



King Saud University  
**Journal of the Saudi Society of Agricultural Sciences**

[www.ksu.edu.sa](http://www.ksu.edu.sa)  
[www.sciencedirect.com](http://www.sciencedirect.com)



## FULL LENGTH ARTICLE

# Osmotic dehydration and convective drying of coconut slices: Experimental determination and description using one-dimensional diffusion model



Wilton Pereira da Silva \*, Cleide Maria Diniz Pereira da Silva e Silva,  
 Juarez Everton de Farias Aires, Aluizio Freire da Silva Junior

Center of Sciences and Technology, Federal University of Campina Grande, Brazil

Received 28 March 2013; accepted 22 May 2013

Available online 28 May 2013

### KEYWORDS

Analytical solution;  
 Convective boundary condition;  
 Osmotic dehydration kinetics;  
 Drying kinetics;  
 Optimization

**Abstract** Mass migrations in coconut slices during osmotic dehydration and drying are described using a diffusion model with boundary condition of the third kind. The osmotic dehydration experiment was performed at 35°Brix (water and sucrose) and 40 °C. The convective drying experiments were performed at 50, 60 and 70 °C. The one-dimensional solution of the diffusion equation for an infinite slab was coupled with an optimizer to determine the effective mass diffusivities  $D$  and convective mass transfer coefficients  $h$  of the five processes studied. The analyses of the obtained results indicate that there is a good agreement between each experimental dataset and the corresponding simulation using  $D$  and  $h$  determined by optimization.

© 2013 Production and hosting by Elsevier B.V. on behalf of King Saud University.

## 1. Introduction

Coconut (*Cocos nucifera* L.) is an important agricultural product, which is produced in most countries with wet tropical weather. The coconut palm, also called “life tree”, is highly

tolerant of salinity and it is found on sandy soils, with abundant sunlight and regular rainfall. In 2011, the main producer countries were Indonesia (17.5 million tons), Philippines (15.2 million tons), India (11.2 million tons), Brazil (2.9 million tons) and Sri Lanka with 1.5 million tons (FAO, 2013). The coconut pulp contains, among other, water, carbohydrates, proteins, fat, salts and also vitamins A, B1, B2, B5 and C. Coconut has the following medicinal properties, among others: anti-inflammatory, soothing, moisturizing, nourishing and antioxidant. The coconut palm is cultivated to produce several products including water from green coconut (Ge et al., 2005; Matsui et al., 2008; Yong et al., 2009), oil (Machmüller et al., 2000; Oliveira et al., 2005; Nevin and Rajamohan, 2006; Benjapornkulaphong et al., 2009) and milk (Oliveira et al., 2005) from mature coconut. Its husk is used to obtain activated carbon (Amuda et al., 2007; Tan et al., 2008; Din

\* Corresponding author. Tel.: +55 83 3333 2962.

E-mail addresses: [wiltonps@uol.com.br](mailto:wiltonps@uol.com.br) (W.P. da Silva), [cleidedps@uol.com.br](mailto:cleidedps@uol.com.br) (Cleide Maria Diniz Pereira da Silva e Silva), [juarezeverson@gmail.com](mailto:juarezeverson@gmail.com) (J.E. de Farias Aires), [aluiziofsj.ces@ufcg.edu.br](mailto:aluiziofsj.ces@ufcg.edu.br) (A.F. da Silva Junior).

Peer review under responsibility of King Saud University.



Production and hosting by Elsevier

et al., 2009) or its green coconut shell is used as a natural adsorbent in the removal of toxic metals (Sousa et al., 2007).

In recent years, delicious snacks have been produced from coconut (Lattanzio et al., 2008, 2009). One of these snacks consists, basically, in the removal of water of the coconut pulp, previously cut into small slices (Da Silva et al., 2013a). According to these last authors, after the removal of water from the slices of mature or semi-mature coconut, the snack “dry coconut”, cooled up to room temperature, is ready for consumption. However, the use of hot air to remove water of coconut slices is expensive due to the phase change of this substance from liquid to vapor, once its latent heat of vaporization within the product is very high. Thus, in general, a pre-treatment is accomplished before convective drying. An example of inexpensive pre-treatment is the osmotic dehydration (Conceição Silva et al., 2010; Arballo et al., 2012; Da Silva et al., 2013a). This method consists in the removal of water by immersion of pieces of the product in syrup obtained by mixing water with one or more solutes. The difference in the chemical potential of water between the food and the osmotic medium is the driving force for dehydration (Khin et al., 2006).

Water migration in a product can be described through empirical models (Da Silva et al., 2014) but, according to several authors, osmotic dehydration and convective drying can be considered as diffusion phenomena (Amami et al., 2006; Garcia et al., 2007; Singh et al., 2008; Conceição Silva et al., 2010; Da Silva et al., 2013a). Thus, to describe these processes, the diffusion equation should be used. Da Silva et al. (2013a) have described the mass migrations in coconut slices during osmotic dehydration and convective drying, using a diffusive model which considers the three-dimensional nature of the mass fluxes in each individual piece of the product. This model enables to eliminate a restriction frequently found in the literature, which consists in the consideration of the mass flux in only one direction. However, the time spent in the optimization processes to determine the effective mass diffusivity and convective mass transfer coefficient can be considered very high. In this context, taking account that each piece of coconut is a thin slab, the proposal of a quick and precise model to describe the mass migrations in coconut slices deserves to be considered.

The main objective of this article is to describe the mass migrations in coconut slabs during osmotic dehydration and drying processes, using a one-dimensional diffusion model, including optimization and simulation of the process. To this end, an optimizer was coupled with the one-dimensional analytical solution of the diffusion equation with boundary condition of the third kind. Thus, using experimental datasets, the process parameters were obtained and the kinetics of mass migrations can be simulated and analyzed.

## 2. Materials and methods

### 2.1. Diffusion equation

Osmotic dehydration and thin-layer drying usually are known as diffusion phenomena (Da Silva et al., 2013a). The one-dimensional diffusion equation for an infinite slab is written as (Luikov, 1968; Crank, 1992)

$$\frac{\partial \Phi}{\partial t} = \frac{\partial}{\partial x} \left( D \frac{\partial \Phi}{\partial x} \right), \quad (1)$$

in which  $\Phi$  represents water quantity or sucrose gain (osmotic dehydration) and moisture content (drying), in dry basis (db);  $D$  is the effective mass diffusivity ( $\text{m}^2 \text{s}^{-1}$ );  $t$  is the time (s) and  $x$  is the Cartesian coordinate of position (m).

### 2.2. Analytical solution for the diffusion equation

The convective boundary condition is expressed as follows:

$$-D \frac{\partial \Phi(x, t)}{\partial x} \Big|_{x=\pm L_x/2} = h(\Phi(x, t)|_{x=\pm L_x/2} - \Phi_{eq}). \quad (2)$$

In Eq. (2),  $h$  is the convective mass transfer coefficient ( $\text{ms}^{-1}$ );  $\Phi(x, t)$  is the value of  $\Phi$  in a position  $x$  at instant  $t$ ;  $\Phi_{eq}$  is the equilibrium value for  $\Phi$ ; while  $L_x$  is the thickness of the infinite slab (m).

If it is supposed that the thickness  $L_x$  does not vary during drying; the initial distribution of  $\Phi$  is uniform; the infinite slab is considered homogeneous and isotropic; the process parameters are constant during drying, then Eq. (1) can be analytically solved. For an infinite slab with a uniform initial value  $\Phi_0$  for  $\Phi$  and with a boundary condition defined by Eq. (2), the analytical solution  $\Phi(x, t)$  of Eq. (1) is given by (Luikov, 1968; Crank, 1992):

$$\Phi(x, t) = \Phi_{eq} + (\Phi_0 - \Phi_{eq}) \sum_{n=1}^{\infty} A_n \times \cos \left( \mu_n \frac{x}{L_x/2} \right) \exp \left( - \frac{\mu_n^2}{(L_x/2)^2} Dt \right) \quad (3)$$

in which the origin of the axis  $x$  is located at the central point of the slab. In Eq. (3), the coefficient  $A_n$  is given by

$$A_n = \frac{4 \sin \mu_n}{2\mu_n + \sin(2\mu_n)}, \quad (4)$$

and  $\mu_n$  are the roots of the characteristic equation

$$\cot \mu_n = \frac{\mu_n}{Bi}. \quad (5)$$

In Eq. (5),  $Bi$  is the mass transfer Biot number, given by:

$$Bi = \frac{hL_x/2}{D}. \quad (6)$$

The average value of  $\Phi(x, t)$ , denoted by  $\Phi(t)$ , is given in the following way:

$$\Phi(t) = \Phi_{eq} + (\Phi_0 - \Phi_{eq}) \sum_{n=1}^{\infty} B_n \exp \left( - \frac{\mu_n^2}{(L_x/2)^2} Dt \right), \quad (7)$$

where the parameter  $B_n$  is given by

$$B_n = \frac{2Bi^2}{\mu_n^2(Bi^2 + Bi + \mu_n^2)}. \quad (8)$$

Equation (5) is a transcendental equation which can be solved for a specified mass transfer Biot number. A program in FORTRAN, based on the bisection method, was created and used to calculate the first 16 roots of Eq. (5) for an established mass transfer Biot number. The roots were calculated for 469 Biot numbers from  $Bi = 0$  (which corresponds to an infinite resistance of the water flux at the surface) to  $Bi = 200$  (which practically corresponds to an equilibrium boundary condition).

### 2.3. Determination of the process parameters

To determine  $D$  and  $h$  through the optimization concept, using an experimental dataset, the algorithm developed by Silva et al. (2010) will be adapted for an infinite slab. The objective function to be minimized is given by (Bevington and Robinson, 1992; Taylor, 1997):

$$\chi^2 = \sum_{i=1}^{N_p} [\Phi_i^{\text{exp}} - \Phi_i^{\text{ana}}(D, Bi)]^2 \frac{1}{\sigma_i^2}, \quad (9)$$

where  $\Phi_i^{\text{exp}}$  is the  $i^{\text{th}}$  experimental point of the average value of  $\Phi$ ;  $\Phi_i^{\text{ana}}(D, Bi)$  is the average value of  $\Phi$  obtained analytically at the same point, given as a function of  $D$  and  $Bi$ ;  $\sigma_i$  is the standard deviation of the experimental average moisture content at the point  $i$ ;  $D$  is the effective mass diffusivity; and  $N_p$  is the number of experimental points. For a specified value of  $Bi$ , the chi-square depends only on a single variable, namely the effective mass diffusivity. Thus, optimum values of  $D$  can be determined for each one of the 469  $Bi$  defined for the infinite slab. The better  $D$  is determined by the minimum  $\chi^2$  among the 469 minima calculated. Each one of the 469 optimization processes was accomplished as recommended by Silva et al. (2009). According to these authors, for a stipulated value for  $Bi$ ,  $\Phi_i^{\text{ana}}(D)$  is calculated in each instant  $t$  according to Eq. (7), using the values stipulated for the number of terms (for instance,  $n = 16$ ) and an initial value of  $D$  (for instance,  $10^{-20}$ ). The values of  $\Phi_i^{\text{ana}}(D)$  are used to calculate  $\chi^2$  according to Eq. (9). Then, the value of  $D$  is doubled giving new values for  $\Phi_i^{\text{ana}}(D)$ , which are now used to calculate a new  $\chi^2$ . The value of  $\chi^2$  obtained in the first time is compared with the second value obtained for  $\chi^2$ . If the statement the second  $\chi^2$  is lower than the first  $\chi^2$  is satisfied, the program will continue the previously described procedure, otherwise the program will finish this procedure because an interval that contains a minimum value for chi-square is found. The last three values for  $D$  and  $\chi^2$  are then recorded. The recorded interval of  $D$ , which contains the minimal value of  $\chi^2$ , is then divided into  $n$  equal parts, and each part of this interval is defined as a step. Thus, the  $\chi^2$  of each step is determined, and a more refined interval that contains the minimum is determined. This procedure is repeated until a convergence criterion is satisfied.

### 2.4. Experimental datasets

Semi-mature coconuts (*C. nucifera* L.) were peeled and the dark film adhered in its external part was removed. The product was cut into pieces parallelepiped shaped with the following average dimensions  $L_x = 6.13$ ,  $L_y = 10.12$  and  $L_z = 30.65$  mm. For these dimensions, the coconut pieces were considered, in this article, as infinite slabs with thickness  $L_x$ , in order to describe the water and sucrose migrations within the product. Thus, the results obtained herein can be compared with those obtained considering the typical three-dimensional solution of the diffusion equation (Da Silva et al., 2013a).

#### 2.4.1. Osmotic dehydration

Coconut slices with initial moisture content  $X_0 = 2.33$  ( $\text{kg}_{\text{water}}/\text{kg}_{\text{drymatter}}$ , db) were submitted to osmotic dehydration at 35°Brix (syrup of water and sucrose), at temperature of 40 °C, and the solution movement was achieved using

magnetic stirring with a frequency of 60 Hz. The ratio of the volume of the coconut slices to that of the medium was maintained at 1:20, in order to ensure that the concentration of the osmotic solution does not change significantly during the experiments.

For the osmotic dehydration, the quantities of interest were the water quantity  $W$  within the sample during the osmotic dehydration, and the sucrose gain,  $S$ . The gravimetric method was used to determine  $W$  and  $S$  in each instant  $t$  during the process, up to the equilibrium value. In each instant  $t$ , the weight of a sample was measured, and its dry matter was determined by placing the test sample in a kiln at 105 °C during 24 h. This procedure enables to determine the dry matter at instant  $t$  of each sample that continues immersed in the solution. The equations used to determine  $W$  and  $S$  in each instant  $t$  are given, respectively, by

$$W(t) = \frac{m_W(t)}{m_W(0)} \times 100 \quad (10)$$

and

$$S(t) = \frac{m_S(t)}{m_{d0}} \times 100, \quad (11)$$

where  $m_W(t)$  and  $m_W(0)$  represent the mass of water within the sample at instants  $t$  and zero, respectively;  $m_S(t)$  is the mass of sucrose transferred to the sample up to the instant  $t$  and  $m_{d0}$  is its initial dry matter.

The initial and equilibrium sucrose gain were, respectively,  $S_0 = 0$  and  $S_{\text{eq}} = 8.62\%$  of the initial dry matter. The initial and equilibrium water quantity within the samples was, respectively,  $W_0 = 100\%$  and  $W_{\text{eq}} = 60.6\%$ .

To describe the two processes related to the osmotic dehydration, the generic variable  $\Phi$  should be replaced by  $S$  (sucrose gain) and  $W$  (water quantity) in Eqs. (7) and (9).

#### 2.4.2. Drying

After the osmotic dehydration, where about 39% water was removed, thin-layer convective drying processes were performed using hot air at temperatures of 50, 60 and 70 °C. Average moisture contents  $X$  were determined by the gravimetric method and the equilibrium moisture contents  $X_{\text{eq}}$  at 50, 60 and 70 °C were, respectively, 0.45, 0.18 and 0.07 (db). At the end of each drying, the temperature of a kiln was set at 105 °C, and the product remained there for 24 h, enabling the measurement of the dry matter. The dimensionless moisture content  $X^*$  was determined through Eq. (12):

$$X^*(t) = \frac{X(t) - X_{\text{eq}}}{X_0 - X_{\text{eq}}}, \quad (12)$$

in which  $X_0$  is the initial average moisture content.

To use mathematical model proposed in this article, for the drying description, the replacement of the generic variable  $\Phi$  by the moisture content  $X$  or the dimensionless moisture content  $X^*$  should be performed in Eqs. (7) and (9). In the dimensionless moisture content case, the following values must be imposed in Eq. (7):  $\Phi_0 \equiv X_0^* = 1$  (result of  $X = X_0$  in Eq. (12)) and  $\Phi_{\text{eq}} \equiv X_{\text{eq}}^* = 0$  (result of  $X = X_{\text{eq}}$  in Eq. (12)).

### 2.5. General considerations

Since  $D$  and  $h$  are determined by optimization, Eq. (7) can be used to simulate the process of interest. The analysis of the

results was performed using the statistical indicators: determination coefficient  $R^2$  and chi-square  $\chi^2$ . The optimizer coupled with Eq. (7) was developed in a computer Intel Pentium IV with 2 GB (RAM). The source code was compiled by Compaq Visual Fortran (CVF) 6.6.0 Professional Edition, using the programming option QuickWin Application under the Windows Vista platform. The convergence criterion stipulated for the determination of the effective mass diffusivity was  $1 \times 10^{-15}$ .

During drying, as the thermal diffusivity is much greater than the mass diffusivity, it was considered that the drying process occurs under isothermal conditions. Thus, the effective mass diffusivity as a function of the drying air temperature can be expressed through an Arrhenius-type equation (Nastaj and Witkiewicz, 2009)

$$D = D_0 \exp\left(-\frac{E_a}{R(T + 273.15)}\right). \quad (13)$$

In Eq. (13),  $D_0$  is a pre-exponential factor ( $\text{m}^2 \text{s}^{-1}$ ),  $E_a$  is the activation energy ( $\text{Jmol}^{-1}$ ) and  $R$  is the universal gas constant ( $8.314 \text{ Jmol}^{-1} \text{K}^{-1}$ ). The convective mass transfer coefficient can be also given as a function of the temperature of the drying air by an Arrhenius-type equation:

$$h = a \exp\left[-\frac{b}{(T + 273.15)}\right], \quad (14)$$

where  $a$  and  $b$  are fitting parameters.

### 3. Results and discussion

#### 3.1. Osmotic dehydration

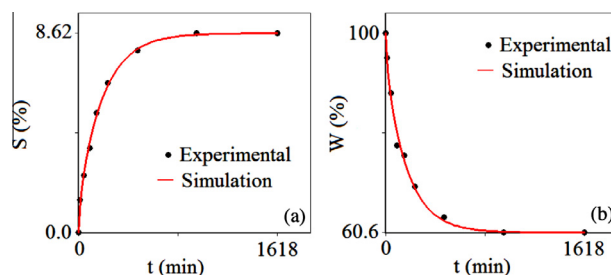
Performing the optimization processes for water quantity and sucrose gain, the obtained results are presented in Table 1. This table also presents the results obtained by Da Silva et al. (2013a) which used a three-dimensional approach to describe water and sucrose migration within the coconut pieces.

Since the process parameters have been obtained by optimization, the simulations of water and sucrose migration are presented, together with experimental datasets, in Fig. 1.

#### 3.2. Drying at $T = 50, 60$ and $70^\circ \text{C}$

##### 3.2.1. Optimizations and simulations

For the drying processes at 50, 60 and  $70^\circ \text{C}$ , the results obtained by optimization are presented in Table 2, which also presents the results obtained by Da Silva et al. (2013a) using a three-dimensional approach.



**Figure 1** Osmotic dehydration kinetics described by one-dimensional model: (a) Sucrose migration; (b) Water migration.

For drying, once the process parameters have been obtained, the simulations of the water migration are presented, together with experimental datasets, in Fig. 2.

##### 3.2.2. Arrhenius-type equations

Using nonlinear regression to fit Eq. (13) to the data ( $T, D$ ) given in Table 2, the following result is obtained:

$$D = 1.03 \times 10^{-2} \exp\left(-\frac{5371}{(T + 273.15)}\right). \quad (15)$$

Comparing Eq. (15) with Eq. (13), the activation energy is obtained:  $E_a = 44.7 \text{ kJ mol}^{-1}$ . On the other hand, Fig. 3 shows the behavior between the effective mass diffusivity and the drying air temperature.

Using nonlinear regression to fit Eq. (14) to the data ( $T, h$ ) obtained in this article (Table 2), the following expression is found:

$$h = 5.30 \times 10^5 \exp\left[-\frac{7799}{(T + 273.15)}\right]. \quad (16)$$

Fig. 4 shows the behavior between  $h$  and  $T$  in the interval  $50\text{--}70^\circ \text{C}$ .

##### 3.3. Discussion

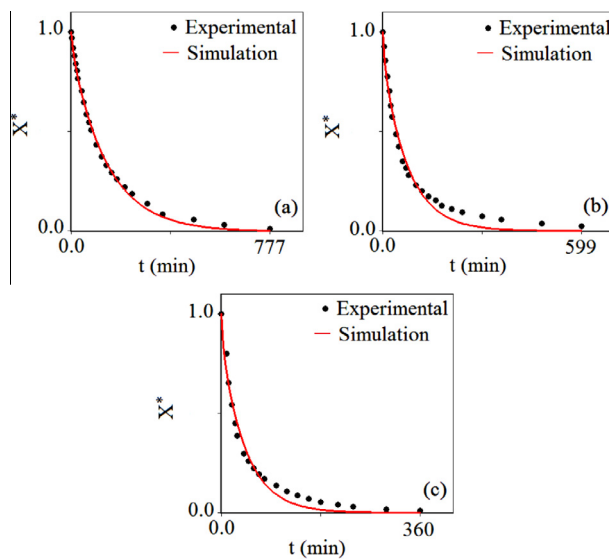
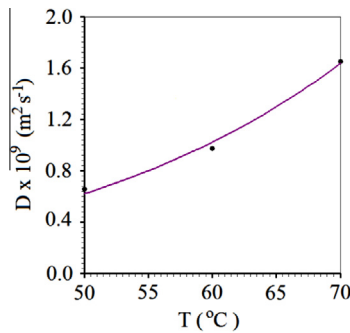
After harvest, the consumption time of coconuts *in natura* is rather limited. In order to avoid losses, coconuts can be submitted to a dehydration process. However, the use of hot air to remove water of coconut slices is expensive due to the phase change of the water. Thus, the osmotic dehydration process is a useful pretreatment which does not involve water phase change. In several countries like Brazil, the osmotic dehydration process (and convective drying) is made in a traditional form, without strong quality control of the final product. This article intends to contribute with information so that the

**Table 1** Results for osmotic dehydration using one (present work) and three-dimensional (Da Silva et al., 2013a) solution of the diffusion equation.

	$h$ ( $\text{m s}^{-1}$ )	$D$ ( $\text{m}^2 \text{s}^{-1}$ )	$Bi$	$R^2$	$\chi^2$
Present Work					
Water	$2.75 \times 10^{-6}$	$3.92 \times 10^{-10}$	21.500	0.9937	$1.104 \times 10^1$
Sucrose	$1.75 \times 10^{-6}$	$3.58 \times 10^{-10}$	15.000	0.9983	$1.406 \times 10^{-1}$
Da Silva et al. (2013a)					
Water	$6.68 \times 10^{-7}$	$2.64 \times 10^{-10}$	7.750	0.9952	$8.499 \times 10^0$
Sucrose	$4.41 \times 10^{-7}$	$2.70 \times 10^{-10}$	5.000	0.9971	$2.477 \times 10^{-1}$

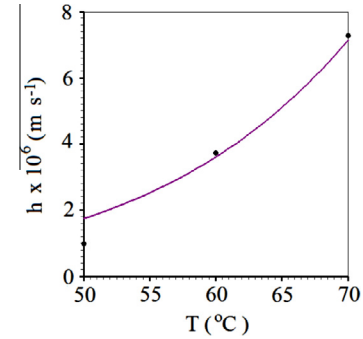
**Table 2** Results for thin-layer convective drying using one (present work) and three-dimensional (Da Silva et al., 2013a) solution of the diffusion equation.

$T$ (°C)	$h_W$ (m s <sup>-1</sup> )	$D_W$ (m <sup>2</sup> s <sup>-1</sup> )	$Bi$	$R^2$	$\chi^2$
Present Work					
50	$9.92 \times 10^{-7}$	$6.58 \times 10^{-10}$	4.625	0.9928	$5.932 \times 10^{-3}$
60	$3.73 \times 10^{-6}$	$9.75 \times 10^{-10}$	11.750	0.9892	$3.005 \times 10^{-2}$
70	$7.27 \times 10^{-6}$	$1.65 \times 10^{-9}$	13.500	0.9828	$3.141 \times 10^{-2}$
Da Silva et al. (2013a)					
50	$4.25 \times 10^{-7}$	$4.83 \times 10^{-10}$	2.700	0.9990	$3.255 \times 10^{-3}$
60	$1.30 \times 10^{-6}$	$6.36 \times 10^{-10}$	6.250	0.9929	$2.127 \times 10^{-2}$
70	$2.12 \times 10^{-6}$	$1.16 \times 10^{-9}$	5.625	0.9862	$2.503 \times 10^{-2}$

**Figure 2** Drying kinetics described by one-dimensional model at  $T =$  (a) 50 °C; (b) 60 °C; (c) 70 °C.**Figure 3** Effective mass diffusivity as a function of the drying air temperature.

osmotic dehydration and convective drying processes of coconuts can be precisely simulated.

In this paper, to minimize cut-off errors, the number of terms of the series that represents the analytical solution of the diffusion equation was established as 16 (Silva et al., 2012). On the other hand, according to Silva et al. (2013), the use of a three-dimensional numerical solution coupled with an optimizer can take several hours to determine  $D$  and  $h$ .

**Figure 4** Convective mass transfer coefficient as a function of the drying air temperature.

With a three-dimensional analytical solution and the optimization algorithm presented here, this time is reduced to several minutes. When the algorithm is coupled with a one-dimensional analytical solution the time is reduced to few seconds (Silva et al., 2009). For drying at 50 °C, for instance, the optimization time using one-dimensional geometry is about 11.7 s. In the three-dimensional case, this time is multiplied by the factor 193 (2263 s). Thus, the reduction of time justifies the large quantity of works in the literature that describe water migration in porous solids using approximated geometries, generally one-dimensional, and analytical solutions together with some type of optimization algorithm (Cunningham et al., 2007; Ruiz-López and García-Alvarado, 2007; Hacıhafızoglu et al., 2008; Mariani et al., 2008).

The use of only the first term of series that represents the analytical solution can lead to significant cut-off errors, particularly in the description of the initial instants of a diffusion process (Da Silva et al., 2013a). Thus, as mentioned above, in this article, 16 terms of the series were used that represent the solution for the boundary condition of the third kind, and the obtained results can be considered good. Regarding the statistical indicators for one- and three-dimensional optimizations, Tables 1 and 2 indicate that one-dimensional model proposed in this article is equivalent to three-dimensional model proposed by Da Silva et al. (2013a). Furthermore, a visual inspection in Figs. 1 and 2 leads to the conclusion that each simulation of the mass migration kinetics agrees with the respective experimental dataset. However, if knowledge of the mass distribution is required at a given time  $t$ , the use of a three-dimensional model is more feasible than the use of a one-dimensional model. Anyway, an idea of this distribution in an infinite slab can be obtained through Eq. (3).

An inspection in Figs. 1 and 2 enables to conclude that the five mass migrations occurred exclusively in falling rate period. In Fig. 1, it is interesting to observe that osmotic dehydration was studied for 1618 min. However, in practical terms, the mass transfers have occurred in about of half this time. In Fig. 2, the simulations of the drying kinetics in the final part of the process are only reasonable for 60 and 70 °C. Observing this figure it is possible to conclude that in this final part the effective mass diffusivity should be less than the value obtained. Thus, a variable mass diffusivity could better describe the process, and in this way a numerical solution of the diffusion equation is required. Even so, the values obtained in this article are useful as initial values in new optimization processes.

Coconut slices are, in fact, parallelepipeds. However, in this study, the thickness is significantly lesser than other two dimensions. In this sense, the one-dimensional model is reasonable despite this model overestimating the process parameters (see Tables 1 and 2), due to the consideration of the flux only in the two largest surfaces of the parallelepiped, ignoring the fluxes in the other four smaller areas. Nevertheless, the results obtained for the simulations of the mass migration kinetics are reasonable, and the optimization times to determine  $D$  and  $h$  are small (only a few seconds).

Once the optimization resource has been used to determine process parameters for some temperatures of the drying air, enabling the obtaining of Eqs. (15) and (16), these optimizations can be substituted by the idea given in the following. For a given temperature between 50 and 70 °C, Eqs. (15) and (16) can be used to calculate  $D$  and  $h$ , instead the optimization resource, and the obtained results can be used to describe the drying kinetics.

#### 4. Conclusion

- (1) The proposed model satisfactorily describes the kinetics of mass transfer.
- (2) The process parameters obtained through one-dimensional model are larger than the corresponding parameters obtained with three-dimensional model.
- (3) In osmotic dehydration, the value of the Biot number for the water transfer is significantly higher than this value for the sucrose transfer.
- (4) The optimization time using one-dimensional model is significantly less than the time for three-dimensional model.
- (5) It was possible to determine Arrhenius-type expressions to calculate the parameters  $D$  and  $h$  as a function of the drying air temperature. The values calculated from the Arrhenius equations make it possible to simulate the drying process in a chosen temperature within the interval 50–70 °C, without the need of new optimizations.

#### Acknowledgments

The authors would like to thank CNPq (Conselho Nacional de Desenvolvimento Científico e Tecnológico) for the support

given to this research through the process number 301697/2012-4.

#### References

- Amami, E., Vorobiev, E., Kechaou, N., 2006. Modelling of mass transfer during osmotic dehydration of apple tissue pre-treated by pulsed electric field. *LWT – Food Sci. Technol.* 39 (9), 1014–1021.
- Amuda, O.S., Giwa, A.A., Bello, I.A., 2007. Removal of heavy metal from industrial wastewater using modified activated coconut shell carbon. *Biochem. Eng. J.* 36 (2), 174–181.
- Arballo, J.R., Bambicha, R.R., Campanone, L.A., Agnelli, M.E., Mascheroni, R.H., 2012. Mass transfer kinetics and regression-desirability optimisation during osmotic dehydration of pumpkin, kiwi and pear. *Int. J. Food Sci. Technol.* 47 (2), 306–314.
- Benjapornkulaphong, S., Ngamcharussrivichai, C., Bunyakiat, K., 2009. Al<sub>2</sub>O<sub>3</sub>-supported alkali and alkali earth metal oxides for transesterification of palm kernel oil and coconut oil. *Chem. Eng. J.* 145 (3), 468–474.
- Bevington, P.R., Robinson, D.K., 1992. *Data Reduction and Error Analysis for the Physical Sciences*, Second ed. WCB/McGraw-Hill, Boston.
- Conceição Silva, M.A., Corrêa, J.L.G., Silva, Z.E., 2010. Application of inverse methods in the osmotic dehydration of acerola. *Int. J. Food Sci. Technol.* 45 (12), 2477–2484.
- Crank, J., 1992. *The Mathematics of Diffusion*. Clarendon Press, Oxford, UK.
- Cunningham, S.E., McMinn, W.A.M., Magee, T.R.A., Richardson, P.S., 2007. Modelling water absorption of pasta during soaking. *J. Food Eng.* 82 (4), 600–607.
- Da Silva, W.P., Amaral, D.S., Duarte, M.E.M., Mata Mário, E.R.M.C., Silva, C.M.D.P.S., Pinheiro, R.M.M., Pessoa, T., 2013a. Description of the osmotic dehydration and convective drying of coconut (*Cocos nucifera* L) pieces: a three-dimensional approach. *J. Food Eng.* 115 (1), 121–131.
- Da Silva, W.P., Silva, C.M.D.P.S., Gama, F.J.A., Gomes, J.P., 2014. Mathematical models to describe thin-layer drying and to determine drying rate of whole bananas. *J. Saudi Soc. Agric. Sci.* 13 (1), 67–74.
- Din, A.T., Hameed, M.B.H., Ahmad, A.L., 2009. Batch adsorption of phenol onto physicochemical-activated coconut shell. *J. Hazard. Mater.* 161 (2–3), 1522–1529.
- FAO – Food and Agriculture Organization of the United Nations (2013). *Statistical databases*. Rome, Italy. Available at: <http://www.fao.org>, (access: 03. 2013.).
- Garcia, C.C., Mauro, M.A., Kimura, M., 2007. Kinetics of osmotic dehydration and air-drying of pumpkins (*Cucurbita moschata*). *J. Food Eng.* 82 (3), 284–291.
- Ge, L., Yong, J.W.H., Goh, N.K., Chia, L.S., Tan, S.N., Ong, E.S., 2005. Identification of kinetin and kinetin riboside in coconut (*Cocos nucifera* L.) water using a combined approach of liquid chromatography–tandem mass spectrometry, high performance liquid chromatography and capillary electrophoresis. *J. Chromatogr. B* 829 (1–2), 26–34.
- Hacıhafızoglu, O., Cihan, A., Kahveci, K., Lima, A.G.B., 2008. A liquid diffusion model for thin-layer drying of rough rice. *European Food Res. Technol.* 226 (4), 787–793.
- Khin, M.M., Zhou, W., Perera, C.O., 2006. A study of the mass transfer in osmotic dehydration of coated potato cubes. *J. Food Eng.* 77 (1), 84–95.
- Lattanzio, V.M.T., Solfrizzo, M., Visconti, A., 2008. Determination of trichothecenes in cereals and derived products by liquid chromatography tandem mass spectrometry. *Food Addit. Contam.: Part A* 25 (3), 320–330.
- Lattanzio, V.M.T., Pascale, M., Visconti, A., 2009. Current analytical methods for trichothecene mycotoxins in cereals. *Trends Anal. Chem.* 28 (6), 758–768.

- Luikov, A.V., 1968. Analytical Heat Diffusion Theory. Academic Press, Inc. Ltd, London.
- Machmüller, A., Ossowski, D.A., Kreuzer, M., 2000. Comparative evaluation of the effects of coconut oil, oilseeds and crystalline fat on methane release, digestion and energy balance in lambs. *Anim. Feed Sci. Technol.* 85 (1–2), 41–60.
- Mariani, V.C., Lima, A.G., Coelho, B., 2008. Apparent thermal diffusivity estimation of the banana during drying using inverse method. *J. Food Eng.* 85 (4), 569–579.
- Matsui, K.N., Gut, J.A.W., Oliveira, P.V., Tadini, C.C., 2008. Inactivation kinetics of polyphenol oxidase and peroxidase in green coconut water by microwave processing. *J. Food Eng.* 88 (2), 169–176.
- Nastaj, J.F., Witkiewicz, K., 2009. Mathematical modeling of the primary and secondary vacuum freeze drying of random solids at microwave heating. *Int. J. Heat Mass Transfer* 52 (21–22), 4796–4806.
- Nevin, K.G., Rajamohan, T., 2006. Virgin coconut oil supplemented diet increases the antioxidant status in rats. *Food Chem.* 99 (2), 260–266.
- Oliveira, A.P., Neto, J.A.G., Nóbrega, J.A., Correia, P.R.M., Oliveira, P.V., 2005. Determination of selenium in nutritionally relevant foods by graphite furnace atomic absorption spectrometry using arsenic as internal standard. *Food Chem.* 93 (2), 355–360.
- Ruiz-López, I.I., García-Alvarado, M.A., 2007. Analytical solution for food-drying kinetics considering shrinkage and variable diffusivity. *J. Food Eng.* 79 (1), 208–216.
- Silva, W.P., Precker, J.W., Silva, C.M.D.P.S., Silva, D.D.P.S., 2009. Determination of the effective diffusivity via minimization of the objective function by scanning: application to drying of cowpea. *J. Food Eng.* 95 (2), 298–304.
- Silva, W.P., Precker, J.W., Silva, C.M.D.P.S., Gomes, J.P., 2010. Determination of effective diffusivity and convective mass transfer coefficient for cylindrical solids via analytical solution and inverse method: application to the drying of rough rice. *J. Food Eng.* 98 (3), 302–308.
- Silva, W.P., Farias, V.S.O., Neves, G.A., Lima, A.G.B., 2012. Modeling of water transport in roof tiles by removal of moisture at isothermal conditions. *Heat Mass Transfer* 48 (5), 809–821.
- Silva, W.P., Silva, C.M.D.P.S., Silva, L.D., Farias, V.S.O., 2013. Drying of clay slabs during the falling rate period: optimization and simulation of the process using diffusion models. *J. Mater. Sci. Res.* 2 (2), 1–13.
- Singh, B., Panesar, P.S., Nanda, V., 2008. Osmotic dehydration kinetics of carrot cubes in sodium chloride solution. *Int. J. Food Sci. Technol.* 43 (8), 1361–1370.
- Sousa, F.W., Moreira, S.A., Oliveira, A.G., Cavalcante, R.M., Nascimento, R.F., Rosa, M.F., 2007. The use of green coconut shells as adsorbents in the removal of toxic metals (In Portuguese). *Química Nova* 30 (5), 1153–1157.
- Tan, I.A.W., Ahmad, A.L., Hameed, B.H., 2008. Optimization of preparation conditions for activated carbons from coconut husk using response surface methodology. *Chem. Eng. J.* 137 (3), 462–470.
- Taylor, J.R., 1997. An Introduction to Error Analysis, 2nd ed. Sausalito, California, University Science Books.
- Yong, J.W.H., Ge, L., Fei Ng, Y., Tan, S.N., 2009. The chemical composition and biological properties of coconut (*Cocos nucifera* L) Water. *Molecules* 14 (12), 5144–5164.