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SUBCOOLED BOILING HEAT TRANSFER UNDER

FORCED CONVECTION IN A HEATED TUBE

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
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SUMMARY

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Single- and two-phase heat-transfer data were obtained by using distilled water flowing through an Inconel X resistance-heated tube. The nonboiling data were correlated with a Colburn-type equation that was modified to include the boiling phenomena by means of three significant parameters obtained by dimensional analysis from basic considerations. Comparable heat-transfer data from reference sources, covering a broad range of conditions, were used in the development of the correlation. The reference data and the limited data obtained from the experimental program extended the generality of the correlation to cover a range of pressure from 16 to 2000 pounds per square inch, heat flux from 0.026 to 56.0 Btu per square inch per second, fluid velocity from 1.33 to 204 feet per second, and subcooling from 6° to 336° F. Liquid-ammonia data were included to demonstrate the applicability of the correlation to fluids other than water.

Comparisons were made between wall temperatures at the incipience of boiling as predicted by an analytically derived equation and the experimental data.

## INTRODUCTION

Emphasis has previously been placed on obtaining engineering correlations of experimental data from both pool and forced-flow boiling systems. Unfortunately, a basic approach at obtaining an understanding of boiling mechanisms is hampered by the complex interaction of the many parameters involved, and analysis becomes difficult. Many unknowns such as the dependence of heat flux or surface conditioning and the statistical nature of bubble growth are difficult to evaluate. Equations presented in the literature are usually derived from limited data by using correlating techniques that do not include all the significant parameters.

The confusion that exists in connection with pool boiling is shown in reference 1 by a partial list of correlations obtained since 1952. These equations are reliable for individual sets of data but not for general use. Calculations have shown that deviations of heat flux can vary by a factor of 2 or more.

The present investigation is concerned primarily with the forced-flow system. The added complexity of the fluid velocity on the ebullition process makes

analysis more difficult than would be expected for the pool-boiling system. Correlations presented in the literature are, therefore, either strictly empirical or based on some semiempirical method. References 2 to 12 contain a partial listing of such correlations, which are subject to the limitations existing in pool boiling. Correlations that work well for one set of data do not necessarily fit data from other facilities even for similar test conditions.

Although it is not expected that a unique set of data could ease the confusion that exists, it is felt that reliable heat-transfer data are required to provide the tools for obtaining a more general understanding of the boiling phenomena. An experimental investigation was initiated with the expectation of using the data obtained to develop a more general type of engineering correlation.

Single- and two-phase heat-transfer data were obtained by using distilled water flowing through an Inconel X resistance-heated tube. The test section was 6.5 inches long and had an inside diameter of 0.311 inch. The system variables included a range of pressure from 37 to 179 pounds per square inch absolute, velocity from 3.8 to 12.5 feet per second, heat flux from 0.37 to 1.60 Btu per square inch per second, and subcooling from 180° to 263° F.

The nonboiling heat-transfer data obtained were first correlated using a Colburn-type equation made up of a group of dimensionless parameters. The boiling phenomena were then included by modification of this convection equation with three significant parameters obtained by dimensional analysis from basic considerations. The initial parameter used relates the volumetric rate of vaporization of the liquid to the fluid velocity along the heated surface. This relation was presented in reference 8 as a correlation of boiling data limited to a fixed pressure level and, when substantiated, was used as the basis for the present correlation. Two additional parameters were used to include the effect of pressure and degree of subcooling in the final correlation. The development of the correlation included forced-convection boiling heat-transfer data obtained from the literature, which covered a wide range of fluid properties and flow conditions. Liquid-ammonia data were shown to fit the correlation.

Experimentally determined wall temperatures were compared with calculated wall temperatures by employing an analytically derived equation (ref. 13) that predicts the incipience of boiling.

## EXPERIMENTAL EQUIPMENT

# Flow System

The flow system, which employed an explusion bag for obtaining steady fluid flow through the test section, is shown schematically in figure 1(a). Distilled water was contained in a neoprene-type bladder installed in the tank upstream of a flow-measuring orifice. Nitrogen gas, at controlled pressures, was introduced between the inner wall of the tank and the outer surface of the bladder to force the fluid through the flow system.

Mixing chambers, each consisting of a system of baffles, were installed

before and after the test section to eliminate temperature stratification in the fluid bulk. A system of valves and regulators controlled the flow rate and pressure level throughout the apparatus. The fluid discharged into the collector tank, which also contained an expulsion bladder for recycling. The piping apparatus was constructed entirely of stainless steel to minimize contamination problems.

#### Test Section

A schematic drawing of the instrumented test section (fig. 1(b)) shows measuring stations for wall temperature, pressure, and voltage drop. Inconel X tubing with an inside diameter of 0.311 inch and a 0.012-inch wall thickness was employed. The resistance-heated portion of the test section was 6.5 inches long. Pressure tubes, voltage taps, and iron-constantan thermocouples were silver soldered to the tube.

A 9000-watt alternating-current generator supplied power to heat the test section through two electrodes brazed to the outer wall of the tube. The power input was controlled by a variable transformer. The test section was electrically insulated from the rest of the flow system and was wrapped in Fiberglas to minimize ambient heat loss.

## Instrumentation

Bulk temperature and pressure were measured in the mixing chambers located at the inlet and the exit of the test section. The test section was instrumented with 12 thermocouples made of 28-gage iron-constantan wires installed in two rows along the length of the tube located 180° apart. The five pressure taps were made of 0.035-inch-outside-diameter stainless-steel thin-wall tubing. The five voltage taps were made of 28-gage copper wire.

All the basic data, including temperatures, pressure, flow rate, and alternating-current tube voltages, were converted to low direct-current voltage so that they could be recorded on a multichannel oscillograph.

## EXPERIMENTAL PROCEDURE

The controlled variables for operating the test apparatus included system pressure, flow rate, and power to heat the test section. For fixed values of pressure and flow rate, data were obtained at discrete intervals of power input to the limitations of the power source. At each power setting sufficient time was allowed for the system to reach steady-state conditions before the data were recorded. The same procedure was repeated for a range of flow rate and system pressure. At low flow rates, the wall temperature limited the amount of electric power that could be dissipated in the tube.

The heat-transfer data covered a range of system pressure from 37 to 179 pounds per square inch absolute, fluid velocity from 3.8 to 12.5 feet per second,

heat flux from 0.37 to 1.60 Btu per square inch per second, and subcooling from  $180^{\circ}$  to  $263^{\circ}$  F.

#### COMPUTATION PROCEDURE AND DATA PRESENTATION

Determination of experimental heat-transfer coefficients required local values of heat flux, inside surface wall temperature, and bulk temperature. The heat flux was obtained directly from measured values of current and voltage drop by the following equation:

$$q = 0.984 \times 10^{-3} \frac{ET}{A_1}$$
 (1)

(All symbols are defined in appendix A.) Equation (1) denotes a uniform heatflux distribution because of the insignificant change in electrical resistivity throughout the range of wall temperatures obtained. Verification of a linear voltage drop was made by five voltage taps spaced over the length of the test section.

Since the heat-transfer coefficient is based on heat flux from the inner surface of the tube, the measured outside wall temperatures were corrected for temperature drop through the wall. The following theoretical equation that assumes uniform internal power generation was obtained from reference 2:

$$T_{i} = T_{o} - K \frac{Q}{k}$$
 (2)

where

$$K = \frac{r_0^2 \ln \frac{r_0}{r_1} - \left(\frac{r_0^2 - r_1^2}{2}\right)}{2\pi L \left(r_0^2 - r_1^2\right)}$$

The local bulk temperatures were obtained by assuming sensible heating of the fluid as indicated by the following equation:

$$T_{b,x} = T_{b,in} + \frac{Qx}{L\dot{m}c_p}$$
 (3)

The second term on the right side of the equation is a measure of the temperature rise of the fluid caused by the heat input. This term was evaluated at each measuring station and added to the measured inlet bulk temperature to obtain the local bulk temperatures. The sensible heating assumption is correct for the single-phase heat-transfer data and can be accepted as valid for the two-phase heat-transfer data because of the high subcooling involved.

In order to eliminate uncontrollable end effects, the data presented were taken from the midportion of the test section. Table I lists the data and completed computations for temperature measuring station number 11, which was

chosen as representative of typical data in the midportion of the test section.

#### CORRELATION PROCEDURE AND DISCUSSION OF RESULTS

#### Nonboiling

The nonboiling heat-transfer data obtained in the present investigation were correlated by using a Colburn-type equation (ref. 2) with fluid properties evaluated at film temperature  $T_{f}$ . The logarithmic plot of the results presented in figure 2 shows a data scatter of approximately 20 percent. The equation of the dashed line representing the correlation is

$$Nu_{calc} = 0.021 \left(\frac{\rho_f V_b d}{\mu_f}\right)^{0.8} \left(\frac{c_p \mu}{k}\right)^{0.4}$$
(4)

References to calculated Nusselt number will imply use of equation (4) only when dealing with the experimental data presented herein. Nonboiling correlations presented in reference sources will be associated with their respective data.

## Subcooled Boiling

Forced-convection boiling data from references 3, 4, 5, 10, and ll along with the data obtained from the experimental program described herein were used to develop an effective correlation. The wide range of variables in the reference data (table II) increased its generality. The data were correlated by means of three significant parameters obtained by dimensional analysis from basic considerations. A nondimensional parameter presented in reference 8 as a limited relation of boiling data was used as the starting point of the present correlation. Two additional parameters were then determined to compensate for a subcooling effect (independent of pressure) and a pressure effect that were revealed by an evaluation of all the data.

The initial correlation of the experimental data is presented in figure 3, which shows a ratio of Nusselt numbers plotted against a dimensionless parameter. The ratio of Nusselt numbers is used consistently in all succeeding plots, and the development of the correlation is indicated by the changes in the parameters on the abscissa. The numerator of the ratio of Nusselt numbers is an experimentally determined Nusselt number based on local values of heat-transfer coefficients, and the denominator is a calculated Nusselt number based on equation (4) or any nonboiling forced-convection correlating technique specified in the references. The Nusselt number ratio remains at a value of unity for all nonboiling data, and it is greater than unity when boiling persists because of the increased heat-transfer coefficient in the experimental Nusselt number.

The parameter  $q/\lambda \rho_v V_b$  depicts a correlation of boiling heat-transfer data obtained at a unique pressure level (ref. 8), and it was developed from a dimensional analysis of the basic heat-transfer mechanism. The existence of two distinct modes of heat transfer was assumed from the laminar transition layer along the wall to the bulk of the boiling fluid. The first mode was responsible for

the amount of heat transfer by turbulent mixing as a result of the velocity gradient. The second mode was a measure of the heat transfer due to molecular mass transfer caused by bubbles departing from the heated surface. A detailed description of the analysis may be found in reference 8.

The parameter  $q/\lambda\rho_V V_D$  was calculated by using the experimental data obtained in this investigation, and figure 3 depicts its limitations in affecting a correlation. Boiling data at a unique pressure level are on a line having a slope of 0.7 and increased pressures shift this line to the left. Both of these observations are resported in reference 9 along with a complete correlation based on two additional parameters to correct for changes in pressure level. The equation presented (ref. 9) does not correlate the present experimental data or the reference data used in this investigation. The unavailability of the data used to obtain this correlation makes explanations for this discrepancy difficult.

An examination of the available data revealed the existence of a subcooling effect, independent of pressure level, that must be compensated in any effective correlating procedure. Figure 4 is a plot of the correlating parameter applied in figure 3 with data from references 3 to 5 obtained at a pressure level of 2000 pounds per square inch absolute. The amount of subcooling is marked at each datum point, and dashed lines with a slope of 0.7 are drawn through nearly constant values of subcooling. The spread of these lines clearly indicates an effect of as much as two orders of magnitude for these data.

In order to compensate for the subcooling effect, a parameter obtained by a strictly empirical approach was determined from the experimental data. The reciprocal of the amount of subcooling raised to the 1.20 power  $[1/(T_s-T_b)]^{1.20}$  proved to be an effective correlation. In order to maintain nondimensionality, the parameter was modified to include the heat of vaporization and the specific heat of the fluid  $[\lambda/c_p(T_s-T_b)]^{1.20}$ . This particular grouping had been obtained from a parametric evaluation of the heat balance in and out of a control volume containing a boiling fluid (ref. 7). The spread in the data of figure 4 was effectively eliminated when the data were replotted in figure 5 by including the parameter  $[\lambda/c_p(T_s-T_b)]^{1.20}$  as an integral part of the correlating equation (fig. 5). The heat of vaporization was evaluated at saturation conditions and the specific heat at the mean temperature between saturation and local bulk.

The spread of data due to pressure (fig. 3) could effectively be eliminated by the inclusion of a parameter consisting of the ratio of vapor density to liquid density previously used in reference 9. An exponent equal to 1.08 was emperically derived when the density ratio was evaluated at saturation conditions  $(\rho_{\rm V}/\rho_{\rm I})^{1.08}$ .

The completed correlation presented in figure 6 includes the data obtained in the present investigation and the boiling heat-transfer data from five reference sources covering a broad range of conditions. Table II lists the range of pertinent variables. The data included a range of pressure from 16 to 2000 pounds per square inch, heat flux from 0.026 to 56.0 Btu per square inch per second, fluid velocity from 1.33 to 204 feet per second, and subcooling from 60 to 3360 F. The spread of the data about the solid line in figure 6 shows the

effectiveness of the correlation. Approximately 92 percent of 260 data points are within  $\pm 12$  percent, as indicated by the dashed lines. Fifteen points from three runs in reference 4 are consistently plotted below the line in the lower portion of the curve and are not included in the evaluation of the data scatter. These points are a small fraction of the data used from that particular reference and appear to be inconsistent. The scatter in the upper portion of the curve is a result of the low subcooling involved since small errors in bulk temperature measurements can result in large deviations. The nonboiling region of the correlation exists for values of  $(q/\lambda \rho_v V_b)[\lambda/c_p(T_s - T_b)]^{1.2}(\rho_v/\rho_l)^{1.08}$  less than 0.00162, which is the incipient boiling point. When boiling persists, the data are correlated by the following equation:

$$\frac{\text{Nu}_{\text{exp}}}{\text{Nu}_{\text{calc}}} = 90.0 \left\{ \left( \frac{\text{q}}{\lambda \rho_{\text{v}} V_{\text{b}}} \right) \left[ \frac{\lambda}{c_{\text{p}} (T_{\text{s}} - T_{\text{b}})} \right]^{1.20} \left( \frac{\rho_{\text{v}}}{\rho_{\text{l}}} \right)^{1.08} \right\}^{0.7}$$
(5)

In order to demonstrate the applicability of the correlation for fluids other than water, liquid-ammonia boiling heat-transfer data from reference 9 were applied to equation (5). The data covered a range of variables that includes pressure from 170 to 1174 pounds per square inch absolute, heat flux from 0.38 to 9 Btu per square inch per second, velocity from 3 to 85 feet per second, and subcooling from 37° to 187° F (fig. 7). The percent deviation is within the range of the water data presented in figure 6 except for the four points obtained at a pressure level of 170 pounds per square inch absolute.

The correlating equation (5) can only be applied to subcooled boiling. The parameter containing the degree of subcooling of the fluid becomes infinite when the bulk temperature approaches saturation conditions. Further studies are required to determine parameters suitable for correlating saturated boiling data.

# Incipience of Boiling

A great deal of interest has been expressed in a method for predicting the conditions required for the incipience of boiling in a subcooled fluid. An analytical treatment of this problem, presented in reference 13, results in an equation that involves the cavity site and the thermodynamic state of the thermal layer. This equation cannot be solved directly because of the difficulty of obtaining the values of two constants. One of the constants is a function of the dimensions of the bubble site cavity. The other constant is the laminar sublayer thickness, which varies with stream velocity. If incipient boiling data are available, it is possible to calculate the value of the ratio of the two constants by using the equation of reference 13. With this ratio evaluated at a unique velocity, it is possible to predict the variation of wall temperature with pressure for that specific velocity. A check on the validity of this equation was made by using the experimental data obtained in this investigation. The incipient boiling data were obtained from figure 6 at the point where the Nusselt number ratio equals unity and the correlating parameter equals 0.00162. culation procedure is presented in appendix B. The results show a small difference between the experimental and calculated wall temperatures at the inception of boiling.

#### SUMMARY OF RESULTS

Single- and two-phase heat-transfer data were obtained by using distilled water flowing through an Inconel X resistance-heated tube. The nonboiling data were correlated by a modified Colburn-type equation within a 20-percent scatter. The subcooled boiling data correlated within ±12 percent by an equation, which included a unique parameter to compensate for changes in subcooling independent of pressure.

The generality of the correlation was increased by using boiling heat-transfer data obtained from reference sources. The range of variables effectively correlated included pressure from 16 to 2000 pounds per square inch absolute, heat flux from 0.026 to 56.0 Btu per square inch per second, fluid velocity from 1.33 to 204 feet per second, and subcooling from 60 to 3360 F. Liquid-ammonia data obtained from the literature correlated readily within the scatter of the water data. Further studies should be made before an attempt is made to employ the boiling correlation to fluids other than those investigated.

Comparisons were made between wall temperatures at the incipience of boiling as predicted by an analytically derived equation and by the experimental data. The results show a small difference between analytical and experimental wall temperatures. The equation used has limited applicability because experimental data must be available to calculate constants that cannot be directly measured. These constants can be evaluated at a specific velocity and then used to predict the variation of wall temperature with pressure for that velocity.

Lewis Research Center
National Aeronautics and Space Administration
Cleveland, Ohio, December 4, 1962

# APPENDIX A

#### SYMBOLS

```
Α
           area
           2\sigma T_{\rm s}/\lambda \rho_{\rm v} (eq. (B1)), units are (ft)( ^{\rm o}R ) when \,\delta\, in eq. (B1) is in ft
а
           1 + \cos \phi
C_3
           specific heat at constant pressure
cp
đ
           inside diameter of tube
E
           voltage
           heat-transfer coefficient
h
I
           current
K
           constant in eq. (2)
           thermal conductivity
k
           total length of test section
L
m
           mass-flow rate
Nucalc
           Nusselt number computed from modified Colburn-type equation by using
             film temperature to evaluate fluid properties
Nuexp
           experimental Nusselt number obtained from measured heat-transfer coef-
             ficient, hd/k
           Prandtl number, (c_p\mu/k)_f
Pr
           pressure
р
           heat flow
Q
           heat flux
q
           Reynolds number, \rho_f V_h d/\mu_f
Re
           radius of tube
r
T
           temperature
           (T_{\text{w.i}} + T_{\text{b}})/2
\mathbb{T}_{\mathbf{f}'}
```

V velocity

distance to temperature station measured from beginning of heated por-

tion of test section

contact angle β

angle of tangent to cavity mouth with respect to horizontal Υ

laminar sublayer thickness δ

 $T_w - T_b$  $\theta_{WO}$ 

 $T_s - T_b$  $\theta_{\rm S}$ 

heat of vaporization λ

viscosity μ

density ρ

surface tension

angle of bubble wall with respect to horizontal,  $\gamma$  +  $\beta$ 

# Subscripts:

bulk fluid b

f film

inner surface of test section i

inlet in

liquid 7

outer surface of test section

saturation S

vapor

wall at incipience of boiling

#### APPENDIX B

#### INCIPIENT BOILING POINT

Experimental data obtained in this investigation were used to check the validity of an analytically derived method of predicting the surface temperature at the inception of boiling (ref. 13). The equation is

$$\theta_{\text{WO}} = \theta_{\text{S}} + \frac{2aC_3}{\delta} + \sqrt{\left(2\theta_{\text{S}} + \frac{2aC_3}{\delta}\right)\left(\frac{2aC_3}{\delta}\right)}$$
 (B1)

The incipience of boiling can be obtained from equation (B1) if  $C_3$  and  $\delta$  are known. The quantity  $C_3$  is a function of the shape of the bubble-site cavity. The quantity  $\delta$ , which is the thickness of the laminar sublayer, is a function of stream velocity. Unfortunately, these values are not readily available.

If the incipient boiling point is experimentally known, it is possible to calculate the ratio  $\delta/C_3$  by equation (Bl). This unique boiling point is readily obtained from the correlation presented in figure 6 at the point where the Nusselt number ratio initially departs from a value of unity. At this point, the value of the correlating parameter on the abscissa is 0.00162.

Four incipient boiling points were chosen; data were obtained at the same velocity but different pressures. The ratio  $\delta/C_3$  was calculated from one of these points and should remain constant as long as the velocity is constant (ref. 13). This ratio was then used to calculate the wall temperatures for the other three chosen points. The calculated and experimental wall temperatures at the inception of boiling were then compared. The computations showing the agreement between computed and experimental wall temperatures are shown in table III.

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TABLE I. - SINGLE- AND TWO-PHASE HEAT-TRANSFER DATA AT STATION 11

Run		Tempe	erature		Pressure,	Heat flux,	Mass-flow	Bulk velocity,	Run		Тель	erature		Pressure.	Heat flux.	Mass-flow	Bulk velocity,
	Outside, To, OF	Inside, T <sub>1</sub> , or	Bulk, Tb, OF	Saturation,	lb/sq in. abs	q, Btu (sec)(sq in.)	rate, m, lb/sec	V <sub>b</sub> , ft/sec		Outside,	Inside,	Bulk,	Saturation, Ts, OF	p, lb/sq in. abs	g, Btu (sec)(sq in.)	rate, m, lb/sec	V <sub>b</sub> , ft/sec
1172 1174 1175 1176 1178	196 255 290 312 369	185 238 265 280 328	81 88 85 94 108	271 272 273 273 264	41.7 42.9 43.8 43.4 37.0	0.398 .632 .914 1.21 1.60	0.221 .219 .234 .237 .217	6.71 6.66 7.12 7.22 6.63	1271 1273 1274 1275 1276	372 387 420 167 208	349 357 382 155 190	113 117 126 89 93	327 328 329 316 343	100.3 99.5 101.2 85.0 119.8	0.905 1.230 1.550 .415 .633	0.141 .143 .143 .383 .388	4.32 4.38 4.39 11.67 11.82
1179 1180 1181 1182 1183	208 278 286 338 376	196 261 262 307 335	85 89 95 105 110	274 277 278 280 280	44.7 46.8 47.6 49.3 49.8	.411 .622 .912 1.22 1.59	.186 .188 .184 .180	5.66 5.74 5.61 5.49 5.75	1277 1278 1279 1284 1286	255 304 349 192 236	231 272 309 180 218	98 100 101 86 89	336 341 345 352 353	123.7 122.4 126.2 139.9 141.6	.892 1.220 1.560 .416	.393 .399 .401 .266 .266	11.98 12.17 12.23 8.09 8.10
1184 1190 1191 1192 1193	381 233 291 298 356	340 222 275 274 324	112 82 83 91 101	282 270 273 275 276	51.0 41.3 43.8 45.1 46.4	1.60 .409 .630 .913 1.24	.182 .144 .164 .164 .162	5.56 4.38 4.99 5.00 4.94	1287 1288 1289 1290 1291	294 360 412 222 285	270 329 373 210 268	92 100 106 93 114	354 344 358 365 355	143.7 145.0 148.0 162.0 163.7	.893 1.210 1.570 .417 .628	.269 .270 .274 .179 .181	8.20 8.24 8.37 5.45 5.54
1195 1196 1197 1198 1199	380 246 291 322 361	340 235 274 298 330	105 80 84 92 101	278 283 282 285 288	48.1 51.5 51.1 53.2 55.7	1.58 .423 .641 .930 1.24	.164 .130 .141 .139 .141	5.00 3.97 4.29 4.23 4.30	1292 1293 1294 1295 1296	349 413 439 241 318	326 383 402 230 302	97 104 111 94 100	366 357 367 366 367	165.0 165.0 165.8 174.3 176.9	.895 1.200 1.540 .405 .625	.186 .190 .190 .143 .146	5.67 5.80 5.81 4.36 4.46
1200 1202 1203 1204 1205	388 165 211 257 311	348 154 194 232 279	111 86 91 94 94	288 312 313 316 319	56.1 80.8 81.2 85.9 88.4	1.59 .400 .630 .899 1.23	.139 .339 .354 .359 .364	4.25 10.31 10.78 10.94 11.09	1297 1298 1307 1309 1310	394 424 442 157 197	372 394 404 147 173	103 110 122 84 89	372 373 358 344 345	177.7 178.6 149.6 124.3 126.6	.900 1.210 1.54 .371 .590	.146 .146 .138 .389	4.45 4.46 4.23 11.83 11.84
1206 1228 1229 1230 1231	361 187 181 238 288	321 175 170 220 264	102 84 83 88 83	310 294 343 344 345	77.8 60.6 119.0 120.3 126.1	1.57 .401 .399 .646 .907	.336 .273 .269 .268 .274	10.25 8.30 8.18 8.15 8.33	1311 1312 1313 1314 1315	239 288 345 294 347	216 257 305 271 317	85 88 93 89 93	348 348 349 354 353	128.9 128.9 132.9 139.8 136.4	.860 1.17 1.54 .856 1.17	.394 .399 .409 .256	11.99 12.14 12.46 7.79 8.16
1232 1233 1235 1236 1258	366 386 210 281 363	335 346 198 265 339	89 94 81 88 96	342 327 330 324 330	117.2 99.0 102.5 96.2 104.5	1.230 1.570 .402 .619	.253 .253 .189 .176 .190	7.70 7.71 5.75 5.35 5.79	1316 1322 1323 1324 1325	410 348 404 437 315	372 326 375 400 299	100 103 111 121 106	354 360 361 361 364	138.6 152.4 153.6 154.1 161.0	1.56 .882 1.18 1.55 .591	.271 .190 .186 .188 .132	8.27 5.80 5.68 5.76 4.03
1260 1261 1262 1263 1264	388 413 229 231 313	358 375 217 219 296	104 109 85 87 93	336 336 339 341 336	110.5 112.6 116.4 119.0 112.6	1.200 1.560 .419 .412 .635	.192 .182 .166 .162 .154	5.86 5.56 5.05 4.93 4.69	1326 1327 1328 1329 1330	395 420 443 262 310	374 391 406 238 279	113 118 127 98 100	365 365 367 320 320	162.7 161.6 163.9 91.1 91.1	.867 1.19 1.55 .864 1.19	.138 .138 .138 .346 .347	4.22 4.22 4.24 10.55 10.59
1266 1267 1268 1269 1270	363 378 403 248 329	340 347 364 237 312	96 102 108 96 103	327 325 326 325 327	98.2 94.4 97.3 97.8 98.6	.894 1.220 1.550 .415 .628	.162 .164 .167 .138	4.94 5.00 5.10 4.20 4.21	1331 1332 1333 1335 1340	366 290 353 397 271	327 266 323 358 254	102 91 103 108 77	324 336 336 337 323	94.5 112.2 113.4 114.0 93.5	1.54 .878 1.21 1.54 .601	.351 .265 .267 .266 .183	10.71 8.07 8.15 8.13 5.56

TABLE I. - Concluded. SINGLE- AND TWO-PHASE HEAT-TRANSFER DATA AT STATION 11

Run		Temperature Pressure, Heat flux, Mass-flow Bulk velocity, Run Temperature				Pressure, Heat flux,		Mass-flow rate,	Bulk velocity,								
٠	Outside, To, OF	Inside,	Bulk, T <sub>b</sub> , <sup>O</sup> F	Saturation, T <sub>S</sub> , F	lb/sq in. abs	g, Btu (sec)(sq in.)	m, lb/sec	V <sub>b</sub> , ft/sec		Outside, To, or	Inside, T <sub>1</sub> , or	Bulk, Tb, °F	Saturation, T <sub>S</sub> , OF	lb/sq in. abs	Btu (sec)(sq in.)	m, lb/sec	ft/sec
1341	347	325	84	324	96.1	0.871	0.191	5.81	1409	442	404	121	358	148.7	1.560	0.141	4.32
1342	378	348	89	325	96.5	1.181	.191	5.81	1412	307	284	86	265	37.7	.886	.228	6.94
1343	407	368	93	327	97.3	1.557	.195	5.94	1413	345	315	90	271	42.4	1.160	.233	7.10
1345	316	300	79	331	104.9	.601	.150	4.56	1414	376	336	93	272	43.2	1.550	.235	7.16
1346	369	347	92	331	104.9	.868	.141	4.29	1415	343	321	89	275	45.1	.863	.174	5.30
1347 1348 1349 1350 1352	398 424 241 306 331	368 386 224 283 300	97 104 72 81 87	333 333 269 269 269	107.5 107.7 40.8 40.4 40.8	1.177 1.556 .603 .875 1.210	.144 .142 .232 .228 .233	4.39 4.33 7.04 6.94 7.09	1416 1417 1418 1420 1421	369 387 350 374 396	337 349 329 345 357	94 98 93 101 112	275 276 289 288 288	45.9 46.6 56.4 55.1 55.1	1.250 1.550 .815 1.160 1.550	.174 .174 .127 .120	5.30 5.31 3.87 3.66 3.79
1353	370	331	89	271	41.6	1.574	.233	7.09	1422	354	315	83	320	89.1	1.550	.363	11.04
1354	276	260	82	283	51.0	.603	.174	5.29	1423	399	370	93	333	116.3	1.170	.187	5.70
1355	312	289	81	289	54.2	.873	.183	5.57	1424	423	385	98	333	116.3	1.550	.187	5.71
1356	348	318	103	272	42.5	1.182	.186	5.68	1425	413	384	97	336	123.9	1.180	.160	4.88
1358	377	338	109	275	45.0	1.542	.190	5.81	1426	437	399	109	339	124.3	1.56	.133	4.06
1359	312	296	98	277	45.9	.603	.144	4.39	1427	405	367	87	346	145.2	1.55	.266	8.09
1360	340	317	104	278	46.3	.873	.144	4.40	1428	421	383	106	358	147.8	1.16	.186	5.68
1361	364	333	112	275	45.0	1.215	.138	4.22	1429	382	353	114	357	147.3	1.56	.194	5.94
1362	387	348	120	275	45.1	1.562	.138	4.22	1430	404	376	115	359	151.5	1.17	.132	4.04
1366	288	265	91	282	49.3	.873	.253	7.71	1431	438	400	130	361	154.5	1.57	.132	4.05
1367 1368 1369 1370 1371	329 370 326 346 386	299 331 304 315 347	98 104 98 102 108	283 284 298 298 298	50.4 52.1 64.1 64.1 64.1	1.190 1.570 .864 1.180 1.560	.244 .256 .182 .186	7.44 7.81 5.55 5.68 5.68	1433 1435 1436 1438 1439	338 362 347 379 358	308 323 316 340 329	102 108 109 119 115	277 280 293 290 295	46.6 48.7 59.4 56.4 62.8	1.17 1.54 1.17 1.56 1.17	.246 .249 .175 .175 .132	7.51 7.61 5.35 5.36 4.04
1372 1374 1375 1376 1377	300 335 370 399 281	284 312 341 361 258	94 99 110 120 107	306 303 300 304 297	72.2 70.6 68.7 71.6 60.7	.596 .854 1.190 1.540 .854	.144 .149 .144 .151	4.39 4.54 4.40 4.63 8.58	1440 1441 1442 1443 1602	393 430 415 447 170	363 392 386 409 158	110 115 114 126 87	369 369 374 373 316	172.8 172.4 181.7 180.4 85.0	1.20 1.55 1.18 1.55 .392	.186 .186 .135 .132 .347	5.68 5.69 4.13 4.05 10.55
1378	345	314	113	297	60.7	1.180	.278	8.50	1603	228	208	90	317	86.8	.723	.351	10.68
1379	377	338	118	298	61.3	1.550	.283	8.66	1604	311	279	95	317	87.6	1.223	.354	10.78
1380	276	260	108	304	71.6	.605	.185	5.65	1605	366	327	99	319	88.4	1.567	.355	10.83
1381	344	322	113	305	72.7	.862	.185	5.66	1606	195	183	88	336	110.9	.399	.243	7.39
1382	364	335	118	305	76.7	1.160	.189	5.79	1607	245	228	90	336	110.8	.607	.242	7.37
1383	398	359	123	304	72.2	1.550	.185	5.67	1608	309	285	95	336	111.5	.910	.246	7.49
1384	310	295	111	312	81.3	.594	.143	4.37	1609	377	346	101	337	113.0	1.231	.246	7.51
1385	350	328	112	314	82.5	.855	.151	4.62	1610	408	369	106	337	111.9	1.580	.246	7.51
1394	396	367	96	342	121.1	1.160	.152	4.63	1611	212	201	89	342	121.3	.391	.200	6.08
1395	429	391	109	344	123.6	1.570	.144	4.40	1612	275	258	94	342	121.3	.619	.200	6.09
1396	286	256	82	360	152.5	1.200	.351	10.68	1613	350	327	99	343	122.3	.904	.200	6.10
1397	338	297	89	353	140.2	1.560	.360	10.95	1614	403	373	106	343	122.5	1.229	.200	6.10
1398	347	315	88	348	129.2	1.220	.259	7.68	1615	428	389	113	344	123.3	1.577	.200	6.09
1399	394	355	95	343	122.8	1.570	.256	7.80	1616	262	238	105	354	143.3	.881	.356	10.86
1400	340	317	100	368	168.7	.882	.190	5.80	1617	315	283	106	354	143.9	1.230	.361	11.01
1401 1402 1404 1406 1407	408 437 320 394 420	379 399 304 373 390	107 108 98 105 113	370 371 363 358 358	172.1 175.8 156.8 148.3 148.3	1.180 1.570 .602 .863 1.210	.194 .196 .129 .138	5.92 5.99 3.93 4.21 4.40	1618 1619 1620 1621 1622	360 259 313 374 424	319 242 289 344 386	109 103 106 111 117	354 353 349 349 348	144.5 142.7 131.9 132.5 133.1	1.582 .624 .909 1.200 1.575	.362 .232 .243 .241 .245	11.06 7.09 7.41 7.36 7.50

TABLE II. - EXPERIMENTAL DATA FROM VARIOUS SOURCES

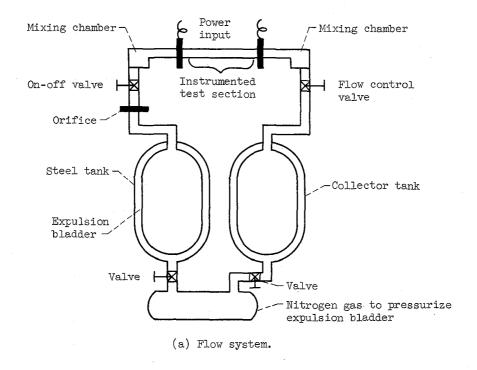
Fluid	Pressure, p, lb/sq in. abs	Heat flux, q, Btu/(sq in.)(sec)	Velocity, V, ft/sec	Subcooling, OF	Number of boiling points	Reference
Water	37 to 179 69 to 307 16 to 202 2000 2000 500 1500 2000	0.37 to 1.60 3.5 to 56.0 0.73 to 2.80 0.27 to 1.41 1.9 to 4.9 0.026 to 0.85 0.052 to 0.57 0.145 to 0.62	3.8 to 12.5 73 to 204 6.2 to 12.6 2.4 to 9.5 20.0 1.33 1.40 1.40	180 to 263 197 to 335 100 to 258 12 to 148 116 to 256 6 to 179 37 to 336 106 to 282	103 18 40 28 16 30 20	Present study 14 11 3 5 4 4 4
Liquid ammonia	170 to 1174	0.38 to 9.00	3.0 to 85.0	37 to 187	31	10

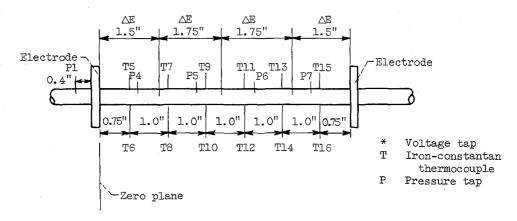
TABLE III. - COMPARISON OF COMPUTED AND EXPERIMENTAL

# INCIPIENT BOILING POINTS

Run	Pressure, p, lb/sq in. abs	Velocity, V, ft/sec	Experimental wall temperature,  Tw,exp,  OF	Wall temperature calculated by eq. (B1)a  Tw.calc, oF
1359	46	4.39	296	292
1271	100	4.32	349	343
1406	148	4.21	373	371

 $<sup>^{2}</sup>Laminar$  thickness ratio  $~\delta/C_{3}~$  of 1482 µin. at velocity of 4.25 ft/sec (obtained from run 1346).





(b) Instrumentation.

Figure 1. - Schematic drawing of test apparatus.

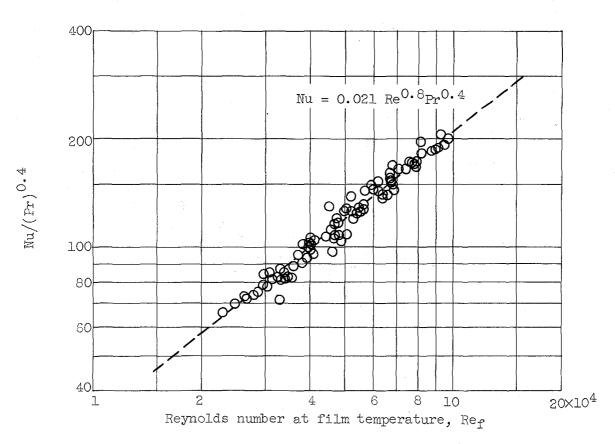


Figure 2. - Correlation of nonboiling heat-transfer data.

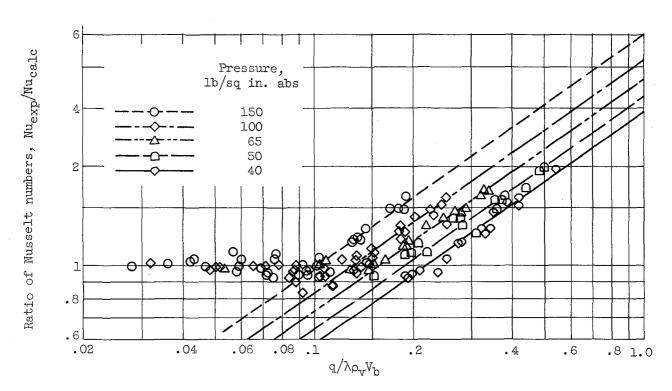


Figure 3. - Partial correlation of boiling heat-transfer data showing pressure effect. Dashed lines drawn at a slope of 0.7.

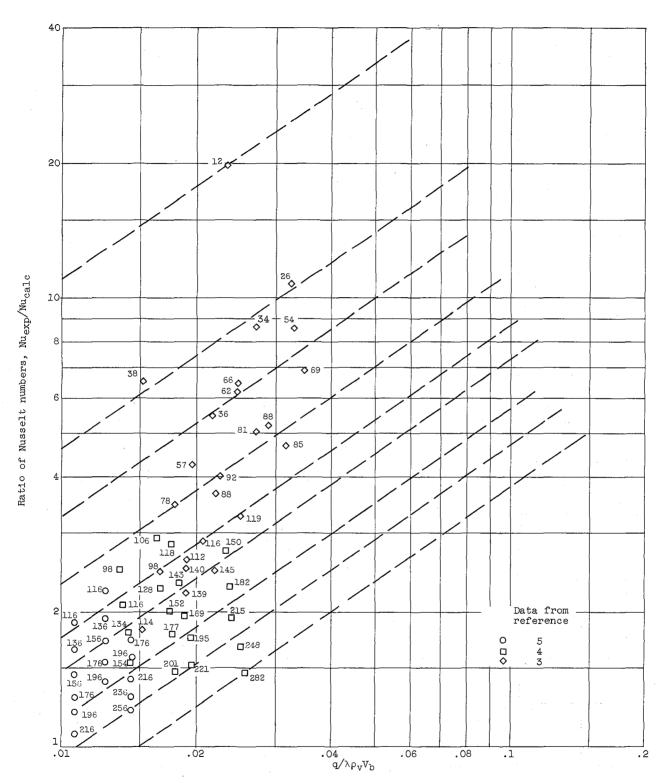


Figure 4. - Effect of subcooling at constant pressure of 2000 pounds per square inch absolute. Degrees of subcooling indicated next to data points. Dashed lines drawn at a slope of 0.7.

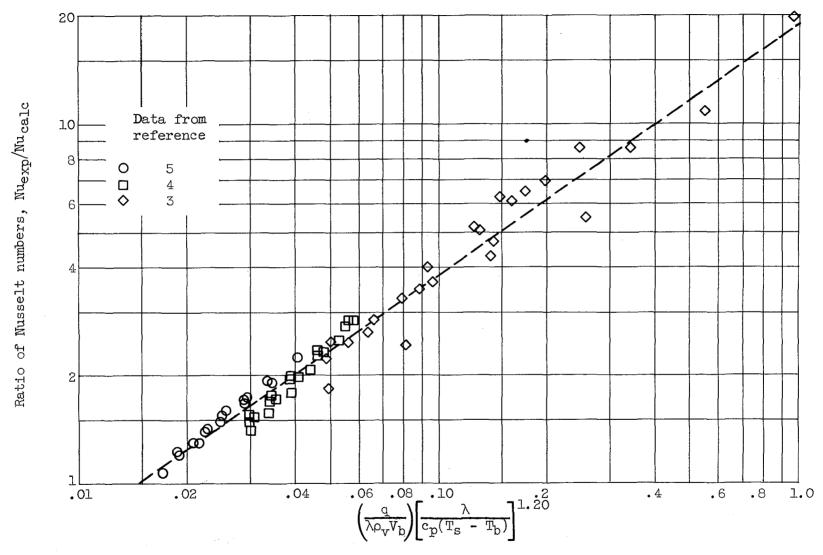


Figure 5. - Effect of subcooling compensated by a correcting parameter. (Replot of data presented in fig. 4.) Constant pressure, 2000 pounds per square inch. Dashed line drawn at a slope of 0.7.

Figure 6. - Completed correlation using density-ratio parameter to compensate for remaining pressure effect. Includes all boiling-water data from present investigation and references 3, 4, 5, 11, and 14.

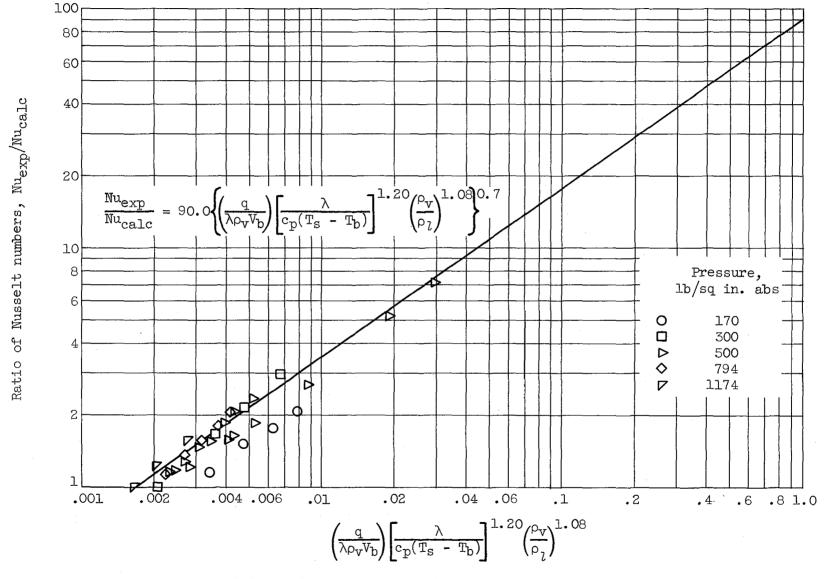


Figure 7. - Correlation of liquid-ammonia data from reference 10. Range of pressure, 170 to 1174 pounds per square inch absolute.