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# Communication-efficient three-party protocols for authentication and key agreement

Tian-Fu Lee<sup>a</sup>, Jenn-Long Liu<sup>b,\*</sup>, Mei-Jiun Sung<sup>c</sup>, Shiueng-Bien Yang<sup>d</sup>, Chia-Mei Chen<sup>b</sup>

<sup>a</sup> Department of Information Management, Leader University, Tainan 709, Taiwan, ROC

<sup>b</sup> Department of Information Management, National Sun Yat-Sen University, Kaohsiung 804, Taiwan, ROC

<sup>c</sup> Institute of Applied Information, Leader University, Tainan 709, Taiwan, ROC

<sup>d</sup> Department of Computer Science and Information Engineering, Leader University, Tainan 709, Taiwan, ROC

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# ABSTRACT

Encrypted key exchange (EKE) authentication approaches are very important for secure communicating over public networks. In order to solve the security weaknesses threeparty EKE, Yeh et al. [H.T. Yeh, H.M. Sun, T. Hwang, Efficient three-party authentication and key agreement protocols resistant to password guessing attacks, Information Science and Engineering 19 (6) (2003) 1059–1070.] proposed two secure and efficient three-party EKE protocols. Based on the protocol developed by Yeh et al., two improved EKE protocols for authentication and key agreement are proposed in this study. The computational costs of the proposed protocols are the same as those of the protocols of Yeh et al. However, the numbers of messages in the communication are fewer than those of the protocols of Yeh et al. Furthermore, the round efficient versions of our proposed protocols are also described.

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# 1. Introduction

Encrypted key exchange authentication approaches are very important and widely applied in network communication [1–6]. In these authentication approaches, the communicating parties share a secrete key with a trusted server and can exchange confidential and authenticated information over an insecure network with the help of a server.

Secure communication protocols should provide security requirements, which are described as follows.

- 1. Mutual authentication: Mutual authentication protocols enable participants mutually to authenticate each other's identity.
- 2. Session key security: A communication protocol exhibits session key security if the session key cannot be obtained without any long-term secrets.
- 3. Off-line guessing attacks: In an off-line password guessing attack, an attacker guesses a password and verifies his guess, but he does not need to participate in any communication during the guessing phase [4,5,7–11].
- 4. Undetectable on-line guessing attacks: In an on-line guessing attack, an attacker searches to verify a guessed password in an on-line transaction and a failed guess cannot be detected and logged by the server [12,13].
- 5. Perfect forward secrecy: A protocol has perfect forward secrecy if the compromise of long-life keys does not compromise previous session keys.

\* Corresponding author. E-mail address: linglong@ms23.hinet.net (J.-L. Liu).

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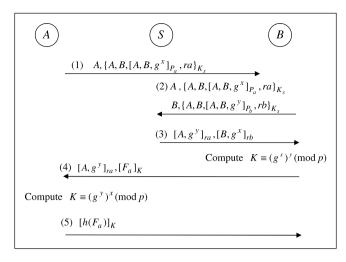


Fig. 1. The three-party EKE protocol of Yeh et al..

- 6. Known-key security: If a protocol has known-key security, the compromise of one session key does not reveal other session keys.
- 7. Intruder-in-the-middle attacks: The intruder-in-the-middle attack is that an intruder interrupts a message and substitutes it for his own message, so that communication parties compute the wrong session key without detecting the intruder.
- 8. Replay attacks: A replay attack is that an unauthorized party records previous messages and uses them to cheat the receiver in later processes [14].
- 9. Stolen-verifier attacks: The stolen-verifier attack is that the adversary who has stolen the verifier of a user's password can impersonate as that user.

Recently, many encrypted key exchange authentication approaches were presented for secure communicating over public networks. Bellovin and Merritt [1] proposed a key exchange protocol based on memorable passwords between two communicating parties known as the Encrypted Key Exchange (EKE) in 1992. From then on, numbers of password-based authentication and key agreement approaches have been proposed and developed in many communication systems. Gong et al. [9] proposed a three party authentication protocol, in which the server is responsible for user authentication and distributes the common session key shared between two users. Later, Steiner et al. proposed a three-party EKE [2] which extended the EKE to a three-party model where two clients registering in the same server can share a secret session key through the protocol. However, Lin et al. [13] and Yeh et al. [15] stated the weaknesses of three-party EKE proposed by Steiner et al. Besides, Yeh et al. [15] proposed two new secure three-party EKE protocols for authentication protocol. In a plaintext-equivalent authentication protocol and the other is a verifier-based authentication protocol. In a plaintext-equivalent protocol becomes instantly compromised if the server's database containing clients' passwords is revealed. Comparatively, a verified-based protocol only requires a verifier to be stored in server's database and hence add another method to verify the client's possession of actual password, as opposed to a stolen verifier from the password file [15].

In a Diffie-Hellman-based authentication protocol, only revealing the information  $g^x$  and  $g^y$  for generating the session key ( $g^{xy}$ ) cannot compromise the session key. The clients can directly exchange the information  $g^x$  and  $g^y$  for generating the session key without the help of the server, and thus the improved protocols can decrease the messages in communications. Using this technique, this investigation proposes communication-efficient three-party EKE protocols based on the protocols of Yeh et al. The computation costs of the protocols developed by Yeh et al. and the proposed protocols herein are equal. However, the numbers of messages in the proposed protocols are reduced. Moreover, the round efficient versions of these protocols are presented.

The rest of this paper is organized as follows. Section 2 reviews the three-party EKE protocols of Yeh et al. Section 3 introduces the improved three-party EKE protocols. Section 4 provides security and performance analyses of the improved protocols. Finally, Section 5 gives the conclusions.

# 2. Preliminaries

This section describes the underlying primitives used in this paper and briefly reviews the three-party EKE protocols of Yeh et al. [15]. The underlying primitives include the Discrete Logarithms problem and the Diffie-Hellman assumptions [16]. Table 1 details the notation used, and Fig. 1 depicts the three-party EKE protocol of Yeh et al., which works as follows.

# Table 1

A and B are two communication parties and S is a trusted server
Passwords of A and B shared with S
(private, public) key derived from P <sub>a</sub> and shared with S
(private, public) key derived from P <sub>b</sub> and shared with S
Public key of the Trust Server
Random numbers
Session key between A and B
Symmetric-key encryption of "info" with key K.
Asymmetric-key encryption of "info" with key K.
Digital signature of "info" with key K
One-way hash function.
A sends a message M to B.
Base generator
The modulus (all exponentiation in modulo <i>p</i> )
The first 64 bits of message 1 in proposed protocol

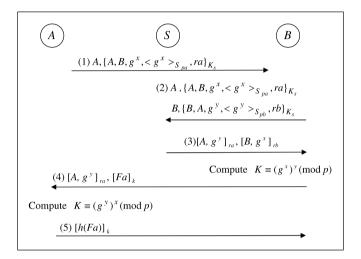


Fig. 2. The verifier-based three-party EKE of Yeh et al..

**Definition 2.1** (*The Discrete Logarithms Problem (DLP)*). Let  $G = \langle g \rangle$  be a cyclic group of prime order q and x is randomly chosen in  $Z_q$ . Consider the equation  $y = g^x \mod p$ . Given g, x and p, it is a straightforward matter to calculate y. However, given y, g and p, it is computationally infeasible to calculate x.

**Definition 2.2** (*The Diffie-Hellman Assumptions*). Let  $G = \langle g \rangle$  be a cyclic group of prime order q and x, y are randomly chosen in  $Z_q$ . Given g,  $g^x$ ,  $g^y$  and p, if the equation  $z = g^{xy} \mod p$  holds, then it is computationally infeasible to calculate z without the value of x or y.

2.1. The three-party EKE protocol of Yeh et al.

Step 1.  $A \rightarrow B$ : A,  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$ 

User *A* selects two random numbers ra, x, and computes  $g^x \pmod{p}$  which is encrypted by password  $P_a$  of *A*. Then *A* encrypts (*A*, *B*, [*A*, *B*,  $g^x]_{P_a}$ , ra) by the public key  $K_s$  of server and sends the ciphertext to *B*.

Step 2.  $B \to S$ : A,  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$ , B,  $\{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}$ 

On receiving the message from *A*, *B* composes a similar message to *A* and sends them to *S*. Step 3.  $S \rightarrow B : [A, g^y]_{ra}, [B, g^x]_{rb}$ 

Server *S* decrypts  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$ ,  $\{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}$  with his private key and checks the authenticities of both *A* and *B*. Then *S* encrypts  $(A, g^y)$  with *ra*, encrypts  $(B, g^x)$  with *rb* and sends them to *B*.

Step 4.  $B \rightarrow A : [A, g^y]_{ra}, [F_a]_K$ 

*B* decrypts  $[B, g^x]_{rb}$  with *rb* and computes the session key  $K \equiv (g^x)^y \pmod{p}$ . Then he sends a key confirmation message  $[F_a]_K$  and forwards  $[A, g^y]_{ra}$  to *A*.

Step 5.  $A \rightarrow B : [h(F_a)]_K$ 

A decrypts  $[A, g^y]_{ra}$  with ra and computes the session key  $K \equiv (g^y)^x \pmod{p}$ . Then he decrypts  $[F_a]_K$  with the session key K, checks its validity, and responds with  $[h(F_a)]_K$  for key confirmation.

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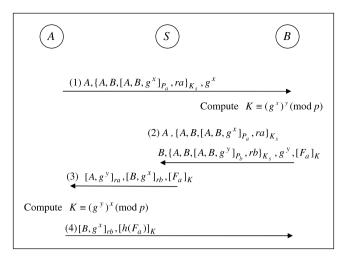


Fig. 3. Proposed efficient three-party EKE protocol.

2.2. The verifier-based three-party EKE protocol of Yeh et al. (shown on Fig. 2)

Step 1.  $A \rightarrow B : A, \{A, B, g^x, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$ 

A generates the message  $A, \{A, B, g^x, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$  and sends it to S via B. B is a similar legitimate user to A. Step 2.  $B \rightarrow S : A, \{A, B, g^x, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}, B, \{B, A, g^y, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}$ 

B composes a similar message and sends it to S. Server S checks the authenticity of both A and B.

Step 3.  $S \rightarrow B : [A, g^y]_{ra}, [B, g^x]_{rb}$ 

Server *S* uses the *ra* and *rb* generated by *A* and *B*, respectively, as encrypting keys replies with message  $[A, g^y]_{ra}, [B, g^x]_{rb}$ .

Step 4.  $B \rightarrow A : [A, g^y]_{ra}, [F_a]_K$ 

*B* gets the messages and computes the session key  $K \equiv (g^x)^y \pmod{p}$ . He then sends  $[A, g^y]_{ra}$ ,  $[F_a]_K$  to *A*, where  $F_a$  is produced by the partial bit stream of  $(A, \{A, B, g^x, \langle g^x \rangle_{S_{Pa}}, ra\}_{K_s})$ .

Step 5.  $A \rightarrow B : [h(F_a)]_K$ 

Similarly, *A* gets the messages and computes the session key  $K \equiv (g^{y})^{x} \pmod{p}$ . If *A* successfully confirms  $[F_a]_K$ , then he uses a hash value as a response value to *B*. Finally, B verifies the key confirmation message  $[h(F_a)]_K$ .

# 3. Communication-efficient three-party EKE protocols

This section presents two communication-efficient authentication and key agreement protocols based on the protocol of Yeh et al. [15]. One is a plaintext-equivalent authentication protocol and the other is a verifier-based authentication protocol. The computation costs of the protocols developed by Yeh et al. are equal to those of the protocols proposed herein. However, the number of transmissions is fewer than those of the protocols of Yeh et al. Figs. 3 and 4 illustrate the proposed authentication and key agreement protocol and verifier-based three-party EKE protocols, respectively. The protocols are described in detail as follows.

# 3.1. Proposed efficient three-party EKE protocol

Step 1.  $A \rightarrow B$ : A,  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}, g^x$ 

A selects two random numbers  $r_a$ , x, and computes  $g^x \pmod{p}$  which is encrypted by password  $P_a$  of A. Then he encrypts  $(A, B, [A, B, g^x]_{P_a}, r_a)$  by the public key  $K_s$  of the server and sends it with  $g^x$  to B.

Step 2.  $B \to S : A, \{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}, B, \{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}, g^y, [F_a]_K$ 

On receiving the message from A, B composes a similar message to A and gets  $g^x$  to produce the session key  $K \equiv (g^x)^y \pmod{p}$ . Then B sends the message to S.

Step 3.  $S \rightarrow A : [A, g^y]_{ra}, [B, g^x]_{rb}, [F_a]_K$ 

Server *S* decrypts {*A*, *B*, [*A*, *B*,  $g^x$ ]<sub>*P<sub>a</sub>*, *ra*}<sub>*K<sub>s</sub>*</sub> and {*A*, *B*, [*A*, *B*,  $g^y$ ]<sub>*P<sub>b</sub>*</sub>, *rb*}<sub>*K<sub>s</sub>*</sub> with his private key and checks the authenticities of both *A* and *B*. Then *S* encrypts (*A*,  $g^y$ ) with *ra*; encrypts (*B*,  $g^x$ ) with *rb*; and sends them with a key confirmation message [*F<sub>a</sub>*]<sub>*K*</sub> to *A*.</sub>

Step 4.  $A \rightarrow B : [B, g^x]_{rb}, [h(F_a)]_K$ 

A decrypts  $[A, g^y]_{ra}$  with ra and computes the session key  $K = (g^y)^x$ . Then he sends  $[h(F_a)]_K$  and forwards  $[B, g^x]_{rb}$  to B. Finally, B validates  $g^x$  by checking and decrypting  $[B, g^x]_{rb}$  with rb.

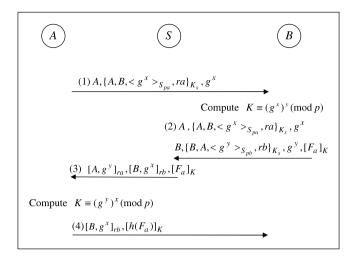


Fig. 4. Proposed efficient verifier-based three-party EKE protocol.

By rearranging and sending the messages in parallel, the proposed efficient three-party EKE protocol can be implemented in less time and obtain a round-efficient version. The round-efficient protocol can be executed in three rounds and is described below.

Round 1.  $A \rightarrow B : A, g^{x}$   $A \rightarrow S : A, \{A, B, [A, B, g^{x}]_{P_{a}}, ra\}_{K_{s}}.$ Round 2.  $B \rightarrow A : B, g^{y}, [F_{a}]_{K}$   $B \rightarrow S : B, \{A, B, [A, B, g^{y}]_{P_{b}}, rb\}_{K_{s}}$ Round 3.  $S \rightarrow A : [A, g^{y}]_{ra}$   $S \rightarrow B : [B, g^{x}]_{rb}$  $A \rightarrow B : [h(F_{a})]_{K}.$ 

3.2. Proposed efficient verifier-based three-party EKE protocol

- Step 1.  $A \to B : A$ ,  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}, g^x$ A generates ra, x; computes  $g^x \pmod{p}, \langle g^x \rangle_{S_{pa}}$  and sends the message A,  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}, g^x$  to S via B. B is a similar legitimate user to A.
- Step 2.  $B \to S : A$ ,  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}, g^x, B, \{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}, g^y, [F_a]_K$   $B \text{ gets } g^x \text{ to compute the session key } K \equiv (g^x)^y \pmod{p}$ . Then he composes a similar message and sends it to S. Server S checks the authenticity of both A and B.
- Step 3.  $S \to A : [A, g^y]_{ra}, [B, g^x]_{rb}, [F_a]_K$ Server *S* decrypts  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$  and  $\{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}$  with his private key for checking the authenticities of both *A* and *B*. Then *S* encrypts  $(A, g^y)$  with *ra*; encrypts  $(B, g^x)$  with *rb*; and sends them with a key confirmation message  $[F_a]_K$  to *A*.

Step 4.  $A \to B : [B, g^x]_{rb}, [h(F_a)]_K$  A decrypts  $[A, g^y]_{ra}$  with ra and computes the session key  $K \equiv (g^y)^x \pmod{p}$ . Then he sends  $[h(F_a)]_K$  and forwards  $[B, g^x]_{rb}$  to B. Finally, B validates  $g^x$  by checking and decrypting  $[B, g^x]_{rb}$  with rb.

Similarly, a round-efficient version of the proposed verifier-based protocol can be obtained by rearranging and sending the messages in parallel. The round-efficient protocol can also be executed in three rounds and is described below.

Round 1.  $A \rightarrow B : A, g^{x}$   $A \rightarrow S : A, \{A, B, \langle g^{x} \rangle_{Spa}, ra\}_{K_{S}}$ Round 2.  $B \rightarrow A : B, g^{y}, [F_{a}]_{K}$   $B \rightarrow S : B, \{B, A, \langle g^{y} \rangle_{Spb}, rb\}_{K_{S}}$ Round 3.  $S \rightarrow A : [A, g^{y}]_{ra}$   $S \rightarrow B : [B, g^{x}]_{rb}$  $A \rightarrow B : [h(F_{a})]_{K}$ .

# 4. Security and performance analyses

This section describes the security analyses of the proposed three-party EKE protocols and compares their performance with that of the three-party EKE protocols of Yeh et al.

# 4.1. Security analyses

# 4.1.1. Security analyses of the improved three-party EKE protocol

1. Mutual authentication

On receiving { $A, B, [A, B, g^x]_{P_a}, ra$ }<sub>Ks</sub> and { $A, B, [A, B, g^y]_{P_b}, rb$ }<sub>Ks</sub> in Step 2, S can authenticate A and B by verifying  $P_a$  and  $P_b$ , respectively. Additionally, A and B can validate  $g^y$  and  $g^x$ , and authenticate S simultaneously by decrypting  $[A, g^y]_{ra}$  with ra and  $[B, g^x]_{rb}$  with rb in Step 3 and Step 4, respectively. Hence, the proposed protocol exhibits mutual authentication.

2. Session key security

Given  $g^x$  (or  $g^y$ ), the value x (or y) is hard to obtain, because of the Discrete Logarithm problem. Given  $g^x$  and  $g^y$ , the session key  $K \equiv (g^y)^x \pmod{p}$  or  $K \equiv (g^x)^y \pmod{p}$  cannot be determined without knowledge of x or y, because of the Diffie-Hellman problem.

3. Off-line guessing attacks

In the proposed protocol, ra,  $g^x$ , rb and  $g^y$  are random numbers and  $K_S$  is the server public key, so no information can be used to verify directly the correctness of the guessed passwords from  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$  in Step 1 and  $\{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}$  in Step 2. Hence, the proposed protocol resists off-line guessing attacks.

4. Undetectable on-line guessing attacks

In the proposed protocol, on receiving messages from *B* in Step 2, server *S* authenticates *A* and *B* by verifying  $P_a$  and  $P_b$  in  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$  and  $\{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}$ , respectively. Therefore, a failed guess will be detected by *S*. Hence, the proposed protocol can resist undetectable on-line guessing attacks.

# 5. Perfect forward secrecy

In the improved protocol, the ephemeral exponents *x* and *y* are randomly selected and independent among each protocol execution. Therefore, the compromised passwords  $P_a$  and  $P_b$  cannot reveal any previous session keys  $K \equiv g^{xy} \pmod{p}$ . Therefore, the proposed protocol has perfect forward secrecy.

6. Known-key security

The session keys  $K \equiv g^{xy} \pmod{p}$  generated in different runs are independent since *A* and *B* randomly selects *x* and *y*, respectively, and these random numbers are independent among protocol executions. Hence, the proposed protocol exhibits known-key security.

7. Intruder-in-the-middle attacks

Since the improved protocol has mutual authentication, the intruder-in-the-middle attacks are necessarily unsuccessful.

8. Replay attacks

An attacker tries to deceive *B* (or *A*) and *S* by sending out a previous message  $\{A, B, [A, B, g^x]_{P_a}, ra\}_{K_s}$  (or  $\{A, B, [A, B, g^y]_{P_b}, rb\}_{K_s}$ ). The attacker cannot compute the session key  $K \equiv g^{x,y} \pmod{p}$  since he does not know the values of *x* and *y*. Accordingly, he cannot correctly send out a key confirmation message and the replay attack will fail.

# 4.1.2. Security analyses of the improved verifier-based three-party EKE protocol

# 1. Mutual authentication

On receiving  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$  and  $\{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}$  in Step 2, *S* can authenticate *A* and *B* by verifying  $S_{pa}$  and  $S_{pb}$ , respectively. Additionally, *A* and *B* can validate  $g^y$  and  $g^x$ , and authenticate *S* simultaneously by decrypting  $[A, g^y]_{ra}$  with ra and  $[B, g^x]_{rb}$  with rb in Step 3 and Step 4, respectively. Hence, the proposed protocol exhibits mutual authentication. 2. Session key security

Given  $g^x$  (or  $g^y$ ), the value x (or y) is hard to obtain, because of the Discrete Logarithm problem. Given  $g^x$  and  $g^y$ , the session key  $K \equiv (g^y)^x \pmod{p}$  or  $K \equiv (g^x)^y \pmod{p}$  cannot be determined without knowledge of x or y, because of the Diffie-Hellman problem.

3. Off-line guessing attacks

In the proposed protocol, ra,  $g^x$ , rb and  $g^y$  are random numbers and  $K_S$  is the server public key, so no information can be used to verify directly the correctness of the guessed passwords from  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_S}$  and  $\{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_S}$ . Hence, the proposed protocol resists off-line guessing attacks.

4. Undetectable on-line guessing attacks

In this protocol, server *S* authenticates *A* and *B* by verifying  $S_{pa}$  and  $S_{pb}$  in  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$  and  $\{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}$ , respectively. Therefore, a failed guess will be detected by S. Hence, the proposed protocol can resist undetectable on-line guessing attacks.

5. Perfect forward secrecy

In the improved protocol, the ephemeral exponents x and y are randomly selected and independent among each protocol execution. Therefore, the compromised password cannot reveal any previous session keys. Therefore, the proposed protocol has perfect forward secrecy.

6. Known-key security

The session keys generated in different runs are independent since *A* and *B* randomly selects *x* and *y*, respectively, and these random numbers are independent among protocol executions. Hence, the proposed protocol exhibits known-key security.

Table 2
Performance comparisons with related protocols.

Protocols	Random numbers	Computational cost		Steps	Rounds
		Exponential	Asymmetric encryption		
Yeh et al.'s 3PEKE	4	4	2	5	_
Proposed 3PEKE	4	4	2	4	3
Yeh et al.'s VB-3PEKE	4	4	4	5	-
Proposed VB-3PEKE	4	4	4	4	3

# 7. Intruder-in-the-middle attacks

Since the improved protocol has mutual authentication, the intruder-in-the-middle attacks are necessarily unsuccessful.

8. Replay attacks

An attacker tries to deceive B(or A) and S by sending out a previous message  $\{A, B, \langle g^x \rangle_{S_{pa}}, ra\}_{K_s}$  (or  $\{B, A, \langle g^y \rangle_{S_{pb}}, rb\}_{K_s}$ ). The attacker cannot compute the session key  $K \equiv g^{x,y} \pmod{p}$  since he does not know the values of x and y. Accordingly, he cannot correctly send out a key confirmation message and the replay attack will fail.

9. Stolen-verifier attacks

The adversary who has stolen the verifier  $V_{pa}$  (or  $V_{pb}$ ) of user *A*'s password  $P_a$  (or user *B*'s password  $P_b$ ) cannot impersonate as that user *A* (or *B*) since  $\langle g^x \rangle_{S_{pa}}$  (or  $\langle g^y \rangle_{S_{pb}}$ ) cannot be determined without knowledge of the private key  $S_{pa}$  (or  $S_{pb}$ ). Accordingly, the proposed protocol can resist stolen-verifier attacks.

#### 4.2. Performance analyses and comparisons

Table 2 compares the performances of the proposed three-party EKE (3PEKE) protocols with those of the three-party EKE protocols of Yeh et al. For plaintext-equivalent, both the three-party EKE protocols of Yeh et al. and the proposed three-party EKE protocol use four random numbers computations, four modular exponential computations and two asymmetric encryption computations. However, the proposed protocol has one step less than the three-party EKE protocol require four random number computations and four asymmetric encryption computations, four modular exponential computations. However, the protocols (VB-3PEKE) of Yeh et al. and the proposed protocol require four random number computations, four modular exponential computations and four asymmetric encryption computations. However, the protocol of Yeh et al. Besides, both the round-efficient protocol can be executed in three rounds.

#### 5. Conclusions

This study proposes two communication-efficient three-party EKE protocols based on the three-party EKE protocol of Yeh et al. One is a plaintext-equivalent authentication protocol and the other is a verifier-based authentication protocol. The computation cost of the proposed three-party EKE protocols is equal to that of the three-party EKE protocols of Yeh et al. In addition, the proposed three-party EKE protocols reveal the same information with the three-party EKE protocols of Yeh et al. According the Diffie-Hellman assumptions and security analyses of the three-party EKE protocols of Yeh et al., the proposed three-party EKE protocols also achieve the security requirements of three-party EKE protocols. However, the proposed protocols have one step less than the three-party EKE protocols of Yeh et al. Therefore, the proposed three-party EKE protocols of Yeh et al. Moreover, the proposed protocols can be executed in three rounds by arranging the messages in parallel.

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