Heat transfer enhancement in two-start spirally corrugated tube

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Abstract Various techniques have been tested on heat transfer enhancement to upgrade the involving equipment, mainly in thermal transport devices. These techniques unveiled significant effects when utilized in heat exchangers. One of the most essential techniques used is the passive heat transfer technique. Corrugations represent a passive technique. In addition, it provides effective heat transfer enhancement because it combined the features of extended surfaces, turbulators and artificial roughness. Therefore, A Computational Fluid Dynamics was employed for water flowing at low Reynolds number in spiral corrugated tubes. This article aimed for the determination of the thermal performance of unique smooth corrugation profile. The Performance Evaluation Criteria were calculated for corrugated tubes, and the simulation results of both Nusselt number and friction factor were compared with those of standard plain and corrugated tubes for validation purposes. Results showed the best thermal performance range of 1.8–2.3 for the tube which has the severity of $45.455 \times 10^{-3}$ for Reynolds number range of 100–700. The heat transfer enhancement range was 21.684%–60.5402% with friction factor increase of 19.2–36.4%. This indicated that this creative corrugation can improve the heat transfer significantly with appreciably increasing friction factor.

1. Introduction

Basically, three approaches are available yet to enhance the rate of heat transfer, active method, passive method and the compound method [1]. A power source is essential for the active, certain surface modifications or extension, and inserts or fluid additives are used in the passive method, while the compound method is a combination of the above two methods such as surface modification with fluid vibration [2].

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The motivation behind this activity is the desire to obtain more effective heat exchangers and other industrial applications [3], with the major objectives being to provide energy, material, and economic savings for the users of heat transfer enhancement technology.

In heat exchangers, corrugation and other surface modifications are commonly used because they are very effective in the heat transfer enhancement, also it is appearing very interesting for practical applications because it is a technique that promotes secondary recirculation flow, by inducing non-axial velocity components [4]. Recently, a swirl or helical flow pattern produced by employing surface modifications or any other passive technique for heat transfer enhancement is very interesting [5]. Also, Spiral corrugation increases heat transfer enhancement due to secondary flow swirls and surface curvatures pass by fluid layers, which also causes pressure losses [6].

There are few studies concerned with spirally corrugated tube. Mimura and Isozaki [7] investigated the effect of corrugations, different corrugation height and depth on friction factor and heat transfer. Withers [8,9] employed the analogy of heat, and momentum to correlate heat transfer and pressure drop expression in tubes, and the enhancement range of 2.5–3 was reported. Ganeshan and Rao [10] studied a single and multiple corrugation start on friction factor and heat transfer characteristics. Rounded corners corrugated ducts studied by Asako and Nakamura [11] to determine the characteristics of pressure drop and heat transfer. Laminar, transitional and turbulent flow in a tube with spiral flute was studied by Garimella et al. [12]. Their outcomes indicated that the most efficient in promoting the secondary flow are the fluted inner tubes. Thermal characteristics of corrugated tubes for different pitch values were studied by Rainieri and Pagliarini [13] which were used to enhance the convective heat transfer.

Isothermal friction factor and heat transfer spiral corrugation of two start tubes with two-step tapes were studied by Zimparov [14]. A higher heat transfer coefficient and a friction factor were observed compared to the smooth tubes.

Experimental study of the effects of pitch-to-diameter ratio and rib-height to diameter ratios of tubes with helical corrugations on the rate of heat transfer was achieved by Pethkool et al. [15]. Their outcomes indicated that the corrugated tube’s thermal performance is higher than those of the smooth tube. Spirally corrugated tubes were tested by Li et al. [16] numerically for the heat transfer evaluation. The corrugation gives better enhancement, which was concluded from their results depending on corrugation parameters of e/d and p/d.

Both friction factor and Nusselt number were experimentally studied by Saha [17]. His study covered the laminar region by employing circular duct having with a helical screw-tape insert.

Many researchers have investigated corrugated tubes before, and this study has been characterized by many features, the variable thermophysical properties of water one of them, which is the actual case of exchangers and gives results very close to the reality. In addition, a unique smooth corrugation profile was employed, and this kind of corrugation has no matches in the literature and supposes to show good thermal performance with minimum pressure drop which is the ultimate aim of all exchanger designers. Hence, the major objective of the current study was to determine the heat transfer enhancement and pressure drop characteristics of two-start spirally corrugated tube numerically, and also determine the effect of corrugation parameters e/dn and p/dn on heat transfer enhancement and pressure drop. This corrugation profile was chosen because it has smooth profile and can be made up at local markets with cheap price.
2. Geometrical configurations

Corrugated tubes are an interesting technique for obtaining efficient heat exchangers to reduced costs [18]. Hence, a 1 mm thickness aluminum tube of two-start spiral corrugation been modeled with configurations based on SolidWorks software. The main corrugation parameters are the corrugation height $e$, corrugation pitch $p$ tube which has a variable envelope diameter $d_{en}$ according to corrugation height $e$, and bore diameter $d_b$ of 18 mm, as shown in Fig. 1. Five tubes were tested, each has a characteristic parameter of spiral corrugation height to diameter $e/d_{en}$, spiral corrugation pitch to diameter $p/d_{en}$ and severity index $\varphi = e^2/(pd_b)$ as shown in Table 1.

3. Governing equations

The governing equation of the flow problem in the Cartesian coordinates system is as follows:

Conservation of mass:

$$\frac{\partial u_r}{\partial r} + \frac{u_r}{r} + \frac{1}{r} \frac{\partial u_\theta}{\partial \theta} + \frac{\partial u_x}{\partial x} = 0$$  \hspace{1cm} (1)

Momentum equation $r$ component

$$\rho \left( u_r \frac{\partial u_r}{\partial r} + \frac{u_\theta}{r} \frac{\partial u_r}{\partial \theta} + \frac{u_x}{r} + u_r \frac{\partial u_x}{\partial x} \right) = \frac{\partial P}{\partial r} + \mu \left( \frac{\partial^2 u_r}{\partial r^2} + \frac{1}{r} \frac{\partial u_r}{\partial r} - \frac{u_r}{r^2} + \frac{1}{r^2} \frac{\partial^2 u_r}{\partial \theta^2} - \frac{2}{r} \frac{\partial u_\theta}{\partial \theta} + \frac{\partial^2 u_x}{\partial x^2} \right)$$  \hspace{1cm} (2a)

Momentum equation $\theta$ component

$$\rho \left( u_\theta \frac{\partial u_\theta}{\partial \theta} + \frac{u_r}{r} \frac{\partial u_\theta}{\partial r} + u_\theta \frac{\partial u_\theta}{\partial x} \right)$$

$$= -\frac{1}{r} \frac{\partial P}{\partial \theta} + \mu \left( \frac{\partial^2 u_\theta}{\partial r^2} + \frac{1}{r} \frac{\partial u_\theta}{\partial r} + \frac{1}{r^2} \frac{\partial^2 u_\theta}{\partial \theta^2} + \frac{2}{r^2} \frac{\partial u_r}{\partial \theta} + \frac{\partial^2 u_x}{\partial x^2} \right)$$  \hspace{1cm} (2b)

Momentum equation $x$ component

$$\rho \left( u_x \frac{\partial u_x}{\partial x} + \frac{u_r}{r} \frac{\partial u_x}{\partial r} + u_x \frac{\partial u_x}{\partial \theta} \right)$$

$$= -\frac{\partial P}{\partial x} + \mu \left( \frac{\partial^2 u_x}{\partial r^2} + \frac{1}{r} \frac{\partial u_x}{\partial r} + \frac{1}{r^2} \frac{\partial^2 u_x}{\partial \theta^2} + \frac{\partial^2 u_\theta}{\partial x^2} \right)$$  \hspace{1cm} (2c)

Energy equation:

$$\rho c_p \left( u_r \frac{\partial T}{\partial r} + \frac{u_\theta}{r} \frac{\partial T}{\partial \theta} + u_x \frac{\partial T}{\partial x} \right) = k \left[ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 T}{\partial \theta^2} + \frac{\partial^2 T}{\partial x^2} \right]$$  \hspace{1cm} (3)

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Corrugated tubes characteristics (all dimensions in mm).</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tube No.</td>
<td>$d_n$</td>
</tr>
<tr>
<td>1</td>
<td>19</td>
</tr>
<tr>
<td>2</td>
<td>19.5</td>
</tr>
<tr>
<td>3</td>
<td>21</td>
</tr>
<tr>
<td>4</td>
<td>21.5</td>
</tr>
<tr>
<td>5</td>
<td>22</td>
</tr>
</tbody>
</table>

Figure 1 Two-start spirally corrugated tube configuration.
4. Numerical procedure

The commercial CFD code ANSYS FLUENT 14.0 was used to simulate the flow model of smooth and corrugated tubes with mesh generation performed by Gambit 2.4.6 mesh environment. The length of the tubes is 2 m, and the number of starts is two. Reynolds Number range is 100–1300, and the applied heat flux is 5000 (W m⁻²), while the inlet temperature was set constant at 300 K. Water thermo-physical properties were set to be varied with temperature, i.e. \( \mu, \varepsilon, \kappa = f(T) \).

For determining the ordered discretization error in a CFD, the primary assessment criteria of laminar forced convective heat transfer performance were indicated by Nusselt number \( Nu \). To validate the current simulation smooth tube data with previous studies, Churchill and Ozoe developed a closed form expression that covers both entrance and fully developed region [20] which is as follows:

\[
Nu_x = \left[ \frac{4.364 \left( 1 + \frac{Gz}{32} \right)^3}{1 + \left( \frac{Pr(0.0267)^{0.5}}{1 + (Gz/29.6)^{0.5}} \right)^3 \left[ 1 + (Gz/19.04)^{0.5} \right]^{0.5}} \right]^{0.66667} \]

where, \( Gz = \frac{\pi}{4L} \left[ (\pi Re_d \cdot Pr)/4(x/d_i) \right] \)

Eq. (5) agrees within 5% with numerical data for 0.7 \( \leq \) Pr \( \leq \) 10, and has the correct asymptotic behavior of large and small \( Gz \) and \( Pr \). At a value of 1000 or less \( Gz \) represents the point of thermal fully developed. Another reliable correlation for laminar flow in smooth tube was proposed by Shah and London [21], which is empirical correlation and well known in the literature.

\[
Nu = \left\{ \begin{array}{ll}
1.953(Re Pr D/L)^{1/3} & (Re Pr D/L) \geq 33.3 \\
4.364 + 0.0722Re Pr L/D & (Re Pr D/L) \leq 33.3
\end{array} \right.
\]

The local heat transfer coefficient can be calculated as follows:

\[
\frac{h}{\lambda} = \frac{Nu}{Re Pr} \frac{L}{D}
\]

where, \( h \) is the local heat transfer coefficient, \( \lambda \) is the thermal conductivity of the fluid, \( Re \) and \( Pr \) are the Reynolds and Prandtl numbers, respectively.

Finite volume method is the tool which discretized the governing equations, then the implicit steady-state format was solved, and velocity and pressure fields were coupled by SIMPLE algorithm. Both first-order upwind and second-order upwind schemes were employed first, then after making sure that they give the same results (the deviation between them is \( 7.3 \times 10^{-3} \)), first-order upwind scheme was chosen.

5. Results and discussion

5.1. Heat transfer results

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Table 2  Grid optimization.

<table>
<thead>
<tr>
<th>Grid normalize</th>
<th>Grid spacing</th>
<th>Bulk temperature recovery</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>306.836</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>306.051</td>
</tr>
<tr>
<td>3</td>
<td>0.5</td>
<td>305.972</td>
</tr>
<tr>
<td>4</td>
<td>0.1</td>
<td>305.968</td>
</tr>
</tbody>
</table>
\[ q'(x) = h(x)[T_w(x) - T_b(x)] \]  
\[ \text{where } q' \text{ represents the heat flux, } T_w(x) \text{ and } T_b(x) \text{ are the local wall and bulk temperatures, respectively.} \]

The local Nusselt number for the corrugated wall is defined as

\[ Nu = \frac{h_d}{k} \]  
\[ \text{The Reynolds number is defined as} \]

\[ Re = \frac{p d_0}{\mu} \]  
\[ \text{where } d_0 \text{ is the nominal diameter, } d_o = (d_o + d_w)/2. \]

The results were compared with Eqs. (5) and (7) at Re of 100 for validation as shown in Fig. 3. It was found that the deviation is less than ±3% and ±5% for Eqs. (5) and (7) respectively, which considered as acceptable, which indicates that the employed models, meshing, and numerical procedure for the simulation steps are also acceptable. The reasons of this deviation came from different sources, such as software residuals, mesh optimization and the error Margins of Eqs. (5) and (7).

Fig. 4 reveals the temperature and vorticity contours of the two-start corrugation tubes for different values of \( \varphi \). The low wall temperature of the tube gives indication of the significant heat been transferred from the wall toward the fluid. The highest wall temperature was noted at \( \varphi = 2.105 \times 10^{-2} \), while the lowest wall temperature observed at \( \varphi = 45.455 \times 10^{-3} \) which gives a sign that the increase in severity leads to increase in the heat transfer due to swirls of fluid at the corrugation gap, and this swirls break the boundary layer, hence, reducing the resistance and prompting the thermal transportation.

As it was expected, the increase in the severity, causes increase in the swirls at secondary flow region, which is mixing fluid layers and increasing convective surface area as this figure showed, and the tube of high value of \( \varphi \) has strong swirls, while the tube of the low value of \( \varphi \) has weak swirls and low thermal performance. Another merit for this kind of corrugation, is that the swirls do not disturb the core flow of the fluid stream which is very important to decelerate the transition of the flow toward the turbulence region and reducing pressure drop.

Fig. 5 shows the comparison between local Nusselt number \( Nu_L \) and inversely Graetz number \( Gz^{-1} \) which is a function of \( Pr, Re, \) and \( X/d_o \) as it is mentioned in Eq. (5), where the \( Nu_L \) is in direct proportion with \( Gz^{-1} \).

This figure gives an evidence that \( Re \) has a dominant effect on \( Gz^{-1} \) among other parameters, and the enhancement of \( Nu_L \) is sufficient as \( Re \) increases from 100 to 1300. This figure shows two regions separated by line of slope \( m = -0.833 \), and the first region of low \( Re \) has accelerated increase in \( Nu_L \) values which ended at line of the following equation:

\[ Nu_L = 21.833 - 0.833 Gz^{-1} \]

The second region showed steady increase of \( Nu_L \), which means the flow becomes uniform and stabilized, i.e., becomes fully developed flow after relatively long time and distance from the tube inlet because the effect of severity was not included in the figure but it has effect on the flow pattern; consequently, its effect reflected on \( Nu_L \) values. We have to mention that Fig. 5 indicates heat transfer enhancement in the range of 21.684%–60.5402% compared to smooth tube.

Fig. 6 shows average \( Nu \) against \( Re \) for different severity indexes \( \varphi \). As mentioned before, severity combined the effects of all corrugation parameters in one expression except the parameter of the surface area parameter, which can be inferred from the enhanced \( Nu \) values.

This figure indicated that the \( Nu \) increases as \( \varphi \) increases especially at the region where \( Re > 400 \) because the severe roughness helps to disrupt the temperature field, the employed roughness represents a smooth repeated disturbance which acts as a swirls promoter for the fluid layers that are in contact with the tube wall, this leads to more heat transfer by mixing fluid layers with the main flow, and all of these reasons in addition to the extensive increase in the convective surface area reduce the retarding of the flow and increase heat transfer.

5.2. Pressure drop results

The drop in pressure was computed for the tube’s entire length, and the laminar friction factor \( f \) of Darcy was given by the analytical as follows:

\[ f = \frac{64}{Re} \]  
\[ \text{Recently, for the flow in corrugated tubes and tube, Barba} \]  
\[ \text{[22] proposed an empirical correlation for laminar flow region} \]
\[ \text{of range } 100 < Re < 800, \text{ which is as follows:} \]

\[ f = 61.639 Re^{-0.8602} \]  
\[ \text{Fig. 7 shows the validation of friction factor } f \text{ of the current} \]
\[ \text{simulation smooth tube data and a corrugated tube which} \]
\[ \text{subjected to the same loads and boundary conditions as it was} \]
\[ \text{employed in [22] with that of Eqs. (12) and (13) respectively,} \]
\[ \text{a good agreement was observed for the simulation data of smooth} \]
\[ \text{tube compared with Eq. (12), the deviation was} \]
\[ \pm 2\%, \text{ while, the deviation of simulation data of corrugated} \]
\[ \text{tube with Eq. (13) was } \pm 5\%, \text{ and the large deviation between} \]
\[ \text{the simulation data of corrugated tube with Eq. (13) came} \]
\[ \text{from many reasons: first, Eq. (13) correlated empirically for} \]
\[ \text{ethylene glycol fluid which has different thermophysical} \]
\[ \text{properties than water; second, Eq. (13) was derived for different} \]
\[ \text{p/d and e/d also for different corrugation style and profile.} \]

The friction factor \( f \) in comparison with \( Re \) presented in Fig. 8 for different values of severity \( \varphi \). Obviously, when \( p/d_o \) decreases and \( e/d_o \) increases the friction factor will be
Figure 4  Temperature and vorticity contours for different values of severity.
increased at constant Re due to the increase in surface area representing by the corrugation surface area, i.e., as the volume that swept by working fluid increased the friction will increase. In addition, there will be more collisions between fluid particles with the tube wall and also between fluid particles itself due to curvatures. This figure indicates reasonable values of f relative to other studies [18,23] because of the successive smooth curvy obstacles representing by corrugations which the current corrugations provided, and also, it offers harmony and orderly swirls at secondary flow region which helps to reduce pressure drop, hence, saving pumping power.

From the mentioned figure, as u increases, the f increases because of deep corrugations which strengthens swirls. Another reasonable interpretation for the power dissipation is that perpendicular component of velocity vector (radial velocity component) to the main direction of flow causes significant retarding and its effect will increase as u increases.

5.3. Criteria of performance

In order to assess the enhanced surfaces’ effectiveness, the Economic criteria represent the major standard. In addition, Thermal and hydraulic standards have to be considered. Web [24] stated that to obtain perfect surface geometry for the flow in tube, the main influential variables the pressure drop, heat transfer rate and flow rate are used; furthermore, he reported a wide range of evaluation criteria based on convective area or other operational parameters.

The applicable criteria for most cases used by many researchers are the performance evaluation criteria (PEC); these criteria are defined as the heat transfer coefficient ratio of enhanced tube with a promoter to that of plain tube at constant pumping power [25].

\[ i_E = \frac{(Nu_i/Nu_s)/(f_i/f_s)^{0.291}}{Re} = f(Re_i) \]  

Fig. 9 presents the performance evaluation criteria (PEC) against Re, and it shows the direct proportion of \( i_E \) with the increase in Re at \( \varphi \) of \( 2.105 \times 10^{-3}, 5.495 \times 10^{-3} \) and \( 11.204 \times 10^{-3} \) for the Re range of <700, then due to roughness effects of \( e/d_n \) and \( p/d_n \) that were included within \( \varphi \) the increase in friction factor becomes greater than the heat transfer obtained; hence, the friction effect will be dominating over the heat gain effect. From this figure, the best thermal performance 1.8–2.3 is for the tube which has \( \varphi \) of \( 45.455 \times 10^{-3} \) for 100 < Re < 700. This figure also shows an increase in f for the flow in a two-start spiral corrugated tubes for different \( \varphi \) values that were in the range of 19.2–36.4%.
1.8–2.3. Respectively acceptable compared to the gained heat transfer.

In this study, two-start spirally corrugated tubes were numerically studied to determine the effects of spiral corrugation characteristics $e/d$ and $p/d$ on overall thermal performance.

From the obtained results, it was found that this geometry with smooth spiral corrugations can improve the heat transfer significantly at low, medium Reynolds Number. While the region after $Re$ of 700 has increase in friction factor much greater than the enhancement in heat transfer, it was concluded that the master key for getting better heat transfer with lowest pressure drop is the corrugation profile, and it has to be optimized to produce more heat transfer at lowest pumping power.

Results indicated that the severity index $\varphi$ has a great effect on heat transfer enhancement and friction factor, and the heat gained accompanied with a pressure loss especially at high $Re$. Also it was concluded that this corrugation profile produced harmony and orderly swirls at secondary flow region which reduces the pressure drop sufficiently and saving pumping power. In addition, the tube of severity value of $\varphi$ of $45.455 \times 10^{-3}$ had the best thermal performance range of 1.8–2.3.

The heat transfer enhancement range is 21.684–60.5402%, which means the tube geometry has a very good profile; hence, we can get a high value of heat transfer coefficient by using simple smart geometry, and the friction factor increase was found in the range of 19.2–36.4%, which is relatively acceptable compared to the gained heat transfer.

References