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Enhanced Higgs mediated lepton flavour violating processes in the supersymmetric inverse seesaw model

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ABSTRACT: We study the impact of the inverse seesaw mechanism on several low-energy flavour violating observables such as $\tau \rightarrow \mu\mu\mu$ in the context of the Minimal Supersymmetric Standard Model. As a consequence of the inverse seesaw, the contributions of the right-handed sneutrinos significantly enhance the Higgs-mediated penguin diagrams. We find that different flavour violating branching ratios can be enhanced by as much as two orders of magnitude. We also comment on the impact of the Higgs-mediated processes on the leptonic B -meson decays and on the Higgs flavour violating decays.

KEYWORDS: Rare Decays, Beyond Standard Model, Neutrino Physics, Supersymmetric Standard Model

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Contents

1	Introduction	1
2	Inverse seesaw mechanism in the MSSM	3
3	Lepton flavour violation: Higgs-mediated contributions	5
4	Higgs-mediated lepton flavour violating observables	8
5	Results and discussion	11
6	Conclusions	13

1 Introduction

Neutrino oscillations have provided indisputable evidence for flavour violation in the neutral lepton sector. In the absence of any fundamental principle that prevents charged lepton flavour violation, one expects that extensions of the Standard Model (SM) accommodating neutrino masses and mixings should also allow for lepton flavour violation (LFV) in the charged lepton sector. Indeed, the additional new flavour dynamics and new field content present in many extensions of the SM may provide contributions to charged LFV (cLFV) processes such as radiative (e.g. $\mu \rightarrow e\gamma$) and three-body lepton decays (for instance $\tau \rightarrow \mu\mu\mu$). These decays generally arise from higher order processes, and so their branching ratios (Brs) are expected to be small, making them difficult to observe. Thus, any cLFV signal would provide clear evidence for new physics: mixings in the lepton sector and probably the presence of new particles, possibly shedding light on the origin of neutrino mass generation.

The search for manifestations of charged LFV constitutes the goal of several experiments [1–13], dedicated to look for signals of processes such as rare radiative decays, three-body decays and muon-electron conversion in nuclei. Despite the fact that a cLFV signal could provide clear evidence for new physics, the underlying mechanism of lepton mixing might be difficult to unravel. In parallel to the low-energy searches for new physics, i.e. via indirect effects of possible new particles, the LHC has started to search directly for these new particles in its quest to unveil the mechanism of electroweak symmetry breaking, thus possibly providing a solution to the SM hierarchy problem.

Among the many possible extensions of the SM, supersymmetry (SUSY) is a well motivated solution for the hierarchy problem, providing many other appealing aspects such as gauge coupling unification and dark matter candidates. If the LHC experiments indeed discover SUSY, it is then extremely interesting to consider supersymmetric models that can also explain neutrino masses and mixings. Furthermore, it is only natural to expect

that such models might also give rise to cLFV. If SUSY is indeed realised in nature, cLFV (mediated by new sparticles) would provide a new probe to explore the origin of lepton mixings, playing a complementary rôle to other searches of new physics, i.e. LHC direct searches and neutrino dedicated experiments.

One of the most economical possibilities is to embed a seesaw mechanism [14–27] in the framework of SUSY models (i.e. the SUSY seesaw) [28, 29]. For any seesaw realisation, the neutrino Yukawa couplings could leave their imprints in the SUSY soft-breaking slepton mass matrices, and consequently induce flavour violation at low energies due to the renormalisation group (RG) evolution of the SUSY soft-breaking parameters. The caveat of these scenarios is that, in order to have sufficiently large Yukawa couplings (as required to account for large cLFV Brs), the typical scale of the extra particles (such as right handed neutrinos, scalar or fermionic isospin triplets) is in general very high, potentially very close to the gauge coupling unification scale. However, such a high (seesaw) scale would be impossible to probe experimentally.

On the other hand, the so-called inverse seesaw [30] constitutes a very appealing alternative to the “standard” seesaw realisations. Embedding an inverse seesaw mechanism in the Minimal Supersymmetric extension of the SM (MSSM) requires the inclusion of two additional gauge singlet superfields, with opposite lepton numbers (+1 and −1). When compared to other SUSY seesaw realisations, cLFV observables are enhanced in this framework, and such an enhancement can be attributed to large neutrino Yukawa couplings ($Y_\nu \sim O(1)$), compatible with a seesaw scale M , close to the electroweak one, thus within LHC reach.

The differences between the inverse seesaw and the standard one can be conceptually understood from an effective point of view and linked to the distinct properties of the lepton number *violating* dimension-5 (Weinberg) operator (responsible for neutrino masses and mixings) and the total lepton number *conserving* dimension-6 operator, which is at the origin of cLFV. Contrary to what occurs in the standard seesaw, these two operators are de-correlated in the inverse seesaw, implying that the suppression of the coefficient of the dimension-5 operator will not affect the size of the coefficient of the dimension-6 operator. In both seesaws, the latter operator is proportional to $(Y_\nu^\dagger \frac{1}{|M|^2} Y_\nu)$; however, in the case of a type I seesaw, the dimension-5 operator is proportional to $(Y_\nu^\dagger \frac{1}{M} Y_\nu)$, while in the case of an inverse seesaw, it has a further suppression of $\frac{\mu}{M}$ (μ being a dimensionful parameter, linked to the mass of the sterile singlets). The dimension-6 operator will thus be extremely suppressed in the case of a type I seesaw, since in this case M is very large to accommodate natural Y_ν . In contrast, in the inverse seesaw, small neutrino masses can easily be accommodated via tiny values of μ , which will not affect the dimension 6 operator. Furthermore, such small values of μ are natural in the sense of ’t Hooft since in the limit where $\mu \rightarrow 0$, the total lepton number symmetry is restored [31].

In view of the strong potential of the inverse seesaw mechanism regarding cLFV, several phenomenological studies have recently been carried out [32–41]. While a non-supersymmetric inverse seesaw requires two pairs of singlets to explain neutrino oscillation data [38], the supersymmetric generalization can accommodate neutrino data [40] with

just one pair of singlets. The latter scenario is also known as the minimal supersymmetric inverse seesaw model (MSISM). This model can also comply with the dark matter relic abundance of the Universe [35].

The extra TeV scale singlet neutrinos may significantly contribute to cLFV observables, irrespective of the supersymmetric states [42–45]. Supersymmetric realisations of the inverse seesaw may enhance these cLFV rates even further (e.g. the contributions to $l_i \rightarrow l_j \gamma$, which has been analysed in [32]). Furthermore, this seesaw model can have LHC signatures: the extra singlets can participate in the decay chains, leading to effects which can be important, particularly in the case in which one of the singlets is the lightest supersymmetric particle (LSP) [40].

In this paper, we focus on contributions to cLFV observables, such as $\tau \rightarrow \mu \mu \mu$, arising from a Higgs-mediated effective vertex. We explore the contributions which are due to the presence of comparatively light right-handed neutrinos and sneutrinos (which are usually negligible in the framework of a type I SUSY-seesaw), while still having large neutrino Yukawa couplings. We find that all these contributions can lead to a significant enhancement of several cLFV observables.

The paper is organised as follows. In section 2, we define the model, providing a brief overview on the implementation of the inverse seesaw in the MSSM. In section 3, we discuss the implications of this model regarding low-energy cLFV observables, particular emphasis being given to the Higgs-mediated processes. In section 4, we study the Higgs-mediated contributions to several lepton flavour violating observables and compare our results to present bounds and to future experimental sensitivities in section 5. Then we draw some generic conclusions on the viability of an inverse seesaw as the underlying mechanism of LFV. We finally conclude in section 6.

2 Inverse seesaw mechanism in the MSSM

The model consists of the MSSM extended by three pairs of singlet superfields, $\widehat{\nu}_i^c$ and \widehat{X}_i ($i = 1, 2, 3$)¹ with lepton numbers assigned to be -1 and $+1$, respectively. The supersymmetric inverse seesaw model is defined by the superpotential

$$\begin{aligned} \mathcal{W} = \varepsilon_{ab} [& Y_d^{ij} \widehat{D}_i \widehat{Q}_j^b \widehat{H}_d^a + Y_u^{ij} \widehat{U}_i \widehat{Q}_j^a \widehat{H}_u^b + Y_e^{ij} \widehat{E}_i \widehat{L}_j^b \widehat{H}_d^a \\ & + Y_\nu^{ij} \widehat{\nu}_i^c \widehat{L}_j^a \widehat{H}_u^b - \mu \widehat{H}_d^a \widehat{H}_u^b] + M_{R_i} \widehat{\nu}_i^c \widehat{X}_i + \frac{1}{2} \mu_{X_i} \widehat{X}_i \widehat{X}_i, \end{aligned} \quad (2.1)$$

where $i, j = 1, 2, 3$ denote generation indices. In the above, \widehat{H}_d and \widehat{H}_u are the down- and up-type Higgs superfields, \widehat{L}_i denotes the SU(2) doublet lepton superfields. M_{R_i} represents the right-handed neutrino mass term which conserves lepton number. Due to the presence of non-vanishing μ_{X_i} , the total lepton number L is no longer a good quantum number; nevertheless, notice that in our formulation $(-1)^L$ is still a good symmetry. Without loss of generality, the terms $\widehat{\nu}_i^c \widehat{X}_i$ and $\widehat{X}_i \widehat{X}_i$ are taken to be diagonal in generation space. Clearly, as $\mu_{X_i} \rightarrow 0$, lepton number conservation is restored, since M_R does not violate

¹ $\widehat{\nu}^c = \widehat{\nu}_R^*$.

lepton number. Although in the present study we consider three generations of $\widehat{\nu}^c$ and \widehat{X} , we recall that in the minimal version of the SUSY inverse seesaw (where only one generation of $\widehat{\nu}^c$ and \widehat{X} is included), neutrino data can be accommodated [40].

The soft SUSY breaking Lagrangian can be written as

$$\begin{aligned}
 -\mathcal{L}_{\text{soft}} = & -\mathcal{L}_{\text{soft}}^{\text{MSSM}} + m_{\widetilde{\nu}^c}^2 \widetilde{\nu}_i^{c\dagger} \widetilde{\nu}_i^c + m_X^2 \widetilde{X}_i^\dagger \widetilde{X}_i \\
 & + \left(A_\nu Y_\nu^{ij} \varepsilon_{ab} \widetilde{\nu}_i^c \widetilde{L}_j^a H_u^b + B_{M_{R_i}} \widetilde{\nu}_i^c \widetilde{X}_i + \frac{1}{2} B_{\mu_{X_i}} \widetilde{X}_i \widetilde{X}_i + \text{h.c.} \right), \quad (2.2)
 \end{aligned}$$

where $\mathcal{L}_{\text{soft}}^{\text{MSSM}}$ denotes the soft SUSY breaking terms of the MSSM. In the above, the singlet scalar states \widetilde{X}_i and $\widetilde{\nu}_i^c$ are assumed to have flavour universal masses, i.e. $m_{X_i}^2 = m_X^2$ and $m_{\widetilde{\nu}_i^c}^2 = m_{\widetilde{\nu}^c}^2$. The parameters $B_{M_{R_i}}$ and $B_{\mu_{X_i}}$ are the new terms involving the scalar partners of the sterile neutrino states (notice that while the former conserves lepton number, the latter gives rise to a lepton number violating $\Delta L = 2$ term). Working under the assumption of a flavour-blind mechanism for SUSY breaking, we will assume universal boundary conditions² for the soft SUSY breaking parameters at some very high energy scale (e.g. the gauge coupling unification scale $\sim 10^{16}$ GeV),

$$m_\phi = m_0, \quad M_{\text{gaugino}} = M_{1/2}, \quad A_i = A_0. \quad (2.3)$$

Before addressing neutrino mass generation, a few comments on the nature of the superpotential are in order. As can be seen from eq. (2.1), the two singlets $\widehat{\nu}_i^c$ and \widehat{X}_i are differently treated in the sense that a $\Delta L = 2$ Majorana mass term is present for \widehat{X}_i ($\mu_{X_i} \widehat{X}_i \widehat{X}_i$), while no $\mu_{\nu_i^c} \widehat{\nu}_i^c \widehat{\nu}_i^c$ is present in \mathcal{W} . Although a generic superpotential with $(-1)^L$ should contain the latter term, let us notice that similar to what occurs for μ_{X_i} , the absence of $\mu_{\nu_i^c}$ also enhances the symmetry of the model; moreover, we emphasise that it is the magnitude of μ_{X_i} (and not that of $\mu_{\nu_i^c}$) which controls the size of the light neutrino mass [36, 41]. In view of this, and for the sake of simplicity, we have assumed $\mu_{\nu_i^c} = 0$ (considering non-vanishing, yet small values of $\mu_{\nu_i^c}$ would not change the qualitative features of the model). Although in our formulation we treat μ_{X_i} as an effective parameter, its origin can be explained either dynamically or in a framework of SUSY Grand Unified Theories (GUT) [36, 37, 41]. Furthermore $\mu_{\nu_i^c} \ll \mu_{X_i}$ can also be realised in extended frameworks [36].

In order to illustrate the pattern of light neutrino masses in the inverse seesaw model and how it is related to the lepton number violating parameter μ_{X_i} , we consider the one-generation case. In the $\{\nu, \nu^c, X\}$ basis the (3×3) neutrino mass matrix can be written as

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D & 0 & M_R \\ 0 & M_R & \mu_X \end{pmatrix}, \quad (2.4)$$

²In our subsequent numerical analysis, we will relax some of these universality conditions, considering non-universal soft breaking terms for the Higgs sector. In what concerns the right-handed sneutrino sector, we will assume that the corresponding soft-breaking masses hardly run between the GUT and the low-energy scale.

with $m_D = Y_\nu v_u$, yielding the mass eigenvalues ($m_1 \ll m_{2,3}$):

$$m_1 = \frac{m_D^2 \mu_X}{m_D^2 + M_R^2}, \quad m_{2,3} = \mp \sqrt{M_R^2 + m_D^2} + \frac{M_R^2 \mu_X}{2(m_D^2 + M_R^2)}. \quad (2.5)$$

The above equation clearly reveals that the lightness of the smallest eigenvalue m_1 is indeed due to the smallness of μ_X ($\mu_X \simeq m_1$). Thus the lepton number conserving mass parameters (m_D and M_R) are completely unconstrained in this model. Finally, it is worth noticing that the effective right-handed sneutrino mass term (Dirac-like) is given by $M_{\tilde{\nu}_i^c}^2 = m_{\tilde{\nu}_i^c}^2 + M_{R_i}^2 + \sum_j |Y_\nu^{ij}|^2 v_u^2$. Assuming $M_R \sim \mathcal{O}(\text{TeV})$, the effective mass term will not be very large, in clear contrast to what occurs in the standard (type I) SUSY seesaw. In our analysis, we will be particularly interested in the rôle of such a light sneutrino (i.e. $M_{\tilde{\nu}^c}^2 \sim M_{\text{SUSY}}^2$) in the enhancement of Higgs mediated contributions to lepton flavour violating observables.

3 Lepton flavour violation: Higgs-mediated contributions

In the SUSY seesaw framework, the only source of flavour violation is encoded in the neutrino Yukawa couplings (which are necessarily non-diagonal to account for neutrino oscillation data); even under the assumption of universal soft breaking terms at the GUT scale, radiative effects proportional to Y_ν induce flavour violation in the slepton mass matrices, which in turn give rise to slepton mediated cLFV observables [46–48]. As an example, in the leading logarithmic approximation, the RGE corrections to the left-handed slepton soft-breaking masses are given by

$$\begin{aligned} (\Delta m_L^2)_{ij} &\simeq -\frac{1}{8\pi^2} (3m_0^2 + A_0^2) (Y_\nu^\dagger L Y_\nu)_{ij}, & L &= \ln \frac{M_{\text{GUT}}}{M_R} \\ &= \xi (Y_\nu^\dagger Y_\nu)_{ij}. \end{aligned} \quad (3.1)$$

(For simplicity, in the above we are implicitly assuming a degenerate right-handed neutrino spectrum, $M_{R_i} = M_R$.) The RGE-induced flavour violating entries, $(\Delta m_L^2)_{ij}$, give rise to the dominant contributions to low-energy flavour violating observables in the charged lepton sector, such as $\ell_i \rightarrow \ell_j \gamma$ (mediated by chargino-sneutrino and neutralino-slepton loops) and $\ell_i \rightarrow \ell_j \ell_k \ell_m$ (from photon, Z and Higgs mediated penguin diagrams).

Compared to the standard (type I) SUSY seesaw, where $M_R \sim 10^{14} \text{ GeV}$, the inverse seesaw is characterised by a right handed neutrino mass scale $M_R \sim \mathcal{O}(\text{TeV})$ and this in turn leads to an enhancement of the factor ξ , (see eq. (3.1)), and hence to all low-energy cLFV observables, in the latter framework. Furthermore, having right-handed sneutrinos whose mass is of the same order of the other sfermions, i.e. $M_{\tilde{\nu}^c}^2 \sim M_{\text{SUSY}}^2$, the $\tilde{\nu}^c$ -mediated processes are no longer suppressed, and might even significantly contribute to the low-energy flavour violating observables. Here, we focus on the impact of such a light $\tilde{\nu}^c$ in the Higgs mediated processes which are expected to be important in the large $\tan \beta$ regime.

Although at tree level Higgs-mediated neutral currents are flavour conserving, non-holomorphic Yukawa interactions of the type $\bar{D}_R Q_L H_u^*$ can be induced at the one-loop level, as first noticed in [49]. In the large $\tan \beta$ regime, in addition to providing significant

corrections to the masses of the b -quark, these non-holomorphic couplings have an impact on $B^0 - \bar{B}^0$ mixing and flavour violating decays, in particular $B_s \rightarrow \mu^+ \mu^-$ [50–57]. Similarly, in the lepton sector, the origin of the Higgs-mediated flavour violating couplings can be traced to a non-holomorphic Yukawa term of the form $\bar{E}_R L H_u^*$ [58]. Other than the corrections to the τ lepton mass, these new couplings give rise to additional contributions to several cLFV processes mediated by Higgs exchange. In particular $B_s \rightarrow \mu \tau$, $B_s \rightarrow e \tau$ (the so-called double penguin processes) were considered in [57], while $\tau \rightarrow \mu \eta$ was studied in [59]. A detailed analysis of the several $\mu - \tau$ lepton flavour violating processes, namely $\tau \rightarrow \mu X$ ($X = \gamma, e^+ e^-, \mu^+ \mu^-, \rho, \pi, \eta, \eta'$) can be found in [60].

Even though the flavour violating processes in the quark and lepton sectors have a similar diagrammatic origin, the source of flavour violation is different in each case. In the quark sector, trilinear soft SUSY breaking couplings involving up-type squarks provide the dominant source of flavour violation [51], while in the lepton case, LFV stems from the radiatively induced non-diagonal terms in the slepton masses (see eq. (3.1)) [58].

In the standard SUSY seesaw (type I), the term $\tilde{\nu}_i^c H_u \tilde{L}_j$ is usually neglected, as it is suppressed by the very heavy right handed sneutrino masses ($M_{\tilde{\nu}_i^c} \sim 10^{14}$ GeV). However, in scenarios such as the inverse SUSY seesaw, where $M_{\tilde{\nu}_i^c} \sim \mathcal{O}(\text{TeV})$, this term may provide the dominant contributions to Higgs mediated lepton flavour violation.

The effective Lagrangian describing the couplings of the neutral Higgs fields to the charged leptons is given by

$$-\mathcal{L}^{\text{eff}} = \bar{E}_R^i Y_e^{ii} [\delta_{ij} H_d^0 + (\epsilon_1 \delta_{ij} + \epsilon_{2ij} (Y_\nu^\dagger Y_\nu)_{ij}) H_u^{0*}] E_L^j + \text{h.c.} \quad (3.2)$$

In the above, the first term corresponds to the usual Yukawa interaction, while the coefficient ϵ_1 encodes the corrections to the charged lepton Yukawa couplings. In the basis where the charged lepton Yukawa couplings are diagonal, the last term in eq. (3.2), i.e. $\epsilon_{2ij} (Y_\nu^\dagger Y_\nu)_{ij}$, is in general non-diagonal, thus providing a new source of charged lepton flavour violation through Higgs mediation. Its origin can be diagrammatically understood from figure 1, where flavour violation is parametrized via a mass insertion $(\Delta m_L^2)_{ij}$ (see eq. (3.1)). The coefficient ϵ_2 can be estimated as

$$\begin{aligned}
 \epsilon_{2ij} = & \frac{\alpha'}{8\pi} \xi \mu M_1 [2F_2(M_1^2, m_{\tilde{E}_{Lj}}^2, m_{\tilde{E}_{Li}}^2, m_{\tilde{E}_{Ri}}^2) - F_2(\mu^2, m_{\tilde{E}_{Lj}}^2, m_{\tilde{E}_{Li}}^2, M_1^2)] \\
 & + \frac{\alpha_2}{8\pi} \xi \mu M_2 [F_2(\mu^2, m_{\tilde{E}_{Lj}}^2, m_{\tilde{E}_{Li}}^2, M_2^2) + 2F_2(\mu^2, m_{\tilde{\nu}_{Lj}}^2, m_{\tilde{\nu}_{Li}}^2, M_2^2)], \quad (3.3)
 \end{aligned}$$

where

$$F_2(x, y, z, w) = -\frac{x \ln x}{(x-y)(x-z)(x-w)} - \frac{y \ln y}{(y-x)(y-z)(y-w)} + (x \leftrightarrow z, y \leftrightarrow w). \quad (3.4)$$

Here, M_1 and M_2 are the masses of the electroweak gauginos at low energies. On the other hand, the flavour conserving loop-induced form factor ϵ_1 (notice that the diagrams of figure 1 contribute to this form factor, but without the slepton flavour mixings in the internal lines) can be expressed as [57, 58]

$$\begin{aligned}
 \epsilon_1 = & \frac{\alpha'}{8\pi} \mu M_1 [2F_1(M_1^2, m_{\tilde{E}_L}^2, m_{\tilde{E}_R}^2) - F_1(M_1^2, \mu^2, m_{\tilde{E}_L}^2) + 2F_1(M_1^2, \mu^2, m_{\tilde{E}_R}^2)] \\
 & + \frac{\alpha_2}{8\pi} \mu M_2 [F_1(\mu^2, m_{\tilde{E}_L}^2, M_2^2) + 2F_1(\mu^2, m_{\tilde{\nu}_L}^2, M_2^2)], \quad (3.5)
 \end{aligned}$$

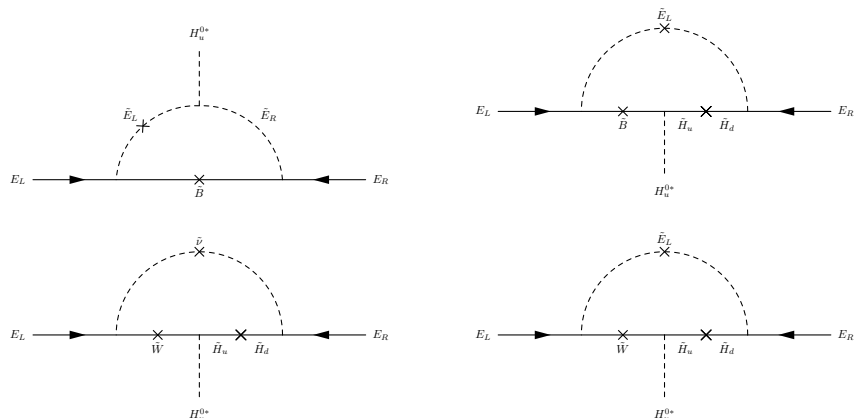


Figure 1. Diagrams contributing to ϵ_2 . Crosses on scalar lines represent LFV mass insertions $(\Delta m_L^2)_{ij}$, while those on fermion lines denote chirality flips.

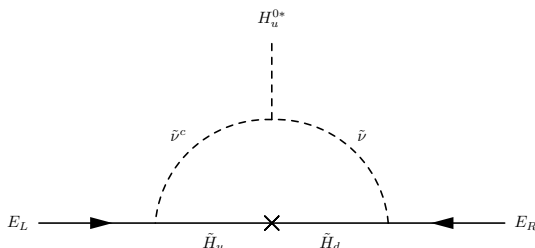


Figure 2. Right-handed sneutrino contribution to ϵ'_2 . This contribution is particularly relevant when $\tilde{\nu}^c$ is light.

with

$$F_1(x, y, z) = -\frac{xy \ln(x/y) + yz \ln(y/z) + zx \ln(z/x)}{(x-y)(y-z)(z-x)}. \quad (3.6)$$

In the standard seesaw mechanism, the diagrams of figure 1 provide the only source for Higgs-mediated lepton flavour violation. However, in the framework of the inverse SUSY seesaw, there is an additional diagram that may even account for the dominant Higgs-mediated lepton flavour violation contribution: the sneutrino-chargino mediated loop, depicted in figure 2. (Due to the large masses of $\tilde{\nu}^c$ in the standard (type I) seesaw, this process provides negligible contributions, and is hence not taken into account.)

The effective Lagrangian terms encoding lepton flavour violation is accordingly modified as

$$-\mathcal{L}^{\text{LFV}} = \bar{E}_R^i Y_e^{ii} \epsilon_{2ij}^{\text{tot}} (Y_\nu^\dagger Y_\nu)_{ij} H_u^{0*} E_L^j + \text{h.c.}, \quad (3.7)$$

where $\epsilon_2^{\text{tot}} = \epsilon_2 + \epsilon'_2$, ϵ'_2 being the contribution from the new diagram. This contribution can be expressed as

$$\epsilon'_{2ij} = \frac{1}{16\pi^2} \mu A_\nu F_1(\mu^2, m_{\tilde{\nu}_i}^2, M_{\tilde{\nu}_j^c}^2). \quad (3.8)$$

In the above, we have parametrized the soft trilinear term for the neutral leptons as $A_\nu Y_\nu$, where A_ν is a flavour independent real mass term.

Below, we provide an approximate estimate of the relative contributions of the terms ϵ_2 and ϵ'_2 : for simplicity we take $M_{\tilde{\nu}^c} \sim \mathcal{O}(\text{TeV})$ and assume common values for the masses of all SUSY particles and dimensionful terms A_ν at low energies, symbolically denoted by $A_\nu \sim \langle \tilde{m} \rangle \sim M_{\text{SUSY}}$. In this limit, the loop functions are given by $F_2(x, x, x, x) = \frac{1}{6x^2}$ and $F_1(x, x, x) = \frac{1}{2x}$. This leads to

$$\epsilon_2 = \frac{1}{8\pi} \xi \tilde{m}^2 \left(\frac{\alpha'}{6\tilde{m}^4} + 3 \frac{\alpha_2}{6\tilde{m}^4} \right) \simeq -0.0007, \quad (3.9)$$

while

$$\epsilon'_2 = \frac{1}{16\pi^2} \tilde{m}^2 \frac{1}{2\tilde{m}^2} \simeq 0.003. \quad (3.10)$$

In this illustrative (leading order) calculation, we have assumed that at M_{GUT} , one has $A_0 = 0$, taking for the gauge couplings $\alpha_2 = 0.03$ and $\alpha' = 0.008$. Following eq. (3.1), and assuming $M_R = 10^3 \text{ GeV}$, one gets $\xi \sim -1.1 m_0^2$. Thus, at the leading order in the inverse seesaw, the lepton flavour violation coefficient becomes $|\epsilon_2^{\text{tot}}| = |\epsilon_2 + \epsilon'_2| \simeq 2 \times 10^{-3}$.

For completeness, let us notice that in the standard seesaw model (where sizeable Yukawa couplings are typically associated to a right-handed neutrino mass scale $\sim 10^{14} \text{ GeV}$), assuming the same amount of flavour violation as parametrized by ξ , one finds $|\epsilon_2^{\text{tot}}| = |\epsilon_2| \simeq 2 \times 10^{-4}$. This clearly reveals that in the inverse SUSY seesaw, ϵ_2^{tot} is enhanced by a factor of order ~ 10 compared to the standard seesaw.

The large enhancement of ϵ_2^{tot} will have an impact regarding all Higgs-mediated lepton flavour violating observables. The computation of the cLFV observables requires specifying the couplings of the physical Higgs bosons to the leptons, in particular $\bar{E}_R^i E_L^j H_k$ (where $H_k = h, H, A$). The effective Lagrangian describing this interaction can be derived from eq. (3.2), and reads [57, 58] as

$$-\mathcal{L}_{i \neq j}^{\text{eff}} = (2G_F^2)^{1/4} \frac{m_{E_i} \kappa_{ij}^E}{\cos^2 \beta} (\bar{E}_R^i E_L^j) [\cos(\alpha - \beta)h + \sin(\alpha - \beta)H - iA] + \text{h.c.}, \quad (3.11)$$

where α is the CP-even Higgs mixing angle and $\tan \beta = v_u/v_d$, and

$$\kappa_{ij}^E = \frac{\epsilon_{2ij}^{\text{tot}} (Y_\nu^\dagger Y_\nu)_{ij}}{[1 + (\epsilon_1 + \epsilon_{2ii}^{\text{tot}} (Y_\nu^\dagger Y_\nu)_{ii}) \tan \beta]^2}. \quad (3.12)$$

As clear from the above equation, large values of ϵ_2^{tot} lead to an augmentation of κ_{ij}^E . Given that the cLFV branching ratios are proportional to $(\kappa_{ij}^E)^2$, a sizeable enhancement, as large as two orders of magnitude, is expected for all Higgs-mediated LFV observables.

4 Higgs-mediated lepton flavour violating observables

Here we focus our attention on the cLFV observables where the dominant contribution to flavour violation arises from the Higgs penguin diagrams, in particular those involving τ -leptons (due to the comparatively large value of Y_τ).

In what follows, we discuss some of these LFV decays in detail.

- $\tau \rightarrow 3\mu$

In the large $\tan\beta$ regime, Higgs-mediated flavour violating diagrams would be particularly important in this decay mode. The branching ratio can be expressed as [57, 58]

$$\begin{aligned} \text{Br}(\tau \rightarrow 3\mu) &= \frac{G_F^2 m_\mu^2 m_\tau^7 \tau_\tau}{1536 \pi^3 \cos^6 \beta} |\kappa_{\tau\mu}^E|^2 \left[\left(\frac{\sin(\alpha-\beta) \cos \alpha}{M_H^2} - \frac{\cos(\alpha-\beta) \sin \alpha}{M_h^2} \right)^2 + \frac{\sin^2 \beta}{M_A^4} \right] \\ &\approx \frac{G_F^2 m_\mu^2 m_\tau^7 \tau_\tau}{768 \pi^3 M_A^4} |\kappa_{\tau\mu}^E|^2 \tan^6 \beta. \end{aligned} \quad (4.1)$$

In the above, τ_τ is the τ life time and the approximate result has been obtained in the large $\tan\beta$ regime. For other Higgs-mediated lepton flavour violating 3-body decays, $\tau \rightarrow e\mu\mu$, $\tau \rightarrow 3e$ or $\mu \rightarrow 3e$, their corresponding branching ratios can easily be obtained with the appropriate kinematic factors and the flavour changing factor κ . While $\text{Br}(\tau \rightarrow e\mu\mu)$ can be as large as $\text{Br}(\tau \rightarrow 3\mu)$ when $(Y_\nu^\dagger Y_\nu)_{13} \sim O(1)$ (which is possible in the case of an inverted hierarchical light neutrino spectrum), other flavour violating decays with final state electrons such as $\mu \rightarrow 3e$ are considerably suppressed due to the smallness of the Yukawa couplings.

- $B_s \rightarrow \ell_i \ell_j$

B mesons can also have Higgs-mediated LFV decays, which are significantly enhanced in the large $\tan\beta$ regime. The branching fraction is given by

$$\begin{aligned} \text{Br}(B_s \rightarrow \ell_i \ell_j) &= \frac{G_F^4 M_W^4}{8 \pi^5} |V_{tb}^* V_{ts}|^2 M_{B_s}^5 f_{B_s}^2 \tau_{B_s} \left(\frac{m_b}{m_b + m_s} \right)^2 \\ &\times \sqrt{\left[1 - \frac{(m_{\ell_i} + m_{\ell_j})^2}{M_{B_s}^2} \right] \left[1 - \frac{(m_{\ell_i} - m_{\ell_j})^2}{M_{B_s}^2} \right]} \\ &\times \left\{ \left(1 - \frac{(m_{\ell_i} + m_{\ell_j})^2}{M_{B_s}^2} \right) |c_S^{ij}|^2 + \left(1 - \frac{(m_{\ell_i} - m_{\ell_j})^2}{M_{B_s}^2} \right) |c_P^{ij}|^2 \right\}, \end{aligned} \quad (4.2)$$

where V_{ij} represents the Cabibbo-Kobayashi-Maskawa (CKM) matrix, M_{B_s} and τ_{B_s} respectively denote the mass and lifetime of the B_s meson, while $f_{B_s} = 230 \pm 30 \text{ MeV}$ [61] is the B_s meson decay constant and c_P^{ij} , c_S^{ij} are the form factors. As an example, the lepton flavour violating (double-penguin) $B_s \rightarrow \mu\tau$ decay can be computed with the following form factors [57]:

$$\begin{aligned} c_S^{\mu\tau} = c_P^{\mu\tau} &= \frac{\sqrt{2} \pi^2}{G_F M_W^2} \frac{m_\tau \kappa_{bs}^d \kappa_{\tau\mu}^{E*}}{\cos^4 \beta \bar{\lambda}_{bs}^t} \left[\frac{\sin^2(\alpha-\beta)}{M_H^2} + \frac{\cos^2(\alpha-\beta)}{M_h^2} + \frac{1}{M_A^2} \right] \\ &\approx \frac{8 \pi^2 m_\tau m_t^2}{M_W^2} \frac{\epsilon_Y \kappa_{\tau\mu}^E \tan^4 \beta}{[1 + (\epsilon_0 + \epsilon_Y Y_t^2) \tan \beta][1 + \epsilon_0 \tan \beta]} \frac{1}{M_A^2}. \end{aligned} \quad (4.3)$$

Here, κ_{bs}^d represents the flavour mixing in the quark sector while $\bar{\lambda}_{bs}^t = V_{tb}^* V_{ts}$. Similarly, ϵ_0 and ϵ_Y are the down type quark form factors mediated by gluino and squark exchange diagrams. The final result was, once again, derived in the large $\tan\beta$ regime. The branching fractions of other flavour violating decays such as

$\text{Br}(B_{d,s} \rightarrow \tau e)$, would receive identical contribution from the Higgs penguins. Likewise, the $\text{Br}(B_{d,s} \rightarrow \mu e)$ can be calculated using the appropriate form factors and lepton masses; as expected, these will be suppressed when compared to $\text{Br}(B_{d,s} \rightarrow \tau \mu)$.

- $\tau \rightarrow \mu P$

Similar to what occurred in the previous processes, virtual Higgs exchange could also induce decays such as $\tau \rightarrow \mu P$, where P denotes a neutral pseudoscalar meson ($P = \pi, \eta, \eta'$). In the large $\tan \beta$ limit, where the pseudoscalar Higgs couplings to down-type quarks are enhanced, CP-odd Higgs boson exchanges provide the dominant contribution to the $\tau \rightarrow \mu P$ decay. The coupling can be written as

$$-i(\sqrt{2}G_F)^{1/2} \tan \beta A(\xi_d m_d \bar{d}d + \xi_s m_s \bar{s}s + \xi_b m_b \bar{b}b) + \text{h.c.} . \quad (4.4)$$

Here, the parameters ξ_d, ξ_s, ξ_b are of order $\mathcal{O}(1)$. Since we are mostly interested in the Higgs-mediated contributions, we estimate the amplitude of these processes in the limit when both $\tau \rightarrow 3\mu$ and $\tau \rightarrow \mu P$ are indeed dominated by the exchange of the scalar fields. Accordingly, and following [60], one can write

$$\frac{\text{Br}(\tau \rightarrow \mu \eta)}{\text{Br}(\tau \rightarrow 3\mu)} \simeq 36 \pi^2 \left(\frac{f_\eta^8 m_\eta^2}{m_\mu m_\tau^2} \right)^2 (1 - x_\eta)^2 \left[\xi_s + \frac{\xi_b}{3} \left(1 + \sqrt{2} \frac{f_\eta^0}{f_\eta^8} \right) \right]^2, \quad (4.5)$$

$$\frac{\text{Br}(\tau \rightarrow \mu \eta')}{\text{Br}(\tau \rightarrow \mu \eta)} \simeq \frac{2}{9} \left(\frac{f_{\eta'}^0}{f_\eta^8} \right)^2 \frac{m_{\eta'}^4}{m_\eta^4} \left(\frac{1 - x_{\eta'}}{1 - x_\eta} \right)^2 \left[\frac{1 + \frac{3}{\sqrt{2}} \frac{f_{\eta'}^8}{f_\eta^0} \left(\frac{\xi_s}{\xi_b} + \frac{1}{3} \right)}{\frac{\xi_s}{\xi_b} + \frac{1}{3} + \frac{\sqrt{2}}{3} \frac{f_\eta^0}{f_\eta^8}} \right]^2, \quad (4.6)$$

$$\frac{\text{Br}(\tau \rightarrow \mu \pi)}{\text{Br}(\tau \rightarrow \mu \eta)} \simeq \frac{4}{3} \left(\frac{f_\pi}{f_\eta^8} \right)^2 \frac{m_\pi^4}{m_\eta^4} (1 - x_\eta)^{-2} \left[\frac{\frac{\xi_d}{\xi_b} \frac{1}{1+z} + \frac{1}{2} \left(1 + \frac{\xi_s}{\xi_b} \right) \frac{1-z}{1+z}}{\frac{\xi_s}{\xi_b} + \frac{1}{3} + \frac{\sqrt{2}}{3} \frac{f_\eta^0}{f_\eta^8}} \right]^2, \quad (4.7)$$

where $z = m_u/m_d, m_\pi, f_\pi$ are the pion mass and decay constant, $m_{\eta, \eta'}$ are the masses of η, η' , $x_{\eta, \eta'} = m_{\eta, \eta'}^2/m_\pi^2$, and $f_{\eta, \eta'}^8$ and $f_{\eta, \eta'}^0$ are evaluated from the corresponding matrix elements. As first discussed in [59], and taking $\xi_s, \xi_b \sim 1$ and fixing the other parameters as in [60], one finds $\frac{\text{Br}(\tau \rightarrow \mu \eta)}{\text{Br}(\tau \rightarrow 3\mu)} \simeq 5$. The other branching fractions such as $\text{Br}(\tau \rightarrow \mu \eta', \mu \pi)$ are considerably suppressed compared to $\text{Br}(\tau \rightarrow \mu \eta)$. While the ratio $\frac{\text{Br}(\tau \rightarrow \mu \eta')}{\text{Br}(\tau \rightarrow \mu \eta)}$ can be as large as 6×10^{-3} , $\frac{\text{Br}(\tau \rightarrow \mu \pi)}{\text{Br}(\tau \rightarrow \mu \eta)}$ would approximately lie in the range $10^{-3} - 4 \times 10^{-3}$ [60]. Since all these ratios are independent of $\kappa_{\tau\mu}^E$, the above quoted numbers can also be applied to the present framework. However, an enhancement in the $\text{Br}(\tau \rightarrow 3\mu)$, due to the large values of $\kappa_{\tau\mu}^E$, would also imply sizeable values of $\text{Br}(\tau \rightarrow \mu \eta)$.

- $H_k \rightarrow \mu \tau$ ($H_k = h, H, A$)

The branching ratios of flavour violating Higgs decays provide another interesting probe of lepton flavour violation. Following [62], the branching fraction $H_k \rightarrow \mu \tau$ (normalised to the flavour conserving one $H_k \rightarrow \tau \tau$) can be cast as:

$$\text{Br}(H_k \rightarrow \mu \tau) = \tan^2 \beta (|\kappa_{\tau\mu}^E|^2) C_\Phi \text{Br}(H_k \rightarrow \tau \tau), \quad (4.8)$$

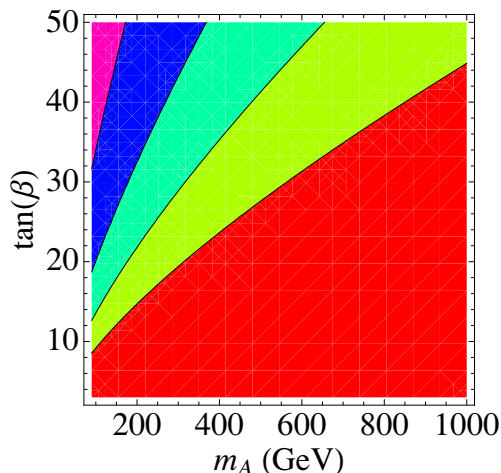


Figure 3. Branching ratio of the process $\tau \rightarrow 3\mu$ as a function of m_A (GeV) and $\tan\beta$. From left to right, the contours correspond to $\text{Br}(\tau \rightarrow 3\mu) = 2.1 \times 10^{-8}, 10^{-9}, 10^{-10}, 10^{-11}$. The purple region has already been experimentally excluded [63].

where we approximated $1/\cos^2\beta \simeq \tan^2\beta$. The coefficients C_Φ are given by:

$$C_h = \left[\frac{\cos(\beta - \alpha)}{\sin\alpha} \right]^2, \quad C_H = \left[\frac{\sin(\beta - \alpha)}{\cos\alpha} \right]^2, \quad C_A = 1. \quad (4.9)$$

5 Results and discussion

As discussed in section 3, in the inverse supersymmetric seesaw, Higgs-mediated contributions can lead to an enhancement of several LFV observables by as much as two orders of magnitude, compared to what is expected in the standard SUSY seesaw.

As expected from the analytical study of section 4, m_A and $\tan\beta$ are the most relevant parameters in the Higgs-mediated flavour violating processes. To better illustrate this, in figure 3 we study the dependence of $\text{Br}(\tau \rightarrow 3\mu)$ on the aforementioned parameters. We have assumed a common value for the squark masses, $m_{\tilde{q}} \sim \text{TeV}$, while for left- and right-handed sleptons we take $m_{\tilde{l}} \sim 400 \text{ GeV}$ and $M_{\tilde{\nu}^c} \sim 3 \text{ TeV}$ for the right handed sneutrinos. The contours correspond to different values of the branching ratios (the purple region has already been experimentally excluded). From this figure one can easily identify the regimes for m_A and $\tan\beta$ which are associated to values of the LFV observables within reach of the present and future experiments.

In what follows, we numerically evaluate some LFV observables. Concerning the mSUGRA parameters (and instead of scanning over the parameter space), we have selected a few benchmark points [64] that already take into account the most recent LHC constraints [65, 66]. We have also considered the case in which the GUT scale universality conditions are relaxed for the Higgs sector, i.e. scenarios of Non-Universal Higgs Masses (NUHM), as this allows to explore the impact of a light CP-odd Higgs boson. In table 1, we list the chosen points: CMSSM-A and CMSSM-B respectively correspond to the 10.2.2 and 40.1.1 benchmark points in [64], while NUHM-C is an example of a non-universal scenario.

Point	$\tan \beta$	$m_{1/2}$	m_0	$m_{H_U}^2$	$m_{H_D}^2$	A_0	μ	m_A
CMSSM-A	10	550	225	$(225)^2$	$(225)^2$	0	690	782
CMSSM-B	40	500	330	$(330)^2$	$(330)^2$	-500	698	604
NUHM-C	15	550	225	$(652)^2$	$-(570)^2$	0	478	150

Table 1. Benchmark points used in the numerical analysis (dimensionful parameters in GeV). CMSSM-A and CMSSM-B correspond to 10.2.2 and 40.1.1 benchmark points of [64].

For each point considered, the low-energy SUSY parameters were obtained using Suspect [67]. In what concerns the evolution of the soft-breaking right-handed sneutrino masses $m_{\tilde{\nu}^c}^2$, we have assumed that the latter hardly run between the GUT scale and the low-energy one. The flavour-violating charged slepton parameters (e.g. $(\Delta m_L^2)_{ij}$ or ξ), were estimated at the leading order using eq. (3.1). Concerning NUHM, we use the same value of ξ as for CMSSM-A. Here, we are particularly interested to study the effect of light CP-odd Higgs boson and this naive approximation will serve our purpose. Furthermore, we use the mass insertion approximation, assuming that mixing between left and right chiral slepton states are relatively small. In computing the branching fractions and the flavour violating factor κ_{ij}^E we have assumed (physical) right-handed sneutrino masses $M_{\tilde{\nu}^c} \approx 3 \text{ TeV}$ and $(Y_\nu^\dagger Y_\nu) = 0.7$, in agreement with low-energy neutrino data as well as other low-energy constraints, which are particularly relevant in the inverse seesaw case such as Non-Standard Neutrino Interactions bounds [68, 69]. Moreover, in our numerical analysis, we have fixed the trilinear soft breaking parameter $A_\nu = -500 \text{ GeV}$ (at the SUSY scale).

We now proceed to present our results for the flavour violating observables discussed in section 4. In table 2, we collect the values of the different branching ratios, as obtained for the considered benchmark points of table 1. We have also presented the corresponding current experimental bounds and future sensitivity.

From table 2, one can verify that from an experimental point of view, the most promising channel in the supersymmetric inverse seesaw is $\tau \rightarrow \mu \eta$ which could be tested at the next generation of B factories. The $B_{d,s}^0 \rightarrow \mu \tau$ decay might also be interesting, but little conclusions can be drawn due to lack of information concerning the future sensitivities.

It is important to stress that the numerical results summarised in table 2 correspond to considering *only* Higgs-mediated contributions. In the low $\tan \beta$ regime, photon- and Z -penguin diagrams may induce comparable or even larger contributions to the observables, and potentially enhance the branching fractions. Thus, the results for small $\tan \beta$ should be interpreted as conservative estimates, representing only partial contributions. For large $\tan \beta$ values, Higgs penguins do indeed provide the leading contributions. Comparing our results with those obtained for a type I SUSY seesaw at high scales (or even with a TeV scale SUSY seesaw), we find a large enhancement of the branching fractions in the inverse seesaw framework.

Another interesting property of the Higgs-mediated processes is that the corresponding amplitude strongly depends on the chirality of the heaviest lepton (be it the decaying lepton, or the heaviest lepton produced in B decays). Considering the decays of a left-

LFV Process	Present Bound	Future Sensitivity	CMSSM-A	CMSSM-B	NUHM-C
$\tau \rightarrow \mu\mu\mu$	2.1×10^{-8} [63]	8.2×10^{-10} [73]	1.4×10^{-15}	3.9×10^{-11}	8.0×10^{-12}
$\tau^- \rightarrow e^- \mu^+ \mu^-$	2.7×10^{-8} [63]	$\sim 10^{-10}$ [73]	1.4×10^{-15}	3.4×10^{-11}	8.0×10^{-12}
$\tau \rightarrow eee$	2.7×10^{-8} [63]	2.3×10^{-10} [73]	3.2×10^{-20}	9.2×10^{-16}	1.9×10^{-16}
$\mu \rightarrow eee$	1.0×10^{-12} [1]		6.3×10^{-22}	1.5×10^{-17}	3.7×10^{-18}
$\tau \rightarrow \mu\eta$	2.3×10^{-8} [70]	$\sim 10^{-10}$ [73]	8.0×10^{-15}	3.3×10^{-10}	4.6×10^{-11}
$\tau \rightarrow \mu\eta'$	3.8×10^{-8} [70]	$\sim 10^{-10}$ [73]	4.3×10^{-16}	1.1×10^{-10}	3.1×10^{-12}
$\tau \rightarrow \mu\pi^0$	2.2×10^{-8} [70]	$\sim 10^{-10}$ [73]	1.8×10^{-17}	8.5×10^{-13}	1.0×10^{-13}
$B_d^0 \rightarrow \mu\tau$	2.2×10^{-5} [71]		2.7×10^{-15}	8.5×10^{-10}	2.7×10^{-11}
$B_d^0 \rightarrow e\mu$	6.4×10^{-8} [72]	1.6×10^{-8} [74]	1.2×10^{-17}	3.1×10^{-12}	1.2×10^{-13}
$B_s^0 \rightarrow \mu\tau$			7.7×10^{-14}	2.5×10^{-8}	7.8×10^{-10}
$B_s^0 \rightarrow e\mu$	2.0×10^{-7} [72]	6.5×10^{-8} [74]	3.4×10^{-16}	8.9×10^{-11}	3.4×10^{-12}
$h \rightarrow \mu\tau$			1.3×10^{-8}	2.6×10^{-7}	2.3×10^{-6}
$A, H \rightarrow \mu\tau$			3.4×10^{-6}	1.3×10^{-4}	5.0×10^{-6}

Table 2. Higgs-mediated contributions to the branching ratios of several lepton flavour violating processes, for the different benchmark points of table 1. We also present the current experimental bounds and future sensitivities for the LFV observables.

handed lepton $\ell_L^i \rightarrow \ell_R^j X$, one finds that the corresponding branching ratios would be suppressed by a factor $\frac{m_{\ell^j}^2}{m_{\ell^i}^2}$ compared to those of the right-handed lepton $\ell_R^i \rightarrow \ell_L^j X$. This can induce an asymmetry that potentially allows to identify if Higgs mediation is the dominant contribution to the LFV observables. Furthermore this asymmetry would be more pronounced in the inverse-seesaw framework.

Due to its strong enhancement of the Higgs-penguin contributions, if realised in Nature, the inverse seesaw offers a unique framework to test Higgs effects in LFV processes. In fact, and as discussed in [47, 48], if photon penguins provide the dominant contribution to both $\text{Br}(\tau \rightarrow 3\mu)$ and $\text{Br}(\tau \rightarrow \mu\gamma)$, then the latter observables are strongly correlated, $\frac{\text{Br}(\tau \rightarrow 3\mu)}{\text{Br}(\tau \rightarrow \mu\gamma)} \sim 0.003$ (see [47, 48]). On the other hand, if the dominant contribution to the three-body decays arises from Higgs penguins, the correlation no longer holds, and the latter ratio can be significantly enhanced. This would be the case of the present framework.

6 Conclusions

If observed, charged lepton flavour violation clearly signals the presence of new physics. In this work, we have studied Higgs-mediated LFV processes in the framework of the supersymmetric inverse seesaw. TeV scale right-handed neutrinos (and hence light right-handed sneutrinos) offer the possibility to enhance the Higgs-mediated contributions to several LFV processes. As shown in this work, in the inverse SUSY seesaw, LFV branching ratios can be enhanced by as much as two orders of magnitude when compared to the standard (type I) SUSY seesaw.

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