



## Performance of Irikura Recipe Rupture Model Generator in Earthquake Ground Motion Simulations with Graves and Pitarka Hybrid Approach

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**Abstract**—We analyzed the performance of the Irikura and Miyake (Pure and Applied Geophysics 168(2011):85–104, 2011) (IM2011) asperity-based kinematic rupture model generator, as implemented in the hybrid broadband ground motion simulation methodology of Graves and Pitarka (Bulletin of the Seismological Society of America 100(5A):2095–2123, 2010), for simulating ground motion from crustal earthquakes of intermediate size. The primary objective of our study is to investigate the transportability of IM2011 into the framework used by the Southern California Earthquake Center broadband simulation platform. In our analysis, we performed broadband (0–20 Hz) ground motion simulations for a suite of M6.7 crustal scenario earthquakes in a hard rock seismic velocity structure using rupture models produced with both IM2011 and the rupture generation method of Graves and Pitarka (Bulletin of the Seismological Society of America, 2016) (GP2016). The level of simulated ground motions for the two approaches compare favorably with median estimates obtained from the 2014 Next Generation Attenuation-West2 Project (NGA-West2) ground motion prediction equations (GMPEs) over the frequency band 0.1–10 Hz and for distances out to 22 km from the fault. We also found that, compared to GP2016, IM2011 generates ground motion with larger variability, particularly at near-fault distances (<12 km) and at long periods (>1 s). For this specific scenario, the largest systematic difference in ground motion level for the two approaches occurs in the period band 1–3 s where the IM2011 motions are about 20–30% lower than those for GP2016. We found that increasing the rupture speed by 20% on the asperities in IM2011 produced ground motions in the 1–3 s bandwidth that are in much closer agreement with the GMPE medians and similar to those obtained with GP2016. The potential implications of this modification for other rupture mechanisms and magnitudes are not yet fully understood, and this topic is the subject of ongoing study. We concluded that IM2011 rupture generator performs well in ground motion simulations using Graves and Pitarka hybrid method. Therefore, we recommend it to be considered for inclusion into the framework used by the Southern California Earthquake Center broadband simulation platform.

### 1. Introduction

The broadband ground motion simulation method of Graves and Pitarka (2010, 2016) and that of Irikura and Miyake (2011, IM2011 hereafter, also known as Irikura recipe) use similar time-domain summation schemes based on kinematic rupture descriptions. Both methods compute ground motion acceleration time series using rupture kinematics for modeling the source, and Green's functions for modeling wave propagation. IM2011 is very efficient in deterministic estimates of near-fault ground motion at target sites, in particular, accurate simulation of near-fault ground motion pulses associated with fault rupture directivity effect. Earlier versions of the Irikura and Miyake method employed empirical Green's functions (e.g., Irikura et al. 2002). However, the scarcity of empirical Green's functions with desired magnitude, distance, focal mechanism and source function motivated several modifications of the method including the use of synthetic Green's functions for periods longer than 1 s (e.g., Kamae et al. 1998; Pitarka et al. 2002). At shorter periods, the method relies on the use of stochastic Green's functions, and the full broadband response is obtained using a hybrid approach. These modifications as well as the adoption of improved empirical relations of rupture parameters extended the method's applicability to earthquakes of various types and with complex rupture. (e.g., Irikura et al. 2002, 2004; Miyake et al. 2003; Irikura 2004; Pitarka et al. 2000; Morikawa et al. 2011; Pitarka et al. 2012; Kurahashi and Irikura 2013; Pulido et al. 2015; Iwaki et al. 2016).

In this article, we analyze the performance of the IM2011 asperity-based earthquake rupture model generator implemented in the hybrid broadband ground motion simulation methodology of Graves

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and Pitarka (2010). The term hybrid simulation procedure refers to a general approach where the long period motions (typically  $>1$  s) are computed using a more deterministic approach and the shorter period motions (typically  $<1$  s) are computed using a more stochastic approach. The full broadband response is then obtained by filtering and summing the individual responses. The IM2011 hybrid method has been validated against several earthquakes in a broad magnitude range (e.g., Iwaki et al. 2016). The method is widely used to model and simulate ground motion from earthquakes in Japan (e.g., Morikawa et al. 2011). An essential part of the method is its kinematic rupture generation technique, which is based on a deterministic rupture asperity modeling approach. The source model simplicity and efficiency of the IM2011 at reproducing ground motion from earthquakes recorded in Japan makes it attractive to developers and users of the Southern California Earthquake Center Broadband Platform (SCEC BBP) (Maechling et al. 2015; Graves and Pitarka 2015; Olsen and Takedatsu 2015; Schmedes et al. 2010). The SCEC BBP is being developed as a computational tool for simulating broad band ground motion, with both scientific and engineering applications.

The primary objective of our study is to investigate the transportability of the IM2011 rupture generation process to broadband simulation methods used by the SCEC BBP. Here we test it using the Graves and Pitarka (2010) hybrid simulation method. At longer periods ( $>1$  s), the simulation approach of Graves and Pitarka (2010) is very similar to IM2011; that is, the full kinematic rupture description is convolved with full waveform Green's functions to obtain the ground motion response. However, at shorter periods, the Graves and Pitarka (2010) approach uses a semi-stochastic procedure (following from Boore 1983) to generate the response, which is different from the stochastic procedure used in the Irikura recipe. Therefore, part of our analysis includes formulating the IM2011 rupture such that it can be inserted into the Graves and Pitarka (2010) method at shorter periods. This process is relatively straightforward, but does require some care to insure that all parameters, and in particular the rupture speed, are properly represented.

To test the implementation process, we performed broadband (0–20 Hz) ground motion simulations for

a series of M6.7 scenario oblique-slip earthquakes with rupture models produced with both IM2011 and rupture generation method of Graves and Pitarka (2016, GP2016 hereafter). The kinematic ruptures for both methods are formatted into the standard rupture format (SRF), which is the rupture format used by all the simulations codes on the SCEC BBP. Ground motions from the two rupture model approaches are generated using the same hybrid simulation approach as described in Graves and Pitarka (2010). At long periods ( $T > 1$  s), we compute full waveform Green's functions (GFs) for the prescribed 1D seismic velocity model and these GFs are convolved with the respective kinematic rupture descriptions. At short periods ( $T < 1$  s), the rupture models are resampled onto a  $2 \text{ km} \times 2 \text{ km}$  grid and the ground motions are computed using the Graves and Pitarka (2010) stochastic formulation. The full broadband response is obtained by summing the individual long- and short-period responses using a set of match filters with a crossover set at 1 s.

In the sections that follow, we first provide an overview of the IM2011 and GP2016 rupture generator procedures. We then describe the scenario ground motion calculations for a hypothetical M6.7 oblique-slip rupture that are used to examine and compare the two rupture generator methodologies. The simulation results are also compared with estimates obtained from four NGA-West2 ground motions prediction equations (GMPEs), which provide a common reference point for analyzing the performance of the different approaches. Based on these comparisons, we also examine a modified version of IM2011 where the rupture speed is increased by 20% across the large-slip asperities, which results in an improved fit to the GMPE levels in the 1–3 s period bandwidth. We conclude with a summary of our findings based on this initial set of assessments, along with recommendations to guide further testing and validation of the rupture generator methodologies.

## 2. Methods: IM2011 and GP2016 Rupture Model Generators

IM2011 is based on the multiple-asperity concept of fault rupture. This concept is an extension of the

single-asperity model of Das and Kostrov (1986). IM2011 uses three sets of parameters, named outer, inner and extra fault parameters, to characterize the fault rupture kinematics. The outer parameters characterize the rupture area and magnitude, and the inner parameters define the spatial and temporal characteristics of slip distribution determined from estimated stress drop in the asperities and background areas of the fault. The extra fault parameters are the rupture nucleation location (hypocenter), rupture initiation point in each asperity, and rupture velocity. The outer and inner fault parameters are linked to the total seismic moment following empirical scaling laws. The number of asperities, total asperity area, and asperity slip contrast follows Somerville et al. (1999). These kinematic rupture parameters have been found to be compatible with those obtained from rupture dynamics modeling of planar faults with multiple asperities. (e.g., Dalguer et al. 2004). In contrast to other rupture generation methods, the rupture kinematics in IM2011 are directly linked to static stress drop (e.g., Dan et al. 2001).

In IM2011 the asperities are rupture areas with both higher static stress drop (high slip) and shorter slip duration. This means that most of the strong shaking energy is generated in the asperities areas, which cover only a small portion of the fault area. Since both rupture velocity and slip within each asperity are assumed constant, the resulting strong ground motion level is mainly controlled by the stress drop, and width and amplitude of the initial pulse in the Kostrov-like slip velocity function adopted by IM2011 (Nakamura and Miyatake 2000). However, the assumption that most of the higher-frequency ground motion originates only in the asperities is debatable. Inversions of recorded strong motion data often indicate that areas of high slip are not necessarily areas that produce large amounts of high-frequency energy (e.g., Frankel 2004; Kurahashi and Irikura 2013). We direct the interested reader to Irikura and Miyake (2011), and Morikawa et al. (2011) for a detailed description of IM2011.

The GP2016 rupture generator uses variable spatial and temporal kinematic rupture parameters that are calibrated using recorded ground motion and observed rupture kinematics. The rupture process, which is randomly heterogeneous at different scale

lengths, controls coherent and incoherent interferences of waves generated at the source. The random perturbations to the rupture kinematics follow empirical rules developed through modeling of past earthquakes. In contrast to IM2011 which follows a fully deterministic approach, GP2016 is designed to model rupture kinematics using a semi-stochastic approach. The deterministic approach used in IM2011 is designed to fully capture near-fault rupture effects, such as forward rupture directivity and seismic energy focusing at target sites. Because of the stochastic nature of the rupture model, ground motion estimates using GP2016 require a suite of rupture realizations that are necessary to capture the overall characteristics of ground motion from a target earthquake.

The GP2016 rupture generation process begins with the specification of a random slip field that is filtered to have a roughly wavenumber-squared falloff (e.g., Mai and Beroza 2002). The slip values are scaled to have a coefficient of variation of 0.85 and to also match the desired seismic moment. Given a prescribed hypocenter, the rupture propagation times across the fault are determined such that the average rupture speed scales at about 80% of the local shear wave velocity. Additionally, the rupture speed is further reduced by a factor of 0.6 for depths of 5 km and less, which is designed to represent the shallow, weak zone in surface-rupturing events (e.g., Marone and Scholz 1988; Dalguer et al. 2008; Pitarka et al. 2009). A perturbation is then applied to the rupture time at each subfault that is partially correlated with local slip such that the rupture tends to propagate faster in regions of large slip and slows down in regions of low slip. The slip-rate function is a Kostrov-like pulse (Liu et al. 2006) with a total duration (rise time) that is partially correlated with the square root of the local slip. Additionally, the rise time is scaled up by a factor of 2 within the 0–5 km depth range (Kagawa et al. 2004). The average rise time across the fault is constrained to scale in a self-similar manner with the seismic moment (Somerville et al. 1999).

The Graves and Pitarka simulation approach has been validated against a number of past earthquakes, as well as with various GMPEs. We direct the interested reader to Graves and Pitarka (2010) for a

detailed description of their hybrid ground motion simulation method and to Graves and Pitarka (2016) for a detailed description of their latest kinematic rupture model generator.

### 3. Ground Motion Simulations Using IM2011 and GP2016 Rupture Model Generators

We investigate the performance of IM2011 in conjunction with the Graves and Pitarka (2010) hybrid simulation method by comparing ground motions simulated with IM2011 and GP2016 rupture models for a hypothetical earthquake. The earthquake we consider is a M6.7 oblique-slip event on a steeply dipping fault. We compute broadband (0–20 Hz) ground motions at 39 stations surrounding the fault, and extending to a closest fault distance of about 22 km. The velocity structure is a simple 1D model with hard rock site condition. The fault mechanism and earthquake rupture parameters are summarized in Table 1. To minimize wave propagation effects, and allow for direct comparison of fault rupture contributions to near-fault ground motion, in our simulations we used a very hard rock velocity model consisting of four layers. The velocity model is listed in Table 2. Figure 1 shows the surface projection of

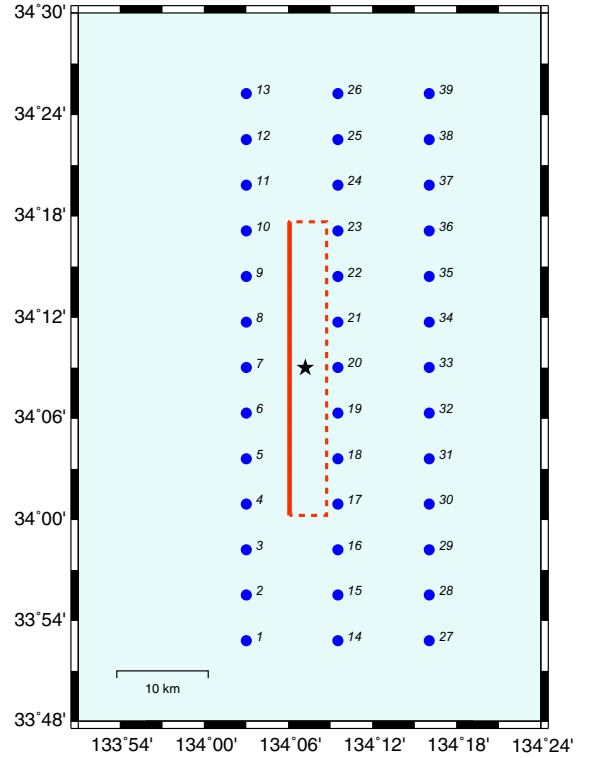


Figure 1

Map of station locations (blue circles) and fault trace (red rectangle) for the M6.7 scenario earthquake simulations. Star indicates the rupture initiation location projected on the free surface

the fault and the station locations. The fault rupture is bilateral and the fault spans from 3 to 19 km depth.

Table 1

*Fault rupture parameters*

Magnitude	6.7
Strike	0°
Dip angle	75°
Rake angle	25°
Fault length	32 km
Fault width	16 km
Depth to the top	3 km
Subfaults size	100 m × 100 m

Table 2

*1D velocity model*

Depth (km)	$V_p$ (km/s)	$V_s$ (km/s)	Density ( $\text{g/cm}^3$ )	$Q_p$	$Q_s$
2.5	4.5	2.6	2.4	300	200
20.0	6.0	3.5	2.7	500	300
30.0	6.7	3.9	2.8	2000	1000
Half space	7.7	4.4	3.2	2000	1000

#### 3.1. Rupture Models

Using the two rupture generators, we computed a suite of 10 randomized realizations for the M6.7 scenario earthquake. For IM2011, the difference between various realizations is simply the locations of the large and small asperities within the fault plane. Following the Irikura recipe, the ratio between the large and small asperity areas is kept the same in all rupture realizations. The depth of the asperities is completely random. For GP2016, each realization results in a different distribution of slip, rupture speed, rise time, and rake. To minimize the number of free parameters in the rupture models, yet still provide a useful comparison, in the analysis shown here, no attempt was made to generate GP2016 models that have similar slip distributions to the



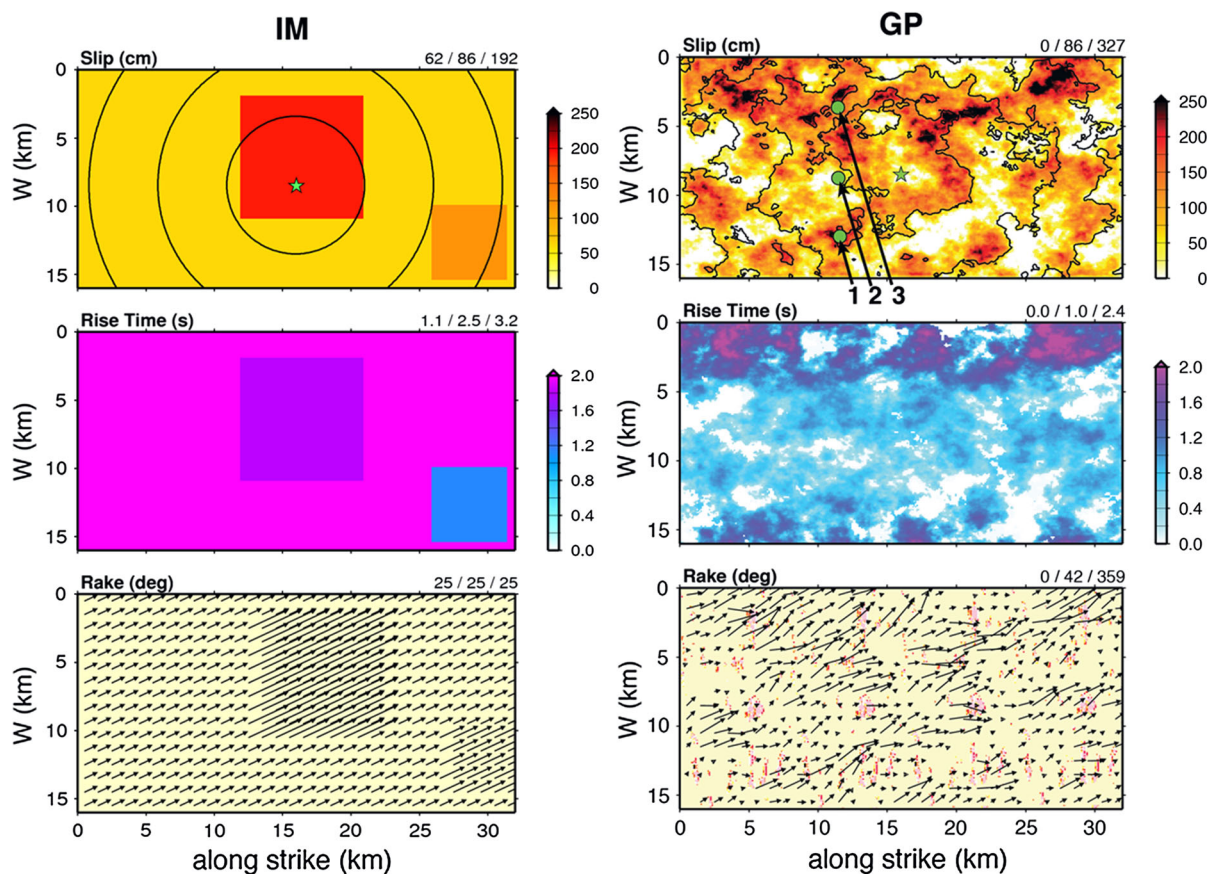


Figure 2

Examples of kinematic rupture models for a scenario M6.7 oblique-slip earthquake, created with IM2011 (left panel) and GP2016 (right panel). The triplet of numbers at the upper right of each panel indicate the minimum, average and maximum values of the parameter being displayed

IM2011 models. Figure 2 illustrates two representative kinematic rupture models generated with IM2011 and GP2016, named IM and GP, respectively. As dictated by the scaling rules in the recipe, the IM rupture has two asperities, one with bigger area and large slip and the other with smaller area and slip (although still above the background slip value). The estimated effective stress drops in the asperities and background areas of the fault are, 14.2 and 2.6 MPa, respectively. The rupture speed for the IM model is set at a constant value of 2.52 km/s, which is prescribed by the recipe as 72% of the assumed shear wave velocity of 3.5 km/s, and the rake is constant across the entire fault with a value of 25°. For the GP rupture, the slip, rupture speed and rise time distribution are much more heterogeneous compared to the IM rupture. This larger degree of

heterogeneity results from the use of randomized spatial fields to generate these parameters in the GP approach. Additionally, the GP method provides partial correlation between rise time and the square root of local slip, and between rupture speed and local slip. This results in a tendency for the rise time to lengthen and the rupture speed to increase as the slip increases. Since the randomized spatial fields are generated to match a roughly wavenumber-squared fall-off, there is sufficient spatial heterogeneity at relatively short length scales. Also apparent in the GP rupture is the systematic reduction of rupture speed and lengthening of rise time along both the top and bottom portions of the rupture. For this buried and dipping fault, this scaling is most prevalent in the upper 4 km of the fault plane, although it is also seen below about 15 km down-dip distance. Note that the

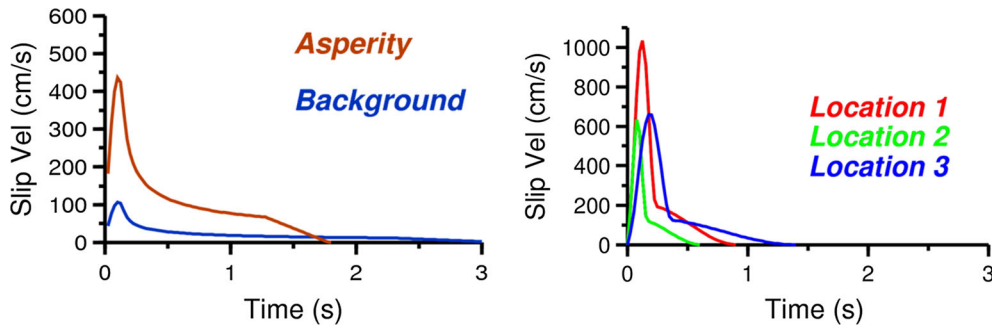


Figure 3

*Left panel* shows comparison of slip velocity functions in the large slip asperity area (*red trace*) and background fault area (*blue trace*) for the IM2011 model. *Right panel* shows slip velocity functions for three locations on the GP2016 rupture (locations indicated in Fig. 2). For the GP rupture, locations 1 and 3 both have the same final slip of 200 cm, and location 2 has 83 cm slip

stochastic approach used in the GP method for computing the high-frequency part of ground motion time history only requires the spatial slip distribution and fault rupture time. These rupture parameters were extracted from the IM2011 rupture models. Consequently, similarly to the original Irikura recipe, the slip in both asperity areas and background rupture areas contributes to generation of high-frequency (>1 Hz) ground motion. In all simulations shown here the Brune stress parameter, used in the GP method (Graves and Pitarka 2010), was set to its default value of 50 bars.

Figure 3 shows time series of slip velocity as prescribed by the two rupture models at selected locations on the fault. For IM (Fig. 3, left panel), one location is inside the large asperity and the other in the background slip area. The IM procedure requires the total duration (rise time) of the slip velocity function to scale with the width of asperity for the asperity area, and width of the fault for the background area. Thus, the rise time for the background area is about twice as long as that for the large asperity, which results in a relatively low peak amplitude and very long tail on the background slip velocity function. Since the radiated strong motion energy is generally correlated with the peak slip velocity, the scaling prescribed by the IM model means most of the strong motion radiation will come from the asperities, with the background areas mainly providing relatively longer period radiation. As noted above, the GP rupture has a more complex and heterogeneous distribution of rupture

parameters, and this is also reflected in the scaling of the slip velocity functions. For GP (Fig. 3, right panel) the functions come from locations that sample both large and small slip, as well as different depths on the fault. Locations 1 and 3 both have slip values of about 200 cm, although the rise time for the slip velocity function at location 3 is about twice that for location 1. This results from the depth scaling of rise time that is prescribed in the GP approach. Location 2 has roughly the average fault slip (83 cm), but since GP tends to scale rise time with slip, this location has a relatively short rise time, and the peak slip velocity at this site is similar to that at location 3. This highlights some key features of the GP approach whereby large shallow fault slip does not necessarily translate into large strong motion radiation. Additionally, it means that strong radiation of shorter period motion does not necessarily coincide with regions of large slip.

### 3.2. Broadband Ground Motion Method

Both set of rupture models were inserted into the Graves and Pitarka (2010) hybrid simulation process as implemented on the SCEC BBP. The low-frequency part of ground motion (0–1 Hz) was calculated using synthetic Green's functions computed with the FK method of Zhu and Rivera (2002). The subfault dimensions used in the simulations of the low-frequency part of ground motion were 0.1 km × 0.1 km, and used the full kinematic rupture descriptions as described earlier.

The high-frequency simulation approach of Graves and Pitarka (2010) uses a semi-stochastic representation that requires some modification of the full kinematic rupture description. The primary modification is the replacement of the deterministic slip velocity function with a windowed time series of band-limited white Gaussian noise. This time series is filtered to a target omega-squared spectrum and scaled to match the target moment release on the subfault. A basic premise of this approach is that it is designed to utilize the random phasing of the radiated subfault waveform to represent the poorly constrained and/or unknown details of the rupture process. For this reason, Graves and Pitarka (2010) recommend limiting the subfault size used for the high-frequency calculation to have a minimum characteristic dimension no smaller than about 1–2 km. More details about this can be found in Graves and Pitarka (2010, 2015). In the scenario simulations considered here, we resample the full kinematic rupture description to a grid of 2 km by 2 km for insertion in the high-frequency portion of the calculations. Another important input parameter for the high-frequency simulations is the average rupture speed, which is related to the subfault corner frequency in the Graves and Pitarka (2010) approach. For IM, this is set to 72% of the local  $V_s$  (Morikawa et al. 2011), and for GP it is set at 77.5% of the local  $V_s$ . An additional 60% reduction of rupture speed along the shallow and deep portions of the fault as dictated by Graves and Pitarka (2010, 2015) was applied to both the IM and GP high-frequency rupture simulations. Following the Irikura recipe, both the asperities and slip background areas were used in the GP high-frequency rupture simulations.

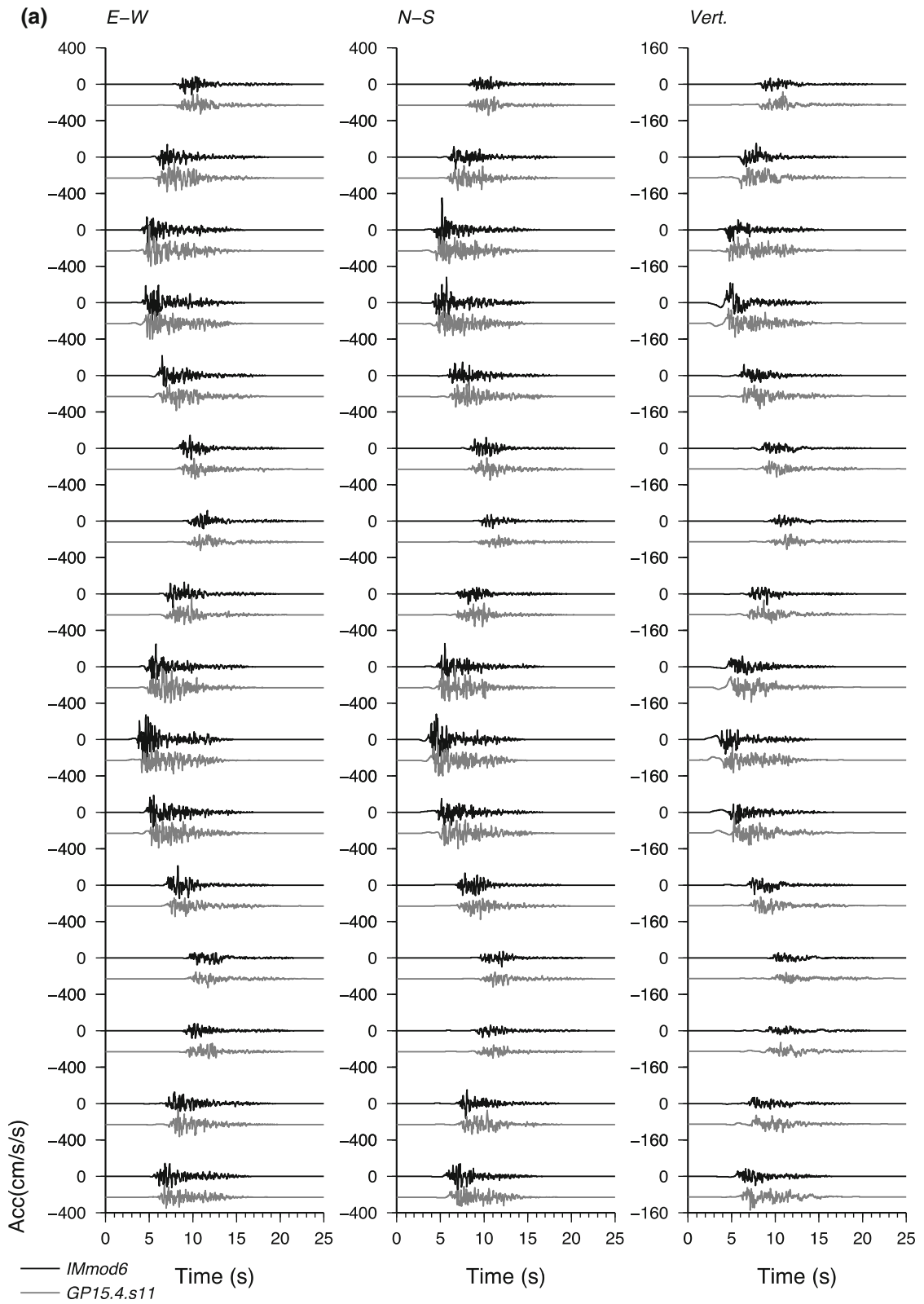
The matching frequency  $f_m$  used to combine the high- and low-frequency portions of the simulated ground motion was set at 1 Hz. In many studies the transition between the deterministic and stochastic characteristics of ground motion is made at 1 Hz, partly due to computational limitations in wave propagation modeling, and limited reliability of seismic velocity and rupture models. However, analysis of observed ground motion has shown that the transition between coherent and incoherent rupture and wave propagation processes generally occurs around 1 Hz (e.g., Liu and Helmberger 1985; Graves

and Pitarka 2016), although there may be some variation with magnitude (Frankel 2009). Therefore, fixing  $f_m$  at 1 Hz is rather arbitrary and subject to further research.

### 3.3. Simulation Results

Figure 4a and b compare time series of ground motion acceleration and velocity, respectively, computed with the IM and GP rupture models shown in Fig. 3 at 16 selected stations. Despite the noted differences in the rupture models, the ground motions produced with these two rupture models are quite similar. In general, the amplitude of the IM acceleration time histories is slightly larger at all distances. In contrast, the velocity time histories are much more similar. This can be explained by the difference in small-scale rupture complexities between the two models. The GP model, which is more heterogeneous than the IM model, creates more deconstructive waveform interference in both time and space. Later we will show that for the same reason GP produces less intra-event variability in near-fault ground motion. IM produces slightly stronger rupture directivity effects near the asperity area, which results from strong constructive interference due to the smooth rupture at constant rupture speed. This effect is manifested by increased amplitude of the fault normal, east–west (EW), component of ground motion velocity at near-fault locations, such as stations 8, 10, 18, 20 and 22.

From the simulated waveforms for each realization, we compute the RotD50 pseudo-spectral acceleration (Boore 2010) at each site. These values are compared with estimates from four NGA-West2 GMPEs (Abrahamson et al. 2014; Boore et al. 2014; Campbell and Bozorgnia 2014; Chiou and Youngs 2014) as a function of distance for various oscillator periods in Fig. 5a (for GP) and 5b (for IM). The GMPE values were computed using a  $V_{s30}$  of 2600 m/s, which is consistent with our specified hard rock velocity model. We recognize that there are little recorded data available for this site condition, and in fact, the GMPEs are constructed so that their site amplification does not change for  $V_{s30}$  above about 1100 m/s. Based on simple 1D site response models, we estimate the amplification difference between  $V_{s30}$





◀Figure 4

**a** Comparison of broadband (0–20 Hz) acceleration time series simulated with the GP (*gray* traces) and IM (*black*) rupture models shown in Fig. 3. **b** Comparison of broadband (0–20 Hz) velocity time series simulated with the GP (*gray* traces) and IM (*black* traces) rupture models shown in Fig. 3

of 1100 m/s and 2600 m/s to be about 15–20%. Given these uncertainties, the comparisons are not designed to find the best match to the GMPE values, but rather to use these values as a common baseline for which we can compare the motions simulated with the IM and GP approaches. Examining the results shown in Fig. 5a, b, we see the simulated values for both IM and GP tend to cluster near the range of the median values of the GMPEs across all periods and distances. It can also be seen in these plots that the variability of the IM responses is greater than that for GP, particularly at the longer periods. We will discuss this further in a later section.

To obtain a more quantitative assessment of the comparison between the simulations and GMPEs, we have used the response spectral acceleration goodness-of-fit (GOF) approach described by Goulet et al. 2015. This is done by first computing the residual between the simulated value and the estimated median value from each of the four GMPEs at each site. This is done for all 10 realizations for each of GP and IM. Then for each oscillator period, we compute the median and standard error for all of the residuals (39 sites and 10 realizations compared with four GMPEs for each rupture model generator). The GOF results are shown in Fig. 6. For periods shorter than 1 s, both methods produce similar results, with similar trend down to 0.1 s. The bias values are centered around zero, with a maximum deviation of about 25%. At longer periods (>1 s), the GP results are near zero bias all the way out to 10 s, whereas the IM results show a systematic under-prediction of the GMPE levels of about 20–30% in the period range 1–3 s.

Given that we are considering a hypothetical earthquake rupture embedded in a very simple 1D velocity structure, and the fact that IM is validated and mainly used in simulations in which the wave propagation effects are modeled using 3D velocity models with softer material in shallow layers, we cannot say what the “correct” ground motion

response should be. Nonetheless, the systematic difference seen between the GP and IM responses in the 1–3 s period range is intriguing, and warrants further investigation.

### 3.4. Modified IM Approach (*IM-fastRS*)

One of the main differences in the IM and GP rupture generator approaches involves the specification of the temporal characteristics of the rupture, i.e., the rupture speed and rise time. In IM, the rupture speed is constant across the entire fault, and the rise time does not vary within the large slip asperity regions. The GP ruptures on the other hand incorporate significant variability in the specification of these parameters, as well as partially correlating these with the spatially heterogeneous slip values. Based on these features, we created a modified version of the IM approach such that the rupture speed is increased on the asperity areas by 20%. Due to the coupling of rupture speed and slip velocity function in the IM method, the increase in rupture speed also resulted in a 16% decrease in rise time, and a 9% increase in peak slip velocity in the asperities. Figure 7 plots one realization of the modified IM approach, which we refer to as *IM-fastRS*.

We generated 10 realizations of the M6.7 scenario using the *IM-fastRS* approach and ran simulations with these in the exact same manner as was done for IM and GP. We then computed RotD50 values and generated GOF comparisons using the NGA-West2 GMPEs. The GOF for the *IM-fastRS* rupture simulations is shown in Fig. 8. Compared to the GOF for IM (Fig. 6, right panel), the *IM-fastRS* result shows slightly stronger motions (downward shift of the bias level) for periods less than about 1 s, and a much larger downward shift for periods great than 1 s. The slight increase in shorter period ground motion levels is not unexpected since the Graves and Pitarka (2010) high-frequency simulation approach uses the rupture speed to scale the subfault corner frequency, which in turn controls the level of high-frequency motions. Thus, the increase in average rupture speed translates directly into an increase in high-frequency ground motion levels. Likewise, the increase in longer period ground motion levels is not unexpected, although the magnitude of the ground motion increase in the 1–3 s

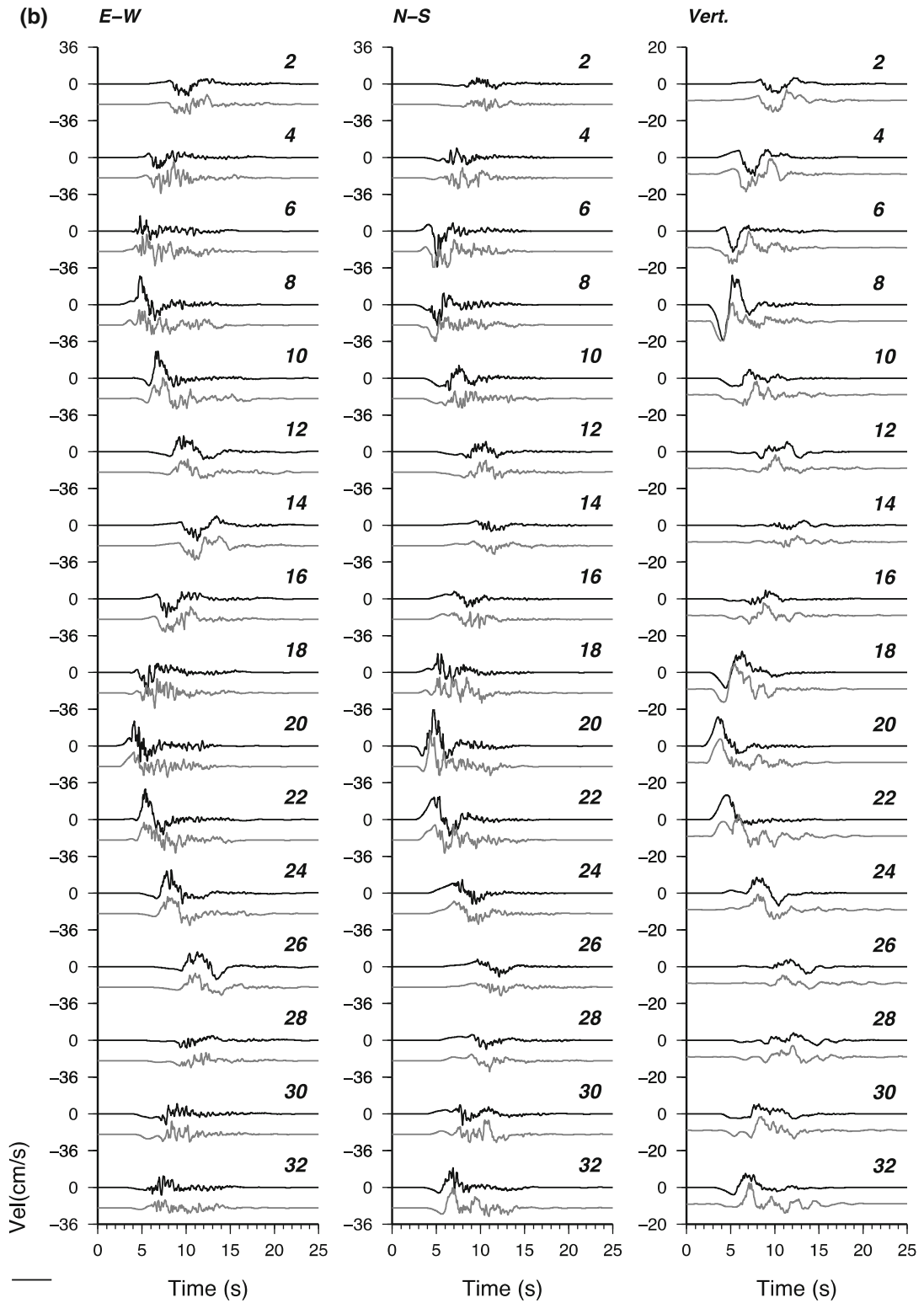


Figure 4  
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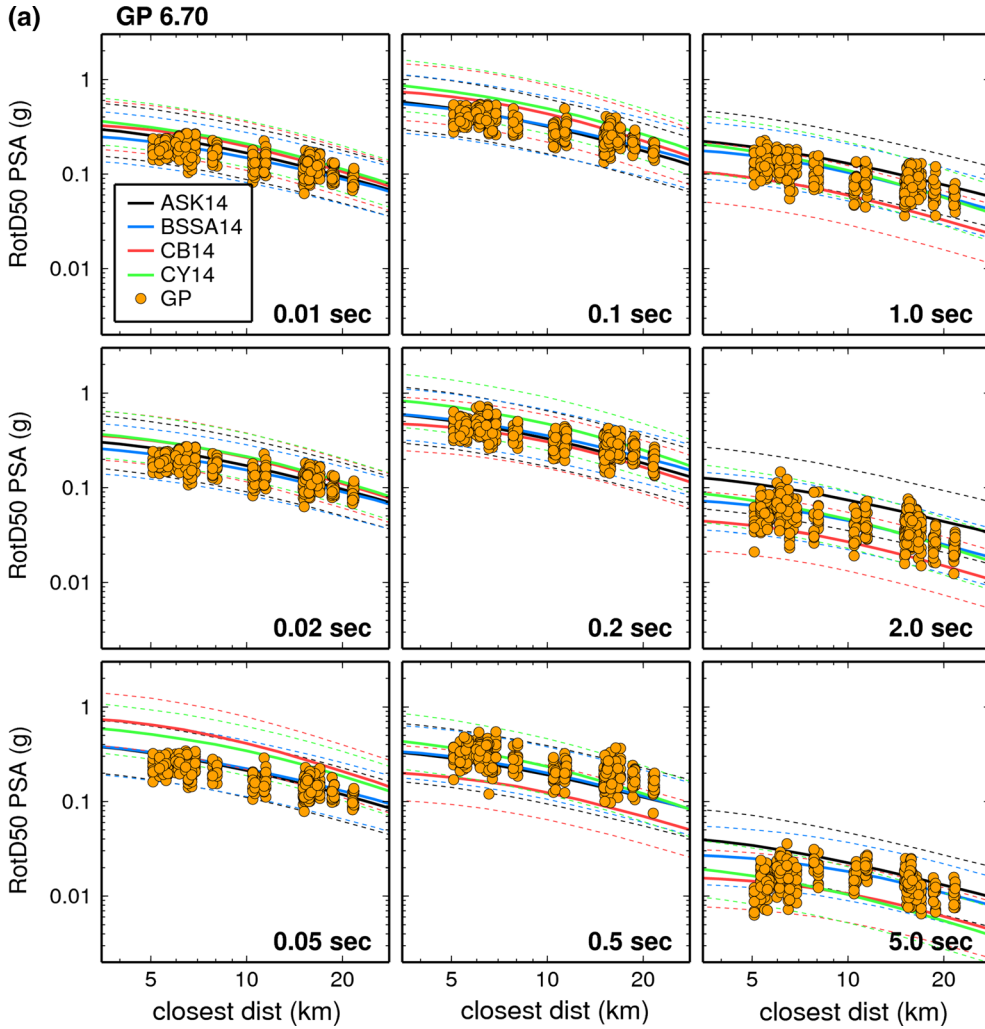
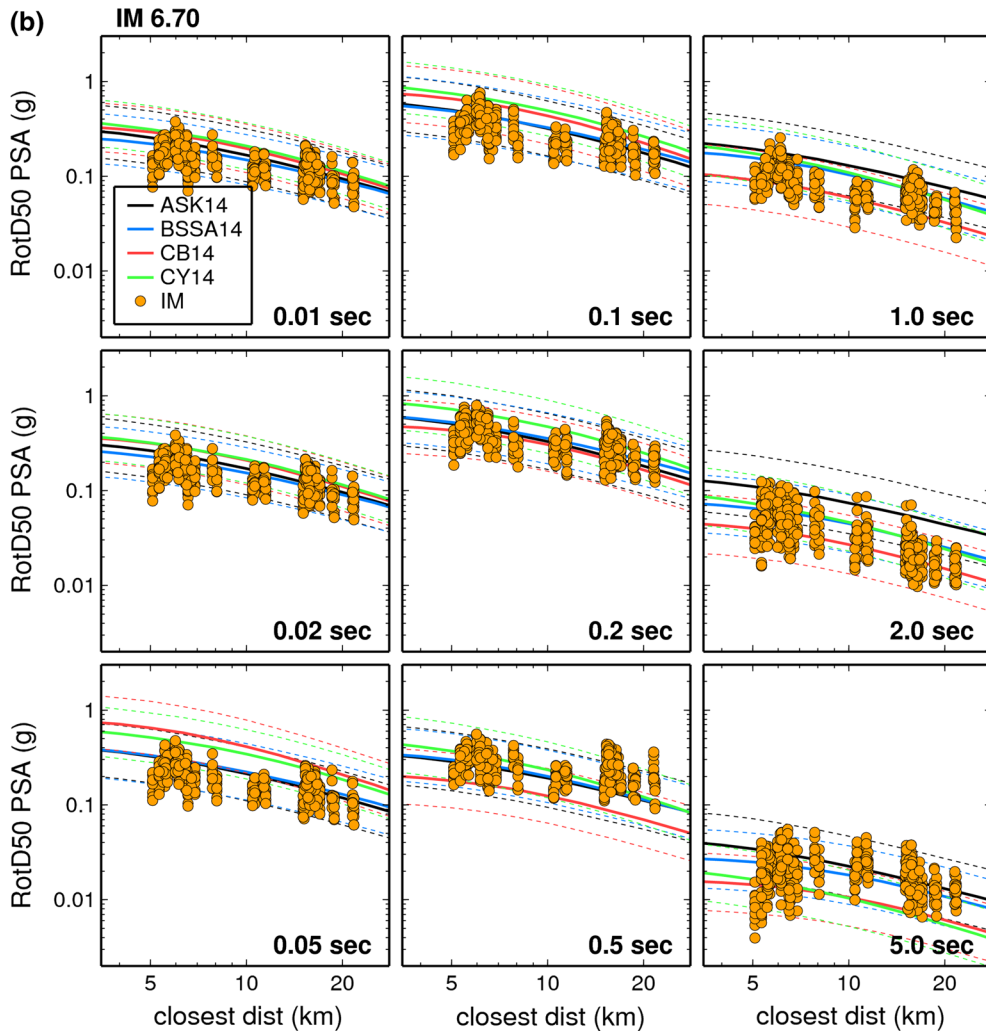


Figure 5

**a** RotD50 horizontal pseudo-spectral acceleration for 10 random realizations of the scenario M6.7 earthquake computed using the GP method (gold circles) compared with estimates obtained from four NGA-West2 GMPEs. Median values for GMPEs are shown in solid lines with dashed lines indicating  $\pm$  one standard deviation (total sigma). GMPEs are ASK14, Abrahamson et al. (2014); BSSA14, Boore et al. (2014); CB14, Campbell and Bozorgnia (2014); CY14, Chiou and Youngs (2014). **b** Same as **a** except simulated values are computed using the IM rupture generator

bandwidth (about 30%) is significantly larger than the 20% change in the rupture speed. We suspect that there is a combination of factors, which are contributing to this ground motion increase. In particular, the increase in peak slip velocity coupled with the increased rupture speed across the large slip asperity time compresses the longer period ground motion radiation into a shorter duration pulse. This can strongly increase the ground motion levels, especially for near-fault sites such as those considered in our simulation experiment. A test with increased rupture

speed by only 10% produced similar effects but the impact on ground motion amplitude was weak. Note that the improved comparison between realizations of the two rupture generators produced here is only warranted when the rupture initiation in each asperity areas of the IM2011 rupture models is computed as a function of earthquake rupture initiation location. In these models the curvature of rupture front remains the same within and outside the asperity areas. However, Irikura recipe includes a second option in which the asperities rupture initiation is prescribed as a single

Figure 5  
continued

point located on the asperity's boundary. The location of the rupture initiation within each asperity can affect the rupture directivity, and therefore can impact ground motion amplitude at a near-fault target site. The concept of selective asperity rupture initiation is successfully used to model ground motion from earthquakes in Japan (e.g., Morikawa et al. 2011). It is, therefore, possible that ground motion simulated with Irikura recipe and the use of rupture models with predetermined asperities rupture initiation point could produce the same effects on ground motion amplitude obtained here, computed with the GP simulation

method and IM2011 rupture models modified for increased rupture speed in the asperity areas.

To examine the distance dependence of simulated ground motion amplitude we have separated the residuals into different distance bins (Table 3). Figure 9 plots the residuals in these distance bins for periods of 0.1 to 10 s for each rupture model. Also shown in these plots is the range of the individual GMPE medians for each period. While a value of zero on these plots represents the average of the median values from the four GMPEs, the spread of the GMPEs varies greatly as a function of period, and in particular, it shows a noticeable increase with

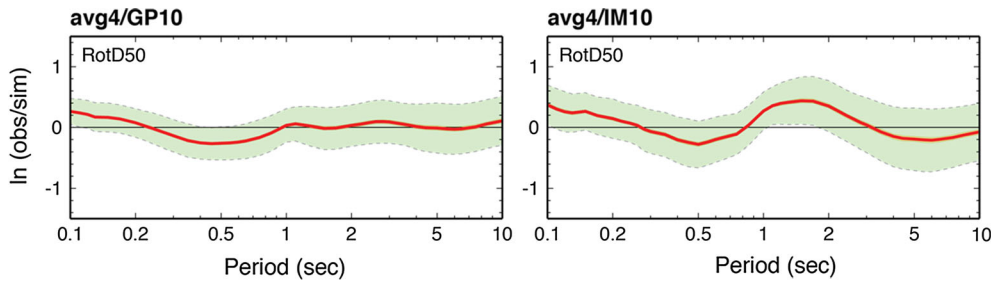


Figure 6

RotD50 horizontal spectral acceleration goodness of fit for the M6.7 scenario earthquake simulations averaged across ten realizations generated with GP (*left panel*) and IM (*right panel*) ruptures. The residuals used to determine the goodness of fit are computed between the simulations and the average of the median values from the four NGA-West2 GMPEs

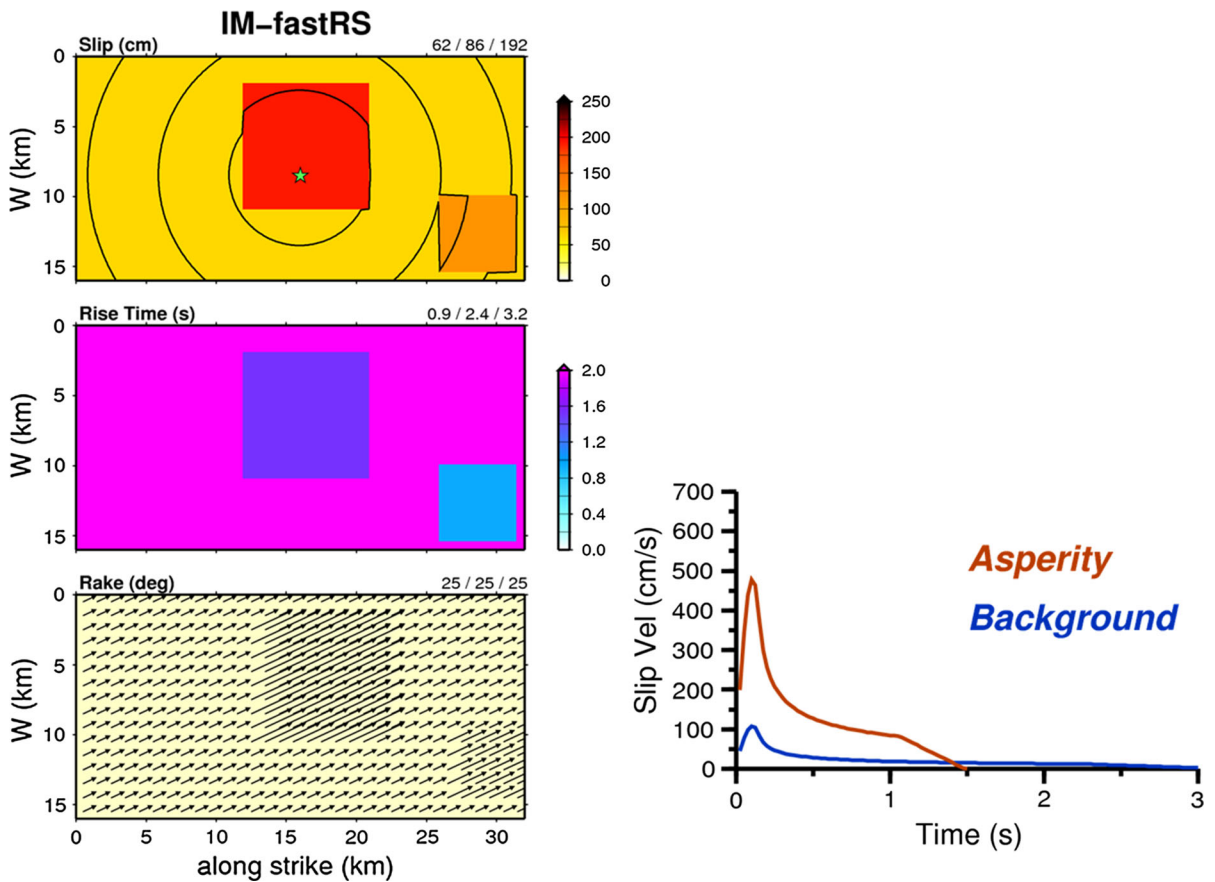


Figure 7

Example rupture generated with a modified version of IM (IM-fastRS) where the rupture speed is increased by 20% within the asperities (*left panels*). Slip velocity functions for the modified IM rupture taken from the largest slip asperity and background locations (*right panel*)

increasing period. This degree of variability suggests caution when comparing the simulations with the individual GMPE values.

There are several trends, readily apparent, from the plots in Fig. 9. First, there are actually very few places where the median residual lies outside of the maximum–minimum spread of the GMPE medians.



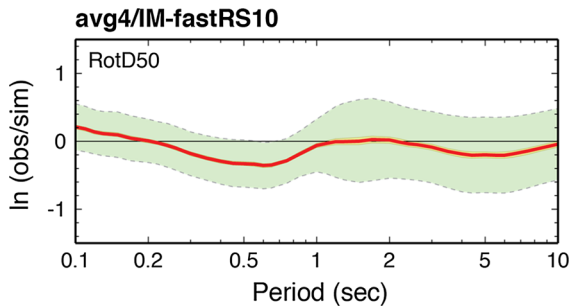


Figure 8

Same as Fig. 6 except simulations use ruptures generated with IM-fastRS approach

Table 3

*Distance bins*

Distance bin (km)	Number of stations
5–6	8
6–7	8
7–12	6
12–22	17

This is encouraging because it indicates that all of the rupture generators are producing results that are generally in agreement with the empirical models. Secondly, there are very similar trends that are seen across all models for periods less than 1 s, for example, under-prediction at very short periods and slight over prediction around 0.5 s. Since this is present for all three models, it shows that the high-frequency approach in Graves and Pitarka (2010) tends to smooth out the differences in the different rupture approaches, and the resulting variability is embedded within the stochastic phasing of the method. Thirdly, the variability of the IM and IM-fastRS results is larger than GP, particularly for periods above 1 s. This is likely due to the large discrete asperities in IM and IM-fastRS compared to the more heterogeneous slip distribution in GP. Thus, asperity proximity, as opposed to simply fault distance, has a much stronger impact on ground motion levels in IM than in GP.

To better understand and quantify the ground motion variability produced by the different rupture model generators, we computed the standard deviation of simulated ground motion ( $\sigma$ ) and analyzed its variability as a function of period and

distance. Again, we grouped the stations into different distance bins so that we could get enough observations to perform the statistical analysis of  $\sigma$ . The distance bins and number of stations in each bin are shown in Table 3.

For each rupture realization, we first computed the standard deviation ( $\sigma$ ) of simulated spectral acceleration across all stations within each distance bin at each oscillator period. This is a measure of intra-event variability since it considers the motions for only a single realization. We then calculated the total  $\sigma$  over ten rupture realizations for the IM, IM-FastRS and GP models. This is a measure of inter-event  $\sigma$  (event-to-event variability) for the limited set of rupture realizations we have simulated. Similarly, we calculated the median ground motion for each model, and its standard deviation as a function of distance bin and period. The standard deviation of the median is a way to measure how much the median value changes from realization to realization within each of the three rupture generators. If each rupture realization produces the same median level of ground motion then the standard deviation of median would be zero. This means no inter-event variability. If the median level of ground motion changes dramatically from realization to realization, then the  $\sigma$  of the median would be very high. This would indicate large inter-event variability. The variability of the median maps into the total variability across all simulations, represented by the average  $\sigma$ . We recognize the set of 10 realizations we have considered for each rupture generator approach is a very limited sample. Furthermore, the current set of realizations only considers variations in slip distribution, which neglects other important sources of event-to-event variability such as changes in hypocenter and fault rupture area (static stress drop). These additional factors would likely have a significant contribution to the simulated inter-event variability. Thus, we regard the current estimate of inter-event  $\sigma$  as a lower-bound value.

Figure 10 shows intra-event  $\sigma$  (orange lines), inter-event  $\sigma$  (red lines) and  $\sigma$  of median (blue line) for IM, IM-FastRS and GP rupture generators. Using the statistical analysis shown in this figure we drew several conclusions about ground motion variability simulated with IM, IM-fastRS and

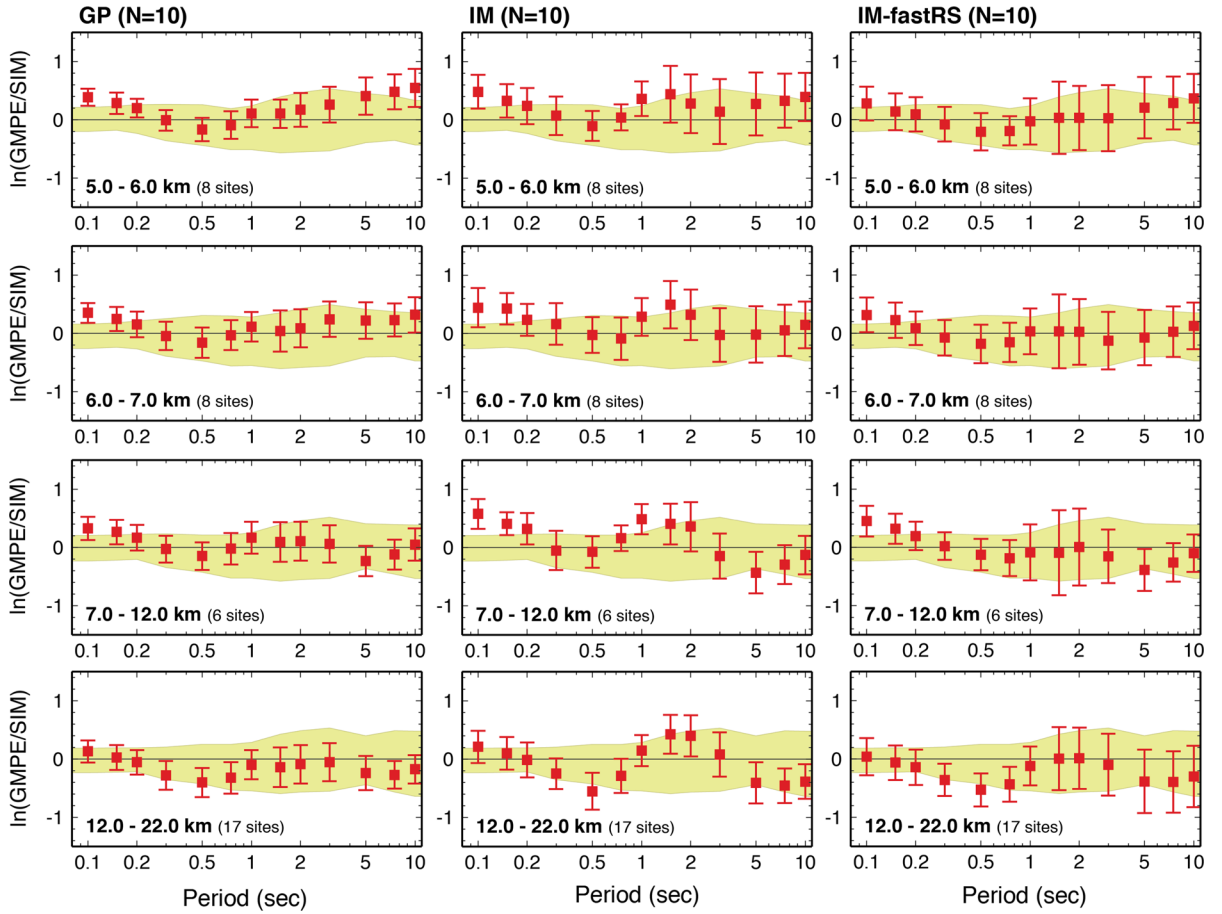


Figure 9

Residuals computed between median GMPE and simulated RotD50 ground motions and plotted as a function of the oscillator period for different distance bins. Results are shown for ruptures generated with GP (*left panel*), IM (*middle*) and IM-fastRS (*right*). Median GMPE values are determined across the four NGA-West2 relations for each period and station distance. The *light-shaded region* in each panel denotes the maximum and minimum deviation of the individual GMPE medians across the range of periods. At each period, the median residual across the 10 simulated realizations is denoted by the *square symbol* with the *error bars* indicating the one standard deviation level of the residuals

GP. First, the level of intra-event sigma is much larger than inter-event sigma across all distances and periods, and for all three rupture model generators. However, we must use caution when comparing absolute levels of intra- and inter-event sigma for this limited set of simulations due to the under-sampling of possible event-to-event variability mentioned above, and fixing of fault rupture initiation location for all rupture scenarios. Nonetheless, these current results suggest that variations in slip distribution contribute only a modest amount to the inter-event sigma at shorter periods ( $<1$  s), with the level being somewhat stronger for IM than for GP. Second,

regardless of modification for rupture speed, IM produces more variability than GP across all periods, especially at the longer periods ( $>1$  s) and closer distances ( $<12$  km). The larger variability for IM and IM-fastRS results from their smoother rupture process, and simple and well-defined asperity areas. At long periods and short distances, these distinct source characteristics generate stronger local directivity effects and consequently stronger ground motion variability depending on the relative location of the station to asperities. The strength of this effect would likely be even greater had we considered different hypocenter locations in our analysis. The long-period

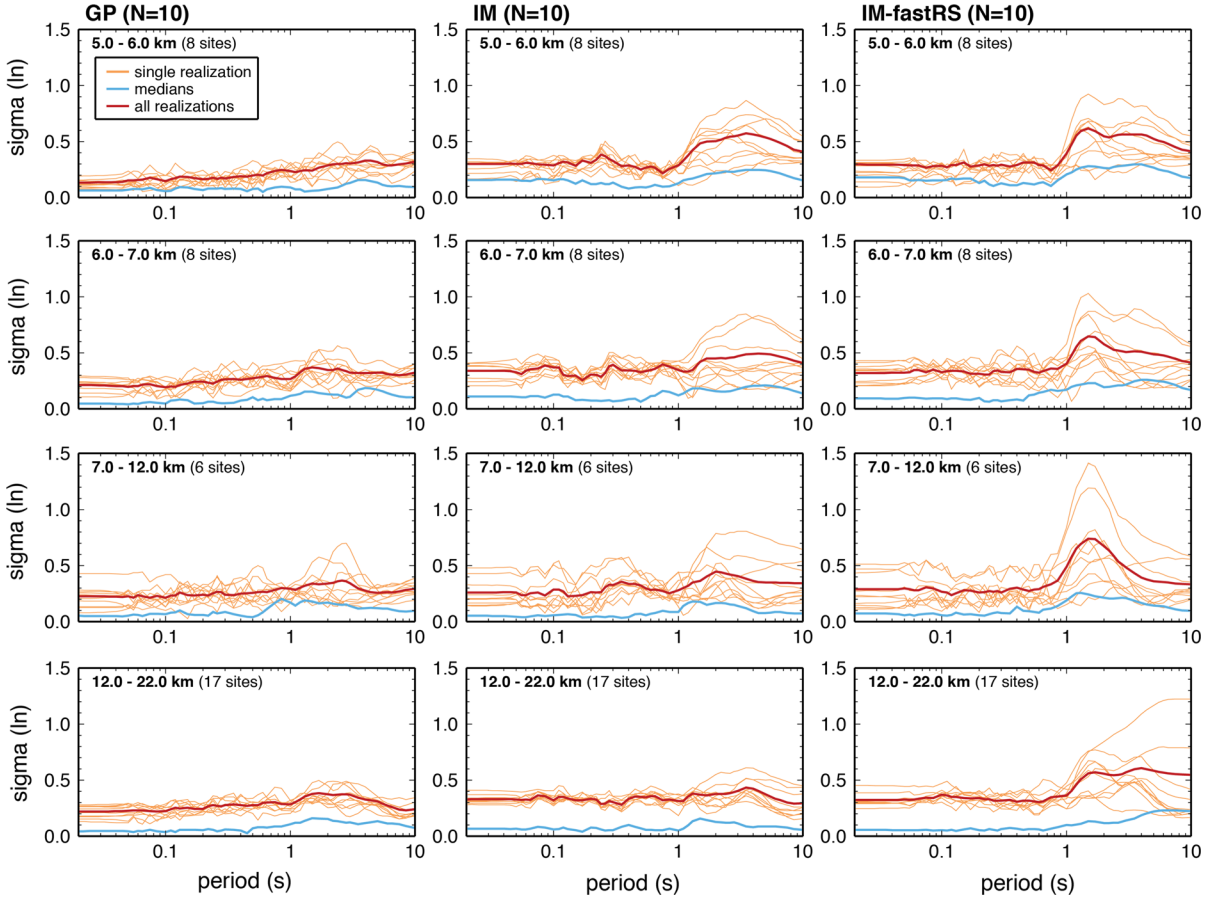


Figure 10

Standard deviation of simulated ground motion (*orange* traces), average standard deviation (*red* traces) and standard deviation of the median of simulated ground motion (*blue* traces) for IM, IM-fastRS and GP rupture generators. Each *panel* represents statistics obtained for the different distance bins indicated in each panel. The number of stations included in each distance bin is shown in *parentheses*

intra-event variability for IM is strongest at near-fault distances, and then is substantially reduced beyond 12 km. At those distances the intra-event ground motion variability for IM approaches the level found for GP. Third, although to a lesser extent, the larger variability for IM compared to that for GP at near-fault distances is also present at short periods ( $<1$  s). Part of the reason for this is that slip resampling on a coarser  $2 \text{ km} \times 2 \text{ km}$  grid, required by the high-frequency modeling in Graves and Pitarka (2010) method affects the IM and GP models differently. In the case of GP models it tends to reduce the original small-scale spatial complexity of slip. Consequently the source contribution to short-period ground motion variability is reduced. This explains the gradual

increase of ground motion variability with period at near-fault distances observed for GP models. In contrast, because of the geometrical simplicity of the asperity area in IM models, slip resampling does not modify the spatial characteristics of the original slip, and therefore it has a smaller impact on simulated ground motion especially at short periods. At those periods sigma for IM models remains roughly constant at all distances.

#### 4. Conclusions

In this study, we investigate the transportability of the IM2011 asperity-based kinematic rupture model

generator into the simulation framework used by the Southern California Earthquake Center broadband simulation platform. For this purpose, we implemented IM2011 within the hybrid broadband ground motion simulation methodology of Graves and Pitarka (2010), which is one of the simulation approaches currently installed on the SCEC BBP. The performance of the IM2011 rupture model was investigated by comparing ground motions simulated using this approach with those obtained from the GP2016 rupture generator and NGA-West2 GMPEs for a suite of realizations of a hypothetical M6.7 crustal earthquake embedded in a hard rock velocity structure. Despite conceptual differences between the two rupture generation approaches the simulations show both models produce ground motions that are similar to those obtained from NGA-West2 GMPEs across the period range 0.1 to 10 s. The largest difference found for this M6.7 scenario is in the period range 1–3 s where the IM ground motion amplitude is somewhat lower ( $\sim 20\text{--}30\%$ ) compared with both GP2016 and the GMPE medians. One possible cause for this band-limited discrepancy is related to the assumption of constant rupture speed over the entire fault made in IM2011. In contrast, GP2016 uses spatially heterogeneous slip and by association heterogeneous rupture speed, and these rupture parameters contain deterministic and stochastic features that are modeled using magnitude and depth dependent empirical relationships. We found that the amplitude of ground motion produced with IM in the 1–3 s period band is sensitive to the rupture speed across the asperities. Increasing the asperity rupture speed by 20%, produces ground motions closer to both the GP results and the GMPE median. Further testing and more IM rupture realizations are needed to determine how this modification can be generalized to other rupture geometries and magnitudes, and other velocity structures. It is important to note that this modification may only be needed when IM is used in Graves and Pitarka method. In the GP approach, the location of rupture initiation in each asperity is controlled by the relative location of the asperity to the rupture hypocenter. In contrast, in Irikura recipe the rupture initiation point in each

asperity is an external model parameter that can be prescribed by the modeler independent of the main rupture hypocenter. Consequently, in Irikura recipe the enhanced local rupture directivity effect produced by the proposed increase in rupture velocity within the asperities could possibly be reproduced by appropriately positioning the rupture initiation in each asperity. Nonetheless, based on the analysis shown here, we concluded that IM2011 rupture generator performs well in ground motion simulations using Graves and Pitarka hybrid method. Therefore, we recommend it to be considered for inclusion into the framework used by the Southern California Earthquake Center broadband simulation platform.

Another important observation made in this study is that the IM model produces larger intra-event ground motion variability than the GP model, particularly for periods greater than 1 s. This is a deliberate feature of the IM approach and is due to the discrete asperities in the IM model compared to the more heterogeneous slip distribution in the GP model. Consequently, the asperity proximity, as opposed to simply fault distance, has a much stronger impact on ground motion levels in IM than in GP. We also find that event-to-event variations in slip distribution only contribute a modest amount to the overall level of ground motion variability ( $\sigma$ ), particularly for periods less than about 1 s. The amount of variability due to this effect is slightly larger for IM than for GP, which again is likely due to the use of large discrete asperities in the IM approach. Furthermore, we recognize that there are other important sources of event-to-event variability that we have not considered in the current study, most notably changes in hypocenter and fault rupture area. Incorporation of this additional variability in the simulations would probably result in a significant increase in the level of inter-event  $\sigma$ , and this topic is the subject of future work.

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