



# Relatively heavy Higgs boson in more generic gauge mediation

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## ARTICLE INFO

### Article history:

Received 29 July 2011

Received in revised form 26 September 2011

Accepted 15 October 2011

Available online 18 October 2011

Editor: T. Yanagida

## ABSTRACT

We discuss gauge mediation models where the doublet messengers and Higgs doublets are allowed to mix through a “charged” coupling. The charged coupling replaces messenger parity as a means of suppressing flavor changing neutral currents without introducing any unwanted  $CP$  violation. As a result of this mixing between the Higgs doublets and the messengers, relatively large  $A$ -terms are generated at the messenger scale. These large  $A$ -terms produce a distinct weak scale mass spectrum. Particularly, we show that the lightest Higgs boson mass is enhanced and can be as heavy as 125 GeV for a gluino mass as light as 2 TeV. We also show that the stops are heavier than that predicted by conventional gauge mediation models. It is also shown that these models have a peculiar slepton mass spectrum.

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## 1. Introduction

A generic feature of models with gauge mediated supersymmetry (SUSY) breaking [1–7] is flavor-blind soft masses at the messenger scale. Additionally, the  $A$ -terms at the messenger scale<sup>1</sup> are generically predicted to be loop suppressed compared to the sfermions masses. An important consequence of small  $A$ -terms at the messenger scale is the lightest Higgs boson of the minimal supersymmetric standard model (MSSM) is at the edge of the presently allowed mass region, i.e.  $m_{h^0} \lesssim 120$  GeV for  $m_{\text{gluino}} \lesssim 3$  TeV [8].<sup>2</sup>

In this Letter, we investigate more generic gauge mediation models for which the  $A$ -terms are generated at one-loop without introducing any new flavor violation. As a result of these large  $A$ -terms, we show that the lightest Higgs boson is relatively heavy for a given gluino mass as compared with conventional gauge mediation models. Furthermore, we also show that the stop masses are predicted to be heavier than expected for such a heavy Higgs boson mass. It is also shown that the models have a peculiar slepton mass spectrum.

The organization of the Letter is as follows. In Section 2, we discuss our more generic model of gauge mediation and explain the origin of the large stop  $A$ -terms. In Section 3, we discuss the

distinct features of the mass spectrum, including the effects of the enhanced  $A$ -terms. The final section is devoted to our conclusions and discussions.

## 2. More generic gauge mediation

### 2.1. Flavor blind models of gauge mediation

Before discussing our more generic setup, we briefly review how conventional gauge mediation produces flavor-blind soft SUSY breaking parameters at the messenger scale. In most models, the messengers ( $\Phi, \bar{\Phi}$ ) are assumed to be a fundamental and anti-fundamental of the minimal grand unified gauge group,  $SU(5)$ . The messengers couple directly with supersymmetry breaking in the superpotential

$$W = gZ\bar{\Phi}\Phi, \quad (1)$$

where  $g$  is some coupling constant and

$$g(Z) = M + F\theta^2. \quad (2)$$

We consider  $g(Z)$  to be a spurion and do not consider its origin in what follows.<sup>3</sup> Integrating out the messengers produces flavor-blind soft SUSY breaking parameters.

An implicit, but crucial, assumption made in the above discussion is that the messengers do not directly couple to the MSSM matter fields. In order to rationalize the above assumptions, quantum numbers are assigned to the messengers to distinguish them

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<sup>1</sup> In this Letter, we define  $A$ -terms as the trilinear scalar couplings divided by the corresponding Yukawa coupling constants.

<sup>2</sup> Here, we roughly assume the reach of the LHC experiments for  $\sqrt{s} = 14$  TeV with the integrated luminosity  $100 \text{ fb}^{-1}$ .

<sup>3</sup> See, for example, Refs. [9,10] for a recent discussion of models of gauge mediation which include the SUSY breaking sector.

**Table 1**

The charge assignments for the broken  $U(1)$  symmetry are presented here. We have used  $SU(5)$  GUT representations for the MSSM matter fields, i.e.  $\mathbf{10} = (Q_L, \bar{U}_R, \bar{E}_R)$  and  $\mathbf{5}^* = (\bar{D}_R, L_L)$ . We also show the charge of the right-handed neutrinos  $\bar{N}_R$ , which is need for the see-saw mechanism [11]. These charge assignments forbid the unwanted interactions in Eqs. (3) and (4) while allowing those in Eq. (5) along with the MSSM Yukawa interactions, the  $\mu$ -term, and mass terms for the right-handed neutrinos.

	$\phi_+$	$H_u$	$H_d$	$\mathbf{10}$	$\mathbf{5}^*$	$\bar{N}_R$	$\Phi$	$\bar{\Phi}$	$Z$
$U(1)$	+1	-2	-3	+1	+2	0	0	0	0

from the MSSM matter fields. Most importantly, these quantum numbers distinguish the messenger doublets from the Higgs doublets. Without this distinction, the messengers would couple directly to the MSSM matter fields<sup>4</sup>

$$W = \rho_1 \Phi_{\bar{L}} Q_L \bar{U}_R + \rho_2 \bar{\Phi}_{\bar{L}} Q_L \bar{D}_R + \rho_3 \bar{\Phi}_{\bar{L}} L_L \bar{E}_R, \quad (3)$$

leading to flavor-violating soft scalar masses.<sup>5</sup> Furthermore, operators inducing rapid proton decay such as,

$$W = \lambda_1 \Phi_D Q_L Q_L + \lambda_2 \bar{\Phi}_D Q_L L_L, \quad (4)$$

could not be forbidden. Here, we have split the messengers into  $\Phi = (\Phi_D, \Phi_{\bar{L}})$  and  $\bar{\Phi} = (\bar{\Phi}_D, \bar{\Phi}_{\bar{L}})$  in accordance with the MSSM gauge charges. Forbidding these two types of operators, via quantum numbers, is crucial for building a successful model.<sup>6</sup> This reasoning seems to eliminate the possibility of the Higgs doublets mixing with the doublet messengers,  $\Phi_{\bar{L}}$  and  $\bar{\Phi}_{\bar{L}}$ .

In supersymmetric theories, however, the Higgs doublets can mix with the doublet messengers while the tree level operators in Eqs. (3) and (4) are forbidden. This is accomplished by assuming that there is a  $U(1)$  symmetry which was spontaneously broken at some high energy scale by a single positively charged spurion field,  $\phi_+$ . If the Higgs doublet is negatively charged under this  $U(1)$ , a combination of  $\phi_+$  and  $H_u$  can mix with the doublet messengers in the superpotential. More explicitly, we may generalize the messenger sector as follows

$$W = g Z \bar{\Phi} \Phi + \frac{\langle \phi_+^2 \rangle}{\Lambda^2} Z \bar{\Phi} H_u, \quad (5)$$

where  $\Lambda$  denotes some high energy cutoff scale such as the Planck scale,  $M_{Pl}$ . The unwanted operators in Eqs. (3) and (4) are forbidden if the charge assignments are as in Table 1. Therefore, with the help of the “charged coupling constant”  $\langle \phi_+ \rangle$ , the messengers and the Higgs pair can have a Yukawa interaction in the superpotential without introducing any other phenomenological problems. This additional interaction will eventually lead to mixing between the Higgs and the doublet messengers. We note here that negatively charged couplings are not allowed in the superpotential because of its holomorphy (i.e. the so-called SUSY-zero mechanism). It is for this reason that the messengers are not allowed to have direct Yukawa interactions with the MSSM matter fields.

From the above arguments, we find four classes of models consistent with flavor constraints and rapid proton decay constraints:

- No mixings between the messengers and the Higgs pair.
- The messenger  $\Phi_{\bar{L}}$  mixes with  $H_u$  with the help of a “charged” coupling constant.

- The messenger  $\bar{\Phi}_{\bar{L}}$  mixes with  $H_d$  with the help of a “charged” coupling constant.
- The messengers  $\Phi_{\bar{L}}$  and  $\bar{\Phi}_{\bar{L}}$  mix with  $H_u$  and  $H_d$ , respectively, with the help of “charged” coupling constants.<sup>7</sup>

The first class of models corresponds to conventional gauge mediation. The second class which we name Type-II gauge mediation is a new class of models. Below we will discuss the mass spectrum of Type-II gauge mediation. We discuss only Type-II gauge mediation since we are most interested in the mass of the lightest Higgs boson. However, these other two classes of models will have their own unique spectrum.

## 2.2. Soft SUSY breaking masses in Type-II gauge mediation

Now we examine in detail Type-II gauge mediation models. In Type-II gauge mediation models, only  $H_u$  mixes with the messengers. The superpotential for Type-II gauge mediation at the messenger scale is

$$W = g Z \bar{\Phi} \Phi + g' Z \bar{\Phi}_{\bar{L}} \tilde{H}_u + \tilde{\mu} \tilde{H}_u H_d + \tilde{y}_{Uij} \tilde{H}_u Q_{Li} \bar{U}_{Rj}, \quad (6)$$

where  $\tilde{\mu}$  ( $\propto \langle \phi_+^5 \rangle / \Lambda^4$ ) is a dimensionful parameter,  $\tilde{y}_{Uij}$  is the usual  $3 \times 3$  Yukawa coupling matrix, and we have replaced  $\langle \phi_+^2 \rangle / \Lambda^2$  by  $g'$ .<sup>8</sup> We have also placed tildes on  $H_u$  and  $\Phi_{\bar{L}}$  for later purposes and have neglected the parts of the MSSM superpotential which are not relevant for our discussion. Because of holomorphy of the superpotential, as explained above, the dangerous terms like  $\Phi_{\bar{L}} Q_L \bar{U}_R$  are forbidden because a negatively charged couplings constant is not allowed.

To elicit the important low-scale phenomenon of these models, we change the field basis by the rotation

$$\begin{pmatrix} \tilde{\Phi}_{\bar{L}} \\ \tilde{H}_u \end{pmatrix} = \frac{1}{\sqrt{g^2 + g'^2}} \begin{pmatrix} g & -g' \\ g' & g \end{pmatrix} \begin{pmatrix} \Phi_{\bar{L}} \\ H_u \end{pmatrix}. \quad (7)$$

In this new basis, the above superpotential becomes

$$W = \bar{g} Z \bar{\Phi} \Phi + \mu H_u H_d + \mu' \bar{\Phi}_{\bar{L}} H_d + y_{Uij} H_u Q_{Li} \bar{U}_{Rj} + y'_{Uij} \bar{\Phi}_{\bar{L}} Q_{Li} \bar{U}_{Rj}, \quad (8)$$

where the parameters are defined as

$$\begin{aligned} \bar{g} &= \sqrt{g^2 + g'^2}, & \mu &= \frac{g}{\sqrt{g^2 + g'^2}} \tilde{\mu}, & \mu' &= \frac{g'}{\sqrt{g^2 + g'^2}} \tilde{\mu}, \\ y_{Uij} &= \frac{g}{\sqrt{g^2 + g'^2}} \tilde{y}_{Uij}, & y'_{Uij} &= \frac{g'}{\sqrt{g^2 + g'^2}} \tilde{y}_{Uij}. \end{aligned} \quad (9)$$

This new basis is much better for low scale physics because the only heavy states are clearly  $\Phi, \bar{\Phi}$ .<sup>9</sup> In this basis, the mixing angle between the Higgs doublet and the messengers is suppressed by  $O(\mu/M)$ , as compared to  $O(g'/g)$  in the original. Since we will

<sup>7</sup> A similar model to the fourth possibility has been considered based on a framework of the extra dimension [12], where the operators causing rapid proton decay are suppressed by brane separation, while they are suppressed by the SUSY-zero mechanism in the present model as explained in the text.

<sup>8</sup> In the following discussion, we assume that  $\langle \phi_+ \rangle \simeq \Lambda \simeq M_{Pl}$ , so that  $g \simeq g' = O(1)$ . In this case, the  $\mu$ -term,  $\tilde{\mu} \propto \langle \phi_+^5 \rangle / \Lambda^4$  is not suppressed by  $\langle \phi_+ \rangle$ 's, and hence, it needs to be suppressed by some other mechanism to explain  $\mu = O(1)$  TeV. In this Letter, we do not discuss the solution to the so-called  $\mu$ -problem in this Letter. (See also some comments at the end of this section.)

<sup>9</sup> In the following arguments, we slightly change the definitions of the spurion VEV from Eq. (2) to

$$\bar{g}(Z) = M + F\theta^2. \quad (10)$$

<sup>4</sup> For simplicity, we have suppress the flavor indices in Eqs. (3) and (4).

<sup>5</sup> Tree level flavor violation from these new interactions could also be problematic unless the messenger scale is above about  $10^5$  TeV.

<sup>6</sup> We assume that the messenger triplets,  $\Phi_D$  ( $\bar{\Phi}_D$ ) have the same quantum numbers as the messenger doublets  $\Phi_{\bar{L}}$  ( $\bar{\Phi}_{\bar{L}}$ ) under the symmetries which forbid the unwanted terms.

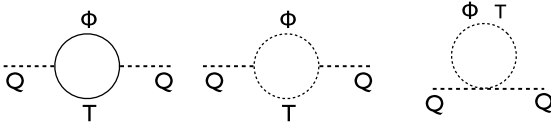


Fig. 1. The diagrams which are relevant for the soft squared mass of  $Q_L$ . The soft squared mass of  $\bar{T}_R$  is obtained by exchanging the  $Q$ 's and  $T$ 's in the diagrams.

consider  $g'/g \sim 1$ , this basis is more suited for physics below the messenger scale.

Here, we reaffirm that the new flavor dependent interactions in this basis,

$$W = y'_{Uij} \Phi_L Q_{Li} \bar{U}_{Rj}, \tag{11}$$

are not dangerous. Since these new flavor dependent interactions are aligned with the MSSM Yukawa coupling,  $y_U$ , diagonalizing the Higgs–Yukawa couplings will simultaneously diagonalize these additional Yukawa couplings.<sup>10</sup> In the MSSM, we are free to chose one of the Yukawa couplings to be diagonal without any loss of generality. In this basis, it is clear that no new significant source of flavor violation is present. In the following discussion, we choose the basis where  $\tilde{y}_U$  is diagonal and neglect everything except the top Yukawa coupling,

$$W = y_t H_u Q_{L3} \bar{T}_R + y'_t \Phi_L Q_{L3} \bar{T}_R. \tag{12}$$

Not only are these interaction not dangerous, but it is these new interactions that give Type-II gauge mediation its unique spectrum.

2.2.1. Tree-level mediation effect

The third term of the superpotential in Eq. (8) leads to a soft SUSY breaking squared mass for  $H_d$  at the “tree-level”. That is, by integrating out the messengers, the down-type Higgs  $H_d$  gets a tree-level soft squared mass,

$$m_H^2 = -\mu'^2 \frac{F^2}{M^4 - F^2}. \tag{13}$$

Here,  $\mu'$  is assumed to be of the same order of magnitude as the  $\mu$ -term, for  $g/g' = O(1)$ . This contribution can be important in low scale gauge mediation where  $F \sim M^2$ . However, as we push up the messenger scale this contribution falls off quickly. Fortunately, this tree-level mediation does not play an important role in most of the parameter space we are interested in.

2.2.2. The one-loop contribution to  $m_{Q_3}^2$  and  $m_{\bar{T}}^2$

Now, let us discuss the one-loop soft squared mass of  $Q_{L3}$  due to the last interaction term in Eq. (12). From the diagrams in Fig. 1, we obtain a one-loop soft squared mass for  $Q_{L3}$ :

$$\delta m_{Q_3}^2 = \frac{y_t'^2}{32\pi^2} \frac{F^2}{M^2} \left( \frac{(2+x)\log(1+x) + (2-x)\log(1-x)}{x^2} \right), \tag{14}$$

where we have defined,

$$x = \frac{F}{M^2}. \tag{15}$$

In a similar way, we obtain the soft mass of  $\bar{T}_R$ :

$$\delta m_{\bar{T}}^2 = 2 \times \delta m_{Q_3}^2. \tag{16}$$

<sup>10</sup> In this sense, the Type-II gauge mediation is a natural realization of the so-called “minimal flavor violation” scenario (see for example Ref. [13]).

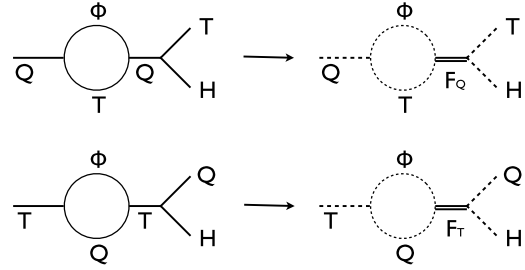


Fig. 2. The diagrams which are relevant for the  $A$ -terms. In terms of supergraphs, the  $A$ -term is generated as a result of the wave function renormalization, which reduces to the 1PI diagrams in component graphs.

It should be noted that these one-loop contributions to the stop squared masses are negative [14]. Thus, one might worry that these one-loop negative contributions dominate the positive but two-loop gauge mediated contributions since  $y'_t \simeq 1$ . This is, however, not the case for  $x \ll 1$  since these one-loop contributions are suppressed by additional factors of  $x$ ,

$$\delta m_{\bar{T}}^2 \simeq -\frac{y_t'^2}{48\pi^2} \frac{F^2}{M^2} \frac{F^2}{M^4} \quad (x \ll 1). \tag{17}$$

The two-loop dominance can be seen explicitly by comparing the above contribution to the stop mass with the traditional gauge mediated contribution,<sup>11</sup>

$$m_{Q,T}^2 \simeq \frac{8}{3} \left( \frac{\alpha_3}{4\pi} \right)^2 \frac{F^2}{M^2} \quad (x \ll 1). \tag{18}$$

The one-loop contribution is subdominant and does not lead to a tachyonic stops mass as long as,

$$\frac{F}{M^2} \ll 2\sqrt{2} \times \frac{\alpha_3}{y_t'}. \tag{19}$$

This condition can be easily satisfied, even for  $y'_t \simeq 1$ , as long as the messenger scale is not too low.

2.2.3. The one-loop contributions to  $A$ -terms

In Type-II models,  $A$ -terms are also generated at the one-loop level (see Fig. 2). The resultant  $A$ -term for the stops is given by

$$A_t = -\frac{3}{32\pi^2} y_t'^2 \frac{F}{M} \frac{1}{x} \log\left(\frac{1+x}{1-x}\right). \tag{20}$$

The  $A$ -term for the sbottoms is also given by,

$$A_b = -\frac{1}{32\pi^2} y_t'^2 \frac{F}{M} \frac{1}{x} \log\left(\frac{1+x}{1-x}\right). \tag{21}$$

In contrast to the one-loop soft squared masses, the  $A$ -terms have no  $x$  suppression in the limit  $x \ll 1$ ,

$$A_t \simeq -\frac{3y_t'^2}{16\pi^2} \frac{F}{M} \quad (x \ll 1). \tag{22}$$

Thus, the one-loop contribution to the  $A$ -terms can be sizable even when the messenger scale is very high (i.e.  $x \ll 1$ ) if  $y'_t \simeq 1$ . As we will see shortly, these relatively large  $A$ -terms push up the mass of the lightest Higgs boson significantly.

<sup>11</sup> We neglected the gauge mediated contributions other than the ones from the strong interactions.

### 2.2.4. The two-loop contribution to $m_Q^2$ and $m_T^2$

Finally, let us discuss the two-loop contributions to  $m_Q^2$ ,  $m_T^2$  and  $m_{H_u}^2$  from the last interaction term in Eq. (12). Unlike the one-loop contributions to  $m_Q^2$  and  $m_T^2$ , the two-loop contributions are not suppressed in the limit of  $x \ll 1$ .<sup>12</sup> The leading two-loop contributions can easily be extracted by analytically continuing the wave function renormalization factor into superspace [17] which leads to<sup>13</sup>

$$\begin{aligned}\delta m_{Q_3}^2 &= \frac{y_t'^2}{128\pi^4} \left( 3y_t'^2 + 3y_t^2 - \frac{8}{3}g_3^2 - \frac{3}{2}g_2^2 - \frac{13}{30}g_1^2 \right) \frac{F^2}{M^2}, \\ \delta m_T^2 &= \frac{y_t'^2}{128\pi^4} \left( 6y_t'^2 + 6y_t^2 + y_b^2 - \frac{16}{3}g_3^2 - 3g_2^2 - \frac{13}{15}g_1^2 \right) \frac{F^2}{M^2}, \\ \delta m_B^2 &= -\frac{y_b^2 y_t'^2}{128\pi^4} \frac{F^2}{M^2}, \\ \delta m_{H_u}^2 &= -9 \frac{y_t^2 y_t'^2}{256\pi^4} \frac{F^2}{M^2}, \\ \delta m_{H_d}^2 &= -3 \frac{y_b^2 y_t'^2}{256\pi^4} \frac{F^2}{M^2},\end{aligned}\quad (23)$$

where  $y_b$  is the bottom Yukawa coupling constant and  $m_B^2$  is the soft squared mass of the right-handed sbottom.<sup>14</sup> It should be noted that the two-loop contributions to  $m_{H_u}^2$  is negative, and can dominate the gauge mediated contributions if  $y_t' \simeq 1$ . Since the Higgs doublets can have a large supersymmetric mass,  $\mu$ , the negative value of  $m_{H_u}^2$  does not lead to a vacuum stability problem.

Several comments are in order. First, let us point out that there are no  $CP$ -phases in Eq. (8). All the phases of  $\tilde{y}_t$  and  $\mu$ , except the CKM phase, can be eliminated by rotating the MSSM fields in the standard way. The phases of the new couplings  $g$  and  $g'$  can also be eliminated by appropriately rotating  $\Phi$  and  $\tilde{\Phi}$ . Therefore, the SUSY  $CP$ -problem is also absent. It should also be noted that Type-II models do not lead to a large  $B\mu$ -term, since the diagrams which leads to the  $B\mu$ -term require two insertion of  $\mu'$ . Thus, these models are also free from the so-called  $B\mu$ -term problem.<sup>15</sup>

## 3. The spectrum of the model

In this section, we show the distinctive features of the spectrum of the Type-II gauge mediation models.

### 3.1. The heavy lightest Higgs region

As we have shown in the previous section, an interesting feature of Type-II gauge mediation is the relatively large stop  $A$ -terms which are generated at the one-loop level. With a relatively large

$A$ -term, the lightest Higgs boson mass, which receives important SUSY breaking corrections via the top-stop loop diagrams [20], is pushed up to

$$m_{h^0}^2 \lesssim m_Z^2 \cos^2 2\beta + \frac{3}{4\pi^2} y_t^2 m_t^2 \sin^2 \beta \left( \log \frac{m_t^2}{m_t^2} + \frac{A_t^2}{m_t^2} - \frac{A_t^4}{12m_t^4} \right). \quad (24)$$

Here,  $m_Z$  and  $m_t$  are the masses of the  $Z$ -boson and top quark, respectively, and  $\tan \beta$  is the ratio of the two vacuum expectation values of the Higgs doublets.<sup>16</sup> The above expression for the Higgs mass is maximized for an  $A$ -term of order  $A_t \simeq \sqrt{6} \times m_t$ . By comparing Eqs. (18), (22), and (23), we see that the lightest Higgs boson receives large  $A$ -term contributions for  $y_t' \simeq 1$ .

In Fig. 3, we show a contour plot of the lightest Higgs boson mass as a function of  $y_t'$  and  $F/M^2$  for a gluino mass of 2.1 TeV,  $\tan \beta = 10$  and the number of messenger  $N_{\text{mess}} = 1$  (left panel). To calculate the weak scale soft masses and Higgs boson mass, we have used *SoftSusy* [21].<sup>17</sup> The figure shows that the Higgs mass becomes large for  $y_t' \simeq 1$  as expected.

The blank regions in Fig. 3 are excluded. For  $x \simeq 1$ , the stop mass is tachyonic (or too light) and for  $y_t' \gtrsim 1$  and  $x \ll 1$  the right-handed slepton masses are tachyonic<sup>18</sup> (or too light). Within the allowed region, we find that the vacuum stability condition [24],

$$A_t^2 + 3\mu^2 < 7.5(m_{\tilde{t}_L}^2 + m_{\tilde{t}_R}^2), \quad (25)$$

is always satisfied and the relatively large  $A$ -terms do not cause vacuum instability problems in Type-II models.

The right panel of Fig. 3 shows the lightest Higgs boson mass for  $y_t' = 1$  and  $x = 0.1$ . From this figure, we see that the mass is raised by about 10 GeV compared to the Higgs boson mass of conventional gauge mediation. As a result of this enhancement, the Higgs boson can be heavier than 120 GeV for a relatively light gluino mass,  $m_{\text{gluino}} \sim 1$  TeV. The figure also shows that the gluino is well within the reach of the LHC experiments even for a relatively heavy Higgs boson mass, i.e.  $m_{h^0} \simeq 125$  GeV.

In addition to a relatively heavy lightest Higgs boson, we also expect that the stops are heavier than those of minimal gauge mediation. This stop mass enhancement is mainly due to the two-loop contribution to the stops in Eq. (23). In Fig. 4, we plot the stop masses for a representative point with a large Higgs mass,<sup>19</sup> ( $y_t' = 1$ ,  $x = 0.1$ ). The figure shows that both stops are predicted to be heavier than those in conventional gauge mediation models ( $y_t' = 0$ ). These mass features provide important clues for probing Type-II gauge mediation models at the LHC.<sup>20</sup>

The models also predict a peculiar slepton mass spectrum in the region where lightest Higgs mass is relatively heavy. This peculiar slepton spectrum is caused by the renormalization group evolution of the sleptons,

$$\frac{d}{dt} m_{\text{slepton}}^2 = - \sum_{a=1,2} 8C_a \frac{g_a^2}{16\pi^2} |M_a|^2 + \frac{1}{8\pi^2} \frac{3}{5} Y g_1^2 S, \quad (26)$$

where  $M_a$  denote the gaugino masses,  $C_2 = 3/4$  and  $Y = -1/2$  for the doublet sleptons, and  $C_2 = 0$  and  $Y = 1$  for the right-handed selectrons.  $S$  is given by,

<sup>12</sup> We appreciate S. Shirai for pointing out the unsuppressed two-loop contributions.

<sup>13</sup> Our results for the two-loop contribution disagrees with the results given in Ref. [12]. In the renormalization scheme in Ref. [12], a superpotential term,  $ZH_u\tilde{\Phi}_L$ , is regenerated due to the radiative kinetic mixing. To eliminate such an unwanted term, we need to do unitary transformation as performed in Eq. (7), which leads to the discrepancy between our results and the one in Ref. [12]. The detailed derivation will be discussed in a separate paper [18].

<sup>14</sup> As pointed out in Ref. [19] there are subtleties in deriving the soft masses by analytically continuing the wave function renormalization factor. However, since our model only has a single pair of messengers, it evades the concerns presented in Ref. [19].

<sup>15</sup> Although we do not discuss the solution to the so-called  $\mu$ -problem in this Letter, we may further extend the Higgs sector so that  $\mu$  and  $B$  are generated with similar size in a  $CP$ -safe way [15]. We may also solve the  $\mu$ -problem by introducing an appropriate Peccei–Quinn  $U(1)$  symmetry [16].

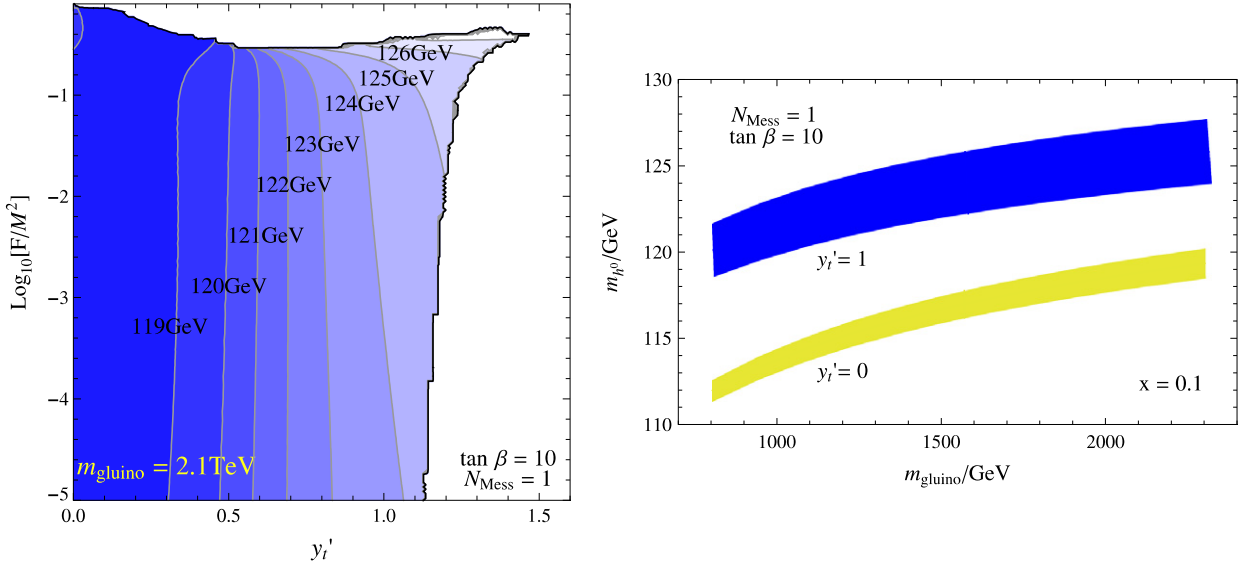
<sup>16</sup> In the above expression, we have neglected the stop mixing from the  $\mu$ -term since it is suppressed for  $\tan \beta \gtrsim 10$ .

<sup>17</sup> The uncertainty of the lightest Higgs boson mass is estimated to be about 2–5 GeV [22].

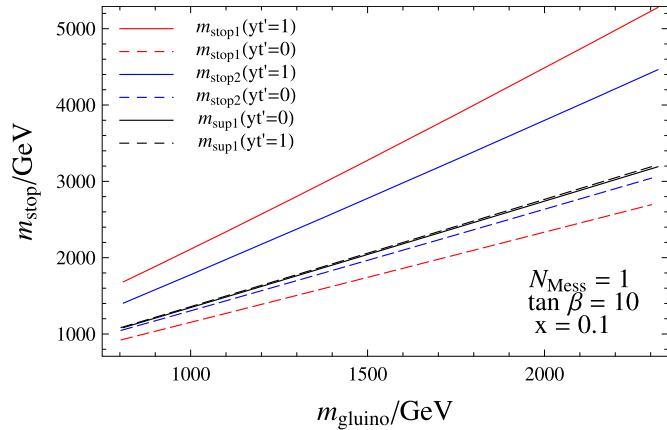
<sup>18</sup> The origin of the tachyonic slepton is discussed below.

<sup>19</sup> The Higgs mass can be further enhanced beyond what is shown. However, this may lead to a Landau pole below the Planck scale.

<sup>20</sup> Detailed phenomenological analysis will be given elsewhere.



**Fig. 3.** (Left) The contour plot of the lightest Higgs boson mass for  $m_{\text{gluino}} \simeq 2.1$  TeV,  $\tan \beta = 10$ ,  $N_{\text{mess}} = 1$  and  $m_t = 173.2$  GeV. The blank region for  $x \simeq 1$  is mainly excluded because of tachyonic stop masses. The blank region for  $y_t' \gtrsim 1$  and  $x \ll 1$  is excluded by the tachyonic slepton masses. The blue band corresponds to the parameters, i.e.  $y_t' = 1$  and  $x = 0.1$ . We also show the upper bound for conventional models of gauge mediation, i.e.  $y_t' = 0$  (yellow band). The upper and the lower boundaries of the each band correspond to the upper and the lower limits of the current world average top mass,  $m_t = 173.2 \pm 0.9$  GeV [23]. The relatively broad band in Type-II gauge mediation represents the fact that our reference point ( $y_t' = 1.0$ ,  $x = 0.1$ ) is not the optimal Higgs mass point for a given value of  $m_t$ . (For interpretation of the references to color in this figure, the reader is referred to the web version of this Letter.)

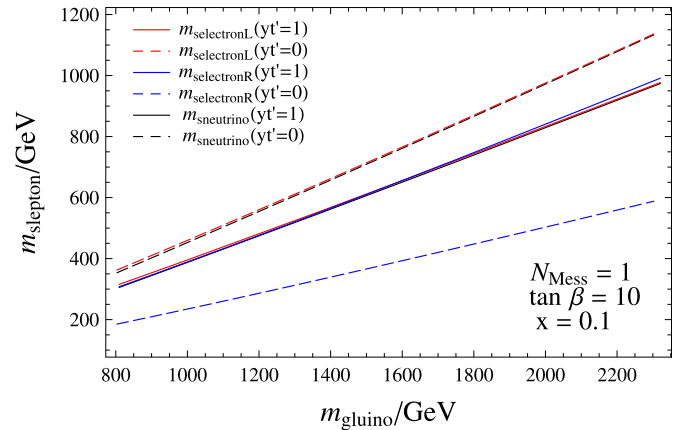


**Fig. 4.** The masses of the stops in Type-II models (solid lines) for  $y_t' = 1$  and  $x = 0.1$  and for conventional models of gauge mediation (dashed lines). The red and blue lines correspond to the masses of two stops. For comparison, we show the sup masses for both models (black lines), however, there is no difference in these masses for the two types of models. In this figure, we have used  $m_t = 173.2$  GeV. (For interpretation of the references to color in this figure, the reader is referred to the web version of this Letter.)

$$\begin{aligned} S = \text{tr}[Y_i m_i^2] &= m_{H_u}^2 - m_{H_d}^2 \\ &+ \text{tr}[m_Q^2 - m_L^2 - 2m_U^2 + m_D^2 + m_E^2]. \end{aligned} \quad (27)$$

The purely gauge mediated contributions to the above expression cancel at the messenger scale. As we have discussed, the two-loop contributions to  $m_{Q_{3,\bar{T}}}^2$  in Eq. (23) are large and positive for  $y_t' \gtrsim 1$ , giving a negative  $S$ . Therefore, through the renormalization group equations, the doublet sleptons become lighter at the low energy scale, while the right-handed selectrons become heavier.<sup>21</sup>

In Fig. 5, we show the slepton masses for  $y_t' = 1$  and  $x = 0.1$ . The figure shows that the right-handed selectrons are heavier than



**Fig. 5.** The masses of the sleptons in Type-II models (solid lines) for  $y_t' = 1$  and  $x = 0.1$  and for conventional models of gauge mediation (dashed lines). The red and blue lines correspond to the masses of two sleptons. The black lines correspond to the sneutrino mass. The figure shows that the right-handed selectron mass is larger than that in the conventional models, while the left-handed selectron and the sneutrino masses are smaller than those in the conventional models. The degeneracy of the slepton masses are just coincidence due to the choice of the parameter. In this figure, we have used  $m_t = 173.2$  GeV. (For interpretation of the references to color in this figure, the reader is referred to the web version of this Letter.)

those in conventional gauge mediation models, while the left-handed selectron and sneutrino are lighter than expected. This peculiar slepton mass spectrum also provides an important clue for probing Type-II gauge mediation models.

In the above analysis, we considered relatively large Yukawa coupling,  $y_t' \simeq 1$ . One might think that such a large Yukawa coupling has a Landau pole problem well below the GUT scale. A Landau pole in the RG running of the Yukawa coupling, however, does not occur. First of all, the Yukawa coupling  $y_t'$  is only important for renormalization group scales larger than messenger scale,  $M$ . For such large energy scales, Eq. (6) is a valid description of the model. Thus, if the other coupling constants  $g$  and  $g'$  are rather

<sup>21</sup> The squark masses also receive the similar size of the renormalization group effects from  $S$  with the signs depending on their  $U(1)$  hypercharges.

small,  $g \sim g' \ll 1$ , the only relevant Yukawa interaction in the high energy theory is

$$W = \tilde{y}_t \tilde{H}_u Q_L \tilde{T}_R, \quad (28)$$

which is just the Yukawa coupling constant of the top quarks. This coupling is related to the low scale parameters as follows

$$\tilde{y}_t = \sqrt{y_t^2 + y_t'^2}. \quad (29)$$

Since  $y_t$  at the messenger scale is around  $y_t \sim 0.6\text{--}0.8$ ,  $\tilde{y}_t$  does not significantly exceed  $\tilde{y}_t = 1$  even for  $y_t' \simeq 1$ . Therefore, the coupling constant  $\tilde{y}_t$  will be perturbative up to the GUT scale.

Finally, let us comment on the effects of the other parameters. In the figures, we have taken  $\tan\beta = 10$ . The Higgs mass prediction is, however, almost independent of the choice of  $\tan\beta$  as long as  $\tan\beta \gtrsim 10$ .<sup>22</sup> We also find that the predicted Higgs boson mass is almost unchanged if we change the sign of the  $\mu$ -term, since the  $\mu$ -term contribution to the stop mixing is suppressed by  $1/\tan\beta$ .

#### 4. Conclusions and discussions

In this Letter, we discussed more generic models of gauge mediation where the messengers are allowed to mix with the Higgs doubles via a “charged” coupling constant. Although the messengers couple to the MSSM matter fields at the weak scale, the flavor structure of these couplings is determined and is aligned to the MSSM Yukawa couplings. Because of this alignment, the mixing does not cause any serious flavor changing neutral current problems.

A distinguishing feature of these models with Higgs-messenger mixing is a one- and two-loop soft supersymmetry breaking mass for the sfermions proportional to the Yukawa couplings. Because of the hierarchy of the Yukawa couplings, the most important contribution is to the stops. This important one-loop stop mass together with a relatively large stop  $A$ -term gives a unique superparticle and Higgs boson mass spectrum. Particularly, we showed that the lightest Higgs boson can be as heavy as 125 GeV, for example, with a gluino mass of around 2 TeV. This is a remarkable difference from the situation in conventional gauge mediation models where the lightest Higgs boson mass cannot exceed 120 GeV for a gluino mass in reach of the LHC. Notice that the particle content in our model is the same as in the minimal gauge mediation. We also found that in regions with an enhanced Higgs boson mass, the stops are heavier than those predicted by conventional gauge mediation.

We should also note that the predictions of heavy stops, sleptons with a large left–right mass splitting, and a heavy lightest Higgs boson mass is unique to these models. The Next-to-MSSM (NMSSM) can also predict a relatively heavy lightest Higgs boson (see for example Ref. [26]), but when combined with gauge mediation has the vanilla mass spectrum of conventional gauge mediation. This is because the stop and slepton masses are unaffected by the additional fields of the NMSSM. Therefore, the interplay between the SUSY particle searches and the Higgs searches are quite important for probing Type-II gauge mediation. We should note here that if we combine our mechanism with the NMSSM, the Higgs mass may be raised up to 140 GeV for example [18].

Finally, let us comment on other interesting features of Type-II gauge mediation models. In this Letter, we were mainly concerned

with the parameter space which maximized the lightest Higgs boson mass, i.e.  $m_{h^0} \gtrsim 120$  GeV. It should also be noted that the LEP bound on the Higgs boson mass,  $m_h^0 \gtrsim 114$  GeV, is easily satisfied even for a gluino mass,  $m_{\text{gluino}} \lesssim 1$  TeV in Type-II gauge mediation (see Fig. 3). Therefore, in this case, SUSY particles may be discovered in the near future at the LHC experiments.

As another interesting possibility for these models, the  $\mu$ -term can be relatively small while keeping the Higgs boson mass above the current lower limit,  $m_{h^0} \gtrsim 114$  GeV. This peculiar mass spectrum is made possible by the negative one-loop contributions to the stops mass and the relatively large  $A$ -terms for  $x \simeq 1$  (for related discussion see Refs. [27,28]).

#### Note added

After the present Letter was posted on arXiv (arXiv:1107.3006), ATLAS and CMS experiments reported excesses in the Higgs boson searches in the mass range of  $m_{h^0} = 120\text{--}140$  GeV at a confidence levels close to  $3\sigma$  [29]. Such a heavy lightest Higgs boson mass favors Type-II gauge mediation with  $y_t' \simeq 1$  if the SUSY particles are also found at LHC experiments in the near future.

#### Acknowledgements

We would like to thank Matt Sudano and Satoshi Shira for useful discussions. This work was supported by the World Premier International Research Center Initiative (WPI Initiative), MEXT, Japan. The work of T.T.Y. was supported by JSPS Grand-in-Aid for Scientific Research (A) (22244021).

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<sup>22</sup> The large  $\tan\beta$  is favorable to explain the observed discrepancy of the observed muon anomalous magnetic moment from the SM prediction [25]. A detailed analysis is in preparation [18].

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