Chatter stability prediction in four-axis milling of aero-engine casings with bull-nose end mill

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Received 26 January 2015; revised 4 March 2015; accepted 13 March 2015
Available online 20 June 2015

Abstract An analytical model for chatter stability prediction in bull-nose end milling of aero-engine casings is presented in this paper. And the mechanics and dynamics variations due to the complex cutter and workpiece geometry are considered by analyzing the effects of the lead angle on the milling process. Firstly, the tool-workpiece engagement region is obtained by using a previously developed method and divided into several disk elements along the tool-axis direction. Secondly, a 3D dynamic model for stability limit calculation is developed and simplified into a 1D model in normal direction considering only the dominant mode of the workpiece. Then the cutting force coefficients, the start and exit angles corresponding to each disk element are determined. And the total stability lobe diagram is calculated using an iterative algorithm. Finally, several experimental tests are carried out to validate the feasibility and effectiveness of the proposed prediction approach.

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1. Introduction

Thin-walled parts have been widely used in the aerospace industry, such as aero-engine casings, blades and impellers. They can significantly help to improve the working performance of aircraft. However, due to the complex structures and weak rigidity of their own, they also bring many machining difficulties and challenges. Chatter is one of the main machining problems, which leads to poor surface finish and low production efficiency.1–16 In order to avoid chatter, the milling process must be conducted in a stable state. Thus, the machining stability prediction becomes very important in achieving good machining quality and high productivity. Many studies have been focused on this issue.

Tobias and Fishwick1, as well as Tlusty and Polacek2 developed the stability lobe theory in orthogonal cutting process, which makes it possible to predict the chatter phenomena of milling process. Altintas and Budak3 presented an analytical method to generate stability lobe diagram directly in the frequency domain. They considered the average term in the Fourier series expansions as the approximation of time-varying directional coefficients and used an eigenvalue solution to solve the critical depth of cut. However, the single-frequency method cannot predict the additional stability region and the
doubling bifurcations at small radial immersions.\textsuperscript{4–7} To overcome this problem, Budak and Altintas\textsuperscript{4,5} developed a multi-frequency solution of chatter stability, which includes the higher order terms of the Fourier series expansions. And Merdol and Altintas\textsuperscript{6}, Gradišeka et al.\textsuperscript{7} extended the multi-frequency approach and the semi-discretization method to the milling cases of low radial immersion.

The dynamics of flat end milling are considered in the transversal directions of the cutter. However, for ball and bull-nose end milling, the dynamics must be considered in all the three directions.\textsuperscript{8–16} Altintas\textsuperscript{8} extended the two dimensional chatter stability theory to a three-dimensional chatter problem by adding the dynamics in the tool-axis direction. Based on this work, Seguy et al.\textsuperscript{9}, Campa et al.\textsuperscript{10,11} and Adetoro et al.\textsuperscript{12,13} calculated the stability lobe diagrams in ball-nose end milling of thin floors and thin walls by considering the nonlinearities of the axial immersion angle and the cutting force coefficients. For multi-axis milling, the effects of tool positions on the process geometry, mechanics and dynamics cannot be ignored. Shamoto and Akazawa\textsuperscript{14}, Budak and Ozturk\textsuperscript{15,16} studied the influences of lead and tilt angles on the engagement region and predicted the chatter stability of five-axis ball end milling.

Aeroengine casings are typical thin-walled parts with ring-shaped and closed geometry structures and also present machining problems due to chatter. However, unlike the milling of thin plates, the dynamics in the milling of aero-engine casings is more complex owing to the symmetry of the structure and the support of the fixture.\textsuperscript{17,18} The cutting deformation and vibration occur mainly in radial direction of the part and have a certain symmetry in circumferential direction of the part. The thinner the wall thickness is, the worse the cutting deformation and vibration become. And the dynamics of the process system such as the natural frequency and the stiffness will change significantly in the material removal process, even a small part of the undesired material is removed. Normally, the aero-engine casings are fixed by the axial pressing and radial supporting forms. And the dynamics of the part will be significantly different with different pressing forces or different supporting positions. All the above factors will make the milling process exhibit the nonlinear and strong time-varying characteristics, thus inducing drastic cutting chatter. Therefore, chatter prediction and suppression in the milling of aero-engine casings become more difficult.

In this paper, a calculation method of stability lobe diagrams in four-axis ball-nose end milling of aero-engine casings is presented. Firstly, the tool-workpiece engagement region is determined by considering the influences of lead angle. And based on the engagement region, the start and exit angles of each disk element, the directional coefficients can be obtained. Secondly, the chatter stability model is developed and simplified to 1D model by considering only the normal direction dynamics. And the total stability lobe diagram is obtained by using an iterative algorithm. Lastly, several milling tests verifies the feasibility and effectiveness of the chatter stability prediction method.

2. Chatter stability model

The chatter stability model used in this paper is the 3D model proposed by Altintas.\textsuperscript{8} And the effects of lead angle on the engagement region, thus, on the directional coefficients are also discussed. The helix angle and the process damping are not taken into account in this chatter theory.

2.1. Calculation of tool-workpiece engagement region

In order to calculate the tool-workpiece engagement region, three coordinate systems are defined in four-axis milling process, as shown in Fig. 1. The first one is a fixed coordinate system, MCS, formed by the $X$, $Y$ and $Z$ axes of the machine tool. The second one is the process coordinate system, FCN, consisting of feed $F$, cross-feed $C$ and surface normal $N$ axes. $x$, $y$, $z$ are the tool-axis coordinate in the TCS.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Fig_1.png}
\caption{Coordinate systems and lead angle.}
\end{figure}
is the tool coordinate system, TCS, which is the rotated form of the FCN. In FCN, the tool-axis direction is defined by a lead angle \( \theta \), which can be determined as

\[
\theta = \arcsin \frac{d_{e1} - \left( \frac{D}{2} - R_c \right)}{R_c}
\]

with

\[
\theta = \arcsin \frac{d_{e2}}{R_m}
\]

\[
d_e = d_{e1} + d_{e2}
\]

where \( D \) is the cutter diameter, \( R_c \) the cutter corner radius, \( R_m \) the machined surface radius, \( d_e \) the eccentric distance, \( d_{e1} \) the first part of the eccentric distance and \( d_{e2} \) the second part of the eccentric distance.

The engagement region is located between the toroidal surface rotated by cutter edges and the workpiece solid, as shown in Fig. 2. In this paper, the previously developed method\(^{19} \) is extended to calculate the tool-workpiece engagement region. The algorithm is as follows. Firstly, several slices are inserted between the machined and blank surfaces to get the intersection curves between the slices and the toroidal surface. Secondly, by determining the minimum distance from the intersection curves to the reference planes, the reference points can be obtained. Then, the engagement boundary can be fixed with a spline curve fitted by the reference points and an intersection curve between the blank surface and the toroidal surface. This method can be used in three different cutting cases: first cut, following cut and slotted cut.

### 2.2. Calculation of dynamic cutting forces

During the milling process, the cutting forces excite the workpiece and then cause dynamic displacements in all three directions, as shown in Fig. 3. \( k_x, k_y \) and \( k_z \) are the \( X, Y \) and \( Z \) axial stiffness in the MCS, respectively. \( c_x, c_y \) and \( c_z \) are the \( X, Y \) and \( Z \) axial damping in the MCS, respectively. The dynamic displacements lead to a modulated chip thickness, which consists of two components: the static and dynamic chip thickness. The static chip thickness can be removed since it does not contribute to the chatter stability. The dynamic chip thickness between the present edge and the previous edge can be calculated as

\[
h_j(\phi_j, \gamma) = (\Delta x \sin \gamma - \Delta z \cos \gamma)g(\phi_j)
\]

with

\[
\Delta r = \Delta x \sin \phi_j + \Delta y \cos \phi_j
\]

\[
\begin{align*}
\Delta x &= x(t) - x(t - T) \\
\Delta y &= y(t) - y(t - T) \\
\Delta z &= z(t) - z(t - T)
\end{align*}
\]

Fig. 3  Dynamic milling model for bull-nose end milling of aero-engine casings.
are the tangential, radial and axial cutting forces contributed by all cutting edges, the total dynamic force coefficients, respectively.

Substituting Eq. (9) into Eq. (10) and summing the cutting forces, the cutting forces can be expressed as the product of the cutting force coefficients, the uncut chip thickness and the chip width. The edge forces do not contribute to the regenerative chatter. The dynamic cutting forces in tooth \( j \) in the tangential, radial and axial directions can be defined as

\[
\begin{align*}
F_x(j,\phi_j,\gamma) &= K_a h_j \sin \phi_j \\
F_y(j,\phi_j,\gamma) &= K_a h_j \cos \phi_j \\
F_z(j,\phi_j,\gamma) &= K_a h_j
\end{align*}
\]

where \( K_a, K_r \) and \( K_c \) are the tangential, radial and axial cutting force coefficients, respectively, \( a \) is the axial depth of cut.

Then those forces can be mapped into Cartesian coordinate system as follows:

\[
\begin{bmatrix}
F_x(j,\phi_j,\gamma) \\
F_y(j,\phi_j,\gamma) \\
F_z(j,\phi_j,\gamma)
\end{bmatrix} = M
\]

where

\[
M = \begin{bmatrix}
-\cos \phi_j & -\sin \phi_j & \cos \gamma \sin \phi_j \\
-\sin \phi_j & -\cos \phi_j & \cos \gamma \cos \phi_j \\
\cos \gamma & \sin \gamma & 0
\end{bmatrix}
\]

Substituting Eq. (9) into Eq. (10) and summing the cutting forces contributed by all cutting edges, the total dynamic milling forces can be obtained as:

\[
\begin{bmatrix}
F_x(t) \\
F_y(t) \\
F_z(t)
\end{bmatrix} = a K_a A \begin{bmatrix}
\Delta x \\
\Delta y \\
\Delta z
\end{bmatrix}
\]

where \( F_x(t), F_y(t) \) and \( F_z(t) \) are the cutting forces along the \( x \)-, \( y \)- and \( z \)-axis directions in time domain, respectively. \( A \) is the matrix of directional coefficients.

Using the mono-frequency solution, Eq. (12) can be reduced to Eq. (13):

\[
\begin{bmatrix}
F_x(t) \\
F_y(t) \\
F_z(t)
\end{bmatrix} = \frac{N_l}{4\pi} a K_a A \begin{bmatrix}
\Delta x \\
\Delta y \\
\Delta z
\end{bmatrix}
\]

where \( N_l \) is the flute number and \( A \) the directional factor matrix.

2.3. Calculation of stability limit

Using the transfer function at the cutter-workpiece contact area, the dynamic displacements can be described in frequency domain:

\[
\begin{bmatrix}
\Delta x(i\omega_l) \\
\Delta y(i\omega_l) \\
\Delta z(i\omega_l)
\end{bmatrix} = \left( 1 - e^{-i\omega_l T} \right) G
\]

\[
\begin{bmatrix}
F_x(i\omega_l) \\
F_y(i\omega_l) \\
F_z(i\omega_l)
\end{bmatrix} = \frac{N_l}{4\pi} a K_a (1 - e^{-i\omega_l T}) A \begin{bmatrix}
F_x(i\omega_l) \\
F_y(i\omega_l) \\
F_z(i\omega_l)
\end{bmatrix}
\]

Then Eq. (15) becomes an eigenvalue problem, where Eq. (16) defines the stability and Eq. (17) defines the eigenvalue \( \lambda \).

\[
\det(I + i\lambda A, G) = 0
\]

\[
\lambda = -\frac{N_l}{4\pi} a K_a (1 - e^{-i\omega_l T})
\]

The critical axial depth of cut \( a_{lim} \) and the corresponding spindle speeds \( n \) for each lobe \( k \) are obtained as

\[
a_{lim} = -\frac{2\pi \text{Re}(\lambda)}{N_l K_r} \left[ 1 + \left( \frac{\text{Im}(\lambda)}{\text{Re}(\lambda)} \right)^2 \right]
\]

\[
n = \frac{60 a_{lim}}{N_l (2k + 1) \pi - 2 \arctan \left( \frac{\text{Im}(\lambda)}{\text{Re}(\lambda)} \right)}
\]

2.4. Simplified 1D model for four-axis milling

During the bull-nose end milling of aero-engine casings, a small lead angle is required to keep the bottom cutting edges from cutting materials, thus achieving a better surface finish. The smaller the lead angle is, the bigger the cutting width becomes. And it can be expressed as the product of the cutting force coefficients, the uncut chip thickness, in other words, they do not contribute to the regenerative chatter. The dynamic cutting forces caused by the plowing between flank face of the cutter and the finished surface can be expressed as the product of the cutting force coefficients and the length of the elemental edge. While the cutting forces caused by the shearing of material at the rake face can be expressed as the product of the cutting force coefficients, the uncut chip thickness and the chip width. The edge forces do not take into account the chatter stability model, as they are not related to the chip thickness, in other words, they do not contribute to the regenerative chatter. The dynamic cutting forces on tooth \( j \) in the tangential, radial and axial directions can be defined as

\[
\begin{align*}
F_x(j,\phi_j,\gamma) &= K_c h_j \sin \phi_j \\
F_y(j,\phi_j,\gamma) &= K_c h_j \cos \phi_j \\
F_z(j,\phi_j,\gamma) &= K_c h_j
\end{align*}
\]

where \( K_c, K_r \) and \( K_a \) are the tangential, radial and axial cutting force coefficients, respectively, \( h \) is the axial depth of cut.

Then those forces can be mapped into Cartesian coordinate system as follows:

\[
\begin{bmatrix}
F_x(j,\phi_j,\gamma) \\
F_y(j,\phi_j,\gamma) \\
F_z(j,\phi_j,\gamma)
\end{bmatrix} = M
\]

with

\[
M = \begin{bmatrix}
-\cos \phi_j & -\sin \phi_j & \cos \gamma \sin \phi_j \\
-\sin \phi_j & -\cos \phi_j & \cos \gamma \cos \phi_j \\
\cos \gamma & \sin \gamma & 0
\end{bmatrix}
\]

Substituting Eq. (9) into Eq. (10) and summing the cutting forces contributed by all cutting edges, the total dynamic milling forces can be obtained as:

\[
\begin{bmatrix}
F_x(t) \\
F_y(t) \\
F_z(t)
\end{bmatrix} = a K_a A \begin{bmatrix}
\Delta x \\
\Delta y \\
\Delta z
\end{bmatrix}
\]

where \( F_x(t), F_y(t) \) and \( F_z(t) \) are the cutting forces along the \( x \)-, \( y \)- and \( z \)-axis directions in time domain, respectively. \( A \) is the matrix of directional coefficients.

Using the mono-frequency solution, Eq. (12) can be reduced to Eq. (13):

\[
\begin{bmatrix}
F_x(t) \\
F_y(t) \\
F_z(t)
\end{bmatrix} = \frac{N_l}{4\pi} a K_a A \begin{bmatrix}
\Delta x \\
\Delta y \\
\Delta z
\end{bmatrix}
\]

where \( N_l \) is the flute number and \( A \) the directional factor matrix.
here can be reduced to a 1D model in the normal direction. The stability problem in Eq. (15) can be simplified into

\[
F_z(i\omega_k) = \frac{N_f}{4\pi} a K_t (1 - e^{-i\omega_k T}) z_{zz} G_z(i\omega_k) F_z(i\omega_k) \\
= \frac{N_f}{2\pi} a K_t z_{zz} \text{Re}[G_z(i\omega_k)] F_z(i\omega_k)
\]

with

\[
z_{zz} = \phi[-K_s(\cos 2\gamma + 1) + K_s \sin 2\gamma]^{\theta_{ns}}
\]

\[
\text{Re}[G_z(i\omega_k)] = \frac{1 - d_z^2}{k_z \left[(1 - d_z^2)^2 + (2d_z d_{\xi})^2\right]}
\]

where \(d_z = \omega_z / \omega_{ns},\) \(\omega_{ns}\) is the natural frequency of the mode, \(k_z\) the stiffness and \(\xi\) the damping ratio.

When the lead angle \(\theta\) is equal to 0 degree, the cutting depth \(a\) is defined along both the tool-axis and surface normal directions. However, in four-axis milling process, the axial depth of cut \(a_z\) varies as the lead angle \(\theta\) changes, as shown in Fig. 4. And it can be determined as

\[
a_z = \frac{a}{\cos \theta}
\]

Then the stability problem in four-axis milling process can be obtained:

\[
F_z(i\omega_k) = \frac{N_f}{2\pi \cos \theta} a K_t z_{zz} \text{Re}[G_z(i\omega_k)] F_z(i\omega_k)
\]

Because of the complex cutter and workpiece geometry, the cutting force coefficients, the start and exit angles are not constant along the tool-axis direction. Then a disk-based method developed by Budak and Ozturk\textsuperscript{15,16} is extended to calculate the stability limit in four-axis milling of aero-engine casings.

The bull-nose end mill is divided into several disk elements along the tool-axis direction. And each disk element has a height of \(\Delta a\). For the disk \(l\), the stability problem in Eq. (24) can be expressed as
\[ F_z(i\omega_c) = \frac{N_f}{2\pi \cos \theta} \Delta a K_z x_z' \text{Re}[G_z(i\omega_c)] F_z(i\omega_c) \]  
(25)

In order to obtain the total stability limit of the process system, the dynamics of all the disk elements have to be summed up:

\[ F_z(i\omega_c) = \frac{N_f}{2\pi \cos \theta} \Delta a \left( \sum_{i=1}^{m} K_z x_z' \right) \text{Re}[G_z(i\omega_c)] F_z(i\omega_c) \]  
(26)

where \( m \) is the total number of disk elements.

Then the stability limit corresponding to \( \Delta a \) is obtained:

\[ \Delta a_{\text{lim}} = \frac{2\pi \cos \theta}{N_f \left( \sum_{i=1}^{m} K_z x_z' \right) \text{Re}[G_z(i\omega_c)]} \]  
(27)

And the spindle speed is expressed as follows:

\[ n = \frac{30 \omega_c}{N_f \left( k + 1 \right) \pi \arctan \left( \frac{h-1}{h+1} \right)} \]  
(28)

Because there are \( m \) disks in the calculation, the total stability limit for a given chatter frequency \( \omega_c \) is calculated in the following form:

\[ a_{\text{lim}} = m \Delta a_{\text{lim}} \]  
(29)

In the solution of the stability limits, the following procedure is used. Firstly, the cutting depth \( a \) begins from an initial value \( \Delta a \) and increases with a step size \( \Delta a \).

And for each cutting depth, the tool-workpiece engagement region is determined. Secondly, the total stability lobe diagram can be obtained by swepting the chatter frequency \( \omega_c \) around a predetermined chatter frequency range. The calculation process will not stop until all the determined stability limits \( a_{\text{lim}} \) in the stability lobe diagram are less than the cutting depth \( a \).

3. Experimental results and discussion

To validate the proposed method, several milling tests were carried out on a high-speed milling center, as shown in Fig. 5. Cemented carbide and 304 stainless steel were used as the cutter and the workpiece materials, respectively. The tool is a bull-nose end mill with 4 flute, 12 mm diameter, 2 mm corner radius and 30° helix angle. The workpiece is a cylindrical pipe with 211 mm inner diameter and 217 mm outer diameter. The milling tests are a series of slotting, where the feed rate is consistent.

Table 1  Start and exit angles for each disk with three different lead angles.

<table>
<thead>
<tr>
<th>Lead angle</th>
<th>Item</th>
<th>Disk</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
</tr>
</thead>
<tbody>
<tr>
<td>0°</td>
<td>( \phi_x ) (rad)</td>
<td>0.0995</td>
<td>0.0555</td>
<td>0.0410</td>
<td>0.0319</td>
<td>0.0249</td>
<td>0.0192</td>
<td>0.0142</td>
<td>0.0097</td>
<td>0.0057</td>
<td>0.0018</td>
<td>0.0000</td>
<td></td>
</tr>
<tr>
<td></td>
<td>( z ) (mm)</td>
<td>0.0100</td>
<td>0.0300</td>
<td>0.5000</td>
<td>0.7000</td>
<td>0.9000</td>
<td>1.1000</td>
<td>1.3000</td>
<td>1.5000</td>
<td>1.7000</td>
<td>1.9000</td>
<td>2.1000</td>
<td></td>
</tr>
<tr>
<td>4°</td>
<td>( \phi_x ) (rad)</td>
<td>0.2887</td>
<td>0.1611</td>
<td>0.1154</td>
<td>0.0879</td>
<td>0.0680</td>
<td>0.0523</td>
<td>0.0391</td>
<td>0.0272</td>
<td>0.0159</td>
<td>0.0051</td>
<td>0.0000</td>
<td></td>
</tr>
<tr>
<td></td>
<td>( z ) (mm)</td>
<td>2.8529</td>
<td>2.9805</td>
<td>3.0262</td>
<td>3.0537</td>
<td>3.0736</td>
<td>3.0893</td>
<td>3.1025</td>
<td>3.1144</td>
<td>3.1257</td>
<td>3.1365</td>
<td>3.1416</td>
<td></td>
</tr>
<tr>
<td>8°</td>
<td>( \phi_x ) (rad)</td>
<td>0.4638</td>
<td>0.2642</td>
<td>0.1886</td>
<td>0.1440</td>
<td>0.1114</td>
<td>0.0854</td>
<td>0.0636</td>
<td>0.0438</td>
<td>0.0252</td>
<td>0.0072</td>
<td>0.0000</td>
<td></td>
</tr>
<tr>
<td></td>
<td>( z ) (mm)</td>
<td>2.6778</td>
<td>2.8774</td>
<td>2.9530</td>
<td>2.9976</td>
<td>3.0302</td>
<td>3.0562</td>
<td>3.0780</td>
<td>3.0978</td>
<td>3.1164</td>
<td>3.1344</td>
<td>3.1416</td>
<td></td>
</tr>
</tbody>
</table>

320 mm/min, the axial depth of cut is 0.5 mm and 1.0 mm and the radial depth of cut is 12 mm. In order to ensure the consistency of dynamics along the circumferential direction, the aeroengine casing was fixed by axial pressing without other supporting forms.

The cutting force coefficients are calculated as functions of the tool-axis coordinate using the approach developed by Gao et al.\textsuperscript{20} as shown in Fig. 7. With elevation \( z \) as the independent variable, the cutting force coefficients corresponding to each disk can be obtained.

The modal parameters of the aeroengine casing measured by using impact tests and finite element simulations are listed in Table 2. The locations for the milling and impact tests are consistent.
Then the stability lobe diagrams for four-axis milling of aeroengine casing with different lead angles can be calculated by the presented approach as shown in Fig. 8. It can be found that the chatter stability boundary grows in the vertical direction which does not move in the horizontal direction with the increase of lead angle. For a fixed milling system, the larger the lead angle, the greater the minimum stability limit. This is because the tool-workpiece engagement region will become smaller as the lead angle increases. And the interaction between the cutter and the workpiece will become weak.

In the stability lobe diagram of 4° lead angle, there are three different cutting status: chatter, transitional and stable, as shown in Fig. 9. The transitional cutting status means that the predicted chatter frequency can be seen very slightly in the spectrum of the measured force. This status often appears near the chatter stability boundary in the stability lobe diagram. And the unstable and stable zones can be seen above and below the chatter stability boundary, respectively.

The normal cutting force data and the corresponding spectra at two points (points A and B in Fig. 9) are presented in Fig. 10. The cutting status at point A with a spindle speed of 3500 r/min and cutting depth of 0.5 mm is unstable with a chatter frequency of 594.0 Hz. It can be seen that the amplitude at the chatter frequency is higher than the amplitude at the tooth passing frequency, which demonstrates that the milling process is unstable. While the cutting status at point B with a spindle speed of 5000 r/min and cutting depth of 0.5 mm is stable. For point B, the maximum amplitude occurs at a tooth passing frequency of 333.3 Hz in the cutting force spectrum, whereas the amplitude at the natural frequency of the workpiece is very small. The surface finishes for the points A and B are also shown in Fig. 10. And the cutting marks validate the accuracy of the proposed prediction approach.
4. Conclusions

(1) A 3D chatter stability model for bull-nose end milling of aeroengine casings is developed in this paper. And the 3D model can be simplified to a 1D model in surface normal direction considering only the dominant mode of the workpiece.

(2) The model is extended to four-axis machining by adding the effects of the lead angle in the milling process. The tool-workpiece engagement region is determined by using a slice-based method and divided along the tool-axis direction into several disks. And the total stability lobe diagram for the process system is obtained by an iterative algorithm.

(3) The model and approach are validated by analyzing experimental results and a good agreement has been achieved.

(4) The proposed method can be used to predict chatter stability in four-axis milling of aeroengine casings, where a small lead angle should be selected. While for the case of large lead angle or five-axis milling, the 3D model that will be developed in the future must be used because the dynamic displacements in all three directions play important roles in the regenerative chatter.

Acknowledgements

This work was supported by the National Basic Research Program of China (No. 2013CB035802) and the 111 Project of China (No. B13044).

References


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