# Stepwise Multiple Regression Method to Forecast Fish Landing 

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#### Abstract

There are six types of linear regression analyses that available in statistics which are simple linear regression, multiple linear regressions, logistic regression, ordinal regression, multinominal regression and descriminant analysis. Multiple linear regressions are the one of linear regression analyses that used to analyze the relationship between single response variable (dependent variable) with two or more controlled variables (independent variables). In this paper, stepwise multiple regression will use because this method is combination of forward selection and backward elimination method. The main objective in this paper is to select the suitable controlled variables in forecast fish landing. Data that has been used in this research were taken from Fisheries Annually Statistics of Department of Fisheries Malaysia. Then, the data will be analyzed by using Minitab 15 and SPSS 17.0. © 2010 Published by Elsevier Ltd. Open access under CC BY-NC-ND license.


Keywords: Forecast; Fish landing; Regression analyses; Stepwise multiple regression

## 1. Introduction

A statistics analysis is widely used in all aspects such as in science, medicine, fisheries (Ofuoku et al., 2007) and also in social sciences (Sarker et al., 2006). There are many methods in statistics and one of them is regression. There are six types of linear regression analyses which are simple linear regression, multiple linear regression, logistic regression, ordinal regression, multinominal regression and desriminant analysis. Multiple linear regression was selected to build a model of fish landing. Some method that categorized in the stepwise-type procedures which is stepwise regression also used in this paper. The main objective in this paper is to select the suitable controlled variables in forecast fish landing.

## 2. Literature review

Wan Nawang et al. (2009) have conducted a research to identify factor of youth's interest to become fishermen. There are two methods that use in their research which are factor analysis and multiple linear regression. According to the MLR that was used in their research, it shows that there are three factors that influence the respondence interest in fishermen career which are training programme, profitable and marketing. MLR also used by Ofuolu et $a l .(2007)$ in their research to determine of adoption of improved fish production technologies among fish farmers in

[^0]Delta States, Nigeria. Level of education, farm size, farm income and extension contact show positively correlation while age and household size shows negatively correlation between fish production technologies. MLR that applied in the research by Khamis et al. (2003) states that the higher of $\mathrm{R}^{2}$ gives good result on model fitting. Combination method of Pearson correlations, multiple and simple linear regression and ANOVA was used by Sain (2006) to see if there was change in measured habitat and fish metrics occurred in relation to increased urbanization. Sain (2006) used multiple and linear regression to explain the strongest relationship between fish and habitat.

## 3. Methodolgy

### 3.1 Data

In this paper, data were taken from Fisheries Statistics at official website of Department of Fisheries Malaysia, Ministry of Agriculture \& Agro-Based Industry Malaysia. The fisheries statistics include during 40 years which is from 1968 until 2007. This research is focusing on the marine fish landing in Terengganu.

### 3.2 Research method

Multiple linear regressions (MLR) are the method of statistics in regression that used to analyze the relationship between single response variable (dependent variable) with two or more controlled variables (independent variables). This method was selected for this research because there were more than controlled variables. In this research, response variable is marine fish landing $(Y)$ while fishermen $\left(X_{1}\right)$, fishing boat ( $X_{2}$ ) and fishing gears licensed ( $X_{3}$ ) were controlled variables.

There were four general steps to build forecasting model of fish landing in MLR. The general steps were checking assumptions, selecting suitable methods of MLR, interpret the output and develop equation of MLR.

## Step 1: Checking assumptions

The first step is to build forecasting model by checking assumptions of data. There are four assumptions that should be check which are normality, linearity, heteroscedasticity and multicollinearity. All of the variables in this paper must be normal distribution. The normal distribution can be seen via histogram graph, plot P-P, plot Q-Q, kurtosis and skewness. If the distribution of data is not normal, so we need to use transformation.

Then, MLR should have linear relationship between response variable and controlled variables. in regression the model, we fit is a linear model ('linear model' just means 'model based on a straight line') (Andy, 2005).

The third assumption in MLR is any data should be free from heteroscedasticity. Heteroscedasticity will happen whenever there is interruption in the model that not fulfilled. If the important variables in the model are missing, hence heteroscedasticity will happen. Any model can be check whether there is heteroscedasticity or not based on Spearman's rank correlation test.

The last assumption that should be checked in research is multicollinearity. Multicollinearity means situation that has high degree of correlation between controlled variables. Any analyses can be known the present of multicollinearity by checking the value of variation inflation factor (VIF). When the value of VIF is less than 5, hence multicollinearity is not serious. While if VIF is more than 5, then multicollinearity is substantial. Multicollinearity will be more serious whenever the value of VIF is more than 10.

## Step 2: Selecting suitable methods of multiple linear regression

There are three methods in MLR which are forward selection, backward elimination and stepwise regression. All three methods can be categorized into stepwise-type procedures. In this research, only stepwise regression method was applied. Stepwise regression method is a combination of forward selection and backward elimination. By
referring Minitab Methods and Formulas, standard stepwise regression both adds and removes controlled variables as needed for each step. Minitab ended its procedure when all variables not in the model have p -value that are less than the specified Alpha-to-Enter value and when all variables in the model have p -value that are greater than or equal to the specified Alpha-to-Remove value. Based on Minitab StatGuide, Alpha-to-Enter is a value that determines if any of the predictors that not currently in the model should be added to the model. While Alpha-toRemove is a value that determines if any of the predictors in the model should be removed from the model.

## Step 3: Interpreting the output

From the SPSS output, we can interpret the values of Pearson coefficient, multiple coefficient of determination $\left(\mathrm{R}^{2}\right)$, multiple correlation coefficient (R) and adjusted multiple coefficient of determination (adjusted $\mathrm{R}^{2}$ ). Correlation analyses is the method in regression that is used to look how far the relationship between two variables. Pearson linear correlation was applied because to check the existence of relationship between two variables in this research. According to Piaw (2006), some of the strength value (r) are as follows:

Table 1. Correlation coefficient value strength

| Correlation coefficient size $(\mathbf{r})$ | Correlation strength |
| :---: | :---: |
| .91 until 1.00 or -.91 until -1.00 | Very strong |
| .71 until .90 or -.71 until -.90 | Strong |
| .51 until .70 or -.51 until -.70 | Medium |
| .31 until .50 or -.31 until -.50 | Weak |
| .01 until .30 or -.01 until -.30 | Very weak |
| .00 | No correlation |

Source: (Piaw, 2006)
$\mathrm{R}^{2}$ means the proportion of the total variation in the $n$ observed values of the dependent variable that is explained by the overall regression model (Bowerman et al., 2005). The higher $\mathrm{R}^{2}$, the better the model fits your data. R is the positive squared root of $R^{2}$ (Levin \& Rubin, 1994).

Adjusted $R^{2}$ is a measure of the loss of predictive power or shrinkage in regression. The adjusted $R^{2}$ will explain how much variance in the outcome would be accounted for if the model had been derived from the population from which the sample was taken (Andy, 2005). The larger adjusted $\mathrm{R}^{2}$, the better the model fits the data.

## Step 4: Developing equation of multiple linear regression

In this research, the hypotheses that used:
$H_{0}: \beta_{1}=\beta_{2}=\beta_{3}=0$
$H_{a}$ : At least one of the $\beta_{1}, \beta_{2}$ and $\beta_{3}$ does not equal to 0
which says that
$H_{0}$ : None of the controlled variable $\mathrm{X}_{1}, \mathrm{X}_{2}$ and $\mathrm{X}_{3}$ is significantly related to Y
$H_{a}$ : At least one of the controlled variable $\mathrm{X}_{1}, \mathrm{X}_{2}$ and $\mathrm{X}_{3}$ is significantly related to Y
The model of multiple linear regression can be represent as:

$$
\begin{equation*}
Y=\beta_{0}+\beta_{1} X_{1}+\beta_{2} X_{2}+\beta_{3} X_{3}+\varepsilon \tag{1}
\end{equation*}
$$

where

```
Y = Response variable (Marine fish landing)
\beta
\beta
\beta
\beta}=\mathrm{ Coefficient of third control variable, X3
X1 = Controlled variable (Fishermen)
X2 = Controlled variable (Fishing boat)
X3 = Controlled variable (Fishing gears licensed)
\varepsilon = Error
```


## 4. Results and discussions

All data was analyzed using Statistical Package for the Social Sciences 17.0 (SPSS 17.0) and Minitab version 15 (Minitab 15).

Table 2. Test of normality

|  | Kolmogorov-Smirnov |  |  |  | Shapiro-Wilk |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Statistic | df | Sig. | Statistic | df | Sig. |  |
| Marine <br> landing | fish | .080 | 40 | .200 | .973 | 40 | .446 |

The normality can check by using two test as shown in Table 2 which are by Kolmogorov-Smirnov (if sample size is more than 50) and Shapiro-Wilk (if sample size is less than 50). Since the sample size in this research ( $n=40<50$ ), so we need to use Shapiro-Wilk which gives a Sig. value equal to .446 . It shows that marine fish landing is normally distributed (Sig. = $446>0.05$ ).

Table 3. Correlations between response variable and controlled variables

| Response variable | Controlled variables | Pearson correlation | Sig. (2-tailed) |
| :--- | :--- | :---: | :---: |
| Marine fish landing | Fishermen | -.429 | .006 |
|  | Fishing boat | -.268 | .095 |
|  | Fishing gears licensed | .630 | .000 |
| Fishermen | Fishing boat | .828 | .000 |
|  | Fishing gears licensed | -.239 | .138 |
| Fishing boat | Fishing gears licensed | -.073 | .655 |

According to Table 3, it shows that correlations between response variable and controlled variables has been determined using Pearson Correlation. From this table, it shows that the weak correlation between marine fish landing and fishermen ( $\mathrm{r}=-.429$ ), while the correlation between marine fish landing and fishing gears licensed ( $\mathrm{r}=.630$ ) is medium. The strong correlation shows between fishermen and fishing boat ( $\mathrm{r}=.828$ ). Therefore the three relationship are significant because Sig. $<.05$.

The strength correlation between marine fish landing and fishing boat ( $\mathrm{r}=-.268$ ), fishermen and fishing gears licensed ( $\mathrm{r}=-.239$ ) also fishing boat and fishing gears licensed ( $\mathrm{r}=-.073$ ) shows very weak. The three relationship explains that there are not significant because Sig. $>.05$. The negative sign in the Table 3 shows the direction of the correlation.

Table 4. Model Summary

| Model | $\mathbf{R}$ | $\mathbf{R}^{\mathbf{2}}$ | Adjusted $\mathbf{R}^{\mathbf{2}}$ | Standard error of the estimate |
| :---: | :---: | :---: | :---: | :---: |
| 1 | .630 | .397 | .381 | 27700.45476 |
| 2 | .692 | .479 | .451 | 26081.83790 |

The model summary is based on the Table 4. The value of $\mathrm{R}^{2}$ is .397 (Model 1) shows that there are $39.7 \%$ ( $\mathrm{R}=.630$ ) changes in response variable (marine fish landing). It is because changes in controlled variable (fishing gears licensed). This explains that fishing gears licensed is major factor to the marine fish landing. The value of $\mathrm{R}^{2}$ is . 479 ( $\mathrm{R}=.692$ ) for Model 2 shows that there are $47.9 \%$ changes in response variable (marine fish landing) is occurred because changes in combination of two controlled variables which are fishing gears licensed and fishermen. By comparing both models, Model 2 is a better model fits to the data than Model 1 . This is because the higher the value or $\mathrm{R}^{2}$ and adjusted $\mathrm{R}^{2}$ (Model $1=.381$; Model $2=.451$ ), the better the model fits to the data.

Table 5. Coefficients

|  | Model | Coefficients | Standard <br> error | Beta | t-value | Significance <br> value |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 1 | Constant | 16062.147 | 14266.689 |  | 1.126 | .267 |
|  | Fishing gears licensed | 33.463 | 6.691 | .630 | 5.001 | .000 |
| 2 | Constant | 88359.030 | 32740.887 |  | 2.699 | .010 |
|  | Fishermen | -6.410 | 2.647 | -.296 | -2.421 | .020 |
|  | Fishing gears licensed | 29.716 | 6.487 | .559 | 4.581 | .000 |

According to Table 5, it shows coefficients. From that coefficient, we can develop two model using MLR equation such as below:

$$
\begin{align*}
& \text { Model 1: } \\
& Y=16062147+33.463 X_{3} \tag{2}
\end{align*}
$$

Model 2:

$$
\begin{equation*}
Y=88359030-6.410 X_{1}+29.716 X_{3} \tag{3}
\end{equation*}
$$

Based on the Model 1, the standardized coefficients for fishing gears licensed ( $\beta=.630, p<.05$ ) is significant. This explained that only fishing gears licensed is factor to the marine fish landing. While in Model 2 , the standardized coefficients for fishermen ( $\beta=-.296, p<.05$ ) and fishing gears licensed ( $\beta=.559, p<.05$ ) are significant. This explained that fishing gears licensed and fishermen are factors to the marine fish landing. As conclude, Model 2 is better model fits to the data than Model 1.

Table 6. Stepwise regression results

|  | Step | $\mathbf{1}$ | $\mathbf{2}$ |
| :--- | :---: | :---: | :---: |
| Constant | 16062 | 88359 |  |
| $\mathrm{X}_{3}$ | 33.5 | 29.7 |  |
| t -value | 5.00 | 4.58 |  |
| p-value | .000 | .000 |  |
| $\mathrm{X}_{1}$ |  | -6.4 |  |
| t -value |  | -2.42 |  |
| p-value | 27700 | .020 |  |
| S | 39.69 | 26082 |  |
| $\mathrm{R}-\mathrm{Sq}$ |  | 47.94 |  |


| R-Sq(adj) | 38.11 | 45.13 |
| :--- | :---: | :---: |
| Mallows Cp | 5.8 | 2.1 |

According to Table 6, it presents the result of stepwise regression using Minitab 15. There are two steps that used to select the controlled variables. In the step $1, X_{3}$ indicates smallest $p$-value than Alpha-to-Enter ( $\mathrm{p}=.000<.05$ ). Therefore $X_{3}$ is the first variable that enters into the model. In the step 2, the p-value for $X_{1}$ shows .020 which is smallest than .05 . Therefore $X_{1}$ is the second variable that needs to enter into the model. $X_{3}$ is retained in the model with the coefficient 29.7, t -value is 4.58 and p -value is .000 . After the second step, there are no controlled variables that enter and remove the model.

For the marine fish landing output, the value of S decreases from step 1 ( $\mathrm{S}=27700$ ) to step 2 ( $\mathrm{S}=26082$ ), R-Sq and $\mathrm{R}-\mathrm{Sq}(\mathrm{adj})$ in the step $2(\mathrm{R}-\mathrm{Sq}=47.94, \mathrm{R}-\mathrm{Sq}(\mathrm{adj})=45.13)$ is higher than step $1(\mathrm{R}-\mathrm{Sq}=39.69, \mathrm{R}-\mathrm{Sq}(\mathrm{adj})=38.11)$ and Mallows Cp in step 2 is closer to number of controlled variables than step 1. Hence, these statistics indicates step 2 which containing controlled variables $X_{3}$ and $X_{1}$ is provides better fits to the data. The final model shows only two controlled variables by using stepwise regression and produced regression model such as follows:

$$
\begin{equation*}
Y=88359+29.7 X_{3}-6.4 X_{1} \tag{4}
\end{equation*}
$$

## 5. Conclusions

This paper using multiple linear regressions (MLR) to built forecasting model for fish landing. Based on the output from SPSS 17.0, there are two model was built. By comparing two models using SPSS 17.0, Model 2 is a better model fits to the data than Model 1. This is because the value of $\mathrm{R}^{2}$ and adjusted $\mathrm{R}^{2}$ in Model $2\left(\mathrm{R}^{2}=.479\right.$, adjusted $\mathrm{R}^{2}=.451$ ) is higher than Model $1\left(\mathrm{R}^{2}=.397\right.$, adjusted $\left.\mathrm{R}^{2}=.381\right)$. In the stepwise regression method shows that only two controlled variables that were selected using Minitab 15 which are fishermen and fishing gears licensed. This explained that only fishermen and fishing gears licensed are factors to the marine fish landing.

## References

Andy, F. (2005). Discovering statistics using SPSS: (and sex, drugs and rock ' $n$ ' roll). London: SAGE.
Bowerman, B.L., O’Connell, R.T. and Koehler, A.B. (2005). Forecasting, time series and regression. $4^{\text {th }}$ ed. United States of America: Brooks/Cole Thomson Learning Inc.
Khamis, A., Ismail, Z. \& Shabri, A. (2003). Pemodelan harga minyak sayuran menggunakan analisis regresi linear berganda. Matematika, Jilid 9, bil. 1, 59-70.
Levinm R.I. and Rubin, D.S. (1994). Statistics for management. $6^{\text {th }}$ ed. Englewood Cliffs, N.J.: Prentice Hall.
Ofuoku, A.U., Olele \& Emah, G. (2007). Determinants of adoption of improved fish production technologies among fish farmer in Delta States, Nigeria. Journal of Fisheries International, 2(2):147-151.
Piaw, C.Y. (2006). Asas statistik penyelidikan (Buku 2). Kuala Lumpur: McGraw-Hill.
Sain, R.L. (2006). Characterizing how fish communities and physical habitat structure are affected by urbanization in an East Tennessee Watershed, Master thesis, University of Tennessee, Knoxville.
Sarker, M.A., Chowdhury, A.H. \& Itohara, Y. (2006). Entrepreneurships barriers of pond fish culture in Bangladesh- A case study from Mymensingh district. Journal of Social Sciences, 2(3):68-73.
Wan Nawang, W.M.Z., Mamat, I. \& Mohd Isa, A.M. (2009). Faktor peramal minat belia untuk menjadi nelayan: Satu kajian di Mukim Kuala Besut, Terengganu. Jurnal Teknologi, 50(E):29-52, Universiti Teknologi Malaysia.


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