

## TECHNICAL NOTE

D-1600

EXPERIMENTAL PANEL FLUTTER RESULTS FOR SOME FLAT AND CURVED TITANIUM SKIN PANELS AT SUPERSONIC SPEEDS

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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SUMMARY

The results of tests at Mach numbers from 1.72 to 2.62 on panels having a thickness from 0.015 to 0.045 inch, length-width ratio from 0.36 to 2.76 , and radius-thickness ratio from 600 to infinity are presented. These results indicate a strong influence of differential pressure, which caused buckling, on the flutter mode and on the dynamic pressure at flutter for the curved panels. Results for both the flat and curved panels fall within an extrapolation of an existing experimental panel flutter boundary.

## INTRODUCTION

Panel flutter has become an increasingly important design consideration for supersonic vehicles. Theoretical methods have not advanced enough to determine reliable panel flutter boundaries, and experimental results are generally used in design work. Minimum weight requirements, new materials, and manufacturing processes have contributed to the complexity of the skin structures, and additional experimental investigations are required for many new vehicles.

In order to supplement available experimental results, an investigation of the flutter characteristics of some low-aspect-ratio flat and curved titanium panels has been conducted in the Langley Unitary Plan wind tunnel. The panels were constructed of 0.050 -inch-thick sheets of titanium riveted to essentially rigid members on the four edges with the unsupported section chemically milled in steps to the desired skin thickness. Two panels having a radius of curvature of 48 inches and a radius-thickness ratio of 2,400 and one panel having a radius of curvature of 12 inches and a radius-thickness ratio of 600 were tested. The effect of pressure differential across the panel was also investigated. Tests were conducted over a Mach number range from 1.72 to 2.62 at dynamic pressures up to $2,670 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$.

E Young 's modulus of elasticity
2 unsupported panel length in streamwise direction, in.
M Mach number
$\mathrm{p} \quad$ static pressure on panel support face, $\mathrm{lb} / \mathrm{sq} \mathrm{ft}$
$\mathrm{p}_{\mathrm{c}} \quad$ cavity pressure behind panel, $\mathrm{lb} / \mathrm{sq} \mathrm{ft}$
$\Delta p \quad$ pressure differential across panel, $p_{c}-p$, lb/sq ft
$q \quad$ dynamic pressure, lb/sq ft
t skin thickness, in.
w unsupported panel width, perpendicular to airstream, in.
$\beta=\sqrt{M^{2}-1}$

## APPARAIUS

Wind Tunnel and Panel Support
Tests were conducted in the low Mach number test section of the Langley Unitary Plan wind tunnel, a variable-pressure, continuous-flow tunnel. The test section is 4 feet square and approximately 7 feet in length. The nozzle leading to the test section is of the asymmetric sliding-block type, and Mach number may be varied from 1.6 to 2.9 without tunnel shutdown.

The panel support system for flutter tests consists of a vertical splitter plate extending from floor to ceiling of the test section. In order to avoid the effects of the tunnel wall boundary layer, the flat surface or test side of the splitter plate is located about 15 inches from the tunnel side wall. Figure 1 includes photographs of the panel support installed in the test section. The face of the test-section door on which the support is mounted is dished out, and this in combination with a $1^{\circ}$ angle of attack of the flat surface of the splitter plate compensates for the presence of the splitter plate in the airstream and, thus, prevents tunnel choking.

A static-pressure survey over the face of the splitter plate indicated that the Mach number was reduced by 0.04 over the panel because of the $1^{\circ}$ angle of attack of the splitter plate. This reduction was indicated for both the flat
splitter plate configuration and the configuration with a curved fairing in place, and all Mach numbers quoted herein are so adjusted. The pressure survey indicated that a maximum deviation over the test panel surface of 3 percent of the free-stream static pressure occurred at a Mach number of 1.72 and diminished to a value of about l percent of the free-stream static pressure at a Mach number of 2.11.

(a) Typical flat and curved panels. L-61-1339

Figure 1.- Model photographs.

(b) Typical curved-panel installation. L-60-8612

Figure 1.- Continued.

Panels and Instrumentation
Panel geometric characteristics are presented in table I, and pretest vibration data with sketches of the node line locations are presented in table II. It should be noted that the node line location and frequencies are in some cases different than are ordinarily expected for a simple panel when only the structural restraints are considered. For example, the sequence of panels 1 to 3 represents a progressive decrease in panel thickness. It was expected that the frequency for a given mode of vibration would decrease with this sequence in an orderly manner, but this did not happen. The variation of frequency with mode shape for an individual panel was also unusual, in most cases. The behavior of these natural modes is thought to be caused primarily by cavity effects and secondarily by construction inaccuracies.

Photographs of the panels and tunnel installation are presented in figure 1 , and sketches of the test panel construction are presented in figure 2. The panels were constructed of 0.050 -inch-thick titanium sheets riveted on the four edges to steel angles. The unsupported portion of the sheets was chemically milled in two steps to lesser skin thicknesses as indicated in table I and as shown in figure 2. The angles supporting the skin were bolted to another steel angle which when mounted in the splitter plate formed a sealed box about 1.8 inches deep with the skin surface of the flat panels flush with the face of the splitter plate.


L-61-5834.1

(c) Stiffened-panel installation. L-61-5835.1

Figure 1.- Concluded.

(a) Flat-panel construction.

Figure 2.- Test panel details. All dimensions in inches.

The curved panels were constructed in a similar manner and curved wooden fairings were added to the face of the splitter plate as shown in the photograph in figure $1(b)$. The projected width of the 48 -inch-radius curved panels was about 22 inches and that of the l2-inch-radius panel was about 16 inches.

Each panel was instrumented with three strain gages and two variable-reluctance deflection pickups. Four of these five channels of information were selected for each run and recorded continuously on a magnetic tape recorder. Pressure in the sealed compartment behind the panels was remotely controlled by a pressure regulator and measured by means of a differential pressure gage which measured the difference between the cavity pressure and the static pressure on the panel support face. Motion pictures were taken during flutter at 1,000 frames per second to study the flutter modes and to insure that the signals recorded originated in the panels and not from faulty instrumentation.

## TEST PROCEDURE

In general, tests were conducted by using the following procedures: Supersonic flow was established at a low dynamic pressure, and the sliding-block nozzle was moved from the optimum starting Mach number position to the desired test Mach number position. Dynamic pressure was then increased in steps or, in some instances, at a slow rate. At each level of dynamic pressure or simultaneously with the slow rate of dynamic-pressure increase, the pressure behind the panel was cycled producing pressure differences across the panel within the range of about $\pm 100 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$. When flutter occurred, tunnel dynamic pressure and the pressure behind the panel were recorded manually. For the flat panels there was a definite pressure differential, usually near zero, for which the panel fluttered at the lowest dynamic pressure. After an approximate flutter level had been initially established and in order to insure that this minimum value of dynamic pressure was obtained, the dynamic pressure was increased into the flutter region several times with the pressure differential set at several positive and negative values.


Figure 2.- Continued.

## DISCUSSION OF RESULTS

The test results are presented in table III. The table includes Mach number, dynamic pressure, pressure differential, a panel flutter parameter $\left(\frac{\beta E}{q}\right)^{1 / 3} \frac{t}{l}$, and the flutter frequency. The data presented represent points at which flutter started during variation of either dynamic pressure or pressure differential, and the arrows appearing beside these quantities indicate the direction in which the quantity was being varied at flutter inception. Arrows pointing up indicate an increasing value; quantities having no arrows were held constant. Points representing maximum available dynamic pressure for panels which did not flutter are also presented.

(c) Stiffened-panel details (test panels 10 and 11).

Figure 2.- Concluded.

## Flat Panels

The results of the flutter tests of panels 1, 2, 3, and 11 are presented in figure 3 in terms of the minimum dynamic pressure at flutter, or the maximum dynamic pressure in cases for which no flutter was obtained, as a function of Mach number. The data do not have a uniform variation with Mach number, but do exhibit the expected trend of increasing dynamic pressure at flutter with increasing panel thickness. The exception to this increase was panel ll which was visibly buckled when installed in the splitter plate. Evidently, the panel was not severely buckled, since it fluttered at a low dynamic pressure. As described in reference 1 , the dynamic pressure at flutter decreases with increasing compressive stress to a minimum; thereafter, an increase in stress increases the flutter dynamic pressure. In reference 1 the minimum dynamic pressure was obtained when the panel was near the critical buckling stress.


Figure 3.- Effects of skin thickness and buckle condition on minimum flutter dynamic pressure for several flat panels.

## Curved Panels

Only one of the curved panels tested
(panel 4) fluttered, and the results
therefore appear somewhat inconsistent since panels 4 and 5 had the same radius and thickness and differed only by a l/2-inch-wide, 0.015 -inch-thick step increase in thickness along each edge of panel 5 . Panel 5 was tested to the tunnel dynamic pressure limit of $2,625 \mathrm{lb} / \mathrm{sq}$ ft and did not flutter. The results for panel 4 at a Mach number of 1.72 are plotted in figure 4 for $q$ as a function of pressure differential. The data are for runs 8 and 12 which were two separate tunnel installations. Only one flutter point was obtained on this panel in the unbuckled condition. This point was at a positive pressure differential of $66 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$ and a dynamic pressure of $1,599 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$. This flutter had a very low amplitude and was not visible to the naked eye and was barely visible in the highspeed motion picture. This behavior is in sharp contrast to the buckled flutter which had amplitudes of about $1 / 4$ inch and was easily visible. The variations in frequencies evident in figure 4 were caused by the different buckle patterns which initially occurred. Buckles having a large area had lower frequencies and higher amplitudes than the buckles having a small area. In some cases, the first buckles which occurred were of small area, and the associated flutter (which began immediately after the buckle formed) was of a higher frequency than the flutter which occurred as the pressure differential decreased and caused the small buckles to merge into larger buckles. For example, the two points in figure 4 at a dynamic


Figure 4.- Flutter boundaries for two tunnel installations of panel 4 at $M=1.72$.
pressure of $1,222 \mathrm{lb} / \mathrm{sq}$ ft were obtained by holding a constant dynamic pressure and decreasing pressure differential. The panel initially buckled at zero pressure differential and began flutter at a frequency of 165 cps . This flutter continued until the pressure differential reached $-31 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$; then, the buckle pattern changed and the flutter frequency decreased to 105 cps .

No panels were destroyed during the tests, and an indication of the fatigue life is given by the 0.015 -inch-thick panel 3, which fluttered an estimated 2.5 hours with only a slight stretching of the skin.

## Comparison of Test Results With Previous Results

Many of the test points obtained were above the minimum flutter dynamic pressure for a particular configuration and are therefore not compared with previously published data. The minimum flutter dynamic pressures for these tests are presented in figure 5 in terms of a panel flutter parameter $\left(\frac{\beta E}{q}\right)^{1 / 3} \frac{t}{2}$ and compared with the empirical envelope of reference 2. The maximum value of this parameter for each panel, which was encountered during the tests, is presented for all flat panels and for a buckled and unbuckled condition of a curved panel. Most of the data fall well within the envelope.


Figure 5.- Comparison of test results with experimental envelope of reference 2 .

The test results show that panel buckling greatly affects the dynamic pressure required for flutter although no degree of buckling was investigated. Results for all flat panels and a curved panel buckled by pressure differential are shown to agree with previous results for flat panels. The flutter characteristics of a curved panel are shown to be highly dependent on the shape the panel assumes when buckled by normal pressure load.

A need for research on the effect of the cavity behind the panel on panel flutter characteristics is indicated by the pretest vibration results.

Langley Research Center,
National Aeronautics and Space Administration, Langley Station, Hampton, Va., October 22, 1962.

REF ERENCES

1. Hess, Robert W., and Gibson, Frederick W.: Experimental Investigation of the Effects of Compressive Stress on the Flutter of a Curved Panel and a Flat Panel at Supersonic Mach Numbers. NASA TN D-1386, 1962.
2. Kordes, Eldon E., Tuovila, Weimer J., and Guy, Lawrence D.: Flutter Research on Skin Panels. NASA TN D-451, 1960.

TABLE I.- PANEL GEOMETRY


| Panel | l, <br> in. | w, <br> in. | l/w | Radius, <br> in. | $t_{1}$, <br> in. | $t_{2}$, <br> in. | t, <br> in. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 8.25 | 22.25 | 0.37 |  | 0.045 | 0.045 | 0.045 |
| 2 | 8.25 | 22.25 | .37 |  | .050 | .035 | .025 |
| 3 | 8.25 | 22.25 | .37 |  | .050 | .035 | .015 |
| 4 | 7.875 | 22.125 | .36 | 48 | .050 | .020 | .020 |
| 5 | 7.875 | 22.125 | .36 | 48 | .050 | .035 | .020 |
| 6 | 7.875 | 16.125 | .49 | 12 | .050 | .035 | .020 |
| 7 | 8.25 | 3.25 | 2.54 |  | .050 | .035 | .025 |
| 8 | 3.25 | 8.25 | .39 |  | .050 | .035 | .025 |
| 9 | 8.25 | 8.25 | 1.00 |  | .050 | .035 | .025 |
| 10 | 23.25 | 8.41 | 2.76 |  | .050 | .035 | .022 |
| 11 | 28.41 | 23.25 | .36 |  | .050 | .035 | .022 |

${ }^{2}$ Panel includes two bays of this dimension separated by stiffener. (See sketch in fig. 2(c).)
table II.- PRETEST vIbration data

| Panel |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| Panel | Run | Point | Mach number | $\begin{gathered} \mathrm{q}, \\ \mathrm{lb} / \mathrm{sq} \mathrm{ft} \\ (\mathrm{a}) \end{gathered}$ | $\Delta \mathrm{p}$, lb/sq ft <br> (a) | $\left(\frac{\beta E}{q}\right)^{1 / 3} \frac{t}{2}$ | Flutter frequency, cps | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.96 \end{aligned}$ | $\begin{aligned} & 2,114 \\ & 2,670 \end{aligned}$ | $\left\lvert\, \begin{aligned} & \text { Vary } \pm 100 \\ & \text { Vary } \pm 100 \end{aligned}\right.$ | $\begin{array}{r} 0.5564 \\ .5467 \end{array}$ | No flutter No flutter | $\begin{array}{\|ll} \text { Max. } & \mathrm{q} \\ \text { Max. } & \mathrm{q} \end{array}$ |
| 2 | $\begin{aligned} & 3 \\ & 3 \\ & 3 \\ & 3 \\ & 4 \\ & 4 \\ & 5 \\ & 5 \\ & 5 \end{aligned}$ | $\begin{array}{r} 3 \\ 4 \\ 5 \\ 6 \\ 8 \\ 9 \\ 10 \\ 11 \end{array}$ | $\begin{aligned} & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.96 \\ & 1.96 \\ & 2.11 \\ & 2.11 \end{aligned}$ | $\begin{aligned} & \uparrow \quad 888 \\ & \uparrow 1,727 \\ & \uparrow 1,816 \\ & 1,733 \\ & \uparrow 1,724 \\ & \downarrow 1,700 \\ & \uparrow 1,882 \\ & \downarrow 1,857 \end{aligned}$ | $\begin{array}{r} \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ 28 \\ 24 \\ \\ \uparrow \\ \hline 22 \\ 22 \\ \downarrow-30 \\ -30 \end{array}$ | .4122 <br> . 3297 <br> . 3248 <br> .3297 <br> . 3515 <br> . 3600 <br> . 3539 <br> .3539 | No flutter No flutter 185 185 156 155 | Min. flutter q <br> Flutter stopped <br> Flutter stopped |
| 3 | $\begin{aligned} & 6 \\ & 6 \\ & 6 \\ & 6 \\ & 6 \\ & 6 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \\ & 7 \end{aligned}$ | $\begin{aligned} & 12 \\ & 13 \\ & 14 \\ & 15 \\ & 16 \\ & 17 \\ & 18 \\ & 19 \\ & 20 \\ & 21 \\ & 22 \\ & 23 \\ & 24 \\ & 25 \\ & 26 \\ & 27 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \end{aligned}$ | $\begin{array}{r} \uparrow \quad 806 \\ 814 \\ 1,017 \\ 1,222 \\ 1,657 \\ 1,686 \\ \uparrow \quad 670 \\ \uparrow 1,175 \\ \downarrow 1,007 \\ 838 \\ 670 \\ 838 \\ 1,007 \\ 1,175 \\ 1,343 \\ 1,016 \end{array}$ |  | .2545 <br> .2533 <br> .2303 <br> . 2230 <br> . 2012 <br> .2000 <br> .2976 <br> .2473 <br> .2606 <br> .2776 <br> .2970 <br> .2776 <br> .2727 <br> .2473 <br> .2315 <br> .7606 | 60,290 60,400 60,320 60 60 60 No flutter Flutter Flutter 60 and 760 60 and 155 Flutter 60 and 750 Flutter Flutter 60 and 175 | Min. flutter q <br> Frequency not determined <br> Frequency not determined <br> Min. flutter $q$ <br> Frequency not determined <br> Frequency not determined <br> Frequency not determined |
| 4 | 8 8 8 8 9 9 10 10 11 11 11 12 12 12 12 12 12 12 12 12 | 28 29 30 31 32 33 34 35 36 37 $3-1$ 39 40 41 42 43 44 45 46 | 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.96 <br> 1.96 <br> 2.11 <br> 2.11 <br> 2.62 <br> 2.62 <br> 2.62 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 <br> 1.72 | $\uparrow$ 677 <br>  683 <br> 685  <br>  671 <br> $\uparrow$ 678 <br>  710 <br> $\uparrow$ 813 <br> $\downarrow$ 589 <br> $\uparrow$ 577 <br>  581 <br>  312 <br> $\uparrow$ 408 <br>  408 <br> 814  <br> 1,017  <br> 1,193  <br> 1,222  <br> 1,222  <br> 1,428  <br> 1,428  | $\begin{aligned} & \downarrow-32 \\ & \downarrow-20 \\ & \downarrow-29 \\ & \downarrow-26 \\ & \downarrow-21 \\ & \downarrow-16 \\ & \downarrow-19 \\ & -19 \\ & \downarrow-45 \\ & \downarrow+11 \\ & \downarrow-26 \\ & \uparrow-5 \\ & \uparrow 62 \\ & \downarrow=0 \\ & \downarrow-42 \\ & \downarrow-39 \\ & \downarrow \\ & \downarrow \\ & \downarrow-31 \\ & \downarrow \\ & \hline \end{aligned}$ | .3784 <br> .3771 <br> .3759 <br> .3810 <br> . 3975 <br> . 3962 <br> . 3924 <br> .4356 <br> .4800 <br> .4787 <br> .5892 <br> .4483 <br> .4483 <br> .3276 <br> .3302 <br> . 3137 <br> .3111 <br> .3111 <br> .2946 <br> .2946 | Flutter 110 117 120 120 115 120 120 and 245 45 No flutter 45 and 78 103 97 165 105 175 115 | Frequency not determined Flutter stopped <br> Flutter stopped <br> Flutter stopped Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition |

${ }^{\text {a }}$ Arrows pointing up indicate an increasing value; arrows pointing down indicate a decreasing value.

| Panel | Run | Point | $\begin{gathered} \text { Mach } \\ \text { number } \end{gathered}$ | $\begin{gathered} q, \\ 1 \mathrm{~b} / \mathrm{sq} \mathrm{ft} \\ (\mathrm{a}) \end{gathered}$ |  | $\left(\frac{\beta E}{q}\right)^{1 / 3} \frac{t}{l}$ | Flutter frequency, cps | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | $\begin{aligned} & 12 \\ & 13 \\ & 13 \\ & 13 \\ & 13 \\ & 13 \\ & 13 \\ & 13 \\ & 13 \\ & \hline \end{aligned}$ | 47 <br> 48 <br> 49 <br> 50 <br> 51 <br> 52 <br> 53 <br> 54 <br> 55 | $\begin{aligned} & 1.72 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \\ & 2.11 \end{aligned}$ | $\begin{array}{r} 11,599 \\ \uparrow 838 \\ 1,007 \\ 1,175 \\ 1,343 \\ 1,508 \\ 1,508 \\ 1,677 \\ 1,845 \end{array}$ | $\begin{array}{r} 66 \\ \downarrow-30 \\ \downarrow-23 \\ \downarrow-34 \\ \downarrow-21 \\ \downarrow-22 \\ \downarrow-25 \\ \downarrow-23 \\ \downarrow-24 \end{array}$ | $\begin{array}{r} \hline 0.2844 \\ .3873 \\ .3644 \\ .3467 \\ .3314 \\ .3187 \\ .3187 \\ .3073 \\ .2971 \end{array}$ | $\begin{array}{r} \hline 760 \\ 62 \\ 72 \\ 78 \\ 88 \\ 89 \\ 83 \\ 100 \\ 91 \end{array}$ | Unbuckled Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition Buckled condition |
| 5 | 14 | 56 | 1.96 | 2,625 | Vary $\pm 100$ | . 2565 | No flutter | Max. q |
| 6 | $\begin{aligned} & 15 \\ & 16 \end{aligned}$ | $\begin{aligned} & 57 \\ & 58 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.96 \end{aligned}$ | $\begin{aligned} & 2,100 \\ & 2,625 \end{aligned}$ | $\begin{aligned} & \text { Vary } \pm 100 \\ & \text { Vary } \pm 100 \end{aligned}$ | $\begin{aligned} & .2590 \\ & .2552 \end{aligned}$ | No flutter No flutter | $\begin{array}{ll} \operatorname{Max} . & q \\ \operatorname{Max} . & q \end{array}$ |
| 7 | $\begin{aligned} & 17 \\ & 18 \end{aligned}$ | $\begin{aligned} & 59 \\ & 60 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.96 \end{aligned}$ | $\begin{aligned} & 1,295 \\ & 1,745 \end{aligned}$ | $\begin{array}{\|l} \text { Vary } \pm 100 \\ \text { Vary } \pm 100 \end{array}$ | $\begin{aligned} & .3635 \\ & .3505 \end{aligned}$ | No flutter No flutter | $\begin{array}{ll} \text { Max. } & \mathrm{q} \\ \text { Max. } & \mathrm{q} \end{array}$ |
| 8 | 19 | 61 | 1.96 | 1,740 | Vary $\pm 100$ | .8876 | No flutter | Max. q |
| 9 | $\begin{aligned} & 20 \\ & 20 \\ & 21 \\ & 21 \\ & 21 \\ & 21 \\ & 21 \\ & 21 \end{aligned}$ | 62 <br> 63 <br> 64 <br> 65 <br> 66 <br> 67 <br> 68 <br> 69 | $\begin{aligned} & 1.96 \\ & 1.96 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \end{aligned}$ | $\begin{array}{r} \uparrow 1,098 \\ 1,098 \\ 900 \\ 1,010 \\ 1,050 \\ 1,110 \\ 1,180 \\ 1,445 \end{array}$ | $\begin{array}{rr} \downarrow-60 \\ \uparrow & 0 \\ -50 \\ \\ \downarrow-50 \\ \downarrow-50 \\ \downarrow-50 \\ \downarrow-50 \\ \downarrow-50 \end{array}$ | $\begin{aligned} & .4086 \\ & .4086 \\ & .4103 \\ & .3947 \\ & .3898 \\ & .3827 \\ & .3727 \\ & .3504 \end{aligned}$ | $\begin{gathered} 230 \\ \text { No flutter } \\ 240 \\ \\ 240 \\ 240 \\ 240 \\ 240 \\ 240 \end{gathered}$ | Min. flutter q; intermittent flutter |
| 10 | $\begin{aligned} & 22 \\ & 22 \\ & 22 \\ & 22 \\ & 22 \\ & 23 \\ & 23 \\ & 23 \\ & 23 \end{aligned}$ | $\begin{aligned} & 70 \\ & 71 \\ & 72 \\ & 73 \\ & 74 \\ & 75 \\ & 76 \\ & 77 \\ & 78 \end{aligned}$ | $\begin{aligned} & 1.96 \\ & 1.96 \\ & 1.96 \\ & 1.96 \\ & 1.96 \\ & 1.72 \\ & 1.72 \\ & 1.72 \\ & 1.72 \end{aligned}$ | $\begin{array}{r} \uparrow \quad 915 \\ 1,025 \\ 1,097 \\ 1,097 \\ 1,098 \\ \uparrow \begin{array}{r} 857 \\ 877 \\ 877 \\ 877 \end{array} \end{array}$ |  0 <br> $\uparrow$ -6 <br> $\uparrow$ -4 <br> $\uparrow$ -2 <br> $\uparrow-10$  <br>  0 <br> $\uparrow$ -5 <br> $\uparrow$ -5 <br> $\uparrow$ -15 | .1322 <br> .1278 <br> .1252 <br> .1252 <br> .1252 <br> .1275 <br> .1265 <br> . 1265 <br> .1265 | $\begin{array}{\|c} 104 \\ 112 \\ 112 \text { and } 220 \\ 280 \\ 105 \\ 280 \\ 280 \\ 125 \\ 150 \end{array}$ | Min. flutter $q$ <br> Min. flutter <br> q |
| 11 | 24 <br> 24 <br> 25 <br> 25 | $\begin{aligned} & 79 \\ & 80 \\ & 81 \\ & 82 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.72 \\ & 1.96 \\ & 1.96 \end{aligned}$ | $\begin{array}{ll} \uparrow & 297 \\ \uparrow & 270 \\ \uparrow & 292 \\ \uparrow & 296 \\ \hline \end{array}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & .5030 \\ & .5190 \\ & .5382 \\ & .5382 \\ & \hline \end{aligned}$ | $\begin{aligned} & 159 \\ & 159 \\ & 145 \\ & 140 \\ & \hline \end{aligned}$ | ```Panel initially buckled Min. flutter q Min. flutter q``` |

${ }^{\text {a }}$ Arrows pointing up indicate an increasing value; arrows pointing down indicate a decreasing value.

