

New correlations for prediction of saturated and undersaturated oil viscosity of Arabian oil fields

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Abstract New correlations for saturated and undersaturated oil viscosity were developed for Saudi Arabian crude oil. The data consist of 79 and 71 experimental measurements of saturated and undersaturated crude oil viscosity, respectively, at reservoir conditions. Other PVT measurements above and below bubble point pressure are also included. The new correlations were developed using genetic programming approach. The new models were developed and tested using linear genetic programming (GP) technique. The models efficiency was compared to existing correlations. Average absolute relative deviation, coefficient of correlation, and crossplots were used to evaluate the proposed models, and their outputs indicate the accuracy of the GP technique and the superiority of the developed models in comparison with the commonly utilized models tested.

Keywords Genetic programming · Oil viscosity · Saturated · Undersaturated · Correlation

Introduction

Crude oil viscosity is an important physical property that controls and influences the flow of oil through porous media and pipelines. The viscosity, in general, is defined as the internal resistance of a fluid to flow. Oil viscosity is a

strong function of many thermodynamic and physical properties such as pressure, temperature, solution gas–oil ratio (GOR), bubble point pressure, gas gravity, and oil gravity. Viscosity of crude oil is a fundamental factor in simulating reservoirs, forecasting production as well as planning thermal enhanced oil recovery methods that make its accurate determination necessary.

Usually oil viscosity is determined by laboratory measurements at reservoir temperature. However, experimental determination of reservoir oil viscosity is costly and time-consuming. A literature survey has indicated that empirical viscosity correlations developed are divided into three major types: dead oil viscosity, saturated oil viscosity, and undersaturated oil viscosity. Figure 1 shows a typical oil viscosity diagram as a function of pressure at constant reservoir temperature.

Saturated oil viscosity

Numerous correlations have been proposed to calculate the oil viscosity. These correlations predict viscosities from available field-measured variables including reservoir temperature, oil API gravity, solution gas–oil ratio, pressure, and saturation pressure.

Chew and Connally (1958) presented their crude viscosity correlation as a function of dead oil viscosity and solution gas–oil ratio under reservoir conditions. Viscosity was measured for data of 457 crude oil samples gathered from different areas of USA, Canada, and South America. Measurements were conducted within the ranges of 72–292 °F, 132–5645 psia, and 51–3544 cu ft/bbl for reservoir temperature, bubble point pressure, and solution gas–oil ratio at bubble point, respectively.

Beggs and Robinson (1975) developed fairly accurate and simple crude oil viscosity model based on API gravity

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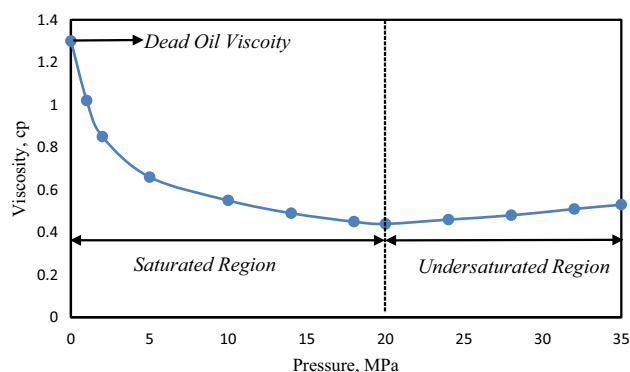


Fig. 1 Typical viscosity trend as a function of pressure

temperature and solution gas–oil ratio. Measurements of 600 samples dataset were used to derive the correlation with pressure range of 0.0–5250 psig, solution GOR of 20–2070 scf/STB, oil gravity of 16–58 °API, and temperature of 70–295 °F. They limit their correlation on data that do not have crude composition and suggest using different correlations for better accuracy if composition is available.

Later, Khan et al. (1987) published their empirical correlation using Saudi Arabian crude oil viscosity measured using rolling ball viscometer at various pressures and temperatures. The study utilized viscosity data of 75 bottom-hole samples taken from 62 Saudi oil reservoirs. A total of 1691 data measurements below the bubble point pressure were used to derive the correlation which is simply based on crude bubble point viscosity, pressure, and bubble point pressure. They compared their model with Beggs and Robinson and Chew and Connally and claimed that their own correlation was the most accurate for Saudi crudes.

Naseri et al. (2005) used PVT experimental data of 472 series of Iranian oil reservoirs in developing their empirical correlation. These data include oil API gravity, reservoir temperature, saturation pressure, solution gas–oil ratio, and PVT measurements at reservoir temperature. Out of the total dataset, 250 were used to develop the empirical model and the rest was spared for validation purposes. Dead viscosity and bubble point pressure were used as input parameter and model developed was of good accuracy exceeding that of the models they compared with average absolute error of 26.31%.

Undersaturated oil viscosity

Many correlations have been proposed to calculate the undersaturated oil viscosity. These correlations predict viscosities from available field samples including reservoir temperature, oil API gravity, solution gas–oil ratio, pressure, and saturation pressure. Vazquez and Beggs (1977) used more than 600 laboratory PVT analyses from fields of different geographical locations. The data encompassed

very wide ranges of pressure, temperature, and oil properties and included more than 6000 measurements of gas solubility, oil formations volume factor, and oil viscosity at various pressures. Regression analysis techniques were used to correlate the laboratory data.

Khan et al. (1987) utilized viscosity data of 75 bottom-hole samples taken from 62 Saudi oil reservoirs. A total of 1503 data measurements above the bubble point pressure were used to derive the correlation which is simply based on crude bubble point viscosity, pressure, and bubble point pressure. They compared their model with Beal's (1946) correlation, and it gives close estimates for undersaturated crude oil viscosity.

Kartoatmodjo and Schmidt (1991) used widespread data collected from PVT reports and literature. A set of 5392 data points was used to develop their correlation. These data represent 740 different crude oil samples. For the development of undersaturated oil properties correlations, a total of 3588 data points collected from 661 different crude oil samples were used. The functional form of Sutton's was used in this study to develop the undersaturated oil viscosity correlation. They developed a crude oil viscosity model based on API gravity, temperature, and solution gas–oil ratio. The used data have the following ranges: oil gravity of 14.4–59 °API, pressure of 14.7–6054.7 psia, temperature of 75–320 °F, and solution–gas ratio of 0–2890 scf/stb.

Hossain et al. (2005) presented their empirical correlations for dead, saturated, and undersaturated heavy oil utilizing three databanks. The databanks consist of heavy oil data from various parts of the world with wide ranges of temperature, pressure, and fluid compositions. A total of 361 data points were used to develop the undersaturated oil viscosity correlation. With temperature range of 118–218.7 °F, solution–gas ratio of 19.4–493 scf/bbl, bubble point pressure of 121–6272 psia, and pressure of 300–6400 psia.

Bergman and Sutton (2006) developed their correlation which provides a wider range of bubble point viscosity and pressure differentials than other existing correlations for undersaturated oil viscosity. This model derives undersaturated viscosity using only bubble point viscosity and pressure differential. The correlation can be satisfactorily used on gas free oils and oil with solution gas. The data used to derive the correlation included samples with bubble point viscosity from less than 0.1–14,000 cp. Accuracy is maintained over this wide range of values.

Genetic programming

Genetic programming (GP) is a development in the field of evolutionary algorithms extending the classical genetic algorithms (GA) to a symbolic optimization technique and

overcoming GA limitation of being a fixed-length representation scheme requiring encoding of the variables and its non-dynamic variability requiring the string length to be defined in advance (Koza 1992). Unlike common optimization methods, GP is able to work with a coding of the design variables as opposed to the design variables themselves. It is a problem-independent application working with a population of points as opposed to a single point. In addition, it requires the objective function value only, not the derivatives. Finally, GP is considered highly exploitative family of probabilistic (non-deterministic) search approach (Alvarez 2000).

GP is based on so-called tree representation in which trees can represent computer programs, mathematical equations, or complete models of process systems. GP initially creates an initial population generating random individuals (trees) of functions and terminals (inputs) to represent the problem. In all iterations, the algorithm executes and evaluates the individuals in the population and assigns a fitness value. Individuals are then selected for reproduction and generate new individuals by mutation,

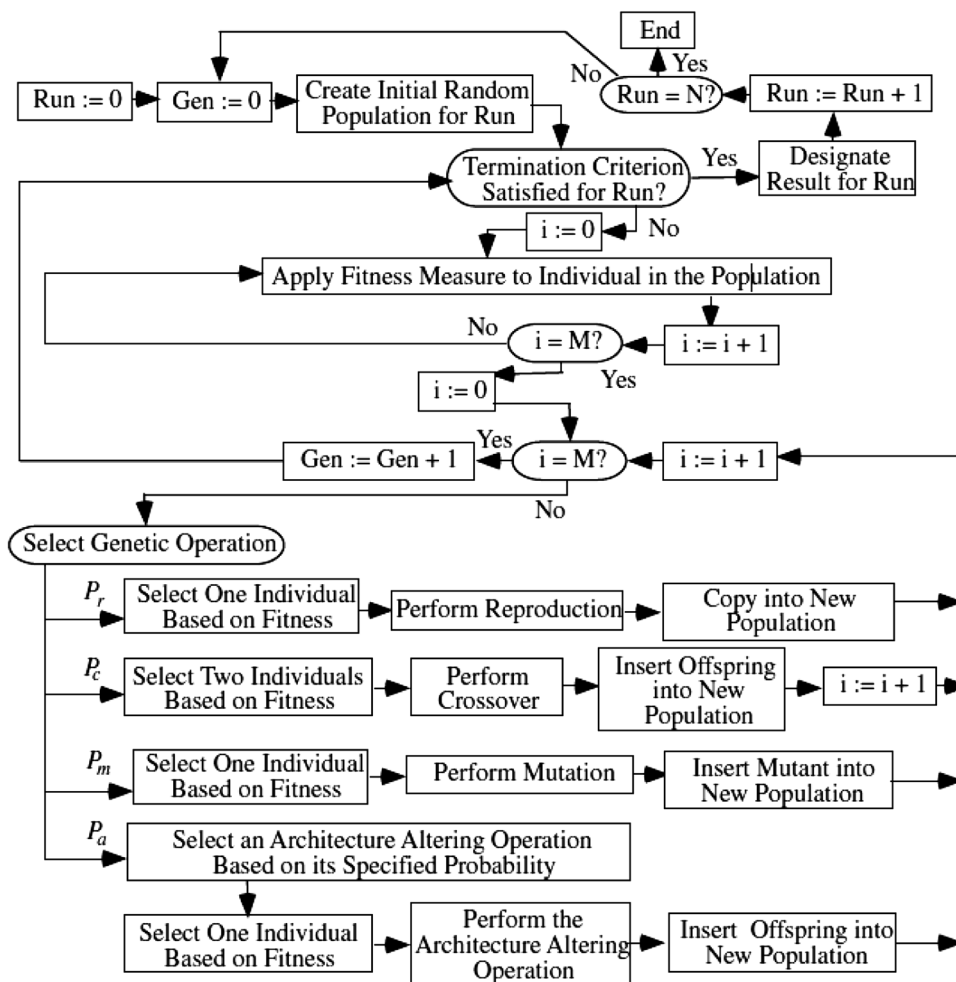
crossover. Finally, the best program in the generation is designated (Koza 1992). Figure 2 shows a flowchart presenting general genetic programming workflow.

The generated potential solutions in the form of a tree structure during the GP operation may have better and worse terms (subtrees) that contribute more or less to the accuracy of the model represented by the tree structure. Orthogonal least squares (OLS) algorithm is used to estimate the contribution of the tree branches to the accuracy of the model, and hence, terms having the smallest error reduction ratio could be eliminated from the tree. Figure 2 illustrates an example of elimination of a sub-tree based on OLS.

Results and discussion

A database of 150 Saudi Arabian crude oil samples was utilized. The database includes 79 saturated samples and 71 undersaturated samples with viscosity measurements (μ) at wide ranges of pressures and temperatures. Other

Fig. 2 General flowchart of genetic programming (Koza et al. 2003)



parameters including dead oil viscosity (μ_d), solution gas-oil ratio (R_s), bubble point pressure (P_{ob}), crude API, gas specific gravity (γ_g), and crude viscosity at bubble point (μ_{ob}) are also included. The quality of the data was judged and compared before they were considered and they were randomized and used in genetic programming (GP) software capable of building computer program out of the data provided to develop, test and validate the two proposed saturated and undersaturated viscosity models. Both saturated and undersaturated datasets were divided into three segments. The first two were used to train and test the model while the third was spared to blind test and validate the model efficiency. The software was run for 1000 generations with a maximum population size of 500. Several values of crossover and mutation rates were investigated, and the optimum setting found was 50 and 95% for crossover frequency and mutation frequency, respectively. The function set used was limited to (+, -, *, / and $\sqrt{\quad}$) while the terminal set was the input parameters for each model in addition to machine randomly generated constants. The generation of genetic programming models was started and terminated when project history showed no improvement (Fig. 3).

Saturated oil viscosity model

A dataset of 79 saturated crude samples was randomized, and two segments of 26 samples each were used for both training and testing. The rest was used for model validation and blind testing. The model was simply developed as a function of solution gas-oil ratio and viscosity at bubble point pressure as input parameters. The evolved viscosity model shows efficient performance, and Table 1 lists the domain of the data segments used in building and testing processes in addition to that used for validation of the developed GP saturated oil viscosity model. Figure 4 presents the best evolved genetic program in C++ code. The f[0], f[1], etc. are temporary computation variables used in

the program evolved. The output is the value of f[0] after program execution. The variable labels V[0], V[1], etc. are the names assigned to input data. Writing up the equation (Eq. 1) representing the evolved program for saturated oil viscosity, we obtained the following:

$$\mu = \frac{a_{15} \left[\left(D + \frac{|2D|-D}{a_{16}} \right) (a_{16}^2 - a_{16}) - \frac{|2D|-D}{a_{16}^2} \right] + a_{16}^3 \mu_d}{a_{16}^4} \tag{1}$$

where

$$D = \left| \frac{a_{13}C - 2A + a_{14}}{B} \right| + 7 \left(\frac{2A}{B} - a_2 \right)$$

$$A = R_s (a_1 - \mu_d^2) - a_2$$

$$B = \frac{a_4 A^2 (2 - a_5 \mu_d)^2}{a_3} + a_6 \mu_d + a_7$$

$$C = \sqrt{|a_{10} \mu_d + a_{11} \mu_d R_s + a_{12}|}$$

The A, B, C, and D are the computation variables used in the program evolved, whereas the a_1, a_2, \dots, a_{16} are the correlation coefficients as listed.

a_1	1.9244	a_9	0.9592
a_2	0.0026	a_{10}	0.6221
a_3	0.6189	a_{11}	0.0023
a_4	2.8541	a_{12}	0.1979
a_5	0.9404	a_{13}	0.6342
a_6	1.0895	a_{14}	0.6617
a_7	1.4270	a_{15}	1.3709
a_8	1.0632	a_{16}	0.9974

The model efficiency was compared to some published correlations such as Chew and Connally (1958), Beggs and Robinson (1975), Khan et al. (1987), and Naseri et al. (2005). Figure 5 consists of crossplots of the predicted

Fig. 3 An example of elimination of a sub-tree

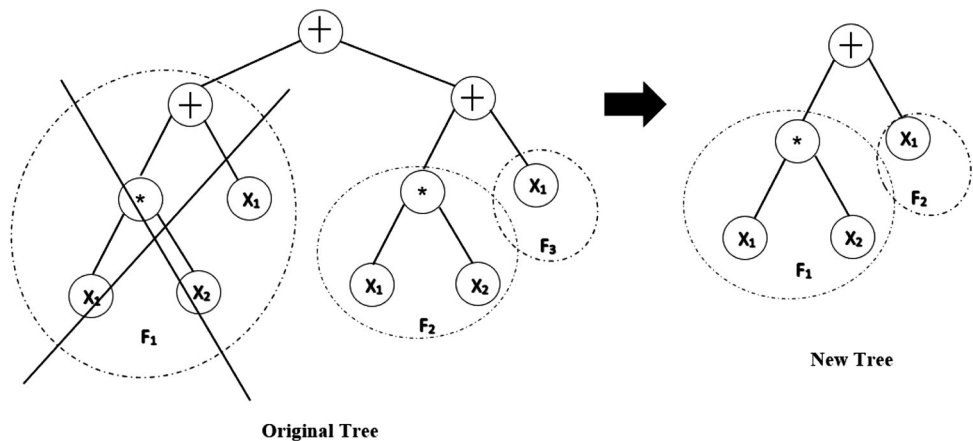


Table 1 Minimum and maximum values for the used data in building and validating the new saturated crude viscosity model

	Building and testing data			Validation data		
	R_s (cf/bbl)	μ_d (cp)	μ_o (cp)	R_s (cf/bbl)	μ_{ob} (cp)	μ_o (cp)
Minimum	0	1.085	0.37	0	1.085	0.38
Maximum	1020	6.72	5.06	895	6.72	6.72

versus experimentally measured viscosities using the developed genetic viscosity model and the four previously mentioned correlations. Average absolute relative error (AARE) and Pearson’s coefficient of correlation (COC) defined in Eqs. 2 and 3 were calculated, and the AARE was used to validate the efficiency of proposed model in comparison with other tested models.

$$AARE = \frac{100}{n} \sum \frac{|\mu_{Actual} - \mu_{Forecast}|}{|\mu_{Actual}|} \tag{2}$$

$$COC = \frac{\sum (\mu_{Actual} - \overline{\mu_{Actual}})(\mu_{Forecast} - \overline{\mu_{Forecast}})}{\sqrt{\sum (\mu_{Actual} - \overline{\mu_{Actual}})^2 (\mu_{Forecast} - \overline{\mu_{Forecast}})^2}} \tag{3}$$

where

- μ_{Actual} = measured viscosity value, cp.
- $\mu_{Forecast}$ = correlated viscosity value, cp.
- $\overline{\mu_{Actual}}$ = average measured viscosity value, cp.
- $\overline{\mu_{Forecast}}$ = average correlated viscosity value, cp.

The figure indicates that the proposed model (Fig. 5a) outperforms the other correlations in predicting the experimentally measured viscosity with the least average absolute relative error (AARE) of 9.37% and highest coefficient of correlation (COC) of 99.35%. Beggs and Robinson (1975) was the second best correlation while the least accuracy was that of Naseri et al. (2005). Khan et al. (1987) correlation was originally developed for Saudi crude oil, and we expected high performance; however, it shows a significant departure from the 45° line for higher viscosity range of our dataset. Table 2 summarizes the accuracy of the developed GP model in comparison with the different correlations in predicting the saturated crude oil viscosity.

Undersaturated oil viscosity model

The dataset used for this model consists of 71 experimental measurements of undersaturated crude oil viscosity. The model was developed as a function of pressure, bubble point pressure, and viscosity at bubble point pressure as input parameters. Table 3 lists the ranges of the data used

in building and validating the new undersaturated oil viscosity model constituting the limits of the model. Figure 6 presents the best evolved genetic program in C++ code. Equation 4 represents the write up of the evolved program for undersaturated oil viscosity,

$$\mu = \mu_{ob} + b_8 * D - b_9. \tag{4}$$

where

$$D = b_6(C - \mu_{ob}) - b_7$$

$$C = \left(\frac{P}{P_b}\right)(b_4 \cdot A \cdot B + b_5 + \mu_{ob})$$

$$B = \mu_{ob} - b_3$$

$$A = b_1 \left(\frac{P}{P_b}\right)(\mu_{ob} - b_2)$$

Again, the A, B, C, and D are the computation variables used in the evolved program, whereas the b_1, b_2, \dots, b_9 are the correlation coefficients listed as follows:

b_1	0.1317	b_4	1.0529	b_7	0.0086
b_2	1.7892	b_5	0.3579	b_8	0.3055
b_3	3.4466	b_6	0.1323	b_9	0.0099

The model efficiency was tested against some commonly used correlations such as Vazquez and Beggs (1977), Khan et al. (1987), Kartoatmodjo and Schmidt (1991), Hossain et al. (2005), and Bergman and Sutton (2006). The evolved undersaturated viscosity GP model shows efficient performance over wide ranges of input variables. Figure 7 consists of plots of the predicted versus experimentally measured viscosities using the developed genetic viscosity model and the four previously mentioned correlations. All models tested shows good accuracy with best performance obtained with the proposed GP model indicating an average absolute relative error of 9.36%. Table 4 shows the accuracy of the developed model in comparison with the different correlations in predicting the undersaturated crude oil viscosity.


```

#define TRUNC(x)((x)>=0 ? floor(x) : ceil(x))
#define C_FPREM(_finite(f0)/f1) ? f0-(TRUNC(f0/f1)*f1) : f0/f1
#define C_F2XMI1 (((fabs(f0)<=1) && (!isnan(f0))) ? (pow(2,f0)-1) : ((!_finite(f0) && !_isnan(f0) && (f0<0)) ? -1 : f0))
float DiscipulusCFunction(float v[])
{
  long double f[8];
  long double tmp = 0;
  int cflag = 0;
  f[0]=f[1]=f[2]=f[3]=f[4]=f[5]=f[6]=f[7]=0;
  L0:   f[0]+=v[0];
  L1:   f[1]+=f[0];
  L2:   f[0]*=f[2];
  L3:   f[0]=fabs(f[0]);
  L4:   f[0]=v[1];
  L5:   f[0]*=v[1];
  L6:   f[0]=-1.924433708190918f;
  L7:   f[0]*=f[1];
  L8:   f[0]=0.002621650695800781f;
  L9:   f[2]=f[0];
  L10:  f[2]=f[0];
  L11:  f[0]/=-1.063283443450928f;
  L12:  f[0]*=v[1];
  L13:  f[1]=f[0];
  L14:  f[0]=f[2];
  L15:  f[0]*=f[0];
  L16:  f[0]/=-1.063283443450928f;
  L17:  f[0]=0.6342074871063232f;
  L18:  f[0]*=f[0];
  L19:  f[0]*=-1.427085638046265f;
  L20:  f[0]=v[1];
  L21:  f[0]=0.9177978038787842f;
  L22:  f[0]=-1.427085638046265f;
  L23:  f[2]=f[0];
  L24:  f[0]/=-0.5786151885986328f;
  L25:  f[0]*=0.1387641429901123f;
  L26:  f[0]=fabs(f[0]);
  L27:  f[0]*=f[2];
  L28:  f[0]*=v[1];
  L29:  f[0]*=f[2];
  L30:  f[0]=f[1];
  L31:  f[1]=f[0];
  L32:  f[0]=f[1];
  L33:  f[0]=f[0];
  L34:  f[0]=fabs(f[0]);
  L35:  f[0]*=f[0];
  L36:  f[2]=f[0];
  L37:  f[0]+=f[3];
  L38:  f[0]=sqrt(f[0]);
  L39:  f[0]=f[0];
  L40:  f[0]=fabs(f[0]);
  L41:  f[0]=v[0];
  L42:  f[0]*=f[3];
  L43:  f[0]=0.002621650695800781f;
  L44:  f[1]=f[0];
  L45:  f[2]=f[0];
  L46:  f[0]/=-1.196667432785034f;
  L47:  f[0]*=v[1];
  L48:  f[0]/=-1.360518217086792f;
  L49:  f[0]*=v[1];
  L50:  f[0]*=v[0];

```

Fig. 4 Saturated crude viscosity model in C++ language

```

L51:  f[0]=0.1387641429901123f;
L52:  f[0]+=v[1];
L53:  f[0]*=-1.360518217086792f;
L54:  f[0]+=v[1];
L55:  f[0]*=1.048232078552246f;
L56:  f[0]+=v[1];
L57:  f[0]=fabs(f[0]);
L58:  f[0]=sqrt(f[0]);
L59:  f[0]=1.047447681427002f;
L60:  f[0]*=0.6342074871063232f;
L61:  f[0]+=f[2];
L62:  f[0]=fabs(f[0]);
L63:  f[0]=f[2];
L64:  f[3]=f[0];
L65:  f[0]=f[2];
L66:  f[0]=f[2];
L67:  f[0]=f[2];
L68:  f[0]=f[2];
L69:  f[0]=f[2];
L70:  f[0]=f[2];
L71:  f[2]=f[0];
L72:  f[0]=f[2];
L73:  f[0]=fabs(f[0]);
L74:  f[0]+=f[2];
L75:  f[0]/=f[1];
L76:  f[0]/=f[1];
L77:  f[2]=f[0];
L78:  f[0]/=f[1];
L79:  f[0]=f[2];
L80:  f[0]/=f[1];
L81:  f[0]+=f[2];
L82:  f[0]/=f[1];
L83:  f[0]/=0.9955191612243652f;
L84:  f[0]=fabs(f[0]);
L85:  f[0]/=f[1];
L86:  f[2]/=f[0];
L87:  f[0]*=-1.364777803421021f;
L88:  f[0]+=v[1];
L89:  if (!_finite(f[0])) f[0]=0;

return f[0];
}

```

Fig. 4 continued

Sensitivity analysis

The impacts of the input independent variables on saturated and undersaturated crude oil viscosity models were calculated and presented by the GP software. The purpose of

variable impact analysis is to measure the sensitivity of model predictions to changes in independent variables. As a result of the analysis, every independent variable is assigned a relative variable impact value. The lower the percent value for a given variable, the less that variable

Fig. 5 Predicted versus experimentally measured saturated oil viscosity

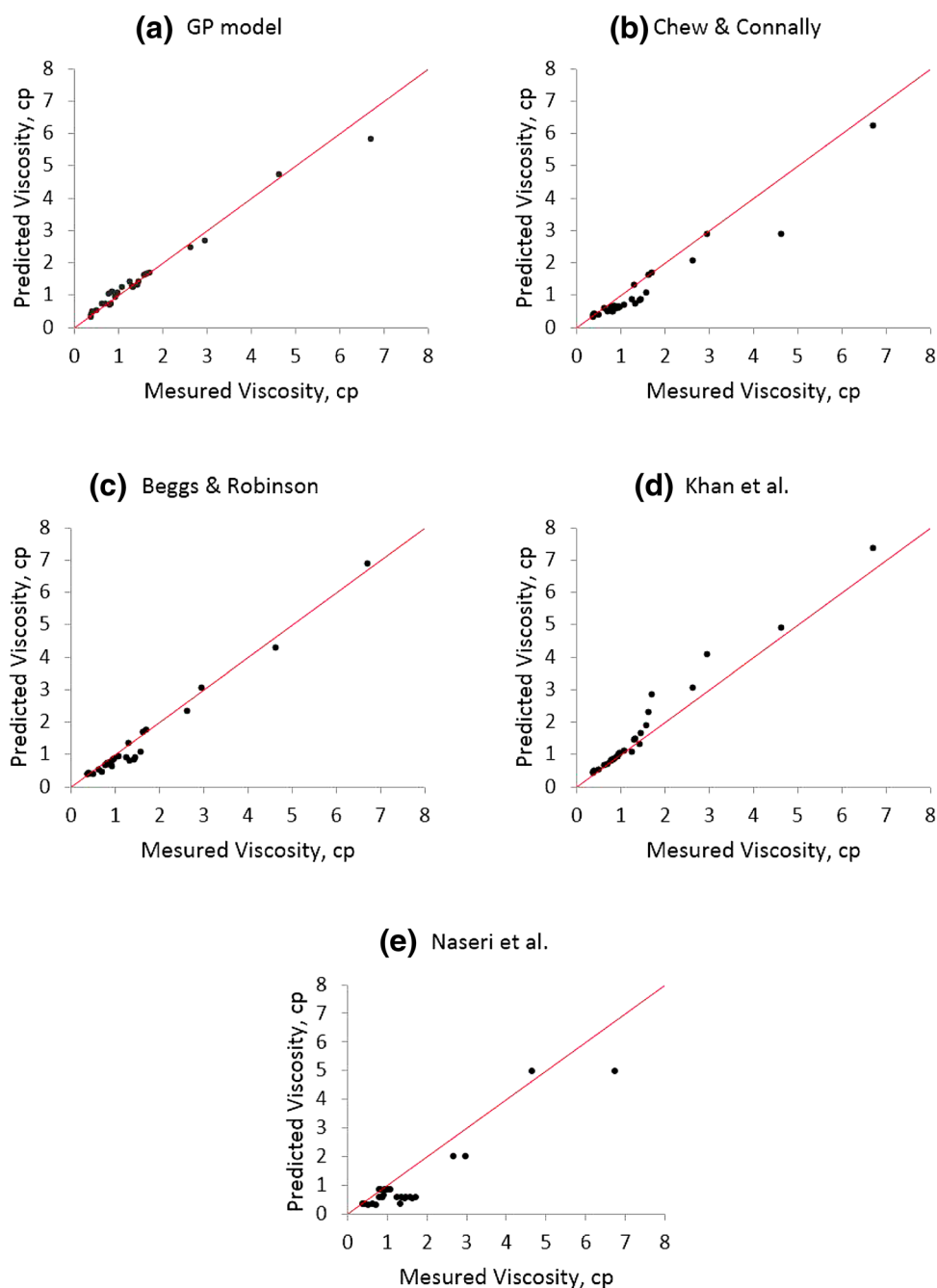


Table 2 Accuracy of developed saturated crude oil viscosity model in comparison with different published correlation

Models	AARE (%)	COC (%)
GP-based model	9.37	99.35
Beggs and Robinson	16.79	98.90
Chew and Connally	25.15	97.07
Khan et al.	17.82	98.40
Naseri et al.	34.34	93.75

affects the prediction. The results of the analysis can help in testing the model results robustness and simplifying the model with adequate accuracy by reducing the number of independent variables (inputs), those that have very low impact, if many were involved (AlQuraishi 2009). Figures 8 and 9 present the impact analysis of independent variables on saturated and undersaturated crude viscosity predictions, respectively. Saturated viscosity model is closely dependent on both R_s and μ_{ob} while undersaturated

Table 3 Minimum and maximum values for the used data in building and validating the new undersaturated crude viscosity model

	Building data				Validation data			
	Pressure (psi)	P_b (psi)	μ_{ob} (cp)	μ_o (cp)	Pressure (psi)	P_b (psi)	μ_{ob} (cp)	μ_o (cp)
Minimum	400	317	0.37	0.38	1000	317	0.37	0.38
Maximum	3495	2530	4.43	5.6	3200	2530	4.43	5.73

Fig. 6 Undersaturated crude viscosity model in C++ language

```

#define TRUNC(x)((x)>=0) ? floor(x) : ceil(x)
#define C_FPREM ( fmite(f[0]/f[1]) ? f[0]-(TRUNC(f[0]/f[1])*f[1]) : f[0]/f[1])
#define C_F2XM1 (((fabs(f[0])<=1) && (!_isnan(f[0]))) ? (pow(2,f[0])-1) : ((!_fmite(f[0]) && !_isnan(f[0]) && (f[0]<0)) ? -1 : f[0]))
float DiscipulusCFFunction(float v[])
{
    long double f[8];
    long double tmp = 0;
    int cflag = 0;
    f[0]=f[1]=f[2]=f[3]=f[4]=f[5]=f[6]=f[7]=0;
    L0:  f[0]+=-1.642645597457886f;
    L1:  f[0]/=0.9955191612243652f;
    L2:  f[0]/=0.9955191612243652f;
    L3:  f[3]+=f[0];
    L4:  f[0]+=v[2];
    L5:  f[0]=-0.1316959857940674f;
    L6:  f[1]+=f[0];
    L7:  f[3]+=f[0];
    L8:  f[0]*=v[0];
    L9:  f[0]/=v[1];
    L10: f[0]/=v[2];
    L11: f[0]+=-0.2174909114837647f;
    L12: f[0]*=0.1387641429901123f;
    L13: f[0]+=-0.03275442123413086f;
    L14: f[0]*=f[3];
    L15: f[0]-=-1.063283443450928f;
    L16: f[0]-=-0.7233922481536865f;
    L17: f[0]*=1.048232078552246f;
    L18: f[0]/=0.9955191612243652f;
    L19: f[0]+=v[2];
    L20: f[0]*=v[0];
    L21: f[0]/=v[1];
    L22: f[0]-=v[2];
    L23: f[0]/=0.9955191612243652f;
    L24: f[0]-=-0.03275442123413086f;
    L25: f[0]-=-0.03275442123413086f;
    L26: f[0]*=0.1316959857940674f;
    L27: f[0]/=0.9955191612243652f;
    L28: f[0]-=-0.03275442123413086f;
    L29: f[0]*=1.047447681427002f;
    L30: f[0]*=0.2877938747406006f;
    L31: f[0]/=0.9955191612243652f;
    L32: f[3]+=f[0];
    L33: f[0]/=0.9955191612243652f;
    L34: f[0]+=v[2];
    L35: if (!_fmite(f[0])) f[0]=0;
    return f[0];
}

```

Fig. 7 Predicted versus experimentally measured undersaturated oil viscosity

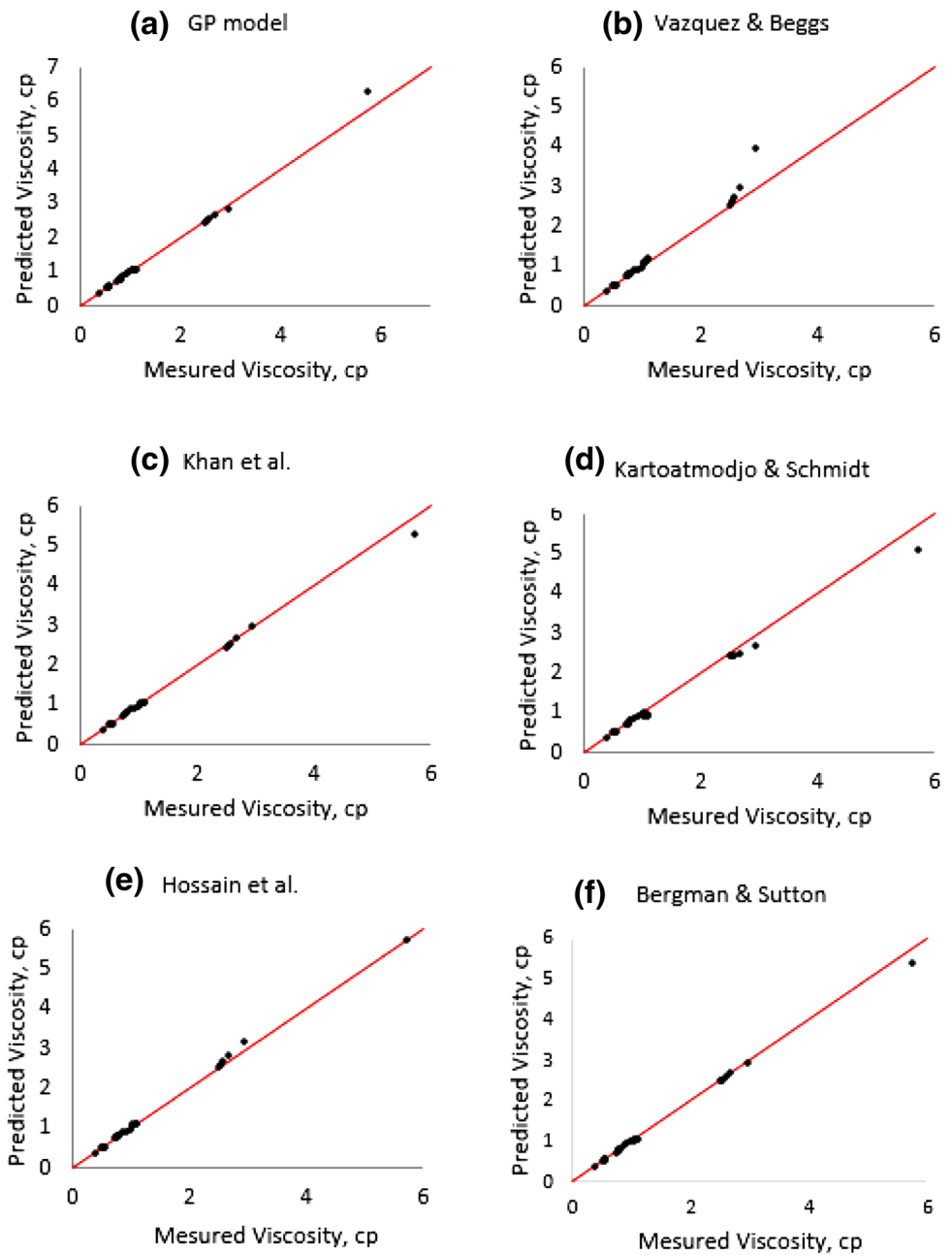


Table 4 Accuracy of developed model in comparison with different methods in predicting the undersaturated crude oil viscosity

Models	AARE (%)	COC (%)
GP-based model	1.64	99.78
Vazquez and Beggs	4.97	99.34
Khan et al.	1.73	99.86
Kartoatmodjo and Schmidt	5.96	99.84
Hossain et al.	2.18	99.91
Bergman and Sutton	1.84	99.89

viscosity model is highly dependent on μ_{ob} . The figures show the negative impact of R_s and the positive impact of μ_{ob} on saturated crude viscosity and the high positive impact of μ_{ob} on undersaturated crude viscosity.

Conclusion

Two models were developed to estimate saturated and undersaturated crude oil viscosity. Genetic programming approach was used to develop these two models using

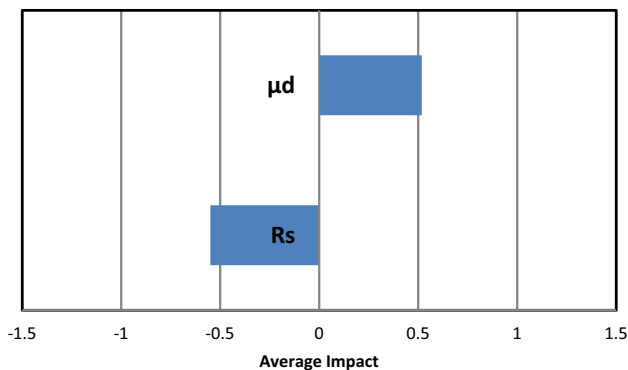


Fig. 8 Sensitivity analysis of the saturated crude viscosity model

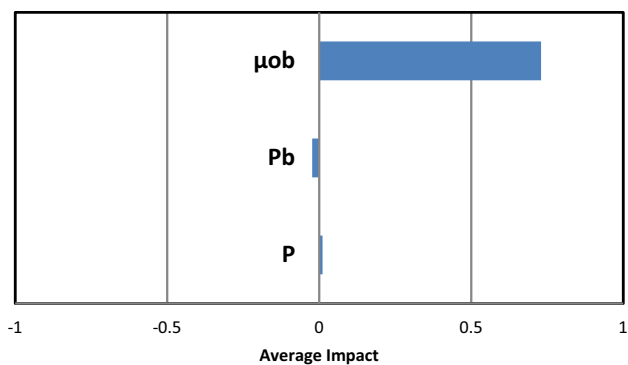


Fig. 9 Sensitivity analysis of the undersaturated crude viscosity model

experimental measurements. The models efficiency was tested against some commonly used correlations, and based on the results obtained, the following are concluded:

- Saturated viscosity model developed using solution gas–oil ratio (R_s) and dead crude viscosity (μ_d) as input variables provided good accuracy in predicting the experimental measurements and outperforms the other tested correlations with AARE of 9.37%.
- Undersaturated viscosity model developed using reservoir pressure (P) and crude bubble point pressure (P_{ob}) and crude viscosity at bubble point pressure (μ_{ob}) as inputs provided good accuracy in predicting the experimental measurements and outperforms the other tested correlations with AARE of 1.64%.
- The developed saturated model sensitivity analysis indicates the equivalent impact of dead crude viscosity (μ_d) and solution gas–oil ratio (R_s) but in opposite trend.
- The developed undersaturated model sensitivity analysis indicates the high positive impact of crude

viscosity at bubble point (μ_{ob}) and small negative impact of bubble point pressure (P_{ob}) and trivial positive impact of reservoir pressure (P).

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