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A partial wave analysis of $\bar{p}p \rightarrow \eta\eta\pi^0$

A.V. Anisovich^c, C.A. Baker^b, C.J. Batty^b, D.V. Bugg^a, V.A. Nikonov^c,
A.V. Sarantsev^c, V.V. Sarantsev^c, B.S. Zou^{a,1}

^a Queen Mary College, London E1 4NS, UK

^b Rutherford Appleton Laboratory, Chilton, Didcot, OX11 0QX, UK

^c St. Petersburg Nuclear Physics Institute, Gatchina 188350, St. Petersburg district, Russia

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Abstract

A partial wave analysis of $\bar{p}p \rightarrow \eta\eta\pi^0$ data from the Crystal Barrel experiment is made in terms of s -channel resonances. The decay channels $a_0(980)\eta$, $f_0(1770)\pi$ and $f_0(2105)\pi$ provide evidence for two $I = 1$, $J^{PC} = 0^{-+}$ resonances. The first has mass $M = 2360 \pm 25$ MeV and width $\Gamma = 300_{-50}^{+100}$ MeV, and the second $M = 2070 \pm 35$ MeV, $\Gamma = 310_{-50}^{+100}$ MeV. There is also evidence for a $J^{PC} = 2^{-+}$ state with $M = 2005 \pm 15$ MeV and $\Gamma = 200 \pm 40$ MeV, decaying strongly to $a_0(980)\pi$.
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The present work is part of an analysis of $\bar{p}p$ annihilation with isospin $I = 1$ and charge conjugation number $C = +1$ in terms of s -channel resonances. A combined analysis of data from final states $3\pi^0$, $\pi^0\eta$ and $\pi^0\eta'$ is reported separately [1]. Here we focus attention on annihilation to $\eta\eta\pi^0$. In these data, signals are visible from final states $a_0(980)\eta$, $f_0(1500)\pi$, $f_0(1770)\pi$ and $f_0(2105)\pi$. They carry no spin and may be analysed simply in terms of Legendre polynomials describing the production process.

We find that the largest contributions to $\eta\eta\pi^0$ data arise from S -wave final states with $J^P = 0^-$; those from 1^+ , 2^- , 3^+ and 4^- are somewhat smaller. Hence these data give a rather direct determination of contributions with quantum numbers 0^- . In contrast, $3\pi^0$ data contain weak 0^- contributions from the final

state $f_2(1270)\pi$ with orbital angular momentum $L = 2$ in the decay process. There, the 0^- amplitude is hard to separate from larger $L = 2$ $f_2(1270)\pi$ amplitudes with $J^P = 2^-$ and 4^- .

The $\eta\eta\pi^0$ data treated here have been presented in two earlier publications [2,3]. They may be fitted with the channels

$$\bar{p}p \rightarrow a_0(980)\eta, \quad (1)$$

$$\rightarrow a_2(1320)\eta, \quad (2)$$

$$\rightarrow a_2(1660)\eta, \quad (3)$$

$$\rightarrow f_0(1500)\pi, \quad (4)$$

$$\rightarrow f_0(1770)\pi, \quad (5)$$

$$\rightarrow f_0(2105)\pi, \quad (6)$$

$$\rightarrow f_2(1980)\pi, \quad (7)$$

$$\rightarrow f_2(1270)\pi. \quad (8)$$

Fig. 1 shows Dalitz plots for data at all nine beam momenta. Figs. 2 and 3 show projections on to masses

E-mail address: bugg@v2.rl.ac.uk (D.V. Bugg).

¹ Now at the Institute for High Energy Physics, Beijing 100039, PR China.

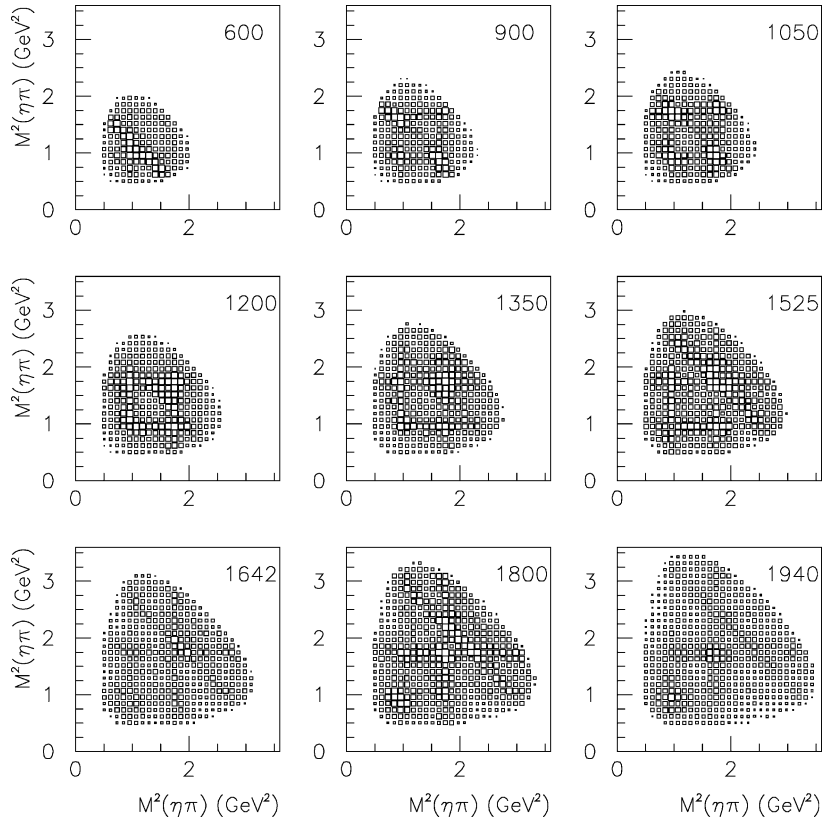


Fig. 1. Dalitz plots for data; numbers in each panel indicate beam momenta in MeV/c.

of $\pi\eta$ and $\eta\eta$ combinations; histograms show the fit described below. There are clear peaks in Fig. 3 due to $f_0(1500) \rightarrow \eta\eta$, and in Fig. 2 due to $a_0(980)$ and $a_2(1320) \rightarrow \pi\eta$. The latter two are stronger than is immediately apparent from the figure, since the a_0 and a_2 peaks originate from only one of the two $\pi^0\eta$ combinations, e.g., from $\pi^0\eta_1$; the other combination $\pi^0\eta_2$ produces a broad background when projected on to $M(\pi^0\eta_1)$, as one sees from Dalitz plots.

In Ref. [3], it was shown that a small but highly significant peak in the $\eta\eta$ channel requires the presence of $f_0(1770)$ at beam momenta 900–1350 MeV/c. In Ref. [2], it was also shown that data at 1525–1940 MeV/c require a strong $f_0(2105) \rightarrow \eta\eta$ signal. That resonance has also been observed in $\bar{p}p \rightarrow \eta\eta$ [4] and was first identified in $J/\Psi \rightarrow \gamma(4\pi)$ data [5], where $f_0(2105) \rightarrow \sigma\sigma$, and σ stands for the $\pi\pi$ S-wave amplitude. Ref. [2] also presented evidence for

a broad 2^+ signal in $\eta\eta$ with $M = 1980 \pm 50$ MeV, $\Gamma = 500 \pm 100$ MeV. There is further evidence for this broad state in WA102 data on central production of 4π [6].

We now describe the partial wave formula, given by Eq. (9) below, used to fit the data. This is the same as in the accompanying paper [1]. A full fit is made to production and decay of all channels (1)–(8) in terms of $\bar{p}p$ partial waves up to $J^P = 4^-$. Each partial wave has a distinctive dependence via relativistic tensor expressions $Z(\theta, \alpha, \beta)$ on production angle θ of each resonance in the centre of mass, and on its decay angles (α, β) in the rest frame of the resonance. The energy dependence of each partial wave amplitude is expressed as the sum of up to two s -channel resonances plus a background. These resonances, described by simple Breit–Wigner functions of s with constant widths, are found to cluster in the

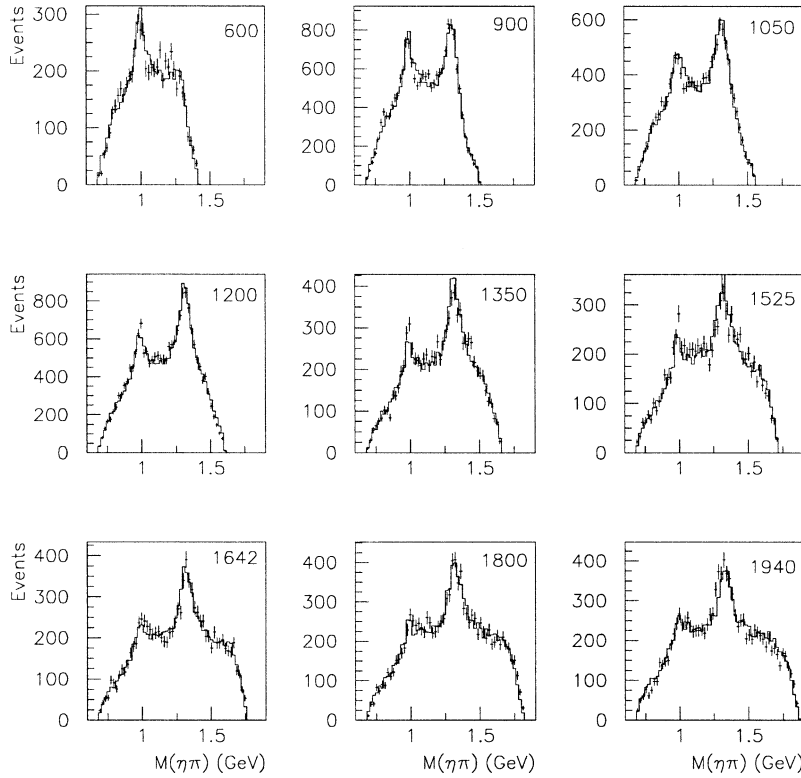


Fig. 2. Projections on to $\eta\pi$ mass; histograms show the partial wave fit. Numbers in each panel indicate beam momenta in MeV/c.

mass ranges 1930–2070 MeV and 2220–2360 MeV. The background, where required, is taken as the high energy tail of a resonance below the $\bar{p}p$ threshold. This parametrisation guarantees that partial wave amplitudes satisfy the necessary condition of analyticity, relating the energy dependence of magnitudes and phases.

Blatt–Weisskopf centrifugal barrier factors $B_\ell(p)$ and $B_L(q)$ are included in the partial wave amplitudes; $B_\ell(p)$ incorporates the correct threshold dependence on momentum p in the $\bar{p}p$ channel for initial orbital angular momentum ℓ , and $B_L(q)$ likewise describes the dependence on L and momentum q in the decay to the final state, e.g., $a_0(980)\eta$. The radius of the barrier is set to 0.83 fm from the determination in Ref. [4]. The $a_0(980)$ amplitude for decay to particles 1 and 2 is described by a Flatté formula $F(s_{12})$ and other resonances are described by Breit–Wigner amplitudes. In summary, the full partial wave

amplitude for channel (1), as an example, is given by

$$f = \frac{\sqrt{\rho_{\bar{p}p}}}{p} B_\ell(p) B_L(q) \sum_i \frac{G_i}{M_i^2 - s - i M_i \Gamma_i} \times [F(s_{12})Z_{12} + F(s_{23})Z_{23}], \quad (9)$$

where G_i are complex coupling constants and the sum i is over s -channel resonances and background. Fitted parameters are G_i , M_i and Γ_i . The factor $1/p$ accounts for the flux in the entrance $\bar{p}p$ channel, and $\rho_{\bar{p}p}$ is the phase space for this channel, $2p/\sqrt{s}$. Near the $\bar{p}p$ threshold, the S-wave cross section is then proportional to $1/p\sqrt{s}$, the well-known $1/v$ law. In Fig. 4 below, fitted cross sections will be shown multiplied by $ps^{1/2}$, so as to display the resonant behaviour free of kinematic factors. The phase space for the final state is accommodated in fitting the Dalitz plot.

The parameters of each resonance are scanned in at least 7 steps over a range of typically ± 100 MeV. For

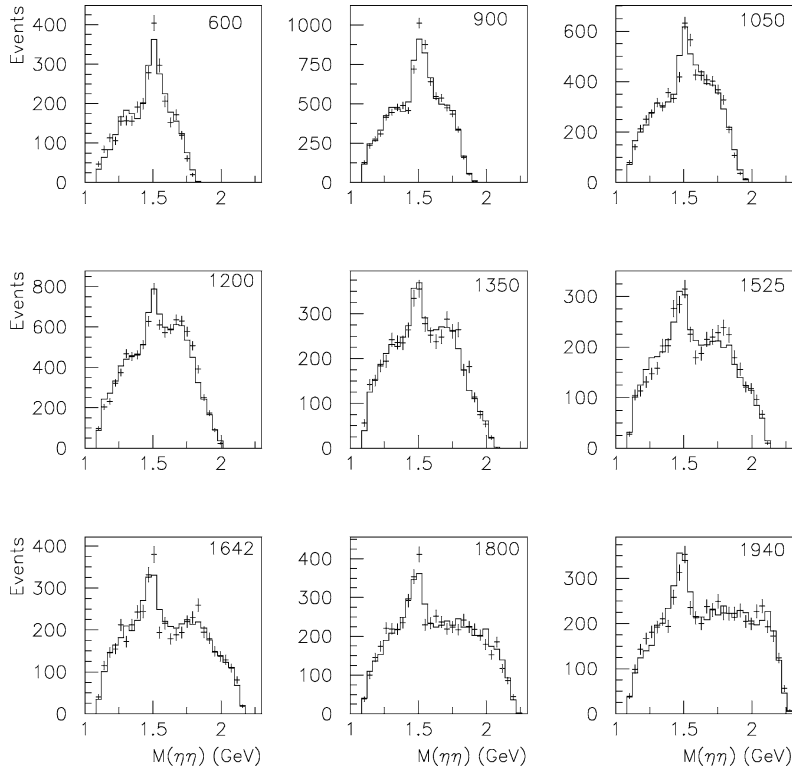


Fig. 3. Projections on to $\eta\eta$ mass; histograms show the partial wave fit. Numbers in each panel indicate beam momenta in MeV/c.

all quantum numbers other than 0^- and 2^- , masses and widths are determined less precisely by $\eta\eta\pi^0$ data than by $3\pi^0$, but are consistent with Ref. [1] within errors. The $3\pi^0$ data have statistics $> 100\,000$ events per momentum whereas present data have typically 5000–9000 events at each momentum.

Columns 3 and 4 of Table 1 summarise masses and widths fitted to present data. Errors cover systematic variations between decay channels; they also cover variations depending on whether small components are included in the fit or are omitted. Table 2 gives a quantitative picture of the significance of each component in the fit. It shows changes in log likelihood when each channel is dropped and the remainder are re-optimised. Our definition of log likelihood is such that it changes by 0.5 for a one standard deviation change in one parameter. Hence a change in log likelihood of 20 is rather significant ($\sim 5\sigma$, bearing in mind the number of fitted parameters).

The black circles on Fig. 4a show the integrated cross section divided by a factor 3, for comparison with those of individual channels. These individual contributions are lower because strong constructive interference between channels contributes positively to the integrated cross section. There is a sizeable cross section for the final state $a_2(1320)\eta$, see the dotted curve of Fig. 4a. However, it does not yield new physics. This channel comes largely from $\bar{p}p$ triplet states with $J^P = 1^+, 2^+$ and 3^+ . Resonances in these partial waves are better determined by $3\pi^0$ data, where statistics are very high and there are strong decays to $f_2(1270)\pi$. The contribution to present data from $J^P = 4^+$ is negligible, probably because of the $L = 3$ centrifugal barriers for both production and decay. There is a small (7%) intensity from $f_2(1270)\pi^0$, but it has little effect on other fitted amplitudes. We find no significant contribution from $f_2'(1525)$ or $f_2(1565)$ at any momentum.

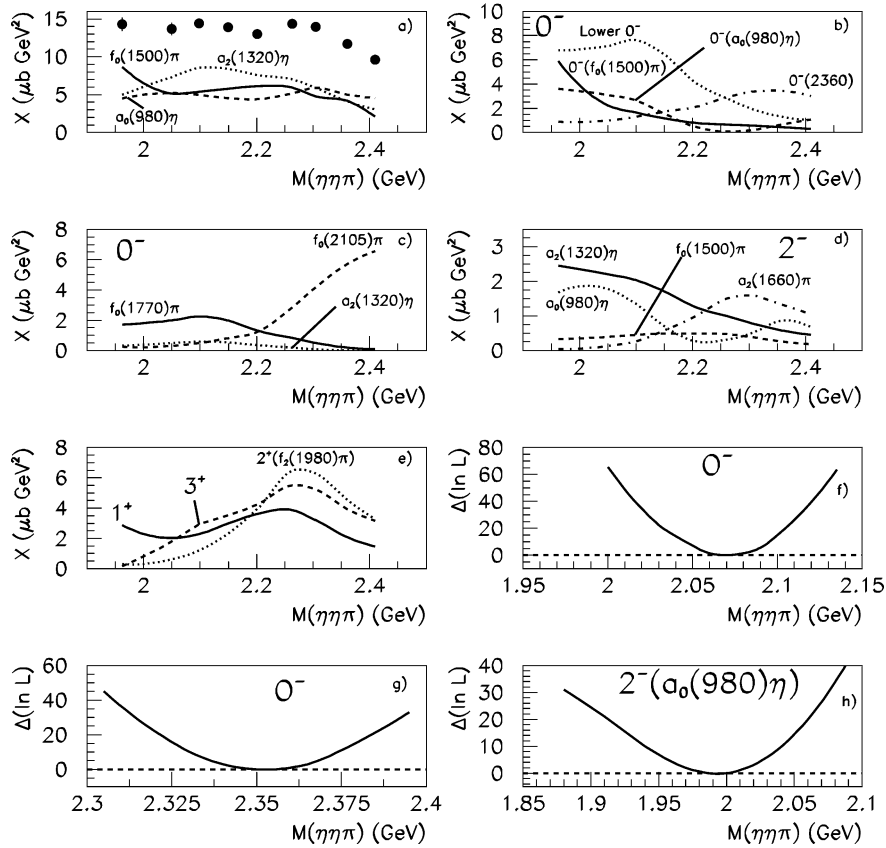


Fig. 4. Values of $X = \text{cross sections multiplied by } ps^{1/2}$ for individual channels. (a) black circles show the overall cross section scaled by $1/3$ for comparison with summed contributions to $f_0(1500)\pi$, $a_2(1320)\eta$ and $a_0(980)\eta$ from all J^P . (b) 0^- contributions: the full curve is the summed intensity from $f_0(1500)\pi$; remaining curves refer to $a_0(980)\eta$; the dashed curve is the combined intensity from all resonances, the dotted curve the coherent sum of $\pi(1800)$ and $\pi(2070)$; the chain curve refers to $\pi(2360)$. (c) and (d): 0^- and 2^- intensities from individual channels. (e): summed 1^+ and 3^+ signals and that from $2^- \rightarrow [f_2(1980)\pi]_{L=1}$. (f), (g) and (h): variations of log likelihood $\ln L$ with mass for $\pi(2070)$, $\pi(2360)$ and the low mass $\pi_2 \rightarrow a_0(980)\eta$ signal.

For $J^P = 0^-$, three resonances are included. One, $\pi(1800)$, is below the $\bar{p}p$ threshold and may simulate physics background. Two further resonances at 2070 and 2360 MeV are needed and are sufficient to provide a good fit to the data. Fig. 4b and c show 0^- contributions to the cross section.

We discuss the highest 0^- state first. It receives large contributions from $f_0(2105)\pi$, shown by the dashed curve on Fig. 4c, and from $a_0(980)\eta$. The $f_0(2105)$ appears only in S-wave production and is very secure. The $f_0(1500)\pi$ channel makes only a small contribution with $J^P = 0^-$ from both resonances at 2360 and 2070 MeV, shown by the full curve

of Fig. 4b. Table 2 shows that $a_0(980)\eta$ makes decisive contributions to both resonances at 2360 and 2070 MeV. For the $a_0(980)\eta$ channel, there is large interference between the upper and lower 0^- resonances; the combined contribution is shown by the dashed curve of Fig. 4b. Despite this interference, contributions from $a_0(980)\eta$ are very stable. This channel and $f_0(2105)\pi$ agree closely on a mass $M = 2355 \pm 25$ MeV for present data. The cross section for production of $f_0(2105)\pi$ rises at high mass faster than phase space for that channel and requires production through $\pi(2360)$. Fig. 4g shows the variation of log likelihood as the mass is varied.

Table 1

Columns 3 and 4 show masses and widths of resonances fitted to $\eta\eta\pi^0$ data. Columns 5 and 6 show masses and widths from weighted averages with fits to $3\pi^0$, $\pi^0\eta$ and $\pi^0\eta'$

Name	J^P	M (MeV)	Γ (MeV)	M (MeV)	Γ (MeV)
π	0^-	2070 ± 35	310^{+100}_{-50}	2070 ± 35	310^{+100}_{-50}
π	0^-	2355 ± 25	270^{+100}_{-50}	2360 ± 25	300^{+100}_{-50}
π_2	2^-	1990 ± 30	290 ± 60	2005 ± 15	200 ± 40
π_2	2^-	–	–	2245 ± 60	320^{+100}_{-40}
π_4	4^-	2255 ± 30	185 ± 60	2250 ± 15	215 ± 25
a_1	1^+	–	–	1930^{+30}_{-70}	155 ± 45
a_1	1^+	–	–	2270^{+55}_{-40}	305^{+70}_{-40}
a_2	2^+	2265 ± 45	295^{+100}_{-60}	2255 ± 20	230 ± 15
a_3	3^+	–	–	2031 ± 12	150 ± 18
a_3	3^+	2260 ± 50	250^{+100}_{-50}	2275 ± 35	350^{+100}_{-50}

All fits with a variety of ingredients give masses in the range 2337 to 2377 MeV. This range is used to assess the systematic error, which is much larger than the statistical error. The fit to $3\pi^0$ data gives a higher but distinctly less accurate mass 2385 ± 45 MeV. The weighted mean of 2360 ± 25 MeV fits both $\eta\eta\pi^0$ data and $3\pi^0$ well. The width is much less well determined: $\Gamma = 300^{+100}_{-50}$ MeV.

At lower masses, there is a sizeable contribution from $a_0(980)\eta$ and also from $f_0(1770)\pi$, shown by the full curve of Fig. 4c. In the previous analysis of Ref. [3], it was shown that $f_0(1770)$ production peaks in the momentum range 900 to 1200 MeV/c. Table 2 shows that $f_0(1770)\pi$ makes a highly significant contribution of 324 to log likelihood. It is particularly useful, since it is again produced only through the S-wave and does not contribute to $\pi(1800)$, which is too low in mass. The cross section for production of $f_0(1770)\pi$ does not follow phase space for that channel, but requires production through the resonance at 2070 MeV; there is very little contribution from the upper 0^- state.

From the present $\eta\eta\pi^0$ data, the optimum parameters of the lower resonance are $M = 2070 \pm 35$ MeV, $\Gamma = 310^{+100}_{-50}$ MeV, where errors are mostly systematic. Fig. 4f shows log likelihood against mass when the background is fitted by $\pi(1800)$. However, the possibility of alternative descriptions of the background introduces a systematic error of ± 35 MeV in the mass determination. The $3\pi^0$ data of Ref. [1] also

Table 2

Changes in log likelihood when each resonance is dropped from the fit, and remaining contributions are re-optimised. In addition $\pi_2(2250) \rightarrow a_2(1660)\pi$ produces a change of 107 and $a_2(2255) \rightarrow f_2(1980)\pi$ a change of 363

Resonance	$a_0(980)\eta$	$f_0(1500)\pi$	$f_0(1770)\pi$	$a_2(1320)\eta$	$f_0(2105)\pi$
$\pi(1800)$	11	82	–	–	–
$\pi(2070)$	272	12	324	126	–
$\pi(2360)$	197	44	9	33	434
$\pi_2(1880)$	–	255	–	176	–
$\pi_2(2005)$	531	–	–	–	–
$\pi_2(2245)$	107	10	–	19	–
$\pi_4(2250)$	213	–	–	–	–
$a_1(1930)$	–	22	–	15	–
$a_1(2270)$	18	77	–	71	–
$a_3(2031)$	15	164	–	185	–
$a_3(2275)$	141	37	–	23	–
$a_2(1950)$	–	–	–	41	–
$a_2(2030)$	–	–	–	48	–
$a_2(2175)$	–	–	–	3	–

require the presence of $\pi(2070)$, but again suffer from interference with a background term. From those data, the optimum is at 2090 ± 65 MeV; the width is large and poorly determined, 285 ± 75 MeV. Both sets of data are well fitted with a mass of 2070 ± 35 MeV.

The two 0^- states lie rather higher in mass than corresponding $I = 0$ states [4]. These were observed at 2010^{+35}_{-60} and 2285 ± 20 MeV. In Ref. [4], all states were found to lie close to straight-line trajectories of M^2 against radial excitation number, with an average slope of 1.143 ± 0.013 GeV² per excitation. The spacing of the two 0^- states observed here is consistent with this empirical rule. One cannot compare accurately with $\pi(1300)$ because of the large uncertainty in its mass. The $\pi(1800)$ is consistent in mass with the required intermediate state, but there is evidence from its decay modes in favour of interpretation as a hybrid [7]. The VES group has also reported evidence in $\omega\rho$ for a 0^- state at 1750 MeV; this is a favoured decay mode for $q\bar{q}$ states [7] and may be the second radial excitation.

We turn now to quantum numbers $J^P = 2^-$. In an earlier publication on the channel $\eta\eta\pi^0\pi^0$ [8],

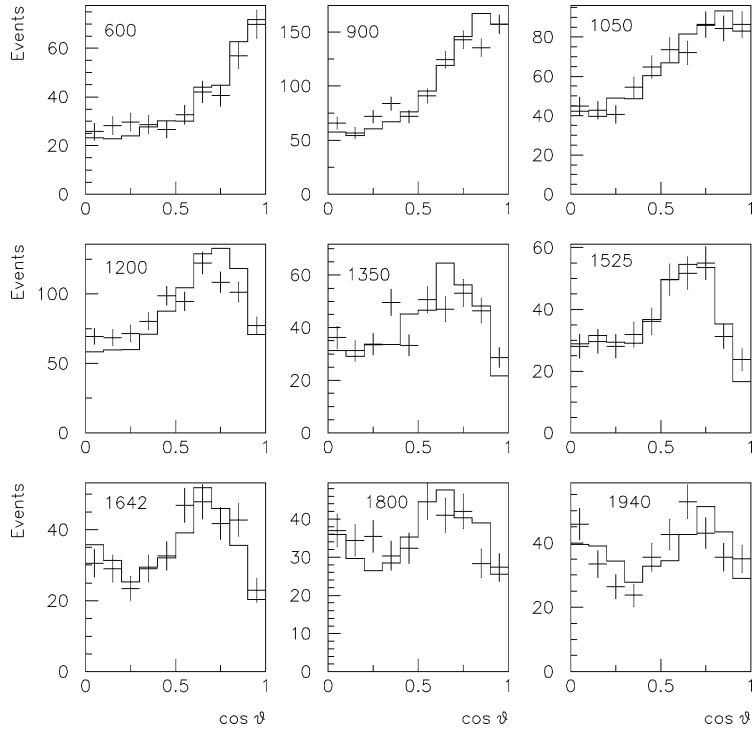


Fig. 5. Angular distributions for production of $a_0(980)$ for events in the $\eta\pi$ mass range 960 to 1020 MeV; histograms show the partial wave fit. Numbers in each panel indicate beam momenta in MeV/c.

we reported evidence for a π_2 with $M = 1880 \pm 20$ MeV, $\Gamma = 255 \pm 45$ MeV, decaying dominantly to $a_2(1320)\eta$. Here, we again find a strong $a_2(1320)\eta$ S -wave contribution shown by the full curve of Fig. 4d; the $2^- \rightarrow [a_2\eta]_{L=0}$ amplitude is distinctive because of its $P_2(\cos\alpha)$ dependence on the decay angle α for $a_2(1320) \rightarrow \eta\pi$. The fitted mass and width for this amplitude are closely consistent with those for $\pi_2(1880)$. The contribution to $f_0(1500)\pi$, shown by the dashed curve in Fig. 4d, is consistent at low masses with the small branching ratio observed for $\pi_2(1880)$ to that channel in Ref. [8].

However, we observe here an additional $a_0(980)\eta$ contribution with $J^P = 2^-$, considerably larger than that allowed in $\eta\eta\pi^0\pi^0$ data of Ref. [8]. It would be conspicuous there, but is absent. Its fitted magnitude in present data is shown by the dotted curve in Fig. 4d. Table 2 shows that it makes a very large improvement in log likelihood, namely 531. Both $a_0(980)\eta$ and $f_0(1500)\pi$ signals for $J^P = 2^-$ are

clearly recognisable from their production amplitude $P_2(\cos\theta)$, which interferes distinctively with the large 0^- amplitudes; this interference is clearly visible at the lowest momenta in the angular distribution against production angle θ in Fig. 5.

If the $2^- \rightarrow [a_0\eta]_{L=2}$ channel is fitted freely, it optimises at $M = 1990 \pm 30$ MeV with a width of 290 ± 60 MeV. The variation of log likelihood with mass is shown in Fig. 4h. Errors quoted for mass and width allow for the possibility of moving an $a_0\eta$ contribution into $\pi_2(1880)$ consistent with the upper limit from Ref. [8]. If the mass and width are set to those of $\pi_2(1880)$, despite the evidence in Ref. [8] against decays of $\pi_2(1880)$ to $a_0(980)\eta$, log likelihood is worse by 31. For two degrees of freedom, this is more than a 7σ effect.

There is further evidence for two distinct π_2 states from the $3\pi^0$ data. They require a strong $f_2(1270)\pi$ amplitude with $L = 2$, consistent in mass and width with $\pi_2(1880)$. The $f_2(1270)\pi$ amplitude with $L = 0$

peaks at a higher mass 2020 ± 17 MeV with $\Gamma = 165 \pm 35$ MeV. The width is considerably less than found here. However, both those data and $\eta\eta\pi^0$ are well fitted with a compromise mass $M = 2005 \pm 15$ MeV and width 200 ± 40 MeV, together with $\pi_2(1880)$.

We have earlier found similar evidence for two neighbouring $I = 0, J^P = 2^-$ states, $\eta_2(1860)$ and $\eta_2(2030)$ [9]. The $\eta_2(1860)$ has been confirmed by WA102 [10]. Two neighbouring $J^P = 2^-$ states with $I = 1$ and different decay modes are then a clear possibility. If the spacing in mass squared follows the empirically observed 1.143 GeV^2 , the radial excitation of $\pi_2(1670)$ is expected at 1985 ± 20 MeV. Because two separate π_2 candidates in a narrow mass range require one of them to be an intruder state (probably the predicted hybrid), and because both lie at the bottom of our available mass range, we acknowledge that confirmation is desirable. We present the evidence so that other experimental groups should be alert to the possibility of two separate states. Present data are consistent with $\pi_2(1880)$ accounting for the entire $a_2(1320)\eta$ and $f_0(1500)\pi$ signals; however, we cannot rule out the possibility that these two channels are also fed in the present data partly by the second state at 2005 MeV.

For other quantum numbers, the $\eta\eta\pi^0$ data are consistent with resonances required by the analysis of $3\pi^0$. There is a small but highly significant 3^+ peak at 2260 ± 50 MeV in the dashed curve in Fig. 4e. Despite large errors for mass and width, this is additional evidence that a 3^+ resonance exists in this mass range. Likewise, there is a distinct peak in the 2^- amplitude for production of $a_2(1660)\pi$, shown by the chain curve of Fig. 4d; unfortunately, the determination of mass and width are poor, both here and in $3\pi^0$ data. There is a distinct 4^- signal in $a_0(980)\eta$; Table 2 shows that it produces a large improvement in log likelihood of 213. It optimises at 2255 ± 30 MeV in present data, very close to the value 2250 ± 15 MeV for $3\pi^0$ data, where there is a large 4^- signal. For $J^P = 1^+$, shown by the full curve in Fig. 4e, there is a definite signal at the higher masses; this is evidence in favour of the state required in the analysis of $3\pi^0$ data at 2270 MeV. At the bottom of the mass range, a second 1^+ state gives a small improvement of 37 in log likelihood. This improvement is sufficient to require some additional low mass contribution, but is not suf-

ficient to determine the mass and width of any possible resonance. Table 2 includes small contributions from 2^+ states at 1950, 2030 and 2175 MeV; those states are required by $3\pi^0$ data, but contributions to $\eta\eta\pi^0$ are too small to help determine masses and widths.

A distinctive feature of the $\eta\eta\pi^0$ data from 1350 to 1940 MeV/c is that they require a strong contribution from a broad $f_2(1980)$ decaying to $\eta\eta$, channel (7). It is clearly visible by eye in the angular distributions for decay to $\eta\eta$, see Fig. 4 of Ref. [2]. The data required the curious property that the $f_2(1980)$ is produced almost purely with spin projection $m' = \pm 1$ along the beam direction in the final state. The present analysis confirms this result but clarifies the reason for the helicity dependence.

The large contribution from this state is shown by the dotted curve on Fig. 4e. It peaks at ~ 2265 MeV, and is well fitted by an $a_2(2255)$ which appears strongly in the analysis of $3\pi^0$, $\pi^0\eta$ and $\pi^0\eta'$ data. We find that the broad $f_2(1980)$ is produced purely by this $a_2(2255)$ decaying to $f_2(1980)\pi$ with $L = 1$. It has a ratio of coupling constants g between 3F_2 and 3P_2 amplitudes of $r_2 = g({}^3F_2)/g({}^3P_2) = -1.9 \pm 0.4$ for present data; this ratio agrees well with the value -2.13 ± 0.20 determined in Ref. [1]. With this value of r_2 , the final state will be almost purely $m' = \pm 1$ for the following reasons. Clebsch–Gordan coefficients for coupling of $\bar{p}p$ to 3F_2 and 3P_2 are such that the initial state will be purely $m = 0$ if $r_2 = -\sqrt{7/2} \simeq -1.9$. The $m = 0$ state decays purely to final states with $m' = \pm 1$, again because of Clebsch–Gordan coefficients. Thus, the curious property that the $f_2(1980)$ is produced almost purely with $m' = \pm 1$ seems to be a fortuitous consequence of the fact that the $a_2(2255)$ has r_2 close to -1.9 .

Figs. 5 and 6 show production angular distributions for $a_0(980)\eta$ and $f_0(1500)\pi$, selecting events within one half-width of the resonance mass. All are fitted quite well. Production and decay angular distributions for $a_2(1320)\eta$ are illustrated in our previous publication [3] and are also well fitted.

In summary, a partial wave analysis of $\eta\eta\pi^0$ data gives masses and widths for s -channel resonances consistent with those found in the analysis of $3\pi^0$ data, $\pi^0\eta$ and $\pi^0\eta'$ [1]. For $J^P = 0^-$, the $\eta\eta\pi^0$ data give the best determination of the mass and width of the state at 2360 MeV. An additional 0^- state at lower mass is also required; data from $3\pi^0$ and $\eta\eta\pi^0$ are both well

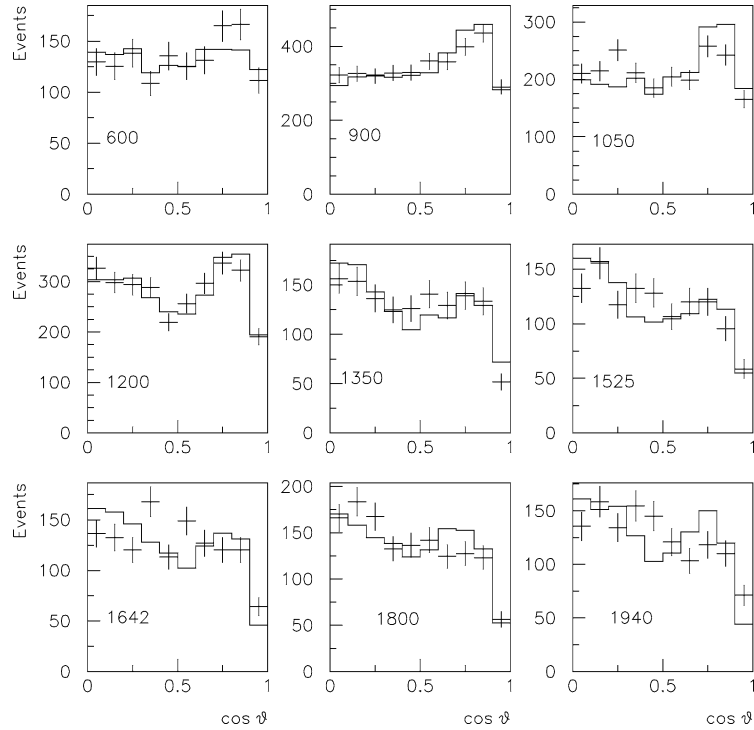


Fig. 6. Angular distributions for production of $f_0(1500)$ in the overall centre of mass for events lying within ± 60 MeV of the resonance; histograms show the partial wave fit. Numbers in each panel indicate beam momenta in MeV/c.

fitted with an average mass of 2070 ± 35 MeV. There is definitely a strong $J^P = 2^-$ amplitude in the $a_0(980)\eta$ channel at low masses, much stronger than observed in Ref. [8] for $\pi_2(1880)$. It suggests a second 2^- state at ~ 2005 MeV, but needs confirmation because both 2^- states are near the bottom of the available mass range.

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