Physics Letters B 701 (2011) 591-596

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Physics Letters B

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# Testing Higgs portal dark matter via Z fusion at a linear collider

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### ARTICLE INFO

Article history: Received 25 February 2011 Received in revised form 3 May 2011 Accepted 15 June 2011 Available online 23 June 2011 Editor: T. Yanagida

*Keywords:* Dark matter Collider physics

# ABSTRACT

We investigate the possibility of detecting dark matter at TeV scale linear colliders in the scenario where the dark matter is a massive particle weakly interacting only with the Higgs boson h in the low energy effective theory (the Higgs portal dark matter scenario). The dark matter in this scenario would be difficult to be tested at the CERN Large Hadron Collider when the decay of the Higgs boson into a dark matter pair is kinematically forbidden. We study whether even in such a case the dark matter D can be explored or not via the Z boson fusion process at the International Linear Collider and also at a multi-TeV lepton collider. It is found that for the collision energy  $\sqrt{s} > 1$  TeV with the integrated luminosity 1 ab<sup>-1</sup>, the signal ( $e^{\pm}e^{-} \rightarrow e^{\pm}e^{-}h^* \rightarrow e^{\pm}e^{-}DD$ ) can be seen after appropriate kinematical cuts. In particular, when the dark matter is a fermion, which is supposed to be singlet under the standard gauge symmetries, the signal with the mass up to about 100 GeV can be tested for the Higgs boson mass to be 120 GeV.

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# 1. Introduction

Dark matter is one of the biggest mysteries in present physics and astronomy. It has been established that more than one fifth of the energy density in our Universe is occupied by dark matter [1]. If the essence of the dark matter is a kind of particle, it must be electrically neutral and must be weakly interacting. As it has turned out that neutrinos cannot be the candidate, the dark matter should necessarily be a new massive content in physics beyond the Standard Model (SM). A plausible candidate for the dark matter is therefore a weakly interacting massive particle (WIMP). According to the WMAP experiment [1], the mass of the WIMP dark matter is at the TeV scale or less. Various direct and indirect dark matter search experiments are currently being performed [2–6] and planned [7–9]. Moreover, we may be able to directly produce the dark matter and to test it at collider experiments such as the CERN Large Hadron Collider (LHC) and future linear colliders.

The fact that the mass scale of the WIMP dark matter is similar to that of the electroweak symmetry breaking would indicate that there is a connection between the Higgs boson and the dark matter. There are many new physics models involving a dark matter candidate. In some of them, it can happen that the dark matter couples only to the Higgs boson in the low energy effective

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theory, where stability of the dark matter is guaranteed by an unbroken discrete symmetry [10–15]. Such a scenario is often called the Higgs portal dark matter scenario [13].

In the scenario of the Higgs portal dark matter, a collider signal at the LHC is expected to come from the *W* boson fusion process  $pp \rightarrow jjW^*W^* \rightarrow jjh^* \rightarrow jjDD$ , where *D* represents the Higgs portal dark matter whose spin is either 0, 1/2, or 1 [16], while *j* is a jet originating in an energetic quark. When the mass of *D* is less than one half of that of *h*, the invisible decay process  $h \rightarrow DD$  opens, so that the signal would be detectable after appropriate kinematic cuts [17] unless the coupling constant between *h* and *D* is too small. On the other hand, if the decay  $h \rightarrow DD$  is not kinematically allowed, the detection of the signal would be hopeless for the dark matter which is consistent with the WMAP and direct detection experiments [16].

In this Letter, we investigate the possibility whether the Higgs portal dark matter can be tested at TeV scale linear colliders such as the International Linear Collider (ILC) [18] and the Compact Linear Collider (CLIC) [19] even in the case where the decay  $h \rightarrow DD$  is not kinematically allowed. In the case of  $m_D < m_h/2$ , the process  $e^+e^- \rightarrow Zh^* \rightarrow ZDD$  has been studied for the collision with the center of mass energy of  $\sqrt{s} = 350$  GeV [20]. We here study pair production processes of the dark matter via *Z* boson fusion from electron–positron  $(e^+e^-)$  and electron–electron  $(e^-e^-)$  collisions. It is found that for the collision energy  $\sqrt{s} > 1$  TeV with the integrated luminosity 1 ab<sup>-1</sup>, the signal  $(e^\pm e^- \rightarrow e^\pm e^-h^* \rightarrow e^\pm e^-DD)$  could be seen even for  $m_D > m_h/2$  after appropriate kinematical cuts, when the mass of *D* is not much heavier than that of the *W* boson, especially for the dark matter *D* being a fermion.

# 2. The model

We here consider the simple model in which a dark matter field is added to the SM. We impose an unbroken  $Z_2$  parity, under which the dark matter is assigned to be odd while the SM particles are to be even. Stability of the dark matter is guaranteed by the  $Z_2$  parity. We consider three possibilities for the spin of the dark matter; i.e., the real scalar  $\phi$ , the Majorana fermion  $\chi$  and the real massive vector  $V_{\mu}$ .

The Lagrangian for each case of the dark matter is given by

$$\mathcal{L}_{S} = \mathcal{L}_{SM} + \frac{1}{2} (\partial \phi)^{2} - \frac{1}{2} M_{S}^{2} \phi^{2} - \frac{c_{S}}{2} |H|^{2} \phi^{2} - \frac{d_{S}}{4!} \phi^{4}, \qquad (1)$$

$$\mathcal{L}_{F} = \mathcal{L}_{SM} + \frac{1}{2} \bar{\chi} (i\partial - M_{F}) \chi - \frac{c_{F}}{2\Lambda} |H|^{2} \bar{\chi} \chi$$

$$- \frac{d_{F}}{2\Lambda} \bar{\chi} \sigma^{\mu\nu} \chi B_{\mu\nu}, \qquad (2)$$

$$\mathcal{L}_{\rm V} = \mathcal{L}_{\rm SM} - \frac{1}{4} V^{\mu\nu} V_{\mu\nu} + \frac{1}{2} M_{\rm V}^2 V_{\mu} V^{\mu} + \frac{c_{\rm V}}{2} |H|^2 V_{\mu} V^{\mu} - \frac{d_{\rm V}}{4!} (V_{\mu} V^{\mu})^2, \qquad (3)$$

where  $M_i$  (*i* = S, F and V) are the bare masses of  $\phi$ ,  $\chi$  and  $V_{\mu}$ ,  $c_i$ and  $d_i$  are dimensionless coupling constants,  $\Lambda$  is a dimensionful parameter, and  $V_{\mu\nu}$  and  $B_{\mu\nu}$  are Abelian field strength tensors. The last term in Eq. (2) is expected to be small because this is induced at the one loop level. Hence, we neglect this term in the following analysis. In this case, the dark matter in Eqs. (1)–(3) only couples to the SM particles via the Higgs doublet field H: i.e., it is so-called the Higgs portal dark matter.

After the electroweak symmetry breaking, the Higgs field H obtains the vacuum expectation value  $\langle H \rangle = (0, v)^T / \sqrt{2}$  with the value of v being 246 GeV, and the physical mass of each dark matter particle is therefore given by

$$m_{\phi}^2 = M_{\rm S}^2 + \frac{c_{\rm S} v^2}{2},\tag{4}$$

$$m_{\chi} = M_{\rm F} + \frac{c_{\rm F} v^2}{2\Lambda},\tag{5}$$

$$m_V^2 = M_V^2 + \frac{c_V v^2}{2}.$$
 (6)

In our analysis, physical masses  $m_i$  and coupling constants  $c_i$  are treated as free parameters. Theoretical constraints and experimental bounds from the WMAP data and the direct search results on these models are discussed in Ref. [16].

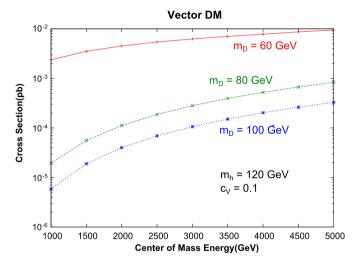
## 3. Dark matter signals at the $e^+e^-$ collider

We consider the possibility to detect the dark matter at next generation of electron-positron linear colliders such as the ILC and the CLIC. In particular, we are interested in the case of  $m_h < 2m_D$ , where the Higgs boson cannot decay into a pair of dark matters. We concentrate on the Z boson fusion process  $e^+e^- \rightarrow$  $e^+e^-Z^*Z^* \rightarrow e^+e^-h^* \rightarrow e^+e^-DD$  depicted in Fig. 1. This process can, in principle, be used to detect the dark matter by measuring the outgoing electron and positron in the final state and by using the energy momentum conservation.

We impose the polarization for both incident electron and positron beams [18]:

$$\frac{N_{e_{R}^{-}} - N_{e_{L}^{-}}}{N_{e_{R}^{-}} + N_{e_{L}^{-}}} = 80\%, \qquad \frac{N_{e_{R}^{+}} - N_{e_{L}^{+}}}{N_{e_{R}^{+}} + N_{e_{L}^{+}}} = 50\%, \tag{7}$$

Fig. 1. Feynman diagram of the signal process.



**Fig. 2.** Cross section of the signal process  $e^+e^- \rightarrow e^+e^-V_{\mu}V^{\mu}$  as a function of the center of mass energy  $\sqrt{s}$ . The mass of the dark matter  $V_{\mu}$  is fixed to be 60, 80 and 100 GeV, while the coupling constant  $c_V$  is taken to be 0.1.

Table 1

Number of events before and after each kinematical cut for the integrated luminosity 1  $ab^{-1}$ . We take  $c_S = c_V = 1$  and  $c_F / A = 0.1$  GeV<sup>-1</sup> and  $m_D = 80$  GeV.

$\sqrt{s} = 1$ TeV	Basic	E <sub>inv</sub>	M <sub>ee</sub>	$\phi_{ee}$	$\sqrt{s} = 5 \text{ TeV}$	Basic	E <sub>inv</sub>	M <sub>ee</sub>	$\phi_{ee}$
$e^+e^-\phi\phi$	91	77	64	43	$e^+e^-\phi\phi$	348	342	232	162
$e^+e^-\nu_e\bar{\nu}_e$	115 000	24600	2510	791	$e^+e^-\nu_e\bar{\nu}_e$	148 000	5150	376	138
$e^+e^-\nu_\mu\bar{\nu}_\mu$	887	103	61	31	$e^+e^-\nu_\mu\bar{\nu}_\mu$	374	191	53	31
$e^+e^-\nu_{\tau}\bar{\nu}_{\tau}$	887	103	61	31	$e^+e^-v_{ au}\bar{v}_{ au}$	374	191	53	31
$\sqrt{s} = 1$ TeV	Basic	E <sub>inv</sub>	M <sub>ee</sub>	$\phi_{ee}$	$\sqrt{s} = 5$ TeV	Basic	E <sub>inv</sub>	M <sub>ee</sub>	$\phi_{ee}$
$e^+e^-\chi\bar{\chi}$	47 800	29200	23 300	15300	$e^+e^-\chi \bar{\chi}$	387 000	361 000	235 000	167 000
$e^+e^-\nu_e\bar{\nu}_e$	115 000	24 600	2510	791	$e^+e^-\nu_e\bar{\nu}_e$	148 000	5150	701	264
$e^+e^-\nu_\mu\bar{\nu}_\mu$	887	103	61	31	$e^+e^-\nu_\mu\bar{\nu}_\mu$	374	191	80	45
$e^+e^-\nu_{\tau}\bar{\nu}_{\tau}$	887	103	61	31	$e^+e^-v_{ au}\bar{v}_{ au}$	374	191	80	45
$\sqrt{s} = 1$ TeV	Basic	E <sub>inv</sub>	M <sub>ee</sub>	$\phi_{ee}$	$\sqrt{s} = 5$ TeV	Basic	Einv	Mee	$\phi_{ee}$
$e^+e^-V_\mu V^\mu$	1830	818	649	427	$e^+e^-V_\mu V^\mu$	75 500	48 400	43 500	31 500
$e^+e^-\nu_e\bar{\nu}_e$	115 000	24 600	2510	791	$e^+e^-\nu_e\bar{\nu}_e$	148 000	5150	2190	820
$e^+e^-\nu_\mu\bar{\nu}_\mu$	887	103	61	31	$e^+e^-\nu_\mu\bar{\nu}_\mu$	374	191	147	79
$e^+e^-\nu_{\tau}\bar{\nu}_{\tau}$	887	103	61	31	$e^+e^-\nu_{\tau}\bar{\nu}_{\tau}$	374	191	147	79

where  $N_{e_{R,L}^-}$  and  $N_{e_{R,L}^+}$  are numbers of right (left) handed electron and positron in the beam flux per unit time. By using the polarized beams, the backgrounds which are mediated by the *W* boson can be reduced. The backgrounds mediated by the *Z* boson are reduced by the basic cut in Eq. (9) as we will see soon.

The cross section of the signal process is the larger as the collision energy  $\sqrt{s}$  increases, and its behavior is  $\ln s$  as can be seen in Fig. 2, so that the higher collision energy may be more useful to detect the signal. However, for  $\sqrt{s} = 1-5$  TeV, the outgoing electron and positron tend to be emitted to forward and backward directions, and the detectability of the leptons near the beam line is therefore essentially important. In this Letter, we assume the detectable area as [21]

$$|\cos\theta| < 0.9999416,$$
 (8)

where  $\theta$  is the scattering angle. Assuming the situation that the Higgs boson mass is already known, we impose the condition for the missing invariant mass  $M_{inv}$  as

$$M_{\rm inv} > m_h, \tag{9}$$

in order to discuss the detection of the dark matter in the case  $m_D > m_h/2$ . The production cross sections of the signal process for  $D = \phi$ ,  $\chi$  and V at the center of mass energy 1 TeV and 5 TeV are shown for  $m_h = 120$  GeV in Table 1.

#### 4. Parton level signal and background

Backgrounds against the signal process are all the process with the final state of  $e^+e^-$  with a missing momentum. The main background processes are those with the final state  $e^+e^-\nu_e\bar{\nu}_e$ ,  $e^+e^-\nu_\mu\bar{\nu}_\mu$  and  $e^+e^-\nu_\tau\bar{\nu}_\tau$ . After the basic cuts given in Eqs. (8) and (9), the cross sections for  $e^+e^- \rightarrow e^+e^-\nu_e\bar{\nu}_e$  and  $e^+e^- \rightarrow$  $e^+e^-\nu_i\bar{\nu}_i$  ( $i = \mu$  or  $\tau$ ) are evaluated as  $1.15 \times 10^{-1}$  pb and  $8.87 \times 10^{-4}$  pb at  $\sqrt{s} = 1$  TeV, while they are  $1.48 \times 10^{-1}$  pb and  $3.74 \times 10^{-4}$  pb at  $\sqrt{s} = 5$  TeV, respectively: see Table 1. The signal to background ratio amounts to  $10^{-3}$ – $10^{-1}$  for the coupling constants being taken as  $c_S = c_V = 1$  and  $c_F/\Lambda = 0.1$  GeV<sup>-1</sup>.<sup>1</sup> In order to gain the signal significance we impose kinematical cuts as follows.

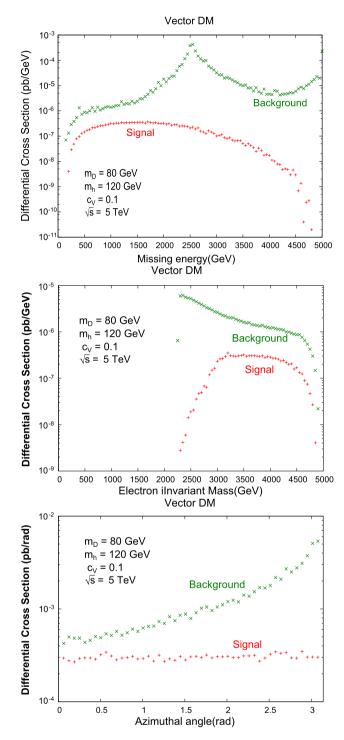
First, as seen in the upper panel of Fig. 3, the signal events tend to be located with lower values of the missing energy  $E_{inv}$ , while the backgrounds are distributed with larger values. We therefore impose the cut on  $E_{inv}$  as

$$E_{\rm inv} < 0.4\sqrt{\rm s} \, {\rm GeV}. \tag{10}$$

By using this cut, the backgrounds from  $e^+e^-\nu_e \bar{\nu}_e$  can be reduced. Second, as seen in the middle panel of Fig. 3, the invariant mass distributions for outgoing electron and positron are clearly different between the signal and the backgrounds. We therefore impose the kinematical cuts to the invariant mass  $M_{ee}$  depending on the spin of the dark matter for  $\sqrt{s} = 1$  TeV and 5 TeV as

$$\begin{split} M_{ee}^{S1} &> 600 \text{ GeV}, \qquad M_{ee}^{F1} > 600 \text{ GeV}, \\ M_{ee}^{V1} &> 600 \text{ GeV}, \qquad M_{ee}^{S5} > 4200 \text{ GeV}, \\ M_{ee}^{F5} &> 3900 \text{ GeV}, \qquad M_{ee}^{V5} > 3000 \text{ GeV}. \end{split}$$

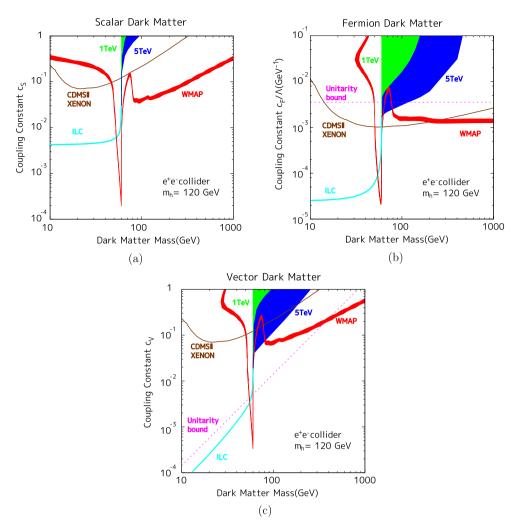
Finally, the distributions of the azimuthal angle  $\phi_{ee}$  between outgoing electron and positron are shown for the signal and the



**Fig. 3.** Distributions of the missing energy  $E_{inv}$  (upper panel), the invariant mass  $M_{ee}$  (middle panel), and the azimuthal angle  $\phi_{ee}$  between outgoing electron and positron (lower panel) for the signal and the backgrounds events. The center of mass energy is fixed to be  $\sqrt{s} = 5$  TeV. The signal (red) is for the vector dark matter with the mass of 80 GeV, while the backgrounds (green) with the final state of  $e^+e^-\nu_e\bar{\nu}_e + e^+e^-\nu_{\pi}\bar{\nu}_{\pi}$  are shown. The coupling constant  $c_V$  is taken to be 0.1. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

background processes in the lower panel of Fig. 3. As can be seen in the figure, the signal is insensitive to the azimuthal angle, while most of the background events are located in the region with relatively large values of the azimuthal angle. We therefore impose the cut on  $\phi_{ee}$  as

<sup>&</sup>lt;sup>1</sup> The cutoff scale  $\Lambda$  should be taken to be higher than  $\sqrt{s}$  in the effective theory. The values for these coupling constants discussed here may be too large to satisfy the unitarity bound in Ref. [16]. For more realistic values, the results presented in Table 1 can be used by rescaling appropriately.



**Fig. 4.** The areas of  $N_S/\sqrt{N_S + N_B} > 5$  at the  $e^+e^-$  collider for  $\sqrt{s} = 1$  TeV (green) and 5 TeV (blue) with 1 ab<sup>-1</sup> data are shown with assuming  $m_h = 120$  GeV. Parameter regions consistent with the WMAP data (red) and the 90% C.L. excluded regions by CDMS II and XENON experiments (brown) are also given. For  $m_D < m_h/2$ , the  $3\sigma$  line (cyan) with  $\sqrt{s} = 350$  GeV and the integrated luminosity 500 fb<sup>-1</sup> is shown. The upper bound on the coupling constants from the tree level unitarity with cutoff scale  $\Lambda = 5$  TeV is also indicated by the dotted (purple) curve. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

 $\phi_{ee} < 2.3 \text{ rad}, \tag{12}$ 

by which a considerable amount of the backgrounds can be eliminated.

In Table 1, the event numbers are shown for both the signal and the backgrounds after imposing the above kinematical cuts in Eqs. (10)–(12) in the models with the scalar, fermion, and vector dark matter. Coupling constants are fixed to be  $c_S = c_V = 1$  and  $c_F/\Lambda = 0.1 \text{ GeV}^{-1}$ . We here assume the center of mass energy  $\sqrt{s}$  to be 1 TeV and 5 TeV and the integrated luminosity to be 1 ab<sup>-1</sup>. The background from  $e^+e^-\nu_e\bar{\nu}_e$  process can be considerably reduced by these kinematical cuts. As a result, the significance to detect the signal, which is defined by

Significance = 
$$\frac{N_S}{\sqrt{N_S + N_B}}$$
, (13)

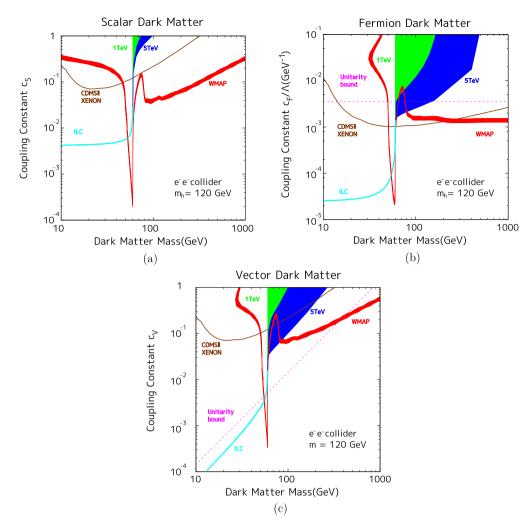
with  $N_S$  ( $N_B$ ) being the event number for signal (backgrounds), can be greater than one even if the Higgs boson cannot decay into a dark matter pair.

In Figs. 4(a)–(c), we show the regions where the significance is larger than five in the plane of the coupling constant and the dark matter mass at  $\sqrt{s} = 1$  TeV (green area) and 5 TeV (blue area) for  $m_D > m_h/2$ . The mass of the Higgs boson is set to be 120 GeV

and the integrated luminosity is assumed to be 1  $ab^{-1}$ . For the region  $m_D < m_h/2$ , where the Higgs boson can decay into a pair of dark matters, the  $3\sigma$  line at  $\sqrt{s} = 350$  GeV with the integrated luminosity 500 fb<sup>-1</sup> is shown by the cyan curve. In each figure, the allowed region which satisfies the WMAP data ( $3\sigma$ ) is indicated by the red area. We also show the excluded region (90% C.L.) from direct search results by CDMS II and XENON 100 by the brown curve.<sup>2</sup> The region below the dotted (purple) curve is allowed by the tree level unitarity with cutoff scale  $\Lambda = 5$  TeV discussed in Ref. [16].<sup>3</sup>

<sup>&</sup>lt;sup>2</sup> We are assuming that the scattering cross section is determined only by the diagram in which the Higgs boson is exchanged. Namely, it is not interfered by other diagrams. Furthermore, the detection rate at the direct search has some ambiguities from the hadron matrix element, the dark matter density in the Solar System, and the velocity distribution of the dark matter in our galaxy. Those curves should be therefore regarded as a reference.

<sup>&</sup>lt;sup>3</sup> The unitarity bound can be relaxed if we add higher dimensional operators (than those we have considered) to the effective Lagrangian equations (1)–(3), because these operators are possible to make the behavior of scattering amplitudes mild at high energy scale. This is exactly what happened in the Little Higgs model with T-parity, where a light vector dark matter ( $m \sim 100$  GeV) is predicted with the cutoff scale being O(10) TeV [22]. Importantly, even if we consider the higher dimensional operators, our conclusions about the ILC signals are not altered, because



**Fig. 5.** The areas of  $N_S/\sqrt{N_S + N_B} > 5$  at the  $e^-e^-$  collider for  $\sqrt{s} = 1$  TeV (green) and 5 TeV (blue) with the integrated luminosity of 1 ab<sup>-1</sup> are shown with assuming  $m_h = 120$  GeV. Other lines are the same as those in Fig. 4. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

First, in Fig. 4(a), the results for the scalar dark matter are shown. There is no overlap between the region of  $N_S/\sqrt{N_S + N_B} > 5$  and that satisfying the WMAP data even at  $\sqrt{s} = 5$  TeV. Second, in Fig. 4(b), the results for the fermion dark matter are shown. For the  $e^+e^-$  collision at  $\sqrt{s} = 1$  TeV, the area where  $N_S/\sqrt{N_S + N_B} > 5$  and the WMAP data are both satisfied is very limited, while the area becomes wider at  $\sqrt{s} = 5$  TeV. Finally, in Fig. 4(c), the results for the vector dark matter are shown. At  $\sqrt{s} = 1$  TeV,  $N_S/\sqrt{N_S + N_B} > 5$  and the WMAP data cannot be compatible, but a wide region of the overlap can be seen at the  $\sqrt{s} = 5$  TeV. In particular, for the  $m_h/2 < m_D < 100$  GeV, it can be seen that the vector dark matter with the coupling constant larger than  $2-4 \times 10^{-3}$  can be tested.

Finally, we discuss the  $e^-e^- \rightarrow e^-e^-Z^*Z^* \rightarrow e^-e^-h^* \rightarrow e^-e^-DD$  in electron–electron collisions. The results are very similar to those for the  $e^+e^-$  collision. In Fig. 5, we show the results for the  $e^-e^-$  collisions, in the model with the scalar, fermion and vector dark matter respectively. For each case, we have imposed the same kinematical cuts as the corresponding processes in the  $e^+e^-$  collision. The results in the figure for the  $e^-e^-$  collision are qualitatively very similar to those in Fig. 4 for the  $e^+e^-$  collision.

Because of electron–electron collisions, the polarization is more effective than the case of the electron–positron collision.

#### 5. Conclusions

We have investigated the possibility of detecting dark matter at TeV scale linear colliders in the Higgs portal dark matter scenario with the scalar, fermion or vector dark matter, via *Z* boson fusion processes at electron–positron and electron–electron collisions. We have found that a multi-TeV collider can be more useful to explore the dark matter in these models than the 1 TeV collider when the invisible decay of the Higgs boson into a pair of dark matters is kinematically forbidden.

We have discussed the signal significance purely by evaluating statistic errors. In order to finally judge the feasibility, clearly we have to take into account more factors which directly depend on properties of the collider and the detector. We stress that the results in this Letter gives a motivation to such a detector level simulation study.

We have mainly presented the results in the case of  $m_h = 120$  GeV. For heavier h, the significance becomes worse. When  $m_h = 150$  GeV, we have confirmed that there is no parameter regions to be tested even at the 5 TeV linear collider experiment.

Suppose that the Higgs boson is found to be 120 GeV at the LHC and that in future an excess will be found for the signal

the essential energy scale of the Z-boson fusion, namely, the energy wasted at the ZZh vertex, is a few hundred GeV at most.

of  $e^+e^-$  plus missing energy above the background at the 5 TeV linear collider. Our results tell us that such a signal would indicate the WIMP DM, which is a fermion and whose mass is 80 to 100 GeV. The interaction is also determined to a considerable extent. Therefore, we conclude that by measuring this process at the multi-TeV linear collider, we may be able to extract the measure property of the WIMP dark matter such as its mass, spin, and coupling constants.

## Acknowledgements

The work was supported, in part, by Grant-in-Aid for Science Research, Ministry of Education, Culture, Sports, Science and Technology, Japan (Nos. 19540277 and 22244031 for S.K., and 21740174 and 22244021 for S.M.), and by World Premier International Research Center Initiative (WPI Initiative), MEXT, Japan.

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