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Assembling ZnO Nanorods into Microflowers through a Facile Solution Strategy: Morphology Control and Cathodoluminescence Properties

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Abstract: In this work, flowerlike ZnO micro/nanostructures assembled from nanorods are obtained through a facile hydrothermal route. The experimental results indicated that the as-synthesized ZnO microflowers have an average diameter of 2 μ m, composed of nanorods of an average diameter of 200 nm and a tapered morphology. ZnO with other morphologies were also obtained by varying the reaction conditions. Systematical condition-dependent experiments were conducted to reveal the growth mechansim of the microflowers. It is suggested that the zinc source types, solution pH value, and reaction temperature, as well as reaction time are responsible for the variations of ZnO morphology. Luminescence properties of ZnO microflowers were investigated through monitoring different parts of nanorods, showing good optical quality.

Keywords: Microflowers; Solution growth; ZnO; Cathodoluminescence

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The size and shape of low dimensional micro/nanoscale materials have a crucial influence on their physical and chemical properties, and on the properties of the integrated nanodevices due to the significant surface effect and quantum size effect [1-3]. In particular, hierarchical assembly of micro/nanoscale building blocks with tunable dimension and structure is essential for the fabrication of micro/nanodevices [4, 5]. Inspired by this, hierarchical and complex micro/nanostructures have been the focus of intensive research in recent years. Fan et al. reported the assembly of ZnO nanorods on SnO_2 nanowire backbones through a two-step growth process that combines the vapor transport and deposition process and a hydrothermal method [6]. Dick et al. synthesized heterogeneous GaP-GaAsP nanotrees via a stepwise deposition of gold nanoparticles on GaP nanowires [7]. Ni et al. reported flowerlike ZnO-ZnS heterogeneous microstructures built up by ZnS-

particle-strewn on ZnO microrods by a hydrothermal route [8]. Some other flowerlike and hierarchical micro/ nanostructures (including metal or ternary compounds) were also reported, such as Au [9], Bi_2SiO_5 [10], Bi_2S_3 [11], ZnS [12], InP [13], SnO₂ [14] and ZnS-ZnO heterostructures [15].

ZnO, as an important semiconductor material, has a wide variety of applications in pigments [16], field effect transistors [17], field emitters [18], ultraviolet detectors [19], cosmetics [20] and energy storage [21-23]. To date, various splendid morphologies of ZnO nanostructures have been reported by different synthesis approaches including thermal evaporation [24-26], hydrothermal reaction [27-29], electrochemical deposition [30-31]. Among them, the solution approach has been proved to be an efficient way with outstanding advantages, such as simplicity, commercial feasibility and potential for scaling up.

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In the literature, there are some reports about ZnO micro/nanoflowers. Ogale et al. synthesized ZnO nanoflowers loaded with gold nanoparticles at 180°C and studied the power conversion efficiency of dyesensitized solar cells based on the ZnO nanoflowers with gold nanoparticles [32]. Tang's group reported 3D ZnO flowerlike nanostructure and the nanorods assembling flowers possess hexagonal shapes [33]. Prabakar and his coworkers synthesized ZnO nanoflowers through spin coating a film seed layer on FTO substrate [34]. Jiang et al. also reported ZnO nanoflowers through a hydrothermal method [35]. However, in the reports mentioned above, the nanorods composing the flowers are either smooth top or hexagonal shape: none of them investigated the effect of nanorod diameter on the luminescence property. In this study, we reported the fabrication of flowerlike ZnO micro/nanostructures through an assembly of the nanorods with the tip tops via a simple solution strategy without using any surfactant or template at mild temperature. The morphologies of the ZnO micro/nanostructures can be tunable by adjusting the growth parameters, such as solution basicity, reaction temperature and time. Cathodoluminescence (CL) properties of the as-prepared ZnO products were investigated by comparing the spectra recorded at different parts of the nanorods. Our strategy of assembly of nanorods into microflowers can be extended to some other compounds and even complex micro/nanostructures with ultrahigh surface areas towards the exploration of their unique functional properties.

ZnO microflowers were fabricated via a simple hydrothermal route. All reagents are analytical grade and were used without further purification. In a typical procedure, 0.352 g zinc acetate dehydrate $(Zn(Ac)_2 \cdot 2H_2O)$ was first dissolved into 30 ml de-ionized water and 1.12 g KOH was dissolved into 5 ml de-ionized water. The solution of KOH was then added dropwise into the above zinc acetate solution under continuous magnetic stirring for 10 minutes at room temperature. Afterward, the above mixture of solution was transferred into a stainless steel autoclave with a 50 ml PTFE container and maintained at 150°C for 20 h. After the reaction, the autoclave was naturally cooled to room temperature. The resulting products were collected, washed several times with de-ionized water and alcohol in sequence, and finally dried at 60°C for 12 h.

The phase of the as-obtained products were examined using x-ray powder diffraction (XRD, Rigaku DmaxrB, CuK α radiation, λ =0.1542nm, 40KV, 100mA). The morphology and microstructure of the samples were characterized with scanning electron microscope (SEM, Hitachi-4800) and transmission electron microscope (TEM, JEOL-3010). The samples for TEM were prepared by suspending the synthesized ZnO product in absolute ethanol by ultrasonic treatment for 5 minutes and then transferring onto a carbon-coated copper grid. The copper grid was air-dried under ambient conditions. Cathodoluminescence (CL) properties were investigated using a thermal field emission scanning electron microscope (Hitachi S4200) equipped with a CL system. The CL spectra and images were taken at room temperature at 3 kV and 320 pA.

Figure 1 shows a typical XRD pattern of the asobtained product. All of the peaks match well with the bulk ZnO, which can be indexed to the hexagonal wurtzite structure of ZnO (JCPDS card No. 05-0664). No peaks were observed from other impurities such as $Zn(OH)_2$, which suggests that as-synthesized product is pure ZnO.



Fig. 1 XRD pattern of the as-synthesized ZnO microflowers.

Representative morphologies of the as-synthesized ZnO micro/nanostructures, as revealed by SEM, are shown in Fig. 2(a)-(b). As seen from the low magnification SEM images (Fig. 2(a)), uniform flowerlike nanostructures were obtained with high yield. These flowerlike structures have an average diameter of $2 \ \mu m$ and are composed of nanorods radially branching out from the center (see in Fig. 2(b)). The average diameter of each nanorod is 200 nm and with a sharp tips. It is realized that this kind of tapered nanorod has a different luminescence property, which will be discussed later. Figure 2(c) shows a typical TEM image of a single microflower. The high resolution lattice TEM (HRTEM) image taken in the red square region (shown in Fig. 2(d)) gives a lattice fringe separation of 0.52 nm, corresponding to the (0001) spacing. The corresponding fast Fourier transform (FFT) pattern (the inset in Fig. 2(d) confirms a single crystal structure with the growth direction along the [0001] direction.

In order to investigate the formation process of the ZnO microflowers, a series of controlled experiments were performed through adjusting several growth parameters, such as reaction temperature, reaction time, dose of the alkali solution and organic solvent. First, SEM images of the products from time-dependent experiments are shown in Fig. 3. When the reaction time



Fig. 2 SEM and TEM images of as-synthesized ZnO microflowers: (a) Low magnification SEM images; (b) High magnification SEM images of single microflower; (c) Low magnification TEM image of single microflower; (d) HRTEM image in Fig. 2(c). The inset is the corresponding SAED pattern.

is 5 h, only a few microflowers appear while the majorities are incomplete flowers or disperse nanorods (indicated by the blue circle in Fig. 3(a)). With the reaction



Fig. 3 SEM images of the products from reaction time dependent experiments: (a) 5 h; (b) 20 h; (c) 30 h and (d) 48 h.

time increased to 20 h, the as-obtained product is composed of nearly pure microflowers with an average diameter of 2 μ m, as shown in Fig. 3(b). With further elongation of the reaction time to 30 h (Fig. 3(c)) and even to 48 h (Fig. 3(d)), the flowerlike morphology still retains whereas the nanorods tend to bundle together forming a sheet-like structure.

Since the growth of micro/nanostructure undergoes a series of continuous reaction process for nucleation and growth, reaction temperature plays an important role in tailoring the final morphology. The above-shown microflowers were formed from a reaction at 150°C for 20 h. When the temperature was reduced to 100°C with other conditions remain unchanged, the obtained microflowers were not uniform, and more than one microflowers attach each other, as revealed in Fig. 4(a). At the elevated temperature of 180°C, some small particles and rods appeared lying randomly on the microflowers. Further increasing the temperature to 220°C resulted in disappearance of the microflowers and only some microcrystals or nanorods were observed. Hence, the optimum temperature is determined to be 150°C.

Furthermore, the dosage of alkali is expected to have a decisive influence on morphology of the resultant



Fig. 4 SEM images of the products from reaction temperature dependent experiments: (a) 100° C; (b) 150° C; (c) 180° Cand (d) 220° C.

products due to the participation of OH⁻ ions in the nucleation and formation of the seeds. SEM images of the as-obtained products with different dosage of akali (0.6 g and 1.0 g) are shown in Fig. 5(a)-(b). One can see that a small amount of alkali (0.6 g) resulted in only some sheets and poor-defined particles. Finally, different zinc salts were also found to induce changes in the morphology of the as-obtained product. The SEM image in Fig. 5(c) shows that only separated nanorods can be seen, without the assembly into microflowers, when $Zn(Ac)_2$ was replaced by $ZnSO_4$ with other growth conditions kept the same as in Fig. 2. Under the condition that $Zn(NO_3)_2$ was used, microflowers appeared but the nanorods are connected each other into sheets, as indicated by the rectangle in Fig. 5(d). Finally, as a typical additive in hydrothermal growth of ZnO nanorods, effect of hexamethylenetetramine (HMT) on the morphology of the as-synthesized product was also studied. It is found that addition of HMT also prevents the formation of microflowers (see Fig. 5(e)-(f)). These results reveal that the resultant morphology of the as-obtained product is a result of a delicate interplay of various parameters; On the other hand, such dependence allows one to tune the desired structure of the final product for applications in which either a high aspect ratio or a high structural integrity is desired.

The formation process of crystals involves two stages: nucleation and growth. External parameters may pose dramatic effects on the size and morphology of the final crystal depending on the degree of participation during the nucleation and initial growth. The overall reaction for ZnO micro/nanostructures in an alkaline solution can be proposed as follows:

$$\operatorname{Zn}^{2+} + 2\operatorname{OH}^{-} \longrightarrow \operatorname{Zn}(\operatorname{OH})_{2}$$
 (1)

$$\operatorname{Zn}(\operatorname{OH})_2 + 2\operatorname{OH}^- \longrightarrow \operatorname{Zn}(\operatorname{OH})_4^{2-}$$
 (2)

$$\operatorname{Zn}(\operatorname{OH})_4^{2-} \longrightarrow \operatorname{ZnO} + 2\operatorname{H}_2\operatorname{O} + 2\operatorname{OH}^-$$
 (3)

In literature, Kim et al. synthesized ZnO nanoflower arrays through using a pre-patterned PMMA mask on the ZnO seed layer deposited on fluorine-doped tin oxide (FTO) glass [36]. Zhang et al. reported flowerlike nanostructures of ZnO by treating $Zn(OH)_4^{2-}$ precursor in water at 180°C, and investigated the shape evolution induced by several growth parameters [37]. Ni et al. proposed the formation of ZnO flower-like structures is sensitive to the amount of ammonia used in the system [8]. This is also the case in our experiment. When the quantity of alkali is small, only some sheets and particles appear, as shown in Fig. 5(a)-(b). Due to the coordination effect of OH^- ions to Zn^{2+} ions, it is possible that OH⁻ ions are adsorbed at the circumference of Zn ions of the ZnO nuclei. Due to the spatial hindrance, ZnO grew only along certain directions, which leads the formation of flowerlike structure [8]. Gao et al believed that the introduction of HMT has an important



Fig. 5 SEM images of the as-obtained product obtained with different dosage of alkali (0.6 g and 1.0 g) (a-b); with different types of zinc sources $[ZnSO_4 \text{ and } Zn(NO_3)_2]$ (c-d) and with addition of HMT (e-f).

influence on the formation of ZnO flowerlike structures [38]. However, this is not the case in our experiments.

Figure 6 shows a typical CL spectrum obtained at room temperature from the ZnO microflowers. The corresponding SEM image is shown in Fig. 6(a). The CL spectra recorded from five spots corresponding to different diameters on a nanorod are recorded. Clearly all spectra have an ultraviolet emission peak at ~ 388 nm and a broad green emission peak ranging from 521 to 539 nm. It is noted that the emission intensity become lower with decreasing diameter. Location of visible emission peaks from spot 1 to spot 5 are 521 nm, 539 nm, 537 nm, 532 nm and 528 nm, respectively. The UV emission peak of the microflowers in this work is 388 nm, which is in good agreement with the typically reported free exciton peak position and could be attributed to UV near-band edge emission [39]. The impurities and structural defects, such as oxygen vacancies and so forth, are responsible for the deep level or trap-state emission in the visible range [40]. For the visible green emission peaks in CL spectrum, it is generally accepted that the green emission originates from the radiative recombination of a photogenerated hole with an electron occupying the oxygen vacancy [41-42]. Li et al. attributed the green emission to point defects, which can easily form recombination center [43]. In our experiment, when the as-synthesized ZnO nanostructures were dried at 60°C for 12 h in air ambient, the surface of the microflowers would get rougher, revealing that there are abundant surface defects in the product. Taking large surface volume ratio in microflower





Fig. 6 SEM image (a) and CL image (b) of the ZnO microflowers recorded at 3 kV and 320 pA and at room temperature.

structures into account, the broadening and enhancement of the green emission peak can be ascribed to abundant surface defects. Abundant defects at the surface of ZnO microflowers can provide new states as visible luminescence centers and broaden the visible emission band.

In summary, we reported an easy and efficient hydrothermal method to synthesize ZnO microflowers through the self-assembly of nanorods at a mild temperature (150°C). A series of control experiments by adjusting several growth parameters were conducted which allows a systematic investigation of the growth process. Optical properties of the as-synthesized ZnO microflowers have been studied, which show both sharp ultraviolet emission peaks and broad green peaks. The emission intensity lowers with decreasing diameter. The ZnO microflowers obtained herein may have potential applications in photocatalyst or photoelectrochemical cells.

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