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Desingularization of the Milne Universe

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ABSTRACT

Resolution of cosmological singularities is an important problem in any full theory of quantum gravity. The Milne orbifold is a cosmology with a big-bang/big-crunch singularity, but being a quotient of flat space it holds potential for resolution in string theory. It is known, however, that some perturbative string amplitudes diverge in the Milne geometry. Here we show that flat space higher spin theories can effect a simple resolution of the Milne singularity when one embeds the latter in 2 + 1 dimensions. We explain how to reconcile this with the expectation that non-perturbative string effects are required for resolving Milne. Along the way, we introduce a Grassmann realization of the İnönü–Wigner contraction to export much of the AdS technology to our flat space computation.

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context where a lot of papers on this topic¹ have been written is the case of the Milne orbifold, which is a time dependent orbifold

of flat space (see [5–12] for related work). It turns out that some

tree level string scattering amplitudes are singular on the Milne

orbifold [13–15], indicating that perturbative string theory breaks

down. Also, because it is an exact CFT, there are no α' -effects that

can result in a resolution of the Milne singularity.² Together, if we

take these two statements at face value, we come to the conclu-

sion that only non-perturbative g_s -effects can come to the rescue

perspective. We will consider it in the context of Chern-Simons

higher spin theories in 2 + 1 dimensional flat space [16,17]. Our

motivation is as follows. It is expected [18,19] that higher spin

theories capture features of string theory in the tensionless limit,⁴

which corresponds to $\alpha' \rightarrow \infty$. Therefore heuristically, the gauge

symmetries of (classical) higher spin theory can be thought of as

a target space realization of the worldsheet gauge symmetries of

tree-level string theory in the $\alpha' \rightarrow \infty$ limit. So in this limit it is

possible to ask whether spacetime singularities are artifacts of a

singular gauge, and if so, whether one can get rid of them by go-

ing to a different gauge. We will indeed see that by doing a flat

space higher spin gauge transformation, we are able to remove the

singularity in the Milne Universe in a very simple and natural way.

In this paper, we will study the Milne orbifold from another

of Milne, perhaps in a context like the AdS/CFT duality.³

1. Introduction and conclusion

General Relativity is expected to require modifications at short distances. The oft-stated reason for this expectation is the existence of an infinite number of perturbative UV divergent couplings when one quantizes metric fluctuations. String theory solves this problem because it has an enormous gauge symmetry, called worldsheet conformal invariance. This gauge symmetry of string theory essentially uniquely fixes the infinite number of couplings arising in perturbative gravity.

Apart from the quantum problem of divergences, there is also a purely classical reason why we expect that gravity might require modifications at short distances. This is because in gravity, spacetime singularities are ubiquitous [1]. Since string theory is expected to be perturbatively finite in the UV, it is natural to wonder whether it can also resolve spacetime singularities. Some progress along this direction, and answers in the affirmative of various degrees of strength, can be found in [2–4].

Singularities in cosmological (a.k.a. time-dependent) spacetimes are especially tricky in string theory because typically we only understand how to quantize string theory in supersymmetric backgrounds, and supersymmetric backgrounds are automatically time *in*dependent. One way forward is to consider cosmological quotients of flat space as simple examples of time dependent singular backgrounds. The idea is that since the covering space is flat, we should be able to use some of the standard tools from flat space string theory to explore these singular geometries. A simple

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 ¹ There is a whole slew of papers written on this topic in the context of singularity resolution in string theory, so our citation list is necessarily incomplete.
 ² However, for a proposal that winding tachyon condensation can resolve singu-

larities, see e.g. [3].

³ We thank Ben Craps and Boris Pioline for correspondence on related questions.

 $^{^4}$ See [20] for a connection between tensionless strings and flat space.

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This is our main result. To accomplish this, we use a Grassmann trick to rewrite the flat space Chern–Simons HS theory in a form that closely resembles the AdS case. This trick in itself is pretty powerful, but seems to have gone unnoticed before.

Note that in this picture the string coupling $g_s \sim 1/N$ never showed up. There is superficially some tension between this and the general belief from string theory that non-perturbative effects are necessary for resolving Milne.⁵

Perhaps the best way to understand our result is to note that the limit $\alpha' \to \infty$ is precisely the opposite of the limit where the usual Einstein gravity emerges in string theory ($\alpha' \rightarrow 0$). That is, higher spin theories are a different classical limit of string theory. In this limit, the stringy gauge invariances have a simple target space realization in terms of higher spin gauge symmetries. So what we do here amounts more precisely to a de-singularization via a gauge transformation, and not to a resolution⁶: the latter is usually accomplished via the addition of new degrees of freedom, and that is the situation that is envisaged in the usual discussions of the Milne orbifold. We emphasize, however, that it is not that the gauge transformation here is singular, it is that the solution (in the metric language) has interpretation as a spacetime singularity [12]. The Chern–Simons gauge field is in fact regular before and after the resolution, even though the metric is non-singular only after.⁷

Some recent papers dealing with cosmologies and singularities in a higher spin set up can be found in [22–24]. In [23] a cosmological singularity resolution was done, but in the context of dS₃ (higher spin) gravity. The reason why Milne is of much more interest than the dS quotients that we considered in the previous paper is because the geometry is locally flat here, so one can potentially consider string propagation on it. Indeed, Milne has been studied rather extensively in a stringy context as already mentioned. By contrast, the singularity we resolved in dS is an obscure and essentially unknown one, and was merely interesting as a proof of principle. We could not resolve Milne at the time, because flat space higher spin theories were constructed only afterwards [16,17].

Indeed, after the first version of this paper appeared, we have revisited the 2-to-2 string scattering amplitude on the Milne orbifold, and exhaustively scanned for divergences [25]. The result is that *all* the singularity-related divergences arise when the α' (made dimensionless by multiplication with appropriate momenta) is less than some numerical value. The remaining divergences all arise when the tower of intermediate string states go on-shell, and are physical IR divergences. Since higher spin theories are morally the $\alpha' \rightarrow \infty$ limit of string theory, we believe the fact that we are able to resolve the geometry at infinite α' and the fact that string amplitudes are UV finite when α' is large enough, is at the very least, suggestive.

2. Flat 2 + 1 D (higher spin) gravity

We will work with the spin-3 theory in this paper. In 2 + 1 dimensions, working with higher spin theories is easily accomplished via the Chern–Simons formulation of gravity [26], but with a higher rank version of *ISO*(2, 1) as discussed in [16,17].

A lot of work on higher spin theories has been done in the context of AdS_3 theories, and we will make an observation that enables us to translate a lot of this AdS machinery to the flat space theory. This observation is that if one makes the replacement

$$\frac{1}{\rho} \to \epsilon$$
 (1)

where ℓ is the AdS₃ radius and ϵ is a Grassmann parameter defined by the condition that $\epsilon^2 = 0$, then the AdS Chern–Simons action⁸ written in terms of the triad and the spin connection (and their higher spin cousins) reduces to the flat space Einstein–Hilbert action (and its higher spin cousin) times ϵ , provided one takes the Newton constant to be

$$\frac{1}{16G} = k.$$
 (2)

Since we are only concerned about classical equations and their solutions, the overall Grassmann factor in the action will not affect our discussions. The basic reason why this trick works is because of the fact that ISO(2, 1) is the İnönü–Wigner contraction of $SL(2, R) \times SL(2, R)$ (and similarly, for the higher spin generalizations). This approach and some of its applications are further explored in [32].

There are two basic reasons why this trick is useful.

- We can adopt the notations and the *SL*(3) generator matrices of [27] without modifications as long as we make sure that $1/\ell \rightarrow \epsilon$ squares to zero. Without the Grassmann approach, we would be faced with the task of constructing an explicit set of matrices for the generators in [16,17], such that they have a non-degenerate trace form.
- The non-degenerate trace form of the AdS Chern–Simons theory descends to give us a non-degenerate trace form for the flat space theory with this trick.

The upshot is that we can work with flat space (higher spin) gravity in 2+1 dimensions by starting with the AdS Chern–Simons theory, writing the gauge field in terms of the vielbein and spin connection, and setting $1/\ell \rightarrow \epsilon$ with $\epsilon^2 = 0$.

3. Milne: metric and connection

We will take the Milne metric in 2 + 1 dimensions in the form [28,29]

$$ds^{2} = -dT^{2} + r_{C}^{2}dX^{2} + \alpha^{2}T^{2}d\varphi^{2},$$
(3)

where for comparison with [30] we define the metric parameters α , r_c in terms of the "mass", M, and "spin", J, by

$$\alpha = \sqrt{M}, \qquad r_C = \sqrt{\frac{J^2}{4M}}.$$
(4)

(We are following the convention, where 8G = 1.) X, φ directions are compact and closed, both with period 2π . The spacetime looks like a double cone. There is a causal structure singularity at T = 0 which is where the φ -circle crunches before re-expanding in a

 $^{^5\,}$ The connection between string theory and higher spin theory (in particular C–S higher spin theory in flat 2 + 1 D space) has not been made precise, and is mostly heuristic at present. So it is not entirely clear that our result is a bona-fide challenge to the string theory expectations.

⁶ Loosely, we will use the two terms interchangeably.

⁷ It is perhaps also worth emphasizing that the Chern-Simons formulation of gravity and higher spin gravity that we are using is best suited for classical questions. Note that in the spin-2 theory (the usual C-S gravity) it is currently believed that the quantization of the gravity is *not* the same as the quantization of the C-S theory [21]. It is best thought of as only a classical equivalence. This is because invertibility of the vielbeins is required for the CS interpretation, so in the path integral one is integrating over different field configurations. Another relevant observation is that the existence of black holes (at least in the AdS₃ context) indicates a huge degeneracy of states which is surprising in a Chern-Simons theory. We will be using the holonomies to distinguish classical solutions, not define observables in the quantum theory.

⁸ See for example Section 2 and Appendix A of [27].

big-bang. The geometry can be understood in terms of an orbifold of flat Minkowski space and that is what makes it tractable in string theory, but we will not elaborate it here. We have taken the X-direction to be compact to match with some of the flat space holography literature, our results are essentially unchanged even if we drop this assumption.

The corresponding expressions for the triads and spin-connection (dualized using ϵ_{abc}) are

$$e^0 = dT, \qquad e^1 = r_C dX, \qquad e^2 = \alpha T d\varphi, \tag{5}$$

$$\omega^0 = 0, \qquad \omega^1 = \alpha d\varphi, \qquad \omega^2 = 0. \tag{6}$$

So in the Chern–Simons language the SL(2) Grassmann valued connection is⁹

$$A^{\pm} = (\omega^{a} \pm \epsilon e^{a})T_{a}$$

= \pm (\epsilon dT)T_{0} + (\alpha d\varphi \pm \epsilon r_{C}dX)T_{1} \pm (\epsilon \alpha T d\varphi)T_{2}. (7)

The φ -circle holonomy is

$$W_{\varphi}^{\pm} \equiv P \exp\left(\oint d\varphi A_{\varphi}^{\pm}\right)$$
$$= \exp\left[2\pi\alpha(T_1 \pm \epsilon T T_2)\right].$$

The eigenvalue spectrum of the holonomy matrix, $w_{\phi}^{\pm} \equiv 2\pi\alpha(T_1 \pm \epsilon TT_2)$ is $(0, \pm 2\pi\alpha)$. Similarly we can compute the *X*-circle holonomy, $W_X^{\pm} = P \exp(\oint dX A_X^{\pm}) = \exp w_X^{\pm}, w_X^{\pm} = \pm \epsilon 2\pi r_C T_1$. Its eigenvalues are $0, \pm 2\pi r_c \epsilon$. For future reference we also note the characteristic polynomial coefficients [27] of these holonomy matrices (these are identical for both \pm sectors, so we drop the superscripts).

$$\Theta_{\varphi}^{0} \equiv \det(w_{\varphi}) = 0, \qquad \Theta_{X}^{0} \equiv \det(w_{X}) = 0, \tag{8}$$

$$\Theta_{\varphi}^{1} = \operatorname{tr}(w_{\varphi}^{2}) = 8\pi^{2}\alpha^{2}, \qquad \Theta_{X}^{1} = 0.$$
(9)

4. Adding higher spins

To avoid clutter we work exclusively with the "holomorphic" gauge field (A^+) and drop the superscript. The "antiholomorphic" (A^{-}) sector works out exactly parallel. With that understood, to resolve/remove the singularity, now we turn on the higher spin sector:

$$A' = A + \sum_{a=-2}^{2} \left(C^a + \epsilon D^a \right) W_a.$$

We demand that C^a , $D^a = C^a(T)$, $D^a(T)$ for simplicity. If we include ϕ , X dependence as well, then the path-ordered exponentials for the holonomies become hard to evaluate. Besides, we hope to be able to resolve Milne without breaking the symmetries of the geometry. Fortunately, we are able to find a resolution while satisfying these restrictions.

The metric component resulting from inclusion of the higher spin generators is then [31]

$$g'_{\mu\nu} = g_{\mu\nu} + \frac{1}{2} D^a_{(\mu} D^b_{\nu)} Tr(W_a W_b)$$

= $g_{\mu\nu} + \frac{4}{3} D^0_{\mu} D^0_{\nu} - 2D^1_{\mu} D^{-1}_{\nu} - 2D^{-1}_{\mu} D^1_{\nu}$
+ $8D^2_{\mu} D^{-2}_{\nu} + 8D^{-2}_{\mu} D^2_{\nu}.$ (10)

Here, $g_{\mu\nu}$ are the components of the Milne metric (3).

For this connection to describe the same gauge configuration, the new holonomy matrices must be in the same conjugacy class. The new holonomies are

$$\begin{split} w'_{\varphi} &= 2\pi \left(\alpha T_1 \pm \epsilon \alpha T T_2 + C^a_{\varphi} W_a + \epsilon D^a_{\varphi} W_a \right), \\ w'_X &= 2\pi \left(\epsilon r_C T_1 + C^a_X W_a + \epsilon D^a_X W_a \right). \end{split}$$

The eigenvalues are hard to evaluate directly, so we work with the characteristic polynomial coefficients instead, i.e., $\Theta'_{\omega,X}^{0} \equiv$ det $(w'_{\varphi,X})$, $\Theta'^{1}_{\varphi,X} \equiv \text{tr}(w'_{\varphi,X}^{2})$. These must be identical to (8)–(9), for the new connection to describe the same gauge configuration.

For general C's and D's, these relations are complicated (but computable) algebraic expressions, so we will not present them in the general case. Our goal is merely to see whether we can come up with some resolution of the Milne singularity for some choice of C's and D's.

Of course, one needs the new connection to be flat so that it will be a solution to the equations of motion.

$$F' = dA' + A' \wedge A' = 0.$$
(11)

Expanding $A' = A + C + \epsilon D$, and noting that A is already flat, the flatness of A' gives (in terms of components)

$$\begin{split} & [C_{\mu}, C_{\nu}] = 0, \\ & \partial_{\mu}C_{\nu} - \partial_{\nu}C_{\mu} + [C_{\mu}, \omega_{\nu}] + [\omega_{\mu}, C_{\nu}] = 0, \\ & \partial_{\mu}D_{\nu} - \partial_{\nu}D_{\mu} + [D_{\mu}, \omega_{\nu}] + [\omega_{\mu}, D_{\nu}] + [C_{\mu}, e_{\nu}] + [e_{\mu}, C_{\nu}] = 0, \\ & [C_{\mu}, D_{\nu}] + [D_{\mu}, C_{\nu}] = 0. \end{split}$$

5. The Milne resolution

We look at the simple ansatz,

$$C^a_\mu = 0. \tag{12}$$

This generates a holonomy condition from preserving Θ_{φ}^{0} ,

$$D_{\varphi}^{0} = 3(D_{\varphi}^{2} + D_{\varphi}^{-2}), \tag{13}$$

while the rest of the holonomy conditions are automatically satisfied by this ansatz.

Also, this ansatz automatically satisfies 3 of the 4 flatness conditions and leads to the following equation of motion for D's,

$$\partial_{\mu}D_{\nu} - \partial_{\nu}D_{\mu} + [D_{\mu}, \omega_{\nu}] + [\omega_{\mu}, D_{\nu}] = 0.$$

This further leads to

- ∂_TD_X = 0, i.e. D^a_X's are constant.
 [D_X, ω_φ] = 0, which sets, D^{±1}_X = 0, D^{±2}_X = -¹/₂D⁰_X.
 ∂_TD_φ + [D_T, ω_φ] = 0.

This system of equations is simply solved by D_X , $D_T = 0$ and $D_{\varphi} =$ const.

In particular, $D_{\varphi}^0 = 3D_{\varphi}^2$ while $D_{\varphi}^{\pm 1}$, $D_{\varphi}^{-2} = 0$ is a solution to the equations of motion with the same holonomy as that of the Milne orbifold. The reason we picked the ansatz (12) is that the resultant metric gets modified only in its $\varphi \varphi$ -component,

$$g'_{\varphi\varphi} = g_{\varphi\varphi} + 12(D_{\varphi}^2)^2.$$
⁽¹⁴⁾

The curvature scalars are well-defined everywhere. We quote the resultant Ricci scalar,

$$\mathcal{R} = \frac{24(D_{\varphi}^2)^2 \alpha^2}{(12(D_{\varphi}^2)^2 + T^2 \alpha^2)^2}$$
(15)

which is finite and continuous at T = 0.

⁹ Note that the $1/\ell$ in the AdS case [27] has been replaced with the Grassmann parameter ϵ .

So the resolution that we have done here effectively ensures that the shrinking Milne circle has a minimum finite radius at the erstwhile singularity. Remarkably and satisfyingly, we are able to preserve all the symmetries of the original geometry in doing this resolution, and the metric now looks like a smooth bounce, instead of the Milne cone with a crunch/bang.

The original geometry did not have any higher spin fields, but after the gauge transformation, we need also to check that the resultant spin-3 field is regular as well. The spin-3 fields can be computed via [31] $\Phi_{\mu\nu\rho} = \frac{1}{9} \operatorname{tr}(E_{(\mu}E_{\nu}E_{\rho)})$. For the resolved Milne orbifold the nonvanishing components are

$$\begin{split} \Phi_{\varphi\varphi\varphi} &= -\frac{16}{3} \left(D_{\varphi}^2 \right)^3 + \frac{4}{3} D_{\varphi}^2 T^2 \alpha^2 \\ \Phi_{TT\varphi} &= \frac{4}{9} D_{\varphi}^2, \\ \Phi_{TX\varphi} &= -\frac{2}{9} D_{\varphi}^2 r_C \end{split}$$

which is manifestly regular everywhere. We can think of these higher spin fields as the matter supporting the resolved Milne geometry.

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References

- S.W. Hawking, G.F.R. Ellis, The Large Scale Structure of Space-Time, Cambridge University Press, Cambridge, 1973.
- [2] A. Strominger, Massless black holes and conifolds in string theory, Nucl. Phys. B 451 (1995) 96, arXiv:hep-th/9504090.
- [3] J. McGreevy, E. Silverstein, The Tachyon at the end of the universe, J. High Energy Phys. 0508 (2005) 090, arXiv:hep-th/0506130.
- [4] http://online.kitp.ucsb.edu/online/singular-m07/.
- [5] L. Cornalba, M.S. Costa, A new cosmological scenario in string theory, Phys. Rev. D 66 (2002) 066001, arXiv:hep-th/0203031.
- [6] L. Cornalba, M.S. Costa, C. Kounnas, A resolution of the cosmological singularity with orientifolds, Nucl. Phys. B 637 (2002) 378, arXiv:hep-th/0204261.
- [7] L. Cornalba, M.S. Costa, Time dependent orbifolds and string cosmology, Fortschr. Phys. 52 (2004) 145, arXiv:hep-th/0310099.

- [8] J. Khoury, B.A. Ovrut, N. Seiberg, P.J. Steinhardt, N. Turok, From big crunch to big bang, Phys. Rev. D 65 (2002) 086007, arXiv:hep-th/0108187.
- [9] H. Liu, G.W. Moore, N. Seiberg, Strings in a time dependent orbifold, J. High Energy Phys. 0206 (2002) 045, arXiv:hep-th/0204168.
- [10] N.A. Nekrasov, Milne universe, tachyons, and quantum group, Surv. High Energy Phys. 17 (2002) 115, arXiv:hep-th/0203112.
- [11] B. Craps, D. Kutasov, G. Rajesh, String propagation in the presence of cosmological singularities, J. High Energy Phys. 0206 (2002) 053, arXiv:hep-th/0205101.
- [12] M. Berkooz, B. Craps, D. Kutasov, G. Rajesh, Comments on cosmological singularities in string theory, J. High Energy Phys. 0303 (2003) 031, arXiv:hepth/0212215.
- [13] B. Pioline, M. Berkooz, Strings in an electric field, and the Milne universe, J. Cosmol. Astropart. Phys. 0311 (2003) 007, arXiv:hep-th/0307280.
- [14] M. Berkooz, B. Pioline, M. Rozali, Closed strings in Misner space: cosmological production of winding strings, J. Cosmol. Astropart. Phys. 0408 (2004) 004, arXiv:hep-th/0405126.
- [15] B. Craps, Big bang models in string theory, Class. Quantum Gravity 23 (2006) S849, arXiv:hep-th/0605199.
- [16] H. Afshar, A. Bagchi, R. Fareghbal, D. Grumiller, J. Rosseel, Higher spin theory in 3-dimensional flat space, Phys. Rev. Lett. 111 (2013) 121603, arXiv:1307.4768 [hep-th].
- [17] H.A. Gonzalez, J. Matulich, M. Pino, R. Troncoso, Asymptotically flat spacetimes in three-dimensional higher spin gravity, J. High Energy Phys. 1309 (2013) 016, arXiv:1307.5651 [hep-th].
- [18] B. Sundborg, Stringy gravity, interacting tensionless strings and massless higher spins, Nucl. Phys., Proc. Suppl. 102 (2001) 113, arXiv:hep-th/0103247.
- [19] E. Witten, talk given at J.H. Schwarz 60th Birthday Conference, 2001.
- [20] A. Bagchi, Tensionless strings and Galilean Conformal Algebra, J. High Energy Phys. 1305 (2013) 141, arXiv:1303.0291 [hep-th].
- [21] E. Witten, Three-dimensional gravity revisited, arXiv:0706.3359 [hep-th].
- [22] C. Krishnan, S. Roy, Higher spin resolution of a toy big bang, Phys. Rev. D 88 (2013) 044049, arXiv:1305.1277 [hep-th].
- [23] C. Krishnan, A. Raju, S. Roy, S. Thakur, Higher spin cosmology, arXiv:1308.6741 [hep-th].
- [24] B. Burrington, L.A. Pando Zayas, N. Rombes, On resolutions of cosmological singularities in higher-spin gravity, arXiv:1309.1087 [hep-th].
- [25] B. Craps, C. Krishnan, A. Saurabh, Low tension strings on a cosmological singularity, arXiv:1405.3935 [hep-th].
- [26] E. Witten, (2+1)-dimensional gravity as an exactly soluble system, Nucl. Phys. B 311 (1988) 46.
- [27] A. Castro, E. Hijano, A. Lepage-Jutier, A. Maloney, Black holes and singularity resolution in higher spin gravity, J. High Energy Phys. 1201 (2012) 031, arXiv:1110.4117 [hep-th].
- [28] G. Barnich, A. Gomberoff, H.A. Gonzalez, The flat limit of three dimensional asymptotically anti-de Sitter spacetimes, Phys. Rev. D 86 (2012) 024020, arXiv:1204.3288 [gr-qc].
- [29] G. Barnich, Entropy of three-dimensional asymptotically flat cosmological solutions, J. High Energy Phys. 1210 (2012) 095, arXiv:1208.4371 [hep-th].
- [30] A. Bagchi, S. Detournay, R. Fareghbal, J. Simon, Holography of 3d flat cosmological horizons, Phys. Rev. Lett. 110 (2013) 141302, arXiv:1208.4372 [hep-th].
- [31] A. Campoleoni, S. Fredenhagen, S. Pfenninger, S. Theisen, Asymptotic symmetries of three-dimensional gravity coupled to higher-spin fields, J. High Energy Phys. 1011 (2010) 007, arXiv:1008.4744 [hep-th].
- [32] C. Krishnan, A. Raju, S. Roy, A Grassmann path from AdS₃ to flat space, arXiv:1312.2941 [hep-th].