# Search for $X Y Z$ states in $\Lambda_{b}$ decays at the LHCb 

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#### Abstract

We consider $X(3872)$ and $Y(4140)$ as the vector tetraquark states of $X_{c}^{0} \equiv c \bar{c} u \bar{u}(d \bar{d})$ and $c \bar{c} s \bar{s}$, respectively. By connecting $\Lambda_{b} \rightarrow X_{c}^{0} \Lambda$ to $B^{-} \rightarrow X_{c}^{0} K^{-}$, we predict that the branching ratios of $\Lambda_{b} \rightarrow$ $\Lambda\left(X(3872)^{0} \rightarrow\right) J / \psi \pi^{+} \pi^{-}$and $\Lambda_{b} \rightarrow \Lambda(Y(4140) \rightarrow) J / \psi \phi$ are $(5.2 \pm 1.8) \times 10^{-6}$ and $(4.7 \pm 2.6) \times 10^{-6}$, which are accessible to the experiments at the LHCb, respectively. The measurements of these $\Lambda_{b}$ modes would be the first experimental evidences for the $X Y Z$ states in baryonic decays. © 2016 The Authors. Published by Elsevier B.V. This is an open access article under the CC BY license


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## 1. Introduction

With the quantum numbers of $J^{P C}=1^{++}$determined by the $B^{-} \rightarrow X(3872)^{0} K^{-}$decay [1], the state of $X(3872)^{0}$ has been established as one of the $X Y Z$ states [2], which are regarded to be exotic due to the non-pure $c \bar{c}$ components. However, it is still a puzzle whether $X(3872)^{0}$ is really a tetraquark state (fourquark bound state) with the quark content $c \bar{c} u \bar{u}(d \bar{d})$ [3]. Note that, while there is no sign of its charged partner to be the $c \bar{c} u \bar{d}(d \bar{u})$ state, $Y(4140)$ can be a tetraquark consisting of $c \bar{c} s \bar{s}$ [4], of which the quantum numbers of $J^{P C}$ are not experimentally assigned. As more investigations are apparently needed, the study of $X(3872)$ has been restricted in the $B$ decays of $B \rightarrow X(3872)^{0} K^{(*)}$ and $B \rightarrow X(3872)^{0} K \pi$ with $K \pi$ partly from $K^{*}[5,6]$, where the resonant $X^{0}(3872)$ decay channels can be $X(3872)^{0} \rightarrow J / \psi \pi^{+} \pi^{-}$, $J / \psi \omega, J / \psi \gamma$ and $D \bar{D}^{*}$. At present, no other observation has been found beyond the $B$ decays.

On the other hand, being identified as the exotic meson, which could be the tetraquark [3], $D \bar{D}^{*}$ molecule [7], or hybrid $c \bar{c} g$ bound state [8], the $X(3872)$ state causes the difficulty of the theoretical calculations. In this study, we will concentrate on the tetraquark scenario by denoting $X_{c}^{0}$ to be composed of $c \bar{c} q \bar{q}$, where $q \bar{q}$ can be $u \bar{u}, d \bar{d}$, or $s \bar{s}$. In particular, we take $X(3872)^{0}$ and $Y(4140)$ as two of these exotic $X_{c}^{0}$ states. Through the $b \rightarrow c \bar{c} s$ transition at the quark level in Fig. 1, the decays of $B \rightarrow\left(X(3872)^{0}, J / \psi\right) K$ correspond to the processes of the $B \rightarrow K$ transition with the recoiled charmed mesons of $X(3872)^{0}$ and $J / \psi$, respectively. Although the

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Fig. 1. The doubly charmful $b$-hadron decays, where (a), (b), (c), and (d) depict $B \rightarrow J / \psi K, \Lambda_{b} \rightarrow J / \psi \Lambda, B \rightarrow X_{c}^{0} K$, and $\Lambda_{b} \rightarrow X_{c}^{0} \Lambda$, respectively, with $X_{c}^{0}$ as the tetraquark to consist of $c \bar{c} q \bar{q}$.
$J / \psi$ formation from the $c \bar{c}$ currents can be calculated within the framework of QCD, the $X(3872)$ one cannot be done at the moment.

However, it is interesting to see in Fig. 1 that all decays of $\left(B, \Lambda_{b}\right) \rightarrow\left(X_{c}^{0}, J / \psi\right) K$ are originated from the $b \rightarrow c \bar{c} s$ transition at the quark level, and therefore connected. As a result, despite the unknown matrix elements of the $X_{c}^{0}$ hadronization through the $c \bar{c}$ currents, we can relate these decays. In particular, we can predict the branching ratios of $\Lambda_{b} \rightarrow X_{c}^{0} \Lambda$. The experimental searches of these $\Lambda_{b}$ decays at the LHCb will clearly improve our understanding of the XYZ states.

## 2. Formalism

From Fig. 1, through the effective Hamiltonian of the $b \rightarrow c \bar{c} s$ transition at the quark level, the amplitudes of $\Lambda_{b} \rightarrow M_{c} \Lambda$ and $B \rightarrow M_{c} K$ can be factorized as $[9,10]$

$$
\begin{align*}
& \mathcal{A}\left(\Lambda_{b} \rightarrow M_{c} \Lambda\right) \\
& \quad=\frac{G_{F}}{\sqrt{2}} V_{c b} V_{c s}^{*} a_{2}\left\langle M_{c}\right| \bar{c} \gamma^{\mu}\left(1-\gamma_{5}\right) c|0\rangle\langle\Lambda| \bar{s} \gamma_{\mu}\left(1-\gamma_{5}\right) b\left|\Lambda_{b}\right\rangle, \\
& \mathcal{A}\left(B \rightarrow M_{c} K\right) \\
& \quad=\frac{G_{F}}{\sqrt{2}} V_{c b} V_{c s}^{*} \hat{a}_{2}\left\langle M_{c}\right| \bar{c} \gamma^{\mu}\left(1-\gamma_{5}\right) c|0\rangle\langle K| \bar{s} \gamma_{\mu}\left(1-\gamma_{5}\right) b|B\rangle, \tag{1}
\end{align*}
$$

where $G_{F}$ is the Fermi constant, $V_{i j}$ are the CKM matrix elements, $M_{c}$ represents $J / \psi$ of $J^{P C}=1^{--}$or the exotic $X_{c}^{0}$ state with its constituent being $\bar{c} \bar{q} q \bar{q}$. For simplicity, we take that the quantum numbers of $X_{c}^{0}$ are $J^{P C}=1^{++}$, such as the established $X(3872)^{0}$ state. Note that $Y(4140)$, observed in the resonant $B^{-} \rightarrow$ $Y(4140) K^{-}, Y(4140) \rightarrow J / \psi \phi$ decay [11,12], is also assumed to be the $J^{P C}=1^{++}$state and treated as one of the $X_{c}^{0}$ states with the tetraquark of $c \bar{c} s \bar{s}$ [4]. To calculate the processes in Fig. 1, we need to know the matrix elements of $\left\langle X_{c}^{0}\right| \bar{c} \gamma_{\mu}\left(1-\gamma_{5}\right) c|0\rangle$, which is the most difficult part unless these can be related to the observed quantities. In Eq. (1), the parameters $a_{2}$ and $\hat{a}_{2}$, involving the nonfactorizable effects, can be extracted from the observed branching ratios of $\mathcal{B}\left(\Lambda_{b} \rightarrow J / \psi \Lambda\right)$ and $\mathcal{B}\left(B^{-} \rightarrow J / \psi K^{-}\right)$, respectively. The matrix elements of the $\Lambda_{b} \rightarrow \Lambda$ and $B \rightarrow K$ transitions in Eq. (1) are in the forms of

$$
\begin{gather*}
\langle\Lambda| \bar{s} \gamma_{\mu} b\left|\Lambda_{b}\right\rangle=\bar{u}_{\Lambda}\left[f_{1} \gamma_{\mu}+\frac{f_{2}}{m_{\Lambda_{b}}} i \sigma_{\mu \nu} q^{\nu}+\frac{f_{3}}{m_{\Lambda_{b}}} q_{\mu}\right] u_{\Lambda_{b}}, \\
\langle\Lambda| \bar{s} \gamma_{\mu} \gamma_{5} b\left|\Lambda_{b}\right\rangle=\bar{u}_{\Lambda}\left[g_{1} \gamma_{\mu}+\frac{g_{2}}{m_{\Lambda_{b}}} i \sigma_{\mu \nu} q^{\nu}+\frac{g_{3}}{m_{\Lambda_{b}}} q_{\mu}\right] \gamma_{5} u_{\Lambda_{b}}, \\
\langle K| \bar{s} \gamma_{\mu}\left(1-\gamma_{5}\right) b|B\rangle=\left[\left(p_{B}+p_{K}\right)^{\mu}-\frac{m_{B}^{2}-m_{K}^{2}}{t} q^{\mu}\right] F_{1}^{B K}(t) \\
+\frac{m_{B}^{2}-m_{K}^{2}}{t} q^{\mu} F_{0}^{B K}(t), \tag{2}
\end{gather*}
$$

with $t \equiv q^{2}$, where the momentum dependences of the form factors are given by [13]
$f_{1}(t)=\frac{f_{1}(0)}{\left(1-t / m_{\Lambda_{b}}^{2}\right)^{2}}, \quad g_{1}(t)=\frac{g_{1}(0)}{\left(1-t / m_{\Lambda_{b}}^{2}\right)^{2}}$,
and [14]
$F_{1}^{B K}(t)=\frac{F_{1}^{B K}(0)}{\left(1-\frac{t}{M_{V}^{2}}\right)\left(1-\frac{\sigma_{11} t}{M_{V}^{2}}+\frac{\sigma_{12} t^{2}}{M_{V}^{4}}\right)}$,
$F_{0}^{B K}(t)=\frac{F_{0}^{B K}(0)}{1-\frac{\sigma_{01} t}{M_{V}^{2}}+\frac{\sigma_{02} t^{2}}{M_{V}^{4}}}$.
Note that the other form factors $f_{2,3}\left(g_{2,3}\right)$ in Eq. (2) that need the loop calculations to flip the valence quark spins have been calculated to be small and safely ignored. In terms of the $S U(3)$ flavor and $S U(2)$ spin symmetries, one can relate $f_{1}(0)$ and $g_{1}(0)$ in Eq. (3) to be [9]
$f_{1}(0)=g_{1}(0)=-\sqrt{2 / 3} C_{F}$,
with $C_{F}$ to be extracted from the measured $\Lambda_{b} \rightarrow p\left(K^{-}, \pi^{-}\right)$decays [13]. With $X_{c}^{0}$ being $J^{P C}=1^{++}$, the matrix elements in Eq. (1)
of the $0 \rightarrow J / \psi$ and $0 \rightarrow X_{c}^{0}$ productions can be parameterized as
$\langle J / \psi| \bar{c} \gamma_{\mu} c|0\rangle=m_{J / \psi} f_{J / \psi} \varepsilon_{\mu}^{*}$,
$\left\langle X_{c}^{0}\right| \bar{c} \gamma_{\mu} \gamma_{5} c|0\rangle=m_{X_{c}^{0}} f_{X_{c}^{0}} \varepsilon_{\mu}^{*}$,
where $m_{J / \psi\left(X_{c}^{0}\right)}, f_{J / \psi\left(X_{c}^{0}\right)}$ and $\varepsilon_{\mu}^{*}$ are the mass, decay constant and polarization for $J / \psi\left(X_{c}^{0}\right)$, respectively. Because of the exotic nature of the $X_{c}^{0}$ state, which could be the $D \bar{D}^{*}$ molecule, the hybrid $c \bar{c} g$ state, or the tetraquark state, no present QCD model can derive $f_{X_{c}^{0}}$. Nonetheless, as we propose that $\Lambda_{b} \rightarrow X_{c}^{0} \Lambda$ and $B \rightarrow X_{c}^{0} K$ are connected, we are able to eliminate the unknown $f_{X_{c}^{0}}$ and predict $\mathcal{B}\left(\Lambda_{b} \rightarrow X_{c}^{0} \Lambda, X_{c}^{0} \rightarrow J / \psi \pi^{+} \pi^{-}\right)$in terms of the observed $\mathcal{B}\left(B \rightarrow X_{c}^{0} K, X_{c}^{0} \rightarrow J / \psi \pi^{+} \pi^{-}\right)$.

## 3. Numerical analysis and discussions

For the numerical analysis, the theoretical inputs of the CKM matrix parameters in terms of the Wolfenstein parameterization are taken to be $(\lambda, A, \rho, \eta)=(0.225,0.814,0.120 \pm 0.022,0.362 \pm$ 0.013 ) [5]. For the form factor in Eq. (5), we choose $C_{F}=0.136 \pm$ 0.009 [13], which is consistent with other QCD model calculations and used to explain the data in the $\Lambda_{b}$ decays [9,13]. In addition, from Ref. [14] we get $F_{1}^{B K}(0)=F_{0}^{B K}(0)=0.36$ with $\sigma_{11}=0.43$, $\sigma_{12}=0, \sigma_{01}=0.70, \sigma_{02}=0.27$ and $M_{V}=5.42 \mathrm{GeV}$. For the parameters $a_{2}\left(\hat{a}_{2}\right)$, we take $\left(a_{2}, \hat{a}_{2}\right)=(0.154 \pm 0.024,0.268 \pm 0.004)$, which are extracted from $\Lambda_{b} \rightarrow J / \psi \Lambda$ [9] and $B^{-} \rightarrow J / \psi K^{-}$[5], respectively. In terms of Eq. (1), we obtain
$\mathcal{R}_{X_{c}^{0}} \equiv \frac{\mathcal{B}\left(\Lambda_{b} \rightarrow X_{c}^{0} \Lambda\right)}{\mathcal{B}\left(B^{-} \rightarrow X_{c}^{0} K^{-}\right)}=0.61 \pm 0.20$,
where the unknown decay constant $f_{X_{c}^{0}}$ has been eliminated. The measurements for $B^{-} \rightarrow X(3872)^{0} K^{-}$and $B^{-} \rightarrow Y(4140)^{0} K^{-}$ give [5]
$\mathcal{B}\left(B^{-} \rightarrow K^{-}\left(X(3872)^{0} \rightarrow\right) J / \psi \pi^{+} \pi^{-}\right)$
$=(8.6 \pm 0.8) \times 10^{-6}$
and [11,12]

$$
\begin{align*}
& \mathcal{B}\left(B^{-} \rightarrow K^{-}(Y(4140) \rightarrow) J / \psi \phi\right) \\
& \quad=(0.149 \pm 0.039 \pm 0.024) \mathcal{B}\left(B^{-} \rightarrow J / \psi \phi K^{-}\right) \\
& \quad=(7.7 \pm 3.5) \times 10^{-6} \tag{9}
\end{align*}
$$

where we have used $\mathcal{B}\left(B^{-} \rightarrow J / \psi \phi K^{-}\right)=(5.2 \pm 1.7) \times 10^{-5}[5]$. By relating Eq. (7) to Eqs. (8) and (9), we find

$$
\begin{align*}
& \mathcal{B}\left(\Lambda_{b} \rightarrow \Lambda\left(X(3872)^{0} \rightarrow\right) J / \psi \pi^{+} \pi^{-}\right) \\
& \quad=(5.2 \pm 1.8) \times 10^{-6}  \tag{10}\\
& \mathcal{B}\left(\Lambda_{b} \rightarrow \Lambda(Y(4140) \rightarrow) J / \psi \phi\right)=(4.7 \pm 2.6) \times 10^{-6} \tag{11}
\end{align*}
$$

respectively, which can be reliable predictions to be compared with the future data. We remark that $\mathcal{B}\left(\bar{B}^{0} \rightarrow \bar{K}^{0}\left(X(3872)^{0} \rightarrow\right) J /\right.$ $\left.\psi \pi^{+} \pi^{-}\right)=(4.3 \pm 1.3) \times 10^{-6}$ [5] can also lead to similar results but with larger uncertainties than those in Eq. (10). It should be noted that the quantum numbers for $Y(4140)$ have not been experimentally identified yet, although they are predicted to be $J^{P C}=0^{++}\left(2^{++}\right)$in Ref. [15] and $1^{-+}$in Ref. [16] besides $1^{++}$in Ref. [4]. We emphasize that, even it is finally measured to have $J^{P C}=0^{++}[17]$ or $1^{-+}$, the decay of $\Lambda_{b} \rightarrow \Lambda(Y(4140) \rightarrow) J / \psi \phi$ can still be examined by our method. However, the factorization
approach would not support the tensor ( $T$ ) identification of the $J=2$ state due to $\langle T| \bar{c} \gamma_{\mu}\left(1-\gamma_{5}\right) c|0\rangle=0$.

Finally, we note that unlike $B^{-} \rightarrow X(3872)^{0} K^{-}$, which receives the dominant contribution from the doubly charmful $b \rightarrow c \bar{c} s$ transition, the decay of $B^{-} \rightarrow X(3872)^{-} \bar{K}^{0}$ is forbidden in Fig. 1 as supported by the experiment due to its non-observation [18], where $X(3872)^{-}$is the charged counterpart of $X(3872)^{0}$. However, this mode can proceed from the charmless $b \rightarrow d \bar{d} s$ transition, provided that the $c \bar{c}$ contents in $X(3872)^{-}$come from the intrinsic charm within the $B$ meson, which is similar to the pentaquark state productions in the $\Lambda_{b}$ decays [19,20]. As a result, in the charmless $B$ decays, the branching ratios of the three possible exotic decays of $\bar{B}^{0} \rightarrow X_{c}^{+} K^{-}, X_{c}^{+} \pi^{-}$, and $B^{-} \rightarrow X_{c}^{-} \bar{K}^{0}$ can be at the same level. In addition, the intrinsic charm mechanism would be used to the productions of the charged Y and Z particles as $\bar{B}^{0} \rightarrow Z(4430)^{+} K^{-}$with $Z(4430)^{+}$to consist of $c \bar{c} u \bar{d}$ [21, 22]. Moreover, the analogous statements for the corresponding $\Lambda_{b}$ decays can also be drawn.

## 4. Conclusions

We have explored the possibility to find the exotic meson states, such as the tetraquark four-quark bound states of $X_{c}^{0}=$ $c \bar{c} u \bar{u}(d \bar{d})$ and $c \bar{c} s \bar{s}$ in the $\Lambda_{b}$ decays. In particular, by concentrating on the scenarios with $X(3872)^{0}$ and $Y(4140)$ being $J^{P C}=1^{++}$, we have studied the doubly charmful $\Lambda_{b} \rightarrow X_{c}^{0} \Lambda$ decays. By connecting $\Lambda_{b} \rightarrow \Lambda X_{c}^{0}$ to $B^{-} \rightarrow K^{-} X_{c}^{0}$, we have found that $\mathcal{B}\left(\Lambda_{b} \rightarrow\right.$ $\left.\Lambda\left(X(3872)^{0} \rightarrow\right) J / \psi \pi^{+} \pi^{-}\right)$and $\mathcal{B}\left(\Lambda_{b} \rightarrow \Lambda(Y(4140) \rightarrow) J / \psi \phi\right)$ are $(5.2 \pm 1.8) \times 10^{-6}$ and $(4.7 \pm 2.6) \times 10^{-6}$, respectively. As these predicted branching ratios are accessible to the experiments at the LHCb, a measurement will be the first clean experimental evidence for the $X Y Z$ states in baryonic decays.

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