MetaMesh: a Hierarchical Computational Model for Design and Fabrication of Biomimetic Armor Surfaces
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KEYWORDS
Biomimetics, bio-inspired design, computational design, hierarchical computation, adaptation, mesh data structure, multi-functional, natural exoskeletons

HIGHLIGHTS
• MetaMesh is a hierarchical computational construct to generate articulated armored surfaces
• The ancient armored fish \textit{Polypterus senegalus} provides source of bio-inspiration
• Local, regional and global levels of organization embed functional differentiation
• Articulation of scale units is preserved by neighborhood morphing techniques
• The model is adaptable to a wide array of complex hosting surfaces

GRAPHICAL ABSTRACT

ABSTRACT
Many exoskeletons exhibit multifunctional performance by combining protection from rigid ceramic components with flexibility through articulated interfaces. Structure-to-function relationships of these natural bioarmors have been studied extensively, and initial development of structural (load-bearing) bioinspired armor materials, most often nacre-mimetic laminated composites, has been conducted. However, the translation of segmented and articulated armor to bioinspired surfaces and applications requires new computational constructs. We propose a novel hierarchical computational model, MetaMesh, that adapts a segmented fish scale armor system to fit complex “host surfaces.” We define a “host” surface as the overall geometrical form on top of which the scale units are computed. MetaMesh operates in three levels of resolution: (i) locally - to construct unit geometries based on shape parameters of scales as identified and characterized in the \textit{Polypterus senegalus} exoskeleton, (ii) regionally - to encode articulated connection guides that adapt units with their neighbors according to directional schema in the mesh, and (iii) globally - to generatively extend the unit assembly over arbitrarily curved surfaces through global mesh optimization using a functional coefficient gradient. Simulation results provide the basis for further physiological and kinetic development. This study provides a methodology for the generation of biomimetic protective surfaces using segmented, articulated components that maintain mobility alongside full body coverage.
1. INTRODUCTION

Structural materials in nature achieve diverse functions such as toughness, flexibility and strength, through spatial variation in material properties and morphometry across organizational hierarchies with precise interfacial control [1-2]. Biologically inspired engineering, or the translation of design schema in nature, being chemical, physical, genetic, or geometric, to synthetic systems requires complex models that both capture the intricacies of biological models and adapt their multi-scale design principles to new operative constraints. The process of mapping functional requirements between design solutions presents several theoretical and technical challenges to ensure continuity and coherence of all components. With the advent of high resolution materials characterization methods, powerful computational simulation capabilities, and increasingly precise digital fabrication technologies, it is now becoming possible to develop novel multifunctional structures with intricate, interactive, and hierarchical design strategies inspired by biological models.

The study of biological armor systems is an emerging field [3-7] with recent initial development of structural (load-bearing) bioinspired armor materials, most often nacre-mimetic [8]. However, the design and manufacture of a bioinspired exoskeleton including salient local-regional-global hierarchical features have yet to be realized. In this paper, we present a computational design methodology that combines scientific analytical methods and computational form finding tools to generate a flexible protective surface based on an armored fish exoskeleton. Our biological model is the exoskeleton of the ancient fish, Polypterus senegalus. Its armor (Figure 1a) is composed of articulated, mineralized scales that act as a protective medium from predatory threats while also allowing biomechanical flexibility in axial bending and torsion [3, 9-13]. The functional framework of the fish scale jacket (Figure 1b) uses spatial variation of unit morphometry (size and shape) and their arrangement into semi-helical rings to balance the two seemingly contradictory functions of full coverage and mobility. Our prior research has begun to explore the geometric design rules underpinning the functional framework [14-16]. One of our previous models constructed a parametric definition of single scale geometries and an associative model to generate an array of homogeneous scales using computer-aided design (CAD) software for multi-material 3D printing of a flexible, flat surface [14]. Another model morphed scale-based geometries along a sequence to determine dimensional parameters that can be varied while maintaining connectivity within a single direction [15].

Our goal is to create a generative computational design framework for functionally graded structures with tunable local performance. These local performances can adapt to any given hosting mesh surface by emulating the design principles observed in the flexible fish exoskeleton. We distill the geometric design rules underlying the P. senegalus exoskeleton across multiple length scales (local, regional, and global). We then present the MetaMesh model that translates these design rules hierarchically to a synthetic system using an efficient framework linking experimental analytical methods (X-ray micro-computed tomography and morphometric analysis) with advanced computational geometry techniques (custom data structures for polygon mesh processing and component adaptation). MetaMesh operates in three levels of resolution: (i) locally - to construct unit geometries based on shape parameters of scales in the P. senegalus exoskeleton, (ii) regionally - to encode articulated connection guides that adapt units with their neighbors according to directional schema in the mesh, and (iii) globally - to generatively extend the unit assembly over arbitrarily curved surfaces through global mesh optimization using a functional coefficient gradient. Unlike component-based parametric techniques that focus on the packed placement of self-similar units over surfaces [17], MetaMesh incorporates complex connectivity and overlap of the units to enable articulation with neighbors. In addition, through functional variation in unit shape, it allows control over regional connectivity and interlocking between units. We demonstrate the MetaMesh model’s potential with its application to a human body mesh surface and further discuss the model’s advantages and limitations. This computational adaptation of an articulated, segmented, flexible surface serves as a proof-of-concept model for enhanced biomimetic structures in various fields such as transportation (e.g. ground, air, water, or space), architecture (e.g. building skins or canopies), sports and military (e.g. personal protection), and consumer products (e.g. packaging) [12, 14].

2. MATERIALS AND METHODS

2.1 X-ray Micro-computed Tomography (µCT)

Eleven scales were excised from a deceased P. senegalus specimen (every 10th scale across a row on the left side of the body) and scanned via x-ray micro-computed tomography (µCT; Viva CT40, Scanco Medical AG,
Switzerland) operated at 45kV and 177µA. The microtomographic data was reconstructed using bilinear and inter-plane interpolation algorithms into polygonal meshes using an interactive medical imaging software (MIMICS®, Materialise, Belgium) to generate digital 3D objects of the scales in stereolithography (STL) format. Further processing was executed in Rhino3D (RHINOCEROS®, Robert McNeel and Associates, USA) to remove noise and internal porosity.

2.2 Morphometric Analysis

Geometric analysis measured variation in scale shape and served as a basis for the computational model. The coordinates of twenty landmarks defining the outline of the scale including all geometrical features were extracted from the 3D STL objects using a custom Visual Basic code programmed in the Rhino3D environment. These landmark coordinates were subjected to translation, rotation, and scaling relative to the centroid. Magnitudes of relative geometric parameters were calculated based on the coordinates. The volume of the scale was measured from the STL file in Rhino3D.

2.3 Computational Modeling

The computational framework defining the MetaMesh data structure (local scale geometric definition, regional directionality patterns, and global functional gradient application) was implemented in C# on top of the design platform in Rhino3D. The mesh optimization process was implemented in Java (Eclipse IDE, © 2013 The Eclipse Foundation) and deployed within a customized applet.

2.4 Multi-material 3D Printing

The closed-surface multi-material prototypes were designed using parametric CAD software (SOLIDWORKS®, Dassault Systèmes SolidWorks Corp., France) as described by Reichert et al. for a flat surface [14]. The components of the prototype were exported as separate STL files per material component and fabricated using multi-material 3D printing (using digital materials from OBJET Connex500™) with 30 µm resolution in the digital mode. Rigid components were printed with VeroWhite (Objet FullCure® 830) and compliant components were printed with TangoPlus (Objet FullCure® 930).

3. RESULTS

3.1 Biological Exoskeleton Design Rules

The geometric design rules in the P. senegalus exoskeleton are characterized across three levels of resolution: local, regional, and global. The individual scales have varying geometries, are articulated with each other to allow flexibility alongside full body coverage, and are organized in a long-range surface over the entire fish body. These design components are formed during the organism’s growth and are thus inseparable; however, we distinguish amongst these levels of resolution for ease of translation using the computational model.

3.1.1 Local

The local level of organization relates to a single scale, its anatomy, and its geometric variation. The scales of the organism are highly mineralized and display a multilayered internal composite structure with a consistent material composition throughout the exoskeleton [3,12,13]. The geometrical features of the scales (Figure 2a, left) include: a protruding peg (P) and a corresponding socket (S) that articulates neighboring scales within a single column of scales (paraserially) and constrains relative motion; the anterior process (AP), a large extension that overlaps with the scales in the next column (interserially) and enables scales to slide relative to each other; and the axial ridge (AR), a protrusion on the underside of the scale that connects the scale to the underlying skin. Based on line lengths and angles between features on the scale (Figure 2a, left), eight parameters were calculated for morphometric analysis of the fish scales (Figure 2a, right): relative length peg to scale (PSL), shape aspect ratio as the length of peg-and-socket axis divided by scale width (SR), bounding box size (E), interserial overlap with the adjacent scale in the next column along v-axis (IO), paraserial overlap with the adjacent scale in the same column along u-axis (PO), relative edge degrees (ANG), anterior process length (APL), and volume (VOL).
The scale geometry varies gradually relative to its position in the exoskeleton [9], as illustrated in the digitally-reconstructed µCT images of subset of 11 *P. senegalus* scales lying in the same row from head to tail (labeled by their column position in the exoskeleton, C1-50) in Figure 2b. Values for the eight shape parameters for these scales are tabulated and plotted as normalized quantities in Figure 2b. The scales exhibit a general trend of feature reduction from head to tail. For instance, in the tail region, variants C45-C50 have smaller magnitudes of the two articulating joints (PSL, IO) compared to front region variants C1-10. The PSL diminishes gradually from 0.22 to 0.03 in scales from head to tail. In the front region, the peg-and-socket joint plays a functional role in stiffening the column of scales, while in the tail region, the lack of peg-and-socket allows scales within a column to move freely relative to each other. The IO between columns also decreases from 0.28 to 0.13, thus compromising the relative sliding between columns. These parameters further relate to regional connectivity between columns as discussed in the next sections.

3.1.2 Regional

The regional level of organization describes the interconnectivity of fish scales in the exoskeleton and the correlation between local shape variation and regional functionality of the system. Two articulating joint structures define the standard unit schema between a single scale and its neighbors as shown in schematic views in Figure 3a: the peg-and-socket joint connects scales down a column (paraserially) while the overlap joint allows interscale sliding between columns (interserially). The geometry of these joints further defines the rotational degrees of freedom, e.g. bending and twisting, that scales have in moving relative to each other (Figure 3b). The overlap joint allows bending, sliding, and twisting, while peg and socket joint allows only limited bending and rotation around its axis [9]. In the construction of the computational model in Section 3.2, we define the axis of peg-and-socket joints as the *u*-direction (paraserial) and the axis of the overlap joint as *v*-direction (interserial); these are two consistently identifiable directions between any set of adjacent scales.

Two fibrous, organic components hold the scales together in the armor: the *stratum compactum* and *Sharpey’s fibers*, illustrated in Figure 3c. The *stratum compactum* is a crisscrossed, layered tissue composed of collagenous fibers that attach the scales to the underlying skin [9]. The fibers are aligned along the paraserial and interserial directions in alternating layers. The *Sharpey’s fibers* are short fibers that connect the peg and socket of adjacent scales [9]. These fibers support and align the peg and socket joint, and allow the paraserial column of scales to withstand compressive and tensile stresses.

The degrees of freedom in relative motion are dependent on the geometric parameters of the scales. Figure 4 demonstrates the difference in ranges of motion between two shape variants: a head region scale and a tail region scale. The head region scale (Figure 4a-d) is bigger and possesses more pronounced shape features: the well-pronounced peg and socket as well as the paraserial overlap restrict rotation between scales within a single column, while the large anterior process enables relative sliding resulting in significant changes in overlap between scales (42-110% [9]) as the exoskeleton bends to extreme curvatures. This variant shows full contact between the scales with additional overlap in peg-and-socket direction and requires additional bending (Figure 4a) or translation (Figure 4b) to rotate around the peg axis. In contrast, in the tail region scale (Figure 4c-h), the anterior process is smaller and has a simpler rhomboid shape, which relaxes the paraserial constraints while still allowing interserial sliding to accommodate the rapid undulation of the tail in steady-state swimming.

3.1.3 Global

The global level of organization relates the long-range assembly of the scales across the body of the fish to its kinetic motion. Semi-helical columns of ‘standard unit’ scales are aligned with their peg and socket joint running top to bottom, and overlap running from head to tail (Figure 5a). These columns of scales are symmetric on the right and left sides of the fish body, and are connected by top and bottom midlines composed of units with a specialized geometry. Two types of specialized units exist in the fish; double-peg unit on the top line and double socket on the bottom line (Figure 5b). Lines of symmetry on the top and bottom of fish trunk possess specialized units (orange) with double pegs and double sockets that receive columns on both sides (blue). The scale shapes and joint configurations are tailored to the varying radius of curvature throughout the structural ring (Figure 5c-e).
The orientation of scales within the assembly exoskeleton further contributes to functional variation within the armor. The structural rings and underlying fibrous tissue have an oblique orientation to the main axis of the trunk, which ranges from 60° in the front region to 45° in the back region [9] as shown in Figure 6a. The front 60° orientation is optimal for extreme curvatures in helical arrangement, as found in eels and worms [18], while the rigid peg-and-socket joint sustains the helical component of the torsional strain [9]. The back region 45° orientation is optimal for restricting torsion in steady-state swimming [19]. Furthermore, the angle between the edges of the scale (ANG) also decreases gradually from 87°-60°, from head to tail, showing that the directionality of the paraserial and interserial axes are regionally adapted to the global kinetic motion of the fish. Local scale geometry further contributes to the functional variation of the armor. A functional coefficient (FC) was calculated as the average value of the normalized geometric parameters PSL, IO, PI, and AP. The FC is mapped onto the fish exoskeleton in Figure 6a. The FC indicates how developed the connective interfaces are between adjacent scales, i.e. how constrained the peg and socket joint is along the paraserial direction compared with overlap sliding along the interserial direction, ranging from 0 (maximum protection) to 1 (maximum flexibility). As a consequence of the local scale geometry and regional orientation, the long range assembly of scales is capable of achieving high radii of curvature throughout the exoskeleton, e.g. in the fast-start escape response depicted in Figure 6b.

3.2 MetaMesh: Hierarchical Computational Model

Our hierarchical computational model, MetaMesh, unpacks the organism-specific design principles and applies them, in a generative way, to a different host surface with new functional specifications. MetaMesh creates and maintains consistent neighborhood relationships for the three-dimensional articulated surfaces of units on a quadrilateral polygonal mesh. The mesh data structure tailored for this model is designed to meet specific topological, algorithmic, and data access requirements.

The topology of our structure is a high-resolution polygonal regular mesh of quads with boundaries. The three components of a polygon mesh (vertices, edges, or faces) determine the connectivity between the mesh elements [20]. To ensure smooth connectivity between component features, each vertex holds one scale unit and each face shares the information of four scale geometries. We specify meshes with boundaries, defined by edges incident to only one face [21] to include neckline and sleeve openings. The paraserial and interserial axes in the fish exoskeleton are translated onto the u- and v- directions of the parametric surface subdivision.

Algorithmic requirements operate on unit orientation and connectivity along u- and v- directions, as well as on unit geometry adaptation to new vertex positions through mesh optimization. Furthermore, our model takes into account functional gradients of protection and flexibility mapped on the human body. In order to preserve smooth continuity of the functional changes over the host surface, the model associates extra geometry to the vertices, edges, and faces of the mesh to share geometrical data with neighboring elements. To do this, we used a finite set of vertex indices (V), a table of 3D vertex coordinates \( X = \{ x_i : i \in V \} \), and a set of polygon faces (F), in which a face \( f = (i_1...i_n) \) is a sequence of non-repeating vertex indices [22].

We further impose access requirements to the sets of data included in the model. The data sets for vertices, edges, and faces are accessible by enumeration of all elements and the oriented transversal of face edges. Given an edge, we are able to access its starting and end vertices. Given a vertex, at least one attached face or edge must be accessible while all other elements in the neighborhood of the vertex (i.e. incident faces, edges, or neighboring vertices) can be enumerated [23].

Our hierarchical computational model, MetaMesh, is designed to meet these requirements at three organizational levels following the geometric rules of assembly: (i) local definition of a standard unit and construction of different unit geometries in association with their neighbors, (ii) regional application of directional patterns and functional gradients that define the locations of different units, and (iii) global optimization of the host mesh to reposition vertices that affect local adaptation of unit shapes.

3.2.1 Local
The local level of organization captures the standard scale unit (S) as a building block by taking into account the features of its neighbors and the underlying host mesh geometry (Figure 7). Each scale unit is centered on top of one mesh vertex and constructed through a set of controllable parameters (Figure 7a). Since each vertex has an associated unit, its geometry can adapt to the host surface curvature. The local set of information per mesh face contains shared data between four units, which takes into account the features of neighboring scales. Each vertex stores the information of four parameters that will affect its associated unit schema in two different directions. Along the u-direction (paraserial), the unit geometry is influenced by the PSL, PO, and APL parameters. Along the v-direction (interserial), the unit geometry and lateral scale superposition are influenced by IO.

Specific parametric dimensions are calculated to determine unit features and their position on the quad in order to unite the underlying mesh with the geometrical parameters and functional requirements of the host surface, described further in Section 3.3.2. A particular vertex is defined as $V_d(i,j)$, and its four neighbor vertices are defined as $V_1(u+1,v), V_2(u-1,v), V_3(u,v+1), V_4(u,v-1)$ as shown in Figure 7a. The midpoints of their edges are then defined as $m_{u,0}, m_{0,v}, m_{0,3}, m_{2,0}$. Figure 7b shows how the unit is constructed from four connecting surfaces for each adjacent mesh quad (blue) and resulting cross-shaped contact surface centered in the vertex (orange). The unit lengths are calculated as shown in the table below and then mapped onto the mesh quads using a unit square bilinear interpolation algorithm [24], as shown in Figure 7c, where an unknown function $f$ at point $X(u,v)$ is found with respect to a unit quad of points $P_1(1,0), P_2(1,1), P_3(1,0)$ and $P_4(0,0)$. We perform a linear interpolation between $P_1$ and $P_2$ resulting in point $A(u,v)$ and another linear interpolation between point $P_3$ and $P_4$ resulting in point $B(u,v)$ providing an estimate for $f(u,v): f(u,v)=f_0,01-11u-v+f1,0u1-v+f1,0u+f1,1u$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scale Width</td>
<td>$L8 = m_{4,0} - m_{0,3}$</td>
</tr>
<tr>
<td>AP Length</td>
<td>$L6 = m_{2,0} - m_{0,1}$</td>
</tr>
<tr>
<td>PO Length</td>
<td>$L7 = APL / L6.$</td>
</tr>
<tr>
<td>Overall Length</td>
<td>$L2 = L1 + L5 + L6$, where $L1 = L2 * PSL$ and $L5 = L2 * PO$</td>
</tr>
<tr>
<td>Overall Width</td>
<td>$L3 = L8 + L4$, where $L4 = L3 * IO$,</td>
</tr>
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<td></td>
<td>$= L8 / (1-IO)$</td>
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The u- and v-directions act as guides for the construction of the peg-socket and overlap connections in a unit. In MetaMesh computation each side of a quad can host either u- or v-direction and this allows definition of new types of specialized units in addition to the ones found in the fish (e.g. A, B, C in Figure 7d). The double-peg and double-socket units in the top and bottom midlines in the fish (e.g. D, E in Figure 7d) are defined as variations from the standard scale through the encoded u- and v-directions. This method of specialized units enabling polygonal mesh connectivity is similar to the stitch mesh method developed by Yuksel et al. for yarn patterns in 2.5D, where course and wale edges have an extra layer of information to define the connectivity of the yarn elements at the mesh edges [25].

3.2.2 Regional

The regional level of organization orients mesh regions against the hosting surface. A mesh is defined as “orientable” if all faces (i.e. normal vectors for all polygons) point consistently to the same side of the mesh. The information encoded in our u- and v-directions does not affect the orientability of the mesh, but tailors edge directionality as extra regional data in the data structure. Figure 8 illustrates the directionality analysis of a human shoulder mesh in response to an estimated biomechanical logic. The u- and v-directions (Figure 8a) are applied to each face of the shoulder mesh (Figure 8b). The complexity of the host in contrast to an idealized tube mesh representing the fish body requires the emergence of more specialized units than the ones present in the $P. senegalus$. The locations of these specialized units that have emerged through the implementation of our MetaMesh model to the complex mesh of human body in contrast to a tube mesh representing the fish body are identified in Figure 8b,c.

3.2.3 Global

The global level of organization applies optimization strategies to the hosting mesh and subsequently automates the adaptation of regional connectivity patterns and local unit shapes. To integrate functional differentiation that exists in the biological system, we assign a FC map to the mesh data structure to modulate the unit geometry of
biological armor into generative computation through local shape construction, regional connectivity pattern, and surface, e.g. a human shoulder.

4. Discussion

The MetaMesh model is a generative computational design framework for translating design principles observed in the flexible fish exoskeleton of P. senegalus into functionally graded structures adapted to a new host surface, e.g. a human shoulder. Figure 11 summarizes the main steps in translational process from analysis of the biological armor into generative computation through local shape construction, regional connectivity pattern, and
global optimization and adaptation to overall geometry. MetaMesh attempts to solve many challenges heretofore unaddressed in architectural geometric design and flexible protective structures by developing bioinspired functional designs with components operating at multiple length scales.

Parametric Component Population (PCP) is a common method to adapt discrete geometrical components to large-scale complex shapes [26]. The host surface is normally structured as a polygonal mesh of quadrilateral faces or as a NURBS surface subdivided into u,v directions. The component’s geometry is described through a parametric model and then repetitively embedded as discretized shapes on the host surface in two steps: component enclosure in an axis-aligned bounding box, and translation of the bottom-face vertex to every vertex of the mesh face in order to parametrically fill the space of the host mesh. Despite its fast distribution of volumetric units over 3D surfaces, PCP restricts the footprint of the volumetric component to the boundaries of the host quadrilaterals, which does not support certain surface contacts or tangent connections of neighboring geometries. Hence, connectivity between component features along the surface is not assured. In the P. senegalus exoskeleton, the peg and socket joint and overlap joint articulations are key connectivity features of the system that must be preserved when translating to a new host environment. MetaMesh solves this challenge by including neighborhood relationships between the units, which PCP fails to do.

Other architectural geometry strategies use quadrilateral meshes with planar faces (PQ meshes) as a rationalization strategy to build envelopes designed as discrete freeform structures [17, 27]. PQ meshes use a heuristic device to segment the envelope into flat panels for efficient fabrication. Introducing rationalization strategies early in the planning can dramatically reduce cost and risk associated with using unconventional geometry for fabrication and assembly phases [27]. The method results in the approximation of a smooth surface to a discrete one with architectural-size panels ranging from half to several meters. We chose quadrilateral polygonal meshes over triangular ones, but we did not choose to work with flat faces, to minimize the number of different components, or to maximize component size. Instead, we utilize face curvature of the mesh quad to inform the fittest unit geometry while encouraging maximum shape variation with high resolution of mesh subdivision, all to ensure adaptation and functional gradation over the host environment.

The originality of MetaMesh lies in its efficient framework linking experimental analytical methods (µCT and morphometric analysis) with advanced computational geometry techniques (custom data structures for polygon mesh processing and component adaptation). The results propose a novel strategy for the multifunctional adaptation of highly elaborate components to complex surfaces with tailored directionality, emergence of new unit types, and the conservation of their interconnectivity patterns. Furthermore, the computational model sets the basis for future work with different exoskeleton systems and for the optimization of requirements beyond the topology of the hosting surface, such as kinematic ranges of motion, porosity for breathability requirements, or material distribution within units to modulate materials and mechanical properties in various regions.

This proof-of-concept model uses rigid, articulated armor units with compliant substrate and interconnections to produce a flexible protective system that provides uniform coverage while preserving user mobility. Current ballistic armor technologies include Kevlar® fibers [28] and ceramic plates [29], which are not flexible enough to cover mobile joints. Alternative flexible armor systems include woven fabrics [29], mosaic tilings [30], and overlapping discs [31], which have shortcomings that diminish ballistic resistance due to inter-yarn friction or designs that inherently include vulnerable regions of armor at interfaces and areas of variable thickness. The MetaMesh model seeks to overcome shortcomings in existing armor solutions by drawing inspiration from the complex architecture of the P. senegalus exoskeleton, which uses a unique geometry of individual armor units combined with inter-unit articulation to yield a system with spatially homogenous thickness and no exposed, vulnerable interfaces. Segmented systems, which utilize smaller protection sub-units, have the potential to reduce cost and ease of fabrication, as well as allow for use of a wider range of constituent materials and selective replacement of damaged units. While high performance properties with strict tolerances are required for functional penetration resistance, there is great opportunity for developing novel approaches to protective joint designs where tunability is key.

In our ongoing research we are building continuity between computational construction and additive fabrication. In previous work on this research project, members of our group have successfully fabricated macroscale assemblies on flat and curved surfaces using multi-material 3D printing [14-16], as well as using materials with graded
material properties within the scale units [16]. The MetaMesh model preserves the closed mesh articulation and the relation amongst the units, but does not yet accommodate material articulation strategies such as layered microstructures, graded material interfaces, and internal porosity. Yet, MetaMesh’s hierarchical organization provides the platform for additional meta organization principles at the local, regional, and global levels of the design process. Additionally, the specialized units for seam lines and the preservation principle of valid connection between units in MetaMesh allow further research and tunability of the system to the complex schema of human kinematics. Further computational development will also require focus on irregular mesh handling and other polygonal topologies to accommodate a variety of host surfaces.

MetaMesh model can be used to incorporate real physiological data and kinetic schema from the human body. This paper presents the computational design platform constructed on the logic of a biological system rather than provide for a specific bio-inspired design solution. In future the hierarchical structure of MetaMesh enables it to incorporate other concepts relevant to human physiology, such as the Lines of Non-Extension (LNE). Lines of Non-Extension, a concept first proposed by Iberall [32] and later developed and implemented in the design of “second-skin” Bio-Suit pressure garment [33], are the directions on human body that are subjected to minimal skin strain during movement. In P. senegalus armor, the restricted and free ranges of motion around the u- and v- directions can be analyzed akin to LNE, and could further serve as a basis for application to new kinematic constraints of human physiology [34]. For instance, MetaMesh could place the u-direction of a regional armor assembly on the mesh edges along the LNE of the human shoulder, while placing the v-direction along lines of maximal movement.

5. CONCLUSION

Customized computational models like MetaMesh provide a novel and effective method for translating the intricate, multifunctional design principles found in natural structures such as mineralized exoskeletons to synthetic, bioinspired structures. These models challenge traditional design techniques and set the basis for the incorporation of multiple layers of information, such as physiological and kinetic dimensions, at any level of the hierarchical computational data structure. MetaMesh is a computational model that embeds the geometric complexity of mineralized exoskeletons to enable functional gradation to the new bearer. The customized data structure provides adaptation of the system, while varying the unit features with neighborhood connectivity ensures graded overlap and interlock. With the MetaMesh model it is now possible to encode hierarchical relationships at local, regional, and global levels to maintain complex connectivity and functional differentiation of articulated structures on complex hosting surfaces.

Through MetaMesh, we see that interdisciplinary research (here drawing on experimental biology, materials science and engineering, mechanical engineering, and architecture) contributes to a better understanding of biological design principles and enhanced translation to bio-inspired and biomimetic devices. Scientific perspectives on the geometric and materials analysis in the P. senegalus exoskeleton better inform the designer in devising computational methods to translate designs to a new hosting surface and fabricate a functional bio-inspired system.

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**FIGURES**

**Figure 1:**

a. Mineralized exoskeleton of *Polypterus senegalus* (image used with permission from [www.digimorph.org](http://www.digimorph.org)).

b. Reconstructed µCT images of individual scales from different locations in the exoskeleton.
Figure 2: Geometric analysis of scale shape variation along the fish in the head-to-tail direction. a. Key geometrical features of a typical scale: P – peg, S – socket, AP – anterior process, AR – axial ridge. b. (top) Table summarizing the morphometric parameters of 11 scales (C1-C50) normalized by maximum value, and (bottom) plot of the normalized scale parameters.
Figure 3: a. Schematic and axonometric view of unit connections within the exoskeleton assembly: u- direction peg-and/socket (paraserial) and v- direction overlap (interserial) connections, stratum compactum (orange) attaching units to the organism, and Sharpey’s fibers (blue) attaching units to each other. b. Schematic of allowable ranges of motion of the unit joints: bending in overlapping joint (upper left), twisting of overlapping joint (upper right), bending in peg-and/socket joint (bottom left), twisting in peg-and/socket joint (bottom right). c. Schematics of the location in plan and section of the Stratum compactum (orange) and Sharpey’s fibers (blue).
Figure 4: Allowable motions between adjacent scales in head region and tail region scale variants. Head region scales: 
- a. rotation around u-axis
- b. translation along u-axis
- c. rotation around n-axis
- d. translation along v-axis.
Tail region scales: 
- e. rotation around u-axis
- f. translation along u-axis
- g. rotation around n-axis
- h. translation along v-axis.

Figure 5: Lines of symmetry on the top and bottom of fish trunk. 
- a. Identification of specialized (orange) and standard (blue) lines of units on the fish. 
- b. 3D-printed prototype mimicking the arrayed rings in the *P. senegalus* exoskeleton and the midlines of double-peg and double-socket specialized units. 
- c. 3D rendering of unit arrangement within two overlapping rings of standard units. 
- d. Section through peg and socket joints showing adaptation to the curved surface. 
- e. 3D-printed prototype showing the location of standard units (blue) and specialized units (orange).
Figure 6: The global organization diagram: a. Spatial functional differentiation color map of unit shape ranging from maximum protection (blue) to maximum flexibility (red). b. Functional differentiation is adapted to the varying radii of curvature (blue dashed line) during the swimming motion of the fish (adapted from [10]).
Figure 7: MetaMesh local unit construction. **a.** Vertex-centric (V0) unit placement on top of the underlying mesh and identification of u- (peg-socket) and v- (overlap) directions in the model. **b.** Unit construction from four connecting surfaces (blue) and a cross-shaped contact surface (orange). **c.** Arrangement of 4 standard units in the model and in the organism and calculation of the unit features from geometrical analysis parameters (L). **d.** Different specialized unit types identified by the u- and v- directions present in the organism (D, E) or defined by the directionality pattern of the new host (A, B, C).
Figure 8: *MetaMesh* regional directionality pattern. 

**a.** Definition of peg-and-socket u- direction (blue arrows) and overlap v- direction (black arrows). 

**b.** Identification of directionality pattern on the human body and emergence of new specialized unit types (orange). 

**c.** u- and v- directions on the idealized tube-shaped body of *P. senegalus* and location of the organism’s specialized units (orange).
Figure 9: Variation of the unit features along an extreme band of Functional Coefficient (FC) mapping from maximum protection (blue) to maximum flexibility (red). 

**a.** The shape variant from head region (c11s10) and from tail region (c31s10) are mapped and morphed on the torus based on the functional gradient of FC (bottom). 

**b.** Identification of the estimated FC gradient on a human chest from maximum protection (blue) above the shoulder and maximum flexibility (red) in the underarm.
Figure 10: *MetaMesh* global iterative steps for regularizing the host mesh Tangential Laplacian Smoothing through 50 iterations. The quality of the quad ranges from distorted (red) to regular (blue).
Figure 11: Graphical summary of the MetaMesh hierarchical computational model.
## APPENDIX: ABBREVIATIONS AND SYMBOLS.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>$A_{(u,v)}$</td>
<td>point interpolation on quad’s boundary</td>
</tr>
<tr>
<td>ANG</td>
<td>normalized angle between two adjacent scale edges</td>
</tr>
<tr>
<td>AP</td>
<td>scale’s front edge extension that overlaps with the scale in the next column</td>
</tr>
<tr>
<td>APL</td>
<td>anterior process length, the relative size of AP to scale’s side length</td>
</tr>
<tr>
<td>AR</td>
<td>axial ridge, a protrusion on the bottom of the scale that connects the scale to the underlying organic tissue</td>
</tr>
<tr>
<td>$B_{(u,v)}$</td>
<td>point interpolation on quad’s boundary</td>
</tr>
<tr>
<td>E</td>
<td>bounding box size, minimum perimeter rectangle area within which the scale can be subscribed</td>
</tr>
<tr>
<td>F</td>
<td>a set of polygon faces, in which a face $f = (i_1, \ldots, i_n)$ is a sequence of non-repeating vertex indices</td>
</tr>
<tr>
<td>FC</td>
<td>functional coefficient, average value of the normalized geometric parameters PSL, IO, PI, and AP, indicates how developed the connective interfaces are between adjacent scales, ranging from 0 for maximum protection to 1 for maximum flexibility</td>
</tr>
<tr>
<td>IO</td>
<td>interserial overlap, overlap between scales in the adjacent columns</td>
</tr>
<tr>
<td>L$_1$</td>
<td>length of the peg</td>
</tr>
<tr>
<td>L$_2$</td>
<td>length of the peg and socket axis</td>
</tr>
<tr>
<td>L$_3$</td>
<td>total width of the scale</td>
</tr>
<tr>
<td>L$_4$</td>
<td>width of the overlap between scales in v-direction</td>
</tr>
<tr>
<td>L$_5$</td>
<td>width of the overlap between scales in u-direction</td>
</tr>
<tr>
<td>L$_6$</td>
<td>length of the short edge of the scale</td>
</tr>
<tr>
<td>L$_7$</td>
<td>length of the long edge of the scale</td>
</tr>
<tr>
<td>L$_8$</td>
<td>width of the scale without the overlap</td>
</tr>
<tr>
<td>LNE</td>
<td>Lines of Non-Extension, the directions on human body that are subjected to minimal skin strain during movement</td>
</tr>
<tr>
<td>m</td>
<td>a midpoint of an edge of the mesh quad</td>
</tr>
<tr>
<td>n-axis</td>
<td>the orthogonal direction normal to the surface of the scale</td>
</tr>
<tr>
<td>P</td>
<td>protruding peg, complemented with socket to form a peg-and-socket joint</td>
</tr>
<tr>
<td>$P_{1,4}$</td>
<td>points defining a mesh quad</td>
</tr>
<tr>
<td>PCP</td>
<td>Parametric Component Population, a common method to adapt discrete geometrical components to large-scale complex shapes</td>
</tr>
<tr>
<td>PO</td>
<td>paraserial overlap, an overlap between scales in the peg-and-socket joint direction</td>
</tr>
<tr>
<td>S</td>
<td>socket, complemented with peg to form a peg-and-socket joint</td>
</tr>
<tr>
<td>SR</td>
<td>shape aspect ratio, the ratio of the length of peg-and-socket axis to scale’s width</td>
</tr>
<tr>
<td>u-axis</td>
<td>the “paraserial” direction within one column of scales, parallel to the line connecting the peg-and-socket joints</td>
</tr>
<tr>
<td>v-axis</td>
<td>the “interserial” direction between columns of scales, parallel to the line connecting the overlapping joints</td>
</tr>
<tr>
<td>V</td>
<td>vertex indices, a table of 3D vertex coordinates $X = {x_i : i \in V}$</td>
</tr>
<tr>
<td>PQ meshes</td>
<td>quadrilateral meshes with planar faces, topology of polygonal regular mesh</td>
</tr>
<tr>
<td>VOL</td>
<td>volume of scale in mm$^3$</td>
</tr>
<tr>
<td>$\Delta x_i$</td>
<td>vertex displacement vector, the change in mesh quad parameters due to mesh optimization</td>
</tr>
<tr>
<td>X</td>
<td>vertex coordinates of the mesh quad</td>
</tr>
</tbody>
</table>
REFERENCES


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VITAE

Designer Neri Oxman is the Sony Corporation Career Development Professor and Assistant Professor of Media Arts and Sciences at the MIT Media Lab. Her group Mediated Matter explores how digital design and fabrication technologies mediate between matter and environment to radically transform the design and construction of objects, buildings, and systems. Oxman was named to ICON's list of the top 20 most influential architects to shape our future (2009), and was selected as one of the 100 most creative people by FASTCOMPANY (2009). In 2008, she was named "Revolutionary Mind" by SEED Magazine. Her work has been exhibited at MoMA (NYC) and is part of the museum's permanent collection. In 2012 the Centre Georges Pompidou Museum (Paris, France) acquired her works for its permanent collection.

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