



Contents lists available at SciVerse ScienceDirect

## Physics Letters B

www.elsevier.com/locate/physletb



# Phenomenology of the interplay between IR-improved DGLAP-CS theory and NLO ME matched parton shower MC precision

S.K. Majhi<sup>a,1</sup>, A. Mukhopadhyay<sup>b</sup>, B.F.L. Ward<sup>b,\*</sup>, S.A. Yost<sup>c,2</sup>

<sup>a</sup> Indian Association for the Cultivation of Science, Kolkata, India

<sup>b</sup> Baylor University, Waco, TX, United States

<sup>c</sup> The Citadel, Charleston, SC, United States

## ARTICLE INFO

## Article history:

Received 23 August 2012

Received in revised form 11 December 2012

Accepted 16 January 2013

Available online 18 January 2013

Editor: G.F. Giudice

## ABSTRACT

We present the current status of the application of our approach of *exact* amplitude-based resummation in quantum field theory to precision QCD calculations, by realistic MC event generator methods, as needed for precision LHC physics. In this ongoing program of research, we discuss recent results as they relate to the interplay of the attendant IR-improved DGLAP-CS theory of one of us and the precision of exact NLO matrix element matched parton shower MC's in the Herwig6.5 environment in relation to recent LHC experimental observations. There continues to be reason for optimism in the attendant comparison of theory and experiment.

© 2013 Elsevier B.V. Open access under CC BY license.

## 1. Introduction

With the recent announcement [1] of an Englert–Brout–Higgs (EBH) [2] candidate boson after the start-up and successful running of the LHC for 2.5 years, the era of precision QCD, by which we mean predictions for QCD processes at the total precision tag of 1% or better, is squarely upon us. The attendant need for exact, amplitude-based resummation of large higher order effects is now more paramount, given the expected role of precision comparison between theory and experiment in determining the detailed properties of the newly discovered EBH boson candidate. Three of us (B.F.L.W., S.K.M., S.A.Y.) have argued elsewhere [3,4] that such resummation allows one to have better than 1% theoretical precision as a realistic goal in such comparisons, so that one can indeed distinguish new physics (NP) from higher order SM processes and can distinguish different models of new physics from one another as well. In what follows, we present the status of this approach to precision QCD for the LHC in connection with its attendant IR-improved DGLAP-CS [5,6] theory [7,8] realization via HERWIRI1.031 [9] in the HERWIG6.5 [10] environment in interplay with NLO exact, matrix element matched parton shower MC precision issues. We will employ the MC@NLO [11] methodology

to realize the attendant exact, NLO matrix element matched parton shower MC realizations for both HERWIRI1.031 and HERWIG6.5 in our corresponding comparisons with recent LHC data that we present herein.

The discussion will therefore be seen to continue the strategy of building on existing platforms to develop and realize a path toward precision QCD for the physics of the LHC. We exhibit explicitly a union of the new IR-improved DGLAP-CS theory and the MC@NLO realization of exact NLO matrix element (ME) matched parton shower MC theory. As our ultimate goal is a provable precision tag on our theoretical predictions, we note that we are also pursuing the implementation [12] of the new IR-improved DGLAP-CS theory for HERWIG++ [13], HERWIRI++, for PYTHIA8 [14] and for SHERPA [15], as well as the corresponding NLO ME/parton shower matching realizations in the POWHEG [16] framework. For, one of the strongest cross checks on theoretical precision is the difference between two independent realizations of the attendant theoretical calculation. Such cross checks will appear elsewhere [12].

In order to expose properly the interplay between the NLO ME matched parton shower MC precision and the new IR-improved DGLAP-CS theory, we set the stage in the next section by showing how the latter theory follows naturally in the effort to obtain a provable precision from our approach [4] to precision LHC physics. In the interest of completeness, we review this latter approach, which is an amplitude-based QED  $\otimes$  QCD ( $\equiv$  QCD  $\otimes$  QED) exact resummation theory [4] realized by MC methods, in the next section as well. We then turn in Section 3 to the applications to the recent data on single heavy gauge boson production at the LHC from the perspective of the analysis in Ref. [9] of the analogous processes at the Tevatron, where we will focus in this Letter on the single  $Z/\gamma^*$

\* Corresponding author.

E-mail addresses: tpskm@iacs.res.in (S.K. Majhi),

aditi\_mukhopadhyay@baylor.edu (A. Mukhopadhyay), bfl\_ward@baylor.edu (B.F.L. Ward), scott.yost@citadel.edu (S.A. Yost).

<sup>1</sup> Work supported by grant Pool No. 8545-A, CSIR, IN.

<sup>2</sup> Work supported in part by U.S. DoE. grant DE-FG02-10ER41694 and grants from The Citadel Foundation.

production and decay to lepton pairs for definiteness. The other heavy gauge boson processes will be taken up elsewhere [12]. Section 4 contains our summary remarks.

## 2. Recapitulation

The starting point for what we discuss here may be taken as the fully differential representation

$$d\sigma = \sum_{i,j} \int dx_1 dx_2 F_i(x_1) F_j(x_2) d\hat{\sigma}_{\text{res}}(x_1 x_2 s) \quad (1)$$

of a hard LHC scattering process using a standard notation so that the  $\{F_j\}$  and  $d\hat{\sigma}_{\text{res}}$  are the respective parton densities and reduced hard differential cross section where we indicate the that latter has been resummed for all large EW and QCD higher order corrections in a manner consistent with achieving a total precision tag of 1% or better for the total theoretical precision of (1). The key theoretical issue for precision QCD for the LHC is then the proof of the correctness of the value of the total theoretical precision  $\Delta\sigma_{\text{th}}$  of (1). This precision can be represented as follows:

$$\Delta\sigma_{\text{th}} = \Delta F \oplus \Delta\hat{\sigma}_{\text{res}} \quad (2)$$

where  $\Delta A$  is the contribution of the uncertainty on the quantity  $A$  to  $\Delta\sigma_{\text{th}}$ .<sup>3</sup> In order to validate the application of a given theoretical prediction to precision experimental observations, for the discussion of the signals and the backgrounds for both Standard Model (SM) and new physics (NP) studies, and more specifically for the overall normalization of the cross sections in such studies, the proof of the correctness of the value of the total theoretical precision  $\Delta\sigma_{\text{th}}$  is essential. If a calculation with an unknown value of  $\Delta\sigma_{\text{th}}$  is used for the attendant studies, the NP can be missed. This point simply cannot be emphasized too much.

In the interest of completeness here, we note that, by our definition,  $\Delta\sigma_{\text{th}}$  is the total theoretical uncertainty that comes from the physical precision contribution and the technical precision contribution [17]: the physical precision contribution,  $\Delta\sigma_{\text{th}}^{\text{phys}}$ , arises from such sources as missing graphs, approximations to graphs, truncations, etc.; the technical precision contribution,  $\Delta\sigma_{\text{th}}^{\text{tech}}$ , arises from such sources as bugs in codes,<sup>4</sup> numerical rounding errors, convergence issues, etc. The total theoretical error is then given by

$$\Delta\sigma_{\text{th}} = \Delta\sigma_{\text{th}}^{\text{phys}} \oplus \Delta\sigma_{\text{th}}^{\text{tech}}. \quad (3)$$

The desired value for  $\Delta\sigma_{\text{th}}$ , which depends on the specific requirements of the observations, as a general rule, should fulfill  $\Delta\sigma_{\text{th}} \leq f \Delta\sigma_{\text{expt}}$ , where  $\Delta\sigma_{\text{expt}}$  is the respective experimental error and  $f \lesssim \frac{1}{2}$ . This would assure that the theoretical uncertainty does not significantly adversely affect the analysis of the data for physics studies.

In order to realize such precision in a provable way, we have developed the QCD  $\otimes$  QED resummation theory in Ref. [4] for the reduced cross section in (1) and for the resummation of the evolution of the parton densities therein as well. In the interest of

<sup>3</sup> Here, we discuss the situation in which the two errors in (2) are independent for definiteness; (2) has to be modified accordingly when they are not.

<sup>4</sup> We have in mind that all gross errors such as those that give obviously wrong results, as determined by cross checks, are eliminated and we have left programming errors such as those in the logic: suppose for programming error reasons a DO-loop ends at 999 steps instead of the intended 1000 steps, resulting in a per mille level error, that could alternate in sign from event to event. As per mille level accuracy is good enough in many applications, the program would remain reliable, but it would have what we call a technical precision error at the per mille level.

completeness and also because the theory in Ref. [4] is not widely known, we recapitulate it here briefly. Specifically, for both the resummation of the reduced cross section and that of the evolution of the parton densities, the master formula may be identified as

$$d\bar{\sigma}_{\text{res}} = e^{\text{SUM}_{\text{IR}}(\text{QCD})} \sum_{n,m=0}^{\infty} \frac{1}{n!m!} \int \prod_{j_1=1}^n \frac{d^3 k_{j_1}}{k_{j_1}} \prod_{j_2=1}^m \frac{d^3 k'_{j_2}}{k'_{j_2}} \times \int \frac{d^4 y}{(2\pi)^4} e^{iy \cdot (p_1 + q_1 - p_2 - q_2 - \sum k_{j_1} - \sum k'_{j_2}) + D_{\text{QCD}}} \times \tilde{\beta}_{n,m}(k_1, \dots, k_n; k'_1, \dots, k'_m) \frac{d^3 p_2}{p_2^0} \frac{d^3 q_2}{q_2^0}, \quad (4)$$

where  $d\bar{\sigma}_{\text{res}}$  is either the reduced cross section  $d\hat{\sigma}_{\text{res}}$  or the differential rate associated to a DGLAP-CS [5,6] kernel involved in the evolution of the  $\{F_j\}$  and where the new (YFS-style [18]) non-Abelian residuals  $\tilde{\beta}_{n,m}(k_1, \dots, k_n; k'_1, \dots, k'_m)$  have  $n$  hard gluons and  $m$  hard photons and we show the final state with two hard final partons with momenta  $p_2, q_2$  specified for a generic  $2f$  final state for definiteness. The infrared functions  $\text{SUM}_{\text{IR}}(\text{QCD})$ ,  $D_{\text{QCD}}$  are defined in Refs. [4,7,8]. This simultaneous resummation of QED and QCD large IR effects is exact.

The key components in the master formula (4) have the following physical meanings. The exponent  $\text{SUM}_{\text{IR}}(\text{QCD})$  sums up to the infinite order the maximal leading IR singular terms in the cross section in the language of Ref. [19] for soft emission below a dummy parameter  $K_{\text{max}}$  and the exponent  $D_{\text{QCD}}$  does the same for the regime above  $K_{\text{max}}$  so that (4) is independent of  $K_{\text{max}}$  – it cancels between  $\text{SUM}_{\text{IR}}(\text{QCD})$  and  $D_{\text{QCD}}$ . Having resummed these terms, we generate, in order to maintain exactness order by order in perturbation theory in both  $\alpha$  and  $\alpha_s$ , the residuals  $\tilde{\beta}_{n,m}$  – the latter are computed iteratively to match the attendant exact results to all orders in  $\alpha$  and  $\alpha_s$  as explained in Refs. [4,7,8].

We note that, as it is explained in Ref. [4], the new non-Abelian residuals  $\tilde{\beta}_{n,m}$  allow rigorous shower/ME matching via their shower subtracted analogs:

$$\tilde{\beta}_{n,m} \rightarrow \hat{\beta}_{n,m} \quad (5)$$

where the  $\hat{\beta}_{n,m}$  have had all effects in the showers associated to the  $\{F_j\}$  removed from them. The connection with the differential distributions in MC@NLO can be seen as follows. The MC@NLO differential cross section can be represented [11] as follows:

$$d\sigma_{\text{MC@NLO}} = \left[ B + V + \int (R_{\text{MC}} - C) d\Phi_R \right] d\Phi_B \left[ \Delta_{\text{MC}}(0) + \int (R_{\text{MC}}/B) \Delta_{\text{MC}}(k_T) d\Phi_R \right] + (R - R_{\text{MC}}) \Delta_{\text{MC}}(k_T) d\Phi_B d\Phi_R$$

where  $B$  is Born distribution,  $V$  is the regularized virtual contribution,  $C$  is the corresponding counter-term required at exact NLO,  $R$  is the respective exact real emission distribution for exact NLO,  $R_{\text{MC}} = R_{\text{MC}}(P_{AB})$  is the parton shower real emission distribution so that the Sudakov form factor is

$$\Delta_{\text{MC}}(p_T) = e^{-\int d\Phi_R \frac{R_{\text{MC}}(\Phi_B, \Phi_R)}{B} \theta(k_T(\Phi_B, \Phi_R) - p_T)},$$

where as usual it describes the respective no-emission probability. The respective Born and real emission differential phase spaces are denoted by  $d\Phi_A$ ,  $A = B, R$ , respectively. From comparison with (4) restricted to its QCD aspect we get the identifications, accurate to  $\mathcal{O}(\alpha_s)$ ,

$$\begin{aligned} \frac{1}{2} \hat{\hat{\beta}}_{0,0} &= \bar{B} + (\bar{B}/\Delta_{MC}(0)) \int (R_{MC}/B) \Delta_{MC}(k_T) d\Phi_R, \\ \frac{1}{2} \hat{\hat{\beta}}_{1,0} &= R - R_{MC} - B \hat{S}_{QCD} \end{aligned} \quad (6)$$

where we defined [11]

$$\bar{B} = B(1 - 2\alpha_s \delta_{BQCD}) + V + \int (R_{MC} - C) d\Phi_R$$

and we understand here that the DGLAP-CS kernels in  $R_{MC}$  are to be taken as the IR-improved ones as we exhibit below [7,8]. Here we have introduced the QCD virtual and real infrared functions  $B_{QCD}$  and  $\hat{S}_{QCD}$  respectively given in Refs. [7,8] which are understood to be DGLAP-CS synthesized as explained in Refs. [4,7,8] to avoid doubling counting of effects. The way to the extension of frameworks such as MC@NLO to exact higher orders in  $\{\alpha_s, \alpha\}$  is therefore open via our  $\hat{\hat{\beta}}_{n,m}$  and will be taken up elsewhere [12].

We stress that in Refs. [7–9] the methods we employ for resummation of the QCD theory have been shown to be fully consistent with the methods in Refs. [20,21]. What is shown in Refs. [7–9] is that the methods in Refs. [20,21] give approximations to our hard gluon residuals  $\hat{\hat{\beta}}_n$ ; for, the methods in Refs. [20,21], unlike the master formula in (4), are not exact results. Specifically, the threshold-resummation methods in Ref. [20], using the result that, for any function  $f(z)$ ,

$$\left| \int_0^1 dz z^{n-1} f(z) \right| \leq \left( \frac{1}{n} \right) \max_{z \in [0,1]} |f(z)|,$$

drop non-singular contributions to the cross section at  $z \rightarrow 1$  in resumming the logs in  $n$ -Mellin space. The SCET theory in Ref. [21] drops terms of  $\mathcal{O}(\lambda)$  at the level of the amplitude, where  $\lambda = \sqrt{\Lambda/Q}$  for a process with the hard scale  $Q$  with  $\Lambda \sim 0.3$  GeV so that, for  $Q \sim 100$  GeV, we have  $\lambda \cong 5.5\%$ . From the known equivalence of the two approaches, the errors in the threshold resummation must be similar. Evidently, we can only use these approaches as a guide to our new non-Abelian residuals as we develop results for the sub-1% precision regime.

The discussions just completed naturally bring us to the attendant evolution of the  $\{F_j\}$ ; for, in order to have a strict control on the theoretical precision in (1), we need both the resummation of the reduced cross section and that of the latter evolution.

When the QCD restriction of the formula in (4) is applied to the calculation of the kernels,  $P_{AB}$ , in the DGLAP-CS theory itself, we get an improvement of the IR limit of these kernels, an IR-improved DGLAP-CS theory [7,8] in which large IR effects are resummed for the kernels themselves. The resulting new resummed kernels,  $P_{AB}^{\text{exp}}$  are given in Refs. [7–9] and are reproduced here for completeness:

$$\begin{aligned} P_{qq}^{\text{exp}}(z) &= C_F F_{\text{YFS}}(\gamma_q) e^{\frac{1}{2}\delta_q} \left[ \frac{1+z^2}{1-z} (1-z)^{\gamma_q} - f_q(\gamma_q) \delta(1-z) \right], \\ P_{Gq}^{\text{exp}}(z) &= C_F F_{\text{YFS}}(\gamma_q) e^{\frac{1}{2}\delta_q} \frac{1+(1-z)^2}{z} z^{\gamma_q}, \\ P_{GG}^{\text{exp}}(z) &= 2C_G F_{\text{YFS}}(\gamma_G) e^{\frac{1}{2}\delta_G} \left\{ \frac{1-z}{z} z^{\gamma_G} + \frac{z}{1-z} (1-z)^{\gamma_G} \right. \\ &\quad \left. + \frac{1}{2} (z^{1+\gamma_G} (1-z) + z(1-z)^{1+\gamma_G}) \right. \\ &\quad \left. - f_G(\gamma_G) \delta(1-z) \right\}, \\ P_{qG}^{\text{exp}}(z) &= F_{\text{YFS}}(\gamma_G) e^{\frac{1}{2}\delta_G} \frac{1}{2} \{ z^2 (1-z)^{\gamma_G} + (1-z)^2 z^{\gamma_G} \}, \end{aligned} \quad (7)$$

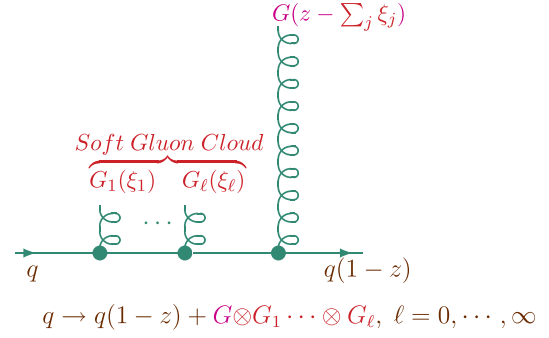


Fig. 1. Bloch–Nordsieck soft quanta for an accelerated charge.

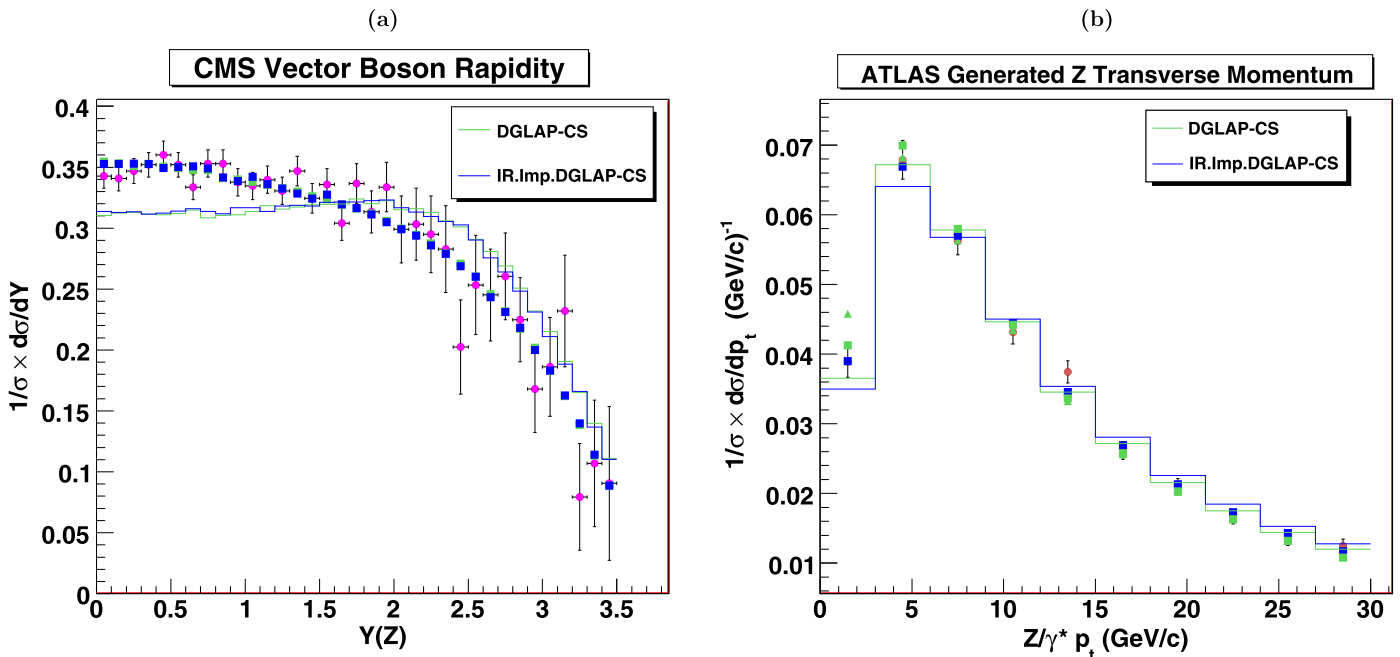
where the superscript “exp” indicates that the kernel has been resummed as predicted by Eq. (4) when it is restricted to QCD alone, where the YFS [18] infrared factor is given by  $F_{\text{YFS}}(a) = e^{-C_E a} / \Gamma(1+a)$  where  $C_E$  is Euler’s constant and where we refer the reader to Refs. [7,8] for the detailed definitions of the respective resummation functions  $\gamma_A, \delta_A, f_A, A = q, G$ .<sup>5</sup>  $C_F(C_G)$  is the quadratic Casimir invariant for the quark (gluon) color representation respectively. These new kernels yield a new resummed scheme for the parton density functions (PDF’s) and the reduced cross section:

$$\begin{aligned} F_j, \hat{\sigma} &\rightarrow F'_j, \hat{\sigma}' \quad \text{for} \\ P_{Gq}(z) &\rightarrow P_{Gq}^{\text{exp}}(z), \quad \text{etc.}, \end{aligned}$$

with the same value for  $\sigma$  in (1) with improved MC stability as discussed in Ref. [9] – there is no need for an IR cut-off ‘ $k_0$ ’ parameter in the attendant parton shower MC based on the new kernels. We point-out that, while the degrees of freedom below the IR cut-offs in the usual showers are dropped in those showers, in the showers in HERWIRI.031, as one can see from (4), these degrees of freedom are integrated over and included in the calculation in the process of generating the Gribov–Lipatov exponents  $\gamma_A$  in (7). We note also that the new kernels agree with the usual kernels at  $\mathcal{O}(\alpha_s)$  as the differences between them start in  $\mathcal{O}(\alpha_s^2)$ . This means that the NLO matching formulas in the MC@NLO and POWHEG frameworks apply directly to the new kernels for exact NLO ME/shower matching.

For completeness, we feature in Fig. 1 the basic physical idea underlying the new kernels as it was already discussed by Bloch and Nordsieck [24]: an accelerated charge generates a coherent state of very soft massless quanta of the respective gauge field so that one cannot know which of the infinity of possible states one has made in the splitting process  $q(1) \rightarrow q(1-z) + G \otimes G_1 \otimes \dots \otimes G_\ell, \ell = 0, \dots, \infty$  illustrated in Fig. 1. The new kernels take this effect into account by resumming the terms  $\mathcal{O}((\alpha_s \ln(\frac{q^2}{\Lambda^2}) \ln(1-z))^n)$  when  $z \rightarrow 1$  is the IR limit. As one can see in (7) and (1), when the usual kernels are used these terms are generated order-by-order in the solution for the cross section  $\sigma$  in (1) and our resumming them enhances the convergence of the representation in (1) for a given order of exactness in the input perturbative components therein. We now turn to the illustration of this last remark in the context of the comparison of NLO parton shower/matrix element matched predictions to recent LHC data.

<sup>5</sup> The improvement in Eq. (7) should be distinguished from the resummation in parton density evolution for the “ $z \rightarrow 0$ ” Regge regime – see for example Refs. [22,23]. This latter improvement must also be taken into account for precision LHC predictions.



**Fig. 2.** Comparison with LHC data: (a) CMS rapidity data on  $(Z/\gamma^*)$  production to  $e^+e^-$ ,  $\mu^+\mu^-$  pairs, the circular dots are the data, the green (blue) lines are HERWIG6.510 (HERWIRI1.031); (b) ATLAS  $p_T$  spectrum data on  $(Z/\gamma^*)$  production to (bare)  $e^+e^-$  pairs, the circular dots are the data, the blue (green) lines are HERWIRI1.031 (HERWIG6.510). In both (a) and (b) the blue (green) squares are MC@NLO/HERWIRI1.031 (HERWIG6.510 (PTRMS = 2.2 GeV)). In (b), the green triangles are MC@NLO/HERWIG6.510 (PTRMS = 0). These are otherwise untuned theoretical results. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

### 3. Interplay of NLO shower/ME precision and IR-improved DGLAP-CS theory

The new MC HERWIRI1.031 [9] gives the first realization of the new IR-improved kernels in the HERWIG6.5 [10] environment. Here, we compare it with HERWIG6.510, both with and without the MC@NLO [11] exact  $\mathcal{O}(\alpha_s)$  correction to illustrate the interplay between the attendant precision in NLO ME matched parton shower MC's and the new IR-improvement for the kernels where we use the new LHC data for our baseline for the comparison.

More precisely, for the single  $Z/\gamma^*$  production at the LHC, we show in Fig. 2 in panel (a) the comparison between the MC predictions and the CMS rapidity data [25] and in panel (b) the analogous comparison with the ATLAS  $p_T$  data, where the rapidity data are the combined  $e^+e^- - \mu^-\mu^+$  results and the  $p_T$  data are those for the bare  $e^+e^-$  case, as these are the data that correspond to the theoretical framework of our simulations – we do not as yet have complete realization of all the corrections involved in the other ATLAS data in Ref. [26]. These results should be viewed from the perspective of our analysis in Ref. [9] of the FNAL data on the single  $Z/\gamma^*$  production in  $p\bar{p}$  collisions at 1.96 TeV.

Specifically, in Fig. 11 of the second paper in Ref. [9], we showed that, when the intrinsic rms  $p_T$  parameter PTRMS is set to 0 in HERWIG6.5, the simulations for MC@NLO/HERWIG6.510 give a good fit to the CDF rapidity distribution data [28] therein but they do not give a satisfactory fit to the D0  $p_T$  distribution data [29] therein whereas the results for MC@NLO/HERWIRI1.031 give good fits to both sets of data with the PTRMS = 0. Here PTRMS corresponds to an intrinsic Gaussian distribution in  $p_T$ . The authors of HERWIG [27] have emphasized that to get good fits to both sets of data, one may set PTRMS  $\cong$  2 GeV. Thus, in analyzing the new LHC data, we have set PTRMS = 2.2 GeV in our HERWIG6.510 simulations while we continue to set PTRMS = 0 in our HERWIRI simulations.

Turning now with this perspective to the results in Fig. 2, we see a confirmation of the finding of the HERWIG authors. To get a good fit to both the CMS rapidity data and the ATLAS  $p_T$  data, one needs to set PTRMS  $\cong$  2 GeV [30] in the MC@NLO/HERWIG6.510 simulations. We again see that at LHC one gets a good fit to the data for both the rapidity and the  $p_T$  spectra in the MC@NLO/HERWIRI1.031 simulations with PTRMS = 0. In quantitative terms, the  $\chi^2/\text{d.o.f.}$  for the rapidity data and  $p_T$  data are (0.72, 0.72) ((0.70, 1.37)) for the MC@NLO/HERWIRI1.031 (MC@NLO/HERWIG 6.510 (PTRMS = 2.2 GeV)) simulations. For the MC@NLO/HERWIG6.510 (PTRMS = 0) simulations the corresponding results are (0.70, 2.23).

Thus, we see that the usual DGLAP-CS kernels require the introduction of a *hard* intrinsic Gaussian spread in  $p_T$  inside the proton to reproduce the LHC data on the  $p_T$  distribution of the  $Z/\gamma^*$  in the pp collisions whereas the IR-improved kernels give in fact a better fit to the data without the introduction of such a hard intrinsic component to the motion of the proton's constituents. The *hardness* of this PTRMS is entirely ad hoc; it is in contradiction with the results of all successful models of the proton wave-function [31], wherein the scale of the corresponding PTRMS is found to be  $\lesssim$  0.4 GeV. More importantly, it contradicts the known experimental observation of precocious Bjorken scaling [32,33], where the SLAC-MIT experiments show that Bjorken scaling occurs already at  $Q^2 = 1_+ \text{ GeV}^2$  for  $Q^2 = -q^2$  with  $q$  the 4-momentum transfer from the electron to the proton in the famous deep inelastic electron-proton scattering process whereas, if the proton constituents really had a Gaussian intrinsic  $p_T$  distribution with PTRMS  $\cong$  2 GeV, these observations would not be possible. What can now say is that the ad hoc “hardness” of the PTRMS  $\cong$  2.2 GeV value is really just a phenomenological representation of the more fundamental dynamics realized by the IR-improved DGLAP-CS theory. This raises the question of whether it is possible to tell the difference between the two representations of the data in Fig. 2.



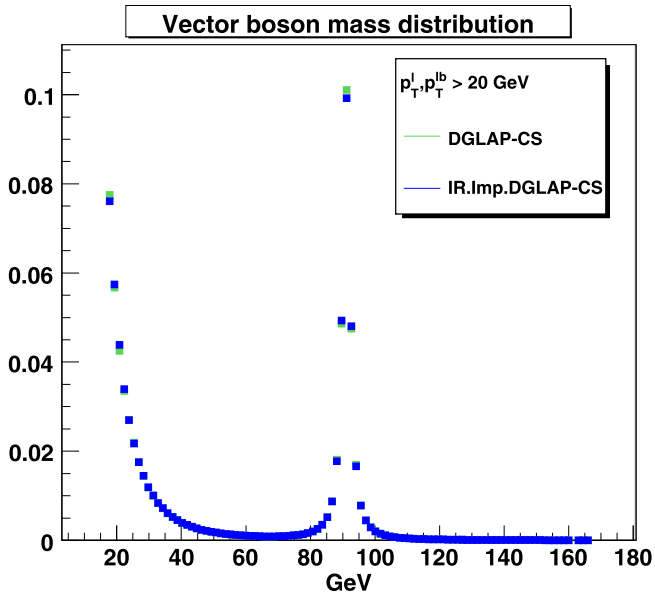


Fig. 3. Normalized vector boson mass spectrum at the LHC for  $p_T(\text{lepton}) > 20$  GeV.

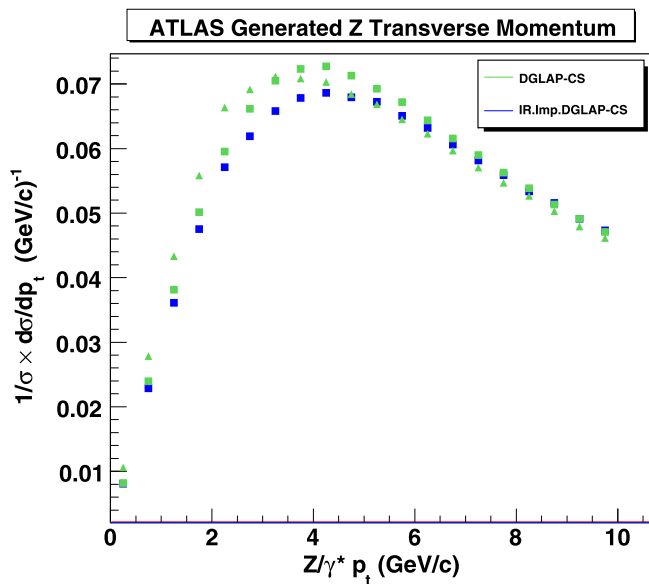


Fig. 4. Normalized vector boson  $p_T$  spectrum at the LHC for the ATLAS cuts as exhibited in Fig. 2 for the same conventions on the notation for the theoretical results with the vector boson  $p_T < 10$  GeV to illustrate the differences between the three predictions.

Physically, one expects that more detailed observations should be able to distinguish the two. Specifically, we show in Fig. 3 the MC@NLO/HERWIRI 1.031 (blue squares) and MC@NLO/HERWIG6510 ( $\text{PTRMS} = 2.2$  GeV) (green squares) predictions for the  $Z/\gamma^*$  mass spectrum when the decay lepton pairs are required to satisfy the LHC type requirement that their transverse momenta  $\{p_T^\ell, p_T^{\bar{\ell}}\}$  exceed 20 GeV. We see that the high precision data such as the LHC ATLAS and CMS experiments will have (each already has over  $5 \times 10^6$  lepton pairs) would allow one to distinguish between the two sets of theoretical predictions, as the peaks differ by 2.2% for example.

Continuing in this way, we make a more detailed snap-shot of the region below 10.0 GeV in Fig. 2(b) in which we plot the three featured theory predictions with finer binning, 0.5 GeV instead of 3.0 GeV. This is shown in Fig. 4. We see that there are significant

differences in the shapes of the three predictions that are testable with the precise data that will be available to ATLAS and CMS experiments. Other such detailed observations may also reveal the differences between the two descriptions of parton shower physics and we will pursue these elsewhere [12]. We await the release of the entire data sets from ATLAS and CMS.

#### 4. Conclusions

We have shown that the realization of IR-improved DGLAP-CS theory in HERWIRI1.031, when used in the MC@NLO/HERWIRI1.031 exact  $\mathcal{O}(\alpha_s)$  ME matched parton shower framework, affords one the opportunity to explain, on an event-by-event basis, both the rapidity and the  $p_T$  spectra of the  $Z/\gamma^*$  in pp collisions in the recent LHC data from CMS and ATLAS, respectively, without the need of an unexpectedly hard intrinsic Gaussian  $p_T$  distribution with rms value of  $\text{PTRMS} \cong 2$  GeV in the proton's wave function. We argue that this can be interpreted as providing a rigorous basis for the phenomenological correctness of such unexpectedly hard distributions insofar as describing these data using the usual unimproved DGLAP-CS showers is concerned and we have proposed that comparison of other distributions such as the invariant mass distribution with the appropriate cuts and the more detailed  $Z/\gamma^*$   $p_T$  spectra in the regime below 10.0 GeV be used to differentiate between the fundamental description of the parton shower physics in MC@NLO/HERWIRI1.031 and these phenomenological representations in MC@NLO/HERWIG6510. We have emphasized that the precociousness of Bjorken scaling argues against the fundamental correctness of the hard scale intrinsic  $p_T$  ansatz with the unexpectedly hard value of  $\text{PTRMS} \cong 2$  GeV, as do the successful models [31] of the proton's wave function, which would predict this value to be  $\lesssim 0.4$  GeV. We have the added bonus that the fundamental description in MC@NLO/HERWIRI1.031 can be systematically improved to the NNLO parton shower/ME matched level which we anticipate is a key ingredient in achieving the sub-1% precision tag for such processes as single heavy gauge boson production at the LHC. Evidently, the use of ad hoc hard scales in models would compromise any discussion of the theoretical precision relative to what one could achieve from the fundamental representation of the corresponding physics via IR-improved DGLAP-CS theory as it is realized in HERWIRI1.031 when employed in MC@NLO/HERWIRI1.031 simulations. We are pursuing additional cross checks of the latter simulations against the LHC data.

#### Acknowledgements

In closing, two of us (A.M. and B.F.L.W.) thank Prof. Ignatios Antoniadis for the support and kind hospitality of the CERN TH Unit while part of this work was completed.

#### References

- [1] F. Gianotti, in: Proc. ICHEP2012, in press; J. Incandela, in: Proc. ICHEP2012, 2012, in press; G. Aad, et al., arXiv:1207.7214; D. Abbaneo, et al., arXiv:1207.7235.
- [2] F. Englert, R. Brout, Phys. Rev. Lett. 13 (1964) 312; P.W. Higgs, Phys. Lett. 12 (1964) 132; P.W. Higgs, Phys. Rev. Lett. 13 (1964) 508; G.S. Guralnik, C.R. Hagen, T.W.B. Kibble, Phys. Rev. Lett. 13 (1964) 585.
- [3] B.F.L. Ward, S.K. Majhi, S.A. Yost, in: PoS (RADCOR2011), 2012, p. 022.
- [4] C. Glosser, S. Jadach, B.F.L. Ward, S.A. Yost, Mod. Phys. Lett. A 19 (2004) 2113; B.F.L. Ward, C. Glosser, S. Jadach, S.A. Yost, in: Proc. DPF 2004, Int. J. Mod. Phys. A 20 (2005) 3735; B.F.L. Ward, C. Glosser, S. Jadach, S.A. Yost, in: H. Chen, et al. (Eds.), Proc. ICHEP04, vol. 1, World. Sci. Publ. Co., Singapore, 2005, p. 588; B.F.L. Ward, S.A. Yost, in: A. De Roeck, H. Jung (Eds.), Proc. HERA-LHC Workshop, CERN-2005-014, CERN, Geneva, 2005, p. 304, preprint BU-HEPP-05-05;

- B.F.L. Ward, S.A. Yost, in: A. Sissakian, et al. (Eds.), Proc. ICHEP 2006, vol. 1, World Sci. Publ. Co., Singapore, 2007, p. 505;  
 B.F.L. Ward, S.A. Yost, Acta Phys. Polon. B 38 (2007) 2395;  
 B.F.L. Ward, S. Yost, in: PoS (RADCOR 2007), 2008, p. 038, arXiv:0802.0724;  
 B.F.L. Ward, et al., in: Proc. ICHEP08, Philadelphia, 2008, eConf C080730, arXiv:0810.0723;  
 B.F.L. Ward, et al., in: H. Jung, A. De Roeck (Eds.), Proc. 2008 HERA-LHC Workshop, DESY-PROC-2009-02, DESY, Hamburg, 2009, p. 168, and references therein, arXiv:0808.3133.
- [5] G. Altarelli, G. Parisi, Nucl. Phys. B 126 (1977) 298;  
 Yu.L. Dokshitzer, Sov. Phys. JETP 46 (1977) 641;  
 L.N. Lipatov, Yad. Fiz. 20 (1974) 181;  
 V. Gribov, L. Lipatov, Sov. J. Nucl. Phys. 15 (1972) 675, 938;  
 See also J.C. Collins, J. Qiu, Phys. Rev. D 39 (1989) 1398.
- [6] C.G. Callan Jr., Phys. Rev. D 2 (1970) 1541;  
 K. Symanzik, Commun. Math. Phys. 18 (1970) 227;  
 K. Symanzik, in: G. Hoehler (Ed.), Springer Tracts in Modern Physics, Springer, Berlin, 1971, p. 222;  
 See also S. Weinberg, Phys. Rev. D 8 (1973) 3497.
- [7] B.F.L. Ward, Adv. High Energy Phys. 2008 (2008) 682312.
- [8] B.F.L. Ward, Ann. Phys. 323 (2008) 2147.
- [9] S. Joseph, et al., Phys. Lett. B 685 (2010) 283;  
 S. Joseph, et al., Phys. Rev. D 81 (2010) 076008.
- [10] G. Corcella, et al., hep-ph/0210213;  
 G. Corcella, et al., J. High Energy Phys. 0101 (2001) 010;  
 G. Marchesini, et al., Comput. Phys. Commun. 67 (1992) 465.
- [11] S. Frixione, B. Webber, J. High. Energy Phys. 0206 (2002) 029;  
 S. Frixione, et al., arXiv:1010.0568;  
 B. Webber, talk at CERN, 03/30/2011;  
 S. Frixione, talk at CERN, 05/04/2011.
- [12] A. Mukhopadhyay, et al., in preparation.
- [13] M. Bahr, et al., arXiv:0812.0529, and references therein.
- [14] T. Sjostrand, S. Mrenna, P.Z. Skands, Comput. Phys. Commun. 178 (2008) 852.
- [15] T. Gleisberg, et al., J. High Energy Phys. 0902 (2009) 007.
- [16] P. Nason, J. High Energy Phys. 0411 (2004) 040.
- [17] See for example S. Jadach, et al., in: Physics at LEP2, vol. 2, CERN, Geneva, 1995, pp. 229–298.
- [18] D.R. Yennie, S.C. Frautschi, H. Suura, Ann. Phys. 13 (1961) 379;  
 See also K.T. Mahanthappa, Phys. Rev. 126 (1962) 329, for a related analysis.
- [19] J.G.M. Gatheral, Phys. Lett. B 133 (1983) 90.
- [20] G. Sterman, Nucl. Phys. B 281 (1987) 310;  
 S. Catani, L. Trentadue, Nucl. Phys. B 327 (1989) 323;  
 S. Catani, L. Trentadue, Nucl. Phys. B 353 (1991) 183.
- [21] See for example C.W. Bauer, A.V. Manohar, M.B. Wise, Phys. Rev. Lett. 91 (2003) 122001;  
 C.W. Bauer, A.V. Manohar, M.B. Wise, Phys. Rev. D 70 (2004) 034014;  
 C. Lee, G. Sterman, Phys. Rev. D 75 (2007) 014022.
- [22] B.I. Ermolaev, M. Greco, S.I. Troyan, in: PoS (DIFF2006), 2006, p. 036, and references therein.
- [23] G. Altarelli, R.D. Ball, S. Forte, in: PoS (RADCOR2007), 2007, p. 028.
- [24] F. Bloch, A. Nordsieck, Phys. Rev. 52 (1937) 54.
- [25] S. Chatrchyan, et al., arXiv:1110.4973;  
 S. Chatrchyan, et al., Phys. Rev. D 85 (2012) 032002.
- [26] G. Aad, et al., arXiv:1107.2381;  
 G. Aad, et al., Phys. Lett. B 705 (2011) 415.
- [27] M. Seymour, Event generator physics for the LHC, in: CERN Seminar, 2011.
- [28] C. Galea, in: Proc. DIS 2008, London, 2008, <http://dx.doi.org/10.3360/dis.2008.55>.
- [29] V.M. Abasov, et al., Phys. Rev. Lett. 100 (2008) 102002.
- [30] P. Skands, private communication, 2011, finds a similar behavior in PYTHIA8 simulations.
- [31] R.P. Feynman, M. Kislinger, F. Ravndal, Phys. Rev. D 3 (1971) 2706;  
 R. Lipes, Phys. Rev. D 5 (1972) 2849;  
 F.K. Diakonas, N.K. Kaplis, X.N. Mawita, Phys. Rev. D 78 (2008) 054023;  
 K. Johnson, Proc. Scottish Summer School Phys. 17 (1976) 245;  
 A. Chodos, et al., Phys. Rev. D 9 (1974) 3471;  
 A. Chodos, et al., Phys. Rev. D 10 (1974) 2599;  
 T. DeGrand, et al., Phys. Rev. D 12 (1975) 2060.
- [32] See for example R.E. Taylor, Phil. Trans. Roc. Soc. Lond. A 359 (2001) 225, and references therein.
- [33] J. Bjorken, in: L. Hoddeson, et al. (Eds.), Proc. 3rd International Symposium on the History of Particle Physics: The Rise of the Standard Model, Stanford, CA, 1992, Cambridge Univ. Press, Cambridge, 1997, p. 589, and references therein.