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## Online/Offline Blind Signature

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### Abstract

The processing ability and response speed of the wireless communication terminals are limited, common signatures become the bottleneck to the development of the wireless networks. For that problem, based on the characteristics of the blind signature, the online/offline blind signature is given in this paper which incorporates with the optimal online/offline signature. Most computations are finished before the blind message is given, after that, only a few operations are needed. The performance analysis is also given in this paper, the new signature scheme can be applied to the security of wireless network, it protect the users' privacy efficiently.

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*Keywords:* bilinear map; online/offline signature; blind signature

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### 1 Introduction

Digital signature schemes play an important role in information security and have exhibited many applications. However, the computation of signature requires a private computer with a reasonable computation power. In practice, there could be a situation, where such a computer is not available.

In order to further reduce the computational cost of signature generation, online/offline signature is preferable in wireless network. Even, Goldreich and Micali proposed a general method for converting any signature scheme into an online/offline signature scheme. The signature can be divided into two parts which are the offline signature and the online signature. In the process of the offline signature, almost all of the calculations are done before the blind message is given. And in the following process of the online signature, only small quantities of computations are needed after the blind message is available. However, the method is impractical since it increases the size of the signature by a quadratic factor. Later, Shamir [1] proposed a new method called 'hash-sign-switch' for designing more efficient schemes. The calculation of

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online phase is one tenth of the modular multiplication. The scheme can resist the chosen message attack but has a problem of the trapdoor leak. Chen[2] proposed a online/offline scheme with double trapdoor hash functions, which can solve the problem of trapdoor leak. Harm[3] introduce the trapdoor function of multi collision in online/offline signature which can sign a variety of message. Gao[4] proposed a scheme which can directly convert the trapdoor hash functions into online/offline signatures. The whole computation in Gao's scheme is half of the computation in Shamir's scheme. Girault proposed GPS scheme[5] in which the length of secret key is short and the operation in online phase is on the integers not the modular calculation, so its efficiency is more efficient than Shamir's scheme. Chevallier-Mames and Joye respectively put forward their schemes in[6][7], which efficiency is the same to the GPS. Guo[8] proposed the optimal online/offline signature which is more efficient than GPS's scheme.

Blind signature[10][11][12] is a special digital signature for the signer doesn't know the specific content of the document. The technology of blind signature has been used widely(e.g. the electronic voting system, electronic cash system, etc.). The blind signature was first proposed by Chaum, which is to make the signature to sign for the blind message. The blind signature can protect the users' privacy for the signer doesn't know the original message and the signer cannot link up the signature with the original message.

Based on the optimal online/offline signature in Guo's scheme, a new scheme proposed in this paper which can convert blind signature into online/offline blind signature that can effectively protect the users' and the merchants' privacy.

## 2 Related works

### 2.1 Bilinear Map

Let  $G$  and  $G_T$  be two cyclic groups of prime order  $p$ . Let  $g$  be a generator of  $G$ . A map  $e: G \times G \rightarrow G_T$  is called a bilinear map if this map satisfies the following properties:

- (1) Bilinear: for all  $u, v \in G$ ,  $a, b \in Z_q$ , we have  $e(u^a, v^b) = e(u, v)^{ab}$ .
- (2) Non-degeneracy:  $g$  is the generator of  $G$ , then  $e(g, g) \neq 1$ .
- (3) Computability: It is efficient to compute  $e(u, v)$  for all  $u, v \in G$ .

### 2.2 Blind message

User dispose the original message  $M$  into  $\tilde{M}$  called blind message and give it to the signer. For example, randomly choose an integer  $d$ , set  $\tilde{M} = dM$ , the integer  $d$  is called blind factor. As the signer does not know the blind factor, the message is blind to signer.

### 2.3 basic online/offline signature

**Definiton 1:** Guo proposed basic online/offline signature which based on Water's scheme of signature[9]. The security of Guo's signature is attributed to the GDH problem. Here we call it on/offline-w scheme which can be described as follows:

**Initialize:** Run the system and output  $q, e, G, G_T$  and bilinear map  $e: G \times G \rightarrow G_T$ , the prime order of  $G$  is  $q$  and the generator is  $g$ . And  $u_0, (u_{10}, u_{11}), (u_{20}, u_{21}), \dots, (u_{n0}, u_{n1})$  are the other random generators. The public params are defined as the following tuple:

$$\text{params} = \{e, q, G, G_T, u_0, (u_{10}, u_{11}), (u_{20}, u_{21}), \dots, (u_{n0}, u_{n1})\}.$$

**KeyGen:** Randomly choose an integer  $\beta \in Z_q$ , and compute the secret key  $SK = g^\beta$ , the public key  $PK = e(g^\beta, g)$ .

**Sign:** The signing is divided into the offline phase for pre-computation and the online phase. Compute most computations in offline phase and store the offline datas which are as the outputs of online phase.

Offline phase: Signer input the secret key and params.

(1) Randomly choose two n-length vectors  $(\mu_1, \dots, \mu_n)$  and  $(v_1, \dots, v_n)$ , such that

$$(\mu_1 + \dots + \mu_n) = (v_1 + \dots + v_n) = 1 \pmod{q}$$

(2) Randomly choose  $r \in Z_q$ , compute  $\tau = g^r$  and the following  $2n$  values:

$$(s_{i0}, s_{i1}) = (g^{\mu_i \beta} (u_0^{v_i} u_{i0})^r, g^{\mu_i \beta} (u_0^{v_i} u_{i1})^r), \text{ for } i=1, 2, \dots, n;$$

(3) Store the following  $2n+1$  elements:

$$w = ((s_{10}, s_{11}), \dots, (s_{n0}, s_{n1}), \tau)$$

Online phase: Given the message  $M \in \{0, 1\}^n$ , let  $M[i]$  be the  $i$ th bit of  $M$ , the signature is generated as follows:

$$(1) \text{ compute } s = \prod_{i=1}^n s_{iM[i]} = \prod_{i=1}^n g^{\mu_i \beta} (u_0^{v_i} u_{iM[i]})^r = g^\beta (u_0 \prod_{i=1}^n u_{iM[i]})^r$$

(2) output the last signature  $(s, \tau)$ .

**Verify:** input  $(M, s, \tau)$ , accept the signature if the following equation holds

$$e(s, g) = e(g^\beta, g) e(u_0 \prod_{i=1}^n u_{iM[i]}, \tau)$$

### 3 Our scheme

#### 3.1 Model of the scheme

**Definitions 2:** The model of our scheme contains the following several parts: Setup, KeyGen, Blind, Sign, Verify. Here the signature that we construct is called online/offline-b-s scheme which can be described as the following.

**Initialize:** Output public params.

**KeyGen:** Input public params, and output public key and the secret key.

**Blind:** User converts the original message  $M$  into the blind message  $\bar{M}$  and then transfer it to the signer.

**Sign:** This algorithm is divided into two phases:

**Offline phase:** Input the secret key and public params, output the offline-datas and store them.

**Online phase:** Input the blind message  $\bar{M}$  and the datas in offline phase, after some simple computations, output the signature on the blind message. And the last signature is a set of the signature and some related coefficients.

**Verify:** Input the original message  $M$  and the last signature, if the equation holds and then accept the signature.

#### 3.2 Scheme construction

**Setup:** run the system,  $h$  is a strong hash function without collision,  $h: \{0, 1\}^* \times Z_q \rightarrow \{0, 1\}^n$ .  $G$  and  $G_T$  are cyclic groups of prime order  $q$ ,  $g$  and  $u_0$  are the generators of  $G$ , randomly choose  $n$  different pairs of generators of  $G: (u_{10}, u_{11}), (u_{20}, u_{21}), \dots, (u_{n0}, u_{n1})$ . Output the public params:

$$\text{params} = \{e, q, G, G_T, g, u_0, (u_{10}, u_{11}), \dots, (u_{n0}, u_{n1})\}$$

**KeyGen:** Randomly choose integer  $\beta \in Z_q$ , compute the secret key  $g^\beta$ , and  $e(g^\beta, g)$  as the public key.

**Blind:** User randomly choose integer  $d \in Z_q$ , compute  $\bar{M} = h(M, d)$ .

**Sign:** The two phases are the offline phase and the online phase.

Offline phase: the blind message is not given.

(1) Randomly choose two n-length vectors  $(\mu_1, \dots, \mu_n) \in Z_q$  and  $(v_1, \dots, v_n) \in Z_q$ , such that

$$(\mu_1 + \dots + \mu_n) = (v_1 + \dots + v_n) = 1 \pmod{q}$$

(2) Randomly integer  $r \in Z_q$ , compute  $\tau = g^r$  and the other 2n values of offline phase

$$(s_{i0}, s_{i1}) = (g^{\mu_i \beta} (u_0^{v_i} u_{i0})^r, g^{\mu_i \beta} (u_0^{v_i} u_{i1})^r), \text{ for } i=1, 2, \dots, n.$$

(3) Store the offline-datas  $w = ((s_{10}, s_{11}), \dots, (s_{n0}, s_{n1}), \tau)$

Online phase: after the blind message  $\bar{M}$  is given,  $\bar{M} \in \{0, 1\}^n$ ,  $\bar{M}[i]$  is the ith bit of  $\bar{M}$ .

(1) In accordance with  $\bar{M}[i]$ , choose  $s_{i\bar{M}[i]}$  from w, and then compute signature  $s = \prod_{i=1}^n s_{i\bar{M}[i]}$

(2) Output the last signature  $(M, \tau, d, s)$ .

**Verify:** Input  $(M, \tau, d, s)$ , and check the equation.

(1) Compute  $M_0 = h(M, d)$ ,  $M_0[i]$  is the ith bit of  $M_0$ .

(2) Accept the signature if the equation holds:  $e(s, g) = e(g^\beta, g) e(u_0 \prod_{i=1}^n u_{iM_0[i]}, \tau)$

## 4 Performance analysis and application

### 4.1 Performance analysis

**Blind:** The message that signer receives is the blind message  $\bar{M}$  not the original message M, so the message is blind to him. It is impossible to regain the original message M from the blind message  $\bar{M}$  for  $\bar{M} = h(M, d)$ , and not only the blind factor d is unknown to the signer but also the hash function is irreversible. Even if the original message M is published, the signer cannot make association with M and  $\bar{M}$ , and then cannot make association the signature with M.

**Verifiability:** Given the message M and  $(\tau, d, s)$ , and compute  $e(s, g)$  whose expansions are as the following:

$$\begin{aligned} e(s, g) &= e\left(\prod_{i=1}^n s_{i\bar{M}[i]}, g\right) = e\left(\prod_{i=1}^n g^{\mu_i \beta} (u_0^{v_i} u_{i\bar{M}[i]})^r, g\right) \\ &= e\left(g^{(\mu_1 + \dots + \mu_n) \beta} (u_0^{(v_1 + \dots + v_n)}) \prod_{i=1}^n u_{i\bar{M}[i]}^r, g\right) \\ &= e\left(g^\beta (u_0 \prod_{i=1}^n u_{i\bar{M}[i]})^r, g\right) = e(g^\beta, g) e\left((u_0 \prod_{i=1}^n u_{i\bar{M}[i]})^r, g\right) \\ &= e(g^\beta, g) e(u_0 \prod_{i=1}^n u_{i\bar{M}[i]}, g^r) = e(g^\beta, g) e(u_0 \prod_{i=1}^n u_{i\bar{M}[i]}, \tau) \end{aligned}$$

after neatening the expansions, we get that:  $e(s, g) = e(g^\beta, g) e(u_0 \prod_{i=1}^n u_{i\bar{M}[i]}, \tau)$ .

Compute  $M_0 = h(M, d)$ , if the signature is effective,  $M_0$  and  $\bar{M}$  are same, the  $M[i]$  and  $M_0[i]$  are same. Then we have the following equation:

$$e(s, g) = e(g^\beta, g)e(u_0 \prod_{i=1}^n u_{iM[i]}, \tau) = e(g^\beta, g)e(u_0 \prod_{i=1}^n u_{iM_0[i]}, \tau)$$

#### 4.2 Efficiency and application

In our online/offline-b-s scheme, as most computations have been done in offline phase, so we only analysis the efficiency in online phase. Different from other online/offline signatures, the computation is only the simple multiplication not the exponentiation.

Our online/offline-b-s can be applied to the wireless network with that the computational capabilities are limited, the scheme can effectively solve the drawback of the wireless terminals in communication. In the offline phase, the computations are done on the terminals with strong processing capacity or in the time when the terminals are vacant. Only a few simple computations are needed after message is given. And online/offline-b-s is also a kind of blind signature, the signer cannot know the content in ocument, so the secret information is protected, for which reason the scheme can applied to the Wireless Mobile Internet(e.g. the wireless e-voting system and e-cash system,etc.).

### 5 Conclusion

The online/offline-b-s is high-efficiency, and the essence of blind signature is that the signer doesn't know the original content of the message. In the fields where the time of message-signing is limited and the computational capability is weak(e.g. wireless sensor network), the scheme is practicable. The future work is to design more secure and more efficient online/offline signature.

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