

3D Trajectories Adopted by Coding and Regulatory DNA Elements: First-Passage Times for Genomic Interactions

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SUMMARY

During B lymphocyte development, immunoglobulin heavy-chain variable (V_H), diversity (D_H), and joining (J_H) segments assemble to generate a diverse antigen receptor repertoire. Here, we have marked the distal V_H and D_H - J_H - E_μ regions with Tet-operator binding sites and traced their 3D trajectories in pro-B cells transduced with a retrovirus encoding Tet-repressor-EGFP. We found that these elements displayed fractional Langevin motion (fLm) due to the viscoelastic hindrance from the surrounding network of proteins and chromatin fibers. Using fractional Langevin dynamics modeling, we found that, with high probability, D_H J_H elements reach a V_H element within minutes. Spatial confinement emerged as the dominant parameter that determined the frequency of such encounters. We propose that the viscoelastic nature of the nuclear environment causes coding elements and regulatory elements to bounce back and forth in a spring-like fashion until specific genomic interactions are established and that spatial confinement of topological domains largely controls first-passage times for genomic interactions.

INTRODUCTION

It is now established that chromosomes fold into territories that rarely intermingle (Rabl, 1885; Boveri, 1909; Bolzer et al., 2005). Chromosome territories display a confined geometry revealed by the presence of chromosome arms and bands (Sedat and Manuelidis, 1978). By comparing experimentally obtained spatial distance distributions to spatial distances derived from computer simulations of various chromatin configurations, it was predicted that the mammalian genome is organized as bundles of loops that fold into distinct domains (Münkel and Langowski, 1998; Jhunjunwala et al., 2008). Chromosome-conformation-capture approaches have validated these findings at a global scale, revealing that mammalian genomes fold into clusters of loops that assemble into topological domains (Lieberman-Aiden et al., 2009; Dixon et al., 2012; Lin et al., 2012). On

average, these domains span genomic distances comparable to the size of the immunoglobulin heavy-chain (Igh) locus (1–3 Mbp) (Dixon et al., 2012; Jhunjunwala et al., 2008).

Antigen receptor assembly in lymphocytes occurs by the random rearrangement of variable (V_H), diversity (D_H), joining (J_H), and constant (C_H) coding elements of the Igh locus (Jung et al., 2006). Antigen receptor genes in pro-B cells undergo ordered rearrangement with D_H J_H joining preceding V_H to D_H J_H rearrangement (Alt et al., 1984). Recombinase activating genes 1 and 2 (RAG-1/2) regulate this process. Collectively, the V_H regions span a genomic distance of ~ 2.5 Mbp and fall into two distinct domains, distal and proximal V_H clusters. The D_H and J_H elements then span a genomic distance of 50 kb and are positioned immediately upstream (~ 1 kb) of the intronic enhancer (E_μ). Finally, constant regions downstream of the J_H elements encode the Igh isotypes (Shimizu et al., 1982; Retter et al., 2007). Given the configuration of the Igh locus and distance between V_H , D_H , and J_H genomic segments, contraction brings otherwise distant genomic neighbors into close proximity for efficient gene rearrangement.

Productive V(D)J gene rearrangement in developing B cells permits surface expression of a pre-B cell receptor (pre-BCR). Signaling through the pre-BCR suppresses RAG-1/2 activity, halting continued rearrangement (Nussenzweig et al., 1988; Manz et al., 1988; Grawunder et al., 1995). Various mechanisms, including DNA methylation, chromatin remodeling, histone acetylation, germline transcription, and transcription elongation, control the temporal and lineage specificity of V(D)J rearrangement (Jung et al., 2006; Cedar and Bergman, 2011).

During developmental progression, the Igh locus undergoes large-scale topological changes (Kosak et al., 2002; Fuxa et al., 2004; Hewitt et al., 2010; Guo et al., 2011a). In progenitor cells, the Igh alleles are sequestered at the transcriptionally repressive nuclear lamina (Kosak et al., 2002). As progenitors enter the pre-pro-B cell stage, the locus is released from the lamina to associate with recombination and/or transcription factories. Committed pro-B cells undergo large-scale conformational changes in which distinct classes of anchors merge the distal and proximal V_H regions into one cloud of V_H regions (Jhunjunwala et al., 2008; Medvedovic et al., 2013). The majority of the proximal V_H regions are located within close genomic proximity to the chromatin anchor CCCTC-binding factor (CTCF) sites (Degner et al., 2009). It has been proposed that

CTCF positions the proximal V_H regions at the base of loops that orbit the D_HJ_H elements (Lucas et al., 2011). In addition, an insulator element that regulates Igh locus rearrangement has been identified (Guo et al., 2011b; Degner et al., 2011). The insulator element contains two CTCF binding sites, together named CBE (CTCF-binding elements). Deletion of the CBE leads to loss of ordered and lineage-specific Igh locus rearrangement involving the most proximal, but not distally located, V_H regions (Guo et al., 2011b). The exact mechanism through which the CBE regulates proximal V_H - D_HJ_H joining remains to be elucidated.

Here, we describe the 3D trajectories adopted by the Igh locus segments. We found that the trajectories adopted by V_H and D_HJ_H elements displayed fractional Langevin motion due to the viscoelastic hindrance from the surrounding network of proteins and chromatin fibers, including the neighboring segments of the chromatin fiber. Using fractional Langevin dynamics modeling, we determined first-encounter times, known as first-passage times, for V_H and D_HJ_H elements and found that V_H and D_HJ_H elements have a high probability of reaching each other within minutes. We found that spatial confinement imposed by chromosomal domains is the dominant factor that determines the encounter times for coding and regulatory DNA elements. Based on these observations, we propose that fLm motion causes coding (V_H , D_H , and J_H), regulatory elements (enhancers and promoters), and double-stranded DNA breaks to bounce back and forth in a spring-like fashion until specific genomic interactions are established. Finally, we suggest that spatial confinement of chromosomal domains largely controls the encounter times of long-range genomic interactions, including those involved in V_H D_HJ_H rearrangement, locus contraction, class switch recombination, and DNA repair, as well as chromosomal deletions in cancers.

RESULTS

Inserting Tet-Operator Binding Sites Adjacent to V_H and D_HJ_H Gene Segments

The immunoglobulin locus is structured into distinct domains comprised of distal V_H , proximal V_H , and the D_HJ_H regions. The V_H regions are associated with promoters, whereas the D_HJ_H elements are located within close genomic proximity of the E_μ enhancer. To address how V_H regions differ from D_HJ_H elements in terms of chromatin motion, we inserted arrays of Tet-operator binding sites into the V_H domains. Specifically, an array was inserted in the center of the distal V_H region cluster, immediately downstream of V8-3 (Figure 1A). A second array of either Tet-operator binding sites or Lac-operator binding sites was inserted between the D_HJ_H elements and the E_μ enhancer (Figures 1A and S1A available online). This region consists of a series of simple repeats involved in class switch recombination. Deletion of this genomic region diminishes class switch recombination (CSR) but does not interfere with V(D)J recombination (Luby et al., 2001).

Each construct was inserted into the embryonic stem (ES) cell genome. Briefly, ES cells were transfected with a vector in which the Tet-operator binding sites were inserted adjacent to the V_H or D_HJ_H regions. Genomic DNA was isolated from transfected ES

cells, and clones were examined for insertion into the Igh locus (Figure 1B). ES cells carrying the insertions adjacent to the V_H and D_HJ_H regions were used to generate chimeric mice. Mice carrying insertions in the distal V_H and D_HJ_H regions readily went germline, establishing two lines of mice that either carry Tet-operator binding sites inserted into the V_H or, alternatively, the D_HJ_H regions (Figure 1C). However, mice carrying arrays of Lac-operator binding sites failed to go germline (Figures S1B and S1C). Upon further inspection, we found that ES cells carrying Lac-operator binding sites display a large degree of chromosomal instability, possibly reflecting the inability of mice that carry Lac-operator binding sites in the genome to undergo germline transmission (Figure S1D). In sum, we generated mice that carry tandem arrays of Tet-operator sites either within the V_H cluster or in close genomic proximity to the D_HJ_H region.

Characterization of Mice Carrying Arrays of Tet-Operator Binding Sites Inserted into the Igh Locus

To ensure that the insertion of arrays of TetO binding sites into the Igh locus did not interfere with B cell development, we analyzed the B lineage compartment in wild-type and mutant TetO mice. Bone marrow cells derived from 6-week-old mice were isolated, analyzed for cellularity, and stained for the expression of CD19 and B220 using flow cytometry. Mice containing Tet-operator binding sites inserted adjacent to either the D_HJ_H segments or the distal V_H segments displayed similar numbers of CD19 and B220 double-positive cells as compared to wild-type mice (Figure 2A). Furthermore, the proportions of pro-B versus pre-B cells were similar in the TetO mice as compared to wild-type mice (Figure 2B). These data indicate that insertion of arrays of Tet-operator binding sites at these locations did not interfere with normal production of developing B cells.

To determine whether B lineage cells carrying insertions of arrays of TetO binding sites in the Igh locus undergo efficient V(D)J recombination, DNA was isolated from pro-B cells derived from wild-type, D_HJ_H -TetO, and V_H -TetO region mice, as well as recombination-activating gene (RAG)-deficient mice. D_HJ_H joints were readily detectable at equal levels in wild-type, D_HJ_H -TetO, and V_H -TetO, but not in control RAG-deficient pro-B cells (Figure 2C). Similarly, the abundance of $V_H D_HJ_H$ joints involving the distal V_H J558 cluster was not affected by the insertion of TetO sites (Figure 2C). In sum, these data indicate that insertion of arrays of Tet-operator binding sites does not affect the developmental progression of early B cell progenitors and Igh locus rearrangements.

Generation of TetR-EGFP Expression Vectors

Previous studies have utilized TetR-EYFP fusion proteins to track DNA motion in bacteria (Lau et al., 2003). Our initial attempts to detect TetR-EYFP mediated fluorescence in pro-B cells failed, plausibly caused by differences in codon usage in bacterial versus mammalian cells. However, a Tet repressor optimized for mammalian codon usage has been utilized in studies to allow for tightly regulated control of gene expression (Urlinger et al., 2000). Hence, we fused the DNA-binding domain of the modified Tet repressor to enhanced green fluorescent protein (EGFP) (TetR-EGFP), along with a nuclear localization signal (PKKKRKV).

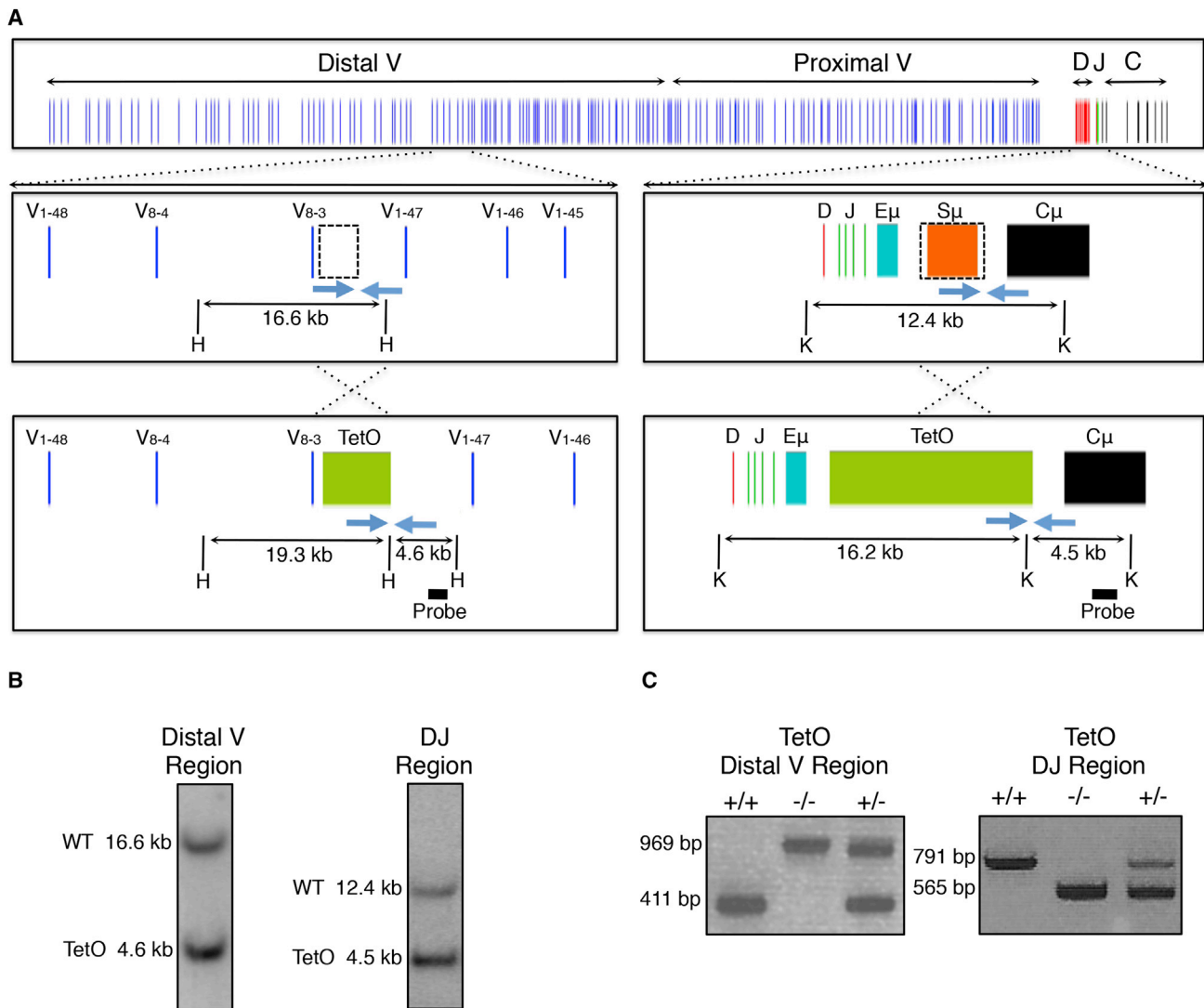


Figure 1. Generation of Igh-TetO-Labeled Mice

(A) Schematic of the Igh locus showing V_H, D_H, J_H, and C_H segments, the intronic enhancer (E μ), and switch region repeats (S μ). Dashed boxes show genomic regions that were replaced by arrays containing 240 copies of the Tet operator. Southern blot screening strategies are indicated using HindIII (H) or KpnI (K) restriction enzymes. Blue arrows show positions of genotyping primers.

(B) Southern blot of embryonic stem cell clones positive for integration of the TetO arrays positioned adjacent to either the V_H or D_HJ_H region of the Igh locus.

(C) PCR-based genotyping results of mice harboring TetO arrays on both (+/+), one (+/-), or neither (-/-) alleles of the Igh locus.

See also [Figure S1](#) and [Table S3](#).

To optimize the signal-to-noise ratio of TetR-EGFP-mediated fluorescence when bound to DNA, we generated and tested multiple vectors. We modified expression levels using three distinct strategies: (1) different promoters were inserted upstream of the TetR-EGFP fusion protein; (2) TetR-EGFP expression was initiated from an internal ribosomal entry site (IRES) rather than directly from a promoter; (3) and the Kozak sequence located upstream of the translation initiation site was mutated to dampen expression levels ([Figure 3A](#)). B lineage cells were transduced with virus expressing TetR-EGFP driven from either the PGK promoter (MinV and LMP vectors) or the Gag promoter (PCS Ret vector) and containing either

wild-type or mutated forms of the Kozak sequence ([Figure 3A](#)). Cells were examined for TetR-EGFP expression using flow cytometry 2 days posttransduction ([Figure 3B](#)). Relatively low but detectable levels of TetR-EGFP expression were achieved using the MinV vector, as well as the LMP vector carrying a mutant Kozak sequence, resulting in optimal signal-to-noise ratios of TetR-EGFP-mediated fluorescence upon binding to the Tet operator sites ([Figure 3C](#)). The LMP construct containing the mutant Kozak sequence displayed a more uniform pattern of TetR-EGFP expression; thus, we utilized this vector for subsequent monitoring of V_H and D_HJ_H motion in pro-B cells.

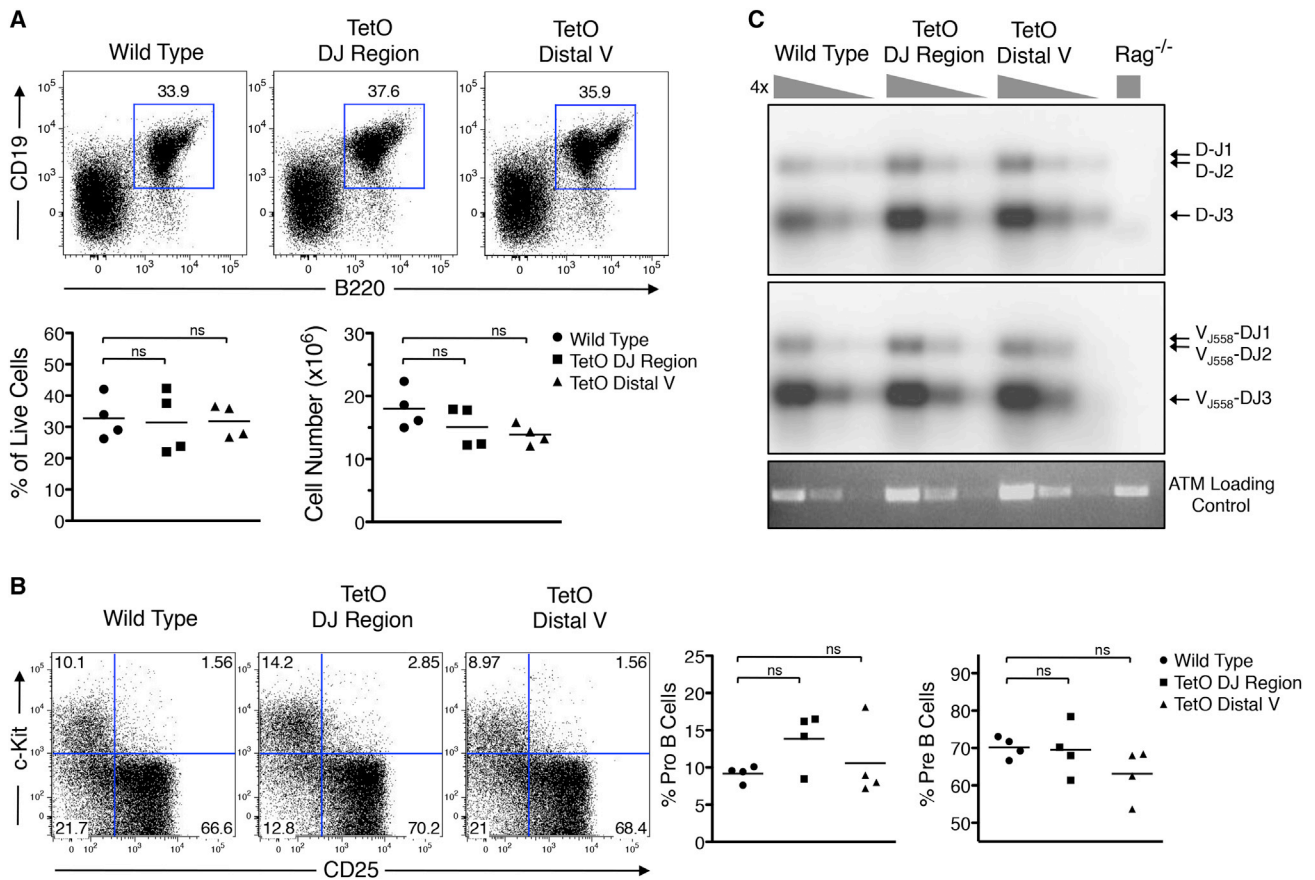


Figure 2. Characterization of Igh-TetO-Labeled Mice

(A) Femoral bone marrow cells from wild-type, D_HJ_H-TetO, and V_H-TetO mice stained with B cell markers CD19 and B220. Bottom shows CD19⁺B220⁺ cell numbers as a fraction of live cells.

(B) Bone marrow cells stained for CD25 and C-kit. The lineage negative (CD11b, Gr1, and Ter119) and B220⁺CD19⁺ population is shown.

(C) D_H-J_H and V_HJ₅₅₈-D_HJ_H rearrangements in B220⁺ cells isolated from wild-type, D_HJ_H-TetO, V_H-TetO, and Rag^{-/-} mice analyzed by Southern blotting using probes corresponding to V_H and D_HJ_H gene segments.

See also Table S3.

Tracking Igh Locus Motion in B Lineage Cells

To describe the trajectories adopted by Igh regions in physical terms, we generated strains of mice carrying TetO binding sites on both alleles. B220-positive pro-B cells from the bone marrow of V_H-TetO and D_HJ_H-TetO mice were cultured in the presence of IL7 and SCF for 5 days and transduced with virus expressing TetR-EGFP. TetO pro-B cells were immobilized by adherence onto poly-lysine-coated optical bottom dishes and imaged 2 days posttransduction (Figure 3C and Movies S1 and S2). One set of z stacks was acquired every 2 s for 400 s (200 time points) or every 40 s for 4,000 s (100 time points). The centers of mass of the TetO signals were determined for each time point. As a control to account for error due to cell motion, TetO pro-B cells were fixed with formaldehyde to prevent motion and labeled with Alexa-488-conjugated anti-GFP antibodies prior to imaging.

Despite attachment of cells with poly-lysine, a significant amount of cell motion, primarily cell or nuclear rotation, was observed (data not shown). To eliminate the effect of such motion in the analysis of loci trajectories, the mean squared

displacement (MSD) was determined by measuring the mean squared change in distance separating the two alleles divided by two, rather than the change in the displacement of each allele. Measured this way, the radial MSD described motion in radial direction (distance between two alleles) only, thus eliminating confounding effects of cell movement and rotation (Vazquez et al., 2001; Cabal et al., 2006). As expected, the radial MSD values varied within the developing pro-B cell population, reflecting differences in cell cycle, cell size, and other intrinsic variations within the population (Figure 4B). We note that, during imaging in a subset of cells, we observed substantial changes in nuclear shape that resulted in large-scale movements of chromosomes and contribute to the displacement of the Igh locus gene segments. The average radial MSD of pro-B cells for both the V_H-TetO and D_HJ_H-TetO alleles were plotted as a function of the time interval τ for the values of τ between 2 and 2,000 s (Figure 4C). As expected, Igh alleles in fixed cells did not show significant spatial displacement (Figure 4C). Anomalous diffusion coefficients (D) and scaling exponents (α) were extracted (radial

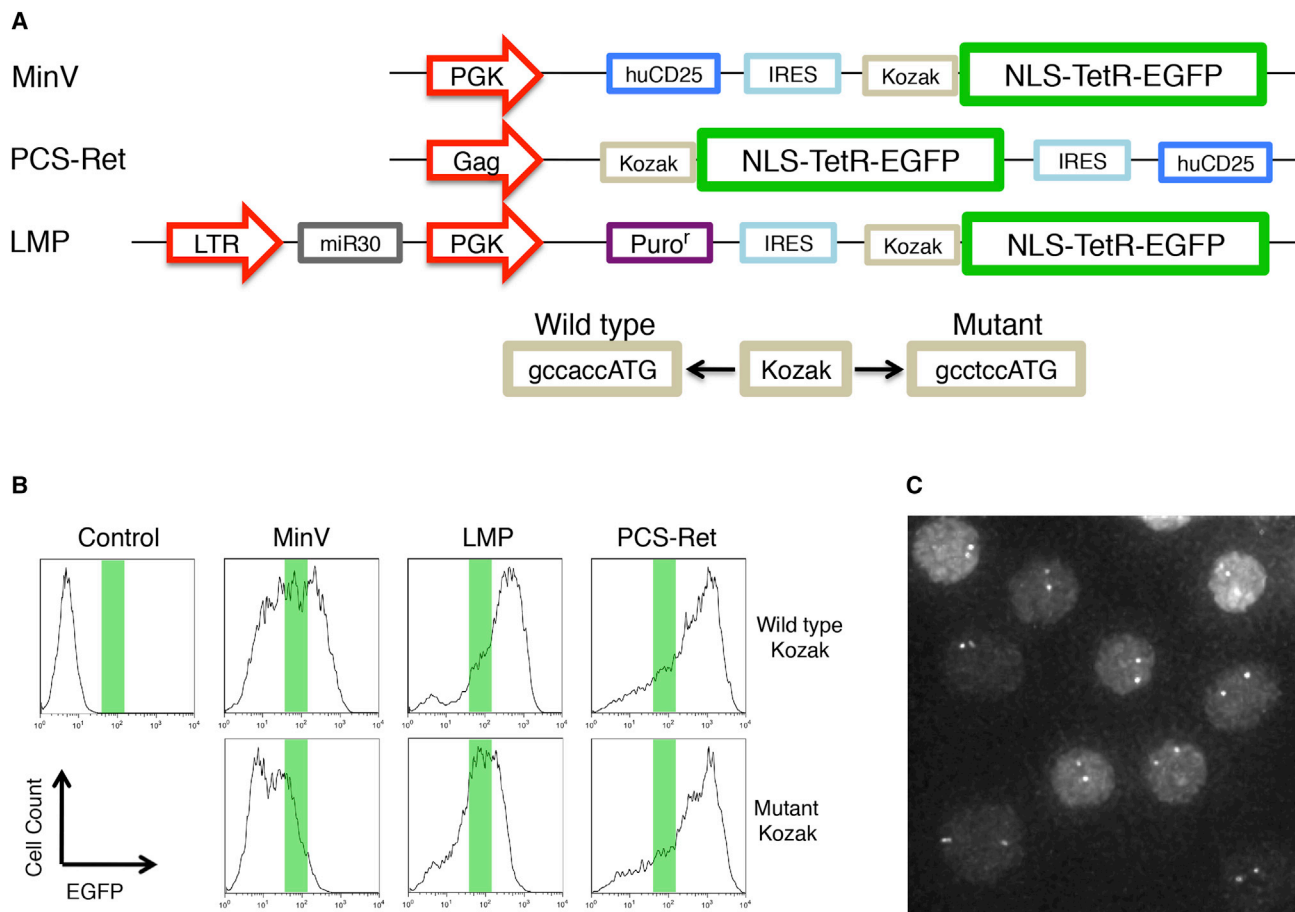


Figure 3. Generation and Optimization of TetR-EGFP Expression

(A) Construction of TetR-EGFP-expressing retroviral vectors. The NLS-TetR-EGFP coding sequence was cloned into three distinct retroviral vectors, MinV, PCS-Ret, and LMP. PGK or Gag promoters were used to drive EGFP expression in each of the vectors. Each construct was made using either a wild-type or mutant Kozak sequence. In the MinV and LMP vectors, the NLS-TetR-EGFP was inserted 3' of an IRES.

(B) D_HJ_H-TetO B lineage cells were infected with NLS-TetR-EGFP-expressing retrovirus, and expression levels were monitored using flow cytometry. Green bars show approximate expression levels leading to high signal to noise ratios of TetO-EGFP-mediated fluorescence.

(C) D_HJ_H-TetO B lineage cells infected with NLS-TetR-EGFP in LMP with a mutant Kozak sequence and visualized by fluorescence microscopy. The dots in each cell show both IgH alleles.

See also [Movies S1](#) and [S2](#).

MSD = 2Dτ^α) for time intervals between 10 and 100 and 40 and 200 s (Figure 4C and Table S1). For wild-type TetO pro-B cells (40–200 s), we found that V_H-TetO motion was characterized by an anomalous diffusion coefficient (D) of 2.0 × 10⁻³ μm²/s^{0.5} and a subdiffusive (i.e., less than unity) scaling exponent (α) of 0.49. For D_HJ_H-TetO motion, we found an anomalous diffusion coefficient of 2.4 × 10⁻³ μm²/s^{0.5} and subdiffusive scaling exponent of 0.52 (Table S1). These data indicate that both V_H and D_HJ_H elements in pro-B cells undergo subdiffusive motion with very similar anomalous diffusion coefficients and subdiffusive scaling exponents.

V_H, D_HJ_H, and Enhancer Elements Display Fractional Langevin Motion

The observations described above show that the trajectories adopted by V_H- and D_HJ_H-TetO segments are associated with

an anomalous diffusive motion. Specifically, the segments are shown to undergo subdiffusion, a process characterized by a nonlinear relationship between the MSD and the elapsed time (MSD = 2Dτ^α with α < 1), in contrast to normal diffusion in which this relationship is linear (i.e., α = 1). What is the underlying mechanism of the observed subdiffusive motion? In the crowded cellular environment, several possible molecular mechanisms may give rise to subdiffusive motion of a chromosomal segment (or any microscopic particle). First, when the diffusive motion of the particle is interspersed by pauses due to the encounters with binding partners, a broad distribution of pausing times makes the particle's motion subdiffusive, as described by the continuous time random walk (CTRW) model (Saxton, 1996; Montroll and Weiss, 1965). Second, when the particle encounters obstacles present at high concentration, the particle's motion becomes subdiffusive, as described by the obstructed diffusion

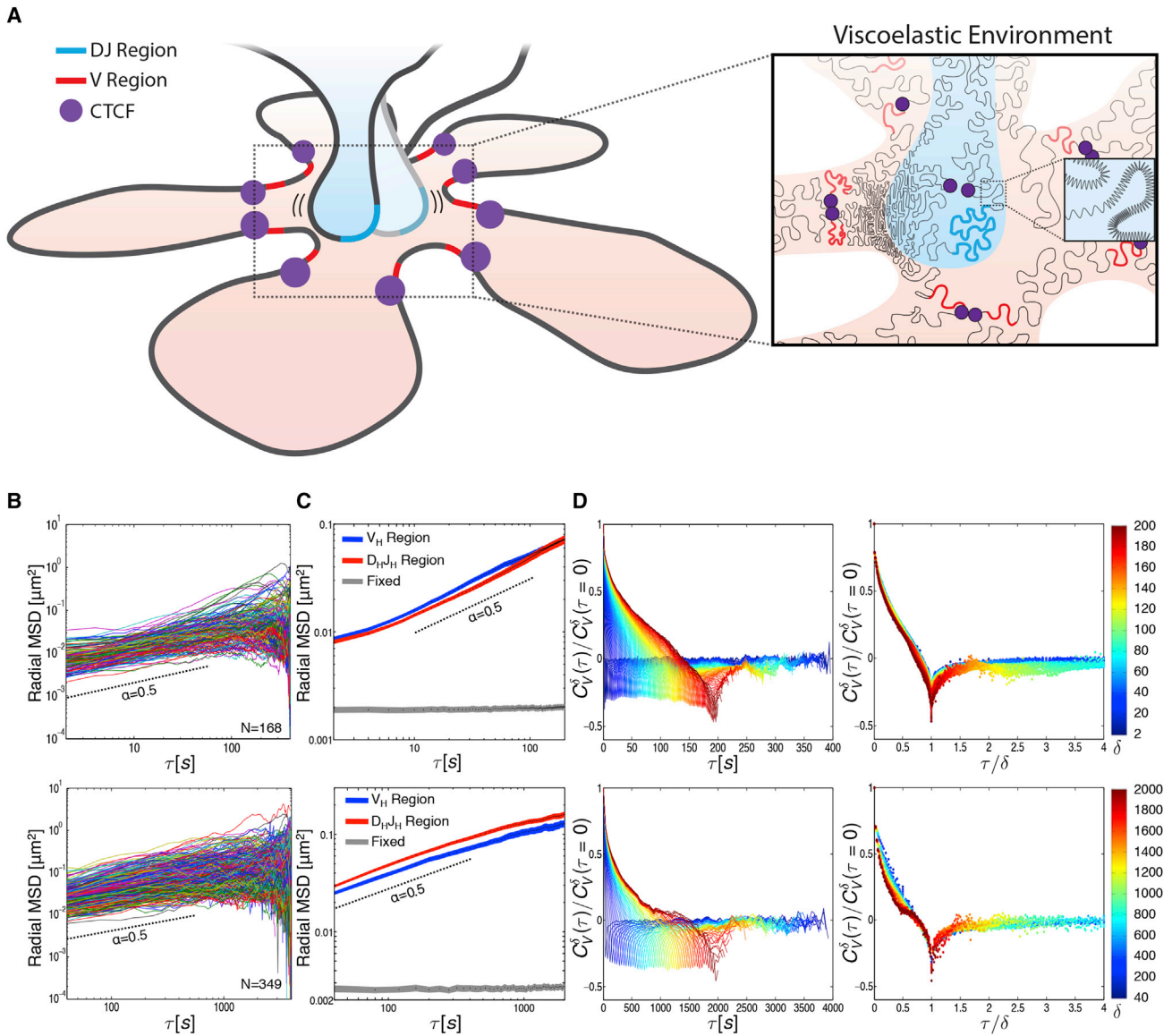


Figure 4. A Viscoelastic Environment Dominates Igh D_{HJH} and V_H Motion in Pro-B Cells

(A) Model depicting fractional Langevin motion across the Igh locus. The Igh locus is organized as bundles of loops, with CTCF (purple) positioning the V_H segments (red) in orbit around the D_{HJH} region (blue). Enlarged region depicts the viscoelastic properties of the chromatin fiber caused by interactions with neighboring networks of nucleic acids and proteins, as well as restoring forces within the fiber itself (shown as springs).

(B) Time-averaged radial MSD plotted as a function of time lag (τ) for the D_{HJH} region in live B220⁺ B lineage cells isolated from TetO mice. Number of cells (N) analyzed is indicated. Cells were imaged once every 2 s for 400 s (top) or once every 40 s for 4,000 s (bottom).

(C) Ensemble- and time-averaged radial MSD plotted as a function of time lag (τ) for the V_H and D_{HJH} regions in live B220⁺ B lineage cells, as well as formaldehyde-fixed pro-B cells. Radial MSD is shown for τ up to one half of total imaging time. Shaded areas represent SEM. Dashed lines indicate a subdiffusive scaling exponent (α) of 0.5.

(D) Velocity autocorrelation analysis of D_{HJH} regions in live B220⁺ B lineage cells (left). Average velocity was calculated over discretization intervals (δ) ranging from 2 to 200 s in 2 s intervals (top) or 40–2,000 s in 40 s intervals (bottom). Velocity autocorrelation curves for different values of δ , plotted against a rescaled time lag (τ/δ) (right). The color scheme represents the values of δ from small (blue) to large (red).

See also [Figures S2](#) and [S3](#) and [Tables S1](#) and [S2](#).

(OD) model ([Saxton, 1994](#)). Third, a particle moving through a dense network of proteins and nucleic acids experiences a response from the surroundings that is characterized by both viscous and elastic components and, hence, is called visco-

elastic response. The viscoelastic response predisposes the particle to bounce back toward its previous position in a spring-like fashion; these reversals, or negative correlations (“memory”) in the particle’s movements lead to subdiffusive

behavior and can be described by fractional Langevin motion (fLm) (Lutz, 2001). Furthermore, when the “particle” is a chromosomal segment embedded in a chromatin fiber, the rest of the fiber itself serves as the viscoelastic environment by exerting restoring forces on the segment. The discussed three mechanisms of random motion may contain contributions from nonthermal active fluctuations, which effectively modify the diffusion coefficient in the corresponding models. Despite the distinct origins of these three mechanisms, they can all lead to the subdiffusive relationship between MSD and elapsed time. Therefore, we applied additional diagnostic measures to identify the mechanism for the observed subdiffusion of V_H and D_{HJH} -TetO segments.

In order to identify the mechanism of subdiffusive motion among the discussed candidate mechanisms (CTRW, OD, and fLm), we compared the time-averaged radial MSD of individual trajectories to the ensemble-averaged radial MSD. Both the time- and ensemble-averaged MSD yielded essentially the same scaling exponent, namely $\alpha \approx 0.5$, suggesting that the trajectories are ergodic (i.e., they display the same time-averaged and ensemble-averaged properties), which, in turn, supports an OD or fLm, but not CTRW mechanism that underpins the subdiffusion process observed here. The observed spread of the time-averaged radial MSD for individual trajectories may be attributed to the limited time over which the trajectories were measured, as well as to the inherent heterogeneity of the cells.

To obtain a more robust measure of the subdiffusive behavior, we calculated the average velocity autocorrelation function, $C_{v}^{\delta}(\tau)$. This function indicates to what degree the average velocity over a time interval δ is correlated with the average velocity over another time interval δ that is separated by τ from the first one. We analyze the correlation properties of the average velocity rather than the instantaneous velocity because experimental measurements are performed at finite time intervals and thus naturally yield the velocity averaged over a time interval. $C_{v}^{\delta}(\tau)$ was calculated for different values of δ and plotted as a function of the time lag τ (Figure 4D, left, and Figure S2). For all δ , $C_{v}^{\delta}(\tau)$ dipped into negative values before decaying to zero. The observed negative values of $C_{v}^{\delta}(\tau)$, which are indicative of negative correlations, cannot be explained by CTRW mechanism, which does not lead to correlations. A negative dip in $C_{v}^{\delta}(\tau)$ can arise in several contexts: (1) OD, (2) fLm, and (3) localization errors in noisy images or (4) an extreme spatial confinement. To resolve the remaining ambiguity in the origin of the negative dips in the average velocity autocorrelation, we analyzed the behavior of $C_{v}^{\delta}(\tau)$ as a function of the ratio (τ/δ) of the two temporal parameters: the time lag (τ) and the time interval (δ) over which the velocity was calculated. Remarkably, when plotted against the rescaled time lag, τ/δ , all of the $C_{v}^{\delta}(\tau)$ curves collapsed onto a single master curve, indicating that the motion of V_H and D_{HJH} segments possesses the property of self-similarity, or similar patterns at different temporal scales (Figure 4D, right, and Figure S2). Such a collapse is not expected to occur for negative correlations in the average velocity caused by OD, localization errors, or by an extreme confinement but rather is a signature of a fLm, or viscoelastic, mechanism (Weber et al., 2010, 2012). The observed negative values of $C_{v}^{\delta}(\tau)$ thus indicate a negative correlation (a reversal) in velocity of the Igh locus

segment caused by the elastic component (“push back”) of the viscoelastic response within the cellular environment. As V_H and D_{HJH} regions of the chromatin fiber collide with a dense network of nucleic acids and proteins, as well as stretch and compress the neighboring segments of the fiber, motion in one direction is likely to be followed by motion in the opposite direction—i.e., the network pushes back (Figure 4A). We conclude that the viscoelastic environment within topological domains is in large part responsible for the subdiffusive motion observed for V_H and D_{HJH} coding, as well as regulatory elements such as enhancers and promoters in B lineage cells.

3D Trajectories Adopted by the Immunoglobulin D_{HJH} Segments in B Cell Progenitors

Recent studies have identified an insulator, named the CBE element, acting to suppress $V_H D_{HJH}$ gene rearrangement involving the most proximal V_H region cluster prior to the formation of a D_{HJH} joint (Guo et al., 2011b; Degner et al., 2011). To determine whether the CBE affects D_{HJH} motion, D_{HJH} -TetO mice were crossed with RAG-deficient mice. Pro-B cells, derived from the bone marrow of D_{HJH} -TetO RAG-deficient mice, were cultured and transduced with virus expressing TetR-EGFP. D_{HJH} motion was monitored as described above (Figure 5A). As expected, the subdiffusive scaling exponents (α) for D_{HJH} motion in RAG-deficient TetO and wild-type TetO pro-B cells were equivalent ($\alpha \approx 0.5$) (Table S1). Consistent with these observations, the velocity autocorrelation functions for the D_{HJH} region were nearly identical for wild-type and RAG-deficient TetO pro-B cells (Figure 5B). The apparent diffusion coefficient associated with D_{HJH} motion increased only slightly (2.4×10^{-3} versus $1.8 \times 10^{-3} \mu\text{m}^2/\text{s}^{0.5}$) in wild-type TetO pro-B cells as compared to RAG-deficient TetO pro-B cells (Figure 5A and Table S1). Taken together, these observations indicate that the CBE insulator does not substantially modulate the diffusion coefficients and subdiffusive scaling exponents associated with D_{HJH} elements.

Simulating V_H and D_{HJH} Encounters

To investigate further the underlying mechanisms of motions associated with coding and regulatory DNA elements, V_H and D_{HJH} dynamics were modeled as an overdamped fractional Langevin motion in a confined sphere of radius R (Jeon and Metzler, 2010). The sphere mimicked the confinement imposed by a chromosomal domain, as the majority of genomic interactions have been demonstrated to occur within domains (Lieberman-Aiden et al., 2009; Dixon et al., 2012; Lin et al., 2012). The initial positions of the V_H and D_{HJH} segments were chosen by randomly drawing from the steady-state distribution (Figure 6D). The correlated fractional Gaussian noise was generated using the circulant embedding method as described previously (Die-trich and Newsam, 1997). The increment for each of the x , y , and z components of motion was calculated and applied at each time step. Reflective boundary condition was applied whenever the diffusing segments were found to be outside of the confinement volume. Parameters in the simulations were chosen such that the anomalous diffusion coefficient $D = 2.4 \times 10^{-3} \mu\text{m}^2/\text{s}^{0.5}$ and the scaling exponent $\alpha = 0.5$ of the simulated motion match those extracted from the radial MSD of our

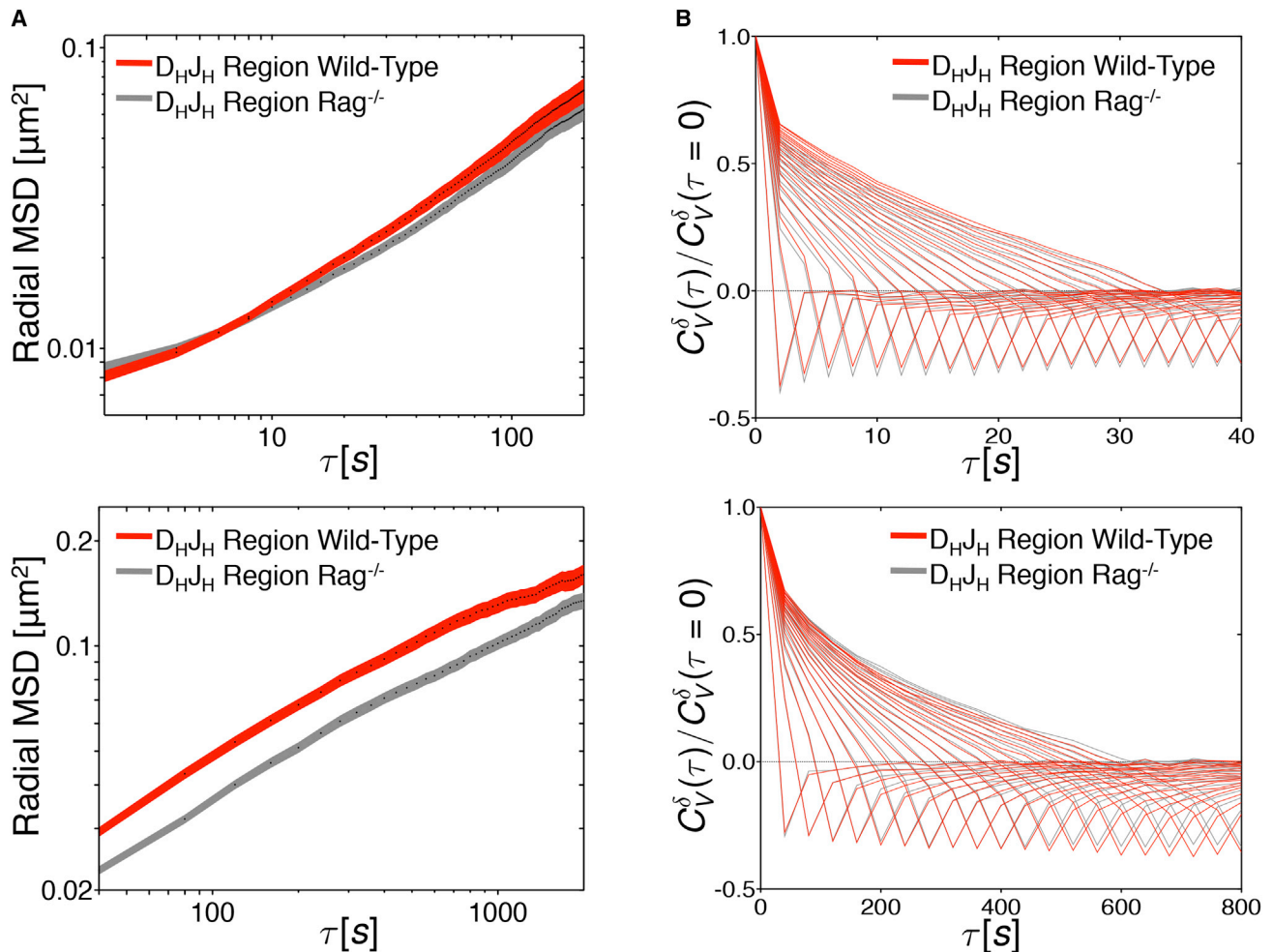


Figure 5. 3D Trajectories Adopted by the Immunoglobulin Heavy-Chain Locus Motion in Wild-Type and Rag-Deficient Pro-B Cells

(A) Ensemble- and time-averaged radial MSD plotted as a function of time lag (τ) for the D_{HJ_H} regions in live B220⁺ B lineage cells derived from wild-type and $Rag^{-/-}$ mice. Cells were imaged once every 2 s for 400 s (top) or once every 40 s for 4,000 s (bottom). Radial MSD is shown for τ up to one half of total imaging time. Shaded areas represent SEM.

(B) Velocity autocorrelation analysis of D_{HJ_H} regions in wild-type and $Rag^{-/-}$ cells. Velocity was calculated over time intervals (δ) ranging from 2 to 40 s in 2 s steps (top) or 40–800 s in 40 s steps (bottom).

experimental measurements. Two values for the confinement radius were used. The value $R = 0.5 \mu\text{m}$ was estimated based on previous 3D FISH measurements (Jhunjhunwala et al., 2008) of spatial distances between the D_{HJ_H} and V_H elements by matching the steady-state distribution of distances between the D_{HJ_H} and V_H gene segments in simulations (Figure 6D) with that measured by 3D-FISH in B lineage cells. The value $R = 1 \mu\text{m}$ was estimated based on the best match between the radial MSD from the simulations and those obtained experimentally in the present study (Figure 6B). Once V_H and D_{HJ_H} segments were within interaction distance r_0 , the corresponding first-passage time was recorded. The interaction distance r_0 was chosen to be 30 nm based on the dimensions of the chromatin fiber. Simulations were repeated 1,000 times (Figure 6A and Movies S3 and S4).

To validate the simulations beyond ensuring a good match between the experimental and simulated MSD and between the

experimental and simulated distributions of distances, we calculated the velocity autocorrelation functions (with $R = 1 \mu\text{m}$) derived from the simulated trajectories. When calculated for different values of the discretization interval (δ) and plotted against the rescaled time lag (τ/δ), the velocity autocorrelation curves collapsed onto a master curve (Figure 6C), as did their experimentally determined counterparts (Figure 4D, right). Collectively, these results indicate that the simulations performed with the experimentally determined physical parameters of V_H and D_{HJ_H} elements reproduce, at the quantitative level, the key aspects of the anomalous diffusion observed in developing B cells.

First-Passage Times for V_H and D_{HJ_H} Encounters

In the murine bone marrow, pro-B cells proliferate with a turnover rate of ~ 1 to 2 days. Hence, V_H - D_{HJ_H} encounters need to occur within this time, which raises the following question: how long

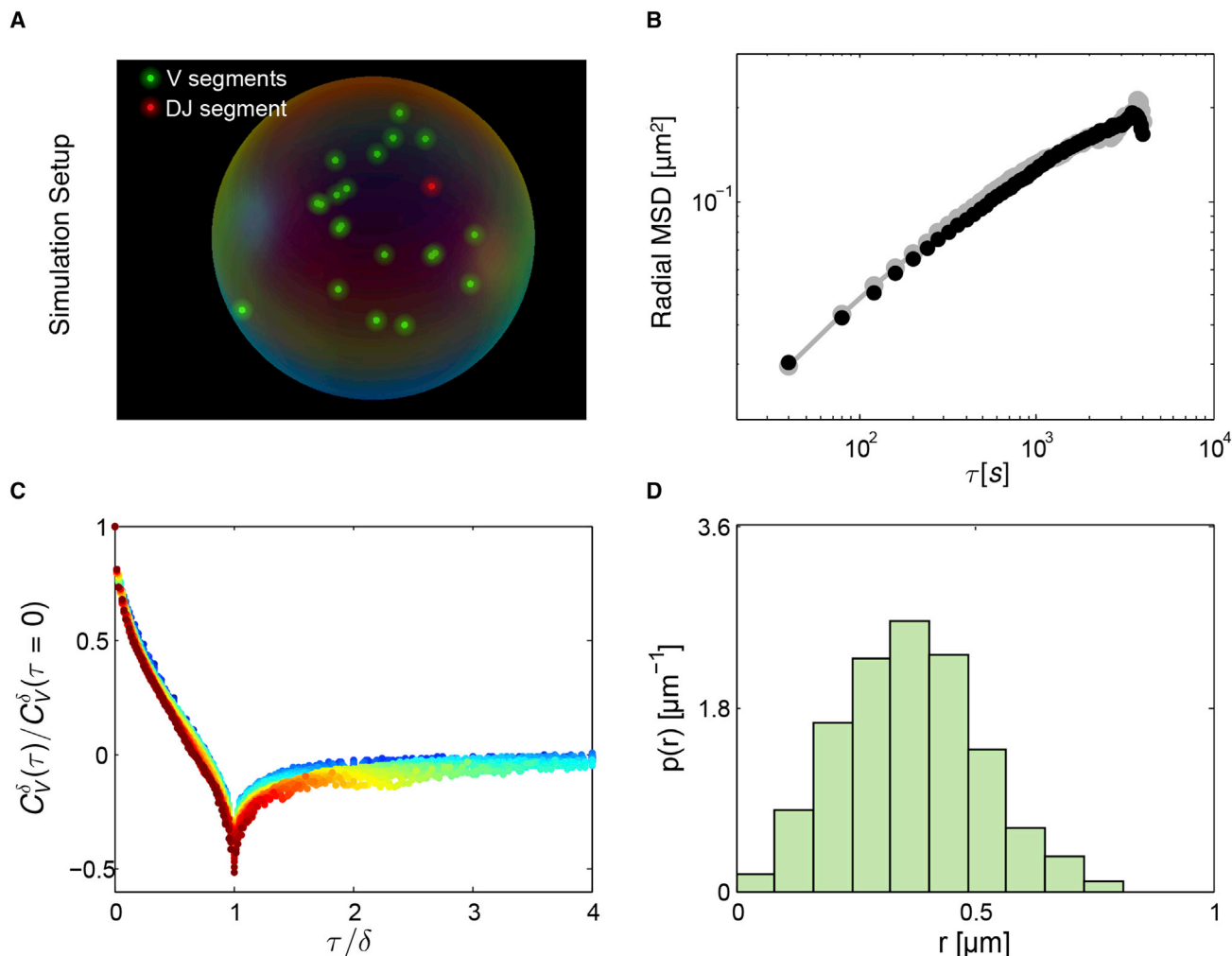


Figure 6. Modeling Anomalous Diffusion of V_H and D_{HJ_H} Elements as Fractional Langevin Motion

(A) V_H and D_{HJ_H} segments confined in a sphere of radius R and subject to fractional Langevin motion using experimentally obtained values of anomalous diffusion coefficient (D) and subdiffusive exponent (α) as physical parameters.

(B) Radial MSD obtained from simulated ($D = 0.0024 \mu\text{m}^2/\text{s}^{0.5}$ and $R = 1 \mu\text{m}$) and experimental measurements. Black symbols are calculated from simulated trajectories. Gray symbols are D_{HJ_H} MSD calculated from measurements in wild-type pro-B cells.

(C) Velocity autocorrelation functions generated from simulations with velocity computed for different values of the discretization interval (δ) exhibit a collapse on a master curve upon rescaling of the time lag τ by δ , as do their experimentally determined counterparts (Figure 4D).

(D) The steady-state distribution of distances between a D_{HJ_H} and a V_H segment generated from the simulation ($D = 0.0024 \mu\text{m}^2/\text{s}^{0.5}$ and $R = 0.5 \mu\text{m}$) agrees well with the experimental distribution of spatial distances previously measured in pro-B cells by 3D-FISH (Jhunjhunwala et al., 2008).

See also Movies S3 and S4.

does it take for D_{HJ_H} elements to reach a V_H region? This question can be addressed via fractional Langevin dynamics modeling using experimentally determined physical parameters of V_H and D_{HJ_H} elements.

We initiated the simulation using a single pair of D_{HJ_H} and V_H elements and a confinement radius of $1 \mu\text{m}$. We found that it takes ~ 30 min on average (Figure 7A) for a D_{HJ_H} and a V_H element to find each other. The mean first-passage time decreased more than 100-fold, to 12 s, when a single copy of D_{HJ_H} and 100 copies of V_H elements were present (Figure 7B).

Prior to V(D)J recombination, the V_H and D_{HJ_H} regions are constrained to distinct topological domains (Jhunjhunwala et al.,

2008). In pro-B cells, at the onset of recombination, locus compaction results in the merging of these domains (Figure 7C). Such events bring into question how the confinement of DNA within topological domains affects first-passage times. To determine to what degree the encounter time is affected by confinement, we repeated the simulations but now using a confinement radius of $0.5 \mu\text{m}$ (Figures 7E and 7F), i.e., half the size of that used in Figures 7A and 7B. Notably, decreasing the radius of confinement 2-fold decreased the mean first-passage time for V_H and D_{HJ_H} elements by 16-fold.

Simple dimensional analysis allows us to determine the general scaling of the encounter time with the confinement radius

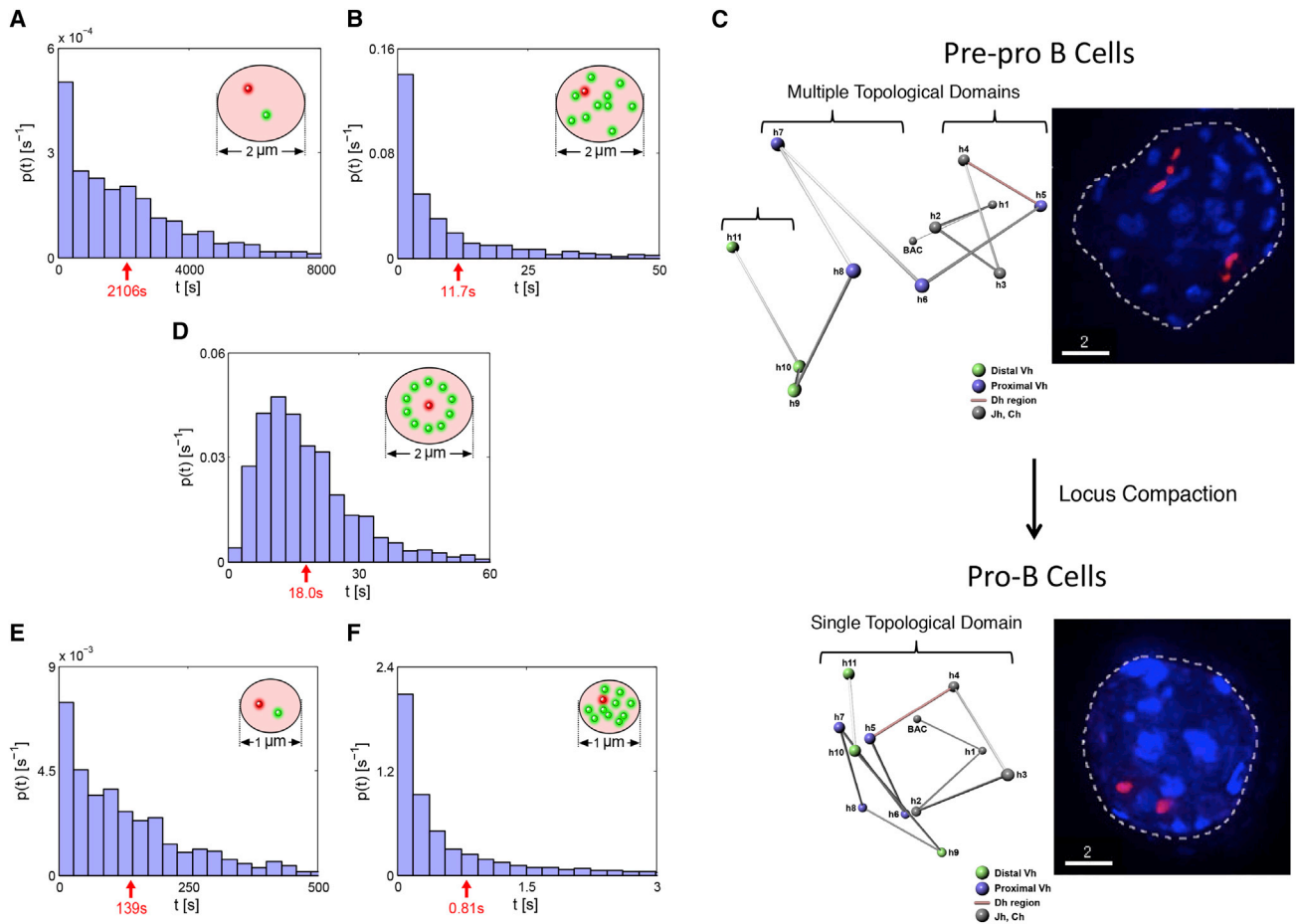


Figure 7. First-Passage Time Distributions for V_H and D_{HJ_H} Segments Undergoing Fractional Langevin Motion

(A) Simulating the behavior of a single pair of V_H and D_{HJ_H} segments in a spatial confinement of radius 1.0 μm and with initial positions randomly chosen from the distribution shown in Figure 6D generated after the system is given enough time to reach the steady state. Motion of V_H and D_{HJ_H} segments as parts of the polymer chain and constrained by anchors is modeled as fractional Langevin motion in a confined sphere of radius R . The distribution of first passage times, the times for the D_{HJ_H} segment to come within 30 nm of the V_H segment, is shown. Red arrow indicates mean first passage time (MFPT).

(B) First-passage time distributions for simulated motion of 100 V_H and one D_{HJ_H} segment in a confinement of radius 1.0 μm .

(C) Left panels show 3D FISH studies revealing the organization and locus contraction of the Igh locus in pre-pro-B and pro-B cells. In pre-pro-B cells, V_H and D_{HJ_H} segments are physically separated into distinct topological domains. Upon differentiating into committed pro-B cells, the proximal and distal V_H regions merge. Right panel indicates the entire Igh locus labeled by overlapping fluorescently labeled BAC probes. Note distinct topological domains in pre-pro-B and pro-B cells (adapted from Jhunjhunwala et al., 2008).

(D) Simulation as performed in (B) but with V_H segments distributed on a sphere with the D_{HJ_H} segment in the center.

(E and F) Simulations as performed in (A) and (B) but with a confinement of radius 0.5 μm .

and the diffusion coefficient. The dimensions of MSD are $[MSD] = [Length]^2 = [D][Time]^\alpha$ (we use the standard notations [...] for “the dimensions of ...”), and hence $[Time] = [Length]^{2/\alpha} [D]^{-1/\alpha}$. Because the relevant parameter with the dimensions of length in this first-passage time problem is the radius of confinement (R) (Condamin et al., 2007), we find that the interaction frequency (equal to the inverse of the mean first-passage time) scales with the confinement radius as $R^{-2/\alpha}$ and with the diffusion coefficient as $D^{1/\alpha}$. Applying this scaling with the value of α extracted from the radial MSD plot (Figure 4C), we find that, upon decreasing the radius of confinement 2-fold, the interaction frequency is predicted to increase $2^4 = 16$ -fold. In contrast, increasing the value of the diffusion coefficient 2-fold leads to

a merely $2^2 = 4$ -fold increase in the interaction frequency. Both of these predictions are consistent with the observations from our simulations. We conclude that the size of confinement largely determines the frequency of interactions between coding elements (such as V_H and D_{HJ_H} regions) and regulatory elements (enhancers and promoters).

Recent observations have suggested that the V_H regions lie in an orbit around a cavity containing the D_{HJ_H} elements (Lucas et al., 2011). We modified the simulations such that V_H regions were distributed on the surface of an imaginary sphere with the D_{HJ_H} elements positioned in the center (Figure 7D). The mean first-passage time for V_H and D_{HJ_H} elements was only modestly affected as compared to the initial random configuration,

although the different initial conditions changed the distribution of first-passage times (Figures 7B and 7D). Taken together, this analysis indicates that confinement size is a dominant factor for first-passage times of genomic elements and that V_H and D_HJ_H elements have a high probability to reach each other within minutes in developing B cells.

DISCUSSION

Although our insights into the folding patterns of the genome are still rudimentary, recent studies have suggested a highly ordered Igh locus configuration. It has been proposed that anchors such as CTCF act to spatially sequester the V_H regions, positioning them “in orbit” around a cavity that contains a D_HJ_H element (Figure 4A) (Lucas et al., 2011). Such a rosette structure would help to ensure that all of the various V_H segments and D_HJ_H segments have the opportunity to find each other in a V(D)J recombination center. Here, we found that the D_HJ_H and V_H elements undergo fractional Langevin motion indicative of a viscoelastic environment likely caused by a surrounding network of V_H and D_HJ_H DNA segments, neighboring DNA segments, tethers such as CTCF, and other factors associated with the chromatin fiber. The value of the scaling exponent $\alpha \approx 0.5$ in B cells approached those observed for chromosomes in other species, including multiple bacterial species, yeast, and human cells (Table S2) (Cabal et al., 2006; Bronstein et al., 2009; Weber et al., 2010). We suggest that fractional Langevin motion prevents rapid displacement of the D_HJ_H elements away from the V_H region cluster. Thus, fractional Langevin motion may provide a physiological advantage: D_HJ_H regions would be bouncing back and forth against genomic elements across the Igh locus fiber until they pair with nearby V_H regions in transit (Figure 4A).

The process of V(D)J gene rearrangement is tightly regulated. Recent studies have demonstrated that ordered rearrangement involving proximal V_H regions is enforced by an insulator element (CBE), which separates the V_H regions from the D_HJ_H regions (Guo et al., 2011b). Our measurements revealed only modest differences in D_HJ_H motion in B cell progenitors that are arrested prior to the onset of D_HJ_H rearrangements versus pro-B cells that carry D_HJ_H joints. How then is proximal V_H - D_HJ_H recombination regulated? It is conceivable that the region containing the CBE insulator element assumes a somewhat stiff conformation or a rod-like structure. Consequently, the proximal V_H and D_HJ_H regions and the intervening rod-like structure may display fractional Langevin motion like any other genomic region, but because the CBE region may not be able to fold back upon itself, V_H and D_HJ_H interactions would be rare. Alternatively, as suggested previously, the CBE may act to form a loop with other CTCF binding sites located downstream of the Igh locus to sequester the D_HJ_H regions away from the V_H region cluster or by suppressing antisense transcription across the proximal V_H domains preventing proximal V_H - D_HJ_H rearrangement prior to the formation of D_HJ_H joints (Guo et al., 2011b; Degner et al., 2011). Future studies involving the tracking of D_HJ_H motion in relation to distal V_H and proximal V_H motion should distinguish between these possibilities.

The simulation results indicate that spatial confinement is the dominant factor that regulates the probability of interaction be-

tween V_H and D_HJ_H elements. Simple dimensional analysis suggests that the encounter frequency scales with the confinement radius as $R^{-2/\alpha}$ and with the diffusion coefficient as $D^{1/\alpha}$. For the value of α (0.5) determined from our measurements, this means that decreasing the radius of confinement 2-fold increases the interaction frequency 16-fold, whereas, in contrast, increasing the value of the diffusion coefficient 2-fold increases interaction frequency merely 4-fold. We conclude that the degree of confinement largely determines the frequency of interactions between coding elements (such as V_H and D_HJ_H regions) and regulatory elements (enhancers and promoters). These findings have implications relating to chromosomal organization, gene regulation, V(D)J recombination, class switch recombination, chromosomal translocations, and chromosomal deletions.

Chromosome conformation capture studies have demonstrated that the large majority of genomic interactions occur within chromatin domains (1–3 Mbp) and with much lower frequencies between domains (Lieberman-Aiden et al., 2009; Dixon et al., 2012; Lin et al., 2012). Thus, the organization of the genome into topological domains constrains the 3D trajectories that are adopted by chromatin fiber. We suggest that the spatially confined geometry is also maintained by the viscoelastic properties of mammalian nuclei, suppressing the rapid diffusion of coding and regulatory DNA elements between chromatin domains. However, topological domains are not static during developmental progression. For example, during the transition from the pre-pro-B to the pro-B cell stage, the genome undergoes large-scale changes in domain organization (Lin et al., 2012). Prominent among these are the antigen receptor loci. Specifically, the distal V_H and proximal V_H regions merge during the transition from the multipotent progenitor to the committed pro-B cell stage (Kosak et al., 2002; Fuxa et al., 2004; Jhunjhunwala et al., 2008). The Ig κ locus also undergoes locus contraction in B cell progenitors (M.C. van Zelm, S. Jhunjhunwala, and C.M., unpublished data). Similarly, the TCR α and β loci contract in cells prone to undergo TCR rearrangement (Roldán et al., 2005). How does locus contraction affect DNA recombination? The simulation results indicate that topological domains merge or segregate during developmental progression to modulate the encounter times of genomic elements localized within topological domains. The merging of topological domains during developmental progression is not restricted to antigen receptor loci. An important example involves the EBF1 locus, which, during the transition from the pre-pro-B to the pro-B cell stage, dissociates from the nuclear lamina to merge with transcriptionally active domains and may allow enhancers and promoters located across this vast locus to interact with high frequencies, ultimately leading to the induction of a B-lineage-specific program of gene expression (Lin et al., 2012). In sum, we suggest that the merging or segregation of topological chromatin domains affects the encounter times of V_H and D_HJ_H or promoter and enhancer elements to permit rapid changes in gene expression during developmental progression.

Somatic recombination during B cell development is not restricted to V(D)J recombination. In the peripheral lymphoid organs, CSR changes the expression of immunoglobulins from one isotype to another. In activated B cells, switch regions join after double-stranded breaks (DSBs) are generated (Zarrin et al.,

2007). It has been suggested that DSBs may rapidly diffuse to promote efficient synapse formation and class switch recombination and that topological confinement may play a key role in this process (Alt et al., 2013; Gostissa et al., 2014). Our simulation results provide support for such a model. In conjunction with previous spatial distance measurements across the switch regions, we predict that DSBs generated across the switch regions reach each other within minutes and that topological confinement is the dominant factor in establishing rapid first-passage times (Jhunjhunwala et al., 2008).

Our findings also have implications for chromosomal deletions that frequently are associated with cancer. Intrachromosomal interstitial deletions associated with illegitimate rearrangements involving nonantigen receptor genes and cryptic recombination signal sequences are frequently linked with lymphoid cancers (Onozawa and Aplan, 2012). Recent studies revealed that proximity of two DSBs is the critical factor in determining the preferences for DSBs translocating in *cis* (Klein et al., 2011; Chiarle et al., 2011, Zhang et al., 2012; Alt et al., 2013). These observations are consistent with the simulation results presented here indicating that spatial confinement is a dominant component in controlling the encounter times of long-range genomic interactions. Hence, we suggest that the predisposition of two DSBs to join intrachromosomally might lead to the development of T-ALL and other types of lymphoid malignancies if the chromatin topology associated with such breaks would permit rapid first-passage times (Alt et al., 2013; Bunting and Nussenzweig, 2013). Finally, we note that rapid first-passage times of paired DSBs may similarly underpin the physical mechanism by which chromosomal deletions are generated in a wide variety of malignancies (Solimini et al., 2012; Beroukhim et al., 2010).

EXPERIMENTAL PROCEDURES

TetR-EGFP Constructs and Retrovirus Production

A TetR-EGFP construct was created by fusing a TetR (tTA2S) with enhanced GFP (EGFP). tTA2S has been previously described (Urlinger et al., 2000). A nuclear localization signal (PKKKRKV) was added to the 5' end by PCR. EGFP vectors are available from Clontech. An XbaI site was added to the 3' end of tTA2S and the 5' end of EGFP for fusion. Finally, either a wild-type (gccaccATG) or mutant (gcctccATG) Kozak sequence was added along with restriction sites for cloning into the MinV, PCS Ret, or LMP vectors. LMP is available from Thermo Scientific, and the TetR-EGFP was inserted in place of the vector's EGFP cassette. MinV and PCS Ret have been previously described (Hawley et al., 1996; Sayegh et al., 2003). Primers used are listed in Table S3. Complete vectors were purified by CsCl gradient and transfected into 293T cells along with retroviral packaging vectors by calcium phosphate transfection. Media were replaced the following morning, and viral supernatant was harvested 1 day later and stored at -80°C until used.

Imaging

Imaging was performed under normal growth conditions using phenol-red free media. Cells were plated on Fluorodish poly-D-lysine-coated plates (World Precision Instruments) and imaged using a $100\times$ 1.4 NA oil immersion objective on a Zeiss CSU spinning disk confocal microscope with a Yokogawa spinning disk scan head and an EM-CCD camera. 20–30 Z sections were obtained with a spacing of 0.5 μm and acquired at a rate of one stack every 2 s for 200 total time points or one stack every 40 s for 100 total time points. Laser intensity was 6%, and exposure time was 30 ms for 2 s intervals and 45 ms for 40 s intervals. For fixed cell measurements, cells were fixed for 10 min in 4% paraformaldehyde in PBS and quenched 5 min in 0.1 M Tris-HCl (pH 7.4) and stained using a 1:2,000 dilution of Alexa 488 conjugated rabbit monoclonal

anti-GFP from Life Technologies (G10362). Axial elongation was corrected prior to calculating probe-to-probe distances (Figure S3).

SUPPLEMENTAL INFORMATION

Supplemental Information includes Extended Experimental Procedures, three figures, three tables, and four movies and can be found with this article online at <http://dx.doi.org/10.1016/j.cell.2014.05.036>.

AUTHOR CONTRIBUTIONS

J.S.L. initiated the study, designed, and performed the experiments, analyzed the data, and contributed to the writing of the manuscript. Y.Z. analyzed the data, performed the simulations, and contributed to the writing of the manuscript. O.K.D. and C.M. supervised the study and contributed to the writing of the manuscript.

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