Application of a rule extraction algorithm family based on the Re-RX algorithm to financial credit risk assessment from a Pareto optimal perspective

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ABSTRACT

Historically, the assessment of credit risk has proved to be both highly important and extremely difficult. Currently, financial institutions rely on the use of computer-generated credit scores for risk assessment. However, automated risk evaluations are currently imperfect, and the loss of vast amounts of capital could be prevented by improving the performance of computerized credit assessments. A number of approaches have been developed for the computation of credit scores over the last several decades, but these methods have been considered too complex without good interpretability and have therefore not been widely adopted. Therefore, in this study, we provide the first comprehensive comparison of results regarding the assessment of credit risk obtained using 10 runs of 10-fold cross validation of the Re-RX algorithm family, including the Re-RX algorithm, the Re-RX algorithm with both discrete and continuous attributes (Continuous Re-RX), the Re-RX algorithm with J48graft, the Re-RX algorithm with a trained neural network (Sampling Re-RX), NeuroLinear, NeuroLinear+GRG, and three unique rule extraction techniques involving support vector machines and Minerva from four real-life, two-class mixed credit-risk datasets. We also discuss the roles of various newly-extended types of the Re-RX algorithm and high performance classifiers from a Pareto optimal perspective. Our findings suggest that Continuous Re-RX, Re-RX with J48graft, and Sampling Re-RX comprise a powerful management tool that allows the creation of advanced, accurate, concise and interpretable decision support systems for credit risk evaluation. In addition, from a Pareto optimal perspective, the Re-RX algorithm family has superior features in relation to the comprehensibility of extracted rules and the potential for credit scoring with Big Data.

1. Introduction

1.1. Background

Within the field of financial analysis, the assessment of credit risk has historically been both of the utmost importance and quite difficult. Beginning in the late twentieth century, the advent of sophisticated electronic data storage technologies meant that financial institutions could readily store information regarding potential customers, such as repayment characteristics. As a result, the process of loaning capital within the United States, the United Kingdom, and other industrialized nations is largely predicated on the use of computer-generated credit scores [1].

This automated calculation of credit scores is markedly superior in a number of respects compared with the former process of hand-calculated risk assessments by banking professionals. Advantages include increased objectivity and reliability, as well as reduced costs and labor during the assessment of new credit applications [2]. Nonetheless, at present, the credit evaluation performance of humans with sufficient expertise can still be superior to the results of automated assessments. For this reason, and because the finance industry relies on the appropriate prediction of lending risks, research aimed at improving the validity of computerized credit assessments is ongoing [3].

As noted, automated lending risk evaluations are currently imperfect, and, in fact, the failure of credit scoring algorithms to identify loan recipients who will eventually default on their loans results in sizable losses [1]. Based on readily available data, Finlay determined that, as of the end of 2014, consumer debt in the United States and the United Kingdom stood at $3.1 trillion [4] and

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in which the knowledge contained in activation neurons and connections is elucidated through the use of symbolic rules. Similarly, the Rule Extraction from Network Ensemble (REFNE) [26] technique has been proposed as a means of obtaining symbolic rules from NN ensembles trained to carry out classifications. This approach extracts rules from instances generated using trained ensembles.

1.5. Rule extraction for credit risk assessment

An increasing number of bank collapses, accompanied by massive losses in the financial sector, has resulted in stricter international banking regulations and created a demand for more accurate models for assessing credit risk and structuring loan portfolios among financial institutions.

A useful credit scoring model achieves a good balance between accuracy and comprehensibility. In this context, the former refers to strong classification performance that minimizes prediction error, while the latter refers to ease of comprehension by the users. Historically, accuracy has been the primary focus of credit scoring because any improvement—regardless of how minor—can potentially lead to considerable savings and profits in the future. Therefore, a considerable amount of literature has focused on evaluating techniques to increase the accuracy of credit scoring models.

However, it is also vital that credit scoring models be comprehensible for the following reasons. First, managers need credit scoring models that are easy to interpret to justify their reasons for accepting or denying credit, which is an industry requirement in numerous countries. Second, such models reduce the reluctance among managers to use statistical techniques for credit evaluations. Third, the more thoroughly managers understand the information they receive, the more insight they gain into the factors affecting credit default, thus allowing them to combine statistical scores and expert judgement to make proper credit decisions. While various techniques have been applied to develop more comprehensible credit risk models, very few have focused on balancing accuracy and comprehensibility, which is required for a more exhaustive decision-making process.

Although increasingly complex models for the assessment of credit risk continue to be developed, these are not empirically useful because professionals in the financial industry primarily need comprehensible models that can be easily used in practice [27].

On the other hand, rule extraction techniques generate classification models that have clear advantages. First, they are comprehensible and can therefore be easily incorporated into financial applications where the classifications need to be extremely clear. Second, extracted rules only sacrifice a small degree of accuracy compared with the black box models from which they are generated [9].
taking sample numbers and subspace sizes into consideration, as well as the quantity of attributes that the rule will contain. In this program, a standard decompositional approach is used to extract rules from NNs, such that NNs having a single hidden layer are trained, after which, the GRG algorithm considers the discretized hidden unit activation values.

Another recent rule extraction rule algorithm is Minerva [29], which is somewhat unique because it is applicable under an extremely wide range of circumstances. Minerva can be applied to regression and classification scenarios with both numerical and categorical data without invoking an underlying black box assumption.

Three quantized SVMs (QSVMs) have recently been proposed, representing unique DIMP networks that are trained by employing an SVM learning algorithm [30] and applied for the purpose of rule extraction.

1.7. The Re-RX algorithm family

From system engineering perspective, the Re-RX algorithm cascade repeats the BPNN, the pruning, and C4.5 in a recursive cascade ensemble.

A major advantage of the Re-RX algorithm recently developed by Setiono et al. [22] is that it was designed as a rule extraction tool. It provides a hierarchical, recursive consideration of discrete variables prior to analysis of continuous data. In addition, it is capable of generating classification rules from NNs that have been trained on the basis of discrete and continuous attributes.

In other words, the Re-RX algorithm achieves highly accurate rule extraction and offers good comprehensibility through the generation of perfect or strict separation between discrete and continuous attributes in the antecedent of each extracted rule. Recently, we proposed using both discrete and continuous attributes to generate the decision tree in the Re-RX algorithm framework (hereafter Continuous Re-RX) [22]. Although this seems to be counterintuitive with the design concept of the Re-RX algorithm, in that it results in the generation of a more complex decision tree, the use of both types of attributes is done to enhance accuracy [31,32].

To achieve both concise and highly accurate extracted rules while simultaneously maintaining the good framework of the Re-RX algorithm, we recently proposed supplementing the Re-RX algorithm with J48graft, a class for generating a grafted C4.5 decision tree (hereafter Re-RX with J48graft) [33,34].

Using the Re-RX algorithm, rules have been extracted from pruned NNs previously trained using all available data samples as well as more limited datasets [35,36]. Interestingly, there is little difference in the accuracy of predictions resulting from rule sets generated by pruned NNs trained using a selection of samples and the predictions made by the same program applying an NN trained using the complete dataset. This approach is deemed the “Sampling Re-RX” method.

Herein we provide the first comprehensive comparison of the results obtained by 10 runs of 10-fold cross validation (CV) of the Re-RX algorithm family based on the assessment of credit risk calculated from four real-life, two-class mixed credit-risk datasets. The results of the following methods are compared: the Re-RX algorithm [22]; Continuous Re-RX [31,32]; Re-RX with J48graft [33,34]; Sampling Re-RX [35,36]; NeuroLinear [19]; NeuroLinear+GRG [28]; and three unique rule extraction techniques involving SVMs [30] and Minerva [29].

We describe the Re-RX algorithm in Section 2.1, Continuous Re-RX in Section 2.2, Re-RX with J48graft in Section 2.5, and Sampling Re-RX in Section 2.7. In Section 3, we describe experimental datasets and setup, while in Section 4, we present the results. In Section 5, we discuss the experimental results and provide a detailed discussion on the Re-RX algorithm family from a Pareto optimal perspective, Continuous Re-RX vs. high performance classifiers, Re-RX with J48graft and Sampling Re-RX for the comprehensibility of extracted rules, and the potential of the Re-RX algorithm family for credit scoring with Big Data. Finally, in Section 6, we summarize our conclusions.

2. Method

2.1. Recursive rule extraction algorithm (Re-RX algorithm)

Although the Re-RX algorithm can easily handle multi-group problems, it was originally developed to consider only two-group classification problems [22]. The outline of the Re-RX algorithm is as follows:

Algorithm Re-RX (S, D, C)
Input: A set of data samples S having discrete attributes D and continuous attributes C.
Output: A set of classification rules.
1. Train and prune [37] an NN by using the dataset S and all of its D and C attributes.
2. Let D’ and C’ be the sets of discrete and continuous attributes, respectively, still present in the network, and let S be the set of data samples correctly classified by the pruned network.
3. If D’ = ϕ, then generate a hyperplane to split the samples in S according to the values of the continuous attributes C’, and then stop.
Otherwise, use only the discrete attributes D’ to generate the set of classification rules R for dataset S’.
4. For each rule, R, is generated:
   If support(R,) > δ, and error(R,) > δ, then
   Let S, be the set of data samples that satisfy the condition of rule R, and
   D, be the set of discrete attributes that do not appear in rule condition R.
   If D, = ϕ, then generate a hyperplane to split the samples in S, according to the values of their continuous attributes C,, and then stop.
   Otherwise, call Re-RX (S,, D,, C,).

Any NN training and pruning method can be used in Step 1 of the Re-RX algorithm, as it does not make any assumptions regarding the NN architecture; however, we have restricted ourselves to the use of BPNNs with only one hidden layer because such networks have been shown to retain the universal approximation property [38].

A crucial component of any NN rule extraction algorithm is an effective NN pruning algorithm. Pruning the inputs that are not needed to solve the problem allows the extracted rule set to be more concise, and a pruned network also helps to filter noise that might be present in the data, such as that from outlying or incorrectly labeled data samples. Therefore, from Step 2 onward, the algorithm only processes training data samples that have been correctly classified by the pruned network. Previously, we developed an NN pruning algorithm that incorporates a penalty function during training and adds a positive penalty value to the sum-of-squared error function for each connection with nonzero weight [37]. Consequently, many of the connections have weights very close to zero when network training is complete, and those with very small values can typically be pruned without adversely affecting the accuracy of the network.

If all discrete attributes are pruned from the network, the algorithm generates a hyperplane in Step 3

\[
\sum_{C_i \in C} w_i C_i = w_0
\]

that separates both groups of samples. Statistical and machine learning methods such as logit regression or SVMs can then be used to obtain the constant and the rest of the coefficients of the hyperplane. We employ an NN with one hidden unit in our implementation.

A set of classification rules comprising only discrete attributes is generated when at least one discrete attribute remains in the
Recursive-Rule Extraction Algorithm

Let $D'$ and $C'$ be the sets of discrete and continuous attributes, respectively, still present in the NN. Let $S'$ be the set of data samples correctly classified by the pruned network.

If $D_1 = \emptyset$, then generate a hyperplane to split the samples in $S_1$ according to the value of their continuous attributes $C_1$ and Stop. Otherwise, call $\text{Re-RX}(S_1, D_1, C_1)$.

Let $S_i$ be the set of data samples that satisfies the condition of rule $R_i$. Let $D_i$ and $C_i$ be the set of discrete and continuous attributes that do not appear in the condition of $R_i$.

If $\text{Support}(R_i) > \delta_1$ and $\text{Error}(R_i) > \delta_2$ No Adopt as a Rule

If $D' = \emptyset$, then generate a hyperplane to split the samples in $S'$ according to the value of their continuous attributes $C'$ and Stop. Otherwise, using only the discrete attributes $D'$, generate the set of classification rules $\mathcal{R}$ for the dataset $S'$.

Fig. 1. Schematic overview of the Recursive-Rule eXtraction (Re-RX) algorithm.

pruned network, which effectively partitions the input space into smaller subspaces based on the values of the discrete attributes. Each subspace corresponds to a generated rule, and when the rule is not sufficiently accurate, the Re-RX algorithm is used to further partition the subspace.

The support of a rule, which is the percentage of samples covered by that rule, and each rule’s corresponding error rate are checked in Step 4. If the support meets the minimum threshold $\delta_1$, and the error rate exceeds the threshold $\delta_2$, then the subspace of the rule is further subdivided either by calling Re-RX recursively when no discrete attributes remain present in the conditions of the rule, or by generating a separating hyperplane involving only the continuous attributes. Because the Re-RX algorithm handles discrete and continuous attributes separately, it generates a set of classification rules that are more comprehensible than those with both types of attributes in their conditions.

To enable a better understanding of its underlying mechanisms, a brief overview of the Re-RX algorithm and the concept behind its design is shown in Fig. 1. C4.5 [39] was used to generate decision trees in the Re-RX algorithm. The subdivision of the Re-RX algorithm is a unique function that is inherent in its nature. Each successive subdivision allows the use of other previously unused attributes; this increases the number of extracted rules as well as their accuracy.

It should be noted that the accuracy, comprehensibility, and conciseness of extracted rules have important trade-offs. Before subdivision, extracted rules are more comprehensible and concise, yet less accurate. Conversely, after subdivision, extracted rules are less concise, yet more accurate.

2.2. Re-RX algorithm with continuous attributes (Continuous Re-RX)

Although a primary aim of the Re-RX algorithm is the strict separation of discrete and continuous attributes in the antecedent of each extracted rule, this design often results in reduced accuracy. Whereas the Re-RX algorithm prunes continuous attributes ($C'$) before the C4.5 decision tree is generated (Fig. 2), Continuous Re-RX uses both discrete ($D'$) and continuous ($C'$) attributes to generate the decision tree [31,32], which results in increased complexity. This may seem counterintuitive to the algorithm’s design, but the use of both types of attributes also results in increased accuracy. An outline of Continuous Re-RX is as follows:

Continuous Re-RX ($S', D', C'$)

Input: A set of data samples ($S'$) having both discrete ($D'$) and continuous ($C'$) attributes.

Output: A set of classification rules.
1. Train and prune [37] an NN using the dataset $S$ and all of its $D$ and $C$ attributes.
2. Let $D'$ and $C'$ be the sets of discrete and continuous attributes, respectively, still present in the network, and let $S'$ be the set of data samples correctly classified by the pruned network.
3. Generate decision tree by using both discrete ($D'$) and continuous ($C'$) attributes [31,32].
4. For each rule, $R_i$ is generated:
   - If support ($R_i$) > $\delta_1$ and error ($R_i$) > $\delta_2$, then
     - Let $S_i$ be the set of data samples that satisfies the condition of rule $R_i$.
     - Let $D_i$ be the set of discrete attributes, and let $C_i$ be the set of continuous attributes that do not appear in rule condition $R_i$.
     - Call Continuous Re-RX ($S_i, D_i, C_i$).
   - Otherwise, Stop.

As shown in Fig. 2, in Continuous Re-RX, we carefully set the value of the values of $\delta_1$ and $\delta_2$ in Step 4.

2.3. J4.8

J4.8 [40] is a Java-based version of C4.5 [39], which itself is an improved version of Quinlan’s ID3 algorithm [41]. The decision trees generated by C4.5 are used for classification, so this algorithm is usually described as a statistical classifier. Although these algorithms are quite similar, the improvements C4.5 has over ID3 are that it uses the gain ratio to determine the best target attribute,
2.4. J48graft

Decision tree grafting was developed in order to improve upon the “simplest is best” method for selecting a good tree. The basic tenet of tree grafting is that similar objects tend to have a high probability of belonging to the same class, and if following this process results in a better classification model, then yielding more complex trees becomes unnecessary.

Grafting is a post-process that can easily be applied to decision trees. The primary objective of grafting is to reclassify regions of an instance space containing no training data or only misclassified data, which in turn decreases prediction error. First, grafting identifies the best-suited cuts of existing leaf regions. Next, new leaves with classifications differing from the original are created via a branching out process, which increases the complexity of the tree naturally. However, tree grafting only considers branches that do not introduce classification errors in the data that has already been classified correctly, which ensures error reduction.

The C4.5A algorithm introduced by Webb, which is also referred to as the “all-tests–but–one partition (ATBOP),” is an even more efficient method for evaluating potentially supporting evidence [42]. It was the implementation of the C4.5A algorithm in open source data mining software (the Waikato Environment for Knowledge Analysis [Weka]) that led to the development of J48graft [40].

Pruning aims to reduce the complexity of a decision tree while retaining good predictive accuracy, and therefore can be thought of as the opposite of grafting. Despite these contrasts, or possibly because of them, Webb [43] concluded that pruning and grafting work well in parallel.

2.5. Re-RX algorithm with J48graft (Re-RX with J48graft)

With the objective of extracting more accurate and concise classification rules, we proposed replacing the conventional Re-RX algorithm, which uses C4.5 as a decision tree [39], with Re-RX with J48graft [33,34]. The conventional pruning used in J4.8 both complements and contrasts that used in J48graft [44]. The performance of the Re-RX algorithm [22] is thought to be greatly affected by the decision tree. To extract more accurate and concise classification rules, in consideration of the grafting concepts associated with J48graft, we decided to replace J4.8 with J48graft in the Re-RX algorithm.

We frequently employ Re-RX with J48graft [33,34] to form decision trees in a recursive manner while training MLPs using BP, which allows pruning [37] and therefore generates more efficient MLPs for rule extraction. A schematic overview of Re-RX with J48graft is shown in Fig. 3.

2.6. Sampling selection

In contrast to the development of more complex models for two-class classification problems such as credit scoring, Setiono [35,36] proposed a supervised learning scheme that aims to increase model accuracy by selecting the most appropriate training data samples.

In this scheme, models for classification problems, such as NNs, are trained using a historical dataset. In the case of classification problems such as credit scoring, the credit risk of each sample is labeled as either good or bad. However, some of these class labels may be incorrectly assigned, resulting in the presence of irregular data samples. Although these samples may have similar attributes, as is commonly the case for most samples in one class, they actually belong to a different class. This is problematic because the presence of irregular and/or mislabeled data samples in a training dataset is likely to adversely affect the performance of the NN.
Recursive-Rule Extraction algorithm with J48graft

In the sampling selection technique proposed by Setiono et al. [35,36], NNs are trained to identify potentially irregular and/or mislabeled data samples. Data samples that are consistently misclassified by a majority of NNs are then removed before a model is constructed to distinguish between good and bad credit risk.

The sampling selection technique can be summarized as follows: (1) Ensemble creation: train an ensemble of \( M \) feedforward NNs using the available training data samples; (2) Sample selection: select training data samples based on the predictions of the NN ensemble; (3) Model generation: use the selected samples to train an NN; and (4) Rule extraction: apply an NN rule extraction algorithm to obtain concise and interpretable classification rules capable of distinguishing between good and bad credits.

The selection of samples in Step 2 is, as the name suggests, a core component of the sampling selection technique. First, we employed an NN ensemble to identify outliers in the training dataset. An effective method for improving the predictive accuracy of numerous learning methods is to remove outliers and noise prior to learning. If a data sample is incorrectly classified by a proportion of NNs exceeding the threshold \( \rho \) and thereby identified as an outlier, it is discarded; otherwise, it is retained in the training dataset.

2.7. Re-RX algorithm combined with sampling selection technique (Sampling Re-RX)

Here we describe Re-RX combined with sampling selection techniques (Sampling Re-RX) for preprocessing.

The objective of this algorithm is to achieve highly accurate, concise, and interpretable classification rules for the credit scoring dataset. However, the credit scoring dataset for rule extraction was a financial dataset, so the focus was on decreasing the number of extracted rules and the average number of antecedents. To extract concise rules, we employed Sampling Re-RX, which is better suited for achieving concise and interpretable, as opposed to accurate, classification rules.

We preprocessed the credit scoring dataset using the sampling selection technique [35,36] to extract a fewer number of rules and a lower average number of antecedents. We then employed Sampling Re-RX to extract a set of concise and interpretable diagnostic rules. A schematic overview of Sampling Re-RX is shown in Fig. 4. As shown in the figure, in Sampling Re-RX, a supplementary cross-validation loop is carried out with sampling selection by an NN ensemble.

The most important objective of Sampling Re-RX in terms of credit scoring is to improve the conciseness and interpretability of extracted rules for financial professionals. Hereafter, Re-RX, Continuous Re-RX, Re-RX with J48graft and Sampling Re-RX are referred to as the “Re-RX algorithm family.”

3. Datasets and experimental setup

Assigning accurate credit scores to consumers is a vital function of financial institutions. Credit scores are typically calculated using a mathematical decision model that establishes risk based on the assessment of various attributes such as the consumer’s age and annual income. This assessment process must be transparent, so credit scores must be generated using a “white box” model.

To highlight both the effectiveness and the appropriateness of our proposed model for assessing credit risk, we used the following four real-life, two-class mixed credit-risk datasets: German, Australian, Ben1 and Ben2. A brief description of these datasets is provided below. These four datasets contain a wide variety of attributes, including continuous variables, nominal variables with a limited number of values, and nominal variables with a large number of values, and are therefore frequently referred to in the literature and utilized by financial researchers.

3.1. Australian credit dataset

Available through the University of California Irvine (UCI) Machine Learning Repository [45], the Australian Credit Dataset
contains 690 samples with 14 attributes, eight discrete with two to 14 values, and six continuous. This dataset also contains 307 (approximately 44.5%) positive and 383 (approximately 55.5%) negative instances. To protect the confidentiality of the data, all attribute names and values have been changed to meaningless symbols. For the purposes of this study, we randomly divided this dataset into 50% training data and 50% test data.

3.2. German credit dataset

Also available through the UCI Machine Learning Repository is the German Credit Dataset [45], which contains 1000 samples with 20 attributes. Credit is classified as either good (about 700 samples) or bad (about 300 samples). Other attributes include: (1) current status of existing checking account; (2) duration of account in months; (3) credit history; (4) credit purpose; (5) credit line; (6) status of savings account(s)/bonds; (7) length of current employment; (8) installment rate in percentage of disposable income; (9) sex and marital status; (10) debtors/guarantors; (11) number of years in current residence; (12) property owned; (13) age; (14) other existing installment plans; (15) type of residence; (16) number of existing credit lines; (17) occupation; (18) current status regarding telephone service; (19) foreign worker status; and (20) number of dependents. For the purposes of this study, we randomly divided this dataset into 70% training data and 30% test data.

3.3. Bene1 and Bene2 credit datasets

In this study, the Bene1 and Bene2 datasets [9] used by Benelux-based major financial institutions to summarize consumer credit data were also used. In accordance with standard banking practices, customers in these voluminous datasets are flagged as high risk if they have ever been in payment arrears for more than 90 days. For the purposes of this study, we randomly divided these datasets into approximately 67% training data and 33% test data.

3.4. Experimental setup

Next, the training sets within each database were used to train NNs and extract classification rules. One input unit was created for each continuous attribute in the dataset, and either thermometer or dummy variable encoding was used to convert discrete attributes into a binary input string [46]. The characteristics of the datasets used for evaluating credit risk are summarized in Table 1. In order to deal with the class imbalance problem commonly associated with credit scoring datasets, we used the area under the receiver operating characteristic curve (AUC-ROC) to evaluate performance because it does not include class distribution or misclassification costs [47].

### Table 1

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Size</th>
<th>Total Input</th>
<th>Continuous Input</th>
<th>Discrete Input</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australian</td>
<td>690</td>
<td>14</td>
<td>6</td>
<td>8</td>
</tr>
<tr>
<td>German</td>
<td>1000</td>
<td>20</td>
<td>7</td>
<td>13</td>
</tr>
<tr>
<td>Bene1</td>
<td>3123</td>
<td>27</td>
<td>18</td>
<td>9</td>
</tr>
<tr>
<td>Bene2</td>
<td>7190</td>
<td>28</td>
<td>18</td>
<td>19</td>
</tr>
</tbody>
</table>

4. Results

4.1. Performance

In order to guarantee the validity of the results, we used 10 runs of 10-fold CV [48] to evaluate the classification rule accuracy.
Table 2
Comparison of results from Minerva, QSVM-L, QSVM-P3, QSVM-G, Re-RX*, Sampling Re-RX, Re-RX with J48graft and Continuous Re-RX for the German dataset (10 runs of 10-fold cross validation).

<table>
<thead>
<tr>
<th>Index</th>
<th>Minerva</th>
<th>QSVM-L</th>
<th>QSVM-P3</th>
<th>QSVM-G</th>
<th>Re-RX</th>
<th>Sampling Re-RX</th>
<th>Re-RX with J48graft</th>
<th>Continuous Re-RX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ave # Antecedents</td>
<td>5.61</td>
<td>5.3</td>
<td>5.4</td>
<td>5.7</td>
<td>6.2</td>
<td>6.19</td>
<td>9.13</td>
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</tbody>
</table>
| Re-RX: Recursive-Rule eXtraction; TS: testing dataset; AUC: area under the receiver operating characteristic (ROC) curve; # rules: number of rules; ACC: accuracy; Ave. # ante.: average number of antecedents; 10CV: 10-fold cross validation; 10×10CV: 10 runs of 10-fold cross validation; SVM: support vector machine.

Table 3
Comparison of results from the Minerva, NeuroLinear, NeuroLinear+GRG, QSVM-L, QSVM-P3, QSVM-G, Re-RX*, Sampling Re-RX, Re-RX with J48graft and Continuous Re-RX for the Australian dataset (10 runs of 10-fold cross validation).

<table>
<thead>
<tr>
<th>Index</th>
<th>Minerva</th>
<th>NeuroLinear</th>
<th>NeuroLinear+GRG</th>
<th>QSVM-L</th>
<th>QSVM-P3</th>
<th>QSVM-G</th>
<th>Re-RX</th>
<th>Sampling Re-RX</th>
<th>Re-RX with J48graft</th>
<th>Continuous Re-RX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ave # Antecedents</td>
<td>2.93</td>
<td>1.0</td>
<td>3.7</td>
<td>2.6</td>
<td>6.23</td>
<td>5.27</td>
<td>2.38</td>
<td>5.95</td>
<td></td>
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</tr>
</tbody>
</table>
| Re-RX: Recursive-Rule eXtraction; TS: testing dataset; AUC: area under the receiver operating characteristic (ROC) curve; # rules: number of rules; ACC: accuracy; Ave. # ante.: average number of antecedents; 10CV: 10-fold cross validation; 10×10CV: 10 runs of 10-fold cross validation; SVM: support vector machine.

Table 4
Comparisons between the Re-RX algorithm family for the Bene1 dataset (10 runs of 10-fold cross validation).

<table>
<thead>
<tr>
<th>Index</th>
<th>Re-RX</th>
<th>Sampling Re-RX</th>
<th>Re-RX with J48graft</th>
<th>Continuous Re-RX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ave. # Antecedents</td>
<td>7.57</td>
<td>6.25</td>
<td>7.38</td>
<td>7.52</td>
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</table>
| Re-RX: Recursive-Rule eXtraction; TS: testing dataset; AUC: area under the receiver operating characteristic (ROC) curve; # rules: number of rules; ACC: accuracy; Ave. # ante.: average number of antecedents; 10CV: 10-fold cross validation; 10×10CV: 10 runs of 10-fold cross validation; SVM: support vector machine.

Table 5
Comparisons between the Re-RX algorithm family for the Bene2 dataset (10 runs of 10-fold cross validation).

<table>
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<tr>
<th>Index</th>
<th>Re-RX</th>
<th>Sampling Re-RX</th>
<th>Re-RX with J48graft</th>
<th>Continuous Re-RX</th>
</tr>
</thead>
<tbody>
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<td>Ave. # Antecedents</td>
<td>7.81</td>
<td>6.1</td>
<td>6.46</td>
<td>7.95</td>
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</tbody>
</table>
| Re-RX: Recursive-Rule eXtraction; TS: testing dataset; AUC: area under the receiver operating characteristic (ROC) curve; # rules: number of rules; ACC: accuracy; Ave. # ante.: average number of antecedents; 10CV: 10-fold cross validation; 10×10CV: 10 runs of 10-fold cross validation; SVM: support vector machine.

5. Discussion

5.1. Performance for the German dataset

Continuous Re-RX showed the best accuracy for the test dataset, nearly identical to that obtained by QSVM-P3 [30] and QSVM-L [30] with a much higher number of extracted rules. Minerva provided the smallest number of extracted rules. The number of extracted rules obtained using Re-RX* was less than half that of Sampling Re-RX and Re-RX with J48graft. Although QSVM-L, QSVM-P3, and QSVM-G [30] showed better accuracy, they also had a much higher number of extracted rules.

5.2. Performance for the Australian dataset

Continuous Re-RX showed the best test accuracy. However, the test accuracies for all algorithms were between 85.5% and 86.93%. On the other hand, QSVM-L showed a remarkably concise number of rules (2.0) with only 1.0 antecedent. However, considering the reduced conciseness for the German Dataset (Table 2), which was obtained using the same method, we should not presuppose such excellent conciseness for all types of datasets.

NeuroLinear+GRG also showed a concise number of rules at 2.8. Comparing NeuroLinear+GRG with NeuroLinear, GRG preprocessing for the Australian Dataset was very effective for conciseness and accuracy.

The number of rules and the average number of antecedents obtained by NeuroLinear for the German Dataset [19] were 2.0...
Table 6: Performance of various classifiers and Continuous Re-RX, Sampling Re-RX, and Re-RX with J48graft for the Australian dataset.

<table>
<thead>
<tr>
<th>Method</th>
<th>TS ACC (%)</th>
<th># Rules</th>
<th>Rule set</th>
<th>Ave. # ante.</th>
<th>Year</th>
<th>ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vertical bagging decision trees model</td>
<td>91.97</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2010 [49]</td>
<td></td>
</tr>
<tr>
<td>Weighted-least squares SVM</td>
<td>90.63</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2011 [50]</td>
<td></td>
</tr>
<tr>
<td>Kernel, fuzzification, penalty factors-multi-criteria optimization classifier</td>
<td>88.84</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2014 [51]</td>
<td></td>
</tr>
<tr>
<td>Weighted-case-based-reasoning with preference functions optimized with GA</td>
<td>88.55</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2012 [52]</td>
<td></td>
</tr>
<tr>
<td>Random space bagging decision tree</td>
<td>88.01</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2012 [53]</td>
<td></td>
</tr>
<tr>
<td>Neighborhood rough set + SVM</td>
<td>87.52 ± 0.052</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2011 [54]</td>
<td></td>
</tr>
<tr>
<td>Decision tree ensemble (boosting-100)</td>
<td>87.23</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2014 [55]</td>
<td></td>
</tr>
<tr>
<td>Hidden Markov model/group method of data handling</td>
<td>87.02 ± 1.56</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2013 [56]</td>
<td></td>
</tr>
<tr>
<td><strong>Continuous Re-RX</strong></td>
<td><strong>86.93 ± 0.29</strong></td>
<td>14</td>
<td>Possible</td>
<td>5.95</td>
<td>2016 [31,32]</td>
<td></td>
</tr>
<tr>
<td>SVM + stratified sampling</td>
<td>86.83 ± 3.96</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2012 [57]</td>
<td></td>
</tr>
<tr>
<td><strong>Sampling Re-RX</strong></td>
<td><strong>86.48 ± 0.26</strong></td>
<td>11.04</td>
<td>Possible</td>
<td>5.27</td>
<td>2015 [35,36]</td>
<td></td>
</tr>
<tr>
<td>Artificial immune network-based classifier</td>
<td>86.38</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2012 [58]</td>
<td></td>
</tr>
<tr>
<td>Axiomatic fuzzy set (5CV)</td>
<td>86.22</td>
<td>451.6</td>
<td>-</td>
<td>-</td>
<td>2013 [59]</td>
<td></td>
</tr>
<tr>
<td>Naive Bayes + wrapper (GA) method</td>
<td>86.09</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2015 [60]</td>
<td></td>
</tr>
<tr>
<td><strong>Re-RX J48graft</strong></td>
<td><strong>86.04 ± 0.87</strong></td>
<td><strong>4.58</strong></td>
<td>Yes</td>
<td><strong>2.38</strong></td>
<td>2016 [33,34]</td>
<td></td>
</tr>
<tr>
<td>Group-wise feature selection (50 × 5CV)</td>
<td>85.6 ± 2.5</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2012 [61]</td>
<td></td>
</tr>
</tbody>
</table>

Re-RX: Recursive-Rule eXtraction; TS: testing dataset; ACC: accuracy; Ave. # ante.: average number of antecedents; 10CV: 10-fold cross validation; SCV: 5-fold cross validation; 10×10CV: 10 runs of 10-fold cross validation; 50×5CV: 50 runs of 5-fold cross validation; SVM: support vector machine; RBF: radial basis function; GA: genetic algorithm.

5.3. Performance for the Bene1 dataset

All methods in the Re-RX algorithm family showed approximately the same test accuracies.

In contrast, Sampling Re-RX and Re-RX with J48graft showed about a 30% reduction in the number of rules extracted using Re-RX*. Since the tendency to generate more rules than other rule extraction algorithms is the most serious problem in Re-RX, this result is quite meaningful.

5.4. Performance for the Bene2 dataset

Continuous Re-RX showed the best test accuracy, but was only slightly better than the other methods. In addition, it showed a much higher number of extracted rules than Re-RX*.* On the other hand, Sampling Re-RX and Re-RX with J48graft showed about the half number of rules extracted using Re-RX*. In the same manner as that in Section 5.3, this result was quite meaningful.

5.5. Performance of the Re-RX algorithm family from a Pareto optimal perspective

As the present experiments have demonstrated, no extraction methods that generate both highly accurate and comprehensible rules for credit scoring datasets have been identified. Therefore, as noted in Section 2.1, the best approach appears to be finding a good balance between the two. However, to the best of our knowledge, no ideal rule extraction algorithm has been reported. In the light of this situation, we decided to develop highly accurate rule extraction methods that also offered high comprehensibility by generating perfect or strict separation between discrete and continuous attributes in the antecedent of each extracted rule.

Obtaining a small number of extracted rules from a dataset does not guarantee that the rules extracted by another algorithm, such as when the Australian Dataset was processed by NeuroLinear-i-GRG, will have higher comprehensibility. To compare the extent of comprehensibility between different algorithms, the average number of antecedents per extracted rule is a good indicator.

Needless to say, if we can find a Pareto optimal solution, we will obtain the best rule extraction algorithm. Ideally, we hope to extend the Pareto optimal curve to obtain a wider viable region and provide improvements in both accuracy and comprehensibility. Several newly developed multi-objective optimization formulas using revolutionary computation and related-techniques could be used to provide a theoretical and practical basis for determining a good balance between accuracy and comprehensibility.

5.6. Continuous Re-RX vs. high performance classifiers

For further analysis, we tabulated the accuracies of high performance classifiers for the Australian Dataset, which were recently reported using 10 runs of 10-fold CV, as an example.

As shown in Table 6, the difference in classification accuracy obtained by Continuous Re-RX has been approaching within 5% of that obtained by the highest current performance classifier [49].

From the perspective of rule extraction, the number of rules for high performance classifiers, if applicable, can be treated as infinite. In other words, the only objective function of the classifier is its accuracy. Therefore, high performance classifiers are no different from resignation to find a compromise between both requirements by building a simple rule set that mimics how the well-performing complex model (black-box) makes it decisions. Although the number of rules extracted using Continuous Re-RX was much higher than that of other algorithms in the Re-RX algorithm family, Continuous Re-RX still has the best rule extraction accuracy, with only slightly lower separation capability between discrete and continuous attributes in the antecedent of each extracted rule. The competition for achieving only better classification accuracy for the credit scoring dataset has appeared to plateau [49,50], and unless classification accuracy can be considerably improved, i.e., close to 100%, a very limited contribution will be made to the financial services industry.

5.7. Re-RX with J48graft and Sampling Re-RX for comprehensibility of extracted rules

Recently, Chen et al. [62] reported that financial rule extraction is completely algorithmic or automatic in most systems, and
has little supervision or user interaction. In order to acquire useful and comprehensible knowledge, users need to be integrated into a black box process through an interactive visual framework. However, in their study, Chen et al. ignored various rule extraction algorithms and/or methods.

In contrast, Fortuny and Martens [63] claimed that comprehensibility is required in any domain in which a model needs to be validated before it can be used in practice, such as medical diagnosis or audit mining.

In credit scoring, this requirement is a legal one [8], as described in Section 1.2. The Basel III Capital Accord includes similar requirements in relation to models for internal capital requirement calculations. Furthermore, findings from previous studies have shown that when the inner workings of a decision-making system are not understood by users, they will be skeptical and reluctant to use the model, even if it is well known to improve performance. Although the importance of comprehensibility has long been established [64], current data mining research seems to have a sole focus on predictive accuracy only. While it is possible to increase comprehensibility by constraining or modifying existing techniques (e.g., as in [65]), it is often more desirable to inspect the behavior of well-studied techniques without altering their inner workings. Rule extraction techniques have been proposed as a method to generate predictive rules that mimic the classifications made by the black-box technique without modifications [66], and they play an important role in data mining, which has been described as a process of finding novel and useful patterns in data [67].

As shown below, the rule set generated from the Australian Dataset using Re-RX with J48graft provides insight into the logic underlying the black-box model in human-readable form. The extracted rule set obtained by the Re-RX with J48graft in the present paper is quite concise and interpretable for users. Since the Australian Dataset includes categorical attributes, A4, A5, A6, A12, we converted these into binary code as follows:

\[
\begin{align*}
R1: & \text{D31} = 0 \text{ Then Class 1} \\
R2: & \text{D28} = 0 \text{ AND D31} = 1 \text{ AND D32} = 0 \text{ Then Class 1} \\
R3: & \text{D28} = 1 \text{ AND D31} = 1 \text{ AND D32} = 0 \text{ Then Class 2} \\
R4: & \text{D31} = 1 \text{ AND D32} = 1 \text{ Then Class 2}.
\end{align*}
\]

The average number of extracted rules was 4.0 and the average number of antecedents was only 1.75. Furthermore, only three attributes (D28, D31 and D32) were used. However, the predictive accuracy of the entire rule set was 86.04 ± 0.29. As shown in Table 6, comparing the classification accuracies, that obtained using Re-RX with J48graft (86.04 ± 0.29) was about 5.93% lower than that of the best performance classifier [49].

Certainly, recent high performance classifiers with a grand-scale techniques have shown very high classification accuracies; however, we believe that if the quality of the extracted rules from the financial datasets is strongly considered, the opportunity for supervision and interaction of financial professionals will be dramatically increased. Because transparency is necessary for datasets, using Re-RX with J48graft and Sampling Re-RX is expected to encourage and motivate new financial data analytics.

In fact, the Re-RX algorithm family has already been used for concise and interpretable extracted rules in regard to medical diagnosis for breast cancer [34] and thyroid diseases [32]. In these cases, the quality of rules is emphasized over the classification accuracy.

5.8. Potential of the Re-RX algorithm family for credit scoring with big data

To date, many studies have used both the German and Australian Datasets as part of a general tendency to employ either small- (below 1000 samples) or medium-sized (1000–10,000 samples) datasets [2]. However, more recently, the use of datasets with more than 10,000 samples has somewhat increased [68].

Finlay [1] demonstrated that the credit risk calculations of prominent financial institutions typically use datasets that are either small or of low dimensionality. The largest dataset used in the present study was the Bene2 Dataset, which contains 7190 samples, because the real-world datasets discussed by Finlay, which contain 88,789 and 138,606 samples [1], were considered too large to allow rule extraction via the Re-RX algorithm family in a reasonable time frame.

Regarding the complexity of the Re-RX algorithm family, Re-RX with J48graft took about 5 s to train the German Dataset using a standard workstation computer (3.1 GHz Intel Xeon E5-2687 W, 3.5 GHz Turbo, 25 MB Cache; 64 GB RAM: 512 GB DDR3 System memory). The testing time was negligible.

Therefore, presently, the Re-RX algorithm family remains difficult to use in real-time and/or online tasks for large-scale credit scoring. However, with considerable improvement in information technology and processing speeds, the Re-RX algorithm family can be expected to run much faster on standard workstations or conventional personal computers.

6. Conclusion

In this study, we conducted the first comprehensive performance comparison based on 10 runs of 10-fold CV between the Re-RX algorithm family, NeuroLinear, NeuroLinear+-GRG, Minerva and three rule extraction techniques from SVMs by applying these programs to four different real-life, two-class mixed credit-risk datasets.

The high accuracy of Continuous Re-RX was superior to that obtained using Re-RX, Re-RX with J48graft, Sampling Re-RX, NeuroLinear, NeuroLinear+-GRG, Minerva and three SVM-based methods. Re-RX with J48graft and Sampling Re-RX both use a recursive cascade ensemble to construct a unique hybrid classifier ensemble with perfect or strict separation between discrete and continuous attributes in the antecedents of extracted rules, so as to maintain high comprehensibility. Therefore, these two algorithms generated highly comprehensible rules with perfect or strict separation.

These findings suggest that Continuous Re-RX, Re-RX with J48graft, and Sampling Re-RX comprise a powerful management tool that allows the creation of advanced, accurate, concise and interpretable decision support systems for credit risk evaluation.

In addition, the superior features of the Re-RX algorithm family from the Pareto optimal perspective were discussed, as well as Continuous Re-RX vs. high performance classifiers, and Re-RX with J48graft and Sampling Re-RX in relation to the comprehensibility of extracted rules and the potential of the Re-RX algorithm family in credit scoring with Big Data.

In future studies, we intend to develop much more accurate and comprehensive rule extraction algorithms for large-sized datasets, and to attempt to come close to achieving true rule extraction from Big Data.

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