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Multi-objective Economic Emission Dispatch Solution Using Dance Bee Colony with Dynamic Step Size

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Abstract

Energy planning considering environment aspect is a vital research area for power system operation and control. This paper introduces an efficient variant namely dance bee colony with dynamic step size adjustment for solving the multi objective economic emission dispatch considering valve point effects. The particularity and robustness of the proposed algorithm is validated on two practical test systems IEEE 30-Bus and to 40 units considering valve point effect and power losses. Results compared to many recent competitive methods confirm the efficiency of the proposed method in term of solution quality and convergence characteristics.

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Keywords: Multi Objective, Dance Bee colony, Environmental/economic dispatch, fuel cost, Emission, Step size.

Nomenclature

| | |
|------|--------------------|
| ED | Economic Dispatch |
| DBC | Dancing Bee colony |
| Cost | fuel cost |
| Emi | Emission |

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1. Introduction.

Energy planning considering emissions control is a vital research area for power system operation and control, this type of problem is complex with non-linear fuel cost functions and constraints. Determining the optimal capacity of units considering emissions and practical generator constraints such as valve point effect and prohibited zones is a complex and important subject for experts and researchers [1].

ED problems have been investigated and a large number of mathematical methods developed and applied to solving the combined economic dispatch and environment. Methods such as lambda iteration method, gradient method, linear programming, quadratic programming and interior point methods [2-3], have been applied with success to solving many problems related to power system planning and operation. However all these developed mathematical methods rely on the form of the objective function and fail to find the near global solution when considering practical generator constraints, authors in [4] surveys the conventional optimization methods.

To overcome the major problems related especially to restriction on the nature of the objective function and to take in consideration the real nature of constraint associated to generators such as valve point effect, and prohibited zones, an alternative optimization category based stochastic heuristic aspect is proposed by experts and researchers for enhancing the solution of practical power system planning and control, particularly the combined economic dispatch. In the literature a large number of meta heuristic methods have been proposed, adapted and applied with success to solving many complex problems such as: Improved genetic algorithm (IGA) [5], Particle swarm optimization [6-7], Stochastic optimal strategy [8], modified NSGA-II algorithm [9], niched Pareto genetic algorithm [10], new honey bee mating optimization algorithm [11], fuzzified multi objective particle swarm optimization algorithm [12], multi objective evolutionary algorithms [13], novel multi objective evolutionary algorithm [14], Elitist multi objective evolutionary algorithm [15], an interactive fuzzy satisfying method [16], multi objective particle swarm algorithm with fuzzy clustering [17], artificial immune system [18], incremental artificial bee colony with local search [19], artificial bee colony algorithm with dynamic population size [20], artificial bee colony algorithm [21], Enhancing artificial bee colony algorithm [22], fuzzy based bacterial foraging algorithm [23], New multi-objective stochastic search technique [24], multi-objective differential evolution [26], A hybrid multi-agent based particle swarm optimization algorithm [26] and an improved Artificial Bee Colony Method [27]. The major contributions related to this category and others hybrid methods reviewed by authors in [28].

In this paper, an efficient variant named Dance bee colony with dynamic step size is adapted and applied for solving the multi objective environment economic dispatch considering practical generator constraints. The performances and robustness of the proposed variant validated on many practical test systems considering the effect of valve point and total active power losses.

2. Economic and emission load dispatch

The environmental/economic dispatch problem is to minimize two competing objective functions, fuel cost and emission, while satisfying several equality and inequality constraints. Generally, the mathematical formulation of the problem is described as follows [1].

2.1. Economic dispatch formulation with valve point effect

The cost function of economic load dispatch problem is defined as follows:

$$F(P_g) = \sum_{i=1}^n \left(a_i + b_i P_{gi} + c_i P_{gi}^2 \right) + \left| e_i \sin \left(f_i \left(P_{gi} - P_{gi}^{\min} \right) \right) \right| \quad (1)$$

Where P_{gi} is the power generation of unit i , a_i , b_i , c_i , are fuel cost coefficients of unit i . e_i and f_i are two coefficients, required for introducing valve point effect.

2.2. Emission dispatch formulation

The emission function of economic load dispatch problem is defined as follows:

$$E(P_g) = \sum_{i=1}^n 10^{-2} (\alpha_i + \beta_i P_{g_i} + \gamma_i P_{g_i}^2) + \xi_i \exp(\lambda_i P_{g_i}) \quad (2)$$

Where α_i , β_i , γ_i , ζ_i , and λ_i are coefficients of the i th generator emission characteristics.

2.3. Minimization of fuel cost and emission:

The Multi-objective combined economic and mission problem with its constraints can be mathematically formulated as a nonlinear constrained problem as follows [20]:

$$OF = \omega \sum_{i=1}^n F(P_{g_i}) + (1 - \omega) \sum_{i=1}^n E(P_{g_i}) \quad (3)$$

The solution of the problem is achieved by minimizing the objective function (OF), the fuel cost rate (\$/h) is shown with, $F(P_g)$ and NOx emission rate (ton/h) with $E(P_{g_i})$.

2.4. Constraints

Power equality constraint in the system with transmission losses is given as follows:

$$\sum_{i=1}^n P_{g_i} - P_{load} - P_{loss} = 0 \quad (4)$$

Where P_{load} is the total load demand and P_{loss} is the total power loss in transmission lines.

The P_{loss} , Since the power stations are usually spread out geographically, the transmission loss has to be taken into account. The commonly used method in power utility industry is the B coefficients method [20], which is expressed as follows:

$$P_{loss} = \sum_{i=1}^n \sum_{j=1}^n P_{g_{i,n}} B_{i,j} P_{g_{j,n}} + \sum_{j=1}^n P_{g_{j,n}} B_{0j} + B_{00} \quad (5)$$

Where B , B_0 and B_{00} are all transmission loss coefficients, and B is a $n \times n$ matrix, B_0 is a $1 \times n$ vector, B_{00} is a constant.

The generation capacity constraints of the thermal generation units are taken from [20].

$$P_{g_i}^{\min} \leq P_{g_i} \leq P_{g_i}^{\max} \quad (6)$$

Where $P_{g_i}^{\min}$ and $P_{g_i}^{\max}$ are the minimum and maximum range of power loading limit for n th generator unit respectively.

3 Dance Bee colony

3.1 Overview

The DBC (Dancing Bee colony) algorithm was developed by Laga and Nouioua 2009, to solve the problem of T-coloring of graphs. This algorithm is inspired by bee behavior when foraging. In this paper a variant of the original DBC is proposed and adapted for solving environmental economic dispatch problem. Figure 1 shows the flowchart of DBC, mechanism search.

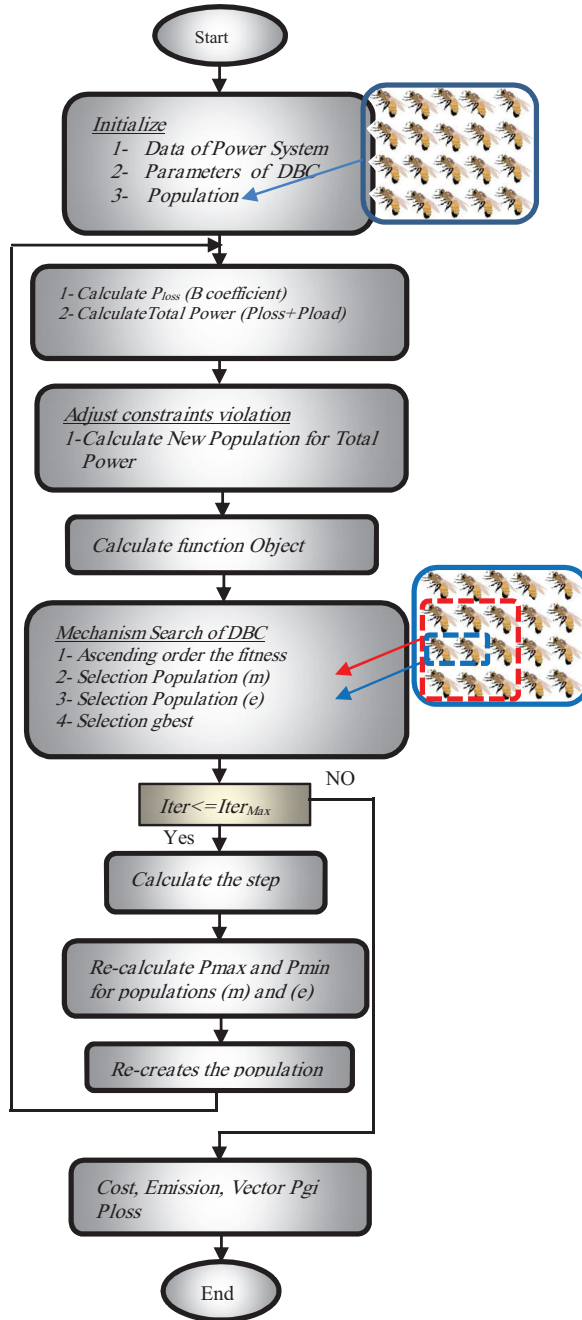


Fig.1 Flowchart of DBC

3.1.1. *Initialization*: The algorithm starts by randomly placing N bees in the search space. The distribution of N bees in the search space is shown in Figure 2.

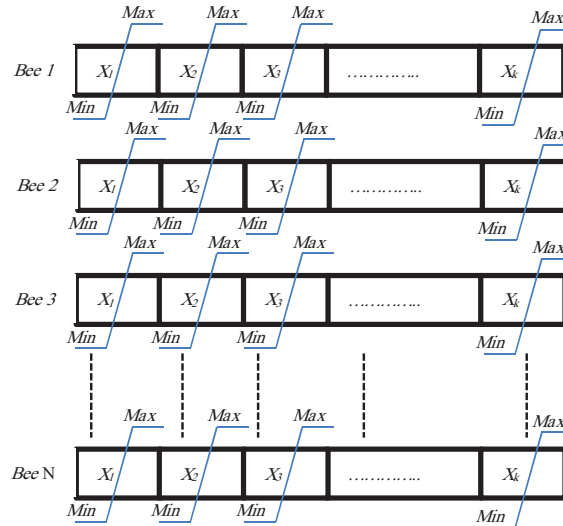


Fig 2 Distribution of a bee in the search space

- 3.1.2. *Evaluation*: calculate the fitness for these bees, the entire population arranged and sorted according to their fitness value.
- 3.1.3 *Decomposition process*: in this step, the search space is decomposed, first a sub group of ‘m’ bees are selected from the entire population, and then a sub group named ‘e’ containing bees with the best fitness is selected from the sub group ‘m’.
- 3.1.3. *The search process adapted described as follows*:
 - a) The search space will be guided principally to the region containing sub group ‘e’ using an adaptive step size with (N_{em}) bees .
 - b) From ($m-e$) space search we recruited a number of bees (N_{es}) for search.
 - c) The rest of bees (N_{gs}) related to other sub groups ($N-m$) affected for random search.

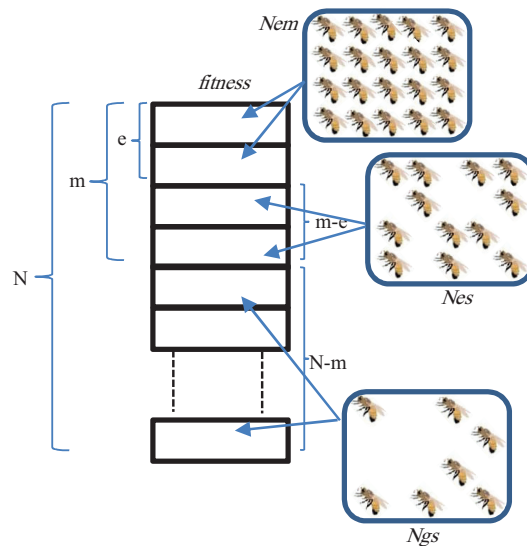


Fig 3 Distribution of all bees in the search space

3.2. Proposed variant:

In this section we will introduce the variant proposed to enhance the performances of the original DBC. The main particularity of the proposed variant is that the search space is dynamic and change dynamically during process search. The following description summarizes the steps of the dynamic steps introduced within the standard DBC algorithm.

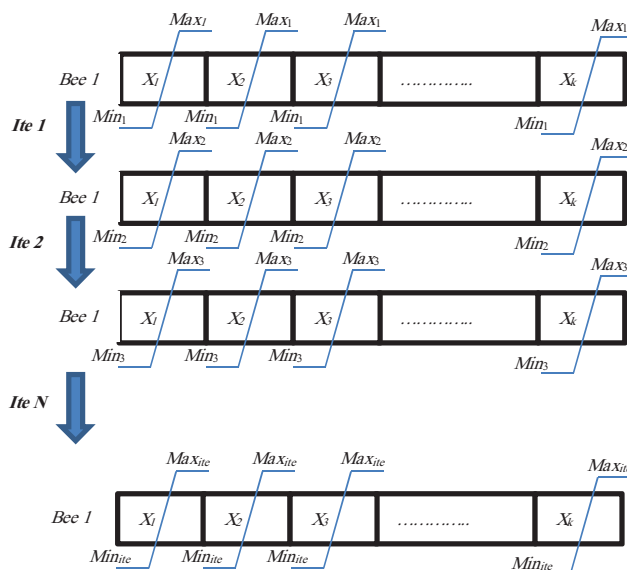


Fig 4 Dynamic evolution of space search during generation

3.2.1. The step is calculated using the following the following relation:

$$S_{now} = S - S \times (itr - 1) / ite \tag{7}$$

Where, S is the initial step, S_{now} is a new step, itr is the actual iteration, and ite is the total number of iteration,

3.2.2. The new search space corresponding to the limits (min and max) of each variable is calculated dynamically during the process search using the following expressions:

$$Max_{now} = x + S_{now} \tag{8}$$

$$Min_{now} = x - S_{now} \tag{9}$$

Where, Max_{now} and Min_{now} are the new estimated limits corresponding to the variable x . Figure 5 shows the direction of the bees to the new estimated space search.

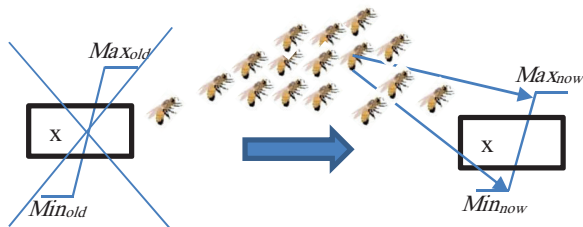


Fig.5 Direction of bees towards the new estimated search space

4 Description of the test systems

4.1 Test system 1:IEEE 30-bus system

This test system consists of 6 generators, the total load to be satisfied is 283.4 (MW). The initial parameters of the DBC algorithm used for this test system are presented in Table 1, the fuel cost rate coefficients, the emission rate coefficients and the B coefficients are given in Tables 6-8. Three cases are considered:

- case1: minimization of fuel cost
- case2: minimization of emission
- case3: minimization of cost and emission

For the first case, the total fuel cost optimized is 605.345\$/h, the convergence characteristic of the algorithm is shown in figure.6. The corresponding total power loss and total emission achieved are 2.2617 (MW) and 0.2207 (ton / h) respectively. In the second case, the total emission is optimized individually, the best value found is 0.19420 (ton/h), the corresponding total fuel cost and power losses achieved are 645.825(\$/h) and 3.39490 (MW). Figure 7 shows the convergence characteristic of the total emission. Details results for optimized control variables are shown in Table 2. In the third case the two objective functions (fuel cost and emission) are optimized simultaneously, the characteristic of the Pareto optimal front corresponding to these two objective functions are shown in Figure 8. In order to verify the efficiency of the proposed variant based DBC, a comparative study in term of solution quality is well presented in Tables 2-3.

Table 1. Parameters of the DBC

| Parameters | <i>N</i> | <i>m</i> | <i>e</i> | <i>Nem</i> | <i>Nes</i> | <i>Ngs</i> | <i>step</i> |
|------------|----------|----------|----------|------------|------------|------------|-------------|
| Value | 100 | 20 | 5 | 20 | 30 | 50 | 20 |

Table 2. Comparison of compromising solutions for Test system 1.

| Generation | $\omega=1.0$ | | $\omega=0.0$ | |
|------------|-----------------|-----------|----------------|-----------|
| | DBC | ABCDP[20] | DBC | ABCDP[20] |
| G1 | 11.4074 | 11.2192 | 41.0803 | 41.0177 |
| G2 | 29.0781 | 29.1144 | 46.2938 | 46.3689 |
| G3 | 58.5793 | 57.9711 | 54.4186 | 54.4481 |
| G4 | 98.8418 | 99.4465 | 39.0882 | 39.0432 |
| G5 | 52.5140 | 52.4485 | 54.3648 | 54.4513 |
| G6 | 35.2412 | 35.5212 | 51.5490 | 51.5520 |
| Cost(\$/h) | 605.3456 | 605.425 | 645.825 | 646.045 |
| Emi(ton/h) | 0.2207 | 0.22090 | 0.19420 | 0.19420 |
| Ploss(MW) | 2.2617 | 2.32110 | 3.39490 | 3.48150 |

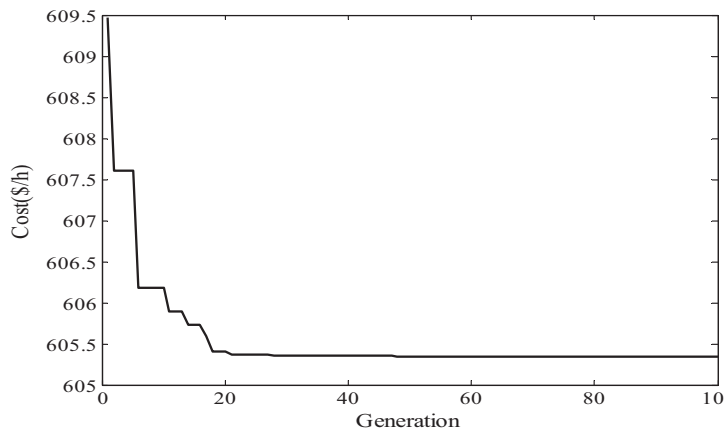


Fig.6. Convergence characteristic for six-unit system: cost minimization

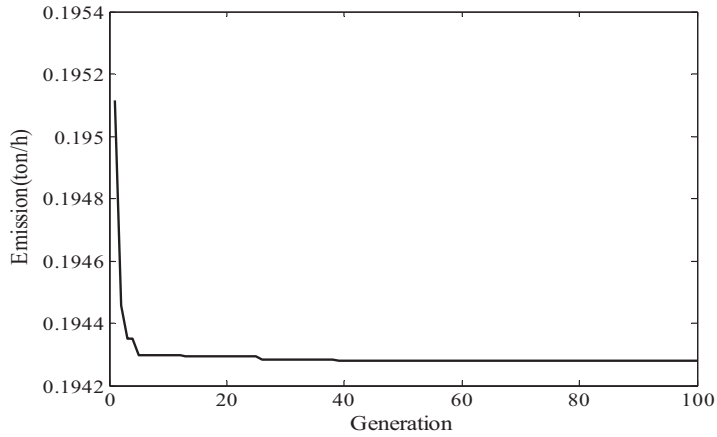


Fig.7 Convergence characteristic for six-unit system: emission minimization

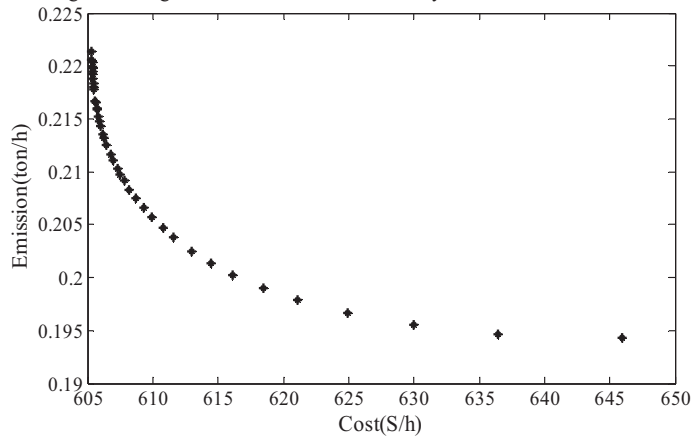


Fig.8. Combined economic emission convergence characteristic; Pareto-optimal front for six-unit system

Table.3.Comparison of the optimisation solution values obtained by different methods

| Methods | $\omega=1.0$ | | | $\omega=0.0$ | | |
|---------------------|-----------------|-------------|---------------|--------------|-------------|------------|
| | Cost (\$/h) | Emi (ton/h) | Ploss (MW) | Cost (\$/h) | Emi (ton/h) | Ploss (MW) |
| MNSGA-II+DCD [9] | 608.1283 | 0.2189 | 3.4548 | 645.3998 | 0.1942 | 3.2894 |
| MNSGA-II[9] | 608.1248 | 0.2199 | 3.4658 | 645.4787 | 0.1942 | 3.3313 |
| MNSGA-II+DCD+CE [9] | 608.1247 | 0.2198 | 3.4709 | 645.6472 | 0.1942 | 3.3173 |
| MBFA [23] | 607.6700 | 0.2198 | 3.2600 | 644.4300 | 0.1942 | 3.2800 |
| FCPSO [23] | 607.7860 | 0.2201 | 3.3500 | 642.8964 | 0.1942 | 3.0900 |
| IABC [20] | 605.4258 | 0.2209 | 2.3197 | 646.0455 | 0.1942 | 3.4815 |
| IABC-LS [20] | 605.4258 | 0.2210 | 2.3200 | 646.0455 | 0.1942 | 3.4815 |
| IABCDP [20] | 605.4258 | 0.2210 | 2.3191 | 646.0455 | 0.1942 | 3.4815 |
| IABCDP-LS [20] | 605.4259 | 0.2210 | 2.3200 | 646.0455 | 0.1942 | 3.4815 |
| DBC | 605.3456 | 0.2207 | 2.2617 | 645.8250 | 0.1942 | 3.3949 |

4.2 Test system 2: forty-unit system.

In order to investigate the importance of the proposed approach, the algorithm is tested on a large test system. This test system consists of forty units with non-smooth fuel cost and emission level function. The DBC parameters related to this test system are shown in Table 4. The fuel cost and emission rate coefficients of the system are shown

in Table 6, transmission loss has not been considered. Total load demand of the system is 10500 (MW). In the first case, the best cost achieved is 121417.00(\$/h), the corresponding emission is 356480.00 (ton/h), while during the emission optimization stage, the best emission achieved is 176682.90 (ton/h), the corresponding fuel cost increased to 130000.00 (\$/h). Figure 9 shows the convergence characteristic of the total cost minimization. The best results of the proposed approach for two cases (fuel cost and emission) compared with other methods are illustrated in Table 5 shows clearly the efficiency of the proposed approach.

Table 4. Parameters of the DBC.

| Parameters | <i>N</i> | <i>m</i> | <i>e</i> | <i>Nem</i> | <i>Nes</i> | <i>Ngs</i> | <i>step</i> |
|------------|----------|----------|----------|------------|------------|------------|-------------|
| Value | 160 | 20 | 5 | 60 | 40 | 60 | 30 |

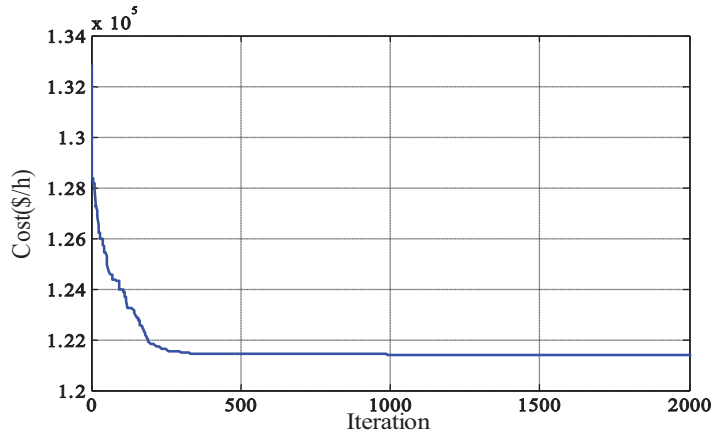


Fig.9. Convergence characteristic for 40 unit system: cost minimization

Table 5. Generation (MW), cost(\$/h), emission(ton/h), for 40-unit system: Pd =10500MW

| Generation | $\omega=1.0$ | | | $\omega=0.0$ | | |
|------------|--------------|-----------|------------|--------------|----------|----------|
| | DBC | DE[25] | HMAPSO[26] | DBC | DE[25] | MBFA[23] |
| G1 | 111.1591 | 110.9515 | 111.136 | 114.0000 | 114.0000 | 114.0000 |
| G2 | 112.2120 | 113.2997 | 111.135 | 114.0000 | 114.0000 | 114.0000 |
| G3 | 97.4007 | 98.6155 | 120.0000 | 119.9997 | 120.0000 | 120.0000 |
| G4 | 179.7341 | 184.1487 | 177.221 | 169.3422 | 169.2933 | 169.3671 |
| G5 | 88.3434 | 86.4013 | 88.699 | 97.0000 | 97.0000 | 97.0000 |
| G6 | 139.9997 | 140.0000 | 140.000 | 124.0863 | 124.2828 | 124.2630 |
| G7 | 259.5996 | 300.0000 | 260.157 | 299.8078 | 299.4564 | 299.6931 |
| G8 | 284.8900 | 285.4556 | 284.723 | 298.0407 | 297.8554 | 297.9093 |
| G9 | 284.6025 | 297.5110 | 285.523 | 297.3179 | 297.1332 | 297.2578 |
| G10 | 130.0016 | 130.0000 | 130.000 | 130.0030 | 130.0000 | 130.0007 |
| G11 | 168.8000 | 168.7482 | 168.805 | 298.2186 | 298.5980 | 298.4210 |
| G12 | 168.8006 | 95.6950 | 168.689 | 297.9521 | 297.7226 | 298.0264 |
| G13 | 214.7599 | 125.0000 | 304.123 | 433.6722 | 433.7471 | 433.5590 |
| G14 | 394.2794 | 394.3545 | 304.678 | 421.6718 | 421.9529 | 421.7360 |
| G15 | 304.5198 | 305.5234 | 304.317 | 422.4145 | 422.6280 | 422.7884 |
| G16 | 394.2792 | 394.71147 | 304.317 | 423.0113 | 422.9508 | 422.7841 |
| G17 | 489.2796 | 489.7972 | 489.187 | 439.3258 | 439.2581 | 439.4078 |
| G18 | 489.2796 | 489.3620 | 489.455 | 439.3993 | 439.4411 | 439.4132 |
| G19 | 511.2797 | 520.9024 | 512.097 | 439.1740 | 439.4908 | 439.4111 |
| G20 | 511.2805 | 510.6407 | 511.349 | 439.2771 | 439.6189 | 439.4155 |
| G21 | 523.2805 | 524.5336 | 523.247 | 439.6522 | 439.2250 | 439.4421 |
| G22 | 523.2814 | 526.6981 | 523.515 | 439.3394 | 439.6821 | 439.4587 |
| G23 | 523.2857 | 530.7467 | 523.454 | 439.8210 | 439.8757 | 439.7822 |
| G24 | 523.2798 | 526.3270 | 523.453 | 439.6367 | 439.8937 | 439.7697 |
| G25 | 523.2800 | 525.6537 | 523.492 | 440.1316 | 440.4401 | 440.1191 |
| G26 | 523.2803 | 522.9497 | 523.307 | 440.4029 | 439.8408 | 440.1219 |
| G27 | 10.0027 | 10.0000 | 10.000 | 29.0831 | 28.7758 | 28.9738 |
| G28 | 10.0008 | 11.5222 | 10.000 | 29.0527 | 29.0747 | 29.0007 |

| | | | | | | |
|------------|------------------|-----------|-----------|------------------|-----------|-----------|
| G29 | 10.0003 | 10.0000 | 10.000 | 29.0411 | 28.9047 | 28.9828 |
| G30 | 88.4221 | 89.9076 | 88.691 | 97.0000 | 97.0000 | 97.0000 |
| G31 | 189.9998 | 190.0000 | 190.000 | 172.3484 | 172.4036 | 172.3348 |
| G32 | 189.9997 | 190.0000 | 190.000 | 172.2801 | 172.3956 | 172.3327 |
| G33 | 189.9997 | 190.0000 | 190.000 | 172.4102 | 172.3144 | 172.3262 |
| G34 | 165.1811 | 198.8403 | 164.218 | 200.0000 | 200.0000 | 200.0000 |
| G35 | 165.7524 | 174.1783 | 200.000 | 200.0000 | 200.0000 | 200.0000 |
| G36 | 165.1722 | 197.1598 | 200.000 | 200.0000 | 200.0000 | 200.0000 |
| G37 | 109.9999 | 110.0000 | 110.000 | 100.8796 | 100.8765 | 100.8441 |
| G38 | 109.9998 | 109.3565 | 110.000 | 100.8725 | 100.9000 | 100.8346 |
| G39 | 109.9996 | 110.0000 | 110.000 | 100.8785 | 100.7784 | 100.8362 |
| G40 | 511.2810 | 510.9752 | 511.009 | 439.4557 | 439.1894 | 439.3868 |
| Cost(\$/h) | 121417,00 | 121800.00 | 121586.90 | 130000,00 | 125730.00 | 129995.00 |
| Emi(ton/h) | 356480,00 | 374790.00 | NR | 176682.90 | 176680.00 | 176682.26 |

NR means not reported in the referred literature.

5 Conclusion

In this paper, a flexible and efficient variant-based bee colony named dance bee colony with dynamic step size adjustment has been successfully adapted and applied for solving multi objective economic emission dispatch considering valve point effect and total transmission losses. The robustness of the proposed approach has been tested and validated on two standard test systems, IEEE 30-Bus considering power losses and to the large test system with 40 units considering valve point effect. It is observed that the proposed variant is capable of enhancing the solution of the combined economic emission dispatch considering practical generator constraints.

6 Appendix:

Table 6. six-unit generator characteristics [20]

| Unit | a_i | b_i | c_i | d_i | e_i | γ_i | β_i | α_i | η_i | δ_i | P_{min} | P_{max} |
|------|-------|-------|-------|-------|-------|------------|-----------|------------|----------|------------|-----------|-----------|
| 1 | 10 | 200 | 100 | - | - | 0.04091 | -0.05554 | 0.0649 | 0.000200 | 2.857 | 5 | 10 |
| 2 | 10 | 150 | 120 | - | - | 0.02543 | -0.06047 | 0.05638 | 0.000500 | 3.333 | 5 | 150 |
| 3 | 20 | 180 | 40 | - | - | 0.04258 | -0.05094 | 0.04586 | 0.000001 | 8.000 | 5 | 150 |
| 4 | 10 | 100 | 60 | - | - | 0.05326 | -0.03550 | 0.03380 | 0.002000 | 2.000 | 5 | 150 |
| 5 | 20 | 180 | 40 | - | - | 0.04258 | -0.05094 | 0.04586 | 0.000001 | 8.000 | 5 | 150 |
| 6 | 10 | 150 | 100 | - | - | 0.06131 | -0.05555 | 0.05151 | 0.000010 | 6.667 | 5 | 150 |

Table 7.40-unit generator characteristics [8].

| Unit | a_i | b_i | c_i | d_i | e_i | γ_i | β_i | α_i | η_i | δ_i | P_{min} | P_{max} |
|------|----------|-------|---------|-------|-------|------------|-----------|------------|----------|------------|-----------|-----------|
| 1 | 94.705 | 6.73 | 0.00690 | 100 | 0.084 | 0.0480 | 2.22 | 60 | 1.3100 | 0.05690 | 36 | 114 |
| 2 | 94.705 | 6.73 | 0.00690 | 100 | 0.084 | 0.0480 | 2.22 | 60 | 1.3100 | 0.05690 | 36 | 114 |
| 3 | 309.540 | 7.07 | 0.02028 | 100 | 0.084 | 0.0762 | 2.36 | 100 | 1.3100 | 0.05690 | 60 | 120 |
| 4 | 369.030 | 8.18 | 0.00942 | 150 | 0.063 | 0.0540 | 3.14 | 120 | 0.9142 | 0.04540 | 80 | 190 |
| 5 | 148.890 | 5.35 | 0.01140 | 120 | 0.077 | 0.0850 | 1.89 | 50 | 0.9936 | 0.04060 | 47 | 97 |
| 6 | 222.330 | 8.05 | 0.01142 | 100 | 0.084 | 0.0854 | 3.08 | 80 | 1.3100 | 0.05690 | 68 | 140 |
| 7 | 287.710 | 8.03 | 0.00357 | 200 | 0.042 | 0.0242 | 3.06 | 100 | 0.6550 | 0.02846 | 110 | 300 |
| 8 | 391.980 | 6.99 | 0.00492 | 200 | 0.042 | 0.0310 | 2.32 | 130 | 0.6550 | 0.02846 | 135 | 300 |
| 9 | 455.760 | 6.60 | 0.00573 | 200 | 0.042 | 0.0335 | 2.11 | 150 | 0.6550 | 0.02846 | 135 | 300 |
| 10 | 722.820 | 12.90 | 0.00605 | 200 | 0.042 | 0.4250 | 4.34 | 280 | 0.6550 | 0.02846 | 130 | 300 |
| 11 | 635.200 | 12.90 | 0.00515 | 200 | 0.042 | 0.0322 | 4.34 | 220 | 0.6550 | 0.02846 | 94 | 375 |
| 12 | 654.690 | 12.80 | 0.00569 | 200 | 0.042 | 0.0338 | 4.28 | 225 | 0.6550 | 0.02846 | 94 | 375 |
| 13 | 913.400 | 12.50 | 0.00421 | 300 | 0.035 | 0.0296 | 4.18 | 300 | 0.5035 | 0.02075 | 125 | 500 |
| 14 | 1760.400 | 8.84 | 0.00752 | 300 | 0.035 | 0.0512 | 3.34 | 520 | 0.5035 | 0.02075 | 125 | 500 |
| 15 | 1728.300 | 9.15 | 0.00708 | 300 | 0.035 | 0.0496 | 3.55 | 510 | 0.5035 | 0.02075 | 125 | 500 |
| 16 | 1728.300 | 9.15 | 0.00708 | 300 | 0.035 | 0.0496 | 3.55 | 510 | 0.5035 | 0.02075 | 125 | 500 |
| 17 | 647.850 | 7.97 | 0.00313 | 300 | 0.035 | 0.0151 | 2.68 | 220 | 0.5035 | 0.02075 | 220 | 500 |
| 18 | 649.690 | 7.95 | 0.00313 | 300 | 0.035 | 0.0151 | 2.66 | 222 | 0.5035 | 0.02075 | 220 | 500 |
| 19 | 647.830 | 7.97 | 0.00313 | 300 | 0.035 | 0.0151 | 2.68 | 220 | 0.5035 | 0.02075 | 242 | 550 |
| 20 | 647.810 | 7.97 | 0.00313 | 300 | 0.035 | 0.0151 | 2.68 | 220 | 0.5035 | 0.02075 | 242 | 550 |
| 21 | 785.960 | 6.63 | 0.00298 | 300 | 0.035 | 0.0145 | 2.22 | 290 | 0.5035 | 0.02075 | 254 | 550 |
| 22 | 785.960 | 6.63 | 0.00298 | 300 | 0.035 | 0.0145 | 2.22 | 285 | 0.5035 | 0.02075 | 254 | 550 |
| 23 | 794.530 | 6.66 | 0.00284 | 300 | 0.035 | 0.0138 | 2.26 | 295 | 0.5035 | 0.02075 | 254 | 550 |
| 24 | 794.530 | 6.66 | 0.00284 | 300 | 0.035 | 0.0138 | 2.26 | 295 | 0.5035 | 0.02075 | 254 | 550 |
| 25 | 801.320 | 7.10 | 0.00277 | 300 | 0.035 | 0.0132 | 2.42 | 310 | 0.5035 | 0.02075 | 254 | 550 |

| | | | | | | | | | | | | |
|----|----------|------|---------|-----|-------|--------|------|-----|--------|---------|-----|-----|
| 26 | 801.320 | 7.10 | 0.00277 | 300 | 0.035 | 0.0132 | 2.42 | 310 | 0.5035 | 0.02075 | 254 | 550 |
| 27 | 1055.100 | 3.33 | 0.52124 | 120 | 0.077 | 1.8420 | 1.11 | 360 | 0.9936 | 0.04060 | 10 | 150 |
| 28 | 1055.100 | 3.33 | 0.52124 | 120 | 0.077 | 1.8420 | 1.11 | 360 | 0.9936 | 0.04060 | 10 | 150 |
| 29 | 1055.100 | 3.33 | 0.52124 | 120 | 0.077 | 1.8420 | 1.11 | 360 | 0.9936 | 0.04060 | 10 | 150 |
| 30 | 148.890 | 5.35 | 0.01140 | 120 | 0.077 | 0.0850 | 1.89 | 50 | 0.9936 | 0.04060 | 47 | 97 |
| 31 | 222.920 | 6.43 | 0.00160 | 150 | 0.063 | 0.0121 | 2.08 | 80 | 0.9142 | 0.04540 | 60 | 190 |
| 32 | 222.920 | 6.43 | 0.00160 | 150 | 0.063 | 0.0121 | 2.08 | 80 | 0.9142 | 0.04540 | 60 | 190 |
| 33 | 222.920 | 6.43 | 0.00160 | 150 | 0.063 | 0.0121 | 2.08 | 80 | 0.9142 | 0.04540 | 60 | 190 |
| 34 | 107.870 | 8.95 | 0.00010 | 200 | 0.042 | 0.0012 | 3.48 | 65 | 0.6550 | 0.02846 | 90 | 200 |
| 35 | 116.580 | 8.62 | 0.00010 | 200 | 0.042 | 0.0012 | 3.24 | 70 | 0.6550 | 0.02846 | 90 | 200 |
| 36 | 116.580 | 8.62 | 0.00010 | 200 | 0.042 | 0.0012 | 3.24 | 70 | 0.6550 | 0.02846 | 90 | 200 |
| 37 | 307.450 | 5.88 | 0.01610 | 80 | 0.098 | 0.0950 | 1.98 | 100 | 1.4200 | 0.06770 | 25 | 110 |
| 38 | 307.450 | 5.88 | 0.01610 | 80 | 0.098 | 0.0950 | 1.98 | 100 | 1.4200 | 0.06770 | 25 | 110 |
| 39 | 307.450 | 5.88 | 0.01610 | 80 | 0.098 | 0.0950 | 1.98 | 100 | 1.4200 | 0.06770 | 25 | 110 |
| 40 | 647.830 | 7.97 | 0.00313 | 300 | 0.035 | 0.0151 | 2.68 | 220 | 0.5035 | 0.02075 | 242 | 550 |

Table 8 .B coefficients matrix [20]

$$[B_{00}] = 0.00098573$$

$$[B_0] = 10^{-2} \times [-1.07 \quad 0.60 \quad -0.17 \quad 0.09 \quad 0.02 \quad 0.30]$$

$$[B] = 10^{-2} \times \begin{bmatrix} 13.82 & -2.99 & 0.44 & -0.22 & -0.10 & -0.08 \\ -2.99 & 4.87 & -0.25 & 0.04 & 0.16 & 0.41 \\ 0.44 & -0.25 & 1.82 & -0.70 & -0.66 & -0.66 \\ -0.22 & 0.04 & -0.70 & 1.37 & 0.50 & 0.33 \\ -0.10 & 0.16 & -0.66 & 0.50 & 1.09 & 0.05 \\ -0.08 & 0.41 & -0.66 & 0.33 & 0.05 & 2.44 \end{bmatrix}$$

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