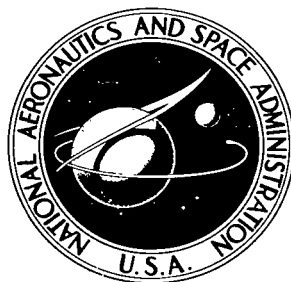


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THE GEOMETRIC PROPERTIES OF AN EXPANDABLE WHIRLING-MEMBRANE SOLAR-ENERGY CONCENTRATOR

by John M. Jerke and Atwood R. Heath, Jr.

Langley Research Center

Langley Station, Hampton, Va.





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SUMMARY

The whirling-membrane concept of solar-concentrator fabrication has been proposed for use with spacecraft-power-conversion devices because of its compact-packaging potential. Three membranes of 0.01-millimeter-thick aluminized plastic were constructed and attached to metal hubs for which the ratios of the hub radius to the membrane radius were 0.20, 0.35, and 0.50. The resulting models that had design focal lengths of 132.1 centimeters and design diameters of 3.05 meters were rotated at 71 radians per second in a vacuum chamber at pressures below 133 newtons per meter². The accuracy with which each membrane achieved the design paraboloidal shape was measured by an optical-ray-trace technique.

The membrane with the metal hub of largest diameter gave the best concentration of energy. For this model, the focal length was 130.5 centimeters or 1 percent less than the design value. A geometric efficiency of 1.00 was obtained at a concentration ratio of 23. Membrane surface mean errors varied from -0.6° to 0.4° in the radial direction and were essentially zero in the circumferential direction. The random error had a standard deviation of 0.5° in the radial direction over most of the membrane and 0.25° in the circumferential direction. Location of supporting cables relative to the metal hub was found to be an important factor in the design of a whirling-membrane concentrator.

INTRODUCTION

Solar-energy concentrators used in conjunction with electrical-conversion systems have been proposed as auxiliary-power units for spacecraft. The choice of basic materials and type of construction used in fabricating the concentrator are dependent upon the method of conversion of solar energy to electrical power, the required power output, and the payload-packaging constraints. As a result various types of concentrators, such as one-piece nickel and inflatable plastic mirrors, have been fabricated, and quantitative data are available on their performance. (See ref. 1.)

One concept that has been proposed for large-diameter concentrators with potentially superior packaging properties is the whirling-membrane concentrator. (See ref. 2.) In this concept, a thin aluminized plastic membrane, which has been preformed to an approximately paraboloidal shape and attached to a metal hub, is rotated about its optical axis (axis of symmetry) to maintain the desired paraboloidal shape. The centrifugal loading plus an axial component of loading applied at the rim by a conical membrane stretch the approximate paraboloid into the desired paraboloid. An analytical study of the problems pertaining to the spinning membrane has been made in reference 2, and methods are given for obtaining static stresses and deflections that can be used in the design of a membrane.

As no experimental data existed on this concept, the main objective of the present investigation was to measure the accuracy with which a whirling-membrane concentrator assumes the design shape while being rotated. Another important objective was to provide a means for preventing the formation of circumferential wrinkles near the periphery of the membrane. This wrinkling problem (discussed in ref. 2) occurs when the meridional stresses in the membrane near the rim are much smaller than the circumferential stresses. One suggested solution is to increase the diameter of the metal hub relative to the concentrator diameter, so that the ratio of meridional stress to circumferential stress near the rim becomes larger. Consequently, three 3.05-meter-diameter whirling-membrane models with metal hubs of different diameters were investigated. An optical-ray-trace device utilizing a light source and solar cells was used to determine the geometric accuracies of the concentrator models.

An appendix by Atwood R. Heath, Jr., and Victor R. Bond discusses the effective reflectance of aluminized plastic membranes under biaxial tensile loading.

SYMBOLS

The units used for the physical quantities defined in this paper are given in the International System of Units (SI). Factors relating this system to U.S. Customary Units are given in reference 3.

- C concentration ratio, ratio of projected area of membrane paraboloid to a circular area in the focal plane centered on the optical axis
- i,j,k orthogonal coordinate system with origin at O' , defining membrane-surface-slope errors where k is the normal to the design paraboloid surface, and j is in a plane containing the optical axis and a membrane radius through O' (see figs. 7 and 13)

r, θ	plane polar coordinates with origin at O' in solar-cell survey plane (see fig. 7)
R	design radius of membrane paraboloid
x, y, z	rectangular Cartesian coordinates with origin at O defining membrane paraboloid (see fig. 7)
r_h	metal-hub radius of concentrator
x_L	light-source position, distance along x-axis from optical axis to center of light source (see fig. 7)
z_c	cable-hub position, distance along optical axis from design paraboloid vertex to intersection of the extension of the cables with the optical axis (see fig. 1)
z_d	z-ordinate of the design membrane
z_e	z-ordinate of the membrane as determined from experiments
z_s	solar-cell-bar position, distance along optical axis from design paraboloid vertex to survey plane containing solar cells (see fig. 7)
$\Delta z = z_e - z_d$	
δ_c	circumferential-slope error, projection of angle between the actual membrane surface normal and the design paraboloid normal in the ik plane (see fig. 13)
δ_r	radial-slope error, projection of angle between the actual membrane surface normal and the design paraboloid normal in the jk plane (see fig. 13)
η_g	geometric efficiency, ratio of energy entering a given-size focal-plane aperture to the total energy that is specularly reflected from the concentrator
σ_c	standard deviation of circumferential-slope errors from the mean errors
σ_r	standard deviation of radial-slope errors from the mean errors

MODELS AND APPARATUS

Models

Configurations.- A sketch of the whirling-membrane solar concentrator is shown in figure 1. The concentrator consisted of an aluminized plastic paraboloid, metal hub, shaft, cables, and cable hub. The design paraboloid diameter was 3.05 meters, the design rim angle was 60° , and the design focal length was 132.1 centimeters. The membrane was constructed of 0.01-millimeter-thick aluminized polyethylene terephthalate plastic and was formed of 45 triangular gores assembled on a convex mold. The gores were attached to each other at a butt joint which was covered with an aluminized plastic strip sealed with thermosetting resin. In figure 2 the ordinates of the paraboloid as constructed on the mold are labeled "initial."

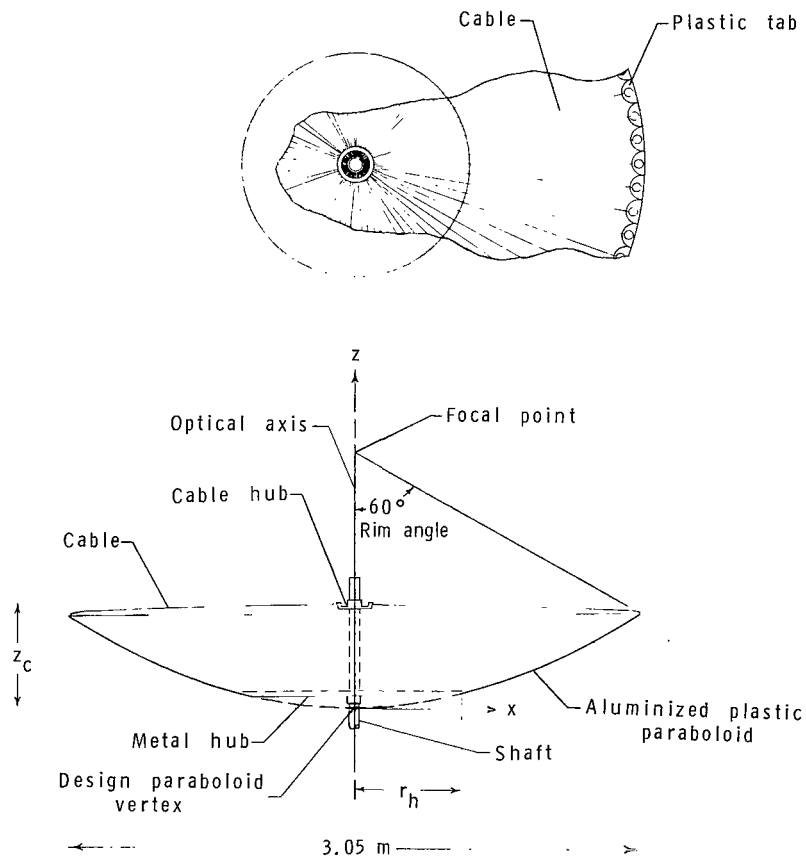


Figure 1.- Sketch of whirling-membrane solar concentrator with design dimensions.

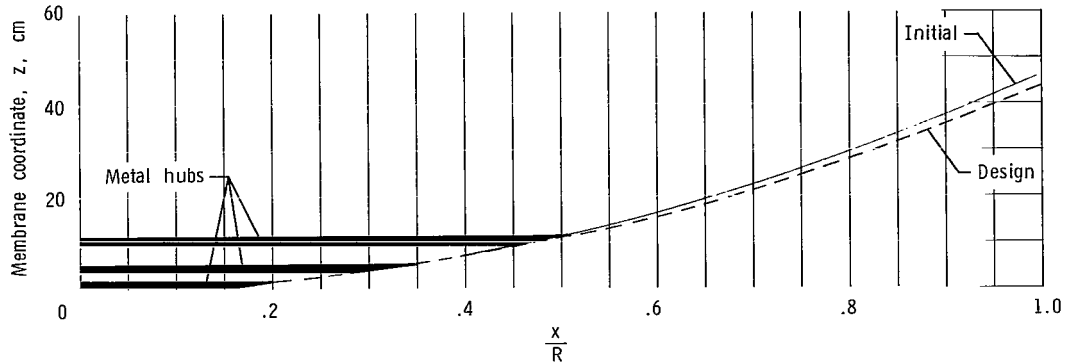


Figure 2.- Radial cross section of membrane showing initial and design configurations.

Three models with ratios of metal-hub radius to concentrator radius of 0.20, 0.35, and 0.50 were built, and a membrane was fabricated for each. The convex mold also served as a jig for attaching each membrane to its respective hub in the assembly process. Each model had seventy-two 0.8-millimeter-diameter steel cables which were attached from the cable hub mounted on the shaft to the plastic tabs at the membrane rim. The vertical location of the cable hub on the shaft was adjusted manually. All model configurations with pertinent dimensions are given in table I. The three models with metal hub radii of 0.20R, 0.35R, and 0.50R are designated "configurations I, II, and III," respectively. For each of these three models, the cable hub was located 40.8 centimeters above the design paraboloid vertex. Configuration III was modified by moving the cable hub to four additional locations, 43.3, 45.8, 48.3, and 50.8 centimeters above the vertex. These four configurations are III-A, III-B, III-C, and III-D, respectively.

TABLE I. - MODELS AND TEST PARAMETERS

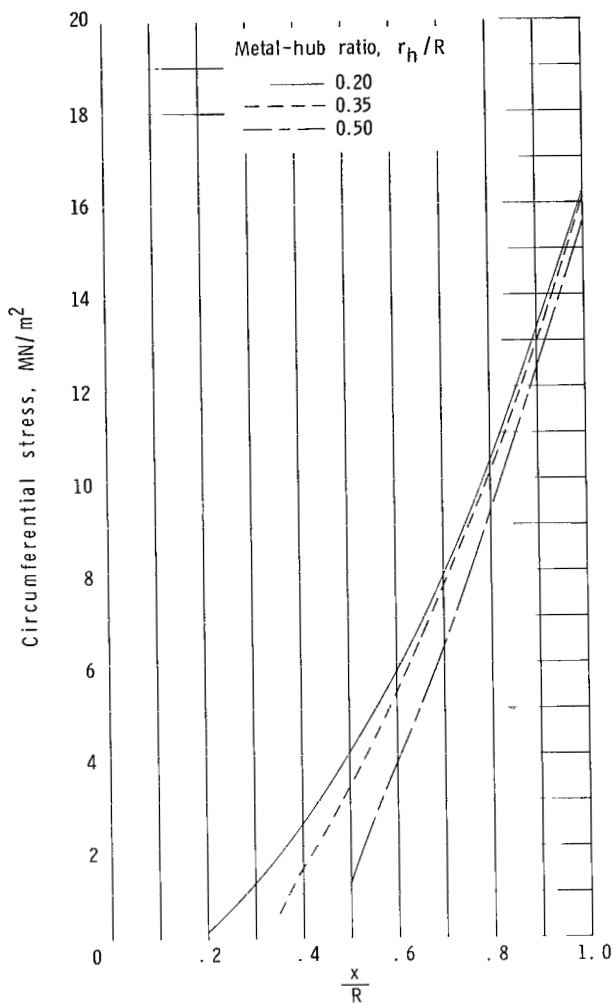
Configuration	Models		Test parameters										
	Metal-hub radius, r_h/R	Cable-hub location, z_c , cm	Light-source location, x_L , cm						Solar-cell bar positions				Angular position, θ , deg*
									Axial position, z_s , cm				
I	0.20	40.8	52.1	86.6	109.7	128.6	141.7	----	129.5	132.1	134.6	} 0° to 315°	
II	.35	40.8	68.3	93.9	113.7	130.5	141.9	----	129.5	132.1	134.6		
III	} .50	40.8	} 86.3	} 104.9	} 120.4	} 134.1	} 144.3	----	129.5	132.1	134.6		
III-A		43.3						----	----	132.1	----		
III-B		45.8						----	----	132.1	----		
III-C		48.3						----	----	132.1	----		
III-D	50.8	127.0	129.5	132.1	----								

*In 45° increments.

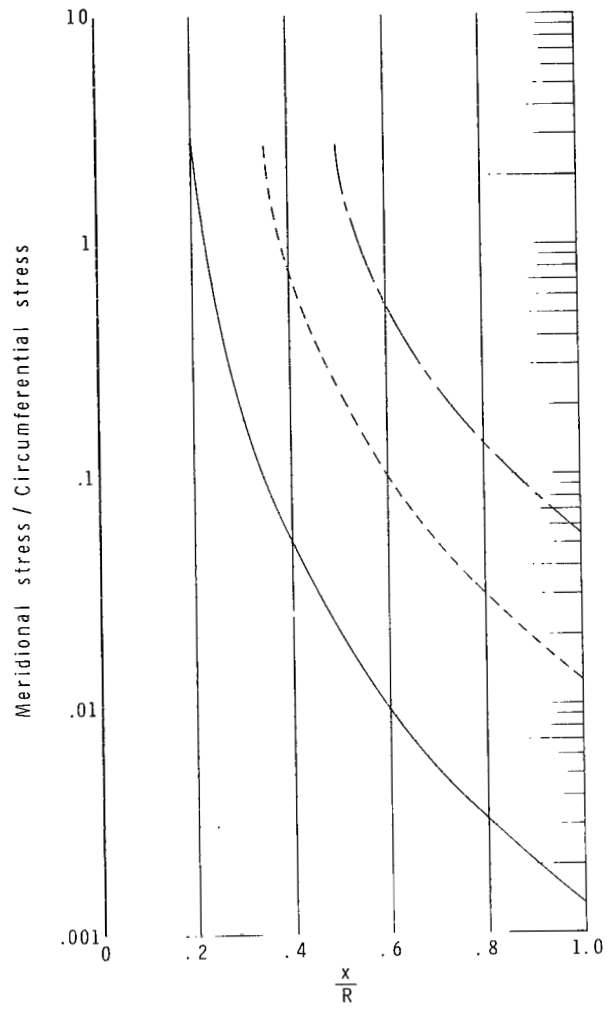
Design considerations.- The equations for the design of a whirling-membrane concentrator (called the paraboloid with a conical covering) are given in reference 2. These equations were used to calculate the membrane deflections under operating conditions and the resulting, or "design," ordinates are given in figure 2. These equations are not strictly applicable when steel cables are used to replace the conical covering because these cables cannot support circumferential stresses. The cables have been used, however, because they are considered to be more resistant to the space environment than a transparent plastic covering. The cables provide at the membrane rim an axial component of loading that is required to give the membrane the desired paraboloidal shape. As previously noted, the cables cannot support circumferential stresses so the equations of reference 2 cannot be used to calculate cable shape. The assumption was made that the cables would be perpendicular to the rim plane at the cable-rim juncture. This assumption with the required axial loading, cable mass, and membrane rotational speed gave a cable shape and thus a cable-hub location on the shaft. The cable hub was made adjustable so that it could be moved vertically on the shaft in the event that the calculated cable shapes were incorrect. Cable lengths were not adjustable so that relocation of the cable hub from the design position resulted in incorrect cable lengths. It should also be noted that blockage of the solar rays by the cables and plastic tabs is about 7.5 percent of the concentrator projected area, which compares favorably with the 8 to 10 percent transmission loss that would be incurred by a plastic covering.

Important factors in the design of the whirling membrane are the membrane stresses. The maximum stress should be well below the material yield stress because of possible failure due to stress concentrations in the neighborhood of the tab-paraboloid junctures. The circumferential and meridional stresses were calculated by means of the equations of reference 2 for a rotational speed of 71 radians per second. The circumferential stress, which is the maximum stress occurring in the membrane, is shown in figure 3(a). All three models have a maximum stress at the rim of approximately 16 meganewtons per meter², which is well below the material yield stress of approximately 100 meganewtons per meter². (Note: 1 meganewton per meter² = 145 pounds per inch².)

Another important design problem is the prevention of membrane wrinkles. The wrinkles would have a degrading effect on the concentration of incident energy of the paraboloid by causing a dispersion of the reflected light. Wrinkling can be caused by



(a) Circumferential stress.



(b) Stress ratio.

Figure 3.- Variation of circumferential stress and stress ratio in the 3.05-meter-diameter whirling-membrane concentrator at a rotational speed of 71 radians per second.

two general processes. First, wrinkling may result from handling, which includes fabrication and packaging. Second, as discussed in reference 2, large-scale wrinkles with crests and troughs parallel to the circumferential stress may form if a suitably large ratio of meridional to circumferential stress is not maintained. This latter wrinkling is called circumferential wrinkling.

Wrinkling due to fabrication occurs if proper care is not taken in assembling the aluminized plastic membrane. A preliminary investigation on various thicknesses of the aluminized plastic was made to determine what stress levels are required to remove this type of wrinkle. The results are given in the appendix, where it is shown that carefully handled samples of the 0.01-millimeter-thick plastic used in the present models were essentially unwrinkled. However, the data of the appendix show that for badly wrinkled samples, such as might occur in packaging, a certain level of stress is required to remove the wrinkles. The present models were carefully handled during fabrication and were not packaged; consequently, they were considered to be essentially unwrinkled.

The calculations of reference 2 indicate, however, that circumferential wrinkles may be a problem because of the low stress ratios near the rim of the paraboloid when a metal hub of a small radius relative to the membrane radius is used. This effect can be seen in figure 3(b) where the calculated ratios of the meridional to circumferential stress in the membrane is shown as a function of membrane radius.

One solution for increasing the stress ratio, suggested in reference 2 and shown in figure 3(b), is to increase the metal-hub radius. Three flat metal hubs with radii of $0.20R$, $0.35R$, and $0.50R$ were selected for testing. Samples of the plastic to be used in the present models were subjected to a range of biaxial-stress ratios, including those expected to be experienced by the whirling-membrane models; the results are described in the appendix. These data and the data of figures 3(a) and (b) show that only the model with the $0.50R$ metal hub should be relatively unaffected by wrinkling. However, for the purpose of taking advantage of the potential for being compactly packaged for launching into space, the smallest possible metal hub is desirable. Therefore the two models with the smaller metal hubs were fabricated to determine the magnitude of the wrinkling and the loss in energy concentration that would actually occur. In a practical model, the flat hub would be replaced by a one-piece paraboloidal mirror. Such a paraboloid would serve the same structural purpose as the flat hub and, by having the same focal length as the membrane, could provide the concentration of additional energy.

Apparatus

The apparatus for testing the concentrators is shown schematically in figure 4, and a photograph of the test arrangement is shown as figure 5. A steel A-frame provided a support for the concentrator and associated optical-ray trace-measuring equipment.

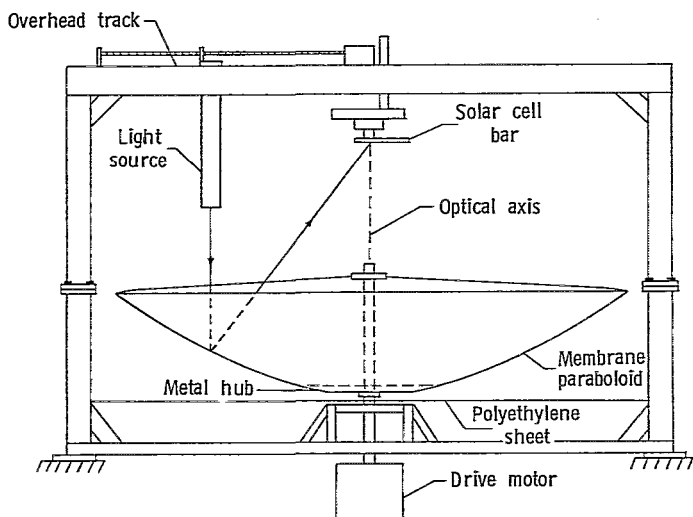


Figure 4.- Schematic of test apparatus.

The concentrator-shaft bearings were located in a platform at the base of the A-frame, and a variable speed electric motor was used to rotate the models. A black polyethylene sheet was stretched across the platform and supported the membrane during spin-up.

The optical-ray-trace equipment consisted of a light source to give a nearly collimated beam of light and 10 silicon solar cells to measure the reflected light distribution in the focal region. The light source utilized a zirconium-arc

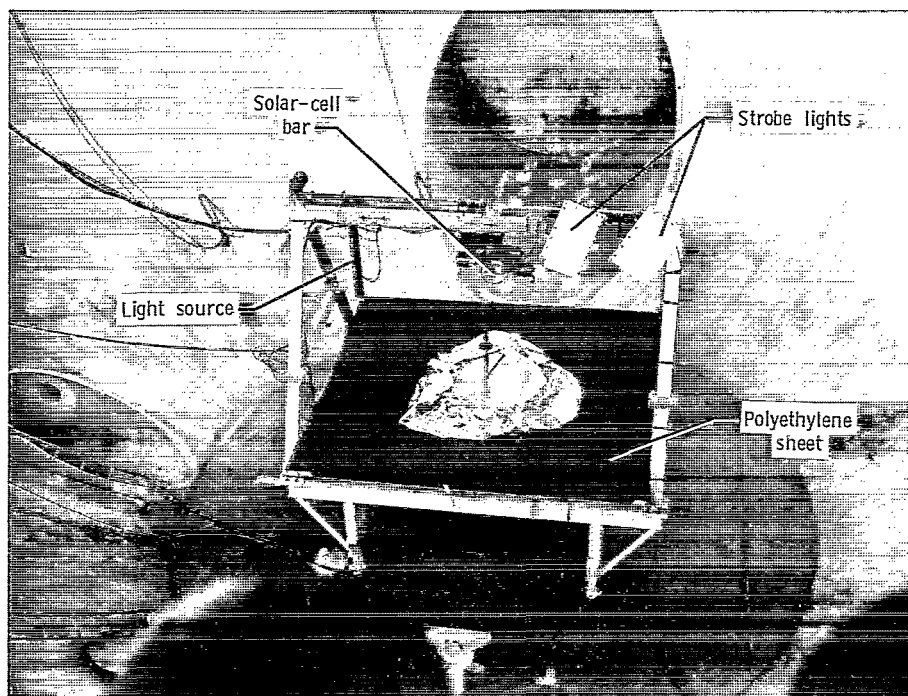


Figure 5.- Whirling-membrane-concentrator test apparatus, with a model installed, in the vacuum sphere preparatory to spin-up. L-64-3674.1

lamp, metal tube, and lens that gave a 7.6-centimeter-diameter light beam with a collimation angle of 0.025° . The light source was positioned along the radial overhead track by means of a remotely controlled electric motor. In this way, different areas of the membrane could be surveyed. The position of the light source was determined from a calibrated selsyn motor-counter system. An additional silicon solar cell was located in the light-source tube to monitor the light irradiance continuously. (Irradiance is defined as the radiant energy incident on a surface per unit area and per unit time.) The 10 solar cells, which were each 0.5 by 0.25 centimeter, were located 2.5 centimeters on centers along the solar-cell bar. The solar-cell bar was designed to survey a volume in the region of the focus and had three modes of operation as follows: (1) rotation about the concentrator optical axis, (2) longitudinal translation perpendicular to the concentrator optical axis, and (3) vertical translation along the concentrator optical axis. The first two modes were controlled by remotely operated electrical motors, and position was determined from calibrated selsyn-motor counter systems. The third mode however was manually set. All solar cells, including that in the light source, had heaters and thermocouples as well as necessary associated equipment to maintain a constant temperature and thus a constant cell sensitivity.

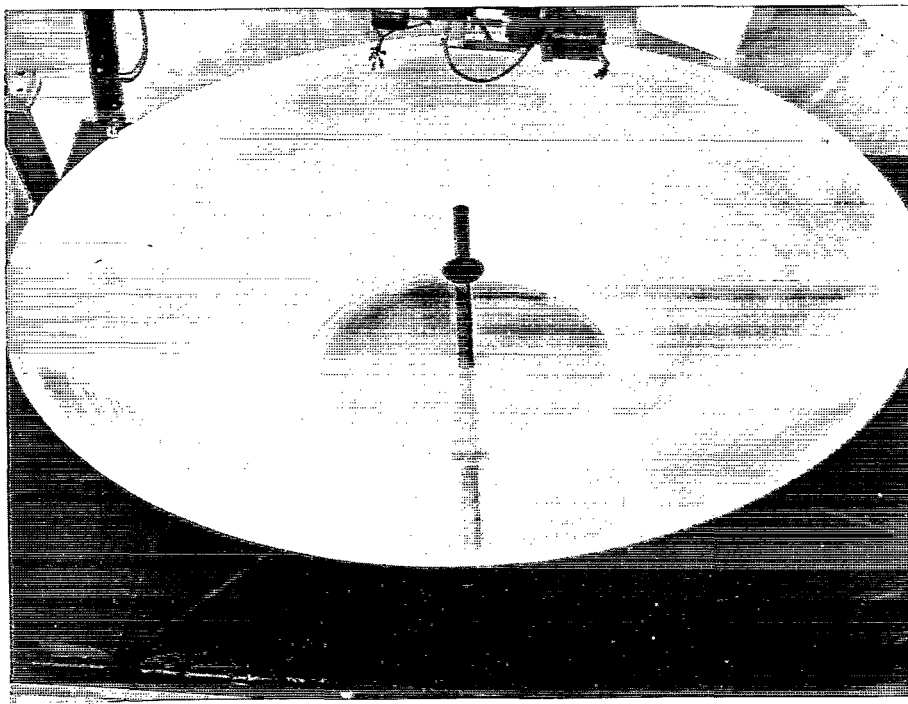
Multipoint self-balancing potentiometers were used to record the output from the thermocouples and the solar cells on the bar, and a continuous-trace self-balancing potentiometer was used to record the monitor-cell output.

Two high-intensity stroboscopic lights located on the upper track of the A-frame were used for visual examination of the concentrator surface. Motion-picture cameras with a film speed of 64 frames per second, located above and to the side of the concentrator, recorded motions of the membrane during operation.

TESTS

All tests were made in an 18-meter-diameter vacuum sphere at pressures below 133 newtons per meter² to prevent flutter of the concentrator membrane. (Note: 1 newton per meter² = 145×10^{-6} pound per inch² = 7.5×10^{-3} millimeter of mercury.) All models were tested at the design rotational speed of 71 radians per second. A photograph of the 0.35R metal-hub model in operation is shown as figure 6.

Table I gives the light source and solar-cell-bar locations in addition to the various model configurations. Figure 7 shows the Cartesian coordinate system used to locate the light source and solar-cell bar with respect to the design paraboloid vertex. Also shown in figure 7 is a plane polar-coordinate system used to locate the solar cells with respect to the optical axis. Configurations I and II, the models with the 0.20R and 0.35R metal hubs, respectively, were tested with the cable hub only at the design location



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Figure 6.- Whirling-membrane concentrator operating at the design rotational speed of 71 radians per second. 0.35R hub model.

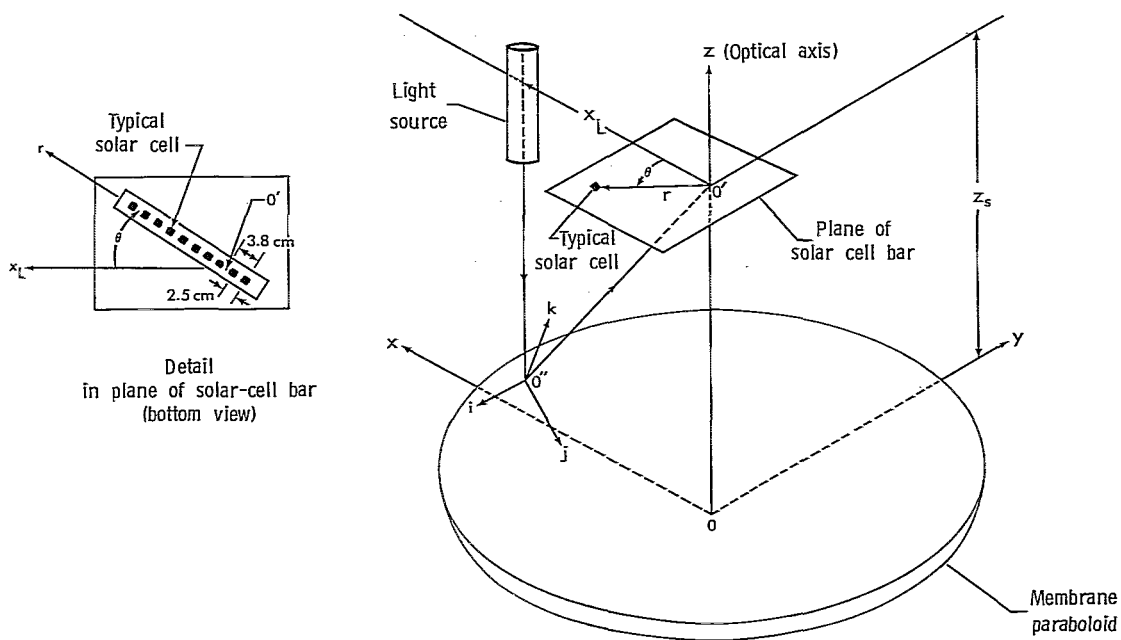


Figure 7.- Coordinate systems relating the location of the whirling membrane, light source, and solar cells.

$z_c = 40.8$ centimeters. (See fig. 1.) Configuration III, the model with the 0.50R metal hub, was tested with the cable hub at the design location and then with the cable hub raised in 2.5-centimeter increments up to a maximum of 10 centimeters above the design value. The light-source locations were determined by first dividing the projected area of each membrane into five annuli of equal area. The light was then positioned at the midradial point of each annulus. The axial position of the solar-cell bar was varied about the design focal plane, $z_s = 132.1$ centimeters, as shown in table I. The angular positions were set by rotating the bar about the optical axis through a range of 0° to 315° in 45° increments. The axis of rotation coincided with the optical or spin axis that passed through a point on the bar 3.8 centimeters from the center of an end solar cell. (See detail of fig. 7.) This axis of rotation was chosen to give a relatively wide coverage of the irradiance distributions and still have two cells give check readings when the bar was rotated to the supplementary angular position.

A typical test consisted of first setting the z_s -coordinate of the solar-cell bar, then evacuating the vacuum sphere to the desired pressure. The membrane was brought up to design rotational speed and the light source was then set at one of the predetermined radial locations, x_L . The solar-cell bar was rotated through eight angular locations (θ -coordinates) and data were taken at each location. The light source was moved to the next radial location and the angular survey made. These last two steps were repeated until all values for the light source and the solar-cell-bar angular position, shown in table I, were complete.

REDUCTION AND ACCURACY OF DATA

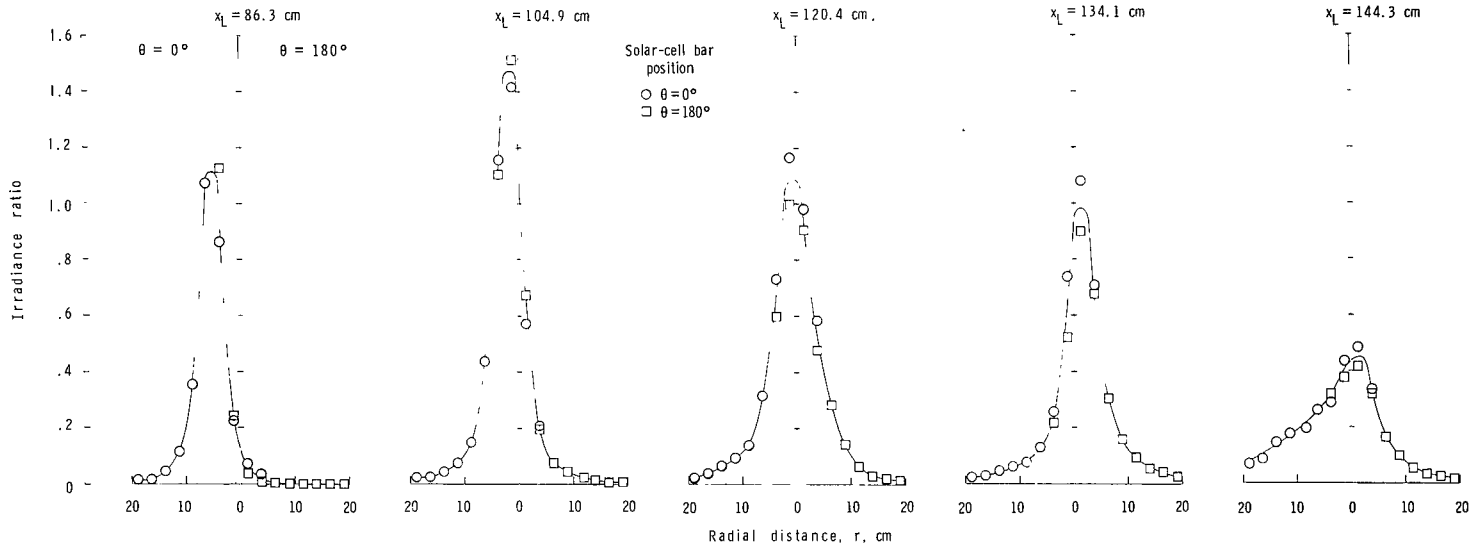
The basic data measured during the investigation were solar-cell voltages. It should be noted here that the readout equipment measured only average voltage. The instantaneous voltage, which would detect such things as blockage due to passage of a cable and local oscillations in the membrane, was not measured. The voltage readings from each solar cell on the bar were divided by the monitor cell voltage, recorded over the same time interval, to eliminate the effect of change in the test light-source irradiance. Because all cells had different sensitivities to the irradiance, calibration factors obtained from laboratory tests were applied to the voltage ratios to put the data on a common basis. No corrections for temperature were made to the data as all cells were maintained at a temperature of $305^\circ \pm 1^\circ$ K. The corrected voltage ratio, defined as irradiance ratio, represents the factor by which the irradiance of the incident energy has been modified by concentrator geometry and specular reflectance of the aluminized plastic. Note that the magnitude of the irradiance ratio will also vary directly with the diameter of the light beam used. However, this ratio provides a convenient means of analyzing

the data inasmuch as the magnitude does not influence such membrane properties as shape, geometric efficiency, and focal length.

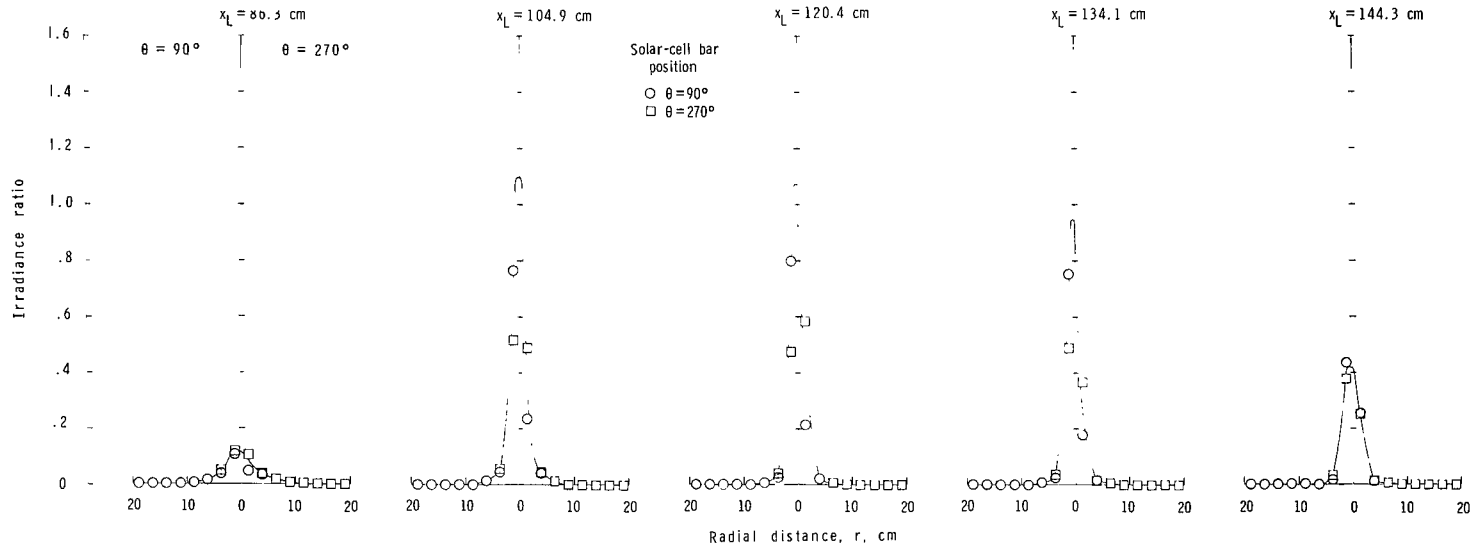
Several sources of error in the magnitude and the location of the irradiance-ratio data existed in the test arrangement. The first and possibly largest error was associated with the solar-cell sensitivity calibration. Twenty sensitivity calibrations were made on each cell at irradiance ratios near 0.70 and the resulting data varied by ± 10 percent about the average values which were used in the reduction of data. The alinement of the light source parallel to the optical axis of the concentrator could be made within only $\pm 0.1^\circ$, which represents a focal-plane image displacement that varies from 0.5 centimeter for the innermost light-source position to 1.1 centimeters for the outermost position. The locations of the solar cells on the bar were determined to be within 0.4 millimeter of the nominal 2.5-centimeter intervals. The axis of rotation of the bar was within 0.8 millimeter of the axis of rotation of the concentrator, and the angular position of the bar was determined to be within $\pm 2^\circ$ of the desired position. The misalinement of the light source and the displacements of the solar cells from their nominal positions are not readily transferable to a percentage error in irradiance ratio; however, the irradiance-ratio error involved is considered to have a minor effect on the overall accuracy of the data.

RESULTS AND DISCUSSION

A thorough exploration of the irradiance-ratio distributions in and near the design focal plane was made in order to determine such factors as level of irradiance ratio, and image location, size, and shape. Configuration III-D was chosen for complete analysis because a preliminary analysis of data obtained on all models showed that it gave the best concentration of energy. An example of the measured irradiance-ratio distributions for this configuration is shown in figure 8 where irradiance ratio is plotted as a function of radial distance from the optical axis. This configuration utilized the 0.50R metal hub, and the cable hub was located in the highest position on the shaft (50.8 centimeters above the concentrator design vertex). The survey plane was located 129.5 centimeters above the design vertex; the light source was positioned at the five different radial stations in turn and distributions at each of the solar-cell-bar angular locations are shown. Curves have been estimated for the data by drawing a smooth curve through the points and averaging repeat points where available. The further condition was imposed that at a given value of x_L the curves obtained for the different values of θ should have the same value of irradiance ratio on the optical axis ($r = 0$). From these and similar data, it is possible to estimate the actual focal length, geometric efficiency, and geometry of the concentrator as discussed in the following sections.

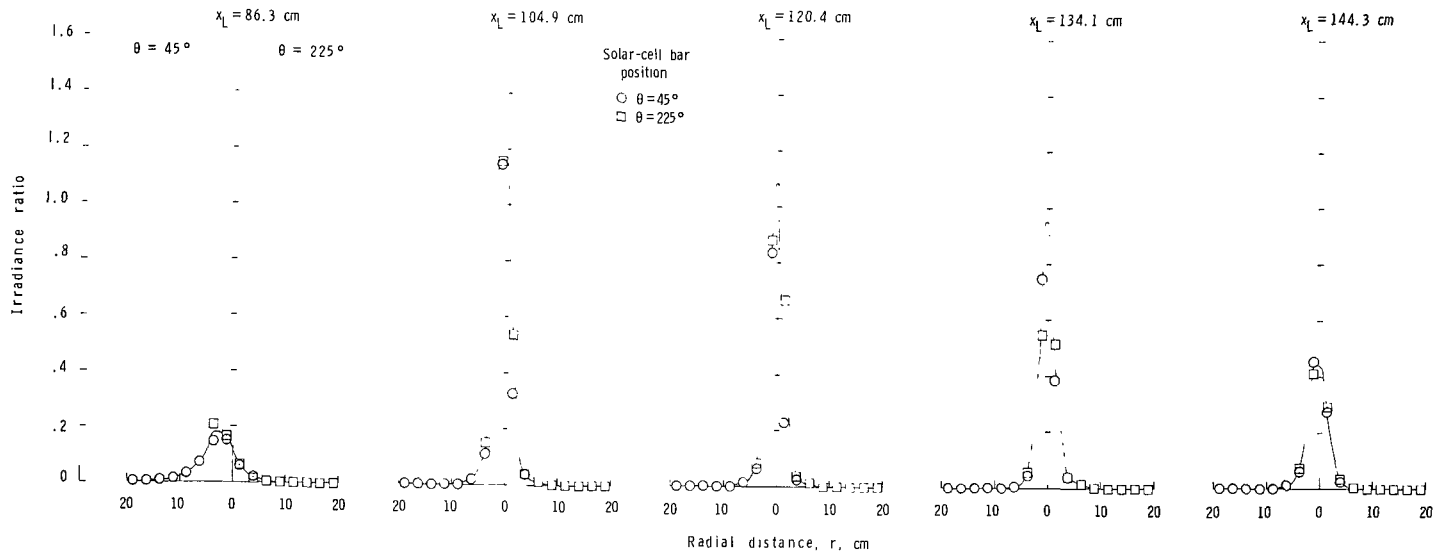


(a) $\theta = 0^\circ$ - 180° axis.

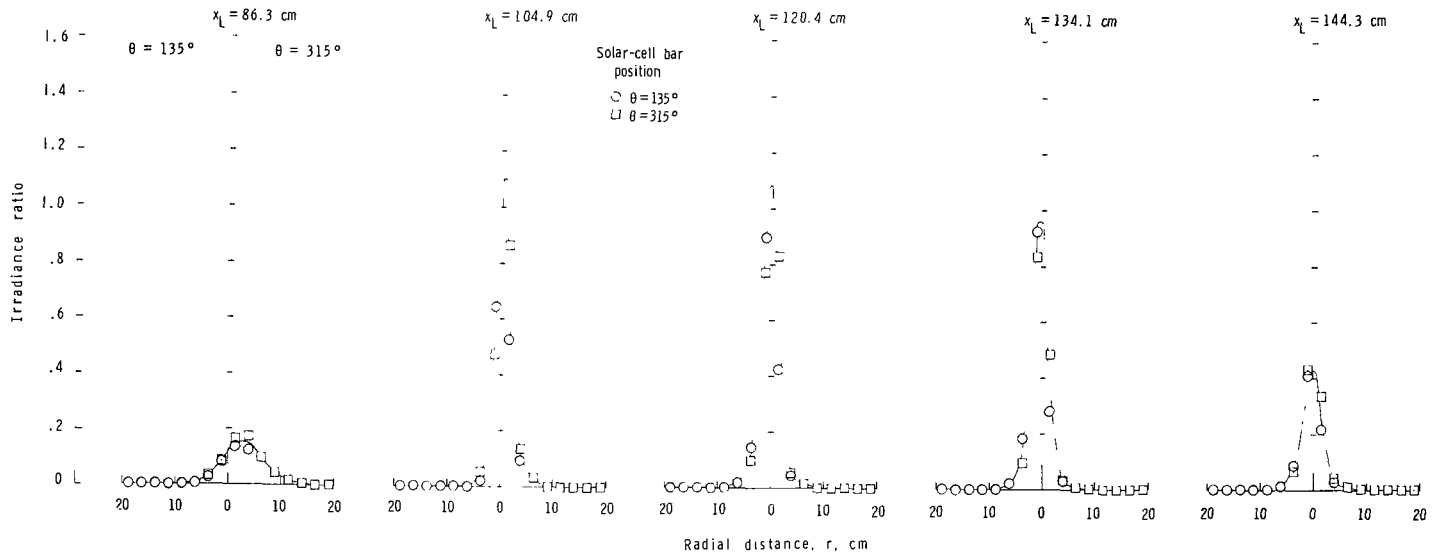


(b) $\theta = 90^\circ$ - 270° axis.

Figure 8.- Irradiance-ratio distributions along various axes in the survey plane $z_s = 129.5$ cm for the 0.50R hub model (config. 111-D) for five light-source locations.



(c) $\theta = 45^\circ$ - 225° axis.



(d) $\theta = 135^\circ$ - 315° axis.

Figure 8.- Concluded.

Concentrator Focal Length

In order to determine concentrator focal length from irradiance-ratio distributions, only the data along the $\theta = 0^\circ$ - 180° axis are used. The data of figure 8 for the $\theta = 0^\circ$ - 180° axis provide an indication of the focal lengths of each of the membrane annuli surveyed for configuration III-D. A consideration of the properties of a parabolic membrane indicates that if the survey plane had been placed inside the focus, all the peaks would have fallen on the $\theta = 0^\circ$ side of the optical axis. If the survey plane were placed outside of the focus, all peaks would have fallen on the $\theta = 180^\circ$ side of the optical axis. The focal length for each annulus may be determined from the displacement of the peak of the irradiance-ratio distribution from the optical axis ($r = 0$) and the survey-plane distance from the concentrator vertex. It should be noted that this focal length is a mean value since laboratory tests of the light source showed that the width of the irradiance-ratio distributions would have been less than 0.2 centimeter for a perfect paraboloid. As each distribution is approximately 20 centimeters or greater in width, it may be assumed that variations in focal length existed over each annulus. However, for purposes of analysis, the mean focal length is considered to be representative of each annulus. The displacements of the irradiance-ratio distribution peaks on both sides of the optical axis show that the membrane is an approximate parabola if only the mean focal lengths are considered.

Because the membrane is approximately parabolic, irradiance-ratio distributions that are representative of the whole membrane are required to obtain the focal length of the entire concentrator. Therefore, the irradiance-ratio distributions for the five annuli of figure 8 have been averaged and the average of these distributions is shown in figure 9. Also shown are average distributions obtained at survey-plane locations of $z_S = 132.1$ and 127.0 centimeters. The focal length for the entire concentrator is defined as the survey-plane distance from the vertex at which the peak of the average irradiance-ratio distribution falls on the optical axis. The irradiance-ratio data along the $\theta = 0^\circ$ - 180° axis of figure 9 show that the peak should fall on the optical axis between $z_S = 129.5$ and 132.1 centimeters. Interpolation gives a value for focal length of 130.5 centimeters, which is about 1 percent less than the design focal length of 132.1 centimeters.

Concentrator Geometric Efficiency

The main purpose of a solar concentrator is to concentrate solar rays into a small image in the focal plane; therefore, the geometric efficiency, a measure of the concentrating ability, is of interest. Geometric efficiency is defined as the ratio of the energy falling within a circle centered about the focus in the focal plane to the energy specularly reflected from the concentrator. Therefore, the geometric efficiency is a function of

only the concentrator geometry and is not affected by such factors as specular reflectance and incident-irradiance level.

Although irradiance-ratio distributions were not obtained at the best focal length, the survey plane at $z_s = 129.5$ centimeters is sufficiently close that the data of figure 9 may be used to give a good indication of geometric efficiency. It should be noted at this point that the complete concentrator should be illuminated to obtain the exact irradiance-ratio distributions, and hence, the exact geometric efficiency. However, a good approximation to the irradiance-ratio distribution for complete illumination was made. The data of figure 9 were converted to the form of a contour map of the average irradiance ratios in the survey plane and are shown in figure 10. Measurements were not made over a sufficiently wide area in the survey plane to obtain the complete profile so the location of the zero average-irradiance-ratio contour has been estimated. This contour plot is the average irradiance-ratio distribution in the survey plane that results from illumination along the x-axis. (See fig. 7.) If the light source were moved so that illumination took place along the

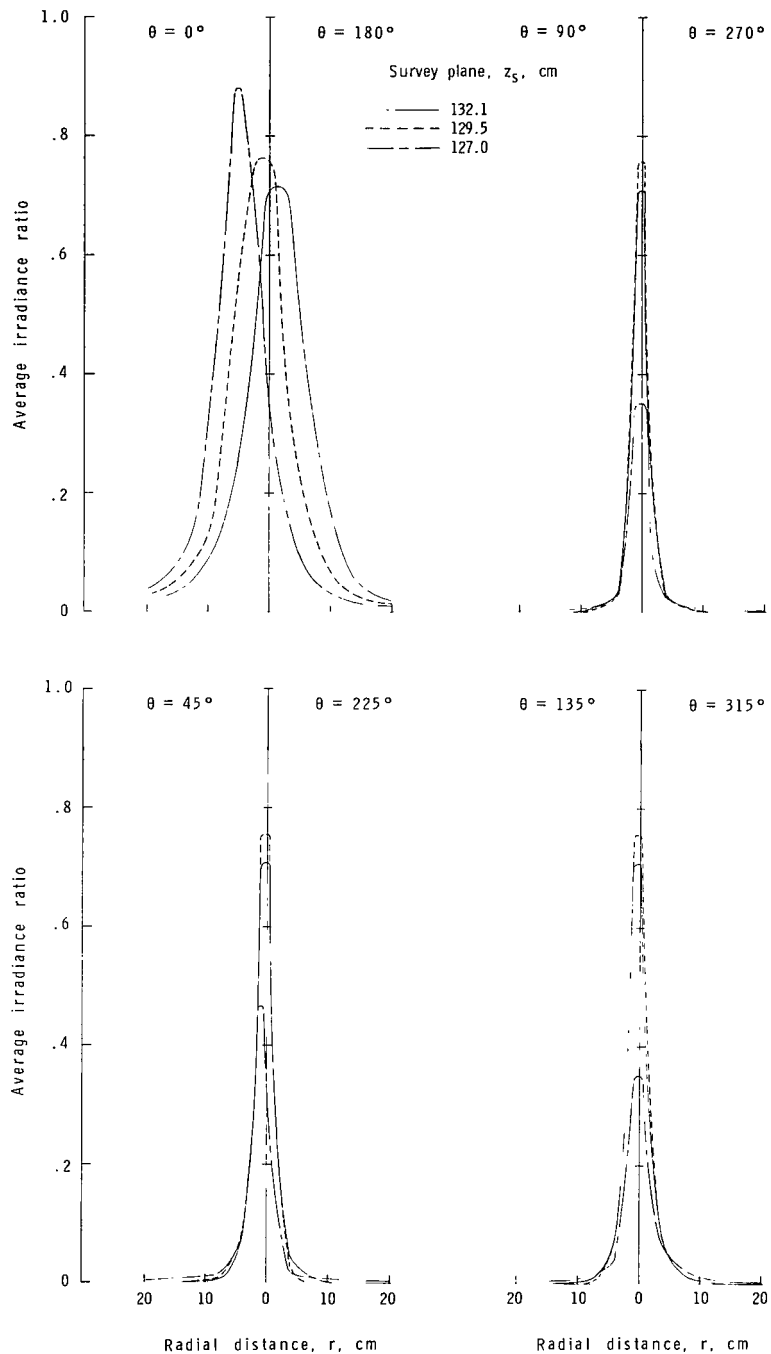


Figure 9.- Average irradiance-ratio distributions along various axes in three survey planes for the 0.50R hub model (config. III-D).

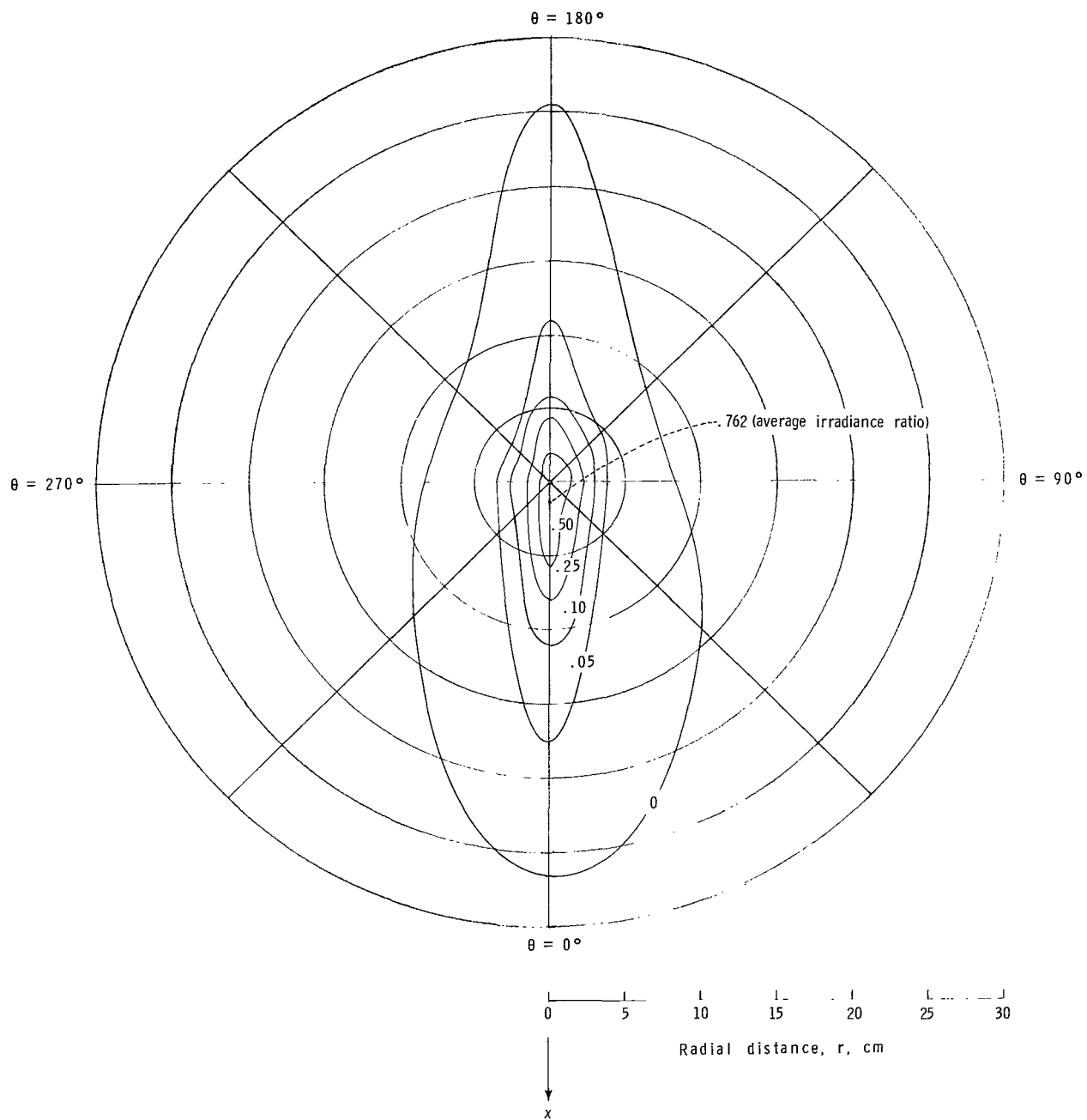


Figure 10.- Contours of constant average irradiance ratios in the survey plane $z_s = 129.5$ cm of 0.50R hub model (config. III-D).

y-axis, it is assumed that the resulting average irradiance-ratio distribution would have the same shape and magnitude as the contour plot of figure 10 because the membrane is a surface of revolution. However, the data would be rotated 90° to the data shown in figure 10; that is, the major axis of the contour would fall along the 90° - 270° axis. Therefore, to obtain the average irradiance ratio, at any specific point in the survey plane, that results from illumination of the entire concentrator, it is necessary only to calculate the line integral of the function shown in figure 10 about a circle of radius r . This procedure has been followed at several radii and the results are shown in figure 11.

In figure 11, the average irradiance-ratio distribution, as calculated for a completely illuminated whirling-membrane concentrator, is shown as a function of radial distance from the optical axis in the survey plane at $z_s = 129.5$ centimeters. The maximum diameter of the distribution is about 50 centimeters, which is much greater than the maximum image diameter of 0.2 centimeter that would be obtained from a perfect paraboloid having the same diameter and focal length and utilizing the test light source. Therefore, as previously noted, it may be concluded that surface errors were present in the whirling membrane. It should be noted that the diameter of the image or width of the irradiance-ratio curve is a function of light-source collimation angle as well as geometric accuracy of the concentrator. If the whirling membrane were illuminated by a light source having an angle of collimation larger than the test source, e.g., the sun, the effect would be to increase the diameter or width of the irradiance-ratio distribution. A focal-plane distribution for a perfect paraboloid illuminated by the sun is shown by the dashed lines in figure 11. The peak magnitude of this curve has been assigned the same value as that of the whirling-membrane data, for convenience. Figure 11 shows, that the image diameter for a perfect paraboloid is 3 centimeters; therefore, the image diameter of the whirling membrane would be increased from 50 centimeters to 53 centimeters for solar illumination.

The two curves of figure 11 were used to determine the geometric efficiencies of the whirling membrane and the perfect paraboloid. The results are shown in

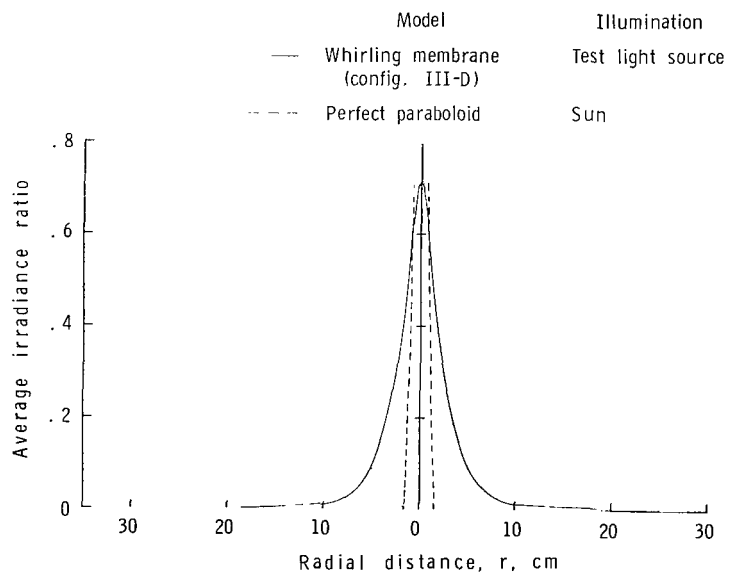


Figure 11.- Variation of average irradiance ratio in the survey plane $z_s = 129.5$ cm for completely illuminated concentrators.

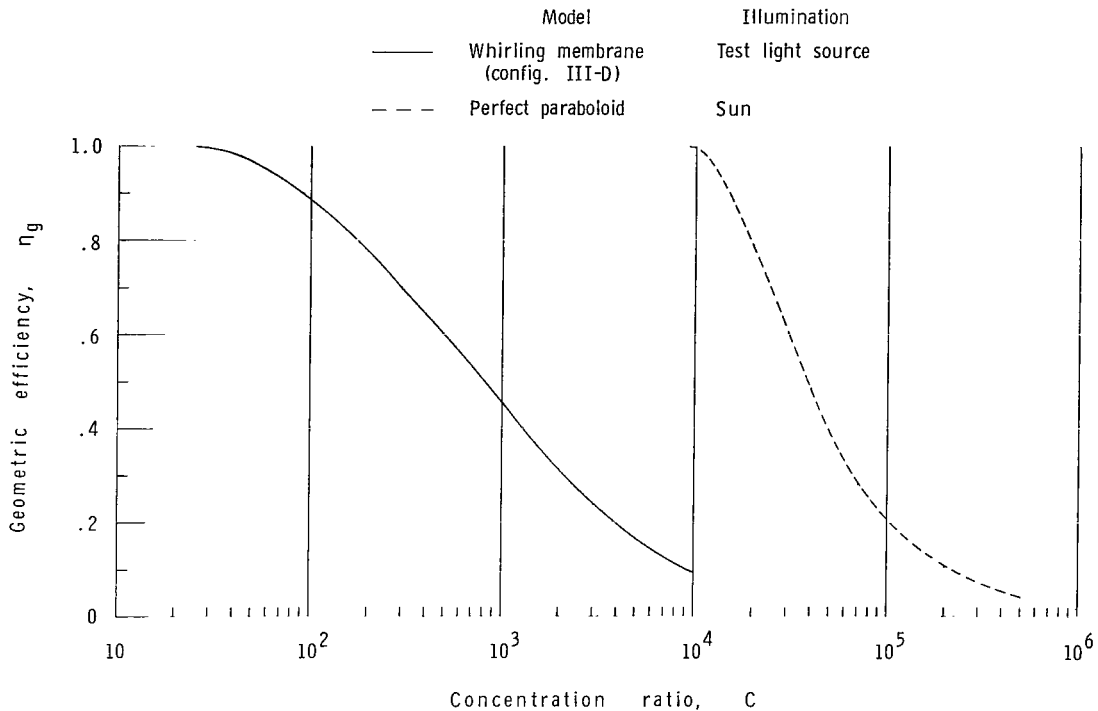


Figure 12.- Concentrator efficiency over a range of concentration ratios.

figure 12 where geometric efficiency is presented as a function of concentration ratio, also known as area ratio. A geometric efficiency of 1.00 for the whirling membrane, illuminated by the test light source, occurs at a concentration ratio of about 25. Had the membrane been illuminated by the sun, the value of 1.00 would have occurred at a concentration ratio of about 23. Hence, for all practical purposes, the efficiencies shown for the whirling membrane, at least for low concentration ratios, are approximately those which would have been obtained with the sun as an illumination source. The perfect paraboloid illuminated by the sun maintains a geometric efficiency of 1.00 up to a concentration ratio of 10 000. At this ratio, the diameter of the circular area in the focal plane becomes smaller than the diameter of the solar image and results in reduced efficiencies for increasing concentration ratio. Although the whirling membrane would not be suitable, in its present form, for systems requiring highly accurate paraboloids, it does give good geometric efficiencies (greater than 0.90) at concentration ratios below 100.

Concentrator Geometry

One common method of characterizing the quality of a solar concentrator is to measure the error distribution of the reflective surface. The irradiance-ratio distributions, of which the data of figure 8 are typical, provide a basis for this analysis. The

error consists of a combination of displacement in the z-direction of the actual surface from the design paraboloid surface and an angle between the actual surface normal and the normal to the design paraboloid. The local coordinate system for the surface normals is shown in figure 7; the radial and circumferential projections of the slope error δ_r and δ_c , respectively, are shown in figure 13. The slope errors in this figure are only approximations since the displacement Δz has been omitted in the sketch. However, the effect of this approximation has been evaluated and has been found to be a maximum of 0.03° which has a negligible effect on the error distribution.

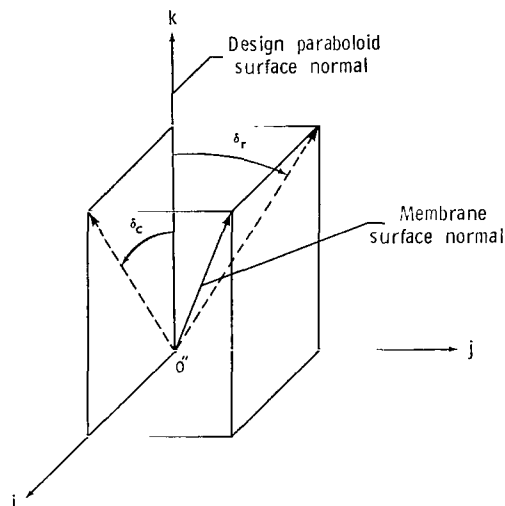
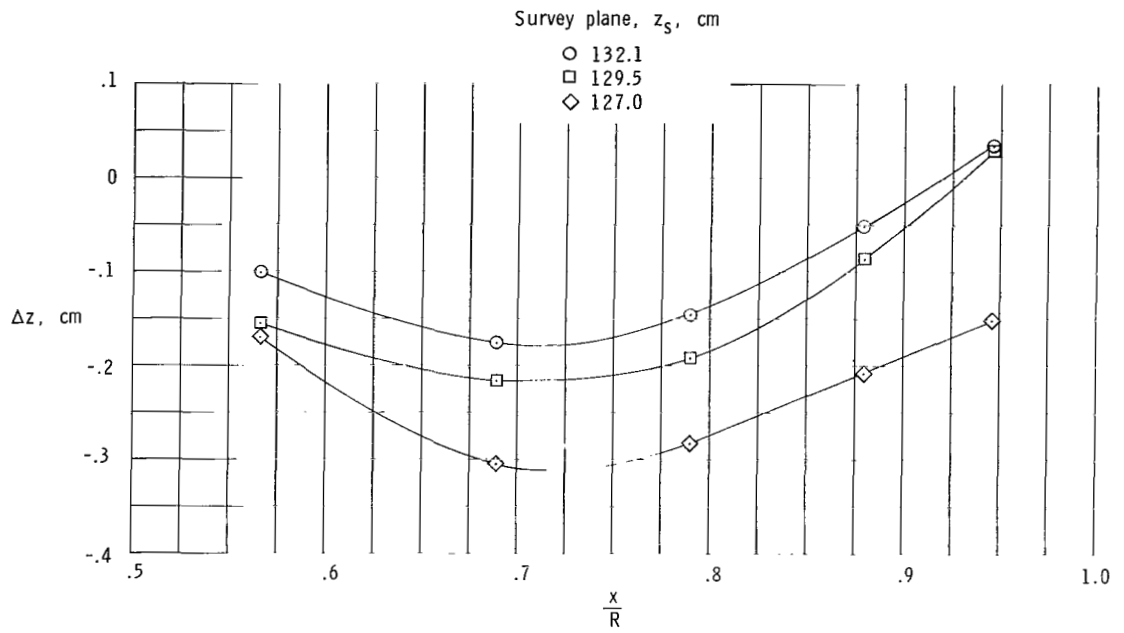


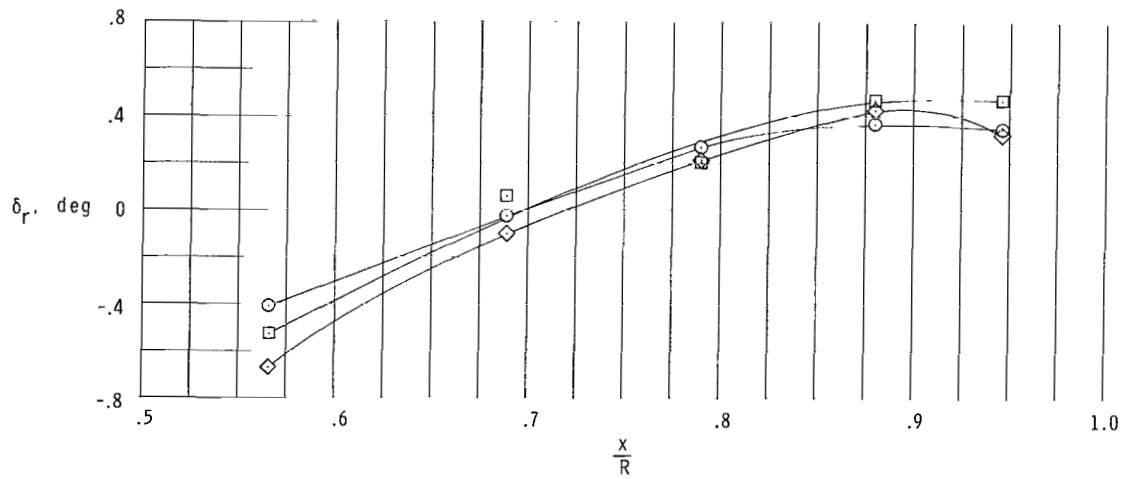
Figure 13.- Coordinate system defining membrane-surface slope errors.

An examination of figure 8(a) indicates that two types of errors are present in the surface.

First, mean errors were apparent as evidenced by the displacement, about the optical axis, of the peaks of irradiance ratio along the $\theta = 0^\circ$ - 180° axis. These displacements, along with such other dimensions as survey-plane distance from the vertex and radial location of the light source, were used in an iterative procedure to determine the membrane general shape. The displacements Δz from the ordinates of the design parabola are shown in figure 14(a); and the radial-slope error δ_r is shown in figure 14(b). The results were calculated from data obtained at survey-plane distances of $z_s = 132.1$ centimeters and 127.0 centimeters as well as from the $z_s = 129.5$ centimeters data of figure 8(a). Although the displacements calculated at the three survey-plane locations do not agree in magnitude, the trends are similar. In general, the displacements show that the membrane sagged below the design ordinates. The reason for this sagging is not known, but one contributing factor may have been the short cables used for this configuration (III-D). Cable lengths were set for a cable-hub design height of $z_c = 40.8$ centimeters (configuration III) in the first tests, but subsequent experimentation indicated that a setting of $z_c = 50.8$ centimeters (configuration III-D) resulted in a more efficient concentrator. The cables were not lengthened when the cable hub was moved to 50.8 centimeters so that a decrease of about 0.4 centimeter occurred in the membrane diameter. This decrease in diameter could modify the membrane-stress distributions and resulting displacements. The membrane slope errors that result from the displacements are shown in figure 14(b). Over the surveyed area of the membrane, the mean slope errors varied from about -0.6° to 0.4° .



(a) Vertical displacement.



(b) Slope error.

Figure 14.- Variation of membrane vertical displacements and mean-slope errors for the 0.50R hub model (config. III-D).

Second, the data of figure 8(a) show that random errors in addition to the mean errors were also present. The existence of random errors may be deduced from the fact that had the paraboloid been perfect, the distribution of figure 8(a) would have been only 0.2 centimeter in width. The irradiance-ratio distributions are actually 20 centimeters or more in width and thus indicate the presence of membrane imperfections. The shapes of the distributions, which are similar to probability curves, indicate the imperfections were approximately random. The standard deviation in the radial direction σ_r has been calculated from the data of figure 8(a), and the results are shown in figure 15. The standard deviation error is roughly 0.5° out to $x/R = 0.90$ where a sharp increase to 0.8° at about $x/R = 0.95$ is noted. These errors could be caused by circumferential wrinkles, which were discussed previously herein and in reference 2, or they could be due to local oscillations in the membrane or a combination of both factors. That there is a large increase in error near the rim tends to support the wrinkle theory since design calculations showed that stress ratios in this region were marginal for the prevention of wrinkles. Local oscillations in the membrane that would have been detectable if values of irradiance ratio had been measured over a small time interval compared to the interval of the oscillations were not observed because the instrumentation measured average values only. However, scrutiny of the membrane under the stroboscopic lights revealed the presence of both factors, but a quantitative assessment of each could not be made.

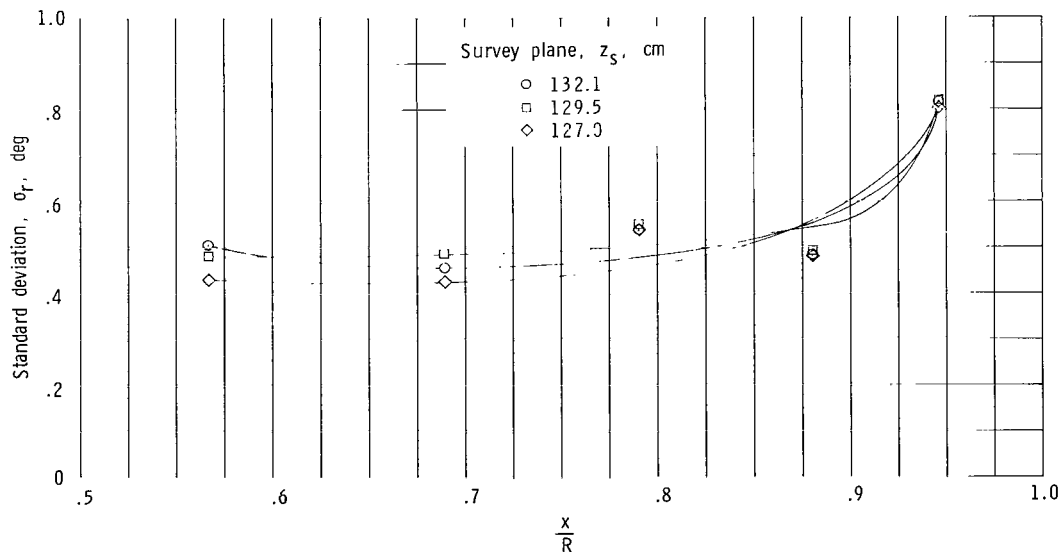


Figure 15.- Variation of standard deviation of radial-slope error for the 0.50R hub model (config. 111-D).

For a complete characterization of the membrane geometry, the circumferential errors, which cause a displacement of the distribution on the $\theta = 90^\circ$ - 270° axis, must also be considered. The data of figure 8(b) show that little or no displacement of the peaks of the distribution occurred and indicate that there were no mean errors in the circumferential direction and that the membrane on an average was a surface of revolution. However, random errors are apparent because the distributions of figure 8(b) are similar in shape to those measured in the membrane radial direction, figure 8(a). A standard deviation error $\sigma_c = 0.25^\circ$ was calculated for a membrane radius of 120.4 centimeters, the only radius at which the peak irradiance-ratio value fell on the optical axis. This circumferential error was only half the standard deviation error measured at the same radius in the radial direction.

Three possible explanations for the presence of the random circumferential errors exist. First, they may be caused by the previously discussed local oscillations in the membrane. Second, the cables may have restrained the membrane at the points of attachment thus allowing the membrane to take the shape of a parachute. Third, the flat membrane gores were strained to conform to the convex mold during fabrication. If these strains were relieved when the membrane was removed from the mold, the shape between gore seams would be similar to an umbrella. Observation of the membrane under the stroboscopic lights did not reveal the source of the errors as they were relatively small compared to the errors in the radial direction.

Effect of Metal-Hub Size

One objective of the present investigation was to determine the effect of metal-hub radius on the circumferential wrinkling of the whirling membrane. As noted in reference 2, the use of hubs of larger radius (with respect to membrane radius) should result in a more favorable ratio of meridional to circumferential stresses and hence less wrinkling and a more accurate concentrator. The effect of hub size is shown in the radial distributions of irradiance ratio along the $\theta = 0^\circ$ - 180° axis in figure 16. The average irradiance ratios for the three different hub radii, 0.20R, 0.35R, and 0.50R, are given as a function of radial distance from the optical axis in the survey plane, $z_s = 132.1$ centimeters, which corresponds to the design focal length. A more severe wrinkling would be evidenced by a lower peak value of average irradiance ratio and a broader distribution. On this basis, the 0.35R and 0.50R hub models are less affected by wrinkling than the 0.20R hub model. This conclusion tends to confirm the analysis of reference 2. However, it should be noted that the data of figure 16 appear to be influenced by factors other than metal-hub size. Figure 17 shows that configuration III-D, for which the cable hub was raised to 50.8 centimeters, had a peak irradiance ratio of 0.76 or about 4 times the peak value for configuration III. An examination of the individual irradiance

ratio plots from which distributions of figure 17 were compiled was made. This examination showed that the increase in peak values resulted from the removal of small random errors such as wrinkles from the membrane rather than from a reduction in the mean errors. It appears that the data of figure 16 are also affected by the presence in the membrane of wrinkles that are caused by factors other than the effect of hub size. Therefore, the differences in the irradiance-ratio distributions of figure 16 are only an indication of the circumferential wrinkling due to the effect of hub size.

Modifications to the Design Configurations

As shown in figure 16, peak average irradiance ratios of only about 0.16 or less were measured on configurations I, II, and III with the test light-source illumination. Calculations show that approximately the same values of peak average irradiance ratios would have been obtained had the sun been used as the source of illumination. As these values are low when compared with a value of about 15 that would be obtained from a perfect paraboloid illuminated by the sun, an attempt was made to improve the membrane shape by modification of the test parameters.

The only successful modification was the relocation of the cable hub to a higher position on the rotating shaft. This modification was made only to the 0.50R hub model. The results are shown in figure 17 where irradiance ratio is given as a function of radial distance from the optical axis in the survey plane located at the design distance of 132.1 centimeters. The cable hub was moved up in increments of 2.5 centimeters, and a definite increase in peak irradiance ratio resulted from each move. The peak irradiance ratio was increased by a factor of

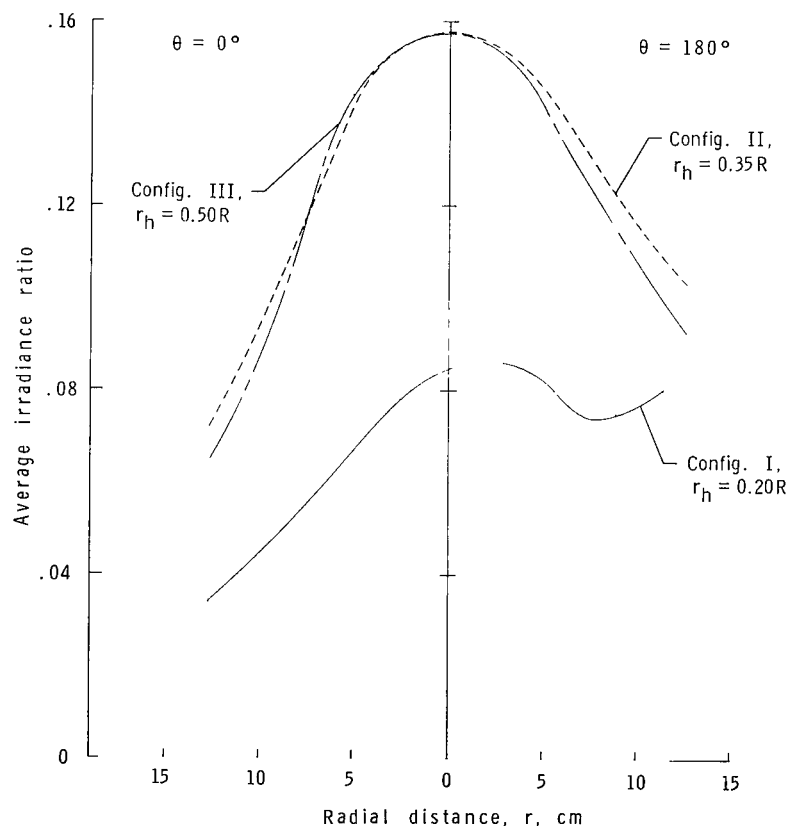


Figure 16.- Average irradiance-ratio distributions of the three hub models along the $\theta = 0^\circ$ - 180° axis in the design focal plane, $z_s = 132.1$ cm.

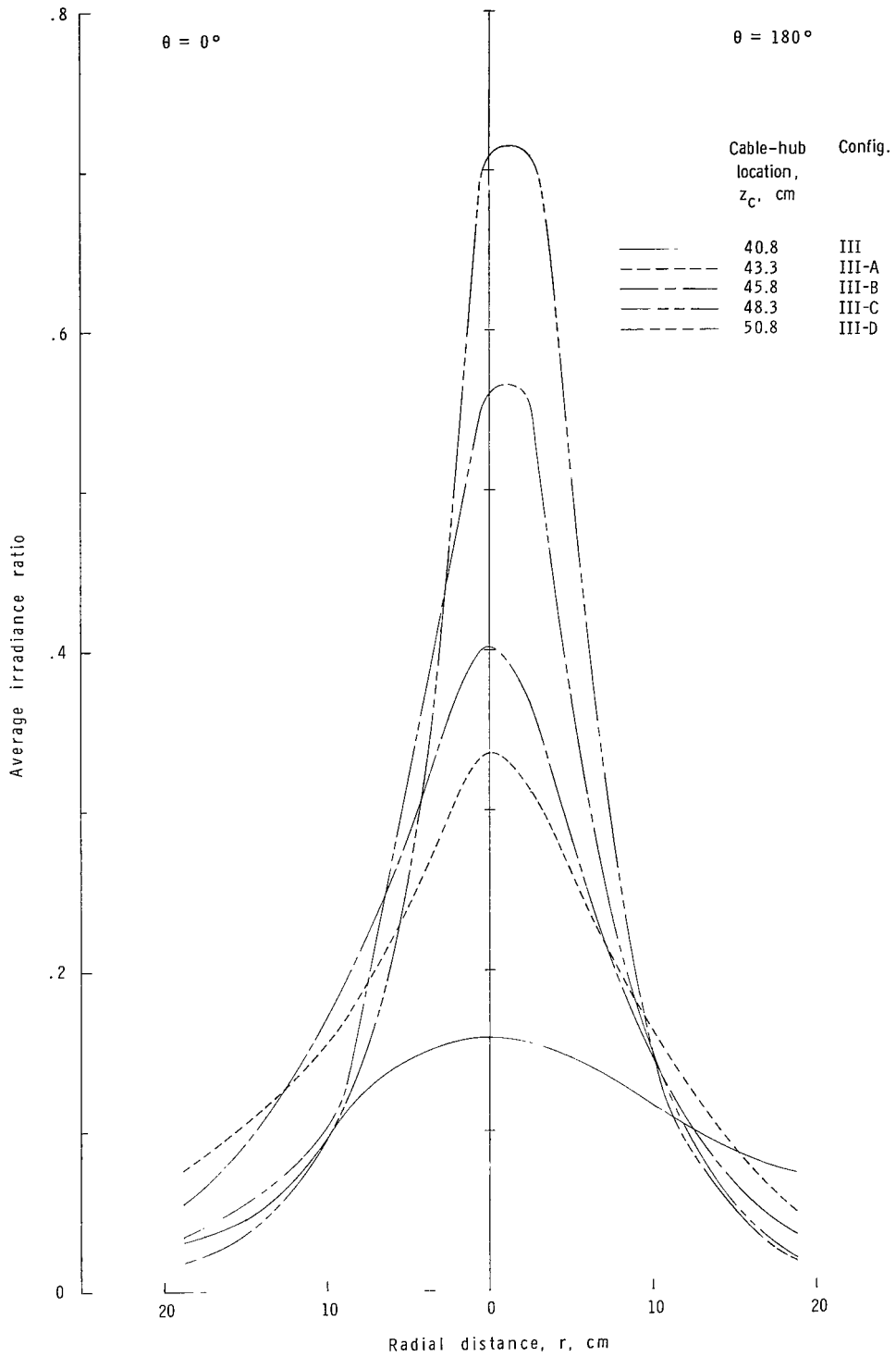


Figure 17.- Average irradiance-ratio distributions along the $\theta = 0^\circ$ - 180° axis in the design focal plane, $z_s = 132.1$ cm, for the 0.50R hub model.

over 4 by moving the cable hub from the design position $z_c = 40.8$ centimeters to the highest position $z_c = 50.8$ centimeters. The increase in peak irradiance ratio was apparently due to the suppression of circumferential wrinkles that had formed because the cables, with the hub in the lowest position, were providing insufficient support to the membrane rim. Motion pictures of the membrane showed that movement of the cable hub from the lowest to the highest position resulted in raising the rim by about 2 centimeters. The pictures also showed that reflections from the membrane were blurred with the hub in the lowest position (as would occur if wrinkles were present), but became sharper as the hub was raised. As previously noted, in the design of the cables it was assumed that at the cable-rim juncture, the cables were perpendicular to the rim plane. It is obvious from the test results that this assumption was incorrect, and the location of the cable hub relative to the metal hub is an important factor in the design of a whirling membrane concentrator.

Configurations I, II, and III were each investigated at rotational speeds above the design value of 71 radians per second with little or no improvement in concentrating ability.

CONCLUSIONS

The whirling-membrane solar-concentrator concept has been investigated by the measurement of the accuracy with which a 3.05-meter-diameter paraboloid focuses incident energy. Three membrane paraboloids constructed of 0.01-millimeter-thick aluminumized plastic were rotated at 71 radians per second in a vacuum chamber at pressures of less than 133 newtons per meter². The three membranes were attached to metal hubs having ratios of hub radius to membrane radius of 0.20, 0.35, and 0.50. The test results indicate the following:

1. The membrane with the 0.50 metal-hub radius and with the cable hub in the highest position gave the best concentration of energy. The following properties of the whirling membrane were determined from the data:

(a) The focal length was 130.5 centimeters which is about 1 percent less than the design focal length of 132.1 centimeters.

(b) A geometric efficiency of 1.00 was determined for a concentration ratio of 23, and efficiencies greater than 0.90 were obtained at concentration ratios up to 100.

(c) In the radial direction, membrane surface mean error varied from -0.6° to 0.4° while the standard deviation of the random error was roughly 0.5° over most of the membrane with a sharp increase to 0.8° near the rim.

(d) In the circumferential direction, little or no mean error was noted, but a standard deviation of the random error of 0.25° was determined at a concentrator radius of 120.4 centimeters.

2. Increased efficiency was indicated for models with the larger hubs; however, conclusive evidence was obscured by the presence of other factors.

3. The peak value of the irradiance-ratio distribution in the focal plane was increased by a factor of over 4 when the cable hub was moved to a position 10 centimeters above the design value. Thus, the cable-hub location relative to the metal hub is an important factor in the design of a whirling-membrane solar concentrator.

Langley Research Center,

National Aeronautics and Space Administration,

Langley Station, Hampton, Va., November 16, 1967,

120-33-06-03-23.

APPENDIX

EFFECTIVE REFLECTANCE OF ALUMINIZED PLASTIC MEMBRANES UNDER BIAXIAL TENSILE LOADING

By Atwood R. Heath, Jr., and Victor R. Bond
Langley Research Center

The results presented in reference 2 indicated that when wide thin sheets of material are subject to pure tension in one direction, large-scale wrinkles tend to form with crests and troughs parallel to the applied force. Reference 2 indicated that the circumferential stresses near the rim of a paraboloidal whirling membrane can be very large compared to the meridional stresses thus resulting in a condition conducive to the formation of circumferential wrinkles. Other types of wrinkles that are of interest relative to the successful operation of a whirling-membrane solar concentrator are randomly oriented wrinkles caused by handling during fabrication and packaging. Therefore, to provide design information, an investigation has been made to determine the effect of equal and nonequal biaxial tensile stresses on the effective reflectance of aluminized polyethylene terephthalate.

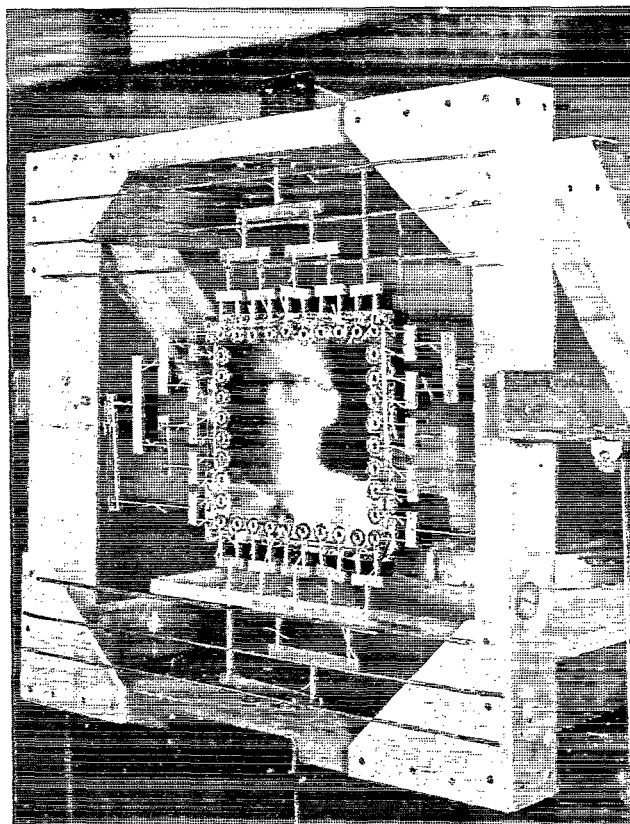
Although reflectance is usually considered to be a property of the reflecting material, the term "effective reflectance" is used herein to indicate a relative measure of the magnitude of the wrinkles. For example, if a reflecting optical flat were illuminated by a collimated light beam of uniform irradiance, the irradiance of the reflected beam would be the product of the incident-beam irradiance and the specular reflectance. If a reflector had a wavy surface such as a wrinkled surface in a reflective membrane, the reflected light would be dispersed so that the irradiance of the reflected beam would be less than the product of the incident-beam irradiance and the specular reflectance. The larger the amplitude of the wrinkles, the greater would be the dispersion of light; hence a lower effective reflectance would result. The effective reflectance will also vary with distance from the reflective surface to the detector; therefore, the data obtained from this investigation will show trends only and should not be used as absolute values.

Figure 18 shows the test arrangement with a specimen in place. The specimens were 28-centimeter-square sheets of 0.005-millimeter- and 0.01-millimeter-thick polyethylene terephthalate with grommets located every 2.5 centimeters around the perimeter. Loads were applied to the specimens along two perpendicular axes through the whiffletrees, as shown in figure 18. A zirconium arc lamp supplied the light which was nearly collimated and gave a 6.4-centimeter-diameter beam. The irradiance of the reflected light was measured by a photometer which was sensitive to radiation in the

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wavelength range from 200 to 680 nanometers. At each loading condition, a front-surface vacuum-deposited-aluminum flat glass mirror was placed just in front of the specimen and a reading of the light irradiance reflected from the mirror was read on the photometer. The mirror was then removed and a reading was made of the light reflected from the specimen. The effective reflectance was then determined as the ratio of the light reflected by the specimen to the light reflected by the front-surface mirror.

Tests were first made with equal loads applied to the two axes and the results are shown in figures 19 and 20, where effective reflectance is presented as a function of membrane stress. The stress varied from about 1 to 58 meganewtons per meter² for the 0.005-millimeter-thick plastic and from about 0.5 to 43 meganewtons per meter² for the 0.01-millimeter-thick plastic. The specimens as received from the fabrication shop had some wrinkles as the result of the handling during the installation of the grommets but were free of scratches and fingerprints in the center where reflectance was measured. The effective reflectance of the 0.005-millimeter-thick sample increased with increasing stress, thus indicating the presence of wrinkles that were being removed by the applied loads. This sample wrinkled easily during handling especially while being attached to the whiffletrees and placed in the testing frame. The 0.01-millimeter-thick sample was more resistant to wrinkling during handling as evidenced by no change in the effective reflectance from an increase in stress. (See fig. 20.) Both specimens were then crushed so that wrinkles showed over the entire surface when the specimens were laid on a flat surface. Care was taken to prevent fingerprints on the surfaces and also to insure that no sharp creases were made. However, the crushing procedure was probably more drastic than a folding procedure, that would be used in packaging a solar concentrator. For both specimens, the reflectance was very low at the lowest stress levels, but increased rapidly with increased stress.



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Figure 18.- Testing frame, with specimen installed, used in determining the effective reflectance of aluminized plastic under biaxial tensile loads.

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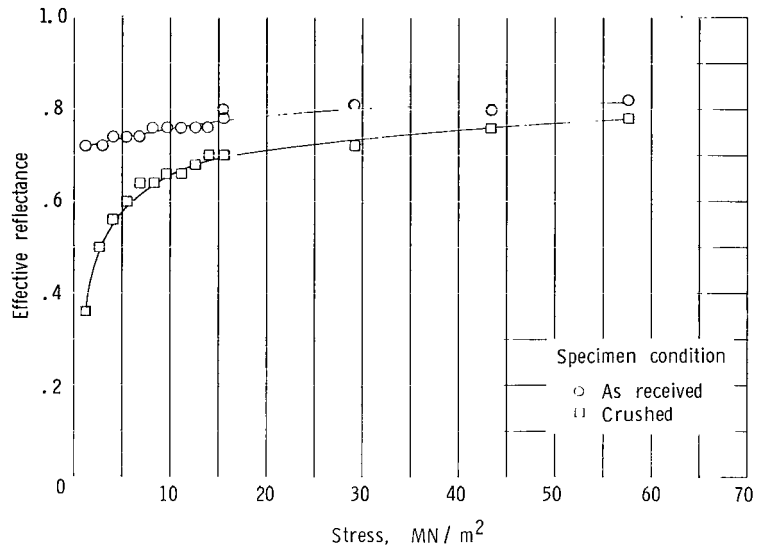


Figure 19.- Variation of effective reflectance of 0.005-mm-thick aluminized plastic under equal biaxial stresses.

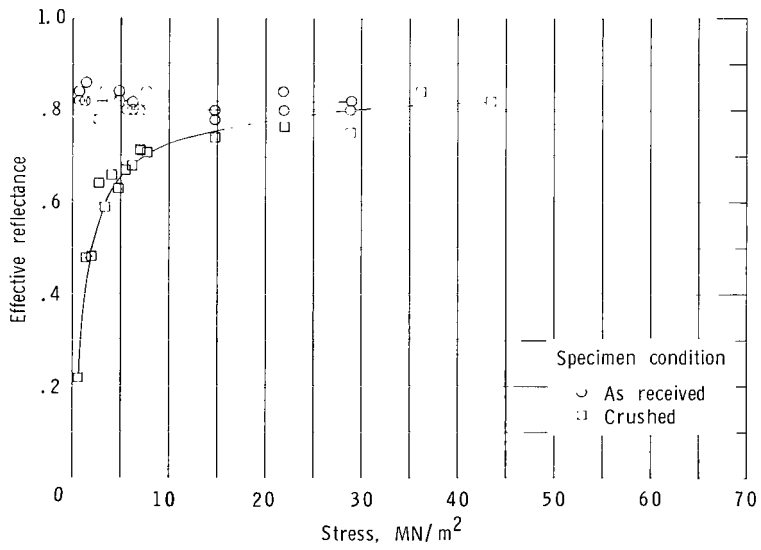


Figure 20.- Variation of effective reflectance of 0.01-mm-thick aluminized plastic under equal biaxial stresses.

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Specimens were then subjected to unequal applied loads along the two axes and the effective reflectance as a function of the ratio of minimum stress to maximum stress is presented for several values of maximum stress. Figure 21 shows the effective reflectance of a 0.005-millimeter-thick plastic membrane as received from the fabrication shop. The effective reflectance remained relatively constant over the stress-ratio range from 0.1 to 1.0. However, below a stress ratio of 0.1, the effective reflectance dropped rapidly. This drop is attributed to large wrinkles that were observed extending in a direction parallel to the maximum load, thus dispersing the reflected light. The specimen was then crushed and retested, and the results are shown in figure 22. A large spread in effective reflectance for the four stress levels, especially at stress ratios near 0.1 is shown. This specimen was retested after remaining under a stress of 7 meganewtons per meter² along each axis for several days. The results are shown in figure 23 where the difference in effective reflectance for the four stress levels is shown to be much less than was noted in figure 22. Therefore, it appears that the wrinkles put in the plastic by crushing are removed to some extent when a relatively small stress is applied for some time. The same specimen was tested with the maximum load applied along the axis at 90° to that applied in figure 23 to determine if the plastic had any directional characteristics. No appreciable difference in the data of the two tests was observed.

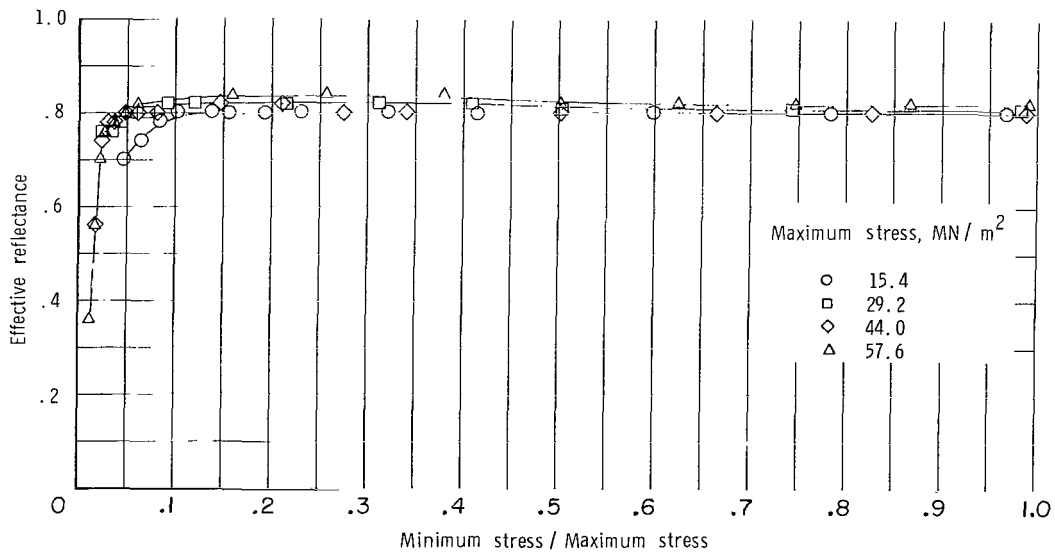


Figure 21.- Effective reflectance of 0.005-mm-thick aluminized plastic under unequal biaxial stresses; specimen as received from fabrication.

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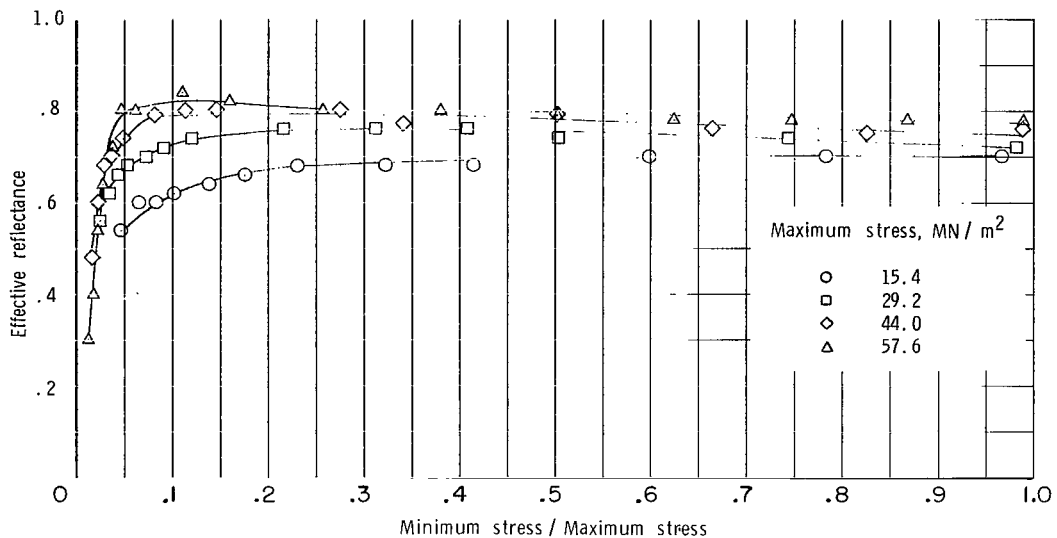


Figure 22.- Effective reflectance of 0.005-mm-thick aluminized plastic under unequal biaxial stresses; specimen crushed.

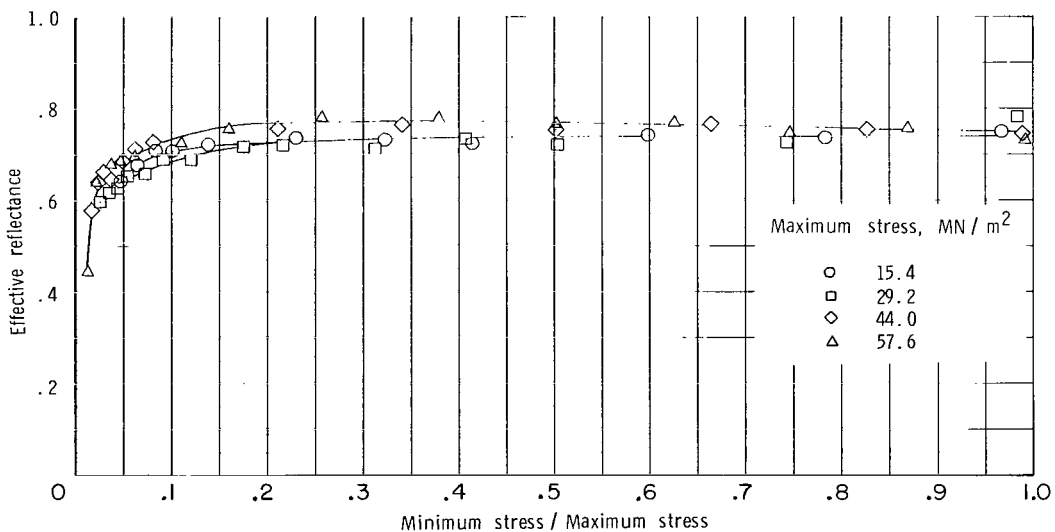


Figure 23.- Effective reflectance of 0.005-mm-thick aluminized plastic under unequal biaxial stresses; crushed specimen after remaining under a stress of 6.9 MN/m² for several days.

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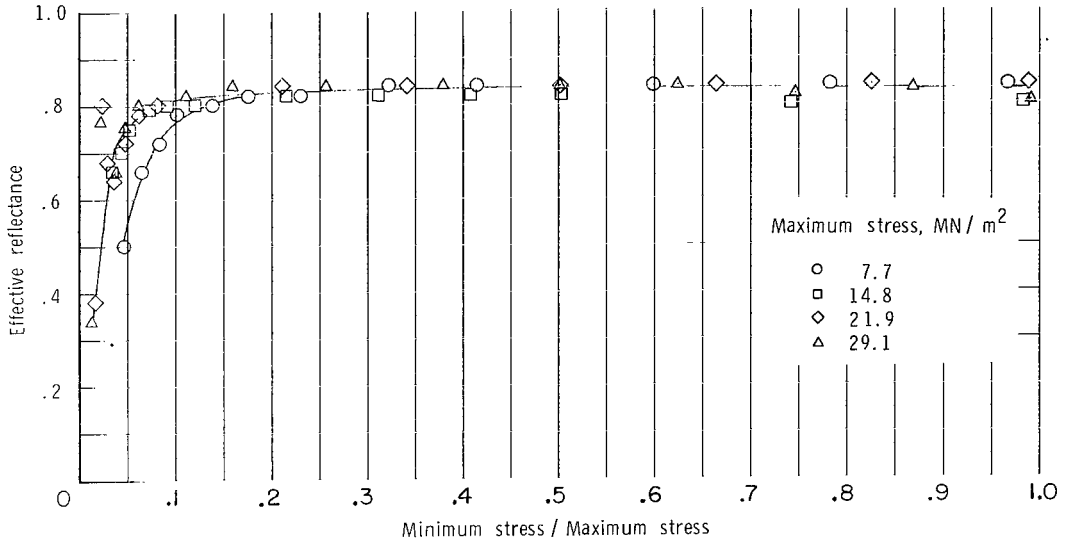


Figure 24.- Effective reflectance of 0.01-mm-thick aluminized plastic under unequal biaxial stresses; specimen as received from fabrication.

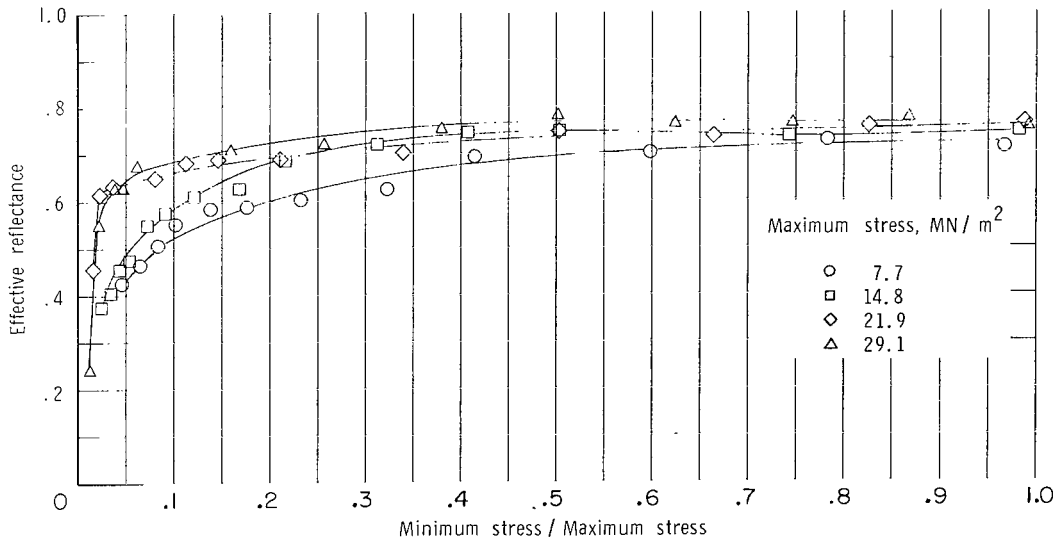


Figure 25.- Effective reflectance of 0.01-mm-thick aluminized plastic under unequal biaxial stresses; specimen crushed.

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A specimen of 0.01-millimeter-thick plastic, as received from the shop, was also tested with unequal loads and the results are shown in figure 24. The results are similar to those obtained on the 0.005-millimeter-thick specimen shown in figure 21. Figure 25 shows data on the crushed specimen. For the same values of maximum stress, the crushed specimen has appreciably lower effective reflectance than the as-received specimen of figure 24.

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