Evolution of Robustness and Plasticity under Environmental Fluctuation: Formulation in Terms of Phenotypic Variances

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Abstract The characterization of plasticity, robustness, and evolvability, an important issue in biology, is studied in terms of phenotypic fluctuations. By numerically evolving gene regulatory networks, the proportionality between the phenotypic variances of epigenetic and genetic origins is confirmed. The former is given by the variance of the phenotypic fluctuation due to noise in the developmental process; and the latter, by the variance of the phenotypic fluctuation due to genetic mutation. The relationship suggests a link between robustness to noise and to mutation, since robustness can be defined by the sharpness of the distribution of the phenotype. Next, the proportionality between the variances is demonstrated to also hold over expressions of different genes (phenotypic traits) when the system acquires robustness through the evolution. Then, evolution under environmental variation is numerically investigated and it is found that both the adaptability to a novel environment and the robustness are made compatible when a certain degree of phenotypic fluctuations exists due to noise. The highest adaptability is achieved at a certain noise level at which the gene expression dynamics are near the critical state to lose the robustness. Based on our results, we revisit Waddington's canalization and genetic assimilation with regard to the two types of phenotypic fluctuations.

Keywords Robustness · Fluctuation-response relationship · Evolution · Genetic variance

1 Introduction

In evolutionary biology, plasticity and robustness are considered the basic characteristics of phenotypes; these characteristics have been widely discussed for decades. In general, phenotypes are shaped from genotypes as a result of developmental dynamics, under an

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¹Here, "development" refers to a dynamic process that shapes the phenotype and is not restricted to multicellular organisms. Developmental dynamics are also observed in unicellular organisms, for instance, gene (protein) expression dynamics by regulatory networks.

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environmental condition. Although these dynamics are determined by genes, they can be stochastic in nature, owing to some noise in the developmental process; further, these dynamics also depend on the environmental condition.

Plasticity refers to the changeability of the phenotype against the environmental change. Through developmental dynamics, the influence of the environment is amplified or reduced [1–6]. In other words, plasticity concerns how the developmental dynamics are affected by the environmental change.

Of course, the phenotype depends on the genotype. This changeability against genetic change is called evolvability and is related to the sensitivity of developmental dynamics against genetic change. In this sense, both plasticity and evolvability represent the responsiveness against external perturbations and, in simple terms, a sort of "susceptibility" in statistical physics.

Robustness, on the other hand, is defined as the ability to function against possible disturbances in the system [7–13]. Such disturbances have two distinct origins: non-genetic and genetic. The former concerns the robustness against the stochasticity that can arise during the developmental process, while the latter concerns the structural robustness of the phenotype, i.e., its rigidity against the genetic changes produced by mutations. If the variance of phenotype owing to disturbances such as noise in gene expression dynamics is smaller, then the robustness is increased. In this sense, the variance of phenotypic fluctuations serves as a measure of robustness, as has already been discussed [14].

Now, there exist certain basic questions associated with robustness and evolution [1–8]. Does robustness increase or decrease through evolution? If it increases, the rigidity of the phenotype against perturbations also increases. Consequently, the plasticity, as well as evolvability, may decrease with evolution. If that is the case, then the question that arises is: How can the plasticity needed to cope with a novel environment be sustained?

The decrease in plasticity and increase in robustness with evolution was actually observed in laboratory experiments under fixed environmental and fitness conditions and was also confirmed through numerical experiments. In a simulated evolution of catalytic reaction and gene regulatory networks under a given single fitness condition, the fluctuation decreases through the course of evolution [14, 15]. Such networks evolve to reduce the fluctuation by noise, for a sufficient noise level. Through this evolution, robustness against noise increases, leading to the decrease in phenotypic plasticity. As a system is more and more adapted to one environment, the phenotype fitted for it would lose the potentiality to adapt to a novel environmental condition.

In the present organisms, however, neither the evolutionary potential nor the phenotypic fluctuation vanishes. Even after evolution, the phenotype in question is not necessarily fixed at its optimal value, but its variance often remains rather large. There can be several sources for the deviation from the optimal state, which is neglected in the idealized numerical and laboratory experiments with a single fitness condition. One of the most typical factors for this deviation is environmental variation. With environmental change, the phenotype for producing the fittest state is not fixed but may vary over generations. Then, we are faced with the following questions: First, under environmental variation, can robustness and plasticity coexist through the course of evolution? Second, are the phenotypic fluctuations sustained, to maintain the adaptability to environmental changes? Third, how are the opposing features of robustness and adaptability to the new environment compromised? Finally, is there a noise level optimal for achieving both adaptability and robustness? We address these questions in the present paper.



2 Background: Isogenic Phenotypic Fluctuation and Evolution Speed

As for the fluctuation, there is an established relationship between the evolutionary speed and the variance of the fitness, namely, the so-called fundamental theorem of natural selection proposed by Fisher [19–21]; this theorem states that the evolution speed is proportional to V_g , the variance of fitness due to genetic variation. Besides the fitness itself, any phenotypes are generally changed by the genetic variation. Now, relationship between the evolution speed of each phenotype with its variance due to genetic change is established as Price equation, formulated through the covariance between a phenotype and fitness [22, 23]. Statistical-mechanical interpretation of Fisher's theorem in terms of the fluctuation-response relationship [24] or fluctuation theorem [25] was also discussed.

Besides the genetic change, there are sources of phenotypic fluctuations even among isogenic individuals and under a fixed environment. In fact, recent observations in cell biology show that there are relatively large fluctuations even among isogenic individuals. The protein abundances over isogenic individual cells exhibit a rather broad distribution, i.e., the concentration of molecules exhibits quite a large variance over isogenic cells [26–29]. This variance is due to stochastic gene expressions and to other external perturbations. Furthermore some of such phenotypic fluctuations are indeed tightly correlated with the fitness, and hence the fitness also shows (relatively large) isogenic fluctuations. For example, large fluctuations in the growth speed (or division time) are observed among isogenic bacterial cells [30, 31].

Hence, there are two sources of variations for the fitness or phenotype: genetic and epigenetic. The former concerns structural change in developmental dynamics with genetic change, and the latter concerns the noise during the gene expression dynamics. As mentioned, the relationship between the former variance with the evolution speed was established as Fisher's theorem (for fitness) and Price equation (for general phenotype). Then, is there any relationship between the latter variance with the evolution speed?

At a glance, the latter variance might not seem to be relevant to evolution, since this epigenetic change itself due to noise is not inherited to the offspring, in general. This is not the case. Here, it should be noted that the degree of variance itself is a nature of developmental dynamics to shape the phenotype, and thus depends on genotype, and can be inherited. Hence, there may exist some correlation between evolution speed and this isogenic phenotypic variance, which is denoted as V_{ip} here.²

Indeed, from evolution experiments for increasing the fluorescence in an inserted protein in bacteria [17] and also from numerical experiments for evolving reaction networks or gene regulatory networks [14, 15] to increase a given fitness, we have observed that

 $V_{ip} \propto \text{evolution speed},$

where the evolution speed is defined as the increase of the fitness. In the experiment, for each mutant bacteria, average fluorescence of isogenic cells was measured and that with highest average fluorescence was selected. Simultaneously, the variance of isogenic bacterial population was measured to obtain V_{ip} . The same procedure was applied to measure

²This is not standard terminology. Phenotypic variance by non-genetic origins is often termed as environmental variation V_e . Here, however, the source of the variance is not necessarily environmental change but, primarily, noise in the developmental process; hence, we use a different term. Note that the total phenotypic variance is $V_{ip} + V_g$ under a certain ideal condition [20, 21], if they are added independently.



the evolution speed and the fitness variance in numerical evolution to increase a given fitness. Interestingly, these experiments support the above relationship, at least approximately. Some 'phenomenological explanation' was proposed by assuming a Gaussian-type distribution P(x;a) of the fitness (phenotype) x as parameterized by a "genetic" parameter, a. and a linear change in the peak position of x against a [16–18]. It should be noted, however, that the argument based on the distribution P(x;a) is not a "derivation" but rather a phenomenological description. Indeed, the description by P(x;a) itself is an assumption: for example, whether a genotype is represented by a scalar parameter a is an assumption.

Now, considering the established Fisher's relationship, the above relationship suggests the proportionality between V_{ip} and V_g through an evolutionary course. Indeed, this relationship was confirmed from several simulations of models. Again, this relationship is not derived from established relationships in population genetics. Indeed, the proportionality between the two is not observed in the first few generations, but observed after robust evolution preserving a single peak in the fitness is progressed. Considering this observation, we previously discussed the relationship, by postulating evolutionary stability of the distribution over phenotype and genotype [14, 15, 35].

The relationship between V_{ip} and V_g also suggests a possible link between developmental robustness to noise and evolutionary robustness to genetic changes (mutation). For this link, we first note that the two types of variances V_g and V_{ip} lead to two kinds of robustness: rigidity of the fitness (phenotype) against genetic changes produced by mutations and robustness against the stochasticity that can arise in an environment or during the developmental process. When the fitness (phenotype) is robust to noise in developmental process, it is rather insensitive to the noise, and therefore, its distribution is sharper. Hence, the (inverse of the) variance of isogenic distribution, V_{ip} , gives an index for robustness to noise in developmental dynamics [14, 15]. On the other hand, if V_g is smaller, the phenotype is rather insensitive to genetic changes, implying higher genetic (or mutational) robustness. Hence the correlation between V_{ip} and V_g implies correlation between the two types of robustness. Indeed, previous simulations suggest that robustness to noise fosters robustness to mutation. Congruence between evolutionary and developmental robustness was also discussed by Ancel and Fontana for the evolution of RNA [5].

To close this section, a brief remark on the measurement of V_g is given here. Because the fitness (phenotype) distribution exists even in isogenic individuals, the variance of its distribution over a heterogenic population includes both the variance among isogenic individuals and that due to genetic variation. To distinguish between the two contributions, we first measure the average fitness (phenotype) over isogenic individuals and then compute the variance of this average over a heterogenic population. This variance will only be attributed to genetic heterogeneity. This variance is denoted by V_g .³

3 Our Standpoint and Model

3.1 Dynamical-Systems Approach to Evolution-Development Relationship

To discuss the evolution, the fitness landscape as a function of genotype is often adopted following Wright's picture [32]. Energy-like fitness function is assigned to a genotype

³According to the conventional terminology in population genetics, this variance is referred to as "additive" genetic variance; The term "additive" is included, to remove the variance due to sexual recombination. Here we do not discuss the influence of recombination and, thus, do not need to distinguish genetic variance from the additive one.



space, i.e., Fitness = f(Genotype). Here the evolution is discussed as a hill-climbing process through random change in genotype space and selection. Although this viewpoint has been important in evolutionary studies, another facet in evolution has to be also considered, to discuss the phenotypic plasticity and evolution-development relationship, that is genotype-phenotype mapping shaped by the developmental dynamics. Here we focus on this evolution-development relationship.

Note that the fitness is a function of (some) phenotypes (say a set of protein abundances). The phenotypes are determined by developmental dynamics (say gene expression dynamics), whose rule (e.g., set of equations or parameters therein) is governed by genes. Thus this evolution-development scheme is represented as follows:

- (i) Fitness = F(phenotype)
- (ii) Phenotype determined as a result of developmental dynamics
- (iii) Rule of developmental dynamics given by genotype

According to (ii) and (iii), genotype-phenotype mapping is shaped, which is not necessarily deterministic. As discussed, the phenotypes from isogenic population are distributed, since the dynamics (ii) involve stochasticity (in gene expression). Indeed, with this stochasticity, reached attractors by the dynamics are not necessarily identical, and accordingly the fitness may vary even among the isogenic individuals, which lead to the variance V_{ip} . If the dynamics to shape the phenotype is very stable, the variance V_{ip} is smaller. Further, the degree of the change in phenotype by the genetic change depends both on (ii) and (iii), and V_g depends on the sensitivity of the phenotype to the change in the rule of the dynamics. With the evolutionary process the genotype, i.e., the rule of the dynamics, changes, so that V_{ip} and V_g change with the evolution.

The developmental dynamics, in general, involve a large number of variables (e.g., proteins expressed by genes), and are complex. Accordingly, genotype-phenotype mapping is generally complex, and the mapping from genotype to the fitness is not simple, even if the function in (i) is simple. In several studies with adaptive fitness landscape, complexity in the fitness landscape has been taken into account, while the developmental dynamics (ii) are not. We take a simple fitness function (say, the number of expressed genes), but instead take complex developmental dynamics into account, to discuss the phenotypic plasticity in developmental and evolutionary dynamics.

If we are concerned only with the fitness landscape (i), we can introduce a single 'energy'-like function for it and formulate the adaptive evolution in terms of standard statistical mechanics. Here, however, we need to consider the dynamics to shape the phenotype (ii) [5, 13–15]. If we adopt statistical-mechanical formulation, we need two 'energy'-like functions, one for fitness and the other for Hamiltonian for the development dynamics, as is formulated by two-temperature statistical physics [33, 34].

So far, such study on evolution-development (so-called 'evo-devo') lacks mathematically sophisticated formulation as compared with the celebrated population genetics, and thus we sometimes have to resort to heuristic studies based on numerical evolution experiments, from which we extract 'generic' properties. We then provide some plausible arguments (or phenomenological theory), while mathematical or statistical-physical formulation has to be pursued in future.

3.2 Gene Expression Network Model

Following the argument in the lase section and to discuss the issue of plasticity and robustness in genotype-phenotype mapping, we adopted a simple model [14, 39, 40] for gene



expression dynamics with a sigmoid input-output behavior [36–38]; it should be noted, however, that several other simulations in the form of other biological networks will give essentially the same result. In this model, the dynamics of a given gene expression level, x_i , is described by the following:

$$dx_i/dt = \gamma \left\{ f\left(\sum_{j=1}^{M} J_{ij}x_j\right) - x_i \right\} + \sigma \eta_i(t), \tag{1}$$

where $J_{ij} = -1, 1, 0$. The noise term $\eta_i(t)$ is due to stochasticity in gene expression. For simplicity, it is taken to be Gaussian white noise given by $\langle \eta_i(t)\eta_j(t')\rangle = \delta_{i,j}\delta(t-t')$, while the (qualitative) results to be discussed below is independent of the choice.⁴ The amplitude of noise strength is given by σ , which determines stochasticity in gene expression. M denotes the total number of genes; and k, the number of target genes that determine fitness. Here, the function f(x) represents a threshold function for gene expression. Previously, we adopted the model (1) with

$$f(x) = \tanh(\beta x),\tag{2}$$

where the gene expression is "on" if x > 0 and "off" if x < 0.

To discuss the environmental condition, however, it is relevant to introduce an "input" term for expressing some genes. To make this input effective, we modify the function (3) as

$$f(x) = 1/(\exp(-\beta(x - \theta_i)) + 1) + \delta. \tag{3}$$

Here, x is positive and is scaled so that the maximal level expression is ~ 1 ; δ takes a small positive value corresponding to a spontaneous expression level. If the input sum from other genes $\sum_{j}^{M} J_{ij}x_{j}$ to gene i exceeds the threshold θ_{i} , the gene (protein) i is expressed so that $x_{i} \sim 1$, as f approaches a step function for sufficiently large β (> 1), which corresponds to the Hill coefficient in cell biology. Now, if all x_{i} 's are initially smaller than the threshold θ_{i} , they remains so if $\delta < \theta_{i}$. Hence, to generate some expression patterns, some input term is needed. Here, we introduce "input" genes $j = 1, \ldots, k_{inp}$, in which x_{j} is set at

$$x_j = I_j > 0 \quad (j = 1, 2, \dots, k_{inp}),$$
 (4)

where I_j is an external input to a set of "input genes." These inputs are needed to express genes; otherwise, the expression levels remain sub-threshold. In this case with Eq. (3), the gene is expressed if $x_i > \theta_i$, The initial condition is given by a state where none of the genes are expressed, i.e., $x_i \sim 0$.

Next, we set the fitness for evolution. The fitness, F, is determined by whether the expressions of the given "target" genes are expressed after a sufficient time. This fitness condition is given such that k target genes are "on" (expressed), i.e., $x_i > \theta_i$ for $M - k < i \le M$. Because the model includes a noise component, the fitness can fluctuate at each run, which leads to a distribution in F and x_i , even among individuals sharing the same gene regulatory network. For each network, we compute the average fitness \overline{F} over L runs as well as the variance. This variance over L identical individuals (having the identical networks J_{ij}) due to noise is V_{ip} , as it represents the fluctuation of the fitness over isogenic individuals (isogenic

⁴Indeed, multiplicative noise depending on x_i , as well as a stochastic reaction model simulated with the use of Gillespie algorithm gives a qualitatively same behavior [41]. Of course the magnitude of the phenotype variance as well as the threshold noise level for error catastrophe, to be discussed below, depends on the form of noise. However, relationship of such threshold noise level with V_g/V_{ip} , as well as the proportionality between V_{ip} and V_g does not depend on the specific form of noise.



phenotypic variance). V_g , to be discussed below, is the variance of \overline{F} over N heterogenic individuals (having different networks J_{ij}).

Here V_{ip} is not the variance over time in a single run, but the variance over runs for identical individuals. With developmental process by gene expression dynamics from a given initial condition, the gene expression pattern (x(j); j = 1, ..., M) reaches an attractor. Reached attractors can be different by each run, due to the stochasticity in expression dynamics during the transient time steps to reach the attractor. The fitness is computed on this attractor, which is also distributed as a result of noise. Once the attractor is reached, the fluctuation of the fitness around it is negligible, since the fitness is not given directly by x_i but defined through a threshold function of $x_i - \theta_i$. The variance is smaller as more runs result in the same attractor (or attractors of the same fitness) under noise. If gene expression dynamics with such global attraction to the same-fitness attractor are shaped through the evolution, the variance V_{ip} is smaller.

Now, at each generation, there are N individuals with slightly different gene regulatory networks $\{J_{ij}\}$, and their average fitness \overline{F} may differ by each. Among the networks, we select the ones with higher fitness values. From each of the selected networks, J_{ij} is "mutated," i.e., J_{ij} for a certain pair i, j selected randomly with a certain fraction switches to one of the values among $\pm 1, 0$. $N_s(< N)$ networks with higher \overline{F} values are selected, each of which produces N/N_s mutants. We repeat this selection-mutation process over generations. For example, we choose N = L = 500 or 700 for most simulations, and $N_s = N/4$; the conclusion, to be shown below, does not change as long as these values are sufficiently large. We use $\beta = 7$, $\gamma = 0.1$, M = 64, and k = 8 and initially choose J_{ij} randomly. The probability is taken to be 1/4 for $J_{ij} = \pm 1$ and 1/2 for 0 for most simulations below, but the results below are independent of this choice [40].

Now, we have two types of variances. Besides V_{ip} , V_g is defined as the variance of \overline{F} over the N individuals having different genes (gene regulatory networks). This shows the variance due to genetic change. As V_g is decreased, the fitness becomes insensitive to the genetic change, i.e., the robustness to mutation is increased. On the other hand, as V_{ip} is decreased, the robustness to noise is increased, since V_{ip} measures the variance due to noise in a developmental process. (It should be remarked that the absolute value of the fitness F is not important, since the model behavior is invariant against the transformation $F \rightarrow c \times F$. Accordingly the absolute values of V_{ip} and V_g are not important, but the ratio between the two or relative change of the variances over generations is important. On the other hand, each expression x(i) is already scaled so that the maximal expression is ~ 1 .)

4 Confirmation of Relationships in Phenotypic Fluctuations

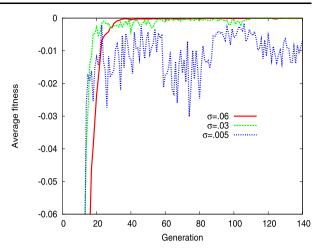
4.1 Proportionality Between the Phenotypic Variances by Noise and by Mutation

From the numerical simulation of the model, we have confirmed the following results.

- (1) There is a certain threshold noise level σ_c beyond which the evolution of robustness progresses, so that both V_g and V_{ip} decrease. Here, most of the individuals take the highest fitness value. In contrast, for a lower noise level $\sigma < \sigma_c$, mutants that have very low fitness values always remain. Several individuals take the highest fitness value, whereas the fraction of individuals with much lower fitness values does not decrease; hence, V_g remains large (see Figs. 1 and 2).
- (2) At around the threshold noise level, V_g approaches V_{ip} . For $\sigma < \sigma_c$, $V_g \sim V_{ip}$ holds, whereas for $\sigma > \sigma_c$, $V_{ip} > V_g$ is satisfied. For robust evolution to progress, this inequality is satisfied.



Fig. 1 Evolutionary time course of the average fitness $\langle \overline{F} \rangle$. The average of mean fitness $\langle \overline{F} \rangle$ over all N = 500 individuals that have different genotypes (i.e., networks J_{ij}) in each generation is plotted. The mean fitness of each genotype is computed from L = 500 runs. The plotted points are for different values of noise strength, $\sigma = 0.005, 0.03, 0.06,$ with different colors. For Figs. 1–3, we choose M = 64, k = 8, and $k_{inp} = 8$ with $I_i = 1$, while θ_i is distributed in [0.1,0.0.3] (Color figure online; open access)



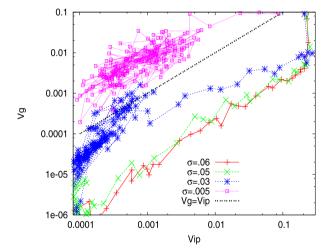


Fig. 2 Relationship between V_g and V_{ip} , the variances of the fitness. V_g is computed from $P(\overline{F})$, the distribution of mean fitness \overline{F} and V_{ip} is computed from the isogenic variance of the fitness over L=500 runs, for each genotype, and then these values are averaged over all existing individuals. (We also confirmed the overall relationship by using the variance for a gene regulatory network that gives the peak fitness value in $P(\overline{F})$.) The plotted points are over 140 generations. $\sigma=0.005$ (\square), 0.03 (*), 0.05 (×) and 0.06 (+). For $\sigma>\sigma_c\approx0.02$, both the variances decrease with generations, so that the *right-top* is the first generation and *left-bottom* is the 140th generation. After initial few generations both decrease roughly in proportion, while at $\sigma=0.03$, the deviation from the proportionality is larger possibly because the noise level is near the critical point to lose the robust evolutionary process. For $\sigma=0.005$, the decrease stops after 20 generations, and the variance values scatter for later generations (Color figure online; open access)

(3) When the noise is larger than this threshold, the two variances decrease, while $V_g \propto V_{ip}$ is maintained through the evolution course. Hence, the proportionality between the two variances is confirmed.

Why does the system not maintain the highest fitness state under a small phenotypic noise level with $\sigma < \sigma_c$? Indeed, the dynamics of the top-fitness networks that evolved under such low noise levels have distinguishable features from those that evolved under high



noise levels. It was found that for networks evolved under $\sigma > \sigma_c$, a large portion of the initial conditions reached attractors that give the highest fitness values, whereas for networks evolved under $\sigma < \sigma_c$, only a tiny fraction (i.e., in the vicinity of the all-off states) reached such attractors.

In other words, for $\sigma > \sigma_c$, the "developmental" dynamics that give a functional phenotype have a global, smooth attraction to the target. In fact, such types of developmental dynamics with global attraction are known to be ubiquitous in protein folding dynamics [42, 44], gene expression dynamics [43], and so forth. On the other hand, the landscape evolved at $\sigma < \sigma_c$ is rugged. Except for the vicinity of the given initial conditions, the expression dynamics do not reach the target pattern.

The observed proportionality between V_{ip} and V_g is not self-evident. Indeed, if a random network is considered for a gene regulatory network, such proportionality is not observed. In the present simulation, after a few generations of evolution, both the variances decrease, following proportionality, if $\sigma > \sigma_c$. Although there is no complete derivation for this relationship, it is suggested that this proportionality as well as the relationship $V_{ip} > V_g$ is a consequence of evolutionary stability to keep a single-peakedness in the distribution P(x = phenotype, a = genotype), under conditions of strong selective pressure and low mutation rate [15, 35].

4.2 Proportionality Between the Two Variances Across Genes

As mentioned above, the gene expression dynamics evolved under a sufficient level of noise have a characteristic property; the attractor providing the phenotype of the highest fitness has a large basin volume and is, hence, attracted globally by a developmental process under noise.

Note that the expression level x_j of non-target genes j could be either on or off, because there is no selection pressure directed at fixing their expression level. Still, each expression level x_j can have some correlation with the fitness in general. Hence it is also interesting to study the variance of each expression level and discuss its evolutionary changes.

Similar to the variances for the fitness, the phenotypic variance $V_{ip}(i)$ for each gene i in an isogenic population is defined on the basis of the variance of the expression of each gene i, with each $X_i = \operatorname{Sign}(x_i - \theta_i)$, in an isogenic population. Accordingly, the variance computed by using the distribution of $\overline{X_i}$ in this heterogenic population gives $V_g(i)$ for each gene i.

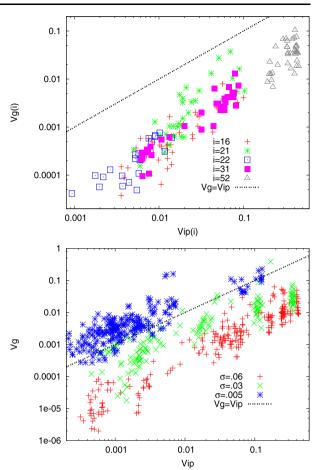
Following Price equation [22], the rate of change in each expression level between generations is expected to be correlated with $V_g(i)$, as it has direct or indirect influence to the fitness, through the gene expression dynamics (1). In contrast, here, we are interested in the variance of isogenic phenotypic fluctuations of each expression level $V_{ip}(i)$. Indeed, this variance decreases over generations for most genes. As the evolution progresses, these expressions also start to be rigidly fixed so that their variances decrease over most genes. In Fig. 3(top), we have plotted $V_g(i)$ versus $V_{ip}(i)$ over generations for several genes i. We can see that they decrease (roughly) in proportion, over generations. Furthermore, the proportion coefficient $V_g(i)/V_{ip}(i)$ seems to take close values across many genes.

In Fig. 3(bottom) we have plotted $(V_{ip}(i), V_g(i))$, across all expressed genes, after evolution reached the genotype with the highest fitness. As shown, the proportionality (or strong correlation) between $V_g(i)$ and $V_{ip}(i)$ holds across many (expressed) genes for a system

⁵Throughout the present paper, $V_g(i)$ and $V_{ip}(i)$ with (i) denote the variances of each phenotype, expression level i, while, V_g and V_{ip} denote the variances of the fitness.



Fig. 3 (Top) Plot of $(V_{ip}(i), V_g(i))$ for the genes i = 16, 21, 22, 31, 52 for the generations 5-40. Each of the variances decreases over generations, so that variance for each gene changes from right (upper) to left (lower) in the figure. As described in the text, $V_{in}(i)$ was computed as the variance of the distribution of $Sign(x_i)$ over L = 500 runs for an identical genotype, while $V_{g}(i)$ was computed as a variance of the distribution of $(\overline{\operatorname{Sign}(x_i)})$ over N = 500individuals, where $\overline{\text{Sign}(x_i)}$ refers to the mean over 500 runs. With generations, both the variances decrease roughly with proportion, with a trend of common proportion coefficient. (Bottom) Plot of $(V_{ip}(i), V_g(i))$ across all expressed genes i (i.e. for such genes i that $\overline{x(i)} > \theta_i$), after evolution is completed (for the generations 25-60), for three values of noise levels $\sigma = 0.005$ (*), 0.03 (×), and 0.06 (+) (Color figure online; open access)



through evolution. The ratio $\rho = V_g(i)/V_{ip}(i)$ increases with the decrease in σ , and at around σ_c , it approaches ~ 1 .

Although the origin of the proportionality has not yet been completely understood, a heuristic argument is proposed by using the distribution $P(x_i, a)$ for each gene expression x_i and by further assuming that the distribution maintains a single peak up to a common mutation rate (i.e., a common mutation rate for the error catastrophe [45] threshold) over genes [40]. The latter hypothesis may be justified as a highly robust system: In such a system with increased error-threshold mutation rates, once the error occurs, it propagates and percolates to many genes, so that a common error threshold value is expected. Note that there are some preliminary experimental supports on this proportionality of the two variances over genes or phenotypic traits [18, 46–48], although future studies are required for the confirmation.

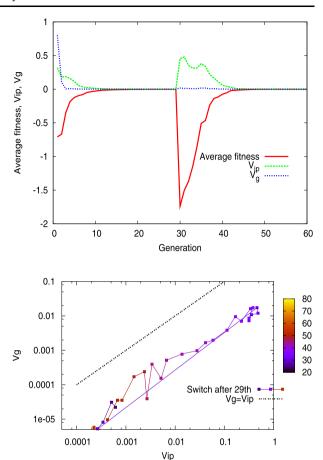
5 Phenotypic Evolution under Environmental Variation

5.1 Restoration of Plasticity with the Increase in Fluctuations by Environmental Change

So far, through the selection process under a fixed fitness/environmental condition, both the fluctuations and the rate of evolution decrease. The system loses plasticity against the



Fig. 4 The time course in the fitness and the variance of the fitness over generations. First, the evolution under an environment $I_i = 1$ for $1 \le j \le 4$, and $I_i = 0$ for $5 \le j \le k_{inp} = 8$ is simulated to progress up to 30 generations. After the 29th generation, we switch the fitness condition to $I_i = 0$ for $1 \le j \le 4$, and $I_i = 1$ for 5 < i < 8, which is maintained at later generations. M = 64, L = N = 700, and θ_i is distributed uniformly in [0.1, 0.3]. The switch initially causes a decrease in the fitness, but after a few dozens of generations, almost all networks evolve to adapt to the new fitness condition. The noise level is set at $\sigma = 0.06 > \sigma_c$. Top: The time course of the average fitness and the variance V_{ip} throughout the evolution. Bottom: The plot of the variances of the fitness, V_g versus V_{ip} for each generation after the switch of the environmental condition. The generations (up to 60) are represented by different colors. Both the variances increase in correlation, after the switch, and later, they decrease in proportion, to adapt to the new condition (Color figure online; open access)



change caused by external noise or external mutation. Nevertheless, in nature, neither the fluctuations nor the evolution potential vanish. How are phenotypic plasticity, fluctuations, and evolutionary potential sustained in nature?

One possible origin for the preservation of plasticity may be environmental fluctuation [51], as has also been studied in terms of statistical physics [52–54]. The plasticity of a biological system is relevant for coping with the environmental change that may alter phenotypic dynamics in order to achieve a higher fitness. In the present modeling, there can be two ways to include such an environmental change.

One is a direct method, in which an input term given in Eq. (4) is changed with each generation, while the fitness condition is maintained. The other method is indirect, in which environmental change is introduced as the change in the fitness condition, while preserving the dynamics itself. Here, we discuss the simulation result of the former procedure first and will consider the result from the other procedure later in Sect. 5.3.

To change the environmental condition, we varied the input pattern at some generation. Here, we change the input pattern I_j $(1 \le j \le k_{inp})$ from the generation at which the system had already adapted to the environment and decreased the phenotypic variances. An example is plotted in Fig. 4. Here, I_j initially takes $I_j = 1$ for $1 \le j \le k_{inp}/2$ and $I_j = 0$ for $k_{inp}/2 < 1$



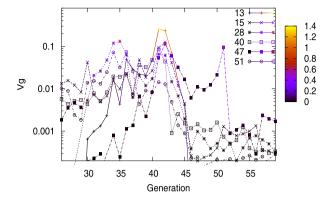


Fig. 5 Change in the variances $V_{ip}(i)$ and $V_g(i)/V_{ip}(i)$ at after the switch in environmental condition after the 29th generation, as given in Fig. 4. The variance $V_{ip}(i)$ is plotted up to generation 60, where the switch is given at the 30th generation. Plotted for the genes i = 13, 15, 28, 40, 47, 51. For the genes 13, 28, and 47, $V_g(i)$ before the switch after 29th generation is smaller than 10^{-4} . The color represents $V_g(i)/V_{ip}(i)$, as shown in the *right bar* (Color figure online; open access)

 $j \le k_{inp}$, before switching to $1 - I_j$ after the 29th generation. By switching the environment, the fitness first decreases and later adapts to the new environment (Fig. 4(top)).

To determine the evolution of phenotypic plasticity, we computed the variances of the fitness, V_{ip} and V_g , over successive generations (see Fig. 4(bottom)). After the switch of the fitness condition, both V_{ip} and V_g first increase to a relatively high level and continuously increasing further over a few generations. At later generations, both V_{ip} and V_g again decrease, maintaining the proportionality. The proportionality law between the genetic and epigenetic variances is satisfied with both increase and decrease in plasticity through the evolution.

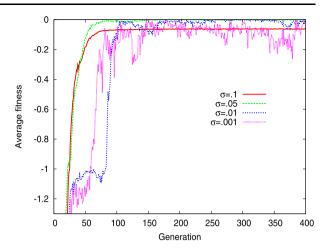
With the increase in V_{ip} , the fitness is more variable with noise, which also leads to higher changeability against environmental conditions. The gene expression dynamics regain plasticity, which allows for the switch of the target genes after further generations. Then, with the increase in V_g , the changeability against genetic change increases, thus increasing the evolvability.

Next, we explore the change in the variances of the expression of each gene. As shown in Fig. 5, both variances $V_{ip}(i)$ and $V_g(i)$ increase, as a result of environmental change. Expressions of all genes are more variable against noise and mutation. Most gene expressions gain higher plasticity by increasing the variance in their expression. Besides the increase in the variances, the ratio $\rho_i = V_g(i)/V_{ip}(i)$ also increase at some generation, to approach $V_{ip} \sim V_g$ (see the color change in Fig. 5, where the red color shows higher ratio ρ_i). This increase in $V_g(i)/V_{ip}(i)$ suggests that the system is closer to the error catastrophe point, where the stability condition in the distribution function $P(x_i = \text{phenotype}, a = \text{genotype})$ is lost. This leads to the increase in plasticity, with which the adaptation to a novel condition is achieved. Once the fitted phenotypes are generated by this adaptation, the variances decrease, with restoring the proportionality between $V_g(i)$ and $V_{ip}(i)$.

To sum up, adaptation to novel environment is characterized by the phenotypic variances as follows. With the increase in $V_{ip}(i)$, the sensitivity of the phenotype to noise and environmental change is increased, thereby increasing plasticity. With the increase in $V_g(i)$, changeability of the phenotype by mutation is increased, thereby accelerating evolutionary change of each expression level. With the increase in $V_g(i)/V_{ip}(i)$, the sensitivity to genetic change is further increased, thus facilitating the evolution. With these trends—the increase



Fig. 6 The average of the mean fitness $\langle \overline{F} \rangle$ plotted for each generation, under continual environmental variation, as described in the text. M = 64, k = 8, and $k_{inp} = 4$, while I_i are changed randomly within [0, 0.8]. The average of the mean fitness, \overline{F} , of each individual (over L = 100 runs) is computed over the total population (N = 100) at each generation. The noise level, σ , is 0.1 (red), $0.05 \ (\sim \sigma_c; green), 0.01 \ (blue),$ and 0.001 (pink). At around $\sigma \sim 0.05$, the average fitness reaches the highest level (Color figure online; open access)



in $V_{ip}(i)$, $V_g(i)$, $\rho_i = V_g(i)/V_{ip}(i)$, the adaptation to a novel environment is fostered. With this increase in plasticity, gene expression dynamics for adapting to a novel condition are explored. Once these fitted dynamics are shaped, the variances decrease, leading to a decrease in plasticity and increase in robustness.

5.2 Optimal Noise Level for Varying Environment

Now, we consider evolution under continual environmental variation. To discuss a long-term environmental change, we switch the environmental condition by generation. To be specific, we change randomly I_i within [0, 1] per generation.

When environmental changes are continuously repeated, the decrease and increase in the variances V_{ip} and V_g are repeated. Note that it takes more generations to adapt to a new fitness condition, if the phenotypic variances have been smaller. In our model, if the noise level in development is larger, the phenotypic variances already take a small value during the adaptation to satisfy the fitness condition. Hence, in this case, it takes more generations to adapt to a new fitness condition. On the other hand, if the noise level σ is smaller than $\sigma_c \sim 0.05$, robust evolution does not progress. Hence, for continuous environmental change, there will be an optimal noise level to both adapt sufficiently fast to a new environment and evolve the robustness of fitness for each environmental condition. In Fig. 6, we have plotted the time course of the average fitness in population. If the noise level is large, the system cannot follow the frequent environmental change and the average fitness cannot increase sufficiently. On the other hand, if the noise level is small, the fitness increases; however, if it is too small, the fitness of some individuals remains rather low. Indeed, there is an optimal noise level at which the average fitness is maximal, as shown in Fig. 7, where the average fitness over generations is plotted against the noise level σ . This optimal noise level is close to the value of the robustness transition σ_c .

Next, we plotted the variances V_{ip} and V_g over generations (see Fig. 8). When $\sigma < \sigma_c$, then $V_g > V_{ip}$ and both the variances remain rather large, demonstrating that robustness has not evolved at all. For $\sigma \gg \sigma_c$, $V_g < V_{ip}$ and the variances remain small. The robustness has evolved, but the system cannot adapt to an environmental change as the variances have become too small. In contrast, for $\sigma \sim \sigma_c$, V_{ip} and V_g vary between low and high values over generations, maintaining the proportionality between the two variances, with V_{ip} slightly larger than V_g .



Fig. 7 The average fitness and the variances, V_{ip} and V_g , through the course of the evolution under environmental variation as in Fig. 6. Each value is further averaged over 200-700 generations. The overall temporal averages are plotted against the noise level σ . Instead of the fitness itself, its sign inversion $-\langle \overline{F} \rangle$ is plotted. At around $\sigma \sim 0.05$, the average fitness takes a maximal value, and at σ slightly below it, V_g approaches V_{in} (Color figure online; open access)

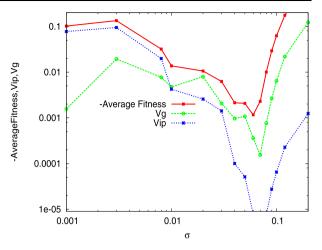
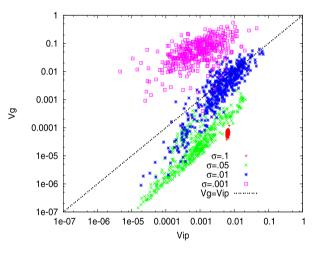


Fig. 8 The variances of the fitness (V_{ip}, V_g) through the course of the evolution under environmental variation as in Fig. 6. Each point is a result of one generation, and the plot is taken over 200–700 generations. The noise level σ is 0.1 (red), 0.005 ($\sim \sigma_c$; green), 0.01 (blue), and 0.001 (pink) (Color figure online; open access)

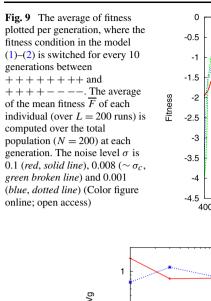


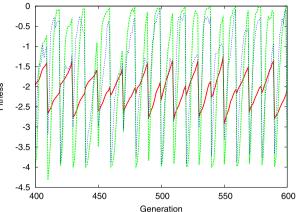
5.3 Adaptation Against Switches of the Fitness Condition

For confirmation of the result in the last section, we also carried out numerical experiments by adopting a separate procedure, i.e., by switching the fitness condition. As a specific example, we carried out the simulation by taking the model (1)–(2), without including input terms (4). After the gene expression dynamics are evolved with the fitness to prefer $x_i > 0$ for the target genes i = 1, 2, ..., k (= 8), then at a certain generation, we change the fitness condition so that the genes i = 1, 2, ..., k/2 are on and the rest are off (i.e., the fittest gene expression pattern is + + + + - - -, instead of + + + + + + +: In this model, the gene is off if $x_i < 0$). Here, we switch after sufficiently large generations when the fittest networks are evolved (i.e., with $x_i > 0$ for target genes).

In this case as well, the variances of the fitness, V_{ip} and V_g , first increase in proportion to adapt to a new fitness condition. Later, they decrease in proportion to gain robustness to noise and mutation. Next, we again computed $V_{ip}(i)$ and $V_g(i)$ successively through the







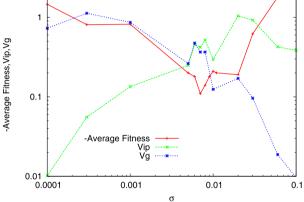


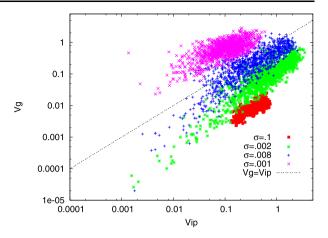
Fig. 10 The temporal average of the average fitness and the variances V_{ip} and V_g in the evolution, with the change in the fitness condition for every 10 generations as in Fig. 9. The overall temporal averages over population and over generations are plotted against the noise level σ . Instead of the fitness itself, its sign inversion $-\langle \overline{F} \rangle$ is plotted. The temporal average is taken over 500–1000 generations. At around $\sigma \sim 0.008$, the average fitness takes a maximal value, and at σ slightly below it, V_g exceeds V_{ip} (Color figure online; open access)

course of the evolution. Immediately after the switch in the fitness, the variances $V_{ip}(i)$ and $V_g(i)$ increase as well as the ratio $V_g(i)/V_{ip}(i)$. These variances in gene expression levels facilitate plasticity, and adaptation to a new environment.

When environmental changes are continuously repeated, the decrease and increase processes of the variances V_{ip} and V_g are repeated. In Fig. 9, we have plotted the time course of the average fitness in population, when the fitness condition is switched after every 10 generations. In this case again, when the noise level is near σ_c , fast adaptation to a new environment and the increase of robustness at later generations are compatible. Dependence of the average fitness on the noise level is shown in Fig. 10, which also shows an optimal noise level near the robustness transition σ_c (which is lower than the case in Sect. 5.2). Indeed, below this noise level, V_g exceeds V_{ip} and the robustness to mutation is lost. The plot of the variances V_{ip} and V_g over generations in Fig. 11 shows that at $\sigma \sim \sigma_c$, they go up and down, maintaining an approximate proportionality between the two, with V_{ip} slightly less



Fig. 11 Variances of the fitness, (V_{ip}, V_g) , are plotted over generations through the course of the evolution with fitness change after every 10 generations, as described in Fig. 9. Each point is a result of one generation, and the plot is taken over 500-1000 generations. The noise level σ is $0.1 \ (red), 0.02 \ (green), 0.008$ ($\sim \sigma_c$; blue), and $0.001 \ (pink)$ (Color figure online; open access)



than V_g . Overall, the behavior here under the fitness switch agrees well with that under the environmental variation in Sect. 5.2.

6 Summary and Discussion

In the present paper, we have studied biological robustness and plasticity, in terms of phenotypic fluctuations. The results are summarized into three points.

(1) Confirmation of earlier results on the phenotypic variances due to noise and due to genetic variation: The two variances, V_{ip} (due to noise) and V_g (due to mutation) decrease in proportion through the course of robust evolution under a fixed environmental condition. After the evolution to achieve robustness to noise and mutation is completed, $V_{ip}(i)$ and $V_g(i)$ are proportional across expressions of most genes (or different phenotypic traits). In short,

plasticity (changeability) of phenotype $\propto V_{ip} \propto V_g \propto$ evolution speed

through the course of the evolution and across phenotypic traits (expressions of genes).

- (2) Increase in the phenotypic variances and recovery of plasticity: When robustness is increased under a given environmental condition, the system loses plasticity to adapt to a novel environment. When the environmental condition is switched, both the phenotypic variances due to noise and due to genetic variation increase to gain plasticity and thus to adapt to the novel environment. This increase is observed both for the variance of fitness and of each gene expression level.
- (3) Optimal noise level to achieve both robustness and plasticity under continuous environmental change. There is generally a threshold level of noise in gene expression (or in developmental dynamics), beyond which robustness to noise and mutation evolves. If the noise level is larger, however, the system loses plasticity to adapt to environmental changes, whereas if it is much lower, a robust, fitted phenotype is not generated. At around the noise level for the "robustness transition," the system can adapt to environmental changes and achieve a higher fitness. There, the phenotypic variances V_{ip} and V_g increase and decrease, roughly maintaining the proportionality between the two, while sustaining $V_{ip} \gtrsim V_g$.

From a statistical-physicist viewpoint, the relationship between responsiveness and fluctuation is expected as a proper extension of the fluctuation-response relationship. In this



context, it is rather natural that the response ratio to environmental change, i.e., plasticity, is proportional to V_{ip} , the isogenic phenotypic fluctuation. On the other hand, as Fisher stated, the variance due to genetic change, V_g , is proportional to evolution speed, i.e., response of the fitness against mutation and selection. Interestingly, our simulations and evolutionary stability argument suggest the proportionality between V_{ip} and V_g . This implies the proportionality between environmental plasticity and evolvability.

In fact, Waddington [49, 50] coined the term genetic assimilation, in which phenotypic changes induced by environmental changes foster later genetic evolution. Since then, positive roles of phenotypic plasticity in evolution have been extensively discussed [3–5]. Our study gives a quantitative representation of such relationship in terms of fluctuations.

Existence of the threshold noise level below which robustness is lost is reminiscent of a glass transition in physics: For a higher noise level, dynamical systems for global attraction to a functional phenotype are generated through evolution, whereas for a lower noise level, the dynamics follow motion in a rugged landscape, where perturbation to it leads to a failure in the shaping of the functional phenotype. In fact, Sakata et al. considered a spin-glass model whose interaction matrix evolves to generate a high-fitness thermodynamic state. The transition to lose robustness was found by lowering the temperature. Interestingly, this transition is identified as the replica symmetry breaking transition from a replica symmetric phase [33, 34].

Under environmental fluctuation, the evolution to achieve both plasticity to a new environment and robustness of a fitted state is possible near this transition, for losing the robustness. In other words, one may regard that a biological systems favors the "edge-of-glass" state.

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