# CP violation in chargino production and decay into sneutrino 

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Received 2 July 2004; received in revised form 21 July 2004; accepted 28 July 2004
Available online 13 August 2004
Editor: G.F. Giudice


#### Abstract

We study CP odd asymmetries in chargino production $e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{ \pm} \tilde{\chi}_{2}^{\mp}$ and the subsequent two-body decay of one chargino into a sneutrino. We show that in the Minimal Supersymmetric Standard Model with complex parameter $\mu$ the asymmetries can reach $30 \%$. We discuss the feasibility of measuring these asymmetries at a linear collider with $\sqrt{s}=800 \mathrm{GeV}$ and longitudinally polarized beams.


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## 1. Introduction

In the chargino sector of the Minimal Supersymmetric Standard Model (MSSM) [1] the higgsino mass parameter $\mu$ can be complex [2]. It has been shown that in the production of two different charginos, $e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{ \pm} \tilde{\chi}_{2}^{\mp}$, a CP violating phase $\varphi_{\mu}$ of $\mu$ causes a non-vanishing chargino polarization perpendicular to the production plane $[3,4]$. This polarization leads at tree level to triple product asymmetries [5-7], which might be large and will allow us to constrain $\varphi_{\mu}$ at a fu-

[^0]ture $e^{+} e^{-}$linear collider [8]. Usually it is claimed that this phase has to be small for a light supersymmetric (SUSY) particle spectrum due to the experimental upper bounds of the electric dipole moments (EDMs) [9]. However, these restrictions are model dependent [10]. If cancellations among different contributions occur and, for example, if lepton flavor violating phases are present, the EDM restrictions on $\varphi_{\mu}$ may disappear [11].

We study chargino production

$$
\begin{equation*}
e^{+}+e^{-} \rightarrow \tilde{\chi}_{i}^{+}+\tilde{\chi}_{j}^{-}, \quad i, j=1,2 \tag{1}
\end{equation*}
$$

with longitudinally polarized beams and the subsequent two-body decay of one of the charginos into a sneutrino
$\tilde{\chi}_{i}^{+} \rightarrow \ell^{+}+\tilde{v}_{\ell}, \quad \ell=e, \mu, \tau$.

We define the triple product
$\mathcal{T}_{\ell}=\left(\mathbf{p}_{e^{-}} \times \mathbf{p}_{\tilde{\chi}_{i}^{+}}\right) \cdot \mathbf{p}_{\ell}$
and the T odd asymmetry
$\mathcal{A}_{\ell}^{\mathrm{T}}=\frac{\sigma\left(\mathcal{T}_{\ell}>0\right)-\sigma\left(\mathcal{T}_{\ell}<0\right)}{\sigma\left(\mathcal{T}_{\ell}>0\right)+\sigma\left(\mathcal{T}_{\ell}<0\right)}$,
of the cross section $\sigma$ for chargino production (1) and decay (2). The asymmetry $\mathcal{A}_{\ell}^{\mathrm{T}}$ is not only sensitive to the phase $\varphi_{\mu}$, but also to absorptive contributions, which could enter via $s$-channel resonances or finalstate interactions. In order to eliminate the contributions from the absorptive parts, which do not signal CP violation, we will study the CP asymmetry
$\mathcal{A}_{\ell}=\frac{1}{2}\left(\mathcal{A}_{\ell}^{\mathrm{T}}-\overline{\mathcal{A}}_{\ell}^{\mathrm{T}}\right)$,
where $\overline{\mathcal{A}}_{\ell}^{\mathrm{T}}$ is the asymmetry for the CP conjugated process $e^{+} e^{-} \rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+} ; \tilde{\chi}_{i}^{-} \rightarrow \ell^{-} \overline{\tilde{v}}_{\ell}$. In this context it is interesting to note that in chargino production it is not possible to construct a triple product and a corresponding asymmetry by using transversely polarized $e^{+}$and $e^{-}$beams [3,12], therefore, one has to rely on the transverse polarization of the produced chargino.

In Section 2 we give our definitions and formalism used, and the analytical formulae for the chargino production and decay cross sections. In Section 3 we discuss some general properties of the CP asymmetries. In Section 4 we present numerical results for $\mathcal{A}_{\ell}$ and the cross sections. Section 5 gives a summary and conclusions.

## 2. Definitions and formalism

### 2.1. Lagrangians and couplings

The MSSM interaction Lagrangians relevant for our study are (in our notation and conventions we follow closely $[1,13])$ :

$$
\begin{align*}
\mathcal{L}_{Z^{0} \ell \bar{\ell}}=- & \frac{g}{\cos \theta_{W}} Z_{\mu} \bar{\ell} \gamma^{\mu}\left[L_{\ell} P_{L}+R_{\ell} P_{R}\right] \ell  \tag{6}\\
\mathcal{L}_{Z^{0} \tilde{\chi}_{j}^{+} \tilde{\chi}_{i}^{-}}= & \frac{g}{\cos \theta_{W}} Z_{\mu} \overline{\tilde{\chi}}_{i}^{+} \gamma^{\mu} \\
& \times\left[O_{i j}^{L L} P_{L}+O_{i j}^{\prime R} P_{R}\right] \tilde{\chi}_{j}^{+}  \tag{7}\\
\mathcal{L}_{\ell \tilde{\nu}_{\ell} \tilde{\chi}_{i}^{+}}= & -g V_{i 1}^{*} \overline{\tilde{\chi}}_{i}^{+C} P_{L} \ell \tilde{v}_{\ell}^{*}+\text { h.c., } \quad \ell=e, \mu  \tag{8}\\
\mathcal{L}_{\tau \tilde{\nu}_{\tau} \tilde{\chi}_{i}^{+}}= & -g \overline{\tilde{\chi}}_{i}^{+C}\left(V_{i 1}^{*} P_{L}-Y_{\tau} U_{i 2} P_{R}\right) \tau \tilde{\nu}_{\tau}^{*}+\text { h.c. } \tag{9}
\end{align*}
$$

with the couplings

$$
\begin{align*}
& L_{\ell}=T_{3 \ell}-e_{\ell} \sin ^{2} \theta_{W}, \quad R_{\ell}=-e_{\ell} \sin ^{2} \theta_{W}  \tag{10}\\
& O_{i j}^{\prime L}=-V_{i 1} V_{j 1}^{*}-\frac{1}{2} V_{i 2} V_{j 2}^{*}+\delta_{i j} \sin ^{2} \theta_{W}  \tag{11}\\
& O_{i j}^{\prime R}=-U_{i 1}^{*} U_{j 1}-\frac{1}{2} U_{i 2}^{*} U_{j 2}+\delta_{i j} \sin ^{2} \theta_{W} \tag{12}
\end{align*}
$$

with $i, j=1,2$. Here $P_{L, R}=\frac{1}{2}\left(1 \mp \gamma_{5}\right), g=e / \sin \theta_{W}$ is the weak coupling constant, and $e_{\ell}$ and $T_{3 \ell}$ denote the charge and the third component of the weak isospin of the lepton $\ell$. The $\tau$-Yukawa coupling is given by $Y_{\tau}=m_{\tau} /\left(\sqrt{2} m_{W} \cos \beta\right)$ with $\tan \beta=v_{2} / v_{1}$, where $v_{1,2}$ are the vacuum expectation values of the two neutral Higgs fields. The chargino mass eigenstates $\tilde{\chi}_{i}^{+}=\binom{x_{i}^{+}}{\bar{\chi}_{i}^{-}}$are defined by $\chi_{i}^{+}=V_{i 1} w^{+}+V_{i 2} h^{+}$ and $\chi_{j}^{-}=U_{j 1} w^{-}+U_{j 2} h^{-}$with $w^{ \pm}$and $h^{ \pm}$the twocomponent spinor fields of the Wino and the charged higgsinos, respectively. The complex unitary $2 \times 2$ matrices $U_{m n}$ and $V_{m n}$ diagonalize the chargino mass ma$\operatorname{trix} X_{\alpha \beta}, U_{m \alpha}^{*} X_{\alpha \beta} V_{\beta n}^{-1}=m_{\tilde{\chi}_{n}^{+}} \delta_{m n}$, with $m_{\tilde{\chi}_{n}^{+}}>0$.

### 2.2. Cross section

We choose a coordinate frame such that in the laboratory system the four-momenta are
$p_{e^{-}}^{\mu}=E_{b}(1,-\sin \theta, 0, \cos \theta)$,
$p_{e^{+}}^{\mu}=E_{b}(1, \sin \theta, 0,-\cos \theta)$,
$p_{\tilde{\chi}_{i}^{+}}^{\mu}=\left(E_{\tilde{\chi}_{i}^{+}}, 0,0,-q\right)$,
$p_{\tilde{\chi}_{j}^{-}}^{\mu}=\left(E_{\tilde{\chi}_{j}^{-}}, 0,0, q\right)$,
with the beam energy $E_{b}=\sqrt{s} / 2$, the scattering angle $\theta L\left(\mathbf{p}_{e^{-}}, \mathbf{p}_{\tilde{\chi}_{j}^{-}}\right)$and the azimuth $\phi$ is chosen zero. For the description of the polarization of chargino $\tilde{\chi}_{i}^{+}$we choose three spin vectors in the laboratory system
$s_{\tilde{\chi}_{i}^{+}}^{1, \mu}=(0,-1,0,0), \quad s_{\tilde{\chi}_{i}^{+}}^{2, \mu}=(0,0,1,0)$,
$s_{\tilde{\chi}_{i}^{+}}^{3, \mu}=\frac{1}{m_{\tilde{\chi}_{i}^{+}}}\left(q, 0,0,-E_{\tilde{\chi}_{i}^{+}}\right)$.
Together with $p_{\tilde{\chi}_{i}^{+}}^{\mu} / m_{\tilde{\chi}_{i}^{+}}$they form an orthonormal set.

For the calculation of the cross section for the combined process of chargino production (1) and the subsequent two-body decay of $\tilde{\chi}_{i}^{+}(2)$, we use the spindensity matrix formalism as in $[13,14]$. The amplitude
squared,

$$
\begin{equation*}
|T|^{2}=\left|\Delta\left(\tilde{x}_{i}^{+}\right)\right|^{2} \sum_{\lambda_{i}, \lambda_{i}^{\prime}} \rho_{P}\left(\tilde{\chi}_{i}^{+}\right)^{\lambda_{i} \lambda_{i}^{\prime}} \rho_{D}\left(\tilde{x}_{i}^{+}\right)_{\lambda_{i}^{\prime} \lambda_{i}} \tag{16}
\end{equation*}
$$

is composed of the (unnormalized) spin-density production matrix $\rho_{P}\left(\tilde{\chi}_{i}^{+}\right)$, the decay matrix $\rho_{D}\left(\tilde{\chi}_{i}^{+}\right)$, with the helicity indices $\lambda_{i}$ and $\lambda_{i}^{\prime}$ of the chargino and the propagator $\Delta\left(\tilde{\chi}_{i}^{+}\right)=i /\left[p_{\tilde{\chi}_{i}^{+}}^{2}-m_{\tilde{\chi}_{i}^{+}}^{2}+i m_{\tilde{\chi}_{i}^{+}} \Gamma_{\tilde{\chi}_{i}^{+}}\right]$. The production matrix $\rho_{P}\left(\tilde{\chi}_{i}^{+}\right)$can be expanded in terms of the Pauli matrices $\sigma^{a}, a=1,2,3$
$\rho_{P}\left(\tilde{\chi}_{i}^{+}\right)^{\lambda_{i} \lambda_{i}^{\prime}}=2\left(\delta_{\lambda_{i} \lambda_{i}^{\prime}} P+\sum_{a} \sigma_{\lambda_{i} \lambda_{i}^{\prime}}^{a} \Sigma_{P}^{a}\right)$.
With our choice of the spin vectors $s_{\tilde{\chi}_{i}^{+}}^{a}(15), \Sigma_{P}^{3} / P$ is the longitudinal polarization of $\tilde{\chi}_{i}^{+}$in the laboratory system, $\Sigma_{P}^{1} / P$ is the transverse polarization in the production plane and $\Sigma_{P}^{2} / P$ is the polarization perpendicular to the production plane. The analytical formulae for the expansion coefficients $P$ and $\Sigma_{P}^{a}$ are given in [13]. The coefficient $\Sigma_{P}^{2}$ is non-zero only for production of an unequal pair of charginos, $e^{+} e^{-} \rightarrow$ $\tilde{\chi}_{1}^{ \pm} \tilde{\chi}_{2}^{\mp}$, and obtains contributions from $Z$-exchange and $Z-\tilde{v}$ interference only [13]:

$$
\begin{equation*}
\Sigma_{P}^{2}=\Sigma_{P}^{2}(Z Z)+\Sigma_{P}^{2}(Z \tilde{v}) \tag{18}
\end{equation*}
$$

with

$$
\begin{align*}
\Sigma_{P}^{2}(Z Z)= & 2 \frac{g^{4}}{\cos ^{4} \theta_{W}}|\Delta(Z)|^{2}\left(c_{R}^{Z Z}-c_{L}^{Z Z}\right) \\
& \times \operatorname{Im}\left\{O_{i j}^{\prime L} O_{i j}^{\prime R *}\right\} E_{b}^{2} m_{\tilde{\chi}_{j}^{-}} q \sin \theta  \tag{19}\\
\Sigma_{P}^{2}(Z \tilde{v})= & \frac{g^{4}}{\cos ^{2} \theta_{W}} c_{L}^{Z \tilde{\nu}} \operatorname{Im}\left\{V_{i 1}^{*} V_{j 1} O_{i j}^{\prime R} \Delta(Z) \Delta(\tilde{v})^{*}\right\} \\
& \times E_{b}^{2} m_{\tilde{\chi}_{j}^{-}} q \sin \theta \tag{20}
\end{align*}
$$

The propagators are defined by
$\Delta(Z)=\frac{i}{p_{Z}^{2}-m_{Z}^{2}+i m_{Z} \Gamma_{Z}}$,
$\Delta(\tilde{v})=\frac{i}{p_{\tilde{v}}^{2}-m_{\tilde{v}}^{2}}$,
and the longitudinal electron and positron beam polarizations, $P_{e^{-}}$and $P_{e^{+}}$, respectively, are included in the coefficients
$c_{L}^{Z Z}=L_{e}^{2}\left(1-P_{e^{-}}\right)\left(1+P_{e^{+}}\right)$,
$c_{R}^{Z Z}=R_{e}^{2}\left(1+P_{e^{-}}\right)\left(1-P_{e^{+}}\right)$,
$c_{L}^{Z \tilde{\nu}}=L_{e}\left(1-P_{e^{-}}\right)\left(1+P_{e^{+}}\right)$.
The contribution (19) from $Z$-exchange is non-zero only for $\varphi_{\mu} \neq 0, \pi$, whereas the $Z-\tilde{v}$ interference term (20), obtains also absorptive contributions due to the finite $Z$-width which do not signal CP violation. These, however, will be eliminated in the asymme$\operatorname{try} \mathcal{A}_{\ell}(5)$.

Analogously to the production matrix, the chargino decay matrix can be written as
$\rho_{D}\left(\tilde{\chi}_{i}^{+}\right)_{\lambda_{i}^{\prime} \lambda_{i}}=\delta_{\lambda_{i}^{\prime} \lambda_{i}} D+\sum_{a} \sigma_{\lambda_{i}^{\prime} \lambda_{i}}^{a} \Sigma_{D}^{a}$.
For the chargino decay (2) into an electron or muon sneutrino the coefficients are

$$
\begin{align*}
& D=\frac{g^{2}}{2}\left|V_{i 1}\right|^{2}\left(m_{\tilde{\chi}_{i}^{+}}^{2}-m_{\tilde{v}_{\ell}}^{2}\right), \\
& \Sigma_{D}^{a}=-g_{(+)}^{2}\left|V_{i 1}\right|^{2} m_{\tilde{\chi}_{i}^{+}}\left(s_{\tilde{\chi}_{i}^{+}}^{a} \cdot p_{\ell}\right), \quad \text { for } \ell=e, \mu, \tag{25}
\end{align*}
$$

where the sign in parenthesis holds for the conjugated process $\tilde{\chi}_{i}^{-} \rightarrow \ell^{-} \overline{\tilde{v}}_{\ell}$. For the decay into the tau sneutrino the coefficients are given by

$$
\begin{align*}
& D=\frac{g^{2}}{2}\left(\left|V_{i 1}\right|^{2}+Y_{\tau}^{2}\left|U_{i 2}\right|^{2}\right)\left(m_{\tilde{\chi}_{i}^{+}}^{2}-m_{\tilde{\nu}_{\tau}}^{2}\right), \\
& \Sigma_{D}^{a}=\underset{(+)}{-} g^{2}\left(\left|V_{i 1}\right|^{2}-Y_{\tau}^{2}\left|U_{i 2}\right|^{2}\right) m_{\tilde{\chi}_{i}^{+}}\left(s_{\tilde{\chi}_{i}^{+}}^{a} \cdot p_{\tau}\right), \tag{26}
\end{align*}
$$

where the sign in parenthesis holds for the conjugated process $\tilde{\chi}_{i}^{-} \rightarrow \tau^{-} \overline{\tilde{v}}_{\tau}$.

Inserting the density matrices (17) and (24) in (16) leads to

$$
\begin{equation*}
|T|^{2}=4\left|\Delta\left(\tilde{\chi}_{i}^{+}\right)\right|^{2}\left(P D+\sum_{a} \Sigma_{P}^{a} \Sigma_{D}^{a}\right) \tag{27}
\end{equation*}
$$

The cross section and distributions in the laboratory system are then obtained by integrating $|T|^{2}$ over the Lorentz invariant phase space element,
$d \sigma=\frac{1}{2 s}|T|^{2} d$ Lips,
where we use the narrow width approximation for the chargino propagator.

## 3. CP asymmetries

Inserting the cross section (28) in the definition of the asymmetry (4) we obtain:

$$
\begin{align*}
\mathcal{A}_{\ell}^{\mathrm{T}} & =\frac{\int \operatorname{Sign}\left[\mathcal{T}_{\ell}\right]|T|^{2} d \mathrm{Lips}}{\int|T|^{2} d \mathrm{Lips}} \\
& =\frac{\int \operatorname{Sign}\left[\mathcal{I}_{\ell}\right] \Sigma_{P}^{2} \Sigma_{D}^{2} d \mathrm{Lips}}{\int P D d \operatorname{Lips}} \tag{29}
\end{align*}
$$

In the numerator only the CP sensitive contribution $\Sigma_{P}^{2} \Sigma_{D}^{2}$ from chargino polarization perpendicular to the production plane remains, since only this term contains the triple product $\mathcal{I}_{\ell}=\left(\mathbf{p}_{e^{-}} \times \mathbf{p}_{\tilde{\chi}_{i}^{+}}\right) \cdot \mathbf{p}_{\ell}$ (3). In the denominator only the term $P D$ remains, since all spin correlations $\sum_{a} \Sigma_{P}^{a} \Sigma_{D}^{a}$ vanish due to the integration over the complete phase space. For chargino decay into a tau sneutrino, $\tilde{\chi}_{i}^{+} \rightarrow \tau^{+} \tilde{\nu}_{\tau}$, the asymmetry $\mathcal{A}_{\tau}^{\mathrm{T}} \propto\left(\left|V_{i 1}\right|^{2}-Y_{\tau}^{2}\left|U_{i 2}\right|^{2}\right) /\left(\left|V_{i 1}\right|^{2}+Y_{\tau}^{2}\left|U_{i 2}\right|^{2}\right)$ is reduced, which follows from the expressions for $D$ and $\Sigma_{D}^{2}$, given in (26).

The relative statistical error of the asymmetry $\mathcal{A}_{\ell}^{\mathrm{T}}$ is $\delta \mathcal{A}_{\ell}^{\mathrm{T}}=\Delta \mathcal{A}_{\ell}^{\mathrm{T}} /\left|\mathcal{A}_{\ell}^{\mathrm{T}}\right|=1 /\left(\left|\mathcal{A}_{\ell}^{\mathrm{T}}\right| \sqrt{N}\right)$, where $N$ is the number of events. For the CP asymmetry $\mathcal{A}_{\ell}$, defined in (5), we have $\Delta \mathcal{A}_{\ell}=\Delta \mathcal{A}_{\ell}^{\mathrm{T}} / \sqrt{2}$. The statistical significance, with which a CP asymmetry can be measured, is then given by $S_{\ell}=\left|\mathcal{A}_{\ell}\right| \sqrt{2 N}$. Note that in order to measure $\mathcal{A}_{\ell}$ in the reaction (1) the momentum of $\tilde{\chi}_{i}^{+}$, i.e., the production plane, has to be determined. This can be done if the corresponding information from the decay of the other chargino $\tilde{\chi}_{j}^{-}$on the opposite side is also available. This is the case if, for example, the $\tilde{\chi}_{j}^{-}$decays like $\tilde{\chi}_{j}^{-} \rightarrow \tilde{\chi}_{1}^{-} Z^{0}, \tilde{\chi}_{j}^{-} \rightarrow \tilde{\chi}_{1}^{0} W^{-}$ or $\tilde{\chi}_{j}^{-} \rightarrow \tilde{\chi}_{1}^{-} H_{1}^{0}$ and $Z, W, H_{1}^{0}$ decay hadronically, $Z^{0} \rightarrow q \bar{q}, W^{-} \rightarrow q \bar{q}^{\prime}, H_{1}^{0} \rightarrow b \bar{b}$. If the masses of the charginos and $\tilde{v}_{\ell}$ as well as the masses of $H_{1}^{0}$ and $\tilde{\chi}_{1}^{0}$ are known, then the momentum $\mathbf{p}_{\chi_{j}^{-}}$can be kinematically reconstructed. This is also possible if the leptonic decays $Z^{0} \rightarrow \ell^{+} \ell^{-}, H_{1}^{0} \rightarrow \tau^{+} \tau^{-}$or $\tilde{\chi}_{j}^{-} \rightarrow \ell^{-} \tilde{\nu}_{\ell}$ are used. In order to predict the expected accuracy of measuring $\mathcal{A}_{\ell}$, it is clear that also detailed Monte Carlo studies taking into account background and detector simulations are necessary. However, this is beyond the scope of the present work.

## 4. Numerical results

We present numerical results for the asymmetries $\mathcal{A}_{\ell}$ (5), for $\ell=e, \mu$ and the cross sections $\sigma=$ $\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \times \operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}\right)$. We study the dependence of the asymmetries and cross sections on the MSSM parameters $\mu=|\mu| e^{i \varphi_{\mu}}, M_{2}$ and $\tan \beta$. We choose a center of mass energy of $\sqrt{s}=800 \mathrm{GeV}$ and longitudinally polarized beams with beam polarizations $\left(P_{e^{-}}, P_{e^{+}}\right)=(-0.8,+0.6)$, which enhance $\tilde{v}_{e}$ exchange in the production process. This results in larger cross sections and asymmetries.

We study the decays of the lighter chargino $\tilde{\chi}_{1}^{+}$. For the calculation of the chargino widths $\Gamma_{\tilde{\chi}_{1}^{+}}$and the branching ratios $\operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{\nu}_{\ell}\right)$ we include the following two-body decays,

$$
\begin{gather*}
\tilde{\chi}_{1}^{+} \rightarrow W^{+} \tilde{\chi}_{n}^{0}, e^{+} \tilde{v}_{e}, \mu^{+} \tilde{v}_{\mu}, \tau^{+} \tilde{v}_{\tau}, \tilde{e}_{L}^{+} v_{e} \\
\tilde{\mu}_{L}^{+} v_{\mu}, \tilde{\tau}_{1,2}^{+} v_{\tau} \tag{30}
\end{gather*}
$$

and neglect three-body decays. The Higgs parameter is chosen $m_{A}=1 \mathrm{TeV}$ and thus the decays into the charged Higgs bosons $\tilde{\chi}_{i}^{ \pm} \rightarrow H^{ \pm} \tilde{\chi}_{n}^{0}$ are forbidden in our scenarios. In order to reduce the number of parameters, we assume the relation $\left|M_{1}\right|=$ $5 / 3 M_{2} \tan ^{2} \theta_{W}$. For all scenarios we fix the sneutrino and slepton masses, $m_{\tilde{v}_{\ell}}=185 \mathrm{GeV}, \ell=e, \mu, \tau$, $m_{\tilde{\ell}_{L}}=200 \mathrm{GeV}, \ell=e, \mu$. These values are obtained from the renormalization group equations [15], $m_{\tilde{\ell}_{L}}^{2}=m_{0}^{2}+0.79 M_{2}^{2}+m_{Z}^{2} \cos 2 \beta\left(-1 / 2+\sin ^{2} \theta_{W}\right)$ and $m_{\tilde{v}_{\ell}}^{2}=m_{0}^{2}+0.79 M_{2}^{2}+m_{Z}^{2} / 2 \cos 2 \beta$, for $M_{2}=$ $200 \mathrm{GeV}, m_{0}=80 \mathrm{GeV}$ and $\tan \beta=5$. In the stau sector [16] we fix the trilinear scalar coupling parameter to $A_{\tau}=250 \mathrm{GeV}$. The stau masses are fixed to $m_{\tilde{\tau}_{1}}=129 \mathrm{GeV}$ and $m_{\tilde{\tau}_{2}}=202 \mathrm{GeV}$.

In Fig. 1(a) we show the contour lines of the cross section for chargino production and decay $\sigma=$ $\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \times \mathrm{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{\nu}_{\ell}\right) \times \mathrm{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow\right.$ $\tilde{\chi}_{1}^{-}$or $\tilde{\chi}_{1}^{0}+$ had. $)$ in the $M_{2}-\varphi_{\mu}$ plane for $|\mu|=$ 400 GeV and $\tan \beta=5$. We calculate the $\tilde{\chi}_{2}^{-}$branching ratio as $\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $)=\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow\right.$ $\left.\tilde{\chi}_{1}^{-} Z^{0}\right) \operatorname{BR}\left(Z^{0} \rightarrow q \bar{q}\right)+\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{0} W^{-}\right) \times$ $\operatorname{BR}\left(W^{-} \rightarrow q \bar{q}^{\prime}\right)+\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-} H_{1}^{0}\right) \operatorname{BR}\left(H_{1}^{0} \rightarrow\right.$ $b \bar{b})$ with $\operatorname{BR}\left(Z^{0} \rightarrow q \bar{q}\right) \approx \operatorname{BR}\left(W^{+} \rightarrow q \bar{q}^{\prime}\right) \approx 0.7$, $\operatorname{BR}\left(H_{1}^{0} \rightarrow b \bar{b}\right) \approx 0.85$, which gives a lower bound on the total hadronic $\tilde{\chi}_{2}^{-}$branching ratio. The production cross section $\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right)$can attain values


Fig. 1. Contour lines of $\sigma=\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{x}_{2}^{-}\right) \times \operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}\right) \times \mathrm{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $)$, summed over $\ell=e, \mu$ (a), and the asymmetry $\mathcal{A}_{\ell}$ for $\ell=e$ or $\mu(\mathrm{b})$, in the $M_{2}-\varphi_{\mu}$ plane for $|\mu|=400 \mathrm{GeV}, \tan \beta=5, m_{\tilde{v}_{\ell}}=185 \mathrm{GeV}, \sqrt{s}=800 \mathrm{GeV}$ and $\left(P_{e^{-}}, P_{e^{+}}\right)=(-0.8,0.6)$. The gray area is excluded by $m_{\tilde{\chi}_{1}^{ \pm}}<104 \mathrm{GeV}$. The area A is kinematically forbidden by $m_{\tilde{v}_{\ell}}+m_{\tilde{\chi}_{1}^{0}}>m_{\tilde{\chi}_{1}^{+}}$. The area B is kinematically forbidden by $m_{\tilde{\chi}_{1}^{+}}+m_{\tilde{\chi}_{2}^{-}}>\sqrt{s}$.
from 10 fb to 150 fb and $\operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}\right)$, summed over $\ell=e, \mu$, can be as large as $50 \%$. The branching ratio of $\tilde{\chi}_{2}^{-}$decays $\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $)$ is of the order of $60 \%(25 \%)$ for $M_{2} \approx 200 \mathrm{GeV}$ ( 350 GeV ). The cross section $\sigma$ plotted in Fig. 1(a) is in fact a conservative lower bound on that cross section which effectively enters in the determination of $\mathcal{A}_{\ell}$. It may be higher if also the leptonic decays $\tilde{\chi}_{2}^{-} \rightarrow \ell^{-} \tilde{v}_{\ell}$ etc. are taken into account. Note that the cross section is very sensitive to $\varphi_{\mu}$, which has been exploited in [3,4] to constrain $\cos \left(\varphi_{\mu}\right)$.

The $M_{2}-\varphi_{\mu}$ dependence of the CP asymmetry $\mathcal{A}_{\ell}$ for $\ell=e$ or $\mu$ is shown in Fig. 1(b). The asymmetry can be as large as $10 \%$ and it does, however, not attain maximal values for $\varphi_{\mu}=0.5 \pi$, which one would naively expect. The reason is that $\mathcal{A}_{\ell}$ is proportional to a product of a CP odd ( $\Sigma_{P}^{2}$ ) and a CP even factor ( $\Sigma_{D}^{2}$ ), see (29). The CP odd (CP even) factor has as sine-like (cosine-like) dependence on $\varphi_{\mu}$. Thus the maximum of $\mathcal{A}_{\ell}$ is shifted towards $\varphi_{\mu}= \pm \pi$ in Fig. 1(b). Phases close to the CP conserving points, $\varphi_{\mu}=0, \pm \pi$, are favored by the experimental upper limits on the EDMs. For example, in the constrained MSSM, we have $\left|\varphi_{\mu}\right| \lesssim \pi / 10$ [9]. However, the re-
strictions are very model dependent, e.g., if also lepton flavor violating terms are included [11], the restrictions may disappear. In order to show the full phase dependence of the asymmetries, we have relaxed the EDM restrictions for this purpose.

For $M_{2}=200 \mathrm{GeV}$, we show the $\tan \beta-\varphi_{\mu}$ dependence of $\sigma$ and $\mathcal{A}_{\ell}$ in Figs. 2(a), (b). The asymmetry can reach values up to $30 \%$ and shows a strong $\tan \beta$ dependence and decreases with increasing $\tan \beta$. The feasibility of measuring the asymmetry depends also on the cross section $\sigma=\sigma_{P}\left(e^{+} e^{-} \rightarrow\right.$ $\left.\tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \times \operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}\right) \times \operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had.), Fig. 2(a), which attains values up to 15 fb and $\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $) \approx 55-65 \%$.

For the phase $\varphi_{\mu}=0.9 \pi$ and $\tan \beta=5$, we study the beam polarization dependence of $\mathcal{A}_{\ell}$, which can be strong as shown in Fig. 3(a). An electron beam polarization $P_{e^{-}}>0$ and a positron beam polarization $P_{e^{+}}<0$ enhance the channels with $\tilde{v}_{e}$ exchange in the chargino production process. For, e.g., $\left(P_{e^{-}}, P_{e^{+}}\right)=(-0.8,0.6)$ the asymmetry can attain $-7 \%$, Fig. 3(a), with $\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \approx 10 \mathrm{fb}$ and $\operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{\nu}_{\ell}\right) \approx 50 \%$, summed over $\ell=e, \mu$. The cross section $\sigma=\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \times \operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow\right.$


Fig. 2. Contour lines of $\sigma=\sigma_{P}\left(e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}\right) \times \operatorname{BR}\left(\tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}\right) \times \mathrm{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $)$, summed over $\ell=e, \mu$, (a), and the asymmetry $\mathcal{A}_{\ell}$ for $\ell=e$ or $\mu(\mathrm{b})$, in the $\tan \beta-\varphi_{\mu}$ plane for $M_{2}=200 \mathrm{GeV},|\mu|=400 \mathrm{GeV}, m_{\tilde{\nu}_{\ell}}=185 \mathrm{GeV}, \sqrt{s}=800 \mathrm{GeV}$ and $\left(P_{e^{-}}, P_{e^{+}}\right)=(-0.8,0.6)$. The area A is kinematically forbidden by $m_{\tilde{v}_{\ell}}+m_{\tilde{\chi}_{1}^{0}}>m_{\tilde{\chi}_{1}^{+}}$.


Fig. 3. Contour lines of the asymmetry $\mathcal{A}_{\ell}$ for $\ell=e$ or $\mu$ (a), and the significance $S_{\ell}$ (b), for $e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-} ; \tilde{\chi}_{1}^{+} \rightarrow \ell^{+} \tilde{v}_{\ell}$; $\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}$or $\tilde{\chi}_{1}^{0}+$ had., in the $\left(P_{e^{-}} P_{e^{+}}\right)$-plane for $\varphi_{\mu}=0.9 \pi$, taking $|\mu|=400 \mathrm{GeV}, M_{2}=200 \mathrm{GeV}, \tan \beta=5, m_{\tilde{v}_{\ell}}=185 \mathrm{GeV}$, $\sqrt{s}=800 \mathrm{GeV}$ and $\mathcal{L}=500 \mathrm{fb}^{-1}$.
$\left.\ell^{+} \tilde{v}_{\ell}\right) \times \operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow \tilde{\chi}_{1}^{-}\right.$or $\tilde{\chi}_{1}^{0}+$ had. $)$ with $\operatorname{BR}\left(\tilde{\chi}_{2}^{-} \rightarrow\right.$ $\tilde{\chi}_{1}^{-}$or $\tilde{\chi}_{1}^{0}+$ had. $)=60 \%$ ranges between 1.4 fb for $\left(P_{e^{-}}, P_{e^{+}}\right)=(0,0)$ and 4.1 fb for $\left(P_{e^{-}}, P_{e^{+}}\right)=$ $(-1,1)$. The statistical significance $S_{\ell}=\left|\mathcal{A}_{\ell}\right| \sqrt{2 \mathcal{L} \cdot \sigma}$ is shown in Fig. 3(b) for $\mathcal{L}=500 \mathrm{fb}^{-1}$. We have $S_{\ell} \approx 4$ for $\left(P_{e^{-}}, P_{e^{+}}\right)=(-0.8,0.6)$, and thus $\mathcal{A}_{\ell}$ could be accessible at a linear collider, even for $\varphi_{\mu}=$ $0.9 \pi$, by using polarized beams.

## 5. Summary and conclusions

We have studied CP violation in chargino production with longitudinally polarized beams, $e^{+} e^{-} \rightarrow$ $\tilde{\chi}_{i}^{+} \tilde{\chi}_{j}^{-}$, and subsequent two-body decay of one chargino into the sneutrino $\tilde{\chi}_{i}^{+} \rightarrow \ell^{+} \tilde{\nu}_{\ell}$. We have defined the T odd asymmetries $\mathcal{A}_{\ell}^{\mathrm{T}}$ of the triple product $\left(\mathbf{p}_{e^{-}} \times\right.$ $\mathbf{p}_{\tilde{\chi}_{i}^{+}} \cdot \mathbf{p}_{\ell}$. The CP odd asymmetries $\mathcal{A}_{\ell}=\frac{1}{2}\left(\mathcal{A}_{\ell}^{\mathrm{T}}-\overline{\mathcal{A}}_{\ell}^{\mathrm{T}}\right)$, where $\overline{\mathcal{A}}_{\ell}^{\mathrm{T}}$ denote the CP conjugated of $\mathcal{A}_{\ell}^{\mathrm{T}}$, are sensitive to the phase $\varphi_{\mu}$ of the higgsino mass parameter $\mu$. At tree level, the asymmetries have large CP sensitive contributions from spin correlation effects in the production of an unequal pair of charginos. In a numerical discussion for $e^{+} e^{-} \rightarrow \tilde{\chi}_{1}^{+} \tilde{\chi}_{2}^{-}$production, we have found that $\mathcal{A}_{\ell}$ for $\ell=e$ or $\mu$ can attain values up to $30 \%$. By analyzing the statistical errors, we have shown that, even for, e.g., $\varphi_{\mu} \approx 0.9 \pi$, the asymmetries could be accessible in future $e^{+} e^{-}$collider experiments in the 800 GeV range with high luminosity and longitudinally polarized beams.

## Acknowledgements

This work was supported by the 'Deutsche Forschungsgemeinschaft' (DFG) under contract Fr 1064/5-2, by the 'Fonds zur Förderung der Wissenschaftlichen Forschung' (FWF) of Austria, project No. P16592-N02, and by the European Community's Human Potential Programme under contract HPRN-CT-2000-00149.
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