

RECEIVED: September 23, 2015 ACCEPTED: November 30, 2015 PUBLISHED: January 8, 2016

Fermionic extensions of the Standard Model in light of the Higgs couplings

Nicolas Bizot and Michele Frigerio

Laboratoire Charles Coulomb (L2C), UMR 5221 CNRS-Université de Montpellier, Place Eugéne Bataillon, F-34095 Montpellier, France

E-mail: nicolas.bizot@umontpellier.fr, michele.frigerio@umontpellier.fr

Abstract: As the Higgs boson properties settle, the constraints on the Standard Model extensions tighten. We consider all possible new fermions that can couple to the Higgs, inspecting sets of up to four chiral multiplets. We confront them with direct collider searches, electroweak precision tests, and current knowledge of the Higgs couplings. The focus is on scenarios that may depart from the decoupling limit of very large masses and vanishing mixing, as they offer the best prospects for detection. We identify exotic chiral families that may receive a mass from the Higgs only, still in agreement with the $h\gamma\gamma$ signal strength. A mixing θ between the Standard Model and non-chiral fermions induces order θ^2 deviations in the Higgs couplings. The mixing can be as large as $\theta \sim 0.5$ in case of custodial protection of the Z couplings or accidental cancellation in the oblique parameters. We also notice some intriguing effects for much smaller values of θ , especially in the lepton sector. Our survey includes a number of unconventional pairs of vector-like and Majorana fermions coupled through the Higgs, that may induce order one corrections to the Higgs radiative couplings. We single out the regions of parameters where $h\gamma\gamma$ and hqq are unaffected, while the $h\gamma Z$ signal strength is significantly modified, turning a few times larger than in the Standard Model in two cases. The second run of the LHC will effectively test most of these scenarios.

Keywords: Higgs Physics, Beyond Standard Model

ARXIV EPRINT: 1508.01645

Contents

1	Inti	roduction	2				
2	Minimal fermionic extensions of the SM						
	2.1	One multiplet	6				
	2.2	Two multiplets	6				
	2.3	Three multiplets	7				
	2.4	Four multiplets	10				
	2.5	Larger sets of new fermions	11				
3	Phe	enomenology of new chiral fermions	12				
4	Phenomenology of non-chiral leptons						
	4.1	Majorana leptons	16				
	4.2	One vector-like lepton	21				
	4.3	Two vector-like leptons (including τ compositeness)	24				
	4.4	Vector-like plus Majorana leptons (including higgsinos plus gauginos)	30				
5	Phenomenology of non-chiral quarks						
	5.1	One vector-like quark	35				
	5.2	Two vector-like quarks (including b and t compositeness)	43				
	5.3	Vector-like plus Majorana quarks	49				
6	Cor	nclusions	50				
\mathbf{A}	Ele	ctroweak precision tests in presence of new fermions	53				
	A.1	Electroweak gauge boson couplings	54				
	A.2	Constraints from S and T	55				
	A.3	Constraints from $Zf\overline{f}$	58				
В	Hig	gs boson couplings in presence of new fermions	60				
	B.1 Tree-level Higgs couplings						
	B.2	B.2 Loop-induced Higgs couplings					
		B.2.1 Higgs coupling to two gluons	63				
		B.2.2 Higgs coupling to two photons	65				
		B.2.3 Higgs coupling to a Z boson and a photon	66				
	B.3	Experimental constraints on the Higgs couplings	69				

1 Introduction

When the Large Hadron Collider (LHC) began its data taking, possible extensions of the Standard Model (SM) at the TeV scale were already severely constrained: electroweak (EW) precision measurements accurately confirmed the structure of the gauge sector [1–3], a number of flavour violating observables showed no significant deviation from the SM predictions [4, 5], all direct searches of non-standard particles at LEP and Tevatron gave null results [2, 6, 7]. After the first run of the LHC, the lower bounds on the masses of new particles increased substantially [8, 9]. The crucial discovery of the Higgs boson [10, 11] and the measurement of some of its properties [12–14] supported the minimal realisation of electroweak symmetry breaking (EWSB), as predicted by the SM. Thus, the room for SM extensions further compressed.

In this phase, it is essential to reassess the possibilities still open for non-standard physics close to the TeV scale. In this paper, we focus on new spin-1/2 degrees of freedom. In particular, we will assume that the scalar and gauge sector is the SM one, with one standard Higgs doublet. In general, additional dynamics in the EWSB sector may well be present, including corrections to the Higgs boson couplings to the electroweak gauge bosons, as well as additional scalar or vector states: here we do not consider these possibilities, assuming that such dynamics takes place at sufficiently higher scale, or it is sufficiently weakly coupled to the SM. In other words, we will study effective field theories containing the SM degrees of freedom plus additional fermions only, being agnostic on the ultraviolet completion at higher energy.

When wondering what fundamental fermions exist in Nature, one may notice that the fermion field content of the SM appears whimsical in some respects. Each fermion family is a set of five chiral multiplets, l_L , e_R , q_L , u_R and d_R , whose gauge quantum numbers are not explained within the SM, with the remarkable property to be anomaly-free. The number of families, three, is unexplained too. All SM fermions are massless before EWSB and, when the Higgs develops a vacuum expectation value (vev), they acquire a mass proportional to their Yukawa coupling to the Higgs doublet. The structure of the Yukawa coupling matrices is not determined by the SM symmetries either. Of course, some of these issues may find a convincing interpretation in very high energy extensions of the SM, such as grand unification or flavour theories, but in this paper we will take a phenomenological point of view and centre on the TeV scale only.

Additional chiral fermions that are massless before EWSB are definitely worth to look for, as their mass is bound to the TeV scale; the classical example of a chiral fourth family, with the same field content as the SM ones, was ruled out long ago [15], but we will show that more exotic possibilities exist. On the other hand, chiral fermions that transform in a real representation or form vector-like pairs, with respect to the SM gauge group, can acquire a mass before EWSB. While in general such mass can be much larger than the EW scale, in a number of well-motivated extensions of the SM there are new, fermionic degrees of freedom close to the TeV scale. Here are some familiar examples:

• Non-zero neutrino masses may be generated through the mixing with heavier fermions, typically sterile neutrinos. The latter may have a mass close to the EW scale. How-

ever very different scenarios are possible, spanning from the eV scale to the grand unification scale.

- The dark matter energy density may be carried by new, weakly interacting fermions. If thermally produced, their mass should be close to the EW scale.
- If the quantum stability of the EW scale is guaranteed by supersymmetry broken at the TeV scale, the SM gauge bosons shall be accompanied by gauginos, and the scalar bosons by higgsinos.
- If the weak scale is stabilised by dimensional transmutation, via a new strongly-coupled sector that condenses at the TeV scale, a number of composite spin-1/2 resonances may be present in the low energy spectrum. For example, in the scenario of partial compositeness [16, 17], the SM chiral fermions, or at least the heaviest ones, are accompanied by vector-like composite partners with the same gauge quantum numbers.

Given the diversity of phenomenological and theoretical motivations, and the wide-ranging discovery reach of the LHC, in section 2 we undergo a classification of the fermionic extensions of the SM, as general as possible. Theoretical consistency requires the absence of gauge anomalies. In addition, all new fermions should acquire a large mass to comply with null direct searches. As we want to explore the new constraints that materialised after the Higgs discovery, we limit ourselves to those fermions that interact with the Higgs doublet via Yukawa couplings. We provide the full list of SM extensions with these properties, formed by up to four new chiral multiplets, and comment on larger sets of new fermions. We note in passing that there may be alternative phenomenological motivations to study fermions that do not interact with the Higgs, for example to avoid the flavour problem altogether, or to look for generic dark matter candidates; some complementary classifications along this line can be found e.g. in refs. [18–20].

The rest of the paper is dedicated to the phenomenology of the fermionic SM extensions, in particular to identify the regions of parameters that survive to three broad classes of constraints: (i) EW precision tests; (ii) collider direct searches; (iii) Higgs boson couplings. Our purpose is to provide a comprehensive, comparative description of all possible sets of fermions, that are presently allowed and may have an observable effect at the second run of the LHC. Such analysis has several limitations that one should keep in mind:

- We compute only the leading order corrections to the Higgs and gauge boson couplings
 due to the extra fermions, and we roughly extract the collider bounds on their masses
 and couplings from the available experimental papers. A precision analysis would
 require a dedicated study for each given set of new fermions (and it is already available
 for several specific cases).
- We assume that the new fermions do not mix with the first and second SM families, in order to avoid the strong constraints coming from flavour observables (tree-level flavour changing neutral currents are absent). Indeed, the mixing with the third

family is sufficient to characterise the corrections to the EW and Higgs observables, that are our main subject of interest. In addition, the Higgs couplings to the light families are presently unconstrained. Note that the mixing with the third family can still induce flavour violating processes at one loop, especially in *B*-meson decays or oscillations, when the top or bottom quarks mix with new fermions. However, the corrections are suppressed with respect to the SM by the masses of the new fermions and their mixing with the SM ones. The constraints are typically mild, but in some cases may be complementary to those discussed in this paper, see e.g. refs. [21–23].

- The new fermions are not supposed to form an ultraviolet complete theory, consistent up to a scale much larger than the TeV. Therefore, we do not impose constraints coming from the coupling evolution at high energies, such as vacuum stability, absence of Landau poles, or gauge unification. We have no pretension to determine the full theory.
- We do not restrict the possible SM extensions using cosmological considerations, that rely in most cases on specific assumptions on the early Universe evolution. For example, we do not impose bounds on the relic abundance of the new fermions, based on the assumption of an initial thermal abundance.

As a matter of fact, these points can be addressed only in a model-dependent manner. In specific, well-motivated scenarios, it would be worth to perform more precise computations and include additional constraints from the other sectors of the theory.

In section 3 we discuss purely chiral sets of fermions, that is, fermions that are massless before EWSB. Fermions with an EW-invariant mass, that is, either a Majorana or a vector-like mass term, are discussed in section 4, if they are colourless, and in section 5, if they are coloured. With a little abuse of terminology, we will call 'leptons' all the colourless fermions, even when they do not mix with the SM leptons, and 'quarks' all the coloured ones, even when they do not transform in the fundamental representation of the colour group $SU(3)_c$. Finally, in section 6 we recapitulate the most interesting results of our analysis.

For each sets of new fermions, we were confronted with the need to compute EW precision observables and Higgs couplings. Thus, we took the opportunity to collect all the relevant formulas in the appendices, that generalise well-known results to the case of a generic fermionic extension of the SM. In appendix A, we present the fermion-gauge boson couplings, the corrections to the S and T parameters, as well as to the $Zf\bar{f}$ vertex. In appendix B, we discuss the fermion-Higgs boson couplings, both the tree-level and the loop-induced ones, and we briefly summarise the present experimental constraints on the Higgs couplings.

2 Minimal fermionic extensions of the SM

Let us consider the extension of the SM by additional fermions, classified according to their transformation under the SM gauge group $SU(3)_c \times SU(2)_w \times U(1)_Y$, whose irreducible representations can be denoted by (R_c, R_w, Y) . The SM extension is defined by the most general renormalizable Lagrangian involving the SM fields and a given set of extra chiral fermion multiplets.

We wish each set of new fermions (i) to be phenomenologically viable, (ii) to be theoretically self-consistent, and (iii) to modify the Higgs couplings. This leads to the following series of requirements:

- (i) No massless fermions after EWSB, except for the three SM neutrinos and gauge singlets. Indeed, massless fermions are phenomenologically forbidden, unless they have no colour $(R_c = 1)$, no electric charge $(Q = T_3 + Y = 0)$, and no coupling to the Z-boson $(T_3 \tan^2 \theta_w Y = 0)$. The latter two conditions imply $Y = T_3 = 0$. These conditions would allow for a massless neutral component in the chiral multiplet $(1, R_w, 0)$ with R_w odd, however the gauge symmetries permit a Majorana mass term for such a multiplet.
- (ii) No SM gauge anomalies. The fermionic extensions of the SM under consideration are intended as effective theories valid up to the multi-TeV scale, therefore they should cancel all SM anomalies self-consistently. (Extra fermions much heavier than the EW scale play no role in the anomaly cancellation, since they form vector-like pairs with respect to the SM gauge group.) Since the SM field content is anomaly-free by itself, the anomaly-cancellation conditions must be imposed on the set of new fermions only.

As we require the absence of massless coloured states, the new fermions form a (reducible) real representation of $SU(3)_c$, therefore the $SU(3)_c$ -cubic anomaly is automatically vanishing. Denoting the new fermion representations by (R_{ci}, R_{wi}, Y_i) , for i = 1, ..., n, the remaining anomaly-cancellation conditions read

$$SU(3)_{c} - SU(3)_{c} - U(1)_{Y} : \sum_{i=1}^{n} N_{wi}C(R_{ci})Y_{i} = 0,$$

$$SU(2)_{w} - SU(2)_{w} - U(1)_{Y} : \sum_{i=1}^{n} N_{ci}C(R_{wi})Y_{i} = 0,$$

$$U(1)_{Y} - U(1)_{Y} - U(1)_{Y} : \sum_{i=1}^{n} N_{ci}N_{wi}Y_{i}^{3} = 0,$$

$$grav - grav - U(1)_{Y} : \sum_{i=1}^{n} N_{ci}N_{wi}Y_{i} = 0,$$

$$(2.1)$$

where $N_w \equiv \dim(R_w)$, $N_c \equiv \dim(R_c)$ — this notation is redundant for SU(2) but not for SU(3) — and the index C(R) of a given representation is defined by $\operatorname{Tr}(T_R^a T_R^b) = C(R)\delta_{ab}$, with the index of the fundamental conventionally normalised to C(N) = 1/2 for SU(N). In the case of SU(2) one has $C(R_w) = N_w(N_w^2 - 1)/12$. In the case of SU(3) each representation R_c is characterised by two integer Dynkin labels (a_1, a_2) with $a_i \geq 0$, and one has $N_c = (1 + a_1)(1 + a_2)(1 + a_1/2 + a_2/2)$ and $C(R_c) = N_c(a_1^2 + 3a_1 + a_1a_2 + 3a_2 + a_2^2)/24$.

Additionally, the $SU(2)_w$ gauge group has a global anomaly, that cancels only when the sum $\sum_{i=1}^n N_{ci}C(R_{wi})$ is an integer number [24]. Note that $C(R_w)$ is half-integer for $N_w = 2 + 4n$, $n = 0, 1, 2, \ldots$, and integer in all other cases. As for the previous anomalies, this condition must be satisfied by the fermions below the multi-TeV scale. (Heavier fermions, decoupled from the EW scale, necessarily give an integer contribution to the sum: only an even number of multiplets with N_w even can acquire a vector-like mass.)

(iii) Non-zero corrections to the Higgs boson couplings. This corresponds to consider only new fermions with a Yukawa coupling to the SM Higgs doublet. More precisely, any subset of new fermions that satisfies the requirements (i) and (ii) by itself — any subset with no massless states nor anomalies — should have a non-zero Yukawa coupling to the Higgs. Otherwise, such subset would interact with the SM only through gauge interactions; strictly speaking, it can still affect the Higgs boson couplings at the two-loop level, but here we neglect such small effects.

We stress that the three requirements above are independent, in the sense that none is automatically implied by the others. In particular: vector-like fermions are automatically massive and anomaly-free, but they may not couple to the Higgs doublet; chiral fermions that have non-zero masses, such as an extra family of quarks, can be anomalous; an anomaly-free set of fermions, such as zero-hypercharge fermions, may contain some massless components.

In the following we classify the sets of n chiral fermions that satisfy the requirements (i), (ii) and (iii), for n = 1, 2, 3, 4, and we briefly comment on larger sets. For convenience, we will mark with the symbol \square each viable set that is identified.

2.1 One multiplet

If we add to the SM only one new chiral fermion $\psi \sim (R_c, R_w, Y)$, the only possibility to avoid massless states with non-zero SM gauge charges is the presence of a Majorana mass term $m_{\psi}\psi\psi$, that requires $R_c=\overline{R_c}$, Y=0 and N_w odd. Such multiplet is anomaly-free. The additional requirement to couple to the Higgs doublet, $H\sim (1,2,1/2)$, restricts the possibilities to $R_c=1$ and $R_w=1$ or 3, that is,

$$\square$$
 $N \sim (1, 1, 0)$ or $\Sigma \sim (1, 3, 0)$. (2.2)

In both cases a Yukawa coupling is allowed among the new fermion, H and the SM lepton doublet $l \sim (1, 2, -1/2)$.

Since N (Σ) forms by itself a self-consistent extension of the SM that modifies the Higgs couplings, n replicas of N (and/or Σ) also define a set of new fermions satisfying all our criteria. We will analyse their phenomenology in section 4.1. Of course, there may also be consistent sets of n new fermions that are partly formed by replicas of N or Σ , and partly by different multiplets, as we will see in the following sections.

2.2 Two multiplets

Let us classify the possible pairs of chiral fermions ψ_1 and ψ_2 that can be added consistently to the SM and that modify the Higgs couplings. The fermion ψ_1 can satisfy all requirements without ψ_2 only if it transforms as (1,1,0) or (1,3,0), as shown in section 2.1. In this case the three obvious possibilities are

$$\square \qquad N_1 + N_2 \,, \qquad \Sigma_1 + \Sigma_2 \,, \qquad N + \Sigma \,. \tag{2.3}$$

For all other representations, a coupling between ψ_1 and ψ_2 is necessary: either there is a vector-like mass term $m_{12}\psi_1\psi_2$, or a Yukawa coupling $\psi_1\psi_2H(\tilde{H})$. The latter possibility

leads to an inconsistent mass spectrum: one has $N_{w1} = N_{w2} + 1$ (or vice versa) and the unbalanced component of ψ_1 has $T_3 \neq 0$, therefore it cannot be massless. Then, either ψ_1 admits a Majorana mass term or it couples to a SM fermion too. One can check that, in both cases, either another unwanted massless state is left, or a SM neutrino acquires a large mass too. An alternative way to exclude the case of the Yukawa coupling $\psi_1\psi_2H(\tilde{H})$ is to solve the anomaly system (2.1) for n=2: one obtains $N_{c1}=N_{c2}$, $C(R_{c1})=C(R_{c2})$, $R_{w1}=R_{w2}$ and $Y_1=-Y_2$. Thus, we conclude that the two chiral fermions should form a vector-like pair,

$$\square \qquad \psi_1 \sim (R_c, R_w, Y) , \qquad \psi_2 \sim (\overline{R_c}, R_w, -Y) . \tag{2.4}$$

In order to modify the Higgs couplings, at least one among ψ_1 and ψ_2 should have a Yukawa coupling with a SM fermion and the Higgs doublet. We take conventionally all chiral fermions to be left-handed. A SM family is formed by $l \sim (1, 2, -1/2)$, $e^c \sim (1, 1, 1)$, $q \sim (3, 2, 1/6)$, $u^c \sim (\bar{3}, 1, -2/3)$, and $d^c \sim (\bar{3}, 1, 1/3)$. In order to have a Yukawa coupling with these representations, the new fermions should transform under SU(3)_c either as singlets or triplets. The former mix with SM leptons and can be called vector-like leptons (VLLs), the latter mix with SM quarks, hence the name vector-like quarks (VLQs). Under SU(2)_w they can transform as singlets, doublets or triplets. All possible vector-like fermions with a Yukawa coupling to the SM fermions are listed in table 1.

To analyse the phenomenology of vector-like fermion multiplets, it is useful to name the components with different electric charge Q. The possible components of the VLLs have charges Q(N) = 0, Q(E) = -1 and Q(F) = -2. Then, the self-conjugate leptons N and Σ and the four VLLs can be written as

$$N, \quad \Sigma = \begin{pmatrix} E^c \\ N \\ E \end{pmatrix}; \quad E, \quad L = \begin{pmatrix} N \\ E \end{pmatrix}, \quad \Lambda = \begin{pmatrix} E \\ F \end{pmatrix}, \quad \Delta = \begin{pmatrix} N \\ E \\ F \end{pmatrix}.$$
 (2.5)

After EWSB, N, E and E^c can mix with the SM leptons ν , e and e^c , respectively, while F does not mix with the SM. We will discuss the phenomenology of these VLLs in section 4.2.

The possible components of the VLQs have charges Q(X) = 5/3, Q(T) = 2/3, Q(B) = -1/3 and Q(Y) = -4/3. They are embedded in seven possible VLQ multiplets,

$$T, \quad B, \quad X_T = \begin{pmatrix} X \\ T \end{pmatrix}, \quad Q = \begin{pmatrix} T \\ B \end{pmatrix}, \quad Y_B = \begin{pmatrix} B \\ Y \end{pmatrix}, \quad X_Q = \begin{pmatrix} X \\ T \\ B \end{pmatrix}, \quad Y_Q = \begin{pmatrix} T \\ B \\ Y \end{pmatrix}. \quad (2.6)$$

After EWSB, T, T^c , B and B^c can mix with the SM quarks t, t^c , b and b^c , respectively. On the contrary, the components X, Y and their conjugate do not mix with the SM. We will discuss the phenomenology of these VLQs in section 5.1.

2.3 Three multiplets

Let us classify the possible sets of three chiral fermions $\psi_{1,2,3}$ that can be added to the SM consistently with the requirements of section 2. Of course, there is the trivial possibility to combine smaller sets that are already consistent on their own:

ψ_{L1}	ψ_{L2}	coupling to
$E \sim (1, 1, -1)$	$E^c \sim (1, 1, +1)$	l, e^c
$L \sim \left(1, 2, -\frac{1}{2}\right)$	$L^c \sim \left(1, 2, +\frac{1}{2}\right)$	l, e^c
$\Lambda \sim \left(1, 2, -\frac{3}{2}\right)$	$\Lambda^c \sim \left(1, 2, +\frac{3}{2}\right)$	e^c
$\Delta \sim (1, 3, -1)$	$\Delta^c \sim (1,3,+1)$	l
$T \sim \left(3, 1, +\frac{2}{3}\right)$	$T^c \sim \left(\overline{3}, 1, -\frac{2}{3}\right)$	q, u^c
$B \sim \left(3, 1, -\frac{1}{3}\right)$	$B^c \sim \left(\overline{3}, 1, +\frac{1}{3}\right)$	q, d^c
$X_T \sim \left(3, 2, +\frac{7}{6}\right)$	$X_T^c \sim \left(\overline{3}, 2, -\frac{7}{6}\right)$	u^c
$Q \sim \left(3, 2, +\frac{1}{6}\right)$	$Q^c \sim \left(\overline{3}, 2, -\frac{1}{6}\right)$	q, d^c, u^c
$Y_B \sim \left(3, 2, -\frac{5}{6}\right)$	$Y_B^c \sim \left(\overline{3}, 2, +\frac{5}{6}\right)$	d^c
$X_Q \sim (3, 3, +\frac{2}{3})$	$X_Q^c \sim \left(\overline{3}, 3, -\frac{2}{3}\right)$	q
$Y_Q \sim \left(3, 3, -\frac{1}{3}\right)$	$Y_Q^c \sim \left(\overline{3}, 3, +\frac{1}{3}\right)$	q

Table 1. Vector-like pairs of left-handed chiral fermions, that provide a consistent extension of the SM and modify the Higgs boson couplings.

- \square Three copies of $N \sim (1,1,0)$ and/or of $\Sigma \sim (1,3,0)$.
- \square A vector-like fermion from table 1 plus one copy of N or Σ . As the latter couples to the SM lepton doublet l, there may be a non-trivial interplay with the VLLs E, L and Δ , that also couple to l. We will discuss this case in section 4.4.

To explore all the other possibilities, note that there are two patterns for the colour representations of $\psi_{1,2,3}$, that guarantee the absence of massless coloured states:

- $R_{c1} = \overline{R_{c1}}$ plus a vector-like pair $R_{c2} = \overline{R_{c3}} \neq R_{c1}$. The only choice allowing for couplings to the Higgs is $R_{c1} = 1$ and $R_{c2} = 3$. In this case the two subsets ψ_1 and $\psi_{2,3}$ do not interact with each other, therefore each should be a consistent extension of the SM by itself, reducing to the trivial possibilities already listed above.
- $R_{c1} = R_{c2} = \overline{R_{c3}}$. These can be either real or complex representations. One may have considered three real representations of $SU(3)_c$ not all equal to each other; in this case, however, it is not possible to allow Yukawa couplings to the Higgs and to give a mass to all coloured components, at the same time.

In the only non-trivial case, $R_{c1} = R_{c2} = \overline{R_{c3}}$ or permutations, the anomaly conditions in eq. (2.1) reduce to

$$\begin{cases}
N_{w1}^{3}Y_{1} + N_{w2}^{3}Y_{2} + N_{w3}^{3}Y_{3} = 0, \\
N_{w1}Y_{1} + N_{w2}Y_{2} + N_{w3}Y_{3} = 0, \\
N_{w1}Y_{1}^{3} + N_{w2}Y_{2}^{3} + N_{w3}Y_{3}^{3} = 0.
\end{cases}$$
(2.7)

The possible solutions of this system (with N_{wi} positive integers) are

- (a) $Y_i = 0$ and N_{wi} arbitrary, for i = 1, 2, 3.
- (b) $Y_1 = 0$ with N_{w1} arbitrary, $Y_2 = -Y_3 \neq 0$ with $N_{w2} = N_{w3}$, or permutations.
- (c) For any pair of integer numbers $n, m \ge 0$,

$$\begin{cases} N_{w1} = 1 + n \,, & N_{w2} = 2 + n + m \,, & N_{w3} = 3 + 2n + m \,, \\ Y_1 \neq 0 \text{ arbitrary}, & Y_2 = -Y_1 \frac{N_{w1}(N_{w3}^2 - N_{w1}^2)}{N_{w2}(N_{w3}^2 - N_{w2}^2)} \,, & Y_3 = Y_1 \frac{N_{w1}}{N_{w3}} \frac{N_{w2}^2 - N_{w1}^2}{N_{w3}^2 - N_{w2}^2} \,, \end{cases}$$
(2.8)

or permutations.

Let us consider these solutions in turn, to analyse whether they can satisfy the other requirements of section 2.

- (a) In order to couple to the Higgs boson, one needs $R_{ci} = 1$ and $R_{wi} = 1$ or 3 for i = 1, 2, 3, that is three copies of N or Σ : a trivial possibility already considered.
- (b) Suppose first that ψ_2 and ψ_3 form a vector-like pair, that is, $R_{c1} = R_{c2} = \overline{R_{c3}}$. But, to avoid unpaired complex representations of $SU(3)_c$, one needs R_{c1} to be real. Barring the trivial cases where ψ_1 and $\psi_{2,3}$ form self-consistent extensions of the SM separately, the necessary condition to modify the Higgs couplings is to allow for a Yukawa coupling between ψ_1 and $\psi_{2,3}$. This leads to

$$\Box \quad \psi_1 \sim (R_c, R_w, 0) \,, \quad \psi_2 \sim \left(R_c, R_w \pm 1, \frac{1}{2} \right), \quad \psi_3 \sim \left(R_c, R_w \pm 1, -\frac{1}{2} \right), \quad R_c = \overline{R_c} \,. \tag{2.9}$$

The choice of R_w is arbitrary up to the $SU(2)_w$ global anomaly: for $N_w = 2 + 4n$, one needs N_c to be even. The colourless case $R_c = 1$ will be discussed in section 4.4. The coloured case $R_c = 8, 27, \ldots$ will be discussed in section 5.3.

Next, suppose that ψ_2 and ψ_3 do not form a vector-like pair, that is, a complex representation $R_{c1} = \overline{R_{c2}} = \overline{R_{c3}}$. In order to have the same number of colour-conjugate representations one needs $N_{w1} = 2N_{w2}$. A Yukawa coupling is also needed among ψ_1 and $\psi_{2,3}$ to provide masses, so the only possibility is

$$\square \qquad \psi_1 \sim (R_c, 2, 0) , \quad \psi_2 \sim \left(\overline{R_c}, 1, \frac{1}{2}\right), \quad \psi_3 \sim \left(\overline{R_c}, 1, -\frac{1}{2}\right), \quad R_c \neq \overline{R_c} . \quad (2.10)$$

The $SU(2)_w$ global anomaly further requires that N_c must be even. Note that this is the minimal, consistent set of chiral fermions that has no vector-like mass terms, rather it acquires a mass from the Yukawa couplings only. The phenomenology of purely chiral fermions is discussed in section 3.

(c) For $(n, m) \neq (0, 0)$, one has $N_{w3} \geq 4$. Then, ψ_3 does not couple to the SM nor to ψ_1 , and even the possible Yukawa coupling to ψ_2 cannot provide a mass to all the N_{w3} components of ψ_3 . Therefore, let us take (n, m) = (0, 0), that implies

$$\psi_1 \sim (R_c, 1, Y) , \quad \psi_2 \sim \left(R_c, 2, -\frac{4}{5} Y \right) , \quad \psi_3 \sim \left(\overline{R_c}, 3, \frac{1}{5} Y \right) .$$
(2.11)

By requiring an equal number of components with opposite electric charge, one finds $Y=\pm 1/2$ or $Y=\pm 1/6$. In both cases one can check that some components of the new fermions remain massless, therefore no consistent SM extension of this type exists.

2.4 Four multiplets

In the previous sections we derived the list of all the consistent sets of n new chiral fermions, with $n \leq 3$, discussing in detail how to implement the requirements of section 2. Here we provide the complete list for n = 4, without displaying the lengthy and involved analysis needed to prove this result.

First of all, there are a number of possibilities to combine smaller subsets of new fermions that are already consistent by themselves. It is worth to list them for bookkeeping and to point out those combinations with special phenomenological relevance:

- \square Four copies of N and/or Σ .
- \square Two copies of N and/or Σ plus a vector-like fermion from table 1. In particular, the set (N, Σ, L, L^c) corresponds to the neutralinos and charginos of the minimal supersymmetric SM: bino, wino and the two higgsinos. This case is discussed in section 4.4.
- \square Two vector-like fermions Ψ_1 and Ψ_2 from table 1. A non-trivial interplay occurs when Ψ_1 and Ψ_2 couple both to a given SM fermion, as indicated in the last column of table 1, and/or when there is a Yukawa coupling between Ψ_1 and Ψ_2 : this happens for E or Δ with L or Λ ; T or X_Q with X_T or Q; B or Y_Q with Q or Y_B . In models of partial compositeness, a SM fermion acquires its mass by mixing with two vector-like composite fermions, with the same quantum numbers as the SM left- and right-handed components: Q and T for the top quark, Q and Q for the bottom quark, Q and Q for the tau lepton. This case is discussed in section 4.3 for leptons and 5.2 for quarks.
- \square One copy of N or Σ and a set of three fermions from eq. (2.9) or eq. (2.10). A non-trivial interplay occurs in the case (1,3,0)+(1,5,0)+(1,4,1/2)+(1,4,-1/2), discussed in section 4.4.

Let us come to the consistent sets of four fermions that are not the union of two smaller self-consistent sets. We found that non-trivial solutions are possible only when the four colour representations R_{ci} are all equal or conjugate to each other. After all requirements of section 2 are taken into account, only two possible patterns emerge:

• For arbitrary R_c and R_w , a viable set of four multiplets is provided by

$$\square \qquad (R_c, R_w - 1, 0) + (R_c, R_w + 1, 0) + (\overline{R_c}, R_w, 1/2) + (\overline{R_c}, R_w, -1/2), \quad (2.12)$$

with one exception: if N_w is odd, then either $C(R_w - 1)$ or $C(R_w + 1)$ is half-integer, therefore one needs N_c even to cancel the global $SU(2)_w$ anomaly.

The case $R_c = 1$ can be described as two Majorana leptons plus a vector-like lepton (see section 4.4). The case $R_c = \overline{R_c} \neq 1$ is the analogue for coloured fermions (section 5.3). Finally, the case $R_c \neq \overline{R_c}$ is purely chiral, with no masses before EWSB (section 3).

• For arbitrary R_c , R_w and Y, a viable set of four multiplets is

$$\square$$
 $(R_c, R_w, Y) + (\overline{R_c}, R_w, -Y) + (R_c, R_w + 1, Y - 1/2) + (\overline{R_c}, R_w + 1, -Y + 1/2)$. (2.13)

For the first time we encounter a pattern where the hypercharges of the new fermions are not determined uniquely.

The case $R_c = 1$ corresponds to two VLLs (section 4.3), except when Y = 0 with N_w odd, or Y = 1/2 with N_w even: then, one has two Majorana leptons plus one VLL (section 4.4). The case $R_c \neq 1$ corresponds to two VLQs (section 5.2), except when $R_c = \overline{R_c}$ and Y = 0 with N_w odd, or Y = 1/2 with N_w even: then, one has two Majorana quarks plus one VLQ (section 5.3).

We found that all other sets of four multiplets relevant for Higgs couplings are not viable: either some component remains massless, or a gauge anomaly is present.

2.5 Larger sets of new fermions

We do not attempt a general classification for $n \geq 5$ new chiral fermions. On the one hand, the general principles and the different phenomenological possibilities are already well illustrated by more minimal sets of fermions. On the other hand, a detailed analysis is worth only in the context of a specific, well-motivated theory beyond the SM. Here we shall mention some prominent examples that have been extensively studied, to situate them in the context of our classification.

- We have shown that there are two sets of purely chiral fermions, displayed in eq. (2.10) and in eq. (2.12), formed by three and four multiplets, respectively. The more traditional chiral extension of the SM is a fourth family, formed by the five multiplets q'_L , t'_R , b'_R , l'_L and τ'_R . It was already excluded at the time of LEP, because the Z invisible width forbids a fourth massless neutrino, but it could be rescued adding a sixth multiplet, a sterile neutrino ν'_R . It is by now excluded by the measurement of the Higgs boson couplings [25], as we will review at the end of section 3.
- The minimal supersymmetric extensions of the SM predicts fermionic partners for the gauge bosons and for the two Higgs doublets. This amounts to five chiral multiplets: a bino $\sim (1,1,0)$, a wino $\sim (1,3,0)$, two higgsinos $\sim (1,2,\pm 1/2)$ and a gluino $\sim (8,1,0)$. The latter does not enter in our classification, since it does not couple to the Higgs doublet. Concerning the other four multiplets, supersymmetry restricts the possible couplings among them and to the SM, therefore it corresponds to a special case in the parameter space of the SM extension by the set (N, Σ, L, L^c) . We will briefly discuss the related phenomenology in section 4.4. Of course, our purely fermionic extension of the SM corresponds to the limit where the scalar supersymmetric partners are significantly heavier than neutralinos and charginos.

Another scenario addressing the hierarchy problem is compositeness. An effective way to couple the SM fermions to a composite Higgs doublet amounts to a partial fermion compositeness: each SM chiral fermion mixes with a composite vector-like fermion with the same quantum numbers. Thus, to induce a Yukawa coupling among two SM fermions and the composite Higgs one needs two vector-like fermions. Therefore, a SM extension by four chiral multiplets is suitable to study this mechanism for one SM Yukawa coupling at a time. Indeed, partial compositeness corresponds to a special subspace of parameters, because the symmetries of composite models restrict the couplings of the new fermions and of the SM ones. We will briefly discuss the phenomenology of τ -compositeness in section 4.4 and the case of b and b-compositeness in section 5.2. Of course, realistic models of partial compositeness require more than two vector-like fermions, e.g. to induce the Yukawa couplings of all the heavy, third family fermions. The interplay between the Higgs and composite vector-like fermions is studied in detail e.g. in refs. [26–30].

3 Phenomenology of new chiral fermions

In this section we study purely chiral sets of new fermions, that is to say, one cannot write any fermion mass term before EWSB, thus their masses are generated by the Higgs vev only. These sets do not contain vector-like pairs of chiral multiplets, that would admit a Dirac mass, nor multiplets in the representations $(R_c, R_w, 0)$ with $R_c = \overline{R_c}$ and R_w odd, that would admit a Majorana mass. A purely chiral set, consistent with the requirements of section 2, constitutes a new fermion 'family', very much analogue to the three SM families.

We identified two classes of purely chiral sets, formed by three and four multiplets respectively, displayed in eq. (2.10) and eq. (2.12). We will discuss the phenomenology of these two classes in some detail. In the last part of the section, we will investigate whether larger chiral sets of fermions may be compatible with present Higgs data.

• Three chiral multiplets. The only consistent 'family' formed by three chiral multiplets is

$$\psi_{1L} \sim (R_c, 2, 0), \quad \psi_{2R} \sim \left(R_c, 1, \frac{1}{2}\right), \quad \psi_{3R} \sim \left(R_c, 1, -\frac{1}{2}\right), \quad R_c \neq \overline{R_c}, N_c \text{ even}, \quad (3.1)$$

the smallest viable representation being $R_c = 6$. The Yukawa interactions are

$$-\mathcal{L}_Y = \lambda_{12}\overline{\psi_{1L}}\tilde{H}\psi_{2R} + \lambda_{13}\overline{\psi_{1L}}H\psi_{3R} + h.c. . \qquad (3.2)$$

Here and in the rest of the paper we do not display the obvious kinetic terms, that must be added for each new fermion. After EWSB one is left with two mass eigenstates F_{12} and F_{13} in the same colour representation R_c , with charge $Q = \pm 1/2$ and mass $m_{12} = \lambda_{12} v / \sqrt{2}$ and $m_{13} = \lambda_{13} v / \sqrt{2}$, respectively.

The lightest new fermion is stable and forms hadrons with exotic charges, that are constrained to be heavier than several hundreds of GeVs. Indeed, the searches for R-hadrons [31, 32] assume the existence of a stable stop or sbottom (scalar with $R_c = 3$), or of

a stable gluino (fermion with $R_c = 8$). In the latter case one finds $m_{R_c=8} \gtrsim 1320 \,\text{GeV}$ [33], and we expect a similar (stronger) bound for $R_c = 6$ (larger colour representations), as these fermions are pair-produced through their coupling to gluons. To roughly estimate the limit on a stable sextet, we rescale the gluino bound by computing the ratio between the sextet and octet production cross section at tree level. Taking into account the different colour contractions and the interference of the s, t and u-channel, we obtain a lower bound $m_{R_c=6} \gtrsim 1400 \,\text{GeV}$. Further discussions and references on the constraints on R-hadrons can be found e.g. in refs. [20, 34]. This limit from direct searches already leads to some tension with the perturbativity upper bound, $m_{12,13} \ll (4\pi)v/\sqrt{2} \simeq 2.2 \,\text{TeV}$.

The contribution of $F_{12,13}$ to the oblique parameters reads

$$S \simeq \frac{N_c}{6\pi}, \qquad T \simeq \frac{N_c}{16\pi s_w^2 c_w^2 m_Z^2} \left(m_{12}^2 + m_{13}^2 - 2 \frac{m_{12}^2 m_{13}^2}{m_{12}^2 - m_{13}^2} \ln \frac{m_{12}^2}{m_{13}^2} \right). \tag{3.3}$$

Note that for $(m_{12}-m_{13}) \to 0$ one finds $T \propto (m_{12}-m_{13})^2$, because in the degenerate limit the custodial symmetry is restored: for $\lambda_{12} = \lambda_{23}$ eq. (3.2) has a global SU(2)_R symmetry with ψ_{2R} and ψ_{3R} transforming as a doublet. The value of S can lie within the 3σ ellipse, but only if $N_c = 6$ and $T \simeq 0.3$ at the same time (see figure A.2). This can be achieved for $(m_{12}+m_{13})/2 \simeq 1500 \,\text{GeV}$ and $(m_{12}-m_{13}) \simeq 50 \,\text{GeV}$. Thus, this 'family' of new fermions is marginally compatible with direct searches and EW precision tests.

After the Higgs discovery, however, one can definitely exclude such a set of new fermions. As they are heavier than the Higgs boson and do not mix with the SM fermions, the Higgs decay width at tree-level are unchanged. However, a huge deviation occurs in the loop-induced Higgs coupling to gluons,

$$R_{gg} \equiv \frac{\sigma(gg \to h)}{\sigma_{SM}(gg \to h)} \simeq [1 + 4C(R_c)]^2 . \tag{3.4}$$

where we have taken the limit $m_t^2, m_{12}^2, m_{13}^2 \gg m_h^2/4$ in the loop form factor (see appendix B.2). Even the smallest possible colour representation has C(6) = 5/2, leading to a huge $R_{gg} = 121$, totally incompatible with LHC data.

• Four chiral multiplets. Let us move to the only consistent 'family' formed by four chiral multiplets,

$$\psi_{1L} \sim (R_c, R_w - 1, 0), \quad \psi_{2L} \sim (R_c, R_w + 1, 0), \quad \psi_{3R} \sim \left(R_c, R_w, \frac{1}{2}\right), \quad \psi_{4R} \sim \left(R_c, R_w, -\frac{1}{2}\right), \quad (3.5)$$

with $R_c \neq \overline{R_c}$ to prevent vector-like or Majorana mass terms, and with N_c even if N_w is odd, to prevent a global $SU(2)_w$ anomaly. The allowed Yukawa interactions are

$$-\mathcal{L}_Y = \lambda_{13}\overline{\psi_{1L}}\tilde{H}\psi_{3R} + \lambda_{14}\overline{\psi_{1L}}H\psi_{4R} + \lambda_{23}\overline{\psi_{2L}}\tilde{H}\psi_{3R} + \lambda_{24}\overline{\psi_{2L}}H\psi_{4R} + h.c. . \tag{3.6}$$

where the explicit $SU(2)_w$ contractions are defined in eq. (B.4). After EWSB the components of $\psi_{1,2L}$ combine with those of $\psi_{3,4R}$ to forms $2N_w$ mass eigenstates: one with charge $Q = N_w/2$; two mixed states with $Q = N_w/2 - 1, \ldots, -N_w/2 + 1$; one with $Q = -N_w/2$.

As they have (half-)integer charges, they do not mix with the SM quarks and the lightest state is stable and hadronises, with collider bounds above 1 TeV, analogue to those discussed above. The discussion of oblique parameters is also similar to the previous case: one can be marginally consistent with data, by choosing the parameters to realise an approximate custodial protection.

The way to definitely exclude this set of chiral fermions is, once again, their contribution to the Higgs boson coupling to gluons. Note that each of the $2N_w$ mass eigenstates belongs to the same colour representation R_c and must be (much) heavier than the top quark, therefore one finds

$$R_{gg} \simeq [1 + 2(2N_w)C(R_c)]^2$$
 (3.7)

Even in the minimal case with $N_w=2$ and C(3)=1/2, one finds a very large $R_{gg}\simeq 25$, incompatible with the LHC Higgs data.

• Larger sets of chiral multiplets. Let us ask the question whether we can exclude any set of purely chiral fermions, even when it is formed by more than four multiplets. Indeed, the Higgs coupling to gluons implies that any new chiral fermion should be colourless, because even the minimal set of chiral coloured fermions, formed by a weak doublet and two weak singlets with $R_c = 3$, leads to a large $R_{gg}^{\min} \simeq 9$. This is not compatible with the range currently allowed by global fits, $0.5 \lesssim R_{gg} \lesssim 1.8$ at 99 % C.L. [35] (see appendix B.3 for details). In particular, in this way one can exclude [25] a fourth SM family, formed by the six multiplets q'_L , t'_R , b'_R , l'_L , τ'_R and ν'_R . Recall that the sterile neutrino is required to avoid an additional massless neutrino, that is forbidden by the Z invisible width; then this set of fermions is not purely chiral, but one may invoke a lepton number symmetry to forbid the sterile neutrino Majorana mass. Let us remark that coloured chiral fermions may be allowed in the case of extended Higgs sectors, not considered in the present paper. For example, adding an Higgs triplet, it is possible to rescue the fourth family [36]. Another example is provided by coloured chiral fermions receiving their mass from a second Higgs doublet [37].

Coming to colourless chiral fermions, some of the mass eigenstates are necessarily charged and thus contribute to the Higgs width to photons as

$$R_{\gamma\gamma} = \frac{\left| \mathcal{A}_{\text{SM}}^{\gamma\gamma} + A_{\text{new}}^{\gamma\gamma} \right|^2}{\left| \mathcal{A}_{\text{SM}}^{\gamma\gamma} \right|^2}, \qquad A_{\text{new}}^{\gamma\gamma} \simeq \frac{4}{3} \sum_k Q_k^2, \tag{3.8}$$

where $R_{\gamma\gamma}$ is defined in eq. (B.41), the SM amplitude is $\mathcal{A}_{\rm SM}^{\gamma\gamma} \simeq -6.5$ and the sum runs over the new fermion mass eigenstates. Note that, to derive eq. (3.8) from eqs. (B.21) and (B.22), we took (i) $2m_i \gg m_h$, that is accurate enough, even though the lower bounds on heavy charged lepton masses are weaker than those on coloured particles; (ii) Higgs-fermion couplings $y_i = m_i/v$ and $\tilde{y}_i = 0$, that is the case for purely chiral fermions, because their mass matrices are proportional to the Higgs vev v, see eq. (B.6). Note also that the result is independent from potential mixing between the new fermions and the SM leptons. The presently allowed range is $0.5 \lesssim R_{\gamma\gamma} \lesssim 1.9$ at 99 % C.L. [35]. For n chiral multiplets

 (R_{wi}, Y_i) , one finds

$$\mathcal{A}_{\text{new}}^{\gamma\gamma} \simeq \frac{2}{3} \sum_{i=1}^{n} \sum_{k=1}^{N_{wi}} Q_k^2 = \frac{2}{3} \sum_{i=1}^{n} \frac{N_{wi}(N_{wi}^2 + 12Y_i^2 - 1)}{12} . \tag{3.9}$$

We added an overall factor 1/2 to take into account that each massive fermion is formed by two chiral components. Equivalently, one may take the sum only over fermions of a given chirality. For example, a minimal set is formed by a weak doublet 2_L of hypercharge Y paired with two weak singlets $(1+1)_R$, giving a contribution $\mathcal{A}_{\text{new}}^{\gamma\gamma} = 2(1+4Y^2)/3 \geq 2/3$. The next-to-minimal set $(2+2)_L$ paired with $(1+1+1+1)_R$ implies $A_{\text{new}}^{\gamma\gamma} > 4/3$, that is still allowed by the present constraint on $R_{\gamma\gamma}$, while for example $(3+2)_L$ gives already $A_{\text{new}}^{\gamma\gamma} > 10/3$, that is almost excluded. Since the SM amplitude has opposite sign w.r.t. the one of new fermions, one can also envisage the contrived possibility of a large $A_{\text{new}}^{\gamma\gamma} \sim -2\mathcal{A}_{\text{SM}}^{\gamma\gamma} \simeq 13$.

This shows that there are purely chiral sets of n fermions that satisfy the $\gamma\gamma$ constraint. However, we have also shown before that no set exists for $n \leq 4$, that satisfies the consistency requirements of section 2. It is non-trivial to check whether purely chiral sets with n > 4 could be consistent. Consider for example the case of two weak doublets plus four weak singlets. In order for all components to receive a mass from the Yukawa couplings to the Higgs doublet, the hypercharges must be chosen as

$$(2, Y_1), (2, Y_2), (1, -Y_1 + \frac{1}{2}), (1, -Y_1 - \frac{1}{2}), (1, -Y_2 + \frac{1}{2}), (1, -Y_2 - \frac{1}{2}),$$

$$(3.10)$$

in the convention where all multiplets have the same chirality. The absence of anomalies requires eq. (2.1) to hold, and this leads to $Y_1 = -Y_2 \equiv Y$. As a consequence, three vector-like mass terms are allowed and such set of fermions does not qualify as purely chiral.

At this point one should recall that, in this paper, we took the point of view that all mass terms and interactions allowed by the gauge symmetries are present. In alternative, one can easily introduce some global symmetry to forbid possible vector-like mass terms, thus imposing by hand that a given set of fermions is chiral. For example in eq. (3.10) take a U(1) symmetry with charge +1 for doublets and -1 for singlets. If one takes this point of view, the set of fermions in eq. (3.10) qualifies as the minimal still viable set of purely chiral fermions. Indeed, besides being consistent with all the requirements of section 2, it can be compatible with direct searches, EW precision tests, and constraints from the Higgs couplings.

Concerning direct collider searches, as the new leptons have charges $Q = Y \pm 1/2$, they do not mix with the SM leptons (except for |Y| = 1/2 or 3/2) and the lightest state is stable. There are severe bounds on the number density of such charged relics [20], but they depend on cosmological assumptions: e.g. for a reheating temperature below their mass, they were never produced in the early Universe. Limits on heavy stable leptons are of the order of a few hundreds of GeVs, and are displayed in table 2 for some representative values of Q. For a review on heavy stable particles see ref. [34].

The contributions to the S and T parameters of a fermion 'family' formed by one doublet and two singlets are given in eqs. (A.25) and (A.26). In the present case we have

Q	1/3	2/3	1	2	3	4	5	6	7	8
bound in GeVs	200	480	574	685	752	793	796	781	757	715

Table 2. The 95 % C.L. lower bounds on the mass of heavy stable leptons, from the CMS collaboration [32]. The production is assumed to occur through the Drell-Yan process only. Limits are obtained for $SU(2)_w$ singlets, but they remain similar in general [20]. The ATLAS collaboration obtains comparable but less stringent limits in the range $2 \le |Q| \le 6$ [38]. For larger values of Q see ref. [39].

two such 'families' with $N_c=1$ and opposite hypercharges $\pm Y$, and one can easily lie within the 3σ ellipse of figure 10. For example in the custodial limit where the two mass eigenstates of each 'family' are degenerate, one finds $T \simeq 0$ and $S \simeq 0.1$. Concerning the Higgs couplings, one finds $\mathcal{A}_{\text{new}}^{\gamma\gamma} = 4(1+4Y^2)/3$, that lies in the allowed range of $R_{\gamma\gamma}$ for $|Y| \lesssim 0.3$ and $1.4 \lesssim |Y| \lesssim 1.6$.

Finally, it is interesting to compare eq. (3.9) with the analogue amplitude for the Higgs boson coupling to γZ . For n chiral multiplets (R_{wi}, Y_i) , one finds

$$\mathcal{A}_{\text{new}}^{\gamma Z} \simeq \frac{2}{3} \sum_{i=1}^{n} \sum_{k=1}^{N_{wi}} Q_k \frac{T_{3k} - s_w^2 Q_k}{c_w^2} = \frac{2}{3} \sum_{i=1}^{n} \frac{N_{wi} (N_{wi}^2 - 12Y_i^2 \tan^2 \theta_w - 1)}{12},$$
 (3.11)

where we used eq. (B.31) particularised to the case of chiral fermions, in the same way we did above for the $\gamma\gamma$ case. Note that, when summing over the mass eigenstates of equal charge Q, the mixing matrices disappear from the Z couplings in eq. (A.6), therefore one reduces to a sum over the interaction eigenstates. For example, the set in eq. (3.10) gives $\mathcal{A}_{\text{new}}^{\gamma Z} \simeq 2 \left[1 - \left(1 + 8Y^2\right) \tan^2 \theta_w\right]/3$.

4 Phenomenology of non-chiral leptons

In this section we discuss new colourless fermions, which admit either a Majorana or a vector-like mass term before EWSB.

4.1 Majorana leptons

Let us consider leptons that admit a Majorana mass term. The latter requires a vanishing hypercharge, Y = 0. The two possibilities relevant for the Higgs couplings are sterile neutrinos $N \sim (1, 1, 0)$, and weak triplets $\Sigma \sim (1, 3, 0)$.

• Sterile neutrinos. In the case of one sterile neutrino, the SM Lagrangian is extended to $\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_N$, where

$$\mathcal{L}_N = -\overline{l_{L\alpha}}\lambda_{N\alpha}\tilde{H}N_R - \frac{1}{2}\overline{N_R^c}M_NN_R + h.c. . \qquad (4.1)$$

Only one linear combination ν_L of the three active neutrinos $\nu_{L\alpha}$ couples to N_R , and since we are not concerned with flavour issues we will drop the index α in the following. After EWSB, ν_L and N_R^c mix and combine into two Majorana fermions ν_l and ν_h with

definite masses, $m_{\nu_l} \leq m_{\nu_h}$; active neutrino mass searches imply $m_{\nu_l} \lesssim 1 \,\text{eV}$. If one takes the limit $m_{\nu_l} \ll m_h$, the type I seesaw mechanism is realised: $m_{\nu_l} \simeq \lambda_N^2 v^2/(2M_N)$ and $m_{\nu_h} \simeq M_N$. The Higgs boson couplings to $\nu_l \nu_l$ and $\nu_h \nu_h$ are proportional to m_{ν_l}/v , and the coupling to $\nu_l \nu_h$ is proportional to $\sqrt{m_{\nu_l} m_{\nu_h}}/v$, leading to a negligibly small decay width, $\Gamma(h \to \nu_l \nu_h) < m_h^2/(8\pi v^2) m_{\nu_l} \lesssim 10^{-8} \,\text{MeV}$. Also, one can check that the decay widths of the Z-boson receive negligible corrections, always proportional to m_{ν_l}/v . For m_{ν_h} above the EW scale, one can compute the ν_h contribution to the S and T parameters, that turns out to be suppressed by the tiny ratio m_{ν_l}/m_{ν_h} .

In the case of two or more sterile neutrinos N_i , in most of the parameter space the arguments above apply to each N_i separately: either the Majorana mass M_i is as small as the eV scale, or the active-sterile mixing $\theta_i \equiv \lambda_{N_i}(v/\sqrt{2})/M_{N_i}$ is suppressed, $|\theta_i^2 M_{N_i}| \sim m_{\nu_l} \lesssim 1 \,\text{eV}$. In either case the corrections to the Higgs and Z/W-boson couplings are tiny. The only exception occurs when much larger θ_i are tuned among each other, in order for the N_i contributions to the light neutrino mass to cancel. Consider for simplicity two sterile neutrinos $N_{1,2}$. At leading order in the mixing angles θ_i one has

$$m_{\nu_l} \simeq |\theta_1^2 M_{N_1} + \theta_2^2 M_{N_2}| \lesssim 1 \text{ eV} .$$
 (4.2)

The two summands have a physical relative phase, therefore they can be orders of magnitude larger than m_{ν_l} , if there is a strong cancellation between the two: the active-sterile mixing can be large, no matter how large the sterile masses $m_{\nu_{h1,2}}$ are. Even though this scenario requires a severe tuning of parameters to lead to observable effects, it may be justified by some symmetry. For example, in the so-called inverse seesaw model [40–42] (see also ref. [43]), the lepton number symmetry $\mathrm{U}(1)_L$ is broken by a small mass parameter, and the cancellation occurs naturally in the limit where this parameter goes to zero. Therefore, it is worth to analyse the phenomenological consequences of a large active-sterile mixing: both Higgs couplings and EW gauge boson couplings can be significantly modified.

Consider first the neutrino mass eigenstates ν_l , ν_{h1} , ν_{h2} in the regime $m_{\nu_l} \ll m_{\nu_{h1,2}} \ll m_h, m_Z$. One finds that the decay widths of the Higgs boson can be significantly modified, in particular $\Gamma(h \to \nu_l \nu_{hi}) \simeq m_h m_{\nu_{hi}}^2 |\theta_i|^2 / (8\pi v^2)$ and $\Gamma(h \to \nu_{hi} \nu_{hi}) \simeq m_h m_{\nu_{hi}}^2 |\theta_i|^4 / (4\pi v^2)$. These rates can be easily as large as the total SM Higgs width, $\Gamma_h^{\rm SM} \simeq 4 \, {\rm MeV}$, therefore the LHC experiments already constrain θ_i and $m_{\nu_{hi}}$. Note that both invisible and visible decay channels are affected, since $\nu_{h1,2}$ decay not only into light neutrinos, but also into SM particles e.g. via virtual W-bosons. Detailed analyses of the parameter space and of various constraints can be found e.g. in refs. [44–48]. Note that the Z-boson invisible width Γ_Z^{inv} , that is measured at the few per mil level, is not significantly affected for $m_{\nu_{h1,2}} \lesssim 1 \, {\rm MeV}$, with $\nu_{h1,2}$ decaying mostly invisibly into three ν_l : even in the presence of large mixing, only the active components of $\nu_{l,h1,h2}$ couple to the Z-boson, and one recovers the SM value of Γ_Z^{inv} once the sum over all neutrino pairs is taken. On the contrary, for larger $m_{\nu_{h1,2}}$ the heavy neutrinos mediate visible Z-decays, therefore Γ_Z^{inv} is depleted and a significant upper bound applies on $|\theta_i|$.

Consider next the complementary regime $m_h, m_Z \lesssim m_{\nu_{h1,2}}$. In this case the Higgs and Z decay width are not modified, but a significant active neutrino fraction in $\nu_{h1,2}$ can still have observable consequences. Direct searches of EW scale sterile neutrinos through their

mixing with active neutrinos have been performed e.g. by ATLAS [49, 50] and CMS [51, 52]. Here we would like to point out that the EW precision parameters S and T can also receive important corrections, that constrain the masses and mixing of the sterile neutrinos. To understand this quite surprising fact, that is generally overlooked, it is convenient to write the 3×3 neutrino mass matrix in the basis $(\nu_L, N_{R1}^c, N_{R2}^c)$ as

$$\mathcal{M}_{\nu} = U^* diag(m_{\nu_l}, m_{\nu_{h1}}, m_{\nu_{h2}}) U^{\dagger}, \qquad (4.3)$$

with U unitary and subject to the constraint $0 = (\mathcal{M}_{\nu})_{11} \simeq U_{12}^{*2} m_{\nu_{h1}} + U_{13}^{*2} m_{\nu_{h2}}$, where we neglected the tiny m_{ν_l} . Then, the active neutrino fractions U_{1i} contained in the mass eigenstates can be parametrized in full generality as follows: $U_{13} = \theta$ taken to be real, $U_{12} = i\theta/\sqrt{r_h}$ with $r_h \equiv m_{\nu_{h1}}/m_{\nu_{h2}}$ and $|U_{11}|^2 = 1 - \theta^2(1 + r_h)/r_h$. The 3σ lower bound on Γ_Z^{inv} implies $\theta^2(1 + r_h)/r_h \lesssim 0.015$. We computed T and S using the formulas in appendix A, as a function of θ , r_h and $r_Z \equiv m_Z/m_{\nu_{h2}}$, neglecting the mass of the SM leptons and including a symmetry factor 1/2 for loops of Majorana fermions. Here we report the result in some physically interesting limits:

(a)
$$m_{\nu_{h2}} = m_{\nu_{h1}} \gg m_Z : T \simeq \frac{\theta^4}{4\pi s_w^2 c_w^2} \frac{m_{\nu_{h2}}^2}{m_Z^2}, \quad S \simeq \frac{2\theta^2}{9\pi} \left(4 + 3\log \frac{m_{\nu_{h2}}^2}{m_Z^2} \right);$$

(b) $m_{\nu_{h2}} \gg m_{\nu_{h1}} = m_Z : T \simeq \frac{\theta^4}{8\pi s_w^2 c_w^2} \frac{m_{\nu_{h2}}^2}{m_Z^2} \left(3 - \log \frac{m_{\nu_{h2}}^2}{m_Z^2} \right), \quad S \simeq \frac{\theta^2}{4\pi} \frac{m_{\nu_{h2}}}{m_Z}.$

$$(4.4)$$

In case (a), taking the maximal allowed value $\theta_{\text{max}}^2 \simeq 0.007$, the correction to T grows quadratically with the sterile neutrino mass: requiring to remain in the 3σ ellipse in the S-T plane (see figure 10), one finds the upper bound $m_{\nu_{h2}} \lesssim 8.5 \,\text{TeV}$. This sensitivity to very large scales is due to the significant fraction of the active neutrino in the heavy states; note that this non-decoupling effect requires a strong tuning among the two sterile neutrino parameters. In case (b), the active fraction in the heaviest sterile neutrino is rather $\theta_{\text{max}}^2 \simeq 0.015(m_Z/m_{\nu_{h2}})$, therefore T grows only logarithmically with $m_{\nu_{h2}}$, while S remains constant: one remains in the ellipse for $m_{\nu_{h2}}$ as large as the Planck scale.

• Weak triplets with zero hypercharge. In the case of a weak triplet $\Sigma_R \sim (1,3,0)$, the SM Lagrangian is extended by

$$\mathcal{L}_{\Sigma_R} = -\sqrt{\frac{2}{3}} \overline{l_{L\alpha}} \lambda_{\Sigma\alpha} \Sigma_R \tilde{H} - \frac{1}{2} \text{Tr} \left(\overline{\Sigma_R^c} M_{\Sigma} \Sigma_R \right) + h.c., \qquad (4.5)$$

where we adopted the matrix notation

$$\Sigma_R \equiv \sqrt{2}\Sigma_R^a \tau^a = \frac{1}{\sqrt{2}} \begin{pmatrix} \Sigma_R^3 & \Sigma_R^1 - i\Sigma_R^2 \\ \Sigma_R^1 + i\Sigma_R^2 & -\Sigma_R^3 \end{pmatrix} \equiv \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma_R^0 & -\Sigma_R^+ \\ \Sigma_R^- & -\frac{1}{\sqrt{2}}\Sigma_R^0 \end{pmatrix}$$
(4.6)

and we normalised the triplet Yukawa coupling according to appendix B.1. After EWSB, the neutral component Σ_R^0 and a linear combination of active neutrinos combine into two Majorana fermions ν and Σ_0 , in complete analogy to the case of ν_l and ν_h discussed above.

As usual, we will consider only the mixing with the third lepton family, taking $\lambda_{\Sigma e, \Sigma \mu} = 0$ and $\lambda_{\Sigma \tau} \equiv \lambda_{\Sigma}$. Indeed, flavour changing neutral current processes such as $\mu \to e \gamma$ or $\mu \to 3e$ are strongly constrained [53, 54]. In the limit $\lambda_{\Sigma} v \ll M_{\Sigma}$ one realises the so-called type III seesaw mechanism: $m_{\nu} \simeq \lambda_{\Sigma}^2 v^2/(6M_{\Sigma})$ and $m_{\Sigma_0} \simeq M_{\Sigma}$. The charged components $(\Sigma_R^+)^c$ and Σ_R^- mix with the SM charged leptons τ_L and τ_R respectively, to form the mass eigenstates τ and Σ_R^- . Then, three real parameters — the Yukawa coupling λ_{Σ} , the mass M_{Σ} and the SM tau Yukawa coupling λ_{τ} — determine the mass of four physical states, m_{ν} and M_{Σ^0} in the neutral sector, m_{τ} and M_{Σ^-} in the charged sector. The mixing angles for neutrinos and left-handed charged leptons are suppressed by $\sqrt{m_{\nu}/M_{\Sigma^0}}$; the mixing of right-handed charged leptons receives an additional suppression by m_{τ}/M_{Σ^-} .

The couplings of Σ_0 to the Z and Higgs bosons are exactly the same as the couplings of ν_h discussed above. In particular, for vanishing m_{ν} all Z and Higgs couplings reduce to their SM values, therefore the corrections are negligibly small. At tree level, $M_{\Sigma^-} - M_{\Sigma^0}$ also vanishes with m_{ν} , however it is well-known that at one loop weak interactions induce a mass split, $M_{\Sigma^-} - M_{\Sigma^0} \simeq 170\,\mathrm{MeV}$ (see e.g. ref. [18]). Neglecting the tiny mixing angles, the only heavy lepton couplings are $Z\Sigma^+\Sigma^-$ and $W^+\Sigma^-\Sigma^0$; other mixing-suppressed couplings are relevant for Σ -decays [55]. The contribution of Σ to the EW precision parameters S and T is vanishingly small, as EWSB is felt only through the mixing angles and through the loop-induced mass splitting among the Σ -components, and both are very small.

Coming to direct searches, LEP looked for new charged leptons pair produced and decaying to $W\nu$, setting a lower bound $M_{\Sigma^-} \gtrsim 100\,\mathrm{GeV}$ [56]. At the LHC heavy leptons are mostly pair-produced via $Z^*/\gamma^* \to \Sigma^+\Sigma^-$ and $W^{\pm *} \to \Sigma^\pm\Sigma^0$. The fraction of Σ that decays into each lepton flavour, $b_\alpha = \theta_\alpha/(\theta_e + \theta_\mu + \theta_\tau)$, characterises the final state. CMS [57] considered either $b_e = b_\mu = b_\tau = 1/3$, $b_e = 1$ or $b_\mu = 1$, obtaining constraints in the range $M_\Sigma \ge 180 - 210\,\mathrm{GeV}$. The most stringent constraint comes from ATLAS [58], with $M_\Sigma \ge 325\,\mathrm{GeV}$ for $b_e = 1$ and $M_\Sigma \ge 400\,\mathrm{GeV}$ for $b_\mu = 1$. We expect a weaker bound in the case $b_\tau = 1$, that we assumed above. Other decay channels relevant for Σ searches at the LHC are discussed in ref. [55], including displaced vertexes, as Σ becomes long-living in the limit of very small mixing.

In the case of two or more lepton triplets Σ_i , the phenomenology is similar, except when the mixing between the SM leptons and the new leptons is not suppressed. As in the case of sterile neutrinos, this is possible only by severely tuning the Yukawa couplings of the various Σ_i to keep m_{ν} small. In the case of two triplets, the neutrino mass matrix is diagonalised as in eq. (4.3), while the charge lepton mass matrix can be written as $M_e = U_L diag(m_{\tau}, M_{\Sigma_1}, M_{\Sigma_2}) U_R^{\dagger}$. Neglecting m_{ν} and m_{τ} , the left-hand mixing matrix U_L coincides with the neutrino mixing matrix up to a $\sqrt{2}$ factor: $(U_L)_{13} \simeq \sqrt{2}\theta$, $(U_L)_{12} \simeq i\sqrt{2}\theta/\sqrt{r_h}$ and $|(U_L)_{11}|^2 \simeq 1 - 2\theta^2(1 + r_h)/r_h$, with $r_h = M_{\Sigma_1}/M_{\Sigma_2}$, while the mixing angles in U_R are further suppressed by m_{τ}/M_{Σ_i} . When θ is large, the corrections to S and T may become significant as already discussed for sterile neutrinos. In addition, the new charged leptons, that are necessarily above the EW scale, could contribute significantly to $h \to \gamma\gamma, \gamma Z$. Before computing these corrections, one should notice that a strong upper bound on the mixing comes from the Z coupling to $\tau^+\tau^-$. The LEP measurement of $\Gamma(Z \to \tau^+\tau^-)$ [3] implies $2\theta^2(1+r_h)/r_h \lesssim 0.004$ at 3σ .

Let us describe in some detail the main corrections to $R_{\gamma\gamma}$ and $R_{\gamma Z}$, defined by eq. (B.41). Similar analytic approximations could be used for the models analysed in the next sections as well. For the diphoton channel, using the results of appendix B.2.2 one finds

$$R_{\gamma\gamma} \simeq \frac{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} + (|(U_L)_{11}|^2 - 1)A_{1/2}(\tau_{\tau}) + |(U_L)_{12}|^2 A_{1/2}(\tau_{\Sigma_1}) + |(U_L)_{13}|^2 A_{1/2}(\tau_{\Sigma_2}) \right|^2}{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} + 2\theta^2 \frac{1 + r_h}{r_h} A_{1/2}(\tau_{\Sigma_k}) \right|^2} \simeq 1 - 4\theta^2 \frac{1 + r_h}{r_h} \frac{A_{1/2}(\tau_{\Sigma_k})}{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} \right|^2} \gtrsim 0.998, \tag{4.7}$$

where we took the maximal allowed values for the mixing angle and the form factor, $A_{1/2}(\tau_{\Sigma_k}) \simeq 1.5$ for $M_{\Sigma_k} \simeq 100\,\mathrm{GeV}$. Note that $R_{\gamma\gamma} \simeq \mu_{\gamma\gamma}$, because the Higgs production rate and the total Higgs width are not significantly modified with respect to the SM. Thus the diphoton signal strength can be slightly reduced (the fermionic part of the amplitude slightly increases and interferes destructively with the W-loops), but only at a few permil level. For the γZ channel the new physics contribution can be written as $\mathcal{A}_{\mathrm{new}}^{\gamma Z} = \mathcal{A}_{\Sigma,diag}^{\gamma Z} + \mathcal{A}_{\Sigma,off-diag}^{\gamma Z}$. Using the results of appendix B.2.3, the loops involving a single mass eigenstate give

$$\mathcal{A}_{\Sigma, \text{ diag}}^{\gamma Z} \simeq \left[\left(|(U_L)_{11}|^2 - 1 \right) \frac{1 - 4s_w^2}{4c_w^2} A_{1/2}(\tau_\tau, \lambda_\tau) + \left| (U_L)_{12} \right|^2 A_{1/2}(\tau_{\Sigma_1}, \lambda_{\Sigma_1}) + \left| (U_L)_{13} \right|^2 A_{1/2}(\tau_{\Sigma_2}, \lambda_{\Sigma_2}) \right], \tag{4.8}$$

where we took the Z couplings to the interaction eigenstates, thus neglecting corrections of higher order in the small mixing. The loops involving two mass eigenstates give

$$\mathcal{A}_{\Sigma, \text{ off-diag}}^{\gamma Z} \simeq -\sum_{k=2,3} \frac{|(U_L)_{11}|^2 |(U_L)_{1k}|^2}{4c_w^2} \times \left[\frac{M_{\Sigma_k} + m_{\tau}}{\sqrt{m_{\tau} M_{\Sigma_k}}} A_{1/2}(\tau_{\tau}, \lambda_{\tau}, \tau_{\Sigma_k}, \lambda_{\Sigma_k}) - i \frac{M_{\Sigma_k} - m_{\tau}}{\sqrt{m_{\tau} M_{\Sigma_k}}} B_{1/2}(\tau_{\tau}, \lambda_{\tau}, \tau_{\Sigma_k}, \lambda_{\Sigma_k}) \right].$$

$$(4.9)$$

Retaining only terms of order θ^2 and neglecting m_{τ}/M_{Σ_k} , the rate relative to the SM can be written as

$$R_{\gamma Z} \simeq 1 - 4\theta^2 \frac{1 + r_h}{r_h} \frac{A_{1/2}(\tau_{\Sigma_k}, \lambda_{\Sigma_k}) - \frac{1}{4c_w^2} \sqrt{\frac{M_{\Sigma_k}}{m_\tau}} A_{1/2}(\tau_\tau, \lambda_\tau, \tau_{\Sigma_k}, \lambda_{\Sigma_k})}{\left| \mathcal{A}_{\text{SM}}^{\gamma Z} \right|} . \tag{4.10}$$

We neglected the $B_{1/2}$ term, as it interferes only with the very small imaginary part of the SM amplitude. The diagonal and off-diagonal form factors have comparable size, $A_{1/2}(\tau_{\Sigma_k}, \lambda_{\Sigma_k}) \simeq 1.3$ and $\sqrt{M_{\Sigma_k}/m_{\tau}}A_{1/2}(\tau_{\tau}, \lambda_{\tau}, \tau_{\Sigma_k}, \lambda_{\Sigma_k}) \simeq 1$, where we took the large M_{Σ_k} limit. Replacing the maximal allowed value for the mixing, we find $R_{\gamma Z} \gtrsim 0.998$, with a suppression at the few permil level, of the same order as for $R_{\gamma\gamma}$.

Finally, let us note that, with two or more sterile neutrinos N_i (or triplets Σ_i) the CP symmetry can be broken. In general, the Higgs couplings to the fermion mass eigenstates are not real, and the off-diagonal couplings of the Z-boson can be complex as well. This does not modify any of the above results, because the CP violating effects vanish in the limit $m_{\nu_l}/m_{\nu_{hk}} \to 0$ (and $m_{\tau}/m_{\Sigma_k} \to 0$ in the triplet case), therefore they are subleading.

4.2 One vector-like lepton

Let us consider the addition to the SM of one vector-like lepton (VLL). The four different possibilities are a weak singlet E, a weak doublet L or Λ , a weak triplet Δ , whose charges are displayed in table 1. As usual, we restrict ourself to mixing with the third SM family, i.e. with τ and ν_{τ} . The SM Lagrangian is extended by

$$-\mathcal{L}_{\psi} = \lambda_{\psi} \overline{l_L} H \psi_R + M_{\psi} \overline{\psi_L} \psi_R + h.c., \qquad \psi = E, \Delta, \qquad (4.11)$$

$$-\mathcal{L}_{\psi} = \lambda_{\psi} \overline{\psi_L} H(\tilde{H}) \tau_R + M_{\psi} \overline{\psi_L} \psi_R + h.c., \qquad \psi = L(\Lambda), \qquad (4.12)$$

where the $SU(2)_w$ contractions are understood (see appendix B.1 for details). In the case of E(L) one could write an additional mass term $m_E \overline{E_L} \tau_R$ ($m_L \overline{l_L} L_R$), but such term can be removed by choosing conveniently the basis for the two fields E_R and τ_R (l_L and l_L), that have identical charges. Thus, in each case there are only two real parameters: the vector-like mass M_{ψ} and the Yukawa coupling λ_{ψ} ; the mixing among the new leptons and the SM ones vanishes for vanishing λ_{ψ} . There is no CP violation.

The components of each multiplet ψ are listed in eq. (2.5). The doubly-charged component F does not mix as there is no SM counterpart with Q=2, therefore $m_F^2=M_\psi^2$. The Q=1 component E mixes with the SM τ to form the two physical mass eigenstates τ' and τ . The mass matrix is given by

$$\mathcal{M}_{e} = \begin{pmatrix} \lambda_{\tau} \frac{v}{\sqrt{2}} & \kappa_{\psi} \lambda_{\psi} \frac{v}{\sqrt{2}} \\ 0 & M_{\psi} \end{pmatrix}, \quad \psi = E, \Delta, \quad \mathcal{M}_{e} = \begin{pmatrix} \lambda_{\tau} \frac{v}{\sqrt{2}} & 0 \\ \kappa_{\psi} \lambda_{\psi} \frac{v}{\sqrt{2}} & M_{\psi} \end{pmatrix}, \quad \psi = L, \Lambda. \quad (4.13)$$

The $SU(2)_w$ Clebsch-Gordan coefficient κ_{ψ} is equal to one, except in the triplet case, $\kappa_{\Delta} = \sqrt{1/3}$. The rotation to the mass basis can be parametrized as

$$\mathcal{M}_e = V_L \begin{pmatrix} m_\tau & 0 \\ 0 & m_{\tau'} \end{pmatrix} V_R^T, \quad V_{L,R} = \begin{pmatrix} c_{L,R} & s_{L,R} \\ -s_{L,R} & c_{L,R} \end{pmatrix} . \tag{4.14}$$

The triangular mass matrix structure of eq. (4.13) implies some strict relations among the mixing angles and the mass eigenvalues. For the case of L and Λ , one finds

$$\tan \theta_L = \frac{m_\tau}{m_{\tau'}} \tan \theta_R \ll \tan \theta_R , \quad s_L = \frac{m_\tau}{M_\psi} s_R , \quad c_L = \frac{m_{\tau'}}{M_\psi} c_R . \tag{4.15}$$

For the case of E and Δ , the same relations hold with $L \leftrightarrow R$. Note that direct searches of charged leptons at LEP [56] require $m_{\tau'} \gtrsim 100\,\mathrm{GeV}$, therefore one angle is at least two orders of magnitude smaller than the other. In the following we will refer only to the dominant mixing angle θ_{ψ} for each ψ , dropping the subscript L, R on (co)sines. Note that

 $m_{\tau'}^2 \simeq M_\psi^2/c_\psi^2 \ge M_\psi^2$. The neutral component N does not mix with the SM neutrino ν_τ in the case of L. In the case of Δ there is mixing in the neutral sector, described by

$$\mathcal{M}_{\nu} = \begin{pmatrix} \sqrt{\frac{1}{3}} \lambda_{\Delta} v \\ M_{\Delta} \end{pmatrix} = U_L \begin{pmatrix} 0 \\ m_{\nu'} \end{pmatrix}, \quad U_L = \begin{pmatrix} \widetilde{c} & \widetilde{s} \\ -\widetilde{s} & \widetilde{c} \end{pmatrix}, \tag{4.16}$$

with $\tilde{s}^2 \simeq 2s_{\Delta}^2/(1+s_{\Delta}^2) \geq s_{\Delta}^2$. One neutrino remains massless, while the second acquires a mass $m_{\nu'}^2 \simeq (1+s_{\Delta}^2)m_{\tau'}^2 \geq m_{\tau'}^2$. In summary, the tree-level spectrum of heavy leptons satisfies

$$M_E \le m_{\tau'}$$
 $(\psi = E)$, $m_F = M_\Delta \le m_{\tau'} \le m_{\nu'}$ $(\psi = \Delta)$,
 $m_{\nu'} = M_L \le m_{\tau'}$ $(\psi = L)$, $m_F = M_\Lambda \le m_{\tau'}$ $(\psi = \Lambda)$. (4.17)

with the mass splitting controlled by the mixing, $\Delta m^2(\psi) \sim s_{\psi}^2 M_{\psi}^2$.

Let us briefly discuss the collider bounds on M_{ψ} . In first approximation one can neglect the mass splitting. It is possible to recast some LHC multi-lepton searches to put bounds on VLLs. The limits on M_{ψ} strongly depend on the SM generation that couples to the heavy leptons. For couplings only to the third one and for the doublet L, ref. [59] reports $M_L \gtrsim 280 \, \text{GeV}$, while the LEP limit remains more constraining in the case of the singlet $E, M_E \gtrsim 100 \, \text{GeV}$. For the exotic doublet Λ with a doubly-charged component, ref. [60] reports $M_{\Lambda} \gtrsim 320 \, \text{GeV}$. To the best of our knowledge, no similar analysis is available for the triplet Δ . We expect a bound comparable or slightly stronger than to the one for Λ . These bounds only apply for promptly decaying particles. We will only consider this possibility, because heavy leptons become long-lived $(c\tau \gtrsim 1m)$ for a tiny mixing $s_{\psi} \simeq 10^{-8} - 10^{-9}$, and the mixing suppresses all the deviations from the SM that we are interested in. More details on the collider phenomenology of Λ and Δ can be found in refs. [61] and [62, 63], respectively.

It is mandatory to require that the Yukawa coupling λ_{ψ} lies in the perturbative regime, $|\lambda_{\psi}| \ll 4\pi$. This consistency requirement translates into an upper bound on the product of the heavy lepton mass and the mixing angle,

$$|\lambda_{\psi}| \simeq \left| \frac{\sqrt{2}}{\kappa_{\psi}} \frac{m_{\tau'}}{v} s_{\psi} \right| \ll 4\pi \ .$$
 (4.18)

The perturbativity constraint on the SM Yukawa coupling λ_{τ} is satisfied a fortiori. The non-zero couplings of the physical Higgs boson to the charged mass eigenstates, using the convention of eq. (B.5), are given by

$$y_{\tau\tau} = c_{\psi}^2 \frac{m_{\tau}}{v}, \quad y_{\tau'\tau'} = s_{\psi}^2 \frac{m_{\tau'}}{v}, \quad y_{\tau\tau'} = c_{\psi} s_{\psi} \frac{m_{\tau} + m_{\tau'}}{2v}, \quad \widetilde{y}_{\tau\tau'} = \pm c_{\psi} s_{\psi} \frac{m_{\tau'} - m_{\tau}}{2vi}.$$
 (4.19)

where the plus (minus) sign holds in the case of E and Δ (L and Λ). In the case of Δ , there are also non-zero couplings to neutral leptons,

$$y_{\nu'\nu'} = \widetilde{s}^2 \frac{m_{\nu'}}{v}, \quad y_{\nu\nu'} = \widetilde{c}\widetilde{s}\frac{m_{\nu'}}{2v}, \quad \widetilde{y}_{\nu\nu'} = \widetilde{c}\widetilde{s}\frac{m_{\nu'}}{2vi}.$$
 (4.20)

Important constraints come from the Z-decays into SM leptons. The couplings of the fermion mass eigenstates to the Z are defined in eq. (A.6). The couplings to the SM leptons τ_L , $\nu_{\tau L}$ and τ_R are modified if they mix with new leptons with a different weak isospin T_3 . Neglecting (m_{τ}/m_Z) -corrections, at tree level one finds

$$R(Z \to \tau^+ \tau^-) \simeq \frac{(g_{\tau\tau}^V)^2 + (g_{\tau\tau}^A)^2}{(g_{\tau\tau}^{V,SM})^2 + (g_{\tau\tau}^{A,SM})^2},$$
 (4.21)

where $g_{\tau\tau}^{V,A}$ receive a correction of order s_{ψ}^2 with respect to the SM. The experimentally allowed range given in eq. (A.29) implies an upper bound on the mixing angle, for any VLL: we find $s_{E,\Delta} \lesssim 6.0 \cdot 10^{-2}$ and $s_{L,\Lambda} \lesssim 6.7 \cdot 10^{-2}$. In addition, in the case of Δ there is a correction to the Z-coupling to neutrinos, and thus to the Z-invisible width,

$$R(Z \to inv) \simeq \frac{2}{3} + \frac{1}{3} \frac{(g_{\nu\nu}^V)^2 + (g_{\nu\nu}^A)^2}{(g_{\nu\nu}^{V,SM})^2 + (g_{\nu\nu}^{A,SM})^2}$$
 (4.22)

The couplings $g_{\nu\nu}^{V,A}$ receive a correction of order \tilde{s}^2 , that leads to a comparable limit $s_{\Delta} \lesssim 8.2 \cdot 10^{-2}$. Extracting the couplings of W_{μ}^{\pm} , W_{μ}^{3} and B_{μ} from eq. (A.4), one can calculate the S and T parameters with the general formulas in appendix A.2. We find, at leading order in the mixing angle,

$$T \simeq \frac{1}{16\pi c_w^2 s_w^2} s_\psi^4 \left(a_\psi^T \frac{m_{\tau'}^2}{m_Z^2} \right) , \qquad S \simeq \frac{1}{6\pi} s_\psi^2 \left(a_\psi^S + b_\psi^S \log \frac{m_{\tau'}^2}{m_Z^2} \right)$$
 (4.23)

where a_{ψ}^T , a_{ψ}^S and b_{ψ}^S are numerical coefficients of order one. Taking into account the upper bound $s_{\psi} \lesssim 0.06$ from $Z \to \tau^+\tau^-$, as well as the perturbativity bound from eq. (4.18), $(m_{\tau'}/m_Z)s_{\psi} \lesssim 10$, we checked that S and T always lie in the allowed ellipse of figure 10.

Coming to the Higgs boson signals, we first recall that all the dominant Higgs production channels at the LHC are not affected by the new leptons, as they leave the Higgs couplings to gluons and quarks unchanged. The total Higgs width also receives negligible corrections, as new leptons affect only the partial widths $\Gamma(h \to \alpha)$, for $\alpha = \tau^+ \tau^-, \gamma \gamma, \gamma Z$. Therefore the Higgs signal is given by the ratio of partial widths in the model w.r.t. the SM, $\mu_{\alpha} \simeq R_{\alpha}$. The tree-level Higgs decays are directly controlled by the couplings in eq. (4.19) and eq. (4.20), in particular

$$R_{\tau\tau} = (1 - s_{\psi}^2)^2 \gtrsim 0.99$$
, (4.24)

where we used the bound from $Z \to \tau^+\tau^-$. There is also the marginal possibility that the new leptons are lighter than the Higgs boson, thus opening the channels $h \to \tau\tau'$ and $h \to \nu\nu'$. However, direct searches seem to allow the singlet E only to be sufficiently light. Using equation (B.7) and neglecting $m_{\tau}/m_{\tau'}$, we find

$$\Gamma(h \to \tau^+ \tau'^-) \simeq \frac{c_E^2 s_E^2 m_{\tau'}^2}{16\pi v^2} m_h \left(1 - \frac{m_{\tau'}^2}{m_h^2}\right)^2 \lesssim 0.2 \text{ MeV} .$$
 (4.25)

Note that both the couplings $y_{\tau\tau'}$ and $\tilde{y}_{\tau\tau'}$ contribute equally to the decay width, see eq. (4.19). We maximised the product $s_E^2 m_{\tau'}^2$ by taking $s_E = 6 \cdot 10^{-2}$ and $m_{\tau'} = 100 \,\text{GeV}$.

As the SM total Higgs width is $\Gamma_h \simeq 4.1\,\mathrm{MeV}$, an enhancement of order 5% may be possible. Note that experimental searches at the LHC concentrated on $h \to \tau\tau$ [64, 65], $\tau\mu$ [66, 67] and $\mu\mu$ [68, 69]. These channels are suppressed due to the small masses of the SM leptons, in contrast with the Higgs decays into a SM lepton plus a heavy lepton. It would be interesting to perform a dedicated search for this channel.

For the photon-photon channel we find

$$R_{\gamma\gamma} = \frac{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} + s_{\psi}^{2} \left[A_{1/2}(\tau_{\tau'}) - A_{1/2}(\tau_{\tau}) \right] \right|^{2}}{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} \right|^{2}} \simeq 1 - 2s_{\psi}^{2} \frac{A_{1/2}(\tau_{\tau'})}{\left| \mathcal{A}_{\rm SM}^{\gamma\gamma} \right|}, \tag{4.26}$$

where the form factors are defined in appendix B.2.2. The addition of a VLL amounts to an additional τ' -loop and a modified τ -loop, that interfere destructively with the W-loops. Maximising the mixing and choosing $m_{\tau'}=100\,\mathrm{GeV}$ (the form factor decreases for larger masses), we find $\delta R_{\gamma\gamma}\simeq -1.9\cdot 10^{-3}$, a permil reduction of the signal strength. For the γZ channel the relevant Z couplings, $g_{\tau\tau,\tau\tau',\tau'\tau'}^{V,A}$, receive corrections of order s_{ψ}^2 relatively to their unmixed values, as follows from eq. (A.6). At leading order in the small mixing and neglecting m_{τ} , we find

$$R_{\gamma Z} \simeq 1 + 2s_{\psi}^{2} \frac{\left(T_{E,\psi}^{3} + s_{w}^{2}\right) A_{1/2}(\tau_{\tau'}, \lambda_{\tau'}) \pm \frac{1}{4} \sqrt{\frac{m_{\tau'}}{m_{\tau}}} A_{1/2}(\tau_{\tau}, \lambda_{\tau}, \tau_{\tau'}, \lambda_{\tau'})}{c_{w}^{2} \left|\mathcal{A}_{SM}^{\gamma Z}\right|}, \qquad (4.27)$$

where $T_{E,\psi}^3$ is the isospin of the Q=-1 component of the multiplet ψ , and the plus (minus) sign in front of the off-diagonal term corresponds to the case $\psi=L$ ($\psi=E,\Lambda,\Delta$). As a consequence, the diagonal and off-diagonal terms always interfere destructively. The relative magnitude of the form factors is given below eq. (4.10). The size of the correction change depending on the VLL under consideration, but it is always very small. The maximal deviation is obtained for Λ , with $\delta R_{\gamma Z} \simeq 1.3 \cdot 10^{-3}$.

4.3 Two vector-like leptons (including τ compositeness)

Let us consider a SM extension by two VLLs. They may couple to each other by a Yukawa interaction or not.

• Two VLLs not coupled to each other. In this case, each VLL must be a consistent extension of the SM by itself, therefore it should have the quantum numbers of E, L, Λ or Δ , that are displayed in table 1. The six possible pairs of VLLs decoupled from each other are $(\psi, \psi') = (E, E'), (L, L'), (\Lambda, \Lambda'), (\Delta, \Delta'), (E, \Delta)$ and (L, Λ) . In the first four cases the additional mass term $\psi\psi'$ can be rotated away without loss of generality. The phenomenological effects are a trivial sum of those discussed in section 4.2 for a single VLL, with one noticeable exception.

When L and Λ have the same Yukawa coupling to the SM and the same mass, the Lagrangian

$$-\mathcal{L}_{L,\Lambda} = \frac{\lambda_{\psi}}{\sqrt{2}} \left(\overline{L_L} \ \overline{\Lambda_L} \right) \begin{pmatrix} H \\ \tilde{H} \end{pmatrix} \tau_R + M_{\psi} \left(\overline{L_L} \ \overline{\Lambda_L} \right) \begin{pmatrix} L_R \\ \Lambda_R \end{pmatrix} + h.c. \tag{4.28}$$

preserves a global $SU(2)_L \times SU(2)_R$ symmetry. In this custodial limit the corrections to the T parameter vanish, and those to the coupling $Z\tau_R\tau_R$ vanish as well [70]. This is the smallest set of tau custodians [71, 72]. A linear combination of the charge-one components of L and Λ , $\tau'' \equiv (E^{(L)} - E^{(\Lambda)})/\sqrt{2}$, does not mix. The orthogonal combination, $E \equiv (E^{(L)} + E^{(\Lambda)})/\sqrt{2}$, mixes with the SM exactly as shown in eqs. (4.13)–(4.15), to form the mass eigenstates τ' and τ . The spectrum reads $m_{\tau''} = m_N = m_F = M_\psi \leq m_{\tau'} \simeq M_\psi/c_R$. As discussed in section 4.2, direct searches already require all these states to be heavier than the Higgs boson. Thanks to the custodial symmetry, the Z couplings to leptons do not constrain the right-handed mixing s_R between τ and τ' : one has $\delta g_{\tau\tau}^R = 0$ and $\delta g_{\tau\tau}^L = s_L^2/2 = (m_\tau/M_\psi)^2 s_R^2/2$, that is negligibly small. The $Z\nu\bar{\nu}$ coupling is SM-like as well. The T parameter is almost SM-like as no additional sources of custodial breaking are introduced, and the correction to the S parameter is within the experimental range.

The most stringent constraint on s_R comes from $R_{\tau\tau} \simeq (1 - s_R^2)^2$. Using the 3σ lower bound $R_{\tau\tau} \gtrsim 0.2$ (see table 4), one finds $s_R \lesssim 0.7$. Indeed, the mixing can be large and reduce significantly the $h\tau\tau$ coupling. As a consequence, the total Higgs width may be slightly reduced and, correspondingly, the signal strength for the other Higgs decay channels, defined in eq. (B.40), may augment by a factor $\Gamma_h^{\rm SM}/\Gamma_h \lesssim 1.04$. The deviation in the $\gamma\gamma$ channel has the same form as in eq. (4.26): imposing the constraint from $h \to \tau\tau$, one finds a lower bound $\mu_{\gamma\gamma} \gtrsim 0.86$, that is close to the present experimental sensitivity. Coming to the γZ channel, the loop involving both τ and τ' vanishes when one neglects the tiny left-handed mixing s_L , because the custodial symmetry imposes $g_{\tau\tau'}^R = 0$. Then, eq. (4.27) reduces to

$$R_{\gamma Z} \simeq 1 + 2s_R^2 \tan^2 \theta_w \frac{A_{1/2}(\tau_{\tau'}, \lambda_{\tau'})}{|\mathcal{A}_{SM}^{\gamma Z}|},$$
 (4.29)

with a maximal correction $\delta \mu_{\gamma Z} \simeq 0.12$. In the near future the increasing experimental precision on $\mu_{\tau\tau}$ can further constrain or eventually determine the mixing parameter s_R in this custodial limit.

• Two VLLs coupled to each other, not mixing with the SM fermions. Next, we have to discuss the case of two VLLs coupled through a Yukawa interaction. The most general assignment for their four chiral components is

$$\psi_{1L}, \psi_{1R} \sim (1, R_w, Y), \qquad \psi_{2L}, \psi_{2R} \sim \left(1, R_w + 1, Y + \frac{1}{2}\right),$$
 (4.30)

with the Lagrangian

$$-\mathcal{L}_{\psi_1\psi_2} = \lambda_{12}\overline{\psi_{1L}}\tilde{H}\psi_{2R} + \lambda_{21}\overline{\psi_{2L}}H\psi_{1R} + M_1\overline{\psi_{1L}}\psi_{1R} + M_2\overline{\psi_{2L}}\psi_{2R} + h.c. . \qquad (4.31)$$

The four phases of λ_{12} , λ_{21} , M_1 and M_2 cannot be all rotated away: one phase is physical and allows for CP violation. In the special case Y = 0 (Y + 1/2 = 0) and R_w odd (even), one should add Majorana mass terms for $\psi_{1L,R}$ $(\psi_{2L,R})$: we postpone to section 4.4 the discussion of sets formed by one VLL plus Majorana leptons. For a few other values of R_w and Y, displayed in eq. (4.41), interaction terms between $\psi_{1,2}$ and the SM leptons are

allowed and should be added to the Lagrangian. We discuss first the no-mixing case and postpone to the end of this section the discussion of the mixing with the SM. In the absence of mixing, the lightest new lepton ψ_{light} is stable, at least at the renormalizable level. If Y is an integer multiple of 1/2, ψ_{light} may decay into a SM lepton through some higher dimensional operator. For all other values of Y, this state is absolutely stable and it has non-zero electric charge. Collider searches put a lower bound on the mass of stable heavy leptons as a function of their charge Q, see the discussion in section 3 and the limits in table 2. The effect of the set of fermions in eq. (4.30) on $h \to \gamma \gamma$ was studied e.g. in ref. [73].

Let us begin by analysing the case $R_w = 1$. There is one state with Q = Y + 1 and mass M_2 , and two states with Q = Y that mix, with mass matrix

$$\mathcal{M}_Y = \begin{pmatrix} M_1 & m_{12} \\ m_{21} & M_2 \end{pmatrix}, \qquad m_{12} = \frac{\lambda_{12}v}{\sqrt{2}}, \quad m_{21} = \frac{\lambda_{21}v}{\sqrt{2}}.$$
 (4.32)

As \mathcal{M}_Y is the most general 2×2 matrix, it is useful to parametrize it in terms of the five physical parameters,

$$\mathcal{M}_Y = U_L \begin{pmatrix} m_1 & 0 \\ 0 & m_2 \end{pmatrix} U_R^{\dagger}, \quad U_L = \begin{pmatrix} c_L & s_L \\ -s_L & c_L \end{pmatrix} \begin{pmatrix} e^{i\varphi} & 0 \\ 0 & 1 \end{pmatrix}, \quad U_R = \begin{pmatrix} c_R & s_R \\ -s_R & c_R \end{pmatrix}, \quad (4.33)$$

where $m_{1,2}$ are the real and positive masses of the eigenstates $f_{1,2}$, the mixing angles θ_L and θ_R vary between 0 and $\pi/2$, and the CP violating phase φ varies between 0 and 2π . The only restriction comes from the perturbativity of the Yukawa couplings,

$$|\lambda_{12}| = \frac{\sqrt{2}|m_2 s_L c_R - m_1 e^{i\varphi} c_L s_R|}{v} \ll 4\pi, \quad |\lambda_{21}| = \frac{\sqrt{2}|m_2 c_L s_R - m_1 e^{i\varphi} s_L c_R|}{v} \ll 4\pi. \quad (4.34)$$

These relations imply e.g. an upper bound on the masses for fixed values of the mixing angles. Vice versa, as the masses become larger and larger, the mixing angles vanish and the new fermions decouple from the EW scale.

The Higgs boson couplings to $f_{1,2}$ are directly obtained from eq. (B.5). Taking for illustration the limit where f_1 and f_2 are mass-degenerate, one has $|M_1| = |M_2| \equiv M$, $|m_{12}| = |m_{21}| \equiv \mu$ and $m_1 = m_2 = \sqrt{M^2 + \mu^2} \equiv m_{\psi}$. In this case the contribution to the amplitude for $h \to \gamma \gamma$ is

$$\mathcal{A}_{f_{1},f_{2}}^{\gamma\gamma} = 2Q^{2}F\left(\theta_{L},\theta_{R},\varphi\right)A_{1/2}\left(\tau_{\psi}\right), \quad F\left(\theta_{L},\theta_{R},\varphi\right) = s_{L}^{2}c_{R}^{2} + c_{L}^{2}s_{R}^{2} - 2c_{L}s_{L}c_{R}s_{R}\cos\varphi \ . \tag{4.35}$$

The CP-odd contribution vanishes because $\tilde{y}_{11} = -\tilde{y}_{22}$ in the degenerate limit. The perturbativity conditions in eq. (4.34) reduce to $F(\theta_L, \theta_R, \pi) \ll 8\pi^2 v^2/m_{\psi}^2$. The interference with the SM is destructive as $\mathcal{A}_{f_1, f_2}^{\gamma\gamma} \geq 0$. There are two allowed regions of parameters:

- (i) A SM-like region for small Q: the smallness of the charge ensures a small, negative departure from the SM.
- (ii) A cancellation region at large Q: for $Q^2 \simeq 4.8/F(\theta_L, \theta_R, \varphi)$, the rate is accidentally close to the SM as $\mathcal{A}_{f_1, f_2}^{\gamma\gamma} \simeq -2\mathcal{A}_{\mathrm{SM}}^{\gamma\gamma}$.

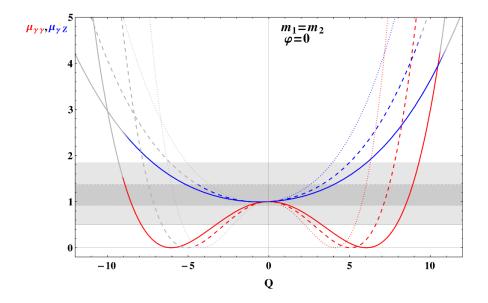


Figure 1. Signal strengths $\mu_{\gamma\gamma}$ (red) and $\mu_{\gamma Z}$ (blue) in the case of two VLLs $\psi_1 \sim (1,1,Q)$ and $\psi_2 \sim (1,2,Q+1/2)$, as a function of Q. We chose the following mass matrix parameters, defined by eq. (4.33): $m_1 = m_2 = 800 \,\text{GeV}$, $\varphi = 0$, and three values for the relevant mixing angle, $\theta_L - \theta_R = \pi/8$ (dotted), $\pi/10$ (dashed), $\pi/12$ (solid). The grey parts of the curves are excluded by S and T, see eq. (4.36). The shaded horizontal band is the presently allowed range for $\mu_{\gamma\gamma}$ at 1σ (dark) and 3σ (light).

This behaviour is illustrated in figure 1 for the CP conserving case $\varphi = 0$, where $F(\theta_L, \theta_R, 0) = \sin^2(\theta_L - \theta_R)$. Indeed the amplitude grows from $\varphi = 0$ to $\varphi = \pi$, as $F(\theta_L, \theta_R, \pi) = \sin^2(\theta_L + \theta_R)$. Further constraints on the parameters come from the EW precision tests. In the limit $m_{\psi} \gg m_Z$ we find

$$S \simeq \frac{1}{6\pi} \left[F(\theta_L, \theta_R, \varphi) + 4\left(Q + \frac{1}{2}\right) \ln \frac{m_{\psi}^2}{M^2} \right],$$

$$T \simeq \frac{1}{8\pi s_w^2 c_w^2 m_Z^2} \left[m_{\psi}^2 - 3M^2 + \frac{2M^4}{m_{\psi}^2 - M^2} \ln \frac{m_{\psi}^2}{M^2} \right],$$
(4.36)

where M is the mass of the unmixed state with Q = Y + 1. Therefore, for fixed values of the mixing parameters, S and T constrain the charge Q, as illustrated in figure 1.

It is interesting to analyse the value of $\mu_{\gamma Z}$ in the allowed space of parameters. Using eqs. (A.6) and (B.31), the CP-even amplitude for $h \to \gamma Z$ is given by

$$\mathcal{A}_{f1,f2}^{\gamma Z} = \frac{Q}{c_w^2} F\left(\theta_L, \theta_R, \varphi\right) \left(g_{11}^V + g_{22}^V\right) A_{1/2} \left(\tau_\psi, \lambda_\psi\right) , \quad g_{11}^V + g_{22}^V = -\frac{1}{2} - 2Qs_w^2 . \quad (4.37)$$

Note that the loops involving both f_1 and f_2 vanish as they are proportional to the Higgs coupling y_{12} , or to the form factor $B_{1/2}$ defined in eq. (B.39), and they both vanish for $m_1 = m_2$. As the SM amplitude is negative, the new contribution interferes constructively as long as $Q(1 + 4s_w^2 Q) > 0$. The CP-odd amplitude $\tilde{\mathcal{A}}_{f_1,f_2}^{\gamma Z}$ is also non zero, because

 $g_{11}^V \neq g_{22}^V$, and it can be sizeable for large values of $\sin \varphi$. Let us distinguish the two regions of parameters allowed by $\mu_{\gamma\gamma}$:

- (i) In the SM-like region at small Q, varying $(\theta_L \theta_R)$ we find $-0.01 \lesssim \delta \mu_{\gamma Z} \lesssim +0.08$.
- (ii) In the fine-tuned region at large Q we find $2.5 \lesssim \mu_{\gamma Z} \lesssim 3.2$ for $\varphi = 0$. This range slightly depends on the sign of Q, see figure 1. It is actually possible to obtain an even larger $\mu_{\gamma Z}$, while keeping $\mu_{\gamma \gamma}$ close to one. For example, taking for simplicity $s_R = 0$, the CP-odd amplitude reads

$$\tilde{\mathcal{A}}_{f_1, f_2}^{\gamma Z} = -4Q^2 c_L s_L \tan^2 \theta_w \sin \varphi \, \tilde{A}_{1/2} \left(\tau_{\psi}, \lambda_{\psi} \right) . \tag{4.38}$$

For $\sin \varphi$ of order one, this contribution becomes important and one can reach $\mu_{\gamma Z} \simeq 7$.

When one allows for the two mass eigenstates $f_{1,2}$ to be non-degenerate, $m_1 < m_2$, the amplitudes for the diphoton channel become

$$\mathcal{A}_{f_{1},f_{2}}^{\gamma\gamma} \simeq 2Q^{2} \left[s_{L}^{2} c_{R}^{2} + c_{L}^{2} s_{R}^{2} - \left(\frac{m_{1}}{m_{2}} + \frac{m_{2}}{m_{1}} \right) c_{L} s_{L} c_{R} s_{R} \cos \varphi \right] A_{1/2} (\tau_{1}) ,
\tilde{\mathcal{A}}_{f_{1},f_{2}}^{\gamma\gamma} \simeq 2Q^{2} \left(\frac{m_{2}}{m_{1}} - \frac{m_{1}}{m_{2}} \right) c_{L} s_{L} c_{R} s_{R} \sin \varphi \ \tilde{A}_{1/2} (\tau_{1}) .$$
(4.39)

where we made the approximation $A_{1/2}(\tau_1) \simeq A_{1/2}(\tau_2)$, that is accurate for $4m_{1,2}^2 \gg m_h^2$. For sufficiently large mass splitting the interference of $\mathcal{A}_{f_1,f_2}^{\gamma\gamma}$ with the SM can be constructive. In the γZ channel the analytic form of the amplitude becomes more involved, in particular the loops involving both f_1 and f_2 are non-zero, and the interference with the SM strongly depends on the ratio m_1/m_2 . One can tune the parameters to cancel the corrections to $\mu_{\gamma\gamma}$ in eq. (4.39), e.g. taking $\varphi = 0$ and $m_1/m_2 = (t_L/t_R)^{\pm 1}$. For the same set of parameters large contributions to the γZ channel are possible. For example one can reach $\mu_{\gamma Z} \simeq 2$ for $\theta_L \simeq \pi/6$, $\theta_R \simeq \pi/10$, $m_1/m_2 \simeq 1.8$, $m_2 \simeq 800\,\text{GeV}$ and $Q \simeq 9$. This region is compatible with S, T and all other constraints.

A similar analysis can be performed when $R_w = 2$ or larger in eq. (4.30). In this case there are N_w pairs of mixing states, with $Q = -(N_w - 1)/2 + Y$, ..., $(N_w - 1)/2 + Y$. For each such sector, the mass matrix is

$$\mathcal{M}_Q = \begin{pmatrix} M_1 & \kappa_Q m_{12} \\ \kappa_Q m_{21} & M_2 \end{pmatrix}, \tag{4.40}$$

where $\kappa_{Q_{\alpha}}$ is the Clebsch-Gordan coefficient coming from the SU(2)_w contraction, determined by eq. (B.4), therefore each sector is controlled by the same physical parameters. In other words, the two mass eigenvalues, the two mixing angles and the CP-violating phase of a given sector determine univocally the other sectors too. The corrections to $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$ are obtained summing over the contributions of N_w sectors, each being qualitatively analog to the case $R_w = 1$ analysed above. Note that, however, one cannot take $Q \to 0$ to recover the SM limit, because there are at least two sectors with different values of Q. Of course, the SM is still recovered for small values of the mixing angles. The two fine-tuned

regions with $\mu_{\gamma\gamma} \simeq 1$ and large $\mu_{\gamma Z}$ are still possible. On the one hand, the different sectors can add up to realise $\mathcal{A}_{\text{new}}^{\gamma\gamma} \simeq -2\mathcal{A}_{\text{SM}}^{\gamma\gamma}$. On the other hand, for $R_w = 2$ we found a choice of mixing parameters such that $\mathcal{A}_{f_1,f_2}^{\gamma\gamma}$ vanishes in both the sectors with $Q = Y \pm 1/2$.

• Two VLLs coupled to each other, mixing with the SM fermions. Finally, let us discuss the possible interactions between $\psi_{1,2}$ in eq. (4.30) and the SM leptons. A non-zero mixing occurs if and only if ψ_1 and/or ψ_2 are identified with the states E, L, Λ or Δ listed in table 1. There are six such cases,

$$R_w = 1 : E + L \ (Y = -1), \quad E + \Lambda \ (Y = 1),$$

 $R_w = 2 : L + \Delta \ (Y = 1/2), \quad \Lambda + \Delta \ (Y = -3/2), \quad \Lambda + \Delta_G \ (Y = 3/2),$
 $R_w = 3 : \Delta + \Omega \ (Y = -1), \quad \Delta + \Omega_G \ (Y = 1).$ (4.41)

There are three cases with an additional weak multiplet: a triplet $\Delta_G = (E, F, G) \sim (1, 3, -2)$, and two quartets $\Omega = (E^c, N, E, F) \sim (1, 4, -1/2)$ and $\Omega_G = (N, E, F, G) \sim (1, 4, -3/2)$, with Q(G) = -3. They do not couple directly to the SM leptons. In these three cases the Q = 2 sector couples to the Higgs and therefore may contribute significantly to $h\gamma\gamma$ and $h\gamma Z$. We have shown in section 4.2 that the mixing angles between the SM leptons and E, L, Λ or Δ must be very small, due to the strong constraints coming from the $Z\tau\tau$ couplings. With two VLLs the mass matrices become larger, but we expect the phenomenology to be qualitatively the same, up to possible fine-tuned cancellations in some observable. A crucial effect of the mixing is to make the new leptons decay into SM leptons. The components with Q = 2, 3 decay more slowly, since their decay chains require a virtual exchange of other components of the multiplet. We already reviewed in section 4.2 the direct bounds on heavy leptons with charge Q = 1, 2, decaying promptly into SM leptons. We are not aware of any dedicated search for a Q = 3 heavy lepton.

A detailed analysis of the parameter space is worth only in the context of a specific, well-motivated model, and it goes beyond the scope of this paper. The case E + L is analyzed in ref. [74]. The phenomenology of a fourth vector-like family of leptons, L+E+N, is studied in detail in ref. [75]. Here we comment only on the interesting possibility to generate the τ mass entirely from the mixing with the VLLs, in the limit where the SM Yukawa coupling $\overline{l_{\tau L}}H\tau_R$ vanishes. There are various ways to induce such coupling through mixing, that are illustrated in figure 2:

- (a) In the case of E only, one can proceed through a Yukawa coupling connecting $l_{\tau L}$ to E_R , followed by two singlet vector-like mass terms.
- (b) Analogously, with L only, one employs two doublet vector-like mass terms and a Yukawa connecting L_L to τ_R .
- (c) In the case of E + L, one can employ a vector-like mass term both for the singlets and the doublets, with a Yukawa coupling involving only the new fermions. This case is particularly interesting, since it corresponds to the scenario of partial compositeness [16] in the τ sector: the SM leptons are elementary fields that mix linearly with composite VLLs, which couple in turn to a composite Higgs doublet. The SM leptons

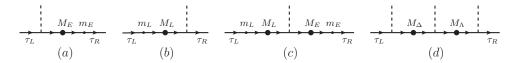


Figure 2. Different ways to generate the τ mass through mixing between the SM leptons and VLLs. The dashed lines stand for Higgs vev insertions, the small dots represent a mass mixing between a SM lepton and a VLL, and the big dots correspond to the mass of a VLL. The case (c) corresponds to the scenario of τ partial compositeness.

feel EWSB only through the mixing with heavy composite leptons. The Q=1 mass matrix and its smallest eigenvalue take the form

$$\mathcal{M}_e = \begin{pmatrix} 0 & m_L & 0 \\ 0 & M_L & \frac{\lambda_{LE}v}{\sqrt{2}} \\ m_E & \frac{\lambda_{EL}v}{\sqrt{2}} & M_E \end{pmatrix}, \qquad m_\tau \simeq \frac{m_L}{M_L} \frac{m_E}{M_E} \frac{\lambda_{LE}v}{\sqrt{2}} . \tag{4.42}$$

The mixing with the heavy leptons also controls the deviations in the Z couplings,

$$\delta g_{\tau\tau}^R \simeq \frac{1}{2} \left(\frac{m_E}{M_E}\right)^2 , \qquad \delta g_{\tau\tau}^L \simeq \frac{1}{2} \left(\frac{m_L}{M_L}\right)^2 .$$
 (4.43)

As these corrections are bounded by $R(Z \to \tau \tau)$, as shown in eq. (A.28), we find that the physical value of m_{τ} can be generated for $\lambda_{EL} \gtrsim 2.5$, pointing indeed to a strong-coupling regime. The phenomenology of τ partial compositeness is studied e.g. in ref. [76].

(d) Finally, in the case $(\psi_1, \psi_2) = (\Lambda, E)$, (L, Δ) or (Λ, Δ) , the τ mass can be induced by three Yukawa couplings, connecting $l_{\tau L}$ to ψ_2 , τ_R to ψ_1 , and ψ_1 to ψ_2 , respectively. Focusing on (Λ, Δ) for definiteness, one finds

$$m_{\tau} \simeq \frac{\lambda_{\Delta} v}{\sqrt{3} M_{\Delta}} \frac{\lambda_{\Lambda} v}{\sqrt{2} M_{\Lambda}} \frac{\lambda_{\Delta\Lambda} v}{\sqrt{6}} \simeq 2 \sqrt{\delta g_{\tau\tau}^R \delta g_{\tau\tau}^L} \frac{\lambda_{\Delta\Lambda} v}{\sqrt{6}}$$
 (4.44)

For $\lambda_{\Delta\Lambda} \gtrsim 4.5$ the physical value of m_{τ} can be generated.

4.4 Vector-like plus Majorana leptons (including higgsinos plus gauginos)

In this section we consider the interplay between Majorana leptons and VLLs, related by one or more Yukawa couplings. If there were no such couplings, the phenomenology would reduce to a trivial addition of the effects of Majorana leptons, see section 4.1, and of VLLs, see sections 4.2 and 4.3. For reference, the smallest sets of this kind are formed by three (four) chiral multiplets: (two copies of) N_R or Σ_R , plus a vector-like pair (E_L, E_R) , (Λ_L, Λ_R) or (Δ_L, Δ_R) .

• One VLL plus one Majorana lepton. The most general set formed by one Majorana lepton interacting with one VLL pair is

$$\chi_R \sim (1, R_w, 0), \qquad \psi_L, \psi_R \sim (1, R_w \pm 1, -1/2),$$
(4.45)

with $N_w \neq 2 + 4n$ to avoid the global $SU(2)_w$ anomaly. The corresponding Lagrangian is

$$-\mathcal{L}_{\chi\psi} = \frac{1}{2} M_{\chi} \overline{\chi_R^c} \chi_R + M_{\psi} \overline{\psi_L} \psi_R + \tilde{\lambda} \overline{\psi_L} \tilde{H} \chi_R + \lambda \overline{\chi_R^c} H \psi_R + h.c. . \qquad (4.46)$$

The Majorana mass M_{χ} is absent in the case of even $SU(2)_w$ representations, $N_w = 4n$: in this case there is a conserved 'new lepton' number, and all multiplet components combine into Dirac fermions. There is a unique physical complex phase, that can be associated to M_{χ} , choosing M_{ψ} , $\tilde{\lambda}$ and λ real. Each component of the new leptons has a (demi-)integer charge Q, therefore it can decay to SM leptons, either through renormalizable interactions or higher dimensional operators. For $R_w = 1$ or 3, couplings to the SM leptons can be added to the Lagrangian, as we will discuss later.

In the case $\psi \sim (R_w + 1)$, after EWSB one identifies: one pair of states with charges $Q = \pm (N_w + 1)/2$, that combine in a VLL of mass M_{ψ} ; three pairs of states with $Q = \pm (N_w - 1)/2$, $\pm (N_w - 3)/2$, ..., down to $Q = \pm 1$ ($\pm 1/2$) for N_w odd (even); when N_w is odd, three additional states with Q = 0. The 3×3 mass matrix in each sector takes the form

$$\mathcal{M}_{Q} = \begin{pmatrix} M_{\chi} & \kappa_{Q}\tilde{\lambda}v & \kappa_{-Q}\lambda v \\ \kappa_{-Q}\tilde{\lambda}v & 0 & M_{\psi} \\ \kappa_{Q}\lambda v & M_{\psi} & 0 \end{pmatrix}, \tag{4.47}$$

where we chose $Q \geq 0$ and a basis with the components of charge Q(-Q) on the left(right)-hand side of \mathcal{M}_Q . The $\mathrm{SU}(2)_w$ Clebsch-Gordan coefficients $\kappa_{\pm Q}$ are defined by eq. (B.4), and they also include for convenience the factor $1/\sqrt{2}$ from the Higgs doublet vev,

$$\kappa_{\pm Q} = \frac{1}{\sqrt{2}} \sqrt{\frac{N_w + 1 \pm 2Q}{N_w(N_w + 1)}} \ . \tag{4.48}$$

In the case $\psi \sim (R_w - 1)$, there are three pairs of states with $Q = \pm (N_w - 3)/2, \pm (N_w - 5)/2, \ldots$, and three states with Q = 0 when N_w is odd. The 3×3 mass matrix in each of these sectors has the form of eq. (4.47), but with Clebsch-Gordan coefficients given by

$$\kappa_{\pm Q} = \frac{1}{\sqrt{2}} \sqrt{\frac{N_w - 1 \mp 2Q}{N_w (N_w - 1)}} \ . \tag{4.49}$$

There are also two pairs of states with $Q = \pm (N_w - 1)/2$ and mass matrix

$$\mathcal{M}_{Q} = \begin{pmatrix} M_{\chi} & \kappa_{-Q} \lambda v \\ \kappa_{-Q} \tilde{\lambda} v & M_{\psi} \end{pmatrix} . \tag{4.50}$$

This is the same structure of eq. (4.32), that was extensively studied in section 4.3.

Note that each 3×3 or 2×2 sector depends on the same five parameters: two masses, two Yukawa couplings, and one physical phase. They determine all the mass eigenvalues and the mixing matrices. We do not attempt a scan of the parameter space here. The corrections to S, T, $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$ from a sector with the mass matrix of eq. (4.50) were analysed in section 4.3. We expect corrections of the same order from the other sectors. Coming to collider searches, for $N_w \neq 1, 3$ there is no mixing with the SM and the lightest

mass eigenstate is stable, at least at the renormalizable level. When it is charged, one can apply the limits on stable leptons reported in table 2. For N_w odd, the lightest state may be neutral, with the typical collider phenomenology of a dark matter candidate.

The phenomenology is radically different when N_w is even. In this case the Majorana mass is absent, $M_\chi=0$, and the χ components are massless before EWSB, therefore one mass eigenvalue for each sector is of the order $\lambda\tilde{\lambda}v^2/M_\psi$. This implies that all masses are bound to the EW scale, whence the situation resembles the one of purely chiral sets of new fermions. In particular, one finds a correction to $h\to\gamma\gamma$ that depends only on Q: taking $M_\chi=0$ in the mass matrix (4.47) or (4.50), and using the LET approximation of eq. (B.24), we find a CP-even amplitude $\mathcal{A}_{\chi\psi,Q}^{\gamma\gamma}\simeq 8Q^2/3$ for a 3 × 3 sector, and the same for a 2 × 2 sector. For comparison, when N_w is odd the Majorana mass is allowed and one finds

$$\mathcal{A}_{\chi\psi,Q}^{\gamma\gamma,3\times3} \simeq -\frac{8}{3} \frac{\lambda v}{M_\chi} \frac{\widetilde{\lambda} v}{M_\psi} Q^2 \left(\kappa_{-Q}^2 + \kappa_Q^2\right) \,, \qquad \mathcal{A}_{\chi\psi,Q}^{\gamma\gamma,2\times2} \simeq -\frac{8}{3} \frac{\lambda v}{M_\chi} \frac{\widetilde{\lambda} v}{M_\psi} Q^2 \kappa_{-Q}^2 \,, \tag{4.51}$$

where we made the approximation λv , $\tilde{\lambda}v \ll M_{\chi}$, M_{ψ} . The correction grows as the $\chi - \psi$ mixing parameters of the type $\lambda v/M$ increase, on the other hand S and T generally put a significant upper bound on these parameters. Obviously, in each model the total $\mathcal{A}_{\text{new}}^{\gamma\gamma}$ is the sum over all the sectors with different Q.

Let us say a few more words on the cases where χ and/or ψ mix with the SM leptons.

- N + L: for $R_w = 1$, the Majorana fermion is a sterile neutrino N, the vector-like fermion is a lepton doublet L, and the Lagrangian in eq. (4.46) is extended to include $\lambda_N \overline{l_L} \ddot{H} N_R + \lambda_L \overline{l_L} H \tau_R + h.c.$. The full parameter space includes two real masses, four reals Yukawa couplings and two physical phases, that can be associated e.g. to λ and λ . The 2×2 mass matrix in the $Q=\pm 1$ sector is given by eq. (4.13): the mixing with the SM is small due to the strong constraint from the $Z\tau\tau$ couplings, implying small deviations in $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$. The 4 × 4 mass matrix in the Q=0 sector is obtained by adding to eq. (4.47) a first row and a first column of the form $(0, \lambda_N v/\sqrt{2}, 0, 0)$. There are some simple limiting cases. If $\lambda, \tilde{\lambda} \to 0$, the matrix reduces to two diagonal blocks, as N and L decouple from each other, and the phenomenology reduces to the one of the previous sections. If $M_{L,N}/v$ are much larger than the Yukawa couplings, all the mixing angles are small and the smallness of the light neutrino mass follows from the usual seesaw mechanism, $m_{\nu} \simeq \lambda_N^2 v^2/(2M_N)$. Still, m_{ν} can be small even in the presence of large Yukawa couplings. In particular, for $\lambda v, \lambda v \sim M_{N,L}$, large mixing angles are possible, and, correspondingly, such intricate neutral sector may induce significant corrections to the S and T parameters.
- For $R_w = 3$, the Majorana fermion is the triplet Σ and the vector-like fermion is the doublet L or the quartet Ω .

 $\Sigma + L$: the Lagrangian in eq. (4.46) is extended to include $\lambda_{\Sigma} \overline{l_L} \tilde{H} \Sigma_R + \lambda_L \overline{L_L} H \tau_R + h.c.$. Up to different Clebsch-Gordan coefficients, the 4 × 4 neutral sector is the same as

in the N+L case. The mass matrix in the charged sector is

$$\mathcal{M}_{1} = \begin{pmatrix} \sqrt{\frac{1}{2}}\lambda_{\tau}v & \sqrt{\frac{1}{3}}\lambda_{\Sigma}v & 0\\ 0 & M_{\Sigma} & \sqrt{\frac{1}{3}}\lambda v\\ \sqrt{\frac{1}{2}}\lambda_{L}v & \sqrt{\frac{1}{3}}\tilde{\lambda}v & M_{L} \end{pmatrix}. \tag{4.52}$$

The $Z\tau\tau$ couplings constrain both mixing parameters $\lambda_{\Sigma}v/M_{\Sigma}$ and $\lambda_L v/M_L$ to be small, as explained in sections 4.1 and 4.2, respectively. When the mixing with the SM is neglected, one is left with a special case of eq. (4.50), which corresponds to the chargino mass matrix in supersymmetry. Note that, in the limit where λ_{τ} vanishes, there is still a contribution to the τ mass, $m_{\tau} \simeq (\lambda_{\Sigma}\lambda_L\lambda v^3)/(3\sqrt{2}M_{\Sigma}M_L)$, as illustrated in figure 2(d). Despite the constraint on the mixing from the $Z\tau\tau$ couplings, one can accommodate the correct size of m_{τ} for $\lambda \gtrsim 3$, see the discussion below eqs. (4.42) and (4.44).

 $\Sigma + \Omega$: the Lagrangian in eq. (4.46) is extended to include $\lambda_{\Sigma} \overline{l_L} \tilde{H} \Sigma_R + h.c.$, as the quartet does not mix with the SM. The 4×4 neutral sector has the same structure as in the N+L and $\Sigma + L$ cases. The Q=1 sector also has a 4×4 mass matrix, that is obtained from eq. (4.47) by adding a first row $(\lambda_\tau v/\sqrt{2}, \lambda_\Sigma/\sqrt{3}, 0, 0)$, and a first column $(\lambda_\tau v/\sqrt{2}, 0, 0, 0)$. In addition, there is a Q=2 state with mass M_Ω . There are no significant phenomenological novelties, as the effects of the SM mixing with Σ and of the Σ mixing with Ω mixing do not interfere significantly.

• One VLL plus two Majorana leptons. Let us come to sets of two Majorana leptons both interacting with one vector-like pair. One obvious possibility is to take two copies of the same Majorana lepton, that is, to replace χ_R in eq. (4.45) with χ_{iR} , i=1,2, with the obvious doubling of each coupling involving χ in the Lagrangian. Note that N_w can be arbitrary and, for even N_w , the Majorana mass terms are forbidden but a Dirac mass term $M_\chi \overline{\chi_{1R}^c} \chi_{2R}$ is allowed. In all other respects, the mass matrix structures and the inherent phenomenology are a straightforward generalisation of those discussed above.

The second and last possibility to couple two Majorana leptons to one VLL is provided by the set

$$\chi_{1R} \sim (1, R_w, 0), \qquad \psi_L, \psi_R \sim (1, R_w + 1, -1/2), \qquad \chi_{2R} \sim (1, R_w + 2, 0), \qquad (4.53)$$

with N_w necessarily odd, and Lagrangian

$$-\mathcal{L}_{\chi\psi} = M_{\psi}\overline{\psi_{L}}\psi_{R} + \sum_{i=1}^{2} \left[\frac{1}{2} M_{\chi_{i}} \overline{\chi_{iR}^{c}} \chi_{iR} + \tilde{\lambda}_{i} \overline{\psi_{L}} \tilde{H} \chi_{Ri} + \lambda_{i} \overline{\chi_{Ri}^{c}} H \psi_{R} \right] + h.c. \quad (4.54)$$

There are two pairs of states with $Q = \pm (N_w + 1)/2$, with a mass matrix given by eq. (4.50) with $M_{\chi}, \lambda, \tilde{\lambda} \to M_{\chi_2}, \lambda_2, \tilde{\lambda}_2$. In addition, there are four pairs of states with $Q = \pm (N_w - 1)/2, \pm (N_w - 3)/2, \ldots, \pm 1$, and four states with Q = 0. The 4 × 4 mass matrix in each such sector takes the form

$$\mathcal{M}_{Q} = \begin{pmatrix} M_{\chi_{1}} & 0 & \kappa_{1,Q}\tilde{\lambda}_{1}v & \kappa_{1,-Q}\lambda_{1}v \\ 0 & M_{\chi_{2}} & \kappa_{2,Q}\tilde{\lambda}_{2}v & \kappa_{2,-Q}\lambda_{2}v \\ \kappa_{1,-Q}\tilde{\lambda}_{1}v & \kappa_{2,-Q}\tilde{\lambda}_{2}v & 0 & M_{\psi} \\ \kappa_{1,Q}\lambda_{1}v & \kappa_{2,Q}\lambda_{2}v & M_{\psi} & 0 \end{pmatrix},$$
(4.55)

with $\kappa_{1,\pm Q}$ given by eq. (4.48), and $\kappa_{2,\pm Q}$ given by eq. (4.49) with $N_w \to N_w + 2$. As in eq. (4.51), one can estimate the contribution of this mass matrix to the $h\gamma\gamma$ coupling, by taking the LET approximation,

$$\mathcal{A}_{\chi_1\chi_2\psi,Q}^{\gamma\gamma,4\times4} \simeq -\frac{8}{3} \sum_{i=1,2} \frac{\lambda_i v}{M_{\chi_i}} \frac{\widetilde{\lambda_i} v}{M_{\psi}} Q^2 \left(\kappa_{i,-Q}^2 + \kappa_{i,Q}^2\right) . \tag{4.56}$$

Let us discuss the minimal cases $R_w = 1$ and $R_w = 3$, that admit a mixing with the SM leptons.

• $N + L + \Sigma$: for $R_w = 1$, the new fermions have the gauge quantum numbers of the bino, the higgsinos and the wino in supersymmetry. Thus, the mass matrices (4.50) and (4.55) are a generalisation of the chargino $(Q = \pm 1)$ and neutralino (Q = 0) mass matrices, respectively (for a review see ref. [77]). Supersymmetry restricts the Yukawa couplings to $\tilde{\lambda}_{1,2}/\lambda_{1,2} = -\tan\beta$, $\lambda_1/\lambda_2 = \tilde{\lambda}_1/\tilde{\lambda}_2 = -\tan\theta_w/\sqrt{3}$, and $\lambda_1 = -\cos\beta g'$. The effect of charginos and neutralinos on the Higgs boson couplings is analysed e.g. in refs. [78–81]. In particular, the chargino loop contributing to $h\gamma\gamma$ and $h\gamma Z$ is controlled by the weak coupling g, and it is typically subleading compared to the SM top quark loop. Without the supersymmetry constraints, the most general chargino mass matrix has the structure of eq. (4.32), therefore one can apply the results of section 4.3 for the Higgs decay amplitudes into $\gamma\gamma$ and γZ .

In the absence of (R-parity conserving) supersymmetry, not only the four Yukawa couplings $\lambda_{1,2}$ and $\tilde{\lambda}_{1,2}$ are unconstrained, but in addition a mixing with the SM leptons is allowed: one should add to the Lagrangian in eq. (4.54) the terms $\lambda_N \bar{l}_L \tilde{H} N_R + \lambda_{\Sigma} \bar{l}_L \tilde{H} \Sigma_R + \lambda_L \bar{L}_L H \tau_R + h.c.$. The $Q = \pm 1$ mass matrix becomes the one in eq. (4.52), and the Q = 0 mass matrix becomes 5×5 , and it is obtained from eq. (4.55) by adding a first row and column of the form $(0, \lambda_N v/\sqrt{2}, \lambda_{\Sigma} v/\sqrt{6}, 0, 0)$. Therefore, one can observe the phenomenological effects of N, Σ and L individually, as analysed in sections 4.1 and 4.2, as well as their interplay, already described above for (N + L) and $(\Sigma + L)$. As usual, the mixing with the SM leptons is typically constrained to be small by the smallness of m_{ν} and by the $Z\tau\tau$ couplings, thus the modifications to the $h\nu\nu$ and $h\tau\tau$ couplings are suppressed. However, even a very small mixing with the SM offers decay modes to the heavy fermions, such that none is stable. A dedicated analysis of the full parameter space would be interesting, to characterise quantitatively the correlations among the different observables, and especially the deviations from the supersymmetric limit.

• $\Sigma + \Omega + \Xi$: for $R_w = 3$, the new fermions are a Majorana triplet, a vector-like quartet, and a Majorana quintuplet Ξ . There is a 2×2 sector with $Q = \pm 2$ given by eq. (4.50). As the triplet mixes with the SM through $\lambda_{\Sigma} \overline{l_L} \tilde{H} \Sigma_R + h.c.$, there is a 5×5 sector with $Q = \pm 1$, that is obtained by adding to the matrix in eq. (4.55) a first row $(\lambda_{\tau} v/\sqrt{2}, \lambda_{\Sigma} v/\sqrt{3}, 0, 0, 0)$ and a first column $(\lambda_{\tau} v/\sqrt{2}, 0, 0, 0, 0)$. This large number of charged states with potentially large mixing can give a significant correction to $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$. For concreteness, neglecting the mixing with the SM and using the

LET approximation, we find

$$\mathcal{A}_{\Sigma\psi\Xi}^{\gamma\gamma} \simeq -\frac{8}{3} \left(\frac{1}{3} \frac{\lambda_1 v}{M_{\Sigma}} \frac{\widetilde{\lambda}_1 v}{M_{\Omega}} + \frac{\lambda_2 v}{M_{\Xi}} \frac{\widetilde{\lambda}_2 v}{M_{\Omega}} \right) , \qquad (4.57)$$

to be compared with the SM top contribution, $\mathcal{A}_t^{\gamma\gamma} \simeq 16/9$. One should take into account the constraints (in particular S and T) on the mixing parameters $\sim \lambda v/M$. The neutral sector has also a 5×5 mass matrix, obtained by adding a first column and row $(0, \lambda_{\Sigma} v/\sqrt{6}, 0, 0, 0)$ to to the matrix in eq. (4.55). As usual, the vanishing neutrino mass requires $\lambda_{\Sigma} v/M_{\Sigma}$ to be very small.

5 Phenomenology of non-chiral quarks

In this section we discuss new coloured fermions that either form vector-like pairs, or admit a Majorana mass term. We will dub them 'quarks' even when they are not in the fundamental representation of $SU(3)_c$.

5.1 One vector-like quark

There are seven possible VLQs that mix with the SM quarks, as listed in table 1. They have been extensively studied under various respects in the literature (see e.g. refs. [22, 82–87]). Here we describe in a compact, systematic way the leading order constraints coming from EW precisions tests, direct searches at colliders, and Higgs couplings. As usual we restrict ourselves to mixing with the third family. In the top (bottom) sector, a mixing appears whenever the VLQ contains a component T(B) with the same charge as t(b). The components of each multiplet are displayed in eq. (2.6). In the case of weak singlets or triplets, the SM Lagrangian is extended by

$$-\mathcal{L}_{\psi} = \lambda_{\psi} \overline{q_L} \tilde{H}(H) \psi_R + M_{\psi} \overline{\psi_L} \psi_R + h.c., \quad \text{for } \psi = T, X_Q(B, Y_Q), \quad (5.1)$$

and, in the case of weak doublets, by

$$-\mathcal{L}_{\psi} = \lambda_{\psi}^{t} \overline{\psi_{L}} \tilde{H}(H) t_{R} + \lambda_{\psi}^{b} \overline{\psi_{L}} H(\tilde{H}) b_{R} + M_{\psi} \overline{\psi_{L}} \psi_{R} + h.c., \quad \text{for } \psi = Q(X_{T}, Y_{B}), \quad (5.2)$$

with the further restriction $\lambda_{X_T}^b = \lambda_{Y_B}^t = 0$. The structure of the top (bottom) sector mass matrix is very close to the charged lepton one in the case of one VLL, therefore we will frequently refer to section 4.2. In the top sector one has

$$\mathcal{M}_{t} = \begin{pmatrix} \lambda_{t} \frac{v}{\sqrt{2}} & \kappa_{\psi}^{t} \lambda_{\psi} \frac{v}{\sqrt{2}} \\ 0 & M_{\psi} \end{pmatrix}, \quad \psi = T, X_{Q}, Y_{Q}, \quad \mathcal{M}_{t} = \begin{pmatrix} \lambda_{t} \frac{v}{\sqrt{2}} & 0 \\ \kappa_{\psi}^{t} \lambda_{\psi}^{t} \frac{v}{\sqrt{2}} & M_{\psi} \end{pmatrix}, \quad \psi = Q, X_{T}, \quad (5.3)$$

with Clebsch-Gordan coefficients $\kappa_{T,Q,X_T}^t = 1$, $\kappa_{X_Q}^t = \sqrt{1/3}$ and $\kappa_{Y_Q}^t = \sqrt{2/3}$. The rotation to the mass basis is parametrized as $\mathcal{M}_t = U_L diag(m_t, m_{t'}) U_R^{\dagger}$, in analogy with eq. (4.14). In the bottom sector one has

$$\mathcal{M}_{b} = \begin{pmatrix} \lambda_{b} \frac{v}{\sqrt{2}} & \kappa_{\psi}^{b} \lambda_{\psi} \frac{v}{\sqrt{2}} \\ 0 & M_{\psi} \end{pmatrix}, \quad \psi = B, X_{Q}, Y_{Q}, \quad \mathcal{M}_{b} = \begin{pmatrix} \lambda_{b} \frac{v}{\sqrt{2}} & 0 \\ \kappa_{\psi}^{b} \lambda_{\psi}^{b} \frac{v}{\sqrt{2}} & M_{\psi} \end{pmatrix}, \quad \psi = Q, Y_{B}, \quad (5.4)$$

with $\kappa_{B,Q,Y_B}^b = 1$, $\kappa_{X_Q}^b = \sqrt{2/3}$ and $\kappa_{Y_Q}^b = \sqrt{1/3}$, and one can write $\mathcal{M}_b = \widetilde{U}_L diag(m_b, m_{b'})\widetilde{U}_R^{\dagger}$.

In all cases except Q, the vector-like mass M_{ψ} and the three independent Yukawa couplings can be taken to be real. In the case of Q, there are four Yukawa couplings and one complex phase ϕ is physical. In full generality, one can choose $\lambda_{t,b}$ and $\lambda_Q^{t,b}$ real, and add a matrix $P_{\phi} = diag(e^{i\phi}, 1)$ on the left of \mathcal{M}_b . Then, eq. (A.4) and eq. (B.5) show that ϕ appears in the W couplings to the fermion mass eigenstates, while the Z and h couplings are independent from ϕ . It is very difficult to observe such CP-violating effect in the charged current, since it vanishes for $\lambda_b \to 0$, that is, it is always suppressed by the small ratio m_b/v . Coming to the mixing angles, the left- and right-hand ones are related as in the case of VLLs, see eq. (4.15): in the case of weak doublet VLQs one finds

$$\tan \theta_L = \frac{m_t}{m_{t'}} \tan \theta_R < \tan \theta_R, \qquad \tan \widetilde{\theta}_L = \frac{m_b}{m_{b'}} \tan \widetilde{\theta}_R \ll \tan \widetilde{\theta}_R,$$
 (5.5)

while for singlet or triplet VLQs, the same relations hold with $L \leftrightarrow R$. In the following we will drop the subscripts L, R and denote θ_{ψ} ($\tilde{\theta}_{\psi}$) the largest mixing angle in the top (bottom) sector, for any given VLQ ψ . For the multiplets with both the T and B components, the mass eigenvalues and the mixing angles in the top and bottom sectors are strictly related,

$$\begin{cases}
 m_{t'}^2 - m_{b'}^2 = s_{\psi}^2 (m_{t'}^2 - m_t^2) - \tilde{s}_{\psi}^2 (m_{b'}^2 - m_b^2) \\
 s_{\psi} c_{\psi} (m_{t'}^2 - m_t^2) r_{\psi} = \tilde{s}_{\psi} \tilde{c}_{\psi} (m_{b'}^2 - m_b^2)
\end{cases} ,$$
(5.6)

where $r_{X_Q} = \sqrt{2}$, $r_{Y_Q} = 1/\sqrt{2}$, and $r_Q \equiv \lambda_Q^b/\lambda_Q^t$. Therefore, one can determine the bottom sector parameters, $m_{b'}$ and $\tilde{\theta}_{\psi}$, as a function of the top sector one, $m_{t'}$ and θ_{ψ} , or vice versa. In the case $\psi = Q$, there is the additional freedom of the choice of r_Q . Note that the custodial symmetry is preserved in the Q sector if $r_Q = 1$, see eq. (5.2). The mass splitting among the heavy quarks is controlled (at tree level) by the mixing with the SM. The mass ordering is determined as

$$T: M_{T} \leq m_{t'}, \qquad B: M_{B} \leq m_{b'}, X_{T}: m_{X} = M_{X_{T}} \leq m_{t'}, \qquad Y_{B}: m_{Y} = M_{Y_{B}} \leq m_{b'}, X_{Q}: m_{X} = M_{X_{Q}} \leq m_{t'} \leq m_{b'}, Y_{Q}: m_{Y} = M_{Y_{Q}} \leq m_{b'} \leq m_{t'},$$

$$(5.7)$$

where we took implicitly into account the experimental upper bounds on the mixing and on $m_t/m_{t'}$, when needed to establish the ordering. In the case of Q, for $r_Q = 1$ one finds $M_Q \leq m_{b'} \leq m_{t'}$, but the ordering between b' and t' can change for different values of r_Q .

Masses and mixing angles are constrained by the perturbativity of the Yukawa couplings,

$$\left|\lambda_{\psi}^{t}\right| \simeq \left|\frac{\sqrt{2}}{\kappa_{\psi}^{t}} s_{\psi} \frac{m_{t'}}{v}\right| \ll 4\pi \,, \qquad \left|\lambda_{\psi}^{b}\right| \simeq \left|\frac{\sqrt{2}}{\kappa_{\psi}^{b}} \tilde{s}_{\psi} \frac{m_{b'}}{v}\right| \ll 4\pi \,.$$
 (5.8)

Note that we do not impose a stronger upper bound such as $4\pi/\sqrt{N_c}$, for reasons discussed in appendix B.1. The perturbativity of the SM couplings λ_t and λ_b is guaranteed a fortiori. For definiteness, in figures 3–6 we delimit with a black dotted line the region of parameters where at least one Yukawa coupling becomes larger than 2π . In the case of Q both

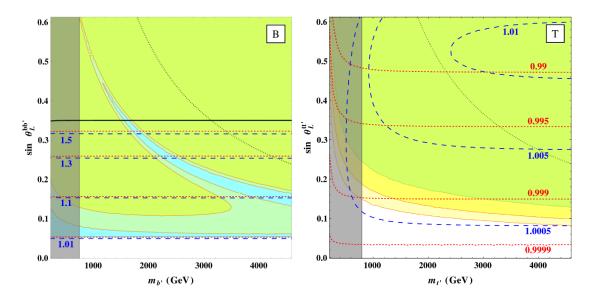


Figure 3. Constraints on the weak singlet VLQs B (left panel) and T (right panel), as a function of the mass of b' (t') and of the mixing angle between b_L and b'_L (t_L and t'_L). The region above the dotted black line is excluded by perturbativity. The blue-shaded region is excluded by the $Zb\bar{b}$ couplings. The (light) yellow-shaded region is excluded by the S and T parameters at (68%) 99% C.L.. The green-shaded region is just the intersection of the previous two. The grey-shaded region is excluded by the collider searches summarised in table 3. The region above the solid black line is excluded by a rough global fit of the Higgs couplings at 99% C.L.. The dashed blue (dotted red) lines correspond to a few relevant values of the signal strength $\mu_{\gamma Z}$ ($\mu_{\gamma \gamma}$).

inequalities must be satisfied at the same time, therefore a large departure from $r_Q = 1$ leads to a stronger constraint, as illustrated by the comparison of the left and right panels of figure 6.

Important constraints come from the Z couplings to quarks, that are affected by the mixing as shown in eq. (A.6). The tree-level deviations with respect to the SM are given by

$$\delta g_{Z\bar{b}b}^{L} = \tilde{s}_{L}^{2} \left(\frac{1}{2} + T_{B}^{3} \right), \quad \delta g_{Z\bar{b}b}^{R} = \tilde{s}_{R}^{2} T_{B}^{3}, \qquad \delta g_{Z\bar{t}t}^{L} = s_{L}^{2} \left(-\frac{1}{2} + T_{T}^{3} \right), \quad \delta g_{Z\bar{t}t}^{R} = s_{R}^{2} T_{T}^{3}, \tag{5.9}$$

where T_B^3 (T_T^3) is the weak isospin of the B (T) component of the VLQ under investigation. The $Zb\bar{b}$ couplings are measured less precisely than their leptonic analog, the $Z\tau^+\tau^-$ couplings, but nonetheless they are strongly constrained, especially for b_L . The top couplings to the Z boson are poorly constrained directly, however they also contribute at one loop to $Zb\bar{b}$. These constraints are summarised in appendix A.3 and they exclude the blue-shaded region in figures 3–6. Deviations in $Z\bar{b}_Lb_L$ are present at tree level in the case of B, Y_B , Y_Q and X_Q . However, in the case of the doublet Y_B , the deviation is suppressed by $(m_b/m_b')^2$ and the most important correction is the one to $Z\bar{b}_Rb_R$. In the case of T and T_T , there is no bottom partner and the deviation to T_T is induced at one loop mostly through T_T leading to a relatively weak constraint. Finally, in the case of T_T and T_T is generated at tree level and T_T are present at tree level and T_T in the case of T_T and T_T there is no bottom partner and the deviation to T_T is induced at one loop mostly through T_T leading to a relatively weak constraint. Finally, in the case of T_T and T_T is generated at tree level and T_T and T_T is generated at tree level and T_T in the case of T_T and T_T is generated at tree level and T_T is given by the T_T is given by the T_T in the case of T_T is given by the T_T in the case of T_T in the case of T_T is given by the T_T in the case of T_T is given by the T_T in the case

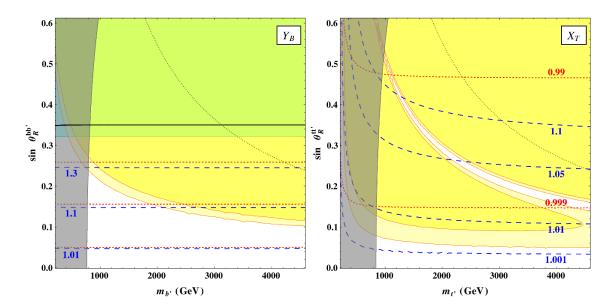


Figure 4. Constraints on the weak doublet VLQs Y_B (Y = -5/6, left panel) and X_T (Y = +7/6, right panel) as a function of the mass of b' (t') and of the mixing angle between b_R and b'_R (t_R and t'_R). The notation is the same as in figure 3.

The VLQ couplings to the EW gauge bosons are also constrained by the EW precision parameters S and T, whose expressions are provided in appendix A.2. Note that, in contrast with the tau and bottom sectors, in the top sector contributions proportional to powers of m_t/m_Z are not suppressed. In figures 3–6 we display in (light) yellow the region corresponding to the (68%) 99% C.L. ellipse of figure 10. Since S and T are proportional to the mixing between the SM quarks and the VLQ, one typically observes an upper bound $s_{\psi}, \tilde{s}_{\psi} \lesssim 0.05 - 0.20$, depending on the VLQ under consideration. Note that this bound relaxes as the heavy quark mass decreases, because S and T eventually vanish in the limit $m_{t'} \to m_t$ or $m_{b'} \to m_b$. Note also that a cancellation is possible among relatively large contributions to S and T, such that large mixing angles may be allowed in a fine-tuned region of parameters. This is especially relevant in the case of X_T , because such region is not excluded by other constraints. Indeed, we find

$$T(X_T) \simeq \frac{3s_{X_T}^2}{16\pi c_w^2 s_w^2} \frac{m_{t'}^2}{m_Z^2} \left[\frac{4}{3} s_{X_T}^2 + \frac{m_t^2}{m_{t'}^2} \left(4 \ln \frac{m_t^2}{m_{t'}^2} + 6 \right) \right], \quad S(X_T) \simeq \frac{s_{X_T}^2}{2\pi} \left(\frac{4}{3} \ln \frac{m_t^2}{m_{t'}^2} + 5 \right), \tag{5.10}$$

where we dropped terms subleading in s_{X_T} and $m_t/m_{t'}$. As the logarithm is large and negative, a cancellation is possible in the T parameter even for large mixing: this explains the allowed strip in figure 4, that reaches $s_{X_T} \simeq 0.5$. A comment is in order for the case of Q: one would expect a milder constraint from T when the two Yukawa couplings $\lambda_Q^{t,b}$ respect the custodial symmetry, i.e. when $r_Q = 1$. However, even in this case there is an important deviation from the SM, because the residual custodial-breaking parameter, $(\lambda_t - \lambda_b)$, differs from the SM one, $\sqrt{2}(m_t - m_b)/v$, as soon as the mixing is non-zero.

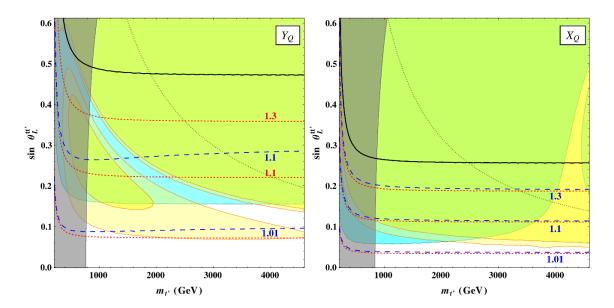


Figure 5. Constraints on the weak triplet VLQs Y_Q (Y = -1/3, left panel) and X_Q (Y = +2/3, right panel) as a function of the mass of t' and of the mixing angle between t_L and t'_L . The notation is the same as in figure 3.

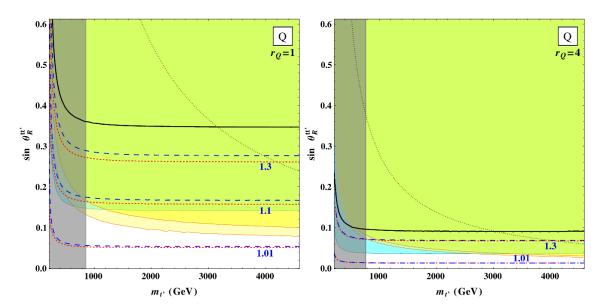


Figure 6. Constraints on the weak doublet VLQ Q as a function of the mass of t' and of the mixing angle between t_R and t'_R . The left panel corresponds to $\lambda_Q^t = \lambda_Q^b$ $(r_Q = 1)$, and the right one to $4\lambda_Q^t = \lambda_Q^b$ $(r_Q = 4)$. The notation is the same as in figure 3.

Let us now turn to the direct searches of VLQs at colliders. As they are coloured, it is easier to produce them at the LHC, relatively to VLLs. Below $\sim 1\,\mathrm{TeV}$ they are dominantly produced in pairs through strong interactions, while for higher masses single production by EW interactions can become dominant [83, 88]. The pair production mechanism, that dominates in the mass range probed at the 8 TeV LHC, is independent from the VLQ (all

are colour triplets) and from the mixing parameters. The ATLAS and CMS searches focus on the following decay channels for the heavy quark mass eigenstates:

$$X \to tW^+$$
, $t' \to tZ, th, bW^+$, $b' \to bZ, bh, tW^-$, $Y \to bW^-$. (5.11)

Note that t' and b' can decay via neutral current at leading order, owing to their vectorlike nature. Decays into another heavy quark coming from the same multiplet, such as $t' \to XW^-$, are kinematically suppressed; decays through loops may also be possible, but they are typically negligible [84]. Here we will disregard these sub-leading channels, and assume that the decay channels in eq. (5.11) have unit branching ratio. In addition, the decays are assumed to be prompt, that is the case whenever the mixing angles are large enough to have an observable effect on the Higgs couplings.

The relative branching ratios of t' and b' in the three decay channels depend mostly on the weak isospin of the VLQ and on the mixing angles. Indeed, since the heavy quarks are already constrained to be heavier than a few hundred GeVs, in good approximation one can neglect the final state masses and find

$$\Gamma(t' \to ht) \simeq \frac{m_{t'}}{16\pi} \left(|y_{tt'}|^2 + |\tilde{y}_{tt'}|^2 \right) ,$$

$$\Gamma(t' \to Zt) \simeq \frac{m_{t'}^3}{32\pi m_Z^2} \left(|(c_L^Z)_{tt'}|^2 + |(c_R^Z)_{tt'}|^2 \right) ,$$

$$\Gamma(t' \to Wb) \simeq \frac{m_{t'}^3}{32\pi m_W^2} \left(|(c_L^W)_{bt'}|^2 + |(c_R^W)_{bt'}|^2 \right) ,$$
(5.12)

and the same for $t' \leftrightarrow b'$ and $t \leftrightarrow b$. Here the Higgs couplings are defined by eq. (B.5), and the Z and W couplings by eq. (A.4). By a straightforward computation, one finds $Br(t' \to ht) \simeq Br(t' \to Zt)$ and

and the Z and W couplings by eq. (A.4). By a straightforward computation, one finds
$$Br(t' \to ht) \simeq Br(t' \to Zt) \simeq \frac{1}{2} \frac{1 - s_T^2}{2 - s_T^2}$$
, $Br(t' \to Wb) \simeq \frac{1}{2 - s_T^2}$; $X_T : Br(t' \to Zt) \simeq \frac{1}{2}$, $Br(t' \to Wb) \simeq 0$; $Q : Br(t' \to Zt) \simeq \frac{1}{2} \frac{1 + s_Q^2(r_Q^2 - 1)}{r_Q^2 + 1 + s_Q^2(r_Q^2 - 1)}$, $Br(t' \to Wb) \simeq \frac{r_Q^2}{r_Q^2 + 1 + s_Q^2(r_Q^2 - 1)}$; $X_Q : Br(t' \to Zt) \simeq \frac{1}{2} \frac{1 + s_{X_Q}^2}{2 + s_{X_Q}^2}$, $Br(t' \to Wb) \simeq \frac{1}{2 + s_{X_Q}^2}$; $Y_Q : Br(t' \to Zt) \simeq \frac{1}{2}$, $Br(t' \to Wb) \simeq 0$. (5.13)

As before, we neglected the SM masses and, therefore, the subdominant mixing angles in eq. (5.5). Note however that some branching ratios are proportional to the SM masses at leading order, for example in the case of X_T one finds $Br(t' \to Wb) \simeq m_t^2/(c_{X_T}^4 m_{t'}^2)$. In the cases where both t' and b' are present, we used the relation $\tan \tilde{\theta}_{\psi} \simeq r_{\psi} \tan \theta_{\psi}$, that follows from eq. (5.6) if one neglects m_b and m_t . The b' branching ratios are obtained from eq. (5.13) by the replacements $T \to B$, $X_T \to Y_B$, $X_Q \leftrightarrow Y_Q$, $t' \to b'$, $t \leftrightarrow b$, $r_Q \to 1/r_Q$ and $s_{\psi} \to \tilde{s}_{\psi}$ for each ψ .

heavy quark	branching ratios	multiplets	mass bound
X (Q = 5/3)	$Br_{Wt} = 1$	X_T, X_Q	$m_X \ge 840 {\rm GeV} [91]$
$t' \ (Q=2/3)$	$Br_{Wb} = \frac{1}{2}, \ Br_{Zt} = Br_{ht} = \frac{1}{4}$	$T, X_Q, Q(r_Q = 1)$	$m_{t'} \ge 800 \text{GeV} [89]$
	$Br_{Wb} = 0, Br_{Zt} = Br_{ht} = \frac{1}{2}$	$X_T, Y_Q, Q(r_Q \ll 1)$	$m_{t'} \ge 855 \mathrm{GeV} [89]$
	$Br_{Wb} = 1, \ Br_{Zt} = Br_{ht} = 0$	$Q(r_Q\gg 1), Q+Y_B$	$m_{t'} \ge 920 \mathrm{GeV} [96]$
	$Br_{Wb} = Br_{Zt} = 0, \ Br_{ht} = 1$	$X_T + Q$	$m_{t'} \ge 950 \mathrm{GeV} [89]$
	$Br_{Wb} = Br_{ht} = 0, \ Br_{Zt} = 1$	$X_T + Q$	$m_{t'} \ge 800 \text{GeV} [89]$
	$Br_{Wb} + Br_{Zt} + Br_{ht} = 1$	T, X_T, Q, Y_Q, X_Q	$m_{t'} \ge 720 \text{GeV} [96]$
$b' \ (Q = -1/3)$	$Br_{Wt} = \frac{1}{2}, Br_{Zb} = Br_{hb} = \frac{1}{4}$	$B, Y_Q, Q(r_Q = 1)$	$m_{b'} \ge 735 \text{GeV}$ [89]
	$Br_{Wt} = 0, Br_{Zb} = Br_{hb} = \frac{1}{2}$	$Y_B, X_Q Q(r_Q^2 \gg 1)$	$m_{b'} \ge 755 \mathrm{GeV} [92]$
	$Br_{Wt} = 1, \ Br_{Zb} = Br_{hb} = 0$	$Q(r_Q^2 \ll 1), X_T + Q$	$m_{b'} \ge 810 \mathrm{GeV} [91]$
	$Br_{Wt} = Br_{Zb} = 0, \ Br_{hb} = 1$	$Q + Y_B$	$m_{b'} \ge 846 \mathrm{GeV} [94]$
	$Br_{Wt} = Br_{hb} = 0, \ Br_{Zb} = 1$	$Q + Y_B$	$m_{b'} \ge 775 \text{GeV} [89]$
	$Br_{Wt} + Br_{Zb} + Br_{hb} = 1$	B, Y_B, Q, Y_Q, X_Q	$m_{b'} \ge 582 \text{GeV} [95]$
Y (Q = -4/3)	$Br_{Wb} = 1$	Y_B,Y_Q	$m_Y \ge 770 {\rm GeV} [89]$

Table 3. Lower bounds at 95 % C.L. on the heavy quark masses $m_X, m_{t'}, m_{b'}$ and m_Y . The experimental searches assume pair production via strong interactions and prompt decays in the indicated channels. In the second column we specify the assumption on the heavy quark-decay branching ratios. Here Br_{Zt} stands for $Br(t' \to Zt)$, and so forth. In the third column we list the VLQ multiplets that correspond to those branching ratios, in the small mixing approximation. Here " $X_T + Q$ " and " $Q + Y_B$ " refer to pairs of VLQs with a custodial symmetry, that are discussed in section 5.2.

The experimental lower bounds on the mass of t' and b' are presented as a function of two independent branching ratios [89, 90]. We choose, in the plane of branching ratios, their approximate values for the VLQ under consideration. To this purpose, we take the limit $s_{\psi} \to 0$ in eq. (5.13) ($\tilde{s}_{\psi} \to 0$ in the case of b'), because the collider bound is relevant at small mixing angles, see figures 3–6). The only exception is X_T , where large mixing is possible, but in this case the strongest collider bound is the one on the component X. The lower bounds on each heavy quark mass are collected in table 3, and vary between ~ 600 and 900 GeV [89, 91–95]. The region excluded at 95 % C.L. is shaded in grey in figures 3–6. A detailed analysis of the lower bound on m'_t is presented in ref. [23] for the case of the VLQ T, taking also into account indirect constraints from B-physics observables.

Let us now discuss the corrections induced by the VLQ on the Higgs boson couplings. The couplings of t, t', b and b' to the Higgs have the same form as those of τ and τ' in eq. (4.19), with the obvious replacement of masses and mixing angles. The heavy quarks X and Y do not couple to the Higgs. The Higgs signal strengths at the LHC μ_{α} , defined in

eq. (B.40), are the product of three factors: Higgs production rate, partial decay rate and lifetime. While new leptons affect significantly the partial decay rate only, new quarks can modify substantially each factor. In particular, the Higgs production via gluon fusion is sensitive to a VLQ, and the mixing in the bottom sector can change significantly the total Higgs width Γ_h . Let us remind that, as discussed below eq. (5.4), the Higgs couplings are CP-conserving for any VLQ.

When the VLQ contains a B component, the Higgs width into $b\bar{b}$ is modified, with respect to the SM, by a factor $R_{b\bar{b}}=(1-\tilde{s}_{\psi}^2)^2$ that, in the light of previously discussed constraints, can be as small as ~ 0.9 . Since in the SM $h \to \bar{b}b$ is the dominant decay channel, this correction enhances μ_{α} for all other decay channels, through the factor $\Gamma_h^{\rm SM}/\Gamma_h$. The Higgs production via gluon fusion is modified by a factor

$$R_{gg} = \frac{\left| \mathcal{A}_{SM}^{gg} + \frac{3}{4} s_{\psi}^{2} \left[A_{1/2}(\tau_{t'}) - A_{1/2}(\tau_{t}) \right] + \frac{3}{4} \tilde{s}_{\psi}^{2} \left[A_{1/2}(\tau_{b'}) - A_{1/2}(\tau_{b}) \right] \right|^{2}}{\left| \mathcal{A}_{SM}^{gg} \right|^{2}},$$
 (5.14)

where the form factors are defined in appendix B.2.1. The effect of the top sector is qualitatively different from the bottom one: given the collider lower bound on $m_{t',b'}$, their form factors are very close to the asymptotic value, $A_{1/2}(0) = 4/3$. While the t loop is also close to this value, the b has a small mass and a suppressed form factor: $A_{1/2}(\tau_{t'}) - A_{1/2}(\tau_t) \simeq -0.04$ and $A_{1/2}(\tau_{b'}) - A_{1/2}(\tau_b) \simeq +1.41$ Therefore, when a b' is present (for $\psi = B, Y_B, Q, X_Q, Y_Q$), its effect dominates and the interference with the SM is constructive. An exception is possible for $\psi = Q$, where $\tilde{s}_Q/s_Q \ll 1$ for $r_Q \ll 1$, see eq. (5.6). In the latter case, and when only a t' is present (for $\psi = T, X_T$), there is a slight destructive interference with the SM. The $t\bar{t}h$ production mode is also modified respect to the SM in the presence of t - t' mixing, with a cross-section reduced by a factor c_{ψ}^4 .

In the diphoton channel

$$R_{\gamma\gamma} = \frac{\left| \mathcal{A}_{SM}^{\gamma\gamma} + \frac{4}{3} s_{\psi}^{2} \left[A_{1/2}(\tau_{t'}) - A_{1/2}(\tau_{t}) \right] + \frac{1}{3} \tilde{s}_{\psi}^{2} \left[A_{1/2}(\tau_{b'}) - A_{1/2}(\tau_{b}) \right] \right|^{2}}{\left| \mathcal{A}_{SM}^{\gamma\gamma} \right|^{2}} . \tag{5.15}$$

Here the SM amplitude is negative, therefore the interference pattern is reversed with respect to R_{gg} . A few different values of the signal strength $\mu_{\gamma\gamma}$ are shown in figures 3–6 by dotted red lines. Once the other constraints are taken into account, one finds at most $\delta\mu_{\gamma\gamma} \sim 0.3$. Finally, for the Higgs decay into a photon and a Z, the new physics amplitude writes

$$\mathcal{A}_{SM+\psi}^{\gamma Z} - \mathcal{A}_{SM}^{\gamma Z} \simeq \sum_{\alpha=t,b} \frac{3Q_{\alpha}}{c_{w}^{2}} \left\{ \delta g_{\alpha\alpha}^{V} A_{1/2}(\tau_{\alpha}, \lambda_{\alpha}) + s_{\psi,\alpha}^{2} \left[g_{\alpha'\alpha'}^{V} A_{1/2}(\tau_{\alpha'}, \lambda_{\alpha'}) - g_{\alpha\alpha}^{V} A_{1/2}(\tau_{\alpha}, \lambda_{\alpha}) \right] + c_{\psi,\alpha} s_{\psi,\alpha} \frac{m_{\alpha} + m_{\alpha'}}{\sqrt{m_{\alpha} m_{\alpha'}}} g_{\alpha\alpha'}^{V} A_{1/2}(\tau_{\alpha'}, \lambda_{\alpha'}, \tau_{\alpha}, \lambda_{\alpha}) \right\},$$

$$(5.16)$$

where $s_{\psi,t} \equiv s_{\psi}$, $s_{\psi,b} \equiv \tilde{s}_{\psi}$, and we neglected the terms proportional to the form factor $B_{1/2}$, that are subdominant. Note also that there is no CP-violating amplitude, as both the h and Z couplings respect CP, see discussion below eq. (5.4). The vector Z couplings

are obtained from eq. (A.6): one finds $\delta g_{\alpha\alpha}^V \equiv (g_{\alpha\alpha}^V - g_{\alpha\alpha}^{V,SM}) \sim s_{\psi,\alpha}^2$ and $g_{\alpha\alpha'}^V \sim s_{\psi,\alpha}$, so that the new physics amplitude of eq. (5.16) is of the order of the mixing squared. The interference with the SM may be constructive or destructive depending on the sign of the Z couplings. A few different values of the signal strength $\mu_{\gamma Z}$ are shown in figures 3–6 by dashed blue lines. When a b' is present, both $\mu_{\gamma Z}$ and $\mu_{\gamma\gamma}$ receive a similar correction, dominated by the increase of R_{gg} and $\Gamma_h^{\rm SM}/\Gamma_h$. A significant correction is possible for Y_B , with both $\delta \mu_{\gamma Z}$ and $\delta \mu_{\gamma\gamma}$ as large as ~ 0.3 . On the other hand, in the case of T or X_T the corrections to the two channels are significantly different, because the small factor $A_{1/2}(\tau_{t'}) - A_{1/2}(\tau_t)$ in eq. (5.15) suppresses the correction to $h\gamma\gamma$. In particular, for X_T one can have $\delta \mu_{\gamma Z} \sim 0.1$ with $\delta \mu_{\gamma\gamma} \sim 0.01$.

In our analysis we computed the relevant signal strengths μ_{α} for $\alpha = b\bar{b}$, $\gamma\gamma$, γZ , WW and ZZ, taking of course into account the corrections to R_{gg} and Γ_h . We compared these predictions with the allowed experimental ranges given in table 4. By simply computing a χ^2 for these five channels, we determined the region of parameters disfavoured at 99% C.L., that is delimited by the solid black line in figures 3–6.

5.2 Two vector-like quarks (including b and t compositeness)

• Two VLQs not coupled to each other. Let us consider first a pair of VLQs (ψ, ψ') that do not couple to each other via a Yukawa coupling. In this case ψ and ψ' must be identified with one of the seven VLQs in table 1, and the phenomenological effects are, in most respects, a trivial addition of those of each VLQ separately, already discussed in section 5.1.

A noticeable exception occurs when the Yukawa couplings and the vector-like masses of ψ and ψ' respect an additional $SU(2)_R$ global symmetry, that provides custodial protection for the EW gauge boson couplings: when the parameters approach this custodial limit, the constraints from EW precision tests drastically relax with respect to the case of a unique VLQ. There are four pairs that may form a doublet under $SU(2)_R$: the weak singlets (T, B), the weak doublets (X_T, Q) or (Q, Y_B) , and the weak triplets (X_Q, Y_Q) . For illustration, we will concentrate on the case of doublets.

The two VLQs transform as bi-doublets under a custodial $SU(2)_L \times SU(2)_R$ symmetry, as long as their Yukawa couplings to the SM fermions and their vector-like masses are equal,

$$-\mathcal{L}_{(X_T,Q)} = \frac{\lambda_{\psi}}{\sqrt{2}} \overline{(X_T \ Q)_L} \begin{pmatrix} H \\ \tilde{H} \end{pmatrix} t_R + M_{\psi} \overline{(X_T \ Q)_L} \begin{pmatrix} X_T \\ Q \end{pmatrix}_R + h.c.,$$

$$-\mathcal{L}_{(Q,Y_B)} = \frac{\lambda_{\psi}}{\sqrt{2}} \overline{(Q \ Y_B)_L} \begin{pmatrix} H \\ \tilde{H} \end{pmatrix} b_R + M_{\psi} \overline{(Q \ Y_B)_L} \begin{pmatrix} Q \\ Y_B \end{pmatrix}_R + h.c..$$
(5.17)

These are the smallest sets of top and bottom quark custodians, respectively [70, 97, 98]. Note that, in this custodial limit, the additional coupling $\overline{Q}_L H b_R$ ($\overline{Q}_L \widetilde{H} t_R$) must vanish in the top (bottom) case. Therefore, a mixing occurs only in the top (bottom) sector, and there are no deviations in the bottom (top) couplings, despite the presence of a b' (t') in the spectrum. The analysis is analogous to the case of τ custodians, discussed in section 4.3. For example, in the top case the linear combination $t'' \equiv (T^{(X_T)} - T^{(Q)})/\sqrt{2}$ does not

couple to the Higgs and therefore it does not mix, while the orthogonal combination mixes with the SM top quark as in eq. (5.3), to form the mass eigenstates t' and t. The mass spectrum is

$$m_{t''} = m_{b'} = m_X = M_{\psi} \le m_{t'} \simeq \frac{M_{\psi}}{c_R}$$
 $(X_T, Q),$
 $m_{b''} = m_{t'} = m_Y = M_{\psi} \le m_{b'} \simeq \frac{M_{\psi}}{\widetilde{c}_R}$ $(Q, Y_B).$ (5.18)

Due to the custodial symmetry, the values of the heavy quark branching ratios into SM particles differ from the case of a single VLQ, discussed in section 5.1. We assume that the decays to another heavy quark are kinematically suppressed, because of the small mass splitting in eq. (5.18), and once again we neglect the SM masses in the final state, as well as the t-t' (b-b') left-handed mixing angle, that is suppressed by $m_t/m_{t'}$ $(m_b/m_{b'})$. Consider for example the top case. The decays $t'/t'' \to Wb$ are suppressed as in eq. (5.13) (here $r_Q = 0$). In addition $t' \to Zt$ vanishes because the Q = 2/3 components of X_T and Q have opposite weak isospin, and $t'' \to ht$ vanishes because t'' does not couple to the Higgs. Similar arguments hold in the bottom case. In summary one finds

$$BR(t'' \to Zt) \simeq Br(b' \to W^-t) \simeq Br(X \to W^+t) \simeq Br(t' \to ht) \simeq 1 \quad (X_T, Q),$$

$$BR(b'' \to Zb) \simeq Br(t' \to W^+b) \simeq Br(Y \to W^-b) \simeq Br(b' \to hb) \simeq 1 \quad (Q, Y_B).$$
(5.19)

It is amusing that, in these two models, there is one heavy quark decaying exclusively in each of the possible decay channels listed in eq. (5.11). The experimental lower bounds on these heavy quark masses can be read off table 3.

The custodial symmetry protects the $Zb\bar{b}$ couplings: in the top case $\delta g_{t\bar{t}}^{R}=0$ and the small $\delta g_{t\bar{t}}^L = (m_t/M_\psi)^2 \hat{s}_R^2/2$ contributes to $Zb\bar{b}$ only at one loop; in the bottom case $\delta g_{b\bar{b}}^R = 0$ and $\delta g_{b\bar{b}}^L = (m_b/M_\psi)^2 \hat{s}_R^2/2$ is very suppressed by the bottom mass. Thus, in this custodial limit large mixing angles are not excluded, as shown in figure 7. Indeed, one can see that the constraint from the other EW precision parameters is significantly relaxed too, as T receives a small correction only, from the difference $(\lambda_t - \lambda_b)$, that is not SM-like because of the mixing, while S acquires a positive correction that remains in the ellipse unless the mixing is very large. Note that in the bottom sector the T parameter is almost independent from $m_{b'}$, since the smallness of m_b ensures $\lambda_b \simeq \lambda_b^{\rm SM}$. On the other hand, when the mixing occurs in the top sector, the coupling λ_t and consequently the T parameter strongly depend on $m_{t'}$. The dominant constraints at small and large heavy quark masses come from the direct collider searches and from perturbativity, respectively. In the top case (right panel of figure 7), the mixing is not constrained by the fit of the Higgs coupling, as the bottom sector is SM-like. As a consequence, for $1.5 \,\mathrm{TeV} \lesssim m_{t'} \lesssim 2 \,\mathrm{TeV}$ the mixing can be as large as $s_R \simeq 0.8$. The $\gamma\gamma$ Higgs decay channel can be suppressed at most by $\delta\mu_{\gamma\gamma}\simeq -0.03$, while the corrections to the γZ channel may be larger, up to $\delta\mu_{\gamma Z} \simeq +0.13$. In the bottom case (left panel of figure 7), the mixing in the bottom sector enhances all the other Higgs channels, as $R_{b\bar{b}}=(1-\widetilde{s}_R^2)^2<1$. This leads to an upper bound $\tilde{s}_R \lesssim 0.35$. Significant corrections as large as $\delta \mu_{\gamma\gamma} \simeq \delta \mu_{\gamma Z} \simeq 0.6$ are possible. Note that the Higgs signal strengths in figure 7 are similar to those with Y_B or X_T only, shown in figure 4. The difference is that the region allowed by EW precision tests largely inflated here, thanks to the custodial symmetry.

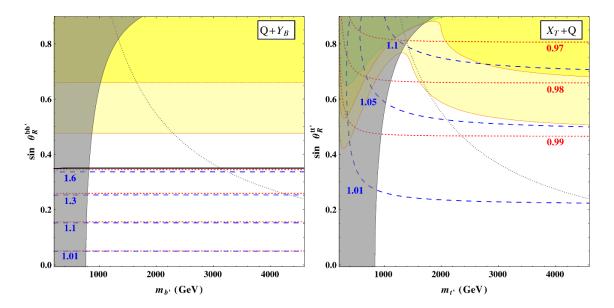


Figure 7. Constraints on the pairs of VLQs (Q, Y_B) (left panel) and (X_T, Q) (right panel), in the custodial limit (equal vector-like masses and Yukawa couplings), as a function of the mass of b' (t') and of the mixing angle between b_R and b'_R (t_R and t'_R). The notation is the same as in figure 3.

• Two VLQs coupled to each other, not mixing with the SM fermions. Let us move to the case of two VLQs coupled to each other via Yukawa interactions. Their chiral components transform as

$$\psi_{1L}, \psi_{1R} \sim (R_c, R_w, Y), \qquad \psi_{2L}, \psi_{2R} \sim \left(R_c, R_w + 1, Y + \frac{1}{2}\right),$$
 (5.20)

with $R_c \neq 1$. The corresponding Lagrangian is the same as in the case $R_c = 1$ (two VLLs), and it is given in eq. (4.31). We bar the special case $R_c = \overline{R_c}$, Y = 0 and R_w odd (Y + 1/2 = 0 and R_w even), that allows for a Majorana mass terms for ψ_1 (ψ_2) and will be discussed in section 5.3. We also bar mixing with the SM quarks, that will be discussed at the end of the section. The effect of two VLQs on $\mu_{\gamma\gamma}$ was discussed in detail in ref. [99].

The number of mass eigenstates with a given electric charge Q and the structure of their mass matrices are the same as in the case of two VLLs, see eqs. (4.32) and (4.40). Therefore, there are five physical parameters: two masses $m_{1,2}$, two mixing angles $\theta_{L,R}$ and one phase φ , defined by eq. (4.33). The analysis of the parameter space proceeds exactly as in section 4.3 and will not be repeated here, however the phenomenology is strongly modified as the colour representation R_c is non-trivial. The main differences are the following:

- The VLQs are pair-produced via strong interactions and, in the absence of mixing with the SM, the lightest state is stable and hadronises. The direct collider bounds on these particle masses are above one TeV, as we already described in some more detail in section 3.
- The contributions of the VLQs to the S and T parameters, as well as to the Higgs decay amplitudes into $\gamma\gamma$ and γZ , have the same form as in eqs. (4.35) to (4.39),

with an additional factor N_c . As in the case of VLLs, for $R_w=1$ and large values of Q we find two regions of the mixing parameters where $\mu_{\gamma\gamma}$ remains SM-like, while $\mu_{\gamma Z}$ can strongly depart from one. (i) For two degenerate masses $m_1=m_2$, the interference with the SM amplitude is destructive for $\gamma\gamma$ and constructive for γZ , as illustrated in figure 1. Therefore, there are values of the mixing parameters where accidentally $\mu_{\gamma\gamma}$ goes back to the allowed range, while at the same time one can even saturate the present upper bound $\mu_{\gamma Z} \lesssim 10$. Note that the gluon-gluon channel remains nearly SM-like, because its amplitude is not enhanced by the large factor Q^2 . (ii) For $m_1 \neq m_2$, the amplitude $\mathcal{A}_{f_1,f_2}^{\gamma\gamma}$ in eq. (4.37) can be tuned to zero, while at the same time one can have large contributions to $\mu_{\gamma Z}$ together with sufficiently small corrections to S and T. E.g. taking $N_c=3$, $Q\simeq 8$, mixing parameters $\varphi=0$, $\theta_L\simeq\pi/8$, $\theta_R\simeq\pi/10$, $m_1/m_2\simeq1.3$ and $m_2\simeq1$ TeV, one obtains $\mu_{\gamma Z}\simeq2$. For the cases $R_w>1$, we refer to the discussion below eq. (4.40).

• The VLQs also contribute to the Higgs production by gluon fusion, with an amplitude that can be easily obtained from the $\gamma\gamma$ one. For the pair of mass eigenstates f_1, f_2 of charge Q, one has $\mathcal{A}_{f_1,f_2}^{gg} = [3C(R_c)/2]/(N_cQ^2)\mathcal{A}_{f_1,f_2}^{\gamma\gamma}$, see appendix B.2. The interference with the SM is constructive in the gluon case, thus enhancing the Higgs production. Note that the gluon-gluon channel also receives a non-zero contribution from the Q=0 sector.

For illustration, we display in figure 8 the parameter space for the case $R_c = 3$, $R_w = 1$ and Y = -1/3 (Y = -2/3), that corresponds to the pair of VLQs B and Q (T and Q), in the limit of no-mixing with the SM quarks. In figure 9 we illustrate how the constraints change for a larger colour representation, as we replaced $R_c = 3$ by $R_c = 8$. For definiteness, we assumed that there is no CP violation, $\varphi = 0$, and that the two mixing mass eigenstates $f_{1,2}$ of charge Q = Y are degenerate in mass, $m_1 = m_2$. In the case of colour octets, larger deviations in the Higgs signal strengths are possible, but the various constraints are correspondingly stronger. One can reach $\mu_{\gamma Z} \simeq 1.4$ for the octets and $\mu_{\gamma Z} \simeq 1.2$ for the triplets. In the case Y = -1/3, $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$ are very close to each other, because $\mathcal{A}_{f_1,f_2}^{\gamma Z}/\mathcal{A}_{f_1,f_2}^{\gamma \gamma} = (g_{11}^V + g_{22}^V)/(Yc_w^2)$ is numerically close to one, see eqs. (4.35) and (4.37), and $\mathcal{A}_{\rm SM}^{\gamma Z}/\mathcal{A}_{\rm SM}^{\gamma \gamma}$ is close to one as well. The strongest constraint on the mixing among the heavy states comes from the S and T parameters. In the octet case the fit of the main Higgs decay channels (see the end of section 5.1 for details) is also a relevant constraint. The mass scale $m_1 = m_2$ is constrained by the searches of stable coloured particles, discussed in section 3.

• Two VLQs coupled to each other, mixing with the SM fermions. Let us briefly discuss the possible interactions between the two VLQs $\psi_{1,2}$ in eq. (5.20) and the SM quarks. This requires of course $R_c = 3$. A non-zero mixing with the bottom and/or top quark can occur if and only if at least one VLQ belongs to the set of seven VLQs in table 1. The complete list is

singlet + doublet :
$$\begin{cases} T + X_T (2t'), & T + Q (2t' + b'), \\ B + Q (t' + 2b'), & B + Y_B (2b'), \end{cases}$$
(5.21)

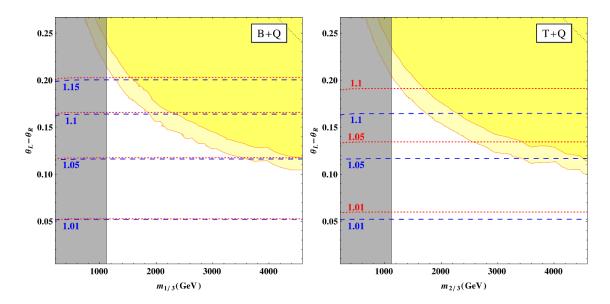


Figure 8. In the left (right) panel, we show the constraints on the pair of VLQs B and Q (T and Q), in the limit of vanishing mixing with the SM quarks, degenerate mass eigenvalues $m_{b'} = m_{b''} \equiv m_{1/3}$ ($m_{t'} = m_{t''} \equiv m_{2/3}$) and no CP violation, $\varphi = 0$. In this case the relevant mixing angle is $\theta_L - \theta_R$, see eq. (4.35). The notation for the various constraints is the same as in figure 3.

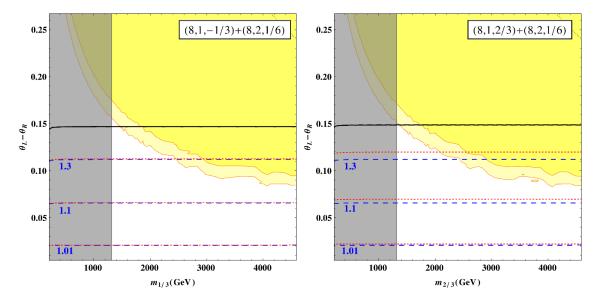


Figure 9. The same as in figure 8, but replacing colour triplets with colour octets.

doublet + triplet :
$$\begin{cases} X_T + Z_{X_T} (2t'), & X_T + X_Q (2t' + b'), \\ Q + X_Q (2t' + 2b'), & Q + Y_Q (2t' + 2b'), \\ Y_B + Y_Q (t' + 2b'), & Y_B + W_{Y_B} (2b'), \end{cases}$$
(5.22)

triplet + quartet :
$$\begin{cases} X_Q + \Omega_{X_T} (2t' + 2b'), X_Q + \Omega_Q (2t' + 2b'), \\ Y_Q + \Omega_Q (2t' + 2b'), Y_Q + \Omega_{Y_B} (2t' + 2b'), \end{cases}$$
(5.23)

where we indicated in brackets the number of new states mixing with the top and with the

bottom quark. We also introduced a few new multiplets, with no Yukawa couplings to the SM fermions: $Z_{X_T} \sim (3,3,5/3), W_{Y_B} \sim (3,3,-4/3), \Omega_{X_T} \sim (3,4,7/6), \Omega_Q \sim (3,4,1/6),$ and $\Omega_{Y_B} \sim (3,4,-5/6)$. They can be written in components as

$$Z_{X_T} = \begin{pmatrix} Z \\ X \\ T \end{pmatrix}, \quad W_{Y_B} = \begin{pmatrix} B \\ Y \\ W \end{pmatrix}, \quad \Omega_{X_T} = \begin{pmatrix} Z \\ X \\ T \\ B \end{pmatrix}, \quad \Omega_Q = \begin{pmatrix} X \\ T \\ B \\ Y \end{pmatrix}, \quad \Omega_{Y_B} = \begin{pmatrix} T \\ B \\ Y \\ W \end{pmatrix}, \quad (5.24)$$

where the two new exotic states Z and W have charges Q(Z) = 8/3 and Q(W) = -7/3. Recasting LHC searches, ref. [100] puts a lower bound of 940 GeV on the mass of the Q = 8/3 state.

When there is only one t' (b') state, the mixing in the top (bottom) sector has the same pattern as in section 5.1. On the other hand, when there are two t' states, the top sector mass matrix takes the form

$$\mathcal{M}_{t} = \begin{pmatrix} \lambda_{t} \frac{v}{\sqrt{2}} & \lambda_{1} \frac{v}{\sqrt{2}} & m_{2} \\ m_{1} & M_{1} & \lambda_{12} \frac{v}{\sqrt{2}} \\ \lambda_{2} \frac{v}{\sqrt{2}} & \lambda_{21} \frac{v}{\sqrt{2}} & M_{2} \end{pmatrix}, \qquad (5.25)$$

where we dropped possible Clebsch-Gordan coefficients. Here ψ_1 (ψ_2) is a weak singlet or triplet (doublet or quartet), m_1 (m_2) vanishes unless $\psi_1 = T$ ($\psi_2 = Q$), and $\lambda_{1,2}$ vanishes if $\psi_{1,2}$ is one of the multiplets in eq. (5.24). The bottom sector mass matrix in presence of two b' states has an analog structure. The mixing with the SM is controlled by ratios of the type $\lambda v/M$ or m/M. They are mostly constrained by the $Zb\bar{b}$ couplings and by S and T. One typically expects $|\lambda v/M|, |m/M| \lesssim 0.1 - 0.2$, in analogy with figures 3–6. Possible cancellations among the various contributions could relax these constraints. A detailed analysis of the whole parameter space of these models is beyond the scope of this paper. Some recent study can be found in ref. [101], that discusses the phenomenology of the 2t' and 2t' + b' cases.

Let us focus on the possibility to generate the top mass (and analogously the bottom one) through the mixing with the VLQs, in the limit where the SM Yukawa coupling λ_t (λ_b) vanishes. This is possible whenever the determinant of \mathcal{M}_t in eq. (5.25) is non-zero for $\lambda_t = 0$, that is, if and only if the two VLQs both couple directly to the SM. The resulting top mass is of order $m_t \sim \lambda v(\lambda v/M)^2$, $\lambda v(m/M)$ or $\lambda v(m/M)^2$. The latter possibility is motivated by partial compositeness. In this scenario, the SM fermions do not couple directly to the composite Higgs, therefore $\lambda_t = \lambda_1 = \lambda_2 = 0$ in eq. (5.25). Rather, they couple linearly to a composite vector-like fermion with the same quantum numbers. This corresponds to the VLQs T and Q for the case of the top quark, leading to $m_t \simeq (m_T/M_T)(m_Q/M_Q)\lambda_{QT}v/\sqrt{2}$, and analogously B and Q for the case of the bottom. The phenomenology of top and bottom partners in composite models, and the associated constraints, are analysed e.g. in refs. [98, 102, 103] (see also ref. [88] for warped extra dimensional models).

5.3 Vector-like plus Majorana quarks

We define a Majorana quark to be a Y=0 fermion multiplet in a non-trivial, real colour representation, $R_c=\overline{R_c}\neq 1$. Such object may couple to the Higgs only in the presence of a VLQ in the same colour representation. As a consequence, these new fermions do not mix with the SM ones and the lightest mass eigenstate is stable. For the smallest possible representation, $R_c=8$, the searches for a stable gluino lead to a lower bound $\simeq 1.3\,\text{TeV}$ [33]. For bigger representations, $N_c\geq 27$, one expects an even more stringent limit, given the larger production cross-section and a similar hadronisation behaviour.

• One VLQ plus one Majorana quark. The most general set formed by a Majorana quark coupled to a VLQ can be written as

$$\chi_R \sim (R_c, R_w, 0), \quad \psi_L, \psi_R \sim (R_c, R_w \pm 1, -1/2), \qquad R_c = \overline{R_c} \neq 1.$$
(5.26)

If R_c is odd, one needs $N_w \neq 2+4n$ to avoid the global $SU(2)_w$ anomaly. The Lagrangian and the structure of the mass matrices are identical to the analogue leptonic case $R_c = 1$, see eqs. (4.46) to (4.52). Here we discuss only the phenomenological differences due to the effect of colour. The new states contribute with an additional factor N_c to the one-loop diagrams for the S and T parameters, as well as for the Higgs signal strengths $\mu_{\gamma\gamma}$ and $\mu_{\gamma Z}$. In addition, they also contribute to the Higgs production via gluon fusion, with an amplitude related to the photon-photon one. For each sector of charge Q that couples to the Higgs, one has $\mathcal{A}_{\chi\psi,Q}^{\gamma\gamma} = (N_c Q^2)/[3C(R_c)/2]\mathcal{A}_{\chi\psi,Q}^{gg}$. The gluon-gluon channel receives a non-zero contribution even from the Q = 0 sector, that is present when N_w is odd.

Since the new quarks are necessarily heavy, their loop contributions can be estimated with good accuracy using the LET approximation, as described in appendix B.2 and in section 4.4. In particular, $\mathcal{A}_{\chi\psi,Q}^{\gamma\gamma}$ is obtained from the amplitude in eq. (4.51), times a factor N_c . For the gluon-gluon channel, summing over the different sectors one finds

$$\mathcal{A}_{\chi\psi}^{gg} \simeq K_{N_w} C(R_c) \frac{\lambda v}{M_\chi} \frac{\tilde{\lambda} v}{M_\psi}, \qquad (5.27)$$

where $K_1 = -4$, $K_2 = -2$, $K_3 = -8/3$, $K_4 = -2$, and so on. As the top quark amplitude is approximately equal to one, $\mathcal{A}_{gg}^{\chi\psi}$ gives roughly the ratio between the contribution of new fermions and the SM one. Note that either constructive or destructive interference with the SM amplitude is possible. The mixing parameters, of the generic form $\lambda v/M$, must satisfy the constraints from R_{gg} and $R_{\gamma\gamma}$, whose allowed ranges are given in appendix B.3. In the minimal case with $R_c = 8$ and $R_w = 1$, only R_{gg} receives a correction, leading to the upper bound $|\lambda v/M| \lesssim 0.17$. One expects similar or even stronger bounds from S and T, in analogy with the cases of figures 8 and 9. Up to possible cancellations, a larger R_c leads to stronger constraints on the model, and to larger deviations in the Higgs couplings.

• One VLQ plus two Majorana quarks. Coming to sets formed by two Majorana quarks plus one VLQ, the first obvious possibility is to add a second copy of χ_R to the previous case. The additional Majorana multiplet automatically cancels the global SU(2)

anomaly, therefore N_w is arbitrary. The phenomenology is the generalisation of the one discussed above

The second and last possibility is provided by the set

$$\chi_{1R} \sim (R_c, R_w, 0), \quad \psi_L, \psi_R \sim (R_c, R_w + 1, -1/2), \quad \chi_{2R} \sim (R_c, R_w + 2, 0), \quad R_c = \overline{R_c} \neq 1,$$
(5.28)

with N_w necessarily odd if R_c is odd. The Lagrangian is the same as in eq. (4.54), and the structure of the mass matrices is also the same as in section 4.4. Let us just present the amplitude for Higgs production into gluon-gluon fusion, that is obtained by generalising eq. (5.27),

$$\mathcal{A}_{\chi_1\chi_2\psi}^{gg}(R_w) \simeq C(R_c) \left(K_{N_w} \frac{\lambda_1 v}{M_{\chi_1}} \frac{\widetilde{\lambda}_1 v}{M_{\psi}} + K_{N_w+2} \frac{\lambda_2 v}{M_{\chi_2}} \frac{\widetilde{\lambda}_2 v}{M_{\psi}} \right) . \tag{5.29}$$

In the minimal case where $R_c = 8$ and $R_w = 1$, the allowed range for R_{gg} leads to a bound on the mixing parameters $|\lambda v/M| \lesssim 0.13$, where we assumed there is no hierarchy nor cancellations among the various mixing parameters. The $R_{\gamma\gamma}$ constraint is less restrictive.

6 Conclusions

We undertook a systematic analysis of new fermions interacting with the Higgs boson. Their properties (gauge charges, masses, Yukawa couplings) are significantly more constrained after the measurement of the Higgs mass and couplings at the first run of the LHC. It is intriguing to identify the few extensions of the SM that outlived this test. We especially aimed at those scenarios that may depart from the decoupling limit, in which the new fermions become very heavy and/or their mixing with the SM becomes very small.

In section 2 we presented the complete classification of sets of n chiral fermions interacting with the Higgs, for $n \leq 4$. While the minimal possibilities are well-known, already for n=3 and 4 we singled out several exotic sets of fermions with a peculiar phenomenology. They emerge from a non-trivial interplay of several self-consistency conditions: cancellation of gauge anomalies, absence of charged massless components, non-zero Yukawa coupling to the SM Higgs doublet. In our classification we recovered as a special case the fermion content of well-motivated theories beyond the SM, such as the seesaw, supersymmetry, or partial compositeness. These cases are situated in a more general context, by considering the most general Lagrangian for the new fermions, not restricted by additional theoretical considerations. Would the evidence of a new particle emerge from data, one should indeed explore the full parameter space, before endorsing a specific model. We also argue that larger sets of new fermions, with $n \geq 5$, do not allow for qualitatively different phenomena, as all the possible building blocks of a fermion mass matrix already appeared in our classification.

In order to examine the phenomenology of the new fermions, in the appendices A and B we derived the general expression of the fermion couplings to the EW gauge bosons and to the Higgs boson, for fermions in arbitrary SM representations (R_c, R_w, Y) . We also provided the formalism to define the gauge and Higgs boson couplings to the fermion mass eigenstates, after EWSB. Besides these tree-level results, we presented the general

one-loop amplitudes for the gauge boson vacuum polarisation, $\Pi_{VV'}$, that allows to define the EW oblique parameters S and T, and for the Higgs coupling to gauge bosons, hVV', that allows to compute the rate for $h \to gg, \gamma\gamma, \gamma Z$.

Let us summarise the main results of our phenomenological survey of sections 3 to 5:

- Several exotic families of chiral fermions, that receive a mass from EWSB only, are still marginally compatible with EW precision tests and direct collider bounds. However, the coloured ones are neatly excluded, as they would greatly enhance the hgg coupling. On the other hand, a colourless family formed by two weak doublets and four singlets is still compatible with the measured $h\gamma\gamma$ coupling.
- The mixing of two or more sterile neutrinos with the SM leptons can have observable effects, despite the smallness of the neutrino masses. If the sterile neutrinos are lighter than the EW scale, they may modify significantly the Higgs invisible width; if heavier, they can appreciably contribute to the S and T parameters.
- In general, a heavy charged lepton τ' cannot mix significantly with the τ because of the $Z\tau\tau$ -coupling constraint. Nonetheless, in a few special regions of parameters interesting phenomena are possible: (i) If $m_{\tau'} < m_h$, the decay rate for $h \to \tau'\tau$ can be significant despite the small mixing. (ii) When both τ_L and τ_R mix with heavy leptons, it is possible to generate m_{τ} entirely through the small mixing permitted by the Z couplings, as long as the two heavy leptons are connected by a Yukawa coupling $\lambda \gtrsim 3$. (iii) If the new lepton sector is arranged to have an approximate custodial symmetry, the Z couplings are protected. In this case a large $\tau \tau'$ mixing is allowed, and it may strongly suppress $h \to \tau\tau$.
- There are two extended classes of new fermions that can couple to the Higgs doublet without involving the SM fermions: either a pair of vector-like fermions, whose components can have an arbitrary charge Q, or a pair formed by a vector-like and a Majorana fermion, whose components have (demi-)integer Q. These fermion pairs were not studied in full generality in the previous literature, and they can produce large observable effects, even when the mixing with the SM fermions is zero. By varying their mass matrix parameters, one can typically scan over the full allowed range for the signal strength $\mu_{\gamma\gamma}$, while remaining in agreement with direct collider searches and EW precision tests. In most cases $\mu_{\gamma Z}$ receives a correction comparable to $\mu_{\gamma\gamma}$, but when the latter is accidentally close to one, it is possible to have $\delta\mu_{\gamma Z}\gg\delta\mu_{\gamma\gamma}$. We will discuss this point in detail below.
- The mixing θ of a heavy quark t' or b' with its SM partner is constrained by the EW precision tests. Nonetheless, the b-b' mixing may significantly suppress the $hb\bar{b}$ coupling, leading to corrections as large as $\delta\mu_{\gamma\gamma} \simeq \delta\mu_{\gamma Z} \simeq 0.6$. We also notice two remarkable circumstances that allow for a large mixing: (i) The corrections to $Zb\bar{b}$ from t-t' mixing are loop-suppressed and may be also suppressed by $(m_t/m_{t'})^2$. The T parameter receives opposite sign corrections that cancel each other for a specific value of $\sin\theta \times m_{t'}$. Both conditions can be realised in the case of the VLQ doublet

(X,T), allowing for a large $\sin \theta \lesssim 0.5$. (ii) The Lagrangian of the new quarks can preserve a custodial symmetry, that suppresses the corrections to T as well as to the $Zb\bar{b}$ couplings. In this custodial subspace of parameters, the upper bound on the mixing relaxes, the exact value depending on the model: for the VLQ doublet Q coupled to t_R and b_R we find $\sin \theta \lesssim 0.15$, while for the two doublets $Q + Y_B$ coupled to b_R ($X_T + Q$ coupled to t_R) one can reach $\sin \theta \lesssim 0.45$ ($\sin \theta \lesssim 0.8$).

In the course of our analysis, we paid special attention to the relative contribution of the new fermions to $h \to \gamma \gamma$ and $h \to \gamma Z$, as the former rate is already constrained to be close to the SM prediction, while the latter could still depart strongly from its SM value. It is commonly believed that new physics cannot provide a large correction to the γZ channel without affecting $\gamma \gamma$ as well. Indeed, let us consider the effective Lagrangian before EWSB, that corresponds to the limit where the new fermions are heavier than the EW scale. There are several dimension-six operators involving the Higgs doublet H and the field-strengths $B_{\mu\nu}$, $W^a_{\mu\nu}$, listed e.g. in ref. [104]. The operators contributing to $h\gamma Z$ can be generated, at one loop, only by two fermion multiplets coupled to H. At least one of these fermions has non-zero hypercharge, thus it necessarily induces the operator $H^{\dagger}HB_{\mu\nu}B^{\mu\nu}$ as well, that contributes to $h\gamma\gamma$. One can rephrase the same argument in terms of the effective Lagrangian for the hVV' couplings after EWSB, that is displayed in eq. (B.8). The coefficients of the dimension-five operators, generated at one loop by the fermion mass eigenstate f_i , are given in eq. (B.22) for $h\gamma\gamma$ and in eq. (B.34) for $h\gamma Z$. The fermion f_i cannot contribute to the γZ channel only, simply because one needs a charge $Q_i \neq 0$ and a non-zero coupling y_i (or \tilde{y}_i) to the Higgs, therefore the $\gamma\gamma$ channel receives a contribution too. This argument, however, has some loopholes: first, the sum over all fermion mass eigenstates can lead to a cancellation in the signal strength $\mu_{\gamma\gamma}$ and not in $\mu_{\gamma Z}$, as the summands in the two channels differ by a factor $\sim g_i^V/Q_i$; second, $h\gamma Z$ receives an additional contribution from loops involving two fermion mass eigenstates, with off-diagonal couplings to both h and Z, see eqs. (B.31) and (B.32).

As a matter of fact, in our survey of fermionic extensions of the SM, we encountered a few scenarios where $\delta\mu_{\gamma Z}\gg\delta\mu_{\gamma\gamma}$:

- (i) One can exploit the order one differences between the Z and γ couplings and loop functions. For example, in the case of t-t' mixing, $\delta\mu_{\gamma\gamma}$ is proportional to $A_{1/2}(\tau_{t'})-A_{1/2}(\tau_t)$, that is very small as both form factors are close to the asymptotic value $A_{1/2}(0)$. On the contrary, the correction to $\mu_{\gamma Z}$ is controlled by $g^V_{t't'}A_{1/2}(\tau_{t'},\lambda_{t'})-g^V_{tt}A_{1/2}(\tau_t,\lambda_\tau)$, that is in general of order one. Also, off-diagonal loops provide an additional contribution of the same order. Unfortunately, the absolute size of the correction is too small to be observed, as the mixing between the SM and new fermions is subject to the EW precision constraints. We find at best $\delta\mu_{\gamma\gamma} \ll \delta\mu_{\gamma Z} \simeq 0.2$, hardly visible even with 3000 fb⁻¹ at 14 TeV, see table 5.
- (ii) A much larger $\delta\mu_{\gamma Z}$ is possible when new fermions couple to each other through the Higgs. Each sector of heavy states with given charges N_c and Q gives a contribution to the $h\gamma\gamma$ amplitude proportional to $\sum_i y_i v/m_i$. We found that the structure of the

fermion mass matrix allows this sum to vanish, see the discussion below eq. (4.39). At the same time, the γZ amplitude is proportional to $\sum_i g_i^V y_i v/m_i$. One can obtain e.g. $\mu_{\gamma Z} \simeq 2$, by means of a pair of states with $N_c Q s_\psi^2 \simeq 3$, where s_ψ is the relevant mixing parameter. Alternatively, the same effect is produced by several states with smaller charges. The required set of parameters can be in agreement with S and T as well. This opens a discovery opportunity for the second run of the LHC.

(iii) There is a second possibility to achieve a large $\mu_{\gamma Z}$. The signal strength $\mu_{\gamma \gamma}$ may be accidentally close to the SM, because the amplitude generated by two new fermion multiplets coupled to the Higgs has sign opposite to the SM one, and for $\mathcal{A}_f^{\gamma \gamma} \simeq -2\mathcal{A}_{\rm SM}^{\gamma \gamma}$ one recovers $\mu_{\gamma \gamma} \simeq 1$. One needs either small weak multiplets with large charges, $N_c Q^2 s_\psi^2 \simeq 5$, or larger multiplets with smaller charges. In this region of parameters the S and T constraint can be satisfied and, moreover, one generically expects $\mu_{\gamma Z}$ much larger than one, because for large values of Q the amplitude $\mathcal{A}_f^{\gamma Z}$ interferes constructively with the SM. We find that one can almost saturate the present experimental bound $\mu_{\gamma Z} \lesssim 10$, therefore coming LHC data will be able to quickly probe this scenario.

In the cases listed above, a mild tuning of the parameters is sufficient to comply with the presently allowed range for $\mu_{\gamma\gamma}$, shown in table 4. In the future, the room for a large $\mu_{\gamma Z}$ will progressively shrink.

The second run of the LHC, that recently started data taking at 13 TeV, will close in on most of the scenarios we have been considering. The allowed regions of parameters at low masses will be covered by direct searches for new fermionic resonances. The islands that survive at large mixing between the SM and new fermions will be probed by the increasing precision in the Higgs coupling measurements, even though there are models where one needs to wait for a high accuracy. In the absence of a signal, we shall be virtually cornered to the region of very heavy masses and/or very small mixing. Even when the new fermions are too heavy to be directly produced and mix negligibly with the SM, their Yukawa couplings to the Higgs can be effectively constrained by the radiative Higgs couplings.

Acknowledgments

NB and MF acknowledge the partial support of the OCEVU Labex (ANR-11-LABX-0060) and the A*MIDEX project (ANR-11-IDEX-0001-02), funded by the "Investissements d'Avenir" French government program managed by the ANR. MF acknowledges the partial support of the European Union FP7 ITN INVISIBLES (Marie Curie Actions, PITN-GA-2011-289442). MF thanks SISSA, Trieste for hospitality during the accomplishment of this project. We thank C. Delaunay, L. Di Luzio, M. Knecht, G. Moultaka, M. Nardecchia, E. Salvioni for relevant discussions.

A Electroweak precision tests in presence of new fermions

In this appendix we provide general formulas for the EW gauge boson couplings to fermions, as well as for their vacuum polarisation amplitudes. This allows to define and compute the

oblique parameters S and T [105–108]. We discuss the experimental constraints on these parameters, as well as on the Z couplings to light SM fermions, such as $Zb\bar{b}$.

A.1 Electroweak gauge boson couplings

The couplings of the EW gauge bosons to a chiral fermion multiplet in a given representation (R_w, Y) of the EW gauge group are determined by the covariant derivative

$$D_{\mu} = \partial_{\mu} - igT^{a}W_{\mu}^{a} - ig'YB_{\mu} = \partial_{\mu} - i\frac{g}{\sqrt{2}}(T^{+}W_{\mu}^{+} + T^{-}W_{\mu}^{-}) - igT^{3}W_{\mu}^{3} - ig'YB_{\mu}, \text{ (A.1)}$$

where T^a are the $SU(2)_w$ generators for R_w , $T^{\pm} = T^1 \pm iT^2$ and $W^{\pm}_{\mu} = (W^1_{\mu} \mp iW^2_{\mu})/\sqrt{2}$. In full generality, the resulting non-vanishing couplings are

$$c^{W^{\pm}}(\overline{f_{m'}}, f_m) = \frac{g}{\sqrt{2}}(T^{\pm})_{m'm} = \frac{g}{\sqrt{2}}\sqrt{j(j+1) - T_m^3(T_m^3 \pm 1)}\delta_{m',m\pm 1},$$

$$c^{W^3}(\overline{f_{m'}}, f_m) = gT_m^3\delta_{m'm}, \qquad c^B(\overline{f_{m'}}, f_m) = g'Y\delta_{m'm},$$
(A.2)

where $j=(N_w-1)/2$ is the weak isospin, and the N_w components of R_w are labelled by $m, m'=-j, -j+1, \ldots, j-1, j$, and have electric charge $Q_m=T_m^3+Y$. It is straightforward to derive from eq. (A.2) the couplings of $Z_\mu=c_wW_\mu^3-s_wB_\mu$ and $A_\mu=s_wW_\mu^3+c_wB_\mu$,

$$c^{Z}(\overline{f_{m'}}, f_m) = \frac{g}{c_w} (T_m^3 - s_w^2 Q_m) \delta_{m'm}, \qquad c^{A}(\overline{f_{m'}}, f_m) = eQ_m \delta_{m'm}. \tag{A.3}$$

After EWSB, for each value of the charge Q, the fermion mass term can be written as $\overline{f_{L\alpha}}(\mathcal{M}_Q)_{\alpha\beta}f_{R\beta}$, where $\alpha, \beta = 1, \ldots, n_Q$ run over the n_Q fermions of charge Q (in a given colour representation). In general the mass matrix is not diagonal and the mixing can be described by $f_{L\alpha} = (U_Q^L)_{\alpha i} f_{Li}$ and $f_{R\alpha} = (U_Q^R)_{\alpha i} f_{Ri}$, where f_i are the mass eigenstates. Therefore, the couplings of the gauge bosons to the mass eigenstates are

$$(c_{L,R}^V)_{ij} = (c_{L,R}^V)_{\alpha\beta} (U_O^{L,R})_{\alpha i}^* (U_{O'}^{L,R})_{\beta j}, \quad V = W^{\pm}, W^3, B,$$
 (A.4)

where the $(c_{L,R}^V)_{\alpha\beta}$ are given in eq. (A.2), and $Q=Q'\pm 1$ for $V=W^\pm,\ Q=Q'$ for $V=W^3,B$.

The mixing cancels out in the photon couplings, because $U(1)_{em}$ is unbroken, and one finds immediately $(c_{L,R}^A)_{ij} = eQ\delta_{ij}$. The Z-boson couplings to the mass eigenstates, instead, do depend on the mixing. Using the parametrisation

$$\mathcal{L}_{\bar{f}fZ} = \frac{g}{c_w} Z_{\mu} \sum_{i,j} \overline{f_i} \gamma^{\mu} \left(g_{ij}^L P_L + g_{ij}^R P_R \right) f_j \equiv \frac{g}{c_w} Z_{\mu} \sum_{i,j} \overline{f_i} \gamma^{\mu} \left(g_{ij}^V - g_{ij}^A \gamma_5 \right) f_j , \qquad (A.5)$$

one finds

$$g_{ij}^{L,R} = T_{\alpha}^3 \delta_{\alpha\beta} (U_Q^{L,R})_{\alpha i}^* (U_Q^{L,R})_{\beta j} - s_w^2 Q \delta_{ij}, \qquad g^{V,A} \equiv \frac{g^L \pm g^R}{2}.$$
 (A.6)

The matrices $g^{L,R}$ ($g^{V,A}$) are hermitian, with possibly non-vanishing off-diagonal entries. Note that the mixing of fermions with equal EW charges does not affect the couplings to the neutral gauge bosons: if T^3_{α} (or, equivalently, Y_{α}) is the same for all α , then one can use $(U_Q^{L,R})^*_{\alpha i}(U_Q^{L,R})_{\alpha j} = \delta_{ij}$, and the couplings to Z (as well as to W^3 and B) reduce to their

unmixed values. Thus, the neutral-current couplings of SM fermions receive a correction, only when they mix with new fermions with a different value of T^3 (of Y). For example, the mixing of two left-handed fermions f_{La} and f_{Lb} of charge Q amounts to

$$U_Q^L = \begin{pmatrix} c & s \\ -s & c \end{pmatrix}, \qquad g^L = \begin{pmatrix} T_a^3 - s_w^2 Q & 0 \\ 0 & T_b^3 - s_w^2 Q \end{pmatrix} + (T_a^3 - T_b^3) \begin{pmatrix} -s^2 & sc \\ sc & s^2 \end{pmatrix} .$$

In this paper we assume that new fermions mix with the third SM family only. Indeed, flavour-changing neutral currents among the different SM families are strongly constrained experimentally.

A.2 Constraints from S and T

The vacuum polarisation amplitudes for the EW gauge bosons, defined by the effective momentum space Lagrangian

$$\mathcal{L}_{\Pi} = -W_{\mu}^{+} \Pi_{WW}^{\mu\nu}(p) W_{\nu}^{-} - \frac{1}{2} B_{\mu} \Pi_{00}^{\mu\nu}(p) B_{\nu} - W_{\mu}^{3} \Pi_{30}^{\mu\nu}(p) B_{\nu} - \frac{1}{2} W_{\mu}^{3} \Pi_{33}^{\mu\nu}(p) W_{\nu}^{3}, \quad (A.7)$$

can be decomposed into transverse and longitudinal parts,

$$\Pi^{\mu\nu}_{VV'}(p) = \Pi^T_{VV'}(p)(p^2g^{\mu\nu} - p^\mu p^\nu) + \Pi^L_{VV'}(p)p^\mu p^\nu = \Pi_{VV'}(p^2)g^{\mu\nu} + (p^\mu p^\nu - \text{terms}) \; . \; (A.8)$$

As in the experiments the mass of the external fermions is much smaller than the EW scale, $m_f^2 \ll m_Z^2$, one can drop the $p^\mu p^\nu$ -terms and expand in p^2 ,

$$\Pi_{VV'}(p^2) = \Pi_{VV'}(0) + p^2 \Pi'_{VV'}(0) + \mathcal{O}(p^4) . \tag{A.9}$$

The lowest terms in this expansion are sufficient to describe accurately the effect of heavy new physics: when new particles at scale m_F contribute to the vacuum polarisation amplitudes, the higher order corrections are suppressed by powers of m_Z^2/m_F^2 . Taking into account that three coefficients can be traded for the experimental values of α , s_w and m_Z , and two others are determined by the Ward identities for the photon, one finds that two parameters are sufficient to characterise the effect of new physics at leading order in m_Z^2/m_F^2 [107, 108]. The combination that describes the custodial symmetry breaking at leading order is given by

$$T \equiv \frac{1}{\alpha c_w^2 m_Z^2} \left[(\Pi_{33}(0) - \Pi_{33}^{SM}(0)) - (\Pi_{WW}(0) - \Pi_{WW}^{SM}(0)) \right]. \tag{A.10}$$

The combination that breaks the weak isospin at leading order, but respects the custodial symmetry, is given by

$$S \equiv \frac{4s_w c_w}{\alpha m_Z^2} \left[\left(\Pi_{30}(m_Z^2) - \left(\Pi_{30}(0) \right) - \left(\Pi_{30}^{\text{SM}}(m_Z^2) - \Pi_{30}^{\text{SM}}(0) \right) \right] \simeq \frac{4s_w c_w}{\alpha} \left[\Pi_{30}'(0) - \Pi_{30}'^{\text{SM}}(0) \right]. \tag{A.11}$$

The approximation in terms of amplitude derivatives evaluated at $p^2 = 0$ is appropriate only for new physics much heavier than m_Z that does not mix with light SM particles; in the general case one should keep the definition of S in terms of amplitude differences,

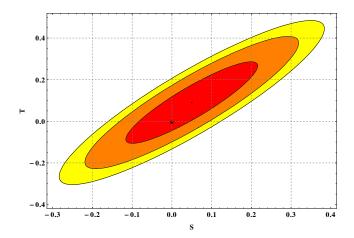


Figure 10. The 68 % (red), 95 % (orange) and 99 % (yellow) C.L. ellipses in the S-T plane, from the fit of ref. [109], with the other EW parameter U left free. The black dot indicates the best fit, while the star at S=T=0 is the SM point, with $m_{t,\text{ref}}=173\,\text{GeV}$ and $m_{h,\text{ref}}=125\,\text{GeV}$.

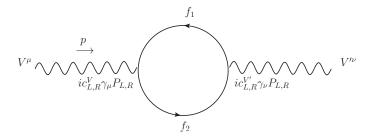


Figure 11. Contribution of two fermion mass eigenstates f_1 and f_2 to the vacuum polarisation amplitude for the gauge bosons V^{μ} and V'^{ν} . The relevant couplings are defined by $\mathcal{L}_{\bar{f}fV} = V_{\mu} \overline{f_i} \gamma^{\mu} [(c_L^V)_{ij} P_L + (c_R^V)_{ij} P_R] f_j$.

to avoid unphysical singularities that may appear in the derivative. The subtracted SM contribution is evaluated at a reference point for the SM parameters. Following ref. [109], if one takes $m_{t,\text{ref}} = 173\,\text{GeV}$ and $m_{h,\text{ref}} = 125\,\text{GeV}$, the present experimental allowed ranges are given by

$$S = 0.05 \pm 0.11$$
, $T = 0.09 \pm 0.13$, (A.12)

with a correlation coefficient $\simeq 0.9$. In figure 10 we display the allowed region in the S-T plane, that we adopt in the rest of the paper to constrain the parameter space of each model.

In order to estimate the contributions to S and T, in any theory where the new physics is weakly coupled, one should just compute the one-loop diagram contributing to the EW gauge boson vacuum polarisation amplitudes, shown in figure 11. The most general couplings of the EW gauge bosons to the fermion mass eigenstates are defined in eq. (A.4). The functions $\Pi_{VV'}(p^2)$ defined in eq. (A.8) will receive different contributions from the left- and right-handed couplings,

$$\Pi_{VV'} = c_L^V c_L^{V'} \Pi_{LL} + c_R^V c_R^{V'} \Pi_{RR} + c_L^V c_R^{V'} \Pi_{LR} + c_R^V c_L^{V'} \Pi_{RL} . \tag{A.13}$$

Performing the computation with dimensional regularisation, one finds the following general result:

$$\Pi_{LL,RR}(p^2) = \frac{N_c}{(4\pi)^2} \left[\frac{(m_1^2 - m_2^2)^3}{6p^4} \ln \frac{m_1^2}{m_2^2} - \frac{(m_1^2 - m_2^2)^2}{3p^2} - (m_1^2 + m_2^2) \left(\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2\mu^2}{m_1m_2} + \frac{1}{6} \right) + \frac{2}{3}p^2 \left(\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2\mu^2}{m_1m_2} + \frac{7}{6} \right) + \left(\frac{(m_1^2 - m_2^2)^2}{3p^2} + \frac{m_1^2 + m_2^2}{3} - \frac{2}{3}p^2 \right) R(p^2) \right],$$
(A.14)

$$\Pi_{LR,RL}(p^2) = \frac{2N_c m_1 m_2}{(4\pi)^2} \left[-\frac{m_1^2 - m_2^2}{2p^2} \ln \frac{m_1^2}{m_2^2} + \frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m_1 m_2} + \frac{3}{2} - R(p^2) \right], \tag{A.15}$$

where N_c is the dimension of the SU(3)_c representation of the fermions $f_{1,2}$, $m_{1,2}$ are the masses of $f_{1,2}$, $\bar{\epsilon}$ and μ are defined by $d^4k \equiv \mu^{4-n}d^nk$ and $1/\bar{\epsilon} \equiv 2/(4-n) - \gamma - \ln \pi$ with $\gamma \simeq 0.5772$, and finally

$$R(p^2) \equiv \frac{\sqrt{\lambda}}{p^2} \log \frac{m_1^2 + m_2^2 - \sqrt{\lambda} - (p^2 + i\epsilon)}{2m_1 m_2}, \qquad \lambda \equiv (m_1^2 - m_2^2)^2 - 2p^2(m_1^2 + m_2^2) + p^4.$$
(A.16)

Note that $R(p^2)$ is invariant for $\sqrt{\lambda} \to -\sqrt{\lambda}$ and it has a non-vanishing imaginary part for $p^2 > (m_1 + m_2)^2$. When evaluating S in eq. (A.11), one must include only the real part of $R(m_Z^2)$, while the imaginary part contributes to the decay width of the EW gauge bosons, that may be also modified with respect to its SM value. Note also that, when $f_{1,2}$ are Majorana fermions, one must include in the amplitude an additional symmetry factor 1/2.

Let us provide for convenience the form of $\Pi_{VV'}(p^2)$ in some relevant limits. For $m_1 = m_2 = 0$ one has

$$\Pi_{LL,RR}(p^2) = \frac{2N_c}{3(4\pi)^2} p^2 \left(\frac{1}{\bar{\epsilon}} + \log \frac{4\pi^2 \mu^2}{-(p^2 + i\epsilon)} + \frac{7}{6}\right), \qquad \Pi_{LR,RL}(p^2) = 0. \tag{A.17}$$

This limit is relevant for loops involving the light SM fermions (all but the top quark), whose mass can be neglected. In order to compute T and S (in the derivative approximation), it is sufficient to compute the first and second term in the p^2 -expansion of $\Pi_{VV'}(p^2)$, respectively:

$$\begin{split} &\Pi_{LL,RR}(0) = -\frac{N_c}{(4\pi)^2} \left[(m_1^2 + m_2^2) \left(\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m_1 m_2} \right) + \frac{m_1^4 + m_2^4}{m_1^2 - m_2^2} \ln \frac{m_2}{m_1} \right], \\ &\Pi_{LR,RL}(0) = \frac{2N_c m_1 m_2}{(4\pi)^2} \left[\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m_1 m_2} + \frac{1}{2} + \frac{m_1^2 + m_2^2}{m_1^2 - m_2^2} \ln \frac{m_2}{m_1} \right], \\ &\Pi'_{LL,RR}(0) = \frac{2N_c}{3(4\pi)^2} \left[\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m_1 m_2} - \frac{1}{6} - \frac{2m_1^2 m_2^2}{(m_1^2 - m_2^2)^2} + \frac{m_1^6 + m_2^6 - 3m_1^4 m_2^2 - 3m_1^2 m_2^4}{(m_1^2 - m_2^2)^3} \ln \frac{m_2}{m_1} \right], \\ &\Pi'_{LR,RL}(0) = \frac{N_c}{(4\pi)^2} \frac{m_1 m_2}{(m_1^2 - m_2^2)^3} \left(m_1^4 - m_2^4 + 4m_1^2 m_2^2 \ln \frac{m_2}{m_1} \right). \end{split} \tag{A.19}$$

For $m_1 = 0$ and $m_2 = m$ (relevant e.g. for the bottom-top quark loop) one obtains

$$\Pi_{LL,RR}(0) = -\frac{N_c m^2}{(4\pi)^2} \left(\frac{1}{\overline{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m^2}\right), \qquad \Pi'_{LL,RR}(0) = \frac{2N_c}{3(4\pi)^2} \left(\frac{1}{\overline{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m^2} - \frac{1}{6}\right), \tag{A.20}$$

and $\Pi_{LR,RL}(0) = \Pi'_{LR,RL}(0) = 0$. For $m_1 = m_2 = m \neq 0$ (loops involving a unique fermion mass eigenstate) one reduces to

$$\Pi_{LL,RR}(0) = -\Pi_{LR,RL}(0) = -\frac{2N_c m^2}{(4\pi)^2} \left(\frac{1}{\bar{\epsilon}} + \ln\frac{4\pi^2\mu^2}{m^2} - \frac{1}{2}\right), \tag{A.21}$$

$$\Pi'_{LL,RR}(0) = \frac{2N_c}{3(4\pi)^2} \left(\frac{1}{\bar{\epsilon}} + \ln \frac{4\pi^2 \mu^2}{m^2} - 1 \right), \qquad \Pi'_{LR,RL}(0) = \frac{N_c}{3(4\pi)^2}. \tag{A.22}$$

As an illustrative example, consider the case of a fermion "family" with no mixing with the SM fermions, formed by one weak doublet $Q_L = (T_L, B_L) \sim (R_c, 2, Y)$ and two singlets $T_R \sim (R_c, 1, Y + 1/2)$ and $B_R \sim (R_c, 1, Y - 1/2)$, with $\dim(R_c) = N_c$. After EWSB they combine into two mass eigenstates T and B with masses m_T and m_B ; their non-zero couplings to EW gauge bosons are obtained from eq. (A.2),

$$c_L^{W^{\pm}}(T,B) = \frac{g}{\sqrt{2}}, \qquad c_L^{W^3}(T) = \frac{g}{2}, \qquad c_L^{W^3}(B) = -\frac{g}{2},$$
 (A.23)

$$c_L^B(T) = c_L^B(B) = g'Y, \quad c_R^B(T) = g'\left(Y + \frac{1}{2}\right), \quad c_R^B(B) = g'\left(Y - \frac{1}{2}\right). \quad (A.24)$$

To compute the correction to S, one should evaluate eqs. (A.14)–(A.15) for $p^2 = m_Z^2$ and $m_1 = m_2 = m_{T,B}$, while for $p^2 = 0$ one can use directly eq. (A.21) with $m = m_{T,B}$. Adding the various contributions to Π_{30} as shown in eq. (A.13), and replacing into eq. (A.11), the result is

$$S_{T,B} = \frac{N_c}{6\pi} \left[\left(1 - 2Y \ln \frac{m_T^2}{m_B^2} \right) + \frac{m_Z^2}{m_T^2} \left(\frac{1}{2} + \frac{4Y}{3} \right) + \frac{m_Z^2}{m_B^2} \left(\frac{1}{2} - \frac{4Y}{3} \right) + \mathcal{O}\left(\frac{m_Z^4}{m_{T,B}^4} \right) \right]. \quad (A.25)$$

If one adopted the approximate expression for S in terms of derivatives, given by the right-hand side of eq. (A.11), then using eq. (A.22) one finds only the first term in the squared bracket of eq. (A.25), which is accurate for $m_{T,B} \gg m_Z$. To compute the correction to T, one should use eq. (A.21) for the T and B loops that contribute to Π_{33} , and eq. (A.18) for the T/B loop that contributes to Π_{WW} . Replacing into eq. (A.10) one obtains

$$T_{T,B} = \frac{N_c}{16\pi c_w^2 s_w^2 m_Z^2} \left(m_T^2 + m_B^2 - 2\frac{m_T^2 m_B^2}{m_T^2 - m_B^2} \ln \frac{m_T^2}{m_B^2} \right) . \tag{A.26}$$

Particularising these results to the case of the SM top and bottom quarks ($N_c = 3$, Y = 1/6), and neglecting the uncertainty on m_b as well as (m_b^2/m_t^2) -corrections, we can immediately extract the well-known dependence of S and T on the value of the top quark mass,

$$S_{\text{top}} = -\frac{1}{6\pi} \ln \frac{m_t^2}{m_{t,\text{ref}}^2}, \qquad T_{\text{top}} = \frac{3}{16\pi c_w^2 s_w^2} \frac{m_t^2 - m_{t,\text{ref}}^2}{m_Z^2}.$$
 (A.27)

A.3 Constraints from $Zf\overline{f}$

The Z-boson couplings to the SM fermions are precisely measured. We discuss only those with the third family, since in this paper we assume that the mixing of the new fermions

with the light families is negligible. The deviations with respect to the SM can be expressed in terms of the Z partial decay width into any given final state $f\overline{f}$,

$$R(Z \to f\overline{f}) \equiv \frac{\Gamma(Z \to f\overline{f})}{\Gamma_{\rm SM}(Z \to f\overline{f})} \equiv 1 + \delta R(Z \to f\overline{f}) , \quad f = \nu_{\tau}, \tau, b . \tag{A.28}$$

For each fermion f there are two independent couplings $g_{f\overline{f}}^{L,R}$ as shown in eq. (A.6), that can be separately constrained if the angular distribution of the fermions is measured.

Beginning from leptons, the Z invisible width and its width into taus are determined at the per mil level [3], $\Gamma(Z \to inv) = 499.0 \pm 1.5 \,\text{MeV}$ and $\Gamma(Z \to \tau^+ \tau^-) = 84.08 \pm 0.22 \,\text{MeV}$. Given this precision and the relatively good agreement between the central values and the SM predictions, we constrain the mixing with the new leptons by imposing a rough 3σ upper bound,

$$|\delta R(Z \to inv)| \le 9 \cdot 10^{-3}$$
, $|\delta R(Z \to \tau^+ \tau^-)| \le 8 \cdot 10^{-3}$. (A.29)

Coming to the Z coupling to bottom quarks, a more detailed discussion is worth, to fairly gauge the resulting constraint on the new fermions. The $Zb\bar{b}$ Lagrangian can be written as

$$\mathcal{L}_{Zb\bar{b}} = \frac{g}{c_w} Z_{\mu} \bar{b} \, \gamma^{\mu} \left[\left(g_{b\bar{b},SM}^L + \delta g_{b\bar{b}}^L \right) P_L + \left(g_{b\bar{b},SM}^R + \delta g_{b\bar{b}}^R \right) P_R \right] b \,, \tag{A.30}$$

where the SM couplings at tree-level are given by $g_{b\bar{b},SM}^L = -1/2 + s_w^2/3$ and $g_{b\bar{b},SM}^R = s_w^2/3$. Deviations at tree-level occur when the bottom quark mixes with a new fermion with a different value of T^3 (and Y). The present experimentally allowed range is given by [110]

$$\delta g_{b\bar{b}}^L = 0.0016 \pm 0.0015 \,, \qquad \delta g_{b\bar{b}}^R = 0.019 \pm 0.007 \,,$$
 (A.31)

with a correlation coefficient $\simeq 0.8$. In figure 12 we display the allowed region in the $\delta g_{b\bar{b}}^R - \delta g_{b\bar{b}}^L$ plane. Note that the left- and right-handed couplings are determined with per mil and per cent precision, respectively, and the best fit region is incompatible with the SM at about 99% C.L.. In some analyses, a slightly better agreement is obtained, at about 95%, due to different details in the global electroweak fit, see e.g. ref. [111]. The discrepancy with the SM comes mostly from the measurement of the forward-backward asymmetry A_{FB}^b , that may be just an upward statistical fluctuation, an unidentified systematic error, or alternatively an indication for a significant new-physics contribution. In this paper, in order to constrain the new fermions that modify the $Zb\bar{b}$ -couplings, we will conservatively enlarge the 99% C.L. region, by allowing it to shift towards the SM point, till the latter touches the 68% ellipse, as illustrated in figure 12. Such a shift roughly corresponds to introduce a systematic error in the measurement of A_{FB}^b .

The mixing with new fermions can be such that no tree-level deviations occur in the $Zb\bar{b}$ -couplings, but they do occur in the $Wt\bar{b}$ coupling and/or in the $Zt\bar{t}$ couplings. These deviations may affect significantly $g_{b\bar{b}}^{L,R}$, because the contribution of one-loop diagrams involving the top quark and the W-boson is larger than the experimental uncertainty. Also new fermions may correct significantly $Zb\bar{b}$ at the one-loop level, if they are not much

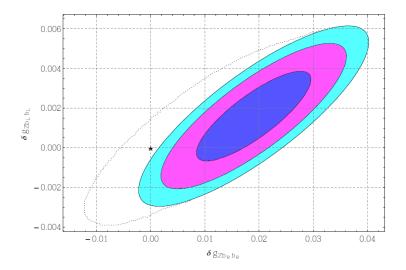


Figure 12. The 68% (blue), 95% (magenta) and 99% (cyan) C.L. ellipses in the $\delta g_{b\bar{b}}^R - \delta g_{b\bar{b}}^L$ plane, extracted from ref. [110]. The black dot indicates the best fit, while the star at the origin represents the SM. In our analysis, we allow for a larger parameter space, delimited by the dotted line, that is obtained by shifting the 99% ellipse towards the origin, till the SM point enters the 68% region.

heavier than the top. The detailed structure of the one-loop corrections to $Zb\bar{b}$ can be found e.g. in ref. [112], that we employ for our analysis of models with modified top couplings. For example, the correction to the left-handed coupling, from the top loops only, can be written as

$$\delta g_{b\bar{b}}^{L} = \delta g_{t\bar{t}}^{L} f_{L}(m_{W}/m_{t}) + \delta g_{t\bar{t}}^{R} f_{R}(m_{W}/m_{t}) + \delta g_{t\bar{b}}^{L} f_{W}(m_{W}/m_{t}),$$
 (A.32)

where $\delta g_{t\bar{t}}^{L,R}$ are defined in analogy to eq. (A.30) with $t \leftrightarrow b$, the $Wt_L\overline{b_L}$ coupling is given by $(g/\sqrt{2})(1+\delta g_{t\bar{b}}^L)$, and the functions $f_{L,R,W}$ can be extracted from ref. [112].

B Higgs boson couplings in presence of new fermions

In this appendix we present a general parametrisation for the Yukawa couplings among the SM Higgs doublet and two arbitrary fermion multiplets. We then analyse the resulting modifications in the Higgs couplings to the SM particles, at leading order: corrections at tree-level to the Higgs-fermions couplings, and one-loop corrections to the Higgs-gauge bosons couplings. Finally, we briefly review the present experimental constraints on these couplings.

B.1 Tree-level Higgs couplings

The SM Yukawa couplings are given by

$$-\mathcal{L}_{Y}^{\text{SM}} = y_{u}\overline{q_{L}}u_{R}\tilde{H} + y_{d}\overline{q_{L}}d_{R}H + y_{e}\overline{l_{L}}e_{R}H + h.c.,$$
(B.1)

where $q_L = (u_L d_L)^T$, $H = (H^+ H^0)^T$ and $\tilde{H} \equiv i\sigma_2 H^*$ are $SU(2)_w$ doublets, while u_R , d_R and e_R are singlets, and flavour indexes are understood.

In full generality, the Higgs doublet may have a non-zero Yukawa interaction with any pair of chiral fermions that transform under $SU(3)_c \times SU(2)_w \times U(1)_Y$ as $\psi_L \sim (R_c, R_w, Y)$ and $\psi_R^{u,d} \sim (R_c, R_w - 1, Y \pm \frac{1}{2})$:

$$-\mathcal{L}_{Y} = \sum_{\psi_{L}} \left[\sum_{\psi_{R}^{u}} y_{\psi_{L}\psi_{R}^{u}} \left(\overline{\psi_{L}} \psi_{R}^{u} \tilde{H} \right) + \sum_{\psi_{R}^{d}} y_{\psi_{L}\psi_{R}^{d}} \left(\overline{\psi_{L}} \psi_{R}^{d} H \right) \right] + h.c. . \tag{B.2}$$

Here the parentheses stand for the appropriate contraction of the $SU(2)_w$ indexes. Let us denote the components of ψ_L by the index $m = j, j-1, \ldots, -j+1, -j$, where $j = (N_w-1)/2$. Then, the multiplet $\overline{\psi_L}$ with components $(\overline{\psi_L})_m \equiv (\overline{\psi_L})_m$ transforms in the conjugate representation R_w^* . It is possible to define a multiplet $\overline{\psi_L}'$ that properly transforms in the representation R_w , by using the $SU(2)_w$ conjugation matrix R, $(\overline{\psi_L}')_m = R_{mn}(\overline{\psi_L})_n \equiv (-1)^{j-m}(\overline{\psi_L})_{-m}$. The 2j components of ψ_R^u pair with the upper (lower) 2j components of $\overline{\psi_L}'$ to form the upper (lower) component of a weak doublet D. The corresponding Clebsch-Gordan coefficients are given by

$$\left\langle j, j - \frac{1}{2}; m, -m \pm \frac{1}{2} \middle| \frac{1}{2}, \pm \frac{1}{2} \right\rangle = \pm (-1)^{j-m} \sqrt{\frac{j \pm m}{j(2j+1)}}$$
 (B.3)

Contracting D with \tilde{H} into a weak singlet, $D_a(i\sigma_2)_{ab}\tilde{H}_b$, one finds

$$\left(\overline{\psi_L}\psi_R^u \tilde{H}\right) \equiv \sum_{m=-j+1}^{j} \sqrt{\frac{j+m}{j(2j+1)}} \left[\overline{(\psi_L)_m} (\psi_R^u)_{m-\frac{1}{2}} \tilde{H}_{\frac{1}{2}} + \overline{(\psi_L)_{-m}} (\psi_R^u)_{-m+\frac{1}{2}} \tilde{H}_{-\frac{1}{2}} \right]. \quad (B.4)$$

The same expression holds for $\psi_R^u \leftrightarrow \psi_R^d$ and $\tilde{H} \leftrightarrow H$ as well. Of course, all the results above also apply when one makes everywhere the replacement $L \leftrightarrow R$.

The relative size of the Clebsch-Gordan coefficients has important phenomenological consequences, e.g. the different components of the fermion multiplets acquire a different mass after EWSB. The overall normalisation of the $SU(2)_w$ contraction is also important, to establish the perturbative range for a Yukawa coupling y: for instance, the contribution of y to the Higgs wavefunction renormalisation at one-loop goes as $y^2/(16\pi^2)$ times the sum of the Clebsch-Gordan coefficients squared, taken over all possible isospin components in the loop. Adopting the above conventions, such a sum is normalised to one, and we can easily define the region where perturbation theory can be trusted, by requiring $y/(4\pi) \ll 1$. However, we keep the conventional normalisation for the doublet-doublet contraction into a singlet, with no overall factor $1/\sqrt{2}$, that strictly-speaking should be included: the issue of $SU(2)_w$ normalisation is more relevant for large weak multiplets.

We note that the perturbative upper bound on a Yukawa coupling y depends on the process under consideration. Schematically, the next-to-leading order amplitude is given by the leading order one times a factor $y^n g^m F_c/(16\pi^2)$, where g stands for other couplings such as gauge couplings, and F_c is the colour factor, with typical values $F_c = 1, N_c, C(R_c)$. In the example of the Higgs wavefunction normalisation adopted above, one has n = 2, m = 0 and $F_c = N_c$, therefore we could have taken into account the SU(3)_c contraction by adding

a factor $1/\sqrt{N_c}$ on the right-hand side of eq. (B.4), or alternatively requiring $y\sqrt{N_c}/(4\pi) \ll 1$. However, the one-loop amplitudes relevant in our analysis (EW precision tests, Higgs couplings to fermions and gauge bosons, etc.) behave differently from each other, and the perturbativity criterion varies correspondingly. In some cases the colour enhancement is absent, or compensated by small gauge couplings, or by a small mixing between new and SM fermions. Therefore, we find more conservative to stick to the bound $y \ll 4\pi$.

At EWSB, H^0 can be replaced by $(v + h)/\sqrt{2}$, to obtain the couplings of the physical Higgs boson h to the fermions in the interaction basis. All fermions with equal charge and in the same colour representation may mix, and their mass matrix $\mathcal{M} = U_L diag(m_1, \ldots, m_n)U_R^{\dagger}$ may include both v-independent vector-like mass terms, and the EWSB contributions $\sim yv$. Thus, one can derive the h-couplings to the fermion mass eigenstates as follows:

$$-\mathcal{L} \supset \overline{f_{L\alpha}}[\mathcal{M}(v)]_{\alpha\beta} f_{R\beta} + \overline{f_{L\alpha}} \frac{\partial}{\partial v} \left[\mathcal{M}(v) \right]_{\alpha\beta} f_{R\beta} h + h.c.$$

$$= \sum_{i} m_{i} \overline{f_{Li}} f_{Ri} + \overline{f_{Lj}} \left[U_{L}^{\dagger} \frac{\partial \mathcal{M}(v)}{\partial v} U_{R} \right]_{jk} f_{Rk} h + h.c.$$

$$= \sum_{i} m_{i} \overline{f_{i}} f_{i} + \overline{f_{j}} \left(y_{jk} + i \gamma_{5} \tilde{y}_{jk} \right) f_{k} h . \tag{B.5}$$

where y and \tilde{y} are hermitian matrices defined by

$$y = \frac{\lambda + \lambda^{\dagger}}{2}, \qquad \tilde{y} = \frac{\lambda - \lambda^{\dagger}}{2i}, \qquad \lambda \equiv U_L^{\dagger} \frac{\partial \mathcal{M}(v)}{\partial v} U_R.$$
 (B.6)

In the CP-conserving case λ is real, therefore $y=y^T$ is real and $\tilde{y}=-\tilde{y}^T$ is imaginary. In the case of purely chiral masses (e.g. in the SM), one has $\mathcal{M}(v) \propto v$, therefore $\partial \mathcal{M}(v)/\partial v = \mathcal{M}/v$, $y=\lambda=diag(m_1,\ldots,m_n)/v$ and $\tilde{y}=0$. On the other hand, in presence of both chiral and vector-like masses, the Higgs boson can have both scalar and pseudo-scalar, CP-even and CP-odd, diagonal and off-diagonal couplings to the fermions mass eigenstates, and its couplings are not proportional to the fermion masses. A simplification occurs in those SM extensions such that $(\partial \mathcal{M}/\partial v)_{\alpha\beta} = \mathcal{M}_{\alpha\beta}c_{\beta}$, that is, each row of the mass matrix has the same dependence on v. In this case U_L^{\dagger} and U_L cancel out in λ and one finds $\lambda_{jk} = m_j \sum_{\beta} c_{\beta}(U_R^*)_{\beta j}(U_R)_{\beta k}$. Similarly, when $(\partial \mathcal{M}/\partial v)_{\alpha\beta} = c_{\alpha}\mathcal{M}_{\alpha\beta}$, one finds $\lambda_{jk} = m_k \sum_{\alpha} c_{\alpha}(U_L^*)_{\alpha j}(U_L)_{\alpha k}$.

The mixing with new fermions modifies the Higgs boson decay width into SM fermions at the tree-level. In addition, there may be new Higgs decay channels, with one or more new fermions in the final state, as long as they are lighter than h. In full generality, the Higgs decay width into two fermions at leading order is given by

$$\Gamma_{\text{tree}}(h \to \overline{f_j} f_k) = \frac{N_c \Delta_{jk}}{8\pi} m_h \left[|y_{jk}|^2 (\beta_{jk}^+)^3 \beta_{jk}^- + |\tilde{y}_{jk}|^2 \beta_{jk}^+ (\beta_{jk}^-)^3 \right] \theta(m_h - m_j - m_k) , \quad (B.7)$$

where $\beta_{jk}^{\pm} \equiv [1 - (m_j \pm m_k)^2/m_h^2]^{1/2}$, $\Delta_{jk} = 2$ if the final state particles are identical Majorana fermions $(j = k \text{ and } f_j = f_j^c)$, and $\Delta_{jk} = 1$ otherwise.

Besides the Yukawa couplings to fermions, the Higgs boson has tree-level couplings to WW, ZZ and to itself. In the presence of new fermions, all the tree-level couplings

may receive corrections at the one-loop level. Even though these corrections may become relevant in view of precision measurements of the Higgs couplings, they represent in general a sub-leading effect and we will not discuss them further. In the following subsection we will focus instead on a more sensitive probe of new physics: those Higgs couplings that are absent at tree-level in the SM.

B.2 Loop-induced Higgs couplings

At one-loop new couplings are induced between the Higgs boson and the SM particles, that are absent at tree-level. In particular, $U(1)_{em}$ and $SU(3)_c$ gauge invariance prevents renormalizable couplings to photons and gluons, therefore the tree-level amplitudes for $h \to gg$, $h \to \gamma\gamma$ and $h \to Z\gamma$ are zero, and in addition the one-loop amplitudes for these processes are free from divergences. The effective Higgs boson couplings generated at one-loop can be described in full generality by two dimension-five operators,

$$\mathcal{L}_{hVV'} = \left(c_{hVV'} V_{\mu\nu} V'^{\mu\nu} + \frac{1}{2} \tilde{c}_{hVV'} V_{\mu\nu} V'_{\rho\sigma} \epsilon^{\mu\nu\rho\sigma} \right) h , \qquad (B.8)$$

where $VV' = gg, \gamma\gamma, \gamma Z$ and $V_{\mu\nu} = G^a_{\mu\nu}, F_{\mu\nu}, Z_{\mu\nu}$ are the field strength tensors for the gluon, the photon and the Z, respectively. The CP-even (odd) coefficients $c_{hVV'}$ ($\tilde{c}_{hVV'}$) have mass dimension minus one, and may receive contributions from loops of both SM and new particles. One should be careful to avoid double-counting: if one considers $\mathcal{L}_{hVV'}$ as part of the effective Lagrangian valid below the EWSB scale v, $c_{hVV'}$ and $\tilde{c}_{hVV'}$ should include only the contributions of particles heavier than v.

In momentum space, the hVV' couplings are given by

$$\mathcal{L}_{hVV'}(p,p') = 2 \left[c_{hVV'}(p'^{\mu}p^{\nu} - p \cdot p'g^{\mu\nu}) + \tilde{c}_{hVV'}\epsilon^{\mu\nu\rho\sigma}p_{\rho}p'_{\sigma} \right] h(p+p')V_{\mu}(p)V'_{\nu}(p') . \tag{B.9}$$

The decay width of the Higgs boson into two vector bosons is then given by

$$\Gamma(h \to VV') = \frac{N_c \Delta_{VV'}}{8\pi} m_h^3 \, \beta_{VV'}^+ \beta_{VV'}^- \left[c_{hVV'}^2 \left(\beta_{VV'}^{+2} \beta_{VV'}^{-2} + \frac{6m_V^2 m_{V'}^2}{m_h^4} \right) + \tilde{c}_{hVV'}^2 \beta_{VV'}^{+2} \beta_{VV'}^{-2} \right], \tag{B.10}$$

where $N_c = 8$ (1) for gluons (for γ and Z), $\Delta_{VV'} = 2$ for V = V' and $\Delta_{VV'} = 1$ for $V \neq V'$, and finally $\beta_{VV'}^{\pm} \equiv [1 - (m_V \pm m_{V'})^2/m_h^2]^{1/2}$. In the following, we will match the explicit loop computation with the effective coefficients $c_{hVV'}$ and $\tilde{c}_{hVV'}$.

B.2.1 Higgs coupling to two gluons

The Higgs-gluon-gluon coupling c_{hgg} (\tilde{c}_{hgg}) receives a one-loop contribution from each coloured fermion with a non-zero CP-conserving (CP-violating) Yukawa coupling to the Higgs boson, see figure 13. The gluon coupling to fermions is determined by SU(3)_c gauge invariance,

$$\mathcal{L}_{g\bar{f}f} = g_s \sum_{i} \overline{f_{ib}} \gamma^{\mu} A^a_{\mu} (T^a_i)_{bc} f_{ic} , \qquad (B.11)$$

where T_i^a are the SU(3)_c generators in the representation R_{ci} of the fermion f_i . As the SU(3)_c symmetry is unbroken, there are no 'off-diagonal' gluon couplings to two different

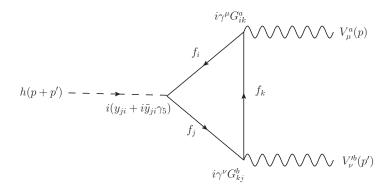


Figure 13. Fermionic triangle loop contributing to the coupling of the Higgs boson to two gauge bosons. A crossed diagram with the two gauge boson insertions interchanged has to be added too, and one must sum over all possible sets (f_i, f_j, f_k) of fermion mass eigenstates. For the gluons one has $G_{ik}^a = g_s \delta_{ik} T_i^a$, for the photon $G_{ik}^{\gamma} = e \delta_{ik} Q_i$, and for the Z boson $G_{ik}^Z = g(g_{ik}^V - \gamma_5 g_{ik}^A)/c_w$.

mass eigenstates. Recall that the Higgs is mostly produced via gluon fusion, with a partonic cross-section that can be expressed as a function of the partial decay width,

$$\sigma(gg \to h; \hat{s}) = \frac{\pi^2}{8m_h} \delta(\hat{s} - m_h^2) \Gamma(h \to gg) . \tag{B.12}$$

In the SM, the contribution of the quarks triangle loop to $h \to gg$ reads

$$\Gamma_{\rm SM}(h \to gg) = \frac{\alpha_s^2 m_h^3}{72\pi^3 v^2} \left| \frac{3}{4} \sum_q A_{1/2}(\tau_q) \right|^2,$$
(B.13)

where $\tau_q \equiv m_h^2/(4m_q^2)$ and the form factor is given by

$$A_{1/2}(\tau) = \frac{2[\tau + (\tau - 1)f(\tau)]}{\tau^2}, \quad f(\tau) = \begin{cases} \arcsin^2 \sqrt{\tau} & \text{for } \tau \leqslant 1, \\ -\frac{1}{4} \left(\log \frac{1 + \sqrt{1 - \tau^{-1}}}{1 - \sqrt{1 - \tau^{-1}}} - i\pi \right)^2 & \text{for } \tau > 1. \end{cases}$$
(B.14)

As illustrated in figure 14, the top quark gives the dominant contribution, because $\tau_t \ll 1$ and $\tau_{b,c,...} \gg 1$. In a generic extension of the SM, the fermions will couple to the Higgs as in eq. (B.5), but only the diagonal, real couplings $y_i \equiv y_{ii}$ and $\tilde{y}_i \equiv \tilde{y}_{ii}$ are relevant for $h \to gg$. One obtains

$$\Gamma(h \to gg) = \frac{\alpha_s^2 m_h^3}{72\pi^3 v^2} \left(|\mathcal{A}_f^{gg}|^2 + |\tilde{\mathcal{A}}_f^{gg}|^2 \right) , \tag{B.15}$$

where the CP-even and CP-odd amplitudes are

$$\mathcal{A}_{f}^{gg} = \frac{3}{2} \sum_{i} C(R_{ci}) \frac{y_{i} v}{m_{i}} A_{1/2}(\tau_{i}) , \qquad \tilde{\mathcal{A}}_{f}^{gg} = \frac{3}{2} \sum_{i} C(R_{ci}) \frac{\tilde{y}_{i} v}{m_{i}} \tilde{A}_{1/2}(\tau_{i}) , \qquad \tilde{A}_{1/2}(\tau) = 2 \frac{f(\tau)}{\tau} ,$$
(B.16)

with the Dynkin index $C(R_{ci})$ defined below eq. (2.1).

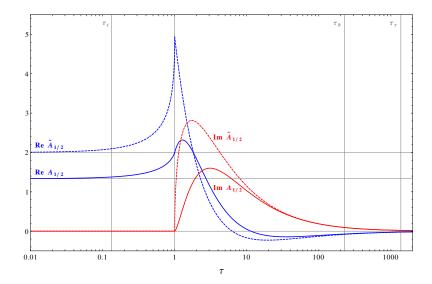


Figure 14. Real (blue lines) and imaginary (red lines) parts of the form factors $A_{1/2}(\tau)$ (solid lines) and $\tilde{A}_{1/2}(\tau)$ (dashed lines). The horizontal lines correspond to the asymptotic values 2, 4/3 and 0. The vertical lines correspond to the reference values $\tau_t \simeq 0.13$, $\tau = 1$, $\tau_b \simeq 230$ and $\tau_\tau \simeq 1300$.

By matching with eq. (B.10), one finds that the contribution of a fermion loop to the effective hgg-couplings is

$$c_{hgg}^{i} = \frac{\alpha_s}{8\pi v} C(R_{ci}) \frac{y_i v}{m_i} A_{1/2}(\tau_i) , \qquad \tilde{c}_{hgg}^{i} = \frac{\alpha_s}{8\pi v} C(R_{ci}) \frac{\tilde{y}_i v}{m_i} \tilde{A}_{1/2}(\tau_i) , \qquad (B.17)$$

where $c_{hgg} \equiv |\sum_i c_{hgg}^i|$ and $\tilde{c}_{hgg} \equiv |\sum_i \tilde{c}_{hgg}^i|$. In the heavy fermion limit, $2m_i \gg m_h$, one can use $A_{1/2}(0) = 4/3$ and $\tilde{A}_{1/2}(0) = 2$. We note that, in the literature, a factor 1/2 is sometimes missing in the expression for \tilde{c}_{hgg}^t .

One can use the Low Energy Theorem (LET) [113, 114] (see also [115–117]) to evaluate the effective hVV' couplings induced by states much heavier than the EW scale. For a given sector of mixing states in the representation (R_c, Q) of $SU(3)_c \times U(1)_{em}$, the low energy result is a function of their mass matrix \mathcal{M} only. For the CP-conserving and CP-violating [118] gluon-gluon case one finds, respectively,

$$c_{hgg}^{LET} = \frac{\alpha_s}{12\pi} C(R_c) \frac{\partial}{\partial v} \ln\left[\det\left(\mathcal{M}\mathcal{M}^{\dagger}\right)\right], \qquad \widetilde{c}_{hgg}^{LET} = \frac{\alpha_s}{4\pi} C(R_c) \frac{\partial}{\partial v} \arg\left[\det\left(\mathcal{M}\right)\right]. \quad (B.18)$$

This is very useful in the case of a large, complicated mass matrix \mathcal{M} , because this expression is much easier to evaluate, with respect to an explicit computation of the mass eigenvalues m_i and of the mass eigenstate couplings y_i and \tilde{y}_i . Note, however, that this approximation requires all the mass eigenstates in a given sector to be heavy, $2m_i \gg m_h$. It is easy to check the consistency of eq. (B.17) and eq. (B.18) for one heavy chiral fermion (e.g. the SM top quark), as $\mathcal{M}_i = m_i = y_i v$ and $A_{1/2}(\tau_i) \simeq 4/3$.

B.2.2 Higgs coupling to two photons

The fermions charged under $U(1)_{em}$ contribute to the Higgs-photon-photon couplings $c_{h\gamma\gamma}$ and $\tilde{c}_{h\gamma\gamma}$ at one loop. In the SM, there is also the contribution from W-boson loops, that

we include using the SM tree-level couplings of the W to the Higgs and to the photon. The SM decay width is given by [113, 114, 119]

$$\Gamma_{\rm SM}(h \to \gamma \gamma) = \frac{\alpha^2 m_h^3}{256\pi^3 v^2} \left| A_1(\tau_W) + \sum_{f_i \in \rm SM} N_{ci} Q_i^2 A_{1/2}(\tau_i) \right|^2, \tag{B.19}$$

where $\tau_W \equiv m_h^2/(4m_W^2)$, $\tau_i \equiv m_h^2/(4m_i^2)$, and the form factor for the W-loops reads

$$A_1(\tau) = -\frac{2\tau^2 + 3\tau + 3(2\tau - 1)f(\tau)}{\tau^2} \ . \tag{B.20}$$

The W contribution is dominant, $A_1(\tau_W) \simeq -8.36$, and it interferes destructively with the top-quark loop, $N_{ct}Q_t^2A_{1/2}(\tau_t) \simeq 1.83$.

In presence of extra fermions, there are new contributions to $h \to \gamma \gamma$ that depend, as in the case of $h \to gg$, on the Yukawa couplings y_i and \tilde{y}_i ,

$$\Gamma(h \to \gamma \gamma) = \frac{\alpha^2 m_h^3}{256\pi^3 v^2} \left[|A_1(\tau_W) + \mathcal{A}_f^{\gamma \gamma}|^2 + |\tilde{\mathcal{A}}_f^{\gamma \gamma}|^2 \right], \tag{B.21}$$

where

$$\mathcal{A}_f^{\gamma\gamma} = \sum_i \frac{y_i v}{m_i} N_{ci} Q_i^2 A_{1/2}(\tau_i) , \qquad \tilde{\mathcal{A}}_f^{\gamma\gamma} = \sum_i \frac{\tilde{y}_i v}{m_i} N_{ci} Q_i^2 \tilde{A}_{1/2}(\tau_i) . \qquad (B.22)$$

In terms of the coefficients of the effective Lagrangian eq. (B.8), the contribution of each fermion is given by

$$c_{h\gamma\gamma}^{i} = \frac{\alpha}{8\pi v} \frac{y_{i}v}{m_{i}} N_{ci} Q_{i}^{2} A_{1/2}(\tau_{i}), \qquad \tilde{c}_{h\gamma\gamma}^{i} = \frac{\alpha}{8\pi v} \frac{\tilde{y}_{i}v}{m_{i}} N_{ci} Q_{i}^{2} \tilde{A}_{1/2}(\tau_{i}).$$
 (B.23)

The LET approximation, for a set of heavy fermions in the representation (R_c, Q) with a mass matrix \mathcal{M} , is given by

$$c_{h\gamma\gamma}^{LET} = \frac{\alpha}{12\pi} Q^2 N_c \frac{\partial}{\partial v} \ln\left[\det\left(\mathcal{M}\mathcal{M}^{\dagger}\right)\right], \qquad \widetilde{c}_{h\gamma\gamma}^{LET} = \frac{\alpha}{4\pi} Q^2 N_c \frac{\partial}{\partial v} \arg\left[\det\left(\mathcal{M}\right)\right], \quad (B.24)$$

in analogy with eq. (B.18).

B.2.3 Higgs coupling to a Z boson and a photon

The last loop-induced coupling to be considered is $hZ\gamma$. It is generated by W-boson loops, that we take to be SM-like, as well as by fermionic triangle loops. The Z-boson couplings to fermion mass eigenstates are defined in eq. (A.6).

The Higgs decay width into a photon and a Z in the SM is given by [120, 121]

$$\Gamma_{\text{SM}}(h \to \gamma Z) = \frac{\alpha g^2 c_w^2 m_h^3}{512\pi^4 v^2} \left(1 - \frac{m_Z^2}{m_h^2} \right)^3 \left| A_1(\tau_W, \lambda_W) + \sum_{f_i \in \text{SM}} \frac{N_{ci} Q_i g_i^V}{c_w^2} A_{1/2}(\tau_i, \lambda_i) \right|^2,$$
(B.25)

where $\lambda_W \equiv m_Z^2/(4m_W^2) = (m_Z/m_h)^2 \tau_W \simeq 0.52 \tau_W$, and analogously $\lambda_i \equiv m_Z^2/(4m_i^2) \simeq 0.52 \tau_i$. Note that only the $Z f_i \overline{f_i}$ vector coupling contributes, $g_i^V = T_3(f_{Li})/2 - Q_i s_w^2$. The form factors are given by

$$A_1(\tau, \lambda) = 2 [3 + 2\tau - 2\lambda(1 + 2\tau)] I_1(\tau, \lambda) - 16(1 - \lambda)I_2(\tau, \lambda),$$
 (B.26)

$$A_{1/2}(\tau,\lambda) = 4 [I_2(\tau,\lambda) - I_1(\tau,\lambda)],$$
 (B.27)

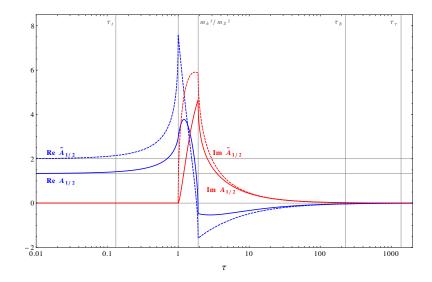


Figure 15. Real (blue lines) and imaginary (red lines) parts of the form factors $A_{1/2}(\tau,\lambda)$ (solid lines) and $\hat{A}_{1/2}(\tau,\lambda)$ (dashed lines), for $\lambda = (m_Z/m_h)^2 \tau \simeq 0.52\tau$. The horizontal lines correspond to the asymptotic values 2, 4/3 and 0. The vertical lines correspond to $\tau_t \simeq 0.13$, $\tau = 1$, $\tau \simeq 1.9$ $(\lambda = 1)$, $\tau_b \simeq 230$ and $\tau_\tau \simeq 1300$.

$$I_{1}(\tau,\lambda) = -\frac{1}{2(\tau-\lambda)} + \frac{f(\tau) - f(\lambda)}{2(\tau-\lambda)^{2}} + \frac{\lambda[g(\tau) - g(\lambda)]}{(\tau-\lambda)^{2}}, \quad I_{2}(\tau,\lambda) = \frac{f(\tau) - f(\lambda)}{2(\tau-\lambda)}, \quad (B.28)$$

$$g(\tau) = \begin{cases} \sqrt{\tau^{-1} - 1} & \text{arcsin } \sqrt{\tau} & \text{for } \tau \leq 1, \\ \sqrt{1 - \tau^{-1}} & \text{1 + } \sqrt{1 - \tau^{-1}} & \text{1 - } \sqrt{1 - \tau^{-1}} \end{cases}$$

 $g(\tau) = \begin{cases} \sqrt{\tau^{-1} - 1} \arcsin \sqrt{\tau} & \text{for } \tau \leq 1, \\ \frac{\sqrt{1 - \tau^{-1}}}{2} \left(\log \frac{1 + \sqrt{1 - \tau^{-1}}}{1 - \sqrt{1 - \tau^{-1}}} - i\pi \right) & \text{for } \tau > 1. \end{cases}$ (B.29)

The normalisation is chosen to match with the $\gamma\gamma$ form factors: $A_1(\tau,0)=A_1(\tau)$ and $A_{1/2}(\tau,0) = A_{1/2}(\tau)$. The behaviour of $A_{1/2}(\tau,\lambda)$ is displayed in figure 15, for the relevant case $\lambda = (m_Z/m_h)^2 \tau$. The W-boson and t-quark summands in eq. (B.25) take the value $A_1(\tau_W, \lambda_W) \simeq -6.64$ and $N_{ct}Q_tg_t^V A_{1/2}(\tau_t, \lambda_t)/c_w^2 \simeq 0.37$, with the lighter SM fermions adding a very small contribution.

In a generic fermionic extension of the SM, we find a decay width

$$\Gamma(h \to \gamma Z) = \frac{\alpha g^2 c_w^2 m_h^3}{512\pi^4 v^2} \left(1 - \frac{m_Z^2}{m_h^2} \right)^3 \left[|A_1(\tau_W, \lambda_W) + \mathcal{A}_f^{Z\gamma}|^2 + |\tilde{\mathcal{A}}_f^{Z\gamma}|^2 \right], \quad (B.30)$$

with the CP-even and odd fermionic amplitudes given by

$$\mathcal{A}_{f}^{Z\gamma} = \sum_{j,k} \frac{N_{ck}Q_{k}v}{c_{w}^{2}\sqrt{m_{j}m_{k}}} \left[\operatorname{Re}(g_{kj}^{V}y_{jk})a_{1/2}(m_{j}, m_{k}, m_{k}) + i\operatorname{Im}(g_{kj}^{A}\tilde{y}_{jk})b_{1/2}(m_{j}, m_{k}, m_{k}) \right],$$
(B.31)

$$\tilde{\mathcal{A}}_{f}^{Z\gamma} = \sum_{j,k} \frac{N_{ck} Q_k v}{c_w^2 \sqrt{m_j m_k}} \left[\text{Re}(g_{kj}^V \tilde{y}_{jk}) \tilde{a}_{1/2}(m_j, m_k, m_k) + i \text{Im}(g_{kj}^A y_{jk}) \tilde{b}_{1/2}(m_j, m_k, m_k) \right].$$
(B.32)

The explicit expression of the four independent form factors will be given below. As far as we know, this expression for $\Gamma(h \to \gamma Z)$, corresponding to a generic set of fermions, was not

available in the literature. Here the sum runs over all pairs of fermion mass eigenstates: the triangular fermion loop is formed by one f_j propagator from the h vertex to the Z vertex, and two f_k propagators from Z to γ , and from γ to h. As both h and Z can have off-diagonal couplings, j and k can be different. Note that only those combination of couplings that are even under the charge conjugation C contribute, because the transition $h \to Z\gamma$ is even: under C, one has $Q \to -Q$, $g_{ij}^V \to -g_{ij}^{V*}$ and $x_{ij} \to x_{ji} = x_{ij}^*$, for $x = g^A, y, \tilde{y}$. The P and CP-even (odd) amplitude corresponds to an even (odd) number of axial-vector and pseudo-scalar couplings g^A and \tilde{y} .

Let us discuss first the loops involving one fermion mass eigenstate only (j = k). The diagonal couplings $g_i^{V,A}$, y_i and \tilde{y}_i are all real, therefore the form factors $b_{1/2}$ and $\tilde{b}_{1/2}$ are irrelevant, while the others reduce to

$$a_{1/2}(m, m, m) = A_{1/2}(\tau, \lambda), \qquad \tilde{a}_{1/2}(m, m, m) = \tilde{A}_{1/2}(\tau, \lambda) \equiv 4I_2(\tau, \lambda).$$
 (B.33)

These two form factors are displayed in figure 15 as a function of τ . As usual the normalisation matches with the $\gamma\gamma$ form factors, in particular $\tilde{A}_{1/2}(\tau,0) = \tilde{A}_{1/2}(\tau)$. Comparing with eq. (B.10), one finds that the contributions of such fermion 'diagonal' loop to the effective $h\gamma Z$ couplings are

$$c_{h\gamma Z}^{i} = \frac{\alpha}{4\pi s_{w} c_{w} v} \frac{y_{i} v}{m_{i}} N_{c_{i}} Q_{i} g_{i}^{V} A_{1/2}(\tau_{i}, \lambda_{i}), \quad \tilde{c}_{h\gamma Z}^{i} = \frac{\alpha}{4\pi s_{w} c_{w} v} \frac{\tilde{y}_{i} v}{m_{i}} N_{cf} Q_{i} g_{i}^{V} \tilde{A}_{1/2}(\tau_{i}, \lambda_{i}).$$
(B.34)

Let us now discuss the loops involving two fermion mass eigenstates $(j \neq k)$. The form factors are given by

$$\begin{split} \frac{a_{1/2}(m_j,m_k,m_k)}{\sqrt{m_jm_k}} &= -\frac{4}{m_Z^2 - m_h^2} \bigg\{ \left[\frac{A_0(m_j) - A_0(m_k)}{m_h^2} + 1 \right] (m_j + m_k) \\ &+ \frac{B_0(m_h^2;m_j,m_k)}{m_Z^2 - m_h^2} \left[(m_j + m_k) \left(2m_j^2 - 2m_k^2 - m_h^2 + \frac{m_Z^2}{m_h^2} (m_k^2 - m_j^2) \right) + 2m_k (m_h^2 - m_Z^2) \right] \\ &+ \frac{B_0(m_Z^2;m_j,m_k)}{m_Z^2 - m_h^2} \left[(m_j + m_k)(m_k^2 - m_j^2) + m_k (2m_Z^2 - m_h^2) + m_j m_h^2 \right] \\ &+ C_0(m_Z^2,0,m_h^2;m_j,m_k,m_k) \left[2m_k^2(m_j + m_k) + m_k (m_Z^2 - m_h^2) \right] \bigg\} , \end{split} \tag{B.35}$$

$$&\frac{\tilde{a}_{1/2}(m_j,m_k,m_k)}{\sqrt{m_jm_k}} = -4 \left[\frac{B_0(m_h^2;m_j,m_k) - B_0(m_Z^2;m_j,m_k)}{m_Z^2 - m_h^2} (m_j - m_k) + C_0(m_Z^2,0,m_h^2;m_j,m_k,m_k) m_k \right] , \tag{B.36}$$

$$&\frac{b_{1/2}(m_j,m_k,m_k)}{\sqrt{m_jm_k}} = \frac{a_{1/2}(-m_j,m_k,m_k)}{\sqrt{m_jm_k}} , \frac{\tilde{b}_{1/2}(m_j,m_k,m_k)}{\sqrt{m_jm_k}} = \frac{\tilde{a}_{1/2}(-m_j,m_k,m_k)}{\sqrt{m_jm_k}} , \tag{B.37}$$

where A_0 , B_0 and C_0 are the standard Passarino-Veltman scalar functions [122, 123], in the convention of ref. [124]. In the literature, these 'off-diagonal' loops are often neglected but, in models with significant h and Z off-diagonal couplings, they may provide a contribution

to the decay width of the same order as the 'diagonal' loops. For example, the form factors in eqs. (B.35)–(B.37) have been already employed in supersymmetric models to compute the charginos loops [125–127].

It is useful to combine all the loops involving two given fermions f_j and f_k . As $\operatorname{Re}(g_{kj}^V y_{jk}) = \operatorname{Re}(g_{jk}^V y_{kj})$ and $\operatorname{Im}(g_{kj}^A \tilde{y}_{jk}) = -\operatorname{Im}(g_{jk}^A \tilde{y}_{kj})$, the combinations that appear in the total amplitude are

$$A_{1/2}(\tau_j, \lambda_j, \tau_k, \lambda_k) \equiv \frac{1}{2} \left[a_{1/2}(m_j, m_k, m_k) + a_{1/2}(m_k, m_j, m_j) \right] , \qquad (B.38)$$

$$B_{1/2}(\tau_j, \lambda_j, \tau_k, \lambda_k) \equiv \frac{1}{2} \left[b_{1/2}(m_j, m_k, m_k) - b_{1/2}(m_k, m_j, m_j) \right] , \qquad (B.39)$$

and analog definitions for the CP-odd counterparts $\tilde{A}_{1/2}$ and $\tilde{B}_{1/2}$. In figure 16 we illustrate the behaviour of these four form factors as a function of $\tau = m_h^2/(4m^2)$, where m is the mass of the lightest fermion, for a fixed value of the ratio r = m'/m, where m' is the mass of the heaviest fermion. In the limit r = 1 one recovers the diagonal form factors, shown in figure 15. Since m' is the mass of a new charged fermion, it should be sufficiently large to comply with experimental lower bounds; requiring for example $m' > m_h$, one finds that only the region $\tau < r^2/4$ is relevant for phenomenology. Note that the behaviour of the form factors as $\tau \to 0$ is sensitive to the mass ratio: as r increases from 1 to infinity, the asymptotic regime settles at larger values of τ , and the asymptotic value of the form factors $A_{1/2}$ and $\tilde{A}_{1/2}$ tends to zero as $1/\sqrt{r}$. The form factors $B_{1/2}$ and $\tilde{B}_{1/2}$ are zero for r = 1, then become of order one as r grows, then tend to zero in the large-r limit.

B.3 Experimental constraints on the Higgs couplings

Here we collect the constraints on the Higgs couplings that we use in our analysis. For a given Higgs-decay final state α , the LHC measures the signal strength μ_{α} defined as

$$\mu_{\alpha} \equiv \frac{\sigma(pp \to h)}{\sigma^{\text{SM}}(pp \to h)} \frac{Br(h \to \alpha)}{Br^{\text{SM}}(h \to \alpha)} = \frac{\sigma(pp \to h)}{\sigma^{\text{SM}}(pp \to h)} \frac{\Gamma(h \to \alpha)}{\Gamma^{\text{SM}}(h \to \alpha)} \frac{\Gamma_h^{\text{SM}}}{\Gamma_h}, \tag{B.40}$$

where Γ_h is the total Higgs width. In table 4 we report the present determination of μ_{α} for $\alpha = \gamma \gamma, ZZ^*, WW^*, b\bar{b}, \tau \tau, \gamma Z, \mu\mu$ as well as on the invisible width, by the ATLAS and CMS collaborations. The expected precision for a luminosity of $300 - 3000 \,\mathrm{fb^{-1}}$ at $14 \,\mathrm{TeV}$ [128, 129] is reported for these same channels in table 5.

From a global fit of the Higgs data, one can also extract information on the Higgs coupling to gluons. Taking a rough extrapolation from the fit in figure 16 of ref. [35], we find $0.5 \lesssim R_{gg} \lesssim 1.8$ at 99% C.L., where R_{gg} is defined in eq. (3.4). In the same way we extract the analogue quantity for the diphoton channel, $0.5 \lesssim R_{\gamma\gamma} \lesssim 1.9$ at 99% C.L., that we employ throughout this paper.

The new fermions may or may not affect each of the three factors on the right-hand side of eq. (B.40). Let us discuss first the Higgs production cross section. The dominant gluon fusion channel can be modified at leading order only by coloured fermions. The weak-vector-boson fusion and associated production can be modified, at tree level, only by fermions mixing with the initial state quarks: as we limit our analysis to mixing with

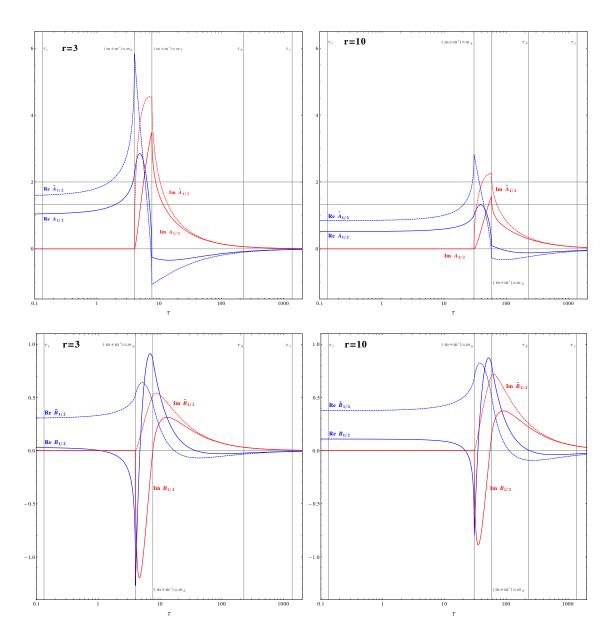


Figure 16. Form factors for the triangle loops involving two fermions of mass m and m' = r m, for r = 3 and r = 10, in the left and right-hand panels, respectively. We show the real (in blue) and imaginary (in red) parts of $A_{1/2}(\tau, \lambda, \tau/r^2, \lambda/r^2)$ (solid lines, upper panels), $\tilde{A}_{1/2}(\tau, \lambda, \tau/r^2, \lambda/r^2)$ (dashed, upper), $B_{1/2}(\tau, \lambda, \tau/r^2, \lambda/r^2)$ (solid, lower) and $\tilde{B}_{1/2}(\tau, \lambda, \tau/r^2, \lambda/r^2)$ (dashed, lower), as a function of $\tau \equiv 4m_h^2/m^2$, for a fixed value of $\lambda \equiv (m_Z/m_h)^2\tau \simeq 0.52 \ \tau$. The horizontal lines correspond to the asymptotic values for the case r = 1 (see figure 15). The vertical lines correspond to the third family masses, $\tau_t \simeq 0.13$, $\tau_b \simeq 230$ and $\tau_\tau \simeq 1300$, and to the threshold values, $m + m' = m_h \ [\tau = (1+r)^2/4]$, and $m + m' = m_Z \ [\tau = (m_h/m_Z)^2(1+r)^2/4]$.

	ATLAS	CMS	ATLAS+CMS	
\sqrt{s}	7+8 TeV	7+8 TeV	7+8 TeV	
\mathcal{L}	$4.7 + 20.3 \ fb^{-1}$	$5.1 + 19.7 \ fb^{-1}$		
m_h	$125.36 \pm 0.41 \mathrm{GeV}$ [14]	$125.02^{+0.29}_{-0.31} \text{GeV} [12]$	$125.09 \pm 0.24 \mathrm{GeV}$ [13]	
$\mu_{\gamma\gamma}$	$1.17^{+0.28}_{-0.26}$ [14]	1.12 ± 0.24 [12]	$1.13^{+0.24}_{-0.21}$ [35]	
$\mu_{ZZ^* o 4l}$	$1.46^{+0.40}_{-0.34}$ [14]	1.00 ± 0.29 [12]	$1.29^{+0.29}_{-0.25}$ [35]	
μ_{WW^*}	$1.18^{+0.24}_{-0.21}$ [14]	0.83 ± 0.21 [12]	$1.08^{+0.22}_{-0.19}$ [35]	
$\mu_{ au au}$	$1.44^{+0.42}_{-0.37}$ [14]	0.91 ± 0.28 [12]	$1.07^{+0.35}_{-0.28} [35]$	
$\mu_{bar{b}}$	$0.63^{+0.39}_{-0.37}$ [14]	0.84 ± 0.44 [12]	$0.65^{+0.37}_{-0.28} [35]$	
$\mu_{ m global}$	$1.18^{+0.15}_{-0.14}$ [14]	1.00 ± 0.14 [12]	$1.09^{+0.11}_{-0.10} [35]$	
$\mu_{\gamma Z}$	< 11.0 [130]	< 9.5 [131]		
$\mu_{\mu\mu}$	< 7.0 [68]	< 7.4 [69]		
$\Gamma_{\rm invisible}/\Gamma_h$	< 0.29 [132]	< 0.58 [133]		

Table 4. Higgs signal strengths measured by the ATLAS and CMS collaborations at $\sqrt{s} = 7$ and 8 TeV and their combination. The error bars and upper limits correspond respectively to $\pm 1\sigma$ and 95% C.L.. In this paper we adopt the value of the Higgs mass and of the signal strengths from the combined fit of the ATLAS and CMS data, reported in the last column.

the third family, we neglect these modifications. Finally, the $t\bar{t}$ associated production can be corrected by those fermions mixing with the top quark. Concerning the total Higgs decay width Γ_h , the dominant branching ratio into $b\bar{b}$ is affected by fermions mixing with the bottom quark, and the second dominant decay channel into WW^* is not modified by new fermions at leading order. Finally, Γ_h may be modified significantly by new invisible decays, that are possible in the presence of sterile neutrinos. When both $\sigma(pp \to h)$ and Γ_h are close to their SM value, the signal strength in eq. (B.40) reduces to $\mu_{\alpha} \simeq R_{\alpha}$, where

$$R_{\alpha} \equiv \frac{\Gamma(h \to \alpha)}{\Gamma^{\text{SM}}(h \to \alpha)} = \frac{|\mathcal{A}_{\text{SM}}^{\alpha} + \mathcal{A}_{\text{new}}^{\alpha}|^{2} + |\widetilde{\mathcal{A}}_{\text{new}}^{\alpha}|^{2}}{|\mathcal{A}_{\text{SM}}^{\alpha}|^{2}} . \tag{B.41}$$

Here $\mathcal{A}_{\text{new}}^{\alpha}$ and $\widetilde{\mathcal{A}}_{\text{new}}^{\alpha}$ are the parity-even and odd new physics amplitudes, respectively. The approximation $\mu_{\alpha} \simeq R_{\alpha}$ holds for all colourless new fermions, with the possible exception of light sterile neutrinos.

Several groups performed global fits of the Higgs couplings to the SM particles, allowing for deviations in both the fermionic and bosonic decay channels, see e.g. refs. [134–141]. The fit of ref. [142] analyzed deviations in the Higgs couplings in the presence of new fermions only.

	ATLAS	[128]	CMS	[129]
$\Delta\mu_{\alpha}/\mu_{\alpha}$	$300 \ fb^{-1}$	$3000 \ fb^{-1}$	$300 \ fb^{-1}$	$3000 \ fb^{-1}$
$\gamma\gamma$	0.13	0.09	[0.06,0.12]	[0.04,0.08]
ZZ	0.11	0.09	[0.07,0.11]	[0.04, 0.07]
WW	0.13	0.11	[0.06,0.11]	[0.04, 0.07]
au au	0.21	0.19	[0.08, 0.14]	[0.05, 0.08]
$b\bar{b}$	0.26	0.14	[0.11,0.14]	[0.05, 0.07]
γZ	0.46	0.30	[0.62, 0.62]	[0.20,0.24]
$\mu\mu$	0.39	0.16	[0.40,0.42]	[0.20,0.24]
$\Gamma_{ m invisible}/\Gamma_h$	< 0.22	< 0.14	< [0.17, 0.28]	< [0.06, 0.17]

Table 5. Expected relative uncertainty at 1σ on the signal strengths μ_{α} for ATLAS and CMS. The expected precisions correspond to $\sqrt{s} = 14 \,\text{TeV}$ and $\mathcal{L} = 300$ and $3000 \,fb^{-1}$. We also display the expected limit at 95% C.L. on $\Gamma_{\text{invisible}}/\Gamma_h$ for the same luminosities. For CMS the two numbers correspond to two different estimations of the future uncertainties [129].

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- [1] H. Flacher, M. Goebel, J. Haller, A. Hocker, K. Monig and J. Stelzer, Revisiting the Global Electroweak Fit of the Standard Model and Beyond with Gfitter, Eur. Phys. J. C 60 (2009) 543 [Erratum ibid. C 71 (2011) 1718] [arXiv:0811.0009] [INSPIRE].
- [2] DELPHI, OPAL, LEP ELECTROWEAK, ALEPH and L3 collaborations, S. Schael et al., Electroweak Measurements in Electron-Positron Collisions at W-Boson-Pair Energies at LEP, Phys. Rept. 532 (2013) 119 [arXiv:1302.3415] [INSPIRE].
- [3] Particle Data Group collaboration, K.A. Olive et al., Review of Particle Physics, Chin. Phys. C 38 (2014) 090001 [INSPIRE].
- [4] M. Raidal et al., Flavour physics of leptons and dipole moments, Eur. Phys. J. C 57 (2008) 13 [arXiv:0801.1826] [INSPIRE].
- [5] G. Isidori, Y. Nir and G. Perez, Flavor Physics Constraints for Physics Beyond the Standard Model, Ann. Rev. Nucl. Part. Sci. 60 (2010) 355 [arXiv:1002.0900] [INSPIRE].
- [6] D. Toback and L. ŽIvković, Review of Physics Results from the Tevatron: Searches for New Particles and Interactions, Int. J. Mod. Phys. A 30 (2015) 1541007 [arXiv:1409.4910] [INSPIRE].
- [7] Particle Data Group collaboration, K. Nakamura et al., Review of particle physics, J. Phys. G 37 (2010) 075021 [INSPIRE].

- [8] ATLAS collaboration, https://twiki.cern.ch/twiki/bin/view/AtlasPublic.
- [9] CMS collaboration, http://cms-results.web.cern.ch/cms-results/public-results/publications/.
- [10] ATLAS collaboration, Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC, Phys. Lett. B 716 (2012) 1 [arXiv:1207.7214] [INSPIRE].
- [11] CMS collaboration, Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC, Phys. Lett. B 716 (2012) 30 [arXiv:1207.7235] [INSPIRE].
- [12] CMS collaboration, Precise determination of the mass of the Higgs boson and tests of compatibility of its couplings with the standard model predictions using proton collisions at 7 and 8 TeV, Eur. Phys. J. C 75 (2015) 212 [arXiv:1412.8662] [INSPIRE].
- [13] ATLAS and CMS collaborations, Combined Measurement of the Higgs Boson Mass in pp Collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS and CMS Experiments, Phys. Rev. Lett. 114 (2015) 191803 [arXiv:1503.07589] [INSPIRE].
- [14] ATLAS collaboration, Measurements of the Higgs boson production and decay rates and coupling strengths using pp collision data at $\sqrt{s} = 7$ and 8 TeV in the ATLAS experiment, arXiv:1507.04548 [INSPIRE].
- [15] SLD ELECTROWEAK GROUP, DELPHI, ALEPH, SLD, SLD HEAVY FLAVOUR GROUP, OPAL, LEP ELECTROWEAK WORKING GROUP and L3 collaborations, S. Schael et al., Precision electroweak measurements on the Z resonance, Phys. Rept. 427 (2006) 257 [hep-ex/0509008] [INSPIRE].
- [16] D.B. Kaplan, Flavor at SSC energies: A New mechanism for dynamically generated fermion masses, Nucl. Phys. B 365 (1991) 259 [INSPIRE].
- [17] R. Contino and A. Pomarol, Holography for fermions, JHEP 11 (2004) 058 [hep-th/0406257] [INSPIRE].
- [18] M. Cirelli, N. Fornengo and A. Strumia, Minimal dark matter, Nucl. Phys. B 753 (2006) 178 [hep-ph/0512090] [INSPIRE].
- [19] E. Del Nobile, R. Franceschini, D. Pappadopulo and A. Strumia, *Minimal Matter at the Large Hadron Collider*, *Nucl. Phys.* B 826 (2010) 217 [arXiv:0908.1567] [INSPIRE].
- [20] L. Di Luzio, R. Gröber, J.F. Kamenik and M. Nardecchia, Accidental matter at the LHC, JHEP 07 (2015) 074 [arXiv:1504.00359] [INSPIRE].
- [21] I. Picek and B. Radovcic, Nondecoupling of terascale isosinglet quark and rare K- and B-decays, Phys. Rev. D 78 (2008) 015014 [arXiv:0804.2216] [INSPIRE].
- [22] G. Cacciapaglia, A. Deandrea, L. Panizzi, N. Gaur, D. Harada and Y. Okada, *Heavy Vector-like Top Partners at the LHC and flavour constraints*, *JHEP* **03** (2012) 070 [arXiv:1108.6329] [INSPIRE].
- [23] C. Han, A. Kobakhidze, N. Liu, L. Wu and B. Yang, Constraining Top partner and Naturalness at the LHC and TLEP, Nucl. Phys. B 890 (2014) 388 [arXiv:1405.1498] [INSPIRE].
- [24] E. Witten, An SU(2) Anomaly, Phys. Lett. B 117 (1982) 324 [INSPIRE].

- [25] O. Eberhardt et al., Impact of a Higgs boson at a mass of 126 GeV on the standard model with three and four fermion generations, Phys. Rev. Lett. 109 (2012) 241802 [arXiv:1209.1101] [INSPIRE].
- [26] A. Azatov et al., Higgs boson production via vector-like top-partner decays: Diphoton or multilepton plus multijets channels at the LHC, Phys. Rev. D 85 (2012) 115022 [arXiv:1204.0455] [INSPIRE].
- [27] M. Montull, F. Riva, E. Salvioni and R. Torre, *Higgs Couplings in Composite Models*, *Phys. Rev.* D 88 (2013) 095006 [arXiv:1308.0559] [INSPIRE].
- [28] T. Flacke, J.H. Kim, S.J. Lee and S.H. Lim, Constraints on composite quark partners from Higgs searches, JHEP 05 (2014) 123 [arXiv:1312.5316] [INSPIRE].
- [29] C.-Y. Chen, S. Dawson and I.M. Lewis, Top Partners and Higgs Boson Production, Phys. Rev. **D** 90 (2014) 035016 [arXiv:1406.3349] [INSPIRE].
- [30] O. Matsedonskyi, G. Panico and A. Wulzer, On the Interpretation of Top Partners Searches, JHEP 12 (2014) 097 [arXiv:1409.0100] [INSPIRE].
- [31] ATLAS collaboration, Searches for heavy long-lived sleptons and R-Hadrons with the ATLAS detector in pp collisions at $\sqrt{s} = 7$ TeV, Phys. Lett. B 720 (2013) 277 [arXiv:1211.1597] [INSPIRE].
- [32] CMS collaboration, Searches for long-lived charged particles in pp collisions at $\sqrt{s} = 7$ and 8 TeV, JHEP 07 (2013) 122 [arXiv:1305.0491] [INSPIRE].
- [33] ATLAS collaboration, Searches for heavy long-lived charged particles with the ATLAS detector in proton-proton collisions at $\sqrt{s} = 8$ TeV, JHEP **01** (2015) 068 [arXiv:1411.6795] [INSPIRE].
- [34] M. Fairbairn, A.C. Kraan, D.A. Milstead, T. Sjöstrand, P.Z. Skands and T. Sloan, Stable massive particles at colliders, Phys. Rept. 438 (2007) 1 [hep-ph/0611040] [INSPIRE].
- [35] ATLAS and CMS collaborations, Measurements of the Higgs boson production and decay rates and constraints on its couplings from a combined ATLAS and CMS analysis of the LHC pp collision data at $\sqrt{s} = 7$ and 8 TeV, ATLAS-CONF-2015-044 (2015).
- [36] S. Banerjee, M. Frank and S.K. Rai, Higgs data confronts Sequential Fourth Generation Fermions in the Higgs Triplet Model, Phys. Rev. **D** 89 (2014) 075005 [arXiv:1312.4249] [INSPIRE].
- [37] A. Alves, E. Ramirez Barreto, D.A. Camargo and A.G. Dias, A Model with Chiral Quarks of Electric Charges -4/3 and 5/3, JHEP 07 (2013) 129 [arXiv:1306.1275] [INSPIRE].
- [38] ATLAS collaboration, Search for heavy long-lived multi-charged particles in pp collisions at $\sqrt{s} = 8 \text{ TeV}$ using the ATLAS detector, Eur. Phys. J. C 75 (2015) 362 [arXiv:1504.04188] [INSPIRE].
- [39] ATLAS collaboration, Search for Massive Long-lived Highly Ionising Particles with the ATLAS Detector at the LHC, Phys. Lett. B 698 (2011) 353 [arXiv:1102.0459] [INSPIRE].
- [40] D. Wyler and L. Wolfenstein, Massless Neutrinos in Left-Right Symmetric Models, Nucl. Phys. B 218 (1983) 205 [INSPIRE].
- [41] R.N. Mohapatra and J.W.F. Valle, Neutrino Mass and Baryon Number Nonconservation in Superstring Models, Phys. Rev. D 34 (1986) 1642 [INSPIRE].

- [42] M.C. Gonzalez-Garcia and J.W.F. Valle, Fast Decaying Neutrinos and Observable Flavor Violation in a New Class of Majoron Models, Phys. Lett. B 216 (1989) 360 [INSPIRE].
- [43] S.S.C. Law and K.L. McDonald, Generalized inverse seesaw mechanisms, Phys. Rev. D 87 (2013) 113003 [arXiv:1303.4887] [INSPIRE].
- [44] A. de Gouvêa, GeV seesaw, accidentally small neutrino masses and Higgs decays to neutrinos, arXiv:0706.1732 [INSPIRE].
- [45] J.-H. Chen, X.-G. He, J. Tandean and L.-H. Tsai, Effect on Higgs Boson Decays from Large Light-Heavy Neutrino Mixing in Seesaw Models, Phys. Rev. **D** 81 (2010) 113004 [arXiv:1001.5215] [INSPIRE].
- [46] P.S. Bhupal Dev, R. Franceschini and R.N. Mohapatra, Bounds on TeV Seesaw Models from LHC Higgs Data, Phys. Rev. D 86 (2012) 093010 [arXiv:1207.2756] [INSPIRE].
- [47] C.G. Cely, A. Ibarra, E. Molinaro and S.T. Petcov, *Higgs Decays in the Low Scale Type I See-Saw Model*, *Phys. Lett.* B **718** (2013) 957 [arXiv:1208.3654] [INSPIRE].
- [48] S. Antusch and O. Fischer, Testing sterile neutrino extensions of the Standard Model at future lepton colliders, JHEP 05 (2015) 053 [arXiv:1502.05915] [INSPIRE].
- [49] ATLAS collaboration, Search for Majorana neutrino production in pp collisions at \sqrt{s} =7 TeV in dimuon final states with the ATLAS detector, ATLAS-CONF-2012-139 (2012).
- [50] ATLAS collaboration, Search for heavy Majorana neutrinos with the ATLAS detector in pp collisions at $\sqrt{s} = 8$ TeV, JHEP 07 (2015) 162 [arXiv:1506.06020] [INSPIRE].
- [51] CMS collaboration, Search for heavy Majorana neutrinos in $\mu^{\pm}\mu^{\pm}$ + jets and $e^{\pm}e^{\pm}$ + jets events in pp collisions at $\sqrt{s} = 7$ TeV, Phys. Lett. B 717 (2012) 109 [arXiv:1207.6079] [INSPIRE].
- [52] CMS collaboration, Search for heavy Majorana neutrinos in $\mu^{\pm}\mu^{\pm}$ + jets events in proton-proton collisions at $\sqrt{s} = 8$ TeV, Phys. Lett. B 748 (2015) 144 [arXiv:1501.05566] [INSPIRE].
- [53] A. Abada, C. Biggio, F. Bonnet, M.B. Gavela and T. Hambye, $\mu \to e \gamma$ and $\tau \to l \gamma$ decays in the fermion triplet seesaw model, Phys. Rev. D 78 (2008) 033007 [arXiv:0803.0481] [INSPIRE].
- [54] A. Abada, C. Biggio, F. Bonnet, M.B. Gavela and T. Hambye, Low energy effects of neutrino masses, JHEP 12 (2007) 061 [arXiv:0707.4058] [INSPIRE].
- [55] R. Franceschini, T. Hambye and A. Strumia, Type-III see-saw at LHC, Phys. Rev. D 78 (2008) 033002 [arXiv:0805.1613] [INSPIRE].
- [56] L3 collaboration, P. Achard et al., Search for heavy neutral and charged leptons in e⁺e⁻ annihilation at LEP, Phys. Lett. B 517 (2001) 75 [hep-ex/0107015] [INSPIRE].
- [57] CMS collaboration, Search for heavy lepton partners of neutrinos in proton-proton collisions in the context of the type-III seesaw mechanism, Phys. Lett. B 718 (2013) 348 [arXiv:1210.1797] [INSPIRE].
- [58] ATLAS collaboration, Search for type-III Seesaw heavy leptons in pp collisions at $\sqrt{s} = 8 \text{ TeV}$ with the ATLAS Detector, Phys. Rev. **D** 92 (2015) 032001 [arXiv:1506.01839] [INSPIRE].
- [59] A. Falkowski, D.M. Straub and A. Vicente, Vector-like leptons: Higgs decays and collider phenomenology, JHEP 05 (2014) 092 [arXiv:1312.5329] [INSPIRE].

- [60] W. Altmannshofer, M. Bauer and M. Carena, Exotic Leptons: Higgs, Flavor and Collider Phenomenology, JHEP 01 (2014) 060 [arXiv:1308.1987] [INSPIRE].
- [61] T. Ma, B. Zhang and G. Cacciapaglia, Doubly Charged Lepton from an Exotic Doublet at the LHC, Phys. Rev. D 89 (2014) 093022 [arXiv:1404.2375] [INSPIRE].
- [62] A. Delgado, C. Garcia Cely, T. Han and Z. Wang, Phenomenology of a lepton triplet, Phys. Rev. D 84 (2011) 073007 [arXiv:1105.5417] [INSPIRE].
- [63] T. Ma, B. Zhang and G. Cacciapaglia, Triplet with a doubly-charged lepton at the LHC, Phys. Rev. D 89 (2014) 015020 [arXiv:1309.7396] [INSPIRE].
- [64] ATLAS collaboration, Evidence for the Higgs-boson Yukawa coupling to tau leptons with the ATLAS detector, JHEP **04** (2015) 117 [arXiv:1501.04943] [INSPIRE].
- [65] CMS collaboration, Evidence for the 125 GeV Higgs boson decaying to a pair of τ leptons, JHEP **05** (2014) 104 [arXiv:1401.5041] [INSPIRE].
- [66] ATLAS collaboration, Search for lepton-flavour-violating $H \to \mu \tau$ decays of the Higgs boson with the ATLAS detector, arXiv:1508.03372 [INSPIRE].
- [67] CMS collaboration, Search for Lepton-Flavour-Violating Decays of the Higgs Boson, Phys. Lett. B 749 (2015) 337 [arXiv:1502.07400] [INSPIRE].
- [68] ATLAS collaboration, Search for the Standard Model Higgs boson decay to $\mu^+\mu^-$ with the ATLAS detector, Phys. Lett. B 738 (2014) 68 [arXiv:1406.7663] [INSPIRE].
- [69] CMS collaboration, Search for a standard model-like Higgs boson in the μ⁺μ⁻ and e⁺e⁻ decay channels at the LHC, Phys. Lett. B 744 (2015) 184 [arXiv:1410.6679] [INSPIRE].
- [70] K. Agashe, R. Contino, L. Da Rold and A. Pomarol, A Custodial symmetry for Zbb, Phys. Lett. B 641 (2006) 62 [hep-ph/0605341] [INSPIRE].
- [71] F. del Aguila, A. Carmona and J. Santiago, Tau Custodian searches at the LHC, Phys. Lett. B 695 (2011) 449 [arXiv:1007.4206] [INSPIRE].
- [72] A. Carmona and F. Goertz, Custodial Leptons and Higgs Decays, JHEP **04** (2013) 163 [arXiv:1301.5856] [INSPIRE].
- [73] L.G. Almeida, E. Bertuzzo, P.A.N. Machado and R.Z. Funchal, *Does H* $\rightarrow \gamma \gamma$ *Taste like vanilla New Physics?*, *JHEP* 11 (2012) 085 [arXiv:1207.5254] [INSPIRE].
- [74] J. Kearney, A. Pierce and N. Weiner, Vectorlike Fermions and Higgs Couplings, Phys. Rev. D 86 (2012) 113005 [arXiv:1207.7062] [INSPIRE].
- [75] A. Joglekar, P. Schwaller and C.E.M. Wagner, Dark Matter and Enhanced Higgs to Di-photon Rate from Vector-like Leptons, JHEP 12 (2012) 064 [arXiv:1207.4235] [INSPIRE].
- [76] M. Redi, Leptons in Composite MFV, JHEP 09 (2013) 060 [arXiv:1306.1525] [INSPIRE].
- [77] S.P. Martin, A Supersymmetry primer, hep-ph/9709356 [INSPIRE].
- [78] H.K. Dreiner, J.S. Kim and O. Lebedev, First LHC Constraints on Neutralinos, Phys. Lett. B 715 (2012) 199 [arXiv:1206.3096] [INSPIRE].
- [79] B. Ananthanarayan, J. Lahiri, P.N. Pandita and M. Patra, *Invisible decays of the lightest Higgs boson in supersymmetric models*, *Phys. Rev.* **D 87** (2013) 115021 [arXiv:1306.1291] [INSPIRE].

- [80] J.A. Casas, J.M. Moreno, K. Rolbiecki and B. Zaldivar, *Implications of light charginos for Higgs observables, LHC searches and dark matter*, *JHEP* **09** (2013) 099 [arXiv:1305.3274] [INSPIRE].
- [81] B. Batell, S. Jung and C.E.M. Wagner, Very Light Charginos and Higgs Decays, JHEP 12 (2013) 075 [arXiv:1309.2297] [INSPIRE].
- [82] F. del Aguila, M. Pérez-Victoria and J. Santiago, Observable contributions of new exotic quarks to quark mixing, JHEP 09 (2000) 011 [hep-ph/0007316] [INSPIRE].
- [83] J.A. Aguilar-Saavedra, Identifying top partners at LHC, JHEP 11 (2009) 030 [arXiv:0907.3155] [INSPIRE].
- [84] G. Cacciapaglia, A. Deandrea, D. Harada and Y. Okada, Bounds and Decays of New Heavy Vector-like Top Partners, JHEP 11 (2010) 159 [arXiv:1007.2933] [INSPIRE].
- [85] S. Gopalakrishna, T. Mandal, S. Mitra and R. Tibrewala, *LHC Signatures of a Vector-like* b', *Phys. Rev.* **D 84** (2011) 055001 [arXiv:1107.4306] [INSPIRE].
- [86] Y. Okada and L. Panizzi, LHC signatures of vector-like quarks, Adv. High Energy Phys. 2013 (2013) 364936 [arXiv:1207.5607] [INSPIRE].
- [87] J.A. Aguilar-Saavedra, R. Benbrik, S. Heinemeyer and M. Pérez-Victoria, Handbook of vectorlike quarks: Mixing and single production, Phys. Rev. D 88 (2013) 094010 [arXiv:1306.0572] [INSPIRE].
- [88] S. Gopalakrishna, T. Mandal, S. Mitra and G. Moreau, *LHC Signatures of Warped-space Vectorlike Quarks*, *JHEP* **08** (2014) 079 [arXiv:1306.2656] [INSPIRE].
- [89] ATLAS collaboration, Search for production of vector-like quark pairs and of four top quarks in the lepton plus jets final state in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector, ATLAS-CONF-2015-012 (2015).
- [90] CMS collaboration, Search for vector-like T quarks decaying to top quarks and Higgs bosons in the all-hadronic channel using jet substructure, JHEP 06 (2015) 080 [arXiv:1503.01952] [INSPIRE].
- [91] ATLAS collaboration, Search for vectorlike B quarks in events with one isolated lepton, missing transverse momentum and jets at $\sqrt{s} = 8$ TeV with the ATLAS detector, Phys. Rev. **D** 91 (2015) 112011 [arXiv:1503.05425] [INSPIRE].
- [92] ATLAS collaboration, Search for pair and single production of new heavy quarks that decay to a Z boson and a third-generation quark in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector, JHEP 11 (2014) 104 [arXiv:1409.5500] [INSPIRE].
- [93] CMS collaboration, Search for vector-like quarks in final states with a single lepton and jets in pp collisions at $\sqrt{s} = 8$ TeV, CMS-PAS-B2G-12-017 (2012).
- [94] CMS collaboration, Search for pair-produced vector-like quarks of charge -1/3 decaying to bH using boosted Higgs jet-tagging in pp collisions at $\sqrt{s} = 8 \text{ TeV}$, (2014).
- [95] CMS collaboration, Search for pair-produced vector-like quarks of charge -1/3 in lepton+jets final state in pp collisions at $\sqrt{s} = 8 \text{ TeV}$, (2012).
- [96] CMS collaboration, Search for Vector-Like Charge 2/3 T Quarks in Proton-Proton Collisions at $\sqrt{s} = 8$ TeV, arXiv:1509.04177 [INSPIRE].
- [97] R. Contino, L. Da Rold and A. Pomarol, Light custodians in natural composite Higgs models, Phys. Rev. D 75 (2007) 055014 [hep-ph/0612048] [INSPIRE].

- [98] A. Pomarol and J. Serra, Top Quark Compositeness: Feasibility and Implications, Phys. Rev. D 78 (2008) 074026 [arXiv:0806.3247] [INSPIRE].
- [99] E. Bertuzzo, P.A.N. Machado and R. Zukanovich Funchal, Can New Colored Particles Illuminate the Higgs?, JHEP **02** (2013) 086 [arXiv:1209.6359] [INSPIRE].
- [100] O. Matsedonskyi, F. Riva and T. Vantalon, Composite Charge 8/3 Resonances at the LHC, JHEP 04 (2014) 059 [arXiv:1401.3740] [INSPIRE].
- [101] G. Cacciapaglia, A. Deandrea, N. Gaur, D. Harada, Y. Okada and L. Panizzi, Interplay of vector-like top partner multiplets in a realistic mixing set-up, JHEP 09 (2015) 012 [arXiv:1502.00370] [INSPIRE].
- [102] M. Gillioz, A Light composite Higgs boson facing electroweak precision tests, Phys. Rev. D 80 (2009) 055003 [arXiv:0806.3450] [INSPIRE].
- [103] A. Azatov and J. Galloway, Light Custodians and Higgs Physics in Composite Models, Phys. Rev. D 85 (2012) 055013 [arXiv:1110.5646] [INSPIRE].
- [104] J. Elias-Miró, J.R. Espinosa, E. Masso and A. Pomarol, Renormalization of dimension-six operators relevant for the Higgs decays $h \to \gamma\gamma, \gamma Z, JHEP$ 08 (2013) 033 [arXiv:1302.5661] [INSPIRE].
- [105] M.E. Peskin and T. Takeuchi, A New constraint on a strongly interacting Higgs sector, Phys. Rev. Lett. 65 (1990) 964 [INSPIRE].
- [106] G. Altarelli and R. Barbieri, Vacuum polarization effects of new physics on electroweak processes, Phys. Lett. B 253 (1991) 161 [INSPIRE].
- [107] M.E. Peskin and T. Takeuchi, Estimation of oblique electroweak corrections, Phys. Rev. D 46 (1992) 381 [INSPIRE].
- [108] R. Barbieri, A. Pomarol, R. Rattazzi and A. Strumia, Electroweak symmetry breaking after LEP-1 and LEP-2, Nucl. Phys. B 703 (2004) 127 [hep-ph/0405040] [INSPIRE].
- [109] GFITTER GROUP collaboration, M. Baak et al., The global electroweak fit at NNLO and prospects for the LHC and ILC, Eur. Phys. J. C 74 (2014) 3046 [arXiv:1407.3792] [INSPIRE].
- [110] M. Ciuchini, E. Franco, S. Mishima and L. Silvestrini, Electroweak Precision Observables, New Physics and the Nature of a 126 GeV Higgs Boson, JHEP 08 (2013) 106 [arXiv:1306.4644] [INSPIRE].
- [111] S. Gori, J. Gu and L.-T. Wang, The Zbb Couplings at Future e^+e^- Colliders, arXiv:1508.07010 [INSPIRE].
- [112] P. Bamert, C.P. Burgess, J.M. Cline, D. London and E. Nardi, R(b) and new physics: A Comprehensive analysis, Phys. Rev. D 54 (1996) 4275 [hep-ph/9602438] [INSPIRE].
- [113] J.R. Ellis, M.K. Gaillard and D.V. Nanopoulos, A Phenomenological Profile of the Higgs Boson, Nucl. Phys. B 106 (1976) 292 [INSPIRE].
- [114] M.A. Shifman, A.I. Vainshtein, M.B. Voloshin and V.I. Zakharov, Low-Energy Theorems for Higgs Boson Couplings to Photons, Sov. J. Nucl. Phys. 30 (1979) 711 [INSPIRE].
- [115] B.A. Kniehl and M. Spira, Low-energy theorems in Higgs physics, Z. Phys. C 69 (1995) 77 [hep-ph/9505225] [INSPIRE].
- [116] M. Carena, I. Low and C.E.M. Wagner, *Implications of a Modified Higgs to Diphoton Decay Width*, *JHEP* **08** (2012) 060 [arXiv:1206.1082] [INSPIRE].

- [117] M. Gillioz, R. Grober, C. Grojean, M. Muhlleitner and E. Salvioni, *Higgs Low-Energy Theorem (and its corrections) in Composite Models*, *JHEP* **10** (2012) 004 [arXiv:1206.7120] [INSPIRE].
- [118] M.B. Voloshin, *CP Violation in Higgs Diphoton Decay in Models with Vectorlike Heavy Fermions*, *Phys. Rev.* **D 86** (2012) 093016 [arXiv:1208.4303] [INSPIRE].
- [119] M.B. Gavela, G. Girardi, C. Malleville and P. Sorba, A Nonlinear R(xi) Gauge Condition for the Electroweak $SU(2) \times U(1)$ Model, Nucl. Phys. B 193 (1981) 257 [INSPIRE].
- [120] R.N. Cahn, M.S. Chanowitz and N. Fleishon, Higgs Particle Production by $Z \to H\gamma$, Phys. Lett. **B 82** (1979) 113 [INSPIRE].
- [121] L. Bergstrom and G. Hulth, Induced Higgs Couplings to Neutral Bosons in e⁺e⁻ Collisions, Nucl. Phys. B 259 (1985) 137 [Erratum ibid. B 276 (1986) 744] [INSPIRE].
- [122] G. Passarino and M.J.G. Veltman, One Loop Corrections for e^+e^- Annihilation Into $\mu^+\mu^-$ in the Weinberg Model, Nucl. Phys. **B 160** (1979) 151 [INSPIRE].
- [123] D.Y. Bardin and G. Passarino, International Series of Monographs on Physics. Vol. 104: The standard model in the making: Precision study of the electroweak interactions, Clarendon Press, London U.K. (1999).
- [124] A. Denner, Techniques for calculation of electroweak radiative corrections at the one loop level and results for W physics at LEP-200, Fortsch. Phys. 41 (1993) 307 [arXiv:0709.1075] [INSPIRE].
- [125] A. Djouadi, V. Driesen, W. Hollik and J. Rosiek, Associated production of Higgs bosons and a photon in high-energy e⁺e⁻ collisions, Nucl. Phys. **B 491** (1997) 68 [hep-ph/9609420] [INSPIRE].
- [126] A. Djouadi, V. Driesen, W. Hollik and A. Kraft, The Higgs photon Z boson coupling revisited, Eur. Phys. J. C 1 (1998) 163 [hep-ph/9701342] [INSPIRE].
- [127] J. Cao, L. Wu, P. Wu and J.M. Yang, The Z+photon and diphoton decays of the Higgs boson as a joint probe of low energy SUSY models, JHEP 09 (2013) 043 [arXiv:1301.4641] [INSPIRE].
- [128] ATLAS collaboration, Projections for measurements of Higgs boson signal strengths and coupling parameters with the ATLAS detector at a HL-LHC, ATL-PHYS-PUB-2014-016 (2014).
- [129] CMS collaboration, Projected Performance of an Upgraded CMS Detector at the LHC and HL-LHC: Contribution to the Snowmass Process, arXiv:1307.7135 [INSPIRE].
- [130] ATLAS collaboration, Search for Higgs boson decays to a photon and a Z boson in pp collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS detector, Phys. Lett. B 732 (2014) 8 [arXiv:1402.3051] [INSPIRE].
- [131] CMS collaboration, Search for a Higgs boson decaying into a Z and a photon in pp collisions at $\sqrt{s} = 7$ and 8 TeV, Phys. Lett. B 726 (2013) 587 [arXiv:1307.5515] [INSPIRE].
- [132] ATLAS collaboration, Search for an Invisibly Decaying Higgs Boson Produced via Vector Boson Fusion in pp Collisions at $\sqrt{s} = 8$ TeV using the ATLAS Detector at the LHC, ATLAS-CONF-2015-004 (2015).

- [133] CMS collaboration, Search for invisible decays of Higgs bosons in the vector boson fusion and associated ZH production modes, Eur. Phys. J. C 74 (2014) 2980 [arXiv:1404.1344] [INSPIRE].
- [134] J.R. Espinosa, C. Grojean, M. Muhlleitner and M. Trott, First Glimpses at Higgs' face, JHEP 12 (2012) 045 [arXiv:1207.1717] [INSPIRE].
- [135] D. Carmi, A. Falkowski, E. Kuflik, T. Volansky and J. Zupan, Higgs After the Discovery: A Status Report, JHEP 10 (2012) 196 [arXiv:1207.1718] [INSPIRE].
- [136] G. Cacciapaglia, A. Deandrea, G.D. La Rochelle and J.-B. Flament, *Higgs couplings beyond the Standard Model*, *JHEP* **03** (2013) 029 [arXiv:1210.8120] [INSPIRE].
- [137] A. Azatov and J. Galloway, Electroweak Symmetry Breaking and the Higgs Boson: Confronting Theories at Colliders, Int. J. Mod. Phys. A 28 (2013) 1330004 [arXiv:1212.1380] [INSPIRE].
- [138] A. Falkowski, F. Riva and A. Urbano, Higgs at last, JHEP 11 (2013) 111 [arXiv:1303.1812] [INSPIRE].
- [139] P.P. Giardino, K. Kannike, I. Masina, M. Raidal and A. Strumia, The universal Higgs fit, JHEP 05 (2014) 046 [arXiv:1303.3570] [INSPIRE].
- [140] A. Djouadi and G. Moreau, The couplings of the Higgs boson and its CP properties from fits of the signal strengths and their ratios at the 7 + 8 TeV LHC, Eur. Phys. J. C 73 (2013) 2512 [arXiv:1303.6591] [INSPIRE].
- [141] G. Bélanger, B. Dumont, U. Ellwanger, J.F. Gunion and S. Kraml, Global fit to Higgs signal strengths and couplings and implications for extended Higgs sectors, Phys. Rev. D 88 (2013) 075008 [arXiv:1306.2941] [INSPIRE].
- [142] G. Moreau, Constraining extra-fermion(s) from the Higgs boson data, Phys. Rev. D 87 (2013) 015027 [arXiv:1210.3977] [INSPIRE].