

NOTE

**A NOTE ON: 'DEQUE AUTOMATA AND A SUBFAMILY OF
CONTEXT-SENSITIVE LANGUAGES WHICH CONTAINS
ALL SEMILINEAR BOUNDED LANGUAGES' (BY K. AYERS)
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The topic of Ayer's paper are nondeterministic automata with one output restricted deque as worktape and operating in quasi-realtime (see [2, 5]). Clearly, in its mode of operation, an output restricted deque lies between a queue and a multihead Turing tape. Hence, the family \mathcal{D} of languages accepted by the machines under consideration lies between $\text{Post}(n)$, the family of languages accepted in real time by nondeterministic machines with one queue or Post tape (see [3]), and $\text{NTIME}(n)$, the family of languages accepted in real time or in linear time by multitape Turing machines (see [2]).

The latter insight improves [1, Theorem 2.1], and the further relation together with results from [6] show that Theorem 3.6 in Ayer's paper is *false*: languages in the class $\text{Post}(n)$ have an undecidable emptiness problem. For a proof, observe that deterministic machines with a queue as a worktape can simulate a Turing machine in quadratic time.

At last let me state an open problem in the field of Ayer's paper. See also [4]. Consider the families of languages accepted in real time (or in linear time) by nondeterministic machines whose worktape is a queue, or an output restricted deque, or a deque, or a finite number of Turing tapes respectively. Is this a strict hierarchy of families of languages?

References

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