

# Problem identification using program checking

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## Abstract

We describe *AlgoVista*, a web-based search engine that assists computer scientists find algorithms and implementations that solve specific problems. *AlgoVista* also allows algorithm designers to advertise their results in a forum accessible to programmers and theoreticians alike. *AlgoVista* is not keyword based. Rather, users provide *input*⇒*output* samples that describe the behavior of their needed algorithm. This *query-by-example* requires no knowledge of specialized terminology—the user only needs an ability to formalize her problem. *AlgoVista*'s search mechanism is based on a novel application of *program checking*, a technique developed as an alternative to program verification and testing. *AlgoVista* operates at <http://www.algovista.com>.

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## 1. Background

Frequently, working software developers encounter a problem with which they are unfamiliar, but which—they suspect—has probably been previously studied. Just as frequently, algorithm developers work on problems that they suspect have practical applications.

Unfortunately, the programmer with a problem in search of a solution and the theoretician with a solution in search of an application are unlikely to connect across the geographical and linguistic chasms that often separate the two. In many organizations working programmers do not have easy access to a theoretician, and, when they do, they often find communication difficult.

In this paper we will describe *AlgoVista*, a web-based, interactive, searchable, and extensible database of problems and algorithms designed to bring together applied and theoretical computer scientists. Practicing programmers can query *AlgoVista* to look for relevant theoretical results, and theoretical computer scientists can extend *AlgoVista* with problem solutions.

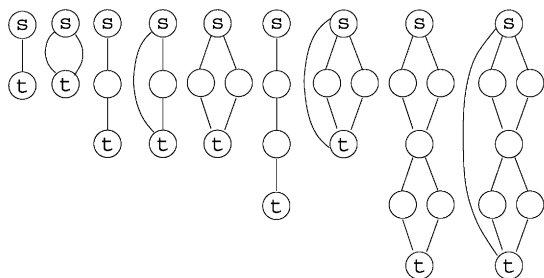
*AlgoVista* relies on a novel application of a *program (or result) checking*. Program checking was developed by Manuel Blum and others [3–5,9,15,16,18] as an alternative to program verification and testing. Program checking extends programs with *checkers* that verify the correctness of the results they compute.

### 1.1. Two motivating episodes

To motivate the need for specialized search engines for computer scientists, we will consider two concrete episodes from the experience of the authors.

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Working on the design of graph-coloring register allocation algorithms, the second author showed his theoretician colleague Sampath Kannan the following graphs:

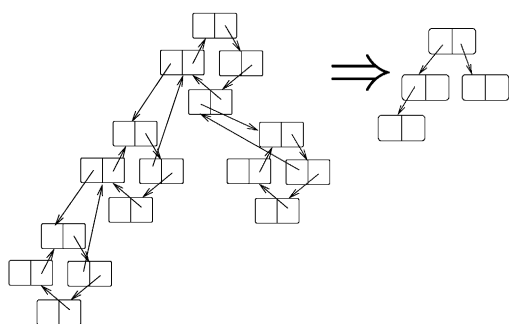


“Do these graphs mean anything to you?” Todd asked.

“Sure”, Prof. Kannan replied, “they’re series-parallel graphs”.

This was the beginning of a collaboration which resulted in a paper in the *Journal of Algorithms* [12].

In a similar episode, the first author showed his theoretician colleague Clark Thomborson the following graph-transformation:



“Do you know what I am doing here?” Christian asked.

“Sure”, Prof. Thomborson soon replied, “you’re shrinking the biconnected components of the underlying (undirected) graph”.

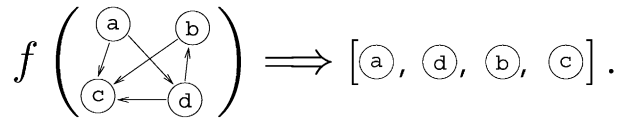
This result became an important part of a joint paper on software watermarking [7].

It is important to note that, while in both these episodes the authors had a pretty good grasp of the problem they were working on, they lacked knowledge of the relevant terminology. Hence, standard keyword-based search techniques would not have been of much assistance. In these episodes, the theoretical computer scientist provided the crucial problem identification that allowed the authors to conduct further bibliographical searches themselves.

## 1.2. Interacting with *AlgoVista*

*AlgoVista* is an online database that stores and codifies problems, algorithms, and combinatorial structures developed within the Computer Science theory community. An applied computer scientist will typically interact with *AlgoVista* by providing *input*  $\Rightarrow$  *output* samples. *AlgoVista* will then search its database looking for problems that map *input* to *output*.

As a concrete example, consider the following query:



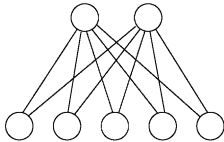
This query asks:

Suppose that from the linked structure on the left of the  $\Rightarrow$  I compute the list of nodes to the right. What function  $f$  am I then computing?

$\lambda$ goVista might then respond with:

This looks like a *topological sort* of a *directed acyclic graph*. You can read more about topological sorting at <http://www.nist.gov/dads/HTML/topologsort.html>. A Java implementation can be found at <http://www.math.grin.edu/~rebelsky/Courses/152/97F/Outlines/outline.49.html>.

$\lambda$ goVista is also able to identify some simple combinatorial structures. Given the following query:



$\lambda$ goVista might respond with:

This looks like a *complete bipartite graph*. You can read more about this structure at <http://mathworld.wolfram.com/CompleteBipartiteGraph.html>.

### 1.3. Organization

The remainder of this paper is organized as follows. Section 2 introduces *program checking* and describes how *checklets* (program checkers in  $\lambda$ goVista) are used as the basic entries in  $\lambda$ goVista's database. Section 3 presents the overall architecture of  $\lambda$ goVista and discusses relevant security issues. Section 4 describes the design of the  $\lambda$ goVista query language and type system. Section 5 introduces *query transformations* that the system uses to bridge any potential semantic gap between user queries and checklets. Section 6 evaluates the performance of the search algorithms. Section 7 discusses related work, and Section 8, finally, summarizes our results.

## 2. Program checking

$\lambda$ goVista can be seen as a novel application of *program checking*, an idea popularized by Manuel Blum and his students. The idea behind program checking is simply this. Suppose we are concerned about the correctness of a procedure  $P$  in a program we are writing. We intend for  $P$  to compute a function  $f$ , but we are not convinced it does so. We have three choices:

- (1) We can attempt to *prove* that  $P \equiv f$  over the entire domain of  $P$ .
- (2) We can test that  $P(x) = f(x)$ , where  $x$  is drawn from a reasonable domain of test data.
- (3) We can include a *result checker*  $C_f^P$  with the program. For every actual input  $x$  given to  $P$ , the result checker checks that  $P(x) = f(x)$ .

We normally require  $C_f^P$  and  $P$  to be independent of each other; i.e. they should be programmed using very different algorithms. We also want the checker to be *efficient*. To ensure that these conditions are met, it is generally expected that a result checker  $C_f^P$  should be asymptotically faster than the program  $P$  that it checks. That is, we expect that if  $P$  runs in time  $T$  then  $C_f^P$  should run in time  $o(T)$ .

```

checklet sorting (int[] input => int[] output)
  if length(input) ≠ length(output) then reject
  for i ← 1 to length(output)-1 do
    if output[i] > output[i+1] then reject
  if the multisets input and output do not contain
  the same elements then reject
  accept http://www.nist.gov/dads/HTML/sort.html

```

(a)

```

checklet topologicalSort (
  Digraph inGraph => Node[] outNodeList)
  if the nodes of inGraph ≠ outNodeList then reject
  for (f,t) ← the edges of inGraph do
    if index of f in outNodeList > index of
    t in outNodeList then reject
  accept http://www.nist.gov/dads/HTML/topologcsort.html

```

(b)

Fig. 1. Some simple checklets. (a) A *sorting* checklet. Its speed depends on how fast we can compare two multisets for equality. If the elements are small enough we can use bucket sort in  $O(n)$  time. Otherwise, we can use a hashing scheme that runs in time proportional to the size of the hash table. (b) A *topological sorting* checklet.

Table 1  
Partial list of problem and graph descriptions found in *AlgoVista*

Maximal independent set	Transitive closure
Longest common subsequence	Clique problem
Independent set	Proper edge coloring
Perfect matching	Spanning Tree
AVL Tree	Undirected Graph
Complete graph	Single destination shortest path
All pairs shortest path	Strongly connected Graph
Single source shortest path	Combination
Maximum bipartite matching	Least common multiple
Directed Acyclic Graph	Hamiltonian cycle
Articulation points	Eulerian graph
Matching	Permutation
Euler cycle	Biconnected Graph
Connected graph	Single pair shortest path
Bipartite Graph	Clique
Maximum consecutive subsequence	

### 2.1. Checklets: result checkers in *AlgoVista*

The *AlgoVista* database consists of a collection of result checkers which we call *checklets*. A checklet typically takes a user query  $input \Rightarrow output$  as input and either *accepts* or *rejects*. If the checklet accepts a query, it also returns a description of the problem it checks for.

Fig. 1 shows some simple checklets. Fig. 1(b), is a particularly interesting checklet for topological sorting. Any acyclic graph will typically have more than one topological order. It is therefore not possible for the checklet to simply run a topological sorting procedure on the input graph and compare the resulting list of nodes with the output list given in the query. Rather, the checklet must, as shown in Fig. 1(b), first check that every node in the input graph occurs in the output node list, and then check that if node  $f$  comes before node  $t$  in the output list then there is no path  $t \rightsquigarrow f$  in the input graph.

*AlgoVista* currently contains some three-hundred problem descriptions, some of which are listed in Table 1.

### 2.2. Examples

We will next examine two examples of what *AlgoVista* can do.

**Example 1.** Suppose Bob is trying to write a program that identifies the locations for a new franchise service. Given a set of potential locations, he wants the program to compute the largest subset of those locations such that no two locations are close enough to compete with each other. It is trivial for him to compute which pairs of locations would compete, but he does not know how to compute the feasible subset. He starts by trying to come up with an example of how his program should work:

- If there are three locations  $a, b, c$  and  $a$  competes with  $b$  and  $c$ , then the best franchise locations are  $b$  and  $c$ .

If Bob is unable to come up with his own algorithm for this problem he might turn to one of the search-engines on the web. But, which keywords should he use? Or, Bob could consult one of the algorithm repositories on the web, such as <http://www.cs.sunysb.edu/~algorithm/>, which is organized hierarchically by category. But, in which category does this problem fall? Or, he could enter the example he has come up with into *AlgoVista* at [algovista.com](http://algovista.com):

$$[a--b, a--c] ==> [c, b]$$

This query expresses:

If the input to my program is two relationships, one between  $a$  and  $b$  and one between  $a$  and  $c$ , then the output is the collection  $[b, c]$ .

Another way of thinking about this query is that the input is a graph of three nodes  $a, b$ , and  $c$ , and edges  $a-b$  and  $a-c$ , but it is not necessary for Bob to know about graphs. *AlgoVista* returns to Bob a link directly to <http://www.cs.sunysb.edu/~algorithm/files/independent-set.shtml> which contains a description of the Maximal Independent Set problem. From this site there are links to implementations of this problem.

**Example 2.** Suppose Bob is writing a simple DNA sequence pattern matcher. He knows that given two sequences  $\langle a, a, t, g, g, g, c, t \rangle$  and  $\langle c, a, t, g, g \rangle$ , the matcher should return the match  $\langle a, t, g, g \rangle$ , so he enters the query

$$([a, a, t, g, g, g, c, t], [c, a, t, g, g]) ==> [a, t, g, g]$$

into *AlgoVista* which (within seconds) returns the link <http://www.nist.gov/dads/HTML/longestcommn.html> to a description of the longest common subsequence problem.

### 2.3. Checklet construction

Much research has gone into the search for efficient result checkers for many classes of problems. In some cases, efficient result checkers are easy to construct. For example, let  $P(x)$  return a factor of the composite integer  $x$ . This is generally thought to be a computationally difficult problem. However, checking the correctness of a result returned by  $P$  is trivial; it only requires one division. On the other hand, let  $P(x)$  return a least-cost traveling salesman tour of the weighted graph  $x$ . Checking that a given tour is actually a minimum-cost tour is as expensive as finding the tour itself.

In some cases it may be difficult to construct checklets which run in an acceptable amount of time. This is particularly true of NP-hard problems for which it would seem to be impossible to find polynomial time result checking algorithms. In these cases we may have to use *spot-checking* [9], a recent development in result checking, to check hard problems probabilistically.

## 3. System overview

A typical user will search *AlgoVista* by submitting a query through the *AlgoVista* web page, where it is matched against the checklets in the checklet database. The output from any accepting checklet is transferred back to the client and presented to the user.

To extend the database with new problem identifications, a user downloads a checklet template, modifies and tests it, and uploads the new checklet into the server where it is added to the checklet database. *AlgoVista* is the first search engine on the web to allow arbitrary users to upload executable code into its database. In [8] we address a number of related security issues.

The basic *AlgoVista* search algorithm is very simple:

```

function search (query)
   $q \leftarrow \text{parse}(\text{query})$ 
  responses  $\leftarrow \{\}$ 
  for every combination of query transformations  $T_1(T_2(\dots))$  do
     $q' \leftarrow T_1(T_2(\dots q \dots))$ 
    for every checklet  $c$  in the database do
      if  $c$  accepts  $q'$  with response  $r$  then
        responses  $\leftarrow$  responses  $\cup \{r\}$ 
  return responses

```

The algorithm is essentially an exhaustive search: a query is submitted to every checklet in the database, and the response of every accepting checklet is returned. In Section 5, we show that a query may also undergo a set of *representation transformations* prior to being submitted. These transformations try to compensate for the fact that user queries and checklets may use different data representations for the same problem.

#### 4. The query language

The primitives of QL, the *AlgoVista* query language, include integers, floats, booleans, lists, tuples, atoms, and links. Links are (directed and undirected) edges between atoms that are used to build up linked structures such as graphs and trees. Special syntax was provided for these structures since we anticipate that many *AlgoVista* users will be wanting to identify graph structures and problems on graphs.

The following grammar shows the concrete syntax of the query language:

```

 $S \rightarrow \text{int} \mid \text{float} \mid \text{bool} \mid$ 
   $S ::= S$ 
   $\text{atom} [ '/' S ]$ 
   $\text{atom} \text{'->'} [ '/' S ] \text{atom}$ 
   $\text{atom} \text{'--'} [ '/' S ] \text{atom}$ 
   $\text{'[ ' } [ S \{ ',' S \} ] \text{'}$ 
   $\text{'( ' } S \text{' , ' } S \text{' )'}$ 
 $\text{bool} \rightarrow \text{'true'} \mid \text{'false'}$ 
 $\text{atom} \rightarrow \text{'a'} \dots \text{'z'}$ 
 $\text{int} \rightarrow \text{'0'} \dots \text{'9'} \{ \text{'mbox0'} \dots \text{'9'} \}$ 
 $\text{float} \rightarrow \text{int} \text{'.'} \text{int}$ 

```

$\text{'S} ::= S'$  maps inputs to outputs,  $\text{'(S,S)'}^{\text{'}}$  represents a pair of elements, and  $\text{'[S\{,S\}]'}^{\text{'}}$  represents a list of elements. Atoms,  $\text{'atom[/S]'}^{\text{'}}$ , are one-letter identifiers that are used to represent nodes of linked structures such as graphs and trees. They can carry optional node data. Links between nodes can be directed  $\text{'atom->[/S]atom'}^{\text{'}}$ , or undirected  $\text{'atom-[/S]atom'}^{\text{'}}$ , and can also carry edge data.

Fig. 2 gives some example queries. In the query in Fig. 2 ①, a directed graph is mapped to a directed graph. The query in Fig. 2 ② asks *AlgoVista* to identify a particular graph, which turns out to be a strongly connected directed graph.

Fig. 2 ③, finally, shows a query that maps a pair of vectors to a vector:

$$\text{'([3,7], [5,1,6]) ==> [5,1,6,3,7]'}^{\text{'}}$$

*AlgoVista* returns the result  $\langle \text{List append} \rangle$  since

$$\text{append}([5,1,6], [3,7]) = [5,1,6,3,7].$$

To arrive at this result *AlgoVista* first swapped the input pair using a *query transformation*. Query transformations yield alternative *input* $\Rightarrow$ *output* queries for *AlgoVista* to consider.

#### 5. Query transformations

Early on in the design of *AlgoVista* we realized that there is often a representational gap between a user's query and the checklet that is designed to match this query. For example, there are any number of reasonable ways for a user to express a topological sorting query, including representing the input graph as a *list of edges*, an *adjacency matrix*, or a




#	QL query	Query explanation
①	$[a \rightarrow b, b \rightarrow c] \implies [a \rightarrow a, a \rightarrow b, a \rightarrow c, b \rightarrow b, b \rightarrow c, c \rightarrow c]$ Query result: (Transitive closure)	What function maps  to  ?
②	$[a \rightarrow b, b \rightarrow c, c \rightarrow a]$ Query result: (Strongly connected graph)	What kind of graph is this:  ?
③	$([3, 7], [5, 1, 6]) \implies [5, 1, 6, 3, 7]$ Query result: (List append)	What function maps the lists $[3, 7]$ and $[5, 1, 6]$ to the list $[5, 1, 6, 3, 7]$ ?
④	$[a \rightarrow c, a \rightarrow d, b \rightarrow c, d \rightarrow c, d \rightarrow b] \implies [a, d, b, c]$ Query result: (Topological sort)	List of edges representation. Node set is implied.
⑤	$[[0, 0, 1, 1], [0, 0, 1, 0], [0, 0, 0, 0], [0, 1, 1, 0]] \implies [1, 4, 2, 3]$ Query result: (Topological sort)	Adjacency matrix representation.
⑥	$[a \rightarrow [c, d], b \rightarrow [c], c \rightarrow [], d \rightarrow [c, b]] \implies [a, d, b, c]$ Query result: (Topological sort)	List of neighbors representation. Node set is implied.

Fig. 2. Example QL queries.

*list of neighbors*. These queries are shown in Fig. 2 ④–⑥. The corresponding topological sorting checklet, on the other hand, might expect the input graph only in a matrix form.

AlgoVista provides a set of *query transformations* that will automatically mutate queries between common representations. For example, given the topological sorting query in Fig. 2 ④, AlgoVista would automatically produce the queries in Fig. 2 ④–⑥, all of which would be matched against the checklets in the checklet database.

In Section 3 we described a straightforward algorithm that employs exhaustive search to submit every possible mutation of a query to every checklet in the checklet database. Obviously, with dozens of transformations and maybe hundreds of checklets this procedure will be prohibitively expensive. Precomputing *viable* transformations can speed up searching by eliminating any such useless transformations. Whenever a new checklet is added to the database, AlgoVista generates a new search procedure  $S_{T,C}$  automatically. This procedure is hardcoded to handle exactly the set of transformations  $T$  which are available in the database of transformations, and the set of checklets  $C$  which are currently available in the checklet database.  $S_{T,C}$  is constructed such that given an input query  $q$  whose type is  $T[q]$ ,  $S_{T,C}$  will apply exactly those combinations of transformations to  $q$  that will result in *viable* mutated queries. A query is *viable* if it is correctly typed for checking by at least one checklet. In other words, AlgoVista’s optimized search procedure  $S_{T,C}$  will never perform a useless transformation, one that could not possibly lead to a mutated query correctly typed for some checklet.

In order to apply transformations and to test checklets efficiently, AlgoVista determines the signature of an input query upon its arrival. Given the query’s signature, AlgoVista knows exactly which, if any, checklets to test, and which, if any, transformations to apply. Furthermore, AlgoVista knows the exact signature of each newly-generated query because it knows the input query signature and how the transformation will transform the signature. For example, AlgoVista knows that applying the FlipPair transform to

Map(Pair(Float, Int), Float)

will yield

Map(Pair(Int, Float), Float).

This observation yields a very simple, but highly optimized architecture that applies transformations and tests checklets based on signatures, in which there is one function per signature responsible for all the operations that affect queries of that signature. Each function has three parts: verifying the originality of the query, testing all matching checklets, and generating isomorphic queries by applying transformations. All generated queries are simply handed off to the function that handles their signature.

Fig. 3 is a graphical representation of the functions that would be generated for the checklets and transformations in our running example. The nodes depict the signature-bound functions and the edges show transformations from one signature to another. The shaded nodes are those nodes that have associated checklets.

To construct this query signature graph we start with those signatures accepted by checklets—they are trivially acceptable. Then, for all of those signatures, we apply the inverted transformations wherever possible.

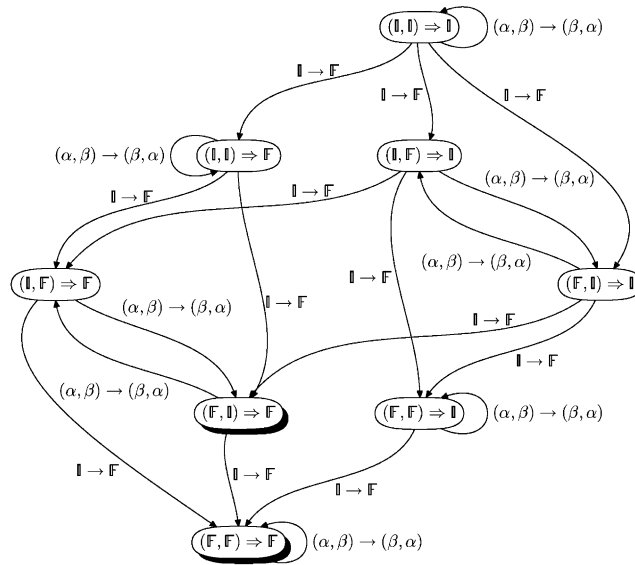


Fig. 3. A query signature graph. The two transformations Int2Float and FlipPair are represented by  $\mathbb{I} \rightarrow \mathbb{F}$  and  $(\alpha, \beta) \rightarrow (\beta, \alpha)$ , respectively. Shaded nodes represent *viable* signatures, those that have associated checklets.

There is, however, one unfortunate complication. Consider the following example:

```
[a->b,b->c]
  Vector2VectorPair
=>      ([a, b, c], [a->b, b->c])
  Vector2VectorPair
=>      ([a, b, c], ([a, b, c], [a->b, b->c]))
  Vector2VectorPair
=>      ([a, b, c], ([a, b, c], ([a, b, c], [a->b, b->c])))
=>      ...
```

In this particular example, the query  $\lceil [a \rightarrow b, b \rightarrow c] \rceil$  (representing a linked list  $\langle a, b, c \rangle$ ) is transformed into  $\lceil ([a, b, c], [a \rightarrow b, b \rightarrow c]) \rceil$ . This is the standard *AlgoVista* representation of a linked structure, a pair of a node-list and an edge-list. However, the *Vector2VectorPair* transformation can be re-applied to the edge-list in the transformed query, *ad infinitum*.

As it turns out, with any sufficiently rich set of transformations, it is always possible to generate an infinite number of signatures. To avoid this problem, and to bound the number of signatures, we put a limit on the number of transformations that will be applied to any query. Typical values for this limit is four to six. With our current database of 95 checklets, with 28 unique signatures, and 23 transformations, *AlgoVista* can accept queries with 9828 different signatures. The generation of the decision tree and all of the signature-specific functions is done automatically by a small Icon program [11].

## 6. Evaluation

Table 2 shows the search times for some typical queries. The times were collected by running each query four times and averaging the wall clock times of the last three runs. The reason for discarding the first measurement is that Java start-up times are quite significant and unpredictable. Furthermore, in web applications such as this one, programs are typically pre-loaded into (a large) primary memory and queries are fielded without any disk accesses.

The five columns of Table 2 show the query, the average wall clock times for the query using the exhaustive and the precomputed search, and the average wall clock times for generating all mutated queries using the exhaustive and the precomputed algorithms. In other words, the last two columns do not include the execution times of the checklets, just the time it takes to generate the transformed queries that would be submitted to the checklets.



Table 2  
Timing measurements

Query	Search		Mutations	
	Exhaustive	Precomputed	Exhaustive	Precomputed
$\lceil [1, 3] \Rightarrow 2 \rceil$	0.41	0.37	0.12	0.39
$\lceil (1, 2) \Rightarrow 3 \rceil$	0.41	0.44	0.12	0.46
$\lceil ([a, b, c, d], [a \rightarrow b, b \rightarrow c, c \rightarrow d, d \rightarrow a]) \rceil$	0.79	0.32	0.17	0.31
$\lceil ([a, b, c, d], [a \rightarrow b, b \rightarrow c, c \rightarrow d]) \Rightarrow [a, b, c, d] \rceil$	2.2	0.55	0.83	0.54
$\lceil [a \rightarrow b, b \rightarrow c, c \rightarrow d] \Rightarrow [a, b, c, d] \rceil$	0.16	0.44	0.04	0.37
$\lceil [a \rightarrow b, b \rightarrow c] \Rightarrow [a, b] \rceil$	0.69	0.39	0.13	0.42
$\lceil ([a, b, c, d], [a \rightarrow /2b, b \rightarrow /2c, c \rightarrow /3d]) \Rightarrow 3 \rceil$	2.1	0.45	0.78	0.49
$\lceil [a \rightarrow /1b, b \rightarrow /2c, c \rightarrow /3d] \Rightarrow 6 \rceil$	0.17	0.47	0.04	0.36
$\lceil ([1, 2, 3], [4, 5, 6]) \Rightarrow [1, 2, 3, 4, 5, 6] \rceil$	0.41	0.45	0.09	0.42
$\lceil [6, 5, 4, 3, 2, 1] \Rightarrow [1, 2, 3, 4, 5, 6] \rceil$	0.05	0.34	0.01	0.34

Times are in seconds. Anomalous measurements are due to rounding errors and inadequate timer resolution. The measurements were collected on a lightly loaded Sun Ultra 10 workstation with a 333 MHz UltraSPARC-III CPU and 256 MB of main memory, running *AlgoVista* on Sun JDK 1.2.1.

Looking at Table 2 it is clear, as would be expected, that in most cases the precomputed search algorithm is superior to the exhaustive algorithm. However, it should be stressed that the comparison is inherently unfair. The exhaustive algorithm, although slower, will sometimes report results that the precomputed algorithm will overlook. The reason is that the precomputed algorithm limits the number of transformations that can be applied to a query, while the exhaustive one does not.

It is interesting to note that the size of the exhaustive algorithm is constant whereas the size of the implementation of the precomputed algorithm grows with the number of checklets and transformations. This will sometimes result in detrimental instruction cache effects. This is illustrated in Table 2 where for simple queries the exhaustive search algorithm performs better than the precomputed algorithm.

We expect that as the system grows with more checklets and query transformations, the performance of the precomputed search algorithm will greatly exceed that of the exhaustive algorithm. The reason is that the execution time of the exhaustive algorithm for a query  $Q$  is

$$O(\#\text{mutations}(Q) \times \#\text{checklets})$$

while the execution time of the precomputed search algorithm is

$$O(\#\text{viable\_mutations}(Q)),$$

where we expect

$$\#\text{viable\_mutations}(Q) \ll \#\text{mutations}(Q).$$

## 7. Related work

A number of web sites, for example the *CRC Dictionary* [2] and the *Encyclopedia of Mathematics* [19], already provide encyclopedic information on algorithms, data structures, and mathematical results. Like all encyclopedias, however, they are of no use to someone unfamiliar with the terminology of the field they are investigating.

More relevant to the present research is *Sloane's On-Line Encyclopedia of Integer Sequences* [17]. This search service allows users to look up number sequences without knowing their name. For example, if a user entered the sequence  $\lceil 1, 2, 3, 5, 8, 13, 21, 34 \rceil$ , the server would respond with "Fibonacci numbers." It is interesting to note that, although many of the entries in the database include a program or formula to generate the sequences, these programs do not seem to be used in searching the database. Similar search services are *Plouffe's Inverter* [14] where one can look up real numbers and the *Encyclopedia of Combinatorial Structures* [13].

*Inductive Logic Programming* (ILP) [1] is a branch of Machine Learning. One application of ILP has been the automatic synthesis of programs from examples and counter-examples. For example, given a language of list-manipulation primitives (`car`, `cdr`, `cons`, and `null`) and a set of examples

```
append([], [], []).
append([1], [2], [1,2]).
append([1,2], [3,4], [1,2,3,4]).
```

an ILP system might synthesize the following Prolog-program for the `append` predicate:

```
append(A, B, B) :- null(A).
append(A,B,C) :- car(A, X), cdr(A, Y),
                 append(Y, B, C1),
                 cons(X, C1, C).
```

Obviously, this application of ILP is far more ambitious than *AlgoVista*. While both ILP and *AlgoVista* produce programs from *input*  $\Rightarrow$  *output* examples, ILP *synthesizes* them while *AlgoVista* just retrieves them from its database. The ILP approach is, of course, very attractive (we would all like to have our programs written for us!), but has proven not to be particularly useful in practice. For example, in order to synthesize *Quicksort* from an input of sorting examples, a typical ILP system would first have to be taught *Partition* from a set of examples that split an array in two halves around a pivot element:

```
partition(3, [], [], []).
partition(5, [6], [], [6]).
partition(7, [6], [6], []).
partition(5, [6,3,7,9,1], [3,1], [6,7,9]).
```

*AlgoVista* is essentially a *reverse definition* dictionary for Computer Science terminology. Rather than looking up a term to find its definition (as one would in a normal dictionary), a reverse definition dictionary allows you to look up the term given its definition or an example. The *DUDEN* [6] series of pictorial dictionaries is one example: to find out what that strange stringed musical instrument with a hand-crank and keys is called, you scan the *musical instruments* pages until you find the matching picture of the *hurdy-gurdy*. Another example is *The Describer's Dictionary* [10] where one can look up "mixture of gypsum or limestone with sand and water and sometimes hair used primarily for walls and ceilings" to find that this concoction is called *plaster*.

## 8. Summary

*AlgoVista* provides a unique resource to computer scientists to enable them to discover descriptions and implementations of algorithms without knowing theoretical nomenclature. *AlgoVista* is a web-based search engine that accepts

*input*  $\Rightarrow$  *output*

pairs as input and finds algorithms that match that behavior. This Query-By-Example mechanism relieves users of the burden of knowing terminology outside their domain of expertise. *AlgoVista* is extensible—algorithm designers may upload their algorithms into *AlgoVista*'s database in the form of checklets that recognize acceptable input/output behavior.

*AlgoVista* is operational at <http://www.algovista.com>.

The current implementation of *AlgoVista* provides several different search modes. Users can choose to search *compressively* or *quickly*, using the exhaustive or precomputed search algorithms, respectively. Furthermore, searching can be done by *value* (the default search mode as described in this paper), by *signature*, or by *keyword*. Signature searching provides faster but less precise results by only matching the types of queries and checklets. Finally, *AlgoVista* also provides signature searching of the Java APIs.

It should be obvious that *AlgoVista* is not able to solve *all* programmers' problems *all* of the time. A programmer who is unable to abstract away from details of the problem at hand, formalizing it into one or two crisp examples will not be helped by *AlgoVista*. He will also not be helped by any other search tool or Computer Science text-book. Furthermore, a programmer who is not able to come up with these simple *input*  $\Rightarrow$  *output* samples for his problem also will not be able to generate test data for his finished program.

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