The Spontaneous Loss of Coherence Catastrophe in Fourier Transform Ion Cyclotron Resonance Mass Spectrometry

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The spontaneous loss of coherence catastrophe (SLCC) is a frequently observed, yet poorly studied, space-charge related effect in Fourier-transform ion cyclotron resonance mass spectrometry (FTICR-MS). This manuscript presents an application of the filter diagonalization method (FDM) in the analysis of this phenomenon. The temporal frequency behavior reproduced by frequency shift analysis using the FDM shows the complex nature of the SLCC, which can be explained by a combination of factors occurring concurrently, governed by electrostatics and ion packet trajectories inside the ICR cell. (J Am Soc Mass Spectrom 2009, 20, 247–256) © 2009 Published by Elsevier Inc. on behalf of American Society for Mass Spectrometry

Since the introduction of the soft ionization methods [1–3], mass spectrometry has been steadily gaining prominence, and is currently one of the most important experimental techniques in the biosciences. It is impossible to imagine contemporary proteomics, genomics, or glycobiology without mass spectrometric analytical methods. There is an increasing number of different types of mass spectrometers and hybrid instruments being developed and deployed every year, starting from simple quadrupole [4] instruments up to hybrid Fourier transform mass spectrometers (FTICR MS) [5–8].

In general, requirements for higher mass accuracy and resolving power of the contemporary mass spectrometers are becoming more and more pronounced [9]. As studies have shown [10, 11], proteomic experiments require sub-ppm mass accuracy for unique determination of peptide amino acid composition. Currently FTICR MS [12, 13] instruments are established leaders in mass accuracy and resolving power, capable of achieving \sim 1 ppm accuracy internally calibrated [14– 17] and \sim 5 ppm externally calibrated [18, 19] under normal conditions, yet routine measurements in the sub 0.1 ppm region have not yet been reported. It is a substantial challenge for instrumentation, theorists, and experimental scientists to break through this 100 ppb "barrier".

The major contributor to mass error in FTICR MS is space-charge—a phenomenon rising from the coulombic interaction between and within ion clouds in the ion cyclotron resonance (ICR) cells [65]. Frequency shifts due to space-charge were reported to be greater than ± 400 ppm within an isotopic beat [20], which affects both position and width of the peaks, although these periodic shifts tend to mostly average out over a long transient. Substantial effort has been invested and there have been previous attempts to study it in situ [21, 22], yet the phenomenon remains poorly studied due to its rather fast nature, which requires frequency shift analysis on very short segments of transient signals. Most of the widely used signal processing techniques are not applicable to the task. For Fourier transform (FT) based techniques such as the FFT [23], wavelet and chirplet transforms [24], and the shifted basis technique [25], the limiting factor is the FT uncertainty principle [26]. For such high-resolution techniques as linear prediction [27, 28] and Prony method-based techniques [29, 30], the limiting factors are the time complexity of the calculations and poor tolerance for noise, which generate false positives (hence rendering these techniques impractical for experimental data).

The filter diagonalization method (FDM) [31–39] is a recent addition [20] to the repertoire of computational techniques in mass spectrometry, which addresses these issues. Like the FFT, it finds a solution for the generic harmonic inversion problem [37] (HIP) eq 1,

$$C(t_n) = c_n \equiv \sum_{k=1}^{K} d_k e^{-in\tau\omega_k},$$
(1)

where the d_k 's and ω_k 's are complex amplitudes and complex frequencies respectively, and $C(t_n)$ is a time signal defined on an equidistant time grid $t_n = n\tau$, n = 0, 1, ..., N - 1, where *N* is the number of data points, τ

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is the time step, and complex frequencies $\omega_k = 2\pi f_k - i\gamma_k$ include damping γ_k .

Because FDM's resolution depends not on the length of the transient signal, but rather on the local peak density [38], it bypasses the FT uncertainty principle [32] and is thus capable of operating on very short transients. Even 1000 data points (1 ms with a 1 MHz acquisition rate) can provide sufficient information for the FDM to produce resolution defined only by the damping constant γ_k (eq 1) in frequency, and consequently, in mass domains [20], while having the similar time complexity in computation to the FFT. It is reliable under noisy conditions [39], and it reproduces complete information about a peak, namely position, amplitude, width, decay parameter, and phase. All of these factors make it an ideal technique for studying rapid spacecharge induced frequency modulations in FTICR MS.

This manuscript presents application of the FDM to the study of a space-charge related frequency behavior of ion clouds in ICR called the spontaneous loss of coherence catastrophe (SLCC), colloquially known as the "nipple effect". Unlike the theoretical behavior of a transient signal that decays exponentially (Figure 1a) or that acquired under near ideal conditions (Figure 1b), during the SLCC, a transient starts off with exponential decay, but at some point, which can be somewhat controlled by changing the number of ions in the cell, the transient collapses and dies out rather quickly (Figure 1c), forming a nipple-like shape. This is a space-charge related phenomenon, which directly depends on the number of charges in the ICR cell, an observation which was also reproduced by computer simulations [40]. When the number of charges is relatively low, the nipple effect is not observed in the experimental lifetime (Figure 1b). On the other hand, it is easy to reproduce this particular behavior (Figure 1c) by overloading the cell. Understanding of the ion cloud's behavior during the SLCC should give insight into its behavior under high space-charge conditions in general, which potentially can be used in modeling, deconvolution, and data reduction in FTICR MS, improving mass accuracy and resolution.

Methods

The experiments were conducted on custom MALDI-FTICRMS [41] and ESI-qQq-FTICRMS [6, 8] instruments, both based on 7 T actively shielded superconducting magnets (Cryomagnetics, Oak Ridge, TN), and each equipped with capacitively coupled cylindrical cell [42] with additional external trapping plates. All the



Figure 1. Examples of the transient signals: (**a**) hypothetical exponentially decaying sinusoidal signal; (**b**) transient of a high-resolution substance-P spectrum; (**c**) an example of SLCC where a period of exponential decay is followed by a rapid noncorrelated decay.

experiments were conducted in the positive ion mode. The ions were trapped with +15 V during the excite event, but the potential was lowered to +1 V during detection. The MALDI instrument is equipped with 355 nm Nd:YAG laser, a novel modular data system [43], a low noise amplifier [44], and a 16 bit ADC, with ion optics consisting of a pair of hexapoles driven by RF oscillators [45, 46], and separated by a thin gate valve [47]. The analytes and matrices used in the experiments, substance P (MW 1347), renin substrate (MW 1759), angiotensinogen (1-13) (MW 1645.9), cesium iodide, 2,5-dihydroxy benzoic acid (DHB), and sinapinic acid (SA) were purchased from Sigma Chemical Co. (St. Louis, MO).

For all the MALDI experiments, DHB and SA were dissolved in methanol:acetonitrile:water (2:2:1) to make saturated solutions. For each sample, 0.5 uL of the 10 μ M standard aqueous solution was applied on a target on top of the matrix crystals using the dried droplet method [48]. The acquisition rate was set at 1 MHz, and up to 4 s transients were stored.

Electrospray solutions of Substance-P were prepared in 49:49:2 methanol:water:formic acid solvents and that of cesium iodide in 70:30 water:methanol. The isolation of the species of interest was done in Q1. The ions were axially cooled by pulsing Nitrogen gas twice (2 ms pulse, 2 mbar backing pressure, pulsing to 1.4×10^{-5} mbar in the cell) into the cell during a 2 min cool down period after ion injection into the cell and before the excitation event. Substance-P 25 s transients were acquired in heterodyne mode at 10 kHz sampling rate and those of cesium iodide at 4 MHz (direct detection mode) using IonSpec electronics.

The ESI-FTICR mass spectrometer [6, 8] used in this study is a hybrid instrument with a triple quad front end, consisting of mass resolving quadrupole, ion accumulation, and collision cell linear trap, and a transmission quadrupole coupled with a set of ion guide hexapoles via the thin gate valve [47]. The instrument is equipped with the electron gun for ECD [49–52] experiments, which was used in all the electron promoted ion coherence (EPIC) [53–55] experiments. The electron beam was turned on during the detection event only. The current on the electron gun heater was set at 1.2 A, 4.7 V, and the voltage on the reflector was set at -1.0 V to propel electrons into the cell, while kept at +7.0 V otherwise.

Data analysis was performed on the latest release of the Boston University Data Analysis (BUDA) [56] system (soon to be available online). All frequency chasing experiments were performed using an FFTW-based [57], in-house C++ implementation of the FFT square window FDM [20] integrated into BUDA.

To produce the frequency behavior picture, frequency shift calculations [20] were conducted on the acquired spectra. For the angiotensinogen transients, the monoisotopic peak at ~65 kHz was monitored. The parameters for FDM used were: K_{win} of 7, 5 ms (5000 data points) of the time domain window, stepping 5 ms (5 data points) into

the transient. For the frequency shift analysis, the cesium iodide (Cs₁I₂+) 272.7 kHz peak was studied, with K_{win} of 5, 0.75 ms (3000 data points) of the time domain window, stepping 1 μ s (4 data points) into the transient.

Results

An illustration of different time domain signals is presented in Figure 1. A transient of a hypothetical exponentially decaying harmonic signal is shown in Figure 1a. Figure 1b shows a nearly ideal experimental transient of Substance-P, and 1c is an example of the SLCC transient of Substance-P with its characteristic concave shape.

The application of EPIC can eliminate the SLCC altogether. Figure 2a shows the example of the nipple effect in the course of ESI-FTICRMS experiment. By turning the electron beam on during the detection, yet keeping all the other experimental conditions the same, it was possible to achieve a nearly ideal exponentially decaying signal (Figure 2b), which looks almost identical to that in Figure 1a.

Figure 3a shows the ESI-FTICR frequency spectrum of an isolated Cs_2I_1 + cluster and its time domain signal (see the insert). An FDM frequency shift calculation is shown in Figure 3b. To detect periodic frequency modulations, the FFT was performed on the frequency shift calculation results. Figure 4 presents Fourier transforms of the frequency shift calculations conducted on the cesium iodide signals without (Figure 4a) and with (Figure 4b) the electron beam. There are two general regions in the frequency domain where modulations were stable and systematic. The major peak is at double that of axial frequency (the factor of two is due to the cell's symmetry in Z direction), which should be in the vicinity of 700 Hz [58]. The minor peak is centered at the native ICR frequency in the standard Cs_2I_1 + spectrum, but is conspicuously absent in the Cs_2I_1 + EPIC signal.

Frequency shift analysis calculations using FDM of the SLCC angiotensinogen signals (Figure 5a) are shown in Figure 5 reproduce the evolution of the amplitude (I, II) and frequency (III) parameters of the induced harmonic signal (damping constant and phase are also produced by FDM but are omitted due to the clutter produced by isotopic beat pattern [59, 60] and noise). The temporal behavior of the amplitude, d_k from eq 1 follows exactly the outline of the transient signal in pre- as well as post-nipple stages).

The frequency behavior of the ions (Figure 5b, c III) through the SLCC has several signature features. Initially, frequency spikes are observed, which correspond in time with minima in the time domain transient isotopic beat pattern. These frequency spikes increase in magnitude with time (Figure 5b III), whereas the baseline stays relatively constant. Later, during the SLCC, these spikes "flip" becoming negative dips (Figure 5c III). The dips also coincide with the amplitude minima. This behavior is consistent, and a second set of data is



Figure 2. An illustration of an effect EPIC has on SLCC: (a) a SLCC during substance-P signal acquisition; (b) complete elimination of SLCC by applying EPIC (all other experimental parameters are kept the same).

available in the supplementary materials, which can be found in the electronic version of this article.

Figure 6a presents a simple plot of the inhomogeneities of the electric field inside the ICR cell experienced by a coherently excited ion cloud. As long as the contributions of magnetron and axial motions are small (orbit I), an ion packet does not experience much deviation from the largely hyperbolic electric field as it progresses through its cyclotron orbit. On the other hand, when both magnetron and ion axial contributions



Figure 3. (a) A frequency domain spectrum and the transient of an isolated cesium iodide cluster and (b) the frequency shift modulation calculations of the ICR peak at 272.75 kHz.



Figure 4. A Fourier Transform of the frequency shift calculations (see Figure 3b) conducted on the cesium iodide signals acquired without (a) and with (b) application of EPIC.

become significant (illustrated in extremis in orbit II), ion packets travel through highly inhomogeneous regions of the ICR cell. Figure 6b presents a schematic representation of an ion packet being temporarily positioned in the center of the cell as a result of superimposition of the cyclotron and magnetron motions (see the Discussion section below).

Discussion

Kaiser et al., who pioneered EPIC, showed that application of the technique, substantially increases the lifetime of the ICR experiment [55]. These experiments were reproduced on SLCC spectra (Figure 2a) demonstrating that the alteration to the electric field within the cell caused by the electron beam can not only prolong the duration of the signal, but eliminate the nipple effect altogether (Figure 2b). To analyze its effects on the temporal behavior of the ICR frequency and to minimize all other space-charge related frequency perturbations (except for "self space-charge" of the ions of the same m/z [61, 62], as was described in the Methods and Results sections, a single cesium iodide cluster (Figure 3a) was isolated for ICR experiments under normal and EPIC conditions. The resulting signals were subjected to the FDM frequency shift calculations (Figure 3b) followed by Fourier transform to find stable harmonic modulations.

The major difference between the two modulation spectra is a much larger peak at the native ICR frequency (Figure 4a) under non-EPIC conditions—a clear indication that the center of the cyclotron orbit is substantially off-center in the XY-plane (a non-zero magnetron component), and the modulations are due to the radial inhomogeneity of the trapping field within its diameter. A virtual elimination of this peak in Figure 4b suggests that EPIC prevents or delays magnetron expansion so that the cyclotron orbit remains centered at the center of the cell for the duration of the experiment, which strongly supports earlier findings [54].

This evidence of the relationship between magnetron motion and the nipple effect will be instrumental in investigation of another tell-tale observation-temporal frequency fluctuations within an isotopic envelope going through the SLCC. An isotopic beat pattern [59, 60] in the observed ICR signal is not simply a result of superimposition of multiple sinusoids. Had it been, the observed frequencies would not vary in time. It has been shown previously [20] and can be observed in the pre-nipple stage of the experiments (Figure 5b) that frequencies "spike" up at the points when the amplitude of the transient is the smallest. This phenomenon can be described as a straight forward manifestation of the fundamentals of the classical principles of ion motion [63] in a Penning trap [64] including the spacecharge correction [65]:

$$\omega_{\pm} = \frac{\omega_c}{2} \left(1 \pm \sqrt{1 - 4 \left(\frac{2qV_0 G_T}{dm} + \frac{q^2 \rho G_i}{\varepsilon_0 m} \right) / \omega_c^2} \right)$$
(2)



Figure 5. The results of the frequency shift calculations conducted on (**a**) the experimental SLCC of angiotensinogen. (I) is the magnification of the region of the time domain transient signal under investigation, (II) its amplitude d_k , and (III) frequency f_k temporal behaviors calculated using FDM (**b**) before, and (**c**) after the nipple.

$$\omega_c = \frac{qB}{m} \tag{3}$$

$$\omega_+ = \omega_c' \tag{4}$$

$$\omega_{-} = \omega_{m} \tag{5}$$

where ω_c , ω_m , ω'_c are fundamental cyclotron, magnetron, and reduced cyclotron frequencies, q is the charge, Bmagnetic field, V_0 trapping potential, m particle's mass, d is the distance between the trapping plates, G_T is the geometry factor of a specific ICR cell, G_i is the geometry factor of an ion cloud, ε_0 permittivity of a vacuum, and ρ , is the ion density.

Under the high space-charge conditions, when the ion density ρ is maximum, the space-charge correction term in eq 2 is maximized and the observed frequency $\omega'_c = \omega_+$ is minimized. These conditions occur when the ion packets of different isotopes are in-phase (the beats of the beat pattern) therefore the minima of the frequency beat pattern in the pre-nipple part of the transient of the experimental SLCC (Figure 5b) coincide with amplitude maxima. On the other hand, when the packets are in anti-phase, the space-charge effect is minimized and the ω'_c is the largest, which explains the frequency spikes at the amplitude minima.

A steady increase in the magnitude of frequency "spikes" is the manifestation of the positive frequency "drift" [66]. This behavior can be explained by the isotope beat pattern (ion clouds coming into phase with each other), which scatters and dephases the ion packets reducing ion density. Furthermore, image charge [67, 68], being oppositely charged, is reflected as attraction of the ions to the ICR cell walls, which slows down the cyclotron motion. Consequently, the detected frequency is reduced by $\Delta \omega$ according to

$$\omega_{eff} = \omega_c - \omega_m - \Delta\omega = \omega_c - \omega_m - \frac{\rho}{4\pi^2 \varepsilon_0 B(r_{trap}^2 - r_{ion}^2)}, \quad (6)$$

where r_{trap} and r_{ion} are cylindrical cell and cyclotron motion radii respectively. Over time, dephasing and expansion of the ion clouds decreases ρ (more rapidly under high space-charge conditions); therefore the detected average frequency shows positive drift.

On the other hand, a simple electrostatics explanation for the nipple and post-nipple behavior fails at the SLCC. For instance, rapid negative frequency shifts ("dips") (Figure 2c) corresponding to the "out-ofphase" ion position (abundance minima) violate eq 2 if one neglects consideration of the magnetron/cyclotron orbital geometries. Moreover, neither loss of ions nor the expansion of the ion clouds can explain the deviation from the exponential decay in the time domain data and beating in the frequency domain post-SLCC.

As was previously mentioned, a simple coulombic explanation of the post-nipple frequency behavior fails.



Figure 6. (a) An illustration of the inhomogeneities in the electric field experienced by a trapped ion packet in a closed, cylindrical ICR cell. When the ions follow the cyclotron orbit close to the middle of the cell (trajectory I), they are subjected to nearly hyperbolic electric potential. As the axial and magnetron components start to contribute ions travel through highly inhomogeneous electric field (for example, trajectory II), which perturbs the motion further increasing the magnetron component. The orbits are not drawn to scale. (b) A schematic representation of the ions being temporally positioned in the center of the cell as consequence of the superimposition the cyclotron and magnetron orbits. The figure is not drawn to scale.

Indeed, initially the ions are tightly bundled into a packet, and the frequency minima correspond to the isotopic ion packets coming into phase. At such a point, as discussed above, the space-charge is maximum, which causes the observed frequency to minimize (Figure 5b). The reverse happens later on (Figure 5c) in the course of the SLCC, when the frequency minimizes ("dips") at the minimum of the amplitude. Since frequency minima correspond to the positions of the highest ion density (eq 2), and since amplitude corresponds to net ion cloud distance from the cell detection

plates, the *maximum* space-charge condition must be occurring with the *center* of mass of the ion cloud at, or near, the center of the cell.

This seeming contradiction disappears in the light of evidence of substantial magnetron expansion obtained in the EPIC experiments. Indeed, since the transient amplitude minima correspond to the center of masses being in the center of the ICR cell (or rather, the furthest away from the detection plates, hence minimum signal intensities), the only feasible explanation to the observed (Figure 5) post-nipple "dips" is a shift in the ion

trajectories via a significant increase in average magnetron radius. As the magnetron trajectory expands and its radius becomes sufficiently large, ions, when in phase, find themselves periodically positioned (without loss of momentum) very close the center of the cell as a consequence of the superposition of the cyclotron and magnetron motions as schematically shown in the Figure 6b.

Thus, the SLCC can be explained by uncorrelated magnetron expansion. Magnetron motion in a Penning trap always expands [63, 69] under normal conditions. Moreover, the magnetron expansion rate tends to increase as the magnetron orbit increases due to the increased gradient in the potential hill [70]. Indeed, in the center of the ICR cell, the trapping potential is nearly hyperbolic, but closer to the edges it squares off (Figure 6a). So, as ion packets move away from the center of the cell along the magnetron orbit, they are exposed to increasingly inhomogeneous electric fields in both axial and cyclotron motions (Figure 6a I). While some of the ions will experience substantial magnetron expansion, collide with the ICR cell walls, and be neutralized, all ions will experience rapid fluctuations in their instantaneous electric fields over their axial and cyclotron oscillations before collision with the cell wall becomes a possibility. These fluctuations in electric field will modulate ω'_c (from eqs 2 and 3) as well as the axial frequency which will contribute strongly to the dephasing of the ion cloud. In other words, space- and imagecharge induced (diocotron) drift shifts ions into the regions of the ICR cell where electric field inhomogeneities cause dephasing, and the rate of expansion governs the SLCC position in time, which is itself governed by ion density (eq 6).

Rapid, uncorrelated magnetron expansion thus yields an intuitive and plausible explanation for the SLCC "nipple effect" phenomenon. While this model nicely explains the unexpected observations of frequency decreases that correlate with amplitude minima, it is hardly a tested theory. A more thorough investigation, which uses these same frequency shift analysis methods and explores the behavior of these frequency shifts with varying excitation radius, ion population, trapping potentials, electric/magnetic field homogeneity, as well as global and local space-charge should yield a better understanding of the SLCC and space-charge phenomena in general.

Summary and Conclusions

This work presented an application of the filter diagonalization method (FDM) in the study of the spacecharge in the form of the spontaneous loss of coherence catastrophe (SLCC). Due to its high-resolution on short transients and tolerance to noise, the FDM made possible detailed frequency chasing experiments, which provide some insight into ion cloud behavior in the ICR cell. The temporal frequency and abundance behavior thus revealed the cause of such a mysterious phenom-

enon as the SLCC. Specifically, the fact that frequency spikes are observed pre-SLCC that correlate with amplitude minima agrees with the known observation that frequency increases are correlated with low spacecharge conditions. The fact that this correlation flips over at the SLCC suggests that the isotope ion packets are temporarily coming back into phase (high spacecharge) at the amplitude minima, which is only possible geometrically if the magnetron orbit diameter is similar to that of the cyclotron orbit. This claim is supported by the EPIC experiments, which show that the SLCC is observed only when there is a strong magnetron component. Thus, the SLCC occurs when (1) the image charge drift, the space-charge related scattering, and scattering of ions off neutral molecules result in substantial magnetron expansion, which moves the ion clouds radially into the regions of the cell with large electric field inhomogeneities, and (2) when the magnetron orbit expands to approximately the same diameter as the cyclotron orbit diameter.

These findings yet again reinforce the need for reduction of magnetron drift and space-charge induced frequency modulation when pursuing the higher mass accuracy and resolving power capabilities of the FTICR MS. A number of experimental techniques and cell designs have been proposed in the literature to deal with this issue [71–81]. Clearly, EPIC [53–55] has proven to be a good countermeasure for magnetron expansion and a capable tool to counteract image charge drift and stabilize the transient. Quadrupolar axialization methods should also be revisited [82-91]. This area of research remains active, and such combined methods should help address these issues.

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