Adaptive Neural Network-Based Control of a Hybrid AC/DC Microgrid

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Abstract — In this paper, the behavior of a grid-connected hybrid AC/DC Microgrid has been investigated. Different Renewable Energy Sources – photovoltaics modules and a wind turbine generator - have been considered together with a Solid Oxide Fuel Cell and a Battery Energy Storage System. The main contribute of this work is the design and the validation of an innovative online-trained artificial neural network based control system for a hybrid microgrid. Adaptive Neural Networks are used to track the Maximum Power Point of renewable energy generators and to control the power exchanged between the Front-End Converter and the electrical grid. Moreover, a fuzzy logic based Power Management System is proposed in order to minimize the energy purchased from the electrical grid. The operation of the hybrid microgrid has been tested in the Matlab/Simulink environment under different operating conditions. The obtained results demonstrate the effectiveness, the high robustness and the self-adaptation ability of the proposed control system.

Index Terms — Adaptive interaction, fuel cells, microgrid, neural networks, photovoltaics, predictive control, wind energy, battery energy storage system.

NOMENCLATURE

AC Alternate Current
ADALINE ADApative Linear NEuron
AI Adaptive Interaction
BESS Battery Energy Storage System
BP Back-Propagation
CL Context Layer
CPL Constant Power Load
DC Direct Current
DPC Direct Power Control
DPCM Deadbeat Predictive Control Method
ENN Elman Neural Network
FEC Front-End Converter
FFNN Feed Forward Neural Network
FL Fuzzy Logic
HL Hidden Layer
IncCond Incremental Conductance
IL Input Layer
LMS Least Mean Squares
MG Micro-Grid
MPP Maximum Power Point
MPPT Maximum Power Point Tracking
NN Neural Network
OL Output Layer
PI Proportional Integral
PMS Power Management System
PMSG Permanent Magnetic Synchronous Generator
PV Photovoltaic
RBFN Radial Basis Function Network
RES Renewable Energy Sources
SOFC Solid Oxide Fuel Cell
SN-RBFN Single Neuron Radial Basis Function Network
SMC Sliding Mode Control
SOC State Of Charge
SVM Space Vector Modulator
TS-AF Tangent-Sigmoid Activation Function
VF Virtual Flux
WT Wind Turbine
WEGS Wind Energy Generation System

I. INTRODUCTION

NOWADAYS, the wide diffusion of distributed RES presents a new scenario for the regulation of distribution networks and the availability of new technologies for storage systems encourages their use in power systems [1]. In general, a hybrid AC/DC MG integrates different Distributed Generators (e.g. solar power sources, wind power generators, cogenerators, etc.), a energy storage system and a number of AC and DC loads. A FEC can interface the MG with the electric grid and can operate either in a grid-connected or islanded mode. The use of a PMS is crucial to optimize the power flow through the different components of the MG and the exchange of energy with the electric grid. Moreover, since the power produced by RESs depends on the climatic conditions, MPPT algorithms are needed in order to harvest the maximum available energy. The intermittent nature of RESs with the time-varying loads demand make the use of advanced control structures fundamental in order to make the operation of the MG reliable, economic, and secure under different operating conditions. The MG must also guarantee a high quality power supply to both local loads and electrical grid.

Many works have focused on hybrid microgrids and have proposed a number of control schemes for different mode of operations [2]-[8]. A multiagent-based energy management system to optimizes the economic operation of a MG is presented in [2]. A reactive power sharing algorithm in hierarchical droop control is developed in [3]. A novel coordinated voltage control scheme with islanding capability for a MG is proposed in [4]. For highly nonlinear and complex AC/DC MGs, control schemes based on artificial intelligence techniques such as Fuzzy Logic (FL), Neural Network (NN), and evolutionary algorithms are gaining widespread interest. Intelligent controllers are very promising because they can
adapt to uncertainties and they can be used also when the model of the system to be controlled is not available. Recently, the NNs with the learning capability are widely applied for the control of complex power systems. In [9], a back-propagation NN is applied for the real-time estimation of the wind speed. A novel discrete-time NN controller for the control of DC distribution system is designed in [10]. In [11], a RBFN and an improvedENN are proposed as MPPT controllers for different types of RES. A RBFN with an ENN have been also analyzed in [12] for the wind speed prediction in a wind farm.

The different NNs based techniques proposed in the literature can be classified, according to the training algorithm, into two categories [13]: offline and online trained NN. Offline learning of a neuro-controller is usually accomplished using a training dataset coming from the system model or from experimental data. When the controlled system is too complex to be modeled and/or experimental datasets are not available, it is more adequate to use online trained NNs that respond dynamically to the system uncertainties resulting from nonlinearities, parameters changing and exterior perturbations.

In this paper, a grid-connected hybrid MG which consist of a PV source, a WT generator, a SOFC, a BESS and two equivalent DC and AC loads is studied. A PMS based on FL is proposed to supervise the power flow in the MG. Online-trained NNs based MPPT for the RESs in addition to ADALINE based linear controllers for both SOFC stack and BESS are introduced. Moreover, a simplified deadbeat based predictive control scheme is applied for the WEGS. Further, a VF-DPC strategy for the bidirectional FEC is adopted. A FFNN is proposed for the regulation of the DC-bus voltage. Two ENNs based controllers are adopted to ensure the control of the bidirectional flow of the active power as well as the compensation of the AC load reactive power. An AI based algorithm is applied for the online weights adaptation of the proposed FFNN and ENNs. The investigated MG is simulated in the Matlab/Simulink environment. Then, the effectiveness of the proposed controllers is verified for different test cases.

The paper is organized as follows: the next Section in on the configuration and the modeling of the MG, Section III deals with the control scheme, the simulation results are given in Section IV, and Section V is on Conclusions and Perspectives.

II. SYSTEM CONFIGURATION AND MODELING

As shown in Fig.1, the investigated MG is connected to the electric grid though a FEC, while the DC-Bus is fed by four energy sources: a 21kWp PV generator, a 10kW WEGS, a 10kW SOFC, and a 20Ah Lithium-Ion BESS. A bidirectional buck-boost converter interfaces the BESS with the DC link. Whereas, boost converters are used for coupling the PV source and SOFC with the DC-bus. A filter capacitor $C_{dc}$ is connected to the DC-bus to minimise the DC voltage ripples. Moreover, the MG includes also AC and DC loads. The circuit model of the converters used in the MG is shown in Fig.2.

A. Modeling the PV generator

The equivalent circuit used to model a PV module is shown in Fig.3 and is represented by the following equation [14]:

$$I_{PV} = n_p I_{ph} - n_p I_S \exp \left( \frac{q}{n_q} \left( \frac{V_{PV}}{n_q} + I_{PV} R_S \right) - 1 \right) \quad (1)$$

Where $I_{PV}$ and $V_{PV}$ are the PV module’s output current and voltage, $R_S$ is the series resistance, $I_{ph}$ is the photocurrent, $I_S$ is the saturation current, $q$ is the electron charge, $K$ is the Boltzmann constant, $A$ is the diode ideality factor, $T$ is the temperature, while $n_p$ and $n_q$ are the numbers of series and parallel-connected solar cells.

![Fig. 3. Single diode equivalent circuit of PV module.](image)

B. Modeling the Wind Energy Generation System

The WEGS consists of a WT coupled to a PMSG, where an AC-DC Rectifier is used for the interfacing with the DC-bus. The mathematical model of the PMSG implemented in the synchronous rotating frame $dq$ is given as [15, 16]:

$$\begin{align*}
V_{sd} &= -R_s I_{sd} - L_s \frac{d I_{sd}}{dt} + L_{sq} \omega_i I_{sq} \\
V_{sq} &= -R_s I_{sq} - L_s \frac{d I_{sq}}{dt} - L_{sq} \omega_i I_{sd} + \omega_e \phi
\end{align*} \quad (2)$$

Where $V_{sd}, V_{sq}, I_{sd}$ and $I_{sq}$ are the $d$ and $q$-axis components of the stator voltages and currents; $L_{sd}$ and $L_{sq}$ are the $d$ and $q$-axis inductance, $\omega_i$ is the generator speed defined as [15]: $\omega_i = p \cdot \omega_e$ such that $p$ is the number of pole pairs and $\omega_e$ is the angular velocity of WT, $\phi$ is the permanent magnet flux, and $R_s$ is the stator resistance. The electromagnetic torque $T_e$ developed by the generator can be written as [16]:

![Fig. 1. Hybrid Microgrid configuration.](image)

![Fig. 2. Circuit model of the considered converters.](image)
\[ T_e = \frac{3}{2} p \left( (L_{st} - L_{sq}) I_{sq} I_{st} + \phi I_{sq} \right) \]  

(3)

Considering that for non-salient PMSG \( L_{st} = L_{sq} = L_s \), Eq.3 can be rewritten as:

\[ T_e = \frac{3}{2} p I_{sq} \phi \]  

(4)

Since the magnetic flux is constant, the electromagnetic torque and the q-axis stator current component \( I_{sq} \) are directly proportional. Whereas, the reactive power may be controlled depending on the d-axis current component \( I_{st} \). The motion equation is given by [15]:

\[ J \frac{d^2 \omega_m}{dt^2} = T_e - F \omega_m \]  

(5)

Where \( F \) is the viscous friction factor, \( J \) is the moment of inertia. The aerodynamic power of WT is defined as the ratio between the aerodynamic power \( P_t \) and the WT angular velocity:

\[ T_i = P_t / \omega_t = 0.5 \pi \rho R^2 C_p V_{\text{rad}}^3 / \omega_t \]  

(6)

Where \( \rho \), \( V_{\text{rad}} \), \( R \), \( C_p \) are the air density, the wind speed, the radius of turbine blade and the power coefficient, respectively.

C. Modeling the Solid Oxide Fuel Cell

The dynamic model adopted for the SOFC [17,18] is based on the relationship between the FC output voltage \( V_f \) and the partial pressures of hydrogen, oxygen, and water \( P_H2, P_O2, P_H2O \), respectively. The SOFC terminal voltage \( V_f \) is determined using the Nernst’s equation and Ohm’s law as [17,18]:

\[ V_f = N_0 \left( E_0 + \frac{RT}{2F} \ln \left( \frac{P_{H2}P_{O2}^2}{P_{H2O}} \right) \right) - r I_f \]  

(7)

Where \( N_0 \) is the number of series connected cells, \( E_0 \) is the free reaction voltage, \( R \) is the universal gas constant, \( T \) is the temperature, \( F \) is the Faraday’s constant, \( I_f \) is the FC output current, and \( r \) is the ohmic resistance.

D. Modeling the Battery Energy Storage System

The Matlab/Simulink module used for the BESS simulation consists of a controlled voltage source series-connected with an internal resistance [19]. The battery output voltage and the State Of Charge (SOC) are calculated as follows:

\[ V_b = V_{n0} - R_{inb} I_b - \frac{K}{Q} \int_0^Q I_b(t) dt + A \exp \left( -B \int_0^Q I_b(t) dt \right) \]  

(8)

\[ SOC = 100 \left( 1 - \frac{\int_0^Q I_b(t) dt}{Q} \right) \]  

(9)

Where \( V_{n0} \) and \( I_b \) are the BESS terminal voltage and current, \( E_{n0} \) is the BESS no-load voltage, \( R_{inb} \) is the internal resistance, \( K \) is the polarization voltage, \( Q \) is the BESS capacity, \( A \) is the exponential zone amplitude, and \( B \) is the inverse exponential zone time constant. In this paper, a 20 Ah Lithium-Ion battery bank is used.

III. CONTROL STRUCTURE OF THE HYBRID MICROGRID

The main tasks of the control system of a hybrid MG are: to minimize the amount of power purchased from the electric grid, to make the RESs based generators operate at their MPPs and to ensure a high-quality power supply to local loads and to electric grid. Being motivated by the benefits of learning ability, robustness against uncertainties and adaptability, a number of intelligent NN controllers have been designed and used instead of the conventional controllers, in order to satisfy the above requirements.

A. MPPT control of PV generator

The PV source exhibits a nonlinear behavior depending upon the variable operating conditions, and the maximum output power is generated at an unique operating point. Several MPPT algorithms have been proposed in the literature to extract the maximum energy from PV modules. One of them is the well-known incremental conductance (IncCond) algorithm [20,21]. This method consists in the regulation of the PV voltage according to the MPP voltage reference. At each iteration, the PV voltage reference is adjusted based on the comparison of the incremental conductance (dI/dV) of the PV source with the negative instantaneous conductance (-I/V). The position of the operating point with respect to the MPP on the PV power curve is known based on the following equation [20]:

\[ \begin{align*}
\frac{dt}{dv} &= \begin{cases} 
1 & \text{at the MPP} \\
> 1 & \text{at left of the MPP} \\
< 1 & \text{at right of the MPP}
\end{cases}
\end{align*} \]  

(10)

The IncCond method is simple and easy to implement. But, the convergence speed and the steady state power oscillations depend mainly on the size of the step change in the reference voltage. In this paper, a SN-RBFN based controller is applied to overcome the nonlinear issues arising with such MPPTs. The aim is to enhance the dynamic performance and the tracking accuracy of the IncCond algorithm. The MPP of the studied PV generator is tracked through a DC-DC boost converter. As shown in Fig.4a, a PI voltage controller generates the gate signal of the power switch, while the SN-RBFN based controller generates the PV voltage reference. The proposed MPPT regulator is based on the principle of the IncCond technique. The learning ability of the SN-RBFN tracker ensures the self-adaptation to any change of operating conditions. The adopted SN-RBFN contains a single hidden node that uses the Gaussian function defined as [22]:

\[ f(x) = \exp \left( -\frac{(x-c)^2}{2\sigma^2} \right) = h \]  

(11)

Where \( c \) is the central point of the Gaussian function \( f(x) \), \( b \) is the width value of \( f(x) \), and \( x=[x_1,x_2,x_3] \) is the input vector and \( || \cdot || \) denotes the Euclidean norm. The SN-RBFN output \( y \) is calculated as:

\[ y = V_{\text{pref}} = a_0 + a_1 f(x) \]  

(12)

Where \( a_0 \) and \( a_1 \) are the bias and the weight of the SN-RBFN respectively, and \( V_{\text{pref}} \) is the PV voltage reference at the output of MPPT controller. The SN-RBFN’s inputs are: the instantaneous conductance \( (I/V) \), the incremental conductance \( (dI/dV) \), and the reference voltage error \( (AV_{\text{pref}}(k) - V_{\text{pref}}(k) - V_{\text{pref}}(k-1)) \). In this paper, a supervised learning rule based gradient descent method [11,23] is adopted for the online update of the SN-RBFN parameters. The objective function used for the weights adaptation is defined as:

\[ \sigma(k) = e_y(k)^2 / 2 = (y_d - y)^2 / 2 \]  

(13)

Where \( e_y \) is the output error, and \( y_d \) is the desired output voltage. The goal of the online learning process of the SN-
RBFN is to minimize the performance index function $\sigma(k)$. Thus, the adaptation laws of the SN-RBFN gains are given according to the gradient descent method as follows:

$$a_i(k + 1) = a_i(k) + \Delta a_i(k) + a_i(a_i(k) - a_i(k - 1))$$ (14)

$$c_{ij}(k + 1) = c_{ij}(k) + \Delta c_{ij}(k) + a\left(c_{ij}(k) - c_{ij}(k - 1)\right)$$ (15)

$$b(k + 1) = b(k) + \Delta b(k) + a(b(k) - b(k - 1))$$ (16)

Where $a$ is the momentum factor, $k$ is the k-th iteration, $i=0,1, \ldots, j=1,2,3$. According to the control algorithm based on the gradient descent rule, the SN-RBFN parameters $a_i$, $c_{ij}$ and $b$ are adjusted by computing the gradient of the error function $\sigma(k)$ with respect to the SN-RBFN coefficients, so that $\sigma(k)$ is eliminated. The derivative of the error function $\sigma(k)$ against each SN-RBFN’s gain is evaluated by propagating the error term back through the NN. Thus, the SN-RBFN parameters are adjusted using the formulas:

$$\Delta a_i(k) = -\mu \frac{\partial \sigma}{\partial a_i} = -\mu \frac{\partial \sigma}{\partial a_i} = \mu e_y(k)$$ (17)

$$\Delta a_1(k) = -\mu \frac{\partial \sigma}{\partial a_1} = -\mu \frac{\partial \sigma}{\partial a_1} = \mu e_y(k)f(x)$$ (18)

$$\Delta c_{ij}(k) = -\mu \frac{\partial \sigma}{\partial c_{ij}} = -\mu \frac{\partial \sigma}{\partial c_{ij}} = \mu a_1 e_y(k)(x_j - f_j) f(x)/b^2$$ (19)

$$\Delta b(k) = -\mu \frac{\partial \sigma}{\partial b} = -\mu \frac{\partial \sigma}{\partial b} = \mu a_1 e_y(k)||x - c||^2 f(x)/b^3$$ (20)

Where $\mu$ denotes the learning rate. We define the variable $G_{ad}(k) = (I(k)/V(k)) + (I(k)/V(k))$ that has to be equal to zero at the MPP. Since the desired output of SN-RBFN based MPPT controller $y_{d1}$ is unknown, the error $e_{c}(k) = (0 - G_{ad}(k))$ is used instead of $e_{c}(k)$ in Eq.17-20. Thus, the iterative learning algorithm of the SN-RBFN based MPPT controller is given as:

$$a_0(k + 1) = a_0(k) + \mu G_{ad}(k) + a(a_0(k) - a_0(k - 1))$$

$$a_1(k + 1) = a_1(k) + \mu G_{ad}(k)f(x) + a(a_1(k) - a_1(k - 1))$$

$$c_{ij}(k + 1) = c_{ij}(k) + \mu a_1 G_{ad}(k)(x_j - f_j) f(x)/b^2 + a(c_{ij}(k) - c_{ij}(k - 1))$$

$$b(k + 1) = b(k) + \mu a_1 G_{ad}(k)||x - c||^2 f(x)/b^3 + a(b(k) - b(k - 1))$$ (21)

Once the term $G_{ad}(k)$ converges to zero, the SN-RBFN stabilizes at the reached operating point that correspond to the MPP of PV source at the given climatic condition.

B. Predictive torque control for the PMSG

The block diagram of the control scheme of the AC-DC converter used for the PMSG is depicted in Fig.4.b. A DPCM based on the Deadbeat approach [24-26] is applied to drive the AC-DC rectifier in order to improve the dynamic performance of the classical direct torque control scheme of PMSG. Besides, an ADALINE based MPPT controller is proposed for the tight regulation of the rotating speed of WT. The main tasks of the PMSG control system are to instantaneously follow the MPP of WT generator, to track the electromagnetic torque reference, and to maintain the direct stator current component close to zero.

The basic idea of the adopted DPCM is to compute, at each sampling period, and apply the optimal stator voltage vector that ensures the minimization, at the next sampling instant, of the tracking errors between the predicted and the reference values of the controlled variables [24,25]. Using the calculated voltage vector, the proper switching pulses for rectifier are generated through the Space-Vector Modulator (SVM).

- Discrete time model

The model of the PMSG developed in the rotating $dq$ frame is used to predict the future values of the controlled variables, which are the electromagnetic torque $T_e$ and the direct stator current $i_d$. Then, the reference stator voltage components $V_{sd}$ and $V_{sq}$ that should be generated during one sampling period are calculated in function of the tracking errors of the regulated quantities $T_e$ and $i_d$. The stator flux magnitude of PMSG is indirectly controlled using the d-axis current component.

Thus, the continuous-time model represented by Eq.2 is discretized using the Euler forward method, such that the current derivatives are approximated as [27]:

$$\frac{di}{dt} \approx \frac{i(k+1) - i(k)}{T_s}$$ (22)

Where $T_s$ is the sampling period, $k$ and $k+l$ are the actual and future sampling instants, respectively. The future values of d-axis and q-axis components of stator current are expressed using Eq.2 and Eq.22 as follows:

$$\begin{align*}
i_{sd}(k+1) &= \frac{2}{\tau_e}\left[-V_{sd}(k) - R_s i_d(k) + L_s \omega_s i_q(k) + \frac{2}{\tau_e} I_d(k)\right] \\
i_{sq}(k+1) &= \frac{2}{\tau_e}\left[-V_{sq}(k) - R_s i_q(k) - L_s \omega_s i_d(k) + \omega_s \phi + \frac{2}{\tau_e} i_q(k)\right]
\end{align*}$$ (23)

The linear relationship between the q-axis stator current and the generator torque of Eq.4 can be rewritten as:

$$I_{sq} = \frac{2}{\tau_e} T_e$$ (24)

By replacing Eq.24 in Eq. 23, we found:

$$\begin{align*}
i_{sd}(k+1) &= \frac{2}{\tau_e}\left[-V_{sd}(k) - R_s i_d(k) + \frac{2}{\tau_e} L_s \omega_s T_e(k)\right] + I_{sd}(k) \\
i_{sq}(k+1) &= \frac{2}{\tau_e}\left[-V_{sq}(k) - \frac{2}{\tau_e} T_e(k) - R_s L_s i_d(k) + \omega_s \phi\right] + I_{sq}(k)
\end{align*}$$ (25)

According to deadbeat principle [26], the predictive control target here is to get, at the next sampling instant (k+1), both predicted values of the generator torque and d-axis current component ideally equal to their respective references:

$$\begin{align*}
T_e(k+1) &= T_e(k+1) \\
i_{sd}(k+1) &= I_{sd}(k+1)
\end{align*}$$ (26)

By substituting Equ.26 in Equ.25, we obtain:

$$\begin{align*}
i_{sd}(k+1) &= \frac{2}{\tau_e}\left[-V_{sd}(k) - R_s i_d(k) + \frac{2}{\tau_e} L_s \omega_s T_e(k)\right] + I_{sd}(k) \\
i_{sq}(k+1) &= \frac{2}{\tau_e}\left[-V_{sq}(k) - \frac{2}{\tau_e} T_e(k) - R_s L_s i_d(k) + \omega_s \phi\right] + I_{sq}(k)
\end{align*}$$ (27)

Since the d-axis current reference $I_{sd}$ is constantly zero, it can be assumed that the present setpoint of d-axis current is equal to the future reference [26]:

$$I_{sd}(k+1) = I_{sd}(k)$$ (28)

On the other hand, as shown in Fig 4.b, the external speed control loop provides the actual torque set point $T_e(k)$. Assuming that the tracking error of the rotational speed is constant during two successive sampling period, the future reference value of $T_e$ at the instant (k+1) is estimated using the linear Lagrange extrapolation [24,27] as presented in Fig4.c. Thus, the future torque reference is calculated as:

$$T_e(k+1) = 2T_e(k) - T_e(k-1)$$ (29)
Substituting Eq.29 and Eq.28 in Eq.27, the d-axis and q-axis components of the required stator voltage vector are given as:

\[
\begin{align*}
V_d(k) &= -R_i I_d(k) + \frac{2}{3p_0} L_i \omega_0 T_e(k) - \frac{1}{6} \Delta I_d(k) \\
V_q(k) &= -\frac{2p_0}{3p_0} T_e(k) - L_i \omega_0 I_d(k) + \omega_k \phi - \frac{2p_0}{3p_0} \Delta T_e(k) + d T_e^*(k)
\end{align*}
\]

(30)

Where \(\Delta T_e(k)\) and \(\Delta I_d(k)\) are the instantaneous tracking errors of the torque and the d-axis current, respectively. While, \(d T_e^*(k)\) is the current variation in the torque reference:

\[
\begin{align*}
\Delta T_e(k) &= I_d^*(k) - I_d(k) \\
\Delta I_d(k) &= T_e^*(k) - T_e(k) \\
d T_e^*(k) &= T_e^*_*(k) - T_e^*_*(k-1)
\end{align*}
\]

(31)

- ADALINE based speed controller

Traditionally, a Proportional Integral (PI) controller is used to regulate the rotating speed of WT in order to extract the maximum wind energy. However, a PI controller with fixed gains for a time-varying WEGS, which is subject to random wind speed and parameters variations, can yield poor dynamic performance. To overcome this drawback, an adaptive ADALINE (ADaptive Linear NEuron) network based controller is adopted in this paper, to control the rotational speed by producing the reference for the electromagnetic torque. The ADALINE based speed controller consists of a single neuron with linear activation function, where the output is calculated as [13, 28]:

\[
y_w(k) = T_e^*(k) = \sum_{i=1}^{n} w_i(k) x_i(k) = X_w^T W_w
\]

(32)

Where \(w_i\) is the \(i^{th}\) weight coefficient \((i=1,2,3)\), \(x_i\) is the \(i^{th}\) input signal and \(n\) is the number of inputs. \(X_w\) and \(W_w\) are the inputs and weights vectors, respectively. The ADALINE output is the electromagnetic torque reference \(T_e^*(k)\), while the inputs are the measured speed at the instant \(\omega(k)\), the actual speed error \(e_{\omega}(k) = \omega^*(k) - \omega(k)\), and the previous error \(e_{\omega}(k-1)\). Such that \(\omega^*(k)\) is the speed reference. The Widrow–Hoff Least Mean Square (LMS) learning algorithm [28] is used for the online update of the ADALINE’s weights. Where, the goal of the self-learning process of the ADALINE based speed controller is to minimize the mean square of the instantaneous error \(e_{\omega}(k)\). Using the transformation \(X' = 0.5 \text{ sgn}(X_w) + 0.5 X_w\) [28], the weight vector is adjusted as:

\[
W_w(k+1) = W_w(k) + a_\omega(k) x_i' \frac{e_{\omega}(k)}{\lambda + ||x_i'||^2}
\]

(33)

Where \(W_w(k+1)\) and \(W_w(k)\) are the weight vectors at the next and present iteration, \(k+1\) and \(k\), respectively. \(\lambda\) is a correction factor, \(a_\omega\) is the learning rate, and \(||x_i'||^2\) is the squared norm of the input vector \(X'\). The learning coefficient \(a_\omega\) which has a value in the interval \([0,1]\) affect considerably the speed of convergence to the optimal weighting factors of the ADALINE network. The continuous adjustment of the ADALINE’s weights using the normalized LMS law of Equ.33, ensures the self-adaptation of the adopted speed controller to any change of working conditions unlike the PI regulator with fixed gains .

C. Control of the SOFC stack

As depicted in Fig.4.d, an ADALINE based power controller with two adaptive weights regulates the SOFC’s output power to follow the power reference provided by the central power supervisor. The inputs of the ADALINE controller are the power error \((e_{\omega}(k) = P_{\omega}(k) - P_{\omega}^*(k))\), and the change of error \((\Delta e_{\omega}(k) = e_{\omega}(k) - e_{\omega}(k-1))\). Such that, \(P_{\omega}^*(k)\) and \(P_{\omega}(k)\) are the power reference and the output power generated by the SOFC stack, respectively. Whereas, the output is the duty cycle \(D_{\omega}(k)\) that controls the commutation time of the switching device of the boost converter. The control error \(e_{\omega}(k)\) used for the online learning process of the SOFC’s power controller is defined in function of the sliding surface \(S_{\omega}(k)\) as:

\[
e_{\omega}(k) = 0 - S_{\omega}(k) = -\left[\lambda_1 e_{\omega}(k) + d e_{\omega}(k)\right]
\]

(34)

Where \(\lambda_1\) is a positive constant. According to the SMC principle [29], the control goal here is to maintain the trajectory of the state variable, which is the SOFC’s output power, on the sliding surface \(S_{\omega}(k)=0\) for the whole time. With reference to the LMS algorithm [13], the weight vector \((W_e)\) of the SOFC’s controller is updated at each iteration of the online training process as follows:

\[
W_e(k+1) = W_e(k) + 2a_\omega e_{\omega}(k) X_w(k)
\]

(35)

Where \(X_w\) is the input vector and \(a_\omega\) is the learning rate of the SOFC’s controller. In this case, the connective weights are adapted in such way that the sliding surface \(S_{\omega}(k)\) tend to zero, so that the power tracking error will be eliminated.
D. Control of the BESS

The control of the charge and discharge of BESS is performed through a bidirectional DC-DC converter. As shown in Fig.4.e, the BESS power reference \( P^*_h \), provided by the PMS, is divided by the BESS terminal voltage to generate the current set point \( I_b' \). Then, an ADALINE based controller is used to regulate the BESS’s output current \( I_b \) to follow its setpoint \( I_b' \). The inputs of the BESS’s ADALINE regulator are the actual BESS current error \( e_b(k) \) and the past current error \( e_b(k-1) \). Whereas, the output is the duty cycle \( D_b(k) \) of the PWM control signal of the buck-boost converter. Such that, the present current error \( e_b(k) \) is defined as the difference between the current reference \( I_b'(k) \) and the measured BESS current \( I_b(k) \). The control objective used for the adaptation of the gains is expressed in term of the sliding surface \( S_b(k) \) as:

\[
E_b(k) = 0 - S_b(k) = -[\alpha_3 e_b(k) + de_b(k)]
\] (36)

Where \( E_b(k) \) is the error term used for the weights update, \( de_b(k) = e_b(k) - e_b(k-1) \) is the change of the BESS current error, and \( \alpha_3 \) is a positive constant. Where, the ADALINE’s weights vector \( W_b \) are online adjusted via a LMS-rule as follows:

\[
W_b(k + 1) = W_b(k) + 2\alpha_3 E_b(k)X_b(k)
\] (37)

Where \( X_b \) and \( \alpha_3 \) are, respectively, the input vector and the learning rate of the BESS’s controller. If the sliding function \( S_b(k) \) in the steady state, is close to zero, that means that the trajectory of the BESS’s current \( I_b \) is forced to stay on it.

E. Control of the FEC

A Virtual Flux based Direct Power Control [30] scheme is applied for the control of the FEC. Assuming that the grid voltage vector \( V_g \) and the inductance filter \( L \) are virtual AC motor quantities, the grid VF voltage \( \Psi_g \) is defined as:

\[
\Psi_g = \int \Psi_{ad} dt = \int \Psi_{ac} - R I_c - L \frac{dI_c}{dt} dt
\] (38)

\( \Psi_{ad} \) is the inverter voltage vector and \( I_c \) is the FEC output current vector. The voltage drop across the filter resistance \( R \) is neglected. In the stationary \( dq \) frame, the \( d \) and \( q \) components of the grid VF are calculated in term of the inverter switching states \( S_n \), the \( d \) and \( q \) current components \( i_{ca}, i_{cb} \) and the measured DC-link voltage \( V_{DC} \):

\[
\begin{align*}
\Psi_{ga} &= \int \frac{V_{ac}}{2}(2S_a - S_b - S_c) dt - L i_{ca} \\
\Psi_{gb} &= \int \frac{V_{ac}}{2} (S_b - S_c) dt - L i_{cb}
\end{align*}
\] (39)

Based on the grid VF components \( \Psi_{ga,b} \), the instantaneous active and reactive power \( (P,Q) \) can be estimated as [30]:

\[
\begin{align*}
P &= \frac{3}{2} \omega \left( \Psi_{ga} i_{qb} - \Psi_{gb} i_{qa} \right) \\
Q &= \frac{3}{2} \omega \left( \Psi_{ga} i_{qa} + \Psi_{gb} i_{qb} \right)
\end{align*}
\] (40)

In a conventional DPC scheme, PI controllers are used to control the DC-bus voltage as well as the active and reactive power flows. However, the irregular RESs power generation and the time-varying load demand require that the FEC works dynamically over a wide range of MG operation. For this purpose, NN based controllers are used in the adopted VF-DPC scheme instead of the linear PI controllers in order to improve the dynamic performance and to react adaptively to the varying conditions. As depicted in Fig.5, a FFNN is employed for the outer DC voltage control loop, while ENNs based controllers are applied for the power control loops. The Adaptive Interaction algorithm proposed by Brandt and Lin [31] is used for the online weights adaptation of the proposed FFNN and ENN controllers.

- The principle of the AI algorithm for NN training

The adjustment of the NN weights with the adaptive interaction algorithm is equivalent but simpler than the well-known BP approach. Moreover, it does not need to back propagate the output error through the network [31]. The most prominent features of the AI approach are the adaptation during the interaction of neurons and the low computational requirements in comparison to the BP algorithm. In this subsection, the NN weights adaptation law based on the AI algorithm is given. The output of each node in the l-th layer of a NN is calculated as:

\[
x_n^{(l)} = f_n^{(l)} \left( \sum_{i=1}^{N} w_{ij} x_i^{(l-1)} \right)
\] (41)

Where \( x_n^{(0)} \) and \( f_n^{(l)} \) are the output and the activation function of the n-th node in the l-th layer respectively, \( x_i^{(l-1)} \) is i-th input of n-th node, \( w_i \) is the connection weight from i-th input to the n-th node, and \( N \) is the number of inputs to the l-th layer. The training process aims to minimize the cost function \( E \) expressed as [13]:

\[
E = \frac{1}{2} \sum_{i=1}^{N} e_i^2
\] (42)
Where \( e_n = \begin{cases} x_n^{(i)} - d_n & \text{for output node} \\ 0 & \text{otherwise} \end{cases} \) for output node

\( m \) is the number of the output neurons. \( d_n \) is the desired output of the \( n \)-th output neuron. The weights of the NN can be dynamically updated according to the AI law \([13,31]\) as follows:

\[ \Delta w_i = f_n^{(i)}(net_n^{(i)}) \sum_{j=1}^{P} w_{oj} \Delta w_{oj} - \gamma f_n^{(i)}(net_n^{(i)}) x_i^{(i-1)} e_n \]

(44)

Where \( \gamma > 0 \) is the adaptation coefficient and \( P \) is the number neurons in the next layer. \( w_{oj} \) is the weight connecting \( o \)-th with \( j \)-th neuron. The Tangent-Sigmoid Activation Function (TS-AF) of neurons is defined as:

\[ x_n^{(i)} = f_n^{(i)}(net_n^{(i)}) = \frac{2}{1 + e^{-net_n^{(i)}}} - 1 = \frac{1 - e^{-net_n^{(i)}}}{1 + e^{-net_n^{(i)}}} \]

(45)

The time derivative of TS-AF is so calculated as:

\[ f_n^{(i)}(net_n^{(i)}) = \frac{1}{2} (1 - (x_n^{(i)})^2) \]

(46)

- ENN based power controllers

The proposed ENN based power controller shown in Fig.6.a consist of four layers \([32]\): the IL, the HL, the CL, and the OL. The neurons in the CL known as memory units store the previous outputs of the hidden neurons that offer better learning efficiency. The inputs of ENN based active power controller are the tracking error \( \epsilon_s(k) = P^*(k)-P(k) \) and its derivative \( \epsilon_d(k) = \epsilon_s(k)-\epsilon_d(k-1) \) whereas, its output is the \( q \)-axis component of the control voltage vector \((V_{eq})\). Further, the inputs of the reactive power ENN controller are the error \( \epsilon_o(k) = Q^*(k)-Q(k) \) and the change of error \( \epsilon_d(k) = \epsilon_o(k)-\epsilon_d(k-1) \). While, the output is the \( d \)-axis component of the inverter voltage vector \((V_{eq})\). The TS-AF is used for the neurons of the HL and OL of the ENNs. The basic function of each layer is described as follows:

1) The output of each node in the IL is defined as:

\[ x_i^{(1)}(k) = f_{i}^{(1)}(net_{i}^{(1)}) = net_{i}^{(1)}, \quad i = 1,2 \]

(47)

\( k \) is the \( k \)-th iteration and \( net_{i}^{(1)} \) is the input of the \( i \)-th node.

2) The output of the Hidden layer’s neurons is:

\[ x_i^{(2)}(k) = f_{j}^{(2)}(net_{j}^{(2)}) = f_{j}^{(2)}(\sum_{r} w_{jr} x_r^{(3)}(k) + \sum_{l} w_{lj} x_l^{(1)}(k)) \]

(48)

Where \( x_i^{(2)} \) is the output of the \( j \)-th node in HL. \( w_{jr} \) are the connective weights from the input nodes to hidden nodes, \( x_r^{(3)}(k) \) is the output of the CL, \( w_{lj} \) are the connective weight from the hidden neurons to the context neurons, and \( f_{j}^{(2)} \) is the TS-AF in the HL.

3) The feedback from the HL to the CL input is described as:

\[ x_r^{(3)}(k) = x_l^{(2)}(k-1) \]

(49)

4) The output signal from the Output Layer is calculated as:

\[ x_o^{(4)}(k) = f_{o}^{(4)}(net_o^{(4)}) = f_{o}^{(4)}(\sum_{j} w_{oj} net_{j}^{(3)}(k)) \]

(50)

Where \( x_o^{(4)} \) is the network output, \( f_{o}^{(4)} \) is the TS-AF, and \( w_{oj} \) are the weights connection between the HL and the OL. The ENN weights are online adjusted based on the AI law (of Eq.44), by taking into account the Eq.46, as follows:

\[
\begin{align*}
\Delta w_{ij}(k) &= \frac{1}{2} \left[ 1 - (x_j^{(2)}(k))^2 \right] x_i^{(1)}(k) w_{ij} \Delta w_{ij} \text{ weights between IL and HL} \\
\Delta w_{ij}(k) &= \frac{1}{2} \left[ 1 - (x_j^{(2)}(k))^2 \right] x_i^{(2)}(k) w_{ij} \Delta w_{ij} \text{ weights between CL and HL (51)} \\
\Delta w_{ij}(k) &= -\frac{1}{2} \left[ 1 - (x_o^{(3)}(k))^2 \right] x_j^{(2)}(k) \Delta e_n \text{ weights between HL and OL} \\
\end{align*}
\]

The invariance condition \( S_P \epsilon_s(k).dS_P \epsilon_s(k)=0 \) that should be satisfied in the sliding mode is considered for the training algorithm of the ENN based power controller as suggested in [33]. Thus, the term \( S_P \epsilon_s(k).dS_P \epsilon_s(k) \) is used instead of the output error \( \epsilon_s(k) \) in the adaptation law of ENN of Eq.(51), where:

\[
\begin{align*}
S_P \epsilon_s(k) &= \lambda_S \epsilon_s(k) + d \epsilon_s(k) \\
\lambda_S \epsilon_s(k) &= S_P \epsilon_s(k) - S_P \epsilon_s(k-1) \quad \text{(52)}
\end{align*}
\]

Where \( S_P \epsilon_s \) and \( dS_P \epsilon_s \) are the sliding surface and its derivative for, respectively, the active and reactive powers \((P \text{ and } Q)\). \( \lambda_s \) is a positive constant. The control goal of the proposed ENNs is to drive the state variables \( P \) and \( Q \) to the sliding surfaces \( S_P \) and \( S_Q \) respectively, in finite time.

- FFNN based DC voltage controller

The three-layer FFNN \([31]\) described by Eq.53 controls the DC-bus voltage. The tracking error of the DC voltage \( \epsilon_v(k) = V_{dc}^*(k)-V_{dc}(k) \) and the previous error \( \epsilon_v(k-1) \) represent the inputs of the adopted FFNN.

\[
\begin{align*}
x_i^{(1)}(k) &= f_{i}^{(1)}(net_{i}^{(1)}) = net_{i}^{(1)} \\
x_i^{(2)}(k) &= f_{j}^{(2)}(net_{j}^{(2)}) = f_{j}^{(2)}(\sum_{r} w_{jr} x_r^{(3)}(k)) \\
x_i^{(3)}(k) &= f_{o}^{(3)}(net_o^{(3)}) = f_{o}^{(3)}(\sum_{j} w_{oj} x_j^{(2)}(k))
\end{align*}
\]

(53)

Where \( net_{i}^{(1)} \) is the \( i \)-th input of FFNN, \( x_i^{(2)}(k) \) is the \( i \)-th output of the IL, \( x_i^{(3)}(k) \) is the \( i \)-th output of the HL, \( net_{o}^{(3)} \) is the output of the input neuron, \( x_o^{(3)}(k) \) is the output of FFNN, \( w_{ij} \) means the weight between the \( i \)-th node of the IL and \( j \)-th node of the HL, \( w_{oj} \) is the weight connecting the \( j \)-th node of the HL to the OL, and \( f_{j}^{(2)}, f_{o}^{(3)} \) are the TS-AFs for the HL and the OL respectively. The control output signal of the FFNN is multiplied by the measured DC-bus voltage to determine the active power reference \( P^*(k) \). As depicted in Fig.6.b, the FFNN weights are online adapted according to the AI law using the following:

\[
\begin{align*}
\Delta w_{ij}(k) &= \frac{1}{2} \left[ 1 - (x_j^{(2)}(k))^2 \right] x_i^{(1)}(k) w_{ij} \Delta w_{ij} \text{ weights between IL and HL} \\
\Delta w_{ij}(k) &= -\frac{1}{2} \left[ 1 - (x_o^{(3)}(k))^2 \right] x_j^{(2)}(k) \Delta e_n \text{ weights between HL and OL} \\
\end{align*}
\]

(54)

The error \( \epsilon_s \) between the desired and estimated output, in Eq.54, is replaced by the term \( S_v(k)+dS_v(k) \) such that:

\[
\begin{align*}
S_v(k) &= \lambda \epsilon_s(k) + d \epsilon_s(k) \\
dS_v(k) &= S_v(k) - S_v(k-1) \quad \text{(55)}
\end{align*}
\]

Where \( S_v \) and \( dS_v \) are, respectively, the sliding surface and its derivative for the DC-link voltage control.

F. Fuzzy Logic based Power Management System

A centralized PMS is used in order to minimize the power flow from the electric grid. For several conditions of power generation and demand, it imposes the power references for the power converters interfacing the SOFC and BESS. The
SOC of BESS should be maintained in secure range \([SOC_{\text{min}} - SOC_{\text{max}}]\). The power supervision process begins from the calculation of the net power value \(P_{\text{net}}\):\[
P_{\text{net}} = P_{\text{RES}} - P_{\text{L}} = (P_{\text{pv}} + P_{\text{WT}}) - (P_{\text{Lac}} + P_{\text{Ldc}}) \quad (56)
\]

Where \(P_{\text{RES}}\) is the power produced by the RESs, \(P_{\text{L}}\) is the total load demand, \(P_{\text{pv}}\) is the power produced by the PV source, \(P_{\text{WT}}\) is the power provided by the WT, \(P_{\text{Lac}}\) and \(P_{\text{Ldc}}\) are the DC and AC loads demand. The FES injects power to the electric grid only when the renewable power generation exceeds the loads demand and the BESS is fully charged \((SOC > SOC_{\text{max}})\). If the load demand is greater than the available RESs power, the SOFC and the BESS contribute to cover the energy shortage. In the case where \(SOC < SOC_{\text{min}}\), the SOFC feeds the loads and guarantees the charge of the BESS. Vice versa, if \(SOC > SOC_{\text{min}}\) and the power demand exceeds the SOFC rated power, the BESS starts to discharge in order to feed the loads. Otherwise, the needed power comes from the electric grid, if the demand surpasses the rated power of the MG. A Mamdani inference system [34] based fuzzy logic controller calculates the power references \(P_{\text{fc}}^*\) and \(P_{\text{b}}^*\) for the local controllers of FC and BESS. The PMS has two inputs and two outputs: the inputs are \(P_{\text{net}}\) and \(SOC\), while the outputs are the set points for the BESS and the SOFC controllers. The fuzzy rule table of the PMS, proposed to decide the power setpoints \(P_{\text{fc}}^*\) and \(P_{\text{b}}^*\), are given in Table I.

<table>
<thead>
<tr>
<th>(P_{\text{net}}) SOC</th>
<th>NM</th>
<th>NS</th>
<th>PS</th>
<th>PM</th>
<th>PB</th>
<th>PB+</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>ZE/-</td>
<td>ZE/-</td>
<td>PB/-</td>
<td>PS/P</td>
<td>PB/PB</td>
<td>PB/PB</td>
</tr>
<tr>
<td>M</td>
<td>NB/-</td>
<td>NS/-</td>
<td>ZE/PS</td>
<td>ZE/P</td>
<td>PS/PB</td>
<td>PB/PB</td>
</tr>
<tr>
<td>L</td>
<td>NB/-</td>
<td>NS/-</td>
<td>NB/P</td>
<td>NS/P</td>
<td>NS/P</td>
<td>NS/P</td>
</tr>
</tbody>
</table>

Linguistic terms assigned to the fuzzy sets mean: Negative Medium (NM), Negative Small (NS), Zero (ZE), Positive Small (PS), Positive Medium (PM), Positive Big (PB), and Positive very Big (PB+). H, L, M mean High, Low, and Medium membership functions, respectively.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_s)</td>
<td>Stator resistance</td>
<td>0.00829</td>
</tr>
<tr>
<td>(L_d, L_q)</td>
<td>d and q stator inductance</td>
<td>0.174mH</td>
</tr>
<tr>
<td>(\phi)</td>
<td>Permanent magnet flux</td>
<td>0.071wb</td>
</tr>
<tr>
<td>p</td>
<td>Number of pole pairs</td>
<td>6 pair</td>
</tr>
<tr>
<td>J</td>
<td>System Inertia</td>
<td>0.089kg.m(^2)</td>
</tr>
<tr>
<td>(V_{\text{OC}})</td>
<td>Open circuit voltage</td>
<td>42.1V</td>
</tr>
<tr>
<td>(I_{\text{SC}})</td>
<td>Short circuit current</td>
<td>3.87A</td>
</tr>
<tr>
<td>(V_{\text{MPP}})</td>
<td>MPP voltage</td>
<td>33.7V</td>
</tr>
<tr>
<td>(I_{\text{MPP}})</td>
<td>MPP current</td>
<td>3.56A</td>
</tr>
<tr>
<td>(K)</td>
<td>Boltzmann constant</td>
<td>1.38x10(^{-23})J/K</td>
</tr>
<tr>
<td>(e)</td>
<td>Electron charge</td>
<td>1.6x10(^{-19})C</td>
</tr>
<tr>
<td>(Q)</td>
<td>Rated capacity</td>
<td>20 Ah</td>
</tr>
<tr>
<td>(E_0)</td>
<td>Nominal voltage</td>
<td>240 V</td>
</tr>
<tr>
<td>(R_i)</td>
<td>Internal Resistance</td>
<td>0.12 (\Omega)</td>
</tr>
</tbody>
</table>

IV. SIMULATION RESULTS

In order to demonstrate the effectiveness of the proposed control structure, the operation of the MG has been tested in the Matlab/Simulink environment for different climatic conditions and loads demand. The main simulation parameters are listed in Table II. The DC loads, which are interfaced with the DC-microgrid through power electronic converters, behave as Constant Power Loads (CPLs) [35].

A. Test under variable irradiance and wind speed

First of all, the investigated MG is tested for variable irradiation level and changing wind speed in order to check the tracking capability of the proposed MPPT controllers. The DC and AC loads demand are fixed to 5kW and 20kW, respectively. The rapid and gradual change in the irradiation level is depicted in Fig.7.a. The variation of the current and voltage at the output of PV source are shown in Fig.7.b and Fig.7.c. The PV reference voltage provided at the output of the SN-RBFN is depicted in Fig.7.d. Further, for the comparison purpose, the Fig.7.e illustrates the PV output power obtained using both the adopted SN-RBFN controller and the standard IncCond algorithm. It is clear that the adopted neural tracker for PV source performs very well for changing solar irradiation. The correct MPP is rapidly reached for each irradiation level thanks to the online learning process of the SN-RBFN. The convergence time of the SN-RBFN for the insolation level of 1kW/m\(^2\) is about 38ms, which is less than the time achieved with the IncCond algorithm (about 92ms). Moreover, as can be seen from Fig.7.e, the power oscillations around the MPP in the steady state are considerably reduced with the SN-RBFN in comparison with the IncCond method. The static power error of the SN-RBFN is (about 0.305W) lower than the static error of the IncCond method (0.887W). When a change in the solar irradiance happens, the proposed PV controller converges rapidly and re-tracks accurately the new MPP as presented in Fig 7.b and 7.c. At the beginning of each step change in irradiance, the online learning process of the SN-RBFN restarts to recalculate the new optimal parameters \((a_0, c_1, b)\) that justify the presence of small transient ripples in the voltage reference as shown in Fig7.d.

![Fig. 7.](image-url)

- a) Solar irradiance, b) PV current, c) PV voltage, d) SN-RBFN output voltage reference e) PV output power (T=25°C).
In the same test case, the wind speed changes from 12m/s to 10m/s at the instant 0.25s then increases to 14m/s at 0.5s. The obtained results with the applied DPC are presented in Fig. 8. As shown in Fig.8.a, the ADALINE based speed controller outperforms the classical PI controller and offers a shorter response time (about 38ms), an minimal overshoot and closely zero steady-state error during each step change in wind speed. By applying the adequate stator voltage vector, the correct control of the generator torque and d-axis current component \(I_{sd}\) is assured for different wind conditions as depicted in Fig.8.b. A fast transient response of the electromagnetic torque is obtained with good steady state characteristic. Further, due to the fixed switching frequency, the torque and flux ripples are considerably reduced as shown in Fig.8.b.c. The FFNN ensures the stabilization of the DC-bus voltage at the desired setpoint as depicted in Fig.8.d regardless of the climatic conditions.

![Graph](image)

**B. Test for variable loads demand**

A second test was performed in order to validate the proposed control system under varying loads demand. In this case, the power demand of the DC equivalent load \(P_{ldc}\) changes from 5kW to 8kW at 0.25s then increases to 10kW at 0.5s. Further, the unbalanced ohmic-inductive AC load demand \(P_{lac},Q_{lac}\) varies from \(39kW,0kVAR\) to \(53kW,0kVAR\) at \(t=0.25s\), then changes at \(t=0.5s\) to \(1kW,15kVAR\) and finally varies to \(24kW,7kVAR\) at the instant \(t=0.75s\) as depicted in Fig.9.a and 9.d. As expected the proposed control scheme performs well and reacts dynamically to the change of load conditions without the need to a priori knowledge about the controlled system. The weights of the proposed neuro-controllers are continually adapted during the operation of the system. The decoupled control of the active and reactive powers is achieved based on the recurrent ENNs controllers as shown in Fig.9.b and Fig.9.d. With reference to the behavior of the proposed fuzzy based PMS, Fig.9.c shows that, the power set-points for the local controllers of both SOFC and BESS are tightly determined according to the availability of the power generated by the RESs. While the RESs with the SOFC stack cannot meet the loads request in the period \([0.0.25s]\), the BESS is activated to feed the energy lack as presented in Fig9.b and Fig9.c. On the contrary, when the power of the MG is not enough in the time interval \([0.25s-0.5s]\), the power deficit is covered by the electric grid, while both FC and BESS are switched on to generate their rated powers as depicted in Fig9.b and Fig9.c. When the total load demand \(P_L\) does not exceed the available RESs power in the period \([0.5s-0.75s]\), the BESS operates in the charge mode and the inverter injects the energy excess into the electric grid. In the period \([0.75s-1s]\), the SOFC stack responds to the load demand where, the BESS is set in the idle mode as shown in Fig9.c. The ADALINE based controllers developed for the SOFC and BESS ensure an accurate following of the references delivered from the PMS as shown in Fig.9.c. The Fig.9.d shows the capability of the inverter to compensate the reactive power of the AC load. To verify the performance of the proposed fuzzy PMS, a comparison with the conventional one based on states is completed. The classical PMS is established based on deterministic supervision rules with the same strategy of power managing of the proposed PMS. The Fig.10 shows the power references for both FC and BESS using the PMS based on states and the supervisory based on FL.

A second case study was performed and depicted in Fig.11, where the DC load demand \(P_{ldc} = 20kW\) is greater than the AC side demand \(P_{lac} = 5kW \text{ and } Q_{lac} = 0kVAR\) and the available RESs power is insufficient \(G = 0.1kW/m^2, V_w = 8m/s\), where initial SOC = 30\%. In this case, the FEC operates as rectifier and provides the power deficit form the electric grid to the DC load as shown in Fig11.b. The DC link voltage is perfectly maintained in tolerable range as depicted in Fig11.a. It can be noticed that the MPP of PV source is reached using the SN-RBFN after 0.31s as shown in Fig11.b. The obtained results show the ability of the neural based VF-DPC scheme to control the FEC with a bidirectional flow of active power.

**C. Test for Perturbed grid conditions**

This test was performed in order to prove the robustness of the proposed control system against faults in the electric grid. A three-phase voltage sag (70% of voltage RMS) occurs during the period \([0.3s, 0.45s]\) when the climatic conditions are stable. The initial SOC value is set 30\%. As shown in Fig12.a, the power needed to feed the loads is provided by the 11 RESs. During the voltage dip period, the active power surplus is injected into the grid. In this case, the central PMS commands are to turn off the SOFC stack and to charge the BESS. Thus, the renewable generation surplus is used to charge the BESS whereas, the FC power is constantly zero as depicted in Fig12.b. As can be seen from Fig 12.c, the DC-link voltage is maintained stable at the desired reference with reduced transient fluctuations. Further, the phase current waveforms shown in Fig.12.d are sinusoidal and balanced irrespective of grid fault. The negative sequences of the inverter output current in the \(aβ\) coordinates, shown in Fig.12.e, demonstrate the symmetry of the FEC output current.
then decreases at 0.5s to 23°C. The Fig 13.b illustrates the wind speed profile. According to [36], the wind speed is calculated using the following model:

\[ V_w = A_0 + 0.6 \sin(\omega t) + 0.6 \sin(3.5 \omega t) + 0.3 \sin(12.35 \omega t) + 0.06 \sin(35 \omega t) \]  

(57)

In our case, the average speed \( A_0 = 11.5 \text{m/s} \), \( \omega = 2\pi/\text{tw} \) and \( \text{tw} = 2.5\text{s} \). Furthermore, the DC power demand is decreased from \( P_{\text{Load}} = 9\text{kW} \) to \( P_{\text{Load}} = 4\text{kW} \) at the instant 0.5s. The active and reactive power demand of the ohmic-capacitive AC load are varied, respectively, from \( (P_{\text{Load}} = 26\text{kW}, Q_{\text{Load}} = -15\text{kVAR}) \) to \( (P_{\text{Load}} = 44\text{kW}, Q_{\text{Load}} = -38\text{kVAR}) \) at \( t=0.35s \) then change to the initial values at the instant 0.705s.

Fig. 9. a) AC and DC loads, b) inverter, and grid Powers c) SOFC and BESS powers d) Inverter, grid and AC load reactive Powers \( (V_w = 14\text{m/s}, T = 25°C, G = 1\text{kW/m}^2\text{, initial SOC = 70%}). \)

Fig. 10. Comparison of the PMS based FL and PMS based states.

Fig. 11. a) DC bus voltage, b) Total load, microgrid, and grid powers.

D. Test for variable temperature and noisy wind speed

This test aims to verify the stability of the proposed control method under changing temperature and noisy wind speed. At constant irradiance \( (G=1\text{kW/m}^2\text{ and initial SOC=90%}) \), the temperature varies at the instant 0.25s from 27°C to 25°C and

With reference to the Fig.13.a, the proposed SN-RBFN exhibits satisfactory tracking performance and offer a less static PV voltage oscillations than the IncCond algorithm. The
response time of the SN-RBFN is less (about 35ms) than that of the IncCond controller (70ms). As can be seen from Fig.13.c, the ADALINE based speed controller ensures good control performances for a noisy wind speed guarantees the response to the AC loads demand of active and reactive power as shown in Fig.13.f with better control performances than the classical VF-DPC based PI regulators: With the ENN based active power control, a shorter settling time and more smooth static response is obtained. Whereas, a more precise tracking of the reactive power setpoint is achieved with the adopted ENN.

V. CONCLUSION

This work is on the design and validation of an online trained neural network based control system for a grid-connected hybrid AC/DC microgrid.

A number of artificial intelligence based controllers have been developed to follow the maximum power point of the renewable energy sources available in the microgrid, to control the power flow between the front-end converter and the electric grid, and to minimize the purchased energy optimizing the utilization of the battery energy storage system.

The performance of the proposed control system has been tested for different situations: variable climate conditions, variable loads demand, and perturbed grid conditions.

The obtained results show the possibility to control complex non-linear systems without the availability of precise models. Moreover, the proposed techniques are flexible, adaptable, require low computational costs, and are easy to implement in real-time applications.

The simulation runned for a number of different conditions of power generation and demand demonstrate the effectiveness, robustness and self-adaptation ability of the proposed control system.

As perspective of this paper, the developed artificial intelligence based controllers will be implemented on a Field Programmable Gate Array (FPGA) platform and tested under real conditions.

VI. REFERENCES


**VII. BIOGRAPHIES**

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