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A composition-based cartilage model for the assessment of compositional changes during cartilage damage and adaptation

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Summary

Objective: The composition of articular cartilage changes with progression of osteoarthritis. Since compositional changes are associated with changes in the mechanical properties of the tissue, they are relevant for understanding how mechanical loading induces progression. The objective of this study is to present a computational model of articular cartilage which enables to study the interaction between composition and mechanics.

Methods: Our previously developed fibril-reinforced poroviscoelastic swelling model for articular cartilage was combined with our tissue composition-based model. In the combined model both the depth- and strain-dependencies of the permeability are governed by tissue composition. All local mechanical properties in the combined model are directly related to the local composition of the tissue, i.e., to the local amounts of proteoglycans and collagens and to tissue anisotropy.

Results: Solely based on the composition of the cartilage, we were able to predict the equilibrium and transient response of articular cartilage during confined compression, unconfined compression, indentation and two different 1D-swelling tests, simultaneously.

Conclusion: Since both the static and the time-dependent mechanical properties have now become fully dependent on tissue composition, the model allows assessing the mechanical consequences of compositional changes seen during osteoarthritis without further assumptions. This is a major step forward in quantitative evaluations of osteoarthritis progression.

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Key words: Cartilage, Permeability, Intra-fibrillar, Depth-dependent, Finite element analysis.

Introduction

Articular cartilage covers the articulating ends of diarthrodial joints. It serves to allow almost frictionless motion, distribute the loads over a large contact area, and dissipate the energy associated with dynamic loads. Osteoarthritis which involves degeneration of the articular cartilage is the most common cause of disability in the elderly. During this disease both the structure and composition of articular cartilage change. Computer models have been successful in predicting the initial changes that occur during cartilage damage initiation^{1–3}. To study the influence of these changes on the progression of cartilage damage, which is mostly induced by excessive loading at high loading rates, a model is needed that can take into account local changes in tissue constitution as well as the transient mechanical tissue behavior. Therefore the goal of this study was to develop a model for articular cartilage in which all local material properties that determine the equilibrium and the transient behavior are the direct consequence of the local composition of the tissue. Such a model enables

us to study the influence of local changes in composition that occur during cartilage degeneration and adaptation.

We have recently developed a model in which the equilibrium behavior of articular cartilage is the direct result of its local composition⁴. With this model we were able to explain the depth- and strain-dependent equilibrium behavior of articular cartilage during confined compression. To be able to account for the transient behavior as well, the model must be extended to include viscoelastic behavior. This essential model extension requires validation with experimental data from literature.

Two distinct mechanisms are responsible for the viscoelastic behavior of articular cartilage^{5–7}: the frictional drag force of interstitial fluid flow through the porous solid matrix (i.e., the flow-dependent mechanism) and the time-dependent deformability of the solid matrix (i.e., the flow-independent mechanism). Fluid movement in loaded cartilage is governed by the hydraulic permeability of the solid matrix. It was shown that the negative fixed charge density of the proteoglycans limits fluid flow and thereby affects the permeability of the tissue^{8–11}. The permeability is also highly dependent on pore sizes in the extracellular matrix^{10–14}. When the tissue is deformed the fixed charge density and pore sizes change^{8,10,11,14,15}. Hence, the permeability of cartilage is strain-dependent. It has also been shown that the permeability in articular cartilage is depth-dependent^{16,17}.

Several empirical equations for deformation-dependent permeability of cartilage have been proposed^{13,15,18,19}. In these empirical equations the permeability is based on the changes in fluid content of the tissue. However, not all the fluid is able to flow out freely. Part of the water in the tissue

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is absorbed by the collagen fibrils^{20–23}. It has been shown that the amount of intra-fibrillar water depends on the osmotic pressure in the tissue²³. As the osmotic pressure is highly dependent on volumetric strain, this introduces an additional strain-dependency of the permeability.

We hypothesize that if the properties of the constituents of articular cartilage are chosen correctly, the appropriate global and depth-dependent cartilage behavior, including permeability, results from the composition of the tissue.

To assess this hypothesis a relation between permeability and tissue composition is derived. This relation together with a new viscoelastic law for the collagen fibrils will be implemented in the model of Wilson *et al.*⁴. To determine the unknown material parameters and to validate the model, the model was fitted to confined compression, unconfined compression and indentation data of DiSilvestro and Suh²⁴ and to 1D-swelling data of Wilson *et al.*⁴ and Eisenberg and Grodzinsky²⁵.

Methods

MODEL

In the fibril-reinforced poroviscoelastic swelling theory^{4,26}, articular cartilage is assumed as biphasic, consisting of a porous solid matrix saturated with water. The porous solid matrix consists of a swelling nonfibrillar part which contains mainly proteoglycans, and a fibrillar part representing the collagen network. According to Wilson *et al.*⁴ the total tissue stress is given by

$$\sigma_{tot} = -\mu_f \mathbf{I} + n_{s,0} \left(\left(1 - \sum_{i=1}^{toft} \rho_c^i \right) \sigma_{nf} + \sum_{i=1}^{toft} \rho_c^i \sigma_f^i \right) - \Delta\pi \mathbf{I}, \quad (1)$$

where μ_f is the water chemical potential, \mathbf{I} the unit tensor, $\Delta\pi$ the osmotic pressure gradient, $n_{s,0}$ the initial solid volume (in the unloaded and nonswollen state), σ_{nf} the stress in the nonfibrillar matrix, σ_f^i the fibril stress in the i th fibril with respect to the global coordinate system, $toft$ the total number of fibril compartments included, and ρ_c^i the volume fraction of the collagen fibrils in the i th direction with respect to the total solid volume.

Fibrillar part

The fibril stress tensor is given by⁴

$$\sigma_f = \frac{\lambda}{J} P_f \vec{e}_f \vec{e}_f, \quad (2)$$

where J is the determinant of the deformation tensor \mathbf{F} , λ the elongation of the fibril, P_f the first Piola–Kirchhoff fibril stress, and \vec{e}_f the current fibril direction. In Wilson *et al.*²⁶ the viscoelastic behavior of the collagen fibrils was represented by a linear spring S_1 , parallel to a nonlinear spring S_2 in series with a linear dashpot with dashpot constant η (Fig. 1). Hence, the equilibrium stiffness of the collagen fibrils was assumed to be strain-independent. However, Charlebois *et al.*²⁷ have shown that the equilibrium stiffness of the collagen fibrils is strain-dependent. Therefore, the mechanical behaviors of springs S_1 and S_2 were replaced by the two-parameter exponential stress–strain relationships^{28–31}

$$\begin{aligned} P_1 &= E_1 (e^{k_1 \epsilon_f} - 1) & \text{for } \epsilon_f > 0 \\ P_1 &= 0 & \text{for } \epsilon_f \leq 0 \end{aligned} \quad (3)$$

and

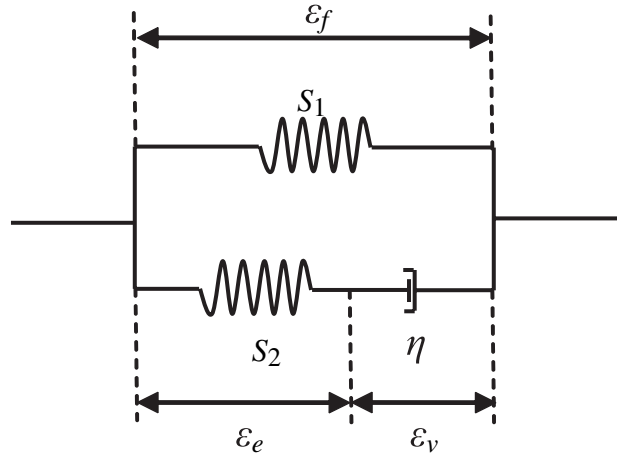


Fig. 1. Schematic model for a viscoelastic collagen fibril (ϵ_f is the total fibril strain, ϵ_v the dashpot strain and ϵ_e the strain in spring S_2).

$$\begin{aligned} P_2 &= E_2 (e^{k_2 \epsilon_e} - 1) & \text{for } \epsilon_e > 0 \\ P_2 &= 0 & \text{for } \epsilon_e \leq 0 \end{aligned} \quad (4)$$

respectively, with E_1 , E_2 , k_1 and k_2 positive material constants, ϵ_f the total fibril strain, and ϵ_e the strain in spring S_2 . Since the strains in the upper and lower part of the spring system in Fig. 1 are the same, the total fibril stress is given by

$$P_f = P_1 + P_2. \quad (5)$$

The derivation of P_2 as a function of the fibril strain ϵ_f is given in Appendix A.

As discussed in Wilson *et al.*²⁶ the fibril structure was implemented as two primary and seven secondary fibril directions. The density of each fibril with respect to the total collagen density is given by

$$\begin{aligned} \rho_c &= \rho_{c,tot} \frac{C}{2C+7} & \text{for the primary fibrils} \\ \rho_c &= \rho_{c,tot} \frac{1}{2C+7} & \text{for the secondary fibrils} \end{aligned} \quad (6)$$

with C a positive constant greater than 1. For the determination of the fibril strains and directions, the reader is referred to Wilson *et al.*^{26,32}.

Nonfibrillar part

Although the solid material itself is virtually incompressible due to its porous structure, the entire solid matrix is compressible. For a solid fraction of 1 there are no pores, hence the entire matrix has become incompressible. As the solid fraction approaches 0 the volume fraction of the pores approaches 1. Because the pores themselves are fully compressible the entire solid matrix is also fully compressible. Based on the assumption that the solid matrix becomes incompressible when the solid fraction approaches 1 and becomes fully compressible when the solid fraction approaches 0, the stress in the nonfibrillar solid matrix is given by following modified Neo-Hookean law⁴,

$$\begin{aligned} \sigma_{nf} &= \frac{1}{6} \frac{\log(J)}{J} G_m \mathbf{I} \left[-1 + \frac{3(J + n_{s,0})}{(-J + n_{s,0})} + \frac{3 \log(J) J n_{s,0}}{(-J + n_{s,0})^2} \right] \\ &+ \frac{G_m}{J} (\mathbf{F} \cdot \mathbf{F}^T - J^2/3 \mathbf{I}), \end{aligned} \quad (7)$$

where G_m is the shear modulus.

Osmotic swelling

For the swelling behavior the biphasic swelling theory^{26,33} was used. This theory is based on the hypothesis that electrolyte flux can be neglected in mechanical studies of charged materials³⁴. This means the ion concentrations can always be assumed in equilibrium.

When the distinction between extra- and intra-fibrillar water is taken into account, the effective fixed charge density should be expressed as mEq fixed charges per ml extra-fibrillar water and not based on the total fluid content as is usually done. The osmotic pressure gradient $\Delta\pi$ is then given by⁴

$$\Delta\pi = \phi_{\text{int}} RT \sqrt{c_{\text{F,exf}}^2 + 4 \frac{(\gamma_{\text{ext}}^{\pm})^2}{(\gamma_{\text{int}}^{\pm})^2} c_{\text{ext}}^2 - 2\phi_{\text{ext}} RT c_{\text{ext}}}. \quad (8)$$

where the fixed charge density based on the extra-fibrillar fluid fraction $c_{\text{F,exf}}$, is given by

$$c_{\text{F,exf}} = \frac{n_{\text{f}} c_{\text{F}}}{n_{\text{exf}}}, \quad (9)$$

with n_{f} the total fluid fraction, n_{exf} the extra-fibrillar fluid fraction and c_{F} the normal fixed charge density in mEq per ml total fluid. For more details about determining the extra-fibrillar fluid fraction the reader is referred to Wilson *et al.*⁴. The osmotic (ϕ_{α}) and activity coefficients (γ_{α}) were implemented as proposed by Huyghe *et al.*³⁵. The external salt concentration (c_{ext}) was 0.15 M, the temperature (T) 293 K and the gas constant (R) 8.3145×10^{-3} N m/mmol K.

Permeability

In Wilson *et al.*^{26,32} the permeability (k) was assumed to be strain-dependent, and given by³⁶

$$k = k_0 \left(\frac{1+e}{1+e_0} \right)^M = k_0 \left(\frac{1-n_{\text{f},0}}{1-n_{\text{f}}} \right)^M, \quad (10)$$

where k_0 is the initial permeability, M a positive constant, and e and e_0 the current and initial void ratios, respectively, and n_{f} and $n_{\text{f},0}$ the current and initial fluid fractions, respectively. When accounting for the fact that only the extra-fibrillar fluid can flow out of the tissue, this becomes

$$k = k_0 \left(\frac{1-n_{\text{exf},0}}{1-n_{\text{exf}}} \right)^M. \quad (11)$$

Based on the assumption that the depth- and strain-dependent permeabilities are governed by the same mechanism, the initial extra-fibrillar fluid fraction $n_{\text{exf},0}$ is replaced by a reference value c_{ref} that is constant over the depth of the tissue

$$k = k_0 \left(\frac{1-c_{\text{ref}}}{1-n_{\text{exf}}} \right)^M = \alpha (1-n_{\text{exf}})^{-M}, \quad (12)$$

with α a positive material constant. Hence, the permeability is only a function of the current extra-fibrillar fluid fraction.

Composition

The fluid fraction, collagen fraction and fixed charge density distributions as a function of the normalized depth z^* were taken the same as in Wilson *et al.*⁴.

$$n_{\text{f}} = 0.9 - 0.2z^*, \quad (13)$$

$$n_{\text{coll}} = 1.4(z^*)^2 - 1.1z^* + 0.59, \quad (14)$$

$$c_{\text{F}} = -0.10(z^*)^2 + 0.24z^* + 0.035, \quad (15)$$

where n_{f} is the total fluid volume fraction, n_{coll} the collagen density per solid volume, and c_{F} the fixed charge density in mEq/ml water.

The model was implemented in ABAQUS v6.5-1 (Hibbit, Karlsson & Sorensen, Inc., Pawtucket, RI, USA). For more details about this model see Wilson *et al.*^{4,26,32}.

DETERMINATION OF UNKNOWN MATERIAL PROPERTIES

Based on Wilson *et al.*²⁶ we used $C = 3$ [Eq. (6)]. The factor M was directly determined by fitting Eq. (12) to the depth-dependent permeability as measured by Maroudas¹⁷. The shear modulus G_{m} was determined by fitting the model to the 1D-swelling data from Eisenberg and Grodzinsky²⁵. The remaining unknown material parameters E_1 , E_2 , k_1 , k_2 , η_0 and α were determined by fitting them to the confined compression, unconfined compression and indentation data of DiSilvestro and Suh²⁴ and the 1D-swelling data of Wilson *et al.*⁴. The fitting procedures were the same as used in Wilson *et al.*^{4,26,32}. For the confined compression, unconfined compression and indentation tests the same meshes and boundary conditions were used as in Wilson *et al.*²⁶. For the 1D-swelling tests the same meshes and boundary conditions were used as in Wilson *et al.*⁴. The experiments are briefly described below.

In the 1D-swelling test of Wilson *et al.*⁴ the free swelling strains of articular cartilage were measured as a function of the external salt concentration at 0.00, 0.07, 0.15, 0.30, 0.67, 1 and 2 M NaCl. The swelling strain was assumed to be 0 at an external salt concentration of 2 M NaCl. These tests were performed on cartilage from calf tibia plateaus with an average thickness of 1.03 mm.

In the 1D-swelling experiments of Eisenberg and Grodzinsky²⁵ cartilage plugs with a radius of 3.2 mm were axially compressed by 15% in a confined compression setup. After full relaxation, the external salt concentration was decreased to 0.0001 M. After equilibrium the salt concentration was repeatedly increased with 0.05 M until an external salt concentration of 2 M was reached. During this process the height of the sample was held constant, while the axial reaction forces were computed. The used samples were taken from the patellae-femoral groove of mature 1–2-year-old cattle.

During the confined compression, unconfined compression and indentation test of DiSilvestro and Suh²⁴, cartilage plugs with a radius of 1.5 mm and an average thickness of 1.281 mm were compressed with 10% either a flat platen (confined and unconfined compression) or a spherical impermeable indenter with a radius of 1.53 mm (indentation). After full relaxation, an additional 5% strain at a ramp strain rate of 0.001 s⁻¹ was applied. This strain was held constant until full relaxation. While the additional 5% straining and relaxation occurred, axial reaction forces were computed. The used samples were taken from the patellae of mature 1–2-year-old cattle.

Results

DETERMINATION OF UNKNOWN MATERIAL PROPERTIES

The depth-dependent permeability of the model [Eq. (12)] was fitted to experimental data of Maroudas¹⁷ (Fig. 2). The resulting value for M was 1.339.

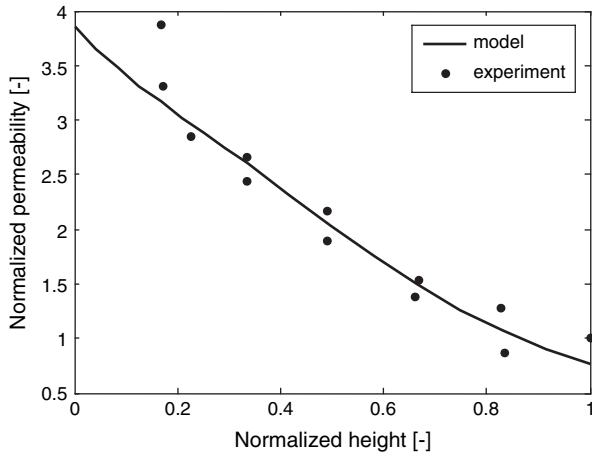


Fig. 2. Depth-dependent permeability as measured by Maroudas *et al.* (1976) along with the FEA-model curve fit.

The fit of the model to the 1D-swelling data of Eisenberg and Grodzinsky²⁵ resulted in a value for G_m of 0.903 MPa. The normalized reaction force was almost in perfect agreement with the experimental data [Fig. 3(a)].

The remaining unknown material parameters E_1 , E_2 , k_1 , k_2 , η_0 and α were determined by fitting the confined compression, unconfined compression and indentation data of DiSilvestro and Suh²⁴, and 1D-swelling data of Wilson *et al.*⁴ (Figs. 3(b)–6). The resulting model parameters were determined at $E_1 = 4.316$ MPa, $E_2 = 19.97$ MPa, $k_1 = 16.85$, $k_2 = 41.49$, $\eta = 1.424 \times 10^5$ MPa s and $\alpha = 1.767 \times 10^{-17}$ m⁴/N s.

All model fits were in good agreement with the experimental data. The coefficients of determination (R^2) for the different fits are given in Table I.

Discussion

The goal of this study was to develop a model for articular cartilage in which all local material properties are the direct consequence of the local composition of the tissue. Such a model enables us to study the influence of local changes in composition that occur during cartilage degeneration and adaptation. To do this our fibril-reinforced poroviscoelastic swelling model for articular cartilage²⁶ was combined with our tissue composition-based model⁴, and expanded with a new permeability law and a new law for the viscoelastic behavior of the collagen network. The new permeability law is based on the assumption that both the depth- and strain-dependencies of the permeability are governed by the same mechanism and are the direct result of the composition of the tissue. We have previously shown that this model can account for the strain-dependent compressive equilibrium properties of articular cartilage during confined compression⁴. In the current study it has been shown that this model can also account for the transient behavior of articular cartilage. It was shown that the combined model can simultaneously describe the behavior of articular cartilage in confined compression, unconfined compression, indentation and two different 1D-swelling tests. With the proposed permeability law, the strain-dependent permeability of articular cartilage can be explained. There is no literature data available to compare directly to the strain-dependent permeability.

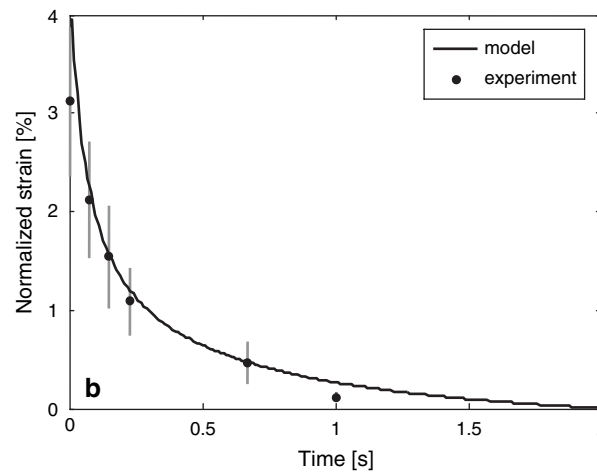
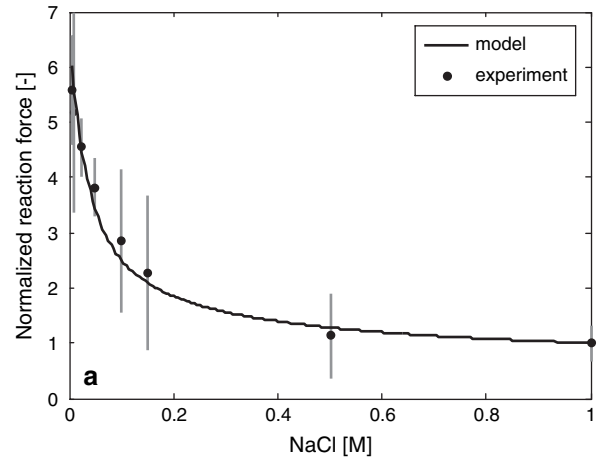


Fig. 3. (a) Axial reaction force, normalized with the reaction force at an external salt concentration of 2 M, measured from 1D swelling tests (Eisenberg and Grodzinsky, 1985) along with FEA-model curve fit. (b) Axial strain measured from 1D free swelling tests (Wilson *et al.*, 2005c) along with FEA-model curve fit.

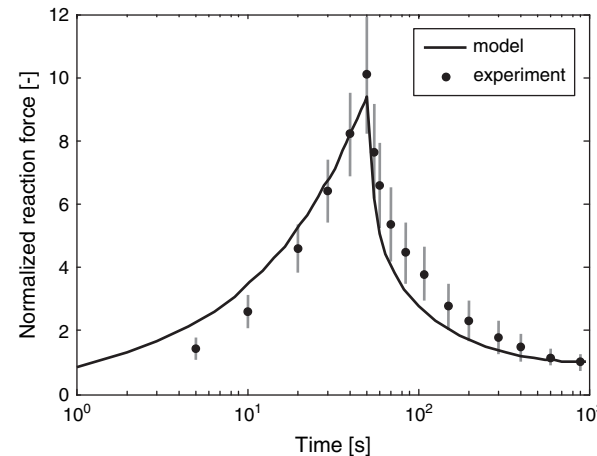


Fig. 4. Axial reaction force, normalized to equilibrium, measured from confined compression tests²⁴ along with FEA-model curve fit.

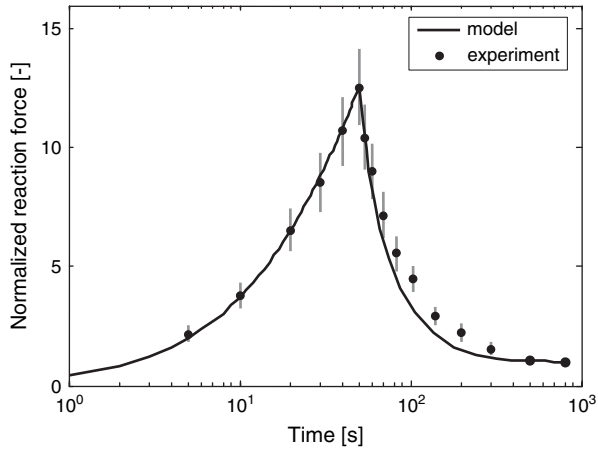


Fig. 5. Axial reaction force, normalized to equilibrium, measured from indentation tests²⁴ along with FEA-model curve fit.

However, since the resulting strain- and time-dependent behavior of the model concur with the experimental data, it is concluded that the strain-dependent permeability in the model is correct.

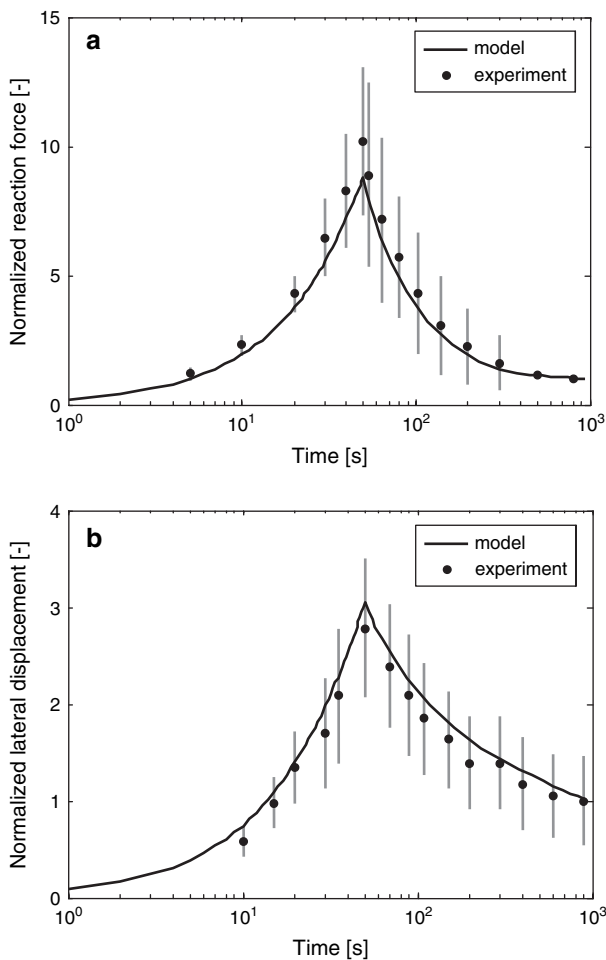


Fig. 6. (a) Axial reaction force, normalized to equilibrium, measured from unconfined compression tests²⁴ along with fibril-reinforced model curve fit. (b) Lateral displacement, measured from unconfined compression tests²⁴ along with FEA-model curve fit.

Table I
The coefficients of determination (R^2) for the performed model fits

Test	R^2
Permeability ¹⁷	0.930
1D-swelling confined swelling ²⁵	0.977
1D-swelling free swelling ⁴	0.980
Confined compression ²⁴	0.938
Unconfined compression (reaction force) ²⁴	0.998
Unconfined compression (lateral displacement) ²⁴	0.987
Indentation ²⁴	0.985

All material parameters (G_m , E_1 , E_2 , k_1 , k_2 , η_0 , α and M) were assumed constant over the depth of the tissue and were derived from fits to experimental data. Hence, all depth-dependent behavior is due to the depth-dependent tissue composition and structure. As the tissue composition was not measured in experiments that were used to fit our material parameters, we were obliged to base the prescribed tissue composition on distinct literature data. Due to this there might be an error in the obtained material parameters.

Viscoelastic and anisotropic properties of the biphasic nonfibrillar matrix⁵ were not included in this model. Although we anticipate that the major viscoelastic and anisotropic properties of the solid matrix come to the account of the fibrillar part, this may also explain part of the mismatches between the model and the experimental data.

As we used a biphasic swelling model the influence of ion fluxes on the transient behavior of articular cartilage have not been included in this study. However, as it was shown in Wilson *et al.*³³ that under physiological conditions the biphasic swelling model behaves very similar to the full mechano-electrochemical model, it is assumed that this does not significantly influence our results.

To the best of our knowledge this is the first model that includes a continuous depth-dependent permeability that is based on the tissue composition, with constant, not depth-dependent mechanical properties of the tissue components themselves. Previously, depth-dependent permeability was included by directly defining different permeability values for different layers of the tissue^{38,39}.

In conclusion, our recently developed composition-based cartilage model⁴ was expanded with a new permeability law and a new law for the viscoelastic behavior of the collagen network of articular cartilage. In the new permeability law the permeability is only dependent on the extra-fibrillar fluid fraction. With this law both the depth- and strain-dependent permeabilities of articular cartilage can be explained based on the composition of the tissue, with constant material properties for the tissue constituents themselves. In the resulting model all local material properties are the direct consequence of the local composition and structure of the tissue. This new model will enable us to study the influence of well-characterized local changes in composition that can occur during cartilage degeneration and adaptation.

Acknowledgments

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Appendix A. Determination of the viscoelastic fibril stress

The stresses in the dashpot and the spring S_2 in Fig. 1 must be the same. Hence, P_2 can also be given by

$$P_2 = \eta \dot{\varepsilon}_v = \eta (\dot{\varepsilon}_f - \dot{\varepsilon}_e), \quad (\text{A1})$$

where ε_v is the dashpot strain, and η the dashpot constant. From Eq. (4) follows that

$$\varepsilon_e = \frac{1}{k_2} \log \left(\frac{P_2}{E_2} + 1 \right), \quad \dot{\varepsilon}_e = \frac{\dot{P}_2}{(P_2 + E_2)k_2}. \quad (\text{A2})$$

The time derivative of the fibril strain is then given by

$$\dot{\varepsilon}_f = \dot{\varepsilon}_e + \dot{\varepsilon}_v = \frac{\dot{P}_2}{(P_2 + E_2)k_2} + \frac{P_2}{\eta}. \quad (\text{A3})$$

From Eqs. (A1) and (A3), and after time integration with an implicit backward Euler scheme, P_2 becomes

$$P_2 = -\frac{b}{2} + \frac{1}{2} \sqrt{b^2 - 4c} \quad \text{for } \varepsilon_e > 0, \quad (\text{A4})$$

$$P_2 = 0 \quad \text{for } \varepsilon_e \leq 0$$

with

$$b = -\frac{\varepsilon_f^{t+\Delta t} - \varepsilon_f^t}{\Delta t} \eta + \frac{\eta}{k_2 \Delta t} + E_2, \quad (\text{A5})$$

$$c = -\frac{\varepsilon_f^{t+\Delta t} - \varepsilon_f^t}{\Delta t} \eta E_2 - \frac{\eta P_2^t}{k_2 \Delta t}. \quad (\text{A6})$$

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