diodes	194	
Pigtails and Connectors	26	
Sauib Wiring	8	ł
Terminals and Crossover Busses	52	
Total		280
Structure		
Shear Clips	12	
Gusset Plates	34	~
Diagonal Tension Ties	156	
Shear Ties	206	
Internal Fittings	38	
Main Members	2642	
Total		3088
TOTAL		6092

5.1.2.1 Array Vibration Model

To derive a dynamic model of the total array and simulate all of the structural members for each foldout panel results in an unusually large problem and would be unnecessary for an adequate analytical simulation. Therefore, each panel was idealized into a simpler model. Also, since the array is symmetric, it was possible to model only one-half the array and adjust the boundary conditions of the center longitudinal spar nodes (Figure 5-31) of the main panel members in the same manner as was done for the rollup array. The dynamic model derived is shown in Figure 5-33. The construction of one panel, such as the panel bounded by nodes 1, 3, 15 and 13, can be considered as an X-braced rectangular frame with a lateral and longitudinal spar. To account for the stiffness of the remaining lateral and longitudinal intercostals of the frame (Figure 5-31), the stiffnesses of these members were distributed and added to the stiffnesses of the end frames and lateral and longitudinal intercostals. Adjacent panels of the structure are hinged and the two adjacent beams on which the hinges are located were considered as a single beam. These beams are shown as the heavy lines on Figure 5-33. The wing section is attached by struts to the space station tunnel at nodes 97 and 98 and in determining the frequencies of the model, the array was considered as rigidly constrained at nodes 97 and 98.

Mass loading for the idealized panel consists of a center mass point and a mass point at each corner. One quarter of the panel weight was allocated to the center point and the balance was divided equally between the four corners. The weight associated with the nodes of Figure 5-33 are listed in Table 5-7.



Figure 5-33. Idealized Dynamic Model for Foldout Panel Array

Nodes	 Weight (lbs)
1,13	15.4
3,5,15	30.8
8,10	20.52
12	10.26
17	66.42
19,29,35,45	17.81
21,31,37,47	35.62
24,26,40,42	23.75
28,44	11.87
33	71.24
49	76.12
51,61,67,77	20.25
53,63,69,79	40.5
56,58,72,74	27.0
60,76	13.5
65	81.0
81	85.88
83,93	22.69
85,95,97	45.38
55,9U	30.25
54	15.13

TABLE 5-7 NODAL WEIGHTS, FOLDOUT PANEL ARRAY MODEL

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5.1.2.2 Foldout Panel Array Modes

Foldout panel array frequencies and corresponding modal deflections were computed up to 25 Hz. For the out of plane motions, 48 symmetric and 42 antisymmetric vibration modes were obtained. For the in-plane motions, one symmetric and five antisymmetric modes were obtained. The antisymmetric, out of plane modes represent the torsional deflections of the array while the symmetric modes represent out of plane bending deflections. For the in-plane modes, the symmetric modes represent axial deflections and the antisymmetric modes represent in-plane bending deflections. Resulting modal frequencies for the various cases are listed in Tables 5-8, 5-9, and 5-10.

Graphical presentations of selected modes and corresponding modal participation factors are given in Figures 5-34 to Figure 5-45. The participation factors are based on the same quantities as described for the rollup array modes. The displacement vectors for the out of plane modes (Figures 5-34 through 5-41) are only plotted at nodes with associated mass points. In Figure 5-42 the undeflected array is shown in dashed lines while the deflected shape is shown in solid lines. In Figures 5-43 through 5-45, only the deflected mode shapes are shown. All the modes shown are to be inputs to subsequent dynamic interaction analyses using the generated computer program. The frequencies and modal participation factors for these modes are listed in Table 5-11.

5.1.2.3 Panel Breathing Mode

As a verification of the dynamic model used, a more detailed model of one panel (Figure 5-31) was derived to analytically evaluate the fundamental panel breathing mode. It is required to maintain TABLE 5-8. FREQUENCIES OF FOLDOUT PANEL ARRAY, OUT OF PLANE, SYMMETRIC

10.0173 10.0992 6. 9385 7.8235 12.6855 13.3285 18.8390 7.0980 7.1827 7.9082 8.3442 9.4665 7.6312 11.1912 1.9995 13.8218 14.6318 16.1680 17.5238 7.5044 7.7656 8.5362 14.0497 15.6202 Frequency (Hz) 25 25 25 25 25 28 30 32 34 35 36 31 37 38 39 45 46 47 48 12 40 13 Mode Frequency (Hz) . 2072 1.1429 1.2950 .0344 . 5293 1.4353 .8861 4.2284 6.5716 1.4971 L. 5291 l. 6344 1.7653 1.9877 2.2596 2.8494 6.7198 6.8655 L. 6078 2.5279 6.4331 3.3752 6.3315 5.6543 Mode 21 22 23 24 15 16 18 19 20 14 17 2 27 13

Mode	Frequency (Hz)
1	.1184
2	.3606
3	.6075
4	.8607
5	1.0980
6	1.2871
7	1.5609
8	1.7386
9	1.8536
10	1.9813
11	2.1327
12	2.3362
13	3.7286
14	3.9908
15	4.2144
16	4.4811
17	4.9012
18	5.6379
19	5.7335
20	6.4064
21	6.6507
22	6.8024
23	7.0102
24	7.4163
25	7.8218
26	7.8506
27	7.9083
28	9.2626
29	9.6278
30	9.9170
31	9.9937
32	10.1300
33	10.3267
34	10.6231
35	11.2053
36	11.4311
37	11.5634
38	12.4228
39	13.2525
40	13.7070
41	14.9116
42	17.2326

TABLE 5-9.FREQUENCIES OF FOLDOUT PANEL ARRAY,OUT OF PLANE, ANTISYMMETRIC

TABLE 5-10. FREQUENCIES OF FOLDOUT PANEL ARRAY, IN-PLANE

Mode	Description	Frequency (Hz)
1	Symmetric	24.76
1	Antisymmetric	1.669
2	Antisymmetric	6.934
 3	Antisymmetric	13.765
4	Antisymmetric	19.771
5	Antisymmetric	23.5


f = .0344 Hz **%** = 63

Figure 5-34. Mode 1, Foldout Panel Array, Out of Plane, Symmetric



f = .2072 Hz % = 19.6

Figure 5-35. Mode 2, Foldout Panel Array,

Out of Plane, Symmetric



f = .5293 Hz% = 7.2

Figure 5-36 Mode 3, Foldout Panel Array, Out of Plane, Symmetric



f = .8861 Hz

% = 3.4

Figure 5-37 Mode 4, Foldout Panel Array, Out of Plane, Symmetric



f = .1184 Hz

% = 78.6

Figure 5-38 Mode 1, Foldout Panel Array, Out of Plane, Antisymmetric



f = .3606 Hz % = 9.4

Figure 5-39, Mode 2, Foldout Panel Array, Out of Plane, Antisymmetric



f = .6075 Hz

% = 3.65







6

f = 24.76 Hz % = 83





f = 1.669 Hz % = 64.5

Figure 5-43. Mode 1, Foldout Panel Array, Inplane, Antisymmetric



f = 6.934 Hzo% = 21.3

Figure 5-44. Mode 2, Foldout Panel Array, Inplane, Antisymmetric



FOLDOUT PANEL ARRAY, MODAL PARTIOIPATION FACTORS TABLE 5-11.

Participation Participation Percent Percent 4.03 3. 65 2.06 64.5 21.3 78.6 9.4 Antisymmetric Antisymmetrlc Frequency . 6075 Frequency (Hz) .1184 . 3606 . 8607 1.669 6,934 13, 765 (Hz) Mode Mode 2 က 4 3 2 rH Out of Plane In-Plane Participation Participation Percent Percent 19.6 7.2 3.4 63 83 i Symmetric Symmetric Frequency Frequency .0344 .2072 . 5293 24.76 .8861 (Hz) (HZ) Mode Mode ์ **ณ** က 4 m က 2

an adequate frequency separation between the breathing mode and the array's out of plane modal frequencies since the model used in the array analysis did not include sufficient degrees of freedom for the description of breathing modes. The nodal numbering and dimensions of the panel model analyzed is shown on Figure 5-46. There are 53 nodes in the model and nodes 44 through 53 were rigidly constrained for the dynamic analysis. The first mode of this model was 7.634 Hz which is sufficiently separated from the array out of plane mode frequencies. The nodal weights are tabulated in Table 5-12 and the mode shape of the breathing mode is shown on Figure 5-47.

5.2 PHASE II STUDY ANALYSES

The structural analyses described were performed to obtain modal data to compliment the formulated digital simulations. The analyses were conducted on the solar array and space station configurations described in Section 2.0, which correspond to both the zero "G" and artificial "G" conditions. A requirement of the dynamic interaction analysis digital simulation is that cantilever modal data for the solar arrays and free-free modal data for the space station be initially determined and used as input. Each of the structural models and corresponding modal data is described in the following.

5.2.1 ZERO "G" SPACE STATION CONFIGURATION

The stiffness and mass properties used to represent the space station structural arrangement were those resulting from preliminary configuration studies performed by North American Rockwell (Reference 5.7). These properties were obtained from NAR and are given in Table 5-13 and Figure 5-48, comprising the total structural arrangement.



Figure 5-46 Breathing Mode Model

TABLE 5-12. NODAL WEIGHTS FOR BREATHING MODE MODEL

Node	Weight (lbs)
1.5	2.059
2,4	3.401
3	4.578
6,9,12,13,16,19,20,24,25,29	1.955
7, 11, 14, 18	2.261
8, 10, 15, 17	2.066
21,23,26,28	3.708
22,27,33,40	3.191
30,36,37,43	1.336
31,35,38,42	2.064
32,34,39,41	2.284





TABLE 5-13

WEIGHT (LBS.)
2 5, 0 00
25,000/module
17,500

Mass Properties of Zero "G" Space Station Configuration

A finite element model representing this configuration was derived, using a limited number of nodal points, and it is depicted in Figure 5-49. The corresponding descrete masses of the model and grid point geometry is given in Table 5-14. Each of the discrete points was allowed three translational degrees-of-freedom and one rotational degree-of-freedom, corresponding to torsion of each module. Shear flexibility was considered for appropriate degrees-of-freedom because of the relatively small length to diameter ratio of each module. The model geometry, inertial properties and stiffness properties were input to the NASTRAN program (Reference 5.12) for the determination of modal properties, i. e., frequencies, mode shapes, and modal masses. A partial list of these quantities are listed in Table 5-15. A comprehensive listing of the zero "G" modal properties, together with a graphical presentation of lower modes of vibration, are given in Appendix A to this report.

5.2.2 ARTIFICIAL "G" SPACE STATION CONFIGURATION

The artificial "G" space station configuration was discretized into the finite element model presented in Figure 5-50. Stiffness and inertial properties are similar to those presented for corresponding modules in Table 5-13 and Figure 5-48 except for the power boom and extended boom; the mass



TABLE 5-14 Mass-Geometry Data

Of Zero G Space Station

		MASS ,			
		(1bsec)		
NODE	NO.	in.	- x	Y	7
	1	16.189	120.	0.	-492.
	2	16.189	120.	0.	492.
	3	16.189	120.	492.	0.
	4	16.189	120.	-492.	0.
	5.	16.189	120.	0.	-372.
	6	16,189	120.	0.	372.
	7	16,189	120.	372.	0.
	8	16,189	120.	-372.	0
	9	16,189	120.	0.	-252.
	10	16,189	120.	0	252.
	11	16,189	120.	252.	0.
	12	16,189	120.	-252.	0.
	13	16,189	120	0.	-132.
	14	16.189	120.	0.	132.
	15	16.189	120.	132.	0.
	16	16,189	120.	-132.	0.
	17	0.	120.	0.	-72.
	18	0.	120.	0.	72.
	19	0.	120.	72.	0_
	20 .	0.	120	-72	0.
	21	8.1	120	-, L .	0.
	22	8.1	60	0.	0.
· .	23	0	100	0	0
	24	4 05	100.	0	0
	24	4.05	260	- 492	0
	20	10+107	360.	-476 +	0
	20	10,104	300.	-312.	0
	29	16 190	360	~252	0
•	20	16 189	360	-132	0
	27	10,107	360	~72	0.
	21		360.	-12.	0.
	22	12 15	360.	V• 73	···
	32	16,15	360.	16.	73
	3.3	0	360	0.	72
	34		300 -		
	37 -	0+1	420.	132	0
	30	10,109	360.	1.32 •	122
	31	10.109	300.		1.32.0
	38	10.104	360	0.	-136.
	37	16 1919	400.	0.	0
	40	10.109	360.	2764	- 11
	41	10,109	360.	0.	252.
	42	10.109	300.	0.	-252.
	43	11.4034	700.5	- U.∎	
	44	10.107	300.	312.	U.
	40	10.187	350.	U .	312.
	40	10-194	350.	U• -	
	41	14.086	921.	U •	U.
	48	10.189	360.	472.	U.
	49	16,189	360.	U •	492.
	50	16.189	360.	.0.	-492 •

Table 5-15. Modal Data, Space Station

(Zero G Configuration)

	Freq	luency	Generalized Mass
Mode	(H	Iz)	(lbsec. 4 in.)
1	1 2.0		6.281594E 02
2	-0.0	Dirid Dad-	6.281594E 02
3	- c . (Rigia Boay	6.281594E 22-
¢.	0.0 (Modes	2.477312E 02
5	n'a•è n		1.200991E 02
6	0.0 l		1.200991E 02
7	165579	5775 00 ···	2.2977175 02
8	2.2774	NG 78 0 0	3.636589E 01
9	2.2787	772-0	3.6600572-01
10	3.1473	397日 00	8.37324AE 01
11	3.2450	78E 00	1.085563E 02
12	4.3915	578= 00	1.511382E 02
13	4.4838	3922-00	30124590E 02
14	5.7027	100E 00	7•439223E 01
15	66035*	575 00	7.1A2155E 01
16	6.4775	575 00	8.401511E 01
17	€ € 8753	38 <i>9</i> 2 00 00	1.1117005 02
18	6.8753	395 7 00 1	1.111700E 02
19	707653	384E 00	5.186711E 01
20	8.2635	37A5 10	10006247E 02
21	8-8509	1535 DO	
22	8.9355	523E 00	
23	1.0132	241E 01 V	
24	1.1304	435 01	
25	1.1317	81E 01	
26	1.4755	548E 01	
27	165347	285 01	
<u>.</u> 28	1.9580	186 01	
29	1.9555	015E 01	
30	2.2.2778	5325 01	
31	2.3199		
32	203391	(815-71 1997-191 - 197 - 19	
33	2.09429		
	209717	7799 VI 7095 31	
. 30	2-6530	10 2E 01	
ີ 37	20000	645 01 ···	
37	2.7521	395 01	
- 30 	207.221	02E 01	
A C	2.9421	805 01	
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	2.9672	575 01	
42	2.9672	5CE 01	
<b>4</b> 3	2.9773	96月 01	
44	2.9837	235 01	
45	2.9847	262.01	
4.6	2.9922	938 21	· · ·
4,7	3.0039	22F 01	•
48	3.055	89F 01	
49	-3.0057	307 01	
50	3.0279	895 01	

50



and geometry properties for this modal are listed in Table 5-16. It was originally intended to utilize the stated capability of the NASTRAN program in the performance of the modal analysis of the spinning structure; however, initial attempts with NASTRAN failed (Version 12). An eigenvalue-eigenvector program obtained from the Jet Propulsion Laboratory (JPL) in Pasadena, California, and formulated by Dr. K. K. Gupta (Reference 5.8 and 5.9) was used. As is required for modal analysis of spinning structures, a coriolis force matrix and centrifugal force matrix were derived for the total description of the equations of equilibrium of the discretized system. A comprehensive description of typical terms in these matrices can be found in Reference 5.10. The centrifugal force matrix is a function of the motion variables while the coroilis force matrix is dependent upon the first derivatives of the motion variables. Orthogonalization of this system of equations results in complex conjugate pairs of eigenvalues (zero real part) and corresponding complex conjugate pairs of eigenvectors. The digital simulation, for the artificial "G" condition, is programmed to accept this modal data format.

For the structural configuration shown, the artificial "G" condition was attained by spinning the space station at 4 RPM about a point 44 feet outboard of the space station-solar array attachment as depicted in Figure 5-51. The coriolis force and centrifugal force matrices were computed by hand and the stiffness matrix was generated with the NASTRAN computer program. It was also determined that the influence of static spin loads upon the station's structural stiffness (beam column effect) was negligible and therefore neglected. The matrices together with the mass matrix were input into the JPL program for determination of complex eigenvalues and eigenvectors for a range of steady state spin rates. Resulting frequencies are presented in Table 5-17 for spin rates of 0, 4, 8, and 12 RPM together with

# TABLE 5-16 ARTIFICIAL "G" SPACE STATION

## FINITE ELEMENT MODEL DATA

NODE	MASS LBSEC ² /IN	IN LB	ERTIA SEC ²	IN	NO. OF STRUCTURAL D.O.F.	D.O.F. SEQUENCE NO.
		x Axis	y Axis	z Axis		
1	21.578		66641		6	1-6
2	21.578		66641		6	<b>7-12</b> [°]
3	21.578		66641		6	13-18
4	21.578		66641		6	19-24
5	21.578		66641		6	25-30
6	21.578		66641		6	31-36
7		<b></b> .			6	37-42
8					6	43-48
9	15.382	41621			6	49-54
10	8.094	21886			6	55-60
11	4.047	10956		·	. 6	61-66
12	17.814	49417			6	67-72
13	15.379	41595			6	73-78
14	12.795	18700			6	79-84
15	10.632	9350			6	85-90
16	25.952	20642	]		6	91-96
17	.01295	10.282			6	97-102



# TABLE 5-17

# Artificial "G" Space Station Configuration List of Eigen Values in Hertz

Elastic Mode No.	NASTRAN Results	"GUPTA" Program Results								
	$\Omega = 0$	Ω = 0	$\Omega = 4RPM$	Ω= 8RPM	$\Omega = 12 \mathbf{R} \mathbf{P} \mathbf{M}$					
1	2.2967	2.2948	2.2929	2.2890	2.2851					
2	4.2003	4.2027	4.2027	4.2026	4.2027					
3	8.4202	8.4224	8.4147	8.4068	8.3914					
4	8.6787	8.6711	8.6789	8.6867	8.6944					

the modal frequencies obtained by NASTRAN for the same model in a zerospin condition. It is seen that the frequency correlation between NASTRAN and Gupta's program is excellent and that the frequency change with spin rate is minimal. A comprehensive list of modal data in terms of modal deflection and graphical description of the lower frequency modes in terms of absolute deflection coefficients, are given in Appendix A to this report. Also presented are the structural degrees of freedom considered in the analysis. Examination of the shape for the second mode shows this mode is represented by out-of-the-spin-plane bending only and would not be influenced by centrifugal or coriolis forces. This explains the constant frequency results with spin rate for the second mode which is shown in Table 5-17. The general conclusion indicated by the performed modal analyses is that the spin rate does not significantly alter the zero spin modal frequencies if the zero spin modal frequencies are sufficiently separated from the spin frequency.

#### 5.2.3 ZERO "G" SOLAR ARRAY CONFIGURATION

The rollup solar array was analyzed in a similar manner as is described for past study analyses in Section 5.1. Updates in configuration data, however, were obtained from the Lockheed Space and Missiles Company and these were incorporated into the description of the derived vibration analysis model.

The total array area (two wing sections) is approximately 10,000 square feet and the electrical power output is rated as 10 watts per square foot. The rollup array dimensions and structural components are depicted in Figure 5-52. It is comprised of 10 membrane substrates



Figure 5 -52 Zero "G" Solar Array Configuration

per wing section, tensioned between an inner and outer boom by an extendible boom. Two guide wires are provided for each membrane strip and each is tensioned to 5.1 pounds. Each strip is attached to the inner boom assembly by a linear spring and tensioned to 12 pounds. A guy wire is also provided between the outboard end of the extendible boom and the extremity of the inner boom and acts as a tension load carrying member only. Pertinent stiffness and mass properties data for the array structural components are given in Table 5-18.

As was considered in Section 5.1, the symmetry properties of the solar array were utilized in the performance of its modal analysis. Only one-half of the wing section was discretized into a finite element model and it is presented in Figure 5-53. Four separate vibration conditions were established for the complete evaluation of modal properties and correspond to out -of-plane symmetric bending, out-of-plane antisymmetric bending (about the extendible boom), in-plane symmetric bending and in-plane antisymmetric bending. The NASTRAN finite element program (Reference 5.11) was utilized to obtain the modes; the four vibration conditions were obtained by constraining appropriate structural degrees-of-freedom. The nodal weights associated with the rollup array dynamic model and nodal geometry are given in Table 5-19. An assumption was made in the analyses for treating the stiffness provided by the guy wire; it was considered as a tension-compression member with only one-half of its actual tension stiffness properties. In addition, the lateral stiffness of the membrane strips was assumed to be described in terms of the tension force only. These stiffness terms were entered in the NASTRAN program by means of the "CELAS" stiffness elements.

A complete list of modal results and graphical presentation of modes for the four vibration conditions are given in Appendix A of this report. Modal participation factors, for each normal mode of the solar

**TABLE 5 -18** 

STIFFNESS AND MASS PROPERTIES DATA FOR ROLLUP SOLAR ARRAY

MEMBER	AE (lbs.)	$\mathbf{Ei}_{\mathbf{X}}^{*}$ (lb-in. 2)	$\mathrm{El}_{\mathrm{Y}}^{*}$ (1bin. ² )	$\operatorname{EI}_{Z}^{*}$ (1b in. ² )	GJ 2) (lb-in. ² )	RUNNING WEIGHT (lbs/in.)
Extendible Boom (Full)	22.4 x 10 ⁶		2.8 x 10 ⁸	2.8 x 10 ⁸		. 212
Outer Support	10.4 x 10 ⁶ (Y=0 to 72) 5.9 x 10 ⁶ (Y=72 to 369)	9.3 x 10 ⁸		$\begin{array}{c} 3.32 \times 10^{8} \\ (Y=0 \ to72) \\ 1.87 \times 10^{8} \\ (Y=72 \ to369) \end{array}$	26.8 x 10 ⁶	. 130
Inner Support	5.9 x 10 ⁶	9.3 x 10 ⁸		1.87 x 10 ⁸	26.8 x 10 ⁶	. 115
Membrane Strip	3. 33 lb/ in.					.2
Guy Wire	. 203 x 10 ⁶					

* - For axis system refer to Figure 5-52.



# Figure 5-53 Structural Model for Roll-up Solar Array Zero "G" Configuration

## TABLE 5-19

## Mass - Geometry Data

## Of Zero G Solar Array

					· · ·
NODF	NO.	WEIGHT(12	s.)X	Y	7
	1	21.48	1056.	347.	- 0 .
	5	32.3	888.	347.	<b>.</b>
	3	26 06	1056.	275.	Λ.
	4	32.3	720.	347.	0.
	5	35.3	888	275.	۰.
	6	26.06	1056.	503.	0.
	7	32.3	552.	347.	Ο.
	8	35.3	720.	275.	Λ.
	9	32.3	888.	503.	0.
	10	26.06	1056.	131.	Ο.
	11	32.3	384.	347.	θ.
	12	32.3	552.	275.	0.
	13	32.3	720.	503.	Λ.
	14	32.3	998.	131.	· · · · · · · · · · · · · · · · · · ·
	15	25.32	1056.	59.	. <b>n</b> .
	16	32.3	216,	347.	0.
	17	32.3	384	275	· - ··· <del>A</del>
	18	. 32,3	552.	203.	Λ.
	19	32,3	720.	131.	Ο.
<b>.</b>	-5 <del>0</del>	- 323.	888		• • • • • • • • • • • • • • • • • • •
	S1	12.74	1056.	0.	0.
	22	20.84	48.	347.	0.
	23	32.3	216.	275.	<b>∩</b> -∎
	24	35.3	384,	203.	0.
	25	32.3	552.	131.	0.
•	26	32.3	720.	59.	Ĥ. <b>.</b>
	27	17.81	888.	0.	0.
	28	24.98	48.	275.	0.
	59	32,3	516.	203.	0
	30	32.3	384.	131.	0.
	31	32.3	552,	59.	Ο.
	35	17.81	720.	0.	0.
	33	24.98	48.	203.	0.
	34	32.3	216 <b>,</b>	131.	0.
	35	32.3	384,	59.	0.
	36	17.81	552.	0.	0.
	37	24.98	48.	131.	<u>n</u> .
	38	-32.3	216.	59.	Ο.
	39	17.81	384.	0.	0.
	40	24.23,	48.	59.	0.
	41	17.31	216.	···· <b>··</b> •	0
	42	12.30	48.	0.	0.
	43	0.	0.	0.	Ο.

.....

NOTE: Weights along the boom (Y = 0.) are one half the actual weight.

array, using root constraint loads were also computed in order to determine those modes of importance for describing interaction loads. The properties of those modes having relatively large load participation factors are listed in Table 5-20.

#### 5.2.4 ARTIFICIAL "G" SOLAR ARRAY CONFIGURATION

The rollup solar array for the artificial "G" condition consists of the same structural geometry as that of the zero "G" configuration, however, only four membrane strips are utilized -- the two on each side of and adjacent to the extendible boom. The derived finite model of the artificial "G" array is presented in Figure 5-54. Average tension in each strip during spin is increased to 340 pounds and the strips lateral deflection stiffness values are based upon this tension. The stiffness matrix for each finite element of the extendible boom was computed by hand so as to include the beam columning effect and input into the NASTRAN program by the "direct matrix input" method. Additional structural restraints are provided at the extremities of the inner boom for this spin condition and were included in the dynamic model. The stiffness matrix for the entire model was formulated by NASTRAN and the coriolis force coefficient and centrifugal force coefficient matrices were generated by hand computations. The configuration was taken to spin in a plane containing the solar arrays. These matrices, together with the mass matrix were input in the JPL program (References 5.8 and 5.9). A list of all resulting modal data for spin rates of 0, 4, 8, and 12 RPM are presented in Appendix A of this report. A list of data for those modes which were identified to have large load participation (zero spin) are presented in Table 5-21. The modal constraint forces used in the calculation of participation factor were those resulting at each point of array restraint. Table 5-22 lists the frequencies of these modes with large participation factors for each

TABLE 5-20 ROLLUP SOLAR ARRAY MODAL DATA, ZERO "G" CONFIGURATION

actor	Torque				. 779	.074	. 078			-							
Participation F	Bending Moment	.415	.044	.001					• .			. 514	. 137	.105	.084	* ~i	· · · · · · · · · · · · · · · · · · ·
Modal	Force	. 681	.003	. 119				. 520	.165	.058	. 062	. 712	.001	. 077	. 055	- -	
Generalized	Mass ₂ (lbsec. ² /in.)	1.36	1.30	. 158	. 609	. 547	. 689	. 705	. 770	. 607	. 104	1.35	1.41	1.46	1.83		-
	Frequency (Hz)	. 0925	.187	. 835	. 0640	.167	.241	1.35	3.28	3.49	6.07	,0974	.189	,265	.324		
	Mode No.	1	9	22		9	11	26	27	28	31	 1	9	11	16		
	Type	Symmetric			Anti- Symmetric			Symmetric				Anti- Symmetric					
	Direction	Out of Plane						In Plane				<b>.</b>					


Table 5-21 Artificial "G" Solar Array,

.

Modal Participation Factors

Zero Spin

			Out of Plane				
	Symmetric		-		Antisymmetric		
		% Partic	tipation			% Parti	icipation
Mode	Frequency (Hz.)	Shear	Moment	Mode	Frequency (Hz.)	Mo	ment
5	0.203	41.9	15.2	1	0.199	12,	5
<b>5</b>	0.504	1.7	0	10	0.521	<b>1</b>	4
17	0.778	2.1	0	18	0.794	5	0
		-		19	0.905	78.	6
			In Plane				·
	Symmetric				Antisymmetric		
Mode	Frequency (Hz.)	% Partic She	apation ar	Mode	Frequency (Hz.)	% Parti Shear	cipation Moment
32	3.84	76.5	<u>i</u>	ñ	0.378	33. 2	30.0
			<u> </u>	11	0.704	0.5	9.6
				20	0.935	4.7	7.0
				28	1.065	7.6	17.7

# **TABLE 5-22** ART "G" SOLAR ARRAY CONFIGURATION

## LIST OF EIGENVALUES IN HERTZ

ELASTIC MODE NO	NASTRAN BESILLTS	NASTRAN "GUPTA" PROGRAM RESULTS RESULTS				
	$\Omega = 0$	Ω <b>=0</b>	Ω=4 RPM	$\Omega = 8 \text{ RPM}$	$\Omega = 12 \text{ RPM}$	
	0 1989	0 1786	0 1786	0 1787	0, 1787	
• 2	0.2032	0.1977	0.1977	0. 1977	0.1977	
3	0.3784	0.3768	0.3710	0.3524	0.3185	
9	0.5037	0.5031	0.5025	0.5025	0.5025	
10	0.5215	0.5142	0.5151	0.5151	0.5151	
11	0.7045	0.7010	0.6969	0.6881	0.6716	
17	0.7782	0.7774	0.7777	0.7777	0.7777	
18	0.7941	0.7912	0.7911	0.7911	0.7911	
19	0.9051	0.9047	0.9049	0.9049	0.9049	
20	0.9349	0.9315	0.9291	0.9224	0.9090	
28	1.0654	1.0544	1.0506	1.0454	1.0331	
32	3.8422	3.8402	3.8413	3.8441	3.8462	
				· · ·		

Modes 1, 2, 9, 10, 17, 18, 19 are out-of-plane modes.

Modes 3, 11, 20, 28, 32 are in-plane modes.

of the considered spin rates. It is noted that out-of-plane modal frequencies are invariant with spin rate; this is due to the coriolis forces and centrifugal forces not coupling these associated motions. The in-plane modal frequencies are seen to be significantly influenced by spin rate. The zero spin frequency of mode No. 3, whose zero spin natural frequency is nearest to the highest spin frequency considered, is reduced considerably (15%) at  $\Omega$ = 12 RPM. It is to be emphasized that the membrane (strip) tension was considered invariant for all spin rates considered and corresponded to the LMSC average tension specified for 4 RPM. Higher spin rates would decrease this average tension, thereby further reducing frequency.

It is noted that the fundamental mode frequency obtained by the NASTRAN program is significantly different than obtained by the JPL program and cannot be explained at this time. Dr. K. K. Gupta of JPL (private communications) relates the numerical accuracies afforded by digital computers are not sufficient to accurately obtain this modal frequency by the "Givens" eigenvalue-eigenvector extraction method, contained in the NASTRAN program.

#### 5.3 **REFERENCES**

- Ref. 5.1 Rosen, Richard, "STARDYNE User's Manual", Mechanics Research, Inc. Document, Los Angeles, California, January, 1970.
- Ref. 5.2 "Proposal for Large Space Station Solar Array Technology Evaluation Program - Vol. I.", LMSC A96774, Lockheed Missile and Space Company Report.
- Ref. 5.3 Coyner, J. V. and Ross, R. G., "Analysis of Performance Characteristics and Weight Variations of Large Area Roll-Up Solar Arrays", 69-WA/Ener-11, paper presented at the ASME Winter Annual Meeting, Nov. 16-20, 1969, Los Angeles, California.
- Ref. 5.4 Martin, H. C., "On the Derivation of Stiffness Matrices for the Analysis of Large Deflection and Stability Problems," Proceedings on Conference, <u>Matrix Methods in Structural</u> Mechanics, AFFDL-TR-66-80, October, 1965.
- Ref. 5.5 "Quarterly Report No. 3, Rollup Subsolar Array", General Electric Company Report No. GE-SSO-69SD4373, December 15, 1969.
- Ref. 5.6"Third Quarterly Report Large Area Solar Array", TheBoeing Company Report No. D2-113355-3, July 1967.
- Ref. 5.7 "Modular Space Station-Phase B Extension, First Quarterly Review", North American Rockwell, Space Division, PDS-71-2, May 1971.
- Ref. 5.8
  K. K. Gupta, "Eigenvalues of (B A*) Y=O with Positive Definite Band Symmetric B and Band Hermitian A* and its Application to Natural Frequency Analysis of Flexible Space Vehicles, "Space Program Summary 37-60, Volume 3, Jet Propulsion Lab, Pasadena, California, December 1969.

- Ref. 5.9 K. K. Gupta, "Free Vibration Analysis of Spinning Structural Systems," International Journal for Numerical Methods in Engineering, to be published.
- Ref. 5.10Patel, J. A., and Seltzer, S. M., "Complex EigenvalueSolution to a Spinning Skylab Problem, "NASTRAN: USERSEXPERIENCES, NASA TMX-2378, September 1971.
- Ref. 5.11 "The NASTRAN Users Manual, "NASA SP-222, Section 3-4, 1970, Office of Technology Utilization, NASA, Washington, D. C.

#### 6. SIMULATION VERIFICATION ANALYSIS

Various simplified analyses were performed to verify the formulated interactions computer program and contained methodology. These analyses were divided into two parts--one part to verify the structural dynamics methodology used (Reference 6-1) and to gain some insight into the accuracy of this methodology, and the other part to verify the various subroutines or subprograms contained within the simulation.

#### 6.1 STRUCTURAL DYNAMICS VERIFICATION

## 6.1.1 SIMULATION OF FLEXIBLE APPENDAGES & RIGID SPACE STATION

A planar problem considering a structural arrangement of two uniform beams representing flexible appendages and connected to a rigid space station mass (taken to be zero) was formulated and analyzed for interaction (interface) forces caused by an applied step force. The closed form solution to this problem is presented in Reference 6-2 when using a finite number of orthogonal cantilever modes as flexible appendage degrees-offreedom. As represented in the simulation program, this structural arrangement of two cantilevers simulates a free-free beam (Figure 6-1).





An orthogonalization of the coupled motion equations of the two cantilever beams (appendages), which are formulated within the simulation from the input data, produces the comparisons shown in Figure  $6^{-2}$  and Table 6-1. Figure 6-2 presents the comparison of the resulting orthogonal deflection shapes using three cantilever mode degrees-of-freedom for each beam appendage and theoretical free-free beam shapes obtained from Reference 6.3.

#### TABLE 6-1

Frequency Comparison of (Uniform Beam) Cantilever + Rigid Body Mode Representation of a Free-Free Uniform Beam

Reference Frequency Ratios		Calculated Coupled Mode Frequency Ratios					
Symmetric Mode No., n 1	Free- Free Beam 1.000	Uncoupled Canti- lever Beam 0. 632	1 Mode Canti- lever Beam + Rigid Body 1,0101	2 Mode Canti- lever Beam + Rigid Body 1.0006	3 Mode Canti- lever Beam + Rigid Body 1,0003	4 Mode Canti- lever Beam + Rigid Body 1,0000	5 Mode Canti- lever Beam + Rigid Body 1.0000
2	5.404	3.958		5.548	5.420	5,408	5.405
3	13.344	11,074			13.749	13,410	13.367
4	24, 814	21.652	,			25, 584	24, 965
δ	39. 812	35.861					41.030

Frequency Ratio	s: f /t	free-free
-----------------	---------	-----------

Table 6-1 presents the comparison of resulting frequencies using a varied number of cantilever mode degrees of freedom for each beam appendage with theoretical free-free beam frequencies.

These comparisons show the adequacy of the structural dynamics methodology that has been used in the interactions simulation; the degree of accuracy in the approximation is seen to be dependent upon the number of cantilever modes used. Transient load responses were obtained for this structural system using the formulated computer program with all control

systems inactive. Each of the cantilever beam modes was input into the program by modal descriptions of 25 discrete mass points representing 50 inertial degrees of freedom. A step force was applied at the zero-mass space station C.G. The shear force at the 1/4 span of the free-free arrangement, as obtained by the simulation, is compared with results obtained by Reference 6.4 in Figure 6-3. The entire free-free structural configuration (2 connected cantilevers) was modeled by 40 discrete mass points for input into the "direct transient method" of Reference 6.4. Comparisons are seen to be good, and as expected, higher frequency transients result in the force history obtained by Reference 6.4 since all system modes of vibration are represented. Another comparison is provided for the simulation results in Reference 6.2 and reproduced in Figure 6-4. A variable order Adams numerical integration method and the first five symmetric free-free beam modes were used to obtain the 1/4span shear force resulting from a step input. Again, the comparison shows the simulation results to be very comparable.

## 6.1.2 SIMULATION OF RIGID APPENDAGES AND RIGID SPACE STATION

A simple planar problem was formulated to show verification of the rigid body dynamics solutions given by the simulation. This formulation consisted of two simulated rigid appendages connected to a simulated rigid space station and perturbed by a step force. The resulting appendage interaction forces and moments given by the simulation are compared to the exact result in Figure 6-5.

## 6.1.3 SIMULATION OF FLEXIBLE APPENDAGES AND FLEXIBLE SPACE STATION

A planar problem was formulated for verification purposes and consisted of three uniform beams forming a "T" arrangement (Figure 6-6). This arrangement is representative of a flexible center body (space station) and two flexible appendages (solar arrays). Stiffness and mass properties of each beam were chosen so that the center beam had an uncoupled fundamental free-free axial deflection mode frequency of 1 Hz and that the appendage beams had an

uncoupled fundamental cantilever bending frequency of 1 Hz. Initially, results were obtained from the simulation and by hand calculations using the same simulated methodology (Reference 6, 2) considering one cantilever mode of each flexible appendage and a rigid center body. Corresponding shear and moment interaction histories are presented in Figure 6-7. It is seen that the solutions are coincident at time zero but are slightly different in amplitude and phase. This is attributable to integration interval used ( $\Delta t = 0.05$  sec.) together with the NASTRAN numerical integration algorithm (Reference 6.4) which is coded in the simulation computer program. Although not directly applicable to the above formulated problem, the variation of amplitude, frequency and phase errors with integration sample rate per cycle of the highest system frequency resulting from use of this algorithm, were determined for a five cantilever mode representation of the flexible appendages and are presented in A higher degree of required simulation solution accuracy than Figure 6-8. that shown in Figure 6-7 therefore requires the use of a smaller integration interval.

Several methods of obtaining interaction moment solutions of the formulated problem, with the flexibility of the center body included, were used and compared with the simulation results to show the adequacy of the methodology. These solutions, together with that obtained from the simulation program are presented in Figure 6-9. Modal solutions of the structural arrangement considered as a system were obtained by the transient response solution method provided in Reference 6.5 and an independent method utilizing a variable order Adams integration method. The results shown using system modes utilize one rigid body translational degree of freedom and the first four orthogonal elastic modes. Both the modal displacement and modal acceleration methods of load calculation were considered. A solution of interaction moment produced by a coupled system response, as given by the direct transient response method of NASTRAN, is also presented. The finite element model of the "T" beam for input for the above solutions is represented by a total of 79 discrete mass

points and complete description of this model and system mode results are given in Reference 6.6. The interaction moment of the "T" beam given by the simulation reflects the use of the first 10 free-free axial deflection modes of the center body and the first two cantilever modes of the flexible appendages. The results obtained by all of the methods compare very well and show the adequacy of the methodology contained in the simulation.

### 6.1.4 VERIFICATION OF COMPLEX EIGENVALUE-EIGENVECTOR ROUTINE (REFERENCES 6.7 AND 6.8)

As part of the study program effort, a computer program received from the Jet Propulsion Laboratory (References 6.7 and 6.8) and formulated by Dr. K. K. Gupta, was converted for operation on the CDC 6000 Series Computer. This program has the capability of solving for the orthogonal properties of a set of coupled second order equations having non-zero coefficients of the first derivatives of the time dependent variables, which are representative of a finite element structural model in a spinning environment. A simple uniform beam problem was formulated to verify the correctness of program conversion. The finite element model and results from both the converted program and the NASTRAN program, for a zero-spin condition, are shown in Table 6-2. The comparisons show both a comparable method of orthogonalization with the similar techniques of NASTRAN and the verification of the converted program.

#### 6.2 SUBPROGRAM VERIFICATION

The various subprograms comprising the complete digital simulation of the space station and solar arrays were verified for correctness of formulations by a number of program executions with simple structural arrangements and initializations. Each of the program executions was performed with the derived simulation of the first study phase which is described in References 6.9 and 6.10. This simulation considers the flexible dynamics of appendages and only the rigid body dynamics of the space station. The simulation resulting from the second study phase and described in Report Section 4 utilizes many of the same subprograms; and therefore, the performed subprogram verification is taken to be a partial verification of the Phase II digital simulation.

The total subprogram verification is represented by the following outline. Verification of each of the given program output quantities is made by comparison with hand computed results.

#### SYSTEM RIGID BODY MOTION

• Space Station Rigid Body Motion

X-, Y-, and Z- translations: due to a force input to space station  $\theta_X^-$ ,  $\theta_Y^-$ , and  $\theta_Z^-$  rotations: due to a force input to space station Disturbance force input variations for check of interpolation procedure

Location variation of disturbance force, {LR}

Solar Array Rigid Body Motion

Sun Vector Misalignment, {Sun} Initial Attitude Error {EULER (7)}, {EULER (8)} Solar Array Drive Selection {RBC (1)}, {RBC (2)}  $\theta_X$ - and  $\theta_{\overline{Z}}$  rotations: due to a force input to space station.

### SPACE STATION CONTROL DYNAMICS

- Response to Reaction Jet Control Torques
  Threshold not exceeded, i.e.,  $\theta_{\epsilon} < 1/2^{\circ}$  {EULER (1-6)}
  Threshold exceeded, i.e.,  $\theta_{\epsilon} > 1/2^{\circ}$ Variable SS guidance commands, {SSGTIME}, {DELTSSG}
- Response to CMG Control Torques

Threshold not exceeded, i.e.,  $T_{CMG_{REG'D}} < T_{CMG_{LIMIT}}$ {EULER (1-6)} Threshold exceeded, i.e.,  $T_{CMG_{REG'D}} > T_{CMG_{LIMIT}}$ {EULER (1-6)} Variable SS guidance commands, {SSGTIME}, {DELTSSG}

#### SOLAR ARRAY CONTROL DYNAMICS

#### Linear OCS Response

Solar Array Drive Gear-train variation, {GEARKON} Sun Vector Misalignment, {Sun} Initial Attitude Error, {EULER (7)}, {EULER (8)} Variable SA guidance commands, {SAGTIME}, {DELTSAG}

#### Non-Linear OCS Response

Solar Array Drive Gear-train variation,  $\{\text{GEARKON}\}$ Threshold not exceeded, i.e.,  $\theta_{\epsilon} < 5^{\circ}$ Threshold exceeded, i.e.,  $\theta_{\epsilon} > 5^{\circ}$  $\{\text{EULER (7-8)}\}$ 

Variable SA guidance commands,  $\{SAGTIME\}$ ,  $\{DELTSAG\}$ 

#### SYSTEM ELASTIC BODY MOTION

- Solar Array Modal Response, DEBUG (20) = . F.
  - Cantilever Dynamics,  $\{RBC(1) = .T.\}$ ,  $\{RBC(2) = .T.\}$ Pinned-joint Dynamics,  $\{RBC(1) = .F.\}$ ,  $\{RBC(2) = .F.\}$ Initial SA attitude error,  $\{EULER(7)\}$ ,  $\{EULER(8)\}$ Variable SA guidance commands,  $\{SAGTIME\}$ ,  $\{DELTSAG\}$

#### • Orbital Mechanics

Semi-major axis variation, {A} Orbit Eccentricity variation, {E} Orbit Inclination variation, {INC} Orbit Initialization point, {M}, {P}, {N}

The above bracketed quantities are variable names used in the various subprograms and are defined in Reference 6.9.

### 6.3 REFERENCES

- 6.1 "Dynamics and Control of Flexible Space Vehicles," P.W. Likens, NASA CR 105592.
- 6.2 "Integrated Dynamic Analysis of a Space Station, with Controllable Solar Arrays," J. A. Heinrichs, et al, paper presented at the 42nd Shock and Vibration Symposium.
- 6.3 D. Young and R. P. Felgar, Jr., "Tables of Characteristic Functions Representing Normal Modes of Vibration of A Beam," University of Texas Publication No. 4913, 1 July 1949.
- 6.4 "The NASTRAN Theoretical Manual," NASA-SP-221, Section 11.3, 1970., Office of Technology Utilization, NASA, Washington, D. C.
- 6.5 "The NASTRAN Users Manual," NASA SP-222, Sections 3.10 and 3.13, 1970., Office of Technology Utilization, NASA, Washington, D. C.
- 6.6 "The Study of Dynamic Interactions of Solar Cell Arrays with Space Stations and the Development of Solar Array Structural Requirements, "Fairchild Industries/FSED Monthly Progress Report for October 1971, NASA/LRC Contract NAS5-10155.
- 6.7 K. K. Gupta, "Eigenvalues of (B-λA^{*}) Y=0 with Positive Definite Band Symmetric B and Band Hermitian A^{*} and its Application to Natural Frequency Analysis of Flexible Space Vehicles, "Space Programs Summary 37-60, Volume 3, Jet Propulsion Lab, Pasadena, California, December 1969.
- 6.8 K. K. Gupta, "Free Vibration Analysis of Spinning Structural Systems," International Journal for Numerical Methods in Engineering, to be published.

- 6.9 "Solar Array-Space Station Dynamic Interaction Analysis, Digital Simulation Documentation Users Manual," prepared by Fairchild Hiller Corporation, SESD, February 26, 1971, under NASA/LRC Contract NAS5-10155.
- 6.10 "Interim Report, The Study of Dynamic Interactions of Solar Arrays with Space Stations and Development of Array Structural Requirements, "Fairchild Industries Report 858-1R-1, February 1971, Fairchild Industries, Germantown, Maryland.













0,5 ÷İ 0.4 Shear (lbs.) SIMULATION RESULTS 0.3 Moment (It-Ibs.) E 0.2 0.1 ñ 0.1 0.2 Time (sec.) MASS SPACE STATION = 1 slug MASS EACH SOLAR ARRAY = 0.5 slug 2 LB STEP INPUT 0.5 014 Shear (lbs.) EXACT Moment (ft - 166.) SOLUTIONS 0.3 0,2 0.1 0 0.1 0,2 Time (sec.) . . . ::: FIGURE 6-5. Interaction Shear and Moment 6-13 :

EUGENE DIETZGEN CO. MADE IN U. S. A.

> 340 -20 DIETZGEN GRAPH PAPER 20 X 20 PER INCH

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#### TABLE 6-2

## COMPARISON OF NASTRAN AND GUPTA EIGENVALUE SOLUTIONS FOR CANTILEVER BEAM





### FREQUENCY COMPARISON (RAD. /SEC.)

MODE	GUPTA	NASTRAN
1	55.5344	55.5349
2	357.7820	357.8042
. 3	1009.7656	1010.5280

### MODE SHAPE COMPARISON

POINT #	MODE 1		MODE 2		MODE 3	
	GUPTA	NASTRAN	GUPTA	NASTRAN	GUPTA	NASTRAN
- 1	0.0925	0.0925	-0.5052	0.5052	1.0000	1.0000
2	0.3281	0.3281	-1.0000	1.0000	0.3358	0.3389
3	0.6470	0.6470	-0.5438	0.5438	-0.9656	-0.9724
4	1.0000	1.0000	0.7265	-0.7266	0.4162	0.4270

6+18

►1<u>8</u>

#### APPENDIX A

This Appendix presents detailed vibration mode data which were derived for the space station and solar array structural configurations considered in Phase 2. Analytical data are presented for the structural configurations in both Zero "G" and Artifical "G" environments. Explanations of the presented data can be found in Report Section 5. The data are presented in the following appendix sections:

8	A.1 Zero "G" Space Station Configuration	page A-2
Ø	A.2 Zero "G" Roll-up Solar Array Configuration	page A-14
0	A.3 Artificial "G" Space Station Configuration	page A-36
0	A. 4 Artificial "G" Roll- up Solar Array Configuration	page A-65

## A.1 VIBRATION MODE DATA ZERO "G" SPACE STATION CONFIGURATION

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NOTE: Mode shapes shown are elastic mode shapes. Mode 1 in Figure A-2 is the first elastic mode, which corresponds to Mode 7 in Table A-1.

# Table A-1, Modal Data, Space Station

### (Zero G Configuration)

	Freque	ncy	Generalized Mass
Mode	(Hz)		(lbsec. 2/in.)
	(22-7)		
·			
1			6.281 2956 02
2	0.0 F	ligid Body	6.281594E 02
<u>.</u>	· · · · · · · · · · · · · · · · · · ·	Modes	6.2815945 22-
¢.	Ģ.●Ğ		2.773120 02
5	n 0 <b>°</b> ₀0 n _ n		1.2119915 02
6	0		1.2049918 02
7		15 00 T T T	2.2977175 02
8	20277007	C 00	3.636589E 01
9*		1217 <b>fr 0</b>	mm3.6600572:01:
10	3.147397	E 00	8.3732048 01
	3.245078	8 100 mm	1.0855638 02
12	A.391578	- C C	1.5118825 02
13	4683892	a oo	3.1245908 02 :
1 ^	5.702700	ຮ່ວວ	7.4392235 01
-15		**************************************	7.102155F 01
16	6-27757	= <u>00</u>	8.4515118 01
17	E	2000 2000	1 1117005 00
17	6 978705	- 00 - 00	1 1117005 00
10	0070093 		
19			
20	80453573	e 99 E 66	1.0006287E 32
21	8.850953	5 75	
22	8,935523	E 00	
23	1.013241	日 31	· .
24.	1.130443	Ξ 01	•
25	1.131781	田 01	•
26	1.475518	刊 21	
27	1.531728	E 01	
、28	1.958418	E 01	
29	- <b>1</b> .983515	E 01 👘	
30	2.277832	日 01	
31	2.319455	C C 1	
32	2.339781	E 01	· .
33	2.342052	E 01 m mm m	
36	2.490974	5 01	· .
76	2.57.719	F 21	•
36	2.658602	8 01	
- 30 - 37	2.60896A		· · · · · ·
ວ <i>1</i> ກວ	200-0-0-0-		
	20112139		· · ·
39	2.9%1.722		
- SC - 50	2.9%2130	- 11	
41	2.957257	7 01	
¢ 2	2.967250	E 01	
¢.3	2.977396	F 01	
44	2.984723	E <b>^1</b>	
° 45	<b>2</b> ₀98472€	E 01 - T	
46	2.992293	21	- · ·
47	3.003922	स. <b>७1</b>	•
<b>¢</b> 8	3.005589	F C1	
49	-3.005730	T 01	
50	3.027989	7 01	
-			· ·

A-3



A-4

# TABLE A - 2

### Listing of Mass - Geometry Data

## Of Zero G Space Station

NODE	NO.	MASS	x	Y	7
	1	16,189	150.	- 0,	-492 .
	Ζ.	16,189	150.	0.	492.
	3	16.189	120.	492.	0.
	4	- 16,189	120.	-492.	<b>0</b> • • • • • • • • • • • • • • • • • • •
	5	16.189	120.	0.	-372.
	6	16,189	120.	0.	372.
-	7	16,189	120.	372.	0.
	8	16,189	120.	-372.	0.
	9	16,189	150.	0.	-252.
	10	16.189	150.	0.	252.
	11	16,189	120.	252.	0.
	12	16.189	150.	-252.	0.
••	13	16,189	120.	0.	-132.
	14	16.189	120.	0.	132.
	15	16.189	150.	132.	0.
<i>.</i> .	16	16,189	120.	-132.	0.
	17	0.	120.	0.	-72.
	18	0.	120.	0.	72.
· · · · · · · · ·	19	0	120.		0 • • • • • • • • • • • • • • • • • • •
	20	0.	150.	-72.	0.
	51	8.1	120.	0.	0.
••• ·	55	8.1	60.	· O • · · ·	· () • · · · · · · · · · · · ·
	23	0.	180.	0.	0.
	24	4.05	0.	0.	0.
	25	16.189	360.	-492.	<b>0</b> • • • • • • •
	26	16.189	360.	-372.	0
	27	12.15	300.	0.	0.
	28	16.189	360.	-252.	0.
	29	16.189	360.	-132.	0.
	30	0.	360.	-72.	0.
·· -	-31	8.1 -	360.	0	. 🗛 📲 🖏 🛶 🗤 🗤 👘
	32	12.15	360.	72.	0.
	33	0.	360.	0.	72.
	34	0.	360.	0	-72.
	35	8.1	420.	0.	0.
	36	16.189	360.	132 •	0, •
	-37-	16.189	360.	0.	
	38	16.189	360.	0.	-132.
	39	12.7919	480.	0.	0.
	40	16.189	360.	252.	0.
	41	16.189	360.	0.	252.
	42	16.189	360.	<u>0</u> •	-252.
	43	17.4839	700.5	0.	0.
	44	16.189	360.	372.	∩ <b>.</b>
	45	16.189	360.	0.	372.
•• •• • •	46	16.189	360.	0.	-372.
	47	19.086	951.	0.	Λ.
	48	16.189	360.	492 •	0.
-	49	16.189	360.	<b>0</b> • • • • •	492.
	50	16.189	360.	0.	-492.
		2 /	•		
× - Mas	s uni	ts are lb-sec ⁻ /	in. ∴∧ ⊏		-
			A-0		





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×

A-7

<del>∫</del> = 2.28 Hε

Figure A-3

Mode 2 Space Station.





A-9

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A-10



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A-12



A-13
# A.2 VIBRATION MODE DATA ZERO "G" ROLLUP SOLAR ARRAY CONFIGURATION

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1

	Frequency	Generalized Mass
Mode	(Hz)	(lbsec. ² /in.)
	مى	
	9.7373722-02	1.350/13E 00
2	1.035253E=01	6.2/4160E-01
	1.035253E-01	4.967223E-01
4 .	1.0352532-01	6.0005712-01
5	1.035253E-01	6.9348C7E-01
6	1.837441E-01	1.405378E 00
7	1.99999522-01	9.246593E-01
8	<b>1.</b> 9999556 <b>-01</b>	8.365354E-01
g	1.9999552-01	9.231566E-C1
10	1.9099552-01	8.366C65E-01
	2.654166E-01	1.456272E 00
12	2.328362E-01	6.936469E-01
13	2.623363E-01	6.273965E-01
14	2•020363E-01	6.923639E-01
	2.8293535-01	6.274614E-C1
16	3.237091E-01	1.832071E GO
10	3.454023E-01	9.248542E-01
18	3.4640256-01	8.365350E-01
+0 10	3.4640252-01	9.231666E-01
19	3.4640258-01	8.366C50E-C1
<u> </u>	3.0122376-01	1.765825E 00 _
21	3.6635155-01	6.936590E-01
<u> </u>	3.003016E-01	4.845103E-01
23	3.8635182-01	5.731879E-01
24	3.0030108-01	5.045E6dE-01
25	3.8715596-01	1.503639E 00
20	5.941957E-01	8.893200E-01
27	2.523427E 00	1.298081E-C1
28	3.1978236 00	8.005888E-C1
29	3.495915E 00	7.669923E-01
30	3.523140E 00	6.305750E-01
31	3.528254E 00	6.6C7162E-01
32	4.353931F 00	1.495981E-01
33	6.507502E 00	4.5711426-01
34	6.9314338 00	2.305118E-01
35	9.2977576 00	8.740416E-01
36		7.663497E-01
37	1.015473E 01	6.2931636-01
38		6-667687E-C1
40		
41	1.200002E C1	4.911662E-01 7.353544E-01
42		
43	1 - 001-00 01 1 - 001-00 01	1036000-01
44		C.133050E-01
45	1.501517E 91	0.539617E-01
46	1.772331E 01	I.UYEE66E 00
47	1.334437E 01	4.0044658-01
48	1.965033E 01	7.0087E5E-01
49	2.091042E 01	7-5311232-01
50	2.056432E 01	6.381914E-01

Table A-4, Modal Data, Solar Array, Inplane, Symmetric, Zero G

	Frequency	Generalized Mass
Mode	(Hz)	(lbsec. $2/in.$ )
	1.035250E-01	6.471123E-01
2	1.035251E-01	6.662618E-01
3 .	1+035252E-01	7.732370E-01
4	1.0352535-01	3.702315E-01
5	1.035319E-01	5.658236E-01
6	1.999946E-01	8.627804E-01
. 7	1.999952E-01	8.883575E-01
8	1•999952E-01	6.1976785-01
9	1 • 9999 52E- 01	8.961747E-01
10	1.999955E-01	6.240916E-01
- 11	2.828338E-01	6.471033E-01
12	2.828356E-01	4.734812E-01
13	2.828363E-01	6.5365395-01
14	2.828363E-01	6.072990E-01
15	2.828363E-01	6.702858E-01
16	3.464020E-01	8.6280035-01
17	3.464025E-01	1.045781E 00
18	3.464025E-01	7.491596E-01
19	3.464026E-01	6.347124E-01
20	3.464026E-01	8.882823E-01
21	3.863617E-01	. 6.470776E-01
22	3.863618E-01	- 7.813119E-01
23	3.863618E-01	5.618995E-01
24	3.863618E-01	4.768397E-01
25	3.863618E-01	6.663127E-01
26	1.354412E 00	7.051653E-01
- 27	3.278625E 00	7.702565E-01
28	3.490318E 00	6.074610E-01
29	3.519975E 00	5.617070E-01
30	3.527668E 00	6.061066E-01
31	6.072317E 00	1.035868E-01
32	6.882595E 00	4.122061E-01
<b></b>	9.511100E 00	8.556120E-01
34	1.007151E 01	6.032084E-01
- 35	1.014669E 01	5.632485E-01
36	1.016592E 01	6.006349E-01
37	1.280494E 01	4.3430822-01
38	1.518822E 01	7.910441E-01
	1.590481E 01	5.698990E-01
40	1.599190E 01	5.694355E-01
41	1.601352E 01	5.922735E-01
42	1.783336E 01	5.2830895-01
43	1.987668E 01	8.288176E-01
44	2.049608E 01	5.615127E-01
45	2.055783E 01	5.868033E-01
46	2.057259E 01	5.877689E-01
	2.154462E 01	4.647811E-01
48	2.300127E 01	1.731334E-01
. 49	2.315868E 01	6.691886E-01
50	2.344269E 01	5.389919E-01

÷

Table A-5, Modal Data, Solar Array, Out of Plane, Symmetric, Zero G

	Frequency	Generalized Mass
Mode	(Hz)	$(lbsec.^{2}/in.)$
1	9.244967E-12	1.3633555 00
2	1.225 55E-F1	4.851304E-01
	227098E- 1	5.9565235-21
4	1-227105E-01	5.221769E-01
5	1.227164E-01	5.439427E-01
6	1-866132E- 1	1.301536E DD
. 7	2.3354925-1	4.7387685-31
8	2.338332E-01	6.763698E-01
	2.338462E-^1	5.8732302-01
10	2.338475E-01	5.149174E-01
	2.723567E-71	
12	3.224235E-01	4.7559822-01
. 1.3	3•226471E-11	6.820915E-31
14	3.226523E-*1	5.9249002-01
	3.226532E-01	5.1949275-01
16	3.411543E1	1.341820E CO
. <b>17</b>	3.802172E-01	4.683117E-C1
18	3-8%5961E-01	6.7765435-11
. 19.	3.8%(9812-11	5.8885575-71
20	-3-8(+934E-11	5.163653E-71
		1.156975E 00
22		1.581258E-71
	1.6210372E 99.	2.4104505-01
24	1.621616E 00	2.41(4)9E-01
20 26	1.6217575 (.3	2.2006145-01
20	1.6198965 00	1-406597=-01
28	2.2737745 00	1.1058965-01
20	3.660591E 00	1-346217E-^1
30230	5.304781E CC	1.555309F-01
31	1.037197E 01	1.700534E-01
32	1+150986E 01	2.3811825-01
		1.640180E-01
34	2.536168E 01	2.053636E-01
	2.451262E 01	.1.4795495-01
36	3.032007E 01	2.375647E-C1
	. 5.002257E .01	1.6820475-01
38	5.146941E 01	1.8004582-01
_39	7.553278E 11	1.761178=-11
46	9.195334E 11	1.597598E-C1
41	_1.138354E \$2	6.968695E-12
42	1.408619E C2	9.4822765-22
		• •

A-17

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Table A-6, Modal Data, Solar Array, Out of Plane, Antisymmetric, Zero G

	Frequency	Generalized Mass
Mode	(Hz)	(lbsec. 2 /in.)
	<u>5.399534E-02</u>	6.093149E-01
2	1.2259122-01	6.959703E-01
3	1.2270310-01	7.329165E-01-
4	1.2271028-01	6.202382E-01
······ 5, ····	102271065-01	0.423883E-01
6	1.6678028-01	5.472140E-01
7	2:3330422-01	6-814334E-01
9	2.3334455-01	7.183616E-01
	2.3334750-01	6.1823985-01
10	2.3384322-01	6.3340282-01
11	2.4131855-01	5.890857E-01
12	. 3.084885H <b>−01</b>	7.381489E-01
13	302252345-01	6.943066E-01
14	3.2265127-01	7.345921E-01
15	3.2265357-01	6.107412E-01
16	3.2265385-01	6.392808E-01
17	3.531117E-01	5.835944E-01
18	3-800878t-u1	6.890357E-01
19	3.8039755-01	7.275511E-01
20	3.800982E-01	6.101235E-01
21	3.8709842-01	6.354181E-01
22	3.8902882-01	5•942361E-01
23	1.011542E 00	2.52.251E-01
24	1.0208902 00	2.669843E-01
25	1.021528E 00	2.242702E-01
26	1.0217538 00	2.333972E-01
27	T.58%146E CJ	2.103242E-01
28	< 8.2251.00E 00	1.584330E-01
29	1.0544825 C1	1.610069E-01
30	2.5148718 31	2.J37958E-01
31	3。今72条5条形 01	20118104E-01
32	5·3338148 01	1.683161E-01
33	E.9351612 01	1.759176E-01
34	8•2937888 01	1.8142315-01
35	1.0823255 32	1.893509E-01





### Mass - Geometry Data

Of Zero G Solar Array

		• •		
NODE NO.	иетент(1	bs.)X	Y	<u>Z</u>
1	21.48	1056.	347.	0.
<u> </u>	3 <u>2.3</u> .4	888.	347 .	···· 0 •·····
3	26 06	1056.	275.	Λ.
4	32:3	720,	347.	0.
5		888.		·····
6	26.06	1056.	203.	Λ.
7	32.3	552.	347.	Λ.
<u>8</u>	· · · <u>32.3</u> ····		275	····· •••
9	32.3	888.	S03•	Ο.
<u>1</u> 0	26.06	1056.	131.	0.
			347 • -	0
12	32.3	552.	275.	0.
13	32.3	720,	503.	Λ.
	35.3			·····
15	25.32	1056.	59.	0.
16	32.3	216.	347.	Λ.
17			275.	··· 0 •···
18	32,3	552.	503.	Λ.
19	35.3	720.	131.	Λ.
<u>S</u> U	-35•3 -	- 888.		····· 0 ••
51	12.74	1056.	0.	0.
22	20.84	48.	347.	0.
	- 32.3	216	275	·····
24	32.3	384,	503.	0.
25	32.3	552.	131.	0.
	-32.3	720		·
27	17.81	888.	0.	n•
28	24.98	48.	275.	0.
29	32.3	216.	203.	··· () •····-
30	32.3	384 •	131.	0.
31	32.3	552.	59.	0.
	17.81	/20 •	0.0.	·····() •··- ··
55	24.98	48.	203.	
34	36.3	216.	1.31.	P.
······································	37.3	384	· · · · · ·	0.
- 36	- 17,01	752.	0.	0.
.57	24.98	48. 01.	131.	U.
··	3C • 3 17 01	216	57• ·	····· () • · ···
39	17.01	3H4 •	0.	U.
40	24,23	48.	54.	€F ●
4]	17.31	<10. ( )	·· •	0.
42	12,30	4ו	0.	
43	U 🖕	U .	U .	- + F •

NOTE: Weights along the boom (Y = 0.) are

one half the actual weight.

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Mode 26 String Solar Array, In Plane Symmetric



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Force Modal Participation

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Figure A-14 Mode 31 Solar Array, In Plane Symmetric



# Figure A-15 Mode

Mode 1 String Solar Array, In Plane Antisymmetric



Mode 6 String Solar Array, In Plane Antisymmetric





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Mode 11 String Solar Array, In Plane Antisymmetric

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Mode 16 String Solar Array, In Plane Antisymmetric



Mode 27 String Solar Array, In Plane Antisymmetric

A-29

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Mode 6 String Solar Array, Out of Plane Symmetric



Mode 22 String Solar Array, Out of Plane, Symmetric



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Figure A-23 Mode 1 Solar Array, Out of Plane, Antiaymmetric



# Figure A-24 Mode 6 String Solar Array, Out of Plane, Antisymmetric

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Mode 11 String Solar Array, Out of Plane, Antisymmetric

### A.3 VIBRATION MODE DATA

# ARTIFICIAL "G" SPACE STATION CONFIGURATION

CO	ΟN	ΤE	EN I	ГS
		_		

TABLES

#### PAGE

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A-9	Mass-Geometry Data	<b>A-3</b> 9
A-10	Structural Model Data	A-46
A-11	Coriolis Force Matrix	A-47
A-12	Centrifugal Force Matrix	A-48

#### FIGURES

A-26	Structural Model	A-38	
A-27 ^{to} A-32	Mode Shapes of First Six Elastic Modes (NASTRAN Results)	A-40 _{to}	A-45

NOTE: Mode 1 shown in Figure A-27 is the first elastic mode and corresponds to Mode 7 of Table A-8.

Computer Listings of	JPL Eigenvalue-Eigenvector	A-49
Modes	Program Results for Spin Rates of 0, 4, 8, and 12 RPM. The	
	numbers and their corresponding node number are described in Table A-10.	

TABLE A-8 MODAL DATA ARTIFICIAL "G" SPACE STATION CONFIGURATIC

ZERO SPIN, NASTRAN RESULTS

MODE	FREQUENCY	GENERALIZED MASS
	(*****)	$(BS-SEC^2/IN)$
•	A-2213426-(3) Diata	2.87450.)E 02
1	13 6 26-14 Rigio	
5	Body	
3 -	Mode	
4	5.8528732-1.3	101028892 02
5	761582652-96	1.794931E 02
£	8,5139522-55/	1.5727738 01
··· 7.	252957292 00	8.672661E
8	<b>≮</b> ∋27°3392 (€)	5.8685595 90
	-8642-20VE-00	-7•261933E 00
10	8.578633E III	7.816177E 01
• •	1.4379-76-51	7.559761- 01
11	1.25/3785 11	7-4825015 23
12		
1.3		4900000 M
15	10/331002 /1	190189545 01
·1.5.	20160903E 01	2,9240605 03
16	2,7957412 (1	5.702883E 01
17	357313322 01	2.432465E 05
18	3,2813322 .1.	6.314181E 0¢
19.	3.3°( 37)E 01	7.612518E ^1
20	32-01-2-01	1.1491875 02
21	5-9221-3F (1)	1 . 977763E 00
		1-8501325 00
22		7.6709745 07
23		
21	502189272 /1	30518303E U1
25	E. 529 %74E 21 ··	302033258 00
26	55711957 <u>1</u> 01	3.315745E 20
-2-7	€,072257± 01	8.26CA58E 02
28	E 3 3 3 1 7 2 9 E - 0 1 - 1	109694038 01
29-	E:3399555E 1	1.996732E 04
30	Es 770B262 1	5.345604E-01
31	7 of # 1739£ 11	
30	7.5385275 1	
22	A.3A72137	
30		
35-	2022/222	
36	9311337DL 01	
37-	9-1253275 1	ʻ.
38	シッさらし し21 1	:
	9.736 HOOE 01	:
<b>40</b>	10)255302 22	,
41	15.37150E 22	
A 9	1.5 23:11 2	:
A 7		
0.0		
A5-	4.5195352 22	· · · · · · · · · · · · · · · · · · ·
16	4,27235.2 22	
A. 7.	152173132	:
<b>≜</b> 8	15283130E 2	
· <b># 9</b> -	1,247-192 22	
50	1.6731215 2	
,*		: :
	Λ_97	
	8=0/	



# MASS - GEOMETRY DATA FOR ARTIFICIAL 'G' SPACE STATION

Node	Mass	<u> </u>	<u>Y</u>	<u>Z</u>
1	21.578	120.	492.	.0
2	21.578	120.	-492.	.0
3	21.578	120.	312.	• 0
4 :	21.578	120.	-312.	•.0
5	21.578	120.	132.	• 0
6	21.578	120.	-132.	• 0
. 7	0.	120.	72.	•0
8	0.	120.	-72.	• 0
9	15.382	120.	• 0	• 0
10	8.094	60.	• 0	• 0
11	4.047	•0	• 0	• 0
12	17.814	270.	• 0	•0
13	15.379	420.	• 0	•0
14	12.795	480.	• 0	•0
15	10.632	552.	• 0	•0
16	25.952	921.0	• 0	•0
17	.01295	1290.	• 0	•0

Mass units are lb-sec²/in.





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FIGURE A-30 ARTIFICIAL "G" SPACE STATION MODE 4 FREQ. = 8, 6 8 Hz ZERO SPIN

A-43

N

 $\times$ 

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# ARTIFICIAL "G" SPACE STATION

### FINITE ELEMENT MODEL DATA

NODE	MASS LB SEC ² /IN	IN LB	NERTIA SEC ²	IN	NO. OF STRUCTURAL D. O. F.	D.O.F. SEQUENCE NO.
		x Axis	y Axis	z Axis		
1	21.578		66641		6	1-6
2	21.578		66641		6	7-12
3	21.578		66641		6	13-18
4	21.578		66641		6	19-24
5	21.578		66641		6	25-30
6	21.578		66641	·	6	31-36
7			<del>.</del> -		6	37-42
8	<b></b> '			<b>-</b> - '	6	43-48
9	15.382	41621			6	49-54
10	8.094	21886			6	55-60
11	4.047	10956			6	61-66
12	17.814	49417			6	67-72
13	15.379	41595			. 6	7 <i>3 -</i> 78
14	12.795	18700			6	79-84
15	10.632	9350			6	85-90
16	25.952	20642			6	91-96
17	.01295	10.282			6	97-102

#### CORIOLIS FORCE MATRIX

### (NORMALIZED TO $\Omega$ )

*			
D. O. F.			
Sequence No.			
1 - 3	-43-15581	0.	0.
1 0	0-	0.	0.
4 - b	-43, 15581	0.	0.
etc.	0.	0.	0.
	-43,15581	0.	0.
	0.	0.	0.
	-43.15581	0.	0.
	0.	0.	0.
	-43.15581	0.	0.
	0.	0.	0.
	-43.15581	0.	ο.
	0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	-30.76417	0.	0.
	-41621.02691	0.	0.
	-16.18755	0.	0.
	-21885.53002	Q •	0.
	-8.09377	0.	0.
	-10955.20496	· O •	0.
	-35.62841	Q •	0.
	-49417.88198	0.	0.
	-30.75889	0.	0.
	-41595.14699	0.	0.
	-25.49926	Q •	0.
	-18699.30020	0.	0.
	-21.26381	0.	0.
,	-9349.65010	0.	0.
	-51.90365	0.	0.
	-20642.29399	0.	0.
	-0.02588	.0 •	0.
100 - 102	-10.28432	. 0 •	Ο.
		1. s	
		· .	

* - Refer to Table A-10 for corresponding node number.

ł

# CENTRIFUGAL FORCE MATRIX (NORMALIZED TO $\sigma^2$ )

D. O. F. Sequence No.

1 - 3	-21.57791	-21.57791	0.
4 - 6	0.	0.	0.
	-21.57791	-21.57791	0.
etc.	0.	0.	0.
	-21.57791	-21.57791	0.
	0.	0.	- 0.
	-21.57791	-21.57791	0.
	0.	0.	0.
	-21.57791	-21.57791	0.
	0.	0.	0.
	-21.57791	-21.57791	0.
	0•	0.	0.
	0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	-15.38208	-15.38208	0.
	0.	0.	0.
	-8.09375	-8.09375	0.
	0.	0.	0.
	-4.04687	-4.04687	0.
	0.	0.	0.
	-17.81401	-17.81401	0.
	0.	0.	0.
	-15.37949	-15.37949	0.
	0.	0.	0.
	-12.79468	-12.79468	0.
	0.	0.	0.
	-10.63191	-10.63191	0.
	0•	0.	0.
	-25.95188	-25.95188	0.
	0.	0.	0.
	-0.01294	-0.01294	0.
100 - 102	0.	0.	0.

* - Refer to Table A-10 for corresponding node number.

_ ≡°υΝ 1υθα αυσ αυ1ΟσΛιόζίς

Mode 1. Frequency = 2.2948 Hz,  $\mathcal{I}$  = 0 RPM

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A 2 2 2 2	بة إيارة	1471°1 =	aa456 02 (rad/	sec.)			,		
c 173:	1924		·						
-		7	J.2895F 00	-0.3391F-01	-0.7647E-05	-1.3272E-08	10-35362-0-	-0.6066E-03	-0.2895E 00
n	42	14	-7.3385F-01	-U-16495-05	0.3240ε-ηθ	-0-35305-07	-0 <b>.</b> 63~5 ² -33	0.1806F 03	-0.3380E-01
15	ç	21	-0-10755-05	-0°2386E-06	-u-2040F-n7	-0-9012E-03	00 g⊋_s1°C-	-0.3382F-01	-0.7080E-05
5	r +	a .	<b>0.2973F-08</b>	-0-2949E-07	-0.5012F-03	1C-joc21v	10-37282.0-	-0.6619E-05	-0.19126-08
د2	1	35	-0-36902-01	-0.58015-03	-0.7379E-01	-0.33756-01	-1.65245-05	0.1931F-08	-0.2943E-07
3 ĉ	¢. ₩	47	-0.5801E-03	10-34765.n	-0-3370F-01	-0.6533E-05	6C-3cc04°0-	-0.29376-07	-0.5605E-03
43	5	40	-0.39755-01	-0-311Er01	-0.6537F-05	0.93725-09	-0.2937E-37	-0.5605E-03	-0.4130E-05
5.	¢ F	55	-1.3366F-01	-0.6501E-35	0.2631E-10	-0.29335-37	-0°542 s£-33	-0.41455-05	-0.1091F-02
5.7	L L	53	ラリーゴラドくだ。シー	0.2637E-10	-0.78645-07	54296-33	-3.41635-05	0.31495-01	-0-99456-05
* *	C F	77	い。アちょごドーし	-0.78415-37	-7.54305-03	-1-42325-35	10-22196-0-	-0.21196-05	0.2681E-10
11	¢. ►	• •	-0.2079E-07	-0-2682F-03	-0-43175-05	-0.1158F 00	9-25225-15	0.2717F-10	-0.2598E-07
n. F	5	44	-0°570rF-04	-0-4351E-75	-0.1133E JD	0.3476E-05	01-325-20	-1.2240E-07	0.1116E-03
5 c	C) F	le	-0.4301F-05	-0-32 E 0b *0-	0.4293E-05	0.27475-10	66-32521-0-	1.5425F-03	-0.4533E-05
Ĵ	۲.	٥b	1.3722E nr	-0, 2061E-75	0.29026-10	0.52205-07	<b>0.15455-02</b>	-0.4559F-05	0.1000f 01
C.	4	192	-0.2739F-94	0.29265-10	0.48765-07	1.1729F-D7			
いしじゃん	1 7945	P 4 8 T							
1	5	~	0.0	0.0	0.0	0.0	0.0	0.0	0.0
a	C ⊨	- 14	U.*U	0.0	0.0	Ú•0	0-0	0-0	0.0
15	C P	12	0.0	0° u	0.0	0°0	C.0	0.0	0-0
22	۲)	28	0.0	0°U	0.0	0.0	0.0	0.0	0.0
د2	4 7	35	0.0	0-0	0.0	0°ù	0-0	0-0	. 0.0
3 S	C F	42	0.0	0.0	0° U	0-0	0.0	0.0	0.0
£ 3	4	¢ 0	0°0	0.0	0-0	0-0	0-0	0.0	0-0
ŝ	10	56	0.0	0.0	0.0	0.0	C • 0	0.0	0-0
57	5	63	0°0	0.0	0-0	0.0	L°U	0.0	0-0
64	5	70	0.0	0.0	0°U	0.0	0.0	0.0	0.0
11	C L	77	0-0	0.0	0.0	0-0	0.0	0.0	0-0
÷۲	10	34	0°0	0.0	0.0	0-0	0-0	0.0	0.0
ê5	12	۱٥	0.0	0-0	0.0	0-0	0.0	0.0	0.0
2 c	Ę	94	0-0	0-0	0.0	0.0	0-0	0-0	0-0
60	¢,	132	0.0	0-0	0-0	0-0			

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פנטנֿיוֹ∧ננעוט נוש מווע יויי=

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Mode 2, Frequency 4.2027 Hz, **L** = 0 RPM

/sec
(rad
ĉ
3-38408382
=invalue=

	VALUTE	- + G - + C	Lad the lead	sec. )					
1100	PART								
<b>"</b> . 1	۲.	7	3	<b>0.12555-35</b>	-1.489°F-31	-1.510RE-04	2-1-16-11-0-	3.9347F-08	0.4023E-05
n	1.	14	- 1 2 5 4 5 5	*****	<b>1.51715-74</b>	-0.11695-32	0.93515420	-3.23605-05	0.1250E-05
÷.	Ĺ	12	lu-jesti"	-J*422t-U4	-1.11645-32	<b>0_9</b> 067F-3R	0.27535-55	1.1250E-05	-3-3986E-01
22	C. 1	79	- 4 - 2 + 5 5	-0.11645-92	0.3470E-39	-J.9497E-26	0.1241210	-0.3262F-01	-0.3061E-04
(ř Pi	ÚΙ	ר. י	21-35511-2-	J.521F+∩9	0° 02002-08	<b>0-12415-05</b>	12-22425.0-	<b>30515-04</b>	-0.11555-02
55	C 1	4.2	a(-35631.5	-0-4265c-36	0.12356-75	-0.31245-01	-0.14755-54	-0.11486-02	0-6448E-08
r. . 1	•	40	ダビーコムをごちゃい	C.1275E-05	-0.3123F-01	0.1464E-34	-0.11425-22	J. 6449F-08	0.1108F-08
С ф	۲. ۲	5.6	らいーヨいをくしゃい	-0-3088F-01	-3.59145-37	-0.1142E-02	0.53245273	0.1174E-09	0.9062E-06
ي. ۲	L) L	53	11-51866"	-u-5639E-01	-0-1147E-02	Ú.5431€−08	°€-j≈621°0	<b>J.5816E-06</b>	-0.1683E 00
4	C L	70	-1.594ac-07	*114de-02	0.5416E-08	n.8202F-39	0.9325-25	<b>J.1309F 00</b>	-0.6062E-07
١.	C F	77	-2.22775-33	-j.8962F-08	0.5759E-09	-0.1216E-35	0.25945 73	-0-6226E-07	-0.7097E-03
n) r	11	4	としーコンカコ しゃいー	6C-jllo7°u	-0.2427E-05	0.2955E 30	-0.62355-77	-0.4901E-03	-0-2171E-07
ሆ 11	ر. ۲	lo	5.3745c-na	-3.37305-95	<b>1.</b> 3036E 30	-0.6412E-37	0.252:5-13	-0.1447E-07	0.4863E-10
¢:	c H	<b>b</b> C	50-32034	-n.2367F JA	-3.58695-17	0.2070F-02	0-30240	-3.7443E-10	-0.4029E-05
С 0	10	<i>c</i> ul	l. 30001°	-0-29898-01	0.705AF-02	0.9962E-12			
.127n]	VAPY D	<b>AR T</b>							
<b></b> 1	5	7	<b>C</b>	C-0	<b>u</b> -u	0.0	0-0	0.0	0.0
п	с, Н	14	<b>د</b> • ر	<b>c</b> •0	с.•с	0.0	0-0	0-0	0-0
۲ ۲	Ç. ►	21	¢. • •	<b>u</b> •0	0.0	0.0	0.0	0.0	0 0
2	C F	39	с. •	<b>0</b> "U	0° J	0-0	0.0	0.0	0 0
50	1Ü	35		0°ù	0°ú	0.0	0.0	0.0	0-0
5	1	4 2	€) <b>*</b> c	0°u	0.0	0.0	0.0	0.0	0.0
м. •3	Ę	49	<b>c</b> •	ú•ŭ	0.0	0.0	0-0	0.0	0.0
€ 5 ₩ 5	Ļ	56		<b>د •</b> 0	0-0	0-0	0.0	0-0	0-0
¥ -	C 1	63	· · ·	0-0	0.0	0.0	0.0	<b>J.</b> 0	0.0
<b>.+</b> -0	13	70	C.C.C	0.0	0.0	0.0	0-0	0.0	0-0
71	10	77	<b>c</b> •c	0.0	<b>0-</b> 0	0.0	0.0	0.0	0-0
er: P	C.	R4	<b>c</b> •0	0.0	. 6*6	0-0	0.0	0-0	0.0
η. Π	1Û	lb	0°0	c•c	0.0	0.0	0.0	0-0	0-0
ĉ	11	ĝĝ	<b>6</b> •0	9.0	0.0	0-0	0.0	0-0	0.0
<b>t</b> ::	C -	102	<b>c</b> • c	0.0	0.0	0.0			

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FIGENVECTOR FOR POOT NY.=

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A = 0 RPMMode 3. Frequency = 8.4224 Hz.

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32365 Pr 6 2 1 4
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o ت	1 . 70								
	-	:.	04 j€12!•L-	1		éC−325c5***	10-30665.N	2.37015-03	P.1213E 33
Ċ		.* .~•	10-38862°C	• • • • •		1, - 1000F - 17	n.37acc-13	-0.5551:-31	7.876F-01
15	1(,	12	0.4691F-06	1 . 51.52	16-20 02.02	-31515-03	1-15550	0-7874c-Cl	<b>7.4681F-0</b> 6
2		а. С.	-1.5356F-QB.		5 7 3 5 1 7 J 3	-J.69835-N2	0.75495-01	-0.3370F-05	0.3317E-09
5	£	<b>9</b>	<b>0.2859E-07</b>		05 - 05	0.76495-01	90-30166.0-	-0-3317E-0a	0.2859E-07
35	;- 	ny at	0.1840F-03	eu-selter.	· · · · · · · · ·	-1.48135-06	9.14475-28	0.2782F-07	0.5233F-04
¢ 7	, .	5 <b>1</b>		1-34052 :	いっ ういちょうけいけいじょ	80-36951-0-	1. 1.975.0	0.52336-04	12151 - 7 ÷
5 D	; _	5.5	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1		1.6284F-1	10-21622 1	÷ - : :29° : -	0.1219E-75	
•••	<b>C</b> )	<b>F</b> .	0.1114F 25	1	3.27615-37		0.121.55-00	0-82405-51	29-37775.0
64	C F	101	0.645813	TC 11 55 0	-3*16436-04	C.14648-36	-0*** -1**0-	-0.31165-05	0.51835-19
	Ļ10	7.7	0.92076-19	-7.134 -57	3.1591E-06	00 30162 0-	-0-30kch-15	21-3465.0	-0.8915E-08
70	5	34	-0.16605-72	90-26221 °C	-0.3767F 00	56	0.192 - Y-12	- 3, 115F-07	<pre>~ 14 78E -0 &gt;</pre>
<u>ຜ</u> . ເ	5	ο	1832F-94	C 22 . *		21-32231	AL GOLA ["U-	-0.46655-73	1.2329E-11
6	C. ;~	30		S. She h.	jue11•ù	dense, in the	J. 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	0.2257F-01	P.1000E CI
1	ú.	, I, I		سون					
1.2.2.3	1 1941	40							
-	10	2	0.0	0°J	0.0	0.0	0-0	0.0	0.0
or	C'	14	0-0	0.0	0 <b>.</b> J	0.0	0° U	0-0	0-0
15	c T	17	0-0	с <b>-</b> с	0• J	0.0	0.0	0.0	0.0
د در د	10	ů Č	с <b>-</b> с	0.0	0.0	0-0	0.0	0.0	0.0
53	C L	35	0-0	0°0	0-0	0-0	0.0	0.0	0.0
35	11	42	0.0	0.0	C-0	0-0	0-0	0.0	0-0
4	Ċ	49	0.0	C • O	0.0	0-0	0.0	0.0	0.0
50	C F	56	0.0	J.C	0.0	· 6•0	U-D	0.0	0-0
57	10	63	0.0	Ú°Ú	2°0	C"u	0.0	. 0.0	0-0
54	<b>C</b> '	10	0-0	0.0	0.0	0.0	0.0	0-0	0-0
7	10	77	0.0	0.0	0.0	0.0	0.0	0.0	0.0
78		84	0.7	0.0	0-0	0.0	0-0	0-0	0.0
2 80 1	Ū	10	0-0	0.0	0.0	0.0	0.0	0.0	0-0
26	70	9.8	0-0	0°0	0.0	0.0	0.0	0.0	0-0
66	10	102	0-0	0.0	0.0	0.0			

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Mode 4. Frequency = 8.6711 Hz, **J.** = 1 RFM

					·.				
f 1 G F 4	עלווב≃	: J. 544R	2422F 72 (rad/s	sec. )					
JEAL	PART								
~	L J	٢	-0.1000F 01	1405E-02	9-2-2-20	7.21725-09		3,37155-02	-0.9962F 00
er.	۲ c	14	0.1400E-02	-3.12385-75	0.12046-37	-1.24765-06		-J.3545E nJ	0-13776-02
15	1 L	21	0.35056-05	J. 72445-05	-0.24355-06	0-3377E-02		7.13745-02	0.8537F-06
22	1 >	9 ¢	r.10705-97		20-39162-0-	0.1479F 00		7.37125-75	0-3207F-08
53	1	35	-0.23545-06	6.20255-32	~ 1431E 00	0.1330F-02	<b>.</b>	).5631E-08	-0-23545-06
36	5	42	-0.20215-32	0.23255 30	2.134551.0	0.2874F-05		- 2- 22855 - 76	n.9289E-03
£3	C L	4.7	1.2324F nn	0.13945-02	0.27325-35	0.2382F-08	6	92795-03	0.2668E 00
53	c F	5.5	0.12905-02	0.29235-75	0.12746-39	-0.2238E-76		J.2593E 00	0.1366E-02
57	5	61	-0°]J785-74	0.13765-79	-0°22795-36	-0.14565-05		2. 1453E-02	-0.2442E-04
64	10	Ŭ <b>L</b>	<b>3.1324F-no</b>	-0.2272E-06	-).14455-35	0.3741E 00	5-33 · 5 · C -	1.2928E-04	0.1797F-09
11	C.		-n.12085-05	-0*5183er54	<b>1.</b> 455ac J1	-0.4428E-32		2.201E-09	0.1268F-07
a 4	L L	94	-0.2546E-34	<b>0.5046</b> F 30	-1.5=z=z-12	0-34125-04		J.9953E-07	-0.2106E-04
a a	Ū,	16	0.5547E 01	-0.66125-12	0.17425-34	0.29736-09	0 • 3 <u>6</u> • 5 <del>6</del> • 0	- 3. 2213F-06	0.7520E 00
0	t u	Я	0.3511E-02	-0-22142-02	0.45765-79	3.49195-76	7.75.45-24	<b>J.7509E 00</b>	0.6990F-02
60	(` ►	201	<b>20−30</b> €22°0-	0.52395-20	7.0-30-95-07	0.33795-06	4 4 •		
12221	4 7 5 6 V	Адт							
-	r F	7	0°0	с.•с	( • 6	0-0	, ,		0-0
<b>7</b>	ţ	14	0.0	ر • ر	, . , .	0.0			0.0
ч П	Ċ,	71	J• D	د. د		0.0		0.0	0-0
22	17	2 a	0.0	с• С	C • C	0.0		0.0	0-0
E.	-	35	0-0	0.7	0 <b>.</b>	0.0	Ċ	0.0	C • 0
35	C F	42	0.0	0.0	0.7	0.0		0.0	0.0
4	5	40	0.0	с <b>.</b> С	۲. ۲.	0.0		0.0	0.0
ŝ	C -	56	0.0	0°0	1.3	0-0	۲. ۲.	0-0	0.0
5	C	63	0.0	د • <del>د</del>	0.0	0.0		0°C	0.0
54		10	0°0	0.0	0.0	0.0	<b>0.</b>	0.0	0*0
1	U L	77	0.0	C • 0	9.0	0.0		. 0.0	0-0
		84	0•0	0°0	0° J	0.0	0.7	. 0*0	0.0
in i Biri		16	0•0	c • 0	<b>0.</b> 0	0.0	<b>3</b> .7	Q=0	0-0
<b>D</b>		86	0*0	0.0	0.0	0-0	CO	0.0	0-0
0	LL L	102	00	0°0	C.0	0-0		:	

FIGENVECTOR FOR ROOT NO.=

€£GFNVALUE=

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 $\mathcal{L} = 4 R P M$ Mode 1. Frequency = 2.2729 Hz,

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1•144	05738F 02 (rad/s	iec. )				•	·
:	0.3613E 00	-0.21385-31	-3.1556F-04	-0.5927E-08	-0.51736-79	-0.7497E-03	-0.3613
	-3.21165-31	-0-1553E-04	0.57305-38	-0.5179c-DA	-0.7496E-D3	0.2266F 00	-0.2110
•	-0.14525-34	-U.54235-0ª	-3.5170E-09	-0.7457E-03	-0.2266E 00	-0.2116F-01	-0-1452
	0-32333 Ú	-0°61705-79	-ŭ•74575-03	10-30266-01	-0.2110F-01	-0.1369F-04	-0.3471
	-0.6156E-9P	-0-7279F-03	-0.9370E-01	-0.2112E-31	-0.13715-04	0.34955-08	-0.6156
	-0.72785-03	0.50545-01	-0.21085-01	-0-13535-04	-0.1613E-09	-0-6144F-08	-0.1099
	-0.5055E-71	-0°2106E-01	-0.1355F-04	0.17655-38	-0.61445-38	-9.7100F-03	-0.2343
~	-u-21065-J1	-J.134pE-n4	0.1011E-09	-0-6135E-38	-C.6933F-D3	-0.2336E-05	0-2055
	-0.1378E-94	0°1014⊑-06	-3°44715-08	-0.6937F-J3	-0.2325F-05	<b>0.621AF-01</b>	-0.1402
	0 10145-00	-7 37615-00	-0 -0000 -03	30-3726 0-	-0 1070E 00	-0 13765-02	2201 0

	<b>1-3613F 00</b>	-0.21385-31	-J.1556F-04	-0.5927F-08	-0.4179F-78	-0.7497F-03	-0.3613E 00
-3-21165-7	-	-0-15535-04	0-51305-08	-0-517ac-0A	-0-74965-03	0.2266F 00	-0.2110F-01
-0-14526-0	4	-0°2453E-08	-3.5170E-09	-0.7457E-03	-0.2266E 00	-0.2116F-01	-0.1452E-04
0-32833°	α	-0°61705-09	-0.74575-03	10-30266-0	-0.2110F-01	-0.1369F-04	-0.3471E-08
-0-6156E-91	۵.	-0-72795-03	-0.9370E-01	-0-2112E-31	-0.13715-04	0.34955-08	-0.6156E-09
-0.7278E-J3		0.50545-01	-0.21085-01	-0.1353F-04	-0.1613E-09	-0.61445-08	-0.7099E-03
-0.5055E-71		-0.2109F-01	-9.1355F-04	0.17655-38	-0.61445-38	-9.7100F-03	-0.2343E-05
-n.21065-01		-J.134pf-n4	0.1011E-09	-0.6135E-08	-0.6933F-D3	-0.2336E-05	0.2055E-01
-J.1378E-74		0°10145-09	-0.4401F-08	-0.69375-33	-0.2325F-05	<b>0.621AF-01</b>	-0.1402E-04
0.1016F-09		-0.3741F-08	-U.5929E-D3	-0.2576F-05	-0"1049F n0	-0.12245-04	0.1033F-09
-0°083E-04		-0.42765-03	-0.2795E-05	-0.15045 JO	-0.10665-94	<b>3.104RE-09</b>	-0.1036E-07
-0.18385-03		-0°2069c-02	-0.1570F 00	-0.1011E-04	0.10555-09	-0.77615-08	-0.3693E-04
-0.29745-05		-1.1426E 30	-0.1033E-04	0.1071F-09	0.1416E-07	0.4262E-03	-0.3342E-05
n.3121F n3		+i-32682°i-	0.1128F-09	0-6418E-07	0.1733E-02	-0.3456F-05	0.1000E 01
-0-20250-04		0.11465-39	0.55416-07	0.19305-02			
0.4549E-03		0.1005F-03	0.5932E-08	0.8129E-11	0.5998F-11	-0.4900E-06	0.5464E-03
-0-91655-34		-0-35Coc-08	0.8939E-11	0.63025-11	<b>0.6602E-05</b>	0.3795E-03	0.7718E-04
0-44565-09		0.9352F-11	U•36003•U.	-0.4438E-06	0.4304E-03	-0.6836E-04	-0.1300E-08
C. 89325-11		ũ•\$00\$ε−1]	<b>3.5126F-06</b>	0.3133F-03	0.3991F-04	0.2901E-08	0.8982E-11
n.59805-11		-Ü-ZÝZVE-V9	0.3342E-03	-0.3110E-04	0.3421E-09	0.93045-11	0.5981E-11
0-4254F-06		0.3026E-03	0.2163E-04	0.2342F-0A	0.ª678E-11	<b>J.5969F-11</b>	-0.8764E-07
0.31386-03		-0.12835-04	0.9152F-09	0.99215-11	0.5970E-11	0.2459E-06	0.3019E-03
0 <b>.</b> 4393F-05		0.16315-08	0-1008E-10	0.5961E-11	0.7674F-07	0.2974F-03	-0.2120E-06
0 <b>.1</b> 9825-0P		0.1922E-10	0.5737E-11	0.7677E-07	0.26885-03	-J.4819E-05	0.23196-08
0.1079F-10		<b>0.55595-11</b>	0.7679c-07	0.29885-03	0.13n7F-04	0.7250E-09	0.9126E-11
0-60A5F-11		0-3951E-07	9.2768E-J3	0.1650F-04	-0.1723E-39	<b>3.6929E-11</b>	n.5769E-11
<b>0-68755-0</b> 4		0.25355-03	0.1633F-04	-0.501 RE-09	0.47765-11	0.51955-11	-0.1223E-07
0-10025-03		0.1326F-04	-3.7476E-09	-0.3331E-11	0.1614E-11	-0.7142E-07	-0.1432E-03
-0-49265-04		n.9981E-00	-0.4038E-10	-0.71835-11	-0.2250F-06	-0-1461F-03	-0.13556-03
0.34095-08		-C.4100F-10	-0.5654E-11	-0.2381E-06			

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Mode 2. Frequency = 4.2027 Hz,  $\mathcal{D}$  = 4 RPM

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5155*VALUE= 0.26406250E 02 (rad/sec.)

-0.6079E-07 0.1564E-08 -0.3117E-03 -0.3934E-10 0.2591E-07 8 -0.2841E-10 0.7639E-09 -0-17046-06 -0.2140E-05 0.2212E-08 -0.1315E-05 0.3825E-05 -0.1155E-02 0-9486E-09 0.9008E-06 0.2749E-10 0.9382E-07 -0.7622E-08 0.1222F-05 -0-3985E-01 -0.3058E-04 C-6063E-08 -0.7097E-03 -0.4126E-05 -0.1254E-07 -0-3831E-04 -0.2167E-07 -0.1682E 0.1013E-08 0.5984E-06 80 0.1222E-05 0.3048E-04 0-5064E-08 -0.1236E-07 0.3410F-09 -0.7296E-04 -0.2126E-05 0.2056E-08 0.10565-08 -0.9089F-06 0-39595-0A -0.2237F-05 -0.3261F-01 -0.114AF-02 -0.6234E-07 -0-4901F-03 -0.1442F-07 -0.1267F-09 0.76085-10 -0.5818E-07 -0.6854E-11 0.24265-03 0-30994-01 -0.25965-10 0.2592F-07 0.1309E 0-32415-78 0.1215-78 0.1215-50 0.12135-01 -0-1474E-04 -0.11435-72 9.11225-38 -0-46=55-0F 0+1445=-39 -0.1225E-36 -0-21245-35 80-3=161.0 9-13425-36 0.54375-76 0.54375-11 0.50245-08 0.835=E-06 0.25045 23 -0-62715-07 -0-21655-13 +0-3222+34 EC-31184.0 70-32717.0--0.1159F-J2 0.29635-03 0.245=5-11 0-6006E-09 -0.1169E-32 90-38558-08 -U-1992E-36 9.1213F-35 0.1463E-04 -0.1142E-02 0.5030F-08 -0.1291E-05 0.2°55E 00 -0.2368E-06 -0.7166E-05 0.70235-10 -0.1402E-38 0-2725E-08 -0.6412E-04 -0.2116E-35 0.6357E-08 -0.2543c-08 0.5475E-03 -0.5618E-36 0.3331E-05 -0.3248E-19 -0-34613-04 -0-6307E-37 0.2070E-02 0.9R07F-12 -0.6858E-07 0.8450E-11 -0.3123F-01 J.5196E-04 -0.1154E-72 0.8560F-08 0.8011E-06 S -0-6324E-07 0.17495-09 -0.2937E-05 0.1208F-05 -0-30072-07 -0.1147E-02 0.5044F-09 0.4536E-29 7.2068E-02 -0.1508F-03 -0.4615E-07 -9.2157E-05 -0.4066E-10 9.1321F-09 -0.5151E-04 -0-7902E-07 -0.4739F-0P 0.3833E-05 -0.3122F-01 -0.2501E-05 -0-2125E-05 9.1069E-37 0.5628E-03 -3°4 896E-01 0-3460F-11 0.3036E 0.120PE-25 0.12265-35 +^.40026-71 -0-4750F-n4 -0.5833E-07 -0.23675 30 -0.43245-37 -3.226E-36 Úl-sáúat°ú 0°-31105-00 0-30022°u C-21721.0 -<u>0</u>-365F-03 -0.1164E-32 0.72255-09 -0°3004E-36 -1.306ªc-31 -j.1149c-j2 -u.9105F-n. 0L-3UL92°C -J. 3808F-75 n.3250E-19 -0.2387E-04 ---?!515-u2 -0-2680E-04 -0-1146c-37 -0.2129E-05 -j.14795-10 -0-71025-09 -0.2038F-05 0.12025-25 -0.1091F-03 0.2247E-08 -7.3823E-75 0.4742E-04 0.40145-75 -0.9876F-03 -0.2330F-10 -0.1941F-03. -0-3359E-10 -0.3988E-01 -0.1155E-32 -0.5952F-07 0.75926-79 -0.2571E-07 0.39255-00 -U-30Cat "U--0.2140F-75 C.20715-29 -0.1830E-05 -0.1251F-02 0-1273E-09 -0-4490E-v2 0.2566E-77 -0.82915-7P -0°637E-01 -0.18485-07 Ē **0.1543E-07** -0.1000F 0 10 102 ŝ 25 5 5 PAPT 23 \$ 5 63 03 14 5 1.4 14 4 80 16 DART 7 9 7 V 55 ΞĒ E Ē ç C Ę ç Ē C C £ 2 E 55 1 77 30 15 2 5 5 57 \$9 ŝ e 22 2 33 4 ŝ 5 6 5 1 5 5.6 6

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="UN ICLA BUE BLICE":sSis

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Mode 3, Frequency = 8.4147 Hz,  $\mathcal{D}$  = 4 RPM

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ETSEN144LUF= n.52271394E 02 (red/sec.

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	101								
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	.) y=4	1	*	1-1:2552	-0•1×1°c-	-9.25625-04	-0.13125-36	-0°47776-96	<b>9.643</b> 0F-04	0.2380E-01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	•	۲ ۲	14	-2.159651.7-	-0°2442c-04	0.12695-06	-1.4717E-76	り ちょらに しん	-9.14115-01	-0.1532E-01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5	[	21	sú−33962°ù-	-J.115511-	-0.46465-05	0.6167F-04	0.14r2F-21	-0.15285-01	-0.2479E-05
1       3       7       3       -0.44765-0       0.50375-01       0.14576-0       0.54376-0       0.54776-0       0.54776-0       0.54776-0       0.54776-0       0.54776-0       0.54776-0       0.54776-0       0.54776-0       0.74776-0       0.74776-0       0.74776-0       0.74776-0       0.74776-0       0.74776-0       0.747595-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71575-0       0.71056-0       0.74075-0       0.71575-0       0.71056-0       0.74075-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.71056-0       0.710566-0       0.710566-0       0.710566-0	:	۲. ۲.	29	~.1121E-11	-0-4644F-36	7.5334E-04	-0.3049E-02	-0-14515-01	0.14045-04	-0.6797E-07
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	et.	Ú.	35	-0.4499E-n6	n.4867E-74	9.5087F-02	-0.1459E-31	0.14575-04	<u>0.6631E-07</u>	-0.44985-06
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	41	<b>C F</b>	25	ちしていいたちゃい	-0.14125-02	-3.14345-01	0.1701c-34	10-32226-0-	-9.4377F-06	0.35415-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	m	( )	40	21-329220	-0-1433E-01	0.169RF-34	9.322F-37	9U-3LLE7"L-	n. 3323F-04	0.7153E-03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	(	ري ا	<b>б</b>	14-30641-1-	0°l⊦ll⊑-04	0°5044E-00	-3.4790°-36	0.27125-24	0-J143E-03	-0.1501E-01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	*	5	63	-0°1236-02	0°3002E-00	-0.43195-06	0.5691E-05	n.71215-03	-0.14955-01	-0.3362E-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	.+	r F	70	0.3048E-n9	-0.4308°-76	-0.43945-05	0.7919F-J3	-0.2027E-01	0.7038E-04	0.4032E-09
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-	5	77	-3+575-04	-0-1048E-03	0.86215-33	-0.4711E-J1	0.07515-24	7.4875E-09	0.2198E-07
1       0.97315-7       -0.11145 70       0.44095-04       0.62685-75       -0.73475-73       0.10005 01         1       1       1       0.11155-71       0.111115-78       0.10055-03       0.01005 01         1       1       1       0.1155-71       0.11115-78       0.10057-08       0.10056-07       0.10056-01         1       1       1       0.1155-71       0.11016-75       0.10056-01       0.10066       0.10066       0.10066         1       1       1       0.1155-71       0.11016-75       0.10056-01       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10066       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666       0.10666	m	C F	84	-1.26255-73	0,9802E-ni	-0.6687E-01	9.80675-04	0.5555E-09'	n.2087E-06	-0.4010E-03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	<b>.</b>	( <del> </del>	10	0.9231E-J ²	-0.11145 20	0°4430E-34	0.626RE-39	0.70-55-35	-0.75475-03	0.1060E-02
7 $102$ $-0.5015-03$ $0.111116-08$ $0.78776-07$ $0.41946-02$ $711207$ $7$ $7$ $7$ $7$ $11526-01$ $0.23276-06$ $7$ $7$ $7$ $7$ $7$ $7$ $0.10706-05$ $0.16746+08$ $0.47346-04$ $7$ $7$ $7$ $7$ $7$ $0.11546-04$ $0.11646-04$ $0.232406-06$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $0.232466-06$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$	<b>N</b> 1	r +	ар	-1-3ctu2-C-	-0 <b>-</b> 4540E-03	0.1029E-08	0 <b>-</b> 1095F-N5	0.14-55-07	0.99176-03	0.1000E 01
71.1290.1152E-010.1070F-050.1624F-080.4315F-100.6784F-040.1164F-0177771.152E-010.0.7237F-050.0.1070F-050.1674F-080.2340F-0477770.1131E-050.1070F-050.1674F-080.4315F-100.2340F-047770.1131E-050.1070F-050.1674F-030.0.1946F-030.0.1946F-067770.1131E-050.1070F-050.1377F-040.2340F-060.2340F-067770.1131E-050.13497F-040.13497F-060.2340F-067770.1134F-030.2317F-050.2340F-060.2340F-06777770.13495F-040.1184F-030.2340F-067777770.2346F-040.1164F-010.1164F-01777770.2633F-040.1177F-010.1026F-010.1949F-067777770.2546F-080.1191F-010.6974F-060.6974F-067777770.2546F-080.66326F-010.6974F-060.6994F-067777770.2533F-080.2546F-080.6994F-06777790.2633F-080.2546F-080.6994F-067777790.2746F-010.9974F-01777770.1346F-030.2546F-0	r	r +	201	といーろし しゅういつ	0.11115-38	n.7877F-07	0.4194E-32			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-	1 701	7925							
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-4	r . F	٠	0.1152E-21	-0.7237F-35	0.10?0F-05	0.1624F-08	0.42545-13	-0.67845-04	0.1164E-01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	a	( +	14	<b>1.12495-5</b> 2	-0.1016E-35	0.1624F-99	<b>0.4315E-10</b>	0.6=215-34	-0-19476-03	0.2340E-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	L)	( ·	14	0.7131E-34	0.186PE-~9	0.42275-10	-U.5959F-34	-0.13=7E-73	n.1556F-03	-0.70865-06
7 $35$ $0.41345-10$ $-0.34775-74$ $-0.36475-74$ $-0.34955-74$ $0.41145-10$ $5$ $72$ $42$ $0.34955-94$ $-0.104525-74$ $0.118905-76$ $0.25455-98$ $0.39995-17$ $-0.15495-04$ $7$ $42$ $0.34955-74$ $-0.11025-701$ $0.11025-701$ $0.11025-701$ $0.1025-91$ $0.11025-701$ $7$ $7$ $0.34955-74$ $0.11275-701$ $0.10395-710$ $0.11025-701$ $0.99775-04$ $7$ $7$ $0.27455-710$ $0.254457-701$ $0.959557-04$ $0.699577-04$ $7$ $0.27755-710$ $0.27755-701$ $0.959575-04$ $0.699575-04$ $7$ $0.27755-710$ $0.25125-701$ $0.959575-04$ $0.699575-04$ $7$ $0.27755-710$ $0.25475-704$ $0.69945-08$ $7$ $0.27755-710$ $0.25475-704$ $0.69945-08$ $7$ $0.27755-710$ $0.25475-704$ $0.69945-08$ $7$ $0.25125-704$ $0.195257-94$ $0.69945-08$ $7$ $0.25475-704$ $0.25475-704$ $0.27695-11$ $7$ $7$ $0.25475-704$ $0.194325-08$ $7$ $0.25475-704$ $0.194525-704$ $0.194525-708$ $7$ $0.25475-704$ $0.103276-704$ $0.194325-708$ $7$ $0.25475-704$ $0.1033276-704$ $0.194325-708$ $7$ $0.25475-704$ $0.1033276-704$ $0.194325-708$ $7$ $91$ $-0.123155-10$ $0.123257-01$ $0.17037-705$ $7$ $91$ $-0.123255-75$ $0.103327-705$ $0.17037-705$ <	<b>~</b> '	۲.) ۲.)	9.0	<b>3.1</b> 858E-J ²	0.42405-10	0.5991F-04	20-34660-0-	0.57115-04	0.3353F-06	0.2320E-08
5       T2       42       0.34955-04       -0.10455-01       0.18005-06       0.25455-08       0.30995-10       -0.11025-01         3       T2       42       0.10135-03       -0.18475-06       0.25465-08       0.40735-10       0.15565-04       -0.11025-01         3       T2       55       0.8565-04       0.11025-01       0.89775-04       0.11025-01       0.89775-04         3       T2       55       0.8565-74       0.25465-08       0.40735-10       0.15565-04       0.01025-01         3       T2       53       0.27155-08       0.40735-10       0.95555-04       0.69945-06         4       T7       53       0.25165-07       0.25465-07       0.256467-08       0.256565-04       0.69945-06         7       0.25745-03       0.40115-10       -0.11275-01       0.95555-08       0.256456-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.256565-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.27665-08       0.276656-08       0.276656-08<	r	۲ ۲	35	0.4104E-10	-0-34776-74	-0-36256-03	0.1184E-03	-0.33125-06	0.2319E-08	0.4114E-10
3       72       49       -0.10456-01       0.10136-03       -0.11026-01       0.89776-04         7       75       0.85045-04       0.25466-08       0.30246-10       0.15566-04       -0.11026-01       0.89776-04         7       75       0.85045-04       0.21676-08       0.30246-10       0.15566-04       0.89776-04         7       75       0.85045-04       0.21676-08       0.30246-10       0.95546-01       0.89776-04         7       7       0.27746-08       0.40116-10       -0.6111776-01       0.95546-08       0.69946-08         6       7       0.2111776-01       0.0111776-01       0.0111276-04       0.69946-08         7       0.25746-10       0.21046-06       -0.11916-11       -0.53476-04       0.69946-08         7       0.15746-10       -0.10046-06       -0.11916-01       -0.19826-08       0.27696-08         7       0.15746-10       -0.12746-01       -0.12946-01       0.19436-01       0.19436-01         7       91       -0.12746-01       -0.1266-04       0.48566-08       0.13456-08       0.19436-08         7       91       -0.12746-01       -0.1266-08       0.119476-08       0.194466-08       0.194466-08         7       91	\$. \$	Ci F	4.2	<b>0.3495</b> F-04	-0.1042E-01	9.7149E-04	0.18905-36	0.25455-08	ú <b>1</b> -3666€°ú	-0.1549E-04
7       75       0.85745-74       0.26335-08       0.30245-10       0.63575-01       0.89775-06         7       7       53       0.45385-75       0.27455-76       0.69945-08         6       7       0.11775-01       0.95575-04       0.69945-08         7       7       0.27755-73       0.40115-10       -0.111915-71       0.95575-04       0.69945-08         7       7       0.27755-74       0.40115-10       -0.111915-71       0.95575-04       0.69945-08         7       7       0.277555-74       0.40115-10       -0.11915-71       -0.577695-08       0.27695-08       0.27695-08         7       7       0.15795-10       0.11915-71       -0.11915-71       -0.127695-08       0.27695-08         8       -7       7       0.25412-09       0.125455-01       0.19435-05       0.19435-05         7       91       -7.12915-74       0.465555-09       0.119435-03       0.19525-95       0.119435-05         7       91       -7.12915-74       0.455555-09       0.18435-10       0.19435-05       0.119435-05         7       91       -0.12915-74       0.255555-09       0.18435-10       0.19435-05       0.119435-05         7       91       -0.12915-	~	C '	49	-0.10455-01	0,10135-03	0.1847E-n6	0.2546F-n8	0.40735-10	<b>0.1556F-04</b>	-0.1102E-01
7       7       53       0.4538F-0*       0.27245-08       0.69945-08       0.69945-08         4       7       0.27755-0*       0.41365-10       -0.10046-06       -0.11916-01       -0.53475-04       0.69945-08       0.27695-08         1       7       7       0.15785-0*       0.41365-10       -0.10046-06       -0.11916-01       -0.54175-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-08       0.27695-01       -0.682655-01       -0.682655-01       -0.682655-01       -0.682655-01       -0.682655-01       -0.682655-01       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.19435-05       -0.13455-05       -0.13455-05       -0.13455-05       -0.134555-05       -0.134555-05       -0.1703355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.170355-05       -0.1703555-05       -0.1703555-05       -0.	m	C: F	55	3.85045-74	<b>1.71625-79</b>	<b>9.2633F-0</b> 8	J.zo24E−10		-0.11065-01	<b>0.8977E-04</b>
<pre>     T</pre>	-	C F	53	1.453 BF-16	9.27245-ng	0°4011E-10	-0-915-07	-0-11275-01	0-95575-04	0.69945-08
I       0.       0.       15795-10       -0.       15555-01       -0.       26415-08       -0.       68266-11         3       10       84       -0.       204154-01       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       12455-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       124555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       1245555-05       -0.       120355-05       -0.       1703555-05       -0.       170355555       -0.       1703555555       -0.       17035555555       -0.       1703555555555       -0.       1703555555555555555555555555555555555555	.+	<b>C</b> :	7.7	2.2775E-1a	0.4136F-10	-0.1004F-06	-0.1191E-01	-0-53475-04	-0.19825-08	0.2769E-08
3 *** 84 ***.??62E-75 -0.1274E-71 -0.4620E-03 -0.1843E-08 0.2457E-0° -9.1799F-10 -0.1943E-05 5 *** 91 -0.1291E-01 -0.5716E-03 -0.3485E-09 0.1899E-78 -0.1033E-05 -0.1345E-01 2 *** 98 -0.3712E-14 0.4246E-19 -0.5563E-09 -0.1315E-10 0.35555-05 -0.1232E-01 0.1703E-02 2 *** 10? 0.9531E-02 -0.5559E+00 *0.8887E-11 0.5295E+05		ج	11	0.1579F-10	-0.1599F-75	-0.1255F-01	-0-3410E-03	-0.25135-08	n.26415-08	-0.6826E-11
5 T^ 91 -0.12915-01 -0.57165-03 -0.34855-09 0.19925-08 -0.10335-05 -0.10335-05 -0.13455-01 2 T^ 98 -0.37125-04 0.42465-09 -0.55635-09 -0.13155-10 0.35555-05 -0.12325-01 0.17035-02 3 T^ 10? 0.95315-02 -0.55595-00 -0.88875-11 0.52955-05	m	C +	84		-0-1274E-JI	-0.4620E-03	-0.1843E-38	9.2457E-08	-1.17995-10	-0.19435-05
z T^ 98 -0.3712E-14 0.42465-09 +0.5563F-09 -0.13155-10 0.355455-05 -0.1232F-01 0.1703F-02 = T^ 102 0.4531F-C2 -0.55595+00 -0.8887E-11 0.5295E+05	ur.	C F	۱٥	-0.12915-01	-0.5716E-03	-0-34855-09	0.19995-78	-9.10525-13	-0.1033E-05	-0.1345E-01
a T∩ 102 0.9531F-C2 -0.5550€+00 -0.4887E-11 0.5295E+05		17	98	-0.3712E-74	j.42465-ng	-0.5563F-09	-0.13155-10	0.3555505	-0.1232F-01	0.1703F-02
	'n	C +	192	0°4231E-UB	-0 <b>*</b> 2220E+00	-0 <b>.</b> 8897E-11	0.5295E-05			

Mode 4. Frequency = 8.6789 Hz,  $\Omega$  = 4 RPM

ETGENVECTOR FOR ROOT NO.=

4

N N	RT .							
F	۲ ۲	<b>1.6187E 1</b>	<b>0.51575-02</b>	-0-398995-06		-0.13725-06	-0.22376-02	0.6237E 00
Ĩ	0 14	20-3115-2	0.2133E-05	-0.1046F-08	-0.1372F-06	9.2254E-02	00 36622°C.	0-5304E-D2
F	0 21	<b>」。2515E-DF</b>	-0-36365-08	-0.1350E-06	-D.2007F-02	0.2319F 01	0.5380E-02	0.19245-05
۴.	8C L	ec-326-1-	-j.135je	0.2022E-02	-0-3C2C1-0-	3.54345-92	<b>7.13295-05</b>	-0.4045E-09
Ē	35	-2+13055-05	-0-1224E-02	-0.7089E-01	0°24535-02	9.1629E-05	-0.16965-08	-0-13055-06
F	24 C	7.12355-02	-0.1252F 00	0.54435-02	0.1493E-35	-0-1392F-09	-0.12675-06	-0.5666E-03
÷	67 U	-2.1254E 01	0.546re-02	0.1559E-05	-0-3116F-09	-1.1267E-06	9.5657E-03	-0.1463E 00
F	n 56	3-54535-02	0.1541F-05	0.7212E-10	-0.1240F-96	-0.34795-05	-0.1482E 00	0.5679E-02
Ē	с 93		0-14115-10	-0.1262E-06	-0-3049E-05	-0.1491E 00	0.5917E-02	-0.1354E-04
F	0 10	J * 754 [ E - 1 ]	-0-1257-06	-0.3963E-05	-n.21415 00	0.2096E-02	0.16245-04	0.1009E-09
Ē	11 ü	-J-5740E-07	-0°3640E-04	-0.2723E 00	-0.499]E-32	0-2090E-04	0.1227E-09	0-6432E-08
-	0 4 5	<u>-</u> 5150E-04	-0°5°70° JU	-0 <b>.</b> 7997E-02	0.1974E-34	0.1329E-09	0.5458E-07	-0.4749E-04
Ē	16 L	-3-3291F 01	-0.1042F-01	0.9832F-35	0 <b>.</b> 1594F-79	<b>3.1955E-96</b>	-0.1938F-04	-0.4556E 00
÷	96 0	-J-3160F-02	-0-11055-03	0.267 <u>e</u> r-09	0.2716E-06	0.2226E-04	-n.4590F 00	-0.3289E-02
÷	0 102	-2.1505E-03	0°5000E-00	0.2179E-07	-0.11665-34			
NAL	19 <u>7</u> 0 79							
ř	۲ ۲	7415F 01	0-5325E-02	-0.1609F-05	-0°4433E-78	0-3821E-04	-0.28156-02	0.7817E 00
-	51 i	ごじーコじん ジン・レ	0.137nF-05	-0.5597E-09	n.3¤23E-3¤	0.2991F-02	0.27225 00	0.5125E-02
Ĩ	ו2 נ		-0.4169E-08	n.3758F-08	-0.25235-07	0.7912F 09	<b>3.5288E-02</b>	0.8861E-06
Ŧ	۲ 28 2	もんーろらんこう - つる	0-3767F-08	0.25A0E-02	-0°1024E 30	<b>0-37</b> 78402	-0.1703E-06	-0-2963E-08
F	35	-3633E-05	-0~1241E-02	-0.1046E 00	0.42915-02	n.7456E-07	-0.3497E-08	0.3634E-08
ì	C 42	C.1571E-02	-0.1737E 00	C.4652E-02	-0-55685-37	-Ù-È¢6¢E-Û9	0.3529E-08	-0.7111E-03
Ì	64 67	CL 30,221"L-	n.46875-02	-0.5738F-07	-0-4224E-j9	0.3529E-08	0.71725-03	-0.2002E 00
F	ن ى	2,4508F−n2	-0*6655E-37	0.6155E-09	0.34555-08	-9.72135-05	-0.2026E 00	0.4949E-02
F	63	<b>7-1435E-76</b>	0.6410F-29	0.35375-09	-0 <b>.</b> 741°E-75	-0.2036E 01	0.5395F-02	0.3574E-06
1	01 L	J * 854 9E - JC	0.3580F-08	-0.7449E-05	-0.2935E 10	-0.6190E-02	-0.4189F-06	0-6452F-09
F	<b>11</b>	<b>7.1235F-09</b>	-0.1181E-03	-0.3547E 00	-0-2607E-01	-0-448BE-06	0.60565-09	-0.7521E-09
F	0 84	-0.1320E-03	±00 3848€ 00	-0.3324E-01	-0.3747E-06	0.5612E-09	-0.1671F-08	-0.1048E-03
-	. <b>16</b> C		-0-36496-01	-0-25335-06	0.43436-04	-0.1553E-08	0.1598E-04	-0.5775E 00
Ľ.	66 C	<b>j.2695F-J1</b>	-0.1759F-07	-0°22652°0-	-J.4495E-10	9.1656E-03	-0.5778E 00	0-47455-01
Ĭ	201 C		-0 2501E-00	0 63046-11	-0 35/35 V-			

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Mode 1, Frequency = 2.4421 Hz  $\Lambda$  = 8 RPM

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1 Mode I, Frequency  $= \mathcal{L}$ .

ETGENVil "= ___143a2324E_02 (rad/sec.)

J¢ja	1010	•							•
-	r F	•	0.7267F 00	1C-316E4.0	-0.3981F-04	-0.52565-38	0.4358E-05	-0.14776-02	-0.7267E 00
	r - F	14	0.43595-01	-0.39635-14	<b>1.4366F-79</b>	<b>1.43525-06</b>	-7.14775-32	0.4606F 00	0.4368E-01
15	1 +		-J.3870E-04	-0°2321E-16	0.4353E-96	-1.14al£-32	-0.4505E 00	0.4347E-01	-0.3882E-04
23	( ) F	C ()	1.4669E-09	0.4354F-26	-0.14916-02	0° 1-4-E 30	1.4343E-01	-0.3777E-04	-0.3817E-08
¢2	- <del>-</del>	S.	0.4344F-06	-0°1414E-03	-0.1940° יח	0.43345-31	-0-3799F-04	0.4256F-0R	0.4344E-06
5 E	( ) +	5	-0 <b>-1479E</b> -02	0.1055E Jr	0.4333E-31	-0.3761E-04	-0.1358E-08	0.4335E-06	-0.1470E-02
4	Ļ	6.5	-0.1055F 0n	0.43285-31	-0-37775-04	<b>0.3144F-38</b>	0.4335F-06	-0.1470E-02	0.1247E-04
ŝ	(	C L	0.4324E-01	-0.3760E-14	. 0 <b>.1154</b> €-78	5.43296-78	-0.14595-02	0.1312E-n4	0.1309F 00
57	1		-0.11376-04	<b>0.1157</b> E-10	<b>0.4405E-76</b>	-3.14515-32	70-386rl°C	0.2185E 00	0.1521F-04
4	t •		<b>9.11595-09</b>	シーコンタケケー い	-1.1462E-72	<b>0.17755-34</b>	-0 <b>.15</b> 99E nn	-0.9978F-04	0.1177E-08
11	ſ	77	n.3947F-05	-0.124052	い。9204E-75	-0.3267F 10	-7.15565-33	<b>7.1194F-08</b>	0.3520E-06
4 2	{	J. N	-7.97935-13	0 <b>.</b> 8599E-35	<b>υ. 3667</b> ε.Ω-	-1.1761E-33	0.1232E-29	2.3790F-06	-0.79556-03
<u>ن</u> م م	C F	5	0.79325-95	-0°4144E JU	£C-38101°C-	0.1219E-38	0.27º2E-06	-0.1687F-03	0.5733E-05
6	r ⊧	с :)	<b>J.481RE-02</b>	-0*2704F-13	j•12dú£−ué	0.12485-36	<b>0.2179E-32</b>	<b>3.4687E-05</b>	0.1000E 01
60	ſ		-0-30116-03	ar-30651.n	n.98925-07	n.79595-32			
1 UAG	A 0 1 1	2 1 3 1							
<b>••</b>	۲ ۲	•	0.20954-02	r.3993f.	<b>1.23</b> 40F-16	0 <b>*</b> 4842E-Ja	-0.3962F-10	n.7506E-06	0.1874E-02
ď	۲.	.1	-J. 3004E-J3	-0.25916-26	0.5391E-39	-0-3255E-10	-0.1257E-35	3.2216F-02	0.3018E-03
15	4		0.1468E-06	0.484.85-70	-0.3955E-10	0.6607E-96	0.2058F-02	-0.3nn8F-03	-0.1625F-06
22	r +	e Ĺ	7.526F-39	-0 <b>-</b> 3952E-10	-J.Ila5F-25	3.73125-32	0.1475E-03	0.5966F-07	n.4824E-09
53	ſ	3 5	-0.3945E-10	330676-C	0.2246F-02	-0.14555-73	-0.6927E-07	0.51145-09	-0.3943E-10
35	ſ	¢ 7	-3.85765-05	n.2324F-32	0.71agf-74	0.31945-07	0-4779E-09	-0.39365-10	0.4252E-07
43	Ļ	C *:	1.2299F-02	-0*70795-14	-1.3916E-17	60-37167°U	-0-3035F-10	-0.5426F-06	0.2318E-02
ç	(  -	ר הי	<b>9.5603F-06</b>	-0.3407E-39	0.4732F-39	-0.30305-10	-3•2464E-0K	0,2200E-02	0.1534E-04
57	( ) ►	د ع	-0-5755E-MB	0-4424E-0C	-J.3970F-12	-0.7453E-36	<b>0.7055E-02</b>	<b>J.3012F-04</b>	-0.8222E-08
64	5	U 1	0.4300E-09	-0 <b>.41</b> 84E-10	-1.2461F-36	0.25735-92	-0-3179E-04	<b>0.2576⁶-0</b> 9	0.2516F-09
11	۲. ۲		-0.3976F-10	-0.19486-26	0.2976E-02	-0-5497F-34	0.91845-38	<b>0.12395-09</b>	-0.3502E-10
7.3	r <b>F</b>	70	-0.12305-36	0.3076F-32	-3 <b>-3</b> 4019-04	0.13175-37	0.8673E-19	-0.3113F-13	-0.8322F-07
ŝ	۲ ۲	lc	0.3155F-02	-0.622RE-14	0.11ª2F-07	0.27475-10	-0.1496E-10	0.4696E-07	0.3177E-02
6	۲. ۲	۰t	0.46305-04	0 <b>.</b> 804 75-39	-0.1320F-09	0-20145-10	0.4704E-06	0.3157E-07	0.2457E-03
C C	5	172	0 <b>.1</b> 579F-Ja	-0.13205-09	0.1512E-13	0.5754E-06			

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EIGENVECTOR FOR ROOT NO.* 2 Mode 2 Frequency

Mode 2, Frequency = 4.2026 Hz, D = 8 RPM

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" ¢165vVALUE= n.26406250F 02 (rad/sec.)

$ \begin{array}{c} 0.12595 - 0.2 \\ 0.48995 - 0.11645 - 0.2 \\ 0.47895 - 0.11645 - 0.2 \\ 0.47895 - 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.11645 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1044 - 0.2 \\ 0.1$	90-496/9*f. 70-46-11*0+ +
47457-01 $-0.47457-04$ $-0.11647-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.11957-02$ $-0.116217-02$ $-0.116217-02$ $-0.116217-02$ $-0.116217-02$ $-0.116217-02$ $-0.116217-02$ $-0.1116217-02$ $-0.111627-02$ $-0.111627-02$ $-0.111627-02$ $-0.111627-02$ $-0.111627-02$ $-0.111627-02$ $-0.1011627-02$ $-0.1011627-02$ $-0.1011627-02$ $-0.1011627-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.2011027-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ $-0.202707-02$ <td></td>	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 7.8751F-J9 -0.2184E-05
$ \begin{array}{c} 47375-34 & -0.11645-02 & 0.83875-09 & -0.773255-36 & 0.1195 \\ 11555-07 & 0.70575+08 & 0.11976-05 & -0.31255-35 & -0.3253 \\ 370355-01 & 0.58345-01 & -0.58345-01 & -0.5131255-35 & -0.32535 \\ 97355-07 & -0.11975-02 & 0.48945-09 & 0.55395-30 & 0.9093 \\ 98775-03 & -0.31055-07 & -0.11472 & -0.11472 \\ 99355-01 & -0.58345-07 & -0.11472 & -0.11472 \\ 99355-01 & -0.58345-07 & -0.11472 & -0.11472 \\ 99355-01 & -0.58345-07 & -0.11472 & -0.11472 \\ 99355-01 & -0.58345-07 & -0.48945-09 & 0.131255-35 & -0.5233 \\ 98775-03 & -0.230565-39 & -0.48945-09 & -0.553955-30 & 0.9093 \\ 98415-07 & -0.230565-39 & -0.48945-09 & -0.553955-30 & 0.2031 \\ 98415-07 & -0.230565-39 & -0.48945-09 & -0.553955-30 & 0.2031 \\ 98415-07 & -0.230565-39 & -0.48945-09 & -0.553955-30 & 0.2031 \\ 987355-07 & -0.230565-39 & -0.495555 & -0.55375 & -0.52373 \\ 987355-07 & -0.230565-39 & -0.48945-07 & -0.553955-30 & -0.52373 \\ 987355-07 & -0.24175-05 & -0.24355-07 & -0.43355-35 & -0.43557 \\ 10005 & -0.44175-05 & -0.24355-07 & -0.43355-35 & -0.43557 \\ 10005 & -0.44175-05 & -0.43355-07 & -0.43355-35 \\ 10005 & -0.44175-07 & -0.243555-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43357-35 \\ 10005 & -0.45565-03 & -0.43355-07 & -0.43355-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43355-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43355-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.45555-07 & -0.43555-07 & -0.43555-07 & -0.43555-35 \\ 10005 & -0.43$	2.7.1°5F-05 0.1204F-05
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5 0.1196F-05 -0.3260E-01
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5 -0.325af-n1 0.3045E-04
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	L -1.14725-04 -0.11485-02
11856-05 $-0.2767F-01$ $-0.5762F-07$ $-9.1142F-02$ $0.4834F-02$ $0.4935F-03$ $0.1016$ $-8775F-07$ $-0.1149F-02$ $0.4834F-03$ $0.5599F-09$ $0.8099$ $-8775F-07$ $-0.1149F-02$ $0.4834F-03$ $0.5599F-09$ $0.8099$ $-9.1149F-03$ $-0.1149F-03$ $0.25526F-09$ $0.5595F-09$ $0.25527$ $-1841F-07$ $0.2056F-09$ $-0.1315F-05$ $0.5232$ $-1841F-07$ $0.2055F-09$ $-0.20527$ $0.25237$ $-1841F-07$ $0.2056F-09$ $-0.20527$ $0.25527$ $-1841F-07$ $0.2056F-07$ $0.257376-07$ $0.257376-07$ $-10.4475-05$ $0.2056F-07$ $0.25955F-07$ $0.25375770F-02$ $-10.4417F-07$ $0.273757-07$ $0.273757-07$ $0.24476-07$ $-10.4417F-05$ $-0.4417F-05$ $-0.44375-07$ $-0.44375-07$ $-10.4417F-07$ $-0.140775-07$ $-0.140775-07$ $-0.44375-07$ $-10.4417F-07$ $0.17075-07$ $-0.140775-07$ $-0.44375-07$ $-10.4417F-07$ $0.28137F-07$ $-0.44375-07$ $-0.44375-07$ $-10.441$	+ -0.11435-02 0.5905E-08
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 0.4874E-09 0.9014E-09
5875E-07       -0.1149E-02       0.4894E-09       0.5599E-09       0.25595         1841E-07       -0.2056E-09       -0.3025E-09       -0.1315E-05       0.25395         1841E-10       -0.238706-05       0.2056E-09       -0.25305       0.2535         0.2056E-09       -0.25206-05       0.2056E-09       -0.5595       0.2535         0.2056E-09       -0.25066-05       0.20566-07       0.20576-07       0.20575         0.2016       -0.23876       0.20666-07       -0.59956-07       0.20576-07       0.20706-02         0.2016       -0.23656-07       -0.20666-07       -0.205666-07       0.20706-02       0.20556-07         0.1000       0.120666-07       -0.206666-07       -0.244346-07       0.2025656-09       0.26527         0.1016       0.1       -0.264176-07       -0.140366-07       -0.4436       -0.4436         0.1016       0.044176-07       -0.140366-07       -0.44366       -0.44366       -0.443666         0.1016       0.044176-07       -0.140366-07       -0.140366       -0.4436       -0.44366         0.1016       0.044176-07       0.140366       -0.44366       -0.44366       -0.44366       -0.44366         0.1016       0.044176-07       0.2106576       -0.140366	3 0.1019F-04 0.5993F-06
9877F-03       -0.419F-08       0.3025E-09       -0.1315E-05       0.2535         1841F-07       0.2056F-08       -0.2520F-05       0.2055F       00.5233         0411E-10       -0.23820F-05       0.3035F       00.2055F       00.2057         0411E-10       -0.23876       00.2055F       00       -0.5237       0.2573         0416507       -0.2367F       00       -0.5057       0.20557       00.2031         10007       -0.2650F-07       0.2056F-07       0.205757       0.2031         10007       -0.2650F-07       0.20349F-02       0.2031         10007       -0.2068F-07       0.204497       0.24497         10007       0.9978F-09       -0.30657F-07       0.1443475-05       -0.4434         27107       0.9978F-09       -0.30657F-07       -143475-05       -0.4435         27107       0.99787F-09       -0.443775-07       -14345-07       -0.4435         27107       0.964176-07       -0.130976-03       -0.4435       -0.4435         27107       0.964176-07       0.134076-07       -0.4435       -0.4435         27107       0.96416-07       0.134076-07       0.17056       -0.4435         27011610       0.1646600       0.134076-07<	3 0.8097E-06 0.1309F 00
18416-07       0.20565-09       -0.25206-05       0.20556-07       0.52705-02         0.44765-05       -0.38206-05       0.38206-07       0.25705-02       0.25705-02         0.44765-05       -0.250656-07       0.27705-02       0.25705-02       0.25705-02         0.10006       -0.46506-07       0.20546-07       0.27705-02       0.25705-02         0.10006       -0.46506-07       0.20546-07       0.25705-02       0.25705-02         0.10006       -0.46506-07       0.20546-07       0.254574       0.254574         0.17597       -0.244366-03       -0.44366973       -0.44366973       -0.44366973         0.11516-07       0.964176-05       -0.44366708       -0.44366708       -0.44366703         0.11516-07       0.044176-05       -0.44366703       -0.44366703       -0.44366703         0.44176-07       0.26416-01       0.26416603       -0.130976-03       -0.4356777         0.44176-07       0.27456-03       0.1706-10       0.54026-03       -0.435677         0.45076-07       0.136576-07       0.17076-03       0.17076-07       0.25676-07       0.25676-07         0.45076-07       0.136576-07       0.170696-07       0.170696-07       0.256472       0.256472         10.11616-10       <	5 0.2595E n0 -0.6270E-07
9311E-10       -0.3820F-05       0.3837F-07       0.29370F-02       0.29370F-02         .4476E-05       -0.2367F-07       0.20370F-02       0.29370F-02       0.29370F-02         .1000F       01       -0.4650F-07       0.20349F-12       0.29370F-02       0.29370F-02         .5151F-07       0.9877F-09       -0.3065F-03       -0.4457F-02       0.29474       0.29572         .5151F-07       0.9877F-09       -0.3065F-03       -0.4437F-02       -0.44374       0.29572         .7759F-08       -0.4417F-05       -0.4417F-05       -0.4437F-08       -0.44375       -0.44375         .7759F-03       -0.4417F-05       -0.2813F-08       -0.1309F-08       0.3124         .7519F-10       0.2641F-10       0.25413F-09       -0.4356F-03       -0.4356F-03         .45375-03       0.4417F-05       -0.2813F-09       -0.1309F-03       -0.4356F-03         .45375-03       0.1558F-03       -0.1309F-03       -0.4356F-03       -0.4356F-03         .45375-03       0.2332F-05       0.1709F-10       0.2332F-075       0.29507F-03         .5001F-03       -0.1365F-07       0.1709F-10       0.2332F-075       0.2435F-075         .5001F-03       -0.3435F-07       0.1709F-10       0.21375F-075       0.29507F-075 <td>) -0.6239F-07 -0.4901E-03</td>	) -0.6239F-07 -0.4901E-03
.4476E-05       -0.2367E 00       -0.4651E-07       0.2705E-02       0.2949EE-02         .1000E       01       -0.4650EE-07       0.2069EE-02       0.2949EE-12       0.29357         .5151E-07       0.99776E-03       -0.4657EE-03       -0.44357       0.293573         .77595E-07       0.99776E-03       -0.4417E=05       -0.44357       -0.44357         .77595E-07       -0.4417E=05       -0.4417E=05       -0.44357       -0.44357         .77595E-07       -0.4417E=05       -0.44356E-03       -0.44356E-03       -0.44356E-03         .77595E-07       -0.4417E=05       -0.44356E-03       -0.44356E-03       -0.44356E-03       -0.44356E-03         .77597E-07       0.05641E+10       0.27346E-03       -0.143369E-03       -0.43555       -0.26555         .47337E-07       0.16576E-03       -0.143369E-03       -0.43555       -0.265555         .47377       0.116576-03       -0.21776666       0.273555       -0.255555         .432976-07       0.179776       -0.433376-05       0.179776       0.23555         .432976-07       0.179776       -0.179776       0.27646-07       0.23555         .43376977       0.179776       -0.433376-05       0.179776       0.255555         .432976-07	7 0.25225-03 -0.1431E-07
<ul> <li>IDDE 01</li> <li>IDDE 01</li> <li>0.93785-07</li> <li>0.93785-06</li> <li>0.93785-07</li> <li>0.93785-07</li> <li>0.93785-07</li> <li>0.94375-07</li> <li>0.94475-07</li> <li>0.44175-07</li> <li>0.444175-07</li> <li>0.445175-07</li> <li>0.444175-07</li> <li>0.44415-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li> <li>0.44405-07</li></ul>	2 0.29315-38 -3.3608E-09
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5 -0.44345-05 0.1518E-09
<ul> <li>2719F-03</li> <li>0.4517F-75</li> <li>0.5254F-09</li> <li>0.4417F-75</li> <li>0.7800E-10</li> <li>0.5225F-99</li> <li>0.3145F-09</li> <li>0.5225F-99</li> <li>0.3145F-09</li> <li>0.5225F-99</li> <li>0.1659F-09</li> <li>0.3745E-03</li> <li>0.1359F-03</li> <li>0.1259F-03</li> <li>0.1259F-03</li> <li>0.1449F-07</li> <li>0.1153F-02</li> <li>0.1121F-02</li> <li>0.1449F-07</li> <li>0.1449F-07</li> <li>0.1153F-02</li> <li>0.1254F-03</li> <li>0.1254F-02</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> <li>0.1254F-03</li> </ul>	5 -3.85725-10 -0.24875-07
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3 -0.96525-19 0.69425-08
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3. n.3124F-08 -0.1488F-03
<pre>4410F=10 0.1659F=09 0.3746E=08 -0.1309F=03 -0.2472 4537E=09 0.4949F=09 0.3746E=03 -0.1340E=06 -0.4354 4329F=09 0.4949F=02 -0.1584E=06 -0.4338E=05 0.1722 3769F=03 -0.2332E=07 -0.4351F=05 0.1797E=10 0.35642 5091F=07 -0.4358E=05 0.1799F=10 0.1269E=07 0.23542 3747E=07 -0.3435F=10 0.2137E=07 0.1269E=07 0.2325 59747E=10 0.2541E=07 -0.9618F=08 0.1121E=02 -0.1435 5911F=10 0.2541E=07 0.1153F=02 0.1121E=02 0.9553 3044E=07 0.1449F=07 0.1153F=02 0.1121E=02 0.9553</pre>	2 -0.9¤23E-04 -0.1134E-06
<pre>45375-00 0.49485-08 -0.10576-03 -0.13405-76 -0.4354 43295-09 -0.11625-72 -0.15848-06 -1.43338-05 0.1722 37695-73 -0.23325-77 -0.43515-05 0.17975-10 0.3542 50915-77 -0.43585-75 0.17995-10 0.12695-97 0.2355 37478-75 -0.34355-10 0.21378-07 0.1215-92 0.9524 379448-07 0.12545-07 0.11515-92 0.1435 379448-07 0.12545-02 0.14545-92 0.1435 379448-07 0.12545-92 0.14545 3.04448-92 0.15545 3.04448-92 0.14448 3.04448 3.04448 3.04448 3.04448 3.04448 3.04448 3.04448 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.0444 3.044 3.0444 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.044 3.0</pre>	3 -0.2472E-35 -0.4354E-05
<pre>4329F+0P = 0.1162F=02 = 0.1584E=06 =4333E-05 0.1707 3769F=03 = 0.2332F=07 = 0.4351F=05 0.1707F=10 0.3541 5091F=07 = 0.4358F=05 0.1709F=10 0.1269F=07 0.2207 3747E=05 = 0.3435F=10 0.2137E=07 0.1269F=07 0.2005 5941F=10 0.2541F=07 = 0.9618F=08 0.1121F=02 0.9503 5000F 07 0.1154F=07 0.1154F=02 0.1121F=02 0.9503</pre>	5
.3769F-73 -0.2332F-77 -0.4351F-05 0.1797F-10 0.3544 .5091F-77 -0.4358F-05 0.1709F-10 0.1269F-07 0.2225 .3747E-75 -0.3435F-10 0.2137E-07 -0.5567E-08 0.3245 .471F-10 0.2541F-77 -0.9618F-08 0.1121F-72 -0.1435 .472F-07 -0.1449F-07 0.1153F-02 -0.1124F-05 0.9553	5 n.17005-10 0.3994F-08
.50915+07 -0.47585-05 0.17095-10 0.12695-07 0.2305 .37476-05 -0.34355-10 0.21376-07 -0.55076+08 0.3045 .69115-10 0.25415-07 -0.96185-08 0.11215-02 -0.1435 .30946-07 -0.14495-07 0.11535-02 -0.11245-05 0.9503	) 0.3541F-08 0.2171E-08
.3747E-75 -0.34355-10 0.2137E-07 -0.5007E+08 0.3045 64115-10 0.25415-77 -0.96185-08 0.11215-72 -0.1435 1.30845-07 -0.14495-07 0.11535-02 70.11245-05 0.9573	7 0.23255-09 0.4968E-03
.69116-10 0.25416-07 -0.96186-08 0.11216-02 -0.1435 .30946-07 -0.14496-07 0.11536-02 -0.11246-05 0.9523 .3056 03 0.00000 00 00000 00 000000 000000000	a 0.9945E-33 0.9283E-07
.ang4E-07 -0.1449E-07 0.1154E-02 -0.1124E-05 0.9523	2 -0.14355-05 -0.1861E-05
	5 0.9523E-05 -0.5354E-10
•10325401 -0******** -0******** -0*************	5 0.11255-13 0.5176E-07
.3790E-02 -0.5976E-05 0.7851F-05 0.2713E-19	

ETGENVECTOR FOR POOT NO.=

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Mode 3, Frequency = 8.4068 Hz,  $\Omega = 8$  RPM

e I Ce	NVAL U	с с Ц	528229645 22 (red)	sec. )				•	1
QEAL	D A R T						:		
l	1 U	۲		10-36011°i	-0-1487F-04	-0-77505-07	-0.26575-25	<b>0.1524F-03</b>	0.5104F-01
œ	¢ F	14			1.7508E-17	-0.2650°-06	2= 2 - 7 1 - 0	-3.2571c-01	0.1140E-01
15	5	21	日代まれたというです。	10-30189°C-	-0.2610F-06	7.1382E-03	<b>0.2553</b> =11	<b>0.1162^c-01</b>	-0.1189E-05
22	L L	58		-2.24,39F-96	0.1327E-03	-0.4816E-02	0.11755-11	<b>J.8563</b> E-05	-n.4007E-07
53	10	35		<b>3.26115−34</b>	9.5457F-32	n-1143E-31	<b>0.857</b> 05-75	<b>0-39095-07</b>	-0.2527E-06
35	4	4.2	1 E	έl-30666°ι	0.1115F-01	0.1031E-04	-1-29821-0-	-0-2459E-05	0.3955F-04
43	C.	0 <b>7</b>	きし しいいい ちょう	しいーコレビーして	0.1030F-94	0.1782E-07	-0.24525-15	0.3808 ^c -04	0.4188F-03
<b>2</b> 2	2	56		ι.]יακε-η4	0.1700F-09	-0.2411F-06	-0.14945-75	0.41855-03	0.1151F-01
57	10	۶ ۲		<b>0.17355-09</b>	-0.2475E-06	-0.1713E-04	0.41735-53	0.1287E-01	-0.1809E-04
• •	C.	70	0 F   0 F 0 F 0 F 0 F	-3.24195-06	-0.2541E-04	0.4804E-33	-0.26355-51	<b>3.4052F-04</b>	0.2330F-09
11	C:	17	9	-1.4556E-33	0.5364F-03	-0.1131E 20	0.50515-14	0.28195-09	0.1074E-07
73	5	45		3.55976-92	-0.1541F 00	0.4566F-34	0.30455-79	0.11715-05	-0.7051E-03
5	ĥ	le		ji 329uZ•u-	<b>3.256RE-04</b>	0.3676F-09	0.45775-75	-1.6945E-03	0.6917E-03
20 0	C.	u C	1 - 1 1 - 1 1 - 1 1 - 1 1 - 1 1	-3-32519-03	<b>1.5959F-09</b>	0.6363E-76	0.15975-72	<b>3.6565F-03</b>	0.1000E 01
00	F	cůl		0-10270	0.4366F-07	0.3708F-02			
I SAVI	750V	PART							
	( . H	۲		-1.41015-13	0.1151E-05	0.1893F-38	-1-=1521-0-	-0-3379F-04	-0.1527E-02
m	r. H	14		11555-75	0.1846F-09	-1-1737E-39	J.334:5-24	-7.6187c-32	-0.3573E-03
5	Ē	lì		36-3631632	-0.1218F-09	-0-304a2-04	-9.6775=-22	-0.8601F-04	-0.8062E-06
22	C F	њ.,	11-1 - 11	-1.121 AE - 19	0.254RF-04	-0-1010E-01	-0-27775-73	0.3695F-n5	0.2644E-08
<b>0</b> N	¢.	5.		7-14051°	-0.1026E-01	-0.1519E-03	52-26222*0-	0.2623F-0R	-0.1180E-09
9 i m		42		li-j2e.l	-0.2411E-03	0.2041F-06	0.29555-79	-0.11486-09	-0-6041E-05
m. ( 1		6.3			-0.2133F-06	0.7848F-08	Cl−ie511*0-	0.5481 ^E -05	-0.1103F-01
	<b>r</b> .	۲. ۲	C :::::::	<b>ロビージビントゥー いー</b>	<b>9.2930E-09</b>	-0.1125F-09	0.15415-75	-0.11056-01	-0.2177E-03
2		۲. ۲		。(-コミミット。	- <b>u</b> -1140E-00	n.2125E-06	11-=2111-0-	-3.2314E-03	-0.1835E-07
÷ ;		63. F		1136F-10	0.2366E-0F	-0.10265-01	21-22210	9 <b>°6878⊏</b> 0€	0.3059F-08
	5	<u> </u>	しいというたちょうとう	J°4440E−J2	-J.9419F-J2	0.9714E-J3	<b>n.</b> 45215-22	<b>3.2893F-A</b>	0.1904F-10
6) i  -	C. (	7 a		-0°33775-32	n.1300E-02	0.6413E-08	44-41e92°C	0.4903E-10	0.5232E-05
2. (		۱u		<b>~15345-</b> 02	n.2485F-08	0.2006E-08	0.47255-27	0.2491 ^c -05	-0.6136E-02
0		n ()		<b>1,3552F-7</b>	-0.9161E-09	0.2541E-10	-0.975;=-;5	-0.4554E-02	-0.4574E-02
7	-	i.l		-J.ol576-09	0.2359E-10	-0.1355F-04			

Mode 4. Frequency = 8.6867 Hz,  $\Omega$  = 8 RPM

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£ΙGFNVECTOR ΕΓΩ ΒΟΠΤ ΝΟ.=

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EIGENVALU	с ц	.54580078F n2 (rad/s	ec. )					
RFAL PART								
<b>1</b> Tŋ	~	0.8512E 10	<b>3.5379E-02</b>	-3 <b>-1260F-</b> 75	-0-9141E-JB	-0.1735E-06	-0.3073F-02	0.8534E 00
01 <b>8</b>	14	0.5362F-02	0.29445-05	-7.1435-08	-0.179cE-76	0.3033E-02	0.3169F 00	0.5502E-02
15 / 10	21	0.4201E-05	-9.97775-70	-1.1755E-06	21-32526-0-	0.3175E 00	0.5530E-02	0.2550E-05
ZZ IV	e.	-0 <b>-1</b> 9985-19		?7655-72	1レーコミごうで・ビー	9.5590F-32	0.1732F-05	-0.5502F-0R
29 IN	ς. Έ	-0-1697F-34	16975-02	s+41E-01	0.57125-72	0.7143E-05	-0.23285-09	-0.1697F-06
35 TŪ	42	0.1689E-32	-3.17105 90	2.572JE-J2	0.19555-75	-0-1994F-0e	-0-15485-06	-0.7777E-03
43 TO	40	-0-1713E CO	0.57265-02	7.2246F-05	-0°10126-70	-J.164¤E-35	1.7751E-03	-0.1999E 00
50 TO	56	0.5749E-02	C.2021F-25	0 <b>1</b> -3232-10	-0.15135-76	-1.3093F-05	-0.2025E 00	0.5951E-02
57 TU	63	-3.7775F-05	<b>0−10¢0E−0</b> 0	-3.1541E-06	-0.3405E-75	-0.2037F 00	0.6157E-02	-0.1760E-04
64 TU	0	0.10685-79	-0.1635E-0A	-2-3412E-05	-0.293lf JJ	9.3605F-02	0.2113E-04	0.1369E-09
71 17	17	-0.8744F-07	54675-04	-7.2730F 00	-9.11735-32	3.27146-04	0.1623E-09	0.86525-08
13 IV	94	-0.35956-34	-1-4169F 0r		ヤC-コlょヤc。い	0.1742F-09	0.7123F-07	-0-3400F-04
R5 TO	10	-1.4510E 33	-2.57965-02	12735-04	0°23775-39	· 1.75395-36	- 3.15645-04	-0.5242F 00
62 . 10	ЧP	-0.5225F-12		7.3453E-09	C-3523E-36	-0.1619E-04	-0.6288F 00	-0.2275E-01
U1 66	102	-0.1952E-73	J_3728F-09	20-3923200	-0-5315E-34			
VARVISAVI	PAGT							
1 10	7	<b>0.4685E JJ</b>	7.12615-71	*2535E-08	-0°-15210-00	0.13256-07		0.5213F 33
5	14	0.1440F-01	2 <b>° c : 24 c - 3</b> f	-[.]acilE-08	0.17255-77	3.1°10E-32	0.1660F 00	0-1311E-01
12 IÚ	21	1367E-34	00-10823	Li-servi*.	-0.15515-~2°	n.1805€ 1n	1.1362F-01	0.29515-96
22 TÚ	а: ¢	-J-3505E-JA	7.1200E-07	どいーっじ にん にー	- <b>ປ</b> ຸ5ເງ2E−ງໄ	0.1229E-01	-7.4366E-07	-0.1092E-10
29 · TJ	۳. ۳.	<b>1.97515-09</b>	-j.c5a5t-03	10-31659*	0.12525-31	-0.2028F-06	-3.17925-08	0.97546-08
36 10	÷.	0.10365-02	1107E 0C	10-36Ell	-C-34541-0-	0.1150F-08	<b>3.9472F-08</b>	-0.4500F-03
43 TU	4	-0.1114F JJ	10-30021-0	-1.245aE-96	οι-οιξτέ•υ	0°9473E-09	<b>0.4657F-03</b>	-0.12805 00
	56	0.11525-71	1751F-JE	-15?2F-0A	0.92735-QP	-0.1904F-04	-3.1295E NO	0.1269E-31
57 17	•	0.3870E-34	dC−dćaýl°:	T.9473E-08	-0 <b>-</b> 10202-04	-9.13015 39	0.1386F-01	0-9596E-06
64 TU	70	<b>1.1726F-19</b>	3°-3576F-08	+U-J5+61-J-	-0°12142 00	-u.165nF-nl	-7.1130E-05	0.1706E-08
11 10	11	0.34045-03	-0°3000c-03	-7.2271E 00	-0-53465-01	-0.1224E-35	. J.1608⊏-09	-0.1925E-09
TA TO	94	-0 <b>.</b> 3445F-03	-U-2444F 00	-7-87155-01	-0.17305-75	0.1494E-08	-J.4426E-09	-0.2730E-03
85 10	16	-0.2714E 00	10-30336°C-	7014E-06	0.1-215-1.0	-0.4296E-09	1.4371F-04	-0.3700F 00
ÚL Zo	8 0	0.7130517.0	-1.735E-19		-0.45715-30	J.4373E-03	-0.3702F 00	0.1252E 00
CI 66	102	0.33335-37	-0° \$1 \$2 E - Ja	7.2817F-11	0°2218E-J9			1

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Mode 1, frequency = 2.2851 Hz,  $\Omega = 12 \text{ RPM}$ 

(rad/sec)
ĉ
jùlo∠šc†l°c

		•								
י של געג גע געג גע	7636				:	:				
•:	ų 1		0.27375 70	1 <b>6−31≈</b> 54°0~	0.1344E-05	0.54145-39	_j.1_56E-j7	-J.4746E-03	-0.2232E 00	
H-	۲ ۱	14	しーコービンサ・レー	0-1344E-05	-0*24445-09	-0-17465-37	21-39525-0-	0.12925 00	-0.4526E-01	
۱. 	r +	12	<b>1</b> 250E-05	n.4891F-09	-Ū-1744E-O7	-0.46785-33	Cv a2ežl•v-	-1.4577E-01	0.12495-05	
<b>f</b> .	r •	۲, 1	00-12007°c-	-0-17445-07	-0-4678E-03	0.5500E-01	10-36154-0-	0.11765-05	0-30165-09	
81 811	Į,	а 5 С	-0-174n5-07	-u-4436E-Na	-0°22802-01	-0.4517F-01	0.11755-25	-ū-34642-ū	-0-1740F-07	•
47 (*)	ł	¢.,	<b>2</b> - - - - - - - - - - - - -	Û°-30∠bč°û	-0.45115-01	0.1162E-75	<b>2-15951-</b> 03	-0.1737F-07	-0.4227E-03	
r. T	ŗ	U •†	-7.29775-51	-1.4511E-01	0.1162E-05	-0.1531E-29	-3°1132-01	-0.4227E-03	0.4074E-05	
L	f.	ų, L		0.1156 ^E -05	0.336011	-0.17345-37	ビレーコヒヒビ マービー	0.40585-05	-0.2083F-01	•
r 11 -	r +	۲ ع ب	30-357-26	1.3360F-11	-0.17585-07	-0.4038E-73	0 4 7 4 2 E - 1 E	9.3398F-02	-0.9505F-06	
• •	r	1	11-355651	1766  07	-0.403AF-33	0.48605-35	:ú-32cē-°ú-	7.3514c-05	0.340nF-11	
; '	t Þ	<b>,</b>	-J.14975-97	1211E-03	0.579PE-35	-J.83675-Jl	3r-jages C	0.34445-11	-0.1100E-07	
ŀ	1	.t 8	3.115CF-73	7.6332E-N5	-0.7245F-J1	0.5977E-05	<b>11-36745.</b> C	-0.86865-08	0.2488E-03	
11 11	{ }	• - 17	· - Trate-NS	<b>Ιυ−</b> ⊒28οέ°υ−	0-6044F-05	n.3567E-11	ヒレーコタビビックレ	0.6500F-03	0.1234E-04	
( 11	1	n P	1,477CE 11	-1.405FE-N5	U.3973F-11	9.42075-37	°,1565E−12	1.1235E-04	0.1000F 01	
, , , ,	r •	<b>,</b>	70-32262-04	U_4076-1]	0.43115-07	0.15436-32		-		
	****	) () ()						•		
• -	r -	P.	u-32501°ú	サレーヨビロデ しゃの	-n.3753F-nR	-0.1146E-10	-3°-7343E-12	-0.46805-05	0.2132E-03	
11	f `	•	-J.32695-13	· 0°54745-08	-0.1152F-10	-0.73405-10	ji-jEril.n	<b>0.10255-02</b>	-0.2753E-04	
н . ч	(  -	5	-U <b>*</b> 1724E-J0	0[-306vl*ŭ-	-0.7332E-10	-0.4417F-05	1.9573E-25	-0.2360F-03	0.3418F-08	
<b> </b>  -,	ſ		-1-32CI1°L-	01-326210-	0.5866F-06	0-3077F-03	71-30EED"1-	0.7506E-10	-0.9742F-11	
i.	( )	з с	72155-17	-j.j.gne-ne	-7.10345-03	-0.21955-33	0.1636F-29	-0.8749E-11	-0.7315E-10	
4. 19	1 +	ŗ,	96-39521.05	13245-03	-0.12565-03	0.5067E-30	-1.512E-11	-0.73005-10	-0.2410E-05	
н. А	1	1. 1	*87215-74	-0-19685-03	0.11715-08	-0.5592F-11	-0.73705-17	-0.70395-06	-0.9436E-05	
6 · 10 ·	( )	-4+ 11		0°-32759.0	-0.36145-11	-n.7290E-10	-7.14975-25	-0-3048c-05	-0.5663E-04	
, P h-	r •	5 3	-J.35555-JP	-1.19101	-0.7340E-10	-0.149JE-05	2.2317E-25	0.227RE-04	-0.7966F-0R	
. 1 14	ł	1 4	- <b>5.9</b> 225-12	-3°73595-10	-0-14006-05	-0.2263E-J3	-3-3:2:05-53	0.10985-07	-0.9843E-12	
• '	1	r 7	-J.67115-13	-0-4662E-06	-0-5154404	-0.31085-03	20-39461-01	-0.34445-11	-0.5077F-10	
•	1	1	い。ろちなった」へん	-0-53545-03	-3.27505-13	<b>0.2271F-07</b>	-1.7552E-11	-0.4162E-10	0.8284F-06	
1/ 11	ſ			-U-16271-07	0.2307F-37	-0.272E-10	<b>1-16101-1</b>	0-22655-05	-0.2331F-02	
р. 12	ſ	11 12	20-3109100	I E J L E - 0 1	-0°-96°0E-10	0.1532F-39	1.5593E-05	-0.23335-02	0.3552F-02	
(† 1)	( +	¢ ,	-0°73365-07	-n.9603r-10	0.15515-09	<u>.5556F-05</u>				

Mode 2, frequency = 4.2027 Hz,  $\Omega$  = 12 RPM ~ בנקעערכדות בוע מחוד עון=

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(rad/sec)	
6	
1.26496250F	
FIGENVALUE=	

OFAL	DART								
	Ú,	۲.	-0-3641E-05	0.11425-75	-u.4a52E-01	-1.53515-04	-0-11445-02	<b>0.8770F-08</b>	0.4101E-05
æ	1	14	7.1157E-75	10-37905-0-	2.53535-34	11435-32	<b>3.</b> 51355-CA	2082c-05	0.1151E-05
15	c ¥	Ic	16-32204-0-	tu-sus st "U-	<b>ςC−∃6εll*c−</b>	9C-39545	0-241az-02	<b>2.1168E-05</b>	-0*40756-01
22	C F	28	0-4891E-04	-0.11395-12	7.8774F=03	0.5548F-J6	1.154E-35	-0.32795-01	-0.3144E-04
29	5	35	-0-11306-02	0.7245c-na	J. 90835-06	9.11625-35	-0.327at-01	0.31305-04	-0.113nF-02
Ϋ́Ε.	5	42	0.746ac-ng	-0-24026-35	°.1153F-05	-1.3137E-71	-J-1513c-04	-0.11235-07	0.62125-08
5	42	40	<b>0</b> *58475-06	0.11575-25	-3.31365-01	P.1504E-04	-0.1123E-r3	0.6321F-08	0.16495-06
<del>ر</del>	C F	56	0.1150E-05	1	-u-5509E-77	-u-jll1e-J2	0.522750	0.1748F-06	0.8315F-06
51	5	. 69	-9.98005-01	-0-26406-04	-3.1122E-32	0.5348F-08	9°-10202-07	<b>3.5082E-06</b>	-0.1654E 00
÷4	C. ►	۰ ۷۷	-9.56556-07	-0.112452	<b>3.5406E-0</b> 8	0.12635-36	0.86525-25	0.1272E 00	-0.5871E-07
11	C F	77	EU-3647E-03	-n.P347c-15	0°374E-07	-0-11275-05	0.2524E ry	-1.6023F-07	-0.5877E-03
79	<b>C</b> : ₩	84	- 2- 32 24 76 - 77	C-31418-0	-j.72735-35	0.2971E 00	-0.6newe-07	-7.4679E-03	-0.2056E-07
ςa).	Ē	10	0.67635-07	32-3907c°ú-	n.?9355 jn	-v.6122c-07	9.77835- <u>3</u> 3	-1.12875-07	0.2631E-07
66	C F	аç	-0-34346-05	201252-0-	-0.6252E-n7	0.20675-32	るじーコテレシヤ・ひ	2.1102F-07	-0.2833F-05
66	C H	107	-0.101.F JI	-0-92529-0-	1,1090E-12	0-1471-00			
ICVAL	YAAY	PART							
-	5	۲	-0-2840F-07	-0-44275-17	-J.6529F-74	-0.1758F-36	-U-5069E-J6	2.11425-09	-0.8928E-07
đ	C L	14	とひーヨン 1 マミ・レー	J32222.	-3.1298E-36	-0.5058E-06	-1.24515-70	- J. 9690F-08	-0.40325-07
15	5	۱۲	-0-35156-04	-0.15^56-^6	-j.5n4AF-16	01-24700.	といううに はちやじー	-1.2731E-07	0.11495-06
22	Ľ,	۵.	-0-10845-06	すいーゴビオンションー	23de-Ja	0.511 AE-28	21-30558-0-	-7.14335-04	-0.7137E-07
<del>د</del> ک	C.	35	-0-20005-02	0.45125-10	-j.q472E-09	とじーコンドほう・いー	70-22071-0-	-3.4431E-07	-0.5009F-06
36	۲ ۲	42	-0-16585-09	0.6371c-19	-0-3224F-07	-0.11955-34	-0-624753-0-	-0.4976E-06	-0.5533E-11
43	-	40	-0-1430E-JB	-J.29235-J7	-3.15445-04	0.57545-38	-0.4075E-35	-0-1064E-09	0.4353E-09
5.7	5	56	-0.3060F-77	-ù-1342i-u+	0*4a23F-07	-3.4957E-06	-0-523aE-12	7.4457F-08	-0.2714E-07
57	Ę	63	-0-43236-34	yi-sca≯2*U	*ta15e-04	-0.6301F-10	0.42750	-1.2300F-07	-0.7310E-04
64	Ċ.	Ú r	0.35845-06	Ju-siebt u-	Ul-⊐ZiilL°u-	9.1513c-07	-n.32375-07	0.5659F-04	0.5446E-06
2	۲ ۲	77	-3.427aF-06	u.20045-1~	<b>1.26625-07</b>	-0.22735-07	0.11225-13	j.3911E-06	-0.30635-06
19	C F	84	0 <b>.</b> 90005-13	0.37015-17	-0-16436-07	9.12775-03	0-34445-07	-3.7101E-06	0.1045E-09
9.5 1	5	16	0.39745-07	ai−39£26°0-	1300E-03	-3.14375-95	o.llsie-re	1.1004E-09	0.6670F-07
62	5	Вę	0.32476-09	-0.1075c-12	-7.85045-75	0.9045E-06	0.4412E-12	J. 6907E-07	0.3326E-08
60	C F	102	-0.43805-03	-0°82040-02	90-25162°C	-0.1789F-16			×

EIGENVECTAR FOR POOT NT.=

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Mode 3, frequency = 8.3914 Ez,  $\Omega$ = 12 RPM

	02 (rad/sec)
	0.52724609F
	ETGENVAL UE=

0 E AF	TOAC								
		~	<b>J.1028E 03</b>	-0-14295 20	-J.5559E-J4	-0°43236-36	-0.17355-35	-0.3541E-03	-n.1075F.00
œ	۲,	1 ¢	-0.1475F jn	-0.82425-04	7.4155E-36		E	3.42195-01	-0.13495 00
15	( F	21	1717E-74	-0.30ng-n6		6643426800-	-7.42146-01	-n.1374E 00	-0.1041E-04
22	40		0.36765-06	-0 <b>-11</b> 08E-02	-0.3267F-03		-0.1337E 00	n.43825-04	-0.2242E-06
Ę	C F	35	1652-05	-0.1330F-03	っ。26735-32	CC =1221*C-	1.4242F-04	<b>0.2182</b> €-06	-0.1655 ^E -05
35	42	6.5	-0-1410c-03	-0.28275-02	-3 <b>.</b> 13795 20	0.53425-74	-j°i-jlc-1°ù-	-0.1610F-05	<b>9.1022F-04</b>
43	11	. 04	0.70235-52	-0.1306F 30	1.5353E-34	Lu-sj_té*0	-J.16175-05	3.39745-05	0.2212E-02
5 Q	C. 4	56	-0.1284E Jr	い。57265-74	j.1355c-3e	50-22251-0-	0-3555'°ú	3.2207E-02	-0.1357F 00
57	C: F	63	-0.37935-04	9.13605-3P	-J.] 5095-05	0.1-575-33	C.2198E-02	-7.1413F 00	-0.13326-03
64	C.	70	0.10755-08	-0.1587F-05	0. P556F-04	20-2319200	7.1391F-01	0.2489F-03	0.1420E-08
71	C.	77	-U-\$666°U-	0.1541c-n7	1.2677F-92	0.2455E MO	1.3125E-03	0.1715E-08	0.7389E-07
7.9	C F	5	n.1583£-n2	j.26¤]⊏-j2	ひぃ ヨダネタミック	0-2-11-02-U	°,1a51⊏-09	1472E-06	0.1015F-02
ዓ የ	5	10	j.27715-92	<b>1.33455 10</b>	3.15775-03	ai-sei22*6	Sũ-dbeic°c	-0.1231E-02	0.3140E-02
5	1,	c O	-0.5342E hh	-0°12051-05	b(− <u>⊐7</u> 2,2 °;	90-36236 0	1° JakgE−J¢	3.29225±-02	0.1000F 01
60	17	<i>i</i> L I	-1.21265-23	0°-38032°u	-2002€-36	22-35-390			
12121	VOVV	D A7 T							
-1	C Fi	۲	0.1475F JA	-0.9896-74	-1169E-14	Lí-3: 3=1°U	24965-11	-0.7900E-03	n.1665F 00
σ	5	14	じょうらん ビニコス	40-32411°0-	1,1841E-J7	- 1、1 5 5 2 5 - 1 1	r, 7779E-03	0.3238F-01	0.84895-05
5	( +		1.7072F-75	0.212re-27	-J.23125-11	FC-3-1-6-0-	10-38°l2°C	7.2669F-03	-0.79465-05
22	5	а (-) а	lu-séul2∙u	-0°12512-11	2,6899F-73	16-301-200-	tú-sovús°u	0-3715F-05	<u>0.2599E-07</u>
53	5	ŝ	-J.2113E-11	-0.4126E-03	li-i2li2	アレービー・アウ	, ?7  3F-05	0.2590E-07	-0.14755-11
36	۲J	¢.7	n.41105-03	10-⊒020€*0-	<b>11175-23</b>	0.21 HIF-25	Lū-386ė2°ü	-J.J200F-11	-0.18665-03
£ 4 .	C 1-	<b>7</b>	10-38288°C-	ču−jčoÿl°ü	-3.70925-35	しょうろうちょう り	-1.1435E-11	<b>0.1860^E-03</b>	-0.950RE-01
ر ۲	C •	55	20-3103100	-3.11345-00		[[];]*U-	-1,!?r55-06	-J.95575-01	0.1485F-03
57	C.	63		とじーゴサをいと。い	21-352Cc*u	90-3333;°C-	- ].35495-01	0.1583E-03	-0.78055-09
64	Ċ F	7.7	10-3000E-0	<b>J-1114</b> E-1C	16755-96	CC 3=111°0-	っ。 こうしちロークチ	-0.13R7F-08	0.31135-07
17	C.	77	21-34455.0	-ŭ-d666r-ŭ6	-3.1255c 00	€C-3to.l*6-	-0*5306F-00	D.3001F-07	-0.1161E-10
79	5	44	-0-13715-75	-0.1306F J <u>C</u>	±20475-03	51-37252 1	1°, 3040°, 01	-j.1997E-10	-0.1228E-05
35	C.	١٥	-n.1362F 31	-0.2729F-13	3.2157F-nº	0.22-75-27	<b>℃I-</b> 36€2 <i>2°</i> 6-	-9.61745-06	-0.1546F 00
6	C, ₽	38	-J.Q.G.G.G.F.F.J.G	1.12925-17	2442e-08	-0-255250-	- 1.157E-05	-1.14745 00	0.4027E-03
5	ŗ	117	r.lalat-37	ĸ└−コムヒ9ሪ*∪-	11-34042	9.14445-35			

Mode 4. frequency = 8.6944 Hz,  $\Omega$  = 12 RPM

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1. 3.5462 "00.66" [0] (Tad/sec) 1. 3.3275-57 1. 3.3275-57 1. 3.3275-57 1. 3.3275-57 1. 3.3275-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.3775-57 1. 3.377		,					•	
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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	14		0.79005-05	1.13615-17		C - 12/CC - 0	20-16-26	0 027700 0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12	70825-05	-0-21605-27	-3.0729F-96	-0.29135-72	3603C-0	1.83935-07	0-1016F-06
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 A	1.0065E-0P	- u - c 1 ) e c - J e	7.2941E-02		0.862753	11966-04	-1.11005-07
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	<u>م</u> ۲	-0-3672E-36	-1-17821-1-	10-3830c-C-	0.85565-32	0-1132E-1-	70735-00	-0-34026-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	42	21-32021-0	-0.17a7F nu	1. 2592E-02	0.1139F-34		-1,91205-06	-0-395-03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	49	-0.1791F 73	1.555ac - 12	7.11435-04	0.13735-38	91-3CElo"U-	2. 8234E-03	-0.2093E 00
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	56	Ú-8224-02	0.11495-74	0°2300E-00	-0-80376-36	-0-57855-75	-7.21215 00	0.8936E-02
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	63	- U-42825-04	r.54715-19	-1°3100E-08	-0.6532c-05	-0.21345 27		-0-9730E-04
77 $0.44776$ $0.46376-04$ $0.14376-05$ $0.66376-04$ $0.63376-04$ 91 $0.47706$ $0.630466-04$ $0.11456-75$ $0.23976-04$ $0.06316-76$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.06066$ $0.060666$ $0.060666$ $0.060666$ $0.060666$ $0.060666$ $0.060666$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.06066606$ $0.060666066$ $0.060666606$ $0.060666066$ $0.060666066$ $0.060666066$ $0.060666066$ $0.060666066$ $0.0606666066$ $0.060666066$ $0.0606666066$ $0.060666066$ $0.0606660666066$ $0.06066660666066$ $0.06066660666066$ $0.060666606660666606666666666666666666$	70	0°2281E-00	-0 <b>-</b> 32735-36	-1.5530F-05	-0.3088F 00	C32052-0	2.11705-03	0.7382E-09
q4 $-0.47765 - 0.43015 - 0.11575 - 0.11575 - 0.30315 - 0.30375 - 0.80265 - 0.4         q1       -0.47765 - 0.1256 - 0.0 0.569145 - 0.6065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.66065 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6605 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - 0.60005 - 0.600000 - 0.6000000 - 0.6005 - 0.6005 - 0.6005 - 0.6005 - $	77	-U-44145-JF	-Û-Vê6685-J4	-0°3040E 00	-0.99995-02	0.14975-73	0. 2917E-09	0.53025-07
01       -0.47705 fm       -0.18955-01       0.59145-04       0.11535-08       0.14155-5       -0.24895-05       0.0.45775-1       -0.56595 fm       -0.33785-02         107       -0.10985-77       -0.27985-72       0.19595-05       0.45775-1       -0.5595 fm       -0.33785-02         117       -0.10985-77       -0.27985-05       0.1725-07       0.15355-07       -0.41295 fm         114       0.274915-71       -1.16676-07       0.166895-07       0.153556-07       -0.255556-05         21       0.274915-71       -1.16676-07       0.168965-07       0.153556-07       0.125565-07         21       0.274915-71       -1.16676-07       0.168965-07       0.153565-07       0.155565-07         21       0.274915-71       -1.18576-01       0.2153157       0.1103566       0.135565-07         21       0.27656567       0.175-11       -2.184965-01       0.2135656-07       0.1555657         28       0.16676-07       0.158965-01       0.2135656-07       0.1555657       0.165565-07         28       0.1655667       0.175-11       -2.135665-07       0.15556577       0.15556577       0.15556577         28       0.165765-07       0.15846507       0.15556577       0.155565777       0.155565777       0.1555	44		-0*4301E JJ	-2.1514E-01	0.13595-03	0.96315-75	J. 39975-06	-0-80265-04
98 $-0.1256-0^{\circ}$ $0.21587E-06$ $0.1335E-04$ $0.4577E-5$ $-0.1256F-0^{\circ}$ $0.4577E-5$ $-0.1236F-02$ $0.4129F-02$ $0.4129F-02$ $0.4129F-02$ 7 $0.2741F-7$ $0.25321F-08$ $0.172E-07$ $0.172E-07$ $0.4577E-02$ $0.4129F-02$ $0.4129F-01$ 7 $0.2741F-7$ $0.25321F-08$ $0.172E-07$ $0.1235F-07$ $0.2559F-01$ $-0.3376F-05$ 21 $0.2772F-7$ $0.172E-07$ $0.1531F-7$ $0.1235F-01$ $-0.3376F-05$ $0.1235F-01$ 21 $0.457F-07$ $0.118F-7$ $0.172F-01$ $0.1531F-7$ $0.1531F-7$ $0.1235F-01$ 21 $0.457F-02$ $0.1531F-7$ $0.1531F-7$ $0.1531F-7$ $0.1521F-07$ 21 $0.457F-02$ $0.1531F-7$ $0.1531F-7$ $0.1521F-07$ $0.1572F-01$ 21 $0.457F-02$ $0.1531F-7$ $0.1531F-7$ $0.1555F-01$ $0.2556F-07$ 21 $0.457F-02$ $0.1522F-7$ $0.1552F-7$ $0.1555F-01$ $0.1572F-01$ 21 $0.2566F-07$ $0.1555F-01$ $0.1572F-01$ $0.1572F-01$ $0.1572F-05$	10	-U*47705 AN	lü-2508l°u-	0-5914E-04	0.11535-08	0.14155-75		-0-6606F 00
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	<b>9</b> 6	-0.12596-07	-0°60226-33	0.1335E-08	0.1959E-05	0.45775-2+		-0.33785-02
187 $0.37415$ $0.37415$ $0.41295-01$ $0.41295-01$ 14 $0.372415-01$ $0.477955-01$ $0.53215+03$ $0.41295-02$ $0.41295-01$ 14 $0.2724915-01$ $0.477955-01$ $0.13955-01$ $0.13755-01$ $0.37255-01$ 14 $0.27215-01$ $0.13755-01$ $0.15725-01$ $0.15725-01$ $0.15725-01$ 15 $0.70005-07$ $0.16655-07$ $0.16655-07$ $0.16655-07$ 15 $0.16655-01$ $0.15725-01$ $0.21725-01$ $0.215725-01$ 15 $0.16655-01$ $0.15725-01$ $0.215725-01$ $0.215725-01$ 16 $0.16655-07$ $0.15656-07$ $0.15725-01$ $0.15725-01$ 16 $0.16655-01$ $0.113555-01$ $0.21725-01$ $0.15725-01$ 17 $0.209456-01$ $0.217255-01$ $0.217255-01$ $0.15725-01$ 16 $0.65945-07$ $0.13375-01$ $0.15525-07$ $0.15655-01$ 16 $0.66945-07$ $0.13375-01$ $0.15525-07$ $0.15726-07$ 16 $0.25945-07$ $0.15565-07$ $0.15565-07$ $0.15726-07$ 16 $0.25945-07$ $0.15565-07$ $0.15565-07$ $0.15726-07$ 16 $0.25955-07$ $0.15565-07$ $0.15726-07$ $0.15726-07$ 16 $0.259555-07$ $0.15565-07$ $0.15726-07$ $0.157726-07$ 16 $0.259555-07$ $0.15565-07$ $0.157726-07$ $0.157726-07$ 16 $0.259555-07$ $0.15565-07$ $0.157726-07$ $0.157726-07$ 16 $0.259555-07$ $0.15575-07$ $0.157726-07$ $0.$	žul	-0 <b>-1</b> 048E-02	ບ້າວິກຮູຂະງາວ	3.15P7E-06	-0.3153E-04			
7       0.3741F 7       0.4756571       0.4126570       0.4126570         21       0.22491E-01       0.4756577       0.5321F-08       0.10875707       0.16965701       0.22535011         21       0.4071F-05       0.16605707       0.16805701       0.16255701       0.22535011         28       0.7005707       0.166157       0.16805701       0.2172501       0.2205501       0.3255501         28       0.7005707       0.16615701       0.12124501       0.21559501       0.1605501         29       0.16615701       0.1336501       0.2175701       0.21559501       0.16055501         29       0.444501       0.20895501       0.21556501       0.1572505       0.16055501         40       0.98045501       0.2175701       0.21575577       0.16555601       0.1572505         40       0.801501       0.21556501       0.21556501       0.21556501       0.1572505         40       0.20895504       0.1866504       0.186555670       0.1572505       0.1577505         40       0.20895504       0.15265501       0.15265501       0.1577505       0.1577505         50       0.20895504       0.15265501       0.15265501       0.1577505       0.15775505         50	 <b>A</b> 0 T							
14 $0.294915-01$ $0.47865-07$ $0.16605-07$ $0.16655-01$ $0.272515-01$ 21 $0.402155-57$ $0.116615-77$ $0.16665-07$ $0.12655-07$ $0.12655-07$ 28 $0.70005-07$ $0.16615-77$ $0.16655-07$ $0.12655-07$ $0.12655-07$ 28 $0.1695-07$ $0.16655-07$ $0.12655-07$ $0.12655-07$ 29 $0.6051-07$ $0.16655-07$ $0.12655-07$ $0.12655-07$ 29 $0.6051-07$ $0.2572-01$ $0.22535-01$ $0.22555-07$ 29 $0.80515-01$ $0.21275-01$ $0.21555-77$ $0.12655-07$ 20 $0.80515-01$ $0.21555-01$ $0.215555-07$ $0.15555-07$ 40 $0.70015-01$ $0.20855-01$ $0.22655-01$ $0.25755-05$ 40 $0.7015-01$ $0.15555-07$ $0.15555-07$ $0.15725-05$ 56 $0.7015-01$ $0.15555-07$ $0.15725-05$ $0.15725-05$ 57 $0.15725-05$ $0.15725-07$ $0.23955-08$ 57 $0.55055-07$ $0.15555-07$ $0.23955-08$ 56 $0.705505-07$ $0.15555-07$ $0.15725-05$ 57 $0.16575-07$ $0.15725-05$ $0.16706-01$ 57 $0.55055-07$ $0.15725-05$ $0.15725-05$ 57 $0.55055-07$ $0.15725-05$ $0.16706-01$ 57 $0.55055-07$ $0.15725-05$ $0.1657209$ 57 $0.55075-07$ $0.15725-05$ $0.1657209$ 57 $0.55075-07$ $0.12395-07$ $0.204557-07$ 57 $0.55075-05$ $0.1146570$ $0.15235-07$ <t< td=""><td>~</td><td>0.3241F 00</td><td>ir-gace2°u</td><td>7.6021E-05</td><td>0.11725-07</td><td>0.15355-77</td><td>-J.1210F-02</td><td>0.4129F 00</td></t<>	~	0.3241F 00	ir-gace2°u	7.6021E-05	0.11725-07	0.15355-77	-J.1210F-02	0.4129F 00
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	14	0.7491E-01	-10.4780E-15	3.5321F-08	0.1690F-07	7.14255-73	2-11375 00	C-2253F-01
$\begin{array}{llllllllllllllllllllllllllllllllllll$	12	J-402lé-ué	J•11866-77	J.1660E−07	-0.11875-72	i ilisit"	1. 2359F-01	37265-05
35       0.4635-01       0.2172-01       0.2172-01       0.1035-07       0.16655-07         42       0.40515-03       -0.4635-01       0.888375-01       0.45565-07       -0.32665-03         42       0.40515-03       -0.80175-11       0.20656-01       0.15595-07       -0.35656-03         42       0.40515-01       0.15765-07       0.15595-07       0.15595-01       -0.337590         40       0.20645-01       0.15565-07       0.15565-07       0.15595-01       0.21575-05         56       0.2067601       0.15565-07       0.15525-07       0.15725-05       0.15725-05         56       0.2067607       0.15565-07       0.15525-07       0.15725-05       0.15725-05         56       0.2076501       0.15365-07       0.15525-07       0.15725-05       0.15725-05         56       0.2595501       0.1556507       0.1556507       0.15575-05       0.16776-07         70       0.5595501       0.155750       0.1566507       0.1557507       0.15575-05         70       0.1566501       0.1566507       0.1566507       0.1657607       0.1657607         70       0.55950507       0.1566507       0.1566507       0.15575607       0.1657607         70       0.5567507 <td>28</td> <td>eu-juoul "u</td> <td>r_1661c_17</td> <td>20-332E1.C</td> <td>-0-4987E-01</td> <td>0.21235-11</td> <td>1585c-05</td> <td>0-139651-01</td>	28	eu-juoul "u	r_1661c_17	20-332E1.C	-0-4987E-01	0.21235-11	1585c-05	0-139651-01
42       0.90516-03       -0.80175-11       0.2066-01       0.803375-01         40       -0.81445-01       0.208355-11       -0.32665-03       -0.93375-01         40       -0.81445-01       0.208355-11       -0.13505-03       -0.93375-01         56       -0.81445-01       0.208355-01       -0.32665-07       -0.35205-01       -0.21985-01         56       0.2065-01       -0.13505-07       0.15265-07       -0.35165-01       0.15725-05         57       0.2067-01       0.15725-07       -0.337355-01       0.15725-05       0.16776-01         57       0.56965-07       0.15065-07       -0.33355-01       0.15725-05       0.16776-01         70       0.56965-07       0.15765-07       0.13325-01       0.15725-05       0.16776-07         71       0.56965-07       0.15765-05       0.16776-07       0.15725-05       0.16776-07         71       0.56965-07       0.15265-07       0.012975-05       0.16776-07       0.16776-07         71       0.56965-07       0.15265-05       0.16706-05       0.16776-05       0.16776-05         71       0.56965-07       0.15295-05       0.16706-05       0.16776-05       0.16776-05         71       0.569650       0.16606-05       0.1	۲. ۳	20-35091-0	ビレーコチキビチ・ビー	-7.4633E-01	n.21725-01	-J.21095-75	<b>J.11035-07</b>	0.16C5E-07
40       -0.81445-01       0.208355-01       -0.93375-01       -0.93375-01         56       0.27015-01       -0.208355-01       0.15725-05       0.15725-05         57       0.62965-01       0.15725-05       0.15725-05       0.15725-05         67       0.62965-01       0.15725-05       0.15725-05       0.15725-05         70       0.62965-01       0.15725-05       0.15725-05       0.15725-05         71       0.65935-01       0.15725-05       0.15725-05       0.15775-05         71       0.55035-03       0.15775-05       0.15775-05       0.15775-05         71       0.55035-03       -0.16776-05       0.11465       00       -0.193755-03         71       0.55035-03       -0.16776-05       0.11465       00       -0.193555-03       0.16576-03         71       0.55035-03       -0.16505-05       0.11465       00       -0.11365       0.1554255-05       0.165765-05         71       0.55035-03       -0.16505-05       0.11665       0.012395-05       0.155725       0.56955505       0.27426       0.227425         71       0.1775       0.1275       0.12575       0.12575       0.69055505       0.27426       0.20766       00         91	4.2	0.8051E-03	1-32 IU8 -0-	<b>11–30805</b> -11	0°8043è-09	3.15226-77	2.1559E-07	-0-3266E-03
56       0.27015-1       -0.200555-01       0.15515-01       0.15725-05         67       0.629655-07       0.15775-07       -0.337355-04       -0.04595-01       0.15725-05         70       0.629655-07       0.15775-07       -0.33735504       -0.045955-01       0.15725-05         70       0.15775-07       0.15775-04       -0.13525-05       0.16776-07       0.15725-05         71       0.55035-08       0.15775-07       0.15775-07       0.15775-07       0.15775-07         71       0.55035-08       0.15775-07       -0.18535-07       0.15775-07       0.15775-07         72       0.55035-08       0.11465       00       -0.11465       00       -0.165750       0.15775-03         73       0.56035-03       0.115450       0.115450       0.115450       0.2745501       0.2745501         91       -0.20045       0.11775       -0.24055-04       -0.2745501       0.27765       0.2076501         92       -0.11775       -0.56675-05       0.12395-07       -0.27765501       0.2076501         93       -0.40065-07       -0.13705-03       0.1703355-05       0.2076501       0.2076501         93       -0.40065-07       -0.137055-05       0.12705-03       0.2076501       0.	¢ 0	-0.8144F-71	G.ZARZE-71	1350F-US	0.1294F-07	n.155357	1. 3520E-03	-0-33375-01
67       0.62966-01       0.15726-07       -0.33236-04       -0.04036-01       0.15726-05       0.15726-05         70       0.16476-07       0.15776-07       -0.33476-04       -0.13326       00       -0.16706-07         71       0.55076-08       -0.51996-07       -0.33676-05       0.16706-07       -0.185076-05       0.16706-07         77       0.55076-08       -0.51996-03       -0.11465       00       -0.19976-15       -0.16736-07         77       0.55076-08       -0.51977       -0.18776       0.011465       00       -0.19976-15       -1627426         78       -0.58105-03       -0.1877       -0.16666       00       -0.11465       0.156726-77       -0.46156-03         94       -0.20046       01       -0.12396-07       -0.103356-75       -0.27426       00         91       -0.20046       01       -0.12396-07       -0.123356-75       0.20766       00         92       -0.1775       -0.12665-76       -0.23356-75       0.12596-07       -0.207666       00         92       -0.1775       -0.1275       -0.12672       -0.25665-76       -0.20766       00         92       -0.1775       -0.1276       -0.1273356-77       -0.27477       0.207666	56	てい こうしんしょう しょう	70°32856°01	2.1551E-07	0.15265-07	~1-suli€°G-	-3.9450F-01	0-319PE-01
T0       1.16425-07       1.15775-07       -0.33475-06       -0.13325       0       -0.07125-12       -0.18595-05       0.16705-07       -0.33055-09         77       0.55025-08       -0.51935-07       -0.18725       -0.18726-07       -0.33055-09         77       0.55025-08       -0.18175       -0.18455       0       -0.19975-15       -0.16235-07       -0.33055-09         84       -0.58105-03       -0.18175       -0.14675       0       -0.116425       -0.164145-09         84       -0.20045       0.18175       -0.11655       0       -0.12335-17       -0.44145-09         91       -0.20045       0       -0.11255-03       0.12395-07       -0.703355-7       -0.244155-03         91       -0.20045       0       -0.12395-07       -0.12395-07       -0.27425       00         92       -0.1775       0       -0.73355-77       -0.264055-74       -0.207455       0         92       -0.1775       0       -0.1775       -0.20355-72       -0.207455       0         92       -0.1775       -0.12775       -0.12775       -0.207455       0       -0.2074557       -0.2074555       0         92       -0.1775       -0.17755656556       -0.5665562	<b>د</b> ع	, 0*6296E-af	じ。1 61 75-77	1.1540F-77	-0.3323F-04	11-26c70 <b>*</b> 0-	7.2398E-01	0.1572F-05
77       0.550%=0%       -0.510%T=0       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.510%T=0%       -0.5615%T=0%       -0.5742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2742%T=0%       -0.2076%T=0%	70	20-2659100	7.15775-17	-0.3347F-04	-0.1332F 00	1	185aE-05	0.1670E-07
94     -0.5Pl05-03     -0.1Pl7E     -0.1467F     00     -0.1660F-05     0.15425-17     -0.7414F-08     -0.4615F-03       91     -0.2004F     -0.1177F     -0.1177F     -0.2742F     00       92     0.1177F     -0.2745F     -0.2742F     00       92     0.1177F     -0.2745F     -0.2742F     00       92     0.1177F     -0.245F     -0.2742F     00       93     0.1177F     -0.25667F     -0.2076F     00       94     0.1177F     -0.25667F     -0.2076F     00       92     -0.4090F     07     -0.4090F     00	17	0.5503E_78	51-366   3°u-	-7.15735 00	-0.11465 DO	-0-10075-15	-16235-07	-0-33056-08
91 -0.2004F 0 -0.1605F 0 -0.1125F-05 0.1239F-07 -0.70335F-75 0.6005F-24 -0.2742E 00 98 0.1177E 0 -0.7463F-07 -0.5603F-09 -0.5401E-09 0.73115-23 -0.747F 00 0.2076E 00 102 -0.4000F-07 -0.5562F-05 0.1370F-10 -0.4308F-07	9 4 9	-0.5Plos-03	-J.18175 20	-0.1462F 00	-0.1669Ê-35	0.154257	-j*14t-jb	-0.4615t-03
90 0.1175 00 -0.74636-01 -0.56036-09 -0.54015-09 0.73115-23 -0.27475 00 0.20765 00 102 -0.40905-07 -0.55625-95 0.13705-10 -0.43085-07	16	-V.2014F 01	-r.35031-1-	-0.1125E-05	0.1239E-37	-0.70335-75	3.69055-C4	-0-2742E 00
102 -0.4090F-07 -0.5562F-0° -1.370F-10 -0.4308F-07	G.	u-1177E nn		<u>5603</u> -09	5401E	r11r7.n	-2.7475 PJ	0.2076F 00
	102	-0°4040E-01	-0.55625-35	1.1370F-10	-0.4308F-07			

#### A. 4 VIBRATION MODE DATA ARTIFICIAL "G" ROLLUP SOLAR ARRAY CONFIGURATION

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	Results				

#### Computer Listings

of Modes	JPL Eigenvalue-Eigenvector	A-85 to A-132	
	Program Results for Spin Rates of		
	0, 4, 8, and 12 RPM. The degree of		
	freedom sequence numbers and their		
	corresponding node number are described		
	in Table A-15.		

942) 1990 - 1990 - 1992

# TABLE A-13 MODAL DATA, ARTIFICIAL "G" SOLAR ARRAY CONFIGURATION

#### ZERO SPIN, NASTRAN RESULTS

MODE	FREQUENCY (HZ)	GENERALIZED MASS (LBS-SEC ⁷ IN)
		7 1675565-01
1		1.2922585 00
2	2.0315152-01	1.0632495.00
3		1.0016445.00
4	3.9797752-01	
5		9-5392518-21
0	3.0803025+01	6.2100125-01
7	3 9803020-01	6.0184455-01
8	5-036502=-01	1.465514= 00
10	5.214531 =-01	9.017361=-01
11	7.044816F-01	1.066769= 30
12	7.3535945-01	9.928919=-01
13	7.354488E-01	5.9914745-01
14	7.354546E-01	6.0979195-01
15	73546085~01	3.4085557-01
16	7.3546472-01	4.3380642-01
17	7.731657E-01	1.0389585 00
18	7.9412985-01	6.5387865-01
19	9.051450 =- 01	8.818574E-01
20	9.348565E-01	1.0961243 00
21	9.6092723-01	5.9155052-01
22	9.609300E-01	6.1082345-01
23	9.6093155-01	9.547644=-01
24	9.6093195-01	6.211393E-01
25	9.609702E-01	9.5595762-01
26	9.713216E-01	1.036751E 00
27	9.7723145-01	6.5864455-01
28	1.065360E CC	1.054537 <u>=</u> 00
29	1.652814E 00	2+813135=-01
30	2.106756E 00	4.305415=-01
31	-2.8258875 00	
32	3.842224E 20	
33	4.707289= 00	
34	5.006941E 00	
35	5.7139242 00	
36	5.790833= 00	
37	6.093275= 00	
38	6.099439E 00	
39	6.462175- 00 8.13505-5 00	
40		
41		
46 A 1	1-006208E 01	
45	1.067541 = 01	
45	1.136669F 01	
46	1.143346F 01	
47	1.267509= 01	
48	1.302590E 01	
49	1.485096 = 01	
50	1.497922E 01	



# TABLE A-14

# MASS-GEOMETRY DATA

## FOR ARTIFICIAL "Ğ" SOLAR ARRAY

Node	Mass	Х.	¥	Ż
1	.1252	552.	-130.5	•0
2	.1252	552.	130.5	• 0
3	.1252	552.	-58.5	• 0
4	.1252	552.	58.5	• 0
5	.1252	.804.	-130.5	• 0
6	.1252	804.	130.5	• 0
. 7	.1252	804.	-58.5	•0
8	.1252	804.	58.5	• 0
9	.1252	300.	-130.5	• 0
10	.1252	300.	130.5	• 0
11	.1252	300.	-58.5	•0
12	.1252	300.	58.5	• 0
13	.1394	1056.	-130.5	• 0
14	.1394	1056.	130.5	• 0
15	.0897	1056.	-58.5	• 0
16	• 0897	1056.	58.5	• 0
17	.8609	48.	-130.5	• 0
18	.8609	48.	130.5	• 0
19	.0822	48.	-58.5	• 0
-20	.0822	48.	58.5	•0
21	.1418	1056.	• 0	• 0
22	.7873	48	369.0	• 0
23	0.	48.	369.0	• 0
24	.0996	48.	• 0	• 0
25	.1383	804.	• 0	• 0
26	0.	• 0	• 0	• 0
27	.1383	300.	• 0	•0
28	.1383	552.	• 0	• 0

*** - Mass** units are lb-sec²/in.

















FIGURE A-42 ARTIFICIAL "G" SOLAR ARRAY MODE 19, FREQUENCY = 0.905 Hz ZERO SPIN

**Z** .

X

F FIGURE A-43 ARTIFICIAL "G" SOLAR ARRAY MODE 20, FREQUENCY = 0.935 Hz ZERO SPIN ~ Z.





₹.

X

## TABLE A-15

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Artificial "G" Solar Array

Finite Element Model Data

Node	Mass lb-sec ² /in	No. of Structural D.O.F.	D.O.F. Sequence No.
1	0.1252	3	1 - 3
2	0.1252	3	4 - 6
3	0.1252	· 3	7 - 9
4	0.1252	3	10 - 12
5	0.1252	3	13 - 15
6	0.1252	3	16 - 18
7	0.1252	3	19 - 21
8	0.1252	3	22 - 24
9	0.1252	3	25 - 27
10	0.1252	3	28 - 30
11	0.1252	3	31 - 33
12	0.1252	3	34 - 36
13	0.1394	5	37 - 41
14	0.1394	5	42 - 46
15	0.0897	5	47 - 51
16	0.0897	5	52 - 56
17	0.8609	5	57 - 61
18	0.8609	5	62 - 66
19	0.0822	5	67- 71
20	0.0822	5	72 - 76
21	0.1418	6	77 - 82
22	0.7873	5	83 - 87
23	0.0	3	88 - 90
24	0.0996	6	91 - 96

#### (TABLE A-15- CONTINUED) Artificial "G" Solar Array

Finite Element Model Data

Node	Mass lb-sec ² /in	No. of Structural D.O.F.	D.O.F. Sequence No.
25	0.1383	6	97 - 102
26	0.0	0	÷
27	0.1383	6	103 - 108
28	0.1383	6	109 - 114

### TABLE A-16 CORIOLIS FORCE MATRIX (NORMALIZED TO $\Omega$ )

Somerce No			
Sequence No.			
1 - 3	-0.25043	· 0.	0.
4 - 6	-0.25043	0.	. 0.
2 0	-0.25043	0.	0.
etc.	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.25043	0.	• 0•
	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.25043	0.	0.
	-0.27878	• 0.	· 0•
	0.	0.	-0.27878
	0.	0.	· • • • • • • • • • • • • • • • • • • •
	0.	-0.17940	С.
	0.	0.	0.
	-0.17940	0.	• 0.
· ·	0.	0.	-1.72184
	0.	0.	0.
	0.	-1.72184	0.
	0.	0.	0.
	-0.16439	0.	0.
	0.	0.	-0.16439
	0.	0.	0.
	0.	-0.28364	0.
	0.	0.	0.
	. 0.	0.	0.
	0.	0.	0.
	0.	0.	0.
	-0.19928	0.	0.
	. 0.	0.	0.
	-0.27652	0.	. 0.
	0.	0.	0.
	-0.27652	0.	0.
	0.	0.	0.
	-0.27652	0.	0.
112 - 114	0.	0.	0.

* ~ Refer to Table A-15 for corresponding node number.

#### TABLE A-17

#### CENTRIFUGAL FORCE MATRIX

(NORMALIZED TO  $\Omega^2$ )

D. O. F.			
Sequence No.			_
1 - 3	-0.12527	-0.12527	0.
4 - 6	-0.12527	-0.12527	0.
etc.	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.12527	-0.12527	0.
	-0.13939	-0.13939	0.
	0.	0.	-0.13939
	-0.13939	0.	0.
	0.	-0.08970	-0.08970
	0.	0.	0.
	-0.08970	-0.08970	0.
	0.	0.	-0,86092
	-0.86092	0.	0.
	0.	-0.86092	-0.86092
	0.	0.	0.
·	-0.08219	-0.08219	0.
	0.	0.	-0.08219
	-0.08219	0.	0.
	0.	-0.14192	-0.14192
	0.	0.	0.
	0.	-0.78787	0.
	0.	0.	0.
	0.	0.	0.
	-0.09964	-0.09964	0.
	0.	0.	0.
	-0.13836	-0.13836	0.
	0.	0.	0.
	-0.13836	-0.13836	0.
	0.	0.	0.
	-0.13836	-0.13836	0.
112 - 114	0.	0.	• 0•

* - Refer to TableA-15 for corresponding node number.

			0.25577 0.255777 0.21317 0.25777 0.21317 0.25777 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13377 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.137777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.13777 0.137777 0.137777 0.137777 0.137777 0.137777 0.137777 0.137777 0.137777 0.1377777 0.1377777 0.1377777 0.1377777777 0.13777777777777777777777777777777777777																											
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			0-8857E-10	0-20496-05	-0.7423F 00	-0.3171E-10 0.1309E-05	-0.6522F-10	-0.8436E 00	0.5047F-12	0.1156E-10 0.1457E-04	0-17136-12	-0.87755-02	0.8770F-14	-0-1070F 00	-0-4081E-03		0-0	0.0	0.0		0.0	0.0	0-0	0.0	0.0			0.0	0.0	0-0
			-0.6533E 00	<b>0.1247F-09</b>	0.2049F-05	-0.2363F 00 -0.2324F-10	0.6602F-12	0.16195-08	-0.82825-03	-0.4379E-10	0.3385F-12	0.18655-10	-0.2240F-12	0.1530F-08	-0.3093F 00		0.0	0.0	0.0			0.0	0.0	0.0	0-0			0.0	0.0	0•0
	RPM		0.3345E-05	-0.6147E 00	0.6934F-10	-0.3067F 00	-0.82596-03	0.32936-10	-0.9403E 00	-0.8615E-13 0.1799E-10	0.7965E-05	0.5318E-12	0.2332E-15	0.5062E-13	0.3022F-08		0.0	0.0	0.0		0.0	0.0	0.0	0.0			0.0	0-0	0.0	0•0
•	0.1977 Hz, <u>n</u> = 0		-0.1597E-10	0.3345E-05	-0.9792F 00	0.1399F-10	-0.7841E 10	0.4781E-12	0.16215-08	0-36124 0-38116-10	-0.25075-32	0.12395-72	0.87145-05	-0.4293F-11	0.8251E-13		0-0	0.0		0.0	0.0	0.0	0.0	0-0			0.0	0.0	0.0	0•0
	= 2, frequency =		-0.5144E 00	-0-10705-11	0.2048F-05	0.5997F-10	0.1616E-08	-0.8247E-03	-0.3015f-10	-0.1031F-12	0.15036-10	-0.8270E-03	-1-12422-D-	0.11785-02	0.3690F-11	4	0.0	0.0		0.0	0.0	0.0	.0.0	0.0			0.0	0.0	0.0	0•0
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			-0.1205E-0	0-2220E-0	0 36104 • 0-			0-4950E-0	0.2802E-0	-0.5777E-0	0.1878E-0	0-35664-0	-0-33896-0	0.1520E-0	0.1856E-0	0-9045E-0		0_0	0.0	0.0	0.0		0-0	0.0	0.0	0-0	0,0		0.0	0.0	0-0		•				
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			-0.4098E-34	-9.1146E 33	10-18488-01		-0	-0.1091E-36	0.4953F-02	-0.1053F-18	0.4362E-74	0.10165-07	-0.2024F-08	-0.7841E-38	0.4323E-06	0.1094E-36		0-0	0.0	0-0			0.0	0-0	0.0	0.0			0.0	0-0	0.0						
	;		-1.1950E-01	-0.28/3E-04	-U. JOSC UU	10-110270	0-0-0-0-0-0	0.3070E-07	0.1326E-04	0.1894E-06	-0.4976E-07	0.2530F-07	-0.3390F-06	-0.69545-09	0.2262E-07	0.1065E-04		0.0	0.0	0.0	0.0		0.0	0.0	. u•0	0.0	0,0		0-0	0.0	0-0						
and the second of the second of the			-0.5151F 00	0-44926-01	-0-1919194	-0-11016-01	-0.1366-04 -0 13666-06	0.25475-05	-0.11546-06	0.2335E-04	0.11455-08	-0.4/515-04	0.6148F-12	0.1706E-06	0.2041E-07	-0-24475-07	0.6921E-05	0-0	0.0	0.0	c • 0			0.0	0.0	0.0	0.0		0.0	C-0		0.0					
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IGEVALUE     0.11011736     0.101173.4     9     Mode 9, frequency = 0, 5031 Hz, T = 0 RPM       IGEVALUE     0.11011736     0.1011736     0.1101174     0.1101174       IGEVALUE     0.11011746     0.110176-00     0.110176-00     0.110176-00       II     1     0.1011736     0.110176-00     0.110176-00     0.110176-00       II     0.101174-00     0.110176-00     0.110176-00     0.110176-00     0.110176-00       II     0.101174-00     0.110176-00     0.110176-00     0.110176-00     0.110176-00       III     0.100177-00     0.110176-00     0.110176-00     0.110176-00     0.110176-00       III     0.100176-00     0.11016-07     0.110176-07     0.110176-07     0.110176-07       III     0.10016-00     0.11016-07     0.11016-07     0.110176-07     0.110176-07       III     0.10016-00     0.11016-07     0.11016-07     0.110176-07     0.110176-07       IIII     0.10016-00     0.11016-07     <	<b>X</b>					f • •			·		<b>91−31141°C</b>		· · · · · · · · · · · · · · · · · · ·				11-11-1-1				11-12261-0				5.5		e	65 ( • •			C*0	5 • C					r. p	
(EFWEETOB         First         D. 3031         Hz, B = 0.5031         Hz, B = 0.5031         Hz, B = 0.5031           (EFWALUEs         0.1101137E         01         (mad/mec)         0.4417E         0.7107           (EFWALUEs         0.1101137E         01         (mad/mec)         0.4417E         0.7107           (EFWALUEs         0.1101137E         0.4117E         0.7107         0.7107         0.7107           1         1         1         0.4477E         0.711257         0.4477E         0.7107           1         1         0.4477E         0.711257         0.4477E         0.711976         0.711976           1         1         0.4477E         0.711257         0.11177         0.711977         0.711977           1         1         0.4477E         0.711277         0.4477E         0.711977         0.711977           1         1         0.4477E         0.711777         0.4477E         0.711977         0.711977           1         1         1.41460         0.717777         0.44777         0.44777         0.44777         0.44777           1         1         1         1.41476         0.7117677         0.447777         0.44777         0.44777         0.447777			•								-0.1279£ 07	3.17915-05	0.51465-02	-0.4920E 00	0-1634F+09	0.17495-05	0.2357F-04	-0.98995-07	-0.74795-03	0.4267E-37	-0-4951c-09	0.27255-09	10-360440-		0.0	0.0	0.0	0.0		0.0	. 0.0	0.0			0-0	0.0	<b></b>	
(ErWVECTOR FIR 2007 VJ 9     Mode 9, frequency = 0.5031 Hz, G = 0 RP       (ErWVECTOR FIR 2007 VJ 9     0.110545-05     0.4175-07     0.66446-07       11     1     1     0.11641056     0.4175-07     0.66446-07       11     1     1     0.11641056     0.11705-07     0.6475-07       11     1     1     0.11646-05     0.11705-07     0.6475-07       12     1     0.11646-07     0.11705-07     0.4475-07       13     10     0.11646-07     0.11756-07     0.4475-07       14     1     1     0.11646-07     0.4475-07       15     11     1     0.11646-07     0.4475-07       16     11     1     0.11646-07     0.45946-07       17     42     0.14076-07     0.1166-07     0.45946-07       16     11     0.1076-07     0.1166-07     0.1166-07       17     42     0.40176-07     0.1166-07     0.1166-07       17     42     0.4016-01     0.1166-07     0.1166-07       18     17     42     0.4016-01     0.1166-07       18     17     42     0.4016-01     0.1166-07       18     17     42     0.4016-01     0.1166-07       18     18     0.4016-01<		:				W					0.3771E-02	3.7609F 01	7.1913E-06	7.776F-02 -0 22075 00	0.1970F-04	0.7185E-07	-7.9072E-01	-0.1953E-09	0.4114E-07 0.3339E-05	0.10916-09	<b>J.4909E-12</b>	0.2394F-08	7.7036E-05		0.0	0.0	0.0	0.0		0.0	0.0	0.0			0.0	0-0	0-0	
(6:WALUF     0.11011376E     0.1 (had/sec)     Mode 9, frequency = 0.50       (6:WALUF     0.11011376E     0.1 (had/sec)     0.4135E       (6:WALUF     0.101757E     0.1 (had/sec)     0.4135E       (1110111110)     0.1 (had/sec)     0.1 (had/sec)     0.1 (had/sec)       (111111111111111111111111111111111111			:			$31 \text{ Hz}, \Omega = 0 \text{ RP}$			,		0.6648F-J7	n.3424E-72	-0.26425 70	0.1344F-96 0.4354F-03	-0.8483E-01	0 1150E-78	0.37475-05	0.5731F-75	n.8533F-77 -0 20066-73	0.58545-04	-0.34335-76	0.2087F-34 -0 12046-07	0.1825E-09	·	0-0	0.0	0.0			0.0	0.0	0.0			0.0	0.0	0.0	•
IGENVECTOR     FOR     RnDT     No.     Mode     9.       IGENVALUF=     0.316011328E     0.31770F-02     0.3770F-02       I     T     7     0.1954F-76     0.3776F-01       I     T     7     0.1954F-77     0.1376F-01       I     T     7     0.1954F-76     0.1376F-01       I     T     7     0.1954F-77     0.1376F-01       I     T     7     0.1976F-01     0.1156F-01       I     T     0.1976F-07     0.1976F-01     0.1166F-07       I     T     0.1977F-05     0.1976F-01     0.1166F-07       I     T     0.1977F-05     0.1967F-01     0.1166F-07       I     T     0.10107F-05     0.1967F-01     0.1166F-07       I     T     0.1037F-03     0.1166F-07     0.1166F-07       I     T     0.1037F-03     0.1166F-07     0.1166F-07       I     T     0.10107     0.11057F-03     0.166F-07       I     T     0.00     0.00     0.00       I	•		•			frequency = 0.50	·				0.6135F 00	0.4677E-07	n.6994F-07	0.11205 30 0.11475-04	0.37485-05	0.2799F-04	-0.61335-07	-0.1106E-02	-0.7549F-09 0 3630E-07	0.23545-04	-0.495RE-09	0.3848F-05 0.73646-05	0-2022F-07		0-0	0.0	u • 0	0.7		0.0	0.0	0.0			0.0	0.0	0.0	1
GENVECTOR FOR RNDT V3.*     9       IGENVECTOR FOR RNDT V3.*     9       ICEVALUE=     0.31611328E     01 (rad/8e       ICT     7     9       ICT					-	Mode 9,			•		0.37705-02	-0.9345F 00	0.37055 03	-0 4633E 00	0.18305-06	-0.7905E-01	0.1359F-AR	0.4143F-07	0.1961F-05	-0-4212E-01	0.49095-12	-0.4995F-03 0 1761F-76	0.99575-04	Q.8990F-11	0.0	u•0	0.0			0.0	0 <b>-</b> 0	0.0		0.0	0.0	0.0	L • 0	•
16     10     16     10       16     17     1     1       1     15     17     1       1     15     17     1       1     17     1     1       1     17     1     1       1     17     1     1       1     17     1     1       2     17     1     1       2     17     23     3       2     17     23     3       2     17     35     3       3     17     35     3       45     17     35     3       13     17     35     3       13     17     35     3       14     17     35     3       15     17     35     3       35     17     35     3       36     17     35     3       37     45     45     4       36     17     35     3       36     17     35     3       37     45     4     4       38     17     35       37     45     4       45     4       45<	•			•		6 ** CN		as/per/ to section	The sector of the sector		0.19545-76	7.3656F-02	J. 49245 JN	0-1024E-)/ 0-7077E-02	-0.44455 00	0.37475-05	<b>3.2096E-94</b>	0.9439E-07	- ]. [0] 4F-03	0-3747F-05	9.8073E-95	3.40965-77 -0.46165-01	0-5717F-05	0.10375-03	0.0	0.1	0.0			0.0	, <b>r</b> .4	0-0		0.0	0-0	0.0	0.0	•
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EIGF4V	ECTOR FI	ับบส สบ:	01 = °u	PoM	le 10, frequency	= 0. 5142 Hz, 2 =	0 RPM	s.	ч.	
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DE AL	A D T									:
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e,	TO 14	. 4	0.96156-03	0.2377F 00	0-36995-08	0.96345- 3		1.5781F-07	0.14625-02	
15	TO. 21	:	0.795PF-01	-0-4927F-08	0.9465-03	-1.92975-	32128-0	20-19061-0	-0-13556-01	
23	10 · 21		0.13195-09	0.19065-02	0.18965 00	0.46725	0.19235-57			
29	10 1	ŝ	0.19275-02	-9.945JE 00	20-36445.0	0.11755	0.42945	-0.12526-07	9.1176E-02	
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53	17 56	6	0.44445-02	0°44985-09	-0.21345-07	0.11075-75	0.25545 77	3.44445-02	0.3630E-09	
15	10 6.		<b>9.2774E-07</b>	0°1142±-01	0.537°F-02	-0-453355	-1.51415-77	-9.29215-97	0.75075-09	
\$9	11 71	ç	-0.2350F-02	-0°4041E-75	-0°70115-10	0.24755	1.1137E-17	2.2222-22	-0-4001E-04	
1	TA 7:	-	0.2007E-09	-0.2659F-J7	0.99245-00	-0-1300El-0-	-1-245-24	<b>0.2266</b> F-09	0.1075E-09	
7.9	TO 94	t	n.1107F-05	0.4205F-03	0.4443F-02	0 <b>.1</b> 64¤r5	0.3929£-10	<b>0-123</b> 75-07	0.16795-01	
8 5	TO OI	1	-0°4944E-04	0.1341F-12	-U.1489F-79	•∃u611•u	7.13415-12	-0-14975-09	0.5477E-11	•
6	TN 95	er.	0.1192F-07	0.1146E-03	-0.31165-04	-0°34015-15	1.6331⊊-1a	0.77955-10	0.1278E-05	
66	10, 10,	ŕ	0.7984E-01	0.33245-02	0.12045-35	÷:-⇒01∀2°û-	3-31175-15	J. 1022E-35	0.76165-03	
105	TO 112	2	0.1087E-02	-0.1655E-05	90-34045-08	3.52195-55	0.2719°-75	96355-03	0.22065-02	
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<b>[</b> <del>]</del>	1.7 4.	ç				0.0	0.0	0.0	0.0	
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57	10 6	ŗ	c•c	0.0	0.0		0°J	0-0	0-0	
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43 T	ъ с.	c	-0-36904-05	0.3469F-01	9.26125-03	-0.21915-J7	-0.1615E-05	-0-20555-25	-37851-6-
50 1	ν̈́ c		<b>1.</b> 764AF-03	-0.25425-07	0.16105-05	-0-20435-05	10-34451°u	9.26765-73	
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54 T	۲ د	-	0.58655-73	0.13755-05	-0.7005F-09	9.2327F-06	0.1290E-06	-0.63155-73	- Svall":
7 17	r c	*	9.1372F-0P	-0-20005-06	0-10445-06	9.35755-03	0.50535-05	0.99815-39	- 19295 - 0
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85 T	ë c		0.17325-04	<b>N.R697F-17</b>	-0-44005-00	-0.4374F-05	0.8697E-12	-0.83735-33	- séo6 <b>†°</b> C
1	č	<b>e</b> r	1.1265F-96	-0-35455-04	0°84695-05	0.10525-05	0.71955-08	0.73615-70	- 32 1 1 2 2 6 -
99 1	۔ د		-j.2415c-ji	これーヨスドロく。ロ	-0.450aF-37	-0.57315-07	0.74715-09	7.11275-24	-34861-1-
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7 1	۲. د	•	c "c	0.0	0.0	0°0	0.0	0.0	6 <b>-</b> 6
7.A T	č		C•C	0.0	c.0	0.0	0.0	0-0	с, <b>г</b>
85 1	с с	_	<b>J.</b> 0	0.7	0°0	c • 0	0.0	0-0	<b></b>
92 F	ē	•	0-0	. u-c	<b>c</b> .0	0 <b>-</b> 0	0.0	0.0	r: T C
99	č. c	ſ	0.0	0.0	0°0	<b>0</b> .0	0.0	0.0	د <b>.</b> .
106 7	= c	•	0°0	0,0	0-0	0.0	0.0	0.0	,
							;		

Mode 18, frequency = 0.7912 Hz, Ω = 0 RPM

AI =-CN TOTA FOR FOR ROOT NO.

A-92

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	L	:			:			-																:				•				L			/
		•		-0-2191E-35	0.1151E-01	-0.49935-15		0.1150=-25	0-26325-03	-0-8976-77 -0-6445-77	0.45435-04	-0-35475-04	-0.22455-31	-0.15745-15 -0.89715-05	r0-32210-0-	-0-14955-35			0.0			0.0	0-0	0-0	0-0	0-0	0.0	0.0	0.0				•.		
:				-0.5776E-01	-0.8240F-06	7.499F-03	0.32495-06	-1.849 <u>8</u> E-09	-0-10775-04	-0.3691E-04	-0.24295-02	-0-2401E-08	-0.90335-07	7.14025-08 -0.28915-09	-0.6607F-05	-0.9491F-03		0.0	0.0	. 0.0		0.0	0-0	0.0	0.0	0.0	0-0	0.0	. 0-0 .		•				
RPM	-			-0.21875-02	-0.63345-01	-0.7677E-06	0-1000F 01	-0.36995-04	-0.5678E-06	-0.4050F-02	-0.45535-07	n. 1903F-04	-0.1011F-07	0.5179E-12 -0.4728E-08	-0.98445-10	-0.1193E-04			0.0	0.0		0.0	0.0	0.0		0.0	0.0	0.0	0.0						
0.9047 Hz, Ω = 0				0.7858F-06	-0.6982E-03	0.6231F-91 -0 30575-06	0-71195-02	0.79265-02	-0-3E248-0-	-0.10755-04 0 50675-06	-0.1453c-06	0.1277F-02	0.2470F-05	-0.1523F-04 0.4857F-05	0.6063F-08	-038FUS79		0.0	0.0	0.0		0.0	0.0		0.0	0-0	0.0	0-0	0.0			•			
19, frequency =		* * *		0.6491F 00	0.4477E-06	0.17035-02	-0-1918F-06	-0.10805-04	-0-34995-04	0.5510E-06	-0.9169E-10	-0.71715-07	-0.3694F-04	0.1149F-04	0.21095-05	-0.34125-07			0.0	0-0		0.0	0.0	0.0		0.0	0.0		0.0				•		
Mode	*	c)		-0.19285-01	-0.8994F 00	0.96275-06	-0-21965-01	-0.12185-n5	-0.67165-02	-0.92925-0P	0.4469E-75	0.21805-06	-0.1899F-02	-0.16095-03	-0.1920F-04	7.1355-05	0.21595-09	0.0	0.0	0.0		<b>v</b> •0	0.0			0-0	0.0	0.0							
61 = °CN	-	57035 Ol (rad/se		-0-51625-36	-0.7346E-03	-0.12315 00 0 50235-06	-0.76865-03	0.9320F-02	-0.19755-94	-0.456975-04 -0.73866-06	0.2067F-02	-0.14395-09	-7.1075F-04	-0-36385-07	-0.1306E-02	7.1621E-74	0.38515-96	0.0	c.0	0.0		0.0	0.0	0.0	0.0	0.0	c.c	0.0	c c	•	-				
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0.33965-07 0.95755 07 0.95756 07 0.337435 00 0.337735 07 0.13615-07 0.13615-07 0.10675-02 0.96505-02 0.93705-03 0.93705-03 0.83705-03 0.83705-03 0.83705-03 0.83705-03 0.837055-03 0.837055-03 0.837055-03 -0.2443F 00 0.1094F-01 0.9573F 00 0.13975F 00 0.1331F-02 0.1731F-02 0.1731F-02 0.4547F-03 0.1146F-03 0.1146F-03 0.1146F-03 0.1146F-03 0.11650F-03 -0.1557F-06 -0.1557F-05 -0 ł ••••••••••••••••• -0.9997F 00 -0.2234F 30 0.51722F-07 0.5122F-07 0.5122F-07 0.5967F-05 0.6967F-05 0.6967F-05 0.1779F-05 0.1779F-05 0.1779F-05 0.1779F-05 0.1779F-05 0.1779F-05 0.2781F-06 0.2712F-01 -0.10005 01 -7.17745 00 -0.10565-71 0.35715 00 7.17265 00 ••••••••••••••••• 1.562544835 nl (rad/sec.) 3.74595-02 -0.909955 03 -0.511150.57 0.17595 03 0.15525 00 0.15525 00 0.15525 00 0.25525-05 -0.88115-05 -0.88115-05 -0.88115-05 -0.25095-05 -0.19076-03 0.59926-03 0.42506-75 0.29966-75 195 112 114 0487 101 A B B õ ETGENVALUE= ₽₽₽₽₽₽₽₽₽₽₽₽₽**₽**₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽ PART 113 MAG 2 46.25 QFAL 5 6 525 5 5.7

Mode 28, Frequency = 1.0544 Hz, **G** = 0 RPM

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FIGENVECTOP FOR POIL YJ.= 29

A-95

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		0.3568F 00 0.9511F-02 0.9609F-02 0.9609F-02 0.98381F-02 0.4764F 03 0.47646 03 0.47646 03 0.2599F-02 0.13965F-01 0.13965-01 0.1346F-01 0.1346F-01 0.2080F-02 0.2080F-02		
		0.8944 0.89446 0.96116-02 0.96116-02 0.96116-02 0.29176-02 0.11366-03 0.11366-03 0.11366-03 0.10166-03 0.10496-03 0.10496-03 0.10496-03 0.55376-02 0.55376-02 0.55376-02 0.29716-02		
· · ·	= 0 RPM	9.894455-02 0.89446-02 0.89446-02 0.80646 00 0.80646 00 0.80646 00 0.80646 00 0.80646 00 0.17896 00 0.23456-03 0.43456-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.23436-05 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.2446 0.24466 0.2446 0.24466 0.24466 0.24466 0.24466 0.24466 0.24466 0.		
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	2, Frequency =	0.89475-77 0.35595 00 0.35595 00 0.95795 00 0.20115-02 0.11715-03 0.11715-03 0.11415-03 0.11416-03 0.11416-03 0.111465-05 0.10145-05 0.10775-05 0.10775-05		· · ·
	Mode 3	9.894455-02 9.894455-02 9.44545-02 9.44545-02 9.44545-03 9.47745-03 9.47745-03 9.47745-03 9.47745-03 9.47745-03 1.11745-03 9.12745-03 9.12745-03 1.11745-03 9.17405-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11745-03 1.11		
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•			10	.15555-02			10-10-15	-26245 30	00-3830E"	60-399UE*.	*0-je281*.	P11425-09	~2141E~U5	.59715-11	-1425-US	*125ac-03	26-31425.			"I:41F-05	50-35961"	ſ	\$C-355\$5".		80-jetul*;		11-3500\$*1			-26565-09		11-1422			
				1	0.15555-72 -2 2 20525 20			1.12575-75	9.44275-07	-1.34276-27	-0.754253	J. 76495-CO	<b>0.14435-27</b>	-).17535-03	0.9667F-10 C	3C-scoll"6	-0.1241c-73 -			CT. 010	-0.60-35-05.00		c	-)- 40-16-00(-	-0.94455-11 -0				r	0.25835-11 -0					•,
Wd			<b></b>	0° 31189°0	3.5379F-77	0.1053F-72	3-4681E-02	J. 2576E-07	a.26195 an	-1.47545-17	- 10-38041°C	J.7495-75	0.41475-09	- 21-3c2el.	0-37878-00	<b>7.3756F-17</b>	0.2366E-D5 -			0.30795-06	- -	-0.5977E-16	1,00975-75	• • •	· · ·		6.6	-0.13456-11	<1-32 2E 1 - L-	1.0 2 22215 12					
1786 Hz, <b>n</b> = 4 RI ,			-v-1232E-11	0.25455-D2	0.97975 30	131015-77	-0.50515 10	0.37405-39	3.12%9E-35	J.14145-34	7.29935-77	12-35212+0	0.45565-06	-J.63995-J5	J_RR42F-76	<b>ゎ</b> Ĺーヨどゞ゙゙゙ぇぇ゜゚゚じー	0.5463F-13			-0.10415-05	<b>30-38861°C</b>	0.0	-1.45955-16	0.J578F-16	0.0	1-36610°C	-U-35126-U-	C*U	6L-38961-L-	с. с	5		1.76755-16 7.76755-16	-14045-79	
Frequency = 0.			- ,. - 7, 15435 (-	-J-76495-00	3.1545c-02	0 37277°L	1 1 7 4 5 E - 7 5	7.641F-02	-0, 359F-17	-1,1757E-17	-].970f-10	J-1176E-77	7.44315-02	-v-1754[-Ja	3.11245-04	3.25165-76	3.67976-99			<b></b>	-3°-1701-02	3.1195-75		-)-++=516	-].14445-[]				11-30121-0	-3.753E-12				1-2776-16	• • • • • • •
Mode 1,	ec. )		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	-1.1296 JA	L			1 5244E 00	3 - 32 E - 3C	142]c-14	っ.21725-75	-1.31115-07	としっっし うくしいつ	21-36261+6	-1.33445-04		1-26627-1	1-3125.5		50-51512•0		50-16607°, ~	トレーンドのフロー・・・	•	-1.97F-09		11-39129-0-	21-26461.		-:		• •	•		•
	i1112F ∩l (rad/s		v-julliv	3.75456-12	10 30001.0-			0.12525-75	2 1 8 4 4 L	11-31 CFF °C	50-38638°C	3.74645-33	1.1259E-15	<b>プl</b> 425c-76	0 <b>.1</b> 30AF-07	といーコキドス 1 - 0-	0.117fc-17	7 <b>.</b> ]ÅA4F-]3		らしー コンタント・フラ	1.9414F-71	د د		J.64 ]45 - J I		-0.1955F-11		-1.20445-79	<b>c</b> • <b>c</b>	-0.26475-11		7.1 - 65855-17			
TOR FOR RINT	i⊨= ).11?5	•	7	4	10			. 45	56	¢ \$	70	17	44	lo	6. C	175	211	- 114	Y DAOT	۴.	14	-		15		5	ţ	<b>5</b>	C -	77	ŧ.	1.			
1 GE NVEC	I CENVAL I	EAL PAR	1	5	15 27			11 63	5.0 TO	57 13	54 TJ	01 12	73 10	45 TJ	G7 10	CF C0	105 10	113 LU	AVAL SVA	1 1	<b>F</b> .	15 10	LJ ic		11 - 11 1			57 10	64 43				5 10	115 10	

3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1775-7       3.1755-6       3.1775-7       3.1755-6       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1755-7       3.1567-17       3.1755-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.1575-7       3.15755-7       3.15755-7       3.15755-7		(						
Ayrr-In       n.yokstenk       -0.37346-0       -0.4735-0       -0.4735-0       -0.4735-0         Ayre       -0.37346-0       -0.4735-0       -0.4406-0       -0.4735-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4455-0       -0.4555-0       -0.4455-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4555-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0       -0.4055-0	1.140974194 F.44 9.64376195 F.5.5	4 4 - C - 1	26-37-8 6435 JO	-0.57955 -0.	-7.2534E-13 7.42316-75	0.4331€-05 -7 £041€ ∩1	-1.64635 77	7.1243F-09
Accels      1135      2535      2535      2535      2535      2535      2535      2535      2535      2535      2535      2535      2535      2535      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      2335      1335      2335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335      1335	-9.68555 00 -0.5	- 0 - F	v1-3224	0.295AF-75	-0.91145 30	0.3667F-10	1. 296AE -16	00 36224 C-
5976 70       0.33916-17       0.27256-75       0.30346-17       0.27556-75       0.3056-17       0.25566-05         7006 71       0.27566-07       0.275676-79       0.04775-10       0.27566-07       0.72575-12       0.25575-12       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.14506-112       0.12506-108       0.11056-012       0.11056-012       0.11056-012       0.12506-108       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012       0.11056-012	-3.2027E-10 0.2	c	0 K 05 - 75	-1. p14c	1.113ac-17	い ういろくち いい	-1.20435 -1	-1-30-23013
1355-00       0.22545-00       0.53115-12       0.4775 00       0.23545-12       0.4775 00       0.23555-12       0.4775 00       0.23555-12       0.4775 00       0.23555-12       0.47755 00       0.23555-12       0.13555-12       0.14505-12       0.175505       0.175505       0.175505       0.175505       0.175505       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.11555-12       0.110555-12       0.110555-12       0.110555-12       0.110555-12       0.110555-12       0.110555-12       0.110555-12       0.110555-12       0.1105555-12       0.1105555-12       0.110555-12	3.27265-75 -n.3		êrerî	J-∃1958.r	らんーコシングウェーフラ	-J.JA46E AD	-1-=1222-1-	1.7756 -05
73475       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,775       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776       7,776 <td< td=""><td>L*ປ ບບ່ອໄຢະະ∿⊷</td><td>5.1</td><td>りょうちょういつ</td><td>ピビーニカらるをつい</td><td>-1.7334F JA</td><td>-7.8276F-U3</td><td>( 1-31770°(</td><td>u1-3494c°u-</td></td<>	L*ປ ບບ່ອໄຢະະ∿⊷	5.1	りょうちょういつ	ピビーニカらるをつい	-1.7334F JA	-7.8276F-U3	( 1-31770°(	u1-3494c°u-
5345-12       -0.4905-12       -0.4905-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.41955-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.419555-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410165-12       -0.410255-10       -0.410255-10       -0.410255-10       -0.4102555-10       -0.4102555-10       -0.4102555-10       -0.4102555-10       -0.4102555-10       -0.4102555-10       -0.4102555-10	J-2260E-J9 -C.1	1.0-	ור שטרט	ני"שלטנפ"ט-	21-311€3°v	J_47735-10	1. 7542c - ra	じい コムミラの・レー
5156-10       0.40165-12       0.40165-12       0.4016-12       0.14606-16         106-10       0.22336-12       0.7766-12       0.246016-12       0.14606-16         117 00       0.82326-11       0.12336-12       0.77666-12       0.1266-12       0.1266-12         116-10       0.12336-12       0.12336-12       0.1236-12       0.1216-12       0.1266-16         116-10       0.12336-13       0.12306-11       0.17766-12       0.2566-08         0.1176-00       0.12376-13       0.14306-11       0.17766-12       0.2566-08         0.1176-01       0.11766-03       0.14306-11       0.17766-12       0.2566-08         0.1176-02       0.11406-17       0.14306-11       0.17766-12       0.2566-08         0.1176-03       0.11406-17       0.14366-13       0.11766-09       0.2566-08         0.1176-03       0.11776-01       0.14466-0       0.264066-06       0.2566-08         0.1176-04       0.101726-04       0.010166-09       0.01166-09       0.01166-09         0.1016-04       0.10166-04       0.010166-04       0.010166-04       0.010166-04         0.10166-04       0.010166-04       0.010166-04       0.010166-04       0.01166-04         0.10166-04       0.010166-04       0.0		а. С	5345-12	· l- 300€ 9 °	よい- うじタイち・い	<b>℃ ∃2℃9e°υ-</b>	£に−⇒にじを≖*ぃ−	~.7323E-12
195-55       -).14176-12       0.5736-72       0.74736-12       0.13336-73       0.14776-12       0.33336-73       0.14776-12       0.33336-73       0.14776-12       0.35336-73       0.14756-12       0.35356-72       0.14756-12       0.35356-72       0.14756-12       0.35356-72       0.14756-12       0.35566-13       0.12136-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.3556-12       0.2556-13       0.21106-12       0.21106-12       0.220366-13       0.21106-12       0.220366-13       0.21106-12       0.21106-12       0.21106-12       0.21106-12       0.21106-12       0.21106-12       0.21106-12       0.21106-12       0.220266-13       0.21106-12       0.220266-13       0.21106-12       0.220266-13       0.21106-12       0.220266-13       0.21106-12       0.21106-12       0.21106-12       0.220266-13       0.21206616       0.0       0.220266-13       0.1220666       0.220266-13       0.220266-13       0.2120666       0.0       0.0       0.2202660       0.2120666       0.0       0.010666       0.0       0.010666       0.0 <td< td=""><td>J.50165−1∩ 0.25</td><td>0.25</td><td>01-3515</td><td>du-selot"u-</td><td>ן גיאב-זג,</td><td>-7.11555-12</td><td>-0°8100E-10</td><td>el-sleyi.e</td></td<>	J.50165−1∩ 0.25	0.25	01-3515	du-selot"u-	ן גיאב-זג,	-7.11555-12	-0°8100E-10	el-sleyi.e
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-1.1969E-17 J.73	5.7	80-36B	-J.1410E-12	01-27065-0	ul-12692°u	-1.33.357	ちロー コレジサ i~ い
175 00       -0.82acc/a       0.123ac-07       0.3108c-15       0.3108c-17       0.12105c-11       0.11015c-01       0.02015c-114       0.02115c-01       0.02115c-01 <t< td=""><td>J.49985-12 -0.55</td><td>- J. 5 - 5 -</td><td>01-201</td><td>v1-32€L2°v</td><td>-j.2513E-j2</td><td>7°72°-35</td><td>3.47255-12</td><td>~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~</td></t<>	J.49985-12 -0.55	- J. 5 - 5 -	01-201	v1-32€L2°v	-j.2513E-j2	7°72°-35	3.47255-12	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
705-15       7.21355-17       7.01235-17       7.21355-17       7.21355-17         705-15       7.11755-12       7.11755-12       7.2555-08         755-14       7.11755-12       7.21175-12       7.2555-08         755-18       7.11755-12       7.21175-12       7.2555-08         755-18       7.11755-12       7.11755-12       7.2555-08         755-18       7.11755-13       7.1175-12       7.25055-08         755-18       7.1745-13       7.1745-12       7.25055-08         755-18       7.1745-13       7.1745-12       7.25055-08         755-18       7.1745-14       7.1745-12       7.27455-14         755-11       7.7545-14       7.7       7.12155-14         755-11       7.7545-14       7.7       7.12155-14         757-12       7.1755-14       7.7       7.12555-14         755-11       7.7       7.7       7.12155-14         755-11       7.7       7.7       7.7         755-11       7.7       7.7       7.7         755-12       7.1       7.7       7.1         755-14       7.7       7.7       7.7         755-14       7.7       7.7       7.7         7	v.22≤aE-AR -A.89	68° ° 6 –	175 JA	rl-jor28.0-	iv-sciit•u	7.7645-12	0 <b>~</b> 3284E-10	20-31016-02
305-07       0.11075-04       0.12375-03       0.12365-03       0.22056-03         305-03       0.11765-07       0.11765-13       0.211655-13       0.211650-07         765-14       0.11765-07       0.11765-17       0.11765-07       0.20055-08         755-08       0.1       0.11765-07       0.211650-07       0.20055-08         755-08       0.1       0.12735-08       0.20055-08       0.220255-08         755-08       0.10055-09       0.01055-09       0.016509       0.20055-08         755-08       0.100255-03       0.010255-03       0.200555-08       0.200555-08         755-01       0.100255-03       0.010255-04       0.120255-04       0.200555-08       0.120255-04         755-11       0.100255-04       0.1002555-14       0.120255-14       0.120255-14       0.120255-14         755-11       0.1005555-14       0.10005555-14       0.1200555-14       0.120255-14       0.1202555-14         755-15       0.1005555-15       0.10005555-15       0.1202555-14       0.120255-14       0.120255-14         755-15       0.1005555-15       0.10005555-15       0.1202555-14       0.120255515       0.120255515         755-15       0.10005555-16       0.10005055555555555555555555555       0.12025555555555	<b>3.1637</b> E-04 - 0.31	1	300-15 .	-1-35515-1-	うく-ってひちゅ い	7.31995-15	21-=7212 "1-	3.1210F-13
#GE-J3       J.[]FE-J2       -9.59076-11       J.69856-13       J.2][]FE-F9       -0.10106       J.2         766-14       J.127056-17       J.11666-17       J.11666-17       J.11666-17       J.20066-13       J.20066-13         756-08       J.1       -0.22736-18       J.59076-09       J.0       J.22026-08         7.5       J.11666-13       J.11666-13       J.11666-13       J.20066-03       J.20066-03         7.5       J.11756-14       J.117266-14       J.117266-14       J.117266-14       J.20066-03       J.20066-03         275-11       J.77466-14       J.117266-14       J.117266-14       J.117266-14       J.117266-14       J.117266-14         276-11       J.77466-14       J.117266-14       J.117266-14       J.117266-14       J.117266-14         276-11       J.77466-14       J.117266-14       J.117266-14       J.117266-14       J.127266-14         276-11       J.117266-14       J.117266-14       J.117266-14       J.127266-14       J.127266-14         276-11       J.11766-12       J.1016607       J.000       J.127266-14       J.127266-14         276-12       J.1016607       J.000       J.127266-14       J.127266-14       J.127266-14         27646616       J.000       <	0*5471E-13 -0.3V	UF " U -	c C - SOE	4U-32011°0	0.1272F-73	0.1430F-11	21-27021.0	1.2626E-0R
\$75-73       0.1705-17       0.1705-17       0.1705-17       0.1705-17       0.1205-19       0.1205-19       0.1205-19       0.1205-19       0.1205-19       0.1205-19       0.1205-19       0.1205-108       0.1706-108       0.1706-108       0.1706-108       0.1706-108       0.1706-108       0.1706-108       0.000       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09       0.1006-09	יייצאלאב מיט יייאוֹ	マッシュ	80-308	jr-24711.c	li-staste-	<b>1.69855-13</b>	1.2117E-ro	úu Jolul'u-
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-3*1901E-13 0*61	7.6 T	Éu-sét	J-30121°0	21-20211-6	0.4179F-0°	-0.31915 .C-	£J-3vov7°v-
755-08       7.1       -7.2273F-78       9.507F-09       -0       -9.2202E-08         825-08       -1.2203E-09       -0.1944E-09       -0.1442E-09       -0.2202E-08         825-08       -1.2203E-09       -0.1944E-09       -0.1944E-09       -0.2202E-09         101       -1.102E-04       -0.1955E-09       -0.1944E-09       -0.1944E-09         101       -0.1102E-04       0.1955E-09       -0.1101E-09       -0.1101E-09         101       -0.101E-08       0.1102E-04       0.100E-09       -0.1125E-14         101       -0.101E-09       0.0       -0.1955E-10       -0.1125E-14         102       0.1946E-11       0.0       -0.1955E-10       -0.12125E-14         102       0.219F-14       -0.2319F-12       -0.23135E-15       -0.12125E-14         146-12       0.2118E-14       0.0       -0.1235E-16       -0.3396E-12         146-12       0.2118E-14       0.0       -0.1235E-16       -0.3396E-12         146-12       0.2118E-14       0.0       -0.4945E-16       -0.3396E-12         0.5111E-14       0.0       -0.6405E-16       -0.3396E-12       -0.3795E-18         0.5019E-17       0.0       -0.4405E-16       -0.51386E-16       -0.51386E-12	3 <b>.</b> 09355-03 C.52	ŭ.52	745-14					
75-70       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5       7.5 <td< td=""><td>-0 3371E-78 0 26</td><td>, , , , , , , , , , , , , , , , , , ,</td><td>00-236</td><td>•</td><td>0, 35,56 0.</td><td>0 50016 00</td><td>6 6</td><td></td></td<>	-0 3371E-78 0 26	, , , , , , , , , , , , , , , , , , ,	00-236	•	0, 35,56 0.	0 50016 00	6 6	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			00- n :	0 - 30000 V-				
735-10       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7       7.7 <t< td=""><td></td><td></td><td>0.75-0.0</td><td></td><td></td><td></td><td></td><td>346441E-05 -</td></t<>			0.75-0.0					346441E-05 -
-7.1701E-73       -7.1701E-73       -7.1701E-73       -7.1201E-73         2.7       -7.7575-14       7.0       -7.1301E-73       -7.1202E-13         2.7       -7.7575-14       7.0       -7.13575-14       -7.1202E-13         2.7       -7.13575-14       7.0       -7.13575-14       -7.21256-14         2.7       -7.7575-14       7.0       -7.13575-14       -7.12256-14         2.7       7.7       -7.1555-14       -7.21256-14       -7.21256-14         2.7       7.7       -7.12555-15       -7.12256-14       -7.21256-14         2.7       7.7       7.0       7.0       7.0       7.25356-14         2.7       7.7       7.7       7.7       7.7       7.12256-14         2.7       7.7       7.7       7.7       7.7       7.7         2.7       7.7       7.7       7.7       7.7       7.7         2.6       7.7       7.7       7.7       7.7       7.7       7.7         2.6       7.7       7.7       7.7       7.7       7.7       7.7       7.7         2.146-12       7.7       7.7       7.7       7.7       7.7       7.7       7.7         7.6		c	1.1.2.5		11125-18			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			•		0,7779E-70		-1.10015-78	00-17071-7-
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2°0- 0°C	- U- 2	11-3262	~J-j0+52°0~	c. c	0.0	-1.13526-11	11-3512-0-
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	u°C 71-∃1€ca°u-	• • •		0.0	0°1040E-13	-J°d282c-l2	-0.7646E-14	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0°0 0°6	-0.12	51-3769	-0-94445-12	-1-325E1-14	с <b>°</b> г	0.0	1.1223E-13
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-0"2885E-12 0"37	0.72	+575-1S	U"Ú	0 <b>°</b> 0	-7.29235-14	-1.5657E-12	-1.1210114
S!4F-12     -0.1496F-14     0.0     0.0     0.5339F-12       0.0     0.0     0.0     0.5111F-14     0.3       0.5111F-14     0.0     0.0     0.0     0.64010F-14     0.3       0.51     0.0     0.0     0.6402F-16     0.3       0.5     0.5111F-14     0.3     0.5442F-12     -0.4540F-12     -0.5130F-12       0.5     0.5611F-12     0.5442F-12     -0.5642F-12     0.5010F-12     0.5       775-27     0.5610F-17     -0.3445F-14     0.3     0.7	2.0 D.1	۰. •		1.2713F-14	-0-213E-12	-0.2820F-15	C•;	0.1
0.0     0.0     0.0     0.5111875-16     0.0       0.51116-14     0.0     0.0     0.4     0.57956-13       0.0     0.0     0.5     0.5     0.571965-13       0.0     0.0     0.564256-12     0.573955-13       0.0     0.5     0.56195-12     0.51385-14     0.0       0.50195-17     0.561955-12     0.34955-14     0.0       1775-22     0.561955-17     0.3495555     0.5	-J.5559E-14 -J.29	-1.2	5145-12	143651-14	¢.*¢	0 <b>°</b> 0	J.5359F-14	-7.53395-12
0.5111E-14 0.0 0.0 -0.4919E-14 -0.3795E-13 0.0 0.0 -0.5442E-16 -0.4549E-12 -0.5138E-14 0.0 0.4557E-17 -0.1970E-12 -0.4021E-14 0.0 0.5018E-17 -0.3335E-12 -0.3495F-14 0.0 0.0	-0"1633E-14 0"0	0°0		0.0	0.0		-1.11R75-14	Ć•Ċ
0.0 0.0 0.0 -0.5442E-16 -0.4249E-14 0.0 0.0 0.56019E-17 -0.4557F-17 -0.13485F-14 0.0 0.56019E-17 -0.3338F-12 -0.3485F-14 0.0 0.0	0.0	0.0		0.5111E-14	0.0	0-0	-0.49195-14	3795E-l3
ו י ה.ט איס	- <b>1</b> -9356E-15 7.r	c.	_	0.0	0.0	-3.5442E-16	-).47495-12	-1.513A5-14
י 0.601¤בּוז -ח.33੨פּר-ו2 -ז.34¤גר-ו4 ח.ט מדדר-ז?		c.		0°0	0.4557E-17	-1-10101-12	-1,502l5-14	Ċ°u
at7c=37	J*C 0*C	с• с	_	0.5nl¤E-17	-n.333gF+12	-1.3495F-14	0°L	с•;
		5	9775-22					

**Mode 2, Frequency = 0.** 1977 Hz, **n** = 4 RPM

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="LN lute ors orlist-suls

FIGFWVALUF= J.73303324F ol (rad/sec.)

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4 RPM

Mode 3, Frequency = 0.3710 Hz, **D** 

=°uN Juta eus aulos∧nsis

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9 6 41 6	7 0 T								
-	5		10-313e3-C	-1.4877F.00.	.0.7306F-02	10-31656-0-	-0,7489E 00	0-1100F-03	0-1734E-03
-		14	-0.2771E 31	0.4413E-01	0.47070-34	-0.3452c-31	J.23195-01	-0-50125-03	-0.951/1E 93
15	ţ,	21	-0.19715-31	-1.11555-03	-7.4709F Jn	-0.97155-13	1.4947F-74	-J.4194F AA	0.72285-01
"	17	5.6	0.35715-04	-0.5605F DO	10-3898F.C .	£0-36701°0-	-J.4977F 00	J. 3614F-01	-0-2202E-01
5	5	1,5	-0.4117-0-	-v • 2354c - U1	2.13245-73	-1.421nE )1	10-32366°L	-0-3115C-C4	-0.509'5F 0 <b>3</b>
3 5	5	47	16-364640 .	そし-3ビルシド・リヨ	1.05250.1	71-32515.14	<b>J.L</b> 1276-35	-7.20956-05	0-10+51°C
5	5	ta	0 <b>-</b> 3622F-03	n.7632F-05	0.8980F-07	-J.\$53JF-J6	-3.15165-03	0.9585F-03	-0.1403F-04
ç	C F	5.5	1.94965-97	-0-27055-05	1.1137E-13	n.94315-33	-2.37536-05	0.96525-07	-0.1289F-05
57	Ċ	5.1	-1.57925-14	9.12375-04	-1.14995-36	1.6279E-J3	-U-JZ072-UP	-0.16415-04	0.8352E-05
94	10	70	0.2692F-76	-U- 11 19F -09	<b>0</b> *4082E-04	0.5724F-35	<b>J.1195F-24</b>	<b>0.4551F-06</b>	0.6720E-08
11	٢	77	-0.50726-35	+U-3287e*6-	7.12045-04	<b>2.37595-76</b>	-1,1,12F-39	7.54925-06	n.43215-06
79	C.F	44	iu-jr180.n	-1.47546-055	<b>り。</b> キトネテヒークア	<b>0,11505-36</b>	-7.2376-25	J.1434E-04	0°1001E-02
8 S	F	16	-0.16165-07	0.21345-11	7.70695-76	-0,133RF-3A	J.2134F-11	-3.68415-06	0.2653F-06
ĉ	10	94	· 3.12955-04	1°57995-06	RA-3[68].0-	-0.7596E-07	J.7419E-06	0.76335-06	0.2096E-n2
6	5	115	· +∪-∃  6 °u	n.59745-17	<b>り。Rたちなにーップ</b>	-0.40955-75	<b>3.4125F-36</b>	<b>J.1279F-02</b>	C.1861F-04
5ul	10	711	0.2447F-07	-7.81755-07	<b>0.1</b> 255F-05	0.7195F-76	<b>3.7569F-07</b>	<b>J.3020F-04</b>	3.488lF-07
113	C.	114	じょう4945-10	0°14412-05		•			-
- LUANT	VARY C	3 4 0 T							
-	10	1	n <b>.</b> 7865E-33	-0,797nF 00	0°0	0.7128F-33	-3.2035F 00	0 <b>°</b> 0	0-5524E-03
m	4	14	0.145.00	· ,	1.755lF-03	7.12145 JJ	1.7	<b>J.7013F-03</b>	-0.3090E 03
¥.	5	1		60-34004.0	-u.1551.nn	0°C	n.4549E-n3	0.1136F NO	0-0
27	5	29	3.7569F -03	-0-74755-01	0.0	0.5154E-03	-n.2325F 31	0°C	0-5474E-03
5	t	51.	-9.1619F 02	ت•ن	n. 48245-33	0. 32251°C	0.0	7.7311E-03	-0.75735-01
i.	5	¢,		-01 AGE -17		r.,	0 <b>.</b> J	-1.31525-05	0-200803
4 1	C.	¢ 7	-0.55945-04	c · c	0°0	-0-2136F-35	-n.8131F-04	-0-30E-04	0-0
ç	5	5.5	ເ ະ	-0°19175-35	ウトコレロイド・フル	-0.5471F-74	0.0	<b>0</b> -0	-1.1367F-05
57	۲ ۲	5.2	-3.257575-15	36-302 c2° c	0°0	<b>د •</b> ر	-7.1617F-06	<b>J.1812F-04</b>	n. 7490F-06
÷4	1	7.0	0°0	u <b>°</b> u	-3.79755-36	0°72115-05	0 <b>.43</b> 39F-35	0-0	0-0
1	۲ ۲	77	7.11235-77	-0-34/95-0E	n.3541E-15	, <b>,</b> ,	0.0	-n.1332E-06	-0-3185E-05
79	٤,	J.	-1.54135-74	υ <b>-</b> υ	r.n	1.J	-0.1132F-05	0.4112E-n5	0.0
92 °	-1-1	16	0 <b>-</b> 0	0 <b>-</b> 0	n.9604F-07	c.c	0-0	0.2626F-05	-0-27835-06
65	Ļ	<del>د</del> د .	<b>J.</b> 3014E-15		1.1	0.0	<b>9.1554F-96</b>	-0.35955-05	0.329.75-03
6	Ę	175	0.0	0.7	<b>.</b> .C	-1.15716-35		0.15P9E-03	
501	Ľ,	112		U"U	20-39061-05	-U-36[[[°u-	ù-31FA2€	0°0	<b>0-</b> 0
511	¢ F	114	<b>.</b> .0	0.56465-06					•

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رو کام. = ع Mode 9. Frequency = 0.5025 Hz, D = 4 RPM

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n.1544E-06 0.5441E-02 -0.1000E 01

0-44575-07

-0-31845-07

-0.16535-05 -0.40305-01 0.12405-09 0.29165-09 0.46765-09 0.46765-03 0.46765-03

-0.13136-04 -0.6260F-05 0.0

-0-96545-05

0-42316-02 -0.1815E-01

0.1541E-04

0.20415-10

0.5506F-05 -0.55705-09 0.1 -0.1173F-11 -0.8839F-13 -0.2442E-10 0.5391°-11 0.0

0-0

-9.6788F-09 0.0

0°0

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רע זערג איז פרעספעענדט פירע זערג איז פרעספענדט

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FIGENVALUE= ראוןאַזיּליסאָר 10 (rad/sec.)

-0.59475-05 1.81945-12 3.25775-10 2.0 -0.21965-10 .11405-10 1.1825-10 1.1825-10 0.35055-11 0.0 -0.1352F 00 0.1903F-05 0.7288E-02 -2.34945-07 -2.18375-09 0.40535-05 0.31245-04 -0.10735-05 10-38082-00 0-38185-00 0-38185-00 0.0 -0.1098E-04 -0.9649E-06 ე,2099₽-78 ∩,0 -3.52145 nn -0.78576-03 **1.92915-0**7 0-45645-07 -0.54235-00 0.73595-02 -9.49525 00 0.25975-04 0.83545-07 -0.19975-00 0.75495-79 0.11915-09 0.74955-05 0_8367F-35 ^_0 -0.1051F-34 -0.41615-34 0.0 0.31956-13 -9.32356-39 0.20556-31 -3.61496-39 3.8 1.11055-16 0.15536-12 3.3723F-37 3.8027F 33 1.439RF-07 21-21011 L aù-39621°u 9.5055-12 11-361795-11 1-36275-0 с. с 0.0.0 c c -0+1126F-34 3.545aF-05 0.0 -3,96546-35 -0,25936-05 0,0 0.15955-06 0.44576-02 -0.0235-01 0.40525-05 0.60145-05 0.91595-07 7.7 0.3364E-13 -0.5675F-09 -0-1355-04 -0-13575-04 -0.7675E-12 9.2574E-12 0.3141F-02 -0.2821F 20 0.13215-38 -7.31455-73 50-308r×°0 0.87675-09 0,92096-07 -0-3171E-06 с. с с. с 0*0 с• с 0.15555-07 0.15595-07 0.12395-05 0.12395-05 0.30405-05 0.3109610 1.109610 1.5530610 1.5530610 1.554306 1.1910610 1.2154610 1.2154610 1.2154610 -0110105-34 0119555-94 011 -9.58475-75 7.25375410 3.77595-11 0.7 1.5391F 00 1.5519E-17 -9.12396-97 -9.11595-72 -0.10055-10 £1-30611-0--3.26415-09 -1.5370F-09 0.0 -0-17345-10 7.35755-07 с**1**е 0.0 0.0 0.0 3,3956F-02 -3,0407E -07 7,1524E-07 3,1348F-02 -0,4447E -07 0,27487-07 0,27427E -07 -0-34555-01 -0-53455-12 -0-53455-0-0.0 0.01235-05 0.41795-05 0.4 0.0 0.6415-21 10-20124-08 10-30544.0-0.20365-05 21-20000-0-0.95142-06 - 3.54 ( TE - n'9 0.14125-11 11-22520-0 50-20100 0 0.10545-03 11-35640.0 ດ. ເ с**.**с ¢•€ د. د 0.0 с•с 1,2354F-76 7,37426-78 1,470ng 30 0.2149F447 0-84175-05 0-43735-07 -0-71125-07 9.2155555-19 0.25265-19 0.0 0.11175-05 -1-11511-0 rr 39004.r-3.40525-05 1.28355-74 0.13725-76 -0-11545-03 3.73635-00 3-40525-05 -1.1230E-04 3-17495-05 7.2715F-10 9.2365F-79 11-30062.0 0.0 ۰ د с•с с с 115 211 211 114 4 N 4 ۲ ۲ C C R M C F 4 c o 1000 Idra YERVI ¢, Ē Ĕ C I 55 17 £ C Ę Ę Ē ĉ 5 5 5 5 ĥ Ē E ŗ Ē 5 C. ť 5 55 LAN C IV J a ĉ 105 ž .† € д3 - 11 5 ŝ -----5 6 5 4 5 ć

-0.33415-05 -0.14335-05 0.2 -0.30776-05 0.19916-05 -1.42412-09 20-34961°C -7.12735-02 -^.139325-02 -1.14435-07 11-31684°. 10-31682°. 0.1465F-02 10-28225-0-0°44775 03 J. 45.865-79 6ú-360\$6°€ **1.59**095-04 0.13535-09 51-34966°U -0.13275-12 00-3862 c ° 0-0.14115-05 0.0 с. с ີ -1.16745-25 7.5 -3.3753£-∩5 -9.10955-∩5 1.21635-12 2.-21635-1 or-=1324. 00-31168°C-J-5506F-09 20-34591-0-01-39381-1-0.97056-13 -0.14085-05 11-29661-0-1-26:01.6 -70875-07 10-22151-6-よじーヨサじんと ・ レー 1.1552-07 ==>16°C 0.0 c -0.3575E-05 -2.24475-05 0.0 0°-0 11-30121°C 11-32106°0 0.4570E-13 0.4570E-13 ιΙ-άδοσξ°ί υ°8481ε-υο 7.7910F-25 -3,17545-79 7,28745-12 ĉ 0.4959F-DO -J.3061E-C-J.1194E-32 0-40255-07 26-35155-10-30205-01 -J.7557E-03 7.31355-07 -J.44875 00 -7.63775-13 7.14035-77 76-32052 0 0.15795-17 1.25425-05 0.4923E-14 39000.0  $\Omega = 4 \text{ RPM}$ 0.0 -n.3692F-05 0.[8356-05 0.] 9.8173E-11 7.71335-77 5.11755-02 0.11755-02 -0.21995-n5 -0.31695-14 -0.3377F-05 7.2691F-79 00-30022-0-00-33335"0 0.14005-05 0.1465-32 ק. זנאר אר 1.79145-74 0.596nF-05 -3:23:-3e 0.45705-10 11-32401-0 9.54255-17 7.-36515.0 3.24145-02 : Frequency = 0.5151 Hz, ۰**.** 0.0 **د.**۲ ducec ron 0-0 -0-13415-05 0-30786-05 0-3 -0.87765 JJ -3.18965-79 -3.15545-05 0.73055-08 -0.1 RORE-05 -0-3107E-09 -0.3115E-11 3.5421F-12 -3.5516F-11 0.0 0-11456-02 n.4554F nn 7.14025-75 -0.75576-13 11-30922-0--0*8724E-lû -0.76556-32 0-5377E-04 11-21257.0 -9.33726-14 1-30-51-0 9.42756-07 -1. 9194F-72 0.12525-07 , . . 0.0 0.0 ÷ Mode 10, -7.57295-72 7.7555-95 0-35035-u9 60-37614°u-21-362 36 "0-9.27395-09 1.1242F-12 -0.1922-08 1.2360E-02 -0.1615E 00 0-36323°0 n.10405-n4 -0.9101F-03 -0.1961-07 1-32445-1 -0.10695-05 -1214c-u2 0.76945-11 0.0 n.14695-70 0-1504r-07 -9.1000E 01 7.157Pc-12 0.0 с•с с**°с** ، ٥ د . د с с с. С ن د 1.32766947F 01 (rad/sec.) 1.74445-77 0.11765-77 7.11235 77 0.34925-79 7.23755-79 0.1099E-11 0.0 0.0 1.1401F-75 7.9558F-74 0.73445-05 0.n 0-63725-09 -0-7657E-02 0-36456-00 -0.19745-nz -5-555-02 -3-3425E-02 0.3386F-05 0.92465-11 11-36238-0 -0.55495-05 じ・475ءヒーク 3.14925-07 0-1217E-04 11-35508-0 0.35235-17 5 د. د 0.0 c • 0 0.0 ELGENVECTIR ERE BART NA.= 1.3 5 114 ų P \$ 5 25 5.0 117 14 5 \$ ç 55 ***** 5 4 10 1 CF G ä FIGENVALUE= 7549 VOEN | CAN | Ę Ē £ E Ľ 5 £ Ę ÷ ç 5 5 5 £ Č, ĉ Ē £ Ê Ξ 5 ĉ 5 RFAL ŝ ŝ 11 ŝ 5 5 50 F : : ; i . ;

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		<b>1</b>	•					n.1361F-03 ^_1000F 01	-0.3195F 00	-0.2015-03 -0.36535 00	-0.5974F-03	-0.2333F-04 0.4587F-05	-0-8341E-05	0.27745-07 -9.9541E-07	-0.42875-05	-0.4514F-09 -0.8094F-05	3-3546E-04	0.30726-07	-0.9718E-04	0-1414E-02	0.0 0.2621F-93	20-1702F-02	-4.43036-03 3.0	0.32435-07	C.1642E-08	-0.2717F-09	0.0 0 83105-01	-0-312E-05	0.0			
	、			-				0.2004F 07 ' 0.4326F-03	0.4287F 00	-0.75595-04	0.38455-05	0.7847E-37	-0-83726-04	<b>1.8463F-06</b> <b>3.822F-06</b>	-0-11206-04	-0.43406-05 -0.69876-07	-0-13275-02	0.5778£-04	0.0	-7.8519F-03	0.0 0.0	0.2019E-03	-0-56755-05	0.0	0.2709E-05	-0.25896-07	-3.11615-07 0 34435-07	0.3510F-06	-0.1045F-05	5	·	
				2	I RPM			0.7937F-31 -9.1772F 30	0.20655-03		-1.155E-n9	).24575-04 -0.14775-04	0-3047E-06	-9.1305E-94 -9.5400E-04	3.53955-05	1.2945€-11 `~1.5947€-06	-0-27785-07	-J.2024E-12	<b>3.1939E-</b> 32	0.0	-0-3597E-02		-7.1554E-05	0.0	3-2727E-37	0.0	-0-7445F-08	0.17795-10	0-3439F-06 0 7330E-07			
					, e969 Hz, G = ,				0.45345 70	70-317F1-0-			20-31215°C	7.12505-74 7.55175-74	51-35222°ū	-).56736-39 -r.53636-37	n.13865-34	-0,-51995-97	¢€-36\$66°0-	£v-3356c°C	0.5315E-73	-1.1522F-J2	0.5400F-37	-0.55935-75	0.1100E_15	0.0	0 <b>•</b> 0	0.0	-0.1525F-07.			
					Frequency = 0.		•	0.1973F 90 -0.1347E-01	0.49765 00	-7.45545 00 9.7557F-04	0-23155-02	0.28485-33 -0.28485-33	-0-23016-05	0.P159E-06 -0.1374E-04	0.90415-07	-0.91395-36 -0.76875-08	0-11205-06	-0°6541E-05		-7.81116-74	-0.14/05-07	r0-2254E-03	-010190000000000000	-J.A9316-16	. 0.n _0.15106_77	-0°-J*ot1*C-	3.3 -0 3000-07	0.0	0-0			
				•	Mode 11,	c.)		/ 0.1204F 00 -0.1026F 39	-0-11 44 736-03	-0.34575 n0	.n. 5765E-03	-0.933F-05 r.4453F-05	-0-15406-04	0.37075-09 -9.12165-94	-0-1960-04	1.2846F-11	0.53455-07	-0.15485-05 n.29245-05	-0-17195-02	3.7 2.2222	-0.60965-03	).) 2.53005 05	0.0	-n.43605-37	-0.94795-08 0.0	0.10715-05	c. c		0.0			
				3.= 11	•	Cilf of (rad/se		J.3349E-73	00 30404 C	-0-20815-03 -0-41405 -03	0.4754E 00	<b>].23235-72</b> <b>.39435-07</b>	76-36128-04	3.76145-76 7.92945-76	7.23245-32	-3.4374E-3° -5.1259E-05	3404F-04	3 <b>.11125-</b> 07 0 <b>.14</b> 406-09	-3.24495-03	-3-99545-33	a_n ⊷]3395_∩j	3.3647F-02	-3-56995-95	<b>C</b> •C	3.0	9.3758E-07	-3.5678E-05 7 0	-3.41336-30	0.0			
-	•		· • ·	 1. 1.000 EQ3 or		ic 1.437a5		- 1	12	35	4 7	5 T T T	51	01 11	<b>7</b> 6	16	105	112	- 44	4	10	35	. ta	5.5	63	1	9 - C	-				
				EIGENVELT		, IFANJÜLJ	1515 1830	: : - •	12 21	(	1	1 1 1 1 1 1 1 1	5 F 5	3 F	11 51		, tt	- 1 - 201 - 1 - 101		5	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1		ſ	57 73 14	ן 12		5	er te			

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EIGENVECTOR FOR PONT NO.=

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G Frequency = 0.777 Hz, Mode 17,

4 RPM

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J.48864746F ELGENVALUE=

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BEAL

01 (rad/sec.)

0.1105E 00 -9.0513E 00 9.6936F-05 -0.3670F-07 -0.37676-07 n. 75245-33 - 3.41555-15 90-17E12-0-3-11 94E-05 **7.75555-23** 12-3585[.0 0.2267E-01 0.3337FE-01 0.1824E-05 0.1824E-05 0.1824E-05 0.1874E-04 0.1334E-04 0.25612E-05  0.25612E-056 0.25612E-056 0.25612E-056 0.25612E-056 0.2561 1.1500E-75 -0.52695-95 -3.49345-37 0.18836-01 0.18836-0 0.85636-0 -0.85636-35 3.6864F-34 0.39970E-35 -0.6150F-05 -0.9473F-07 -0.7650F-07 0.36315-35 -0.23305-01 -r .97875-75 -0.1501F-04 A.4797E-76 -0.2426E-33 0.71595-01 0.18725-05 -0.18725-05 -0.18555-01 -0.17335-06 -0.17335-05 -0.87076-05 0.26105-05 0.26105-05 0.26105-05 0.13445-06 0.14445-06 -0.85305-09 -0.85355-05 0.55775-05 0.77945-07 -0.75005-03 -0.16605-01 0.47715-05 -0.11055-01 -0.75805 00 0.20475-11 0.16205-03 0.10465-04 0-15041-06 10-51961-0--U-4114E-07 -0.1653E-05 -0-316-06 -9.21515-01 -3.24575-05 -9.42975-01 0.429275 00 1.24135-05 0.45755-01 -9.45755-01 -9.45775-01 0.4179E-08 -0.4179E-08 -0.4178E-05 -0.16930F-06 0.1602E-05 0.1366F-74 0.4318F-06 -0.4ª46E-03 1000 1444444 R 4 50 555555

1.30195-01 0.37535 03 1.14895-05 2.39295-05

0.52515-05 -j+904E-U1 0-1029E-06 -3.11926-04 0-14665-08 n_5394F-02 01-35006-0

-0-385-01

-7.91056-06

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0-0 0-1723E-10 0-0 0-61316-04 -0-12046-93 0-0 -0.33428-09 -1.20346-09 0.0 -3.44228-04 -0.35666-04 -0.43165-08 0-12365-04 0-33865-04 0-65075-05 -0.3617F-09 0.0 0-0-21215-00 -0-31215-00 112215-00 0-0 7.7 7.32255-04 7.62495-25 7.0 -0.37975-04 -0.11255-10 -0.37125-29 0.2 0.0 0.0 -0-1840E-10 0.10775-73 7.0 0.0 -0.4077E-09 7.0 -0.99936-12 -0.21615-35 -0.221255-09 0.2097E-11 0.9529E-09 0.4678E-09 0.2712E-04 -9.3776-13 0.4215F-34 0.1 -0.1650E-04 11-38122-0--0.1672F-11 0.0 0.0 -0.91395-75 -1.23125-74 -0.57976-76 -0.11775-04 -1.3 0.5941E-11 -0.3969E-30 2.5 -0.8338F+13 -0.34475-∩A 0.0 0.54165-09 0.0 0 ۰°-۲ 0.0 1.7196F-04 -3.3534E-09 0-0 0-0 -0-3446F-17 0.9932E-12 0.1924F-11 0.3 -0-5049E-35 0-1093F-03 -0.3968F-39 -n.3118--11 =11 e . 1 , c. c 0°0 0.0 0.0 0.0 0.0 0.9 0.958FF-14 0.53905-34 -0.4891E-78. 0.0 -0.1105F-10 -0.47045-10 0.7151E-09 -0.1466F-04 0.10605-09 0.37855-04 0.0 0°0 0.0 ċ ċ 0.57195-04 -0.69625-04, 0.1 0.1534E-10 -0.3791E-09 -0.2277E-10 -0.0 0.0 0.2584E-05 0.1557F-04 0.1639E-04 -0.6401E-75 -0.3918F-09 3-152 75-09 0°U 0.0 C.C ; ; ;

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-14-55-55-55

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II (a) (frad/sec) III (a) (frad/sec) III (b) (frad/sec) III (c) (frad/sec) (c)	
<ul> <li>19 Mode 18, Frequency = 0.7911 Hz, G = 4 RPM</li> <li>11 (rad/acc)</li> <li>12.3746-53</li> <li>-0.13776-50</li> <li>-0.17176-50</li> <li>-0.11776-51</li> <li>-0.48776-51</li> <li>-0.49766-51</li> <li>-0.44766-56</li> <li></li></ul>	-0.61945-06 -0.23946-01 -0.23946-01 -0.23946-01 -0.23916-01 -0.28346-01 -1.1110725-04 -1.1110725-04 -1.1110725-04 0.1110725-04 0.1110725-04 0.11106299 -0.33816-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13226-03 0.13106-03 0.13106-03 0.031616-11 0.0 0.0
<pre>.= 18 Mode 18, Frequency = 0.7911 Hz, <b>A</b> = 4 RPM 11F 01 (rad/sec) </pre>	
<pre>.= 18 Mode 18, Frequency = 0.7911 Hz, Q = 41517F-05 -0.1048F-01 0.2044F-07 -0.41517F-05 -0.1048F-01 0.2044F-07 -0.491F-01 0.2104F-01 0.2044F-01 -0.491F-01 0.2107E-01 0.2117FE-05 -0.1177FE-01 -0.7531F-03 0.255FE-03 -0.254FF-01 -0.7531F-03 0.255FE-03 -0.254FF-05 -0.7531F-03 0.255FE-03 -0.254FF-05 -0.7531F-03 0.255FE-03 -0.2449FE-07 -0.7117FE-04 0.2 -0.7531F-05 0.1110F-04 0.1116F-04 -0.7535FF-04 -0.1110F-04 -0.1110F-04 -0.1574FE-05 -0.1747FE-04 -0.1574FE-04 -0.1534FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1574FE-0 -0.1110FE-04 -0.1110FE-0</pre>	RPMI -0.48275-02 -1.127355-01 -0.127355-01 -0.127355-01 -0.12755-01 -0.12755-01 -0.12755-01 -0.14755-01 -0.14755-01 -0.14755-05 -0.14495-07 0.14495-07 0.14495-07 0.14495-07 0.14495-07 0.23755-04 0.23755-09 0.43715-00 0.43715-00 0.43715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.543715-00 0.5475-10 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.5237555-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.523755-01 0.5237555-01 0.523755-01 0.523755-01 0.5237555-01 0.523755-01 0.523755-01 0.5237555-01 0.5237555-01 0.5237555-01 0.5237555-01 0.5237555-01 0.5237555-01 0.5237555-01 0.523755555555555555555555555555555555555
<pre></pre>	911 Hz, <b>Q</b> = 4 9.27445-75 0.27445-75 0.243475-71 0.243475-71 0.243455-71 0.243455-75 0.243455-75 0.243455-75 0.213455-75 0.212375-75 0.11375-75 0.11375-75 0.11375-75 0.11375-75 0.11375-75 0.11375-75 0.12375-75 0.12375-75 0.13375-15 0.13375-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.133475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13 0.134475-13475-13 0.134475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-13475-
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<ul> <li>18</li> <li>18</li> <li>11. 01</li> <li>15.375-05</li> <li>15.375-05</li> <li>14.555-05</li> <li>14.555-05</li> <li>14.555-05</li> <li>14.555-05</li> <li>14.555-05</li> <li>15.55555-03</li> <li>15.55555-03</li> <li>15.55555-03</li> <li>16.55555-03</li> <li>16.55555-03</li> <li>17.225555-03</li> <li>18.555-05</li> <li>18.55555-03</li> <li>18.55555-03</li> <li>18.55555-03</li> <li>18.5555-03</li> <li>18.5556-03</li> <li>14.555-03</li> <li>15.5555-03</li> <li>15.55555</li> <li>15.55555</li> <li>15.5555</li> /ul>	Mode 18, E Mode 18, E -0.10486-01 -0.22105-05 -0.331356-01 -0.331356-01 -0.223075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.23075-05 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0.2005 -0
	<pre>Vl.= 18 SfallE 01 (rad/se -0.1537F-05 -0.1537F-05 -0.1537F-05 -0.2554F-05 -0.2554F-05 -0.2554F-05 0.2554F-05 0.2554F-05 0.2554F-05 0.2554F-05 0.2554F-05 0.2554F-05 0.1567F-05 0.1567F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.1505F-05 0.12557F-05 0.1505F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.12557F-05 0.125</pre>
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0.9775E-09 0.6776E-02 0.16776-02 0.143945-01 0.21435-01 0.21435-07 0.21435-07 0.21435-07 0.214365-07 0.235965-07 0.65346-07 0.82936-06 0.0 0.32496-07 0.23036-07 0.23036-07 0.0 0.1470-11 0.47026-09 0.47026-09 0.33126-10 0.41346-11 0.1 0.20255-01 -0.15785-11 -0.7415-06 -0-3433E-10 3.952RF-03 11-3816+°Ŭ--0-1573E-04 -3.59785-01 0.29165-07 0.27916-04 0.21357-0 0.12325-07 0.12325-05 0.21965-05 -0.49635-05 -0.49635-05 0.27715-07 0.21675-07 -0.18605-00 0.13805-00 0.13805-00 -0.28055-15 .0.0 -0.1084E-05 -0.1106E-05 -0.9619E-07 -0.9512E-11 0.1941E-10 -0.27815-11 -0.23135-12 0.29695-11 0.25145-11 0.25145-11 0.3221E-09 0.85115-07 1 0.0 0.0 0.13896-07 -0.13896-07 -0.10006-01 -0.173056-05 0.17316-07 0.17316-07 0.19395-11 -0.37165-12 0.0 0.54895-06 3.1 0.75746-07 3.36916-06 1.0 0.0 0.3437F-99 9.5A11E-13 -9.473AF-09 0.6134E-09 0.0 0.4107F-13 7.7167F-09 7.7293F-11 -0.8405F-08 -0.9993E-11 0.1037F-12 -0.2176F-03 -0.5487E-01 -0**-1**640F-04 7.1919F-11 4 RPM 0.0 n 0.859% - 08 -0.859% - 04 0.5955 - 04 0.5945 - 03 -0.1397 - 03 -0.2142 - 03 0.2715 - 02 0.27515 - 05 -0.40515 - 05 0.8539E-07 0.3600E-06 0.0 0.3246E-07 0.4331E-06 0.11585-74 0.13855-74 -0.44575-74 -0.7213E-11 0.1839F-10 0.3715E-09 0.1517E-79 -0.5n305-04 01-30202-04 -0-2029E-10 C -0.11435-32 10-38F71-0-0.9049 Hz, 0.00 0.0 6°0 ŕ, 0.6762E 70 9.10605-77 0.3601F-03 0.3501F-03 0.3533F-09 -0.3533F-09 -0.70275-08 -0.72916-05 0.13835-09 -0.28585-04 0-55385-97 0-33715-06 0.0 -0.96175-07 0.19235-10 0.0 n.r -9.3112E-11 9.9 7.5 u 0.53965-02 0.94285-11 -0.1232E-35 0.6070F-09 0.0 -0.1503E-11 0.8556E-12 0.9797F-35 -0-3403E-09 C.1037F-13 Frequency 0•° Mode 19, 0.42215-11 -0.11875-11 0.0 -1.1936F-05 -0.22932E-02 -0.9142E-09 -0.9381E-09 -0.9381E-09 -0.2703E-04 -0.45695-02 0.25195-09 -0.84775-98 0.19145-07 -0.37235-02 0.50115-13 0.14615-03 3.0 -1.25756-96 0.13096-96 0.0 0.1728F-09 3.0 J-1412E-09 1-36196-07 ------0.[[qaf-14 -0.1432E-05 0.37A5F-15 ۰. ۲ 7.562549585 01 (rad./sec.) , 0.17695-02 -0.49516-06 -0.72956-05 -0.72956-05 -0.22136-07 -0.18005-02 0.20495-75 0.14005-07 0.0 0.75735-07 0.75735-07 0.30195-11 0.18435-10 0.0 0.32565-12 0.0 0.0 0.19016-07 -0.12716-04 -0.11676 70 -9.15096-04 -0.15985-09 -0.49555-06 -0.69275-04 -0.81415-08 7.3485E-09 0.0 -0.2148E-74 0.1825F-19 -0.9361E-73 2 0.0 0°0 1.5 TUCA E-LGENVECTAR FIR 5112 1055005 0 5 3365 513 œ 52 112 114 P 42 T 5 5 Ē E 1 CC VVALUE = 7 94 7 **CEPEEEEEEEEE** VANNICAMI 55555 5 5 55 5 EEEEEEEE q F ∆l 22 1 6 35 \$ 95 9951 9 5 7.9

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	· · · · · · · · · ·		·		-0.6421F-01 -9.5365F-03	0.87036-01 -0.61946-01	3.5431E-04 0.51355 05	0-95126-03	9.2263E-08 -0.4267F-04	-7.22145-05	0.28505-04	-0.2075E-06 0.1600E-06	0-2539F-02	0 <b>.</b> 8494F-04		0. 3306E-03	-0.2754F-03 0.0	-0.1448E-04	-0.1346F-07 -0.8407E-07	0.0	-0.1591F-05	0.0 0.1270f-07	-9.8024F-08	-7.1468F-07 -3.2606F-05	-0.22445-07	6 • D	•				
		= 4 RPM	·		7.6235F 00 -2.27535-01	-0.7532F-03 -1.2977E 30	3.21295 DD	-1-3517E-03	-3.7319E-06 -3.7334ë-06	3.2754F-34	-3+192E-35	1.3470E-11 7.1542E-05 .	0-6645F-07	<b>3.5115F-02</b>	-0-36145-02	0-0	-0-14435-03	C• C	J.7 -^ 39355-A5	0 • 0	-3.9858F-DA	0-01-020-03	-3*3315E-04	7.7 -0.2473F-09	-0.13596-05	1(1-2000).**	•			-	
•		0. 9291 Hz, <b>Q</b> -			0.3780E-03 1.4274E 00	0-3100E-01 -0-1437E-13		-0.4032E-35	0.5554E-33 2.1920E-36	0.50815-04	0.4900E-06	-7.11385-77 -7.64395-07	-3-12156-34	<b>3.1216</b> E-76	-0-42965-03	-0-1935-32	0-3 -0-17355-04	-0.3747E-J3	0.0 ∩ 86785-∩9	-0.79165-37	0.100EC 34	0	······································	0.0	-0.8216E-13		· · · · · · · · · · · · · · · · · · ·				
		. Frequency =			0.4945E-01 0.1495E-03	-0.10305 00 7.31205-01	-9.6837E-34	50-31164°C-	7.35846−∩∃ -0.15936−04	-3.12335-96	0.4107F-0A	-3.20745-36 3.11206-37	0.3678E-76	J.1415F-74		-0.5094E-73	0.515F-03 0.3	-0.9438E-05	-3.91116-37 7.7	-0.2351E-75	0.01005 08	-0°31516-00	c.0	11-38441.0 0.0	3.7 0 71106-11						
• • •		Mode 20,	î		0.17005 01 -0.2579F 10	0.5235E-03 0.9473F-01	1.2564F-01 -	-0-1835-04	-0.57125-05 0.27855-04	3.57785-78 -0 67385-06	-0-78465-04	0.39705-11 1.1555-05	0.75565-77	+0.23255-76 0.23855-75	0-34935-02		-0-79585-04 0.26.735-03			-1.91736-09	-0.65965-78 2 0		0.0	0.0	0.0	11-stle1.0		,			
	· · · · · · · · · · · · · · · · · · ·	1.= 2n	744F nl (ræd/sec		-0.33026-03 1.25065 03	3.2266F-01 7.254DF-17	-1.26795 00	0.65645-03	-0.21405-04 0.48935-04	n.13296-75 7 12786-76	0.4547F-13	9.3065E-97 0.27315-04	J. 3466F-04	0.61495-07 0.26285-99	-0-7737E-03	3.1553E-72	0.7 -9.2733F-33	0.11005-72	- 3.50 -1.76015-37	0.0	-0.1594F-05		-0+9262F-37	U.0 -1.4831E-78 .	c•0	· · ·			•		
	•	וא דהרא ארא אין אין אין אין אין אין אין אין אין אי	= n.\$8375	1	14	21 29	5.00		55 53	11 01	36	16	115	112	1 404	14	11 C. C.	35		56	F 4 F	11	9¢		1.15	114					
		ELGENVECTO	2(1784421)5	REAL PART		15 TO 22 Th	23 TC	11 E4	57 17 	64 T 48	CI 11	28 17 17	11 66 ·	105 TA	TT I	6 I I I I I I I I I I I I I I I I I I I		21 CZ		57 57	57 IJ	11 12	TT FT		01 101 01 101					•	
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11 201 2	1 4 L IJF =	1.5A01	ואָסאָר חן (rad/s	sec. )					
DEALO	AOT		- - - -		•		•		•
	C F	1	1.198F-J1	-0-1000 -0-	-1.23275-71	-0.11575-31	-0.9983E 03	10-31918-0-	0.55525-32
α	13	14	CC 34000	16-31642.0-	CC-35255 U-	00 36860 0-	-0-30806-01	lú-slsil°u	Cr 35168.0
5	ŗ	21	16-3901206	-0-14055-71	CC artes.	16-3915200	3.77745-02	00 35418°C	10-34840.0
·	4	29	-1.7775L-	C JILOS"C	lr-stive L	0.4379F-12	7.7764E 33	lú-sciel".	-0-27269-0-
52	Ú1	15	0.31¤15 OG	10-34122*0	0-34116-02	0° 32622°0	J.1932F-01	20-31146-0-	0.27345 33
5	2	42	10-3012c°u	IL-JZEUE U	01 36701°0	14513	7.0-317no.0	Eù-sèttit.	-0-2007-01
£3	7 7	• •	טי ומאחד אח	-0-19291-03	U- 79! 35-97	r. joit.	20-35186-0	ט"וַזּקּזר טָט	-0-181+E-03
5	17	5 5 5	7.843 JE-07	r.150051.0	-1°04275-17	0. 3698l°u	-9.17 it l.	20-36292°ū	u"J Strie-us
57	ţ	ۍ . ۱	<b>3.19355-02</b>	ビューコー いっとっし	ちんーニさょでんやじ	-3.24135-76	<b>0°1003E−U</b> ¢	-3.213TE-32	5 <u>-1297</u> 503
5	5	10	-J*6234E-J2	-J.27605-n7	ji-jill1°i	トピーコレヤイト・	7.2192F-33	96-31531.0	-0-31515-06
11	13	17	J.14775-04	-0-11065-02	10-27241-0	-3.377F-75	-0-345£8-07	3.27245-04	3-16555-35
7 8	¢.	94	<b>9.18475 JA</b>	-0.17565-03	0. Rrale-17	0 <b>*1</b> 044c-15	2.17905-03	2.52475-03	0.11445-03
85	Ę	اد	-0.31256-95	U-945259"U	-0 <b>°1</b> 5a1č-j¢	n_53435-97	7.66525-11	70-siti'u-	1.745zE-37
9	1.7	аŖ	1.20195-03	9.40945-05	-n.13025-n6	-0.15875-76	<b>3.11335-34</b>	30-32821-6	UU JEBII,"U
6	1	175	v~241 dc-14	10-32202-6	90-scere"ŭ	, 79anc-11	0°44735-36	10-3642100	90-31106-0
105	5	112	7.5525F-07	9ú-slav9°0-	£i-sc211°i	JC-36818°.	<b>3,571 25-01</b>	5.1475-n3	C. 79735-07
113	10	114	0.37315-09	0.7141F-AT-					
LISANI	IAFY DI	40 T							
-	5	•	9.25375-93		0.0	Q.2532F-J3	· 3.5133E-32	1. • C	0-34555-03
a	Ľ,	14	といーヨラ じとし じー	с <b>"</b> с	34475-13	).3247E-07	0.0	20-25121-0-	20-25-20
15	Ċ,	. I.	, <b>r</b> .	cu-3cuel-u-	cu-suile"u-	с <b>~</b> с	-0-3F7C102	26-3622.0	0.0
57	<b>۲</b> ٦.		-1.17725.1.1-	1 3 5 1 5 - 1 2	· · · · · · · · · · · · · · · · · · ·	0 <b>.</b> 3255 <b>.</b> 13	7.4n52E-07		-J.,34435-03
ť.	۲. ۲	35	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	J. C	FP-36125_0-	C_34576_02	с <b>-</b> г	£0-35tlt°u-	-0-23:15-05
S.F.	Ē	47	<b>,</b> .	Fr-7979613	51-32 CEE "U-	۲ <b>۰</b> ۲	 	~3~34346~02	-0"23162"C-
4	5	t 1	-1.36aje-15	J•7	<b>0</b> •0	<b>1.2555c-</b> 75	-J.1235E-03		0.0
5	с н	54,	U°U	-9.14335-05	-0.12245-Ji	-0,3581E-75	0°0	1. U	0.16065-05
57	ţ	51	-7.15525-74	しょんしつにした	с. с	<b>د</b> - ر	- <u>,</u> ,3947E-07	+0-39c31-u-	-0-15115-06
54	ç	¢,	· · ·	¢ • c	i Chase la"u	-J.\$873F-05	9.2977E-07	•	
11	5	77	-0-11+0E-06	-0.6172F-05	-0.8750F-07	 C•C	c*0	0-10110 V	-0-69615-04
79	٢	94	-0.3509F-75	0°,	<b>3.</b> 3	<b>1.</b> ]	-0.7505E-08	20-3532102	0.0
<b>و</b> 5	5	<b>.</b>	ر•ر ر	<b>د</b> .• ر.	0°1413E-04	с. с	0.0	-2.1175-96	-0.37545-05
čò	ţ.	۳ ۲	-7.344KE-07	<b>c</b> •c	0°0	u"u	-0.3071F-08	-1.575 E-04	-U.J 7325-05
6	5	וזק	0°0	, ,	۔ ۲۰۲	-1.35F2B	-J.1977E-04	-1.5453; -15	0.0
101	5	117	<b>د •</b> د	0°0	-0-40,45-04		らいーコレごね i やいー		0.0
	۲. ۲.	114	0-0	0.1510 ^c -03					

. Mode 28. Frequency = 1.051 Hz,  $\Omega_{-}$  = 4 RPM

.Etgewyertio Fna annt yj.∎ 28

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へとってしっ	ALIFE	J.241159105 02 (rad/se	ic. )	•	· · · · · · · · · · · · · · · · · · ·				
0 T 0	40 T								
r		([ 31100 U	0.55946-72	0.4276E-73	1.99955 1	0 57075_03	0 2001E.07	0 1551 0	
đ	1 14	5	0.42765-02		1.49456-72	9.4747F-02	0-4414F 00	0.55065_03	
5	10 01	0 47245-03	1. 44175 JA	1.5340F-32	0-44775-02	0-JUATE 00	0-40405-02	0-20-20-20-20-20-20-20-20-20-20-20-20-20	
"	F7 78	7,39435 77	1.5099c-n7	0.45476-77	J. 95735 JC	J. 5959E-02	0.46255-02		
۴.	Tn 35	7 .6052E-12	じ。44745-72	0.3015F 3n	J.5391E-32	7.4629E-12	0.3023E 00	0-51235-02	
34	17 42	0 *4637F = 02	00 34087 00	1. ROJZE-G3	-0.19765-33	9.8096F-06	0-47945-02	0-4790F 00	:
4	4.0 F		+C-3v2 lb*U-	1.44125-74	47625-33	9.17945 30	0.79865-03	-0-14365-03	
5	ta 55	3.54776-75	י,>ם55ב−י2	<b>1.17975 JJ</b>	1.70645-73	-9.13995-03	0-19045-06	-0-29455-02	
5	10 51	D. AA54F CD	0.15305-03	7.5471F-74	-0.26405-07	0-44495-02	0-66415 00	0-6072E-04	
\$	T1 70	う。54335~74	-u-56585-77	cù-sl\$\$\$*6-	J.22565 JD	n.1269E-03	J. 50195-04	-0-41516-07	
2	11 11	3.61555-32	ύ <b>ι</b> 3250ε 30	り。95475-74	9.540AE-34	7.4649E-07	-J.61425-07	7-8338F-01	
13	10 84	10-12101°C	-C-11611-01	0.24ANF-06	21285-05	-0-465RF-04	0-26165-03	0-66445-05	:
д.	10 01	. 31645-75	い。19145-79	-0-54 J9E-72	-3°=13616°C-	9.1914E-09	0.63985-02	0-10376-01	
6	11 9.9	1.10575-03	r.5ng25-n4	3.49545-07	-j.22155-j5	0-42715-05	0-65535-01	0-13595-02	
6	10 ID5	0.1318F-J2	7.5926F-07	0.275RF-05	-3-3446F-35	0-3558-01	n.12615-02	0-12715-02	:
۲ ن ر	r. 11.	7.12225-15	らじー コビヤシヒー じこ	い。48705-15	-1C-36F74.	J.7079E-02	9.1421E-92	0.99605-07	
11	114	7.79345-77	n.15695-07						-
210981	A7V DA2T					•			-
	1 1	12-316940	しーコットじっしい	0°0	0.55195-71	-7.23126-01	0.0	0.1753E-01	
<b>e</b> -	11 14	-ü-aCblb-ü-	د	16-32602-01	- ).31595-12	0.0	<b>J.3564F-01</b>	-0.1892E-01	
5	12 01	C • C	10-jo105"0	-0.18715-01	0°0	A.1294F-01	-7.67075-02	0-0	:
~	с. Г.	1.17101.01	-0.46265-02	· C • L	16-30852.	-7.22515-31	0-0	0-45556-01	
ς.	10 15	10-3256686-	۲ <b>۰</b> ۲	0.17595-31	- 7. 19555 - 72	1.0	<b>n.1688E-01</b>	-0-78165-02	
	57 F2		11-31-11-0	10-30621-0-	C.6	0-0	0.1836F-03	0.33376-01	
ļ	C +	10-36021-0-	0°C	c•0	ίι-slllt.u-	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	-0.1392-01	0.0	
ŝ	Υ.Υ. Υ.Υ.	r • r	· • 7355-94	10-34121.0	16-26661"	<b></b> 0	0.0	-0.21805-01	
~	1.7 F.	10-36836.01	0.10525-02	0°0	0.6	<b>J.2356F-03</b>	0.3221F-01	0.68375-03	
÷,ç	10 10	0.0	<b>).</b> 0	-0.22145-73	0.1292F-01	<b>J.9154F-Ul</b>	0.0	0-0	
1	17 FT	10-30566 0	1.10405-11	U.7456E-MR	C • c	0°1	-0+3001E-03	0-43095-02	
8 <b>4</b>	1U 84	lv-3c62l*v-	с <b>°</b> с	· • • 0	0°0	-0.6678E-04	0.10615-02	0-0	:
e.	1, ,	0.0	c•c	-0.3467E-03	0.0	0.0	0-31345-01	0-53465-03	
6	1.0	n.79195-11	<b>.</b>	C.•C	<b>0</b> •0	0-2222E-04	0-3787E-02	-0-10256-03	
6	TΩ 105.	<b>ن•ر</b>	υ <b>•</b> υ	0.0	-0"54775-04	9.14925-02	7.2642E-02	0-0	!
105	10 112	· , ,	0.0	-0.79345-75	う。24435-72	n. 7906F-06	0.0		
11.	11 114	<b>c</b> *c	r.46295-12						
					:				
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ELGENVECTOR FOR FUUT NO.=

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Mccet 1. Frequency = 0.1787 Hz,  $\Omega = 8 \text{ RPM}$ 

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	(rad/sec.)	
	01	
	0.11227112E	•
	EIGENVALUE≈	

	TOAC								
		I						1	
-	ÚL	1	0.1154E-06	0.29765-02	-1.453BE 30	-0.13765-07	0.2978E-02	0.9604E 00	0.7224E-07
er;	10	14	<b>0.2978F-02</b>	-C.42965 00	-:-:73cE-08	0.2978E-02	0.4313E 00	0.1030F-06	0.1837E-02
15	1Ū	e1	-0.1000E G1	-0.3139E-37	:.::37E-32	0.9997E 00	0.55945-37	0.1837E-02	-0.4481E 00
22	r F	23	-0.1127E-07	U.1037E-02	00 Utate!	0.649UE-U7	0.1254E-02	-0.3953E 00	-0.2585E-07
502	10	35	0. 1254E-02	0.39495 20	[ • + 5 + 3 E - 0 7	0.1254E-02	-0.1769E 00	-0.1901E-07	0.1254E-02
36	10	42	0.1775E 10	0.6424E-37	:-1228E-05	-0.5851E 00	0.4481E-02	0.5361E-09	-0.5344E-07
43	10	49	0.1292E-05	0.5846E 00	:.**:1E-02	0.3909E-09	0.2696E-07	0.1291E-05	-0.2624E 00
50	10	56	0.4481E-32	0 <b>-4</b> 831E-05	-:-:475E-07	0.1292E-05	0.2619F 00	0.4482F-02	Q.4136E-09
57	10	¢ 63⁺	C.338CE-07	0.1442E-07	-:.17525-02	0.1414E-04	-0.6723E-10	-0.3487E-07	0.9176E-08
54	5	70	<b>J.8438E-03</b>	0.21025-05	-:-:1316-10	0.3023E-07	0.14285-07	-0.7548F-03	0.1329E-04
11	10	11	0.2502E-09	-0.31505-07	1-11936-07	0.5123E-03	0.7249E-05	0.2699E-09	0.1354E-09
78	10	84	0.1291F-05	-0.25115-33	:-++?1E-02	0.4556E-06	0.4375E-09	0.1481E-07	-0.5141E-02
85	10	16	0.1425E-04	0.1629E-12	-1.1739E-09	-0.6389E-05	0.1829E-12	-0.1788E-09	0.6929E-11
92	10	98	0.1416E-07	-0-30445-04	: • : 124E-04	0.8842E-06	0.8153E-09	0.9758E-10	0.1505E-05
66	5	105	-0.1534E-03	0.33645-32	:-2516E-06	-0.3384E-08	0.4001E-10	0.1213E-05	-0.1258E-03
136	5	112	C.1129F-02	0-69225-07		0.6527E-10	0.23956-05	-0.1281E-03	0.2247E-02
113	C F	114	0.1824E-04	0.33555-11				•	
19471	イトロノ	PART							-
1	0 F		-0.247nE-05	0.52035-35	•. • •	-0.2470E-05	0.6613E-06	0.0	-0.2469E-05
ar.	۲ <b>۲</b>	14	0.2346E-05	0.0	-1-14-05-J5	0.1942E-06	0.0	-0.1667E-05	0.3315E-05
15	Ū.	21	0.0	-0.1667E-J5	:.::735E-06	0.0	-0.1666E-05	0.1468E-05	0.0
22	C'	28	-0.1605E-05	0.965 <u>e</u> f-77	ć.,	-0.1132E-05	0.2215E-05	0.0	-0.1:132E-05
62	С Г	35	0.9057E-07	0.0	-:.:31E-05	0.8814E-06	0-0	-0.1131E-05	-0.1582E-06
9 <b>6</b>	¢.	42	6. C.	-0.2337F-78	-:-:152E-11	0•0	0.0	-0.2082E-10	-0.2255E-08
£3	C F	49	-0.3895E-11	0.0	- - - -	0.1966E-10	-0.1015E-08	-0.81046-11	0.0
5.5	5	56	0.0	-0-13476-10	-1-5597E-09	-0-8494E-11	0.0	0.0	0.1298E-10
57	10	51	-0.6354E-09	0.23265-12	• •	0.0	-0.3649E-11	-0.6116E-09	-0.2029E-11
4. U	C: H	70	0.0	0-0	:-::3E-11	-0.2825E-09	-0.3380E-12	0.0	0.0
11	10		-0.6027E-11	-0.27155-59	-:-1602E-11	0.0	0-0	0.5806E-11	-0.5631E-09
16	C 1	5 H	-0.8262E-11	0•0	€. •	0*0	-0.6632E-13	-0.1337F-11	0.0
a, L	<b>ں</b>	16	0.0	C-0 .	:-5520E-11	0.0	0.0	-0.5318E-11	-0.4015E-10
5	10	98	-0.1017E-11	<b>F</b> 0.0	{	0.0	-0.5815E-13	-0.4475E-09	-0.5505F-11
<b>6</b> .7		105	0.0	5 0 ° 0	4 x 4 1 1	0.4706E-14	-0.2073E-09	-0.6331E-11	0.0
÷01		112	0°0	0.0	[•===53E-14	-0.3577F-09	-0.3733E-11	0.0	0.0
'n	C F	114	0.0	0.13545-19			1		1

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FEGENVECTOR FOR ROUT NO.=

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Mode 2. Frequency = 0.1977 Hz,  $\Omega$  = 8 RPM

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ETGENVALUE= 0.12424011E 01 (rad/sec.)

~ ;	0.2047E-09	0-2169F-05	-3.5036E 00	-0-3265E-10	0.2169E-05	-0.6463E 00	0.1286E-09
	0.2439E-05	-0.54635 00	-0.6307E-11	0.2439E-05	-0.6381E 00	0.1884E-09	0.1562E-05
	- <b>-</b> *6855F 00	-0-6643E-15	<b>2.1562F-05</b>	-0.2734F 00	0.10235-09	0.17126-05	-0.7372E 00
	-0.74735-1)	0.1713E-35	-2.5214E 00	0.1218E-09	-0.1083E-06	-0.2843E 00	-0.4964E-10
	-U.1083E-J6	-0.3590E 00	0.85346-10	0.1664E-05	-0.3046E 00	-0.3472E-10	0.1664E-05
	-0.3381E UU	0.1266F-09	0.2346E-08	-0.7836E 00	-0.8276E-03	0.10396-11	-0.1072E-09
	0.2352E-08	-0.1000E 01	-0.8305E-03	0.7766E-12	0.5392E-10	0.2350E-08	-0.8432E 00
	-0.8279E-03	0.9539E-12	-0.4998F-10	0.2352E-08	-0.9402E 00	-0.8300E-03	0.8292E-12
	0.6131E-1C	0.2532F-10	-2.4918E-02	0.15985-04	-0.1131E-12	-0.63395-10	0.1643E-10
	-0.19695-02	Q. 7332E-05	-0.1404E-12	0.5429E-10	0.2557E-10	-0.38036-02	0.1460E-04
	0.45465-12	-0.5894E-10	C.2137E-10	-0.2503E-02	0.7872E-05	0.49296-12	0.2404E-12
	0.2351F-06	-0.8917E 00	-0.8288E-03	0.12395-02	0.8394E-12	0.25536-10	-0.8791E-02
	Q.1637E-04	0.3198E-15	-0.3299E-12	0.8691E-05	0.3198E-15	-0.3287E-12	0.1229E-13
	0.2536E-10	-0.30395-02	0.1102E-04	0.1232E-03	0.14565-11	0.17346-12	0.2693E-08
	-0.5844F UD	-0.6189F-03	C.1178E-02	-0.5908E-11	0.71016-13	0.21635-08	-0.1019E 00
	EC-31661-C-	0.6343F-03	5.1226E-10	0.1161F-12	0.4267E-08	-0.3091E 00	-0.4090E-03
	0.9835E-U3	0.6C12E-14					
							•
	-0.1317E-05	0.3927F-05	0.0	-0.1317E-08	0.1174E-08	0°0	-0.2783E-08
	0.2151E-0P	0•0	-0.2784E-08	0.1008E-08	0.0	-0.1012E-08	0.3117E-08
	0.0	-0.1012E-09	J.6463E-09	0.0	-0.1963E-08	0.15656-08	0-0
	-0.1963F-J3	0.5285F-09	0°C	0.1052F-09	-0.2600E-08	0.0	0-1053E-09
	0.1541F-JS	0.0	-0.1672E-08	-0-9982E-09	0.0	-0.1672E-08	0.15215-08
	0.0	-0.4865E-11	-3.1742E-13	0.0	0.0	-0.43485-13	-0.4697E-11
	-0.1924E-13	0.0	0.0	0.4108E-13	-0.2104E-11	-0.17406-13	0.0
	0.0	-0.2815E-13	-0.2073E-11	-0.1833E-13	0.0	0.0	0.27136-13
	-0.1353E-11	0.43ò7E-15	0-0	0-0	-0.650JE-14	-0.1305E-11	-0.4217E-14
	0.0	0.0	J.6267E-14	-0.6003E-12	-0.6736E-15	0-0	0-0
	-0.1286F-13	-0.5780E-12	-0.3326E-14	0-0	0.0	0.1241E-13	-0.1160E-11
	-0.17796-13	0.0	ũ.0	0*0	-0.1394E-15	-0.27966-14	0.0
	0.0	0.0	D.1176E-13	0*0	0-0	-0.11356-13	-0.8289E-13
	-0.2091E-14	0•0	0.0	0-0	-0.1135E-15	-0.9189E-12	-0.11366-13
	0.0	0.0	0-0	0.7864E-17	-0.4248E-12	-0.1290E-13	0-0
	0-0	0.0	0.1318E-16	-0.7330E-12	-0.76195-14	0.0	0-0
	c c		1				

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Mode 3. Frequency = 0.3524 Hz,  $\Omega$  = 8 RPM

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ELGENVECTOR FUR RUCT NJ.=

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Ê I GE VV	, ער טיי =	0 <b>•</b> 2214	4775F UI (rad/s	ec. )			•		· · ··································
HEAL P	ART								
~	10	7	Ċ.1236E-02	-0.2601F 00	0.4525E-03	0.1315E-02	-0.1500F 00	-0.2957E-02	0-1071E-02
70 •	10	14	-0.1713E 00	0.4280E-02	0.11216-02	-0-44346-01	0.1507E-01	0.1087E-02	-0.5129E 00
15	10	21	-0.3375E-02	0.1306E-02	-0.3038E 00	-0.97285-02	0.9261E-03	-0.2980E 00	0.3774E-02
22		26	0-10446-00	-1.22456 90	J.2414F-31	9.74945-03	-0.2786E 00	-0.2987E-02	0.1093F-02
50		35	-0.2725E.DO	-0.11526-01	J.1043E-J2	-0,31926 00	0.1032F-01	0.1027E-02	-0.2399E 00
35	10	42	0.3791F-01	-0.57685-03	-0.3167E-02	-0.2655E-05	0.3071E-07	-0.5869E-05	0.2393E-03
4. 19.	10	40	-0.31635-02	0.5651E-05	<b>0.3443E-07</b>	-0.1826E-05	-0.1996E-03	-0-3164E-02	-0.4340E-06
50	10	56	70-30116-07	-C.3973E-05	0.1C85E-03	-0.3162E-02	0.3222E-05	0.3223E-07	-0.1783E-05
57	10	53	-0.358CE-04	-0.65375-05	0.1121E-06	-0.8655E-09	-0.4679E-06	0.2816F-05	-0-3674E-05
	10	70	0-1049E-09	-0.31546-10	0 <b>.</b> ¤346E-07	-0.3514E-04	-0.6398E-05	0.2943E-07	-0.8605E-09
11	1.7	77	-0.3004E-36	P.+6693E+C5	-0.4305E-05	0.3857E-08	-0.4215E-10	-0.3820E-07	-0.1198E-04
75	. 61	4	-0.31635-02	0.13955-05	0.31025-07	-0.22345-08	-0.2654E-05	-0.7755£-05	-0.1291E-06
. 85	10	10	0.1950E-36	J.5410E-12	0.7736E-06	0.83786-11	0.5410E-12	-0.2435E-07	-0.9155E-06
2÷	10	8	-0.5133£-05	C-7440E-3E	-0.1011F-09	-0.6484E-09	-0.1887E-06	-0.9130F-05	-0.1972E-02
65	10	05	0.9051E-06	<b>0.2164F-37</b>	-0.16415-08	-0.6019E-05	-0.3526E-05	0.2968E-04	0-6406E-06
105	T0 1.	12	0.6671E-0F	-J.18725-J8	-0-4589E-06	-0.6237E-05	-0.5514E-03	0.6855E-06	0.1366E-07
113	10 1	14	0.6320E-10	-C.4319F-J5					
1 1 0 V A	APY PA:	ат [.]				÷			
1	10	7	J.3176E-03	J.4493E 00	0•0	0.9188E-03	0.1769E 00	0.0	0.7844E-03
(f	10	14	0.1211F 00	ರಿ <b>-</b> ೧	<b>0.6462E-03</b>	0.1256E 00	0-0	0.7767E-03	0.8584E 00
15	L'	21 <u>.</u>	0.0	0•6480E-03	0.5122E 00	0.0	0.6709E-03	0.4354E 00	0.0
22	10	28	0.6081E-03	J.3948F 00	0.0	0.5136E-J3	0.4287E 00	0.0	0.7657E-03
53	10	35	0.4053E 00	ر• ی ر	<b>0-6675E-03</b>	0.5025E 00	0.0	0.6171E-03	0.4468E 00
9 ( M		42	Ú. J	-0.1693F-03	-C.5441E-02	0•0	0.0	-0.2306E-05	0.17176-03
		40	-0-54505-02	0.0	0.0	-0.1866E-05	-0.3169E-04	-0.54465-02	0-0
201	0	50	0.0	-0.1145E-05	0.5617E-04	-0-5449E-02	0-0	0-0	-0.1081E-05
57	0	53	-0.81646-04	-0-29435-04	0.0	0.0	-0.1761E-06	0.1320E-03	-0.1817E-04
6 <b>4</b>		70	0°0,	<b>い</b> •0	-0.4125E-06	-0.5328E-04	-0.2829E-04	0.0	0*0
F	۔ ۲	77	-0.5955E-Ju	0.75576-04	-0.2302E-04	0•0	0-0	-0.1089E-05	0.1158E-04
13	Ū	84	-0-54435-02	0.0	0.0	0•0	-0.5355E-06	-0.3220E-04	0.0
35	Ü	16	0.0	0.0	0.6014E-06	0-0	0.0	0.1037E-05	·· 0.1081E-05
92	0	98	-0.2716E-04	0.0	0.0	0•0	-0.1446E-05	0.91336-05	-0.5288E-02
66	10 1	35	0.0	0.0	0.0	-0.1532E-05	<b>0.3866E-05</b>	-0.1895E-02	0.0
106		12	0.0	0.0	-0.1058E-04	0.6585E-05	-0.4299E-02	0.0	0*0
113	TO 1.	14	0.0	-0.7085E-05					

FIGENVECTOP FOR POUT NO.=

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Mode 9. Frequency = 0.5025 Hz,  $\Omega$  = 8 RPM

3027F       00       0.3953f-06         2118E-06       0.3552f-02         3745E-02       -0.5214f       00         4952E       00       -0.1826f-07         9346f-07       0.1832f-08       03         9346f-07       0.1832f-08       03         1889f-09       0.11336f-06       4542f-07         1889f-07       0.3124f-06       6471f-01         1889f-09       0.1130f-06       4542f-07         1530f-08       0.8785f-09       1530f-06         1530f-08       0.4701f-07       1530f-07
3027F 00 2118E-06 4952E 00 4952E 00 3545E-02 3345E-02 1889E-07 1580E-07 3397E-07 3397E-07 1530E-08 1530E-08
0.3745E-02 -0.3745E-01 -0.9223E-08 0.4239E-08 0.4239E-08 0.4239E-08 0.4239E-08 0.4239E-07 0.6380E-07
23305-05 0405-05 6295-07 6295-07 16295-07 16295-07 0 16295-09 0 117975-09 0 117975-09 0 11795-09 0 11795-09 0 10795-09 0 0 10795-09 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания состания соста
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77 77 77 77 77 70 70 70 70 70
-0.11546-03 0.78006-05 0.42385-05 0.3417E-05
0. 3417 0. 3417 0. 3417
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Mode 10. Frequency = 0.5151 Hz,

Ω = 8 RPM

ERENVECTOR FOR FOR MUL- 10

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		7 0.3444E-02 0.9168E 00 0.5251E-C	Z 0.9009F 00 0.7449F-07 0.1786F-C	0 0.4157F-07 0.2416F-02 0.5083E-C	7 0.9913E-03 0.2169E 00 0.1995E-0	3 0.4020F-01 -0.7312E-08 0.9913E-0	0 -0.76576-02 0.7474E-09 -0.7318E-0	9 0.3673E-07 0.1481E-05 0.4470E C	5 -0.4487E 00 -0.7656E-02 0.5526E-C	4 -0.5955E-10 -0.3928E-07 0.9960E-C	7 0.1554E-07 -0.3831E-02 0.6909E-C	2 0.3507E-04 0.3069E-09 0.1385E-(	5 0.5941F-09 0.1609E-07 -0.2901E-C	4 0.1678E-12 -0.2047F-09 0.7041E-1	5 0.8993E-09 0.1004E-09 0.1668E-C	8 0.4081E-10 0.1334E-05 -0.1273E-C	0 0.2617E-05 -0.1606F-02 -0.3802E-0	-		5 0.1753E-04 0.0 -0.1110E-0	5 0.0 -0.5584E-05 -0.1924E-0	-0.6907E-05 -0.2685E-06 0.0	5 -0.2325E-05 0.0 -0.3327E-C	5 0.0 -0.3327E-05 0.3403E-(	0.0 -0.7981E-11 -0.1300E-C	1 -0.8038E-09 0.1470E-10 0.0	0 0.0 0.0 0.4684E-1	0.5617E-11 0.1216F-08 -0.5562E-1	9 0.3253E-11 0.0 0.0	0.0 -0.1291E-10 -0.6594E-(	0.8066E-13 0.7069E-11 0.0	0.0 0.1057F-10 -0.2960E-1	-0.1070E-14 -0.5937E-09 0.1549E-1	3 -0.2844E-09 -0.5938E-13 0.0	9 -0.2043E-12 0.0 0.0
·		00 0.5179E-0	01 0.5796E-U	72 -0.1017E 00	00 0.5597E-0	0.9913E-0	0.9983E 0(	0.5649E-0	07 0.1481E-0	02 0.7814E-04	10 0.3265E-0	0.2414E-0	02 -0.2188E-0	09 -0.3069E-04	04 0.5960E-01	05 -0.3531E-0(	<b>0.6740E-1</b>			-0.7378E-0	04 0.8546E-0	0.0	-0.3327E-0	05 -0.1640E-0	0.0.01	0.7834E-1	0.1503E-1(	0.0	11 0.4980E-0	12 0.0	0.0	0.0 01	0-0	0.2556E-13	14 -0.4991E-09
		2 -0.6736E (	0 0.2837F-(	E 0.1135E-(	2 0.4554E (	0 0.4052E-(	7 0.1482E-(	1 -0.7657F-(	9 -0.3287E-(	7 -0.9186E-(	4 -0.8493E-1	7 0.1299E-(	3 -0.7655E-(	2 -0.2049E-(	3 0.5377E-(	2 -0.1554F-(	5 0.7518E-(	I		5 0.0	-0.1110E-(	5 0.5253E-(	5 0.0	-0.3327E-(	9 0.1468E-1	0-0	1 -0.8114F-(	1 0.0	-0.5831E-1	9 0.8215E-1	0.0	-3.1027E-1	0.0	0.0	-0.5669E-]
sec.)		0-45326-0	-0.5059E D	0-80296-0	0.24155-0	-0.1615E 3	0-8856E-0	-0.1000E 3	0.6633F-0	0-15666-0	0-1040E-0	-0-3513E-0	-0.9101E-0	U.1678E-1.	-0-1961E-0-	-0.5729F-0	0.2675F-0	0.33766-1		-0-3241F-0	0.0	-0.4320E-0	0.2062E-0	0.0	-0-1298F-0	0.0	-0.4524F-1	0.5217F-1	0.0	0-50756-0	0.0	0•0	0.0	0.0	0.0
1.32366943F 01 (rad/		0.72195-07	0.5797E-02	0.11235 90	0.72445-08	0-99135-03	-0.6688E-01	0.1431E-05	-0.7657E-02	0.3733E-U7	n.4053E-02	0.2709E-09	0.1481E-05	0. A558F-04	0.1546E-07	-0 <b>-1</b> 409E-02	-0.1874.5-72	0.1237E-36		-0-9134F-05	0.4678F-00	0.0	-0.6905E-05	0.7681E-05	0.0	0.1512E-10	<b>u</b> • 0	0.113cE-U8	0-0	0.1263E-10	U.1489E-10	0.0	0.1792E-11	0.0	0.0
ر ۲		7	14	21	23	. <b>5</b> € .	42	49	56	. 63	70	11	34	16	98	105	112	114	PART	~.	14	21	2я	35	42	64	56	63	10	17	84	16	94	105	112
NVALUI	PART	10	10	σı	10	.10	. 01 .	10	10	2	C F	10	Ú I	10	10	10	<b>1</b> 0	10	Y NAV I	L)	10	10	J L	10	. 10	10	10	U L	10	10	10	01	01	10	10
FIGE	1E AL	~	æ	15	22	52	36.	£3	50	57	64	11	73	95	92	66	10.0	113	LMAG	-	æ	15	22	29	36	£3	50	57	<b>6</b> 4	11	14	85	61	8.	901

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EIGENVECTOF FOF POOT NO.= 11

Mode 11, Frequency = 0.6881 Hz;  $\Omega = 8RPM$ 

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-	10	7	0.3790F-03	U.9779E-01	0.4139E-01	-0.3194E-03	0.9941E-03	0.1421E-01	0.1335E-03	
œ	10	14	0.5181F-02	-0.11746-01	-0.182 <u>9</u> E-03	0.2641E-02	<b>0.1513E-01</b>	0.5535E-03	0.9997E 00	
15	10	21	0.5456E-01	-0.43855-03	0.46645 00	0.1965E-01	0.1858E-03	0.4103E 00	-0.4571E-01	
22	10	28	-0.2928F-J3	0.3805F CO	0.1264E-01	0.2100F-03	-0.9590E 00	-0.2785E-01	-0.2694E-03	
29	10	35	-0.4435E 00	0.2551F-02	0.1263E-03	-0.3991E 00	0.6560E-01	-0.5577E-04	-0.3866E 00	
36	10	42	0.1009E-01	0.6738E-03	0.3901E-02	-0.3723E-04	0.8558E-07	0.4671E-05	-0.6566E-03	
43	đ	49	0.3889E-02	-0.19046-04	0.65285-07	0.4455E-05	0.3253E-03	0.3893E-02	-0.3127E-04	
50	10	56	0.7714E-07	0.5180F-05	-0.3211E-03	0.3889F-02	-0.2363E-04	0.6054E-07	0.5051E-05	
57	10	63	0.1067E-03	-0.94756-05	0.8456E-35	-0.7606E-07	0.8931E-06	-0.1063E-03	-0.6438E-05	
64	10	10	-0.1992E-05	-0.66265-08	0.8997E-06	0.2467E-04	-0.9876E-05	0.3532E-05	-0.5820E-07	
11	10	11	0.1024E-05	-0.24115-04	-0.8195F-05	-0.9927Ê-06	-0.2161E-07	0.1017E-05	-0.6506E-07	
78	10	84	0.3840E-02	-0.27166-04	0.6348E-07	0.1718E-06	0.6057E-05	-0.7521E-05	0.2933E-04	
85	10	16	-0.9322E-07	0.1663E-11	-0.1118E-05	0.1584E-07	0.1663E-11	-0.1118E-05	-0.6120E-09	
92	10	96	-0.9463E-05	0.72126-06	-0.3802E-07	-0.2746E-07	-0.3967E-06	-0.3933E-07	0.1256E-02	
66	1C	105	0.1255F-04	0.42946-07	0.1278E-06	0.1256E-04	-0.9051E-08	-0.1070f-02	0.1651E-04	
106	10	112	0.1051E-07	-0-31356-07	-0.4886E-05	-0.1655E-07	-0.1266E-02	0.3035F-04	0.2557E-07	
113	10	114	0.11526-09	C.4984E-05						
I SAMJ	VARY	PART	•							
-	10	-	-0.4048E-03	0.4352E-02	0.0	-0.1394E-03	0.1847E-01	0.0	-0.1234E-03	
es S	10	14	-0.1391E-01	0.0	-0.9241E-04	-C.9504E-02	0.0	-0.1612E-02	0.2384E-01	
15	10	21	0.0	-0.77235-03	0.3733F-01	0.0	-0.6739E-03	-0.3345E-01	0.0	
22	10	28	-0.6096E-03	-0.33396-01	0.0	0.1074E-02	-0.2754E-01	0•0	0.4967E-03	
29	10	35	-0.3153E-01	0.0	0.44245-03	0.3017E-01	0.0	0.4329E-03	0.3452E-01	
36	10	42	0.0	0.5512F-04	-0.5119F-04	0.0	0.0	0.1044E-05	-0.79295-05	
43	10	49	-0.5122E-04	0.0	0-0	0.3890E-06	-0.1452E-05	-0.5121E-04	0.0	
50	01	56	0.0	0.2700E-06	0.9733E-05	-0.5122E-04	0.0	0•0	-0.4184E-07	
57	10	63	0.8387E-U5	-0.1656F-06	0.0	0*0	0.5654E-07	0.1217E-04	-0.8711E-07	
. 49	10	.10	0-0	0.0	-0.6804E-07	0.2912E-05	-0.1424E-06	0-0	0.0	
11	01	77	0.7763E-07	0.4851F-05	-0.1066E-06	0-0	0.0	-0.1151E-06	-0.1896E-06	
18	10	84	-0.5121E-04	0.0	0.0	0.0	-0.1996E-06	-0.1645E-06	0.0	
85	10	16	0.0	0.0	-0.8102E-07	0*0	0.0	0.1105E-06	0.2905E-06	
26	10	98	-0.1373E-06	0°0	0.00	0-0	-0.9365E-08	0.1011E-05	-0.79386-05	
<b>g</b> .	10	105	0.0	0.0	0-0	-0.1337E-06	0.1169F-05	0.4408E-05	0.0	
106	10	112	0*0	0.0	0.4069E-07	0.2091E-05	0.1162E-04	0•0	0-0	
113	10	114	0.0	-0.13476-07				•		

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Mode 17, Frequency = 0.7777 Hz,  $\Omega$  = 8 RPM

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FIGE WVECTOR FOR ROOT NO.= 17

EIGEN	VALUE=	0.4386	4740E 01 (rad/s	ec. )						
REAL	PART								•	
-	10	7	-0.3051E-05	-0.2057E-01	0.7159E-01	0.4390E-05	-0.9714E-02	0.1068E-01	-0.1281E-05	
æ	10	14	0.4323E-03	-0.1660E-01	0.2200E-05	0.4263E-01	0.3337E-01	-0.5442E-05	0.5827E-01	
15	Ű F	- 12	0.9727E 00	°.6126E−05	0.4178E-01	0.7425E 00	-0.2405E-05	0.2504F-01	0.9753E 00	
. 22	 61	2 R.	<b>0.3034E-05</b>	-0.44225-01	0.9665E 00	-0.1286E-05	-0.2508E-01	-0.9513E 00	0.1841E-05	
- 53	10	35.	-0.1013E-01	-0.7580E 00	-0.4919E-05	0.49716-02	-0.1000E 01	0.76815-06	0.6786E-01	
36	13	42	-0.9673E 00	-0.7721E-05	-0.4977E-05	-0.2330E-01	0.1331E-04	-0.5256E-07	0.7.608E-05	
43	10	67	-0.4908E-05	-0.1961E-01	0.1442E-J4	-0.5083E-07	-0.3774E-05	-0.4935E-05	-0.2233E-01	
50	10	56	0.1366F-04	-0.5933E-07	0.3761E-05	-0.4908E-05	-0.2065E-01	0.1469F-04	-0.5862E-07	
57	10	63	0.5U41E-06	0.2973E-06	0.1742E-U2	-0.1501F-04	-0.2402E-08	-0.4419E-06	0.1.909E-06	1
<b>9</b>	10	70	-0.4886E-03	-0.1653E-05	-0.1635E-08	0.5453E-06	0.3017E-06	0.7666E-03	-0.11926-04	
11	10	77	C.3229E-08	-0.4676E-06	0.2486E-06	-0.2426E-03	-0.5269E-05	0.2104E-08	0.2311E-08	
75	10	84	-0.4915E-05	-0.2151F-01	0.1444E-04	0.6864E-04	-0.7144E-07	0.2827E-06	0.6004E-02	
85	10	16	-0.1930F-04	0.2087F-11	-0.1968E-08	0.3900E-05	0.2087E-11	-0.1963E-08	0.1175E-09	
56	10	9A	0.2957E-06	C.1620E-03	-0.8636E-05	-0.61505-05	0.1682E-07	0.1730E-08	0.2621E-04	
66	10	105	-0.5316E-U2	U.IC46F-04	0.5577E-04	-0.1393E-06	0.68725-09	0.2635E-04	0.3386E-02	:
106		. 12	<ul> <li>0.2584E-05.</li> </ul>	-0.1466E-04	0.1375E-06	0.1167E-08	0.4792E-04	0.4288E-02	0.6507E-05	
113	10	114	0.1567E-04	0.2053E-09			•			1
19491	VARY PL	1KJ							· · · · · · · · · · · · · · · · · · ·	:
-	10	2	0.1421E-04	0.7183E-04	0.0	-0.82376-05	0.7375E-04	0.0	-0.2963E-04	
er)	۲ņ	14	-0.5061E-05	0.0	-0.1197E-03	0.55176-04	0.0	-0.8615E-04	-0.1499E-04	
15	10	21	0.0	-0.6708E-04	0.2796E-04	0.0	-0.4766E-04	0.8227E-04	0*0	:
22	10	28	0,3234E-04	0.1044E-04	0.0	0.5031E-04	0.3027E-04	0.0	0.2031E-04	
29	10	35	-0.3127E-05	0.0	-0.9985E-05	-0.6754E-04	0.0	-0.1362E-03	-0.21785-05	
35	10	. 42	0•0	-0.1486E-07	-0.7726E-09	0.0	0.0	0.2190E-11	-0.1253E-07	
43	10	49	-0.7950E-09	0.0	0.0	-0.25986-10	-0.1492E-07	-0.7758E-09	0-0	
50	10	56	0.0	-0.2116E-11	-0.1412E-07	-0.1953E-09	0.0	0.0	-0.14446-10	:
. 57	10	63	-0.9122E-08	-0.1257E-09	0.0	0-0	-0.6926E-10	-0.7661E-08	0.1818E-10	
40	10	70	0.0	0.0	0.6125E-10	-0.3118E-08	-0.1048E-09	0-0	0-0	
	10	17	-0-6327E-10	-0.2500E-08	-0.1008E-10	0.0	0-0	0.5002E-10	-0.1468E-07	:
73	10	94	-0.7856E <del>.</del> 09	0.0	0*0	0.0	-0.6005E-11	-0.1052E-09	0*0	
<del>9</del> 5	10.	16	. 0.0	0.0	0.9199E-10	0.0	0.0	-0.7898E-10	-0.1456E-08	
26	10	98	-0.6198E-1C	0.0	0•0	0-0	-0.3113E-11	-0.1507E-07	-0.8907E-10	i
66	10	05	0.0	0.0	0.0	-0.4469E-12	-0.8473E-08	-0.1013E-09	0-0	
106	01	112	0.0	0.0	0.5678E-12	-0.1375E-07	-0.1319E-09	0-0	0.0	
113	10	14	0.0	0.8087E-14		a para na ang ang ang ang ang ang ang ang ang				ļ

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EIGENVECTOR FOR RUCT NO.=

18

Mode 18. Frequency = 0.7911 Hz,  $\Omega$  = 8 RPM

FICEN	VAL UE	н	1254-0	05811E 01 (rad/se	ic.)					
REAL	PART				· \		•			
l	τu	7		-2.15525-35	-0.1275E-01	-0.4999F-01	0.2158E-05	-0.5623E-02	0.7488F-01	-0-6660F-0
80	1 U	14		-0.12225-32	-0.7211E-01	0.1075E-05	0.2016E-01	-0.8530E-01	-0.2733E-05	0.2535E-0
12	Ē,	21		-3+3424E 00	0.3042E-05	0.1690F-01	0.8343E UO	-0.1225E-05	0.1083E-01	-0.2720E 0
22	10	сі а,		0-101001-0	-7.16425-21	0.7499E 00	-C.6684F-06	-0.94945-02	0.1000E 01	0.9067E-D
29	01	35		-0-21848-02	-0.9491E 00	-0.24546-06	0.2927E-02	0.3459E 00	0.3736E-06	0.2654E-0
36	01	42		-0.75335 JO	-6.38885-05	-0.2177E-05	-0.3355E-01	0.2558E-03	-0.26486-07	0-3830F-0
43	10	40		-0-213cE-35.	0.3313E-01	0.2551E-03	-0.2560E-07	-0.1900E-05	-0.2154E-05	-0-1514F-0
50	0	56		C.2555E-03	-0.2988E-07	0.1893E-05	-0.2139E-05	0.1476E-01	0.2554E-03	-0-2950F-0
57	10	63		2.26725-36	0.15685-06	-0.1449E-02	0.1306E-04	-0.11655-08	-0.2376E-06	0-9899F-0
64	10	70		0.5054E-03	0.1272E-05	-0.7938E-09	0.2826E-06	0.1573E-06	-0.5903E-03	0.1072E-0
11	10	17		<b>J.17165-J3</b>	-0.2455E-06	0.1239E-06	0.3471E-03	0.4905E-05	0.11795-08	0+.1170E-0
78	10	34		-3.21435-35	-C.19345-03	0.2555E-03	-0.1483E-06	-0.3596E-07	0.1549E-06	-0.5131E-0
85	10	16		10-350010	0.94845-12	-0.1098E-08	-0.4191E-05	0.9484E-12	-0.10956-08	0-5874E-1
92	10	9 Q		2-15325-36	-0.33315-04	0.8113E-05	0.1005E-05	0.8699E-08	0.8709E-09	0.1352E-0
66	<b>1</b> 3	105		+1+575+E+03	0.19415-03	-0.7423E-07	-0.7009E-07	0.3444E-09	0.1351E-04	-0.1823E-0
106	Ū L	112		0-70056-04	0.3010E-06	0.7008E-07	0.5693E-09	0.2444E-04	-0.22556-03	0.1322E-0
113	2	114		2.72435-37	0.1208E-09					
IDVAL	VARY	PART					•			
	J D	1		1-12221-04	0-28556-04	0-0	-0.2344E-05	0.3425E-04	0•0	-0-1194E-0
en)	Ū I	14		-3.07158-35	0.0	-0.5611E-04	0.2642E-04	0.0	-0.3662E-04	0-3384E-0
15	<b>℃</b>	21			-0.27256-04	0.7264E-05	0-0	-0.2074E-04	0.37135-04	0-0
22	10	28		3+3+3+5-05	0.12695-05	0.0	0.2055E-04	0.46865-05	0-0	0-4722F-0
29	10	35		0-1+365-05	0.0	-0.6345E-05	-0.2848E-04	0.0	-0.57495-04	0-11626-0
36	0	42		0 <b>•</b> 7	-C.75945-08	-0.2923E-09	0.0	0-0	0.1270E-10	-0.6278E-0
<b>\$</b> (	0	64		-2.42465-09	0.0	0.0	-0.2704E-10	-0.8380E-08	-0.2856E-09	0.0
21		56		•	0.71976-11	-0.7963E-08	-0.2827E-09	0.0	0.0	-0.1627E-1
<b>7</b>		63		10+40019+01	-0.4130F-10	0.0	0-0	-0.3693E-10	-0.44445-08	0.4224F-1
* i 0 i		20		0.0	0.0	0.3271E-10	-0.1901E-08	-0.3817E-10	0.0	0.0
21		11	,	-0-37145-10	-0.1587E-08	-0.7643E-11	0-0	0.0	0.3024E-10	-0.8546E-0
E i	-	4. 80	•	-C-2?42E-09	0°0	0.0	0.0	-0.2987E-11	-0.3558E-10	0.0
£ (		16	:.	က • ထ	0-0	0.5116E-10	0-0	0.0	-0.4439E-10	-0.8424E-0
20		5: I 5: I	•	-2*5252-10	0•0	0-0	0*0	-0.1448E-11	-0.8811E-08	0.7717E-1
5	=;	105	• ·		0.0	0.0	-0.2767E-12	-0.4905E-08	0.4666E-10	0.0
51	<u>-</u>	211		0 0 1	0.0	0.6122E-12	-0.8064E-08	0.5920E-10	0.0	0.0
	) ) -	* 1 1	•.		0.85436-14					

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U ---FIGE WECTOR FOR ROWT NO.=

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U.Stafferstersur (rad/sec.)

EIGÉ 4VALUE =

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Ω = 8 RPM Mode 19. Frequency = 0. 9049 Hz,

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•	-0.1271E-06	0.1364E-02	-0.4384E-01	0.1337E-06	0.1669E-03	0.7047E-06	-0.3296E-02	-0.5424E-08	0.2161E-07	-0.3956E-04	0.2103E-09	0.2025E-01	0.1055E-10	0.2727E-05	0.9628E-03	-0.1673E-04	-	•	-0.6584E-07	0.2538E-05	0.0	0.1264E-06	0.2994E-06	-0.2508E-08	0-0	-0.6107E-11	-0.4128E-11	0.0	-0-33386-08	0-0	-0.3115E-09	0.1386E-09	0•0	0.0	
	-0.5878E-01	-0.5134F-06	0.3400E-04	-0.5136E 00	0.4707E-07	-0.4945E-0B	-0.1559E-06	-0.7254E-05	-0.6637E-07	0.2162E-02	0.3987E-09	0.3396E-07	-0.3721E-09	0.1606E-09	0.2665E-05	0.86115-03	. •	-	0.0	-0.1911E-05	-0.1862E-06	0.0	-0.1529E-06	0.5273E-11	0.6227E-10	0-0	-0.1498E-08	0.0	0.1086E-10	0.5048E-12	-0.1377E-10	-0.3416E-08	0.1015E-09	0-0	
	-0.5446E-04	-3.5480E-01	-0.2406E-06	-0.1417E-03	0.1000F 01	-0.7305E-05	-0.3505E-06	-0.4148E-02	-0.2559E-09	0.3351E-07	-0.1640E-04	-0.6621E-08	0.5011E-13	0.1906E-08	0.6304E-10	0.4711E-05			-0.2941E-06	0•0	0.8747E-07	0.2201E-06	0.0	0-0	-0.3223E-08	0•0	-0.9815E-11	-0.5539E-12	0*0	-0.6269E-12	0•0	-0.2369E-12	-0.1841E-08	0.1262E-09	
	0.3353E-06	0.2147E-04	0.5855E-01	-0.1157E-06	0.1669E-03	-0.2771E-02	-0.4718E-08	-0.1534E-06	-0. 5030E-04	0.7570E-07	-0.1160E-02	0.1168F-04	0.1386E-04	-0.4457E-05	-0.1282E-07	0.1133E-09			-0.1222E-06	-0.7474E-07	0.0	0.1261E-06	0.6100E-06	0.0	-0.9853E-11	0.7328E-10	0•0	-0.7301E-09	0.0	0.0	0.0	0.0.0	-0.1778E-13	-0.3165E-08	
·	0.6762E 00	0.1552E-06	C.3416E-03	J.2303E-J1	-0.25746-07	-0.1607E-06	-0.7232E-05	0.3430E-06	0.5396E-02	-0.9112E-10	0.2812E-07	-0.7281E-05	-0.3724E-09	+0.2858E-04	0.9797E-05	0.1343E-07			0-0	-0.7021E-07	0.3873E-06	0.0	-0.1529E-06	0.5380E-10	0-0	-0.3125E-08	0.0	0.8674E-11	-0.2499E-11	0.0	0.1551F-10	. 0.0	. 0-0	0.4405E-12	
	-0.21186-32	-6.9142E 3C	0.5253±-0¢	0.321F5-C4	-0.2090F-01	-0.7206E-06	-f .4669F-92	-0.5530E-0F	· 0.3362E-07	-C.4082E-05	-C.5513E-07	-0.37235-02	0.5011F-13	<b>ċ.l+6l€</b> = <b>ö3</b>	-).1190E-J4	-0.15366-05	0.4485E-10		-0.7440E-05	0.0	-0.5677E-36	6.1713F-06	0.0	-0.268CE-08	0.0	C.3664E-11	0.3350E-11	0.0	-0.65776-09	0•0	<b>c</b> •0	C•0	0.0	C.O	0.5406E-14
	-().3135E-U6	0.1F36E-04	-0.1147E 00	2543E-06	-0.1419E-33	<b>0.1769E-02</b>	-0.15355-96	-J.7295E-05	0-7957E-07	-0.1980E-02	0.6385E-09	-0.1541E-06	-0.6827E-04	0.3341E-07	-0.9361E-03	-0.214EE-04	0.3687E-J5		0.2961F-05	Q.77665-96	<b>6.</b> 0	U.9C03F-07	0.2609E-06	0.0	0.8154E-1C	0.0	-0 <b>.1</b> ¤£5£-08	0.0	-0.1259E-1C	<b>J.6773F-10</b>	0.0	-0-2368F-11	0.0	0.0	0-0
									,	•																									
	7	14	21	67 14		42	540	56	63	· 7.0	17	94	16	96	105	112	114	P AR T	~	14	21	28	5	42	49	56	63	70	17	94 194	16	. <i>8</i> 6	105	112	114
PART	10	10	10	¢;	01	10	10	10	10	1 C	10	10	10	Ċ.		10	10	VARY	C F	10	Ü	10	0	10	10	10	5	Ľ.	0	10	10	10	C L	5	10
REAL	-	er.	15	5	- 62	36	ç	50	57	<b>6</b> 4	11	13	35	92	7 <b>6</b>	L05	113	I SAM I		۴	15	22	29	36	43	50	57	64	11	19	85	92	66	106	113

FIGENVECTOP FOR FOR NO.=

20

Ω = 8 RPM Mode 20. Frequency = 0.9324 Hz,

Rell         Degr         Description         Description <thdescription< th="">         Description         <thdescripti< th=""><th>E I GE NV</th><th>141 UE =</th><th>0.57a5</th><th>4112E 01 (rad/s</th><th>ec.)</th><th></th><th></th><th></th><th></th><th></th></thdescripti<></thdescription<>	E I GE NV	141 UE =	0.57a5	4112E 01 (rad/s	ec.)					
1         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0         0	REAL P	ART	•			#				
5         10         14         0.5555570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.64395570         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700         0.643955700 <th0.672700< th="">         0.643955700         <t< th=""><th><u>نن</u></th><th>TO</th><th>2</th><th>0.9832E-35</th><th>0.1000E 01</th><th>-0.4238E-03</th><th>-0.1304E-04</th><th>0.4972E 00</th><th>0.3067E-02</th><th>0.2489E-04</th></t<></th0.672700<>	<u>نن</u>	TO	2	0.9832E-35	0.1000E 01	-0.4238E-03	-0.1304E-04	0.4972E 00	0.3067E-02	0.2489E-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ac:	Ú.	14	0.3£91E_05	-C.3(54E-01	-0.2201E-34	0.4061E 00	0.5652E-02	-0.1396E-03	-0.6969E 00
27       77       77       0.023475       0.012005-01       -0.12005-01       -0.12005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012005-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.012055-01       -0.01205550       -0.0100550       -0.01205550	1:5: 1	Ú1	21	0.7206F-J2	2.131+E-C3	-0.6146F-01	-0.3295E-02	-0.6191E-04	0.6689E-01	0.3713E-03
27       73       7.5       7.0       7.5       7.0       7.5       -0.23475-01       -0.23456-01       -0.23456-01       -0.23456-01       -0.23466-05       -0.23466-05       -0.23466-05       -0.23466-05       -0.23466-05       -0.23466-05       -0.24446-05       0.13346-01       -0.24446-05       0.13346-01       -0.24446-05       0.13346-01       -0.24446-05       0.13346-05       0.144516-05       0.13346-05       0.144516-05       0.13346-05       0.144516-05       0.13346-05       0.144516-05       0.13346-05       0.144516-05       0.13346-05       0.143516-05       0.144516-05       0.13346105       0.13346105       0.133466-05       0.144516-05       0.144516-05       0.144516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147516-05       0.147	22	10	· 2 R	0.62495-04	J. 671CE-31	-0.2231E-02	0.120GE-03	-0.2345F 00	-0.10065-01	-0.1187E-03
3)     17     42     0.1334F-01     0.1334F-01     0.2334F-03     0.2334F-03     0.2334F-03     0.2334F-03     0.1334FF-01     0.0330FF-04     0.0308FF-04     0.0408FF-04<	29	10	, ъ.	-0.23475 UJ	-357452	<b>J.91515-34</b>	-0.2195E UD	0.2544E-01	-0.8650E-04	-0.2318F 00
6       0.1335F-05       -0.1335F-05       -0.1465F-05       0.1334F-01       -0.05895F-05       -0.1334F-01       -0.05895F-05       -0.1334F-01       0.1134F-01       0.01391F-03       0.01391F-03 </th <th><u>з</u>с</th> <th>1,</th> <th>42</th> <th>-0<b>.</b>34656-02</th> <th></th> <th>0.1333F-01</th> <th>-0.3197F-C4</th> <th>J. 3251E-06</th> <th>-0.1810E-05</th> <th>0.2743E-03</th>	<u>з</u> с	1,	42	-0 <b>.</b> 34656-02		0.1333F-01	-0.3197F-C4	J. 3251E-06	-0.1810E-05	0.2743E-03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	43	1 U	<b>4</b> 0	0.13355-J1	0-5215E-04	0.3225F-06	-0.1637E-05	-0.1469E-03	0.1334E-01	-0.8594E-05
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	50	01	56	0.3239E-36	-0-2201E-05	0.1451E-03	0.1334E-01	0.2901E-04	0.3207E-06	-0.2109E-05
71 $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$ $71$	57	10	63	0.24195-33	0.7219E-04	0.5334E-04	-0.4°50F-06	0.3608E-06	-0.2362E-03	0.4430E-04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	64	UU 1	70	-0.1910E-04	-C.35645-07	0.4301E-06	0.1630E-03	0.6982F-04	0.21666-04	-0.3892E-06
78         70         84 $0.13345-04$ $0.1255E-04$ $0.31345-05$ $0.2396E-05$ $0.1772E-05$ $0.2396E-05$ $0.1772E-05$ $0.2396E-05$ $0.2395E-05$ $0.2395E-05$ $0.2395E-05$ $0.1440E-05$ $0.1440E-05$ $0.1475E-05$ $0.2399E-05$ $0.1440E-05$ $0.1772E-05$ $0.00972E-03$	71	1:0	77	0.1942E-05	+_*1559 <u>5</u> -03	0.573IE-04	-0.1185E-04	-0.1687E-06	0.1839E-05	0:4716E-06
91       0.0.6566F-36       0.1437E-05       0.1430E-07       0.2369F-05       0.1440E-05       0.23697E-05       0.1441E-01         93       10       11       0.10       11       0.10556E-34       0.1575F-04       0.1457E-05       0.1441E-01       0.1155F-04       0.1457E-05       0.1447E-01       0.1155F-04       0.1457E-04       0.1457F-04       0.1155F-04       0.1755F-04       0.1557F-04       0.1755F-04       0.1557F-04       0.1557F-04       0.1557F-04       0.1557F-04       0.1557F-04       0.1755F-04       0.1755FF-04       0.1557F-04       0.1557F-04       0.1557F-04       0.1557FF-04       0.1557FF-04       0.1557FF-04       0.1557	7.8	Ú1	84	0.1334E-C1	C - 1-C 2 F E - 34	0.3210E-06	0.8128E-08	-0.2952E-05	0.7872E-04	0.2024E-03
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8 <del>2</del>	10	16	-0.6000F-06	:.37555-12	-0.1732E-05	0. I.400 E-06	0.3768E-12	-0.1701E-05	0.2390E-07
99         10         105 $0.1266E-3^4$ $0.4631E-96$ $0.4631E-96$ $0.1255E-04$ $0.1755E-04$ $0.4753E-06$ 113         17         112 $0.2153E-37$ $0.3023E-97$ $0.3023E-97$ $0.4755E-04$	- 26	. 01	<b>9</b> 8.	0:57:60E-34	-1573E-05	-0.2899E-06	-0.4839E-07	0-3697E-05	0.3682E-06	0.1441E-01
100         17         112 $0.2796E-10$ $0.2736E-04$ $0.4733E-06$ 11         17         11 $0.2796E-10$ $0.2796E-10$ $0.2796E-10$ $0.4738E-06$ 11         17         7 $0.2796E-10$ $0.2796E-102$ $0.0796E-03$ $0.00$ 11         17         7 $0.1536F-02$ $0.20323E+02$ $0.0796E-03$ $0.00$ 18         10         17 $0.13232F-02$ $0.23232F-02$ $0.0796E-03$ $0.00$ 18         10         14 $0.03232F-02$ $0.23237F-02$ $0.07972F-03$ $0.00$ 222         17         28 $0.03232F-02$ $0.0407F-03$ $0.00$ $0.0446F-03$ $0.00$ 222         17         28 $0.01923F-03$ $0.00$ $0.0323E-04$ $0.4731F-03$ $0.00$ 223         17         28 $0.01923F-03$ $0.00$ $0.0323E-04$ $0.0431F-03$ $0.00$ 239 $0.00$ $0.01925F-04$ $0.0232E-04$ $0.0232E-04$ $0.01312F-04$ $0.01312F-04$ $0.01312F-04$	66	10	105	0.1206E-34	··· 15215-06	0.46315-09	-0.1009E-05	0.1440E-06	0.5160E-02	0.1075E-04
113 $0.2796F-12$ $2226F-74$ $0.2796F-12$ $2226F-74$ $0.2796F-12$ $0.2796F-12$ $0.2793F-02$ $0.2935F-02$ 87017 $0.23232F-72$ $0.56401F-02$ $0.0$ $0.7046E-03$ $0.7032F-03$ 157021 $0.0$ $0.1353F-02$ $0.6675F-03$ $0.06401F-02$ $0.07046E-03$ $0.07016E-03$ 157021 $0.0$ $0.01923F-02$ $0.001923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ 277027 $0.001923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ 277042 $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ 27700.001923F-02 $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ $0.0011923F-02$ 27700.001923F-02 $0.0011923F-02$ $0.0011927F-02$ $0.0011927F-02$ $0.0011927F-02$ 27700.001923F-02 $0.001195F-03$ $0.001195F-03$ $0.001195F-03$ $0.0011926F-04$ $0.0011926F-04$ 287063700.0011237F-05 $0.001195F-03$ $0.0011926F-04$ $0.001107F-04$ 287063700.0011237F-05 $0.0011926F-04$ $0.001107F-04$ $0.00100F-06$ 2970700.0011200F-06 $0.00100F-06$ $0.00100F-06$ $0.00100F-06$ 2970 $0.00100F-06$ $0.001$	100	ن. ۲	11.2	-0.1513E-04	-1.235=5-37	0.3023E-04	0.2639E-06	0.1224E-01	0.1255E-04	0.4753E-08
Refletaky pakt         O. 1535E-02 $0.0$ $0.1535E-02$ $0.0$ $0.0461E-03$ $0.02323E-03$ $0.02332E-03$ $0.02332E-03$ $0.02332E-03$ $0.02332E-03$ $0.02332E-03$ $0.02332E-03$ $0.02526-03$ $0.006E-03$ $0.06774E-04$ $0.07737E-06$ $0.00$ $0.07737E-06$ $0.00$ $0.07737E-06$ $0.00$ $0.07737E-06$ $0.00$ $0.07737E-06$ $0.00$ $0.07771E-06$ $0.00$ $0.07771E-06$ $0.00$ $0.07771E-06$ $0.00$ $0.07771E-06$ $0.00$ $0.077771E-06$ $0.00$ $0.00$ $0.077771E-0$	113	Ú.	114	0.2798E-10	Z.Z6E-34					
I         T $-0.153F-32$ $0.0323F-32$ $0.0323F-32$ $0.0786F-03$ $-0.7802F-03$ $-0.7802F-04$ $-0.7802F-04$ $-0.7802F-04$ $-0.7802F-04$ $-0.6774F-04$ $-0.7876F-06$ $-0.22106F-04$ $-0.2100F-04$ $-0.2100F-04$ $-0$	NIDAMI	IARY P	ART		•				· •	
BT014 $0.323275-32$ $0.56756-03$ $-0.32345-02$ $0.00$ $0.170466-03$ $-0.78026-03$ 15T021 $0.0$ $-0.37355-32$ $-0.47656-03$ $-0.362356-33$ $-0.79026-03$ $-0.00$ 27T028 $0.192557-32$ $-0.476576-03$ $-0.068356-34$ $-0.19146503$ $0.00$ $-0.6714576-03$ $0.00$ 27T028 $0.192557-32$ $-0.476576-37$ $-0.47676-04$ $-0.99116503$ $0.00$ $-0.631356-04$ $0.99516-03$ 28T043T049 $0.079257-32$ $0.00$ $-0.631366-04$ $0.00$ $-0.63135-04$ 36T042 $0.00$ $-0.3166-04$ $0.00$ $0.00$ $-0.63135-04$ $0.001666-05$ 36T043T049 $0.00$ $0.00$ $-0.631366-04$ $0.00$ $0.32066-06$ 36T049 $0.00$ $0.00$ $0.00$ $0.00$ $0.00$ $0.32066-06$ $0.001666-06$ 57T063 $-0.223766-06$ $0.00$ $0.00$ $0.0023966-06$ $0.00$ $0.0023966-06$ 57T063 $-0.223666-06$ $0.00$ $0.0023966-06$ $0.00$ $0.0023966-06$ 57T063 $0.00$ $0.0023966-06$ $0.00$ $0.0023966-06$ $0.0023966-06$ 57T063T070 $0.00$ $0.0023966-06$ $0.0023966-06$ $0.00239666-06$ 57T071T1T1T1T1 $0.000239666-06$ $0.000239666$	-	10 61	7	-0.1539E-32		00	-0.1055E-02	-0.6401E-02	0.0	-0.9293E-03
1510210.0 $-0.4715F-03$ 0.0 $-0.6774F-03$ 0.0 $-0.6774F-03$ 0.0227728 $-0.3753F-3$ $0.0$ $-0.6774F-03$ $0.0$ $-0.6774F-04$ $0.6774F-04$ $0.6774F-04$ 237035 $0.01223F-32$ $0.0$ $-0.6313E-03$ $0.0$ $-0.6313E-03$ $0.0$ 3672 $-0.9116F-03$ $0.0$ $-0.6313F-04$ $0.60313F-04$ $0.60313F-04$ $0.6313F-04$ 3672 $-0.7972F-06$ $0.0$ $0.0$ $0.0$ $0.0326F-04$ $0.6313F-04$ 3677 $-0.2375F-3$ $0.7909F-06$ $0.0$ $0.7937F-06$ $0.0311FF-07$ 5770 $0.0$ $0.7937F-06$ $0.7937F-06$ $0.03111FF-07$ $0.02326F-04$ $0.03111FF-07$ 5770 $0.0$ $0.7937F-06$ $0.03130F-06$ $0.03946E-08$ $0.0$ $0.022326F-04$ $0.03111FF-07$ 5770 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.02336F-06$ $0.03111FF-06$ 5770 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.795F-06$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.795F-06$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.795F-06$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.77396F-06$ $0.0$ $0.0$ $0.0$ $0.0$ 71	æ	10	14	0.3232F-J2		-0°•5675E-03	-C.3234E-02	0.0	0.7046E-03	-0.7802E-03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1.5	1.0	21	0•0		0.8003E-03	0.0	-0.3623E-03	-0.471.5E-03	0.0
291035 $0.1923F-32$ $0.3$ $-0.4767E-04$ $-0.9116F-03$ $0.0$ $-0.4801E-04$ $0.9051E-03$ 367242 $0.0$ $-0.5145F-06$ $0.0$ $-0.5145F-06$ $0.0313E-04$ 3672 $0.0$ $-0.5145F-06$ $0.0$ $0.3206F-06$ $-0.5137E-06$ $0.0$ 5170 $0.0$ $-0.5145F-06$ $0.0$ $0.3206F-06$ $-0.5137F-06$ $0.0$ 5170 $0.0$ $-0.5145F-06$ $0.0$ $0.3206F-06$ $-0.5137F-06$ $0.0$ 5170 $0.0$ $-0.5137F-06$ $0.0$ $0.3206F-06$ $-0.3111E-07$ 5170 $0.0$ $-0.23137F-06$ $0.0$ $0.3206F-06$ $-0.2103F-06$ 5170 $0.0$ $0.1330F-06$ $0.0$ $0.0$ $0.0$ 7170 $0.0$ $0.1336F-06$ $-0.21396F-06$ $0.0$ $0.2109F-06$ 7170 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7170 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $-0.214F-75$ $-5.4275F-75$ $-0.1880F-06$ $0.0$ $0.0$ 7177 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7177 $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ 7171 $0.0$ $0.0$ $0.0$ $0.0$ <td< th=""><th>22</th><th>с. Н</th><th>28</th><th>-0.3753F-03 +</th><th>C.4761E-J3</th><th>0.0</th><th>-0.6836E-34</th><th>-0.1914E-02</th><th>0.0</th><th>-0.6774E-04</th></td<>	22	с. Н	28	-0.3753F-03 +	C.4761E-J3	0.0	-0.6836E-34	-0.1914E-02	0.0	-0.6774E-04
36 $70$ $42$ $0.0$ $-0.5145E-06$ $-0.6313E-06$ $-0.6313E-06$ $43$ $10$ $49$ $0.7937E-06$ $0.0$ $0.3206E-06$ $0.0$ $53$ $10$ $56$ $0.7937E-06$ $0.0$ $0.3226E-06$ $0.0$ $51$ $10$ $56$ $0.7$ $0.7937E-06$ $0.0$ $0.3226E-06$ $0.03111E-07$ $51$ $10$ $56$ $0.7$ $0.7937E-06$ $0.0$ $0.02326E-04$ $0.03111E-07$ $51$ $10$ $56$ $0.0$ $0.0$ $0.0$ $0.02326E-06$ $0.02326E-06$ $0.02070E-06$ $51$ $10$ $63$ $-0.22375E-04$ $0.03946E-08$ $0.0$ $0.0$ $51$ $10$ $63$ $-0.2336E-04$ $0.02326E-06$ $0.02070E-06$ $51$ $10$ $63$ $-0.22375E-06$ $0.0$ $0.0$ $0.0$ $71$ $17$ $10$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $71$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $71$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $71$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $71$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $71$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $10$ $92$ $10$ $92$ $10$ $0.0$ $0.0$ $71$ $92$ $10$ <	29	Ũ	35	0.19235-32	ن• را ن	-0.4767E-04	-0.9116E-03	0.0	-0.4801E-04	0.9051E-03
43T0 $49$ $0.79395-5c$ $0.0$ $0.032065-06$ $0.0$ $50$ $10$ $56$ $0.0$ $0.32265-04$ $0.322065-06$ $0.0$ $51$ $10$ $56$ $0.0$ $0.0$ $0.32265-04$ $0.322665-04$ $0.321115-07$ $51$ $10$ $56$ $0.0$ $0.0$ $0.0$ $0.0$ $0.023265-04$ $0.321115-07$ $51$ $10$ $53$ $-0.23755-5-0$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $51$ $10$ $63$ $-0.23755-5-0$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $-0.21445-75$ $-0.19555-06$ $0.0$ $0.0$ $0.0$ $71$ $17$ $-0.213455-06$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $-0.213455-06$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $0.0$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $9465-06$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $17$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $9465-06$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $9465-06$ $0.0$ $0.0$ $0.0$ $0.0$ $71$ $9465-06$ $0.0$ $0.0$ $0.0$ $71$ $910$ $0.0$ $0.0$ $0.0$ $710$ $92$ $10$ $0.0$ $0.0$ $92$ $10$ $92$ $0.0$ $0.0$ <td< th=""><th>36</th><th>10</th><th>42.</th><th>0.0</th><th>10-0100-04</th><th>0- 7909E-06</th><th>0.0</th><th>0.0</th><th>-0.5145E-06</th><th>-0.6313E-04</th></td<>	36	10	42.	0.0	10-0100-04	0- 7909E-06	0.0	0.0	-0.5145E-06	-0.6313E-04
57       10       56       0.0       0.772E-06       0.7972E-06       0.0       0.3206E-06       0.3206E-06       0.3206E-06       0.3206E-06       0.3206E-06       0.3206E-06       0.3111E-07         57       70       0.0       0.0       0.0       0.0       0.0       0.0       0.01111E-07         57       70       0.0       0.0       0.0       0.0       0.0       0.0       0.0         71       77       0.0144F-7       0.1954E-05       0.01860E-07       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0	1 19 1	. 01	49	0-14446-04	· · · ·	0.0	0.5028E-06	-0.3160E-04	0.7937E-06	0.0
57       70       0.0       -0.1380E-06       -0.2326E-04       -0.3111E-07         64       77       70       0.0       0.0       0.0       0.0         71       77       -0.2144E-12       -0.4195E-05       0.1860E-06       -0.2326E-04       -0.2010E-06       -0.0         71       77       -0.2144E-12       -0.41860E-05       0.0       0.0       0.2100E-06       -0.2010E-06       -0.2010E-06       -0.2010E-06       -0.2010E-06       -0.2010E-06       -0.2010E-06       -0.2010E-06       -0.2139E-06       -0.1517E-05       0.1517E-05       0.10306E-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105116-05       0.0105105       0.0105116-05       0.0105105	21	9	56	Ú•Ú	-C-3274F-26	-0-3130E-04	0.7972E-06	0.0	0.0	0.3206E-06
64       73       71       70       0.0       0.0       0.0         71       71       71       71       0.0       0.2100E-06       -0.2070E-06       -0.2070E-06         71       71       71       71       0.0       0.2100E-06       -0.2070E-06       -0.2070E-06       -0.2070E-06         78       70       84       0.7954E-06       0.0       0.0       0.0       0.2139E-06       -0.1517FE-05         85       70       91       0.0       0.0       0.0       0.0       0.0       -0.2139E-06       -0.1517FE-05         92       70       92       70       92       0.0       0.0       0.0       -0.2139E-06       0.01086E-05         92       70       93       70       0.0       0.0       0.0       0.0       0.01771E-04       0.1086E-05         92       70       98       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0.0       0	75		6.3	-0.2375E-)+	10-31551°C	0.0	0.0	-0.1390E-06	-0.2326E-04	-0.3111E-07
11     17     17     -U.2144F-7c     -C.4223EE-C5     -G.1880E-07     0.0     0.2     0.2100E-06     -O.2070E-06       78     10     84     0.7954E-06     0.0     0.0     -0.2094E-08     0.0       85     10     91     0.0     0.2139E-06     -0.1517fE-09     0.0       92     10     98     0.0     0.0     0.0     -0.2139E-06     -0.1517fE-04       92     10     98     0.0     0.0     0.0     0.0     0.1771E-04     0.1086E-05       92     10     98     0.0     0.0     0.0     0.0     0.0     0.1771E-04     0.1086E-05       92     10     98     0.0     0.0     0.0     0.0     0.1771E-04     0.1086E-05       92     10     98     0.0     0.0     0.0     0.0     0.1771E-04     0.1086E-05       94     10     105     0.0     0.0     0.0     0.1365E-09     0.0     0.0       103     112     0.0     0.1256E-08     0.0     0.0     0.0     0.0       95     10     112     0.0     0.0     0.1365E-04     0.0     0.0       103     112     0.0     0.0     0.2700E-05     0.0     0.0	<b>64</b>		10	0.0	<b>0</b> • 0	0.1351E-06	-0.9402E-05	0.3946E-08	0.0	0.0
10       84       0.7954E-06       0.0       0.0       -0.2085E-08       0.0         85       10       91       0.0       0.1317E-05       0.1517E-05       0.1517E-05       0.1517E-05         85       10       91       0.0       0.0       0.0       0.0       0.0       0.1771E-04       0.1086E-05         92       10       98       -0.7290E-09       0.1771E-04       0.1086E-05       0.0         92       10       105       0.0       0.0       -0.1771E-04       0.1086E-05       0.0         92       10       105       0.0       0.0       0.0       0.0       0.0       0.1771E-04       0.1086E-05         93       10       105       0.0       0.0       0.0       0.0155E-09       0.0       0.0       0.0         94       10       112       0.0       0.2566E-03       0.1365E-04       0.8483E-06       0.0       0.0         103       10       0.0       0.1365E-04       0.8483E-05       0.0       0.0       0.0	11		11	-U-2144E-75		-0.19606-07	0.0	0.0	0.2100E-06	-0.2070E-04
85 T0       91       0.0       -0.2139E-06       -0.1517E-05         92 T0       98       -0.7290E-09       -0.1771E-04       0.1086E-05         92 T0       98       -0.7290E-09       -0.1771E-04       0.1086E-05         94 T0       105       0.0       -0.1780E-05       0.0       0.1086E-05         94 T0       105       0.0       0.0       -0.1780E-05       0.0         94 T0       105       0.0       0.0       -0.1780E-05       0.0         94 T0       105       0.0       0.0       -0.1780E-05       0.0         105 T0       112       0.0       0.0       0.1365E-04       0.8483E-06       0.0         105 T0       114       0.0       0.1994E-08       0.0       0.0       0.0       0.0	18		84	0.7954E-06	C • C	0.0	00	-0.2094E-08	-0.2085E-08	0-0
92 T0 98 -0.1771E-04 0.1086E-05 94 T0 T05 0.0 0.0 2.2 0.0 0.0 -0.1760E-05 0.2700E-06 0.0 105 T0 112 0.0 0.0 0.0 0.0 0.0 0.1365E-04 0.8483E-06 0.0 0.0 113 T0 114 0.0 0.1994E-08 0.2260E-08 -0.1365E-04 0.8483E-06 0.0	82		16	0.0		0.2184E-06	0.0	0.0	-0.21395-06	-0.1517E-05
95 10 105 0.0 0.0 0.0 0.0 0.0 0.0 1059E-09 -0.7780E-05 0.2700E-06 0.0 105 10 112 0.0 0.0 0.0 0.0 0.0 11365E-04 0.8483E-06 0.0 0.0 0.0 113 10 114 0.0	. 92		. 86	-0. F664E-JE	•	0.0	0•0	-0.7290E-09	-0.1771E-04	0.1086E-05
105 10 112 0.0 0.0 0.0 0.0 0.0 0.2260E-03 -0.1365E-04 0.8483E-06 0.0 0.0 0.0	56		105	0.0	с, •	0•0	-0.1059E-09	-0.7780E-05	0.2700E-06	0-0
113 11 114 0.0 C.1990E-08	105	2	112	0.0		0.2260F-03	-0.1365E-04	0.8483E-06	0.0	0-0
	· 113		114	0.0	C.IS905-08			:		

Mode 28. Frequency = 1.0454 Hz.  $\Omega = 8 \text{ RPM}$ 

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ElGenteCTDP TECH EUCT NO.= 28

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EIGE**VALUE= 0.65686035F 01 (rad/sec.)

	10	7	C. LCCLC C		CC LOCEF C				
		•	20-42648-0	-0.9999F UU		-0.8337E-UZ	-0.9985E 00	-0.9345E-01	0.3900E-(
5 Å Å Å	10	14.	0.9992F 00	-0.1573F 00	-0.4001E-02	-0.9986E 00	-0.1139E 00	0.1246E-01	0.9446E (
61 17 4 N 17 4	10	21	0.1758E 00	-0.1206F-01	0.9439E 00	0.9259E-01	0.5845E-02	0.9437E 00	0.1538E (
22	C. ₩	25	-0 <b>.</b> 5834E-U2	D.9434E 00	0.1165E 00	0.4357E-02	0.3332E 00	0.1107E 00	-0.4393E-(
	1.) _	35	6.3313E JO	C.9112F-01	0.1335E-02	0.3327E 00	0.1063E 20	-0.2054E-02	0.3322E (
5	T.	42	0.95UZE-J1	0.16URF-01	0.5995E-01	-0.8816E-C3	C.814JE-06	0.1143E-03	-0.1547E-(
4	ن 1	07.	U.6004E-01	-0.695rE-03	0.7163E-06	0.1659F-03	0.7641E-02	0.6001E-01	-0.8241E-
5	10	56	0.76685-06	0.1231E-03	-0.7530E-02	0.6004E-01	-0.7456E-03	0.6421E-06	0.1190E-C
57	, U	63	0.7451E-04	-0.1532E-03	0.1517E-03	-0.1313E-05	0.5893E-05	-0.3386E-03	-0.1051E-(
<b>P i</b>	10	70	-0.3022E-04	-0.1259E-06	0.2574E-05	-0.2879E-03	-0.1582E-03	0.6560E-04	-0.1005E-(
11	1C	11	0.5101F-06	-0-4406 -04	-0.1366E-03	-0.1213E-04	-0.3876E-06	0.5312E-05	-0.8254E-(
15	10	34	P. 5002E-01	-0.7822E-03	0.6553E-06	0.4789E-05	0.1411E-03	-0.1363E-03	0.4883E-(
62	י. רי	10	-0.1401E-05	0.2591F-16	-0.3414E-05	0.2532E-06	0.2991E-10	-0.3423E-05	-0.4282E-(
62	10	9 R	-0.1621E-03	0.1796F-04	-0.6479E-06	-0.6942E-06	-0.9123E-05	-0.6507E-06	0.8500E-0
96	- 01	105	0.3211F-03	0.4657F-06	0.3535E-05	0.1846E-03	-0.2585E-06	-0.14405-01	0.4353E-(
105	10	112	0.24295-06	-0-21846-05	-0.5643E-04	-0.4754E-C6	-0.1683E-01	0.8098E-03	0.3343E-(
113		114	0.1775E-08	0.3638E-04				•	
1 2 2 2 1 1 1	AXY PI	4R T							
	11	. <b>L</b>	U.6149E-03	-0.1037E-01	0.0	U.6106E-03	0.1036E-01	. 0.0	0.6814E-(
er:	10	14	-0.5331F-02	0.0	0.6916F-03	0.5567E-02	0.0	-0.2183E-02	0-7496E-C
12	CL	21	0.0	-0.2177F-02	-0.71896-02	0.0	-0.2088E-02	0.3881E-02	. 0-0
22	10	2 B	-0.2087E-02	-0.3723E-02	0-0	-0.7716E-03	0.7784E-02	0.0	-0.7678E-(
56	11	35	-ú <b>.</b> 7472£-02	0°0	-0.7384E-03	0.4659E-02	0.0	-0.7370E-03	-0.4460E-(
36	10	. 24	0.0	-0.1578F-03	-0.4844E-05	0-0	0.0	-0.1745E-05	-0.1527E-(
43	10	64	-0.5415F-05	0.0	0.0	0.16735-05	-0.4788E-04	-0.5016E-05	0-0
20	C) F	50	0.0	-0.1092F-05	-0.4692E-04	-0.5241E-05	0.0	0.0	0.1062E-(
57	1C		0.5254F-06	-0.2816E-07	0•0	0.0	-0.9625E-08	-0.1407E-07	-0.4528E-(
64	10	70	0.0	0.0	0.1392E-07	0.1032E-05	-0.1939E-07	0.0	0-0
2	2		0.1372E-08	0.3970E-06	-0.2940E-07	0.0	0.0	0.3713E-08	-0-1184E-0
18	e F	84	-0.5123E-J5	0.0	. 0.0	0.0	-0.5227E-08	-0.1620E-07	0•0
85	L L	16	0.0	0.0	0.1500E-08	0.0	0.0	-0.7123E-08	0.7657E-(
62	Ū	<b>4</b> 3	-0.1641E-07	0*0	0.0	0-0	-0.7535E-09	-0.3269E-06	-0.3253E-(
06		105	0.0	0.0	0.0	-0.4790E-08	0.4604E-05	-0.2298E-05	0•0
105	TO 1	112	0.0	0.0	-0.9266E-08	0.7475E-05	-0.3136E-05	0-0	0-0
113	- -	114	0.0	0.6712E-09					

A-119

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 $\Omega = 8 \text{ RPM}$ Mode 32, Frequency = 3.8441 Hz,

FIGENVECTOR FOR ANT NO.E

1.24155520# 02 (rad/sec.) E16F VVAL UE =

14.20	1 2 4 0							
<b>;</b>	61	۱. •	-3-44035-31	-0.6128E-01	0.81135-03	-0-30465-01	-0-6769F-01	0.8130F-03
en	C L	+	-2.2329E-71	0.8117E-03	-0.4440E-02	-0.2339E-01	0.8125E-03	-0.3207F-01
15	C L	12	C-33059-C	-0.676CF-02	-0.5665E-01	9.6497E-03	-0.8844E-02	-0.1929E-01
, <b>7</b> . 1	L.		いし - コニニレビー・	- 7.1952F-J1	0.5c30F-C3	-0.1629E 00	-0.6432E-01	0.87785-03
24	0 <b>I</b>		【つーヨシャシャン・	U. a 796F-U3	-0-44046-01	-0.21215-01	0.8793E-03	-0.5150E-01
36	C L	4.2	0°916203	-0.43636-01	-0.7780F-01	-0.3755E-04	0.1540E-06	-0.3976E-03
4	10	U-4	- 7.2 7 3 2 E - J 1	-0.1553F-04	0.8387E-07	0.1998£-03	-0.1736E-01	-0.2782E-01
50	C' H	j.	<b>12225-0</b> 5	-0.2962E-03	-0.2472E-02	-0.2782E-01	-0.2053E-04	0.3616E-07
57	C: ►	53	3334E+01	0.2182E-02	0.1043E-34	-0.5054F-08	-0.2390E-03	-0:4282F-01
44	Ċ.	10	C.1332E-04	-0.1072E-07	0.2769E-03	-0.1018E-01	0.1882E-02	0.9529E-05
11	¢.			-0.15265-01	U.15325-02	U.1U27F-04	0.8861E-08	0.3919E-03
79	1.	י. מי י	-3-27925-01	-0.2210E-04	0.4713E-07	0.1354E-05	-0.1315E-03	+0.2189E-02
85	12 12 12	5 L L		0.34535-09	0.3292E-03	-0.59556-07	0.3453F-09	-0,4058E-03
26	TO,	50.	C.16375-02	U.9667E-35	0.9227E-08	-0.4207E-06	0.4638E-04	-0.3168E-02
60	10	105	C + 25038+03	5.1126F-07	U.5228E-U6	-0.5123E-04	-0.1314E-02	0.5399E-02
105	€) ₩	211	2+23256+17	-0.6715E-06	-0.14795-04	-0.21895-02	0.4987E-03	0.2695E-03
113	C F	114	1.14991.0	-0-5858F-06				-
150-1	144X	7 FA C						
-	C) H	۲.	3, 9990F 00	U.4347E-01	0.0	-0.9989E 00	0.4249E-01	0.0
æ	r. H	14	. :.1495E-D1	C•D	-0.3529F 00	0.1460E-01	. 0-0	~0.8360E 00
15	с, Г	•••	() • •	+C.8359E 00	0.3724E-01	0.0	-0.3012E 00	0.1371E-01
22	C/ ₩		-3-3034E UD	0.1293F-01	0.0	-0.9371E 00	0.3934E-01	0.0
62		10 17	0-3404E-01	0.0	-0.3260E 0C	0.1365E-01	0.0	-0.3259E 00
36	10 1	t 1	0.0	-0.4865E 00	0.4743E-03	0.0	0-0	-0.4853E-02
43		4	C.4295E-03	0.0	0-0	0.4862E-02	-0.1818E 00	0.4516E-03
л С	() ••	55	0.0	-0.2991E-02	-0.1821E 00	0.4398E-03	0.0	0.0
57	10	er: vCi	-0.57405 JO	-0.1916E-03	0.0	0-0	-0.4507E-02	-0.6741E 00
40	ر، ۲	- 1-	0-0	0.0	0.4509E-02	-0.2284E 00	-0.1490E-03	0.0
11	¢.	77	• -0.6234E-02	-0.2283F 0C	-0.1055F-03	. 0•0	0•0	0.6234E-02
18	Ļ	1. 1.	3.4441E-03	0.0	0.0	0-0	0.1523E-05	-0.2849E-03
ġ5	F	l o	0-0	0.0	0.6493E-02	0-0	0.0	-0.6494E-02
92	C) H	5 C	-0.1139E-03	0.0	0-0	0.0	-0.1322E-05	-0.6608E-01
99	Ľ,	1 J 5	0.0	0.0	0.0	-0.6195E-05	-0.2914E-01	0.1768E-02
106		112	0.0	0.0	0.7764E-05	-0.4770E-01	0.2376E-02	0.0
113	с. Н	1,1 4	C*L	-0.7634E-07				

0.8840E-03 -0.1626E 00 -0.2183E-01 -0.1335E-01 -0.2729E-04 0.5680E-04 0.1402E-02 -0.7911E-08

-0.1015E-01 -0.5601E-01 -0.4282E-02 0.1275E-05 -0.5375E-03 -0.3802E-03 0.2413E-03 0.2413E-03

-0.1048E-01 0.1895E-02

0.0

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-0.3534E 00 0.3890E-01 0.0 -0.9382E 00 0.1353E-01 -0.4874E 00 0.0 0.2998E-02 -0.9478E-04 0.0

Mode 1, frequency = 0.1787 Hz, Q = 12 HPM

ELGENVECTUR FOR BOT NO.=

0.11227112F 01 (rad/sec)

€13€ 4VALUF=

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0.78066-07 0.10036-07 -0.4481E 00 -0.32206-03 -0.32206-03 -0.32266-03 -0.73166-03 0.56616-09 0.56616-08 0.3295-04	0.1409E-09 -0.5141E-02 0.7195E-11 0.1298E-05 -0.1258E-03 0.2247E-02	-0.2253E-05 0.2899E-05 0.0 0.23260E-06 0.13250E-06 0.1377E-05 -0.4200E-08	0.2444F-10 0.23767E-11 0.0 0.0 0.0 -0.1013E-10 0.0 0.0
(10,9604E 00 0.1193E-06 0.1193E-06 0.1080E-02 0.1080E-02 0.183E-07 0.1427E-07 0.1427E-07 0.1427E-07 0.1427E-07 0.7548E-07	0.3006E-09 0.1578E-07 -0.2121E-09 0.1017E-09 0.1277E-09 0.1281F-03	0.0 -0.1758E-06 0.1448E-05 0.1448E-05 0.1270E-05 -0.1270E-00 -0.1259E-10	0.0 0.12326-08 0.0 0.11786-10 0.11786-10 -0.26516-11 -0.10726-10 -0.11256-10 0.0
0.13816-02 0.43136 0.43136 0.44096-07 0.44096-07 -0.17596-07 0.36196-02 0.36196-07 0.1526196-07 0.1526196-07 0.1526196-07 0.1526196-07	0.72496-05 0.61606-09 0.61606-09 0.187016-09 0.41616-10 0.41616-10 0.25166-09 0.25166-09	0.8679E-06 U.0 -0.1609E-05 -0.2560E-05 0.0 0.0 0.0 0.0 0.0	0.0 -0.6128f-11 -0.625f-12 0.0 0.0 -0.1284f-12 -0.103f-12 -0.3578f-09 -0.6659f-11
-(.2594E-07 6.15154-07 0.9997E 00 0.72655-07 0.9247E-03 0.52575-03 0.1428E-05 0.14456-03 0.14456-05 0.14456-05 0.14456-05 0.32355-05	C.5123E-03 0.4556F-06 -0.4556F-06 -0.48842F-05 -0.3353E-08 0.6821E-10	-0.9709E-06 u.774E-06 u.0 3249E-06 0.0 3249E-05 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0	-J.1759F-10 0.C -0.5628E-J9 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.
-0.4596.00 -0.68454-08 0.10036-02 0.44346 00 0.50596-07 0.14256-07 0.14256-07 0.14258-02 0.34361-07	0.1264F-U7 0.4491E-02 -0.2022E-04 0.1124E-04 0.7226F-08 0.7226F-08	0.0 -0.2253E-05 0.4584E-00 0.0 0.0 -0.1269E-10 -0.1269E-10 0.0	-0.18371-08 0.0 0.5932E-11 -0.2996E-11 -0.0 0.1107E-10 0.0 0.0 0.1161F-13
0.13815-02 -0.42%65 00 -0.47825-07 0.10905-07 0.30495 00 0.844805-07 0.4895-07 0.4955-09 0.4955-09 0.21025-09	-0.75116-03 -0.75116-03 -0.30446-04 -0.30446-04 -0.30446-04 -0.30446-04 -0.30446-12 0.35646-11	0.3650F-05 C.0 -C.7756F-06 -C.7756F-06 -C.3795F-06 -C.4354F-06 -C.0 C.0	-0.25355-12 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.
3.12505-00 0.15155-02 -0.1005-01 -0.1755-07 -0.1755-03 0.14735-00 0.14735-00 0.44315-02 0.44315-02 0.44315-02 0.44315-02	0.7753F-09 0.1426F-05 0.1426F-04 0.1500F-07 0.1500F-07 0.11234E-03 0.11234E-03	-0.9711F-06 U.1967E-05 U.1967F-05 U.0 -0.1499E-05 U.0 -0.1499E-05 U.0	0.0 0.1273+-05 0.0 0.1216E-10 0.1702E-10 0.0 0.0 0.0 0.0
- 4 - 5 5 4 4 5 9 F	77 84 91 93 93 11 23 11 24 11 24 11 24 11 24 11 24 11 24 11 24 11 24 24 11 24 24 24 24 24 24 24 24 24 24 24 24 24	- 4 - 18 5 7 5 - 4 - 7 8 - 7 7 8 - 7 7 8 - 7 7 7 - 7 7	2201466211 2201466211
57 M. 9201 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.277 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.207 1.20	71 78 78 95 70 95 70 95 70 95 10 11 11 11 11 11 10 11 11 11 10 11 11	1 19 15 10 15 10 22 19 36 10 43 10	22 22 23 24 25 25 25 25 25 25 25 25 25 25 25 25 25

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106	VAL UF	- 0.1	12424011E 01 ( <b>rad/s</b>	ec)		ي هـ. ۱	:		
N H N	PART			٩,					
-	C I	•	C-2325E-39	0.2559F-75	-:.5036F 32	-).5372E-10	0.2559F-05	-0.6463E 00	0.15806-09
n ı		14	er-11246.			J. 2764 5	-J.6J31E 3C	0-22456-09	0.18666-05
15	10	21	. <u>-</u> ,55i J∂	)1-3181c*u-	ldof-~:	00 04010-00	0.1259F-09	0.2447E-05	-0.7372E 00
22	10	٤2.	-3*3600E-10	C.14Ari-05	-[.6214F	0-13155-09	-3.5922E-06	-0.28436 00	-0.6192E-10
52	10	35	-0.5923t-06	-0.3590E 0C	<b>7.11046</b> -35	0.47055-35	-0.3046E 00	-0.4056E-10	0.1532E-05
36	C F	42	-0.3331E 00	0-1050F-04	1.2604E-05	-0.7836E JO	-0.9276E-03	0.13206-11	-0.14496-09
4	10	04	C.261JE-JS	-0.1000E 01		J.1034F-11	0.7254E-10	0.2608F-08	-0.8432F 00
5	10	55	-J.8279E-J3	0.1255£-11	-[.5836E+1]	0.261JE-06	-0.9402E 00	-0.8300£-03	0.1121E-11
57	10	63	5.6740E-1C	0.2754F-10	-:*****	0.15486-34	-J.1012E-12	-0.7009E-10	0.1755E-10
99	10	70	-0.1965E-32	C.73825-05	-:-1363E-1:	0.5s26f-10	0.2724E-10	-0.3803E-02	0.1460E-04
	. 10	11	<b>3.5016F-12</b>	-0.61706-10	:-2280E-1.	-1.2503E-02	· 0.7872E-05	0.55116-12	0.2507E-12
79	Ļ	<b>6</b> 4	0.2609E-08	-0.3917E 30	- :. 2238E-33	0.1239E-32	0.1231E-11	0.2837F-10	-0.8791E-02
<b>3</b> 5	5	16	U.1637E-04	0.319PE-15	-:.3731E-17	J.8691E-05	0.3198E-15	-0.3729F-12	0.1279E-13
55	10	66	0.1-3005-10	-0.3039°-02	:.1102E-:-	J.1232E-03	0.1562E-11	0.18126-12	0.2867E-08
60	10	105	-0.50465 00	-0.6194F-U3	.1178E	-3.55005-11	G.7403E-13	0.2282E-09	-0.1019E 00
<u>ا</u> و	J L	112	66-31991.4	0.63436-05	: 1296E-1:	0.12166-12	0.4495E-08	-0.3091E 00	-0.4090E-03
113	10	114	5-9526-03	C.6409E-14					
19461	Y A A V I	P A P T							
	с <del>г</del>	٢	-0 <b>-1601E-</b> 00	<b>J.7330F-J</b> 8	() ()	-0.1807E-38	0.1533E-08	0.0	-0-14646-07
<b>6</b> 0	21	14	G-5386E-08	C•0	-2-44515-06	J.1436E-J8	0.0	-0.1481E-08	0-6223E-08
5.	0	21	C•:	5C-30921+0-	-1601F-	C.J	-0.9837E-08	0.3805E-08	0.0
22	17	23	-C.3201E-09	0.7201F-35	0•:	J.9251E-J9	-J.5701E-08	0.0	0.9254E-09
57	10	35	0.3582F-04	0.0	-1528F-17	<b>J.9454E-J</b> 5	0-0	-0.2414E-08	0.2956E-08
36.	01	42	0.0	-0.9219t-11	-2.7695E-13	0.0	0.0	-0.8315E-13	-0.8905E-11
ç	Ū1	4 3	-C.403EF-13	0.0	, , ,	<b>J.7673E-1</b> 3	-0.3935E-11	-0.3644E-13	0.0
ŝ	د •	· 5 o	c•0	-0.53955-13	-1.38756-11	-J.3981E-13	0.0	0.0	0.5204F-13
52	1	63	-0.27735-11	<b>J.7637E-15</b>	0 <b>•</b>	0.0	-0.1337E-13	-0.26896-11	-0.7985E-14
\$9	5	70	0.0	0.0	5.12976-13	-0.1223E-11	-0.1190E-14	0.0	0-0
1	ن 1	77	-0.2¢56E-13	-0.11946-11	-[6336E-1.	C.0	0.0	0.2578E-13	-0.2124E-11
78	10	84	-0.37485-13	~ 0•0	0-0.	0-0	-0.2760E-15	-0.5672E-14	0-0
8	Ē	16	0-0	• • ٥	2.2412E-13	0.0	0-0	-0.2342E-13	-0.1535E-12
26	5	96	-0.3939E-14	0.0	0.5	0.0	-0.2142E-15	-0.1666E-11	-0.2132E-13
66	5	105	0.0	0.0	0	0.4423F-17	-0.7653E-12	-0.2331E-13	0.0
901	21	112	0.0	0.0	2.24/19E-1c	-0.1321E-11	-0.1381E-13	0.0	0-0
Ê	<u>.</u>	114	0.0	0.5898F-22	;		:		.,

Mode 2. frequency = 0.1977 Hz,  $\Omega = 12 \text{ RPM}$ 

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~ ELGENVECTOF FOR ROOT VD.=

CIGENVECTOP FOR ROUT NO.#

3 Mode 3, frequency = 0.3185, **Q = 12 RPM** 

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E CC	NALUI	β	n.2005	047664 01 (rad/	sec)	्य				
PEAL	PART				•	ì			Ķ	
7	10	~		0.5659E-J3	-0.24145 00	0.12296-01	0.1406E-03	-0.89886-01	0.1173E-02	-0.2207E-03
7	τC	14		-0.4207E 30	23-346-2.	C.1013F-02	-0.3423F 00	0.4517E-02	0.4041F-03	-0.5950F 00
15	10	21		C = 36 5 2 5 - 35	20-31002*1	-0.4574F 30	- 3.10705-02	-0.38756-04	-0.9983F 00	U.5896E-02
22	£	. 28	۔ ۰۰	· ¿C-3646.u	-0.7658F. UC	0.20985-02	0.5171F-03	-0.6886E 00	-J.6687E-02	0.1698E-03
57	а <b>г</b> .	35		-u-5325f 0.0	0.63756-03	-0.2247F-33	-0.3633E 00	0.4242E-01	0.7693E-03	-0.7117E 00
36	6	42		n.1528E-02	-J.4715E-04	0.4562F-02	-0.8103E-05	0.1384E-06	0.4205E-06	0-3446-04
ŧ	01	53		0.4566F-U2	6-26955-04	0.1365E~36	U.3099E-06	-0.5524E-04	0.4560E-02	0.17995-05
50	ر 1	50		0.1356 - 76	-0.5624F-06	-0.4280F-04	0.4563E-02	0.17256-04	0.1318E-06	-0.4819E-06
57	10	63		U. 8374F-04	0.2204F-04	-0.1227E-06	-0.3849E-08	0.4899E-06	-0.8500E-04	0.1380E-04
94	C I .	70		-0.23146-06	0.35455-09	0.4261E-06	0.3796E-04	0.22466-04	-0.3544E-06	-0.1656E-08
17	10	17		0.5475E-06	-0213f-04	0.1731E-04	-0.2977E-06	0.1106E-08	0.5789F-06	-0.5150E-05
18	01	84		0.4562F-32	G.9633E-U5	0.1312F-06	-0.7495E-07	-0.1080E-05	0.2407E-04	0-63895-06
·58	10	6		-0.2865E-36	J.8567E-12	-0.7716E-06	0.1027E-08	0.8560E-12	-0.7482E-06	-0.5060E-06
56	10	99		0.2121E-J+	-0.362ui-06	0.8674F-09	0.1412F-07	0.1140E-05	-0.3944E-05	0.4915E-02
66	1	105		-1)* 7544[-15	2.44845-07	-0.5534F-07	-0.6166E-06	-0.2062E-05	0.1940E-02	-0.8612E-05
106	C F	112		0.3195F-J7	0.40655-07	0.11J0F-04	-0.30256-05	0.4340E-02	-0.1524E-04	0.6211F-07
Ξ	ТC	114		C-44475-33	0.0270E-05					
DAU I	INARY	P AK I				•				
-	51	~		0.2244F-32	0°-99361-01	0.0	0.1645E-02	-0.3293E-01	0.0	0.2024E-02
¢.	Ľ1	14		-0.9746E-J1	<b>0</b> •0	0.2644E-02	U.2208F 00	0.0	0.1981E-02	0.1056E 00
15	01	21	¢	0.0	j.1524E-02	0.6061E-01	0.0	0.2191F-02	0.5837E-01	0*0
22	10	23		0.2375F-32	0.2674F 00	0.0	0.20666-02	0.1502F 00	0.0	0.1606E-02
52	С Г	35		0.7900E-01	0°0	0.1054E-02	-0.7433E-01	0.0	0.2172E-02	0.2625E 00
Jó	01	40		0.0	-0. IS J4F-74	-0.1798E-02	0.0	0.0	0.4417E-05	-0.2335E-04
. 63	Ú F	49		-0.17996-02		0.0	0.56795-06	-0.3175E-04	-0.17986-02	0.0
5	10	9 <b>5</b> .	•	6.0	-0.18996-06	0.4110E-05	-0.17985-02	0.0	0.0	0.8095E-08
· 51	C.	:63		-C.1305E-04	-0.5767E-05	0°0	0.0	0.35066-06	0.3405E-05	-0.6075E-05
\$9	01	70		0.0	<b>ن.</b>	0.30206-06	-0.2877F-04	-0.10646-04	0.0	0-0
11	10	11		-0.1303E-76	0-1-24 E-04	-0.7026E-05	0.0	0•0	-0.6143E-07	-0.9592E-05
78	61	<b>Р4</b>		-0.174EE-02	, C.(	0-0	. 0.0 ^U	-0.42576-06	-0.1050F-04	0*0
85	10	16		0.0	C•0	-0.9326E-07	0.0	0.0	-0.1297E-06	-0-344E-06
56	10	98		-0.9399F-J5	0.0	0.0	0-0	-0.5269E-06	-0.7058E-05	-0.1618E-02
56	10	105		0.0	0.0	0.0	-0.1006E-05	-0.3822E-05	-0.5135E-03	0.0
106	01	112		0.0	ú•0	-0.2871E-05	-0.5523F-05	-0.1212E-02	0.0	0.0
113	10	114		0.0	-0.2305E-05		•			

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Mode 9, frequency = 0.5025 Hz, Ω = 12 RPM

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EIGENVECTOR FOR KOT 10.

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		0.3528E-04	0.11926-01	-0.1000E D1	-0.1787E-05	-0.78945-02	0.47685-06	-0.9030E-01	-0.38766-08	0.Z168E-07	0.4676E-05	-0.2011E-11	-0.2986E-02	-0.3526E-11	0.3470E-05	-0.1815E-01	0-1541E-04			0.1418E-04	-0.11456-01	0*0	0.6992E-05	0.2534E-02	0.4005E-08	0-0	-0.3377E-10	0.6168E-09	0*0	-0.21685-08	0-0	-0.1541E-09	0.4526E-08	0.0	0.0	
	,	-0.1352E 00	-0.32696-04	0.3855E-02	-0.5214F 00	0.1238E-04	-0.2201F-08	0.8504E-06	0.3124E-04	-0.4381E-07	-0.7857E-03	0.8942E-10	0.34435-07	-0.2809E-09	0.1807E-10	0.3180E-05	-0.4733F-01			0.0	-0.3377E-04	0.1090E-01	0.0	0.3889E-04	-0.5127E-10	-0.5416E-08	0.0	0.1656E-08	0.0	-0.1584E-10	-0.6571E-11	0.1983E-10	-0.2050E-08	0.5547E-08	0-0	
		0.29326-02	0.3J27E 60	J.2527F-04	-0.1215E-02	-0.4952E 00	0.2597F-04	-0.2300£-06	~0.8671E-01	0.116IE-10	0.3369E-07	0.3397E-05	-0.5570£-09	0.5055E-12	0.1835E-08	0.5130E-11	0.5379F-05			-0.1630f-01	0.0	0.13416-04	0.1260F-02	0.0	0.0	-0.4505E-08	0.0	0.1400E-10	-0.9325E-09	0.0	-0.2863E-10	0.0	0.10896-11	-0.90346-09	0.1108E-07	
		-:.34716-34	0.2433F-v1	-u.2621E 00	0.60685-05	-0.9250E-02	-0.923E-01	-0.2229E-08	U.8532E-06	0.6U14E-U5	U.3F95E-07	-0.3145E-03	0.6380E-U4	-0.3171F-06	0.22356-04	-0.1213E-07	6.1751F-11			0.1617E-05	0.1637E-01	0.0	0.6010F-05	-0.3014E-U2	0.0	-0.8128F-10	-0.5387F-08	0.0	0.21285-09	6.0	4,000	0.0	0.0	-0.4220E-10	-0.1585E-08	
		0. 11463.0	0•4c4aE-04	-0.2522E-03	0.7443E 30	-0.1536E-04	0. P451E-06.	0-30+0f-04	U.27665-06	-0.11696-02	U. 6178F-11	0.28236-07	0-3109E-04	-0.2806E-09	0.4021E-05	0.7870E-04	0.1544E-07			0.0	-0.2443F-04	-0.8954E-02	0.0	0.4543E-04	-0.3931E-08	0.0	-0.7781F-09	0.0	-0.1426E-10	0.8194f-09	. 0.0	-0.1585E-10	0-0	0.0	0.3273E-10	
c)		10-まちる。こ	-0.47449-0-	-0.28495-04	0.11036-01	-0.4642F 00	-C.47985-0c	-0.8450F-01	-0 <b>-</b> 39395-06	0.33875-07	J.2086F-U5	-0.391 HE -07	-0.6555t-01	0.50555-12	-9.53465-03	G.232hE-04	u.10581-03	<b>J.</b> 2682E-10		-0.21121-01	0.0	0.4730E-05	0.8451L-02	Ú.O	-0. EU 79E-08	0.0	-0.46775-10	-0.03771-09	0.0	C.3247E-09	0.0	0.0	0°0	0°0	0.0	- A 34.267 13
5744021 11 (rad/se	-	51,-3°6 - 5° - 18	1:	00 30674°C	7.3512F-04	-1.141.6-02	-0.4803F 00 ·	r.8531F-06	P.2835E-04	G. 4370E-07	-7.1154F-03	~1-41646 v	f51Jf-30	(	3.33546-17	10-34117-01-	0 • 7545E - 75	0.1117E-03		-0.5235E-04	0.20055-01	0°0	-0.14425-34	-0-38795-07	0°1	-0.4632E-08	0.0	0 <b>.1</b> 390F-05	0°C	0.1295F-1C	-0.5410E-08	· 0 · )	0.24986-11	0-0	0.0	c c
16.0	÷	۰.	14	21	2.8	35	ru vt	·. • •	50	63	70	77		16	g e	105	112	114	211	7	1-	12	29	35	42	49	56	63	10	17	44	16	4 F	105	112	
= JN IV:	A 8, T		14	10	C1	10	10	01	11	U I	10	16	10	10	10	1	10	۲	A YAA'	с: Н	۲ ۲	10	10	14	01	10	T ()	10	1C	10.	1.0	10	10	17	10	
VN-DT3	d JA 14		'n	15	22	29	36	64	50	57	<b>64</b>	11	74	35	26	66	106	113	110043		9	15.	22	29	36	£3	05	57	<b>4</b> 3	5	79	85	32	66	106	

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FIGENVECTOP FÖR ROOT NC.= 10

Mode 10, frequency = 0.5151 Hz,  $\Omega$  = 12 RPM **ئ**ر ب .

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(rad/sec)	
сı	
0 • 32 366943E	
E 1964VALUE=	

E 1964	v∆l∪£=		0.3236	6943E Cl (rad/e	sec)			 		
N 3 d	PART									
-	10	۲		-v•13a2E-J4	0.935550		-0-10401-04	0.2972E-03	0.9168E 00	0.1301E-04
t.	10	14		U.27705+U2	-0-5355	0.1417E−34	• = 5 + 1 = - 0 Z	0.9008F 00	-j.1361£-04	0.4126E-02
15	10	21	•	0.11236 70	-0.12275-05	-0.49555-03	-0.1017E 00	0.9941E-05	0.9424E-03	0.5083E-01
2	10	2.8		0.1057E-04	0.4200F-22	v 0.4554E .00	. C.4684E-05	-0.5666E-03	0.2169E 00	-0.8190E-06
62	: c.	35		-0.6635F-03	+0.16152 CC C	1°50.5652F-05	-0.31926-02	0.4020E-01	0.5467E-05	-0.20396-02
36	10	42		-0.6688E-31	-0.27515-57	-0.2772E-06	0.9483E 00	-0.7657E-02	-0.2179E-09	0.12256-07
\$	10	49		-().27o2E-J6	-0.101.0	-C.1057E-U2	-0.4518E-10	-0.12195-07	-0.2765E-06	0.4470E 00
50	C 1	56		-0.7657E-32	-0.2201°-09	0.7536E-38	-0.2762E-06	-0.4487E 00	-0.7656E-02	-0.9442E-10
57	10	63		-0.76855-08	9C-3:612.0-	-0.91565-02	0-75145-04	0.18336-10	0.7829E-08	-0.1770E-08
49	10	70		0.4053F-02	0.10455-24	0.1329E-1J	-D.7016E-08	-0.27676-08	-0.38316-02	0.6909E-04
11	<b>61</b>	17		-0.6642E-10	0.657.5E – 3ë	-0.25396-35	0.2414F-02	0.3507F-04	-0.6574E-10	-0.7836E-10
78	10	<b>4</b> 6		-0.27646-06	50-31016°0-	-0.7c55E-02	-0.21956-05	-0.1800E-09	-0.2882E-08	-0.2901E-01
85	1.0	16		0.8559E-04	0.[t7=?-12	0.4.375-10		<b>0.1678E-12</b>	0.4006E-10	-0.4826E-11
. 92	10	98		-0.275UE-08	-0.15610-03	0.5377E-04	0-59605-05	-0.1633E-09	-0.5359E-10	-0.2893E-06
66	10	105		-0.1409E-02	-0.57295-02	-0.15546-05	0.6135E-09	-0.2080E-10	-0.22785-06	-0.1273E-02
90)	10	112		-().1974E-02	0.26755-05	-0.1345E-08	-0.4059E-10	-0.4681E-06	-0.1606E-02	-0.3802E-02
113	L L	114		U.1237E-Ub	0.3°60E-11					
190,1	VAHY P.	1 24								
-	10	~		-G.1737E-04	-6.70F35-02	0.0	0-3092-0 <b>5</b>	-0.3938E-02	0.0	0-6758E-05
80	01	14		G.7044E-02	0.(	-0-12:45-04	0.3962E-02	0.0	-0.1177E-04	-0.4067E-02
15	Ċ.	21		0°0	· 0.3534E-05	-0.22726-92	0.00	0.6092E-05	0.4059E-02	0-0
22	5	28		-0.793E-05	<b>0.</b> 22915-32	0.6	0.2331E-05	0.93746-03	0-0	0.3345E-05
62	10	5	•	-0.1661E-J3	0.Ū	0.1c30E-04	-0.1176F-02	0.0	J.1030E-04	0.1090E-02
35.	C.	4		c•c	-0-21-212-10	0.13435-09	0.0	0.0	-0.3681E-11	0.8694E-09
ç.	بار	54		0 - 734 4F - 1C	0.0	· • • • • •	-0.1092E-10	<b>0.7106F-09</b>	0-46245-10	0.0
3	10	-5¢	.•	· 0•0	-0.12615-11	0.2o2¢E-09	0.4903E-10	0.0	0.0	-0.3211E-11
5	0	63		-3.23176-99	-0.275±÷-1C	0°C	0.0	-0.1624E-11	-0.2659F-09	0.8799E-11
*0	10	1.0	•	0.0	0.0	0.2332E-11	-0.6681t-10	-0.30316-10	0.0	0.0
1	10	11	•	-3.215JF-11	-0.8047E-1C	0.12545-10	0.0	0.0	0.2736E-11	0.2251E-09
73	<b>1</b> 0	4 a.	÷	0.4646E-10	· 0•0	0.5	0.0	0.5156E-12	-0.1438E-10	0-0
95	10	16		0.0	0.0	0.2225E-11	0°C	0-0	-0.2225E-11	0.8975E-11
6	10	98		-0.59245-11	ي. 0•0	0.0	0.0	-0.1041E-12	0.1723E-09	-0.97396-10
\$	Ē	105		0.0	: : : :	0*0	-0.9799E-14	0.8916E-10	-0.8871E-10	0-0
2	6	112		<b>c</b> •0	0°C	0.61735-14	0-1513E-09	-0.8722E-11	0.0	0.0
[]	0	114		0•0	0.41515-16					

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•			-0.2486F-0	0.3157E-0	-0.2775E-0	0.9025E-0	0-9393E-0	0.2634E-0	-0.4126E-0	-0.2225E-0	-0.9288E-0	-0-39E-0	-0.4950E-0	0-34645-0	-0.2623E-0	-0.5378E-0	-0.5062E-0	0-1910E-0		•	-0.1288E-0	-0.9908E D	0-0	0.1899E-0	0.3694E 0	0.5584E-0	0-0	-0.4197E-0	0.1209E-0	0.0	0.1317E-0	0.0	0.3412E-0	0.1902E-0	0-0	0-0	:
:			0.19865-01	-U.2537E-02	-0.2052E-01	-0.1237E-01	0.6640E-C3	-0.16756-06	-0.6506E-02	0.3217E-07	0.9550E-04	0.4538E-06	-0.8177E-06	-0.1887F-04	0.7653E-06	-0.379UE-05	-0.1191E-02	0.2821E-06			0-0	-0.3742E-03	-0.4154E 00	0-0	-0.1115E-03	-0.3109E-05	-0.1304E-03	0.0	0.2974E-04	0.0	-0.3615E-06	0.1882E-04	0.4527E-06	0.1037E-04	0.1855E-02	0-0	•
	A.		0.4272E-01	0.1257F-01	- J.1107E-02	0.5340E-02	0.3723E-01	0.3499E-07	-0.1283E-03	-0.2890F-06	-3.2890E-06	-0.1547E-04	-0.3226E-08	-0.2600E-05	0.1000E-11	-0.9234E-06	-0.1489E-05	-0.33796-02			0.1616E-01	0.0	-0.1336E-03	0.1000E 01	0.0	. 0.0	-0.2294E-03	0.0	-0.7511E-06	0.1906E-04	0.0	-0.4741E-05	0.0	0.9554E-06	0.3817E-05	0.3314E-02	
			<b>3.46995-04</b>	-5.64201-02	0.1690F-01	0.1489E-02	0.3157E-01	-0.6626E-05	-0.1450F-05	-0.650vE-02	-0.1207E-07	-0.5217E-04	-0.2484E-06	0-6951E-08	0.2382E-08	-0.2011E-69	-0.6410E-05	-0.2710E-05			0.1215E-03	0.1780E-01	0.0	-0.1805E-03	0.4198E 00	0.0	+0.3653E-05	-0.12596-03	C.D.	-0.2245E-05	0•0	0.0	0°0,	0.0	-0.9037E-05	0.7210E-05	
			0.2133E-U1	C.5245F-05	0.5a7AF-01	0.8191E-02	0.5984E-03	-0.6506E-02	0.3218E-07	0.14045-03	0.1238E-05	-0.3294E-06	-0.1228E-04	0.3263E-07	0.7253F-06	-0.5A80E-08	0.5375E-08	-0.75385-05		•	0.0	0-13185-03	-0.4604E 00	0.0		-0.13956-03	0.0	0.27265-03	0.0	-0.5323E-06	0.1561E-04	0.0	0.7987E-06	0.0	0.0	0.9562E-35	
. •	ec)		0.1464E-01	-(.1403r-01	-0.87465-03	-C.7è145-01	-0.11936-02	-C.1726F-03	3.20265-05	-0.1511F~05	-0.1601E-04	-0.82726-04	0.5214E-04	-0.2183E-05	0.1330F-11	(.1234F-07	n.2681F-07	-0.78255-09	-0.89746-05		-0-39442-01	0.0	0.2447E-Ú3	-C.3544F UO	0°C	-0.4674E-03	0.0	-0.3096F-05	0.1513E-04	0°C	-0.11616-04	0.0	0.0	0.0	0.0	0.0	C.2912E-07
	•42200928f 01 (rad/se		-0.6773F-01	3.2590E-U2-	7.27415-01	- J. 7250E-03	-3.3386-01	0.6057E-J2	-0.6506E-J2		-0.7234E-04	-0.3924F-06	+0.79UCE-00	-0.65756-02	-0-144,46-07	-6.1508E-34	-0.4933E-06	L.3392F-08	G.1192F-05		-0.2975F-J3	0.3443F-02	0.0	0.3585E-03	0.47305 00	C•.3	- J. I 250F-03	0.0	-0.672BE-04	0.0	-0.7390F-06	-0.12726-03	0.0	0.1854E-04	0°C	0.0	0.0
	UE≈ J	1	•	* <b>1</b> ;;	. 21	28	35	42	4 49	1 56	69 (	02 0	11 1	t 1	16 (	1 9B	1 105	112	1 114	V PART	~	1 14	1 21	1 28	35	: 42	0 <b>1</b>	, 5e.	69	1 70	11 1	94	16	46 t	1 105	112	114
	ETGENVAL	HEAL PAR	1 10	UL e	11 51	22 TC	29 70	36 10	43 TO	50 10	51 10	64 10	71 10	01 01	85 10	92 10	99 10	106 10	113 10	L"AGINAR		6	15 10	22 1C	29 TC	316 T.C	43 IC	50 10	57 10	64 IC	10 10	78 10	85 TO	92.10	01 66	1 401	

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Mode 11, frequency = 0.6716 Hz, Ω = 12 RPM

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ETGENVECTAR FAR RUAT NU.=

11

Mode 17, frequency = 0.7777 Hz, 31= 12 RPM

17 ELGENVECTOR FOR FOOT NO.=

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ELGEN	AVAL UE		<b>9.4</b> 83	1647465 01 <b>(F</b>	a/pa	ec)		٠			
1830	PART									•	
	C F	1		- 7. 32:			0.7159E-UI	0.4431E-05	-J.1262E-01	0.1068E-01	-0.1518E-05
	11	*1		-3.2651F-	. ~	-4.1660E-01	0.2477E-05	0.4449E-Ul	0.3337F-01	-0.5991E-05	0.5565E-01
5	10	21	- :: :	0.9227E	. 20	0.6727E-05	0.3672F-0t-	0.7425E 00	-0.2587E-05	0.2399E-01	0.97536 00
22	0	. 28		0.3313F-	-05	-0.3665E-01	0.9065F 00	-0.1429F-05	-0.2057E-01	-0.9513F 00	0-1986E-05
29	10	56		-0.4526E-		-0.7580F UO	-0.68966-06	0.6254E-02	-0.1000F 01	0.8191E-06	0.5779E-01
36	10	42		-0.46735	00	-0.8576E-05	-0.4730E-05	-0.2330E-01	0.13316-04	-0.5833E-07	0.8448E-05
7	5	4		-0-46455-	50	-0.1961F-01	0.1442F-04	-0.5639E-07	-0.41956-05	-0.4679E-05	-0.2233E-01
65	10	56		1.1366F-	40-	-C.6590F-07	0.4179E-05	-0.4045E-05	-0.2065E-01	0.1469E-04	-0.6508E-07
15	0	63		0.60355-	-06	0-34956-06	0.17426-02	-0.1501E-04	-0.2554E-08	-0.5376E-06	0.2207E-06
\$	2	10		-0-4896F-	<b>Е</b> О.	-0.10536-05	-Q.1741E-08	0.6329E-06	0.3506E-06	0.7666E-03	-0.1192E-04
12	01	17		0.39036-	-08	-C.5506E-06	0.2373E-06	-0.2426E-03	-0.5269E-05	0.2709E-08	0.2600E-08
E	0	48		-0.4695E-	-05	-3.21515-01	0.1444E-04	0.6864E-04	-0.79466-07	0.3454E-06	0.6004E-02
50	10	16		-30691-0-	• •	č.2087E-11.	-0.2517F-08	0.3900E-05	0.2087E-11	-0.2512E-08	0.1304E-09
26	10	96		C.3417F-	ֆ5	0.1420F-03	-0.8636F-05	-0.6150F-05	0.1940E-07	0.1936E-08	0-30106-04
8	2	105		-0.5312E-	.0,	ú.1746F-04	0.55776-04	-0.1557E-06	0.7653F-09	0.3007E-04	Q.3386E-02
901	10	112		0.2534F-1	.05	-0.14566-04	0.1559E-06	0.1310E-08	0.5436E-04	0.4288F-02	0.6507E-05
ELL.	10	114		0.1567E-	40	0.26726-09					
I PAGI	INARY	PART								•	
-	10	1		0.4093F-	<b>*</b> C	9.9233F-04	0*0	-0.7116E-05	0.1108E-03	0.0	-0.3776E-04
e	10	14		-3.23326-	<b>7</b> 0	0.0	-0.1821E-U3	0.8574E-04	0.0	-0.1182E-03	0.1138F-04
53	10	21		0.0		-0.8778E-04	0.2293f-04	0.0	-0.6739£-04	0.1208E-03	0-0
2	10	28		0.30195-	<b>*</b> 0-	0.3718E-05	0*0	0.6593E-04	0.1481E-04	. 0.0	0-1449E-04
52	01	35		0.47156-	·05	0.0	-0.2039F-04	-0.9196E-04	0.0	-0.1854E-03	0.3818E-05
8	10.	42		0.0		-0.24836-07	-0.9118E-09	0.0	0.0	0.4411F-10	-0-2055E-07
<b>9</b> 77	10	6.4		-0.8483E-	. <u>.</u> .	υ•0.	0.00	-0.9101E-10	-0.27575-07	-0:88856-09	0-0
50	01	56		0.0		0 <b>~2542E-10</b>	-0.2623£-07	-0.87685-09	0.0	0-0	-0.5490E-10
. 51	10	63		-0.1692E-	-01	-0.1273F-09	0*0	0.0	-0.11805-09	-0.1445E-07	~0.1347E-11
3	- 10	10		0.0			0.1041E-U9	-0.6300E-08	-0.11976-09	0.0	0.0
2	10	17		-0.1216E-	<b>0</b> 0	-0-52745-08	\ ₃ 0.2546E-10	0.0	0.0	0.9898E-10	-0.2819E-07
81	10	94		-0.8826F-	50	0.0	0.0	0.0	-0.9633E-11	-0.1100E-09	0.0
<b>9</b> 2	10	16		0°0		0.0	0.1654E-09	. 0.0	0.0	-0.1432E-09	-0.2767E-08
56	50	98		-0.81516-	•10	<b>0</b> "C	0.0	0.0	-0.4695E-11	-0.2906E-07	0.2717E-09
8	10	105	•	0.0		0.0	0.0	-0.8247E-12	-0.1615E-07	0.1645E-09	0-0
ê	5	112		0.0		0.0	0.2011E-11	-0.2660E-07	0.2021E-09	. 0.0	0.0
	91	411		0.0		0.2810E-13			-		

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				.,		•		•	
E I GF 4	VALUF=	194.0	05811E01 (rad/s	(oe)		0			
HEAL	PART				С				
-	10	1	-0-94585-0-	-0.76656-02	-0-49995-01	0.16266-05	0-45745-03	0.74885-01	-0-27295-0A
۵.	11	• 1	- ), 74-31 F + 112	-0.2211-11	0. F414F-04	-0.73451-52	-0.8530F-01	-0.16905-05	0.1410F-01
ŝ		51	-)-465544 00	0-71431-05	0.54796-32	0 F++ 3 - 00	-J.8156F-06	0-15495-01	-0-2720E 00
22	10	28	0.1079E-05	0-15495-01	0.74996 00	-0.1992F-06	0.67416-02	0.1000F 01	0.45385-06
62	10	35	0.4740E-02	00 31646.0-	0.37906-07	U.6741F-02	0.3459F 00	0.1963E-06	0-6740E-02
36	10	42	-0.7533F 00	-0.21471-05	-0.25476-05	-0.3355F-01	0.2558E-03	-0.14625-07	0-21075-05
4	10	49	-0.2519£-05	0.33135-01	0.2551F-03	-0.13336-07	-0.105CF-05	-0.25296-05	-0.1514F-01
50	. 01.	56	0.25566-03	-0.1c4uf-07	0.1051E-05	-C.2519E-05	0.14766-01	0.25546-03	-0.1632F-07
57	10	63	0.1712F-06	0 • 7 4 9 2 F - 0 7	-0.14495-02	U-1306E-04	-0.11396-08	-0.1124F-06	0.48395-07
*0	10	70	0.5654E-J3	0.1272t-05	-0.4027E-09	0.14276-06	0.74905-07	-0.5903F-03	0.1072E-04
1	10	11	U.157HE-OR	-11 B+F-0C	U.6301E-07	U.3471E-03	0.4905E-05	0.5084E-09	0.7077E-09
.78	10	R4	-0.2526F-05	-0.19346-03	0.2555F-03	-0.1483F-06	-0.1989E-07	0.7495E-07	-0.5131E-02
85	10	16	0.1663E-04	1. 44 44 -12	-0.5067E-09	-0.4191F-05	0.9484E-12	-0.5059E-09	0.3710E-10
26	0	មុខ	0.74905-07	-0-33416-04	0.8113E-05	u.1035E-05	0.4361E-08	0.5129E-09	0.60496-05
66	10	u5	-C.2254E-33	0.19416-03	-0.7423F-07	-0.3646F-07	0-21435-09	0.63445-05	-0.18236-03
<b>1</b> 06	10 1	12	U. 7005E-U4	0.301CE-06	0.34465-07	0.3508E-U9	0.1203E-04	-0.22556-03	0.1322E-03
113	10 1	14	U.7293E-07	0.95234-10					
I DVACI	NARY PA	1R 1	•,		````				
-	10	1	-0.14665-04	-0.1402E-05	) ) )	-0.2410E-04	0.4663E-04	0.0	-0.15615-04
ຍ	10	14	0.3286E-34	0.0	-0.1561E-04	0.3594E-04	0.0	-0.4232E-04	-0.3718E-04
15	10	21	0.0	-0-52401-04	0.9970F-04	0.0	-0.4572E-04	-0.4292E-04	0.0
22	10	2.8	-0.4572F-04	0.4767[-04	0.0	-0.23436-04	0.4992E-04	0.0	-0.2342E-04
52	10	35	-0.4910E-04	0.0	-0.23435-04	0.2934E-04	0.0	-0.23435-04	-0.2558E-04
36	5	42	0.0	-0.2070f-08	-0.2652E-09	0.0	0.0	0.5332E-10	-0.19386-08
4	02	64	-3.22165-09	0.0	0-0	-0.5091E-1C	-0.53766-08	-0.2504F-09	0-0
50		56	0.0	0.31346-10	-0.5130E-08	-U.2358E-09	0.0	0-0	-G.3327E-10
5	12	63	-5.2011F-08	-0.18066-10	0.0	0-0	-0.1480E-10	-0.144BE-08	-0.56785-12
•		70	0-0	0.0	0.11656-10	-0.80406-09	-0.2250E-10	0.0	0-0
2	5	11	-0.10356-13	-0.57791-09	-0.56146-11	0*0	0.0	0.5052E-11	-0.6340E-08
78	5	84	-0.2431E-09	0.0	0.0	0.0	-0.18996-11	-0.21086-10	0-0
8	2	16	0.0	0.0	0.2006E-10	0.0	0.0	-0.14856-10	-0.6335E-09
2	2:	98	-0.17346-10	0.0	0-0	0.0	-0.1041E-11	-0.6800F-08	-0.41746-10
8		05	0-0	0.0	0-0	-0.2037E-13	-0.3852E-08	-0.4966E-10	0-0
		12	0.0	0•0	0.7756E-13	-0.6445E-08	-0.7795E-10	0.0	0-0
11	1 01	14	0.0	0.93296-14					

Mode 18, frequency = 0.7911 Hz, 11 = 12 RPM

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FIGENVECTOP FUR ROUT NO.= 18

A-128

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Mode 19, frequency = 0. 9049 Hz,  $\Omega$  = 12 RPM

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2 ELGENVECTOR FOR POOT NO.=

FIGEN	4VAL LIÉ	0 ₩		ec)	·	
REAL	PART					
-	5	~	-0.3572f-06	P. 54261-03	P.c762F 00	C. Eredr-Jc
<b>5</b> .	. <u>۲</u>	14	- 0.11045-02	-0.41425 00	0.40125-06	0.9037F-03
5	10	21	-C.1167E 30	U-1424E-05	0.1453E-03	0.5855E-01
22	10	29	0.6869F-36	0.1879F-G3	0.2368F-01	-0.4200E-06
29	10	35	-0.7425E-03	-0.20905-01	-0.1587E-06	0.9688E-03
36	10	42	0.17695-02	-C.1971E-05	-0.1862E-05	-0.2771E-02
њ. Э	·10	.49	-0.18266-05	-0.46695-32	-0.7232E-05	-0.1311E-07
50	10	<u></u> و	-0.72956-75	-0.1513F-07	0.94385-06	-0.1826E-05
57	10	63	0.71445-07	0.57425+07	0.5396E-U2	-0.503UE-04
4 9	C 1	70	-0.16895-02	-C.4CB2F-05	-0.4438E-09	0.97385-07
11	10	. 11	0-36096-05	-0.7712E-07	0.4810E-07	-0.1160E-02
78	10	84	-0.1829£-05	-0.37236-02	-0.7281E-05	· 0.1168E-04
85	10	16	-2.58276-04	0.5011E-13	-0.1239F-09	0.13865-04
56	10	6 6	- 3° 5719 - 07	0.1461E-03	-0.2858E-04	-0.4457E-05
66	Ū,	105	-0.93615-73	-0.11996-04	0.9797E-05	-C.3344E-07
106	10	112	-0.214FF-04	-0.1936F-05	0.3101E-07	0.2630E-09
<b>E11</b>	10	114	0.3687E-05	0.1118E-08		
1 MAC 1	NARY	PART				
-	10	-		0.1556E-04	0.0	-0.4355E-05
er;	10	14	-0.BC27E-06	0.0	-0.31435-05	-0.1007E-04
15	01	21	0*0	-0.1651E-05	0.2047E-05	0.0
22	10	2 B	-0.1069E-05	0.1279E-05	0.0	-0.5398E-06
29.	10	35	0.6015E-05	0-0	0.6911E-06	0.5803F-05
36 	2	3	0-0	-0.4495E-08	-0.5322E-09	0.0
<b>.</b>	СĽ	64	00-34+0+0-	0-0	0.0	-0.1231E-09
ŝ	2	99	0.0	0.6113F-10	-0.9932F-08	-0.4428E-09
21.	2	63	-0.4052E-09	-0.5207E-10	0*0	0-0
40	10	70	0.0	0-0	40.2034E-10	-0.1907E-08
11	61	11	-0.2422F-10	-0.1641E-08	-0.1543E-10	0.0
78	D.	94	-0.4686E-09	0.0	0.0	0.0
<b>6</b> .	10	16	0.0	0.0	0.3724E-10	0-0
62	10	<b>8</b> 6	-0.3085E-10	0.0	0*0	0-0
ġ.	10	105	0-0	0.0	0°0	-0.5238E-12
•	2	112	0*0	0-0	0.1346E+12	-0.1271E-07
	10	114	0.0	0.1976E-13		

-0.5878F-01 -0.1420F-05 -0.1420F-05 -0.5136F 00 0.1746E-05 -0.1359F-07 -0.1359F-07 -0.1359F-07 -0.13528F-07 0.2162E-07 0.2162E-07 0.5528F-07 0.5528F-07 0.5772E-07 0.5618F-05 0.6618F-05

-0,55,670 = 0 -0,55,670 = 0 -0,4196 = 0 -0,4196 = 05 -0,4186 = 05 -0,4186 = 02 -0,4186 = 02 -0,4186 = 02 -0,4186 = 02 0,5116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,50116 = 13 0,501

-0.4157E-06 -0.2624E-03 -0.4384<u>E-01</u>

3.1,1,406-02

0.4251E-05 0.2739E-05 0.0 0.0 0.5392E-06 0.3129E-08 0.3129E-08 0.0 0.0 0.0 -0.495E-10 -0.4588E-11

0.0 -0.7898E-06 -0.1470E-05 0.0 0.0 0.9169E-06 -0.99169E-10 -0.9946E-09

0.0 -0.1241E-07 0.0 -0.1214E-08 -0.1214E-08 0.0

0.1872F-10 -0.5493E-10 -0.3198E-10 -0.1319E-07 -0.1202E-09 0.0

-0.1452E-11 -0.1452E-11 -0.1060E-09

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-0-3449E-08 0.0

-0.1967E-04 0.0 0.1335E-05 0.1335E-05 0.0 0.0 0.0 0.0 -0.1038E-07 0.0 -0.1038E-07 0.0 -0.2353E-10 0.0 0.0

Mode 20, frequency = 0.9090 Hz, Ω = 12 RPM

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FIN LUIS WUSE

FLGENVECTOR

p 1.

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(rad/sec)

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1.571136476

FICENALUE

-0.12976-03 -0.67276 00 0.203264-01 0.252666-03 -0.252666-03 -0.254766-03 -0.25666-03 -0.25666-03 -0.25666-03 -0.25666-03 -0.2717976-04 -0.17876-04 -0.17876-04 -0.17876-04 0.199366-02 0.11046-07 0.10466-07 0.388316-02 -0.9576E-03 -0.8666E-03 -0.8666E-03 -0.8666E-03 -0.8666E-03 -0.1109E-04 0.1109E-04 0.23895E-07 -0.23895E-07 -0.20 -0.00 -0.00 0.00 -0.7553F-01 -0.5188F-03 -0.5188F-03 -0.49465F-01 -0.5067F-04 -0.4990E-05 0.1406F-04 0.1406F-04 0.1406F-04 0.2783F-04 0.2783F-04 0.2783F-06 0.2332F-06 0.2516F-06 0.255F-06 0.58665 00 0.16735 00 0.16735 00 0.272445-03 0.272445-03 0.14105-04 0.14105-04 0.132055-03 0.133055-03 0.134655-01 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-11 0.54655-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-110055-11005 0.29086-03 0.29086-03 0.42096 00 0.42096 00 0.42096 00 0.42086 00 0.83986-05 0.83386-05 0.62386-05 0.62316-05 0.62316-05 0.62316-05 0.62316-05 0.62316-05 0.62316-05 0.6221286-05 0.12226-06 0.12226-06 0.1613f 00 0.1613f 00 0.1312f-03 0.4454f-04 0.1605f-04 0.1606f-04 0.1606f-04 0.2443f-04 0.1406f-04 0.2443f-06 0.1112f-06 0.2332f-06 0.1330ff-06 0.1330ff-06 0.1330ff-06 0.1407ff-06 0.14 -0.1+32F-02 0.1246F-02 0.1 -0.3643E-04 -0.2633F-06 0.0 -0.839E-05 0.0 0.2927E-07 -0.9383E-08 0.0 0.4888F-07 0.4 0.0 0.0 0.0 c.0 6.1006 01 -0.51617 00 -0.51177-03 -51177-03 -51177-03 -51177-03 -55736-05 0.25736-02 0.55736-05 0.55736-05 0.55716-03 0.55716-03 0.56856-11 0.55716-04 0.50776-06 -0.49406-06 -0.49406-06 0.9963E-02 0.752EF-03 0.7548E-03 0.7448E-03 0.7448E-03 0.7448E-03 0.752E-07 0.1738E-07 0.00 0.00 0.00 0.00 0.1458E-10 0.1458E-10 -U.2936E-03 0.2565F 00 ..70345-01 -0.25006 00 -0.25006 00 -0.13946 00 0.14096-04 0.34726-03 0.34726-03 0.34726-03 0.34726-03 0.34726-03 0.34726-03 0.34126-04 0.45196-03 0.42136-05 0.42136-05 -0.2234E-07 0.45265-02 0.0 -).5937E-13 0.3171E+32 -0.2147E-06 9.0 -0.5316E-05 9.0 -0.43291-07 -0.2392F-06 0.0 -0.1396E-07 0.0 0.0 1000440000000011 10004400000000011 PART CCL TERESCORE CERTER N S 

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FIGENSECTOP FOR PUDL ND.≖ 28

Mode 28, frequency = 1.0331 Hz, Q = 12 RPM

EICENVALUE* 0.64909668F 01 (rad/sec)

4FAL PAP	+					2.1		
1 1	• •	0.39205-02	00 16550 70-	- 00.33921.00 -	20-30220-0-	-n.9983F 00	-3-90406-01	0.4097F-02
	- <b>-</b>	0.95A5E UC	-C.1335E 90'	-0-4203E-02	-0-19799-00	-J.104UE 00	0.1297E-01	0.9313E 00
15 17	21	0.1470P CC	-0.1256£-01	0.9305E 00	0.74486-01	0.6093E-02	0.9294E 00	0.1279E 00
22 10	н <b>с</b>	-Ū.6089E-02	C.9290E OC	0.9542E-01	0.4677E-02	0.3144E 00	0.91816-01	-0.4716E-02
UI 67	35	0.3151E 00	0.71345-01	0.2008E-02	0.3136E 00	0.8751E-01	-0.2232E-02	0.3130E 00
36 10	42	0.7836F-01	r.1666F-01	0.76345-01	-0.5670E-03	0.6130E-06	0.1184E-03	-0.1604E-01
43 10	54	0.7612E-01	-0.4252t-03	0.5470E-06	0.10996-03	0.79185-02	0.7609E-01	-0.5237E-03
50 10	55	0.5805F-06	0.1275E-03	-0.7805E-02	0.7612E-01	-0.4634E-03	0.4956E-06	0.1235E-03
57 10	63	0.2825F-03	-0.1046F-03	0.9816E-04	-0.8585E-06	0.6474E-05	-0.5509E-03	-0.7617E-04
64 10	10	-0.1981E-U4	-0.79726-07	0.3103E-05	-0.1644E-03	-0-1111-0-	0.4188E-04	-0.6541E-06
71 10	11	0.2224E-05	-0.1726E-03	-0.9895E-04	-0.82506-05	-0.2486E-06	0.7099E-05	-0.5253E-06
76 13	94	3.76105-01	-C.441EF-03	0.5040F-06	0.2983E-05	0.1462E-03	-0.8050F-04	0.3164E-03
85 10	16	-0.5431E-06	0.1955E-1C	+0.5015F-05	G.1046E-06	0.19556-10	-0.5023E-05	-0.2869E-07
92 10	8.5	-0.1173E-03	0.110RE-04	-0.4167F-06	-0.4273E-06	-0.6604E-U5	-0.4224E-06	0.2220E-01
64 13	105	0 <b>.1</b> 956F-33	0.3594F-06	0.7203E-05	J.1985E-03	-0.1736E-06	-0.1103E-01	0.2678E-03
106 10	11,2	0.1758E-36.	-0.1350F-U5	-0.3545E-04	-0.31916-06	-0.7676E-02	0.5004E-03	0.2555E-06
113 10	114	0.1351E-Jō	0.5541E-04					
AAVI DAMI	Y PAPT	•						
1 10	1	0.42845-03	-0.1606F-01	0.0	0.9314E-03	0.1604E-01	0.0	0.1049E-02
8 TC	14	-0.8347E-U2	0.0	0.1050F-02	0.85766-02	0.0	-0.3241E-02	0.1116E-01
15 10	17	0.0	-0.3232F-02	-0.1096F-01	0.0	-0.3067E-02	0.5838E-02	0-0
22 10	28	-0.3065E-02	-0.5676E-02	0-0	-0.11926-02	0.1174E-01	0.0	-0.1096E-02
01 (62 · ·		-0.1142E-01	. 0*0	-0.1040E-02	0.70605-02	0.0	-0.1037E-02	-0.6803E-02
36 11	42	0.0	-0.31U2F-03	-0.6938F-05	0.0	0.0	-0.3219F-05	-0.3022E-03
43 17	49	-G.7811F-05	0.0	0-0	0.3108F-05	-0.1073E-03	-0.72016-05	0-0
50 10	56	0.0	-0,2016E-05	-0.1057E-03	-0.7544E-05	0-0	0.0	0.1967E-05
57 10	63	-0.4558F-05	-0.8076F-UR	0.0	0.0	-0.4260E-07	-0.4811E-05	-0.1117E-06
64 TD	70	0.0	0.0	0.4584E-07	-0.9921E-06	-0.1860E-07	0.0	0-0
71 10	11	-0.3561E-07	-0.97345-06	-0.6880E-07	0.0	0-0	0.3820E-07	-0.4084E-04
78 10	84	-0.1312E-35	0.0	0.0	0.0	-0.8910E-08	-0.1807E-07	. 0.0
85 70	16	0.0	0.0	0.4995E-07	0-0	0-0	-0.5329E-07	-0-1173E-06
92 10	66	-0.3360E-07	0*0	0*0	0.0	-0.2045E-08	-0.1964E-04	-0.4520E-05
99 10	105	0.0	0•0	0.0	-0.6728E-08	-0.8453E-06	-0.3475F-05	0-0
106 10	112	0.0	0.0	-0.1333E-07	-0.2651E-05	-0.4524E-05	0.0	0.0
113 10	114	0•0	0.19045-08			i a		

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		525F-02 -0.5193F-01	347E 00 -0.6684E-01	395F-U1 0.6007E-02	965E-02 -0.3404E 00	111E 00 -0.2400E-01	095E-02 -0.7017E-01	110F-01 -0.1856E-03	458E-06 0.3934E-03	350F 00 0.2103E-02	477E-04 -0.5393E-07	742E_02 -0.1510E-01	2956-02 0.8692E-05	290E-02 -0.1897E-02	156E-01 0.9981E-03	366E-02 0.1641E-02	331E-02 0.1291E-06			-0°3499E 00	248E 00 0.9479E-01	3586-01 0.0	-0.9042E 00	145F 00 0.3368F-01	734E-02 -0.4799E 00	370E-02 0.0	0.2955E-02	559E 00 -0.3570E-03	0.0	159f-02 -0.8264E-01	893E-03 0.0	416F-02 -0.1033E-01	489E-01 0.4587E-02	423E-02 0.0	0.0	
		-0.3450F-U1 0.55	0.5522t-02 -0.13	-0.4457F-01 -0.19	-0.7957t-01 0.55	0.5969E-02 -0.11	0.10485-05 -0.10	-0.44796-01 -0.41	-0.1396£-03 0.24	-0.8303£-03 -0.13	0.28296-02 0.64	0.6340E-07 0.12	-0.19796-03 0.32	0.23521-08 -0.12	0.7057F-04 -0.11	-0.4982F-02 0.93	0.29156-02 0.18			0.1051F 00 0.0	0.0 -0.82	-C.29R0F 00 0.33	0.9756E-01 0.0	0.0	0.0	-0.1771E 00 0.53	0.0 0.0	-0.4455F-02 -0.66	-0.4843E-03 0.0	0.0 0.61	0.20226-04 -0.66	0.0 -0.64	-0.6770E-05 -0.64	-0.2867E-01 0.34	0.522F-02 0.0	
		-0.14795 00	n76361-31 .	57756-02	-C.3408F 00	-0.2398E-01	-0.25556-03	(1.6032E-03	-9.4112E-01	-0-34575-07	-0.3913E-01	0.6931E-04	0.9211E-05	-0+4040F	-0.2060E-D5	-7.81495-04	-0.62026-02			-0.9871E 00	0.3640E-01	0.0	-0-9012E 00	0.3386F-01	0-0	0.4777E-02	0.5345F-02	0.0	-0.2259F 00	0.0	0.0	0.0	0-0	-0.4831F-05	-0.4633E-01	
		0.5514F-02	-0-42526-21	-0.69336-01	0.56654-32	-0.1093F 00	-0.4107E-01	0.5705F-06	-0.2243E-01	0-7091E-04	0. EA96F-03	0.23J3F-52	G.3205E-06	0.11736-02	0.02785-07	0.3550E-05	-0.1014F-04			0.0	-0°3495E 00	0.51906-01	0.0	-0.3150E 00	0.5418E-02	0.0	-0.1797E 00	0.0	0.44556-02	-0.3737F-03	0.0	0.6419E-02	0-0	0.0	0.1844E-04	
sec)		-J.2287E-U1	2C-31153*	-2.05485-61	-J.ZCE4E-01	0.59776-32	-C.1155E 0C	-0.1056E-03	-C.7520F-03	0.3278E-02	-0.1277E-07	-0-46875-01	-0.1503£-03	C.2352F-08	C.0571E-04	3.7650F-07	-C.4564F-05	-0.5053E-06		0.1069E 00	0•C	-C.6276E 00	(3209E-01	0-0	-0.4742F 00	0.0	-0.291CF-02	-0.5°18F-03	C • O .	-0.2254E 00	0.0	0.0	0.0	0-0	0-0	-0.7107E-U7
24166260E G2 (rad/		-0.1703t 90	10-22465-0-	0.6042E-32	-0.263df-01	-ŋ.8032F-01	U.5974E-02	-0.4111E-31	0.8316F-06	-0.1205E 00	0.7016E-04	-0.1118E-32	-0.4111E-01	0.40H5F-06	0.2453E-32	0.1702F-02	0.1583F-06	0.1024E-06		-0.9853E 00	0.3729F-01	0.0	-0.2556F 00	0.97146-01	0-0	0 5344E-02	0.0	D.6664F 3C	0-0	-0.6163E-32	0.5354E-02	0.0	-0.3946E-03	0.0	0-0	0.0
÷= 0		1	14	21	28	35	42	<b>6</b> 4	50	Ę.	10	17	: 84	16	98	105	112	114	PART	~	•1	- 21	. 82 .	. 35.	¢.	49	56	. 63	10	11	94	16	96	105	112	114
VALU	PART	01	C L	ÛΙ	L L	10	10	5	10	10	10	Ŭ	01	10	10	ΟL	с <b>1</b>	01	1 VARY	10	81	10	10	10	Ó	Ē	5	10	01	10	10	5	2	5	10	01
FIGE	RFAL	-	r	15	22	29	36	\$	C\$	57	40	11	78	9 P	92	66	105	113	<b>SMAG</b>	1	¢	15	22	53	36	<del>6</del> 4	50	57	40	1	7.8	92	92	6	106	113

Mode 32, frequency = 3.8462 Hz, Ω = 12 RPM

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FIGENVECTOR FOR ROOT ND.=

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