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Physics Letters B

www.elsevier.com/locate/physletbAre there nuclear structure effects on the isoscalar giant monopole resonance and nuclear incompressibility near $A \sim 90$?Y.K. Gupta^{a,1}, U. Garg^{a,*}, K.B. Howard^a, J.T. Matta^{a,2}, M. Şenyiğit^{a,b}, M. Itoh^c, S. Ando^c, T. Aoki^c, A. Uchiyama^c, S. Adachi^d, M. Fujiwara^d, C. Iwamoto^d, A. Tamii^d, H. Akimune^e, C. Kadono^e, Y. Matsuda^e, T. Nakahara^e, T. Furuno^f, T. Kawabata^f, M. Tsumura^f, M.N. Harakeh^g, N. Kalantar-Nayestanaki^g^a Physics Department, University of Notre Dame, Notre Dame, IN 46556, USA^b Department of Physics, Faculty of Science, Ankara University, TR-06100 Tandoğan, Ankara, Turkey^c Cyclotron and Radioisotope Center, Tohoku University, Sendai 980-8578, Japan^d Research Center for Nuclear Physics (RCNP), Osaka University, Osaka 567-0047, Japan^e Department of Physics, Konan University, Hyogo 658-8501, Japan^f Department of Physics, Kyoto University, Kyoto 606-8502, Japan^g KVI-CART, University of Groningen, 9747 AA Groningen, The Netherlands

ARTICLE INFO

Article history:

Received 12 June 2016

Received in revised form 7 July 2016

Accepted 7 July 2016

Available online 14 July 2016

Editor: D.F. Geesaman

ABSTRACT

“Background-free” spectra of inelastic α -particle scattering have been measured at a beam energy of 385 MeV in $^{90,92}\text{Zr}$ and ^{92}Mo at extremely forward angles, including 0° . The ISGMR strength distributions for the three nuclei coincide with each other, establishing clearly that nuclear incompressibility is not influenced by nuclear shell structure near $A \sim 90$ as was claimed in recent measurements.

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Nuclear incompressibility is a fundamental quantity characterizing the equation of state (EOS) of nuclear matter [1]. A number of important phenomena such as the radii of neutron stars, the strength of supernova explosions, transverse flow in relativistic heavy-ion collisions, the nuclear skin thickness, etc. require a good understanding of the EOS of nuclear matter [2,3]. The nuclear incompressibility for infinite nuclear matter, K_∞ , may be determined experimentally from the compressional “breathing mode” of nuclear density oscillation, the isoscalar giant monopole resonance (ISGMR), in finite nuclei [4,5]. In the scaling model, the energy of the ISGMR is directly related to the nuclear incompressibility of the nucleus and is given by [4]:

$$E_{\text{ISGMR}} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle_0}}, \quad (1)$$

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where K_A is the incompressibility of a nucleus with mass number A , $\langle r^2 \rangle_0$ is the ground state mean square radius, and m is the nucleon mass. The determination of K_∞ from K_A is achieved within a framework of self-consistent RPA calculations, using the widely accepted method described by Blaizot et al. [6,2]. The presently accepted value of K_∞ , determined from ISGMR in “standard” nuclei such as ^{90}Zr and ^{208}Pb , is 240 ± 20 MeV [7–10]. Because the compressional modes are collective phenomena, the determination of K_∞ should be independent of the choice of the nucleus, provided that approximately 100% of the energy weighted sum rule (EWSR) fraction is exhausted in the ISGMR peak; this condition is satisfied for sufficiently heavy nuclei ($A \geq 90$) [2]. The use of the aforementioned “standard nuclei” stems primarily from the relative ease in doing theoretical calculations for the doubly-magic nuclei.

In recent work by the Texas A & M group [11–13], it has been claimed that the ISGMR strength distributions vary in a rather dramatic manner in nuclei in the $A \sim 90$ region. In particular, the $A = 92$ nuclei, ^{92}Zr and ^{92}Mo , emerged quite disparate from the others: The ISGMR energies (E_{ISGMR}) for ^{92}Zr and ^{92}Mo were observed to be, respectively, 1.22 and 2.80 MeV higher than that of ^{90}Zr . Consequently, the K_A values determined for ^{92}Zr and ^{92}Mo were ~ 27 MeV and ~ 56 MeV, respectively, higher than that of ^{90}Zr . These results, if correct, imply significant nuclear structure

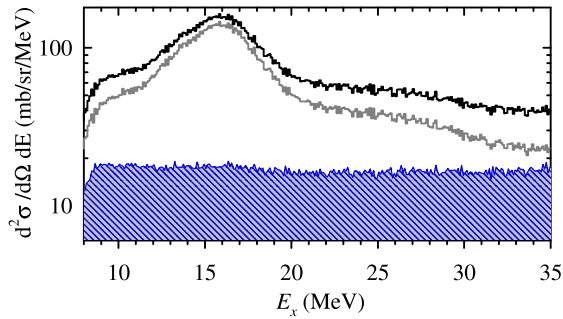


Fig. 1. Excitation-energy spectra for the $^{92}\text{Zr}(\alpha, \alpha')$ reaction at $E_\alpha = 385$ MeV at an averaged spectrometer angle of $\theta_{\text{avg}} = 0.7^\circ$. The blue-gray hatched region represents the instrumental background. The solid black and gray histograms show the energy spectra before and after the instrumental-background subtraction, respectively.

contribution to the nuclear incompressibility in this mass region. Such nuclear structure effects have not been observed in any of the investigations of ISGMR going back to its first identification in the late 1970's [14,15] and, indeed, would be contrary to the standard hydrodynamical picture associated with this mode of collective oscillation [16]. Furthermore, this would lead to a very uncertain determination of the nuclear-matter incompressibility, a key parameter of the equation of state (EOS) of dense nuclear matter that plays “an important role in the supernova phenomenon, the structure of neutron stars, and in the mergers of compact objects (neutron stars and black holes)” [17]. It is also important to note that the only structure effects observed in giant resonances so far are due to ground-state deformation. In addition, there is the apparent softness of nuclei away from the closed shells. Both these effects, entirely different from the claims made for the $A \sim 90$ nuclei, are discussed later.

In this Letter, we report on the ISGMR response in the $^{90,92}\text{Zr}$ and ^{92}Mo nuclei from inelastic α -scattering measurements at an energy of 385 MeV and free of all instrumental background. These nuclei are found to have virtually identical ISGMR responses, revealing no influence of open and/or closed shells for protons and/or neutrons on the ISGMR and, hence, on the nuclear incompressibility.

Inelastic scattering of 385-MeV α particles was measured at the ring cyclotron facility of the Research Center for Nuclear Physics (RCNP), Osaka University. Self-supporting foils of highly enriched targets (97.70%, 95.13%, and 97.37% for ^{90}Zr , ^{92}Zr , and ^{92}Mo , respectively) were used, with thicknesses ranging from 4.0 to 5.38 mg/cm². Inelastically scattered α particles were momentum analyzed with the high-resolution magnetic spectrometer “Grand Raiden” [18], and their horizontal and vertical positions were measured with a focal-plane detector system composed of two position-sensitive multiwire drift chambers (MWDCs) and two plastic scintillators [19]. These detectors enabled particle identification and reconstruction of the trajectories of scattered particles. The vertical-position spectrum obtained in the double-focusing mode of the spectrometer was exploited to eliminate the instrumental background [20,19]. Fig. 1 shows the typical instrumental background, and excitation-energy spectra before and after the background subtraction, for ^{92}Zr as measured at an average spectrometer angle $\theta_{\text{avg}} = 0.7^\circ$.

Data for elastic scattering and inelastic scattering to 2^+ and 3^- states for each nucleus were taken in the angular range of 5.0° to 26.5° . Giant-resonance measurements were performed at very forward central angles of the spectrometer (from 0° to 9.5°) and at magnetic-field settings corresponding to excitation energies in the range $E_x \sim 9.5$ – 35.5 MeV. Using the ray-tracing technique, the angular width of 1.6° for each central angle was divided into four

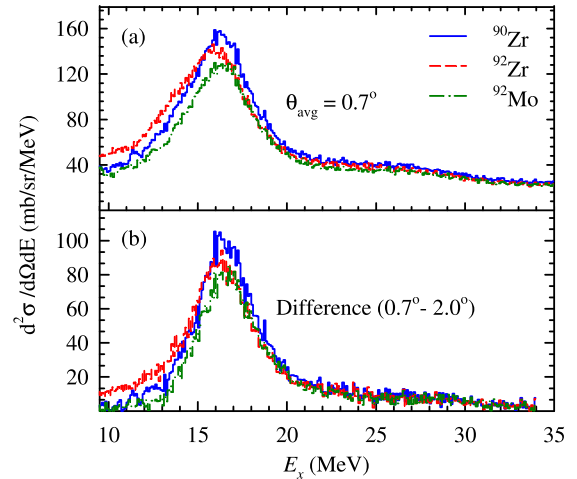


Fig. 2. (Color online.) (a) Excitation-energy spectra measured at an averaged angle 0.7° for the three nuclei, ^{90}Zr (solid blue), ^{92}Zr (red dashed), and ^{92}Mo (green dash-dotted). (b) Difference spectra of averaged angles 0.7° and 2.0° for the same nuclei. The difference spectra comprise essentially the monopole strength (see text).

equal regions during the offline data analysis. Data were also taken with a ^{12}C target at each setting, providing a precise energy calibration. Energy losses in the target foils for the incident beam and outgoing α particles were taken into account.

The excitation-energy spectra at $\theta_{\text{avg}} = 0.7^\circ$ for the three nuclei are overlaid in Fig. 2(a). The spectra near 0° scattering angle exhibit predominantly the monopole strength, and the 0.7° spectra for the three nuclei, shown in Fig. 2(a), are very similar; in particular, for excitation energies beyond 20 MeV, these are nearly identical whereas the results in Refs. [11–13] had shown marked differences in this excitation-energy region. The minor differences in the low-energy part of the spectra (below 16 MeV) are partly due to the different shapes of the ISGMR at low energy (see Fig. 4) and could also be partly due to the different contributions from the toroidal mode, which is not completely understood so far [21].

It has been recognized for quite some time now (see, e.g., Ref. [22]) that the “difference-spectrum”, obtained from subtracting the inelastic spectrum at the first minimum of the expected ISGMR angular distribution from that at 0° (where the ISGMR strength is maximal), essentially represents only the ISGMR strength. This is a consequence of the fact that all other multipolarities have relatively flat distributions in this angular region and, thus, are subtracted out in the “difference-spectrum”. In the present work, the difference spectra for averaged angles of 0.7° (maximal ISGMR strength) and 2.0° (first minimum of ISGMR strength) for all the three nuclei are also almost identical, as shown in Fig. 2(b), again indicating similar ISGMR response in the three nuclei. In particular, the difference spectra beyond $E_x = 20$ MeV fully coincide with each other, whereas the results in Refs. [11–13] had shown dramatically different ISGMR strengths in this region.

In order to extract quantitative strengths for different multipolarities, we have employed the standard multipole-decomposition analysis (MDA) procedure [23,24]. Experimental cross-sections were binned into 1-MeV intervals. The laboratory angular distributions for each excitation-energy bin were converted to the center-of-mass frame using the standard Jacobian and relativistic kinematics. A typical angular distribution for ^{90}Zr at an excitation energy of 16 MeV is presented in Fig. 3. The experimental double-differential cross sections are expressed as linear combinations of calculated double-differential cross sections associated with different multipoles as follows [23,24]:

Table 1

Lorentzian-fit parameters and moment ratios for the ISGMR strength distributions in $^{90,92}\text{Zr}$ and ^{92}Mo . All moment ratios are calculated over the E_x range 10–30 MeV, where, $m_k = \int E_x^k S(E_x) dE_x$ is the k th moment of the strength distribution.

Nucleus	E_m (MeV)	Γ (MeV)	EWSR	m_1/m_0 (MeV)	$\sqrt{m_1/m_{-1}}$ (MeV)	$\sqrt{m_3/m_1}$ (MeV)	K_A (MeV)
^{90}Zr	16.55 ± 0.08	4.2 ± 0.3	0.95 ± 0.06	18.13 ± 0.09	17.66 ± 0.07	19.68 ± 0.13	170.2 ± 2.2
^{92}Zr	16.12 ± 0.04	4.5 ± 0.2	0.97 ± 0.03	18.05 ± 0.05	17.52 ± 0.04	19.77 ± 0.06	174.6 ± 1.1
^{92}Mo	16.79 ± 0.11	4.2 ± 0.4	0.84 ± 0.08	18.20 ± 0.13	17.76 ± 0.11	19.64 ± 0.21	173.3 ± 3.8

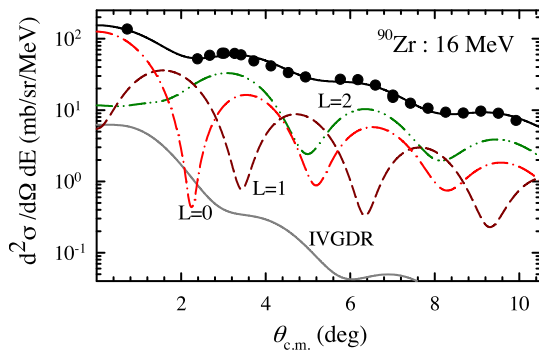


Fig. 3. (Color online.) Typical angular distributions for inelastic α scattering from ^{90}Zr at an excitation energy of 16 MeV. The solid line (black) through the data shows the sum of various multipole components obtained from MDA. The dash-dotted (red), dashed (brown), and dash-double-dotted (green) curves indicate contributions from $L = 0, 1,$ and $2,$ respectively, with the transferred angular momentum L indicated for each of the curves. The solid gray line shows the IVGDR component.

$$\frac{d^2\sigma^{\text{exp}}(\theta_{\text{c.m.}}, E_x)}{d\Omega dE} = \sum_{L=0}^6 a_L(E_x) \frac{d^2\sigma_L^{\text{DWBA}}(\theta_{\text{c.m.}}, E_x)}{d\Omega dE} \quad (2)$$

where $a_L(E_x)$ is EWSR fraction for the L th component and $\frac{d^2\sigma_L^{\text{DWBA}}}{d\Omega dE}(\theta_{\text{c.m.}}, E_x)$ is the calculated DWBA cross section corresponding to 100% EWSR for the L th multipole at excitation energy E_x . The isovector giant dipole resonance (IVGDR) contribution was subtracted out of the experimental data prior to the fitting procedure [25,23]. The DWBA calculations were performed by following the method of Satchler and Khoa [26] using the density-dependent single-folding model, with a Gaussian α -nucleon potential for the real part and a Woods-Saxon imaginary term [23]. We used transition densities and sum rules for various multipolarities as described in Refs. [2,27,28]. The EWSR fractions, $a_L(E_x)$, are determined from a χ^2 minimization. Although we employed DWBA calculated cross sections up to $L = 6$ in the MDA, the strengths could be reliably obtained only up to $L = 3$ due to the limited angular range. The MDA fit to the angular distribution data for the energy bin at $E_x = 16$ MeV in ^{90}Zr , as well as the dominant L contributions are presented in Fig. 3.

The optical model parameters (OMPs) used in the DWBA calculations were determined for each nucleus from elastic scattering angular distributions. The imaginary potential parameters (W , R_I , and a_I), together with the depth of the real part, V , were obtained by fitting the elastic-scattering cross sections using the computer code PTOLEMY [29,30]. Using the $B(E2)$ and $B(E3)$ transition probabilities from the literature, and the OMPs thus obtained, the angular distributions for the 2^+ and 3^- states for each nucleus were calculated within the same DWBA framework. Good agreement between the calculated and experimental angular distributions for the 2^+ and 3^- states for each nucleus established the appropriateness of the OMPs [21].

Experimentally determined ISGMR strength distributions are displayed in Fig. 4 for the three nuclei investigated in the present work. The strength distributions, each consisting of a single, broad peak at $E_x \sim 16.5$ MeV, coincide with each other within exper-

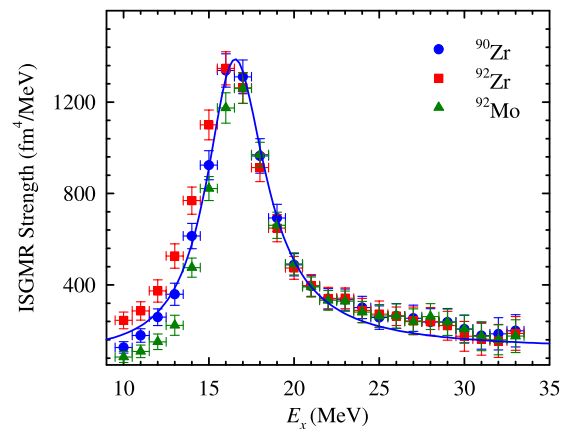


Fig. 4. (Color online.) ISGMR strength distributions for all the three nuclei, ^{90}Zr (blue circles), ^{92}Zr (red squares), and ^{92}Mo (green triangles). The solid line represents the Lorentzian fit for ^{90}Zr .

imental uncertainties, with small differences at the low-energy side. Again, the ISGMR strength in the high-excitation-energy range for ^{92}Zr and ^{92}Mo is identical to that in ^{90}Zr ; the results in Refs. [11–13] had shown marked deviations instead, leading to quite different E_{ISGMR} values. We also note that the ISGMR strength distribution for ^{90}Zr obtained in the present work is in excellent agreement with a previous measurement performed at RCNP [31].

The ISGMR distributions were fitted with Lorentzian curves and the associated peak energies (E_m) and widths (Γ) for the three nuclei are nearly identical as well. A typical Lorentzian fit is also shown in Fig. 4. The extracted parameters are presented in Table 1, along with the various moment ratios typically used in giant-resonance investigations, and nuclear incompressibility, K_A , determined from the moment ratio $\sqrt{m_3/m_1}$ which is employed in the scaling model for E_{ISGMR} [4]. As is clear from the Table, the various moment ratios for all three nuclei, determined over the excitation energy range of 10 to 30 MeV, are also identical within experimental uncertainties, as are the K_A values obtained therefrom (~ 170 MeV in all cases).

The EWSR fractions, determined over the 10–22 MeV excitation-energy range (encompassing the main ISGMR peak), are also provided in Table 1; in all cases, they are close to 100%. It should be noted that the quoted uncertainties in %EWSR values are only statistical and do not include the systematic uncertainties (up to $\sim 20\%$) arising from DWBA calculations, including those attributable to the choice of OM parameters (see, e.g., Ref. [23]).

Determination of the nuclear incompressibility from the ISGMR is based on the assumption that the resonance energies do not depend on detailed structure of the nuclei involved. In fact, there had been no report prior to the results presented in Refs. [11–13] of any “shell effects” leading to significant differences between ISGMR energies in nearby nuclei. For instance, measurements on three Lead isotopes, $^{204,206,208}\text{Pb}$, had resulted in very similar ISGMR energies [32]. Further, detailed investigations of the ISGMR over the Sn and Cd isotopic chains have been performed in recent years [33,23,25]. Although these nuclei emerged as “soft” in comparison to the “standard” nuclei, ^{90}Zr and ^{208}Pb , the ISGMR energies

varied quite smoothly over a wide range of asymmetry parameter $(N - Z)/A$ [23]. [This “softness” of the nuclei in the Sn region is a separate question that has remained open till date [34–38].] Another structure effect appears due to deformation of nuclei, observed in the rare earth region [39,19,40] and, more recently, in the nucleus ^{24}Mg [24], which results in splitting of the strength keeping the ISGMR energy unchanged; the nuclei investigated in this work have no significant deformation, however.

The present results, thus, establish clearly, and strongly, that determination of nuclear incompressibility in nearby medium-heavy to heavy nuclei is not influenced in any appreciable manner by the choice of specific nucleus, or by the underlying nuclear structure.

The obvious question is why the present results are so different from those obtained by the Texas A & M group [11–13]. We believe the answer lies in the way the “background” is accounted for in the two approaches. In the present work, all instrumental background is eliminated because of the superior optical properties of the Grand Raiden Spectrometer (see, e.g., Ref. [19], and Fig. 1), leaving the physical continuum as part of the excitation-energy spectra. In the Texas A & M work, an empirical background is subtracted by assuming that it has the shape of a straight line at high excitation, joining onto a Fermi shape at low excitation to model particle threshold effects [40,41]. This process subtracts the physical continuum as well. It is quite possible, and perhaps likely, that this background subtraction approach is responsible for the differing strengths observed for various nuclei in their work. Since there is no arbitrariness involved in the background-subtraction procedure employed in the present work, it may be argued that our final results are more reliable.

In summary, we have investigated the response of compressional “breathing mode”, the isoscalar giant monopole resonance, in $^{90,92}\text{Zr}$ and ^{92}Mo via inelastic scattering of 385-MeV α particles at extremely forward angles (including 0°). The ISGMR response of these nuclei is practically identical, in contrast with recent reports where significant differences were observed in the ISGMR strength distributions for ^{92}Zr and ^{92}Mo as compared with that for ^{90}Zr , claiming significant nuclear shell structure contributions to the nuclear incompressibility. The present results affirm the standard hydrodynamical picture associated with collective modes of oscillation and clearly indicate that the ISGMR strength distributions vary only in a minor way in nuclei near $A \sim 90$. These variations, the origins of which are unclear, are too small to lead to any significant differences in the extracted nuclear incompressibilities, and it can be concluded that the incompressibilities are not affected by the shell structure of the nuclei near $A \sim 90$.

The authors acknowledge the efforts of the staff of the RCNP Ring Cyclotron Facility in providing a high-quality, halo-free α beam required for the measurements reported here. This work has been supported in part by the U.S. National Science Foundation (Grant No. PHY-1419765). M. Şenyiğit was supported by the Scientific and Technical Council of Turkey (TÜBİTAK) with BİDEB 2219 Scholarship programme.+

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