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Resource-Efficient Technologies 2 (2016) S53–S62

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Research paper

# Modeling the adsorption of benzenecetic acid on CaO<sub>2</sub> nanoparticles using artificial neural network

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Received 17 June 2016; received in revised form 6 October 2016; accepted 10 October 2016

Available online 9 November 2016

## Abstract

The present work reported a method for removal of benzenecetic acid from water solution using CaO<sub>2</sub> nanoparticle as adsorbent and modeling the adsorption process using artificial neural network (ANN). CaO<sub>2</sub> nanoparticles were synthesized by a chemical precipitation technique. The characterization and confirmation of nanoparticles have been done by using different techniques such as X-ray powder diffraction (XRD), high resolution field emission scanning electron microscope (HR-FESEM), transmittance electron microscopy (TEM) and high-resolution TEM (HRTEM) analysis. ANN model was developed by using elite-ANN software. The network was trained using experimental data at optimum temperature and time with different CaO<sub>2</sub> nanoparticle dosage (0.002–0.05 g) and initial benzenecetic acid concentration (0.03–0.099 mol/L). Root mean square error (RMS) of 3.432, average percentage error (APE) of 5.813 and coefficient of determination ( $R^2$ ) of 0.989 were found for prediction and modeling of benzenecetic acid removal. The trained artificial neural network is employed to predict the output of the given set of input parameters. The single-stage batch adsorber design of the adsorption of benzenecetic acid onto CaO<sub>2</sub> nanoparticles has been studied with well fitted Langmuir isotherm equation which is homogeneous and has monolayer sorption capacity.

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**Keywords:** Feed forward neural network; Single-stage batch; Benzenecetic acid; CaO<sub>2</sub> nanoparticles; Adsorption

## 1. Introduction

Carboxylic acids have a wide range of application especially in pharmaceuticals, food, and polymers industries. Hence, recovery of carboxylic acids from aqueous solution is an important process in chemical engineering [1]. A number of separation processes have been developed to recover carboxylic acids from aqueous acid [2–5]. Adsorption is low cost and allows an easy operation for the recovery of carboxylic acids [6].

Benzenecetic acid has a white scale-like crystal look and a honey-like odor at low concentration [7]. It is largely employed in the pharmaceutical industry for making of antibiotics. It is used as a precursor (reactants) in the production of penicillin G

[8]. It is an important chemical for the chemical industry. It is found in neroli, rose oil and in many fruits [9]. It has a wide range of biological activity, antibacterial, analgesic, and virucidal properties [10]. It is produced by both fermentation of soya beans using *Bacillus licheniformis* [11,12] and strains of *Bacteroides asaccharolyticus* and *Bacteroides melaninogenicus* subspecies isolated from human and animal sources [13]. It powerfully inhibits the activity of penicillin acylase. Removal of a benzenecetic from fermentation broth, reaction mixture and waste water is the vital step of complete production process because it directly affects the overall economy of the process [14]. The removal of benzenecetic acid is required to get higher productivity. Because of these multiple applications in various chemical industries and also medicinal, so it is necessary to remove benzenecetic acid from aqueous solution is necessary.

CaO<sub>2</sub> nanoparticles are used as an adsorbent for the recovery of benzenecetic acids because they provide large surface area and are low cost [8]. The basis of separation of benzenecetic acids (adsorbate) from the feed mixture onto the CaO<sub>2</sub> nanoparticles (solid adsorbent) is governed by the variation

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<http://dx.doi.org/10.1016/j.refit.2016.10.004>

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Table 1  
Summary of ANN applications in adsorption processes.

No.	Adsorbent	Objective of the work	References
1	Hybrid material (Ce-HAHC1)	To study the removal of As (III) from aqueous solution using hybrid material as an adsorbent and ANN was used for modeling of experimental (actual) result	[21]
2	Waste Acorns of <i>Quercus Ithaburensis</i> (WAQI)	To study the adsorption of radioactive Gallium-67 which is employed in nuclear medicine and ANN modeling was used to estimate the adsorption amount	[22]
3	Activated carbon wood charcoal rice husk ash	To predict the removal of efficiency of adsorption of carbonaceous adsorbents to remove phenol and resorcinol from aqueous environment	[23]
4	Shelled <i>Moringa oleifera</i> seed (SMOS)	To study the removal of Ni(II) ions from water using SMOS powder by a single layer ANN model	[24]
5	Antep pistachio shells	To study the removal of Pb(II) from aqueous solution by Antep pistachio shells based on 66 experimental sets; three layer artificial neural network model was performed to predict the removal efficiency of Pb(II) ions	[25]
6	Sunflower shells	To study the adsorption potential of shells of sunflower to remove Cu <sup>2+</sup> ions from aqueous solution using a fixed bed adsorption column	[26]
7	Pumice	To study the use of industrial leachate as adsorbent for the removal of Cu (II)	[27]
8	Magnetic zeolite modified with 2-(3,4dihydroxyphenyl)-1,3-dithiane	To predict the removal of cadmium (II) and copper (II) from water and soil by using synthesized magnetic adsorbent; three layer artificial neural network model was used to estimate the parameters	[28]
9	Hyacinth root	To study the removal of Pb(II) ions from aqueous streams by water hyacinth root; ANN model was employed for the prediction of Pb(II) ions removal	[29]

among the concentrations of the benzenecetic acids in liquid and solid phases as compared to their equilibrium concentrations. The mathematical models have been used to correlate these equilibrium conditions. Models have failed to predict because of the complexity of the adsorption process [15].

In present work, the experimental data are modeled by using artificial neural networks to resolve the predicted data. Artificial Neural Network (ANN) is a promising alternative modeling tool for various operations involving nonlinear multivariable relationships. It consists of an input and an output layer and one or more hidden layers while input and hidden layers have neuron which receives input values [16]. ANNs act as a black box model which is composed of highly interconnected processing elements called artificial neurons or nodes to solve a specific problem [17,18]. The outcomes were obtained from the ANN software and they are compared with the experimental data to confirm which approach provides superior levels of accuracy [19,20]. Table 1 gives the application of ANN for the removal of benzenecetic acid in adsorption processes.

Multi Layer Perception (MLP) is a feed forward neural network and is applied in modeling of many chemical engineering applications. It incorporates a network comprising three layers: one input, one output and in between the one hidden layer. The nodes between the two consecutive layers are interconnected by means of weights to find out the layer of neuron. The input layer receives data from the experimental source and are transferred to output layer during hidden layers in the form of array of matrix. The output signal is compared with the target value to produce error signal. Training of the network is carried out to reduce the error by adjusting the weights using suitable algorithm [17,18]. A schematic of the typical structure of an MLP network developed for the adsorption of benzenecetic acid from aqueous solution using CaO<sub>2</sub> nanoparticles as an adsorbent with two hidden layers containing five neurons each is shown in Fig. 1.

In this work, different network and training algorithms were tried to predict removal of benzenecetic acid by using CaO<sub>2</sub> nanoparticles, and commented on their performance based on

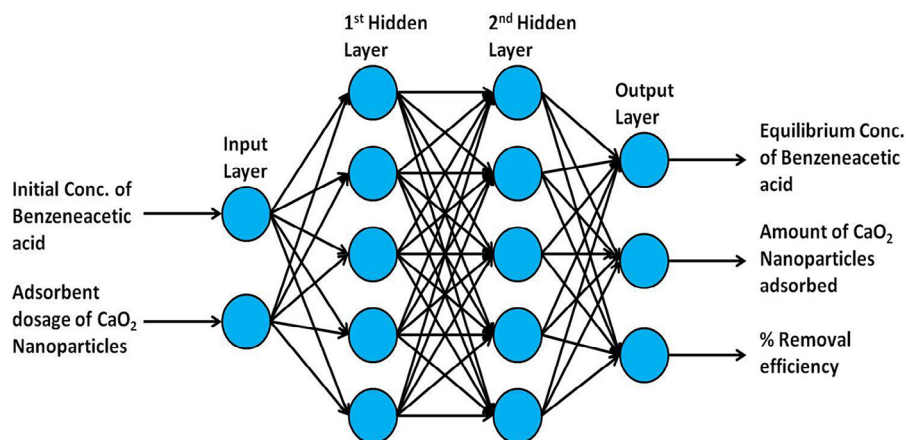


Fig. 1. Neural Network Architecture for ANN model.

determination of coefficient ( $R^2$ ) and root mean square error (RMSE). The influential parameters, the amount of  $\text{CaO}_2$  nanoparticles adsorbent and initial concentration of benzenecetic acid were investigated. The adsorption isotherms of the prepared adsorbent were studied. An artificial neural network model was developed to predict the behavior of the removal of benzenecetic acid in the proposed process under various conditions.

## 2. Experimental section

### 2.1. Material and methods

Benzenecetic acid was purchased from Acros Organics (New Jersey, USA). Standard stock solution of benzenecetic acid of 13.47 g in 1000 mL (0.099 mol/L) was prepared. All solutions were prepared in double distilled water. A digital pH meter (Spectral Lab Instrumental Pvt. Ltd, India) was used to measure pH which was calibrated with three buffers (pH 4.0, 7.0, and 10.0) every day.

### 2.2. $\text{CaO}_2$ nanoparticles preparation

The detailed  $\text{CaO}_2$  nanoparticle synthesis procedure is given in our earlier article [8]. Analytical grade chemicals were purchased and used for the study obtained from Merck (Merck India). Three grams of calcium chloride ( $\text{CaCl}_2$ ) were initially added to 30 mL double distilled water followed by addition of 15 mL ammonia solution ( $\text{NH}_3 \cdot \text{H}_2\text{O}$ ) and then 120 mL of polyethylene glycol (PEG 200). Under constant stirring, 15 mL of 30% hydrogen peroxide ( $\text{H}_2\text{O}_2$ ) was added by rate of three drops per minute. Afterward, the solution was stirred for 2 hr and turns yellowish in color. Then, NaOH solution was added until the pH of the solution comes to 11.5. The nanoparticles suspension becomes white in color and was centrifuged at 10,000 rpm for 5 min to separate nanoparticles. The nanoparticles were washed three times by 0.1 N NaOH solutions and two times by distilled water. The final pH of 8.4 for the residue water was obtained. The resultant nanoparticles were dried at 80°C for 2 hours in a vacuum oven.

### 2.3. Characterization of $\text{CaO}_2$ nanoparticles

X-ray Diffractometer (XRD) analysis [PANalytical X'pert Pro] was performed in  $2\theta$  range from  $10^\circ$  to  $100^\circ$  with a step size of  $0.01^\circ$  using Cu target X-ray tube ( $\lambda = 1.5406 \text{ \AA}$ ). Morphologies of samples were observed with a high resolution field emission scanning electron microscope (HR-FESEM) from Zeiss, model name ULTRA Plus. It comes with a Gemini $\text{\O}$  column that proposes a theoretical resolution of 1.0 nm at 15 kV. The particle size was confirmed using transmission electron microscopy (TEM) [PHILIPS-CM 200] operated at 20–200 kV. High resolution transmission electron microscopy (HR-TEM) of particles was carried out using JEOL JEM-2100.

### 2.4. Batch experiments

The interactive effects of  $\text{CaO}_2$  adsorbent dosage and initial benzenecetic acid were in the range of 0.002–0.05 g and 0.03–0.099 mol/L respectively. For each experimental run, 10 mL

aqueous benzenecetic acid solution of known concentration was taken in 100 mL Erlenmeyer flask containing a known mass of  $\text{CaO}_2$  nanoadsorbent which was kept in water bath controlled shaker, and once the equilibrium is reached the concentration of benzenecetic acid (final mixture) was determined by NaOH titration using phenolphthalein indicator. The suspension was then centrifuged at 3000 rpm and  $\text{CaO}_2$  nanoparticles were collected. The supernatant was filtered using filter (Whatman) and residual  $\text{CaO}_2$  nanoparticles were separated. The experimental values of equilibrium concentration (mol/L), amount of nanoparticles adsorb (mol/L) and % removal efficiency were calculated. ANN models were developed to correlate initial concentration of benzenecetic acid in feed, adsorbent dosage with equilibrium concentration of benzenecetic acid on solid and liquid phases and the removal efficiency achieved. In this study, elite-ANN $\text{\O}$  is employed to develop the entire ANN models [30].

The equilibrium adsorption capacity of benzenecetic acid ( $q_e$ ) on the  $\text{CaO}_2$  nanoadsorbent was calculated as:

$$q_e = \frac{(C_0 - C_e)}{W} \times V \quad (1)$$

where  $q_e$  is the equilibrium capacity of  $\alpha$ -toluic acid on the adsorbent (g/g),  $C_0$  (g/L) is the initial concentration of  $\alpha$ -toluic acid,  $C_e$  is the equilibrium concentration of  $\alpha$ -toluic acid in solution after adsorption (g/L),  $V$  is the volume of solution (L), and  $W$  is the mass of  $\text{CaO}_2$  nanoparticles in (g).

The benzenecetic acid removal efficiency was calculated as:

$$\% \alpha\text{-toluic acid removal} = \frac{(C_0 - C_e)}{C_0} \times 100 \quad (2)$$

## 3. Result and discussion

### 3.1. Characterization study

X-ray diffraction patterns of  $\text{CaO}_2$  are shown in Fig. 2. The 002, 110, 112, 103, 202 and 310 plane reflections are evidently

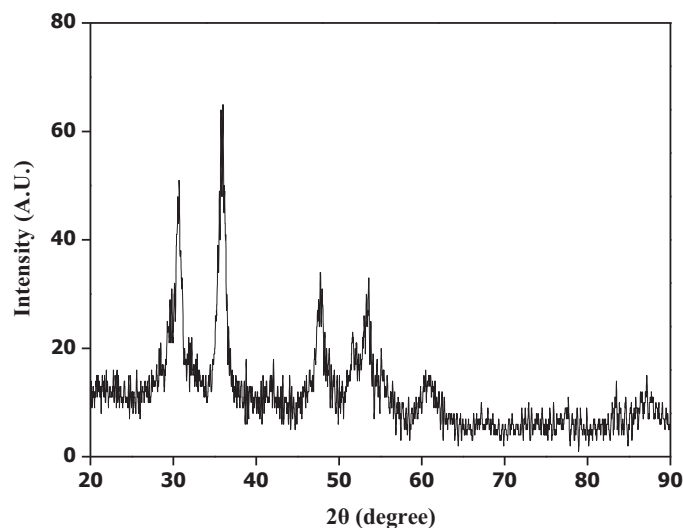


Fig. 2. XRD patterns of  $\text{CaO}_2$  nanoparticles.

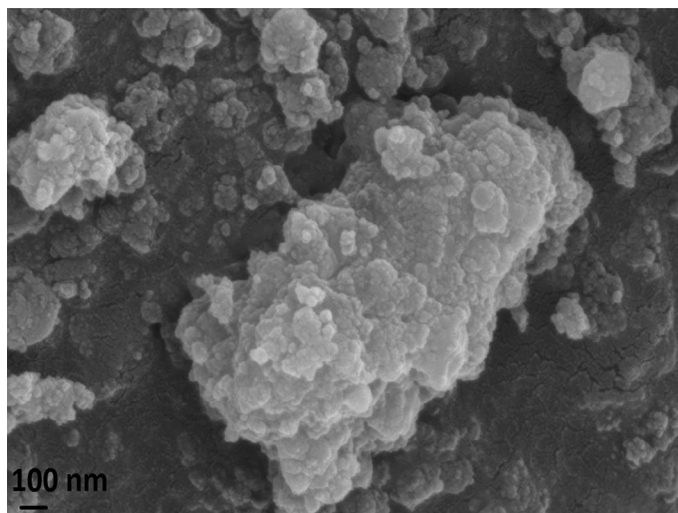


Fig. 3. HR-FESEM images of CaO<sub>2</sub> nanoparticles.

seen and match the reference patterns for CaO<sub>2</sub> (JCPDS) File No. 03-0865 [8]. The average particle size of CaO<sub>2</sub> nanoparticles was determined from the XRD pattern [(112) plane] according to Debye-Scherrer equation:

$$D = K\lambda / (\beta \cos \theta) \quad (3)$$

where  $K$  is the Debye-Scherrer constant equal to 0.89,  $\beta$  is the full width at half maximum of (112) peak,  $\theta$  is the Bragg angle (in radians) and  $\lambda$  is the X-ray wave length equal to 1.5406 Å. The average particle size from Eq. (3) was found to be 16 nm. The morphology of synthesized CaO<sub>2</sub> nanoparticles was studied by the HR-FESEM analysis (Fig. 3). It visibly indicates that CaO<sub>2</sub> nanoparticles showed the aggregated round shape and are generally spherical in shape. Fig. 4(a) and (b) shows TEM and HR-TEM images of CaO<sub>2</sub> nanoparticles with approximately uniform shape and size. The CaO<sub>2</sub> nanoparticles show a very dark image of HR-TEM because CaO<sub>2</sub> nanoparticles possess a higher electron density. The particles were shown as single and isolated because of presence of PEG stabilizer. It can be clearly seen that they are nearly spherical in shape with average particle size of about 10–40 nm.

### 3.2. Influence of adsorbent dosage and initial concentration of benzenecetic acid

Adsorbent dose and initial concentration are important factors in an adsorption process. The effect of adsorbent dose on the removal of benzenecetic acid is investigated at a temperature of  $22 \pm 2^\circ\text{C}$  for 0.002 g–0.05 g keeping all other parameters constant. The removal of benzenecetic acid increases from 24.75% to 97.47% for initial concentration of 0.099 mol/L with increasing CaO<sub>2</sub> nanoparticles adsorbent dosage. Increase in the adsorbent dosage shows larger surface area and the availability of more adsorption. It is observed that no further increase in the adsorption occurs when CaO<sub>2</sub> nanoparticles dose reaches a value of 0.05 g. The dissimilar equilibrium adsorbent dose is found because increasing the concentration gradient involves higher doses for adsorption.

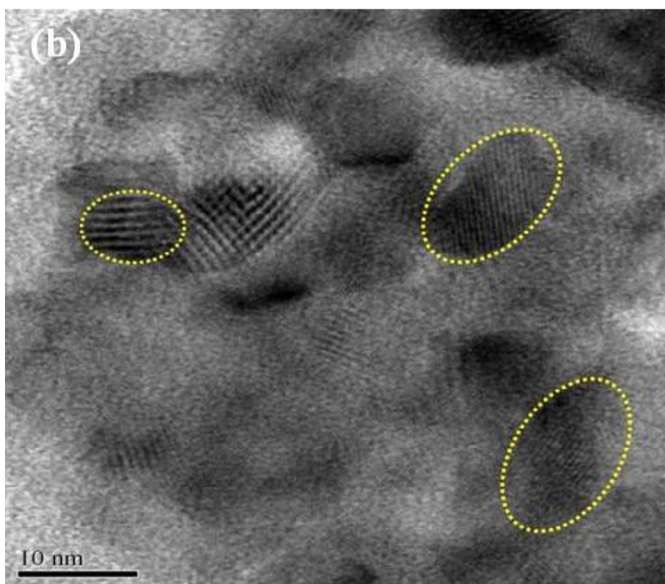
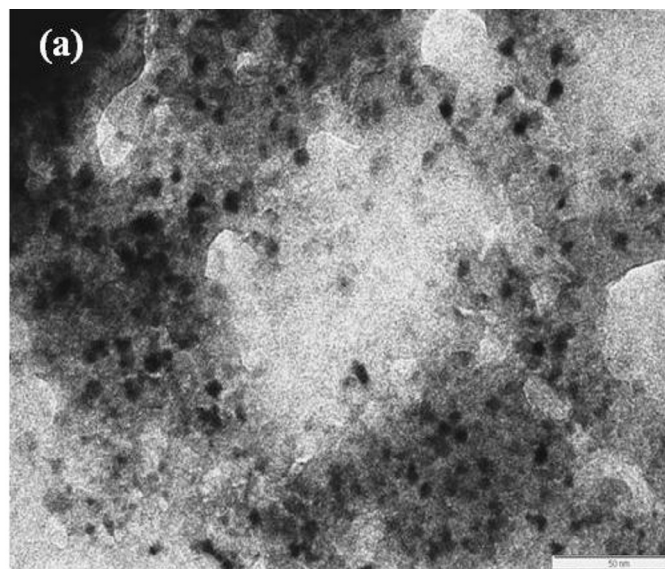


Fig. 4. (a) TEM and (b) HR-TEM images of CaO<sub>2</sub> nanoparticles.

Once the equilibrium dose is achieved, the removal capacity becomes constant and this may be due to collapsing or overlapping of available free sites for adsorption. The effect of initial concentration of benzenecetic acid varied from 0.04 mol/L to 0.099 mol/L. The removal of benzenecetic acid increases from 33.3% to 88.3% with a decrease in the concentration of benzenecetic acid with constant CaO<sub>2</sub> nanoparticles adsorbent dosage of 0.01 g. At low concentration, the number of moles of benzenecetic acid is small relative to the available adsorption sites on the nanoparticle. Consequently, adsorption becomes independent of initial concentration and as a result adsorption was found to increase. Conversely, at higher concentrations, mainly the adsorption sites will be taken by benzenecetic acid and the available sites of adsorption become less, hence the removal of efficiency of benzenecetic acid which depends on the initial decreases in concentration [8,31,32].

Table 2  
Total data for ANN modeling of benzenecetic acid adsorption studies.

Sr. no.	Initial concentration $C_o$ (mol/L)	CaO <sub>2</sub> nanoparticles (g)	Equilibrium concentration $C_e$ (mol/L)	Amount of nanoparticles adsorbed (mol/L)	Removal efficiency (%)
1	0.099	0.002	0.062	0.049	36.87
2	0.099	0.004	0.057	0.056	41.92
3	0.099	0.006	0.063	0.048	35.86
4	0.099	0.008	0.074	0.033	24.75
5	0.099	0.01	0.065	0.046	34.34
6	0.099	0.02	0.045	0.072	54.04
7	0.099	0.03	0.018	0.110	81.82
8	0.099	0.04	0.005	0.127	94.95
9	0.099	0.05	0.002	0.131	97.47
10	0.099	0.01	0.066	0.045	33.30
11	0.08	0.01	0.047	0.046	41.90
12	0.07	0.01	0.040	0.042	43.60
13	0.06	0.01	0.032	0.039	47.50
14	0.05	0.01	0.020	0.041	60.00
15	0.04	0.01	0.006	0.047	86.30
16	0.03	0.01	0.004	0.036	88.30

### 3.3. ANN models development for adsorption of benzenecetic acid

The procedure of designing an ANN model is as follows: (i) to specify the number of inputs and outputs for the network, (ii) to create a database of specified input–output variables, (iii) to select the network type, number of layer, number of neurons and activation function of each layer, (iv) training of the ANN network, and (v) to check the performance and accuracy of the trained neural network; altering and retraining of network as per precision level. The training process was carried out until the network output is equivalent with desired output. The weight function reduces the error between the network and desired output. The objective of the work is to correlate two input parameters' initial concentration of benzenecetic acid and CaO<sub>2</sub> nanoparticles adsorbent dosage with three output parameters that include equilibrium concentration of benzenecetic acid, CaO<sub>2</sub> nanoparticles adsorbed and % removal efficiency of benzenecetic acid by developing ANN models. The data set for ANN modeling of benzenecetic acid adsorption studies as shown in Table 2 is used for this purpose. The features of the ANN topology are shown in Table 3. The ANN model takes around 5000 iterations to converge to final error of 0.0478. The variation of error versus iteration in training mode to develop the model is shown in Fig. 5. The efficacy of ANN model is dependent on its accuracy of prediction. Table 4 and Fig. 6(a–c) show actual (experimental data) and predicted (ANN model's) values of equilibrium concentration, nanoparticles amount after

adsorption and % benzenecetic acid removal efficiencies for training data set. The statistical analysis of the results of the network performance is presented in Table 5. The values of  $R$  for the models are closer to 1. The performance of ANN model is calculated by the relative error and mean squared error (MSE). The most important purpose of the process is to determine the weights and to minimize the error. RMSE is calculated by difference between the ANN prediction and the actual response.

$$RMSE = \left( \frac{1}{n} \sum_{i=1}^n (y_i - y_{di})^2 \right)^{1/2} \quad (4)$$

where  $n$  is the number of points,  $y_i$  is the predicted value and  $y_{di}$  is the actual value.

From these graphs, there is a close agreement between the actual and predicted values indicating high accuracy of ANN model developed. However to confirm the claim of accuracy of prediction further, relative error has been calculated and plotted as shown in Fig. 7(a–c) for training data set.

$$\% \text{ Relative error} = \left( \text{Actual data} - \frac{\text{Predicted data}}{\text{Actual data}} \right) \times 100 \quad (5)$$

The root mean square error (RMSE) of 3.4327, mean percentage error (MPE) of 5.814 and coefficient of determination ( $R^2$ ) of 0.989 were found for prediction and modeling of benzenecetic acid removal for the training data set, as shown in

Table 3  
Neural network topology.

Input layer	First hidden layer	Second hidden layer	Third hidden layer	Output layer	RMSE Training data set
2	00	05	05	3	0.0478

Number of iteration: 5000, time: 25,413 millisecond  
Input parameters: initial concentration, amount of CaO<sub>2</sub> nanoparticles (adsorbent)  
Output parameters: equilibrium concentration, amount of CaO<sub>2</sub> nanoparticles adsorbed, removal efficiency

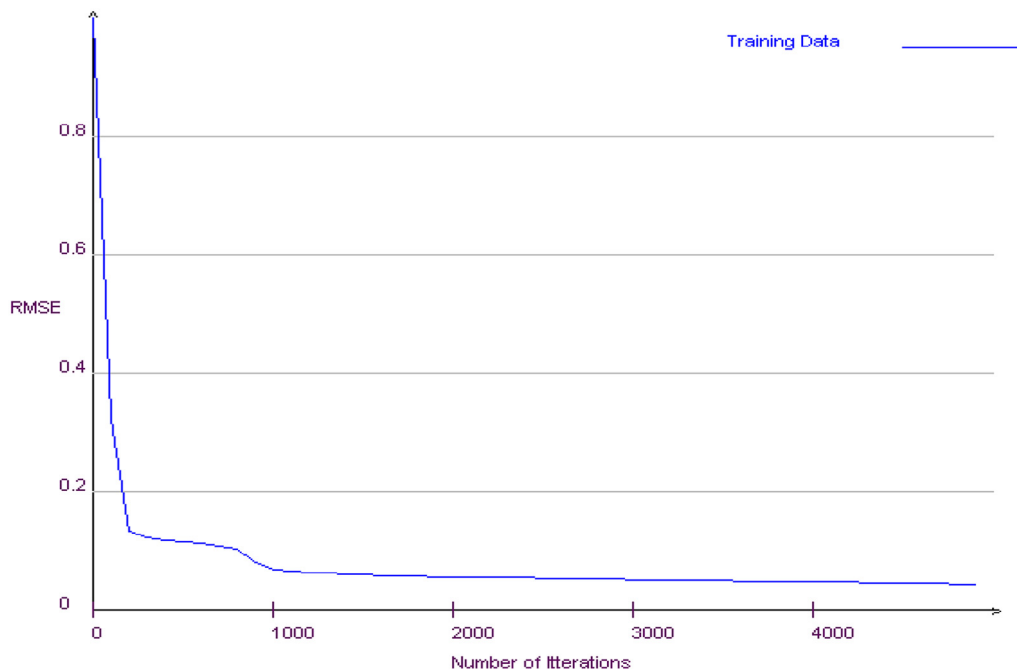


Fig. 5. Performance graph (error versus iteration in training mode).

**Table 5.** The RMSE,  $R^2$ , and APE values are within an acceptable range. The range of correlation coefficients is extremely close to 1, which indicates outstanding agreement between the experimental and the ANN predicted results.

3.4. Adsorption isotherm

The isotherm results were examined using Langmuir and Freundlich isotherms. The function of the adsorption isotherms is to relay the adsorbate concentration in the bulk and the adsorbed amount at the interface [33]. Langmuir isotherm shows monolayer adsorption over the homogeneous  $\text{CaO}_2$

nanoparticle adsorbent surface [34,35]. The Freundlich isotherm considers the heterogeneous surface of an adsorbent and is used to describe the adsorption data [36]. Analysis of adsorption isotherms of benzenecetic acid by  $\text{CaO}_2$  nanoparticles is given in Fig. 8. It is important to develop the equation which is used for design purposes.

The linear forms of the Langmuir and the Freundlich equations are:

$$\frac{C_e}{q_e} = \frac{1}{K_L} + \frac{a_L}{K_L} C_e \tag{6}$$

Table 4  
Comparison of ANN model output and experimental values input for training data.

Sr. no.	Benzenecetic acid removal efficiency (%)		Benzenecetic acid equilibrium concentration (mol/L)		Amount of $\text{CaO}_2$ nanoparticles adsorb (mol/L)	
	Experimental (actual) values	ANN predicted values	Experimental (actual) values	ANN predicted values	Experimental (actual) values	ANN predicted values
1	36.87	34.09	0.063	0.065	0.050	0.045
2	41.92	34.09	0.058	0.065	0.057	0.046
3	35.86	34.2	0.064	0.065	0.048	0.046
4	24.75	34.48	0.075	0.065	0.033	0.046
5	34.34	35.03	0.065	0.064	0.046	0.047
6	54.04	53.26	0.046	0.047	0.073	0.071
7	81.82	81.98	0.018	0.018	0.110	0.111
8	94.95	94.40	0.005	0.006	0.128	0.126
9	97.47	96.42	0.003	0.004	0.131	0.129
10	33.30	35.03	0.066	0.064	0.045	0.047
11	41.90	40.33	0.047	0.048	0.046	0.044
12	43.60	43.27	0.040	0.04	0.042	0.043
13	47.50	47.67	0.032	0.032	0.039	0.041
14	60.00	61.06	0.020	0.019	0.041	0.041
15	86.30	83.89	0.006	0.007	0.047	0.041
16	88.30	90.99	0.004	0.004	0.036	0.041

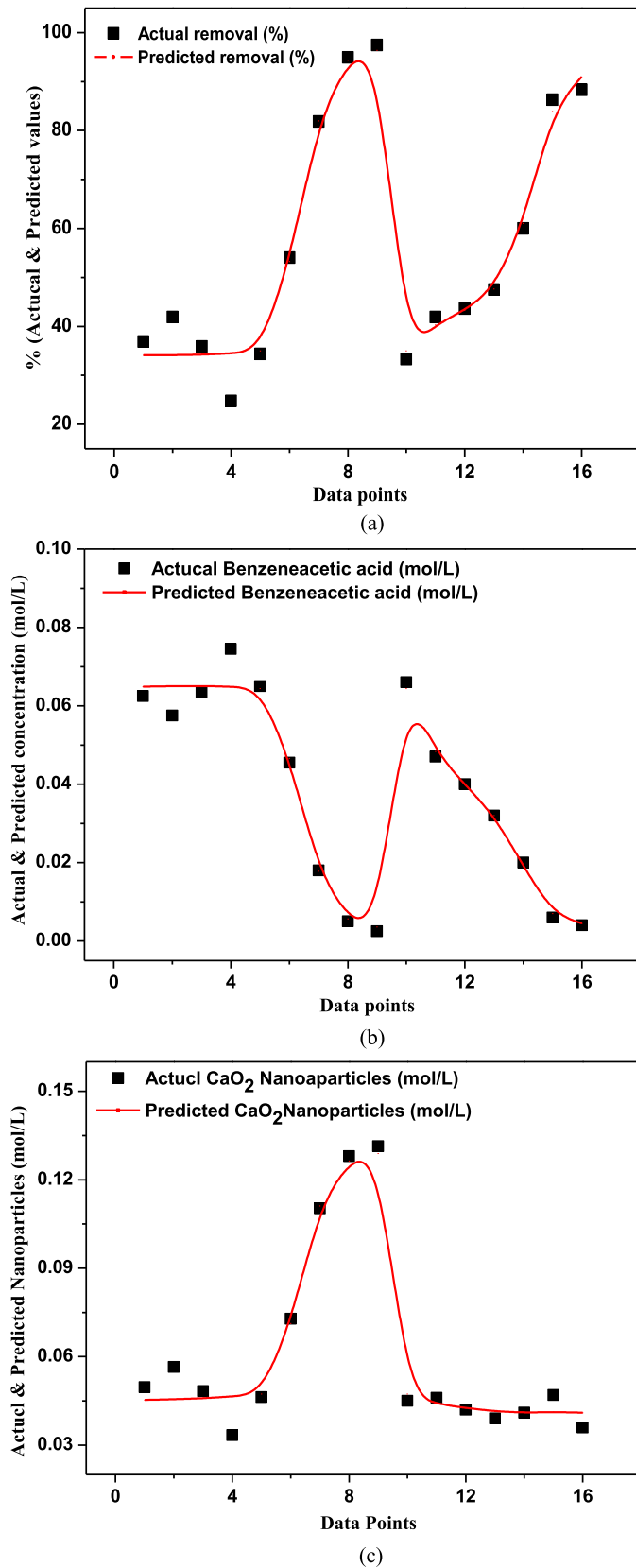


Fig. 6. Comparison of actual and predicted values of (a) removal efficiency of benzeneacetic acid, (b) equilibrium concentration of benzeneacetic acid, and (c) amount of CaO<sub>2</sub> nanoparticles after adsorption for training data set.

Table 5

Statistics of neural network models.

Models parameters	RMSE	Coefficient of determination	Average percentage error
Benzeneacetic acid removal efficiency (%)	3.432	0.989	5.814
Benzeneacetic acid equilibrium concentration (mol/L)	0.003	0.992	8.365
Amount of CaO <sub>2</sub> nanoparticles adsorbed (mol/L)	0.005	0.987	7.768

$$\log q_e = \log K_F + \frac{1}{n} \log C_e \quad (7)$$

where  $q_e$  is the amount of benzeneacetic acid adsorbed per unit mass of CaO<sub>2</sub> nanoparticles adsorbent (g/g),  $C_e$  is the equilibrium concentration of benzeneacetic acid in solution (g/L),  $K_L$  (L/g) and  $a_L$  (L/g) are the Langmuir isotherm constants and  $K_F$  (L/g) and  $n$  are the Freundlich isotherm constants.

In order to best fit of experimental data against the model predictions, error analysis was performed by using the normalized deviation (ND) and normalized standard deviations (NSD) through Eqs. (8) and (9), respectively [37,38].

$$ND = \frac{100}{n} \sum \left| \frac{q_{e(\text{exp})} - q_{e(\text{pred})}}{q_{e(\text{exp})}} \right| \quad (8)$$

$$NSD = 100 \sqrt{\frac{\sum (q_{e(\text{exp})} - q_{e(\text{pred})})^2 / q_{e(\text{exp})}^2}{n}} \quad (9)$$

$q_{e(\text{exp})}$  and  $q_{e(\text{pred})}$  are the experimental and predicted adsorption capacity (g·g<sup>-1</sup>), respectively, and  $N$  is the number of observations made.

Langmuir isotherm fits well with the experimental data ( $R^2 = 0.99$ ), whereas the low correlation coefficients  $R^2 = 0.71$  show poor agreement of Freundlich isotherms with the experimental data. The values of the constant  $K_L$  and  $a_L$  are 20.83 L/g and 4.604 L/g respectively. The values of the constant  $K_F$  and  $n$  values are 2.95 L/g and 4.90 respectively. ND and NSD values for Langmuir isotherm are 4.892 and 10.546 and for Freundlich isotherm are 9.267 and 21.431 respectively. The minimum values of ND and NSD are found for the Langmuir model. Langmuir isotherm offers better correlation with the experimental data as compared to Freundlich isotherm.

### 3.5. Design of batch adsorption system from isotherm data

Isotherm data can be used to predict the design of batch adsorption system. Mass balance study presents superior information in industrial point of view. It provides better information of the quantity of CaO<sub>2</sub> nanoparticles (adsorbent) required for achieving desired efficiency when treating with benzeneacetic acid [39–41]. A schematic diagram of a single-stage batch adsorber mass balance diagram is shown in Fig. 9. Consider  $W$  as the mass of CaO<sub>2</sub> nanoparticles (g),  $V$  as the volume of benzeneacetic acid concentration (L),  $C_0$  as the initial concentration of benzeneacetic acid,  $C_e$  as the equilibrium

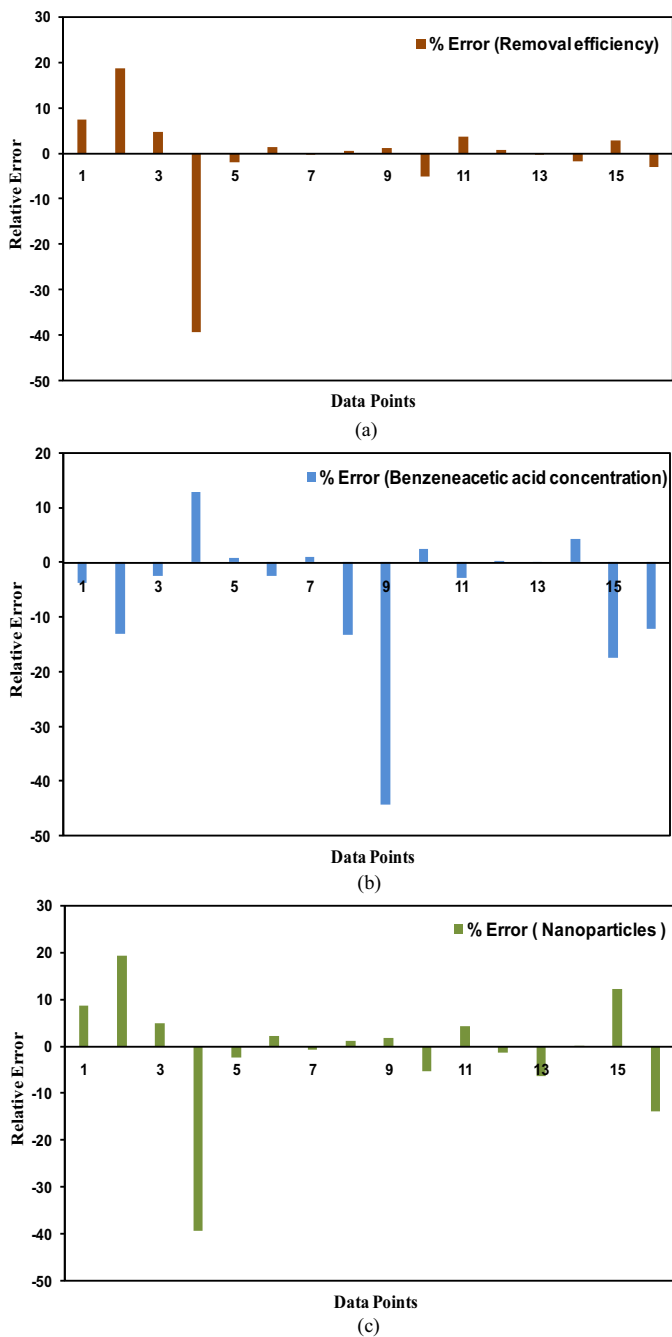


Fig. 7. % Relative error for (a) removal efficiency of benzeneacetic acid, (b) equilibrium concentration of benzeneacetic acid, and (c) amount of CaO<sub>2</sub> nanoparticles adsorbed for training data set.

concentration of benzeneacetic acid, and  $q_0$  and  $q_1$  are g of adsorbed per g of CaO<sub>2</sub> nanoparticles (adsorbent).

The mass balance for the benzeneacetic acid in the single-stage batch adsorption systems is given by:

$$V(C_0 - C_1) = W(q_0 - q_1) \quad (10)$$

For equilibrium condition,

$$C_1 = C_e, q_1 = q_e, q_0 = 0 \quad (11)$$

Eq. (10) can be modified and rearrange as:

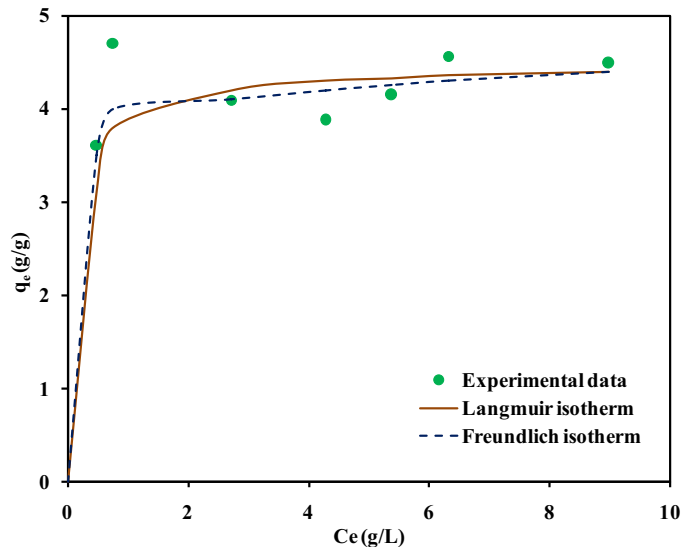


Fig. 8. Adsorption isotherms of benzeneacetic acid by CaO<sub>2</sub> nanoparticles.

$$\frac{W}{V} = \frac{(C_0 - C_e)}{q_e} \quad (12)$$

The Langmuir isotherm is the best fit to experimental data for adsorption of benzeneacetic acid on CaO<sub>2</sub> nanoparticles. Therefore, the Langmuir equation can be best substituted for  $q_e$  in Eq. (12)

$$\frac{W}{V} = \frac{C_0 - C_e}{\frac{K_L C_e}{1 + a_L C_e}} \quad (13)$$

where  $q_e = \frac{K_L C_e}{1 + a_L C_e}$ .

Fig. 10 shows a plot derived from Eq. (13) for 88.3% removal of benzeneacetic acid at different volumes and required amount of CaO<sub>2</sub> nanoparticles; initial concentration of benzeneacetic acid as 4.08 g/L is assumed. The amount of CaO<sub>2</sub>

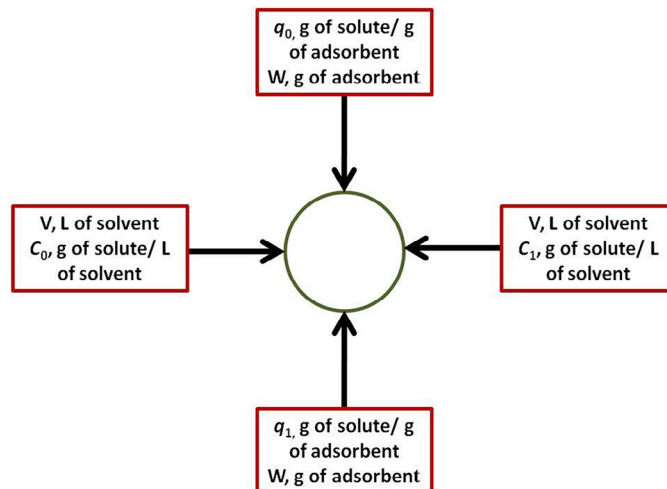


Fig. 9. A single-stage batch adsorber mass balance diagram.



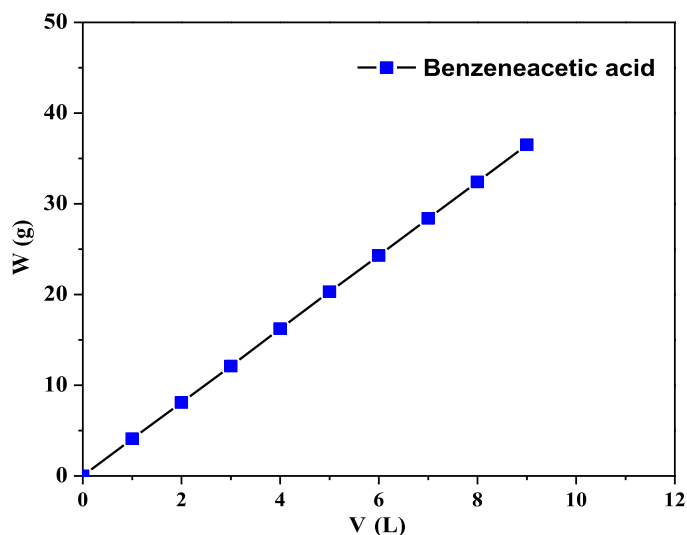


Fig. 10. CaO<sub>2</sub> nanoparticles (adsorbent) mass ( $W$ ) against volume of benzenecetic acid ( $V$ ) treated for 88.3% removal efficiency.

nanoparticles required for the 88.3% removal of benzenecetic acid solution of concentration 4.08 g/L was 4.1, 8.1, 12.1, 16.2, and 20.3 for volumes of 1, 2, 3, 4, and 5 respectively.

#### 4. Conclusion

CaO<sub>2</sub> nanoparticles have been successfully synthesized by a chemical precipitation method. The synthesized CaO<sub>2</sub> nanoparticles were characterized by various analytical techniques such as XRD, HR-FESEM, TEM, and HR-TEM. The present study clearly revealed that synthesized CaO<sub>2</sub> nanoparticles were excellent alternative for removal of benzenecetic acid from aqueous solution. An analysis of the correlation between the predicted results of the designed ANN model and the actual (experimental data) was carried out. The results obtained from the ANN model showed that the values of the coefficient of determination ( $R^2$ ) and root mean square error (RMSE) were found to be 0.989 and 3.432 for benzenecetic acid removal. The Langmuir is the best model for fitting experimental data and it is used for the design of batch adsorption system. At constant percentage, the mass of CaO<sub>2</sub> nanoparticles as adsorbent is achieved for benzenecetic acid removal from aqueous solution. The unique feature of the ANN modeling technique is simple to execute, cost-effective, highly accurate and needs less time.

#### Acknowledgements

We gratefully thank SAIF IIT Bombay for carrying out the TEM facility and SAIF NEHU Shillong for providing the HRTEM facility. We also thank Metallurgical & Materials Engineering Department, VNIT for providing XRD facility.

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